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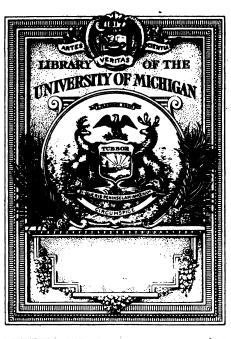
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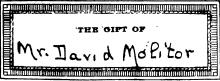
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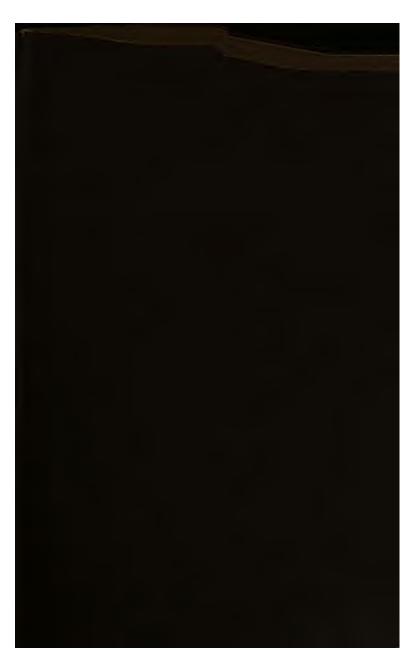
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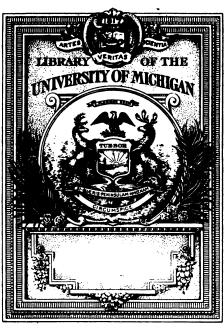
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BY

WILLIAM KENT, A.M., M.E.,

Dean and Professor of Mechanical Engineering in the L. C. Smith College of Applied Science, Syracuse University, Member Amer. Soc'y Mechl. Engrs. and Amer. Inst. Mining Engrs.

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n. David molita PREFACE.

More than twenty years ago the author began to follow the advice given by Nystrom: "Every engineeer should make his own pocket-book, as he proceeds in study and practice, to suit his particular business." The manuscript pocket-book thus begun, however, soon gave place to more modern means for disposing of the accumulation of engineering facts and figures, viz., the index rerum, the scrapbook, the collection of indexed envelopes, portfolios and boxes, the card catalogue, etc. Four years ago, at the request of the publishers, the labor was begun of selecting from this accumulated mass such matter as pertained to mechanical engineering, and of condensing, digesting, and arranging it in form for publication. In addition to this, a careful examination was made of the transactions of engineering societies, and of the most important recent works on mechanical engineering, in order to fill gaps that might be left in the original collection, and insure that no important facts had been overlooked.

Some ideas have been kept in mind during the preparation of the Pocket-book that will, it is believed, cause it to differ from other works of its class. In the first place it was considered that the field of mechanical engineering was so great, and the literature of the subject so vast, that as little space as possible should be given to subjects which especially belong to civil engineering. While the mechanical engineer must continually deal with problems which belong properly to civil engineering, this latter branch is so well covered by Trautwine's "Civil Engineer's Pocket-book" that any attempt to treat it exhaustively would not only fill no "long-felt want," but would occupy space which should be given to mechanical engineering.

Another idea prominently kept in view by the author has been that he would not assume the position of an "authority" in giving rules and formulæ for designing, but only that of compiler, giving not only the name of the originator of the rule, where it was known, but also the volume and page from which it was taken, so that its

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derivation may be traced when desired. When different formulæ for the same problem have been found they have been given in contrast, and in many cases examples have been calculated by each to show the difference between them. In some cases these differences are quite remarkable, as will be seen under Safety-valves and Crank-pins. Occasionally the study of these differences has led to the author's devising a new formula, in which case the derivation of the formula is given.

Much attention has been paid to the abstracting of data of experiments from recent periodical literature, and numerous references to other data are given. In this respect the present work will be found to differ from other Pocket-books.

The author desires to express his obligation to the many persons who have assisted him in the preparation of the work, to manufacturers who have furnished their catalogues and given permission for the use of their tables. and to many engineers who have contributed original data and tables. The names of these persons are mentioned in their proper places in the text, and in all cases it has been endeavored to give credit to whom credit is due. thanks of the author are also due to the following gentlemen who have given assistance in revising manuscript or proofs of the sections named: Prof. De Volson Wood, mechanics and turbines; Mr. Frank Richards, compressed air: Mr. Alfred R. Wolff, windmills; Mr. Alex. C. Humphreys, illuminating gas; Mr. Albert E. Mitchell, locomotives; Prof. James E. Denton, refrigerating-ma. chinery; Messrs. Joseph Wetzler and Thomas W. Varley, electrical engineering; and Mr. Walter S. Dix, for valuable contributions on several subjects, and suggestions as to their WILLIAM KENT. treatment.

Passaic, N. J., April, 1895.

FIFTH EDITION, MARCH, 1900.

Some typographical and other errors discovered in the fourth edition have been corrected. New tables and some additions have been made under the head of Compressed Air. The new (1899) code of the Boiler Test Committee of the American Society of Mechanical Engineers has been substituted for the old (1885) code.

W. K.

PREFACE TO FOURTH EDITION.

In this edition many extensive alterations have been made. Much obsolete matter has been cut out and fresh matter substituted. In the first 170 pages but few changes have been found necessary, but a few typographical and other minor errors have been corrected. The tables of sizes, weight, and strength of materials (pages 172 to 282) have been thoroughly revised, many entirely new tables, kindly furnished by manufacturers, having been substituted. Especial attention is called to the new matter on Cast-iron Columns (pages 250 to 253). In the remainder of the book changes of importance have been made in more than 100 pages, and all typographical errors reported to date have been corrected. Manufacturers' tables have been revised by reference to their latest catalogues or from tables furnished by the manufacturers especially for this work. Much new matter is inserted under the heads of Fans and Blowers, Flow of Air in Pipes, and Compressed Air. The chapter on Wire-rope Transmission (pages 017 to 022) has been entirely rewritten. The chapter on Electrical Engineering has been improved by the omission of some matter that has become out of date and the insertion of some new matter.

It has been found necessary to place much of the new matter of this edition in an Appendix, as space could not conveniently be made for it in the body of the book. It has not been found possible to make in the body of the book many of the cross-references which should be made to the items in the Appendix. Users of the book may find it advisable to write in the margin such cross-references as they may desire.

The Index has been thoroughly revised and greatly enlarged.

The author is under continued obligation to many manufacturers who have furnished new tables and data, and to many individual engineers who have furnished new matter, pointed out errors in the carlier editions, and offered helpful suggestions. He will be glad to receive similar aid, which will assist in the further improvement of the book in future editions.

WILLIAM KENT.

Passaic, N. J., September, 1898.

SIXTH EDITION. DECEMBER, 1902.

THE chapter on Electrical Engineering has been thoroughly revised, much of the old matter cut out and new matter substituted. Fourteen new pages have been devoted to the subject of Alternating Currents. The chapter on Locomotives has been revised. Some new matter has been added under Cast Iron, Specifications for Steel, Springs, Steam-engines, and Friction and Lubrication. Slight changes and corrections the text have been made in nearly a hundred pages.

SEVENTH EDITION, OCTOBER 1904.

An entirely new index has been made, with about twice a many titles as the former index. The electrical engineerin chapter has been further revised and some new matter addec Four pages on Coal Handling Machinery have been inserte at page 911, and numerous minor changes have been made.

w. K.

Syracuse, N. Y.

(For Alphabetical Index see page 1093.)

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NAMES AND ABBREVIATIONS OF PERIODICALS AND TEXT-BOOKS FREQUENTLY REFERRED TO IN THIS WORK.

Am. Mach. American Machinist.
App. Cyl. Mech. Appleton's Cyclopædia of Mechanics, Vols. I and II.
Bull. I. & S. A. Bulletin of the American Iron and Steel Association
(Philadelphia).
Burr's Elasticity and Resistance of Materials.
Clark, R. T. D. D. K. Clark's Rules, Tables, and Data for Mechanical Engineers. gineers.
Clark, S. E. D. K. Clark's Treatise on the Steam-engine.
Col. Coll. Qly. Columbia College Quarterly.
Engg. Engineering (London).
Eng. News. Engineering News,
Engr. The Engineering News,
Engr. The Engineer (London).
Fairbairn's Useful Information for Engineers.
Flynn's Irrigation Canals and Flow of Water.
Jour. A. C. I. W. Journal of American Charcoal Iron Workers' Association.
Jour. F. I. Journal of the Franklin Institute,
Wann's Electric Transmission of Energy. Kapp's Electric Transmission of Energy. Lanza's Applied Mechanics. Merriman's Strength of Materials. Modern Mechanism. Supplementary volume of Appleton's Cyclopædia of Mechanics. Proc. Inst. C. E. Proceedings Institution of Civil Engineers (London).

Proc. Inst. M. E. Proceedings Institution of Mechanical Engineers (Lon-Proc. Inst. M. E. Proceedings Institution of Mechanical Engineers (1 don).
Peabody's Thermodynamics,
Proceedings Engineers' Club of Philadelphia.
Rankine, S. E. Rankine's The Steam Engine and other Prime Movers.
Rankine's Machinery and Millwork.
Rankine, R. T. D. Rankine's Rules, Tables, and Data.
Reports of U. S. Test Board.
Reports of U. S. Testing Machine at Watertown, Massachusetts.
Rontgen's Thermodynamics.
Seaton's Manual of Marine Engineering.
Hamilton Smith, Jr.'s Hydraulics.
The Stevens Indicator.
Thompson's Dynamo-electric Machinery.
Thurston's Manual of the Steam Engine. Thurston's Manual of the Steam Engine. Thurston's Materials of Engineering. Thurston's Materials of Engineering.

Trans. A. I. E. E. Transactions American Institute of Electrical Engineers.

Trans. A. I. M. E. Transactions American Institute of Mining Engineers.

Trans. A. S. O. E. Transactions American Society of Civil Engineers.

Trans. A. S. M. E. Transactions American Society of Mechanical Engineers.

Transactions American Society of Mechanical Engineers.

Transactions American Society of Mechanical Engineers.

The Locomotive (Hartford, Connecticut).

Unwin's Elements of Machine Design. Weisbach's Mechanics of Engineering. Wood's Resistance of Materials. Wood's Thermodynamics.

xxxii

MATHEMATICS.

Greek Letters.

A B C A E Z	βγες	Alpha Beta Gamma Delta Epsilon Zeta	H H I K A M	η θ θ κ λ μ	Eta Theta Iota Kappa Lambda Mu	N E O II P E	ν ξ ο π ρ σ ς	Nu Xi Omicron Pi Rho Sigma	Υ Φ Χ Ψ	τυφχ ψ	Tau Upsilon Phi Chi Psi Omega
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Arithmetical and Algebraical Signs and Abbreviations.

```
plus (addition).
positive.
 - minus (subtraction).

    negative.

± plus or minus.
∓ minus or plus.
= equals.
× multiplied by.
ab \text{ or } a.b = a \times b.
+ \text{ divided by}
  divided by.
   =a/b=a+b.
                         15-16=\frac{15}{16}
2 = \frac{2}{10}; .002 = \frac{2}{1000}
square root.
 V cube root.
 4th root.
: is to, :: so is, : to (proportion).
2 : 4 :: 3 : 6, as 2 is to 4 so is 3 to 6.
: ratio; divided by.
 2:4, ratio of 2 to 4=2/4.
.. therefore
> greater than.
< less than.</p>
D square.
O round.

    degrees, arc or thermometer.

 ' minutes or feet.
" seconds or inches.
"" accents to distinguish letters, as
       a', a'', a'''.
a_1, a_2, a_3, a_b, a_c, read a \text{ sub } 1, a \text{ sub } b,
      etc.
O[1]\{\}
                  - vincula, denoting
       that the numbers enclosed are
       to be taken together; as,
       (a+b)c = 4+8 \times 5 = 35.
a<sup>3</sup>, a<sup>3</sup>, a squared, a cubed.
an, a raised to the nth power.
a^{\frac{1}{2}} = \sqrt[4]{a^2}, a^{\frac{1}{2}} = \sqrt{a^2}.
         -, a-2 =
10^{\circ} = 10 to the 9th power = 1,000,000,
\sin a = the sine of a.
\sin_{\alpha} - 1 a =  the arc whose sine is a.
              sin. a.
log. = logarithm.
log. or hyp. log. = hyperbolic logarithm.
```

```
∠ angle.
 L right angle.
    perpendicular to.
sin., sine.
cos., cosine.
tang., or tan., tangent.
sec., secant.
versin., versed sine.
cot., cotangent.
cosec., cosecant
covers., co-versed sine.

In Algebra, the first letters of the alphabet, a, b, c, d, etc., are generally used to denote known quantities,
and the last letters, w, x, y, z, etc.,
unknown quantities.
 Abbreviations and Symbols com-
                 monly used.

 d. differential (in calculus).

     integral (in calculus).
  a, integral between limits a and b.
Δ, delta, difference.
Σ. sigma, sign of summation.
*, pi, ratio of circumference of circle
        to diameter = 3.14159
g, acceleration due to gravity = 32.16
        ft. per sec.
Abbreviations frequently used in this Book.
L., l., length in feet and inches.
B., b., breadth in feet and inches.
D., d., depth or diameter.
H., h., height, feet and inches.
T., t., thickness or temperature. Y., v., velocity.
F., force, or factor of safety.
f., coefficient of friction.
E., coefficient of elasticity.
R., r., radius.
W., w., weight.
y., w., weight.
P., p., pressure or load.
H.P., horse-power.
I.H.P., indicated horse-power.
B.H.P., brake horse-power.
h. p., high pressure.
i. p., intermediate pressure.
l. p., low pressure.
A.W. G., American Wire Gauge
                         (Brown & Sharpe).
B.W.G., Birmingham Wire Gauge.
r. p. m., or revs. per min., revolutions
```

per minute.

ARITHMETIC.

The user of this book is supposed to have had a training in arithmetic as well as in elementary algebra. Only those rules are given here which are apt to be easily forgotten.

GREATEST COMMON MEASURE, OR GREATEST COMMON DIVISOR OF TWO NUMBERS.

Bule.— Divide the greater number by the less; then divide the divisor by the remainder, and so on, dividing always the last divisor by the last remainder, until there is no remainder, and the last divisor is the greatest common measure required.

LEAST COMMON MULTIPLE OF TWO OR MORE NUMBERS.

Bule.—Divide the given numbers by any number that will divide the greatest number of them without a remainder, and set the quotients with the undivided numbers in a line beneath.

Divide the second line as before, and so on, until there are no two numbers that can be divided; then the continued product of the divisors and last quotients will give the multiple required.

FRACTIONS.

To reduce a common fraction to its lowest terms.—Divide both terms by their greatest common divisor. 39/52 = 3/4.

To change an improper fraction to a mixed number.— Divide the numerator by the denominator; the quotient is the whole number, and the remainder placed over the denominator is the fraction: 39/4 = 9%.

To change a mixed number to an improper fraction.

To change a mixed number to an improper fraction; multiply the whole number by the denominator of the fraction; to the product add the numerator; place the sum over the denominator: $1\frac{7}{8} = 15/8$. To express a whole number in the form of a fraction with a given denominator.—Multiply the whole number by the given denominator, and place the product over that denominator: 13 = 39/3. To reduce a compound to a simple fraction, also to multiply fractions,—Multiply the numerators together for a new numerator and the denominators together for a new denominator:

$$\frac{9}{3}$$
 of $\frac{4}{3} = \frac{8}{9}$, also $\frac{2}{3} \times \frac{4}{3} = \frac{8}{9}$.

To reduce a complex to a simple fraction.—The numerator and denominator must each first be given the form of a simple fraction; then multiply the numerator of the upper fraction by the denominator of the lower for the new numerator, and the denominator of the upper by the numerator of the lower for the new denominator:

$$\frac{\frac{78}{1\frac{3}{4}} - \frac{78}{74} - \frac{28}{56} - \frac{1}{2}.$$

To divide fractions.—Reduce both to the form of simple fractions. invert the divisor, and proceed as in multication:

$$\frac{3}{4} + 1\frac{1}{4} = \frac{3}{4} + \frac{5}{4} = \frac{3}{4} \times \frac{4}{5} = \frac{12}{20} = \frac{3}{5}.$$

Cancellation of fractions.—In compound or multiplied fractions. divide any numerator and any denominator by any number which will divide them both without remainder, striking out the numbers thus divided and setting down the quotients in their stead.

To reduce fractions to a common denominator.—Reduce

each fraction to the form of a simple fraction; then multiply each numera-

tor by all the denominators except its own for the new numerators, and all the denominators together for the common denominator:

$$\frac{1}{2}$$
, $\frac{1}{8}$, $\frac{3}{7} = \frac{21}{42}$, $\frac{14}{42}$, $\frac{18}{42}$.

To add fractions.—Reduce them to a common denominator, then add the numerators and place their sum over the common denominator:

$$\frac{1}{2} + \frac{1}{3} + \frac{3}{7} = \frac{21 + 14 + 18}{42} = \frac{53}{42} = 1\frac{11}{42}.$$

To subtract fractions.—Reduce them to a common denominator, subtract the numerators and place the difference over the common denominator:

$$\frac{1}{2} - \frac{8}{7} = \frac{7 - 6}{14} = \frac{1}{14}$$

DECIMALS.

To add decimals.—Set down the figures so that the decimal points are one above the other, then proceed as in simple addition: 18.75 + .012 = 18.762.

To subtract decimals.—Set down the figures so that the decimal points are one above the other, then proceed as in simple subtraction: 18.78—012 = 18.738.

To multiply decimals.—Multiply as in multiplication of whole numbers, then point off as many decimal places as there are in multiplier and multiplicand taken together: 1.5 × .02 = .030 = .03.

To divide decimals.—Divide as in whole numbers, and point off in

To divide decimals.—Divide as in whole numbers, and point off in the quotient as many decimal places as those in the dividend exceed those in the divisor. Ciphers must be added to the dividend to make its decimal places at least equal those in the divisor, and as many more as it is desired to have in the quotient: 1.5 + .25 = 6. 0.1 + 0.3 = 0.10000 + 0.3 = 0.8833 +

Decimal Equivalents of Fractions of One Inch.

1-64	.015625	17-64	.265625	38-64	.515625	49-64	.765625
1-32	.03125	9-32	.28125	17-32	.53125	25-32	.78125
3-64	.046875	19-64	.296875	35-64	.546875	51-64	.796875
1-16	.0625	5 -16	.8125	9-16	.5625	13-16	.8125
5-64	.078125	21-64	.228125	37-64	.578125	53-64	.82812 5
3-32	.09375	11-32	.34375	19-32	.59375	27-32	.84375
7-64	.109375	23-64	.359375	39-64	.609875	55-64	.85937 5
1-8	.125	8-8	.875	.5-8	.625	7=8	.875
9-64	.140625	25-64	.890625	41-64	.640625	57-64	.890625
5-32	.15625	13-32	.40625	21-32	.65625	29-32	.90625
11-64	.171875	27-64	.421875	43-64	.671875	59-64	.921875
3-1 6	.1875	7 -16	.4875	11-16	.6875	15-16	.9375
13-64 7-32 15-64 1-4	.203125 .21875 .284875 .25	29-64 15-32 31-64 1- 2	.453125 .46875 .484375 .50	45-64 23-32 47-64 8-4	.708125 .71875 .734375 .75	61–64 31–32 63–64 1	.953125 .96875 .984375

To convert a common fraction into a decimal.—Divide the numerator by the denominator, adding to the numerator as many ciphers prefixed by a decimal point as are necessary to give the number of decimal places desired in the result: $\frac{1}{24} = 1.0000 + 3 = 0.3333 + 1.$ To convert a decimal into a common fraction.—Set down

To convert a decimal into a common fraction.—Set down the decimal as a numerator, and place as the denominator 1 with as many ciphers annexed as there are decimal places in the numerator; erase the

Product of Fractions Expressed in Decimals.

14		-	-	- 					•			•				_	
. 0156 . 0234 . 0252 . 0318 . 0469 . 0625 . 0391 . 0686 . 0781 . 0977 . 0469 . 0708 . 0387 . 1172 . 1406 . 0547 . 0820 . 1082 . 1172 . 1406 . 0547 . 0820 . 1082 . 1187 . 1184 . 2508 . 0708 . 1105 . 1406 . 1762 . 2184 . 2734 . 3125 . 3164 . 0708 . 1172 . 1562 . 1988 . 2841 . 2734 . 3125 . 3164 . 0708 . 1289 . 1719 . 2148 . 2878 . 3006 . 3488 . 3867 . 4297 . 4727 . 0838 . 1406 . 1875 . 2344 . 2878 . 3006 . 3488 . 3867 . 4297 . 4727 . 0838 . 1406 . 1875 . 2844 . 2878 . 3008 . 3488 . 3867 . 4297 . 4727 . 1094 . 1641 . 2187 . 2734 . 38281 . 38281 . 3750 . 5469 . 5016 . 1172 . 1778 . 2844 . 2890 . 3816 . 4102 . 4688 . 5278 . 5899 . 6445		18	- 4∞	18 18	-4+	16	ecico	17	- ¢3	18	rcko	#	e)44	200 200 200	ı-bc	140	- 1
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11172 11875 2544 2980 38516 4102 4688 6273 8869 6445 1987 1987 1987 8781 8781 8781 8781 8781	8750	.0547	1001	.1641	.2187	2672	.3281	3888	.4375	.49%	.5469	.6016	.6563	.7109	7656		
19KO 1875 9KOO 819K 87KO 497K KOOO KEOK BOKA BOWA	5786	.0586	.1172	.1758	.2344	.2980	.8516	.4102	.4688	.5278	.5859	5445	.7081	7197.	8088	878	
0100. 0000. 0000. 0105. 0010. 0010.	1.000	.0625	.1250	.1875	.2500	.3125	.8750	.4875	2000	.5625	.6250	.6876	.7500	.8125	.8750	9875	1.000

decimal point in the numerator, and reduce the fraction thus formed to its lowest terms:

.25 =
$$\frac{25}{100} = \frac{1}{4}$$
; .3333 = $\frac{3333}{10000} = \frac{1}{8}$, nearly.

To reduce a recurring decimal to a common fraction.—Subtract the decimal figures that do not recur from the whole decimal including one set of recurring figures; set down the remainder as the numerator of the fraction, and as many nines as there are recurring figures, followed by as many ciphers as there are non-recurring figures, in the denominator. Thus:

Subtract

.79054054, the recurring figures being 054.

79

 $\frac{78975}{99900} = \text{(reduced to its lowest terms)} \frac{117}{148}$

COMPOUND OR DENOMINATE NUMBERS.

Reduction descending.—To reduce a compound number to a lower denomination. Multiply the number by as many units of the lower denomination as makes one of the higher.

8 yards to inches: $8 \times 36 = 108$ inches.

.04 square feet to square inches: $.04 \times 144 = 5.76$ sq. in.

If the given number is in more than one denomination proceed in steps from the highest denomination to the next lower, and so on to the lowest, adding in the units of each denomination as the operation proceeds.

8 yds. 1 ft. 7 in. to inches: $8 \times 3 = 9$, +1 = 10, $10 \times 12 = 120$, +7 = 127 in.

Reduction ascending.—To express a number of a lower denomination in terms of a higher, divide the number by the number of units of the lower denomination contained in one of the next higher; the quotient is in the higher denomination, and the remainder, if any, in the lower.

127 inches to higher denomination.

$$127 + 12 = 10$$
 feet $+ 7$ inches; 10 feet $+ 3 = 3$ yards $+ 1$ foot.
Ans. 8 yds. 1 ft. 7 in.

To express the result in decimals of the higher denomination, divide the given number by the number of units of the given denomination contained in one of the required denomination, carrying the result to as many places of decimals as may be desired.

127 inches to yards: $127 + 36 = 8\frac{1}{3} = 8.5277 + yards$.

RATIO AND PROPORTION.

Ratio is the relation of one number to another, as obtained by dividing one by the other.

Ratio of 2 to 4, or 2: 4 = 2/4 = 1/2. Ratio of 4 to 2, or 4: 2 = 2.

Proportion is the equality of two ratios. Ratio of 2 to 4 equals ratio of 3 to 6, 2/4 = 3/6; expressed thus, 2:4::8:6; read, 2 is to 4 as 3 is to 6. The first and fourth terms are called the extremes or outer terms, the second and third the means or inner terms.

The product of the means equals the product of the extremes:

$$2:4::8:6$$
; $2\times 6=12$; $8\times 4=12$.

Hence, given the first three terms to find the fourth, multiply the second and third terms together and divide by the first.

2:4::8: what number? Ans.
$$\frac{4\times 3}{2} = 6$$
.

Algebraic expression of proportion.— $a:b::c:d; \frac{a}{b} = \frac{c}{d};$ and = bc; from which $a = \frac{bc}{d}$; $d = \frac{bc}{a}$; $b = \frac{ad}{c}$; $c = \frac{ad}{b}$.

Mean proportional between two given numbers, 1st and 2d, is such a number that the ratio which the first bears to it equals the ratio which 1 bears to the second. Thus, 2: 4:: 4: 8; 4 is a mean proportional between 2 and 8. To find the mean proportional between two numbers, extract the square root of their product.

Mean proportional of 2 and $8 = \sqrt{2 \times 8} = 4$.

Single Rule of Three; or, finding the fourth term of a proportion when three terms are given.—Rule, as above, when the terms are stated in their proper order, multiply the second by the third and divide by the first. The difficulty is to state the terms in their proper order. The term which is of the same kind as the required or fourth term is made the third; the first and second must be like each other in kind and denomination. To determine the same that the same terms are the same terms of t mine which is to be made second and which first requires a little reasoning. mine which is to be made second and which first requires a little reasoning. If an inspection of the problem shows that the answer should be greater than the ihird term, then the greater of the other two given terms should be made the second term—otherwise the first. Thus, 3 men remove 54 cuble feet of rock in a day; how many men will remove in the same time 10 cuble yards? The answer is to be men—make men third term; the answer is to be more than three men, therefore make the greater quantity, 10 cuble yards, the second term; but as it is not the same denomination as the other term it must be reduced, = 270 cubic feet. The proportion is then stated:

54: 270:; 8: x (the required number);
$$x = \frac{8 \times 270}{54} = 15$$
 men.

The problem is more complicated if we increase the number of given terms. Thus, in the above question, substitute for the words "in the same time" the words "in 3 days." First solve it as above, as if the work were to be done in the same time; then make another proportion, stating it thus: If 15 men do it in the same time, it will take fewer men to do it in 8 days;

make 1 day the 2d term and 3 days the first term. 3:1::15 men: 5 men. Compound Proportion, or Double Rule of Three,—By this rule are solved questions like the one just given, in which two or more starings are required by the single rule of three. In it as in the single rule, there is one third term, which is of the same kind and denomination as the fourth or required term, but there may be two or more first and second terms. Set down the third term, take each pair of terms of the same kind separately, and arrange them as first and second by the same reasoning as is adopted in the single rule of three, making the greater of the pair the second if this pair considered alone should require the answer to be greater.

Set down all the first terms one under the other, and likewise all the second terms. Multiply all the first terms together and all the second terms tog-ther. Multiply the product of all the second terms by the third term, and divide this product by the product of all the first terms. Example: If 3 men remove 4 cubic yards in one day, working 12 hours a day, how many men working 10 hours a day will remove 20 cubic yards in 8 days?

Yards 3: 1 10: 12 :: 8 men. Days Products 120: 240 :: 8:6 men. Ans.

To abbreviate by cancellation, any one of the first terms may cancel either the third or any of the second terms; thus, 8 in first cancels 8 in third, making it 1, 10 cancels into 20 making the latter 2, which into 4 makes it 2, which into 12 makes it 6, and the figures remaining are only 1:6::1:6.

INVOLUTION, OR POWERS OF NUMBERS.

Involution is the continued multiplication of a number by itself a given number of times. The number is called the root, or first power, and the products are called powers. The second power is called the square and the third power the cube. The operation may be indicated without being performed by writing a small figure called the index or exponent to the

Tight of and a little above the root; thus, $3^3 = \text{cube of } 3, = 27$.

To multiply two or more powers of the same number, add their exponents; thus, $2^3 \times 2^3 = 2^5$, or $4 \times 8 = 3^2 = 2^5$.

see).

To divide two powers of the same number, subtract their exponents; thus, $\frac{1}{22} = \frac{1}{4}$. The exponent may thus be nega-9+21=21=2; 21+24=2tive. $2^3 + 2^3 = 2^0 = 1$, whence the zero power of any number = 1. The first power of a number is the number itself. The exponent may be fractional, as 21, 23, which means that the root is to be raised to a power whose seponent is the numerator of the fraction, and the root whose sign is the denominator is to be extracted (see Evolution). The exponent may be a decimal, as 20°5, 21°5, read, two to the five-tenths power, two to the one and five-tenths power. These powers are solved by means of Logarithms (which

First Nine Powers of the First Nine Numbers.

1st	2d	8d	4th	5th	6th	7th	8th	9th
Pow'r	Pow'r	Power.	Power.	Power.	Power.	Power.	Power.	Power.
1 2 8 4 5	1 4 9 16 95	1 8 27 64 125	1 16 81 256 625	1 82 243 1024 8125	1 64 729 4096 15625	1 128 2187 16884 78125	256 6561 65586 890625	1 512 19688 262144 1958125
6	86	216	1296	7776	46656	279986	1679616	10077696
7	49	848	2401	16807	117649	823543	5764801	40858607
8	64	512	4096	32768	262144	2097152	16777216	134217728
9	81	729	6581	59049	531441	4782969	48046721	887420489

The First Forty Powers of 2.

Power.	Value.	Power.	Value.	Power.	Value.	Power.	Value.	Power.	Value.
0 1 2 8	1 2 4 8 16	9 10 11 12 13	512 1024 2048 4096 8192	18 19 20 21 22	262144 524288 1048576 2097152 4194304	27 28 29 30 31	134217728 268435456 536870912 1073741824 2147483648	36 37 38 89 40	68719476736 137438958472 274877906944 549755813888 1099511627776
5 6 7 8	82 64 128 256	14 15 16 17	16884 32768 65536 131072	23 24 25 26	8388608 16777216 83554432 67108864	32 33 34 35	4294967296 8589934592 17179869184 34350738368		

EVOLUTION.

Evelution is the finding of the root (or extracting the root) of any number the power of which is given.

The sign ψ indicates that the square root is to be extracted: $\psi \psi^n$, the cube root, 4th root, nth root.

A fractional exponent with 1 for the numerator of the fraction is also used to indicate that the operation of extracting the root is to be performed; though, 2¹, 2² = 4√2, ²√2.

When the power of a number is indicated, the involution not being p formed, the extraction of any root of that power may also be indicated

dividing the index of the power by the index of the root, indicating the division by a fraction. Thus, extract the square root of the 6th power of 2:

$$\sqrt{2^6} = 2^{\frac{6}{2}} = 2^{\frac{3}{1}} = 2^3 = 8.$$

The 6th power of 2, as in the table above, is 64; $\sqrt{64} = 8$.

Difficult problems in evolution are performed by logarithms, but the square root and the cube root may be extracted directly according to the rules given below. The 4th root is the square root of the square root. The

rules given below. The 4th root is the square root of the square root. The 6th root is the cube root of the square root, or the square root of the cube root; the 9th root is the cube root of the cube root; the 9th root is the cube root.—Point off the given number into periods of two places each, beginning with units. If there are decimals, point these off likewise, beginning at the decimal point, and supplying as many ciphers as may be needed. Find the greatest number whose square is less than the first left-hand period, and place it as the first figure in the quotient. Subtract its square from the left-hand period, and to the remainder annex the two figures of the second period for a dividend. Double the first figure of the quotient for a partial divisor; find how many times the latter is contained in the dividend exclusive of the right-hand figure, and set the figure representing that number of of the right-hand figure, and set the figure representing that number of times as the second figure in the quotient, and annex it to the right of the partial divisor, forming the complete divisor. Multiply that divisor by the second figure in the quotient and subtract the product from the dividend. To the remainder bring down the next period and proceed as before, in each case doubling the figures in the root already found to obtain the trial divisor. Should the product of the second figure in the root by the completed divisor be greater than the dividend, erase the second figure both from the quotient and from the divisor, and substitute the next smaller figure, or one small enough to make the product of the second figure by the divisor less than or equal to the dividend.

To extract the square root of a fraction, extract the root of numerator and denominator separately. $\sqrt{\frac{4}{9}} = \frac{2}{3}$, or first convert the fraction into a

decimal,
$$\sqrt{\frac{4}{9}} = \sqrt{.4444 +} = .6666 +$$
.

To Extract the Cube Boot.—Point off the number into periods of 3 figures each, beginning at the right hand, or unit's place. Point off decimals in periods of 3 figures from the decimal point. Find the greatest cube that does not exceed the left-hand period; write its root as the first figure in the required root. Subtract the cube from the left-hand period, and to the remainder bring down the next period for a dividend.

Square the first figure of the root; multiply by 800, and divide the product

into the dividend for a trial divisor; write the quotient after the first figure of the root as a trial second figure.

Complete the divisor by adding to 300 times the square of the first figure, So times the product of the first by the second figure, and the square of the second figure. Multiply this divisor by the second figure; subtract the product from the remainder. (Should the product be greater than the mainder, the last figure of the root and the complete divisor are too large; substitute for the last figure the next smaller number, and correct the trial

divisor accordingly.)

To the remainder bring down the next period, and proceed as before to find the third figure of the root—that is, square the two figures of the root already found; multiply by 300 for a trial divisor, etc.

If at any time the trial divisor is greater than the dividend, bring down another period of 3 figures, and place 0 in the root and proceed.

The cube root of a number will contain as many figures as there are periods of 3 in the number.

Shorter Methods of Extracting the Cube Root,--i. From Wentworth's Algebra:

After the first two figures of the root are found the next trial divisor is found by bringing down the sum of the 60 and 4 obtained in completing the preceding divisor, then adding the three lines connected by the brace, and annexing two ciphers. This method shortens the work in long examples, as a seen in the case of the last two trial divisors, saving the labor of squaring 123 and 1234. A further shortening of the work is made by obtaining the last two figures of the root by division, the divisor employed being three times the square of the part of the root already found; thus, after finding the first three figures:

The error due to the remainder is not sufficient to change the fifth figure of

2. By Prof. H. A. Wood (Stevens Indicator, July, 1890):
I. Having separated the number into periods of three figures each, counting from the right, divide by the square of the nearest root of the first period, or first two periods; the nearest root is the trial root.

II. To the quotient obtained add twice the trial root, and divide by 3.

This gives the root, or first approximation.

III. By using the first approximate root as a new trial root, and proceeding as before, a nearer approximation is obtained, which process may be repeated until the root has been extracted, or the approximation carried as far as desired.

EXAMPLE.—Required the cube root of 90. The nearest cube to 90 is 30.

$$8^{2} = 9)\underline{30.0}$$

$$\underline{3}, \underline{3}$$

$$\underline{6}$$

$$3)\underline{8.1}$$

$$2.7 \text{ 1st T. R.}$$

$$\mathbf{3.7^{2}} = 7.29)\underline{20.000}$$

$$\underline{2.743}$$

$$\underline{5.4}$$

$$\underline{8)\underline{6.148}}$$

$$\underline{2.714}, \text{ 1st ap. cube root.}$$

$$\mathbf{3.714^{2}} = 7.365796)\underline{20.0000000}$$

$$\underline{2.7152634}$$

$$\underline{5.428}$$

$$\underline{318.1439534}$$

REMARK.—In the example it will be observed that the second term, or first two figures of the root, were obtained by using for trial root the root of the first period. Using, in like manner, these two terms for trial root, we obtained four terms of the root; and these four terms for trial root gave seven figures of the root correct. In that example the last figure should be 7. Should we take these eight figures for trial root we should obtain at least fifteen figures of the root correct.

2.7144178 2d ap. cube root.

To Extract a Higher Boot than the Cube.—The fourth root is the square root of the square root; the sixth root is the cube root of the square root or the square root of the cube root. Other roots are most conveniently found by the use of logarithms.

ALLIGATION

shows the value of a mixture of different ingredients when the quantity and value of each is known.

Let the ingredients be a, b, c, d, etc., and their respective values per unit w, x, y, z, etc.

$$A =$$
 the sum of the quantities = $a + b + c + d$, etc.
 $P =$ mean value or price per unit of A .
 $AP = aw + bx + cy + dz$, etc.
 $P = \frac{aw + bx + cy + dz}{4}$.

PERMUTATION

shows in how many positions any number of things may be arranged in a row; thus, the letters a, b, c may be arranged in six positions, viz. abc, acb, cab, cba, bac, bca.

Rule.—Multiply together all the numbers used in counting the things; thus, permutations of 1, 2, and $3 = 1 \times 2 \times 3 = 6$. In how many positions can 9 things in a row be placed?

$$1 \times 9 \times 8 \times 4 \times 5 \times 6 \times 7 \times 8 \times 9 = 369890$$

COMBINATION

shows how many arrangements of a few things may be made out of a greater number. Rule: Set down that figure which indicates the greater number, and after it a series of figures diminishing by 1, until ax many are set down as the number of the few things to be taken in each combination. Then beginning under the last one set down said number of few things; then going backward set down a series diminishing by 1 until arriving under the first of the upper numbers. Multiply together all the upper numbers to form one product, and all the lower numbers to form another; divide the upper product by the lower one.

How many combinations of 9 things can be made, taking 8 in each combination?

$$\frac{9\times8\times7}{1\times2\times3}=\frac{504}{6}=84.$$

ARITHMETICAL PROGRESSION.

in a series of numbers, is a progressive increase or decrease in each successive number by the addition or subtraction of the same amount at each step, as 1, 2, 3, 4, 5, etc., or 15, 12, 9, 6, etc. The numbers are called terms, and the equal increase or decrease the difference. Examples in arithmetical progression may be solved by the following formulæ:

Let a = first term, l = last term, d = common difference, n = number of terms, s = sum of the terms:

$$\begin{aligned} l &= a + (n-1)d, &= -\frac{1}{2}d \pm \sqrt{2ds + \left(a - \frac{1}{2}d\right)^{n}}, \\ &= \frac{2s}{n} - a, &= \frac{s}{n} + \frac{(n-1)d}{2}. \\ &= \frac{1}{2}n[2a + (n-1)d], &= \frac{l+a}{2} + \frac{l^{2} - a^{2}}{2d}, \\ &= (l+a)\frac{n}{2}, &= \frac{1}{3}n[2l - (n-1)d]. \\ &= l - (n-1)d, &= \frac{s}{n} - \frac{(n-1)d}{2}, \\ &= \frac{1}{2}d \pm \sqrt{\left(l + \frac{1}{2}d\right)^{2} - 2ds}, &= \frac{2s}{n} - l. \\ &= \frac{l-a}{n-1}, &= \frac{2(s-an)}{n(n-1)}, \\ &= \frac{l^{2} - a^{2}}{2s - l - a}, &= \frac{2(nl-s)}{n(n-1)}, \\ &= \frac{2(nl-s)}{n(n-1)}, \\ &= \frac{2(nl-s)}{n(n-1)}, \\ &= \frac{2l-a}{d} + 1, &= \frac{2l+d}{2d} \pm \sqrt{(2a-d)^{2} + 8ds}, \\ &= \frac{2l+d}{2d} \pm \sqrt{(2l+d)^{2} - 8ds}. \end{aligned}$$

GEOMETRICAL PROGRESSION,

in a series of numbers, is a progressive increase or decrease in each successive number by the same multiplier or divisor at each step, as 1, 2, 4, 8, 16, etc., or 243, 81, 37, 9, etc. The common multiplier is called the ratio. Let a = first term, t = last term, r = ratio or constant multiplier, n = n number of terms, m = n term, as let, kd, etc., s = n sum of the terms:

$$l = ar^{n-1}, \qquad = \frac{a + (r-1)s}{r}, \qquad = \frac{(r-1)sr^{n-1}}{r^{n}-1},$$

$$\log l = \log a + (n-1)\log r, \qquad l(\epsilon - l)^{n-1} - a(s-a)^{n-1} = 0.$$

$$R = ar^{n-1}, \qquad \log m = \log a + (m-1)\log r,$$

$$s = \frac{\alpha(r^n - 1)}{r - 1}, \qquad = \frac{r^1 - \alpha}{r - 1}, \qquad = \frac{r^{-1}\sqrt{r^n} - r^{-1}\sqrt{\alpha^n}}{r - 1\sqrt{l} - r^{-1}\sqrt{\alpha}}, \qquad = \frac{lr^n - l}{r^n - r^{n-1}}$$

 $\log m = \log a + (m - 1) \log r.$

$$a = \frac{l}{r^{n-1}}, \qquad = \frac{(r-1)s}{r^{n-1}}. \qquad \log a = \log l - (n-1) \log r,$$

$$r = \frac{n-1}{a}, \qquad = \frac{s-a}{s-l}. \qquad \log r = \frac{\log l - \log a}{n-1}$$

$$r^{n} - \frac{s}{a}r + \frac{s-a}{a} = 0, \qquad r^{n} - \frac{s}{s-l}r^{n-1} + \frac{l}{s-l} = 0,$$

$$n = \frac{\log l - \log a}{\log r} + 1, \qquad = \frac{\log l - \log a}{\log r},$$

$$= \frac{\log l - \log a}{\log (s-a) - \log (s-l)} + 1, \qquad = \frac{\log l - \log [lr - (r-1)s]}{\log r} + 1.$$

Population of the United States.

(A problem in geometrical progression.)

Population.	Years, per cent.	per cent.
81,448,321		per cent.
89,819,449*	26.63	2.39
50,155,783	25.96	2.88
62,622,250	24.86	2.25
76,295,220	21.834	1.994
		Est. 1.840
" 91,554,000	Est. 20.0	" 1.840
	89,819,449* 50,155,783 62,622,250	Population. Years, per cent. 31,445,321 39,815,449* 26.63 50,155,783 25,96 62,622,250 24.86 76,295,220 21.834 Est. 83,577,000

Estimated Population in Each Year from 1870 to 1909.

(Based on the above rates of increase, in even thousands.)

1870 1871 1872 1878	89,818 40,748 41,699 42,673 48,670	1880 1881 1882 1883 1884	50,156 51,281 52,438 53,610 54,813	1890 1891 1892 1893 1894	62,622 68,871 65,145 66,444 67,770	1900 1901 1902 1903	76,295 77,699 79,129 80,585 82,067
1875 1876 1877 1878	44,690 45,878 46,800 47,893	1885 1886 1887 1888	56,043 57,301 58,588 59,903	1895 1896 1897 1898	69,122 70,500 71,906 73,841	1905 1906 1907	88,577 85,115 86,681 88,276
1879	49,011	1889	61,247	1899	74,803	1909	89,900

The above table has been calculated by logarithms as follows:

 $\log r = \log t - \log a + (n-1),$ $\log m = \log a + (m-1) \log r$ $\log n = \log n$ $\log n = \log$ n = 11, n - 1 = 10; diff. + 10 = .00857708add log for 1890 7.7967285 .00857708 $= \log r$

 $= \log a$ $\log \text{ for } 1891 = 7.80530553 \text{ No.} = 68.871 \dots$ add again .00857703

log for 1892 $7.81388256 \text{ No.} = 65.145 \dots$

Compound interest is a form of geometrical progression; the ratio being 1 plus the percentage.

^{*} Corrected by addition of 1,260,078, estimated error of the census of 1870. Census Bulletin No. 16, Dec. 12, 1890,

INTEREST AND DISCOUNT.

Interest is money paid for the use of money for a given time; the factors are:

p, the sum loaned, or the principal:

t, the time in years; r, the rate of interest;

i, the amount of interest for the given rate and time; a = p + i = the amount of the principal with interest

at the end of the time.

Formulæ:

see:
$$i = \text{interest} = \text{principal} \times \text{time} \times \text{rate per cent} = i = \frac{ptr}{100};$$
 $a = \text{amount} = \text{principal} + \text{interest} = p + \frac{ptr}{100};$
 $r = \text{rate} = \frac{100i}{pt};$
 $c = \text{principal} = \frac{100i}{pt} = a - \frac{ptr}{100}.$

$$p = \text{principal} = \frac{100i}{tr} = a - \frac{ptr}{100};$$

$$t = time = \frac{100i}{pr}$$
.

If the rate is expressed decimally as a per cent,—thus, 6 per cent = .06,—the formulæ become

$$i = prt; \ a = p(1+rt); \quad r = \frac{i}{pt}; \quad t = \frac{i}{pr}; \quad p = \frac{i}{tr} = \frac{a}{1+rt}$$

Rules for finding Interest.—Multiply the principal by the rate per annum divided by 100, and by the time in years and fractions of a year.

If the time is given in days, interest = $\frac{\text{principal} \times \text{rate} \times \text{no. of days}}{\text{order}}$ 865 × 100 In banks interest is sometimes calculated on the basis of 360 days to a

year, or 12 months of 80 days each. Short rules for interest at 6 per cent, when 360 days are taken as 1 year: Multiply the principal by number of days and divide by 6000.

Multiply the principal by number of months and divide by 200.

The interest of 1 dollar for one month is ½ cent.

Interest of 100 Dollars for Different Times and Rates.

Time.	2%	3%	4%	5%	6%	8%	10%
1 year	\$2.00	\$8.00	\$4.00	\$5.00	\$6.00	\$8.00	\$10 00
1 month	.164	.25	.381	.414	.50	.663	.831
$1 \text{ day} = \frac{1}{160} \text{ year}$.00558		.01111	.0188g~	.01663	.02222	.02772
1 day = x dx year	.005479	.008219	.010959	.013699	.016438	.0219178	.0273973

Discount is interest deducted for payment of money before it is due. True discount is the difference between the amount of a debt payable at a future date without interest and its present worth. The present worth is that sum which put at interest at the legal rate will amount to the debt when it is due.

To find the present worth of an amount due at future date, divide the amount by the amount of \$1 placed at interest for the given time. The dis-

count equals the amount minus the present worth.

What discount should be allowed on \$103 paid six months before it is due, interest being 6 per cent per annum?

$$\frac{103}{1+1 \times .06 \times \frac{1}{2}} = $100 \text{ present worth, discount} = 3.00.$$

Bank discount is the amount deducted by a bank as interest on money loaned on promissory notes. It is interest calculated not on the actual sum loaned, but on the gross amount of the note, from which the discount is deducted in advance. It is also calculated on the basis of 360 days in the year, and for 3 (in some banks 4) days more than the time specified in the note. These are called days of grace, and the note is not payable till the last of these days. In some States days of grace have been abolished.

What discount will be deducted by a bank in discounting a note for \$103 payable 6 months hence? Six months = 182 days, add 3 days grace = 185 days, $\frac{108 \times 185}{2}$ = \$3.176. 6000

Compound Interest.—In compound interest the interest is added to the principal at the end of each year, (or shorter period if agreed upon). Let p = the principal, r = the rate expressed decimally, n = no of years.

and a the amount:

$$a = \text{amount} = p (1+r)^n$$
; $r = \text{rate} = \sqrt[n]{\frac{a}{p}} - 1$,
 $p = \text{principal} = \frac{a}{(1+r)^n}$; no. of years $= n = \frac{\log a - \log p}{\log (1+r)}$.

Compound Interest Table.

(Value of one dollar at compound interest, compounded yearly, at 8, 4, 5, and 6 per cent, from 1 to 50 years.)

Years.	8%	45	5≴	6,4	Years.	8≰	45	5%	8≴
1	1.08	1.04	1.05	1.06	16	1.6047	1.8730	2.1829	2,5403
2	1.0609	1.0816	1.1025	1.1236	17	1.6528	1.9479	2.2990	2,6928
8	1.0927	1.1249	1.1576	1.1910	18	1.7024	2.0258	2.4066	2,8543
4	1.1255	1.1699	1.2155	1.2625	19	1.7535	2.1068	2.5269	3,0256
5	1.1598	1.2166	1.2768	1.3382	20	1.8061	2.1911	2.6583	3,2071
6	1.1941	1.2653	1.8401	1.4185	21	1,8603	2.2787	2.7859	3.3995
7	1.2299	1.3159	1.4071	1.5086	22	1,9161	2.3699	2.9252	3.6035
8	1.2668	1.3686	1.4774	1.5938	23	1,9736	2.4647	3.0715	3.8197
9	1.3048	1.4233	1.5513	1.6895	24	2,0328	2.5638	3.2251	4.0487
10	1.3439	1.4802	1.6289	1.7908	25	2,0987	2.665 8	3.3863	4.2919
11	1,3842	1.5394	1,7103	1.8983	30	2.4272	8.2438	4.3219	5.7485
12	1,4258	1.6010	1,7958	2.0122	85	2.8138	8.9460	5.5159	7.6862
13	1,4685	1.6651	1,8856	2.1329	40	3.2620	4.8009	7.0398	10.2858
14	1,5126	1.7317	1,9799	2.2609	45	8.7815	5.8410	8.9847	18.7648
15	1,5580	1.8009	2,0789	2.3965	50	4.3838	7.1064	11.4670	18.4204

At compound interest at 3 per cent money will double itself in 231/4 years, at 4 per cent in 17% years, at 5 per cent in 14.2 years, and at 6 per cent in 11.9 years.

EQUATION OF PAYMENTS.

By equation of payments we find the equivalent or average time in which one payment should be made to cancel a number of obligations due at different dates; also the number of days upon which to calculate interest or discount upon a gross sum which is composed of several smaller sums payable at different dates.

Rule. - Multiply each item by the time of its maturity in days from a fixed date, taken as a standard, and divide the sum of the products by the sum of the items: the result is the average time in days from the standard date.

A owes B \$100 due in 30 days, \$200 due in 60 days, and \$300 due in 90 days. In how many days may the whole be paid in one sum of \$600?

$$100 \times 30 + 200 \times 60 + 300 \times 90 = 42,000$$
; $42,000 + 600 = 70$ days, ans.

A owes B \$100, \$200, and \$300, which amounts are overdue respectively 30, 60, and 90 days. If he now pays the whole amount, \$600, how many days interest should be pay on that sum? Ans. 70 days.

PARTIAL PAYMENTS.

To compute interest on notes and bonds when partial payments have been made:

United States Rule. - Find the amount of the principal to the time of the first payment, and, subtracting the payment from it, find the amount of the remainder as a new principal to the time of the next payment.

If the payment is less than the interest, find the amount of the principal

to the time when the sum of the payments equals or exceeds the interest due, and subtract the sum of the payments from this amount.

Proceed in this manner till the time of settlement.

Note.—The principles upon which the preceding rule is founded are:

1st. That payments must be applied first to discharge accrued interest,
and then the remainder, if any, toward the discharge of the principal.
2d. That only unpaid principal can draw interest.

Mercantile Method.—When partial payments are made on short

notes or interest accounts, business men commonly employ the following method:

Find the amount of the whole debt to the time of settlement; also find the amount of each payment from the time it was made to the time of settlement. Subtract the amount of payments from the amount of the debt; the remainder will be the balance due.

ANNUITIES.

An Annuity is a fixed sum of money paid yearly, or at other equal times greed upon. The values of annuities are calculated by the principles of agreed upon. compound interest.

1. Let i denote interest on \$1 for a year, then at the end of a year the amount will be 1+i. At the end of n years it will be $(1+i)^n$.

2. The sum which in n years will amount to 1 is $\frac{1}{(1+i)^n}$ or $(1+i)^{-n}$, or the present value of 1 due in n years.

8. The amount of an annuity of 1 in any number of years n is $\frac{(1+i)^n-1}{i}$.

4. The present value of an annuity of 1 for any number of years n is $1-(1+i)^{-n}$

5. The annuity which 1 will purchase for any number of years n is $1 - (1+i)^{-n}$

6. The annuity which would amount to 1 in n years is $\frac{1}{(1+i)^n-1}$.

Amounts. Present Values, etc., at 5% Interest.

Years	(1)	(2)	(8)	(4)	(5)	(6)
	$(1+i)^n$	$(1+i)^{-n}$	$\frac{(1+i)^n-1}{i}$	$\frac{1-(1+i)^{-n}}{i}$	$\frac{i}{1-(1+i)^{-n}}$	$\frac{i}{(1+i)^n}$
1 2 8 4 5	1.05 1.1025 1.157625 1.215506 1.276282	.952581 .907029 .863838 .822702 .783526	1. 2.05 8.1525 4.810125 5.525631	.952881 1.859410 2.728248 3.545951 4.829477	1.05 .537805 .367209 .282012 .230975	1. .487805 .317209 .282012 .180975
6 7 8 9	1.840096 1.407100 1.477455 1.551828 1.628895	.746215 .710681 .676889 .644609 .618918	6.801913 8.142008 9.549109 11.026564 12.577898	5.075692 5.786378 6.463213 7.107822 7.721785	.197017 .172820 .154722 .140690 .129505	.147018 .122820 .104722 .090690 .079505

Table I .- Annuity Required to Redeem \$1000 in from 1 to 50 Years.

i	' 2	4 5000000000000000000000000000000000000	######################################	8.8.8.8.8 8.8.8.8.8	48858 8	82,854
	_	848 817 173 148	5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5		*******	————— ⊶ ∞ ∞ ∞ ∞ ∞ ∞ ∞
	878	486.62 815.63 230.29 179.18	20.96 20.86 88.88 77.67 68.57	61.08 44.08 40.28 60.58	37.04 38.92 31.15 28.68 19.55	13.80 7.83 7.43 4.06
		082288 88222	82828	84822	82528 	88888
	10	282. 180. 147.	32825	88284	88888	₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩
	4;4	288.74 182.79 148.88	24.67 06.60 92.57 72.25	28.88.4 26.88.67 20.13 20.13	57.22.83 57.24.83 57.45.84	5.28.8 5.88.8 8.89.8
		88588	15.02.02.02	54728	58482	888888
	*	820.8 820.8 184.0 150.7	128 108.5 2.4.2 74.2 1.1	86.2244	24.28 88.22 24.23	7-850 8-85 8-85 8-85 8-85
cent.	*	821.13 821.13 836.88 185.56	25.58 25.58 25.58 25.58 35.58 35.58	67.51 61.10 55.62 50.88 46.70	83.12 89.90 87.04 84.47	18.60 11.17 8.85 7.09
st, per		1				
Rate of Interest,	%	491.42 821.94 287.26 186.49	128.57 110.48 96.44 85.34 76.09	68.48 56.06 51.83 64.68	44228 28282	15.00 11.88 11.88 14.88
te of	8,4	8.73 8.73 8.44 8.64 8.64	29.54 97.44 86.24 77.08	88.75.85 52.55 67.55 74.65	21:888 8:888 8:888	87.50.08 27.20.38
æ		£88825				
	•	289.0% 289.0% 188.9% 154.61	180.51 112.46 98.44 87.24 78.07	70 46 64.08 58.53 53.77	34.38 37.38 34.38 34.38	22.05 18.56 10.78 87.88
	763	88888	131.50 113.46 199.45 79.09	######################################	48.65.88 4.68.65.88 5.58.88	9:7:37
		25 8 8 5 8 2 8 8 5				
	848	498.78 325.14 240.84 190.24 156.56	132.49 114.47 100.46 89.33 80.33	6.8882 6.827.9	24.98 24.67 26.78 27.88	85.85 86.85 86.86 86.86 86.86 86.86
	214	2.18 2.18 1.18 1.58 1.58	25.5 25.5 26.6 27.5 28.8 27.5 27.5 27.5 27.5 27.5 27.5 27.5 27.5	25.55 25.55	86.94 52.67 52.78 52.18 54.18	28.70 13.00 11.02
	-	24 325 191 191 157	## E E 8 E			
	91	495.05 826.72 842.68 192.16 158.53	134.52 116.51 102.52 91.33 82.18	74.56 62.60 62.60 57.83 53.65	84.84.8 86.63.33	22.00.00 56.00.00 56.00.11
5 9						
Years to run,		20.450	F.80.01	25 4 4 5 5 16 5 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	88882	8245

TABLES FOR CALCULATING SINKING-FUNDS AND PRESENT VALUES. PRESENT

Engineers and others connected with municipal work and industrial enterprises often find it necessary to calculate payments to sinking-funds which will provide a sum of money sufficient to pay off a bond issue or other debt at the end of a given period, or to determine the present value of certain annual charges. The accompanying tables were computed by Mr. John W. Hill, of Cincinnati, Engly News, Jan. 25, 1894.

Table I (opposite page) shows the annual sum at various rates of interest required to not \$1000 in from 2 to 50 years, and Table II shows the present value at various rates of interest of an annual charge of \$1000 for from 5 to

value at various rates of interest of an annual charge of \$1000 for from 5 to

50 years, at five-year intervals and for 100 years.

Table II.—Capitalization of Annuity of \$1000 for from 5 to 100 Years.

Years.	Rate of Interest, per cent.							
	21/4	8	814	4	41%	5	51/6	6
	8,752.17	8,530.18 11,937.80		8,110.74 11,118.06	7,912.67 10,789.42	7,721.78 10,879.58	7,537.54 10,037.48	7,860.19 9,712.30
25 20 25	18,424.67 20,930.59 28,145.81	17,418.01 19,600.21 21,487.04	16,481.28 18,891.85 20,000.48	15,621.93 17,291.86 18,664.87	14,828.12 16,288.77 17,460.89	14,098.86 15,872.86 16,874.86	18,413.82 14,538.68 15,890.48	12,788.88 13,764.85 14,488.65
45 50	25,108.58 26,838.15 28,869.48 36,614.21	24,519.49	23,455.21	20,719.89 21,482.08	19,156.24 19,761.98	17,778.99 18,255.86	16,547.65 16,931.97	15,455.85 15,761.87

WEIGHTS AND MEASURES.

Long Measure.-Measures of Length.

12 inches = 1 foot. 3 feet = 1 yard. 1760 yards, or 5280 feet = 1 mile.

Additional measures of length in occasional use: 1000 mils = 1 inch; 4 inches = 1 hand; 9 inches = 1 span; 2½ feet = 1 military pace; 2 yards = 1 fathon; 5½ yards, or 16½ feet = 1 rod (formerly also called pole or perch).

Old Land Measure.—7.92 inches = 1 link; 100 links, or 66 feet, or 4 rods = 1 chain; 10 chains, or 220 yards = 1 furlong; 8 furlongs = 1 mile; 10 square chains = 1 acre.

Nautical Measure.

6080.26 feet, or 1.15156 stat-= 1 nautical mile, or knot.* ute miles 8 nautical miles = 1 league. 60 nautical miles, or 69.168 = 1 degree (at the equator). statute miles = circumference of the earth at the equator. 360 degrees

^{*}The British Admiralty takes the round figure of 6080 ft. which is the length of the "measured mile" used in trials of vessels. The value varies from 6080.25 to 6088.44 ft. according to different measures of the earth's diameter. There is a difference of opinion among writers as to the use of the word "knot" to mean length or a distance—some holding that it should be used only to denote a rate of speed. The length between knots on the log line is 1/120 of a nautical mile, or 50.7 ft., when a half-minute glass is used so that a speed of 10 knots is equal to 10 nautical miles per hour.

Square Measure.—Measures of Surface.

144 square inches, or 183.35 circular inches = 1 square foot. 9 square feet = 1 square yard. 8014 square yards, or 27214 square feet 10 sq. chains, or 160 sq. rods, or 4840 sq. = 1 square rod. = 1 acre. yards, or 48560 sq. feet, 640 acres = 1 square mile.

An acre equals a square whose side is 208.71 feet.

Circular Inch; Circular Mil.—A circular inch is the area of a circle 1 inch in diameter = 0.7854 square inch.

1 square inch = 1.2732 circular inches.
A circular mil is the area of a circle 1 mil, or .001 inch in diameter.
1000° or 1,000,000 circular mils = 1 circular inch.

1 square inch = 1,273,239 circular mils.

The mil and circular mil are used in electrical calculations involving the diameter and area of wires.

Solid or Cubic Measure.—Measures of Volume.

1728 cubic inches = 1 cubic foot. 27 cubic feet = 1 cubic yard. 1 cord of wood = a pile, $4 \times 4 \times 8$ feet = 128 cubic feet. 1 perch of masonry = $16\frac{1}{2} \times 1\frac{1}{2} \times 1$ foot = $24\frac{1}{4}$ cubic feet.

Liquid Measure.

4 gills = 1 pint. 2 pints = 1 quart. = 1 gallon { U. S. 231 cubic inches. Eng. 277.274 cubic inches. 4 quarts 811/2 gallons = 1 barrel. 42 gali na = 1 tierce. = 1 hogshead. 2 barrels, or 63 gallous 84 gallons, or 2 tierces = 1 puncheon. 2 hogsheads, or 126 gallons = 1 pipe or butt. 2 pipes, or 3 puncheons = 1 tun.

A gallon of water at 62° F, weighs 8.8856 lbs.
The U. S. gallon contains 231 cubic Inches; 7.4805 gallons = 1 cubic foot.
A cylinder 7 in, diam. and 6 in, high contains 1 gallon, very nearly, or 230.9
cubic inches. The British Imperial gallon contains 277.274 cubic inches
= 1.2032 U. S. gallon, or 10 lbs. of water at 63° F.
The Miner's Inch.—(Western U. S. for measuring flow of a stream

The term Miner's Inch is more or less indefinite, for the reason that California water companies do not all use the same head above the centre of the aperture, and the inch varies from 1.36 to 1.73 cubic feet per minute each; but the most common measurement is through an aperture 2 inches high and whatever length is required, and through a plank 11 inches thick. The lower edge of the aperture should be 2 inches above the bottom of the measuring-box, and the plank 5 inches high above the aperture, thus making a 6-inch head above the centre of the stream. Each square inch of this opening represents a miner's inch, which is equal to a flow of 1; cubic feet per minute.

Apothecaries' Fluid Measure.

60 minims = 1 fluid drachm. 8 drachms = 1 fluid ounce.

In the U.S. a fluid ounce is the 128th part of a U.S. gallon, or 1.805 cu. ins. It contains 456.8 grains of water at 39° F. In Great Britain the fluid ounce is 1.732 cu, ins. and contains a ounce avoirdupois, or 487.5 grains of water at 62º F.

Dry Measure, U. S.

8 quarts = 1 peck.4 pecks = 1 bushel. 2 pints = 1 quart. The standard U. S. bushel is the Winchester bushel, which is in cylinder form, 181/4 inches diameter and 8 inches deep, and contains 2150.42 cubic

A struck bushel contains 2150.42 cubic inches = 1.2445 cu. ft.; 1 cubic foot = 0.80556 struck bushel. A heaped bushel is a cylinder 18½ inches diameter and 8 inches deep, with a heaped cone not less than 6 inches high. It is equal to 1½ struck bushels.

The British Imperial bushel is based on the Imperial gallon, and contains 8 such gallons, or 2218.192 cubic inches = 1.2887 cubic feet. The English quarter = 8 Imperial bushels.

Capacity of a cylinder in U. S. gallons = square of diameter, in inches × height in inches × .0034. (Accurate within 1 part in 100,000,)

Capacity of a cylinder in U. S. bushels = square of diameter in inches × height in inches × .0003652.

Shipping Measure.

Register Ton.—For register tonnage or for measurement of the entire internal capacity of a vessel:

100 cubic feet = 1 register ton.

This number is arbitrarily assumed to facilitate computation. Shipping Ton .- For the measurement of cargo:

40 cubic feet = { 1 U. S. shipping ton. 31.16 Imp. bushels. 32.143 U. S. " 42 cubic feet = { 1 British shipping ton. 32,719 Imp. bushels. 33,75 U. S. "

Carpenter's Rule.—Weight a vessel will carry = length of keel × breadth at main beam × depth of hold in feet +95 (the cubic feet allowed for a ton). The result will be the tonnage. For a double-decker instead of the depth of the hold take half the breadth of the beam.

Measures of Weight.—Avoirdupois, or Commercial Weight.

```
16 drachms, or 437.5 grains = 1 ounce. oz.
 16 ounces, or 7000 grains
                              = 1 pound, lb.
 28 pounds
                              = 1 quarter, qr.
= 1 hundredweight, cwt. = 112 lbs.
  4 quarters
  20 hundred weight
                               = 1 ton of 2240 pounds, or long ton.
2000 pounds
                               = 1 net, or short ton.
2204.6 pounds
                               = 1 metric ton.
         1 stone = 14 pounds; 1 quintal = 100 pounds.
```

The drachm, quarter, hundredweight, stone, and quintal are now seldom used in the United States.

Troy Weight.

24 grains = 1 pennyweight, dwt. 20 pennyweights = 1 ounce, oz. = 480 grains. 12 ounces = 1 pound, lb. = 5760 grains.

Troy weight is used for weighing gold and silver. The grain is the same in Avoirdupois, Troy, and Apothecaries' weights. A carat, used in weighing diamonds = 8.168 grains = .205 gramme.

Apothecaries' Weight.

```
20 grains = 1 scruple, D
8 scruples = 1 drachm, 3
8 drachms = 1 ounce, 3
                               = 60 grains.
                               = 480 grains.
12 ounces = 1 pound, lb.
                               = 5760 grains.
```

To determine whether a balance has unequal arms.—
After weighing an article and obtaining equilibrium, transpose the article
and the weights. If the balance is true, it will remain in equilibrium; if To weight correctly on an incorrect balance.—First, by substitution. Put the article to be weighed in one pan of the balance

counterpoise it by any convenient heavy articles placed on the other pan. Remove the article to be weighed and substitute for it standard weighted until equipoise is again established. The amount of these weights is the

weight of the article.

Second, by transposition. Determine the apparent weight of the article as usual, then its apparent weight after transposing the article and the weights. If the difference is small, add half the difference to the smaller of the apparent weights to obtain the true weight. If the difference is 2 per cent the error of this method is 1 part in 10,000. For larger differences, or to obtain a perfectly accurate result, multiply the two apparent weights together and extract the square root of the product.

Circular Measure.

60 seconds, " = 1 minute, '.
60 minutes, ' = 1 degree, °.
90 degrees = 1 quadrant.
860 " = circumference.

Time.

60 seconds = 1 minute. 60 minutes = 1 hour. 24 hours = 1 day. 7 days = 1 week.

865 days, 5 hours, 48 minutes, 48 seconds = 1 year.

By the Gregorian Calendar every year whose number is divisible by 4 is a leap year, and contains 365 days, the other years containing 365 days, except that the centesimal years are leap years only when the number of the year is divisible by 400.

The comparative values of mean solar and sidereal time are shown by the

following relations according to Bessel:

865.24222 mean solar days = 366.24222 sidereal days, whence 1 mean solar day = 1.00273791 sidereal days; 1 sidereal day = 0 99726987 mean solar day; 24 hours mean solar time = 248 3m 56°.555 sidereal time; 24 hours sidereal time = 228 56m 4.091 mean solar time,

whence 1 mean solar day is 3^m 55^s.91 longer than a sidereal day, reckoned in mean solar time.

BOARD AND TIMBER MEASURE.

Board Measure.

In board measure boards are assumed to be one inch in thickness. To obtain the number of feet board measure (B. M.) of a board or stick of square timber, multiply together the length in feet, the breadth in feet, and the thickness in inches.

To compute the measure or surface in square feet.—When all dimensions are in feet, multiply the length by the breadth, and the pro-

duct will give the surface required.

When either of the dimensions are in inches, multiply as above and divide the product by 12.
When all dimensions are in inches, multiply as before and divide product.

When all dimensions are in inches, multiply as before and divide product by 144.

Timber Measure.

To compute the volume of round timber.—When all dimensions are in feet, multiply the length by one quarter of the product of the mean girth and diameter, and the product will give the measurement in cubic feet. When length is given in feet and girth and diameter in inches, divide the product by 144; when all the dimensions are in inches, divide by 1728.

To compute the volume of square timber.—When all dimensions are in feet, multiply together the length, breadth, and depth; the product will be the volume in cubic feet. When one dimension is given in inches, divide by 12; when two dimensions are in inches, divide by 144; when all three dimensions are in inches, divide by 144; when all three dimensions are in inches, divide by 1728.

Contents in Feet of Joists, Scantling, and Timber.

Length in Feet.

Size.	12	14	16	18	20	22	24	26	28	80
			Feet	Boar	i Mea	sure.				
2 × 4	8	9	11	12	18	15	16	17	19	20
2 × 6 2 × 8	12	14 19	16	18	20	22 29	24	26	28 37	80
2 × 10	16 20	98	21 27	24 30	27 38	87	82 40	85	47	40 50
2 × 12	24	23 28	32	36	40	44	48	48 52	56	60
2 × 14	28	33	87	42	47	51	56	61	65	70
3 × 8	24	28	32	36	40	44	48	52	56	60
3 × 10	30	35	40	45	50	55	60	65	70	75
8 × 12	86	42	48	54	60	66 77	72 84	78	84	90
3 × 14	42	49	56	63	70	77	84	91	98	105
4 × 4	16	19	21	24	27	29	85	85	37	40
4 × 6	24	28	82	36	40	44	48	52	56	60
4 × 8	82	87	43	48	58	59	64	69	75	80
4 × 10 4 × 12	40 48	47 56	53 64	60 72	67 80	73 88	80 96	87 104	98 112	100 120
4 × 16							3 0	104	114	120
4 × 14	56	65	75	84	93	103	112	121	181	140
6 × 6	86	42	48	54	60	66	72	78	84	90
6 × 8 6 × 10	48	56 70	64	72 90	80	.88	96	104	112	120
6 × 10	60 72	84	80 96	108	100 120	110 182	120 144	180 156	140 168	150 180
V / 10	۱~ ا	04	- 50	100	120	105	144	100	100	100
6×14	84	98	112	126	140	154	168	182	196	210
8 × 8	64	75	85	96	107	117	128	139	149	160
8 × 10	80	93	107	120	188	147	160	178	187	200
8 × 12 8 × 14	96 112	112 181	128 149	144 168	160 187	176 205	192 224	208 243	224 261	240 280
0 / 14	11.0	101	140	100	101	200	201	240	201	200
10×10	100	117	138	150	167	183	200	217	233	250
10 × 12	120	140	160	180	200	220	240	260	280	800
10 × 14	140	168	187	210	283	257	280	803	827	850
12 × 12 12 × 14	144 168	168 196	192 224	216 252	240 280	264 308	288 336	312 364	336 392	360 420
14 人 14	100	190	£24	202	400	900	030	904	592	4:20
14 × 14	196	229	261	294	827	859	392	425	457	490

FRENCH OR METRIC MEASURES.

The metric unit of length is the metre = 89-37 inches.

The metric unit of weight is the gram = 15.482 grains.

The following prefixes are used for subdivisions and multiples; Milli = $\frac{1}{1000}$, Centi = $\frac{1}{100}$, Deca = 10, Hecto = 100, Kilo = 1000, Myria = 10,000.

FRENCH AND BRITISH (AND AMERICAN) EQUIVALENT MEASURES.

Measures of Length.

FRENCH.

1 metre

BRITISH and U. S.

= 39.37 inches, or 3.28083 feet, or 1.09361 yards.

.8048 metre = 1 foot. 1 centimetre = .8937 inch.

254 centimetres = 1 inch.

1 milimetre = .03937 inch, or 1/25 inch, nearly.

25 4 millimetres = 1 inch.

1 kilometre = 1098,61 yards, or 0.62187 mile.

```
Measures of Surface.
                   FRENCH.
                                                BRITISH and U. S.
                                          = \ \ \frac{10.764 square feet,}{1.196 square yards.}
                 1 square metre
               886 square metre
                                          = 1 square yard.
= 1 square foot.
             .0929 square metre
                  1 square centimetre = .155 square inch.
             6.452 square centimetres = 1 square inch.
                  1 square millimetre = .00155 sq. in. = 1978.5 circ. mils.
     645.2 square millimetres = 1 square inch.
1 centiare = 1 sq. metre = 10.764 square feet.
     1 are = 1 sq. decametre
1 hectare = 100 ares
                                         = 1076.41
                                                     **
                                                              " = 2.4711 acres.
                                         = 107641
      1 sq. kilometre
                                         = .886109 \text{ sq. miles} = 247.11
                                         = 38.6109 "
      1 sq. myriametre
                                  Of Volume.
                    FRENCH.
                                                BRITISH and U. S.
                                               § 35.814 cubic feet.
1.308 cubic yards.
                    1 cubic metre
                                            = 1 cubic yard.
= 1 cubic foot.
                .7645 cubic metre
              .02832 cubic metre
                                            1 cubic decimetre
               28.32 cubic decimetres = 1 cubic foot.
                    1 cubic centimetre = .061 cubic inch.
              16.387 cubic centimetres = 1 cubic inch.
                                          .061 cubic inch.
1 cubic centimetre = 1 millilitre =
1 centilitre =
                                            .610
                                                   66
                                          6.102
1 decilitre =
                                      =
                                                   64
                                                               = 1.05671 quarts, U. S.
1 litre
             = 1 cubic decimetre = 61.028
1 hectolitre or decistere = 3.5314 cubic feet = 2.8375 bushels, "
1 stere, kilolitre, or cubic metre = 1.308 cubic yards = 28.37 bushels, "
                                  Of Capacity.
                 FRENCH.
                                                       BRITISH and U.S.
                                               61.023 cubic inches,
                                               .03581 cubic foot,
         1 litre (= 1 cubic decimetre) =
                                                .2642 gallon (American).
                                              2.202 pounds of water at 62° F.
   28,317 litres
                                          = 1 cubic foot
    4.548 litres
                                          = 1 gallon (British).
= 1 gallon (American).
    3.785 litres
                                  Of Weight.
               FRENCH.
                                                  BRITISH and U. S.
              1 gramme
                                         = 15.432 grains.
           .0648 gramme
                                        = 1 grain.
          28.85 gramme
1 kilogramme
                                        = 1 ounce avoirdupois.
                                        = 2.2046 pounds.
          .4586 kilogramme
                                         = 1 pound.
              1 tonne or metric ton = $\int \text{.9842 ton of 2240 pounds,} \\
10 kilogrammes = \int \text{.9842 ton of 2240 pounds,} \\
2004.6 pounds.
           1000 kilogrammes
          1.016 metric tons
                                              1 ton of 2240 pounds.
           1016 kilogrammes
```

Mr. O. H. Titmann, in Bulletin No. 9 of the U. S. Coast and Geodetic Survey, discusses the work of various authorities who have compared the yard and the metre, and by referring all the observations to a common standard has succeeded in reconciling the discrepancies within very narrow limits. The following are his results for the number of inches in a metre according to the comparisons of the authorities named:

1817.	Hassler	89,86994	inches
1818.	Kater	89.36990	46
1835.	Bailv	39.36978	44
1866.	Clarke	89.86970	66
	Comstock		66
T	he mean of these is	89 86982	66

METRIC CONVERSION TABLES.

The following tables, with the subjoined memoranda, were published in 1890 by the United States Coast and Geodetic Survey, office of standard weights and measures, T. C. Mendenhall, Superintendent.

Tables for Converting U. S. Weights and Measures— Customary to Metric.

LINEAR.

	Inches to Milli- metres.	Feet to Metres.	Yards to Metres.	Miles to Kilo- metres.
1 =	25,4001	0.804801	0.914402	1.60935
2 =	50.8001	0.609601	1.828804	3.21869
3 =	76.2002	0.914402	2.743205	4.82804
i =	101.6002	1.219202	8.657607	6.43739
5 =	127.0008	1.524008	4.572009	8.04674
3 =	152.4003	1.828904	5.486411	9.65608
′ ==	177.8004	2.183604	6.400818	11.26548
=	203,2004	2.488405	7.815215	12.87478
=	228,6005	2.743205	8.229616	14.48412

SQUARE.

	Square Inches to Square Centi- metres.	Square Feet to Square Deci- metres.	Square Yards to Square Metres.	Acres to Hectares.
=	6.453	9.290	0.836	0.4047
=	12.903	18.581	1.672	0.8094
=	19.855	27.871	2.508	1.2141
=	25.807	37.161	8.344	1.6187
=	32.258	46.452	4.181	2.0231
=	88.710	55.742	5.017	2.4281
=	45,161	65.032	5.858	2.8328
=	51.618	74.823	6,689	3 2375
=	58.065	88.618	7.525	8.6422

CUBIC.

	Cubic Inches to Cubic Centi- metres.	Cubic Feet to Cubic Metres.	Cubic Yards to Cubic Metres.	Bushels to Hectolitres.
 =	16.387	0.02832	0.765	0.35242
=	32.774	0.05668	1.529	0.70485
=	49.161	0.08195	2.294	1.06727
=	65.549	0.11827	3.058	1.40969
=	81.986	0.14158	3.823	1.76211
=	98.323	0.16990	4.587	2.11454
'=	114.710	0.19822	5.352	2.46696
=	131.097	0.22654	6.116	2.81938
=	147.484	0.25485	6.881	8.17181

ARITHMETIC.

CAPACITY.

	Fluid Drachms to Millilitres or Cubic Centi- metres.	Fluid Ounces to Millilitres.	Quarts to Litres.	Gallons to
1 =	3.70	29.57	0 94636	3.7854
2 =	7.89	59.15	1 89272	7.5708
8 =	11.09	88.72	2 83908	11.8568
4 =	14.79	118.30	3 78544	15.1417
5 =	18.48	147.87	4 78180	18.9272
6 =	22.18	177.44	5.67816	22.7126
7 =	25.88	207.02	6.62452	26.4980
8 =	29.57	286.59	7.57088	80.2835
9 =	33.28	266.16	8.51724	84.0689

WEIGHT.

	Grains to Milligrammes.	Avoirdupois Ounces to Grammes.	Avoirdupois Pounds to Kilo- grammes.	Troy Oun Gramm
1 = 2 = 3 = 4 = 5 =	64.7989 129.5978 194.3968 259.1957 323.9946	28.3495 56.6991 85.0486 113.3981 141.7476	0.45859 0.90719 1.86078 1.81437 2.26796	81.10 62.20 93.81 124.41;
6 = 7 = 8 = 9 =	388.7985 453.5924 518.3914 583.1908	170.0972 198.4467 226.7962 255.1457	2.72156 3.17515 3.62874 4.08233	186.626 217.724 248.827 279.931

1 chain 20.1169 metres.

259 hectares. 1.829 metres. 1 square mile = 1 fathom =

1 nautical mile = 1853.27 metres.
1 foot = 0.304801 metre.
1 avoir pound = 453.5924277 gram.
15432.35639 grains = 1 kilogramme.

Tables for Converting U. S. Weights and Measure Metric to Customary.

LINEAR.

ĺ	Metres to	Metres to	Metres to	Kilometre
	Inches.	Feet.	Yards.	Miles
1 = 2 = 8 = 4 = 5 =	89.8700	3.28083	1.098611	0.6218
	78.7400	6.56167	2.187222	1.2427
	118.1100	9.84250	3.280838	1.8641
	157.4800	13.12333	4.374444	2.4854
	196.8500	16,40417	5.468056	8.1068
6 = 7 = 8 = 9 =	286,2200	19.68500	6.561667	8.7282
	275,5900	22.96583	7.655278	4.8495
	314,9600	26.24667	8.748889	4.9709
	854,3300	29.52750	9.842500	5.5928

SQUARE.

	Square Centi- metres to Square Inches.	Square Metres to Square Feet.	Square Metres to Square Yards.	Hectares to Acres.
1 =	0.1550	10.764	1.196	2.471
2 =	0.3100	21.528	2.392	4.942
8 =	0.4650	32.292	8.588	7.418
4 =	0.6200	43.055	4.784	9.884
5 =	0.7750	53.819	5.980	12.355
6 =	0.9900	64.588	7.176	14.826
7 =	1.0850	75.347	8.372	17.297
8 =	1.2400	86.111	9.568	19.768
9 =	1.3950	96.874	10.764	22.289

CUBIC.

	Cubic Centi- metres to Cubic Inches.	Cubic Deci- metres to Cubic Inches.	Cubic Metres to Cubic Feet.	Cubic Metres to Cubic Yards.
1 =	0.0610	61.028	35.314	1.308
2 =	0.1220	122.047	70.629	2.616
8 =	0.1831	188.070	105.943	3.924
4 =	0.2441	244.093	141.258	5.232
5 =	0.3051	305.117	176.572	6.540
6 =	0.3661	366,140	211.887	7.848
7 =	0.4272	427,163	247.201	9.156
8 =	0.4882	488,187	282.516	10.464
9 =	0.5492	549,210	817.830	11.771

CAPACITY.

	Millilitres or Cubic Centi- litres to Fluid Drachins.	Centilitres to Fluid Ounces.	Litres to Quarts.	Dekalitres to Gallons.	Hektolitres to Bushels.
1 = 2 = 3 = 4 = 5 =	0.27	0.338	1.0567	2.6417	2.8875
	0.54	0.676	2.1184	5.2834	5.6750
	0.81	1.014	3.1700	7.9251	8.5125
	1.08	1.352	4.2267	10.5668	11.3500
	1.35	1.691	5.2834	18.2085	14.1875
6 =	1.62	2.029	6.8401	15.8502	17.0250
7 =	1.89	2.368	7.8968	18.4919	19.8625
8 =	2.16	2.706	8.4534	21.1386	22.7000
9 =	2.43	3.048	9.5101	28.7758	25 5875

WEIGHT.

•	Milligrammes to Grains.	Kilogrammes to Grains.	Hectogrammes (100 grammes) to Ounces Av.	Kilogram to Pour Avoirduj
1 =	0.01543	15432.36	3.5274	2.2046
2 =	0.03086	30864.71	7.0548	4.4092
8 =	0.04630	46297.07	10.5832	6.6138
4 =	0.06178	61729.43	14.1096	8.8184
5 =	0.07716	77161.78	17.6370	11.0281
6 =	0.09259	92594.14	21.1644	18.2277
7 =	0.10803	108026.49	24.6918	15.4828
8 =	0.12346	123458.85	28.2192	17.6369
9 =	0.13889	138891.21	81.7466	19.8415

WEIGHT-(Continued).

	Quintals to	Milliers or Tonnes to	Grammes to Ou
	Pounds Av.	Pounds Av.	Troy.
1 = 2 = 8 = 4 =	220.46	2204 6	0.03215
	440.92	4409.2	0.06430
	661.88	6613.8	0.09645
	881.84	8818.4	0.12860
5 =	1102.30	11028.0	0.16075
6 =	1822.76	13227.6	0.19290
7 =	1543.22	15482.2	0.22505
8 =	1768.68	17636.8	0.25721
9 =	1984.14	19841.4	0.28936

The only authorized material standard of customary length is Troughton scale belonging to this office, whose length at 59°.62 Fahr. forms to the British standard. The yard in use in the United States is t fore equal to the British yard.

The only authorized material standard of customary weight is the pound of the mint. It is of brass of unknown density, and therefor suitable for a standard of mass. It was derived from the British stan Troy pound of 1758 by direct comparison. The British Avoirdupois p was also derived from the latter, and contains 7000 grains Troy.

Troy pound of 1758 by direct comparison. The British Avoirdupois p was also derived from the latter, and contains 7000 grains Troy.

The grain Troy is therefore the same as the grain Avoirdupois, and pound Avoirdupois in use in the United States is equal to the British p Avoirdupois.

The metric system was legalized in the United States in 1866.

By the concurrent action of the principal governments of the worl International Bureau of Weights and Measures has been established Paris.

The International Standard Metre is derived from the Mètre des Arch and its length is defined by the distance between two lines at 0° Centigr on a platinum-iridium bar deposited at the International Bureau.

The International Standard Kilogramme is a mass of platinum-iric deposited at the same place, and its weight in vacuo is the same as the Kilogramme des Archives.

Copies of these international standards are deposited in the offic standard weights and measures of the U.S. Coast and Geodetic Survey The litre is equal to a cubic decimetre of water, and it is measured by

quantity of distilled water which, at its maximum density, will counter; the standard kilogramme in a vacuum; the volume of such a quantit water being, as nearly as has been ascertained, equal to a cubic decime

COMPOUND UNITS.

Measures of Pressure and Weight.

1 lb. per square inch.	= { 144 lbs. per square foot. 2.0355 ins. of mercury at 82° F. 2.0416 " " 62° F. 2.309 ft. of water at 62° F. 27.71 ins. " 62° F.
1 ounce per sq. in.	= { .1276 in. of mercury at 62° F. 1.782 ins. of water at 62° F.
1 atmosphere (14.7 lbs. per sq. in.	2116.3 lbs. per square foot. 33,947 ft. of water at 62° F. 30 ins. of mercury at 62° F. 29,922 ins. of mercury at 32° F. 760 millimetres of mercury at 32° F.
1 inch of water at 62° F.	= { .08609 lb. or .5774 oz. per sq. in. 5.196 lbs. per square foot0736 in. of mercury at 62° F.
1 inch of water at 32° F.	= \ 5.2021 lbs. per square foot036125 lb. " " inch.
1 foot of water at 62° F.	$= \begin{cases} .433 \text{ lb. per square inch.} \\ 62.355 \text{ lbs.} & \text{foot.} \end{cases}$
1 inch of mercury at 62° F.	= { .491 lb. or 7.86 oz. per sq. in. 1.132 ft. of water at 62° F. 13.58 ins. " " 62° F.

Weight of One Cubic Foot of Pure Water.

At 32° F. (freezing-point)	62.418 lbs.
" 39 1° F. (maximum density)	62.425 "
" 69° F (standard temperature)	62.355 "
" 212º F. (boiling point, under 1 atmosphere)	59.76 "
American gallon = 231 cubic ins. of water at 62° F.	= 8.3356 lbs.
British " = 277.274" " " "	= 10 lbs.

Measures of Work, Power, and Duty.

Work.—The sustained exertion of pressure through space.
Unit of work.—One foot-pound, i.e., a pressure of one pound exerted through a space of one foot.

Horse-power.—The rate of work. Unit of horse-power = 33,000 ft.-lbs. per minute, or 550 ft.-lbs. per second = 1,980,000 ft.-lbs. per hour.

Heat unit = heat required to raise 1 lb. of water 1° F. (from 39° to 40°).

Horse-power expressed in heat units = \frac{33000}{778} = 42.416 heat units per minute = .707 heat unit per second = 2245 heat units per hour.

1 b. of fuel per H. P. per hour= \begin{cases} \frac{1,980,000}{2,545 heat units} & \text{min} & \text{min} \end{cases}.

1,000,000 ft.-lbs. per lb. of fuel = 1.98 lbs. of fuel per H. P. per hour.

Velocity.—Feet per second = $\frac{5280}{8600} = \frac{22}{15} \times \text{miles per hour.}$

Gross tons per mile = $\frac{1760}{2240} = \frac{11}{14}$ lbs. per yard (single rail.)

French and British Equivalents of Compound Units.

FREACA.							
I gramme per square millimetre	=	1.422 lbs. per square inch.					
l kilogramme ner sauare	=	1422 32					
1 centimetre	=						
1.0336 kg. per sq. cm. = 1 atmosphere	=	14.7					
0.070006 kilogramme per square centimetre	=						
1 gramme per litre	=						
1 kilogrammetre	==	7.2330 foot-pounds.					

WIRE AND SHEET-METAL GAUGES COMPAR

Number of Gauge.	Birmingham (or Stubs' Iron) Wire Gauge.	American or Brown and Sharpe Gauge.	Roebling's and Washburn & Moen's Gauge.	Stubs' Steel Wire Gauge. (See also p. 29.)	Wire (dard	U. S. Standard Gauge for Sheet and Plate Iron and St⊷l, Gegal Standard since July 1, 1893.)
0000000 000000 00000 0000 000 000 000	inch. .454 .425 .38 .34 .38 .289 .203 .203 .18 .165 .144 .12 .09 .063 .072 .065 .042 .085 .022 .028 .028 .022 .03 .016 .014 .013 .012 .010 .008 .007 .006 .004	inch. 46 40944 3648 32486 32486 32942 20431 18194 16202 14428 12849 11449 11089 09074 08081 07196 0408 05707 05082 04526 0408 05707 05082 04526 0408 05707 05082 04101 0179 01964 01126 01002 00893 00795 00708 0063 0063	inch49 .46 .43 .898 .802 .881 .807 .283 .244 .225 .207 .192 .148 .125 .092 .068 .072 .088 .028 .028 .028 .028 .028 .028 .02		inch500 .4644 .432 .4 .4 .372 .348 .324 .3 .276 .252 .232 .192 .176 .16 .144 .092 .062 .076 .066 .04 .036 .036 .028 .028 .028 .018 .0164 .0186 .0194 .0108 .0194 .0108 .0194 .0108 .0194 .0108 .0194 .0108 .0108 .01092 .008 .0092 .008 .0092 .008 .0092 .008 .0092 .0093 .0092 .0093 .0094 .0096	millim. 12.7 11.78 10.97 10.97 10.97 10.97 10.98 8.23 7.60 6.4 5.88 4.88 7.60 6.4 5.88 4.87 4.06 6.3.25 2.96 4.87 4.06 3.25 1.83 1.63 1.42 1.22 1.02 91 81 1.71 61 556 518 88 35 31 68 31 1.63 31 31 32 32 32 32 32 32 32 32 32 32 32 32 32	inch5 .469 .438 .406 .875 .344 .313 .281 .281 .282 .296 .25 .234 .219 .503 .172 .156 .141 .125 .109 .094 .07 .0625 .0563 .05 .0488 .0375 .0488 .0172 .0156 .0141 .0125 .021 .0156 .0141 .0125 .021 .0101 .0094 .0086 .0077 .0086*

EDISON, OB CIRCULAR MIL GAUGE, FOR ELECTRICAL WIRES.

Gange Num- ber.	Circular Mils.	Diam- eter in Mils.	Gauge Num- ber.	Circular Mils.	Diam- eter in Mils.	Gauge Num- ber.	Circular Mils.	Diam- eter in Mils.
8	8,000	54.78	70	70,000	264.58	190	190,000	435.89
5 8	5,000	70.72	75	75,000	273.87	200	200,000	447.22
8	8,000	89.45	80	80,000	282.85	2:20	220,000	469.05
12	12,000	109.55	85	85,000	291.55	240	240,000	489.90
15	15,000	122.48	90	90,000	800.00	260	260,000	509.91
20	20,000	141.43	95	95,000	308.23	280	280,000	529.16
25	25,000	158.12	100	100,000	316.23	300	800,000	547.73
80	30,000	178.21	il 110	110,000	831.67	3:20	320,000	565.69
85	35,000	187.09	120	120,000	846.42	840	340,000	583.10
40	40,000	200.00	130	130,000	360.56	360	860,000	600.00
45	45.000	212.14	140	140,000	874.17	1		
50	50,000	228.61	150	150,000	387.30	į	1	ļ
55	55,000	234.58	160	160,000	400.00	ll .	1	1
60	60,000	244.95	170	170,000	412.82	I	1	
65	65,000	254.96	180	180,000	424.27	ll .	l	ł

TWIST DRILL AND STEEL WIRE GAUGE.

(Morse Twist Drill and Machine Co.)

No.	Size.	No.	Size.	No.	Size.	No.	Size.	No.	Size.	No.	Size.
1 2 8 4 5 6 7 8 9	inch. .2280 .2210 .2130 .2090 .2055 .2040 .2010 .1994 .1960	11 12 18 14 15 16 17 18 19	inch .1910 .1890 .1850 .1620 .1800 .1770 .1780 .1695 .1660 .1610	21 22 23 24 25 26 27 28 29 30	inch, .1590 .1570 .1540 .1520 .1495 .1470 .1440 .1480 .1285	31 32 33 34 35 36 37 38 39 40	inch. .1200 .1160 .1180 .1110 .1100 .1065 .1040 .1015 .0995	41 42 48 44 45 46 47 48 49 50	inch. .0960 .0985 .0890 .0860 .0820 .0810 .0785 .0760 .0780	51 52 53 54 55 56 57 58 59 60	inch. .0670 .0635 .0595 .0550 .0465 .0480 .0420

STUBS' STEEL WIRE GAUGE.

(For Nos. 1 to 50 see table on page 28.)

No.	Size.	No.	Size.	No.	Size.	No.	Size.	No.	Size.	No.	Size.
Z Y X W V U T 8 R Q	inch. .418 .404 .897 .386 .377 .368 .358 .348 .339 .332	PON M LKJIHG	inch. .823 .316 .302 .295 .290 .281 .277 .272 .266 .261	FEDCBA1 to 50	inch. .257 .250 .246 .242 .288 .284 (See page 28	51 52 53 54 55 56 57 58 59 60	inch. .066 .068 .058 .055 .050 .045 .042 .041 .040	61 62 63 64 65 66 67 68 69 70	inch. .088 .087 .036 .085 .083 .082 .081 .080 .029	71 72 78 74 75 76 77 78 79 80	inch. .026 .024 .023 .022 .020 .018 .016 .015 .014

The Stube' Steel Wire Gauge is used in measuring drawn steel wire or will rods of Stube' make, and is also used by many makers of American will rods.

THE EDISON OR CIRCULAR MIL WIRE GAUGE.

(For table of copper wires by this gauge, giving weights, electrical resistances, etc., see Copper Wire.)

Mr. C. J. Field (Stevens Indicator, July, 1887) thus describes the origin of

the Edison gauge:

The Edison company experienced inconvenience and loss by not having a wide enough range nor sufficient number of sizes in the existing gauges. This was lett more particularly in the central station work in making electrical determinations for the street system. They were compelled to make use of two of the existing gauges at least, thereby introducing a complication that was liable to lead to missakes by the contractors and linemen.

In the incandescent system an even distribution throughout the entire system and a uniform pressure at the point of delivery are obtained by calculating for a given maximum percentage of loss from the potential as delivered from the dynama. In carrying this out, on account of lack of regular sizes, it was often necessary to use larger sizes than the occasion demanded, and even to assume new sizes for large underground conductors. It was also found that nearly all manufacturers based their calculation for the conductivity of their wire on a variety of units, and that not one used the latest unit as adopted by the British Association and determined from Dr. Matthiessen's experiments; and as this was the unit employed in the manufacture of the Edison lamps, there was a further reason for constructing a new gauge. The engineering department of the Edison company, knowing the requirements, have designed a gauge that has the widest range obtainable and a large number of sizes which increase in a regular and uniform manner. The basis of the graduation is the sectional area, and and uniform manner. The basis of the graduation is the sectional area, and the number of the wire corresponds. A wire of 100,000 circular mils area is No. 100; a wire of one half the size will be No. 50; twice the size No. 200. In the elder gauges, as the number increased the size decreased. With this gauge, however, the number increases with the wire, and the number multiplied by 1000 will give the circular mils.

The weight per mil-foot, 0.0000302705 pounds, agrees with a specific gravity of 8.889, which is the latest figure given for copper. The ampere capacity which is given was deduced from experiments made in the com-

capacity which is given was deduced from experiments made in the company's laboratory, and is based on a rise of temperature of 50° F. in the wire. In 1898 Mr. Field writes, concerning gauges in use by electrical engineers: The B. and S. gauge seems to be in general use for the smaller sizes, up to 100,000 c. m., and in some cases a little larger. From between one and two hundred thousand circular mile upwards, the Edison gauge or its equivalent is practically in use, and there is a general tendency to designate all sizes above this in circular mile, specifying a wire as 200,000, 400,000, 500, 000, or 1,000,000 c. m.

In the electrical business there is a large use of copper wire and rod and other materials of these large sizes, and in ordering them, speaking of them, specifying, and in every other use, the general method is to simply specify the circular milage. I think it is going to be the only system if the future for the designation of wires, and the attaining of it means practically the adoption of the Edison gauge or the method and basis of this gauge as the

correct one for wire sizes.

THE U. S. STANDARD GAUGE FOR SHERT AND PLATE IRON AND STERL, 1898.

There is in this country no uniform or standard gauge, and the same numbers in different gauges represent different thicknesses of sheets or plates. This has given rise to much misunderstanding and friction between employers and workmen and mistakes and fraud between dealers and consumers.

An Act of Congress in 1893 established the Standard Gauge for sheet Iron and steel which is given on the next page. It is based on the fact that a

and steet which is given on the areat page. At is based on the less that a cubic foot of from weighs 480 pounds.

A sheet of from 1 foot square and 1 inch thick weighs 40 pounds, or 610 ounces, and 1 ounce in weight should be 1/640 inch thick. The scale has been arranged so that each descriptive number represents a certain number of ounces in weight and an equal number of 640 the of an inch in thickness.

The law enacts that on and after July 1, 1893, the new gauge shall be used.

in determining duties and taxes levied on sheet and plate iron and seel; and that in its application a variation of 2½ per cent either way may be allowed.

U. S. STANDARD GAUGE FOR SHEET AND PLATE IRON AND STEEL, 1898.

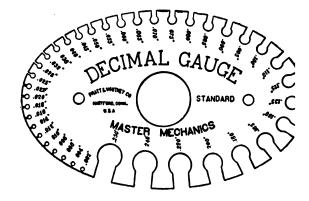
Number of Gauge.	Approximate Thickness in Fractions of	Approximate Thickness in Decimal Parts of an Inch.	Approximate Thickness in in Millimeters.	Weight per Square Foot in Ounces Avoirdupois.	Weight per Equare Foot in Pounds Avoirdupois.	Weight per Square Foot in Kilograms.	Weight per Square Meter in Kilograms.	Weight per Square Meter in Pounds Avoirdupois.
3000000 00000 00000 0000	1-2 15-38 7-16 18-33 3-8	0.5 0.46975 0.4875 0.40625 0.375	12.7 11.90625 11.1125 10.31875 9.525	320 800 280 260 240	20. 18.75 17.50 16.25 15.	9.079 9.505 7.938 7.871 6.804	97.65 91.55 86.44 79.83 78.24	215.28 201.32 188.37 174.91 161.46
90.	11-82	0.84375	8.78125	200	13.75	6.237	67.13	148.00
0	5-16	0.8125	7.9875	200	12.50	5.67	61.08	184.55
1	9-82	0.26125	7.14375	180	11.25	5.108	54.98	121.09
2	17-64	0.265625	6.746875	170	10.625	4.819	51.88	114.87
8	1-4	0.25	6.85	160	10.	4.536	48.82	107.64
4	15-64	0.284375	5.958125	150	9.875	4.252	45.77	100.91
5	7-82	0.21875	5.85625	140	8.75	3.969	42.72	94.18
6	18-64	0.203125	5.159375	130	8.125	3.685	89.67	87.45
7	8-16	0.1875	4.7625	120	7.5	8.402	86.62	80.72
8	11-64	0.171875	4.865625	110	6.875	3.118	38.57	74.00
9	5-82	0.15625	3.96875	100	6.25	2.835	30.52	67.27
10	9-64	0.140625	3.571875	90	5.625	2.552	27.46	60.55
11	1-8	0.125	3.175	80	5.	2.268	24.41	58.82
12	7-64	0.109375	2.778125	70	4.375	1.984	21.36	47.09
13	8-82	0.09375	2.38125	60	8.75	1.701	18.31	40.86
14	5-64	0.078125	1.984375	50	8.125	1.417	15.26	33.64
15	9-128	0.0708125	1.7859275	45	2.8125	1. 276	13.78	30.27
16	1-16	0.0625	1.5875	40	2.5	1.134	12.21	26.91
17	9-160	0.06825	1.42875	36	2.25	1.021	10.99	24.22
18	1-90	0.05	1.427	32	2.25	0. 9 072	9.765	21.53
19	7-1 6 0	0.04375	1.11125	28	1.75	0.7938	8.544	18.84
20	8-80	0.0375	0.9525	24	1.50	0.6804	7.324	16.15
21	11-320	0.034375	0.873125	22	1.875	0.6237	6.718	14.80
22	1-32	0.03125	0.793750	20	1.25	0.567	6.108	13.46
23	9-320	0.028125	0.714875	18	1.125	0.5103	5.498	12.11
24	1-40	0.025	0.685	16	1.	0.4536	4.882	10.76
25	7-320	0.021875	0.555625	14	0.875	0.8989	4.272	9.42
26	8-160	0.01875	0.47695	19	0.75	0.8402	3.662	8.07
27	11-640	0.0171825	0.4365625	11	0.6875	0.8119	8.357	7.40
28	1-64	0.018625	0.396875	10	6.625	0.2835	3.052	6.78
29 30 81 82 83	9-640 1-80 7-640 13-1280 8-820	0.0140625 0.0125 0.0109975 0.01015625 0.009875	0.3571875 0.8175 0.2778125 0.25796875 0.288125	8 7 616	0.5625 0.5 0.4375 0.40625 0.375	0.2551 0.2268 0.1984 0.1843 0.1701	2.746 2.441 2.136 1.963 1.831	6.05 5.38 4.71 4.87 4.04
84 85 86 87 88	11-1280 5-640 9-1280 17-2560 1-160	0.00869375 0.0078125 0.00703125 0.006640625 0.00625	0.21825125 0.1984375 0.17859875 0.168671875 0.15875	5)4 5 4)4 4)4	0.34375 0.3125 0.28125 0.265625 0.25	0.1559 0.1417 0.1276 0.1205 0.1184	1.678 1.526 1.873 1.297 1.221	8 70 3.86 3.03 2.87 2.60

The Decimal Gauge.—The legalization of the standard shee gauge of 1893 and its adoption by some manufacturers of sheet irc only added to the existing confusion of gauges. A joint committee American Society of Mechanical Engineers and the American I Master Mechanics' Association in 1895 agreed to recommend the use master mechanics' Association in 1855 agreed to recommend the use decimal gauge, that is, a gauge whose number for each thickness number of thousandths of an inch in that thickness, and also to reco "the abandonment and disuse of the various other gauges now in tending to confusion and error." A notched gauge of oval form, si the cut below, has come into use as a standard form of the decimal; In 1904 The Westinghouse Electric & Mfg. Co. abandoned the use o

numbers in referring to wire, sheet metal, etc.

Weight of Sheet Iron and Steel. Thickness by De-Gauge.

ę.	Fractions ich.	Millimetres.	Squar	tht per re Foot ounds.		tions	Millimetres.	Weig Squar in Pc
Decimal Gauge.	Approx. Frac	Approx. Milli	Iron, 480 Lbs. per Cu. Ft.	Steel, 489.6 Lbs. per Cu. Ft.	Decimal Gauge.	Approx. Fractions of an Inch.	Approx. Milli	Fron, 480 Lbs. per Cu. Ft.
0.002 0.004 0.006 0.008 0.010 0.012 0.014 0.018 0.020 0.022 0.025 0.025 0.028	1/500 1/250 8/500 1/125 1/100 8/250 7/500 1/64 + 9/500 1/500 1/500 1/40 7/250 1/82 +	0.05 0.10 0.15 0.20 0.25 0.30 0.46 0.51 0.56 0.67 0.81	0.08 0.16 0.24 0.32 0.40 0.48 0.56 0.64 0.72 0.80 0.88 1.00 1.12	0.082 0.163 0.245 0.326 0.408 0.490 0.571 0.653 0.734 0.816 0.898 1.020 1.142 1.306	0.060 0.065 0.070 0.075 0.080 0.085 0.090 0.100 0.110 0.125 0.135 0.150 0.165	1/16 — 13/200 7/100 8/40 2/25 17/200 9/100 19/200 1/10 11/100 1/8 27/200 3/20 3/20	1.52 1.65 1.78 1.90 2.08 2.16 2.28 2.41 2.54 2.79 3.18 3.48 3.43 4.19	2.40 2.60 2.80 3.00 3.20 3.40 3.60 3.80 4.00 4.40 5.00 5.40 6.60
0.036 0.040 0.045 0.050 0.055	9/250 1/25 9/200 1/20 11/200	0.91 1.02 1.14 1.27 1.40	1.44 1.60 1.80 2.00 2.20	1.469 1.632 1.836 2.040 2.244	0.180 0.200 0.220 0.240 0.250	9/50 1/5 11/50 6/25 1/4	4.57 5.08 5.59 6.10	7.20 8.00 8.80 9.60 10.00



ALGEBRA.

Addition. Add a and b. Ans. a+b. Add a, b, and -c. Ans. a+b-c. Add a: and -3a. Ans. -a. Add 2ab, -3ab, -c, -3c. Ans. -ab-4c. **Subtract** a from b. Ans. b-a. Subtract -a from -b.

Ans. -b+a. Subtract b+c from a. Ans. a-b-c. Subtract $3a^2b-9c$ from $4a^2b+c$. Ans. a^2b+10c . By Let. Change the signs of the subtrahend and proceed as in addition.

Multiplication.—Multiply a by b. Ans. ab. Multiply ab by a+b. Ans. a^2b+ab^2 .

Multiply a+b by a+b. Ans. $(a+b)(a+b)=a^2+2ab+b^2$. Multiply -a by -b. Ans. ab. Multiply -a by b. Ans. -ab.

signs give plus, unlike signs minus.

Powers of numbers.—The product of two or more powers of any number is the number with an exponent equal to the sum of the powers: $a^2 \times a^3 = a^6$; $a^2b^2 \times ab = a^2b^3$; $-7ab \times 2ac = -14 a^2bc$

To multiply a polynomial by a monomial, multiply each term of the polynomial by the monomial and add the partial products: $(6a - 3b) \times 3c = 18ac$

To multiply two polynomials, multiply each term of one factor by each term of the other and add the partial products: $(5a - 6b) \times (3a - 4b) = 15a^2 - 38ab + 24b^3$.

The square of the sum of two numbers = sum of their squares + twice

their product. The square of the difference of two numbers = the sum of their squares ~ | wice their product.

The product of the sum and difference of two numbers = the difference of their squares:

$$(a+b)^2 = a^2 + 2ab + b^2;$$
 $(a-b)^2 = a^2 - 2ab + b^2;$ $(a+b) \times (a-b) = a^2 - b^2.$

The square of half the sums of two quantities is equal to their product plus the square of half their difference: $\left(\frac{a+b}{a}\right)$ ab + (3

The square of the sum of two quantities is equal to four times their products, plus the square of their difference: $(a+b)^2=4ab+(a-b)^2$. The sum of the squares of two quantities equals twice their product, plus the square of their difference: $a^2+b^2=2ab+(a-b)^2$.

The square of a trinomial = the square of each term + twice the product

The square of a trinomial = the square of each term + twice the product of each term by each of the terms that follow it: $(a+b+c)^2=a^2+b^2+b^2+c^2+2ab+2ac+2bc$; $(a-b-c)^2=a^2+b^2+c^2-2ab-2ac+2bc$. The square of (any number $+\frac{1}{1}\frac{1}{2}$) = square of the number + the number + $\frac{1}{1}\frac{1}{2}$; (a+ $\frac{1}{2}\frac{1}{2}$) = $a^2+a+\frac{1}{2}$, $=a(a+1)+\frac{1}{2}$. (4 $\frac{1}{2}\frac{1}{2}$) = $a^2+a+\frac{1}{2}$, $=a(a+1)+\frac{1}{2}$. (4 $\frac{1}{2}\frac{1}{2}$) = $a^2+a+\frac{1}{2}$, $=a(a+1)+\frac{1}{2}$. The product of any number $+\frac{1}{2}$ by any other number $+\frac{1}{2}$ = product of the numbers + half their sum $+\frac{1}{2}$. (a $+\frac{1}{2}\frac{1}{2}$) be $+\frac{1}{2}\frac{1}{2}$) = $ab+\frac{1}{2}(a+b)+\frac{1}{2}$. Square, cube, 4th power, etc., of a binomial a+b.

$$(a+b)^2 = a^3 + 2ab + b^2;$$
 $(a+b)^8 = a^3 + 8a^2b + 8ab^2 + b^3;$ $(a+b)^4 = a^4 + 4a^3b + 6a^2b^2 + 4ab^3 + b^4.$

In each case the number of terms is one greater than the exponent of the power to which the binomial is raised.

2. In the first term the exponent of a is the same as the exponent of the power to which the binomial is raised, and it decreases by 1 in each succeed-

3. b appears in the second term with the exponent 1, and its exponent increases by 1 in each succeeding term.

4. The coefficient of the first term is 1.

5. The coefficient of the second term is the exponent of the power to which the binomial is raised.

6. The coefficient of each succeeding term is found from the next precoding term by multiplying its coefficient by the exponent of a, and dividing the product by a number greater by 1 than the exponent of b. Smoonial Theorem, below.)

Parentheses.—When a parenthesis is preceded by a plus sign it may be removed without changing the value of the expression: a+b+(a+b)=2a+2b. When a parenthesis is **preceded** by a minus sign it may be removed if we change the signs of all the terms within the parenthesis: 1-(a-b)-c) = 1 - a + b + c. When a parenthesis is within a parenthesis remove the inner one first: $a - \left[b - \left\{c - (d - e)\right\}\right] = a - \left[b - \left\{c - d + e\right\}\right]$

= a - [b - c + d - e] = a - b + c - d + e. A multiplication sign, \times , has the effect of a parenthesis, in that the operation indicated by it must be performed before the operations of addition or subtraction. $a + b \times a + b = a + ab + b$; while $(a + b) \times (a + b) = a^2 + 2ab + b^2$, and $(a + b) \times a + b = a^2 + ab + b$.

Division.—The quotient is positive when the dividend and divisor have like signs, and negative when they have unlike signs: abc + b = ac;

abc + - b = -ac.

To divide a monomial by a monomial, write the dividend over the divisor with a line between them. If the expressions have common factors, remove the common factors:

$$a^{2}bx + aby = \frac{a^{2}bx}{aby} = \frac{ax}{y}; \quad \frac{a^{4}}{a^{3}} = a; \quad \frac{a^{3}}{a^{6}} = \frac{1}{a^{2}} = a^{-3}.$$

To divide a polynomial by a monomial, divide each term of the polynomial by the monomial: (8ab - 12ac) + 4a = 2b - 3c.

To divide a polynomial by a polynomial, arrange both dividend and divisor in the order of the ascending or descending powers of some common letter, and keep this arrangement throughout the operation.

Divide the first term of the divisor, and

write the result as the first term of the quotient.

Multiply all the terms of the divisor by the first term of the quotient and subtract the product from the dividend. If there be a remainder, consider it as a new dividend and proceed as before: $(a^2 - b^2) + (a + b)$.

$$\begin{array}{c|c}
 a^{2} - b^{2} & a + b \\
 \underline{a^{2} + ab} & a - b \\
 - ab - b^{2} \\
 - ab - b^{2}
 \end{array}$$

The difference of two equal odd powers of any two numbers is divisible

The difference of two equal odu powers of any two numbers a divisible by their difference and also by their sum: $(a^3-b^3)+(a-b)=a^2+ab+b^2; (a^3-b^3)+(a+b)=a^3-ab+b^3.$ The difference of two equal even powers of two numbers is divisible by their difference and also by their sum: $(a^3-b^3)+(a-b)=a+b$.

The sum of two equal even powers of two numbers is not divisible by either the difference or the sum of the numbers; but when the exposure is compared to compare a company of an odd and an eyen factor. of each of the two equal powers is composed of an odd and an even factor, the sum of the given power is divisible by the sum of the powers expressed by the even factor. Thus $x^6 + y^6$ is not divisible by x + y or by x - y, but is divisible by $x^2 + y^2$

Simple equations.—An equation is a statement of equality between

Simple equations.—An equation is a statement of equality between two expressions; as, a+b=c+d.

A simple equation, or equation of the first degree, is one which contains only the first power of the unknown quantity. If equal changes be made (by addition, subtraction, multiplication, or division) in both sides of an equation, the results will be equal.

Any term may be changed from one side of an equation to another, provided its sign be changed: a+b=c+d; a=c+d-b. To solve an equation having one unknown quantity, transpose all the terms involving the unknown quantity to one side of the equation, and all the other terms to the other side; combine like terms, and divide both sides by the coefficient of the unknown quantity. of the unknown quantity. Solve 8x - 29 = 26 - 8x. 8x + 8x = 29 + 26; 11x = 56; x = 5, ans.

Simple algebraic problems containing one unknown quantity are solved by making x = the unknown quantity, and stating the conditions of the problem in the form of an algebraic equation, and then solving the equation. What two numbers are those whose sum is 48 and difference 14 7 Let x =the smaller number, x + 14 the greater. x + x + 14 = 48. 2x = 34, x = 34= 17; x + 14 = 31, ans.

Find a number whose treble exceeds 50 as much as its double falls short

of 40. Let x = the number. 8x - 50 = 40 - 2x; 5x = 90; x = 18, ans. Prov-

 \log_{10} , 54 - 50 = 40 - 86.

Equations containing two unknown quantities.—If one equation contains two unknown quantities, a and y, an indefinite number of pairs of values of x and y may be found that will satisfy the equation, but if a second equation be given only one pair of values can be found that will satisfy both equations. Simultaneous equations, or those that may be satisfied by the same values of the unknown quantities, are solved by combining

the equations so as to obtain a single equation containing only one unknown quantity. This process is called elimination.

Elimination by addition or subtraction.—Multiply the equation by such numbers as will make the coefficients of one of the unknown quantities equal in the resulting equation. Add or subtract the resulting equations according as they have unlike or like signs.

Solve
$$\begin{cases} 3x + 3y = 7$$
. Multiply by 2: $4x + 6y = 14 \\ 4x - 5y = 3$. Subtract: $4x - 6y = 3$ $11y = 11$; $y = 1$.

Substituting value of y in first equation, 2x + 3 = 7; x = 2. Elimination by substitution.—From one of the equations obtain the

value of one of the unknown quantities in terms of the other. Substitu-tate for this unknown quantity its value in the ether equation and reduce the resulting equations.

Solve
$$\begin{cases} 2x + 3y = 8. & (1). \text{ From (1) we find } x = \frac{8 - 3y}{2}. \\ 3x + 7y = 7. & (2). \end{cases}$$

Substitute this value in (2): $3\left(\frac{8-3y}{2}\right) + 7y = 7$; = 24-9y+14y=14, whence y = -2. Bubetitute that value in (1): 2x - 6 = 8; x = 7.

Minimation by comparison.—From each equation obtain the value of one of the unknown quantities in terms of the other. Form an equation from these equal values, and reduce this equation.

Solve
$$\begin{cases} 2x - 9y = 11. & (1), & \text{From (1) we find } \alpha = \frac{11 + 9y}{2}, \\ 8x - 4y = 7. & (2). & \text{From (2) we find } x = \frac{7 + 4y}{8}, \end{cases}$$

Equating these values of x, $\frac{11+9y}{2} = \frac{7+4y}{3}$; 19y = -19; y = -1.

Substitute this value of y in (1): 2x + 9 = 11; x = 1. If three simultaneous equations are given containing three unknown quantities, one of the unknown quantities must be eliminated between two pairs of the equations; then a second between the two resulting equations.

Quadratic equations,—A quadratic equation contains the square of the unknown quantity, but no higher power. A pure quadratic contains the square only; an affected quadratic both the square and the first power.

To solve a pure quadratic, collect the unknown quantities on one side, and the known quantities on the other; divide by the coefficient of the unknown quantity and extract the square root of each side of the resulting conation.

Solve $3x^2 - 15 = 0$. $6x^2 = 15$; $x^2 = 5$; $x = \sqrt{5}$

A root like \$\sqrt{5}\$, which is indicated, but which can be found only approximately, is called a nurd.

Solve $2x^3 + 15 = 0$. $3x^2 = -15$; $x^2 = -5$; $x = \sqrt{-5}$. The square root of -5 cannot be found even approximately, for the square of any number positive of negative is positive; therefore a root which is indicated, but cannot be found even approximately, is called *imaginary*. To solve an affected quadratic.—1. Convert the equation into the form $e^2x^2 \pm 2abx = c$, multiplying or dividing the equation if necessary, so as to make the coefficient of x^2 a square number.

2. Complete the equate of the first member of the equation, so as to convert it to the form of $a^2x^2 \pm 2abx + b^2$, which is the square of the quotient obtained by dividing the second term by twice the square of the quotient obtained by dividing the second term by twice the square root of the first term. first term.

3. Extract the square root of each side of the resulting equation. Solve $3x^2-4x=3k$. To make the coefficient of x^2 a square number, multiply by 3: $8x^2-12x=96$; 18x+4=26. 8x=2; $2^2=4$. Complete the square: $9x^2-12x+4=100$. Extract the root: 8x-2=12x+4=100.

10, whence x=4 or -2.2/8. The square root of 100 is either +10 or -10, since the square of -10 as well as $+10^3=100$. Problems involving quadratic equations have apparently two solutions, as

a quadratic has two roots. Sometimes both will be true solutions, but generally one only will be a solution and the other be inconsistent with the conditions of the problem.

The sum of the squares of two consecutive positive numbers is 481. Find the numbers.

Let x = one number, x + 1 the other. $x^2 + (x + 1)^2 = 481$. $2x^2 + 2x + 1$

 $x^{2} + x = 240$. Completing the square, $x^{3} + x + 0.25 = 240.25$. Extracting the root we obtain $x + 0.5 = \pm 15.5$; x = 15 or -16.

The positive root gives for the numbers 15 and 16. The negative root -16 is inconsistent with the conditions of the problem.

Quadratic equations containing two unknown quantities require different methods for their solution, according to the form of the equations. For these methods reference must be made to works on algebra.

Theory of exponents. $-\sqrt[n]{a}$ when n is a positive integer is one of n equal factors of a. $\sqrt[n]{a^m}$ means a is to be raised to the mth power and the nth root extracted.

 $\binom{\sqrt[n]}{a}^m$ means that the *n*th root of *a* is to be taken and the result raised to the *m*th power.

 $\sqrt[n]{a^m} = \left(\sqrt[n]{a}\right)^m = a^{\frac{m}{n}}$. When the exponent is a fraction, the numerator indicates a power, and the denominator a root. $a^{\frac{9}{2}} = \sqrt{a^6} = a^3$; $a^{\frac{3}{2}} =$ $4/a^3 = a^{1\cdot 5}.$

To extract the root of a quantity raised to an indicated power, divide the exponent by the index of the required root; as,

$$\sqrt[n]{a^m} = a^{\frac{m}{n}}; \qquad \sqrt[3]{a^6} = a^{\frac{6}{3}} = a^2.$$

 $\sqrt[n]{a^m} = a^{\frac{m}{n}}; \qquad \sqrt[3]{a^6} = a^{\frac{6}{3}} = a^2.$ Subtracting 1 from the exponent of a is equivalent to dividing by a:

$$a^{2-1} = a^{1} = a; \quad a^{1-1} = a^{0} = \frac{a}{a} = 1; \quad a^{0-1} = a^{-1} = \frac{1}{a}; \quad a^{-1-1} = a^{-2} = \frac{1}{a^{2}}$$

A number with a negative exponent denotes the reciprocal of the number

with the corresponding positive exponent.

A factor under the radical sign whose root can be taken may, by having the root taken, be removed from under the radical sign:

$$\sqrt{a^2b} = \sqrt{a^2} \times \sqrt{b} = a \sqrt{b}$$
.

A factor outside the radical sign may be raised to the corresponding power and placed under it:

$$\sqrt{\frac{a}{b}} = \sqrt{\frac{a\overline{b}}{b^2}} = \sqrt{ab \times \frac{1}{b^2}} = \frac{1}{b} \sqrt[4]{ab}; \qquad \sqrt{\frac{a}{b^2}} = \frac{1}{b} \sqrt[4]{a}$$

Binomial Theorem.—To obtain any power, as the nth, of an expression of the form x + a

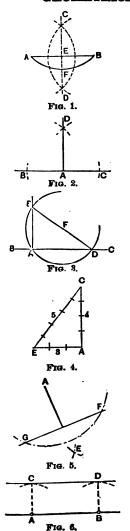
$$(a+x)^n = a^n + na^{n-1} x + \frac{n(n-1)a^{n-2}}{1.2}x^2 + \frac{n(n-1)(n-2)a^{n-2}}{1.2.8.}x^3 + \frac{n(n-1)(n-2)a^{n-2}}{1.2.8.$$

The following laws hold for any term in the expansion of $(a + x)^x$. The exponent of x is less by one than the number of terms.

The exponent of a is n minus the exponent of x. The last factor of the numerator is greater by one than the exponent of a. The last factor of the denominator is the same as the exponent of x.

The last factor of the exponent of x will be r-1. The exponent of a will be n-(r-1), or n-r+1. The last factor of the numerator will be n-r+2. The last factor of the denominator will be n-r+2. Hence the rth term $=\frac{n(n-1)(n-2)\dots(n-r+2)}{1\cdot 2\cdot 3\cdot \dots (r-1)}a^{n-r+1}x^{r-1}$

GEOMETRICAL PROBLEMS.

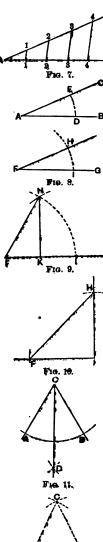


- 1. To bisect a straight line, or an arc of a circle (Fig. 1).— From the ends A. B. as centres, describe arcs intersecting at C and D, and draw a line through C and D which will bisect the line at E or the arc at F.
- 2. To draw a perpendicular to a straight line, or a radial line to a circular arc.—Same as in Problem 1. CD is perpendicular to the line AB, and also radial to the arc.
- 3. To draw a perpendicular to a straight line from a given point in that line (Fig. 2).—With any radius, from the given point A in the line B C, cut the line at B and C. With a longer radius describe arcs from B and C, cutting each other at D, and draw the perpendicular DA.
- 4. From the end A of a given line A D to erect a perpendicular A E (Fig. 3).—From any centre F, above A D, describe a circle passing through the given point A, and cutting the given line at D. Draw D F and produce it to cut the circle at E, and draw the perpendicular A E.

and draw the perpendicular A E. Second Method (Fig. 4).—From the given point A set off a distance A E equal to three parts, by any scale; and on the centres A and E, with radii of four and five parts respectively, describe arcs intersecting at C. Draw the perpendicular A C.

Note.—This method is most useful on very large scales, where straight edges are inapplicable. Any multiples of the numbers 3, 4, 5 may be taken with the same effect as 6, 8, 10, or 9, 12, 15.

- 5. To draw a perpendicular to a straight line from any point without it (Fig. 5.)—From the point A, with a sufficient radius cut the given line at F and G, and from these points describe arcs cutting at E. Draw the perpendicular A E.
- 6. To draw a straight line parallel to a given line, at a given distance apart (Fig. 6).—
 From the centres A, B, in the given line, with the given distance as radius, describe arcs C, D, and draw the parallel lines C D touching the arcs.



F1g. 12.

7. To divide a straight line into a number of equal parts (Fig. 7).—To divide the line AB into, say, five parts, draw the line AC at an angle from A; set off five equal parts; draw B5 and draw parallels to it from the other points of division in AC. These parallels divide AB as required.

Note.—By a similar process a line may be divided into a number of unequal parts; setting off divisions on A C, proportional by a scale to the required divisions, and drawing parallel cutting A B. The triangles A11, A22, A33, etc., are similar triangles.

- 8. Upon a straight line to draw an angle equal to a given angle (Fig. 8).—Let A be the given angle and FG the line. From the point A with any radius describe the arc D E. From F with the same radius describe I H. Set off the arc H equal to D E, and draw F H. The angle F is equal to A, as required.
- 9. To draw angles of 60° and 30° (Fig. 9).—From F, with any radius FI, describe an arc IH; and from I, with the same radius, cut the arc at H and draw FH to form the required angle IFH. Draw the perpendicular HK to the base line to form the angle of 30° FHK.
- 10. To draw an angle of 45° (Fig. 10).—Set off the distance F I; draw the perpendicular I H equal to IF, and join HF to form the angle at F. The angle at H is also 45°.
- 11. To bisect an angle (Fig. 11).—Let $A \subset B$ be the angle; with C as a centre draw an arc cutting the sides at A, B. From A and B as centres, describe arcs cutting each other at D. Draw C D, dividing the angle into two equal parts.
- 12. Through two given points to describe an arc of a circle with a given radius (Fig. 12).—From the points A and B as centres, with the given radius, describe arcs cutting at C; and from C with the same radius describe an arc AB.



Fig. 13.

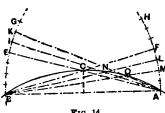
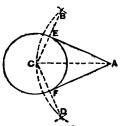


Fig. 14.



Ftg. 15.



F16, 16.

13. To find the centre of a circle or of an arc of a circle (Fig. 13).—Select three points, A, B, C, in the circumference, well apart; with the same radius describe arcs from these three points, cutting each other, and draw the two lines, DE, F. G. through their intersections. The point O, where they cut, is the centre of the circle or arc.

To describe a circle passing through three given points.

—Let A, B, C be the given points, and proceed as in last problem to find the centre 0, from which the circle may

be described.

14. To describe an arc of a circle passing through three given points when the centre is not available (Fig.14).—From the extreme points A, B, as centres, describe arcs A H, B G. Through the third point C draw A E, B F, cutting the arcs. Divide A F and B E into any number of equal parts, and set off a series of equal parts of the same length on the upper portions of the straight lines, BL, BM, etc., to the divisions in AF, and AI, AK, etc., to the divisions in EG. The successive intersections N, O, etc., to the divisions of the divisions of the successive intersections N, O, etc., to the division of the successive intersections N, O, etc., the successive N, O, etc., the of these lines are points in the circle required between the given points A and C, which may be drawn in; similarly the remaining part of the curve' B C may be described. (See also Problem 54.)

15. To draw a tangent to a circle from a given point in the circumference (Fig. 15). Through the given point A, draw the radial line A C, and a perpendicular to it, F G, which is the tangent required.

16. To draw tangents to a circle from a point without it (Fig. 16).—From A, with the radius A C, describe an arc B C D, and from A U, describe an arc B C B, and from C, with a radius equal to the diameter of the circle, cut the arc at B D. Join B C, C D, cutting the circle at E F, and draw A E, A F, the tangents.

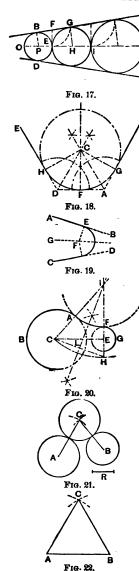
Note.—When a tangent is already

drawn, the exact point of contact may be found by drawing a perpendicular

to it from the centre.

17. Between two inclined lines to draw a series of circles touching these lines and touching each other (Fig. 17).

Bisect the inclination of the given lines A B, O D, by the line N O. From a point P in this line draw the perpendicular P B to the line A B, and



on P describe the circle B D, touching the lines and cutting the centre line at E. From E draw E F perpendicular to the centre line, cutting AB at F, and from F describe an arc EG, cutting AB at G. Draw GH parallel to BP, giving H, the centre of the next circle, to be described with the radius $H_{-}E$, and so on for the next circle IN.

Inversely, the largest circle may be described first, and the smaller ones in succession. This problem is of fre-

quent use in scroll-work.

18. Between two inclined lines to draw a circular segment tangent to the lines and passing through a point F on the line F C which bisects the angle of the lines (Fig. 18).

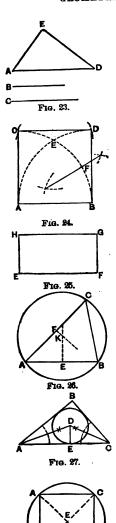
—Through F draw D A a tright angles to F C; bisect the angles A and D, as in Publicant 11 by light services at C. in Problem 11, by lines cutting at C, and from C with radius C F draw the arc H F G required.

19. To draw a circular are that will be tangent to two given lines A B and C D inclined to one another, one tangential point E being given (Fig. 19).—Draw the centre line G.F. From E draw E Fat right to angles AB; then F is the centre of the circle required.

20. To describe a circular are joining two circles, and touching one of them at a given point (Fig. 20).—To join the circles A B, F G, by an are touching one of them at F, draw the radius E F, and produce it both ways. Set of E H one of them are, three me radius E. and produce it both ways. Set off FH equal to the radius A C of the other circle; join CH and bisect it with the perpendicular L I, cutting E F at I. On the centre I, with radius I F, describe the arc F A as required.

21. To draw a circle with a given radius R that will be given radius a that will be tangent to two given circles A and B (Fig. 21).—From centre of circle A with radius equal R plus radius of A, and from centre of B with radius equal to R + radius of B, draw two arcs cutting each other in C, which will be the centre of the circle reauired.

22. To construct an equi-lateral triangle, the sides being given (Fig. 22).—On the ends of one side, A, B, with A B as radius, describe arcs cutting at C, and draw A C, CB.



R

Fig. 28.

23. To construct a triangle of unequal sides (Fig. 23).—On either end of the base AD, with the side B as radius, describe an arc; and with the side C as radius, on the other end of the base as a centre, cut the arc at E. Join AE, DE.

24. To construct a square on a given straight line A B (Fig. 24).-With A B as radius and A and B as centres, draw arcs AD and B
C, intersecting at E. Bisect EB at F.
With E as centre and EF as radius. cut the arcs A D and B C in D and C. Join A C, C D, and D B to form the square.

25. To construct a rectangle with given base E for F and height E H (Fig. 25).—On the base E for draw the perpendiculars E H, F G equal to the height, and join G H.

26. To describe a circle about a triangle (Fig. 26).— Bisect two sides AB, AC of the triangle at EF, and from these points draw perpendiculars cutting at K. On the centre K, with the radius KA, draw the circle ABC.

27. To inscribe a circle in a triangle (Fig. 27).—Bisect two of the angles A, C, of the triangle by lines cutting at D: from D draw a perpendicular D E to any side, and with D E as radius describe a circle.

When the triangle is conflicted.

When the triangle is equilateral, draw a perpendicular from one of the angles to the opposite side, and from the side set off one third of the perpendicular.

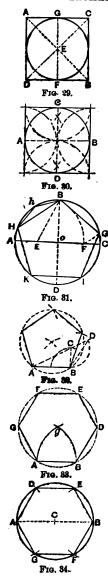
pendicular.

28. To describe a circle
about a square, and to inscribe a square in a circle (Fig.
28).—To describe the circle, draw the
diagonals A B, C D of the square, cutting at E. On the centre E, with the
radius A E, describe the circle.

To inscribe the square.—
Draw the two diameters, A B, C D, at
right angles, and io in the points A, B,

right angles, and join the points A, B, CD, to form the square.

Note.—In the same way a circle may be described about a rectangle.



29. To inscribe a circle in a square (Fig. 29).—To inscribe the circle, draw the diagonals AB, CD of the square, cutting at E; draw the perpendicular EF to one side, and with the radius EF describe the circle.

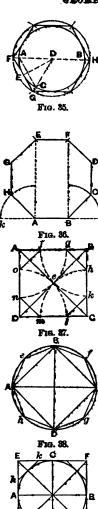
30. To describe a square about a circle (Fig. 30).—Draw two diameters AB, CD at right angles. With the radius of the circle and A, B, C and D as centres, draw the four half circles which cross one another in the corners of the square.

31. To inscribe a pentagon in a circle (Fig. 31).—Draw diameters A C, B D at right angles, cutting at o. Bisect A o at E, and from E, with radius E B, cut A C at F; from B, with radius B F, cut the circumference at G, H, and with the same radius step round the circle to I and K; jointhe points so found to form the pentagon.

32. To construct a pentagon on a given line A B (Fig. 32).—From B erect a perpendicular B C half the length of A B; join A C and prolong it to D, making C D = B C. Then B D is the radius of the circle circumscribing the pentagon. From A and B as centres, with B D as radius, draw arcs cutting each other in O, which is the centre of the circle.

33. To construct a hexagon upon a given straight line (Fig. 33).—From A and B, the ends of the given line, with radius AB, describe arcs cutting at g; from g, with the radius gA, describe a circle; with the same radius set off the arcs AG, GF, and BD, DE. Join the points so found to form the hexagon. The side of a hexagon = radius of its circumscribed circle.

34. To inscribe a hexagon in a circle (Fig. 34).—Draw a diameter A CB. From A and B as centres, with the radius of the circle A C, cut the circumference at D, E, F, G, and draw A D, D E, etc., to form the hexagon. The radius of the circle is equal to the side of the hexagon; therefore the points D, E, etc., may also be found by stepping the radius six times round the circle. The angle between the diameter and the sides of a hexagon and also the exterior angle between a side and an adjacent side prolonged is 60 degrees; therefore a hexagon may conveniently be drawn by the use of a 60-degree triangle.



D Frg. 39.

- 35. To describe a hexagon about a circle (Fig. 35).—Draw a diameter ADB, and with the radius AD, on the centre A, cut the circumference at C; join AC, and bisect it with the radius DE; through E draw FG, parallel to AC, cutting the diameter at F, and with the radius DF describe the circumserbing circle FH. Within this circle describe a hexagon by the preceding problem. A more convenient method is by use of a 60-degree triangle. Four of the sides make angles of 60 degrees with the diameter, and the other two are parallel to the diameter.
- 36. Te describe an octagon on a given straight line (Fig. 36).—Produce the given line A B both ways, and draw perpendiculars A E, B F; bisect the external angles A and B by the lines A H, B C, which make equal to A B. Draw C D and H G parallel to A E, and equal to A B; from the centres G, D, with the radius A B, cut the perpendiculars at E, F, and draw E F to complete the octagon.
- 37. To convert a square into an octagon (Fig. 87).—Draw the diagonals of the square cutting at e; from the corners A, B, C, D, with A e as radius, describe arcs cutting the sides at gn. fk, km, and ol, and join the points so found to form the octagon. Adjacent sides of an octagon make an angle of 135 degrees.
- 38. To inseribe an octagon in a cirele (Fig. 38).—Draw two diameters, AC, BD at right angles; bisect the ares AB, BC, etc., at ef, etc., and join Ae, eB, etc., to form the octagon.
- 39. To describe an octagen about a firele (Fig. 39).—Describe a square about the given circle AB_1 draw perpendiculars h k, etc., to the diagonals, touching the circle to form the octagon.

40. To describe a polygon of any number of sides upon a given straight line (Fig. 40).—Produce the given line AB, and on A_1

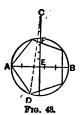




Fig. 41.



Fig. 42.



with the radius AB, describe a semicircle; divide the semi-circumference into as many equal parts as there are to be sides in the polygon—say, in this example, five sides. Draw lines from A through the divisional points D, b, and c, omitting one point a; and on the centres B, D, with the radius AB, cut Ab at E and Ac at F. Draw DE, EF, FB to complete the polygon.

41. To inscribe a circle within a polygon (Figs. 41, 42).—When the polygon has an even number of sides (Fig. 41), bisect two opposite sides at A and B; draw AB, and bisect it at C by a diagonal DE, and with the radius C A describe the circle.

When the number of sides is odd

When the number of sides is odd (Fig. 42), bisect two of the sides at A and B, and draw lines A E, BD to the opposite angles, intersecting at C; from C, with the radius C A, describe the circle.

42. To describe a circle without a polygon (Figs. 41, 42).

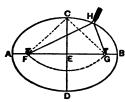
—Find the centre C as before, and with the radius C D describe the circle,

43. To inseribe a polygon of any number of sides within a circle (Fig. 43).—Draw the diameter AB and through the centre E draw the perpendicular EC, cutting the circle at F. Divide EF into four equal parts, and set off three parts equal to those from F to C. Divide the diameter AB into as many equal parts as the polygon is to have sides; and from C draw CD, through the second point of division, cutting the circle at D. Then AD is equal to one side of the polygon, and by stepping round the circumference with the length AD the polygon may be completed.

TABLE OF POLYGONAL ANGLES.

Number	Angle	Number	Angle	Number of Sides.	Angle
of Sides.	at Centre.	of Sides.	at Centre.		at Centre.
No. 8 4 5 6 7	Degrees, 120 90 72 60 51\$ 45	No. 9 10 11 12 13 14	Degrees. 40 86 32,4 80 27.3	No. 15 16 17 18 19	Degrees. 24 224 21 A 20 19 18

In this table the angle at the centre is found by dividing 360 degrees, the number of degrees in a circle, by the number of sides in the polygon; and by setting off round the centre of the circle a succession of angles by means of the protractor, equal to the angle in the table due to a given number of sides, the radii so drawn will divide the circumference into the same number of parts.



F1G. 44.

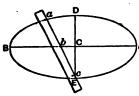
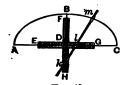
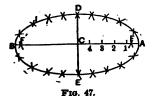


Fig. 45.



F1g. 46.



44. To describe an ellipse when the length and breadth are given (Fig. 44).—A B, transverse axis; CD, conjugate axis; FG, foci. The sum of the distances from C to F and G, also the sum of the distances from F and G to any other point in the curve, is equal to the transverse axis. From the centre C, with A E as radius, cut the axis A B at F and G, the foci; fix a couple of pins into the axis at F and G, and loop on a thread or cord upon them equal in length to the axis A B, so as when stretched to reach to the extremity C of the conjugate axis, as shown in dot-lining. Place a pencil inside the cord as at H, and guiding the pencil in this way, keeping the cord equally in tension, carry the pencil round the pins F, G,

and so describe the ellipse.

Norz.—This method is employed in setting off elliptical garden - plots,

walks, etc.
2d Method (Fig. 45).— Along the
straight edge of a slip of stiff paper
mark off a distance a c equal to A C, half the transverse axis; and from the same point a distance ab equal to CD, half the conjugate axis. Place the slip so as to bring the point b on the line AB of the transverse axis, and the point c on the line DE; and set off on the drawing the position of the point a. Shifting the slip so that the point b travels on the transverse axis, and the point c on the conjugate axis, any number of points in the curve may be found, through which the curve may be traced.

3d Method (Fig. 46).—The action of the preceding method may be em-

bodied so as to afford the means of describing a large curve continuously by means of a bar m k, with steel points m, l, k, riveted into brass slides adjusted to the length of the semi-axis and fixed with set-screws. A rectangular cross E G, with guiding-slots is placed, coinciding with the two axes of the ellipse A C and B H. By sliding the points k l in the slots. By sliding the points k, l in the slots, and carrying round the point m, the curve may be continuously described.

curve may be continuously described. A pen or pencil may be fixed at m.

4th Method (Fig. 47).—Bisect the transverse axis at C, and through C draw the perpendicular D E, making C D and C E each equal to half the conjugate axis. From D or E, with the radius A C, cut the transverse axis at F, F', for the foci. Divide A C, into a number of parts at the conjugate axis. A C into a number of parts at the

points 1, 2, 3, etc. With the radius A I on F and F as centres, describe arcs, and with the radius B I on the same centres cut these arcs as shown.

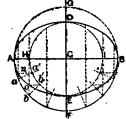
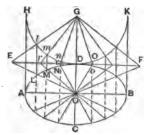
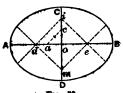


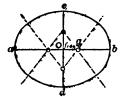
Fig. 48.



Frg. 49.



F1G. 50.



Fre. 51.

Repeat the operation for the other divisions of the transverse axis. The series of intersections thus made are points in the curve, through which the curve may be traced.

curve may be traced. 5th Method (Fig. 48).—On the two axes AB, DE as diameters, on centre C, describe circles; from a number of points a, b, etc., in the circumference AFB, draw radii cutting the inner circle at a', b', etc. From a, b, etc., draw perpendiculars to AB; and from a', b', etc., draw parallels to AB, cutting the respective perpendiculars at ting the respective perpendiculars at a, o, etc. The intersections are points in the curve, through which the curve

may be traced.

6th Method (Fig. 49). — When the transverse and conjugate diameters are given, AB, CD, draw the tangent EF parallel to AB. Produce CD, and on the centre G with the radius of half AB, describe a semicircle HDK; from the centre G draw any number of straight lines to the points E, r, etc., in the line E F, cutting the eircumference at l, m, n, etc.; from the centre θ of the ellipse draw whe centre ψ of the ellipse draw straight lines to the points E, r, etc.; and from the points l, m, n, etc., draw parallels to G C_r cutting the lines O E_r , O r, etc., at L, M, N, etc. These are points in the circumference of the ellipse, and the curve may be traced through them. Points in the other half of the ellipse are formed by extending the intersecting lines as indi-cated in the figure.

45. To describe an ellipse approximately by means of circular arcs.—First.—With arcs of two radii (Fig. 50).—Find the difference of the semi-axes, and set it off and of the semi-axes, and set off from the centre O to a and con O A and O C; draw a c, and set off half a c to d; draw d i parallel to a c; set off O e equal to O d; join e i, and draw the parallels e m, d m. From m, with radius m C, describe an arc through C; and from i describe an arc through D; from d and e describe arcs through a and B. The four arcs form the

ellipse approximately.

Note.—This method does not apply satisfactorily when the conjugate axis is less than two thinds of the trans-

verse axis.

2d Method (by Carl G. Barth, Fig. 51).—In Fig. 51 a b is the major and c d the minor axis of the ellipse to be approximated. Lay off be equal to the semi-minor axis c O, and use a e as radius for the arc at each extremity of the minor axis. Disect e o at f and lay off eg equal to ef, and use g b as radius for the arc at each extremity of the major axis.

The method is not considered applicable for cases in which the minor axis is less than two thirds of the major.

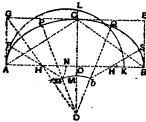
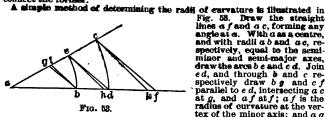


Fig. 52.

8d Method: With arcs of three radii (Fig. 52).—On the transverse axis A B draw the rectangle BG on the height OC; to the diagonal AC draw the perpendicular G HD; set off O K equal to OC, and describe a semi-circle on AK, and produce OC to L; set off OM equal to CL, and from D describe a per with reduce D M. furn describe an arc with radius DM; from A, with radius OL, cut AB at N; from H, with radius HN, cut arc ab at a. Thus the five centres D, a, b, H, H'are found, from which the arcs are described to form the ellipse.

This process works well for nearly all proportions of ellipses. It is used in striking out vaults and stone bridges.

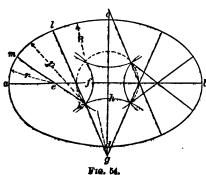
4th Method (by F. R. Honey, Figs. 53 and 54).—Three radii are employed. With the shortest radius describe the two arcs which pass through the very tices of the major axis, with the longest the two arcs which pass through the vertices of the minor axis, and with the third radius the four arcs which connect the former.



vertex of the major axis.

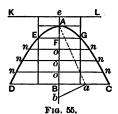
lines a f and a c, forming any angle at a. With a as a centre, and with radii a b and ac, respectively, equal to the semi-minor and semi-major axes, draw the arcs be and c d. Join ed, and through b and c respectively draw b g and c f parallel to ed, intersecting a c at g, and a f at f; a f is the radius of curvature at the vertex of the minor axis; and a gthe radius of curvature at the

Lay off dh (Fig. 53) equal to one eighth of b d. Join e h, and draw c k and b l parallel to e h. Take a k for the longest radius (=R), a l for the shortest radius (=r), and the arithmetical mean, or one half the sum of the semi-axes, for the third radius (=p), and employ these radii for the eight-centred oval

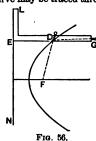


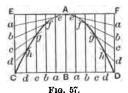
Let a b and cd (Fig. 54) be the major and minor axes. Lay off ae equal to r, and af equal to p, also lay off cg equal to R, and ch equal to p. With g as a centre and g h as a radius, draw the arc h k; with the centre e and radius e f draw the arc f k, intersecting h k at k. Draw the line g k and produce it, making g l equal to R. Draw k e and produce it, making k m equal to p. With the centre g and radius g c (= R) draw the arc c l; with the centre k and radius k l (= p) draw the arc lm, and with the centre e and radius em (=r) draw the arc m a.

The remainder of the work is symmetrical with respect to the axes.



46. The Parabola.—A parabola (DAC, Fig. 55) is a curve such that every point in the curve is equally distant from the directrix KL and the focus F. The focus lies in the axis AB drawn from the vertex or head of the curve A, so as to divide the figure into two equal parts. The vertex A is equidistant from the directrix and the focus, or Ae = AF. Any line parallel to the axis is a diameter. A straight line, as EG or DC, drawn across the figure at right angles to the axis is a double ordinate, and either half of it is an ordinate. The ordinate to the axis EFG, drawn through the focus, is called the parameter of the axis. A segment of the axis, reckoned from the vertex, is an abscissa of the axis, and it is an abscissa of the ordinate drawn from the base of the abscissa. Thus, AB is an abscissa of the ordinate BC.



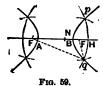


2d Method: By means of a square and a cord (Fig. 56).—Place a straight-edge to the directrix E N, and apply to it a square L E G. Fasten to the end G one end of a thread or cord equal in length to the edge E G, and attach the other end to the focus F; slide the square along the straight-edge, holding the cord taut against the edge of the square by a pencil D, by which the curve is described.

3d Method: When the height and the base are given (Fig. 57).—Let A B be the given axis, and C D a double ordinate or base; to describe a parabola of which the vertex is at A. Through A draw E F parallel to C D, and through C and D draw C E and D F parallel to the axis. Divide B C and B D into any number of equal parts, say five, at a, b, etc., and divide C E and D F into the same number of parts. Through the points a, b, c, d in the base C D on each side of the axis draw perpendiculars, and through a, b, c, d in C E and D F draw lines to the vertex A, cutting the perpendiculars at e, f, g, h. These are points in the parabola, and the curve C A D may be traced as shown, passing through them.

47. The Hyperbola (Fig. 58).—A hyperbola is a plane curve, such that the difference of the distances from any point of it to two fixed points is equal to a given distance. The fixed points are called the foci.





To construct a hyperbola. —Let F' and F be the foci, and F' F the distance between them. Take a ruler longer than the distance F' F, and fasten one of its extremities at the focus F'. At the other extremity, H, attach a thread of such a length that the length of the ruler shall exceed the length of the thread by a given distance A B. Attach the other ex-tremity of the thread at the focus F.

Press a pencil, P, against the ruler, and keep the thread constantly tense, while the ruler is turned around F' as a centre. The point of the pencil will describe one branch of the curve.

2d Method: By points (Fig. 59).—
From the focus F' lay off a distance F' N equal to the transverse axis, or distance between the two branches of the curve, and take any other distance,

as F'H, greater than F'N.

With F' as a centre and F'H as a radius describe the arc of a circle. Then with F as a centre and NH as a

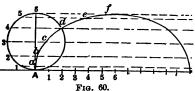
radius describe an arc intersecting the arc before described at p and q.

These will be points of the hyperbola, for F''q - F'q is equal to the trans-

If, with F as a centre and F' H as a radius, an arc be described, and a second arc be described with F' as a centre and NH as a radius, two points in the other branch of the curve will be determined. Hence, by changing the centres, each pair of radii will determine two points in each branch.

The Equilateral Hyperbola.—The transverse axis of a hyperbola.

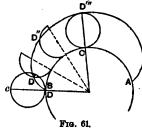
is the distance, on a line joining the foci, between the two branches of the curve. The conjugate axis is a line perpendicular to the transverse axis drawn from its centre, and of such a length that the diagonal of the rectangle of the transverse and conjugate axes is equal to the distance between the foci. The diagonals of this rectangle, indefinitely prolonged, are the asymptotes of the hyperbola, lines which the curve continually approaches, but touches only at an infinite distance. If these asymptotes are perpendicular to each other, the hyperbola is called a rectangular or equilateral hyperbola. It is a property of this hyperbola that if the asymptotes are taken as axes of a rectangular system of coordinates (see Analytical Geometry), the product of the abscissa and ordinate of any point in the curve is equal to the product of the abscissa and ordinate of any other point; or, if p is the ordinate of any point and v its abscissa, and p_1 and v_1 are the ordinate and abscissa of any other point, $pv=p_1v_1$; or pv=a constant.



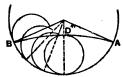
48. The Cycloid (Fig. 60).—If a circle A d be rolled along a straight line A6, any point of the circumference as A will describe a curve, which is called a cycloid. The circle is called the generating circle, and A the generating point.

To draw a cycloid. Divide the circumference

of the generating circle into an even number of equal parts, as A 1, 12, etc., and set off these distances on the base. Through the points 1, 2, 3, etc., on the circle draw horizontal lines, and on them set off distances 1a = A1, 3b=42, 3c=43, etc. The points A,a,b,c, etc., will be points in the cycloid, through which draw the curve.



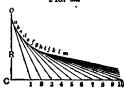
49. The Epicycloid (Fig. 61) is generated by a point D in one circle D C rolling upon the circumference of another circle A C B, instead of on a flat surface or line; the former being the generating circle, and the latter the fundamental circle. The generating circle is shown in four positions, in which the generating point is successively marked D, D', D'', D''', A D''' B is the epicycloid.



50. The Hypocycloid (Fig. 62) is generated by a point in the generating circle rolling on the inside of the fundamental circle.

Fig. 62.

When the generating circle = radius of the other circle, the hypocycloid becomes a straight line.



51. The Tractrix or Schiele's anti-friction curve (Fig. 63).—R is the radius of the shaft, C, 1, 2, etc., the axis. From O set off on R a small distance, o a; with radius R and centre a cut the axis at 1, join a 1, and set off a like small distance ab; from b with radius R cut axis at 2, join b 2, and so on, thus finding points o, a, b, c, d, etc., through which the curve is to be drawn.

Fig. 63.

The Spiral.—The spiral is a curve described by a point which moves along a straight line according to any given law, the line at the same time having a uniform angular motion. The line is called the radius vector.

F1G. 64.

If the radius vector increases directly as the measuring angle, the spires, or parts described in each revolution, thus gradually increasing their distance from each other, the curve is known as the spiral of Archimedes (Fig. 64).

(Fig. 64).
This curve is commonly used for cams. To describe it draw the radius vector in several different directions around the centre, with equal angles

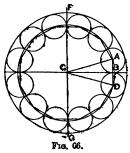
between them; set off the distances 1, 2, 3, 4, etc., corresponding to the scale upon which the curve is drawn, as shown in Fig. 64.

In the common spiral (Fig. 64) the pitch is uniform; that is, the spires are equidistant. Such a spiral is made by rolling up a belt of uniform thickness.

To construct a spiral with four centres (Fig. 55...-Given the pitch of the spiral, construct a square about the centre, with the sum of the four sides equal to the pitch. Prolong the sides in one direction as shown; the corners are the centres for each are of the external angles, forming a quadrant of a spire.

Fig. 65.

53. To find the diameter of a circle into which a certain number of rings will fit on its inside (Fig. 66).—For instance, what is the diameter of a circle into which twelve is inch rings will fit, as per sketch? Assume that we have found the diameter of the required



circle, and have drawn the rings inside of it, Join the centres of the rings by straight lines, as shown: we then obtain a regular polygon with 12 sides, each side being equal to the diameter of a given ring. We have now ameter of a given ring. We have now to find the diameter of a circle circumscribed about this polygon, and add the diameter of one ring to it; the sum will be the diameter of the circle into which the rings will fit. Through the centres A and D of two adjacent rings draw the radii CA and CD; since the polygon has twelve sides the angle $A C D = 30^{\circ}$ and $A C B = 15^{\circ}$. One half of the side A D is equal to A B. We now give the following pro-

Fig. 66. portion: The sine of the angle $A \subset B$ is to $A \cap B$ by the sine of the angle $A \subset B$; the quotient will be the radius of the circumscribed circle; add to the corresponding diameter the diameter of one ring; the sum will be the required diameter FG.

stangeter of one ring; the sum will be the required diameter FG. 54. To describe an arc of a circle which is too large to be drawn by a heatm compass, by means of points in the arc, radius being given.—Suppose the radius is 20 feet and it is desired to obtain five points in an arc whose half chord is 4 feet. Draw a time equal to the half chord, full size, or on a smaller scale if more convenient, and erect a perpendicular at one end, thus making rectangular axes of coordinates. Erect perpendiculars at points 1, 2, 3, and 4 feet from the first perpendicular. Find values of y in the formula of the circle, $x^2 + y^2 = R^2$ by substituting for x the values 0, 1, 2, 3, and 4, etc., and for R^2 the square of the radius, or 400. The values will be $y = \sqrt[4]{R^2 - x^2} = \sqrt[4]{400}$.

√350, √356, √391, √364; = 20, Subtract the smallest, 19.975, 19.90, 19.774, 19.596.

or 19.596 leaving 0.404, 0.879, 0.304, 0.178, 0 feet.

Lay off these distances on the five perpendiculars, as ordinates from the Lay off these distances on the new perpendiculars, as ordinates from unchaif chord, and the positions of five points on the arc will be found.

Through these the curve may be drawn. (See also Problem 14.)

55. The Catemary is the curve assumed by a perfectly fiexible cord when its ends are fastened at two colors the majorit of a unit length

points, the weight of a unit length being constant. The equation of the catenary is

, in which e is the base of the Naperian system of logarithms.

To plot the catenary.—Let o (Fig. 67) be the origin of coordinates. Assigning to a any value as 3, the equation becomes

$$y = \frac{3}{2} \left(e^{\frac{x}{3}} + e^{-\frac{x}{3}} \right).$$

Fig. 67. To find the lowest point of the curve.

Put
$$x = 0$$
; $\therefore y = \frac{3}{2} \left(e^0 + e^{-0} \right) = \frac{3}{2} (1 + 1) = 3$.

Then put
$$x = 1$$
; $y = \frac{3}{2} \left(e^{\frac{3}{2}} + e^{-\frac{3}{2}} \right) = \frac{3}{2} (1.396 + 0.717) = 3.17.$

Fut $x = 2$; $y = \frac{3}{2} \left(e^{\frac{3}{2}} + e^{-\frac{3}{2}} \right) = \frac{3}{2} (1.948 + 0.513) = 3.69.$

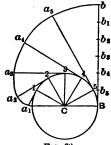
Put x = 8, 4, 5, etc., etc., and find the corresponding values of y. For each value of y we obtain two symmetrical points, as for example p and p^1 . In this way, by making a successively equal to 2, 3, 4, 5, 6, 7, and 8, the curves of Fig. 67 were plotted.

In each case the distance from the origin to the lowest point of the curve

is equal to a; for putting x = o, the general equation reduces to y = a.

For values of a = 6, 7, and 8 the catenary closely approaches the parabola. For derivation of the equation of the catenary see Bowser's Analytic Mechanics. For comparison of the catenary with the parabola, see article by F. R. Honey, Amer. Machinist, Feb. 1, 1884.

56. The Involute is a name given to the curve which is formed by the end of a string which is unwound



from a cylinder and kept taut; con-sequently the string as it is unwound will always lie in the direction of a tangent to the cylinder. To describe tangent to the cylinder. To describe the involute of any given circle, Fig. 68, take any point A on its circumference, draw a diameter AB, and from B draw B b perpendicular to AB. Make Bb equal in length to half the circumference of the circle. Divide Bb and the semi-circumference into the same number of equal parts, the same number of equal parts, say six. From each point of division 1, 2, 3, etc., on the circumference draw lines to the centre C of the circle. Then draw 1 a perpendicular to C1; $2a_1$ perpendicular to C2; and so on.

Fig. 68. Make 1 a equal to bb_1 ; $2a_2$ equal to bb_3 ; and so on. Join the points A, a_1 , a_2 , a_3 , etc., by a curve; this curve will be the required involute.

57. Method of plotting angles without using a protrac-tor.—The radius of a circle whose circumference is 360 is 57.8 (more accurately 57.296). Striking a semicircle with a radius 57.3 by any scale spacers set to 10 by the same scale will divide the arc into 18 spaces of 10° each, and intermediates can be measured indirectly at the rate of 1 by scale for each 1°, or interpolated by eye according to the degree of accuracy required. The following table shows the chords to the above-mentioned radius, for every 10 degrees from 0° up to 110°. By means of one of these,

Angle.	Chord.	Angle.	Chord.
i°	0.999	60°	57.296
10°		70°	65.727
20°	19.899	80°	
30°		90°	81.029
40°		100°	87.782
50°		110°	93.869

a 10° point is fixed upon the paper next less than the required angle, and the remainder is laid off at the rate of 1 by scale for each degree.

GEOMETRICAL PROPOSITIONS.

In a right-angled triangle the square on the hypothenuse is equal to the sum of the squares on the other two sides. If a triangle is equilateral, it is equiangular, and vice versa. If a straight line from the vertex of an isosceles triangle bisects the base,

it bisects the vertical angle and is perpendicular to the base.

If one side of a triangle is produced, the exterior angle is equal to the sum of the two interior and opposite angles.

If two triangles are mutually equiangular, they are similar and their corresponding sides are proportional. If the sides of a polygon are produced in the same order, the sum of the exterior angles equals four right angles. (Not true if the polygon has re-

entering angles) In a quadrilateral, the sum of the interior angles equals four right angles. In a parallelogram, the opposite sides are equal: the opposite angles are equal: it is bisected by its diagonal, and its diagonals bisect each other.

If three points are not in the same straight line, a circle may be passed through them.

If two arcs are intercepted on the same circle, they are proportional to the corresponding angles at the centre.

If two arcs are similar, they are proportional to their radii,
The areas of two circles are proportional to the squares of their radii.

If a radius is perpendicular to a chord, it bisects the chord and it bisects the arc subtended by the chord.

A straight line tangent to a circle meets it in only one point, and it is

perpendicular to the radius drawn to that point.

If from a point without a circle tangents are drawn to touch the circle, there are but two; they are equal, and they make equal angles with the chord joining the tangent points, if two lines are parallel chords or a tangent and parallel chord, they recept equal arcs of a circle.

If an angle at the circumference of a circle, between two chords, is sublended by the same arc as an angle at the centre, between two radii, the same at the circumference is equal to half the angle at the centre.

If a triangle is inscribed in a semicircle, it is right-angled.

If two chords intersect each other in a circle, the rectangle of the segments of the one equals the rectangle of the segments of the other.

And if one chord is a diameter and the other perpendicular to it, the rectangle of the segments of the diameter is equal to the square on half the other chord, and the half chord is a mean proportional between the segments of the diameter.

If an angle is formed by a tangent and chord, it is measured by one half of the arc intercepted by the chord; that is, it is equal to half the angle at the centre subtended by the chord.

the centre subtended by the choru.

Degree of a Railway Curve.—This last proposition is useful in staking out railway curves. A curve is designated as one of so many degrees, and the degree is the angle at the centre subtended by a chord of 100 ft. To lay out uggree is the angle at the centre subtended by a cnord of 100 ft. To lay out a curve of n degrees the transit is set at its beginning or "point of curve," pointed in the direction of the tangent, and turned through 1/2n degrees; a point 100 ft. distant in the line of sight will be a point in the curve. The Tansit is then swung 1/2n degrees further and a 100 ft. chord is measured from the point already found to a point in the new line of sight, which is a second point or "station" in the curve.

The radius of a 1° curve is 5729.65 ft., and the radius of a curve of any degree is 5729.65 ft., are the radius of a curve of any degree is 5729.65 ft., are the radius of a curve of any

degree is 5729.65 ft. divided by the number of degrees.

MENSURATION.

PLANE SURFACES.

Quadrilateral.—A four-sided figure.

Parallelogram.—A quadrilateral with opposite sides parallel.

Varieties.—Equare: four sides equal, all angles right angles. Rectangle: opposite sides equal, all angles right angles. Rhombus: four sides equal, opposite angles equal, angles not right angles. Rhombodd: opposite sides equal, opposite angles equal, angles not right angles.

Traperium.—A quadrilateral with unequal sides.

Trapezoid.-A quadrilateral with only one pair of opposite sides paraliel.

Diagonal of a square = $\sqrt{2 \times \text{side}^2} = 1.4142 \times \text{side}$.

Ding. of a rectangle = \sum of squares of two adjacent sides.

Area of any parallelogram = base × slittude.

Area of rhombus or rhomboid = product of two adjacent sides x sine of angle included between them.

Area of a trapezium = half the product of the diagonal by the sum of the perpendiculars let fall on it from opposite angles.

Area of a trapezoid = product of half the sum of the two parallel

aides by the perpendicular distance between them.

To find the area of any quadrilateral figure.—Divide the quadrilateral into two triangles; the sum of the areas of the triangles is the

area. Or, multiply half the product of the two diagonals by the size of the angle at their intersection.

To find the area of a quadrilateral inscribed in a circle. From half the sum of the four sides subtract each side severally; multiply the four remainders together; the square root of the product is the area.

Triangle.—A three-sided plane figure.

Varieties.—Right-angled, having one right angle; obtue-angled, having one obtuse angle; isosceles, having two equal angles and two equal sides; equilateral, having three equal sides and equal angles.

The sum of the three angles of every triangle = 180°.

The sum of the two acute angles of a right-angled triangle = 90°.

Hypothenuse of a right-angled triangle, the side opposite the right angle. = $\sqrt{\text{sum of the squares of the other two sides}}$. If n and b are the two sides and c the hypothenuse, $c^2 = a^2 + b^2$; $a = \sqrt{c^2 - b^2} = \sqrt{(c+b)(c-b)}$.

To find the area of a triangle:

r

RULE 1. Multiply the base by half the altitude.
RULE 2. Multiply half the product of two sides by the sine of the included

RULE 3. From half the sum of the three sides subtract each side severally; multiply together the half sum and the three remainders, and extract the square root of the product.

The area of an equilateral triangle is equal to one fourth the square of one of its sides multiplied by the square root of $8_1 = \frac{\alpha^2 \sqrt{6}}{100}$, a being the side; or

 $a^2 \times .433013$

Hypothenuse and one side of right-angled triangle given, to find other side. Required side = Vhyp2 - given side2.

If the two sides are equal, side = hyp + 1.4142; or hyp \times .7071. Area of a triangle given, to find base: Base = twice area + perpendicular height

Area of a triangle given, to find height: Height = twice area + base.

Two sides and base given, to find perpendicular height (in a triangle in

which both of the angles at the base are acute).

RULE.—As the base is to the sum of the sides, so is the difference of the sides to the difference of the divisions of the base made by drawing the per-Half this difference being added to or subtracted from half the base will give the two divisions thereof. As each side and its opposite I wision of the base constitutes a right-angled triangle, the perpendicular is ascertained by the rule perpendicular = \(\frac{1}{2} \) hyp2 - base2.

Polygon. — A plane figure having three or more sides. Regular or irregular, according as the sides or angles are equal or unequal. Polygons

are named from the number of their sides and angles. To find the area of an irregular polygon.—Draw diagonals dividing the polygon into triangles, and find the sum of the areas of these triangles.

To find the area of a regular polygon:

RULE.—Multiply the length of a side by the perpendicular distance to the centre; multiply the product by the number of sides, and divide it by 2. Or, multiply half the perimeter by the perpendicular let fall from the centre on one of the sides.

The perpendicular from the centre is equal to half of one of the sides of the polygon multiplied by the cotangent of the angle subtended by the half

The angle at the centre $= 360^{\circ}$ divided by the number of sides.

TARLE OF REGILAR POLVEONS

	TABLE OF REGULAR POLITIONS.										
	i no	_	Radius of Cir- cumscribed Circle.		ibed = 1.	, Ra- mec.	9,	₽ Q -			
No. of Sides.	Name of Polygon.	Area, Side = 1.	Perpen. from Centre = 1.	Side = 1.	Radius of Inscribed Circle, Side = 1.	Length of Side, Radius of Circumsc. Circle = 1.	Angle at Centre.	Angle between faceut Sides,			
8 4 5 6 7	Triangle Equare Pentagon Hexagon Hoptagon	.4380127 1. 1.7204774 2.5980762 8.6389124	2. 1.414 1.238 1.155 1.11	.5778 .7071 .8506 1. 1.1524	.2887 .5 .6882 .866 1.0383	1.782 1.4142 1.1756 1.	120° 90 72 60 51 26′	60° 90 108 120 128 4-7			
8 9 10 11 12	Octagon Ronagon Decagon Undecagon Dodecagon	4.8884271 6.1818242 7.6942068 9.3656399 11.1961524	1.088 1.064 1.051 1.042 1.087	1.3066 1.4619 1.618 1.7747 1.9319	1.2071 1.3737 1.5388 1.7028 1.866	.7658 .684 .618 .5634 .5176	45 40 36 32 43' 80	135 140 144 147 3-11 150			

To find the area of a regular polygon, when the length

of a side only is given:

RULE.—Multiply the square of the side by the multiplier opposite to the name of the polygon in the table.

To find the area of an irregular figure (Fig. 69).—Draw ordinates across its breadth at equal distances apart, the first and the last ordinate each being one half space from the ends of the figure. Find the average breadth by adding together the lengths of these lines included besween the boundaries of the figure, and divide by the number of the lines added; multiply this mean breadth by the length. The greater the number of lines the nearer the approximation.

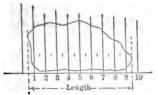


Fig. 69.

In a figure of very irregular outline, as an indicator-diagram from a highspeed steam-engine, mean lines may be substituted for the actual lines of the figure, being so traced as to intersect the undulations, so that the total area of the spaces cut off may be compensated by that of the extra spaces inclosed.

2d Method: The Trapezoidal Rule. — Divide the figure into any sufficient number of equal parts; add half the sum of the two end ordinates to the sum of all the other ordinates; divide by the number of spaces (that is, one less than the number of ordinates) to obtain the mean ordinate, and

one less than the number of ordinates) to obtain the mean ordinate, and multiply this by the length to obtain the area.

3d Method: Simpson's Rule.—Divide the length of the figure into any even number of equal parts, at the common distance D apart, and draw ordinates through the points of division to touch the boundary lines. Add together the first and last ordinates and call the sum A: add together the even ordinates and call the sum B; add together the odd ordinates, except the first and last, and call the sum C. Then,

area of the figure =
$$\frac{A+4B+2O}{3} \times D$$
.

4th Method: Durand's Rule.—Add together 4/10 the sum of the first and last ordinates, 1 1/10 the sum of the second and the next to the last (or the penultimates), and the sum of all the intermediate ordinates. Multiply the sum thus gained by the common distance between the ordinates to obtain the area, or divide this sum by the number of spaces to obtain the mean ordinate.

Prof. Durand describes the method of obtaining his rule in Engineering News, Jan. 18, 1894. He claims that it is more accurate than Simpson's rule, and practically as simple as the trapezoidal rule. He thus describes its application for approximate integration of differential equations. Any definite integral may be represented graphically by an area. Thus, let

$$Q = \int u \, dx$$

be an integral in which u is some function of x, either known or admitting of computation or measurement. Any curve plotted with x as abscissa and u as ordinate will then represent the variation of u with x, and the area between such curve and the axis X will represent the integral in question, no matter how simple or complex may be the real nature of the function u.

Substituting in the rule as above given the word "volume" for "area and the word "section" for "ordinate," it becomes applicable to the determination of volumes from equidistant sections as well as of areas from

equidistant ordinates.

Having approximately obtained an area by the trapezoidal rule, the area by Durand's rule may be found by adding algebraically to the sum of the ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates + sum of the other ordinates) 1/10 of (sum of penultimates — sum of first and last) and multiplying by the common distance between the ordinates) 1/10 of (sum of penultimates — sum of first and last) and multiplying by the common distance between the ordinates) 1/10 of (sum of penultimates — sum of first and last) and multiplying by the common distance between the ordinates) 1/10 of (sum of penultimates — sum of the ordinates) 1/10 of (sum of penultimates — sum of the ordinates) 1/10 of (sum of penultimates — sum of the ordinates) 1/10 of (sum of penultimates — sum of the ordinates) 1/10 of (sum of penultimates — sum of the ordinates) 1/10 of (sum of penultimates — sum of the ordinates) 1/10 of (sum of penultimates — sum of the ordinates) 1/10 of (sum of penultimates — sum of the ordinates) 1/10 of (sum of penultimates — sum of the ordinates) 1/10 of (sum of penultimates — sum of the ordinates) 1/10 of (sum of penultimates — sum of penultimates nates

5th Method.—Draw the figure on cross-section paper. Count the number of squares that are entirely included within the boundary; then estimate of squares that are cut by the boundary, add together the fractional parts of squares that are cut by the boundary, add together these fractions, and add the sum to the number of whole squares. The result is the area in units of the dimensions of the squares. The finer the ruling of the cross-section paper the more accurate the result.

7th Method.—Use a planimeter.

7th Method.—With a chemical balance, sensitive to one milligram, draw

the figure on paper of uniform thickness and cut it out carefully; weigh the piece cut out, and compare its weight with the weight per square inch of the paper as tested by weighing a piece of rectangular shape.

THE CIRCLE.

Circumference = diameter × 3.1416, nearly; more accurately, 3.14159265859, Approximations, $\frac{22}{7} = 8.148$; $\frac{855}{113} = 3.1415929$.

The ratio of circum, to diam, is represented by the symbol π (called Pi),

Multiples of w.	Multiples of $\frac{\pi}{4}$.
$1\pi = 8.14159265859$	$\frac{1}{4}\pi = .7853982$
2w = 6.28318530718	" × 2 = 1.5707963
$8\pi = 9.42477796077$	" $\times 3 = 2.8561945$
$4\pi = 12.56637061486$	" $\times 4 = 3.1415927$
$5\pi = 15.70796326795$	" × 5 = 3.9269908
$6\pi = 18.84955592154$	" \times 6 = 4.7123890
$7\pi = 21.99114857518$	" \times 7 = 5.4977871
$8\pi = 25.18274122872$	" × 8 = 6.2831853
$9\pi = 28.27433388231$	" × 9 = 7.0685885

Ratio of diam. to circumference = reciprocal of $\pi = 0.3183099$,

Reciprocal of
$$\frac{1}{4}\pi = 1.27324$$
.

Multiples of $\frac{1}{\pi}$.

 $\frac{8}{\pi} = 2.54648$
 $\frac{8}{\pi} = 2.54648$
 $\frac{1}{360} = 0.0087266$
 $\frac{1}{\pi} = .31831$
 $\frac{9}{\pi} = 2.86479$
 $\frac{360}{\pi} = 114.5915$
 $\frac{2}{\pi} = .63668$
 $\frac{10}{\pi} = 3.18310$
 $\frac{12}{\pi} = 3.81972$
 $\frac{1}{\pi^2} = 0.101321$
 $\frac{4}{\pi} = 1.27324$
 $\frac{1}{2}\pi = 1.570796$
 $\frac{1}{3}\pi = 1.047197$
 $\frac{6}{\pi} = 1.90986$
 $\frac{1}{\pi} = 0.523599$

Log $\pi = 0.49714987$

Log $\pi = 0.49714987$

Log $\pi = 0.49714987$

Diam. in ins. = $18.5405 \sqrt{\text{area in sq. ft.}}$ Area in sq. ft. = (diam. in inches)² × .0054542. D = diameter, R = radius, C = circumference,

$$C = \pi D; = 2\pi R; = \frac{4A}{D}; = 2\sqrt[4]{\pi A}; = 3.545\sqrt[4]{A};$$

$$A = D^2 \times .7854; = \frac{CR}{2}; = 4R^2 \times .7854; = \pi R^2; = \frac{1}{4}\pi D^2; = \frac{C^2}{4}; = .07958C^2; = \frac{CD}{4}.$$

$$D = \frac{C}{\pi}$$
; = 0.81881C; [= 2 $\sqrt{\frac{A}{\pi}}$; = 1.12838 \sqrt{A} ;

$$R = \frac{C}{2\pi}$$
; = 0.159155C; = $\sqrt{\frac{A}{\pi}}$; = 0.564189 \sqrt{A} .

Areas of circles are to each other as the squares of their diameters.

To find the length of an arc of a circle:

EULE 1. As 360 is to the number of degrees in the arc, so is the circumference of the circle to the length of the arc.

EULE 2. Multiply the diameter of the circle by the number of degrees in

the arc, and this product by 0.0087286.

Belations of Arc, Chord, Chord of Half the Arc, Versed Sine, etc.

Let R = radius, D = diameter, Arc = length of arc.

Cd =chord of the arc, ch = chord of half the arc,

V = versed sine, or height of the arc.

$$Arc = \frac{8ch - Cd}{8} \text{ (very nearly)}, = \frac{\sqrt[4]{Cd^2 + 4V^2} \times 10V^2}{15Cd^2 + 23V^2} + 2ch, \text{ nearly.}$$

$$Arc = \frac{2ch \times 10V}{60D - 27V} + 2ch, \text{ nearly.}$$

Chord of the are =
$$2\sqrt{ch^2 - V^2}$$
; = $\sqrt{D^2 - (D - 2V)^2}$; = $8ch - 3Arc$.
= $2\sqrt{R^2 - (R - V)^2}$; = $2\sqrt{(D - V)} \times V$.

Chord of half the arc, $ch = \frac{1}{2} \sqrt{Cd^2 + 4V^2}$; $= \sqrt{D \times V}$; $= \frac{8Arc + Cd}{2}$

Diameter
$$= \frac{ch^2}{V}; = \frac{\left(\frac{1}{2}Cd\right)^2 + V^2}{V};$$

Versed sine

$$= \frac{ch^2}{D}; = \frac{1}{2}(D - \sqrt[4]{D^2 - Cd^2})$$

(or
$$\frac{1}{2}(D + \sqrt{D^2 - Cd^2})$$
, if V is greater than radius
$$= \sqrt{\frac{ch^2 - \frac{Cd^2}{4}}{4}}.$$

Half the chord of the arc is a mean proportional between the versed sine

and diameter minus versed sine: $\frac{1}{2}Cd = \sqrt{V \times (D - V)}$.

Length of the Chord subtending an angle at the centre = twice the sine of half the angle. (See Table of Sines, p. 157.)

Length of a Circular Arc.—Huyghens's Approximation.
Let C represent the length of the chord of the arc and c the length of the chord of half the arc; the length of the arc

$$L=\frac{8c+C}{8}.$$

Professor Williamson shows that when the arc subtends an angle of 80°, the radius being 100,000 feet (nearly 19 miles), the error by this formula is about two inches, or 1/600000 part of the radius. When the length of the arc is equal to the radius, i.e., when it subtends an angle of 57°.3, the error is less than 1/7680 part of the radius. Therefore, if the radius is 100,000 feet, the error is less than $\frac{100000}{7680}$ = 13 feet. The error increases rapidly with the increase of the angle subtended.

In the measurement of an are which is described with a short radius the error is so small that it may be neglected. Describing an arc with a radius of 13 inches subtending an angle of 30°, the error is 1/50000 of an inch. For 5°,3 the error is less than 0°.0015.

In order to measure an arc when it subtends a large angle, bisect it and measure each half as before—in this case making B = length of the chord of half the arc, and b = length of the chord of one fourth the arc; then

$$L = \frac{16b - 2B}{3}.$$

Relation of the Circle to its Equal, Inscribed, and Circumscribed Squares.

Diameter of circle × .88623 { = side of equal square.

Circumference of circle × .2820 } = perimeter of equal square.

Diameter of circle × .7871 Circumference of circle × .22508 = side of inscribed square. Area of circle × .90031+ diameter 1.2782 .68662 1.4142 = area of circumscribed square, = area of inscribed square. Area of circle × Area of circle × Side of square x = diam. of circumscribed circle. 4.4428 = circum. 44 66 1.1284 = diam. of equal circle. × 8.5449 = circum. Perimeter of square × 0.88623Square inches x 1.2732 = circular inches.

Sectors and Segments.—To find the area of a sector of a circle. RULE 1. Multiply the arc of the sector by half its radius.
RULE 2. As 360 is to the number of degrees in the arc, so is the area of

RULE 2. As now is we are not the sector in the arc, so as the since to the arce of the sector.

Ross 3. Multiply the number of degrees is the arc by the square of the radius and by .00727.

To find the arcs of a segment of a circle: Find the arcs of the sector which has the same arc, and also the arcs of the triangle formed by the chord of the segment and the radii of the sector.

Then take the sum of these areas, if the segment is greater than a semi-circle, but take their difference if it is less.

Another Method: Area of segment = $\frac{1}{2}R(\text{arc} - \sin A)$, in which A is the central angle, R the radius, and arc the length of arc to radius 1. To find the area of a segment of a circle when its chord and height only

are given. First find radius, as follows:

radius =
$$\frac{1}{2} \left[\frac{\text{square of half the chord}}{\text{height}} + \text{height} \right]$$
.

2. Find the angle subtended by the arc, as follows: half chord + radius = sine of half the angle. Take the corresponding angle from a table of sines, and double it to get the angle of the arc.

3. Find area of the sector of which the segment is a part:

area of sector = area of circle \times degrees of arc + 360.

4. Subtract area of triangle under the segment):

Area of triangle = half chord \times (radius - height of segment).

The remainder is the area of the segment.

When the chord, arc, and diameter are given, to find the area. From the length of the are subtract the length of the chord. Multiply the remainder by the radius or one-half diameter; to the product add the chord multiplied by the height, and divide the sum by 2.

Given diameter, d. and height of segment, h.

When A is from 0 to 14d, area =
$$h\sqrt{1.766dh - h^2}$$
;
" " 14d to 14d, area = $h\sqrt{0.017d^2 + 1.7dh - h^2}$

(approx.). Greatest error 0.226, when $h=\frac{1}{2}d$. To find the chord: From the diameter subtract the height; multiply the

remainder by four times the height and extract the square root.

When the chords of the arc and of half the arc and the rise are given: To the chord of the arc add four thirds of the chord of half the arc, multiply

the sum by the rise and the product by .40426 (approximate).

Circular Hing.—To find the wrea of a ring included between the circumferences of two concentric circles: Take the difference between the areas of the two circles; or, subtract the square of the less radius from the square of the greater, and multiply their difference by 3.14159.

The area of the greater circle is equal to πR^2 ; and the area of the smaller,

Their difference, or the area of the ting, is $\pi (R^2 - r^2)$.

The Ellipse.-Area of an ellipse = product of its semi-axes × 8.14159 = product of its axes x .785398.

The Ellipse,—Circumference (approximate) = 3.1416 $\sqrt{\frac{D^2+d^2}{D^2+d^2}}$, D and d

being the two axes. Trautwine gives the following as more accurate: When the longer axis P is not more than five times the length of the shorter axis, d,

Circumference = 3.1416
$$\sqrt{\frac{D^2+d^2}{2} - \frac{(D-d)^2}{8.8}}$$
.

When D is more than 5d, the divisor 8.8 is to be replaced by the following:

For D/d = 6 7 8 9 10 12 14 16 18 20 30 40 5 Then D is more than 5a, the divisor 5.5 is to be repracted by sile following. For D/d=6 7 8 9 10 12 14 16 18 20 30 40 50 Divisor = 9 9.2 9.3 9.35 9.4 9.5 9.6 9.68 9.75 9.8 9.92 9.98 10 An accurate formula is $C=\pi(a+b)\Big(1+\frac{A^2}{4}+\frac{A^4}{16}+\frac{A^6}{256}+\frac{25A^8}{16384}+\ldots\Big)$, in

An accurate formula is
$$C = \pi(a+b)\left(1 + \frac{A^2}{4} + \frac{A^4}{16} + \frac{A^6}{256} + \frac{25A^6}{16384} + \dots\right)$$
, in

which
$$A = \frac{a-b}{a+b}$$
.—Ingenieurs Taschenbuch, 1896.

Carl G. Barth (Machinery, Sept., 1900) gives as a very close approximation to this formula

$$C = \pi(a+b) \frac{64 - 3A^4}{64 - 16A^2}$$

Area of a segment of an ellipse the base of which is parallel to one of the axes of the ellipse. Divide the height of the segment by the axis of which it is part, and find the area of a circular segment, in a table of circuthus found by the product of the two axes of the ellipse.

Cycloid.—A curve generated by the rolling of a circle on a plane.

Length of a cycloidal curve $= 4 \times \text{diameter of the generating circle.}$ Length of the base = circumference of the generating circle. Area of a cycloid $= 8 \times$ area of generating circle.

Helix (Screw).—A line generated by the progressive rotation of a point around an axis and equidistant from its centre.

Length of a helix.—To the square of the circumference described by the generating-point add the square of the distance advanced in one revolution, and take the square root of their sum multiplied by the number of revolutions of the generating point. Or,

$$\sqrt{(c^2+h^2)n} = \text{length}, n \text{ being number of revolutions}.$$

Spirals.-Lines generated by the progressive rotation of a point around a fixed axis, with a constantly increasing distance from the axis.

A plane spiral is when the point rotates in one plane.

A conical spiral is when the point rotates around an axis at a progressing distance from its centre, and advancing in the direction of the axis, as around

Length of a plane spiral line.—When the distance between the coils is

RULE.—Add together the greater and less diameters; divide their sum by 2; multiply the quotient by 3.1416, and again by the number of revolutions. Or, take the mean of the length of the greater and less circumferences and multiply it by the number of revolutions. Or,

length =
$$\pi n \frac{d+d'}{2}$$
, d and d' being the inner and outer diameters.

Length of a conical spiral line.—Add together the greater and less diameters; divide their sum by 2 and multiply the quotient by 3.1416. To the square of the product of this circumference and the number of revolutions of the spiral add the square of the height of its axis and take the square root of the sum.

Or, length =
$$\sqrt{\left(\pi n \frac{d+d'}{2}\right)^2 + \hbar^2}$$
.

SOLID BODIES.

The Prism.—To find the surface of a right prism: Multiply the perimeter of the base by the altitude for the convex surface. To this add the areas of the two ends when the entire surface is required.

Volume of a prism = area of its base \times its altitude.

The pyramid.—Convex surface of a regular pyramid = perimeter of its base x half the slant height. To this add area of the base if the whole surface is required.

Volume of a pyramid = area of base \times one third of the altitude.

To find the surface of a frustum of a regular pyramid: Multiply half the slant height by the sum of the perimeters of the two bases for the convex surface. To this add the areas of the two bases when the entire surface is

required.

To find the volume of a frustum of a pyramid: Add together the areas of the two bases and a mean proportional between them, and multiply the sum by one third of the altitude. (Mean proportional between two numbers

= square root of their product.)

Wedge.—A wedge is a solid bounded by five planes, viz.: a rectangular base, two trapezoids, or two rectangles, meeting in an edge, and two tri-angular ends. The altitude is the perpendicular drawn from any point in the edge to the plane of the base.

To find the volume of a wedge: Add the length of the edge to twice the length of the base, and multiply the sum by one sixth of the product of the

height of the wedge and the breadth of the base.

Rectangular prismold.—A rectangular prismold is a solid bounded by six planes, of which the two bases are rectangles, having their corresponding sides parallel, and the four upright sides of the solids are trapezoids.

To find the volume of a rectangular prismoid: Add together the areas of the two bases and four times the area of a parallel section equally distant from the bases, and multiply the sum by one sixth of the altitude.

Cylinder.—Convex surface of a cylinder = perimeter of base × altitude. To this add the areas of the two ends when the entire surface is required.

Volume of a cylinder = area of base \times altitude.

Come.—Convex surface of a cone = circumference of base × half the slant side. To this add the area of the base when the entire surface is required.

Volume of a cone = area of base \times one third of the altitude.

To find the surface of a frustum of a cone: Multiply half the side by the sum of the circumferences of the two bases for the convex surface; to this add the areas of the two bases when the entire surface is required.

To find the volume of a frustum of a cone: Add together the areas of the two bases and a mean proportional between them, and multiply the sum by one third of the altitude. Or, Vol. = $0.2618a(b^2 + c^2 + bc)$; a =altitude; b =and c, diams, of the two bases.

Sphere.—To find the surface of a sphere: Multiply the diameter by the circumference of a great circle; or, multiply the square of the diameter by 8.14159.

Surface of sphere $= 4 \times$ area of its great circle.

= convex surface of its circumscribing cylinder.

Surfaces of spheres are to each other as the squares of their diameters. To find the volume of a sphere: Multiply the surface by one third of the radius; or, multiply the cube of the diameter by $\pi/6$; that is, by 0.5236. Value of $\pi/6$ to 10 decimal places = .5285987566.

The volume of a sphere = 2/3 the volume of its circumscribing cylinder.

Volumes of spheres are to each other as the cubes of their diameters. Spherical triangle.—To find the area of a spherical triangle: Compute the surface of the quadrantal triangle, or one eighth of the surface of the sphere. From the sum of the three angles subtract two right angles; divide the remainder by 90, and multiply the quotient by the area of the quadrantal triangle.

Spherical polygon.—To find the area of a spherical polygon; Commute the surface of the quadrantal triangle. From the sum of all the angles subtract the product of two right angles by the number of sides less two; divide the remainder by 90 and multiply the quotient by the area of the quadrantal triangle.

The prismoid.—The prismoid is a solid having parallel end areas, and may be composed of any combination of prisms, cylinders, wedges, pyramids, or cones or frustums of the same, whose bases and apices lie in the

end areas.

Inasmuch as cylinders and cones are but special forms of prisms and pyramids, and warped surface solids may be divided into elementary forms of them, and since frustums may also be subdivided into the elementary forms, it is sufficient to say that all prismoids may be decomposed into prisms, wedges, and pyramids. If a formula can be found whiches equally applicable to all of these forms, then it will apply to any combination of the subject of the subje them. Such a formula is called

The Prismoidal Formula.

Let A = area of the base of a prism, wedge, or pyramid; A_1 , A_2 , A_3 = the two end and the middle areas of a prismoid, or of any of its elementary solids;

h =altitude of the prismoid or elementary solid; V =its volume;

$$V = \frac{h}{6}(A_1 + 4A_m + A_2).$$

For a prism, A_1 , A_m and A_2 are equal, A_1 , $V = \frac{h}{a} \times 6A = hA$.

For a wedge with parallel ends, $A_2 = 0$, $A_3 = \frac{1}{2}A_1$; $V = \frac{h}{6}(A_1 + 2A_1) = \frac{hA}{2}$

For a cone or pyramid,
$$A_2 = 0$$
, $A_m = \frac{1}{4}A_1$; $V = \frac{h}{6}(A_1 + A_1) = \frac{hA}{8}$.

The prismoidal formula is a rigid formula for all prismoids. The only approximation involved in its use is in the assumption that the given solid may be generated by a right line moving over the boundaries of the end

The area of the middle section is never the mean of the two end areas if the prismoid contains any pyramids or coues among its elementary forms. When the three sections are similar in form the dimensions of the middle area are always the means of the corresponding end dimensions. This fact often enables the dimensions, and hence the area of the middle section, to be computed from the end areas.

Polyedrons.—A polyedron is a solid bounded by plane polygons. A regular polyedron is one whose sides are all equal regular polygons.

To find the surface of a regular polyedron.—Multiply the area of one of the faces by the number of faces; or, multiply the square of one of the edges by the surface of a similar solid whose edge is unity.

A TABLE OF THE REGULAR POLYEDRONS WHOSE EDGES ARE UNITY.

Names.	No. of Faces.	Surface.	Volume.
Tetraedron	4	1.7320508	0.1178518
Hexaedron	6	6.0000000	1.0000000
Octaedron	8	3.4641016	0.4714045
Dodecaedron	12	20.6457288	7.6631189
Icosaedron		8.6602540	2.1816950

To find the volume of a regular polyedron.—Multiply the surface by one third of the perpendicular let fall from the centre on one of

surface by one third of the perpendicular let islifted the center on one of the faces; or, multiply the cube of one of the edges by the solidity of a similar polyedron whose edge is unity.

Solid of revolution.—The volume of any solid of revolution is equal to the product of the area of its generating surface by the length of the path of the centre of gravity of that surface.

The convex surface of any solid of revolution is equal to the product of the perimeter of its generating surface by the length of path of its centre.

the perimeter of its generating surface by the length of path of its centre of gravity

Cylindrical ring.—Let d = outer diameter; d' = inner diameter; $\frac{1}{2}(d-d')=$ thickness = t; $\frac{1}{4}\pi t^2=$ sectional area; $\frac{1}{2}(d+d')=$ mean diameter = M; πt = circumference of section; πM = mean circumference of ring; surface = $\pi t \times \pi M$; = $\frac{1}{4}\pi^2 (d^2 - d'^2)$; = 9.86965 t M; = 2.46741 $(d^2 - d'^2)$;

volume =
$$\frac{1}{4}\pi t^2 M \pi$$
; = 2.46741 $t^2 M$.

Spherical zone .- Surface of a spherical zone or segment of a sphere = its altitude x the circumference of a great circle of the sphere. A great circle is one whose plane passes through the centre of the sphere. Folume of a sone of a sphere.—To the sum of the squares of the radii of the ends add one third of the square of the height; multiply the sum

by the height and by 1.5708. Spherical segment. - Volume of a spherical segment with one base. - Multiply half the height of the segment by the area of the base, and the cube of the height by .5236 and add the two products. Or, from three times the diameter of the sphere subtract twice the height of the segment; multiby the difference by the square of the height and by .5226. Or, to three times the square of the radius of the base of the segment add the square of the tradius of the base of the segment add the square of the segment add the square of the sembly the height and by .5236.

Spheroid or ellipsoid.—When the revolution of the spheroid is about

the transverse diameter it is prolate, and when about the conjugate it is

oblate.

Convex surface of a segment of a spheroid.—Square the diameters of the spheroid, and take the square root of half their sum; then, as the diameter from which the segment is cut is to this root so is the height of the segment to the proportionate height of the segment to the mean diameter. Multiply the product of the other diameter and 8,1416 by the proportionate

Convex surface of a frustum or zone of a spheroid.—Proceed as by previous rule for the surface of a segment, and obtain the proportionate height of the frustum. Multiply the product of the diameter parallel to the base of the frustum and 8.1416 by the proportionate height of the frustum.

Volume of a spheroid is equal to the product of the square of the revolving axis by the fixed axis and by 5236. The volume of a spheroid is two thirds

of that of the circumscribing cylinder.

Volume of a segment of a spheroid.—1. When the base is parallel to the revolving axis, multiply the difference between three times the fixed axis and twice the height of the segment, by the square of the height and by \$625. Multiply the product by the square of the revolving axis, and divide

by the square of the fixed axis.

2. When the base is perpendicular to the revolving axis, multiply the difference between three times the revolving axis and twice the height of the segment by the square of the height and by .5236. Multiply the product by the length of the fixed axis, and divide by the length of the

revolving axis.

Volume of the middle frustum of a spheroid.—1. When the ends are circular, or parallel to the revolving axis: To twice the square of the middle diameter add the square of the diameter of one end; multiply the sum by the length of the frustum and by .2618.

2. When the ends are elliptical, or perpendicular to the revolving axis:

To twice the product of the transverse and conjugate diameters of the middle section add the product of the transverse and conjugate diameters of one end; multiply the sum by the length of the frustum and by .2618.

Spindles.—Figures generated by the revolution of a plane area, when spincies.—Figures generated by the revolution of a plane area, when the curve is revolved about a chord perpendicular to its axis, or about its double ordinate. They are designated by the name of the arc or curve from which they are generated, as Circular, Elliptic, Parabolic, etc., etc. Convex surface of a circular spindle, zone, or segment of it—Rule: Multiply the length by the radius of the revolving arc; multiply this arc by the central distance, or distance between the centre of the spindle and centre

of the revolving arc; subtract this product from the former, double the remainder, and multiply it by 3.1416.

Volume of a circular spindle.—Multiply the central distance by half the

area of the revolving segment; subtract the product from one third of the

cube of half the length, and multiply the remainder by 12.5654.

Volume of frustum or zone of a circular spindle.—From the square of half the length of the whole spindle take one third of the square of half the length of, the frustum, and multiply the remainder by the said half length of the frustum; multiply the central distance by the revolving area which

or the framework in multiply tale central distance by the revolving area which generates the frustum; subtract this product from the former, and multiply the remainder by 6 2889.

Volume of a segment of a circular spindle.—Subtract the length of the segment from the half length of the spindle; double the remainder and ascertain the volume of a middle frustum of this length; subtract the

result from the volume of the whole spindle and halve the remainder.

Volume of a cycloidal spindle = five eighths of the volume of the circumscribing cylinder.—Multiply the product of the square of twice the diameter of the generating circle and 3.927 by its circumference, and divide this pro-

Parabolic conoid.-Volume of a parabolic conoid (generated by the revolution of a parabola on its axis).—Multiply the area of the base by half the height.

Or multiply the square of the diameter of the base by the height and by .3927.

Volume of a frustum of a parabolic conoid.—Multiply half the sum of the areas of the two ends by the height.

Volume of a parabolic spindle (generated by the revolution of a parabola on its base).—Multiply the square of the middle diameter by the length and by .4189.

The volume of a parabolic spindle is to that of a cylinder of the same

height and diameter as 8 to 15.

Volume of the middle frustum of a parabolic spindle.—Add together 8 times the square of the maximum diameter, 8 times the square of the end diameter, and 4 times the product of the diameters. Multiply the sum by the length of the frustum and by .05236.

This rule is applicable for calculating the content of casks of parabolic

form.

Casks.—To find the volume of a cask of any form.—Add together 39 times the square of the bung diameter, 25 times the square of the head diameter, and 26 times the product of the diameters. Multiply the sum by the length, and divide by 31,778 for the coutent in Imperial gallons, or by

26,470 for U. S. gallons.

This rule was framed by Dr. Hutton, on the supposition that the middle. third of the length of the cask was a frustum of a parabolic spindle, and

each outer third was a frustum of a cone.

To find the ullage of a cask, the quantity of liquor in it when it is not full. For a lying cask: Divide the number of wet or dry inches by the bung diameter in inches. If the quotient is less than 5, deduct from it one fourth part of what it wants of 5. If it exceeds 5, add to it one fourth part of the excess above 5. Multiply the remainder or the sum by the whole content of the cask. The product is the quantity of liquor in the cask, in gallons, when the dividend is wet inches; or the empty space, if dry inches.

2. For a standing cask. Divide the number of wet or dry inches by the length of the cask. If the quotient exceeds .5, add to it one tenth of its excess above .5; if less than .5, subtract from it one tenth of what it wants of .5. Multiply the sum or the remainder by the whole content of the cask. The product is the quantity of liquor in the cask, when the dividend is wet

inches; or the empty space, if dry inches.

Volume of cask (approximate) U. S. gallons = square of mean diam. x length in inches x .0034. Mean diam. = half the sum of the bung and

head diams.

Volume of an irregular solid .- Suppose it divided into parts, resembling prisms or other bodies measurable by preceding rules. Find the content of each part; the sum of the contents is the cubic contents of the solid.

The content of a small part is found nearly by multiplying half the sum

of the areas of each end by the perpendicular distance between them.

The contents of small irregular solids may sometimes be found by immersing them under water in a prismatic or cylindrical vessel, and observing the amount by which the level of the water descends when the solid is withdrawn. The sectional area of the vessel being multiplied by the descent of the level gives the cubic contents.

Or, weigh the solid in air and in water; the difference is the weight of

or, weigh the solid in air and in water; the difference is the weight of water it displaces. Divide the weight in pounds by 62.4 to obtain volume in cubic feet, or multiply it by 27.7 to obtain the volume in cubic inches. When the solid is very large and a great degree of accuracy is not requisite, measure its length, breadth, and depth in several efferent places, and take the mean of the measurement for each dimension, and multiply the three means together.

When the surface of the solid is very extensive it is better to divide it into triangles, to find the area of each triangle, and to multiply it by the mean depth of the triangle for the contents of each triangular portion; the

contents of the triangular sections are to be added together.

The mean depth of a triangular section is obtained by measuring the depth at each angle, adding together the three measurements, and taking one third of the sum.

PLANE TRIGONOMETRY.

Trigonometrical Functions.

Every triangle has six parts—three angles and three sides. When any three of these parts are given, provided one of them is a side, the other parts may be determined. By the solution of a triangle is meant the determined.

mination of the unknown parts of a triangle when certain parts are given.

The complement of an angle or are is what remains after subtracting the

angle or arc from 90°.

In general, if we represent any arc by A, its complement is $90^{\circ} - A$. Hence the complement of an arc that exceeds 90° is negative.

Since the two acute angles of a right-angled triangle are together equal to

Since the two acute angles of a right-angled triangle are together equal to a right angle, each of them is the complement of the other.

The supplement of an angle or are is what remains after subtracting the angle or are from 180°. If A is an are its supplement is 180° — A. The supplement of an are that exceeds 180° is negative.

The sum of the three angles of a triangle is equal to 180°. Either angle is the supplement of the other two. In a right-angled triangle, the right angle being equal to 90°, each of the acute angles is the complement of the other. In all right-angled triangles having the same acute angle, the sides have to each other the same ratio. These ratios have received special names, as follows:

If A is one of the acute angles, a the opposite side, b the adjacent side, and c the hypothenuse.

The sine of the angle A is the quotient of the opposite side divided by the hypothenuse. Sin. $A = \frac{a}{c}$

The tangent of the angle A is the quotient of the opposite side divided by the adjacent side. Tang. $A = \frac{\omega}{h}$

The secant of the angle A is the quotient of the hypothenuse divided by the adjacent side. Sec. $A = \tilde{h}$

The cosine, cotangent, and cosecant of an angle are respectively the sine, tangent, and secant of the complement of that angle. The

terms sine, cosine, etc., are called trigonometrical functions.

In a circle whose radius is unity, the sine of an arc, or of the angle at the centre measured by that arc, is the perpendicular let fall from one extrem-

ity of the arc upon the diameter passing through the other extremity.

The tangent of an arc is the line which touches the circle at one extremity of the arc, and is limited by the diameter (produced) passing through

the other extremity.

The secant of an arc is that part of the produced diameter which is intercepted between the centre and the tangent.

The versed sine of an arc is that part of the diameter intercepted between the extremity of the arc and the foot of the sine.

In a circle whose radius is not unity, the trigonometric functions of an arc will be equal to the lines here defined, divided by the radius of the circle. If I C A (Fig. 70) is an angle in the first quadrant, and C F = radius,

The sine of the angle
$$=\frac{FG}{\mathrm{Rad}}$$
. $\mathrm{Cos} = \frac{CG}{\mathrm{Rad}} = \frac{KF}{\mathrm{Rad}}$. Tang. $=\frac{IA}{\mathrm{Rad}}$. Secant $=\frac{CI}{\mathrm{Rad}}$. $\mathrm{Cot.} = \frac{DL}{\mathrm{Rad}}$. $\mathrm{Cosec.} = \frac{CL}{\mathrm{Rad}}$. $\mathrm{Versin.} = \frac{GA}{\mathrm{Rad}}$.

If radius is 1, then Rad. in the denominator is omitted, and sine = FG, etc.

The sine of an arc = half the chord of twice the

The sine of the supplement of the arc is the same Mine of arc RDF = FGas that of the arc itself. Sine of arc BDF = FG =an arc FA.

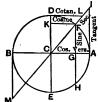


Fig. 70.

The tangent of the supplement is equal to the tangent of the arc, but with a contrary sign. Tang. BDF=BM.

The secant of the supplement is equal to the secant of the arc, but with a contrary sign. Sec. BDF=CM.

Signs of the functions in the four quadrants.—If we divide a circle into four quadrants by a vertical and a horizontal diameter, the upper right-hand quadrant is called the first, the upper left the second, the lower left the third, and the lower left the fourth. The signs of the functions in the four quadrants are as follows:

First quad. Second quad. Third quad. Fourth quad. Sine and cosecant, Cosine and secant, Tangent and cotangent,

The values of the functions are as follows for the angles specified:

	•	•	•	•	•		•	•	•	•	•
Angle	0	80	45		90	190	185	150	180	270	800
Sine	0	1/2	1/2	¥ 8 %	1	8 √ 8	1 1 7 2	1 8	0	1	0
Cosine	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0	$-\frac{1}{2}$	$-\frac{1}{\sqrt{2}}$	$-\frac{\sqrt{8}}{2}$	-1	0	1
Tangent	0	1/8	1	√ §	œ	- √ 3̄	-1	- 1/8	0	œ	0
Cotangent	8	1 * 3	1	1 1/8	0	$-\frac{1}{\sqrt{8}}$	-1	- 1/8	00	0	5
Secant	1	2 √3	₹ 2	2	8	- 2	- √ ∑		-1	~	1
Cosecant	œ	8	4₫	2 V 3	1	2/8	1/2	2	000	-1	80
Versed sine	0	$\frac{2-\sqrt{\tilde{3}}}{2}$	$\frac{\sqrt{2}-1}{\sqrt{2}}$	1 2	1	3 2	$\frac{\sqrt{2}+1}{\sqrt{2}}$	$\frac{2}{3+\sqrt{8}}$	2	1	0

TRIGONOMETRICAL FORMULE.

The following relations are deduced from the properties of similar triangles (Radius = 1):

cos
$$A$$
: sin A : 1: tan A , whence tan $A = \frac{\sin A}{\cos A}$;
sin A : cos A : 1: cot A , "cot an $A = \frac{\cos A}{\sin A}$;
cos A : 1 :: 1: sec A , "sec $A = \frac{1}{\cos A}$;
sin A : 1 :: 1: cosec A , "cosec $A = \frac{1}{\sin A}$;
tan A : 1 :: 1: cot A "tan $A = \frac{1}{\cot A}$."

The sum of the square of the sine of an arc and the square of its cosine equals unity. $\sin^2 A + \cos^2 A = 1$. Also, $1 + \tan^2 A = \sec^2 A$; $1 + \cot^2 A = \csc^2 A$. Functions of the sum and difference of two angles:

Let the two angles be denoted by A and B, their sum A + B = C, and their difference A - B by D.

$$\sin (A+B) = \sin A \cos B + \cos A \sin B; \quad \dots \quad (1)$$

$$\cos (A + B) = \cos A \cos B - \sin A \sin B;$$
 (2)
 $\sin (A - B) = \sin A \cos B - \cos A \sin B;$ (3)
 $\cos (A - B) = \cos A \cos B + \sin A \sin B.$ (4)

From these four formulæ by addition and subtraction we obtain

$$\sin (A+B) + \sin (A-B) = 2 \sin A \cos B;$$
 (5)
 $\sin (A+B) - \sin (A-B) = 2 \cos A \sin B;$ (6)
 $\cos (A+B) + \cos (A-B) = 2 \cos A \cos B;$ (7)

$$\cos(A - B) - \cos(A + B) = 2 \sin A \sin B$$
. (8)

If we put A + B = C, and A - B = D, then $A = \frac{1}{2}(C + D)$ and $B = \frac{1}{2}(C - D)$ D), and we have

$$\sin C + \sin D = 2 \sin \frac{1}{2}(C + D) \cos \frac{1}{2}(C - D); \qquad (9)$$

$$\sin C - \sin D = 2 \cos \frac{1}{2}(C + D) \sin \frac{1}{2}(C - D); \qquad (10)$$

$$\cos C + \cos D = 2 \cos \frac{1}{2}(C + D) \cos \frac{1}{2}(C - D); \qquad (11)$$

$$\cos D - \cos C = 2 \sin \frac{1}{2}(C + D) \sin \frac{1}{2}(C - D), \qquad (12)$$

Equation (9) may be enunciated thus: The sum of the sines of any two angles is equal to twice the sine of half the sum of the angles multiplied by the cosine of half their difference. These formulæ enable us to transform a sum or difference into a product.

The sum of the sines of two angles is to their difference as the tangent of half the sum of those angles is to the tangent of half their difference.

$$\frac{\sin A + \sin B}{\sin A - \sin B} = \frac{2 \sin \frac{1}{2}(A + B) \cos \frac{1}{2}(A - B)}{2 \cos \frac{1}{2}(A + B) \sin \frac{1}{2}(A - B)} = \frac{\tan \frac{1}{2}(A + B)}{\tan \frac{1}{2}(A - B)}.$$
 (18)

The sum of the cosines of two angles is to their difference as the cotangent of half the sum of those angles is to the tangent of half their difference.

$$\frac{\cos A + \cos B}{\cos B - \cos A} = \frac{2 \cos \frac{1}{2}(A + B) \cos \frac{1}{2}(A - B)}{2 \sin \frac{1}{2}(A + B) \sin \frac{1}{2}(A - B)} = \frac{\cot \frac{1}{2}(A + B)}{\tan \frac{1}{2}(A - B)}.$$
 (14)

The sine of the sum of two angles is to the sine of their difference as the mm of the tangents of those angles is to the difference of the tangents.

$$\frac{\sin (A+B)}{\sin (A-B)} = \frac{\tan A + \tan B}{\tan A - \tan B}; \quad \dots \quad (15)$$

$$\frac{\sin (A+B)}{\cos A \cos B} = \tan A + \tan B;$$

$$\frac{\sin (A-B)}{\cos A \cos B} = \tan A - \tan B;$$

$$\frac{\sin (A-B)}{\cos A \cos B} = \tan A - \tan B;$$

$$\frac{\cos (A+B)}{\cos A \cos B} = 1 - \tan A \tan B;$$

$$\cos (A-B) = \frac{\cot A \cot B}{\cot B + \cot A};$$

$$\cos (A-B) = \frac{\cot A \cot B - 1}{\cot B + \cot A};$$

$$\cos (A-B) = \frac{\cot A \cot B + 1}{\cot B - \cot A};$$

$$\tan (A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B};$$

$$\cot (A + B) = \frac{\cot A \cot B - 1}{\cot B + \cot A};$$

$$\cot (A - B) = \frac{\cot A \cot B + 1}{\cot B - \cot A}.$$

Functions of twice an angle:

$$\sin 2A = 2 \sin A \cos A;$$

$$\tan 2A = \frac{2 \tan A}{1 - \tan^2 A};$$

$$\cos 2A = \cos^2 A - \sin^2 A;$$
$$\cot 2A = \frac{\cot^2 A - 1}{2 \cot A}.$$

Functions of half an angle:

$$\sin \frac{1}{2}A = \pm \sqrt{\frac{1 - \cos A}{2}};$$
 $\tan \frac{1}{2}A = \pm \sqrt{\frac{1 - \cos A}{1 + \cos A}};$

$$\cos \frac{1}{6}A = \pm \sqrt{\frac{1 + \cos A}{2}};$$

$$\cot \frac{1}{6}A = \pm \sqrt{\frac{1 + \cos A}{1 - \cos A}}.$$

Solution of Plane Right-angled Triangles.

Let A and B be the two acute angles and C the right angle, and a, b, and c the sides opposite these angles, respectively, then we have

1.
$$\sin A = \cos B = \frac{a}{c}$$
; 8. $\tan A = \cot B = \frac{a}{b}$;
2. $\cos A = \sin B = \frac{b}{c}$; 4. $\cot A = \tan B = \frac{b}{a}$.

In any plane right-angled triangle the sine of either of the acute angles is equal to the quotient of the opposite leg divided by the hypothenuse.
 The cosine of either of the acute angles is equal to the quotient of the

adjacent leg divided by the hypothenuse.

3. The tangent of either of the acute angles is equal to the quotient of the

opposite leg divided by the adjacent leg.

4. The cotangent of either of the acute angles is equal to the quotient of the adjacent leg divided by the opposite leg.

5. The square of the hypothenuse equals the sum of the squares of the

other two sides.

Solution of Oblique-angled Triangles.

The following propositions are proved in works on plane trigonometry. In

any plane triangle—
Theorem 1. The sines of the angles are proportional to the opposite sides.
Theorem 2. The sum of any two sides is to their difference as the tangent of half the sum of the opposite angles is to the tangent of half their differ-

Theorem 3. If from any angle of a triangle a perpendicular be drawn to the opposite side or base, the whole base will be to the sum of the other two sides as the difference of those two sides is to the difference of the segments of the base.

CASE I. Given two angles and a side, to find the third angle and the other two sides. 1. The third angle = 180° – sum of the two angles. 2. The sides may be found by the following proportion:

The sine of the angle opposite the given side is to the sine of the angle opposite the required side as the given side is to the required side.

Case II. Given two sides and an angle opposite one of them, to find the

third side and the remaining angles.

The side opposite the given angle is to the side opposite the required angle as the sine of the given angle is to the mine of the required angle.

The third angle is found by subtracting the sum of the other two from 180°,

and the third side is found as in Case I. CASE III. Given two sides and the included angle, to find the third side and

The sum of the required angles is found by subtracting the given angle from 180°. The difference of the required angles is then found by Theorem II. Half the difference added to half the sum gives the greater angle, and half the difference subtracted from half the sum gives the less angle. The third side is then found by Theorem I.

Another method: Given the sides c, b, and the included angle A, to find the remaining side aand the remaining angles B and C.

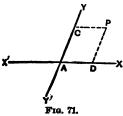
From either of the unknown angles, as B, draw a perpendicular B e to the opposite side. Then

$$Ae = c \cos A$$
, $Be = c \sin A$, $eC = b - Ae$, $Be + eC = \tan C$.

Or, in other words, solve Be, Ae and BeC as right-angled triangles. Case IV. Given the three sides, to find the angles. Let fall a perpendicular upon the longest side from the opposite angle, dividing the given triangle into two right-angled triangles. The two segments of the base may be found by Theorem III. There will then be given the hypothenuse and one side of a right-angled triangle to find the angles. For areas of triangles, see Mensuration.

ANALYTICAL GEOMETRY.

Analytical geometry is that branch of Mathematics which has for the object the determination of the forms and magnitudes of geometrical nagnitudes by means of analysis.



rdinates and abscissas.—In analytical geometry two intersecting lines YY', XX' are used as coördinate axes, XX' being the axis of abscissas or axis of X, and YY' the axis of ordinates or axis of Y. A, the intersection, is called the origin of coordinates. The distance of any point P from the axis of Y measured parallel to the axis of X is called the abscissa of the point, as AD or A is caused the doscused of the point, as AD or CP, Fig. 71. Its distance from the axis of X, measured parallel to the axis of Y, is called the ordinate, as AC or PD. The abscissa and ordinate taken together are called the coordinates of the point P. The angle of intersection is variable to the axis of the point P. tion is usually taken as a right angle, in which case the axes of X and Y are called rectangular coördinates.

The abscissa of a point is designated by the letter x and the ordinate by y. The equations of a point are the equations which express the distances of

the point from the axis. Thus x=a,y=b are the equations when express the distances of the point from the axis. Thus x=a,y=b are the equations of the point P. **Equations referred to rectangular coërdinates.**—The equation of a line expresses the relation which exists between the coördinates of every point of the line.

Equation of a straight line, $y = ax \pm b$, in which a is the tangent of the angle the line makes with the axis of X, and b the distance above A in which

the line cuts the axis of Y.

Every equation of the first degree between two variables is the equation of a straight line, as Ay + Bx + C = 0, which can be reduced to the form y = 0

Equation of the distance between two points:

$$D = \sqrt{(x'' - x')^2 + (y'' - y')^2},$$

in which x'y', x''y'' are the coördinates of the two points. Equation of a line passing through a given point:

$$y-y'=a(x-x'),$$

is which x'y' are the coördinates of the given point, a, the tangent of the agic the line makes with the axis of x, being undetermined, since any number of lines may be drawn through a given point.

Repation of a line passing through two given points:

$$y-y'=\frac{y''-y'}{x''-x'}(x-x').$$

Equation of a line parallel to a given line and through a given point:

$$y-y'=a(x-x').$$

Equation of an angle V included between two given lines:

$$\tan v = \frac{a'-a}{1+a'a},$$

is which a and a' are the tangents of the angles the lines make with the axis of abscissas.

If the lines are at right angles to each other tang $V = \infty$, and

$$1+a'a=0.$$

Equation of an intersection of two lines, whose equations are

$$y = ax + b$$
, and $y = a'x + b'$,
 $x = -\frac{b - b'}{a - a'}$, and $y = \frac{ab' - a'b}{a - a'}$.

Equation of a perpendicular from a given point to a given line:

$$y-y'=-\frac{1}{a}(x-x').$$

Equation of the length of the perpendicular P:

$$P=\frac{y'-ax'-b}{\sqrt{1+a^2}}.$$

The circle.—Equation of a circle, the origin of coordinates being at the centre, and radius = R:

$$x^2+y^2=R^2.$$

If the origin is at the left extremity of the diameter, on the axis of X:

$$y^2 = 2Rx - x^2.$$

If the origin is at any point, and the coordinates of the centre are x'y':

$$(x-x')^2+(y-y')^2=R^2$$

Equation of a tangent to a circle, the coordinates of the point of tangency being a"y" and the origin at the centre,

$$yy'' + xx'' = R^2.$$

The ellipse.-Equation of an ellipse, referred to rectangular coordinates with axis at the centre:

$$A^3y^2+B^2x^3=A^2B^3,$$

in which A is half the transverse axis and B half the conjugate axis.

Equation of the ellipse when the origin is at the vertex of the transverse axis:

$$y^2 = \frac{B_1^2}{A_2^2}(2Ax - x^2).$$

The eccentricity of an ellipse is the distance from the centre to either focus, divided by the semi-transverse axis, or

$$e=\frac{\sqrt{A^2-B^2}}{A}.$$

The parameter of an ellipse is the double ordinate passing through the focus. It is a third proportional to the transverse axis and its conjugate, or

$$2A:2B::2B:$$
 parameter; or parameter = $\frac{2B^2}{4}$.

Any ordinate of a circle circumscribing an ellipse is to the corresponding ordinate of the ellipse as the semi-transverse axis to the semi-conjugate. Any ordinate of a circle inscribed in an ellipse is to the corresponding ordinate of the ellipse as the semi-conjugate axis to the semi-transverse. Equation of the tangent to an ellipse, origin of axes at the centre:

$$A^2yy^{\prime\prime}+B^2xx^{\prime\prime}=A^2B^2,$$

y''x'' being the coordinates of the point of tangency. Equation of the normal, passing through the point of tangency, and perpendicular to the tangent:

$$y - y'' = \frac{A^2y''}{B^2x''}(x - x'').$$

The normal bisects the angle of the two lines drawn from the point of tangency to the foci.

The lines drawn from the foci make equal angles with the tangent.

The parabola.—Equation of the parabola referred to rectangular coordinates, the origin being at the vertex of its axis, $y^2 = 2px$, in which 2pis the parameter or double ordinate through the focus.

The parameter is a third proportional to any abscissa and its corresponding ardinate, or a; y:: y: 2p.

Equation of the tangent:

$$yy''=p(x+x''),$$

y'x' being coordinates of the point of tangency. Equation of the normal:

$$y-y^{\prime\prime}=-\frac{\dot{y}^{\prime\prime}}{p}(x-x^{\prime\prime}).$$

The sub-normal, or projection of the normal on the axis, is constant, and

equal to half the parameter.

The tangent at any point makes equal angles with the axis and with the line drawn from the point of tangency to the focus.

The layperbola.—Equation of the hyperbola referred to rectangular

coordinates, origin at the centre:

$$A^{0}y^{0}-B^{0}x^{0}=-A^{0}B^{0},$$

in which \mathcal{A} is the semi-transverse axis and B the semi-conjugate axis. Equation when the origin is at the right vertex of the transverse axis:

$$y^2 = \frac{B^2}{A^2}(2Ax + x^2).$$

Conjugate and equilateral hyperbolas,-If on the conjugate axis, as a transverse, and a focal distance equal to $\sqrt{A^2 + B^2}$, we construct the two branches of a hyperbola, the two hyperbolas thus constructed are called conjugate hyperbolas. If the transverse and conjugate axes are equal, the hyperbolas are called equilateral, in which case $y^q - x^q = -A^2$ when A is the transverse axis, and $x^q - y^q = -B^2$ when B is the transverse axis.

The parameter of the transverse axis is a third proportional to the transverse axis and its conjugate.

The tangent to a hyperbola bisects the angle of the two lines drawn from the point of tangency to the foci.

The asymptotes of a layperbola are the diagonals of the rectangle described on the axes, indefinitely produced in both directions.

In an equilateral hyperbola the asymptotes make equal angles with the

transverse axis, and are at right angles to each other.

The asymptotes continually approach the hyperbola, and become tangent

to it at an infinite distance from the centre.

Conic sections,—Every equation of the second degree between two variables will represent either a direla, an ellipse, a parabola or a hyperbola.

These curves are those which are obtained by intersecting the surface of a

These curves are those which are obtained by intersecting the surface of a cone by planes, and for this reason they are called conic sections.

Logarithmic curve.—A logarithmic curve is one in which one of the coordinates of any point is the logarithm of the other.

The coordinate axis to which the lines denoting the logarithms are parallel is called the axis of logarithms, and the other the axis of numbers, if y is the axis of logarithms and x the axis of numbers, the equation of the curve

is $y = \log x$. If the base of a system of logarithms is a, we have $a^y = x$, in which y is the

logarithm of x.

Each system of logarithms will give a different logarithmic curve. If y =0.x = 1. Hence every logarithmic curve will intersect the axis of numbers at a distance from the origin equal to 1.

DIFFERENTIAL CALCULUS.

The differential of a variable quantity is the difference between any two of its consecutive values; hence it is indefinitely small. It is expressed by writing d before the quantity, as dx, which is read differential of x.

The term $\frac{dy}{dx}$ is called the differential coefficient of y regarded as a function of x.

The differential of a function is equal to its differential coefficient multiplied by the differential of the independent variable; thus, $\frac{dy}{dx} = dy$.

The limit of a variable quantity is that value to which it continually approaches, so as at last to differ from it by less than any assignable quan-

tity. The differential coefficient is the limit of the ratio of the increment of the

independent variable to the increment of the function. The differential of a constant quantity is equal to 0.

The differential of a product of a constant by a variable is equal to the constant multiplied by the differential of the variable.

If
$$u = Av$$
, $du = Adv$.

In any curve whose equation is y = f(x), the differential coefficient $= \tan a$; hence, the rate of increase of the function, or the ascension of the curve at any point, is equal to the tangent of the angle which the tangent line makes with the axis of abscissas.

All the operations of the Differential Calculus comprise but two objects: 1. To find the rate of change in a function when it passes from one state of value to another, consecutive with it.

2. To find the actual change in the function: The rate of change is the

differential coefficient, and the actual change the differential.

Differentials of algebraic functions.—The differential of the sum or difference of any number of functions, dependent on the same variable, is equal to the sum or difference of their differentials taken separately:

If
$$u = y + z - w$$
, $du = dy + dz - dw$.

The differential of a product of two functions dependent on the same variable is equal to the sum of the products of each by the differential of the other:

$$d(uv) = vdu + udv.$$
 $\frac{d(uv)}{uv} = \frac{du}{u} + \frac{dv}{v}.$

The differential of the product of any number of functions is equal to the sum of the products which arise by multiplying the differential of each function by the product of all the others:

$$d(uts) = tsdu + usdt + utds$$
.

The differential of a fraction equals the denominator into the differential of the numerator minus the numerator into the differential of the denominator, divided by the square of the denominator:

$$dt = d\left(\frac{u}{v}\right) = \frac{vdu - udv}{v^2}.$$

If the denominator is constant, dv = 0, and $dt = \frac{vdu}{dt} = \frac{du}{dt}$.

If the numerator is constant, du = 0, and $dt = -\frac{udv}{v^2}$

The differential of the square root of a quantity is equal to the differential of the quantity divided by twice the square root of the quantity:

If
$$v = u^{\frac{1}{2}}$$
, or $v = \sqrt{u}$, $dv = \frac{du}{2\sqrt{u}}$; $= \frac{1}{2}u^{-\frac{1}{2}}du$.

The differential of any power of a function is equal to the exponent multiplied by the function raised to a power less one, multiplied by the differential of the function, $d(u^n) = nu^{n-1}du$.

Formulas for differentiating algebraic functions.

1.
$$d(a) = 0$$
.
2. $d(ax) = adx$.
3. $d(x + y) = dx + dy$.
4. $d(x - y) = dx - dy$.
5. $d(xy) = xdy + ydx$.
6. $d\left(\frac{x}{y}\right) = \frac{ydx - xdy}{y^2}$.
7. $d(x^m) = mx^{m-1}dx$.
8. $d(\sqrt{x}) = \frac{dx}{2\sqrt{x}}$.
9. $d\left(\frac{r}{x}\right) = -\frac{r}{s}x^{-\frac{r}{s}-1}dx$.

To find the differential of the form $u=(a+bx^n)^m$: Multiply the exponent of the parenthesis into the exponent of the variable within the parenthesis, into the coefficient of the variable, into the binomial raised to a power less 1, into the variable within the parenthesis raised to a power less 1, into the differential of the variable.

$$du = d(a + bx^n)^m = mnb(a + bx^n)^{m-1}x^{m-1}dx.$$

To find the rate of change for a given value of the variable:
Find the differential coefficient, and substitute the value of the variable in the second member of the equation.

EXAMPLE.—If x is the side of a cube and u its volume, $u = x^2$, $\frac{du}{dx} = 8x^2$.

Hence the rate of change in the volume is three times the square of the edge. If the edge is denoted by 1, the rate of change is 3.

Application. The coefficient of expansion by heat of the volume of a body is three times the linear coefficient of expansion. Thus if the side of a cube expands. 001 inch, its volume expands. 003 cubic inch. 1.001² = 1.003003001.

A partial differential coefficient of a function of two or more variables under the supposition that only one of

them has changed its value.

A partial differential is the differential of a function of two or more variables under the supposition that only one of them has changed its value.

The total differential of a function of any number of variables is equal to

the sum of the partial differentials.

If
$$u = f(xy)$$
, the partial differentials are $\frac{du}{dx}dx$, $\frac{du}{dy}dy$.
If $u = x^2 + y^2 - z$, $du = \frac{du}{dx}dx + \frac{du}{dy}dy + \frac{du}{dz}dz$; $= 2xdx + 3y^2dy - dz$.

Integrals.—An integral is a functional expression derived from a differential. Integration is the operation of finding the primitive function from the differential function. It is indicated by the sign f, which is read "the integral of." Thus $\int 2x dx = x^2$; read, the integral of 2x dx equals x^2 . To integrate an expression of the form $mx^{m-1}dx$ or $x^m dx$, add 1 to the exponent of the variable, and divide by the new exponent and by the differential of the variable: $\int 3x^2 dx = x^2$. (Applicable in all cases except when m = -1. For $\int x^{-1} dx$ see formula 2 page 78.)

The integral of the product of a constant by the differential of a variable is equal to the constant multiplied by the integral of the differential:

$$\int ax^{m}dx = a\int x^{m}dx = a\frac{1}{m+1}x^{m+1}.$$

The integral of the algebraic sum of any number of differentials is equal to the algebraic sum of their integrals:

$$du = 2ax^{2}dx - bydy - z^{2}dz; \quad fdu = \frac{2}{3}ax^{3} - \frac{b}{2}y^{2} - \frac{z^{3}}{3}.$$

Since the differential of a constant is 0, a constant connected with a varishie by the sign + or - disappears in the differentiation; thus $d(a+x^m)$ = $dx^m = mx^{m-1}dx$. Hence in integrating a differential expression we?

annex to the integral obtained a constant represented by G to compensate for the term which may have been lost in differentiation. Thus if we have dy = adx; fdy = afdx. Integrating,

$$y = ax \pm C$$
.

The constant C, which is added to the first integral, must have such a value as to render the functional equation true for every possible value that may be attributed to the variable. Hence, after having found the first integral equation and added the constant C, if we then make the variable equal to zero, the value which the function assumes will be the true value

An indefinite integral is the first integral obtained before the value of the

constant C is determined.

A particular integral is the integral after the value of C has been found. A definite integral is the integral corresponding to a given value of the

Integration between limits.—Having found the indefinite integral and the particular integral, the next step is to find the definite integral, and then the definite integral between given limits of the variable.

The integral of a function, taken between two limits, indicated by given

values of x, is equal to the difference of the definite integrals corresponding to those limits. The expression

1

$$\int_{x'}^{x''} dy = a \int dx$$

is read: Integral of the differential of y, taken between the limits x' and x'': the least limit, or the limit corresponding to the subtractive integral, being placed below.

Integrate $du = 9x^3dx$ between the limits x = 1 and x = 3, u being equal to 81 when x = 0. $fdu = f9x^3dx = 8x^3 + C$; C = 81 when x = 0, then

$$\int_{x=1}^{x=8} du = 8(3)^3 + 81, \text{ minus } 8(1)^3 + 81 = 78,$$

Integration of particular forms.

To integrate a differential of the form $du = (a + bx^n)^m x^{n-1} dx$.

1. If there is a constant factor, place it without the sign of the integral and omit the power of the variable without the parenthesis and the differ.

2. Augment the exponent of the parenthesis by 1, and then divide this quantity, with the exponent so increased, by the exponent of the parenthesis, into the exponent of the variable within the parenthesis, into the coefficient of the variable. Whence

$$\int du = \frac{(a+bx^n)^{m+1}}{(m+1)nb} = C.$$

The differential of an arc is the hypothenuse of a right-angle triangle of which the base is dx and the perpendicular dy.

If z is an arc,
$$dz = \sqrt{dx^2 + dy^2}$$
 $z = \int \sqrt{dx^2 + dy^2}$.

Quadrature of a plane figure.

The differential of the area of a plane surface is equal to the ordinate into the differential of the abscissa.

$$ds = ydx$$
.

To apply the principle enunciated in the last equation, in finding the area

of any particular plane surface: Find the value of y in terms of x, from the equation of the bounding line; substitute this value in the differential equation, and then integrate between the required limits of x.

Area of the parabola. Find the area of any portion of the common parabola whose equation is

Substituting this value of y in the differential equation ds = ydx gives

$$\int ds = \int \sqrt{2px} dx = \sqrt{2p} \int x^{\frac{1}{2}} dx = \frac{2\sqrt{2p}}{8} x^{\frac{3}{2}} + C;$$
or, $s = \frac{2\sqrt{2px}}{3} \times x = \frac{2}{3} xy + C.$

If we estimate the area from the principal vertex, x = 0, y = 0, and C = 0; and denoting the particular integral by s', $s' = \frac{2}{4}sy$.

That is, the area of any portion of the parabola, estimated from the vertex, is equal to % of the rectangle of the abscissa and ordinate of the extreme point. The curve is therefore quadrable.

Quadrature of surfaces of revolution. —The differential of a surface of revolution is equal to the circumference of a circle perpendicular to the axis into the differential of the arc of the meridian curve.

$$ds = 2\pi y \sqrt{dx^2 + dy^2};$$

in which y is the radius of a circle of the bounding surface in a plane perpendicular to the axis of revolution, and x is the abscissa, or distance of the

plane from the origin of coördinate axes.

Therefore, to find the volume of any surface of revolution:

Find the value of y and dy from the equation of the meridian curve in terms of x and dx, then substitute these values in the differential equation, and integrate between the proper limits of x.

By application of this rule we may find:

The curved surface of a cylinder equals the product of the circumference of the base into the altitude.

The convex surface of a cone equals the product of the circumference of the base into half the slant height.

The surface of a sphere is equal to the area of four great circles, or equal to the curved surface of the circumscribing cylinder,

Cubature of volumes of revolution.—A volume of revolution is a volume generated by the revolution of a plane figure about a fixed line called the axis.

If we denote the volume by V, $dV = \pi y^2 dx$. The area of a circle described by any ordinate y is πy^2 ; hence the differential of a volume of revolution is equal to the area of a circle perpendicular to the axis into the differential of the axis.

The differential of a volume generated by the revolution of a plane figure about the axis of Y is $\pi x^2 dy$.

To find the value of V for any given volume of revolution:

Find the value of y^2 in terms of x from the equation of the meridian curve, substitute this value in the differential equation, and then integrate between the required limits of x.

By application of this rule we may find:

The volume of a cylinder is equal to the area of the base multiplied by the altitude.

The volume of a cone is equal to the area of the base into one third the skitudo.

The volume of a prolate spheroid and of an oblate spheroid (formed by the revolution of an ellipse around its transverse and its conjugate axis respectively) are each equal to two thirds of the circumscribing cylinder.

If the axes are equal, the spheroid becomes a sphere and its volume = $_{1}^{*}R^{2} \times D = \frac{1}{6}\pi D^{3}$; R being radius and D diameter.

The volume of a paraboloid is equal to half the cylinder having the same base and altitude.

The volume of a pyramid equals the area of the base multiplied by one third the altitude.

Second, third, etc., differentials.—The differential coefficient being a function of the independent variable, it may be differentiated, and we thus obtain the second differential coefficient:

 $d\left(\frac{du}{dx}\right) = \frac{d^2u}{dx}$. Dividing by dx, we have for the second differential coefficients

cient $\frac{d^2u}{dx^2}$, which is read: second differential of u divided by the square of

the differential of x (or dx squared). The third differential coefficient $\frac{d^2u}{dx^3}$ is read; third differential of u divided by dx cubed.

The differentials of the different orders are obtained by multiplying the differential coefficients by the corresponding powers of dx; thus $\frac{d^3u}{dx^3} = \frac{d^3u}{dx^3}$ third differential of u.

Sign of the first differential coefficient.—If we have a curve whose equation is y = fx, referred to rectangular coördinates, the curve will recede from the axis of X when $\frac{dy}{dx}$ is positive, and approach the axis when it is negative, when the curve lies within the first angle of the coordinate axes. For all angles and every relation of y and x the curve will recede from the axis of X when the ordinate and first differential coefficient have the same sign, and approach it when they have different signs. If the tangent of the curve becomes parallel to the axis of X at any point $\frac{dy}{dx} = 0$. If the tangent becomes perpendicular to the axis of X at any

Sign of the second differential coefficient. - The second differential coefficient has the same sign as the ordinate when the curve is

convex toward the axis of abscissa and a contrary sign when it is concave. **Maclaurin's Theorem.**—For developing into a series any function of a single variable as $u = A + Bx + Cx^2 + Dx^3 + Ex^4$, etc., in which A, B, C, etc., are independent of x:

$$u = (u)_{x=0} + \left(\frac{du}{dx}\right)_{x=0} x + \frac{1}{1 \cdot 2} \left(\frac{d^2u}{dx^2}\right)_{x=0} x^2 + \frac{1}{1 \cdot 2 \cdot 3} \left(\frac{d^2u}{dx^2}\right)_{x=0} x^3 + \text{etc.}$$

In applying the formula, omit the expressions x = 0, although the coefficients are always found under this hypothesis.

$$(a+x)^m = a^m + ma^{m-1}x + \frac{m}{1} \frac{(m-1)}{2} a^{m-2}x^2 + \frac{m}{1} \frac{(m-1)}{2} \frac{(m-2)}{8} a^{m-3}x^3 + \text{etc.}$$

$$\frac{1}{a+x} = \frac{1}{a} - \frac{x}{a^2} + \frac{x^3}{a^3} - \frac{x^3}{a^4} + \dots + \frac{x^n}{a^{n+1}}, \text{ etc.}$$

Taylor's Theorem.—For developing into a series any function of the sum or difference of two independent variables, as $u' = f(x \pm y)$:

$$u' = u + \frac{du}{dx}y + \frac{d^2u}{dx^2} \frac{y^2}{1 \cdot 2} + \frac{d^3u}{dx^3} \frac{y^3}{1 \cdot 2 \cdot 3} + \text{etc.},$$

in which u is what u' becomes when y=0, $\frac{du}{dx}$ is what $\frac{du'}{dx}$ becomes when y = 0, etc.

Maxima and minima.—To find the maximum or minimum value of a function of a single variable:

1. Find the first differential coefficient of the function, place it equal to 0,

and determine the roots of the equation.

2. Find the second differential coefficient, and substitute each real root, in succession, for the variable in the second member of the equation. root which gives a negative result will correspond to a maximum value of the function, and each which gives a positive result will correspond to a minimum value.

Example.—To find the value of x which will render the function y a maximum or minimum in the equation of the circle, $y^2 + x^2 = R^2$;

$$\frac{dy}{dx} = -\frac{x}{y}; \text{ making } -\frac{x}{y} = 0 \text{ gives } x = 0.$$

The second differential coefficient is: $\frac{d^2y}{dm^2} = -\frac{x^2 + y^2}{m^2}$.

When x = 0, y = R; hence $\frac{d^2y}{dx^2} = -\frac{1}{R}$, which being negative, y is a maximum for R positive.

in applying the rule to practical examples we first find an expression for the function which is to be made a maximum or minimum.

2. If in such expression a constant quantity is found as a factor, it may be omitted in the operation; for the product will be a maximum or a mini-mum when the variable factor is a maximum or a minimum.

3. Any value of the independent variable which renders a function a maximum or a minimum will render any power or root of that function a maximum or minimum; hence we may square both members of an equition to free it of radicale before differentiating.

By these rules we may find:

The maximum rectangle which can be inscribed in a triangle is one whose altitude is half the altitude of the triangle.

The altitude of the maximum cylinder which can be inscribed in a cone is one third the altitude of the cone.

The surface of a cylindrical vessel of a given volume, open at the top, is a minimum when the altitude equals half the diameter. The altitude of a cylinder inscribed in a sphere when its convex surface is

a maximum is $r \sqrt[4]{2}$. r = radius.

The altitude of a cylinder inscribed in a sphere when the volume is a maximum is $2r + \sqrt{8}$. (For maxima and minima without the calculus see Appendix, p. 1070.)

Differential of an exponential function.

If
$$u = a^x$$
. (1)

in which k is a constant dependent on a.

The relation between a and k is $a^k = e$; whence $a = e^k$. in which e=2.7182818... the base of the Naperian system of logarithms. **Logarithms.**—The logarithms in the Naperian system are denoted by l, Nap. log or hyperbolic log, hyp. log, or \log_e ; and in the common system always by \log_e .

$$k = \text{Nap. log } a, \log a = k \log e.$$
 (4)

The common logarithm of $e_1 = \log 2.7182818 \dots = .4342945 \dots$, is called the modulus of the common system, and is denoted by M. Hence, if we have the Naperian logarithm of a number we can find the common logarithm of the same number by multiplying by the modulus. Reciprocally, Nap. $\log = \text{com. log} \times 2.3025851$. If in equation (4) we make a = 10, we have

$$1 = k \log e$$
, or $\frac{1}{k} = \log e = M$.

That is, the modulus of the common system is equal to 1, divided by the Naperian logarithm of the common base.

From equation (2) we have

$$\frac{du}{u} = \frac{da^x}{a^x} = kdx.$$

If we make a = 10, the base of the common system, $x = \log u$, and

$$d(\log u) = dx = \frac{du}{u} \times \frac{1}{k} = \frac{du}{u} \times M.$$

That is, the differential of a common logarithm of a quantity is equal to the differential of the quantity divided by the quantity, into the modulus. If we make a = e, the base of the Naperian system, x becomes the Naperian system,

10.

rian logarithm of u, and k becomes 1 (see equation (3)); hence M = 1, and

$$d(\text{Nap. log }\mathbf{u}) = dx = \frac{d\mathbf{u}}{a^x}; = \frac{d\mathbf{u}}{u}.$$

That is, the differential of a Naperian logarithm of a quantity is equal to the differential of the quantity divided by the quantity; and in the Naperian system the modulus is 1.

Since k is the Naperian logarithm of a, $du = a^x \cdot l \cdot a \cdot dx$. That is, the

differential of a function of the form a^x is equal to the function, into the Naperian logarithm of the base a, into the differential of the exponent. If we have a differential in a fractional form, in which the numerator is the differential of the denominator, the integral is the Naperian logarithm of the denominator. Integrals of fractional differentials of other forms are circumbelow: given helow:

Differential forms which have known integrals; ex-

1.
$$\int a^{x} l a dx = a^{x} + C;$$
2.
$$\int^{2} \frac{dx}{x} = \int^{2} dx \, x^{-1} = lx + C;$$
3.
$$\int^{2} (xy^{x-1}dy + y^{x} ly \times dx) = y^{x} + C;$$
4.
$$\int^{2} \frac{dx}{\sqrt{x^{2} \pm a^{3}}} = l(x + \sqrt{x^{2} \pm a^{3}}) + C;$$
5.
$$\int \frac{dx}{\sqrt{x^{2} \pm 2ax}} = l(x \pm a + \sqrt{x^{2} \pm 2ax}) + C;$$
6.
$$\int^{2} \frac{2adx}{a^{2} - x^{2}} = l(\frac{a + x}{a - x}) + C;$$
7.
$$\int^{2} \frac{2adx}{x^{3} - a^{3}} = l(\frac{x - a}{x + a}) + C;$$
8.
$$\int^{2} \frac{2adx}{x\sqrt{a^{2} + x^{2}}} = l(\frac{\sqrt{a^{3} + x^{2}} - a}{\sqrt{a^{2} + x^{2}} + a}) + C;$$
9.
$$\int^{2} \frac{2adx}{x\sqrt{a^{2} - x^{2}}} = l(\frac{a - \sqrt{a^{2} - x^{2}}}{a + \sqrt{a^{2} - x^{2}}}) + C;$$

Circular functions. - Let z denote an arc in the first quadrant, y its sine, x its cosine, v its versed sine, and t its tangent; and the following notation be employed to designate an arc by any one of its functions, viz.,

 $\int \frac{x^{-2} dx}{\sqrt{1 + a^2 x^2}} = -l \left(\frac{1 + \sqrt{1 + a^2 x^2}}{x} \right) + C.$

$$\sin^{-1} y$$
 denotes an arc of which y is the sine $\cos^{-1} x$ " " " x is the cosine, $\tan^{-1} t$ " " t is the tangent

seed "are whose sine is y," etc.),—we have the following differential forms which have known integrals (r = radius):

$$\int_{0}^{\infty} \cos z \, ds = \sin z + C;$$

$$\int_{0}^{\infty} -\sin z \, ds = \cos s + C;$$

$$\int_{0}^{\infty} \frac{dy}{\sqrt{1 - y^{2}}} = \sin^{-1} y + C;$$

$$\int_{0}^{\infty} \frac{dy}{\sqrt{1 - x^{2}}} = \cos^{-1} x + C;$$

$$\int_{0}^{\infty} \frac{dy}{\sqrt{2v - v^{2}}} = \cos^{-1} x + C;$$

$$\int_{0}^{\infty} \frac{dy}{\sqrt{2v - v^{2}}} = \operatorname{ver-sin}^{-1} v + C;$$

$$\int_{0}^{\infty} \frac{dy}{\sqrt{2v - v^{2}}} = \operatorname{ver-sin}^{-1} v + C;$$

$$\int_{0}^{\infty} \frac{dy}{\sqrt{x^{2} - u^{2}}} = \operatorname{ver-sin}^{-1} v + C;$$

$$\int_{0}^{\infty} \frac{dy}{\sqrt{x^{2} - u^{2}}} = \operatorname{ver-sin}^{-1} v + C;$$

$$\int_{0}^{\infty} \frac{dy}{\sqrt{x^{2} - u^{2}}} = \operatorname{cos}^{-1} \frac{u}{a} + C;$$

$$\int_{0}^{\infty} \frac{dy}{\sqrt{x^{2} - u^{2}}} = \operatorname{cos}^{-1} \frac{u}{a} + C;$$

$$\int_{0}^{\infty} \frac{dy}{\sqrt{x^{2} - u^{2}}} = \operatorname{cos}^{-1} \frac{u}{a} + C;$$

$$\int_{0}^{\infty} \frac{dy}{\sqrt{x^{2} - u^{2}}} = \operatorname{cos}^{-1} \frac{u}{a} + C;$$

$$\int_{0}^{\infty} \frac{dy}{\sqrt{x^{2} - u^{2}}} = \operatorname{cos}^{-1} \frac{u}{a} + C;$$

$$\int_{0}^{\infty} \frac{dy}{\sqrt{x^{2} - u^{2}}} = \operatorname{cos}^{-1} \frac{u}{a} + C;$$

$$\int_{0}^{\infty} \frac{du}{\sqrt{x^{2} - u^{2}}} = \operatorname{ver-sin}^{-1} \frac{u}{a} + C;$$

$$\int_{0}^{\infty} \frac{du}{\sqrt{x^{2} - u^{2}}} = \operatorname{ver-sin}^{-1} \frac{u}{a} + C;$$

$$\int_{0}^{\infty} \frac{du}{\sqrt{x^{2} - u^{2}}} = \operatorname{ver-sin}^{-1} \frac{u}{a} + C;$$

$$\int_{0}^{\infty} \frac{du}{\sqrt{x^{2} - u^{2}}} = \operatorname{ver-sin}^{-1} \frac{u}{a} + C;$$

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$$\int_{0}^{\infty} \frac{du}{\sqrt{x^{2} - u^{2}}} = \operatorname{ver-sin}^{-1} \frac{u}{a} + C;$$

The cycleid.—If a circle be rolled along a straight line, any point of the circumference, as P, will describe a curve which is called a cycloid. The circle is called the generating circle, and P the generating point.

The transcendental equation of the cycloid is

$$x = \text{ver-sin} - 1 \frac{y}{r} - \sqrt{2ry - y^2},$$
 and the differential equation is $dx = \frac{ydx}{\sqrt{2ry - y^2}}.$

The area of the cycloid is equal to three times the area of the generating

circle.

The surface described by the arc of a cycloid when revolved about its base is equal to 64 thirds of the generating circle.

The volume of the solid generated by revolving a cycloid about its base is equal to five eighths of the droumscribing cylinder.

Integral calculus.—In the integral calculus we have to return from the differential to the function from which it was derived. A number of differential expressions are given above, each of which has a known in-tegral corresponding to it, and which being differentiated, will produce the given differential.

in all classes of functions any differential expression may be integrated when it is reduced to one of the known forms; and the operations of the integral calculus consist mainly in making such transformations of given differential expressions as shall reduce them to equivalent ones whose in-

grais are known.
For methods of making these transformations reference must be made to

the text-books on differential and integral calculus.

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3	.00309597	8	.00257732	3	.00220751	18	.00193424	3	
4	.00308642	9	.00257069	4	.00220264	19	.00192678	4	.00171527
5		390	.00256410	5	.00219780	520	.00192308	5	.00170940
6	.00306748	1	.00255754	6	.00219298	1	.00191939	6	.00170648
7 8	.00305810	2	.00255102	7	.00218818	2	.00191571	7	.00170358
8	.00304878	3	.00254453	8	.00218341	3	.00191205	8	.00170068
330	.00303951	5	.00253807	9	.00217865	4	.00190840	9	.00169779
1	.00303030	6	.00253165	460	.00217391	5	.00190476	590	.00169491
2	.00301205	7	.00251889	2	.00216920	6	.00190114	1 2	.00169205
3	.00300300	8	.00251256	3	.00215983	8	.00189394	3	.00168919
4	.00299401	9	.00250627	4	.00215517	9	.00189036	4	.00168350
5	.00298507	400	.00250000	5	.00215054	530	.00188679	5	.00168067
6		1	.00249377	6	.00214592	1	.00188324	6	.00167785
7	.00296736	2	.00248756	7	.00214133	2	.00187970	7	.00167504
8	.00295858	3	.00248139	8	.00213675	3	.00187617	8	.00167224
340	.00294985	4	.00247525	9	.00213220	4	.00187266	9	.00166945
1	.00293255	5 6	.00246914	470	.00212766	5	.00186916	600	.00166667
2	00292398	7	.00245700	2	.00212314	6	.00186567	1 2	.00166389
3	.00291545	8	.00245098	3	.00211416	8	.00186220	3	.00166118
4	.00290698	9	.00244499	4	.00210970	9	.00185528	4	.00165568
-5	.00289855	410	.00243902	5	.00210526	540	.00185185	5	.00165289
6	.00289017	11	.00243309	.6	.00210084	1	.00184843	6	.00165016
7	.00288184	12	.00242718	8	.00209644	2	.00184502	7	.00164745
8	.00287356	13	.00242131		.00209205	3	.00184162	8	.00164474
350	.00286533	14	.00241546	100	.00208768	4	.00183823	9	.00164204
300	.00284900	15 16	.00240964	480	.00208333	5	.00183486	610	.00163934
2	.00284091	17	.00239808	2	.00207469	7	.00183150	11 12	.00163666
3	.00283286	18	.00239234	3	.00207039	8	.00182482	13	.00163139
4	.00282486	19	.00238663	4	.00206612	9	.00182149	14	.00162866
5	.00281690	420	.00238095	5	.00206186	550	.00181818	15	.00162602
6	,00280899	1	.00237530	6	.00205761	1	.00181488	16	.00162338
00	.00280112	2	.00236967	7	.00205339	2	.00181159	17	.00162075
9	.00279330	3 4	.00236407	8 9	.00204918	3	.00180832	18	.00161812
360	.00277778	5	.00235294	490	.00204499	5	.00180505	19 620	.00161551
1	.00277008	6	.00234742	1	.00203666	6	.00179856	1	.00161230
2	.00276243	7	.00234192	2	.00203252	7	.00179533	2	.00160772
3	.00275482	8	.00233645	3	.00202840	8	.00179211	3	.00160514
4	_00274725	9	.00233100	4	.00202429	9	.00178891	3	.00160256
5	.00273973	430	.00232558	5	.00202020	560	.00178571	. 5	.00160000
6	.00273224	1	.00232019	6	.00201613	1	.00178253	6	.00159744
7 8	.00272480	3	.00231481	7 8	.00201207	2	.00177936	7	.00159490
9	.00271739	4	.00230347	9	.00200803	3 4	.00177620	8	.00159236
370	.00270270	5	.00229885	500	.00200000	5	.00177305	630	.00158982
1	.00269542	6	.00229358	1	.00199601	6	.00176678	1	.00158479
2	.00268817	7	.00228833	2	.00199203	7	.00176367	2	.00158378
3	.00268096	8	.00228310	3	.00198807	8	.00176056	3	.00157978
4	.00267380	9	.00227790	4	.00198413	9	.00175747	4	.00157729
5	.00266667	440	.00227273	5	.00198020	570	.00175439	5	.00157480
6	.00265957	1	.00226757	6	.00197628	1	.00175131	6	.00157233
7 8	.00265252	2 3	.00226244	8	.00197239	2	.00174825	7 8	.00156986
9	.00264550	4	.00225734	9	.00196850	3 4	.00174520	8	.00156740
380	.00263158	5	.00224719	510	.00196078	5	.00173913	640	.00156494

No.	Recipro-	No.	Recipro-	No.	Recipro- cal.	No.	Recipro-	No.	Recipro-
641	.00156006	706	.00141643	771	.00129702	836	.00119617	901	.00110988
2	.00155763	7	.00141443	2	.00129534	7	.00119474	2 3	.00110865
8	.00155521	8	.00141243	3	,00129366	8	.00119332		.00110742
4	.00155279	9	.00141044	4	.00129199	9	.00119189	4	.00110619
6	.00155089 .00154799	710	.00140845	5	.00129032 .00128866	840	.00119048 .00118906	5	.00110497
7	.00154559	11 12	.00140449	7	.00128700	1 2	.00118765	6	.00110375
8	.00154321	13	.00140252	8	.00128535	3	.00118624	8	.00110132
9	.00154083	14	.00140056	9	,00128370	4	.00118483	9	.00110011
650	.00158846	15	,00139860	780	.00128205	5	,00118343	910	.00109890
1	.00158610	16	.00139665	1	,00128041	6	.00118203	11	,00109769
200	.00158374	17	.00139470	2 3	.00127877	8	.00118064	12	,00109649
4	.00158140	18 19	.00139276	4	.00127714	9	.00117334	13	,00109529
5	.00152672	720	.00138889	5	.00127388	850	.00117647	15	.00109408
6	.00152439	1	.00138696	6	.00127226	1	.00117509	16	.00109170
7 8	.0015/2207	2	.00138504	7	.00127065	2	,00117371	17	.00109051
8	.00151975	8	.00138313	8	.00126904	3	00117233	17	,00108932
9	.00151745	4	.00138121	9	.00126743	4	.00117096	19	.00108814
660	.00151515	5	.00137981	790	.00126582	5	.00116959	920	,00108696
1	.00151286	6	.00137741	1 2	.00126422	6	.00116822	1 2	.00108578
23	.00151037	8	.00137363	3	.00126103	8	.00116550	3	.00108460
4	.00150602		.00137174	4	.00125945	9	.00116414	4	.0010834
5	,00150376		.00136986	5	.00125786	860		5	.00108108
6	.00150150	1	.00136799	6	.00125628	1	.00116144	6	.00107991
7 8	.00149925	2	.00136612	7	.00125470	2	,00116009	7	.00107878
.8	.00149701	3			.00125813	3		8	,00107753
9	.00149477		.00136240		.00125156	4	.00115741	9	,0010764
670	.00149254		.00135870	1	.00123000	5		930	,0010752
9	.00148809	7	.00135685		.00124688	7	.00115340	2	.00107296
8	.00148588	8		3	.00124533	8	.00115207	3	
4	.00148368			4	.00124378	9	.00115075	4	.0010706
5	.00148148			5	,00124224	870			
2		1 2		6		1 2			
8	.00147710	3		7 8	.00123916	3		7 8	.0010672
9	.00147275					4			
680			.00134228			5	.00114286		
-1	.00146848	6	.00134048	11	,00123305	6	,00114155	1	.0010627
52.65	.00146628		.00133869			7			
5	.00146418					- 8			
1	.00146199			14					
è	,00145985					1			
2	.00145560					2	.00113379		.0010559
3	.00145349				.00122249	3			.0010548
6		4	.00132626		.00122100	4	,00113122		.00105374
690						5			
1	.00144718	6	.00132275			6			
56.50	,00144509		.00132100			8	,00112740		
4	.00144092					9			
5	.00143885			5	.00121212	890			
6	.00143678	1	.00131406	6	.00121065	1	,00112233		
8	,00148472	2	.00131234	8	,00120919	2	.00112108	7	.0010449
8	.00143266		,00131062		.00120778	3		8	
9	,00143061	4	,00130890		.00120627	4		9	.0010427
700	.00142857	5	.00130719	830	.00120482	5			
0	.00142656		.00130348		.00120192	7	.00111607	1 0	.00104058
284	.00142247	8	.00130208	2 3	.00120048	8	.00111359	200	.00103950
4	.00142045	9	.00130039	4	.00119904	9	.00111235	4 5	,00103784
-	.00141844		.00129870	Ď.	.00119760	900		1 5	.0010362

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No.	Recipro-	No.	Recipro-	No.	Recipro-	No.	Recipro-	No.	Recipro-
966		1031	.000969932	1096	.000912409	1161	,000861326	1226	,000815661
7	.00103413	2	.000968992	7	.000911577	2	.000860585	7	.000814996
8	.00103306	8	.000968054	8	.000910747	3	.000859845	8	.000814332
9	.00103199	4	.000967118	9	.000909918	4	.000859106	9	.000813670
970	.00103093	5	.000966184	1100	.000909091	5	.000858369	1230	.000813008
1 9	.00102881	6	.000964320	1 2	.000907441	6	.000856898	1 2	.00081 2348
3	.00102775	8	.000963391	3	.000906618	8	.000856164	3	.000811080
4	.00102669	9	.000962464	4	.000905797	9	.000855432	4	.000810373
5		1040	.000961538	5	.000904977	1170	.000854701	5	.000809717
6		1	.000960615	6	.000904159	1	.000853971	6	.000809061
7	.00102354	2	.000959693	7	.000903342	2	.000853242	7	.000808407
8		8	.000958774	8	.000902527	3	.000852515	8	.000807754
9		4	.000957854	9	.000901713	4	.000851789	9	.00080710
980	.00102041	5	.000956938	1110	.000900901 000900090	5	.000851064		.000806452
2		7	.000955110	12	.000899281	7	.000849618	1 2	.000805802
3		8	.000954198	13	.000898473	8	.000848896	3	.000804505
4		9		14	.000897666	9	.000848176	4	.000803858
5		1050		15	.000896861	1180	.000847457	5	.000803215
6	.00101420	1	.000951475	16	.000896057	1	.000846740	6	.000802560
7		2		17	.000895255	2	.000846024	7	.0008019:2
8		8		18	.000894454	3	.000845308	8	.000801262
9		4	.000948767	19	.000893655	4	.000844595	9	.000800640
990		5		1120		5	.000843882	1250	.00080000
2	.00100908	6		1 2	.000892061	6	.000843170	1 2	.000799860
3		8		3		8	.000841751	3	.000798722
4		9		4	.000889680	9	.000841043	4	.000797448
5		1060				1190	.00084033€	5	.000796818
6		1	.000942507	6		1	.000839631	6	.000796178
7		2	.000941620	7	.000887311	2	.000838926	7	.000795540
. 8		3		8	.000886525	3	.000838222	8	.000794913
9	-00100100	4			.000885740	4	.000837521	9	.000794281
1000		5		1130	.000884956	5	.000836820		.000793651
2	.000999001	7		1 2		6	.000836120	1 2	.000793021
9		8				8	.000834724	3	.000792393
4		9		4	.000881834	9	.000834028	4	.000791139
5						1200	000833333		.00079051
6		1		6		1	.000832639		.00078988
7	.000993049	2	. OUDDONG		.000879508	2	.000831947	7	.000789266
8						3	.000831255	8	,000788648
9						4	.000830565		.00078802
1010						5	.000829875		.00078740
11	.000989120					6	.000829187	1 2	.000786782
13		8		3		8	.000827815	3	.000786168
14				4	.000874126	9	.000827130		.00078492
15				5		1210	.000826446		.000784314
16			.000925069	6	.000872600	11	.000825764	6	.000783699
17	.000983284	2	.0000001414	7	.000871840	12	.000825082		.00078308
- 18		3		8	.000871080	13	.000824402		.00078247
19		4	+000000000	9	.000870322	14	.000823723	9	.000781861
1020				1150		15	.000823045		.000781250
1	.000979432	6		1 2	.000868810 .000868056	16	.000822368	1 2	.00078064
2 3	.000977517	8		3		18	.000821093		.00078003
4	.000976562	9		4	.000866551	19	.000820344	4	.00077881
- 6	.000975610	1090		5		1220	.000819672		.00077821
6	.000974659	1	.000916590	6		1	.000819001	6	.00077760
7	.000973710	2	.000915751	7	.000864304	2	.000818331	7	.00077700
8	.000972763	3		8		3	.000817661	8	.000776397
9	.000971817	4	.000914077	9		4	.000816993		.00077579
1030	.000970874	5	.000913242	1160	.000862069	5	.000816326	11290	.00077

2 3 4 5 6 7 8 9 1300 1 2 3 4 5 6 7 8 9 1310 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	.000774593 .000774593 .000773994 .000773995 .000772797 .000772201 .000771010 .000770410 .000769281 .000768039 .000768049 .000768587 .000768283 .000768283 .000768049 .000768195 .000768329 .000768329 .000768195 .000768195 .000768195 .000768195 .000768195 .000768195 .000768195 .000768195 .000768195 .000768195	1356 7 8 9 1360 1 2 3 4 5 6 7 8 9 1370 1 2	.000737463 .000736920 .000736377 .000735835 .000735294 .000734214 .000734214 .000733676 .000732064 .000732064 .000732064 .000730460 .000729927 .000728963 .000728863 .000728863	1421 2 3 4 5 6 7 8 9 1430 1 2 3 4 5 6	.000703730 .000703235 .000703241 .000702247 .000701754 .000700771 .000700280 .000699790 .000699301 .000698312 .000698324 .000697350 .000698354 .000697350	1486 7 8 9 1490 1 2 3 4 5 6 7 8 9	.000672948 .000672949 .000672043 .000671592 .000671691 .000670241 .000669792 .000669844 .000668499 .00066849 .000667557 .000667557	1551 2 3 4 5 6 7 8 9 1560 1 2 3 4	.000644745 .0006443915 .000643915 .000643915 .000642673 .000642673 .000642861 .000641848 .000641036 .000640205 .000640205 .000639795 .000639795
2 3 4 5 6 7 8 9 1300 1 2 3 4 5 6 7 8 9 1310 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	.000773994 .000773995 .000772797 .000772901 .000771016 .000770416 .000769823 .000769281 .000768049 .000768049 .000766587 .000766587 .000765597 .000764526 .000764526 .000763942 .00076359	7 8 9 1360 1 2 3 4 5 6 7 8 9 1370 1 2 3 4 4 5 6 7 8 9	0007369201 0007369377 000735835 000735294 000738754 0007332676 000733138 000732064 000732064 000730460 000729927 000729395 0007298863	2 3 4 5 6 7 8 9 1430 1 2 3 4 5 6	.000702741 .000702247 .000701754 .000701262 .000700771 .000700280 .000699790 .000699801 .000698812 .000697837 .000697837	7 8 9 1490 1 2 3 4 5 6 7 8 9	.000672043 .000671592 .000671141 .000670241 .000669792 .000669844 .000668896 .000668449 .000668003 .000667557	2 3 4 5 6 7 8 9 1560 1 2 3	.000643915 .0006435087 .000642673 .000642261 .000641848 .000641026 .000640615 .000640205 .000639795
4 5 6 7 8 9 1300 1 2 3 4 5 6 7 8 9 1310 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	.000772797 .000771201 .000771605 .000771010 .000770416 .000769823 .000769281 .000768639 .000768639 .000766283 .000766871 .000765111 .000764526 .000768342 .000768359 .000768359 .000768376 .00076376 .00076376	9 1360 1 2 3 4 5 6 7 8 9 1370 1 2 3 4	.000735835 .000735294 .000734214 .000734214 .000733676 .000733138 .000732064 .000732064 .000730460 .000730460 .000729927 .000729395 .000728863	4 5 6 7 8 9 1430 1 2 3 4 5 6	.000702247 .000701754 .000701765 .000700771 .000700280 .000699790 .000699301 .000698312 .000697837 .000697837	9 1490 1 2 3 4 5 6 7 8 9	.000671592 .000671141 .000670691 .000669792 .000669792 .00066844 .000668449 .000668449	4 5 6 7 8 9 1560 1 2 3	.000643501 .000643087 .000642673 .000642261 .000641848 .000641026 .000640615 .000640205
5 6 7 8 9 1300 1 2 3 4 5 6 7 8 9 1310 11 12 13	.000772201] .000771605 .000771610 .000770416 .000770416 .000769281 .000768639 .000768949 .00076871 .000768597 .000764526 .000768942 .000768359 .000768376 .000768376	1360 1 2 3 4 5 6 7 8 9 1370 1 2 3 4	.000735294 .000734754 .000734214 .000733676 .000733138 .000732064 .000731529 .000730994 .000730994 .000729927 .000729925 .000728863	5 6 7 8 9 1430 1 2 3 4 5 6	.000701754 .000701262 .000700762 .000700280 .000699790 .000699301 .000698312 .000697350 .000697350 .000696864	1490 1 2 3 4 5 6 7 8	.000671141 .000670691 .000670241 .000669792 .00066894 .000668896 .000668449 .000668003	5 6 7 8 9 1560 1 2	.000643087 .000642673 .000642261 .000641848 .000641026 .000640015 .000640205
6 7 8 9 1300 1 2 3 4 5 6 7 8 9 1310 11 12 13	.000771605 .000771010 .000770416 .000769823 .000769823 .000768639 .000768639 .0007686871 .000766283 .000766871 .000768597 .000763359 .000763359 .00076376 .00076376	1 2 3 4 5 6 7 8 9 1370 1 2 3 4	.000784754 .000734214 .000733676 .000733138 .000732601 .000732064 .000731529 .000730994 .000730994 .000729395 .000729395	6 7 8 9 1430 1 2 3 4 4 5 6	.000701262 .000700771 .000700280 .000699730 .000699301 .000698312 .000697837 .0006978350 .000697850	1 2 3 4 5 6 7 8 9	.000670691 .000670241 .000669792 .000669844 .000668449 .000668003 .000667557	6 7 8 9 1560 1 2 3	.000642673 .000642261 .000641848 .000641026 .000640615 .000640205
7 8 9 1300 1 2 3 4 5 6 7 8 9 1310 11 12 13	.000771010 .000770416 .0007709823 .000769823 .000768639 .000768649 .000766873 .000765697 .000765111 .000764526 .000763532 .00076359 .00076376 .000762776 .000762195	2 3 4 5 6 7 8 9 1370 1 2 3 4	.000734214 .000733676 .000733676 .000732661 .000732064 .000731529 .000730994 .000730994 .000729927 .000729305 .000728863	7 8 9 1430 1 2 3 4 5 6	.000700771 .000700280 .000699790 .000698301 .000698324 .000697837 .000697350 .000696864	2 3 4 5 6 7 8 9	.000670241 .000669792 .000669844 .000668896 .000668449 .000668003 .000667557	7 8 9 1560 1 2 3	.000642261 .000641848 .000641437 .000641026 .000640615 .000640205
8 9 1300 1 2 3 4 5 6 7 8 9 1310 11 12 13	.000770416 .000769823 .000769281 .000768639 .000768049 .000766871 .000766283 .000765697 .000765111 .000764526 .000763359 .000763359 .000762195	3 4 5 6 7 8 9 1370 1 2 3 4	.000733676 .000733138 .000732601 .000732064 .000731939 .000730994 .000730460 .000729927 .000729395 .000728863	8 9 1430 1 2 3 4 5 6	.000700280 .000699790 .000699301 .000698812 .000697837 .000697350 .000696864	3 4 5 6 7 8 9	.000669792 .000669844 .000668896 .000668449 .000668003	8 9 1560 1 2 3	.000641848 .000641437 .000641026 .000640615 .000640205
9 1300 1 2 3 4 5 6 7 8 9 1310 11 12 13	.000769823 .000769281 .000768639 .000768049 .000766871 .000766283 .000765111 .000764526 .000763359 .000763359 .000763776 .000762175	4 5 6 7 8 9 1370 1 2 3 4	.000733138 .000732601 .000732064 .000731529 .000730994 .000730460 .000729927 .000729395 .000728863	9 1430 1 2 3 4 5 6	.000699790 ,000699301 .000698812 .000698324 .000697837 .000697350 .000696864	4 5 6 7 8 9	.000669844 .000668896 .000668449 .000668003 .000667557	1560 1 2 3	.000641437 .000641026 .000640615 .000640205
1300 1 2 3 4 5 6 7 8 9 1310 11 12 13	.000769281 .000768639 .000768049 .000767459 .000766283 .000765697 .000765111 .000764526 .00076359 .00076359 .00076376 .000763159	5 6 7 8 9 1370 1 2 3 4	.000732601 .000732064 .000731529 .000730994 .000730460 .000729927 .000729395 .000728863	1430 1 2 3 4 5 6	,000699301 ,000698812 ,000698324 ,000697837 ,000697350 ,000696864	5 6 7 8 9	.000668896 .000668449 .000668003 .000667557	1560 1 2 3	.000641026 .000640615 .000640205 .000639795
1 2 3 4 5 6 7 8 9 1310 11 12 13	.000768639 .000768049 .00076875 .000766871 .000766283 .000765697 .000763942 .000763942 .000763359 .000762195	6 7 8 9 1370 1 2 3 4	.000732064 .000731529 .000730994 .000730460 .000729927 .000729395 .000728863	1 2 3 4 5 6	.000698812 .000698324 .000697837 .000697350 .000696864	6 7 8 9	.000668449 .000668003 .000667557	1 2 3	.000640615 .000640205 .000639795
2 3 4 5 6 7 8 9 1310 11 12 13	.000768049 .000767459 .000766283 .000765697 .000765111 .000764526 .000763359 .000763359 .000762776 .000762195	7 8 9 1370 1 2 3 4	.000731529 .000730994 .000730460 .000729927 .000729395 .000728863	2 3 4 5 6	.000698324 .000697837 .000697350 .000696864	7 8 9	.000668003	2 3	.000640205
3 4 5 6 7 8 9 1310 11 12 13	,000767459 ,000766871 ,000766283 ,000765697 ,000765111 ,000764526 ,000763942 ,000763359 ,000762776 ,000762195	8 9 1370 1 2 3 4	.000730994 .000730460 .000729927 .000729395 .000728863	3 4 5 6	000697837 000697350 000696864	8 9	.000667557	3	.000639795
4 5 6 7 8 9 1310 11 12 13	,000766871 ,000766283 ,000765697 ,000764526 ,000763526 ,000763359 ,000762776 ,000762195	1370 1 2 3 4	.000730460 .000729927 .000729395 .000728863	4 5 6	000697350 000696864	9			
5 6 7 8 9 1310 11 12 13	.000766283 .000765697 .000765111 .000764526 .000763942 .000763359 .000762776 .000762195	1370 1 2 3 4	$\begin{array}{c} .000729927 \\ .000729395 \\ .000728863 \end{array}$	5 6	.000696864			181	
6 7 8 9 1310 11 12 13	.000765697 .000765111 .000764526 .000763942 .000763359 .000762776 .000762195	1 2 3 4	.000729395 .000728863	6		1500	.000666667	5	.000638978
7 8 9 1310 11 12 13	.000765111 .000764526 .000763942 .000763359 .000762776 .000762195	3 4	.000728863			1	.000666223	6	.000638570
8 9 1310 11 12 13	.000764526 .000763942 .000763359 .000762776 .000762195	3 4			.000695894	2	.000665779	7	.000638162
9 1310 11 12 13	.000763942 .000763359 .000762776 .000762195	4	.000728332	8	.000695410	3	.000665336	8	.000637755
1310 11 12 13	.000763359 .000762776 .000762195		.000727802	9	.000694927	4	.000664894	9	.000637349
11 12 13	.000762776	i D	.000727273	1440	.000694444	5	.000664452	1570	.000636943
12		6	.000726744	1	.000693962	6	.000664011	1	.000636537
	000761615	7	.000726216	2	.000693481	7	.000663570	2	.000636132
1.4		8	.000725689	3	.000693001	8	.000663130	8	.000635728
1.4	.000761035	9	.000725163	4	.000692521	9	.000662691	4	.000635324
15	.000760456	1380	,000724638	5	.000692041	1510	,000662252	5	.000634921
16	.000759878	1	.000724113	6	.000691563	11	.000661813	6	.000634518
17	,000759301	2	.000723589	7	.000691085	12	.000661376	7	.000634115
18	.000758725	3	.000723066	8	.000690608	13	.000660939	8	.000633714
	.000758150	4	.000722543	9	.000690131	14	.000660502	9	.000633312
	.000757576	5	.000722022	1450	.000689655	15	.000660066	1580	,000632911
1	.000757002	6	.000721501	1	.000689180	16	.000659631	1	.000632511
	,000756430	7	.000720980	2	.000688705	17	.000659196	2 3	.000632111
3	.000755858	8 9	.000720461	3 4	.000688231	18 19	.000658761	4	.000631712
	.000753267	1390	.000719424	5	.000687285	1520	.000657895	5	.000630915
6	.000754148	1	.000718907	6	.000686813	1	.000657462	6	.000630517
7	.000753579	2	.000718391	7	.000686341	2	.000657030	7	.000630120
8	.000753012	3	.000717875	8	.000685871	3	.000656598	8	.000629723
9	.000752445	4	.000717360	9	.000685401	4	.000656168	9	.000629327
	.000751880	5	.000716846	1460	.000684932	5	,000655738	1590	.000628931
1	.000751315	6	.000716332	1	.000684463	6	.000655308	1	,000628536
2	.000750750	7	.000715820	2	.000683994	7	.000654879	2	.000628141
3	.000750187	8	.000715308	3	.000683527	8	.000654450	3	.000627746
4	.000749625	9	.000714796	4	.000683060	9	,000654022	4	.000627353
5	.000749064	1400	.000714286	5	.000682594	1530	.000653595	5	.000626959
6	.000748503	1	.000713776	6	.000682128	1	.000653168	6	.000626566
7	.000747943	2	.000713267	7	.000681663	2	,000652742	7	.000626174
8	.000747384	8	.000712758	8	.000681199	8	.000652316	8	.00062578
9	.000746826	4	.000712251	9	.000680735	4	.000651890	1000	.00062539
1340	.000746269	6	.000711744	1470	.000680272	5	.000651466	1600	.000625000
2	.000745712	7	.000711238	1 2	.000679348	7	.000650618	4	.00062344
	.000745150	8	.000710732	3	.000678887	8	.000650195	6	.00062344
4	.000744048	9	.000709723	4	.000678426	9	.000649778	8	.00062189
	.000743494	1410	.000709220	5	.000677966	1540	.000649351	1610	.00062111
6	.000742942	11	.000708717	6	.000677507	1	.000648929	2	.00062034
7	.000742390	12	.000708215	7	.000677048	2	.000648508	4	.00061957
8	.000741840	13	.000707714	8	.000676590	3	.000648088	6	.00061881
9	.000741290	14	.000707214	9	.000676132	4	.000647668	8	.00061804
1350	.000740741	15	.000706714	1480	.000675676	5	.000647249	1620	.00061728
1	.000740192	16	.000706215	1	,000675219	6	.000646830	2	.00061652
2	000739645	17	.000705716	2	.000674764	7	.000646412	4	.00061576
3	.000739098	18	.000705219	3	.000674309	8	.000645995	6	.00061500
4 5	.000738552 .000738007	19	.000704722	4		9	.000645578	8	

No.	Recipro-	No.	Recipro-	No.	Recipro- cal.	No.	Recipro- cal.	No.	Recipro-
1632	.000612745	1706	.000586166	1780		1854	.000539374	1928	.000518672
4	.000611995	8	.000585480	2	.000561167	6	.000538793	1930	.000518135
6	.000611247	1710	.000584795	4	.000560538	8	.000538213	2	.000517599
8	_000610500	12	.000584112	6	.000559910	1860	.000537634	4	.000517063
1640	.000609756	14	.000583430	8	.000559284	5	.000537057	6	.000516528
2	.000609013	16	.000582750	1790	.000558659	4	.000536480	8	.000515996
4	.000608272	18	.000582072	2	.000558035	6	.000535905	1940	.000515464
6	.000607533	1720	.000581395	4	.000557413	8	.000535332	2	.000514933
8	.000606796	2	.000580720	6	.000556793	1870	.000534759	4	.000514403
1650	.000606061	4	.000580046	8	.000556174	2	.000534188	6	.000513874
2	.000605327	6	.000579374	18 00	.000555556	4	.000533618	8	.000513347
4	.000604595	8	.000578704	2	.000554939	6	.000533049	1950	.000512820
6	.000603865	1730	.000578035	4	.000554324	8	.000532481	2	.000512295
8	.000603136	2	.000577367	6	.000553710	1880	.000581915	4	.000511770
1660	.000602410	4	.000576701	8	.000553097	2	.000531350	6	.000511247
2	.000601685	6	.000576037	1810	.000552486	4	.000530785	8	.000510725
4	.000600962	8	.000575374	12	.000551876	6	.000530222	1960	.000510204
6	.000600240	1740	.000574713	14	.000551268	8	.000529661	2	.000509684
. 8	.000599520	2	.000574053	16	.000550661	1890	.000529100	4	.000509165
1670	.000598802	4	.000573394	18	.000550055	2	.000528541	6	.000508647
2	.000598086	6	.000572737	1820	.000549451	4	.000527983	8	.000508130
4	.000597371	8	.000572082	2	.000548848	6	.000527426	1970	.000507614
6	.000596658	1750	.000571429	4	.000548246	8	.000526870	2	.000507099
8	.000595947	2	.000570776	6	.000547645	1900	.000526316	4	.000506585
1680	.000595238	4	.000570125	8	.000547046	2	.000525762	6	.000506073
2	.000594530	6	.000569476	1830	.000546448	4	.000525210	8	.000505561
4	.090593824	8	.000568828	2	.000545851	6	.000524659	1980	.000505051
6	.000593120	1760	.000568182	4	.000545256	8	.000524109	2	.000504541
8	.000592417	2	.000567537	6	.000544662	19 10	.000523560	4	.000504032
1690	.000591716	4	.000566893	8	.000544069	12	.000523012	6	.000503524
2	.000591017	6	.000566251	1840	.000543478	14	.000522466	8	.000503018
4	.000590319	8	.000565611	2	.000542888	16	.000521920	1990	.000502513
6	.000589622	1770	.000564972	4	.000542299	18	.000521376	2	.000502008
8	.000588928	2	.000564334	6	.000541711	1920	.000520833	4	.000501504
1700	.000588235	4	.000563698	8	.000541125	2	.000520291	6	.000501002
2	.000587544	6	.000563063	1850	.000540540	4	.000519750	8	.000500501
ã	.000586854	8	.000562430	2	.000539957	6	.000519211		.000500000

Use of reciprocals.—Reciprocals may be conveniently used to facilitate computations in long division. Instead of dividing as usual, multiply the dividend by the reciprocal of the divisor. The method is especially useful when many different dividends are required to be divided by the same divisor. In this case find the reciprocal of the divisor, and make a small table of its multiples up to 9 times, and use this as a multiplication-table instead of actually performing the multiplication in each case.

EXAMPLE — 9871 and several other numbers are to be divided by 1638. The

reciprocal of 1638 is .000610500.

	ples of the		
rec	iprocal:		
1.	.0006105	The table of multiples is made by	
2	.0012210	of 6105. The tenth line is written to	check the accuracy
8.	.0018315	of the addition, but it is not afterwa	rds used.
4.	.0024420	Operation:	•
5.	.0030525	Dividend 9871	
6.	.0086630	Take from table 1	.0006105
Ξ.	0040705		0.040008

0.042735 00.48840 .0048840 8. 9..... 005 4945 .0061050 Quotient 6.0262455

SQUARES, CUBES, SQUARE ROOTS AND CUBE ROOTS OF NUMBERS FROM .1 TO 1600.

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
.1 .15 .2 .25	.04	.001 .0034 .008 0156 027	.3162 .3873 .4472 .500 .5477	.4642 .5313 .5848 .6300 .6694	3.1 .2 .3 .4 .5	9.61 10.24 10.89 11.56 12.25	29.791 32.768 35.987 39.304 42.875	1.761 1.789 1.817 1.844 1.871	1.458 1.474 1.489 1.504 1.518
.35 .4 .45 .5	.1225 .16 .2025 .25 .3025	0429 064 .0911 .125 .1664	.5916 .6325 .6708 .7071 .7416	.7047 .7368 .7663 .7937 .8193	.6 .8 .9 4 .	12.96 13.69 14.44 15.21 16.	46.656 50.653 54.872 59.319 64.	1.897 1.924 1.949 1.975 2.	1.533 1.547 1.560 1.574 1.5874
.65 .7 .75	.36 .4225 .49 .5625 .64	.216 .2746 .343 .4219 .512	.7746 .8062 .8367 .8660 .8944	.8434 .8662 .8879 .9086 .9283	.1 .2 .3 .4 .5	16.81 17.64 18.49 19.36 20.25	68.921 74.088 79.507 85.184 91.125	2.025 2.049 2.074 2.098 2.121	1.601 1.613 1.626 1.639 1.651
.85 .9 .95 1. 1.05	.7225 .81 .9025 1. 1.1025	.6141 .729 .8574 1. 1.158	.9219 .9487 .9747 1. 1.025	.9478 .9655 .9830 1. 1.016	.6 .7 .8 .9 5.	21.16 22.09 28.04 24.01 25.	97.836 103.823 110.592 117.649 125.	9.145 2.168 9.191 2.214 2.2361	1.663 1.675 1.687 1.698 1.7100
1.1 1.15 1.2 1.25 1.3	1.21 1.3225 1.44 1.5625 1.69	1.331 1.521 1.728 1.953 2.197	1.049 1.072 1.095 1.118 1.140	1.082 1.048 1.068 1.077 1.091	.1 .2 .3 .4 .5	26.01 27.04 28.09 29.16 80.25	182.651 140.608 148.877 157.464 166.375	2.258 2.280 2.302 2.324 2.345	1.721 1.732 1.744 1.754 1.765
1.85 1.4 1.45 1.5 1.55	1.8225 1.96 2.1025 2.25 2.4025	2.460 2.744 3.049 8.375 8.724	1.162 1.183 1.204 1.2247 1.245	1.105 1.119 1.132 1.1447 1.157	.6 .7 .8 .9	31.86 32.49 83.64 84.81 36.	175.616 185.198 195.112 205.379 216.	2.366 2.387 2.408 2.429 2.4495	1.776 1.786 1.797 1.807 1.8171
1.65 1.65 1.7 1.75 1.8	2.56 2.7225 2.89 3.0625 3.24	4.096 4.492 4.918 5.359 5.833	1.265 1.285 1.304 1.823 1.342	1.170 1.182 1.193 1.205 1.916	.1 .8 .4 .5	87.21 38.44 89.69 40.96 42.25	226.981 238.328 250.047 262.144 274.625	2.470 2.490 2.510 2.530 2.550	1.827 1.837 1.847 1.857 1.866
1.85 1.9 1.95 2.	3.4225 3.61 3.8025 4. 4.41	6.332 6.859 7.415 8. 9.261	1.360 1.378 1.396 1.4142 1.449	1.228 1.239 1.249 1.2599 1.281	.6 .7 .8 .9 7.	48.56 44 89 46.24 47 61 49.	287.496 300.763 314.432 328.509 343.	2.569 2.588 2.608 2.627 2.6458	1.876 1.885 1.895 1.904 1.9129
.2 .3 .4 .5	4.84 5.29 5.76 6.25 6.76	10.648 12.167 18.824 15.625 17.576	1.483 1.517 1.549 1.581 1.612	1.801 1.320 1.889 1.857 1.875	.1 .2 .3 .4 .5	50.41 51.84 58.29 54.76 56.25	857.911 373.248 389.017 405.224 421.875	2.665 2.683 2.702 2.720 2.739	1.922 1.931 1.940 1.949 1.957
.7 .8 .9 3.	7.29 7.84 8.41 9.	19.683 21.952 24.389 27.	1.643 1.673 1.708 1.7321	1.892 1.409 1.426 1.4422	.6 .7 .8 .9	57.76 59.29 60.84 62.41	438.976 456.583 474.551 493.089	2.757 2.775 2.798 2.811	1.966 1.975 1.983 1.992

	1								
No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
8.	64.	512.	2.8964	2.	45	2025	91125	6.7092	3.5569
.1	65.61	581.441	2.846	2 008	46	2116	97886	6.7828	8.5880
. 3	67.84	551.868	2.864	2.017	47	2209	103823	6.8557	8.6088
.8	68.89	671.787	2.881	2 025 2 033	48	2804	110592	6.9282	8.6842
.4	70.56	592.704	3.898	2.088	49	2401	117649	7.	8,6598
.5	78.25 73.96	614.195 686.056	2.915 2.988	2.041 2.049	50 51	2500 2601	185000 189651	7.0711	8.6640
.6 .7	75.69	658.508	2.960	2.057	25 21	2704	140608	7.1414	3.7084 3.782
.8	77.44	681.472		2.065	58	2809	148877	7.2801	8.7568
.9	79.21	704.969		2.072	54	2916	157464	7.8485	8.7798
●.	81.	729.	8.	2.0801	55	8095	166875	7.4162	8.6080
.1	82.81	758.571	8.017	2.068	56	8186	175616	7.4688	3.8959
 8. ·	84.64 86.49	778.688 804.857	8.088	2.095 2.108	57 58	8249 8864	185198 195119	7.5496 7.6158	8.6485 8.6709
.4	86.86	880.584	8.066	2.110	59	8481	306879	7.6811	8.8980
.5	90.95	657.875	3.089	2.118	60	8600	216000	7.7460	8.9149
.6 .7	92.16	884.786	8.098	2.125	61	8721	226961	7.8102	3.9865
.7	94.09	912.678		2 188	69	8844	288828	7.8740	3.9579
.8 .9	96.04 96.01	941.19% 970,299	3.180 8.146	2.140 2.147	68 64	8969 4096	250047 262144	7.9878	3.9791 4.
10	100	1000	3.1698 3.3166	2.1544 2.2240	65 66	4995 4856	274625 287496	8.0698	4.0007
11 12	121	1881 1743	3.4641	2.2894	67	4489	800763	8.1240 8.1854	4.0615
13	169	2197	8.6056	2.3513	68	4694	314482	8.2462	4.0617
14	196	2744	8.7417	2.4101	69	4761	328509	8.8066	4.1016
15	995	8875	3.8730	2.4663	70	4900	848000	8.8666	4.1918
16	956	4098	4.	2.5198	71	5041	857911	8.4261	4.1408
17 18	239 8594	4918 58 8 2	4.1281	2.5718 2.6907	73	5184 5899	373948 389017	8.4858 8.5440	4.1602
19	861	6859	4.8589	2.6684	74	5476	405224	8.6028	4.1988
20	400	8000	4.4791	2.7144	78	5625	421875	8.6608	4.2172
21	441	9961	4.5826	2.7589 -	76	5776	438976	8.7178	4.2858
22	484	10648	4.6904	8.8020	77	5999	456588	8.7750	4.2543
98 94	529 576	121 67 13894	4.7958	2.8439 2.8845	78 79	6084 6941	474552 498039	8.8316 8.8682	4.2727
-	696	15695	5.	2.9240	80	6400	512000	8.9448	4.3089
86	676	17576	5.0990	2.9625	81	6561	531441	9.	4.8967
267	799	19688	5.1969	8.	83	6794	551368	9.0554	4.8445
28	784	21968	5.2915	8.0366	88	6889	571787	9.1104	4.8621
89	841	24389	5.8852	8.0728	84	7056	592704	9.1652	4.8795
80	900	27060	5.4772	8.1072	85	7995	614125	9.2195	4.8968
#1 #2	961 1094	29791 82768	5.5678 5.6569	8.1414 8.1748	86 87	7896 7569	636056 658508	9.2786	4.4140
=	1080	85987	5.7446	8.2075	86	7744	681478	9.8808	4.4480
84	1 156	39804	5.8810	8.2396	89	7981	704969	9.4840	4.4647
85	(225	42975	5.9161	8.2711	90	8100	729000	9.4868	4.4814
\$6	1296	46656	6.	8.3019	91	8881	758571	9.5394	4.4979
87	1869	5065%	6.0828	8.3892	99	8464 8649	778688 804357	9.5917	4.5144
86 89	1444 1591	5487 8 59 8 19	6.2450	8.8020	94	8886	804307 880 584	9.6954	4.5468
40	1600	64900	6.3246	8.4900	95	9085	857875	9 7468	4.5629
41	1661	68921	6.4061	8.446%	96	9216	884786	9.7980	4 8790
40	1764	74088	6.4807	8.4760	97	9409	919678	9.8489	4.594
48	1840 1986	79507	6.5574	3.5064	98	9604	941192	9.8995	4.44
44	1906	85184	6.6888	8.5808	99	9801	970299	9.9499	4.

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
	40000	4000000		4 0410		04000		10.4400	
100	10000	1000000 1030801	10. 10.0499	4.6416 4.6570	155 156	24025 24336	8728875	12.4499 12.4900	5.8717 5.8832
101	10201 10404	1061208	10.0995	4.6723	157	24649	3796416 3869898	12.5300	5.8947
102 103	10609	1001200	10.1489	4.6875	158	24964	8944812	12.5698	5.4061
104	10816	1124864	10.1980	4.7027	159	25281	4019679	12.6095	5.4175
104	10010								
105	11025	1157625	10.2470	4.7177	160	25600	4096000	12.6491	5.4288
106	11286	1191016	10.2956	4.7826	161	25921 26244	4173281	12.6886	5.4401
107	11449	1225048 1259712	10.8441 10.8928	4.7475	162 163	26569	4251528 4880747	12.7279 12.7671	5 4514 5.4626
108 109	11664 11881	1295029	10.4408	4.7769	164	26896	4410944	12.8062	5.4787
100									
110	12100	1381000	10.4881	4.7914	165	27225	4492125	12.8452	5.4848
111 .	12321	1367681	10.5857	4.8059	166	27556	4574296	12.8841	5.4959
112	12544	1404928	10.5830	4.8203	167	27889	4657468	12.9228	5.5069
118	12769	1442897	10.6301 10.6771	4.8346	168	28224 28561	4741682	12.9615 13.0000	5.5178
114	12996	1481544	10.6771	4.8488	169	28301	4826809	13.000	5.5288
115	18225	1520875	10.7288	4.8629	170	28900	4913000	13.0384	5.5897
116	13456	1560896	10.7708	4.8770	171	29241	5000211	13.0767	5.5505
117	18689	1601618	10.8167	4.8910	172	29584	5088448	13.1149	5.5618
118	18924	1648082	10.8628 10.9087	4.9049 4.9187	178 174	29929 30276	5177717 5268024	13.1529 13.1909	5.5721 5.5828
119	14161	1685159	10.9067	4.9101	114	00210	0200024	10.1909	0.0000
120	14400	1728000	10,9545	4.9324	175	80625	5359375	18.2288	5.5934
121	14641	1771561	11.0000	4.9461	176	80976	5451776	18.2665	5.6041
122	14884	1815848	11.0454	4.9597	177	31329	5545288	18.8041	5.6147
123	15129	1860867	11.0905	4.9732	178	31684	5639752	18.3417	5.6252
124	15376	1906624	11.1855	4.9866	179	82041	5785889	18.8791	5.6357
125	15625	1953125	11.1808	5.0000	180	82400	5832000	18.4164	5.6462
126	15876	2000376	11.2250	5.0133	181	32761	5929741	18.4586	5.6567
127	16129	2048383	11.2694	5.0265	182	33124	6028568	18.4907	5.6671
128	16884	2097152 2146689	11.8187 11.8578	5.0897 5.0528	183 184	33489 33856	6128487 6229504	18.5277 18.5647	5.6774 5.6877
129	16641	2140009	11.6016	5.0020	104	00000	0429004	10.5011	0.0017
180	16900	2197000	11.4018	5.0658	185	84225	6331625	18.6015	5.6980
181	17161	2248091	11.4455	5.0788	186	34596	6434856	13.6382	5.7083
182	17424	2299968	11.4891	5.0916	187	84969	6539208	13.6748	5.7185
188	17689	2352687	11.5326	5.1045	188	85844	6644672	18.7118	5.7287
184	17956	2406104	11.5758	5.1172	189	85721	6751269	18.7477	5.7888
185	18225	2460375	11.6190	5,1299	190	86100	6859000	18.7840	5.7489
136	18496	2515456	11.6619	5.1426	191	86481	6967871	18.8208	5.7590
137	18769	2571858	11.7047 11.7478	5.1551	192	36864	7077888	18.8564	5.7690
188	19044	2628072	11.7478	5.1676	198	87249	7189057	13.8924	5.7790
189	19321	2685619	11.7899	5.1801	194	87636	7301884	18.9284	5.7890
140	19600	2744000	11.8322	5.1925	195	38025	7414875	18.9642	5.7989
141	19881	2803221	11.8748	5.2048	196	38416	7529536	14.0000	5.8088
142	20164	2868288	11.9164	5.2171	197	88809	7645878	14.0357	5.8186
148	20449	2924207	11.9588	5.2293	198	39204	7762392	14.0712	5.8285
144	20736	2985984	12.0000	5.2415	199	89601	7880599	14.1067	5.8883
145	21025	3048625	12.0416	5.2536	200	40000	8000000	14.1421	5.8480
146	21316	3112136	12.0830	5.2656	201	40401	8120601	14.1774	5.8578
147	21609	3176523	12.1244	5.2776	202	40804	8242408	14.2127	5.8675
148	21904	3241792 3307949	12.1655 12.2066	5.2896 5.8015	203 204	41209 41616	8365427 8489664	14.2478 14.2829	5.8771
149	22201	0901948		0.0019	×02	41010	0409004	19.2029	5.8868
150	22500	3375000	12.2474	5.8188	205	42025	8615125	14.3178	5.8964
151	22801	8442951	12.2882	5.8251 5.8868	206 207	42436 42849	8741816	14.8527	5.9059
152 158	23104	3511808 3581577	12.8288 12.8698	5.3485	208	43264	8869743 8998912	14.8875	5.9155
100	23409	3652264	12 4097			43681	9129829	14.4292	5.9950
1_	28716	-0002204	112 4197	(J. J. (1)	auri	4-3001	A1XA9XA	114.4568	5.9845

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
210	44100	9261000	14:4914	5.9439	265	70225	18609625	16.2788	6.4232
211	44521	9893981	14.5258	5.9533	266	707. 6	18821096	16.8095	6.4818
212	44944	9528128	14.5602	5.9627	267	71289	19084168	16.8401	6.4898
213	45869	9663597	14.5945	5.9721	268	71824	19248832	16.3707	6.4478
214	45796	9800844	14.6287	5.9814	269	72861	19465109	16.4012	6.4558
215	46225	9988375	14.6629	5.9907 6.0000	270	72900	19683000	16.4817	6.4633
216	46656 47089	10077696	14.6969 14.7309	6.0092	271 272	78441 78984	19902511 20128648	16.4621 16.4924	6.4718 6.4792
217 218	47524	10218318	14.7648	6 0185	278	74529	20846417	16.5227	6.4872
219	47961	10508159	14.7986	6 0277	274	75076	20570824	16.5529	6.4951
220	48400	10648000	14.8324	6.0368	275	75625	20796875	16.5881	6.5080
2/1	48841	10798861	14.8661	6.0459	276	76176	21024576	16.6182	6.5108
222 223	49284 49749	10941048 11089567	14.8997 14.9832	6 0550 6.0641	277 278	70729 77284	21258988 21484952	16.6438 16.6788	6.5187 6.5265
24	50176	11289424	14.9666	6.0732	279	77841	21717639	16.7088	6.5848
2:25	50625	11890625	15.0000	6.0822	280	78400	21952000	16.7882	6.5421
226	51076	11548176	15.0833	6.0912	281	78961	22188041	16.7681	6.5499
***	51529	11697083	15.0665	6 1002	388	79524	22425768	16.7929	6.5577
228 220	51 984 52441	11852852 12008989	15.0997 15.1827	6.1091 6.1180	283 254	80039 80656	22665187 22906304	16.8226 16.8528	6.5654 6.5781
280	52900	12167000	15.1658	6.1269	285	81225	28149125	16.8819	6.5808
231	58861	12826391	15.1987	6.1858	286	81796	23398656	16.9115	6.5885
282	58884	12487168	15.2315	6.1446	287	82869	23639903	16.9411	6.5962
283	54289	12649887	:5.2613	6.1534	388 388	82944	23887872	16.9706	6.6089
284	54756	12812904	15.2971	6.1622	×49	88521	24137569	17.0000	6.6115
235	55225	12977875	15.8297	6.1710	290	84100	24389000	17.0294	6.6191
286	55696 56169	18144256 18319058	15.3628 15.3948	6.1797 6.1885	2J1 292	84681 85264	24842171 24897088	17.0587 17.0880	6.6267 6.6848
247 248	56644	13481272	15 4278	6.1972	298	85849	25153757	17.1172	6.6419
239	57121	13651919	15.4596	6.2058	294	86436	25412184	17.1464	6.6494
240	57600	13824000	15.4919	6.2145	295	87025	25672875	17.1756	6.6569
241	58061	13997521	15.5242	6.2231	246	87616	25934336	17.2047	6.6644
242 243	58564 59049	14172488 14348907	15.5568 15.5885	6.2817 6.2403	297 298	88209 88804	26198078	17.2337	6.6719
344	59536	14526784	15.6205	6.2488	299	89401	26468592 26730899	17.2627 17.2916	6.6794 6.6869
345	60025	14706125	15.6525	6.2578	800	90000	27000000	17.8205	6.6948
246	60516	14886936	15.6844	6.2658	801	90601	27270901	17.3494	6.7018
247	61009	15069228	15.7162	6.2748	:303	91204	27543608	17.8781	6.7092
248 249	61504 62001	15252992 15438249	15.7480 15.7797	6.2828 6.2912	303 304	91809 92416	27818127 28094464	17.4069 17.4856	6.7166 6.7240
250	62500	15625000	15.8114	6.2996	805	98025	28372625	17.4642	6.7318
251	63001	15818251	15.8480	6.8080	806	93686	28652616	17.4929	6.7887
252	68504	16003008	15.8745	6.8164	807	94249	28984448	17.5214	6.7460 6.7588
25.1	64009	16194-77	15.9000 15.9874	6.8847	808	94864	29218112	17.5499	6.7588
#5 1	64516	16387064			309	95481	29508629	17.5784	6.7606
255 256	65025 65536	16561375 16777216	15.9687 16.0000	6.8418 6.8496	810 811	96100 96721	29791000 30080281	17.6068 17.6352	6.7679 6.7752
200 257	66049	16974598	16.0312	6.3579	812	97844	30371328	17.6685	6.7824
258	66564	17178512	16.0624	6.8661	818	97969	30664297	17.6918	6.7897
250	67081	17878979	16.0985	6.8748	814	98596	80959144	17.7200	6.7969
200	67600	17576000	16.1245	6.3825	815	99225	81255875	17.7482	6.8041
961	68121	17779681	16.1555	6.8907	816	99856	31554496	17.7764	6.8118
902 963	68644	17984728	16.1864 16.2178	6.8988 6.4070	817	100489	31855013 32157482	17.8045 17.8826	6.816
204 264	69169	18191447 18899744	16.2481	6.4151	818 819	101124 101761	82461759	17.8606	6.8
-	1 00000	10000143	110.4901	0.4101	018	1101101	06401108	144.0000	0.64

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
	100400	82768000	177 990K	6.8899	875	140695	52784875	19.8649	7.8112
890 821	102400 108041	83076161	17.8885 17.9165	6.8470	376	141876	53157876	19.8907	7.2177
835	103684	33386948	17.9444	6.8541	877	142129	58582688	19.4165	7.2240
823	104829	83696967	17.9722	6.8612	378	142884	54010159	19.4422	7.4804
324	104976	84012224	18.0000	6.8688	879	148641	54489989	19.4679	7.2868
825	105625	84828125	18.0978	6.8758	880	144400	54879000	19.4986	7.9432
8:28	106276	34645976	18.0555	6.8824	881	145161	53806841	19.5192	7.2558 7.2558
827 828	106929	84965788	18.0631	6.8894 6.8964	382 883	145924 146689	55749968 56181887	19.5448 19.5704	7.2622
839	107584 108941	85287552 85611289	18.1108 18.1 8 84	6.9084	384	147456	50623104	19.5959	7.2085
890	108900	85987000	18.1659	6,9104	885	148225	57066625	19.6914	7.2748
881	109561	86264691	18.1984	6.9174	38 6	148996	57512456	19.6469	7.2811
333	110224	86594868	18.2209	6.9244	887	149769	57960608	19.6723	7.2874
888	110889	86926087	18.2483	6.9318	888	150544	58411072	19.6977	7.2986
884	111556	87259704	18.2757	6.9882	889	151891	58868869	19.7231	7.2999
885	112225	87595375	18.3080	6.9451	39 0	152100	59319000	19.7484	7.3061
836	112896	87983056	18.3308	6.9521	891	152881	59778471	19.7787	7.8184
337	118569	88272753	18.8576	6.9589	892	153664	60236288	19.7990	7.3186
888	114244	88614472	18.3848	6.9658	898	154449	60698457	19.8242	7.8248
889	114991	88958219	18.4120	6.9727	894	155286	61162964	19.8494	7.8810
840	115600	89304000	18.4391	6.9795	896	156025	61629875	19.8746	7.8872
841	116281	89651821	18.4662	6.9864	396	156816	62099136	19.8997	7.8484
842	116964	40001688	18.4932	6 9982	397	157609	62570778	19.9249	7.3498
843	117649	40858607	18.5203	7.0000	398	158404	63044792	19.9499 19.9750	7.8558 7.8619
844	118886	40707584	18.5472	7.0068	899	159901	68521199		
845	119025	41068625	18.5742	7.0136	400	160000	84000000	20 0000	7.3581
846	119716	41421786	18.6011	7.0208	401	160601	64481201	20 0250	7.8742
847	120409	41781928	18.6379	7.0971	402	161604	64964808	20.0499	7.8808
848	121104	42144198 42508549	18.6548	7.0388	408 404	162409 163916	65450927 65489264	20 0749	7.8964
849	121801		18.6815						
850	122500	42875000	18.7083	7.0478	405	164025	66430125	20.1946	7.8986
851	123201	48943551	18.7850	7.0540	406	164886	66923416	20.1494	7.4047
852	123904	43614208	18.7617	7.0807 7.0874	407 408	165649 166464	67419148 67917812	20.1742 20.1990	7.4108 7.4169
853 854	124609 125816	48986977 44861864	18.7883 18.8149	7.0740		167281	68417929	20.9287	7.4999
855	126025	44788875	18.8414	7.0807	410	168100	68921000	20.2485	7.4290
856	126786	45118016	18.8680	7.0878	411	168921	69426581	20.2781	7.4850
857	127449	45499998	18.8944	7.0940	412	169744	69984528	20.2978	7.4410
858	128164	45882712	18 9909	7.1006	418	170669	70444997	20.3234	7.4470
859	128881	46268279	18.9478	7.1072	414	171896	70957944	20.8470	7.4580
860	129600	46656000	18.9787	7.1188	415	172226	71478375	90.8715	7.4500
861	130821	47045881	19.0000	7.1204	416	178056	71991996	20.8961	7.4650
868	181044	47487998	19.0968	7.1269	417	178889	72511718	20.4206	7.4710
868 864	181769 182496	47889147 48 92854 4	19.0596 19.0788	7.1885 7.1400	418 419	174724 175561	78084682 78560059	20.4450	7.4770
865	188295	48697125	19.1050	7.1466	420	176400	74088000	20.4989	7.4880
866	188956	49027896	19.1811	7.1581	481	177241	74618461	20.5188	7.4049
867	134689	49480868	19.1572	7.1596	422	178084	75151448	20.5426	7.4948 7.5007
368	135424	49886032	19.1888	7.1661	428	178929	75686967	20.5670	7.5067
869	186161	50243409	19.2094	7.1726	424	179776	76925094	20.5918	7.5196
870	136900	50658000	19.2854	7.1791	425	180695	76765625	20.6155	7.5186
871	187641	51064811	19.2614	7.1855	496	181476	77808776	20.6896	7.5944
873	188884	51478848	19.2878	7.1920	427	189899	77854488	20.6640	7.5808
948	189129	51895117	19.8182	7.1984	428	188184	78402758	20.6850	
74	189876	52818694	19.3891	7.2048	447	184041	78958589	20.7198	7.5490

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No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
400	184900	79507000	20.7864	7.5478	485	235925	114084125	22.0227	7.8568
431	185761	80062991	20.7605	7.5587	486	236196	114791256	22.0454	7.8622
49	186694	80621568	20.7846	7.5505	487	237169	115501808	22.0681	7.8676
43	187489 188856	S1182737 81746504	20.8087 20.8327	7.5654 7.5712	488 489	238144 239131	116214372 116930169	22.0907 22.1183	7.8780
		01190004	eu.ouer	1.0712	409	209191	110990109	ZZ. 1100	7.8784
45	189295	82312875	20.8567	7.5770	490		117649000	22.1359	7.8837
47	190096 190969	82881856 83458458	20.8906 20.9045	7.5828 7.5886	491 492		118370771 119095488	22.1585 22.1811	7.8991 7.8944
448	191844	84027672	20.9384	7.5944	498	243049	119828157	22.2036	7.8998
400	192721	84004519	20.9523	7.6001	494	244086	190553784	28.2261	7.9061
440	198800	85184000	20.9762	7.6059	495	245025	121287875	22.2486	7.9105
411	194481 195864	85766121	21.0000	7.6117	496	246016	122023936	22.2711	7.9158
442 448	196849	86350688 86988807	21.0238 21.0476	7.6174 7.6282	497 498	247009 248004	122763478 128505992	22.2985 22.3159	7.9211 7.9264
44	197186	87528384	21.0718	7.6289	499	249001	184251499	22 3883	7.9317
415	198085	88191125	21.0950	7.6346	500	250000	125000000	22.3607	7.9370
446	198916	98716586	21.1187	7.6408	501	251001	125751501	22,3830	7.9428
417	199889	89314623	21.1494	7.6460	502	252004	126506008	23,4064	7.9476
448	900704 201601	8991539-2 90518849	21.1660 21.1896	7.6517 7.6574	503 504	253009 254016	197268527 198094064	28.4277 28.4499	7.9528 7.9581
_			1				180061001		1.9001
450	202500	91125000	21.2132	7.6681	505	255025	128787625	23.4722	7.9684
451 452	908401 904804	91788851 92845408	21.2868 21.2608	7.6688	506 507	256086 257049	1 29 554216 180328843	22.4944 22.5167	7.9686
48	205200	92959677	21.2889	7.6800	508	258064	131096512	22.5389	7.9791
454	306116	98576664	21.3078	7.6857	509	259081	181872229	22.5610	7.9848
456	907095	94196875	21.3807	7.6914	510	260100	132651000	22.5832	7.9896
454	907986	94818816	21.3542	7.6970	511	261121	188482881	23.6058	7.9948
458	208849 209784	95448998 96071919	21.3776 21.4009	7.7026 7.7082	512 518	262144 263169	184217728 185005697	29.6474 24.6495	8.0000 8.0052
450	210681	96702579	21.4248	7.7188	514	264196	185796744	23.6716	8.0104
40	211600	97386000	21.4476	7.7194	515	265225	186590975	29.6936	8.0156
41	212591	97972181	21.4709	7.7194 7.7250 7.7806	516	266256	187388096	29.7156	8.0208
霊	918444	98611128	21.4942 21.5174	7.7808 7.78 63	517	267289 268824	188188418	23.7876	8.0260
機器	214869 215896	99258847 99897844	21.5407	7.7418	518 519	269861	188991832 189798859	29.7596 29.7816	8.0311 8.0363
-	216225	1005 44608	21.5689	7.7478	520	000400			
465 465		100544625 101194696	21.5870	7.7529	521	270400 271441	140608000 141420761	22.8035 22.8254	8.0415 8.0466
487	218089	101847568	21.6102	7.7584	522	272484	142286648	22 8478	8.0517
48	219094	102508282	21.6888	7.7689	528	273529	148055667	22.8692	8.0569
-	319961	105161709	21.6564	7.7695	584	274576	143877824	28.8910	8.0630
170	200000	106823000	21.6795	7.7750	595	275625	144708125	22.9129	8.0671
471 472	\$21841 \$23784	104487111 105154048	21.7025 21.7256	7.7805 8.7860	526 527	276676 277729	145581576 146368188	22.9347 22.9565	8.0723
ä	225730	105823817	21.7486	7.7915	528	278784	147197952	22.9788	8.0774 8.0825
474	224676	106496424	21.7715	7.7970	529	279841	148085889	28.0000	8.0876
175	225625	107171875	21.7945	7.8095	580	280900	148877000	28.0217	8.0927
176	226576	107850176	21.8174	7.8079	581	281961	149721291	28.0484	8.0978
477		106581888 109215 352	21.8408 21.8622	7.8184 7.8188	58% 583	283024 2840 8 9	150568768	28.0651	8.1028
173		109909589	21.8861	7.8248	584	285156	151419487 152278304	23.0968 23.1084	8.1079 8.1180
400		*****	1 1	77 0000	585	00000			
481	380400 351861	110592000 111 28464 1	21.9089 21.9817	7.8297 7.8852	586	286225 287296	158180875 158990656	23.1301 23.1517	8.1180 8.1281
4	303004	111980168	21.9545	7.8406	587	288369	154854158	23.1788	8.1281
	350-100	119678587	21.9778	7.8460	588	289444	155720872	28.1948	8.1389
-	204206	118879004	22.0000	7.8514	589	290521	156590819	23.2164	8.136

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No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
540	291600	157464000	28.2379	8.1488	595	354025	210644875	24.3926	8.4108
541	292681	158340421	28.2594	8.1488	596	855216	211708736	24.4131	8.4155
542	293764	159220088	28.2809	8.1533	597	356409	212776178	24.4336	8.4202
548	294849	160103007	23.8024	8.1583	598	857604	218847192	24.4540	8.4249
544	295936	160989184	28.3238	8.1633	599	358801	214921799	24.4745	8.4296
545	297025	161878625	28.3452	8.1683	600	860000	216000000	24.4949	8.4343
546	298116	162771886	23.8666 23.8880	8.1788 8.1788	602	361201 362404	217081801	24.5153	8.4390
547 548	299209 300304	168667823 164566592	23.4094	8.1888	608	368609	218167208 219256227	24.5857 24.5561	8.4487 8.4484
549	801401	165469149	28.4307	8.1882	604	864816	220348864	24.5764	8.4530
550	802500	166875000	23.4521	8.1982	605	866025	221445125	24.5967	8.4577
551	803601	167284151	28.4784	8.1982	606	367236	222545016	24.6171	8.4623
552	804704	168196608	28.4947	8.2031	607	368449	228648548	24.6374	8.4670
553 554	305809 306916	169112877 170031464	28.5160 28.5872	8.2081 8.2180	608 609	369664 370681	224755712 225866529	24.6577 24.6779	8.4716 8.4763
	1				ŀ	900100	000001000	1 1	
555 556	308025 309136	170953875 171879616	23.5584 23.5797	8.2180 8.2229	610 611	372100 373321	226961000 228099181	24.6982 24.7184	8.4809 8.4856
557	310249	172808698	23.6006	8.2278	612	874544	2:29:220928	24.7386	8.4902
558	811364	178741112	28.6220		618	375769	230346897	24.7588	8.4948
559	312481	174676879	28.6482	8.2877	614	376996	281475544	24.7790	8.4994
560	313600	175616000	23.6648	8.2426	615	378225	232608375	24.7992	8.5040
561	814721	176558481	23.6854	8.2475	616	379456	233744896	24.8198	8.5086
562	815844	177504828	28.7065	8.2524	617	380689	284885118	24.8896	8.5132
563	816969	178453547	28.7276	8.2578	618	381924	286029082	24.8596	8.5178
564	318096	179406144	28.7487	8.2621	619	383161	237170659	24.8797	8.5224
565	819225	180862125	28.7697	8.2670	620	884400	238328000	24.8998	8.5270
566	320356 321489	181821496 182284268	28.7908	8.2719 8.2768	621 622	385641 386884	289488061 240641848	24.9199	8.5816 8.5862
567 568	822624	188250482	28.8118 28.8326	8.2616	628	388129	241804867	24.9899 24.9600	8.5408
569	828761	184220009	23.8587	8.2865	624	389876	242970624	24.9800	8.5458
570	324900	185193000	23.8747	8.2918	625	390625	244140625	25,0000	8.5499
571	826041	186169411	28.8956		626	391876	245314376	25.0200	8.5544
572	327184	187149248	23.9165	8.3010	627	398129	246191888	25.0400	8.5590
573	328329	188182517	28.9874	8.3059	628	394884	247678152	25.0599	8.5685
574	829476	189119224	28.9583	8.8107	629	895641	248858189	25.0799	8.5681
575	880625	190109875	23.9792	8.8155	680	896900	250047000	25.0998	8.5726
576	881776	191102976	24.0000	8.3208	681	398161	251239591	25.1197	8.5772
577	332929	192100088	24.0208	8.3251	682	399424 400689	252485968	25.1896	8.5817
578 579	334084 335241	193100552 194104539	24.0416 24.0624	8.3300 8.3348	688 684	401956	258686187 254840104	25.1595 25.1794	8.58 62 8.5907
580	336400	195112000	24.0882	8.8396	635	403925	256047875	25,1992	8.5952
581	337561	196122941	24.1089	8.3448	636	404496	257259456	25.2190	8.5997
582	338724	197137368	24.1247	8.3491	637	405769	258474858	25.2389	8.6043
588	339889	198155287	24.1454	8.8539	688	407044	259694072	25.2587	8.6068
584	841056	199176704	24.1661	8.3587	689	408821	260917119	25.2784	8.6182
585	342225	200201625	24.1868	8.3634	640	409600	262144000	25.2989	8.6177
586	343396	201280056	24.2074	8.3682	641	410881	268374721	25.3180	8.6222
587	344569	202262008 203297472	24.2281 24.2487	8.3730 8.3777	642 648	412164	264609288 265847707	25.3877 25.3574	8.6267 8.6312
588 589	845744 846921	204386469	24.2693		644	414786	267089984	25.3772	8.6357
590	348100	205879000	24.2899	8.3872	645	416025	268336125	25.3969	8.6401
591	349281	206425071	24 8105		646	417816	269586186	25.4165	8.6446
592	350464	207474688	24.3811		647	418609	270840028	25.4362	
			04 0514	0 4014		419904	279097792	25.4558	8.6585
598 594	351649 352836	208527857 209584584	24.3516 24.8721	8.4014 8.4061	649	421901	278859449	25.4755	

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No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
***	400800	074608000	25.4951	8.6624	705	407005	01040001	06 8810	0 0001
850 851	422500 423801	274625000 275894451	25.5147	8.6668	706	497025 498436	850402625 851895816	26.5518 26.5707	8.9001 8.9043
652	425104	277167808	25.5343	8.6713	707	499849	358393243	26.5895	8.9085
658	426409	278445077	25.5539	8.6757	708	501264	354894912	26.6083	8.9127
654	427716	279726264	25.5734	8.6801	709	502681	356400829	26.6271	8.9169
655	429025	281011375	25.5930	8.6845	710	504100	357911000	26.6458	8.9211
656	430336	282300416	25.6125	8.6890	711	505521	859425431	26.6646	8 9253
657	431649	283593898	25.6320	8.6934	712	506944	360944128	26.6833	8.9295
658 659	43:2964 434281	284890312 286191179	25.6515 25.6710	8.6978 8.7022	713 714	508369 509796	362467097 363994344	26.7021	8.9337 8.9378
			ŀ			1		26.7208	
660	435600	287496000	25.6905	8.7066	715	511225	365525875	26,7395	8.9420
661	436921	288804781	25.7099	8.7110	716	512656	867061696	26.7582	8.9462
\$65	438244	290117528	25 7294 25 7488	8.7154	717	514089	368601813	26.7769	8.9503
663 664	439569 440896	291484247	25.7682	8.7198 8.7241	718	515524	870146232	26.7955	8.9545 8.9587
001	1	292754944			719	516961	871694959	26.8142	
665	442225	294079625	25.7876	8.7285	720	518400	373248000	26.8328	8.9628
666	443556 444889	295408296 296740963	25.8070 25.8268	8.7329 8.7373	721 722	519841	374805361 876367048	26.8514	8.9670 8.9711
667 668	446224	298077632	25.8457	8.7416	723	521284 522729	377983067	26.8701 26.8887	8.9752
669	447561	299418309	25.8650		724	524176	379503424	26.9072	8.9794
670	448900	800763000	25.8844	8.7503	725	525625	381078125	26.9258	8.9835
671	450241	802111711	25.9037	8.7547	726	527076	382657176	26.9444	8.9876
672	451584	303464448	25.9230	8.7590		528529	384240583	26.9629	8.9918
673	452929	304821217	25.9422		728	529984	385828352	26.9815	8.9959
674	454276	306182024	25.9615	8.7677	729	531441	387420489	27.0000	9.0000
675	455625	307546875	25.9808	8.7721	780	532900	389017000	27 0185	9,0041
676	456976	308915776	26.0000	8.7764	731	534361	390617891	27.0370	9.0082
677	458329	310288733	26.0192		732	585824	392223168	27.0555	9.0123
678	459684	311665752	26.0384			537289	393832837	27.0740	9.0164
679	461041	313046839	26.0576	8.7893	784	538756	395446904	27.0924	9.0205
680	462400	814482000	26.0768		735	540225	397065375	27.1109	9.0246
6 81	468761	315821241	26.0960		736	541696	398688256	27.1293	9.0287
682	465124	817214568	26.1151	8.8023	787	543169	400315553	27.1477	9.0328
683	466489	318611987	26.1343		738	544644	401947272	27 1662	
684	467856	820013504	26.1584	8.8109	739	546121	403583419	27.1846	9.0410
685	469225	321419125	26.1725	8.8152	740	547600	405221000	27.2029	9.0450
686	470596	322828856	26.1916		741	549801	406869021	27.2213	9.0491
667	471969	324242703	26.2107	8.8237	742	550564	408518488	27.2397	9.0532
6d8 6d9	473844	325660672 327082769	26.2298 26.2488	8.8280 8.8323	748	552049 558536	410172407	27.2580	9.0572
009	474721	341004108	20.2400		744	000000	411830784	27.2764	9.0613
690	476100	328509000	26.2679	8.8366	745	555025	418493625	27.2947	9.0654
691	477481	829989371	26.2869	8.8408	746	556516	415160936	27.3130	
692	478964	331373888	26.8059		747	558009	416832723	27.8313	
593	480249	332812557	26.3249			559504	418508992	27.8496	
694	481636	834255884	26.3439		749	561001	420189749	27.8679	9.0816
695	488025	885702875	26.3629	8.8578		562500	421875000	27.8861	9.0856
696	484416	387158586	26.3818		751	564001	428564751	27.4044	9.0896
697 698	485809	338608878	26.4008			565504	425259008	27.4226	9.0937
698 699	487204 488 6 01	840068892 841582099	26.4197 26.4386	8.8706 8.8748	758 754	567009 568516	426957777 428661064	27.4408 27.4591	9.0977
	į.		1		•	1		1	1
700	490000	343000000	26.4575 26.4764		755	570025	480368875	27.4778 27.4955	
701 702	491401 492804	844472101 845948408	26.4953		756 757	571536 578049	432081216 433798093	27.5186	9.1098
708		347428927	26.5141		758	574564	435519512	27.5818	
704		348913664	26.5830			576081	437245479	27.5500	9.1218

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No.	Squa r e.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
760	577600	438976000	97 5691	9.1258	815	664225	541848875	98 8489	9.3408
761		440711081		9.1298	816	665856	548888496		9.3447
762		442450728		9.1888	817	667489	545888518		9.3485
768		444194947	27 6225	9.1878	818		547848482	28 6007	9.3528
764		445948744	27.6405	9.1418	819		549353259	28.6182	
765		447697125	27.6586	9.1458	820	672400	551868000		9.3599
766		449455096	27.6767	9.1498	821	674041	558887661	28.6581	9.3687
767	588289	451217668 452984882	27.6948	9.1587	822	675684	655412248		9.3675
768 769		454756609	27.7308	9.1577 9.1617	823 824	677829 678976	557441767 559476224		9.8718 9.3751
770	592900	456538000	97 7489	9.1657	825	680625	561515625	28 7998	9.3789
771		458314011 460099648 461889917	27.7669	9.1696	826	683276	568559976		9.3897
772	595984	460099648	27.7849	9.1786	827	688929	565609288	28.7576	9.3865
778 774	597529	461889917	27.8029	9.1775	828	685584	567668559	28.7750	9.3904
774	599076	463684824	27.8209	9.1815	829	687241	569722789	28.7994	9.3940
775	600625	465484875 467288576	27.8388	9.1855	830	688900	571787000	28.8097	9.8978
776		467288576	27.8008	9.1894	881	690561	578856191		9.4016
777 778	603729	469097488 470910952			882 883	692224 698889	575930868 578009537		9 4058
779		472729139		9.2012	884		580093704		9.4129
780	608400	474552000	27.9285	9.2052	885	697225	582182875	28.8964	9.4166
781		476879541		9.2091	886	698896	584277056	28.9137	9.4204
782		478211768	27.9643	9.2130	887	700569	586876258	28.9810	9.4241
783		480048687	27.9821	9.2170	838	702244	588480479		9.4279
784	614656	481890304		9.2209	889	708991	590589719	28.9655	9.4816
785	616225	483736625		9.2248	840	705600	592704000	28.9628	9.4854
786		485587656		9.2287	841	707281	594828821	29.0000	9.4891
787		487443408		9.2326	842	708964	596947686	29.0172	9.4429
789 789		489803872 491169069		9.2865 9.2404	843 844	710649 712836	599077107 601211584		9.4466
790	624100	498089000	28 1069	9.2448	845	714025	603851125	90 0680	9.4541
791	625681	494918671		9.2482	846	715716	605495786	29.0861	9.4578
792	627264	496793088	28.1425	9.2521	847	717409	607645428	29.1088	9.4618
798		498677257		9.2560	848		609800192	29.1204	9.4652
794	630436	500566184	28.1760	9.2599	849	720801	611960049	29.1876	9.4690
795		503459875		9.2688	850	722500	614125000		9.4727
796		504858886		9.2677	851	724201	616295061		9.4764
797		506261578		9.2716	852 853	725904	618470208		9.4801
798 799		508169592 510082899		9.2754 9.2798	854	727609 729816	620650477 628835864		9.4888
800	640000	519000000	28 2848	9.2882	855	731025	625026875	20 2404	9.4918
801		518922401		9.2870	856	782786	627222016	29.2575	9.4949
802	648204	515849608	28.8196	9.2909	857	734449	029492793	29.2746	9.4966
808		517781627		9.2948	858	736164	631 6287 12	29.2916	9.502
804	646416	519718464	28.3549	9.2986	859	787881	638889779	29.8087	9.5060
805		521660195		9.3025	860	739600	636056000		9.5097
806 807		523606616 598887042		9.8068	861 862	741321 743044	638277861		9.5184
808		525557943 527514112		9.3102 9.3140	868	744769	640508988 642785647		9.5171 9.5207
809	654481	529475129		9.8179	864	746496	644972544	29.3989	9.5244
910	656100	531441000	28.4605	9.8217	865	748225	647214625	89.4109	9.5281
811	657721	533411781	28.4781	9.3255	866	749956	649461896	29.4279	9.5317
812		535887328		9.8294	867	751689	651714368	29.4449	9.5851
813	660969	537367797	28.5182	9.3332	868	753424	653971082	29.4618	9.5391
214	662596	539358144	28.5307	9.3370	869	755161	656234909	29.4788	9.5427

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
870	756900	658508000	29.4958	9.5464	925	855625	791453125	30.4138	9.7435
871	758641	860776311	29 5127	9.5501	926	857476	7940:22776		9.7470
872	760384	663054848		9.5537	927	859329	796597983		9.7505
873	762129		29.5466	9.5574	928	861184	799178752		9 7540
874	763876	667627624	29.5635	9.5610	929	863041	801765089	30.4795	9.7575
875	765625	669921875		9.5647	930	864900	804357000		9.7610
876	767376	672221376		9.5688	931	866761	806954491		9.7645
877 878	769129 770884	674526133 676836152		9.5719 9.5756	932 933	868624 870489	809557568 812166237		9.7680 9.7715
879	772641	679151439		9.5792	934	872856	814780504		9.7750
880	774400	681472000	20 6648	9.5828	935	874225	817400975	30.5778	9.7785
881	776161	683797841		9.5865	936	876096	820025856	30.5941	9.7819
882	7779:24	686128968	29.6985	9.5901	937	877969	822656953	30.6105	9.7854
883	779699	688465387		9.5937	9:38	879844	825293672		9.7889
864	781 456	690807104	29.7321	9.5978	939	881721	827936019	30.6481	9.7934
985	788226	693154125		9.6010	940	889600	830584000		9.7959
886 887	784996 786769	695506456 697864103		9.6046 9.6082	941 942	885481 887364	833237621 835896888		9.7995 9.8028
888	788344	700227072		9.6118	943		838561807		9.8063
889	790321	702595369	29.8161	9.6154	944	891186	841282884	30.7246	9.8097
890	792100	704969000	29.8329	9.61 9 0	945	893025	843908625	30.7409	9.8132
891 892	193881	707847971		9.6226	946	894916	846590536		9.8167
892	795664	70973:2288	29.8664	9.6262	947	896809	849278123		9.9201
898 894		712121957	29.8881	9.6298 9.6334	948	898704	851971893		9.8236
		714516984			949	900601	854670849		9.8270
898		716917875		9.6370	950		857375000		9.8305
896 897		719823186 721734278		9.6406 9.6442	951 952	904401 906804	860085351 862801408		9.8339 9.8374
808		724150792		9.6477	953	908209	865523177		9.8408
896		796579699	29.9888	9 6518	954	910116	868250664		9.8443
900	810000	729000000	30,0000	9.6549	955	912025	870983875	30.9031	9.8477
901	811801	781432701	30.0167	9.6585	956	918986	873722816	30.9192	9.8511
902		788870908		9.6620	957		876467493	30.9354	9.8546
903 904		786314327 788768264		9.6656 9.6692	958 959	917764 91 9681	879217912 881974079		9.8580 9.8614
905		741217625		9 6727	960	921600	884736000		9.8648
909		743677416 746142643		9.6763 9.6799	961 962	923521 925444	887503681		9.8683 9.8717
908	824464	748618312		9.6934	963	927369	890277128 893056347	81 0322	9.8751
900		751089429	80.1496	9.6870	964	929296	895841344		9.8785
910	828100	758571000		9.6905	965	931225	898632125	31.0644	9.8819
911				9.6941	966	933156	901428696		9.8854
912		758550528		9.6976	967	935089	904231063		9.8888
918		761048497	80.2159	9.7012	968	987024	907039232		9.8922
914		768551944		9.7047	969	988961	909853209		9.8956
915		766060875 768575296	80.2490	9.7082 9.7118	970	940900 942841	912673000		9.8990 9.9024
916 917		771095213	80 2890	9.7118	971 972	944784	915498611 918330048		9.9058
918		778620682	80.2985	9.7188	973	946729	921167317		9.9092
919		776151559		9.7294	974	948676	924010424		9.9126
280		778688000 781229961	30.8315	9.7259	975	950625	926859375		9.9160
9:1	848241	781229961	30.3480	9.7294	976	952576	929714176	31.2410	9.9194
922	850084	783777448	30.8645	9.7329	977	954529	932574838	31.2570	9 9227
923		796880467	20.0009 20.0004	9.7864 9.7400	978 979	956484 958441	935441352 938313739		9. 9261 9. 9\$
-	853776	788889024	aU.0¥/41	v.7400 €	9191	300441)	20001010101	01.209U	0.04

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No.	Square.	Cube.	Sq. Root.	Cube. Root.	No.	Square.	Cube.	Sq. Root.	Cube Root,
980	960400	941192000	31.3050	9.9329	1035	1071225	1108717875	32.1714	10.1158
981	962861	944076141	81.8209	9.9363	1086	1073298	1111984656	82.1870	10.1186
982	964324		81.8369	9.9896	1037 1038	1075869	1115157658 1118386872	32.2025	10.1218
988 984	966289 968256	952763904	31.3688	9.9430 9.9464	1039	10779521	1121622819	82.2885	10.1288
985	970225			9.9497		1081600	1124864000 1128111 9 21	32.2490	10.1816
986 987	972196 974169		81 4166	9.9531 9.9565	1041 1042		1181366088		
988	976144		31.4825	9.9598	1048	1087849	1134626507	82.2955	10.1418
989	978121	967361669	31.4484	9.9632	1044	1089986	1187898184	82.8110	10.1446
990	980100					1092025	1141166125	82.8265	10.1478
991	982081			9.9699 9.9783	1046 1047	1094116	1144445836 1147780828	82.8419	10.1510
992 993	984064 986049					1098804	1151022592	82.8728	10.1575
994	988036					1100401	1154820649	32.8883	10.1607
995	990025			9.9833 9.9866	1050 1051		1157625000 1160935651		
996 997	992016 994009						1164252608		
998	996004	994011992	81.5911	9 9933	1058	1108809	1167575877	82,4500	10.1786
999	998001				1054		1170905464		
1000	1000000	100000000 1003008001 1006012008 1009027027	31.6228	10.0000	1055	1113025	1174241875 1177588616 1180982198	32.4808	10.1801
1001 1002	1002001	1008008001	31.6886	10.0083	1056 1057	1115186	1177588616	32.4962 99 5115	10.1888
1002	1006009	1009027027	81.6702	10.0100	1058	1119864	1184287112	82.5269	10.1897
1004	1008016	1012048064	31.6860	10.0183	1059	1121481	1187648879	82.5428	10.1929
1005	1010025	1015075125	81.7017	10.0166	1060		1191016000		
1006	1012086	1018108216	81.7175	10.0200	1061 1062		1194389981 1197770328		
1007 1008	1016064	1021147848 1024192512	81.7490	10.0266			1201157047		
1009	1018081	1027243729	31.7648	10.0299	1064		1204550144		
1010	1020100	1030301000	31.7805	10.0332	1065	1134225	1207949625	32.6848	10.2121
1011 1012	1022121	1033364331 1036433728	81.7962	10.0805	1066 1067	1130300	1211855496 1214767768	82.0497 89.8880	10.2158
1013	1026169	1089509197	31.8277	10.0481	1068		1218186432		
1014		1042590744	31.8434	10.0465	1069		1221611509		
1015		1045678375			1070		1225043000		
1016		1048772096			1071 1072		1228480911 1231925248		
1017 1018		1051871913 1054977832	31.9061	10.0596	1078	1151329	1235376017	32.7567	10.2876
1019	1038361	1058089859	81.9218	10.0629	1074	1158476	1238833224	32.7719	10.2406
1020	1040400	1061208000 1064332261 1067462648	81.9374	10.0662	1075	1155625	1242296875 1245766976 1249248588 1252726559	82.7872	10.2440
1021 1022	1042441	1064332261 1087489849	31.9031	10.0095	1076 1077	1157776 1150090	1240700976	39 8177	10.2472
1023	1046529	1070599167	31.9844	10.0761	1078	1162084	1252726552	82.8329	10.2585
1024	1048576	1078741824	32.0000	10.0794	1079	1164241	1256216089	82.8481	10.2567
1025		1076890625			1080		1259712000		
1026 1027	1052676	1080045576 1088206688	32.0312	10.0809	1081 1082	1170794	1263214441 1266723368	89 8089	10.2680
1027	1056784	1086873952	82.0624	10.0925	1088	1172889	1270238787	32,9090	10.2693
1029	1058841	1089547889	32.0780	10.0957	1084	1175056	1278760704	82.9242	10.2725
1080	1060900	1092727000	82.0936	10.0990	1085	1177225	1277289125	82.9898	10.2757
1031 1032	1062961	1095912791 1099104768	32.1092 32.1949	10.1028	1086 1087	1181560	1280824056 1284365503	89 0607	10.2788 10 9990
1033	1067089	1102302937	32, 1403	10.1088	1088	1183744	1287918472 1291467969	32.9848	10.2851
1034	1069156	1105507304	132.1559	10.1121	1089	1185921	1291467969	38.0000	10.2883

25 97 OF C W

No.	Square.	Cube.	Sq. Root,	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
1090 1091 1092	1190281	1295029000 1298596571 1302170688	33.0303	10.2946	1145 1146	1813316	1501123625 1505060136	33.8526	10.4647
1098 1094	1194649	1205751857 1309338584	33.0606	10.3009	1147 1148 1149	1317904	1509003523 1512958792 1516910949	33.8821	10.4708
1095 1096	1201216	1312932375 1316532736	33, 1059	10.3103	1150 1151	1322500 1324801	1529875000 1524845951	33.9116 33.9264	10.4769 10.4799
1097 1098 1099	1203409 1205604	1320139673 1328753192 1327873299	33.1210 33.1361	10.3134 10.3165	1152 1158	1329409	1524845951 1528828808 1532808577 1536800264	38.9559	10.4860
1100	1210000	1331000000	33 .1662	10.3228	1154 1155	1384025	1540798875	33.9853	10.4921
1101 1102 1103	1214404	1334633301 1338273208 1341919727	33.1964	10.3290	1156 1157 1158	1838649	1544804416 1548816893 1552836812	34.0147	10.4981
1104 1105	1218816	1345572864 1349232625	33.2264	10.3353	1159	1343281	1556862679	31.0441	10.5042
1106 1107	1223286 1225449	1352899016 1356572043	83.2566 33.2716	10.8415 10.8447	1160 1161 1162	1347921 1850244	1560896000 1564936281 1568983528	34.0735 34.0881	10.5102 10.5132
1108 1109	1227664	1360251712 1363938029	33.2866	10.3478	1168 1164		1578037747 1577098944		
1110 1111 1112	1234321	1867631000 1871830631 1875036928	33.8817	10.3571	1165 1166 1167	1859556	1581167125 1585242296 1589824463	84.1467	10.5253
1113	1238769	1378749897 1382469544	33.3617	10.3638	1168 1169	1364224	1593418632 1597509809	34.1760	10.5313
1115 1116	1245456	1386195875 1389928896	33.4066	10.3726	1170 1171	1371241	1601618000 1605723211	34.2199	10.5408
1117 1118 1119	1249924	1393668618 1397415032 1401168159	33.4365	10.3788	1172 1178 1174	1375929	1609840448 1618964717 1618096024	34.2491	10.5463
11 20 1121	1254400 1256641	1404928000 1408694561	88.4664 88.4818	10.3850 10.3881	1175 1176		1622234375 1626379776		
1122 1128 1124	1258884 1261129	1412467848 1416247867 1420084624	83.4968 83.5112	10.3912 10.3943	1177 1178	1385829 1387684	1630532233 1634691752 1638858339	34.3074 34.3220	10.5583 10.5612
1125	1265625	1423828125	33 . 54 10	10.4004	1179 1180	1392400	1643032000	34.8511	10.5672
1126 1127 1138	1270129	1427628376 1481435888 1485249152	33.5708	10.4066	1181 1182 1183	1897124	1647212741 1651400568 1655595487	34.3802	
1129	1274641	1439069689 1442897000	33.6006	10.4127	1184 1185	1401856	1659797504 1664006625	34.4093	10.5791
1131 1132	1279161 1281424	1446781091 1450571968 1454419687	33.6303 33.6452	10.4189 10.4219	1186 1187	1406596 1408969	1668222856 1672446203	34 . 4384 34 . 4529	10.5851 10.5881
1188 1134	1285956	1458274104	83.6749	10.4281	1188 1189	1413721	1676676672 1680914269	34.4819	10.594 0
1135 1136 1137	1290496	1462185875 1466003456 1469878858	88.7046	10.4342	1190 1191 1192	1418481	1685159000 1689410871 1693669888	34.5109	10,6000
1138 1139	1295044	1478760072 1477648619	83.7342	10.4404	1193 1194	1423249	1697936057 1702209384	34.5398	10.6059
1140 1141	1901001	1481544000 1485446221	99 77 9 7	110 <i>41</i> 05 I	1195 1196	1430416	1706489875 1710777536	34.5832	10.6148
1142 1143 1144	1304164 1306449	1489855288 1498271207 1497193984	83.7935 83.8088	10.4525 10.4556	1197 1198 1199	1435204	1715072373 1719374392 1723683599	34.6121	10.620

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Squ ar e.	Cube.	Sq. Root.	Cube Root.
1200	1440000	1728000000	84 6410	10 6968	 1256	1575025	1976656375	85 4260	10.7865
1201		1782323001			1256		1981385216		
1203	1444804	1786654408	34.6699	10.6325	1257		1966121593		
1208	1447209	1740992427	34.6848	10.6854	1258	1582564	1990865512	85.4688	10.7961
1204	1449616	1740992427 1745887664	84.6987	10.6884	1259	1585081	1996616979	85.4824	10. 7980
1206	1452025	1749690125	84.7181	10.6418	1260	1597600	2000376000	85.4965	10.8008
1906	1409480	1754049816	34.72/0	10.0448	1261 1262	1500844	2005142581	33.51U0	10.0007
1207 1208	1400049	1758416748 1762790912	04. (919	10.0472	1268	1808180	2009916728 2014898447	98 8997	10.8000
1209		1767172329			1264	1597696	2019487744	85.5528	10.8122
1210	1464100	1771561000	84.7851	10.6560	1265		2024284625		
1211	1466521	1775056031	84 7994	10 8590	1266	1602756	2029069096	35.5609	10.817 9
1212	1468944	1780 36 0128 1784770697	84.8138	10.6619	1267	1605289	2033901163 2038720832	35.5949	10 8208
1213	1471869	1784770697	84.8281	10.6648	1266	1607824	2038720832	85.6090	10.8286
1214	1478796	1789186344	34.8425	10.6678	1269		2043548109		
1215		1798618875			1270	1612900	2048888000	35.6871	10.8298
1216		1798045696			1271		2058225511		
1217	1481089	1802485318			1272		2058075648		
1218		1806982232			1278	1620529	2062933417	35.6791	10 8378
1219		1811886459		i l	1274		2067798824		
1220	1488400	1815848000 1820816861	84.9285	10.6858	1975	1625625	2072671875	85.7071	10.8485
1221	1490841	1820816861	84.9428	10.6882	1276	1628176	2077552576 2082440988	85.7211	10.8468
1222		1824798048			1277	1680729	2002140933	35.7851	10.8492
1228		1829276567			1278 1279	1898941	2097836952 2092240689	95 7491	10.0020
1224		1888767424					l .	Į l	
1225	1500625	1838965625	35.0000	10.6999	1280		2097152000		
1226		1842771176			1281	1640961	2102071041	35.7911	10.8605
1227	1506529	1847284088	85.0286	10.7057	1282 1283	1048524	21069 9776 8 2111982187	85.8000	10.8688
1228 1229		1851804852 1856881989			1284	1010009	2116874804	25 2000	10.0001
						ĺ		1	
12:30		1860867000			1288		2121824125		
1231		1865409391			1286		2126781656		
12 3 2 12 3 3		1869959168 1874516887	35.0999	10.7202	1297 1288		2181746903 2186719672		
1284		1879080904			1289	1661521	2141700569	85.9026	10.8881
1235	1505006	1888652875	9K 149A	10 7980	1290	1884100	9146660000	85 Q166	10 8880
1236	1527696	1888232256	35 1568	10.7318	1291	1666681	2151685171	85 9805	10.8887
1237	1590169	1892819058	85,1710	10.7847	1292	1669264	2150689088	35.9444	10.8915
1238	1582644	1897418272	85.1852	10.7876	1208	1671849	2146699000 2151685171 2156689088 2161700757	35.9588	10.8948
1289	1583121	1902014919	85.1994	10.7405	1294	1674486	2166720184	35.9722	10.8971
1240		1906624000			1295	1677025	2171747875	35.9661	10.8999
1241		1911240521	35.2278	10.7468	1296	1679616	2176782886	36.0000	10.9027
1242		1915864488			1297	1682209	2181825078	36.0189	10.9055
1243		1920495907			1298	1684804	2186875592	36.0278	10.9083
1244		1925184784			1299	l .	2191938899		
1245	1550025	1929781125	85.2846	10.7578	1800	1690000	2197000000	86.0555	10.9189
1246	1552516	1984434936	35.2987	10.7607	1801		2202078901		
1247		1939096223			1802		2207155608		
1248	1557504	1943764992	35.3270	10.7664	1808		2212245127		
1249		1948441249			1804	1700416	2217842464	36.1109	10.9251
1250	1562500	1958125000 1957816251 1962515008 1967221277	35.3558	10,7722	1805	1703025	2222447625	36.1248	10.9279
1251	1565001	1957816251	85.8695	10.7750	1806	1705636	2227560616	36.1886	10.9807
1252	1567504	1962515008	35.3836	10.7779	1307	1708249	2232681448	86.1525	10.9885
1258	1570009	1907221277	35.8977	10 7508	1808	1710864	2237810112	00.1008	10.9868
1264	10/2016	1971935064	<u>აი.4119</u>	10.78871	1908	1718481	2242946629	100.1601	110.898

Zo.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
:310		2248091000			1365		2543302125	86.9459	11.0929
:311	1718721	2258248231	36 2077	10.9446	1866	1865956	2548895896	36.9594	11.0956
1912 1913		2258408328 2268571297			1867 1868		2554497868 2560108082		
1214		2268747144			1869		2565726409		
:815	1729225	2273930975	36.2629	10.9557	1370	1876900	2571352000	87.0185	11.1064
1316 1317	1731856	2279122496	36.2767	10.9585	1371 1872	1979641	2576987811 2582630818	87.0270 x7.0408	11.1091
1318	1737124	2294822013 2289529482	86.8048	10.9640	1878	1885129	2588282117	87.0540	11.1145
1319	1789761	2294744759	86.8180	10.9668	1874	1987876	2598941694	37.0675	11.1172
1320	1742400	2299968000	36.8818	10.9696	1875	1890625	2599609875	87.0810	11.1199
1321 1322		2305199161 2810488248			1876 1877		2605285376 2610969638	87 0945 97 1090	11.1226
1325		2815685267			1378	1898884	2616662152	37.1214	11.1280
1334	1752976	2820940224	86.3868	10.9807	1379	1901641	3622862989	37.1849	11.1307
1325	1755625	2826208125	86.4005	10.9884	1880		2628072000		
1326	1760020	2381478976 2836752783	30.4140 36.4990	10.9808	1881 1882		2688789841 2689514968	37 1753	11.1361
32	1768584	2342039552	86.4417	10.9917	1388	1912689	2645248887	37.1887	11.1414
133	1766:341	2347834289	86.4555	10.9945	1884	1915456	2650991104	87.2021	11.1441
1336	1768900	2852687000	36.4693	10.9978	1885	1918225	2656741625	87,2156	11.1468
1331 133		2857947691 2868266868	36.4829 88.4048	11.0000	1886 1887		2662500456 2668267608		
183		2368598087			1888	1926544	2674048072		
133	1779556	2373927704	86.5240	11.0088	1889	1929321	2679826869	87.2698	11.1575
131	1782225	2879270875	86.5377	11.0110	1890		2685619000		
183 183	1784890 1787569	2384621056	86.5650	11.0135	1391 1392	1934881	2691413471 2697228288	87.8095	11.1629
138	8 1790244	2889279753 2895346472	86.5787	11 0193	1393	1940449	2697228288	87.8229	11.1682
133	9 1792921	2400721219	86.5928	11.0220	1894	1948236	2708870984	87.8368	11.1709
134	0 1795600	2406104000	36.6060	11.0247	1395	1946025	2714704875	87.8497	11.1736
134 134	1 1798281	2411494821 2416893688	86.6197 86 6838		1896 1897		27205471 8 6 2726397778		
134	3 1808649	24:22300607	86.6469	11.0830	1398	1954404	2732256792	87.3898	11.1816
134	4 1806886	2427715584	36.6606	11.0357	1899	1957201	2788194199	87.4082	11.1842
134	5 1809025	2433138625	86.6742	11.0384	1400		2744000000		
134 134	6 1811710 7 1814409	2438569786 2444008923	86.7015	11.0412	1402	1965604	2749884201 2755776808	87.4438	11.1896
134	8 1817104	9444008923 2449456192	86.7151	11.0466	1403	1968409	2761677827	37.4566	11.1949
134	181 93 01	9454911549	36.7287	11.0494	1404	1971216 	2767587264	87.4700	11.1975
13	0 1822500	2460875000	86.7428	11.0521	1405		2778505125	37.4833	11.2002
132		2465846551 2471826208			1406 1407		2779481416 2785866148		
13	3 1880009	2476813977	86.7881	11.0608	1408	1982464	2791809312	87.5288	11.2082
133	1835316	2482309864	86.7967	11.0680	1409	1985281	2797260929	87.5866	11.2108
13	5 1836025	2487818875	86.8108	11.0657	1410	1988100	2803291000	37.5500	11.2185
14	1041440	2493826016 2498846298	28 8275	111 0219	1411 1419	1993744	2809189581 2815166528	87.5766	11.2101
13	N 1844164	12504874712	1106.001	111.0789	1418	1996569	2821151997	87.5899	11.2214
13	1846881	2509911279	86.8646	11.0766	1414	1999396	2827145944	87.6082	11.2240
13	1849600	2515456000	36.8782	11.0798	1415		2833148375	87.6165	11.2587
13 13	1000044	2521008881 2526569928	138.9053	111.0847	1416 1417	2007889	2839159296 2845178718		
13	1857769	2582189147 2587716544	86.9188	11.0875	1418	2010724	2851206682	87.6568	11.2346
13	1860496	2587716544	86.9324	111.0902	1419	2018561	2857243059	37.6696	11.2872

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
1420	2016400	2863288000	87.6829	11 2399	1475	2175625	8209046875 8215578176 8222118383	38.4057	11.8882
1421	2019341	2869341461	37.6962	11.2425	1476	2178576	3215578176	38,4187	11.3858
1422	20:22084	2875403448	87.7094	11.2452	1477	2181529	3222118333	38,4318	11.3883
1428	2024929	2881478967	37.7227	11.2478	1478	2184484	3228667352	38.4448	11.3909
1424		2887553024	37.7359	11.2505	1479	2187441	3235225239	38.4578	11.3935
1425	2030625	2893640625	37.7492	11.2531	1480		3241792000		
1436	2033470	2899736776 2905841483 2911954752	37.7024	11.2007	1481 1482	2198801	8248367641	90.4000 90 4040	11.8980
1427 1428	9030329	2000041400	97 7880	11 9810	1483	9100024	3254952168 3261545587	98 5007	11 4097
1429	2042041	2918076589	37.8021	11.2636	1484	2202256	8268147904	38.5227	11.4063
1430	2044900	2924207000 2930345991	37.8153	11.2662	1485		3274759125		
1481	2047761	2930345991	37.8286	11.2689	1486		3281879256		
1482	2050624	2936493568	37.8418	11.2715	1487		3288008303		
1433		2942649787			1488		3294646272		
1484	1	2948814504			1489		8301298169		
1485	2059225	2954987875 2961169856 2967360453	87.8814	11.2793	1490	2220100	8807949000 3814618771 3321287488 3827970157	38.6005	11.4216
1486	2062096	2961169856	37.8946	11.2820	1491	2223081	3314613771	38.6185	11.4242
1487	2064969	2967360453	37.9078	11.2846	1492	2226064	3321287488	38.6264	11.4268
1438 1489	2001044	2973559672 2979767519	91,9210	11.2072	1493 1494	2229049 2232036	3827970157 3834661784	38.6528	11.4298 11.4319
1440	2073600	2985984000	37 9478	11 2024	1495	2285025	3341862375	88 6652	11 4844
1441		2992209121			1496		3348071936		
1442	2079364	2998442888	37.9737	11.2977	1497		3354790478		
1448	2082249	3004685307	37.9868	11.3003	1498	2244004	8361517992	38.7040	11.4421
1444	2085136	3010936884	38.0000	11.3029	1499	2247001	3368254499	88.7169	11.4446
1445	2088025	3017196125	38.0132	11.3055	1500	2250000	3375000000 3381754501	38.7298	11.4471
1446	2090916	3023464536	38.0263	11.8081	1501	2253001	3381754501	88.7427	11.4497
1447	2098809	3029741623	30.0395	11.810	1502	22600004	3388518008 3395290527	00.1000	11.4022
1448 1449		3036027892 3042321849			1503 1504		8402072064		
1450	2102500	3048625000	38 0789	11.8185	1505	2265025	8406862625	38.7948	11.4598
1451	2105401	2054026851	28 0920	11 3211	1506		3415662216		
1452	2108804	3061257408	38,1051	11.3237	1507	2271049	8422470843	38.8201	11.4649
1458	2111209	3061257408 3067586677 3073924664	38.1182	11.3263	1508	2274064	8429288512 8436115229	38.8330	11.4675
1454	2114116	3073924664	88.1814	11.3289	1509	2277081	8436115229	38.8458	11.4700
1455	2117025	3080271875	38.1445	11.3315	1510	2280100	8442951000 8449795831	38.8587	11.4725
1456		3086626816			1511	2288121	8449795831	88.8716	11.4751
1457		3092990993			1512		8456649728		
1458 1459		3099363912 3105745579			1518 1514		8468512697 8470884744		
1460	2181600	3112136000	38,2099	11.8445	1515	2295225	3477265875	38,9280	11.4859
1461	2134521	3118585181	38.2230	11.8471	1516	2298256	8484156096	38 9358	11.4877
1462	2137444	3118585181 3124943128	38.2361	11.8496	1517	2301289	8491055418	38.9487	11.4902
1463	2140369	3131359847	38.2492	11.3522	1518	2304324	8491055418 8497968882	88.9615	11.4927
1464	2143296	3137785344	38.2623	11.3548	1519	2307361	3504881859	88.9744	11.4958
1465		3144219625			1520		3511808000		
1466		3150662696			1521		8518743761 8525688648		
1467		3157114568			1522 1523		3582642667		
1468 1469	2157961	31635752 8 2 3170044709	88.8275	11.3677	1523	2822576	3582042007 8589605824	89.0384	11.5079
 1470	2160900	8176529000	88.8406	11.3703	1525	2825625	8546578125	89.0512	11.5104
1471	2163841	3176523000 3183010111	38, 3536	11.3729	1526	2328676	8546578125 8553559576	89.0640	11,5129
1472	2166784	3189506048	38.3667	11.8755	1527	2331729	18560550183	139.0768	111.5154
1473	2169729	3196010817	38.3797	11.3780	1528	2884784	3567549952	 89.0696	11.5179
1474	2172676	3202524424	38.3927	11.3806	1529	2337841	8574558889	89.1024	11.520

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
 1530	2340900	8581577000	39,1152	11.5230	1565	2449225	8833087125	39.5601	11.6102
1531		8588604291			1566		8840889496		
1512		3595640768			1567		3847751263		
1533		3602686437			1568		3855123432		
1534	2353156	3609741304	39.1663	11.5830	1569	2461761	3862503009	89.6106	11.6200
1535		3616805875			1570		3869893000		
1536		8623878656			1571		3877292411		
1337		3630961153			1572		3884701248		
1553		3638052872			1573		3892119517		
1539	2368521	8 64 5153819	39.2301	11.5455	1574	2477476	3899547224	89.6787	11.6824
1540		3652264000			1575		3906984375		
1541		3659 8 83421			1576		8914480976		
1512		3666512088			1577		3921887033		
1543		3673650007			1578		3929352552		
1544	2383930	3680797184	39.2938	11.0080	1579	2495241	3936827539	39.7300	11.0447
1543	2387025	3687958625	39.3065	11.5605	1580		3944312000		
1346		3695119336			1581	2499561	8651805941	39.7618	11.6496
1547		3702294323			1582		3959309368		
1348		3709478592			1583		3966822287		
1549	2 3994 01	3716672149	39.3573	11.5705	1584	2509056	3974344704	39,7995	11.6570
1350		3723875000			1585		3981876625		
1551		3731087151			1586		8989418056		
1552		3738309608			1587		3996969003		
1553		3745539377			1588		400 1529472		
1554	2414916	3752779464	39.4208	11.5829	1589	2524921	401:2099469	39.8628	11.6692
1555		3760028875			1590		4019679000		
:556		3767287616			1591		4027268071		
:557		3774555693			1592		4034866688		
1558		3781833112			1593		4012174857		
1539	2430481	3789119879	39.48#2	11.5953	1594	2540836	4050092584	39.9249	11.6814
1560		3796416000			1595		4057719875		
1561		3803721481			1596		4065356736		
1562		3811036328			1597		4073003178		
1563		3818360547			1598		4080659192		
1564	2446096	3825694144	39.5474	11.6077	1599	2556801	4088324799	59.9875	11.6936
	1	l	1	1	1600	2560000	4096000000	40.0000	11.6961

SQUARES AND CUBES OF DECIMALS.

No.	Square.	Cube.	No.	Square.	Cube.	No.	Square.	Cube.
.1	.01 .04	.001	.01	.0001	.000 001	.001	.00 00 01 .00 00 04	.000 000 001
.2 8 .4 .5	.09 .16 .25	.027 .064 .125	.08 .04 .05	.0025	.000 027 .000 064 .000 125	.003 .004 .005	.00 00 09 .00 00 16 .00 00 25	.000 000 027 .000 000 064 .000 000 125
.6 7. 8.	.86 .49 .64	.216 .848 .512	.06 .07 .08	.0049 .0064	.000 216 .000 343 .000 512	.006 .007 .008	.00 00 86 .00 00 49 .00 00 64	.000 000 216 .000 000 343 .000 000 513
.9 1.0 1.2	.81 1.00 1.44	.729 1.000 1.728	.09 .10 .12	.0081 .0100 .0144	.000 729 .001 000 .001 728	.009 .010 .012	.00 00 81 .00 01 00 .00 01 44	.000 000 729 .000 001 000 .000 001 728

Note that the square has twice as many decimal places, and the cube three ______ times as many decimal places, as the root.

FIFTH ROOTS AND FIFTH POWERS. (Abridged from Trautwine.)

	~		<u> </u>				<u> </u>		
No. or Root.	1	9 4		No. or Root.		5 ti		ند خ ا	ĺ
2.0	Power.	20	Power.	20	Power.	28	Power.	3.8	Power.
\$ ₹	10	No or Root.	2002.	22	2002.	No. or Root.		No. of Root.	2001.
	000010		400 410		00000	24.0	40000000	40	103,100000
.10	.000010	3.7	693.440	9.8	9039:2	21.8	4923597	40	102400000
.15	.000075	8.8	792.352	9.9	95099	22.0	5153632	41	115856201
.20	.000320	3 9	902.242	10.0	100000	22.2	5392186	42	130691232
.25	.000977	4.0	1024.00	10.2	110408	22.4	5639493	48	147008443
.30	.002430	4.1	1158.56	10.4	121665	22.6	5895793	44	164916224
. 35	.005252	4.2	1306.91	10.6	133823	22.8	6161327	45	184528125
.40	.010240	4.3	1470.08	10.8	146933	23.0	6436343	46	205962976
.45	.018453	4.4	1649.16	11.0	161051	$\frac{23.2}{23.4}$	6721093	47 48	229345007
.50	.031250	4 5	1845.28	11.2	176234		7015834		254803968
.55	.050328	4.6	2059.63	11.4	192541	23.6	7320825 7636332	49	282475249
.00	.077760	4.7	2293.45	11.6	210034	23.8		50	312500000
.00	.116029	4.8	2548.01	11.8	228776 248832	24.0	796:1624	51	345025251
.60 .65 .70 .75 .80 .85	168070	4.9	2824.75	12.0		24.2	8299976 8648666	52 53	380204032
.45	,237305	5.0	8125.00	12.2	270271	24.4			418195498
.80	.327680	5.1	3450.25	12.4	293163 817580	24.6	9008978 9381200	54 55	459165024
.00	.443705	5.2	3802 04 4181.95	12.6 12.8	343597	24.8 25.0	9765625	56	503284375
.95	.590490			13.0	871298	25.2	10162550	57	550781776
1.00	.778781	5.4	4591.65	13.0 13.2	400746	25.4	10572278	58	601692057 656356768
	1.00000	5.5 5.6	5032.84 5507.52	13.4	432040	25.6	10995116	59	
1.05	1.27628 1.61051	5.7	6016.92	13 6	465259	25.8	11431377	60	714924299
	2.01135	5.8	6563.57	13.8	500490	26.0	11881376	61	844596801
1.15	2.48832	5.9	7149.24	14.0	537824	26.2	12345437	62	916132832
1.25	3.05178	6.0	7776.00	14.2	577358	26.4	12823886	63	992486548
1.30	3.71298	6.1	8445.96	14.4	619174	26.6	18317055	64	1073741824
1.35	4.48403	6.2	9161 33	14 6	663383	26.8	13825281	65	1160290625
1.40	5.37824	6.3	9924.37	14.8	710082	27.0	14348907	66	1252332576
1.45	6.40973	6 4	10737	15.0	759375	27.2	14888280	67	1350125107
1.50	7.59375	6.5	11603	15 2	811368	27.4	15443752	68	1453933568
1.55	8.94661	6.6	125:3	15.4	866171	27.6	16015681	69	1564031349
1.55 1.60	10.4858	6.7	13501	15.6	923896	27.8	16604430	70	1680700000
1.65	12.2298	6.8	14539	15.8	984658	28.0	17210368	71	1804229351
1.70	14.1986	6.9	15640	16.0	1048576	28.2	17833868	72	1934917632
1.75	16.4131	70	16807	16.2	1115771	28.4	18475309	73	2073071593
1.80	18.8957	7.1	18012	16.4	1186367	28.6	19135075	74	2219006624
1.85	21.6700	7.1 7.2	19349	16.6		28.8	19813557	75	2373046875
1.90	24.7610	7.3	20731	16.8	1338278	29.0	20511149	76	2535525376
1.95	28.1951	7.4	22190	17.0	1419857	29.2	21228253	77 78	2706784157
2.00	32.0000	7.5	23730	17.2	1505366	29.4	21965275	78	2887174368
2.05	36.2051	7.5 7.6	25855	17.4	1594947	29.6	2272 2628	79	3077056399
2.10	40 8410	7.7	27068	17.6	1688742	29 8	23500728	80	3276800000
2.15	45.9401	7.8	28872	17.8	1786899	30.0	24300000	81	3486784401
2 :0	51.5363	7.9	30771	18.0	1889568	30.5	26393634	82	3707398482
2.25	57.6650	8.0	32768	18.2	1996903	31.0	28629151	83	3939040643
2.30	64.3634	8.1	34868	18.4	2109061	31.5	31013642	84	4182119424
2.35	71.6703	8.2	87074	18.6	2226203	32.0	83554432	85	4437058125
\$.40	79.6262	8.3	39390	18.8	2348498	82.5	36259082	86	4704270176
2.45	88.2735	8.4	41821	19.0	2476099	88.0	89185398	87	4984209207
2.50	97.6562	8.5	44371	19.2	2609193	33.5	42191410	88	5277819168
2.55	107.820	8.6	47048	19.4	2747949	34.0	45485424	89	5584059449
2.60	118.814	8.7	49842	19.6	2892547	84.5	48875980	90	5904900000
2.70	148.489	8.8	52778	19.8	3043168	35.0	52521875	91	6240321451
2.80	172.104	8.9	55841	20.0	3200000	85.5	56882167	92	6590815282
2.90	205.111	9.0	59049	20.2	3863232	36.0	60466176	98	6956883693
8.00	248 000	9.1	62403	20.4	3583059	86.5	64783487	94	7339040224
8.10	286.292	9.2	65908	20.6	3709677	37.0	69843957	95	7731809375
8.20	385.544	9.3	69569	20.8	8593289	37.5	74157715	96	8153726976
3.30	891.854	9.4	73390	21.0	4084101	88.0	79235168	97	8587840257
8.40	454.354	9.5	77378	21.2	4282322	38.5	84587005	98	9039207968
3.50 8.60	525.219	9.6	8:537	21.4	4488166	89.0	90224199	99	9509900499
9.00	804.662	9.7	85678	21.6	4701860	89.5	96158012	•	1

	CIRC	umpe	RE:	NCE!	BAND	AREAS	OF	CIRCI	ES.
Diam	Circum	.] Area		Diam.	Circum.	Area.	Diam.	Circum.	Alea.
	3.1414	0.7	854	65	204.20	8816.81	129	405.27	13069.81
1 2 3 4 5	6.283	ad 12 1	41 ISB	66	207.84	3421.19	180	408.41	18278.23
i	9.4248	2 7 0	DOU	67	210.49	3525.65	131	411.55	13478.22
4	12.5664	. 195	564.	68 69	218.68 216.77	8631.68 8789.28	132 133	414.69 417.88	13684 78 13892.01
5	15.7080	19.0	74	70	219.91	8848.45	134	420.97	14102 61
- 6 1	18.850	19.6 28 2 38.4	35	71	223.05	8959.19	185	424.12	14818.88
7 8	21.991 25.183	i SU.Z		72	226.19	4071.50	136	427.26	14526.72
6	28.274	42 5	7	73	229.34 232.48	4185.89 4800.84	137	480.40	14741.14
10	81.416	78.54 95.03		74 75	235.62	4417.86	138 139	438.54 436.68	14957.12 15174.68
11 1	34.558 37.699	95.03 113.10 132.73 153.94 176.71	~ •	76	238.76	4536.46	140	439.82	15898.80
12 1	37.699	132 73	3	77	241.90	4656.63	141	442.96	15614.50
13	40.841 43.982	153.94		78	245.04	4778.86	142	446.11	15836.77
11	47.124			79 80	248.19 251.33	4901.67 5026.55	143 144	449.25 452.89	16060.61 16286.02
is l	50.265	201.06	•	81	254.47	5153.00	145	455.58	16518.90
16 17	53.407	226.98 254.47	- 4	82	257.61	5281.02	146	458.67	16741.55
18	56.549	983 53	1	83	260.75	5410.61	147	461.81	16971.67
19	59. 690 62.832	044 1B	- 1	84	263.89	5541.77	148	464.96	17208.36
21	65.973	R10.30	- 1	85 86	267.04 270.18	5674 50 5868.60	149 150	468.10 471.24	17486 62 17671 46
22	69.115		- 1	87	273.32	5914.68	151	474.88	17907.86
23	72.257	415.48 452.89	- 1	88	276.46	6082.12	152	477.52	18145.84
24	75.898 78.540	490.87	- 1	89	279.60	6221.14	158	480.66	18385.39
n n n n n n n n n	81.681	530.93	-	90 91	282.74 285.88	6361.73 6503.88	154 155	483.81 486.95	18696.50 18869.19
27	84.823	572.56 615.25	- 1	92	289.03	6647 61	156	490.09	19118.45
28	87.963	615.25		93	292.17	6647.61 6792.91 6989.78	157	498.23	19359.28
20	91.106	660.52 706.86		94	295.81	6989.78	158	496.87	19606.68
30 31	94_248	754.77		95	298.45	7088.22	159	499.51	19855.65
12				96	301.59 304.78	7288.23 7889.81	160 161	502.65 505.80	20106.19 20358.81
23	1103.67	855.30 907.92	•	97 98	307.88	7549.96	162	508.94	20611.99
8	106.81	907.92	1	99	311.02	7697.69	168	512.66	20867.24
¥	5 109.96 6 118.10 67 116.24 88 119.38 89 122.52 10 125.66	962.11 1017.88	110	10	314.16	7853.98	164	515.22	21124.07
	6 1118.10 7 1116.24	1075.21	1	01	817.30 320.44	8011.85	165 166	518.86 521.50	21382.46 21642.43
1	8 1119.38	1134.11	1	02	323.58	8171.28 8332.29	167	534.65	21998 97
	122.52	1194.59	16	03	326.78	8494.67	168	527.79	22167 08
	19 125.66 41 128.81	1256.64	10	5	.329.87	8659.01	169	530.93	22481.76
	42 131.95	1820.25 1885.44	10	166 J	.333.01 .336.15	8824.73	170 171	534.07 537.21	22698.01 22965.83
	43 195 00	1452.20	10	7	389.29	8992.02 9160.88	172	540.85	23235.22
	44 138.23	1520.53	10	3 1	342.43	9331.32	173	543.50	28506.18
9		1590.43	11	ő	345.58	9508.32	174	546.64	23778.71
- 7	65 144.51 17 147.65	1661 .90	11	. 2 1	348.72	9676.89 9852.03	175	549.78	24052.82
4	150 Sn	1734.94 1809.56	11	2 1	351.86 355.00	10028.75	176 177	552.92 556.06	24828.49 24605.74
- 4	D 1158 to 1	1885.74	11	3 1	358.14	10207.03	178	559.20	24884.56
5	0 157.08 1 160.22	1963.50	1 11	5 1	361.28	10886 89	179	562.85	25164.94
5		2042.82	11	6 1	364.42	10568.32	180	565.49	25446 90
5	3 166 50	2128.72 2016.118	11	7	367.57 370.71	10751.32 10935.88	181 182	568.68 571.77	25730.43 26015.53
5.	169.85	290.22	11	55 1	373.85	11122.02	183	574.91	26302.20
5. 5. 5.	172.70	2875.8B	112	40 1	376.99	11309.78	184	578.05	26590.44
2	175.93	2463.01	4.0	27 1	380.13	11499.01	185	581.19	26860.25
5	7 179.07 8 182.21 185.35	2551.76	-	, , ,	383.27 386.42	11689.87 11882.29	186 187	584.84 587.48	27171.68 27464.59
5	185.34	2642.08 2733.97	1 1:	23	389.56	12076.28	188	590.62	27759.11
•	188.50	2827.43	3	24 125	392.70	12271.85	189	598.76	28655.21
	191.64	2922.47	1	126	395.84	12468.98	190	596.90	28352 87
,	185.35 188.50 1188.50 191.64 52 1194.78 187.92	8019.07		127	898.98 402.12	12667.69 12867.96	191 192	603.19	28652.11 2895
	64 197.92 64 1981.06	8117.25 8216.99	1	128	1 402.12	1 12001.90	132	1 000.19	1 NORGE
•		0510							

Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
193	606.33	29255.30	260	816.81	53092.92	327	1027.30	83981.84
194	609.47	29559.25	261	819.96	53502.11	328	1080.44	84496.28
195	612.61	29864.77	262	823.10	53912.87	329	1033.58	85012.28
196	615.75	30171.86 30480.52	263 264	826.24 829.38	54325.21 54739.11	880	1036.73 1039.87	85529.86 86049.01
197 198	618.89	30790.75	265	832.52	55154.59	331 332	1043.01	86569.73
199	625.18	81103.55	266	835.66	55571.63	333	1046.15	87092.02
200	628.32	31415.93	267	838.81	55990.25	334	1049.29	87615.88
201	631.46 634.60	81730.87 82047.89	268 269	841.95 845.09	56410.44 56832.20	335 336	1052.43 1055.58	88141.31 88668.31
202 203	637.74	32365.47	270	848.23	57255.53	337	1058.72	89196.88
204	640.88	32685.13	271	851.37	57680.43	338	1061.86	89727.03
205	644.08	33006.36	272	854.51	58106.90	339	1065.00	90258.74
206 207	647.17 650.31	33329.16 33653.53	273 274	857.65 860.80	58534.94 58964.55	840 341	1068.14 1071.28	90792.03 91326.88
208	653.45	33979.47	275	863.94	59395.74	342	1074.42	91863.81
209	656.59	34306.98	276	867.08	59828.49	843	1077.57	92401.81
210	659.73	34636.06	277	870.22	60262.82	844	1080.71	92940.88
211 212	662.88	34966.71 85298.94	278 279	873.36 876.50	60698.71 61136.18	845 846	1083.85 1086.99	98482.02 94024.78
213	669.16	35632.73	280	879.65	61575.22	847	1090.13	94569.01
214	672.30	35968.09	281	882.79	62015.82	348	1093.27	95114.86
215	675.44	36305.03	282	885.93	62458.00	349	1096.42	95662.28
216 217	678.58 681.73	36643.54 36983.61	283 284	889.07 892.21	62901.75 63347.07	350 351	1099.56 1102.70	96211.28 96761.84
218	684.87	87325.26	285	895.35	63798.97	852	1105.84	97818.97
219	688.01	37668.48	. 286	898.50	64242.43	353	1108.98	97867.68
220	691.15	38013.27	287	901.64	64692.46	854	1112.12	98422.96
221 222	694.29 697.43	38359.63 38707.56	288 289	904.78	65144.07 65597.24	355 356	1115.27 1118.41	98979.80 99538.22
223	700,58	39057.07	290	911.06	66051.99	357	1121.55	100098.21
224	703.72	39408.14	291	914.20	66508.30	858	1124.69	100659.77
225 226	706.86	89760.78 40115.00	292 293	917.35 920.49	66966.19 67425.65	359 860	1127.83 1130.97	101222.90 101787.60
220 227	710.00 713.14	40470.78	294	923.63	67886.68	861	1134.11	102353.87
228	716.28	40828.14	295	926.77	68349.28	362	1137.26	102921.72
229	719.42	41187.07	296	929.91	68813.45	363	1140.40	103491.18
280 231	722.57 725.71	41547.56 41909.63	297 298	933.05 936.19	69279.19 69746.50	364 365	1148.54 1146.68	104062.12 104634.67
232	728.85	42273.27	299	939.34	70215.38	505	1149.82	105208.80
233	781.99	42638.48	800	942.48	70685.83	867	1152.96	105784.49
284	735.13	43005.26	301	945.62	71157.86	368	1156.11	106361.76
235 236	738.27 741.42	43373.61 43743.54	302 303	948.76 951.90	71631.45 72106.62	369 870	1159.25 1162.89	106940.60 107521.01
237	744.56	44115.03	304	955.04	72583.36	871	1165.53	108102.99
238	747.70	44488.09	305	958.19	73061.66	372	1168.67	108686.54
239 240	750.84	44862.73 45238.93	306 307	961.33 964.47	73541.54	373 374	1171.81	109271.66
240	753.98 757.12	45616.71	308	967.61	74022.99 74506.01	875	1174.96 1178.10	109858.85 110446.62
212	760.27	45996.06	309	970.75	74990.60	376	1181.24	111036.45
243	763.41	46376.98	810	973.89	75476.76	377	1184.88	111627.86
214	766.55	46759.47 47143.52	311 312	977.04 980.18	75964.50 76453.80	378 379	1187.52 1190.66	112220.88
215 215	769.69 772.83	47529.16	313	983.32	76944.67	880	1193.81	112815.88 113411.49
247	775.97	47916.36	314	986.46	77437.12	381	1196.95	114009.18
248	779.11	48305.13	315	989.60	77981.18	382	1200.09	114608.44
249 250	782.26 785.40	48695.47 49087.39	316 817	992.74 995.88	78426.72 78923.88	383 384	1203.23 1206.37	115209.27 115811.67
251	788.54	49480.87	318	999.03	79422.60	385	1200.51	116415.64
252	791.68	49875.92	819	1002.17	79922.90	386	1212.65	117021.18
253	794.82	50272.55	820	1005.31	80424.77	887	1215.80	117628.80
254 255	797.96 801.11	50670.75 51070.52	321 322	1008.45 1011.59	80928.21 81483 22	388 389	1218.94 1222.08	118286.98
256	804.25	51471.85	323	1011.39	81939.80	890	1225.22	118847.24 119459.06
257	807.39	51874.76	324	1017 88	82447.96	891	1228.86	120072.46
358 359	810.58 813.67	52279.24 52685.29	325 326	1021.02 1024.16	82957.68	392	1281.50	120687.42
20	010.01	J4000.29	0.40	11064.10	83468.98	893	1284.65	121308.96

	la. I			la. I		i	la.	
Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
394	1237.79	121922.07	461	1448.27	166913.60	528	1658.76	218956.44
395	1240.93	122541.75	462	1451.42	167638.53	529	1661.90	219786.61
396 597	1244.07 1247.21	123163.00 123785.82	463 464	1454.56 1457.70	168365.02 169093.08	580 531	1665.04 1668.19	220618.34 221451.65
398	1250.35	124410.21	465	1460.84	169822.72	532	1671.83	222286.58
399	1253.50	125036.17	466	1463.98	170553.92	533	1674 47	223122.98
400	1256.64 1259.78	125663.71 126292.81	467	1467.12 1470.27	171286.70 172021.05	584 585	1677.61 1680.75	223961.00 224800.59
401 402	1262.92	126923.48	468 469	1478 41	172756.97	536	1 1800 00	225641.75
403	1266.06	127555.73	470	1476.55	173494.45	537	1687.04	226484.45
404	1269.20	128189.55	471	1479.69	174238.51	588	1690.18	227328.79
405 406	1272.85 1275.49	128824.93 129461.89	472 473	1482.83 1485.97	174974.14 175716.35	539 540	1693.32 1696.46	228174 66 229022 10
407	1278.68	130100.42	474	1489.11	176460 12	541	1699.60	229871.12
408	1281.77	130740.52	475	1492.26	177205.46	542	1702.74	280721.71
409	1284.91 1288.05	131382.19 132025.43	476	1495.40 1498.54	177952.37 178700.86	543 544	1705.88 1709.08	231578.86 232427.59
410 411	1291.19	132670.24	477 478	1501.68	179450.91	545	1712 17	233282.89
412	1294.34	133316.63	479	1504.82	180202.54	546	1715.81	234139.76
418	1297.48	133964.58	480	1507.96	180955.74	547	1718.45	234998.20
414 415	1300.62 1303.76	134614.10 135265.20	481 482	1511.11 1514.25	181710.50 182466.84	548 549	1721.59 1724.78	235858.21 236719.79
416	1306.90	135917.86	483	1517.39	183224.75	550	1727.88	237582.94
417	1310.04	136572.10	484	1520.53	183984.23	551	1731.02	288447.67
418	1313.19 1316.33	137227.91 137885.29	485 486	1523.67 1526.81	184745,28 185507,90	552	1784.16 1787.80	239313.96 240181.83
419 420	1819.47	138544.24	487	1529.96	186272.10	553 554	1740.44	241051.26
421	1322.61	139204.76	488	1533.10	187087.86	555	1743.58	241922.27
422	1325.75	139866.85	489	1536.24	187805.19	556	1746.73	242794.85
423 424	1328.89 1332.04	140530.51 141195.74	490 491	1589.88 1542.52	188574.10 189844.57	557 558	1749.87 1753.01	243668.99 244544.71
425	1335.18	141862.54	492	1545.66	190116.62	559	1756.15	245422 00
426	1838.82	142530.92	493	1548.81	190890.24	560	1759.29	246300.86
427 428	1341.46	143200.86 143872.38	494	1551.95 1555 09	191665.48	561 562	1762.43	247181.30 248063.30
429	1344.60 1847.74	144545.46	495 496	1558.23	192442.18 193220.51	563	1765.58 1764.72	248946.87
480	1850.88	145220.12	497	1561.87	194000.41	564	1771.86	249832.01
481	1854.03	145896.85	498	1564.51	194781.89	565	1775.00	250718 73
482 433	1857.17 1360.81	146574.15 147258.52	499 500	1567.65 1570.80	195564.93 196349.54	566 567	1778.14 1781.28	251607.01 252496.87
484	1368.45	147934.46	501	1573.94	197135.72	568	1784.42	253388.30
435	1366.59	148616.97	502	1577.08	197923.48	569	1787.57 1790.71	254281.29
436 437	1869.73 1872.88	149301.05 149986.70	503 504	1580.22 1583.36	198712.80 199503.70	570 571	1790.71 1793.85	255175.86 256072.00
488	1876.02	150673.93	505	1586 50	200296.17	572	1796.99	256969.71
439	1879.16	151362.72	506	1589.65	201090.20	573	1800.13	257868.99
440	1382.30	152053.08 152745.02	507 508	1592.79 1595.93	201885.81 202682.99	574 575	1803.27 1806.42	258769.85 259672.27
441	1385.44 1388.58	158438 58	509	1599.07	203481.74	576	1809.56	260576.26
443	1391.78	154133.60	510	1602.21	204282.06	577	1812.70	261481.83
444	1894.87	154830.25	511	1605.35	205083.95	578	1815 84	262388.96
445 446	1898.01 1401.15	155528.47 156228.26	512 513	1608.50 1611.64	205887.42 206692.45	579 580	1818.98 1822.12	268297.67 264207.94
447	1404.29	156929.62	514	1614.78	207499.05	581	1825.27	265119.79
448	1407.43	157632.55	515	1617.92	208307.23	582	1828.41	266033.21
449 450	1410.58 1418.72	158837 06 159048.18	516 517	1621.06 1624.20	209116.97 209928.29	583 584	1881.55 1834.69	266948.20 267864.76
451	1416.86	159750.77	518	1627 34	210741.18	585	1837.83	268782.89
452	1420.00	160459.99	519	1680.49	211555.63	586	1840.97	269702.59
458	1428.14	161170.77	520	1683.63	212371.66	587 588	1844.11 1847.26	270623.86
454 455 456 457 455 456	1426.28 1429.42	161888.18 162597.05	521 522	1636.77 1639.91	213189.26 214008.43	589	1850.40	271546.70 272471.12
44	1483.57	168312.55	523	1643.05	214829.17	590	1853.54	273397.10
407	1485.71	164029.62	524	1646.19	215651.49	591	1856.68	274324.66
	1488.85 1441.99	164748.26 165468.47	525 526	1649.34 1652.48	216475.37 217300.82	592 593	1859.82 1862.96	275253.7P 276184.
22	1445.18	166190.25	527	1655 62	218127.85	594	1866.11	277116.
489								

Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
595	1869.25	278050.58	663	2082.88	845286.69	781	2296.50	419686.15
596 597	1872.89 1875.53	278985.99 279922.97	664 665	2086.02 2089.16	846278.91 847822.70	732 733	2299.65 2802.79	420835.19 421985.79
598	1878 67	280861.52	666	2092.30	848868.07	784	2305.93	423137.97
599	1881.81	281801 65	667	2095.44	849415.00	735	2809.07	424291.72
600	1884.96	282743.34 283686.60	668	2098.58	350468.51 851518.59	736 737	2812.21 2815.85	425447.04 426603.94
602	1888.10 1891.24	284631.44	669 ·	2101.73 2104.87	352565.24	738	2318.50	427762.40
603	1894.88	285577.84	671	2108.01	853618.45	739	2821.64	428922.43
604	1897.52	286525.82	672	2111.15	354673.24	740	2824.78	430084.03
605 606	1900.66 1903.81	287475.36 288426.48	678 : 674	2114.29 2117.43	355729.60 356787.54	741 742	2327.92 2331.06	431247.21 432411.95
607	1906.95	289379.17	675	2120.58	357847.04	748	2334.20	433578.27
608	1910.09	290338.43	676	2123.72	358908.11	744	2337.34	434746.16
609 610	1918.23 1916.37	291289.26 292246.66	677 678	2126.86 2130.00	359970.75 361034.97	745 746	2840.49 2343.63	435915.62 437086.64
611	1919 51	293205.63	679	2183.14	362100.75	747	2346.77	438259.24
612	1922.65	294166.17	680	2136.28	363168.11	748	2349.91	439438.41
618	1925.80 1928.94	295128.28 296091.97	681 682	2139.42 2142.57	364237.04 365307.54	749 750	2353.05 2356.19	440609 16 441786.47
614 615	1932.08	297057.22	688	2145.71	366379.60	751	2359.34	412965.85
616	1935.22	298024.05	684	2148.85	367453.24	752	2362.48	444145.80
617	1938.36	298993.44	685	2151.99	368528.45	753	2365.62	445827.53
618 619	1941.50 1944.65	299962.41 800938.95	686 687	2155.13 2158.27	369605.23 370683.59	754 755	2368.76 2371.90	446511.42 447696.59
620	1947.79	301907.05	688	2161.42	371763.51	756	2875.04	448883.82
621	1950.93	302881.73	689	2164.56 2167.70	372845.00	757	2378.19	450071.63
622 628	1954.07 1957.21	303857.98 304835.80	690 691	2167.70 2170.84	373928.07 375012.70	758 759	2381.83 2384.47	451261.51 452452.96
624	1960.35	805815.20	692	2173.98	376098.91	766	2387.61	453645.98
625	1963.50	306796.16	698	2177.12	377186.68	761	2390.75	454840.57
626	1966.64 1969.78	307778.69 308762.79	694	2180.27 2183.41	378276.03 379366.95	762 768	2393.89 2397.04	456036.73 457234.46
627 628	1972.92	509748.47	695 696	2186.55	380459.44	764	2400.18	458438.77
629	1976.06	310735.71	697	2159.69	381558.50	765	2403.82	459634.64
680	1979.20	311724.53	698	2192.83	382649.18	766	2406.46 2409.60	460837.08 462041.10
634 632	1982.85 1985.49	312714.92 313706.88	699 700	2195.97 2199.11	383746.83 384845.10	767 768	2412.74	463246.69
638	1988.63	814700.40	701	2202.26	385945.44	769	2415.88	464458.84
834	1991.77	815695.50	702	2205.40	387047.36	770	2419.03	465662.57
635 636	1994.91 1998.05	816692.17 817690.42	703 704	2208.54 2211.68	388150.84 389255.90	771 772	2422.17 2425.81	466872.87 468084.74
637	2001.19	818690.23	705	2214.82	390362.52	778	2428.45	469298.18
638	2004.84	819691.61	706	2217.96	891470.72	774	2431.59	470518.19
639 640	2007.48 2010.62	\$20694.56 \$21699.09	707 708	2221.11 2224.25	392580.49 393691.82	775 776	2434.73 2437.88	471729.77 472947.92
641	2013.76	322705.18	709	2227.39	394804.73	777	2441.02	474167.65
642	2016.90	323712.85	710	2230.53	895919. 2 1	778	2444.16	475388.94
643 644	2020.04	324722.09 325732.89	711 712	2233.67 2236.61	397035.26 398152.89	779 78 0	2447.80 2450.44	476611.81 477836.24
645	2025.19	326745.27	718	2239.96	399272.08	781	2453.58	479062.25
616	2029.47	327759.22	714	2243.10	400392.84	782	2456.78	480289.83
647	2032.61	328774.74	715	2246.24	401515.18	783	2459.87 2463.01	481518.97 482749.69
648 619	2095.75 2038.89	329791.83 330810.49	716 717	2249.38 2252.52	402639.08 403764.56	784 785	2466.15	483981.98
659	2042.01	331830.72	718	2255.66	404891.60	786	2469.29	485215.84
651	2045.18	832852.58	719	2258.81	406020.22	787	2472.48	486451.28
652 653	2048.32 2051.46	388875.90 334900.85	726 721	2261.95 2265.09	407150.41 408282.17	788 789	2475.58 2478.72	487688.28 488926.85
654	2054.60	335927.36	722	2268.23	409415.50	790	2481 86	490166.99
655	2057.74	336955.45	723	2271.37	410550.40	791	2485.00	491408.71
656 657	2060.88 2064.03	387985.10 889016.33	724 725	2274.51 2277.65	411686.87 412824.91	792 793	2488.14 2491.28	492651.99 493896.85
6 58	2067.17	840049.18	726	2280.80	418964.52	794	2494.42	495148.28
659	2070.31	84 1083.50	727	2283.91	415105.71	795	2497.57	496391.27
660	2073,45 2076,59	842119.44 848156 95	728 729	2287.08 2290.22	416248.46	796 797	2500.71 2503.85	497649.84 498891.98
661	2079.73	344196.03	780	2293.36	418538.68	798	2506.99	500144.69

Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
799	2510.18	501398.97	867	2723.76	590875.16	985	2937.39	686614.71
800	2513.27	502654.82	868	2726.90	591737.83	936	2940.53	688084.19
801 802	2516.42 2519.56	503912.25 505171.24	869 870	2730.04 2733.19	598102.06 594467.87	937 938	2943.67 2946 81	689555.24
803	2522.70	506431.80	871	2736.33	595835.25	939	2949.96	691027.86 692502.05
804	2525.84	507693.94	872	2789.47	597204.20	940	2958.10	693977.82
805	2528.98 2582.12	508957.64	873	2742.61	598574.72	941	2956.24	695455.15
906 807	2535.27	510222.92 511489.77	874 875	2745.75 2748.89	599946.81 601320.47	942 948	2959.38 2962.52	696934.06 698414.53
808	2538.41	512758.19	876	2752.04	602695.70	944	2965.66	699896.58
809	2541.55	514028.18	877	2755.18	604072.50	945	2966.81	701380.19
810 NII	2544.69 2547.88	515299.74 516572.87	878 879	2758.82 2761.46	605450.88 606830.82	946 947	2971.95 2975.09	702865.38 704852.14
812	2550.97	517847.57	880	2764.60	608212.34	948	2978.23	705840.47
813	2554.11	519123 84	881	2767.74	609595.42	949	2981.87	707330.37
814 815	2557.26 2560.40	520401.68 521681.10	882 883	2770.88	610980.08 612366.31	950 951	2984.51 2987.65	708821.84
816	2568.54	522962.08	884	2774.08 2777.17	613754.11	952	2990.80	710814.88 711809.50
817	2566.68	524244.63	885	2780.31	615143.48	958	2993.94	713305.68
818	2569.82 2572.96	525528.76 526814.46	886	2788.45 2786.59	61 6 534.42 617 92 6.93	954	2997.08	714803.43
850 813	2578.11	528101.73	887 888	2789.78	619321.01	955 956	3000.22 3008.36	716302.76 717803.66
R51	2579.25	529390.56	889	2793.88	620716.66	957	3006.50	719306.12
824	2582.39	530680.97	890	2796.02	622113.89	958	3009.65	720810.16
8:3 8:24	2585.53 2586.67	531972.95 533266.50	891 892	2799.16 2802.30	628512.68 624913.04	959 960	3012.79 3015.98	722315.77 723822.95
823	2591.81	534561.62	898	2803.44	626314.98	961	3019.07	725331.70
826	2594.96	535858.32	894	2808.58	627718.49	962	3022.21	726842.02
827 828	2598.10 2601.24	537156.58 538456.41	895 896	2811.73 2814.87	629123,56 630530,21	968 964	3025.85 3028.50	728853.91 729867.87
829	2604.88	539757.82	897	2818.01	631988.43	965	3031.64	731382.40
\$80	2607.52	541060.79	898	2821.15	633348.22	266	3034.78	732899.01
881 832	2610.66 2613.81	542365.34 545671.46	899 90 0	2824.29 2827.43	634759.58 636172.51	967 968	3037.92	734417.18
883	2616.95	544979.15	901	2830.58	637587.01	969	8041.06 3044.20	735986.93 737458.24
834	2630.09	546288.40	902	2833.72	639003.09	970	3047.34	738981.13
835	2648.28	547599.23	908 904	2836.86	640420.73	971	3050.49	740505.59
836 887	2636.87 2639.51	548911.68 550225.61	902	2840.00 2843.14	641839.95 643260.73	972 973	3053.63 3056.77	742031.62 743559.22
835	2632.65	551541.15 552858.26	906	2846.28	644683.09	974	3059.91	745088.39
1459	2635.80	552856.26	907	2849.42	646107.01	975	3068.05	746619.13
840 841	2636.94 2642.08	554176.94 555497.20	908 909	2852.57 2855.71	647532.51 648959.58	976 977	3066.19 3069.34	748151.44 749685.32
812	2645.22	556819.02	910	2858.85	650388.22	978	3072.48	751220.78
843	2648.86	558142.42	911	2861.99	651818.43	979	3075.62	752757.80
844 845	2651.50 2654.65	559467.39 560798.92	912 918	2865 .18 2868 .27	658250.21 654683.56	980 981	3078.76 3081.90	754296.40 755886.56
616	2657.79	562122.03	914	2871.42	656118.48	982	3085.04	757378.30
847	2660.93	568451.71	915	2874.56	657554.98	963	3088.19	758921.61
818 849	2664.07 2667.21	564782.96 566115.78	916 917	2877.70 2880.84	658993.04 660482.68	984 985	3091.33	760466.48
849 8 50		567450.17	918	2883.98	661873.88	986	3094.47 3097.61	762012.93 763560.95
851	2673.50	568786.14	919	2887.12	663316 66	987	3100.75	765110.54
Kiz	2676.64	570128.67 571462.77	920 921	2890.27 2893.41	664761.01 666206.92	989 989	3103.89	766661.70
858 854	2679.78 2682.92	572803.45	922	2896.55	667654.41	990	3107.04 3110.18	768214.44 769768.74
855	2686.06	574145.69	923	2899.69	669103.47	991	3113.32	771824.61
856	2689.20	575489.51	924	2902.88	670554.10	992	3116.46	772882.06
657 158	2692.84 2695.49	576834.90 578181.85	925 926	2905.97 2909.11	672006.30 673460.08	993 994	3119.60 3122.74	774441.07 776001.66
459	2666.6X	579530.38	927	2912.26	674915.42	995	3125.88	777563.82
860	2701.77	580880.48	928	2915.40	676372.33	996	3129.03	779127.54
861 862	2704.91 2708.05	5882292.15 588585.89	929	2918.54 2921.68	677880.82 679290.87	997 998	3132.17 3135.31	780692.84 782259.71
963	2711.19	584940.20	981 982	2924.83	680752.50	999	3138.45	783828.15
864	2714.84	586296.59	982	2927.96	682215.69	1000	3141.59	785398 16
955 865	922.48	587654.54 598014.07	988 984	2931.11 2984.25	683680.46 685146.80			
-	2700.62	589014.07	904	4501.60	0001301.001		<u> </u>	

CIRCUMFERENCES AND AREAS OF CIRCLES Advancing by Eighths.

Diam.	Circum.	Area.	Dlam.	Circum.	Area.	Diam.	Circum.	Area.
1/64	.04909	.00019	2 3/8	7.4613	4.4301	6 1/6	19.242	29.465
1/32	.09818	.00077	7/16	7.6576	4.6664	6	19.635	80.680
3/64	.14726	.00173	1/2	7.8540	4.9087	8 ₹	20.028	31.919
1/16	.19635	.00307	9/16	8.0503	5.1572	1%	20.420	33.183
1/16 3/32	.29452	00690		8.2467	5.4119	62	20.813	34.472
1,6	.39270	.01227	11/16	8.4430	5.6727	84	21 206	35.785
1/8 5/32	.49087	.01917	13/16 13/16 15/16	8.6394	5.9396	1 76	21.598	37.122
3/16	.58905	.02761	13/16	8.8357	6.2126	7.	21.991	38.485
7/32	.68722	.03758	3/8	9.0321	6.4918	⅓6	22.384	39.871
		25.53	15/16	9.2284	6.7771	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	22.776	41.282
9/32	.78540	.04909	6.0	ł		8 ∕8	23.169	42.718
9/32	.88357	.06213	3.	9.4248	7 0686	3/9	23.562	44.179
5/16	.98175	.07670	1/16	9.6211	7.3662	%	23.955	45.664
11/32	1.0799	.09281	3/16	9.8175	7.6699	8⁄4	24.847	47.178
5/16 11/32 8/6 13/32	1.1781	11045	3/16	10.014	7.9798	₹8	24.740	48.707
13/32	1.2763	12962	34	10.210	8.2958	8.	25.133	50.265
7/10	1.8744	15033	5/16	10.407	8.6179	⅓	25.525	51.849
15/82	1.4726	.17257	7/16	10.603	8.9462	184488448	25.918	53.456
•		9.72	7/16	10.799	9.2806	₹%	26.311	55.088
⅓.	1 5708	.19635	36	10.996	9.6211	1∕2	26.704	56.745
17/32	1.6690	.22166	9/16	11.192	9.9678	5∕6	27.096	58.426
9/16	1.7671	.24850	11/16	11.388	10.321	3⁄4	27.489	60.182
19/82 96 21/32	1.8653	27688	11/16	11.585	10.680	7∕8	27.882	61.862
56	1.9635	80680	34 18/16	11.781	11.045	9.	28.274	63.617
21/32	2.0617	33824	13/16	11.977	11.416	184.848	28.667	65.397
11/16	2.1598	.37122	78 15/16	12.174	11.793	1/4	29.060	67.201
11/16 23/32	2.2580	.40574	15/16	12.370	12.177	38	29.452	69.029
		1,39.7	4.	12.566	12.566	22	29.845	70.882
25/32	2.3562	44179	1/16	12.763	12.962	58	30.238	72.760
25/32	2.4544	47937	3/16	12.959	13.864	24	30.681	74.662
13/16 27/32	2.5525	.51849	3/16	13.155	13.772	78	31.028	76.589
27/32	2.6507	55914	5/16	13.352	14.186	10.	81.416	78.540
20/32 15/16	2.7489	.60134	5/16	13.548	14.607	16	31.809	80.516
29/32	2.8471	64504	7/16	13.744	15.083	24	82.201	82.516
15/16 31/32	2.9452	.69029	7/16	13.941	15.466	98	82.594	84.541
31/32	3.0434	8708	9/16	14.137	15.904	23	32.987	86.590
. 1	0.4440	POR C	9/10	14.834	16.349	58	33.879	88.664
١ ا	3.1416	854	11/16	14.530	16.800	23	88.772	90.763
1/16	3.3379	.8866	11/16	14.726	17.257	11 %	34.165	92.886
3/16	3.5348	.9940	44	14.923	17.721		34.558	95.083
3/16	3.7806	1.1075	13/10	15.119	18.190	78	84.950	97.205
5/16	3.9270	1.2272	13/16 13/16 15/16	15.815	18.665	TO THE PERSON OF	35.343 35.736	99.402
5/10	4.1233	1.3530	19/10	15.512	19.147 19.635	78	36.128	101.62
86 7/16	4.3197	1.4849	1/16	15.708 15.904		73		103.87
7/10	4.5160	1.6230	1/10	10.004	20.129 20.629	79	86.521 86.914	106.14
9/16	4.7124	1.7671	3/16	16.101	21.135	72		108.48
8/10	4.9087	1.9175	9/10	16.297 16.493	21.648	12. 8	37.306 37.699	110.75 113.10
56 11/16	5.1051	2.0739	5/16	16.690	22.166	12.14	88.092	
11/10	5.3014	2.2365	3/10		22.691	78		115.47
3/4 13/16	5.4978 5.6941	2.4053 2.5802	7/16	16.886 17.082	28.221	**************************************	38.485 38.877	117.86 120.28
19/10	5.8905	2.7612	1/10	17.279	23.758	72	89.270	122.72
76 15/16	6.0868	2.9483	9/16	17.475	24.801	73 2	89.663	125.19
19/10	0.0000	4.0403	6/10	17.671	24.850	8%	40.055	127.68
, 1	6.2832	3.1416	58 11/16	17.868	25.406	72	40.448	130.19
1.116	6.4795	3.3410	3/	18.064	25.967	18.78	40.841	182.78
1/16 1/6	6.6759	3.5466	34 13-16	18.261	26.535	14	41.283	135.30
9/14	6.8722	8.7588	76	18.457	27.109	16 14	41.626	187.89
3/16 14 6	7.0686	3.9701	76 15-16	18.653	27.688	74 82	42.019	140.50
74	7.2649	4.2000	6	18.850	28.274	36	42.412	148.14

CIRCUMFERENCES AND AREAS OF CIRCLES.

Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	A
13 56	42.804	145.80	21%	68.722	375.88	80 1/6 1/4 1/6 1/4 1/6 1/6 1/6 1/6 1/6 1/6 1/6 1/6 1/6 1/6	94.640	3
13 %	43.197	148.49 151.20	22.	69.115 69.508	380.13 384.46	<i>2</i> 2	95.088 95.426	255555
14.76	43.590 43.982	15R 94		69,900	388.82	72	95.819	1 2
17.16	44 875	156.70 159.48	<u>%</u> 8	70.298	393.20	28	96.211	13
15. 16. 16. 16. 16. 16. 16. 16. 16. 16. 16	44.768	159.48	<u> </u>	70.686 71.079	397.61 402.04	73	96.604 96.997	13
₹ 6	45.160	162.80 165.13 167.99 170.87 173.78 176.71 179.67	38 82	71.471	406.49	81.78	97.389	1 2
62	45.553 45.946	167.99	1 2	71.864	410.97		97.782	1 7
79	44 999	170.87	128.	72.257	415.48	STEWN STATES	98.175	2000
%	46.781 47.124	178.78	1/8 1/4 8/8	72.649 78.042	420.00 424.56	? 9	98.567 98.960	13
15.	47.124	179.67	86	73.435	429.18	62	99.358	1 2
79	47.517 47.909	1182.00	12	73.827	438.74	94	99.746	1 7
2 2	48.30-2	1185.66	16 58 34	74.220	438.86	82.76	100.138	3
12	48.695	188.69	94 98	74.613 75.006	448.01 447.69		100.531 100.924	8
26	49.087	191.75 194.88	24. 28	75.398	452.39	**********	101.316	1 8
16. \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	49.480 49.878	1197.98		75.791	457.11	98	101.709	18
16.78	50.265	1201.00	18 14 88	76.184	461.86	24	102.102	8
3/6	50.658	204.22	38	76.576 76.969	466.64 471.44	29	102.494 102.887	88888
24	51.051	207.89 210.60	58	77.362	476.26	72	103,280	Ì
79	51.414 51.836	213.82	24	77.754	481.11	88.	103.673	18
72	52.229	213.82 217.08	3/8	78.147	485.98	1/8	104.065	8
32	52.622	220.35 223.65		78.540 78.933	490.87 495.79	<i>7</i> 3	104.458 104.851	8
36	58.014	226.98	16	79.825	500.74	72	105.248	8
17.	53.407 58.800	230.83	36	79.718	505.71	6%	105.636	8
16 14 16 17	54.192	1233.71		80.111	510.71	STATE OF THE STATE	106.029	8
32	54.585	287.10	86	80.508	515.72	84.76	106.421	8
32	54 978	240.53 243.98	32	80.896 81.289	520.77 525.84		106.814 107.207	١
56	55.871 55.768	247.45	26.	81.681	530.93	12	107.600	18
3	56.156	247.45 250.95	14	82.074	586.05	STATES OF THE ST	107.992	1 8
18.78	56.549	INE 4 47	33	82.467 82.860	541.19 546.85	29	108.385 108.778	18
3/6	56.941	258.02 261.59	16	83.253	551.55	38	109.170	1
16 14 14 14 14 14 14 14 14 14 14 14 14 14	57.334 57.727 58.119	265.18	26	83.645	556.76	%	109.563	11
79	58.119	265.18 268.80	34	84.038	562.00	8ō.	109.956	1
22	58.512	1272.40	27.78	84.430 84.823	567.27 572.56	19	110.848 110.741	
\$2	58.905	276.12 279.81		85.216	577.87	S. C.	111.184	1
3/8	59.298 59.690	1283.53	A TANK A SANAN	85.608	583.21	12	111.527	1 9
10	139 000	1997.27	%	86.001	588.57	29	111.919	1.5
16 14 14 14 14 14 14 14 14 14 14 14 14 14	60.476	291.04 294.83	73	86.394 86.786	593.96 599.37	32	112.812 112.705	10
57	60.858	208.65	28 8/2	87.179	604.81	86.	113.097	10
3.4	61.261 61.654	1202.49	%	87.572	610.27		113.490	10
29	62.046	806.35	28.	87.965	615.75	1/4	118.888	10
- 3	62.439	810.24	78	88 857 88 750	621.26 626.80	? 8	114.275 114.668	10
46	Oc.	818.10	86	89.143	682.86	62	115.061	i
14	68.225 68.617	822.06	1%	89.535	637.94	A SAN	115.454	10
7	64.010	1000.00	26	89.928	643.55	3.7 8	115.846	10
3	64.408 64.798	830.06 834.10	W. C.	90.321 90.713	649.18 654.84	87.	116.239 116.632	10
	64.795	338.16	29. 8	91.106	660.52	STATE TO SELECT	117.024	i
2	65.186	942.25		91.499	666.23	8₹	117.417	10
- 3. 3.		3 20.80	1/8 1/4 1/8	91.892	671.96	1/3	117.810	1
21.		5 1200.00	79	92.284 92.677	677.71 683.49	28	118.202 118.596	1
3	9 6 25	858.84	<i>3</i> 2	93.070	689.30	<i>3</i> 2	118.988	i
á	67.15	363.05	§ %	93.462	695.13	88.	119.381	1
1	67.54	363.05 367.28 371.54	80.78	98.855 91.248	700.98 706.86	16 14	119.773 120.166	1:
	08.89							

Diam.	Circum.	Area.	Diam.	Circum.	Ares.	Diam.	Circum.	Area.
86 36 36 36 36 36 36 36 36 36 36 36 36 36	120,559	1156.6	46 5%	146,477	1707.4	54 %	172,395	2865.0
1/2	120,951	1164.2	\$4	146,869	1716.5	55.	172.788	2875.8
52	121.344	1171.7	1 2	147.262	1725.7	1/6	178.180	2386.6
§2	121.787	1179.3	47.	147.655	1734.9	181488188188	173.578	2397.5
36	122.129	1186.9	28 34	148.048	1744.2	86	173.966	2408 3
, v	122.522	1194.6	34	148.440	1753.5	1/8	174.358	2419.2
184 184 184 18	122.915	1202.3	36	148.883	1762.7	5%	174.751	2480.1
14	123.308	1210.0	58	149,226	1772.1	3/4	175.144	2441.1
3/4	128.700	1217.7	5%	149.618	1781.4	1 /8	175.586	2452.0
36	124.093	1225.4	34	150.011	1790.8	5 6 .	175.929	2463.0
98	124.486	1283.2	78	150.404	1800.1	161486148 141486148	176.322	2474 0
3/4	124.878	1241.0	48.	150.796	1809.6	34	176.715	2485.0
. 7/8	125.271	1248.8	1/8 1/4 8/8	151.189	1819.0	8∕6	177.107	2196.1
Ю.	125.664	1256.6	1/4	151.582	1828.5	1/8	177.500	2507.2
18 18 18 18 18 18 18 18 18 18 18 18 18 1	126.056	1264.5	38	151.975	1887.9	5 6	177.898	2518.3
14	126.449	1272.4	1.6	152.367	1847.5	94	178.285	2529.4
₹8	126.842	1230.3	28	152.760	1857.0	7/8	178.678	2540.6
1/2	127.235	1288.2	94	153.153	1866.5	97 .	179.071	2551.8
98	127.235 127.627	1296.2	3/8	158.545	1876.1	⅓6	179.463	2563.0
74	1225.020	1304.2	49.	153.938	1885.7	1 /4	179.856	2574.2
3/8	128.418	1312.2	1/6	1 54 .3 3 1	1895.4	9∕6	180.249	2585.4
H.	128.805	1320.3	4	154.723	1905.0	2/8	180.642	2596.7
1814 SE 1814 S	129.198	1328.3	1/8 1/4 8/6	155.116	1914.7	10142018	181.034	2608.0
14	129.591	1336.4	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	155.509	1924.4	94	181.427	2619.4
₹8	129.983	1344.5	98	155.90 2	1984.2	7 8	181.820	2680.7
2/4	130.376	1352.7	94	156.294	1943.9	58.	182.212	2642.1
98	130.769	1 360 .8	₹8	156 687	1953.7	1/6	182.605	2658.5
24	131.161	1369.0	50.	157.080	1963.5	24	182.998	2664.9
7/8	131.554	1377.2	76 ∣	157.472	1978.3	- 8∕6 ¹	188.890	2676.4
12.	131.947	1385.4	34	157.865	1978.3 1983.2 1998.1	2/8	183.788	2687.8
	132.340	1393.7	**************************************	158.258	1998.1	10,430,430,430	184.176	2699.3
34	132.732	1402.0	2/9	158.650	2008.0	24	184.569	2710.9
% €	133.125	1410.3	28	159.048	2012.9	76	184.961	2722.4
249	133.518	1418.6	24	159.436	2022.8	59	185.854	2734.0
96	133.910	1427.0	78	159.829	2082.8	3/8	185.747	2745.6
24	134.808	1485.4	51.	160.221	2042.8	14	186.139	2757.2
	134.696	1448.8	34 34 36	160.614	2052.8	78	186.532	2768.8
18:	135.088	1452.2	24	161.007	2062.9	3.65	196.925	2780.5
**************************************	135.481	1460.7	28	161.899	2078.0	58	187.817	2792.2
24	135.874	1469.1	26	161.792	2088.1	94	187.710	2808.9
? \$	136.267	1477.6 1486.2	58	162.185	2098.2	*/B	188.103	2815.7
29	136.659	1486.2	40/4	162.577	2103.3	OV.	188.496	2827.4
26	137.052	1494.7	5/8	162.970	2113.5	28	188.888	2889.2
24	137.445	1508.3	52	163.363	2128.7	24	189.281	2851.0
, /8	137.837	1511.9	1/8	163.756	2188.9	56	189.674	2862.9
TT.	138.230	1520.5	34	164.148	2144.2	29	190.066	2874.8
**************************************	138.623	1529.2	76	164.541	2154.5	26	190.459	2886.6
4	139.015	1537.9	28	164.934	2164.8	54	190.852	2898.6
26	139.408	1545.6 1555.3	26	165.326 165.719	2175.1 2185.4	276	191.244	2910.5
29	139.801		23		2100.4	61.	191.637 192.030	2922.5 2934.5
29	140.194	1564.0	. 58	166.112	2195.8 2206.2	78	192.423	
24	140.586	1572.8	58.	166.504 166.897	0016 6	23	192.815	2946.5 2958.5
45. ²⁸	140.979	1581.6	16 14 26	167.290	2216.6 2227.0	78	198.208	2970.6
	141.872	1590.4	24	167. 683	2287.5	23	193.601	2982.7
78	141.764	1599.8	78		2248.0	78	198.998	2994 8
18 14 18 18 18 18 18 18 18 18 18 18 18 18 18	142.157	1608 2	1,97,27,47,8	168.075	2258.5	A TANAN SALA	194.886	8006 9
78	142.550	1617.0 162 6 .0	78	168.468 168.861	2269.1	62. 8	194.779	8019.1
79	142.942		7 9	169.253	2209.1 2279.6		195.171	3081.3
29	148.835	1634.9	× 1/8			78	195.171	
24	143.728	1643.9	54.	169.646	2290.2 2300.8	75	195.054	8043.5 8055.7
/8	144.121	1652.9	16 14	170.039		? 9		3068.0
16.	144.518	1661.9	.4	170.431	2311.5	23	196.850	
16 14 86	144.906	1670.9	1/8 1/8 1/8 1/8 1/8 1/8 1/8 1/8 1/8 1/8	170.824	2322.1 2332.8	N. A. S.	196.742	3080.3
3	145.290	1680.0	29	171.217		73	197.135	8092.6
78	145.691 146.084	1689.1 1698.2	78	171.609 172.002	2343.5 2354.8	68. ⁷⁸	197.528 197.920	3104.9 3117.3

CIRCUMFERENCES AND ABEA

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Diam.	Circ	eum.	Area	. Di	am.	Circum.	Ar
63 14 6 6 6 6 7 8 1 8 1 8 1 8 1 8 1 8 1 8 1 8 1 8 1 8	196	.313	3129	6 71	36	224,281	400
1/4	193	.706		.ŏl	72	224.624	401
36	199	.098	1 3154	. 5	52	225.017	402
25		.491	1 3166	. 9	94	225.409	404
29	199	.884	1 8179	.48	3 /8	225.802	400
23	200	.277	8191	.9 7	z .,	226.195 226.587	407
8 1 2/B	1 300	.669	3204	.4	79	226.980	409
14	1 80	.062	8217 8239	3.6	32	227.378	411
78	20	1.455 1.847	824		32	227.765	412
22	1 30	2.240	2.25	48	62	228.158	414
12		2.688	326	7.5	\$2	228.551	413
52	20	8.025	328	0.1	78	229.944	417
84	20	3.418	320	2.8	788.	229.336	418
- 3/8	\ ≥0	13.81.	830	5.6	- 79	229.729 230.123	418
6 5.	≥0	14.204	331	8.8	23	280.123	42:
₹6	20	4.596	/ 88	31.1 43.9	79	280.907	424
24	1 20	4.989	33	43.9 56.7	32	281.300	42
79	1 2	05.3 82	1 33	69.G	32	281.692	420 427
65. 1614 3614 5634 5634 66.		05.774 06.167	, \ 22	82.4	38	232.085	428
39	15	ar rec	• l 93	395.3	74.	282.478	430
77	\ 3	08 95:	2 \ 3	408.2	3-6	282.871	48
66.	1 2	477 3343		421.2	1 34	283.268	48
66. 18. 19. 19. 19. 19. 19. 19. 19. 19. 19. 19	1 2	07.78	8 8	434.2 447.2 3460.2	79	233 656 234.019	434 485
1,3	\ \ \		1 \ 2	447.2	23	234.441	437
97	. 1 >	208.52 208.91	23 \ \ \ \ \	3460.2 3473.2	29	284.884	436
1.2		208.91	<u>6</u>	3473 2 3486 3	72	285.227	44
5€	• (:			8499.4	75.	235.619	441
- 3≥4	• \ '	209.70 210.0	33 \	3512.5	1/8	236.012	448
34	6	210.4	27	8525 7	34	286.405	444
• • • •	- 1	310.3	79 l	85 25 7 8538.5	3 76	236.798	446
33	} \	210.8	:72 \		23	237,190 237,583	447
3	2 \	211.6 212.0 212.0	665	8565.	25 55 34 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	237.976	450
1	2	212.0)58 \	3578.		238.368	455
5	るし	212.9	150	8005	6 76.	238.761	452 453
5	484848	212. 213. 218.	843	8591. 8005. 3618.	87048% %%%	239.154	455
3	18	218.	628 628	1 2431	7 3	239.546	456
48	\	214	021	3845	0 %	239.939	456
1	<u>ب</u>	914	414	8658	4 %	240.332	461
	2 3		F4 70	8671	.8	940.725 941.117	46
1	7 2	l 215.		8685	.3 .7	241.510	464
1	62	1 213	. 592	3698	2 77.	241.903	465
	4 2	1 4315		8712 3725 3789	7 16	242.295	467
	3 7 8	216		1 3789	.7 .8 .8 .4 .9 .0 .3 .7 .7	242.688	468
69		1 216	163	1 92750	2.8 %	243.081	470
	} 6	1 345	555	376 87 8	3.4	248.473	47
	>4	217 217 217 217	163 555 948	/ 828	9.0	243.866	47
	79	1 218	3.341	389	2 3 72	244.259 244.652	476
	2	218	5 7 33	882	1.0 78.	245.044	47
	33	21	9.120	1 200	4.7	245.437	475
	32	21	9-314	334	8.5	245.830	480
70	D -	21	9 126 9 518 9 911 9 36 9 69	. ∤ 986	32.2 ×	246.222	48
•	1/8	722	69	7 \ 387	76.0	246.615	48
	1.4	1 8	000	<u>~</u> / 88	4.7 18.5 52.2 76.0 89.8 03.6 17.5	247.008	48
	36	\ 5	21.48	22 100	03.6 \$4 17.5 %	247.400 247.793	488
	29	\ 2			31.4 79. ⁷⁸	248.186	490
	79	1 2	22.20	3 \ 89		248.579	49
	72	22	-22 - 00	S \ 89	59.2	248.971	49:
-		' \ 2	44	8	978.1	249.364	49
•	· - 1	<u>د</u> ا خ	28 4	38 18	987.1	249.757	490
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Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
87 3/8	276.067	6064.9	92.	289.027	6647.6	96 1/8	301.986	7257.1
88.	276.460	6082.1		289.419	6665.7	12	302.378	7276.0
	276.858	6099.4	1,2	289.812	6683.8	\$ 2	302.771	7294.9
874 874 8874 8874 8874 8874 8874 8874 8	277.246	6116.7	**************************************	290.205	6701.9	14304430430	303.164	7313.8
82	277.638	6134.1	12	290.597	6720.1	62	803.556	7332 8
1,6	278.031	6151.4	53	290.990	6738.2	5 %	803.949	7351.8
56	278.424	6168.8	8/4	291.383	6756.4	%	804.342	7370.1
84	278.816	6186.2	₹ 2	291.775	6774.7	97.	304.734	7389.8
172	279.209	6203.7	98.´`	292.168	6792.9	1,6	805.127	7408.9
89.	279.602	6221.1	16	292.561	6811.2	*******	305.520	7428.0
1/6	279.994	6238.6	***************************************	292.954	6829.5	82	305.913	7447
A A A A A A A A A A A A A A A A A A A	280.887	6256.1	82	293.346	6847.8	12	306,305	7466.4
87	280.780	6273.7	1,6	293.739	6866.1	56	306.698	7485
1,6	281.178	6291.2	62	294.132	6884.5	84	307.091	7504
5%	281.565	6 08.8	84	294.524	6902.9	%	307.483	7523.3
3%	281.958	6326.4	72	294.917	6921.3	98."	307.876	7543.0
7 %	282.351	6344.1	94.	295.310	6939.8	1/6	308.269	7562.
30.	282.743	6361.7	1,6	295.702	6958.2	**************************************	308.661	7581.5
1/6	283.136	6379.4	**************************************	296 095	6976.7	86	309.054	7600.8
1/4	288.539	6397.1	82	296.488	6995.3	1,6	309.447	7620.1
87	283.921	6414.9	1,6	296.881	7013.8	52	309.840	7639.4
1,6	284.314	6482.6	5 6 ∣	297.278	7082.4	84	310.232	7658 9
5%	284.707	6450.4	94	297.666	7051.0	36	310.625	7678.8
A A STANCE OF THE STANCE OF TH	285.100	6468.2	34	298.059	7069.6	99.	811.018	7697.7
- 14 I	285.492	6486.0	95.	298.451	7088.2	1/8	311.410	7717.
91.	285.885	6503.9	1/6	298.844	7106.9	3/4	311.803	7736.0
1/6	286.278	6521.8	1/4	299.237	7125.6	3/8	312.196	7756.
1/4	286.670	6539.7	84	299.629	7144.8	16	812.588	7775.0
82	287.063	6557.6	16	300.022	7163.0	5%	312.981	7795.
14 36 14 36	287.456	6575.5	***************************************	300.415	7181.8	34	313.374	7814.8
5%	287.848	6593.5	84	300.807	7200.6	3/8	813.767	7834
8/4	288.241	6611.5	1 %	301.200	7219.4	100.	314.159	7854.0
1/2	288.634	6629.6	96.	301.593	7238.2			

DECIMALS OF A FOOT EQUIVALENT TO INCHES AND FRACTIONS OF AN INCH.

Inches.	0	1∕8	1/4	3%	1/2	5%	3⁄4	₹6
0	0	.01042	.02083	.03125	.04167	.05208	.06250	.07292
·ĭ	.0833	10938	.1042	.1146	.1250	.1354	.1458	.1563
2	.1667	.1771	.1875	.1979	.2083	.2188	.2292	.2396
8	.2500	.2604	.2708	.2813	.2917	.3021	3125	3229
4	.8333	.3438	.3542	.3646	.3750	.3854	.3958	.4063
5	.4167	.4271	.4375	.4479	.4583	.4688	.4792	.4896
6	.5000	.5104	.5208	.5313	.5417	.5521	.5625	.5729
7	.5833	.5938	.6042	.6146	.6250	.6354	.6458	.6563
8 9	.6667	.6771	.6875	.6979	.7083	.7188	.7292	.7396
9	.7500	.7604	.7708	.7818	.7917	.8021	.8125	8229
10	.8383	.8438	.8542	.8646	.8750	.8854	.8958	.9063
11	.9167	.9271	.9375	.9479	.9583	.9688	.9792	.9896

EN. DIAMETER.	
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	O In.	**********************************
9	0	### **********************************
	Diam. Feet.	

LENGTHS OF CIRCULAR ARCS. (Degrees being given. Radius of Circle = 1.)

FORMULA.—Length of arc = $\frac{3.1415927}{180}$ × radius × number of degrees.

RULE.—Multiply the factor in table for any given number of degrees by the radius.

EXAMPLE —Given a curve of a radius of 55 feet and an angle of 78° 20'. What is the length of same in feet?

 Factor from table for 78°
 1.3613568

 Factor from table for 20′
 .0058178

 Factor
 1.3671746

 $1.8671746 \times 55 = 75.19$ feet,

	М	Minutes,					
1	.0174533	61	1.0646508	121	9.1118484	1	.0002909
2	.0349066	62	1.0821041	122	2.1293017	2	.0005818
8	.0523599	68	1.0995574	123	2.1467550	3	,0008727
ă l	.0698132	64	1.1170107	124	2.1642083	4	.0011636
4 5	.0879665	65	1.1344640	125	2.1816616	5	,0014544
6	,1047198	66	1.1519173	126	2,1991149	6	.0017450
7	.1221730	67	1.1693706	127	2,2165682	7	.0020369
8	,1396263	68	1.1868239	128	2,2340214	8	.0023271
9	. 1570796	80	1.2042772	129	2.2514747	9	.0026180
10	.1745329	70	1.2217305	130	2,2689280	10	.0029089
1	.1919862	71	1.2391838	131	2,2863813	11	.0031998
12	. 2094395	72	1.2566971	132	2.3038346	12	.0034907
13	.2268928 .2443461	73 74	1.2740904	133	2,3012879	13	.0037815
15	.2617994	75	1.2915436	134	2.3387412 2.3561945	14 15	.0040724
16	.2792527	76	1.3264503	136	2.3736478	16	.0043638
17	.2967060	77	1.3439035	137	2,3911011	17	.0049451
18	.3141593	78	1.3613568	138	2,4085544	18	.0052360
<u>19</u>	.3316126	79	1.3788101	139	2,4260077	19	.0055269
BÓ:	3490659	àŏ	1.3962634	140	2.4434610	20	,0058178
21	3665191	81	1.4137167	141	2,4609143	21	.0061087
22 23	.3839724	82	1.4311700	142	8.4783675	22	.0063995
23	.4014257	83	1.4486233	148	2,4958908	23	.0006904
24	.4188790	84	1.4660766	144	2.5132741	24	,0069813
25	.4363323	85	1.4835299	145	2.5307274	25	.0072722
25 26 27 28 29	.4537856	86	1.5009839	146	2.5481807	26	.0075631
27	.4712389	87	1.5184364	147	2.5656340	27	.0078540
28	.4886929	88	1.5358897	148	2.5830873	28	.0081449
89	.5061455	89	1.5533430	149	2.6005406	29	.0084358
50 31	.6235988	90 91	1 5707963	150	2.6179939	30	.0087266
DO 3T	.5410521	92	1.5882496	151 152	2.6854472 2.6529005	31 32	.0090178
32 33	,5759587	93	1.6231562	158	2.6703538	33	.0093084
34 34	5934119	94	1.6406095	154	2.6878070	34	.0095995
35	6108652	95	1.6580638	155	2.7052003	35	.0101811
36	,6283185	96	1.6755101	156	2.7227136	36	.0104790
36 37	,6457718	97	1.6929694	157	2.7401669	37	.0107639
38	6632251	98	1.7104227	158	2,7576208	38	.0110538
39	6800784	99	1.7278760	159	2,7750735	39	.0113446
40	.6981317	100	1.7453293	160	2,7925268	40	.0116355
ii .	.7155850	101	1.7627825	161	2,8099801	41	.0119264
42	.7330383	102	1.7802358	162	2.8274334	42	.0122173
48	.7504916	103	1.7976891	163	8.8448607	43	.0125082
44	,7879149	104	1.8151424	164	2.8623400	44	.0127991
45	.7853982	105 196	1.8325957	165	2.8797933	45	.0130900
16	.0000010		1.8500490	166	2.8972466	46	.0133809
47 48	.8203047 .8377580	107 108	1.8075023	167	2.9146999	47	.0136717
49	.8552113	108	1.8349556 1.9024989	168 1 09	9,9321531 2,9496064	48 49	.0139626
50	.8796646	110	1.9198622	170	2.9670597	50	.0142535
51	.8901179	111	1.9373155	171	2.9645130	51	.0148355
59	.9075713	112	1.9547688	172	8.9019663	52	.0151969
53	9250245	113	1.9722221	178	3.0194196	53	.0154171
53 54	.9424778	114	1.9896753	174	3.0368729	54	.0157000
55	.9599311	115	2.0071286	175	3.0543262	55	.0159989
56 57	.9773844	116	2.0245819	174	3.0717795	56	.0162897
57	.9918377	117	2 0420352	177	3.0892328	57	.0165806
58	1.0122910	118	2.0594885	178	8.1066861 ·	58	.0168715
59	1.0297443	119	2.0769418	179	3.1241394	59	.0171634
60	1.0471976	120	2.0943951	180	3.1415927	80	.0174533

LENGTHS OF CIRCULAR ARCS.

Diameter = 1. Given the Chord and Height of the Arc.)

RULE FOR USE OF THE TABLE.—Divide the height by the chord. Find in the column of heights the number equal to this quotient. Take out the corresponding number from the column of lengths. Multiply this last number by the length of the given chord: the product will be length of the given chord:

sponding number from the column of lengths. Multiply this last number by the length of the given chord; the product will be length of the arc. If the arc is greater than a semicircle, first find the diameter from the formula, Diam. = (square of half chord + rise) + rise; the formula is true whether the arc exceeds a semicircle or not. Then find the circumference. From the diameter subtract the given height of arc, the remainder will be height of the smaller arc of the circle; find its length according to the rule, and subtract it from the circumference.

Hgts.	Lgths.	Hgts.	Lgths.	Hgts.	Lgths.	Hgts.	Leths.	Hgts.	Lgths.
.001	1.00002	.15	1.05896	.238	1.14480	.326	1.26288	.414	1.40788
.005	1.00007	.152	1.06051	.24	1.14714	.328	1.26588	.416	1.41145
.01	1.00027	.154	1.06209	.242	1.14951	.83	1,26892	.418	1.41503
.015	1.00061	.156	1.06368	.244	1.15189	.832	1.27196	.42	1.41861
.02	1.00107	.158	1.06580	.246	1.15428	.334	1.27502	.422	1.42221
.025	1.00167	.16	1.06693	.248	1.15670	.336	1.27810	.424	1.42583
.03	1.00240	.162	1.06858	.25	1.15912	.338	1,28118	.426	1,42945
.035	1.00327	.164	1.07025	.252	1.16156	.84	1.28428	.428	1.43309
-04	1.00426	.166	1.07194	.254	1.16402	.342	1.28739	.43	1,43673
.045	1.00539	.168	1.07365	.256	1.16650	.814	1.29052	.432	1.44089
.05	1.00665	.17	1.07587	.238	1.16899	.346	1.29366	.434	1.44405
.055	1.00805	.172	1.07711	.26	1.17150	.348	1.29681	.436	1.44773
.06	1.00957	.174	1.07888	.262	1.17403	.35	1.29997	.438	1.45142
.065	1.01123	.176	1.08066	.264	1.17657	.852	1.30315	.44	1.45512
.07	1.01802	.178	1.08246	.266	1.17912	.354	1.30634	.442	1.45883
.075	1.01493	.18	1.08428	.268	1.18169	.356	1.30954	.444	1.46255
.08	1.01698	.182	1.08611	.27	1.18429	.856	1.31276	.446	1.46628
.085	1.01916	.184	1.08797	.272	1.18689	.86	1.31599	.448	1.47002
.09	1.02146	.186	1.08984	.274	1.18951	.362	1.31923	.45	1.47377
.095	1.02389	.188	1.09174	.276	1.19214	.864	1.32249	.452	1.47758
.10	1.02646	.19	1.09865	.278	1.19479	.366	1.32577	.454	1.48181
.102	1.02752	.192	1.09557	.28	1.19746	.368	1.32905	.456	1.48509
.104	1.02860	.194	1.09752	.282	1.20014	.87	1.38234	.458	1.48889
.106	1.02970	.196	1.09949	.284	1.20284	.372	1.33564	.46	1.49269
.108	1.03082	.198	1.10147	.286	1.20555	.874	1.33896	.462	1.49651
.11	1.03196	.20	1.10847	.288	1.20827	.876	1.34229	.464	1.50033
,112	1.03312	202	1.10548		1.21102	.378	1.34568	.466	1.50416
.114	1.03430	.204	1.10752	.292	1.21877	.88	1.34899	.468	1.50800
.116	1.03551	.206	1.10958	.294	1.21654	.882	1.35237	.47	1.51185
.118	1.03672	.208	1.11165	.296	1,21933	.884	1.35575	472	1.51571
. 12	1.03797	.21	1.11874	.208	1.22213	.386	1.35914	.474	1.51956
. 122	1.03928	.212	1.11584	.30	1.22495	.388	1.36254	.476	1.52346
. 124	1.04051	.214	1.11796	.802	1.22778	.89	1.36596	.478	1.52736
. 126	1.04181	.216	1.12011	.304	1.28063	.392	1.36989	.48	1.53126
. 128	1.04313	.218	1.12225	.806	1.23349	.894	1.37283	.482	1.53518
.18	1.04447	.22	1.12444	.308	1.28636	896	1.37628	.484	1.53910
. 182	1.04584	222	1.12664	.81	1.23926	.398	1.37974	.486	1.54302
. 134	1.04722	.224	1.12885	.312	1.24216	.40	1.38322	.488	1.54696
.136	1.04962	.226	1.13108	.314	1.24507	.402	1.88671	.49	1.55091
.138	1.05008	.228	1.13331	.816	1.24801	.404	1.39021	.492	1.55487
.14	1.05147	.28	1.13557	.818	1.25095	.406	1.39372	.494	1.55834
.142	1.05298	.232	1.13785	.32	1.25391	.408	1.39724	.496	1.56282
.144	1.05441	.234	1.14015	322	1.25689	.41	1.40077	.498	1.56681
-146	1.05591	.236	1.14247	. 324	1.25988	.412	1.40432	.50	1.57080
.148	1.05743	1	1		1	1		11	1

AREAS OF THE SEGMENTS OF A CIRCLE. (Diameter = 1; Rise or Height in parts of Diameter being given.)

RULE FOR USE OF THE TABLE.—Divide the rise or height of the segment by the diameter. Multiply the area in the table corresponding to the quotient thus found by the square of the diameter.

If the segment exceeds a semicircle its area is area of circle — area of seg-

ment whose rise is (diam. of circle - rise of given segment)

Given chord and rise, to find diameter. Diam = (square of half chord + rise) + rise The half chord is a mean proportional between the two parts into which the chord divides the diameter which is perpendicular to it.

Rise		Rise		Rise		Rise		Rise	
	Area.	+	Area.	+	Area.	1	Area.	+	Area.
Diam.	22.00	Diam.	11100	Diam.	25.1.0	Diam.		Diam.	
]		ll		ll			
.001	.00004	.054 .055	.01646	.107	.04514	.16	.08111	.218	.12285
.002	.00012	.055	.01691	.108	.04576	.161	.08185	.214	.12317
.002 .003 .004 .005 .006 .007 .008	.00022	.056	.01737	.109	.04638	.162	.08258	.215	.12399
.004	.00034	.057	.01783	.11	.04701	.163	.08332	.216	.12481
.005	.00047	.058	.01830 .01877	.111	.04763	.164	.08406	.217	.12568
.006	.00062	.059	.01877	.112	.04826	.165	.08480	.218	.12646
.007	.00078	.06	.01924	.118	.04889	.166	.08554	.219	.12729
.008	.00095	.061	.01972	.114	.04958	.167	.08629	.22	.12811
.009	.00118	.062	.02020	.115	.05016	.168	.08704	.221	.12894
.01 .011 .012 .018	.00188	.068	.02068	.116	.05080	.169	.08779	.223	.12977
.011	.00158	.064	.02117 .02166	.117	.05145	.17	.08854	.224	.13060
.012	.00175	.066		.118	.05274	.171 .172	.09004	.224	.18144
.010	.00197	.067	.02215 .02265	.12	.05338	.178	.09080	.226	.13227 .13311
.014 .015 .016 .017 .018	.0022	.068	.02205	121	.05404	.174	.09155	.227	.13395
.010	.00244	.069	.02366	.122	.05469	.175	.09231	.228	.13478
.010	.00208	.07	.02417	123	.05585	.176	.09231	.229	.13562
.011	.0032	.071	.02468	.124	.05600	177	.09384	.28	19848
.010	.00347	.072	.02520	.125	.05666	.178	.09460	.231	.13646 .13731
.010	.00375	.078	.02571	.126	.05783	.179	.09537	. 600	.18815
0.00	.00403	.074	.02624	.127	.05799	.18	.09618	.232 .233	.13900
.051	.00482	.075	.02676	.128	.05866	.181	.09690	.284	.13984
008	.00462	.076	.02729	.129	.05933	.182	.09767	.285	.14069
.004	.00492	.077	.02782	.13	,06000	188	.09945	236	.14154
025	00598	078	.02886	.131	06067	184	09992	237	.14239
.02 .021 .022 .028 .024 .025 .026	.00523 .00555	.078	.02889	.132	.06067 .06135	.188 .184 .185	.09922	.237 .238	.14324
097	.00587	.08	.02943	.188	.06208	.186	.10077	239	.14409
.027 .028 .029	.00619	.081	.02998	.184	.06271	.187	.10155	.24	.14494
029	.00658	.082	.03058	.185	.06339	.188	10238	.241	.14580
.08	.00687	.088	.03108	.136	.06407	.189	.10238 .10312	.242	.14666
.08 .081	.00721	.084	.03163	.137	.06476	.19	.10390	243	.14751
.032 880.	.00756	.085	.03219 .03275	.138 .189	.06545 .06614	.191	.10469	.244	.14837
.038	.00791	.086	.03275	.189	.06614	.192	.10547	.245	.14923
.084 .085 .036	.00827	.087	.03331	.14	.06683	.193	.10626	.246	.15009
.085	.00864	.088	.03387	.141	.06758	.194	.10705	.247	.15095 .15182
.036	.00901	.089	.03444	.142	.06822	.195	.10784	.248 .249	.15182
087	.00938	.09	.03501	.148	.06892	1.196	.10864	.249	.15268
.088	.00976	.091	.03559	.144	.06968	.197	.10943	l.25 l	. 15355
.039	.01015	.092	.03616	.145	.07033	.198	.11028	.251	.15441
.04	.01054	.093	.03674	.146	.07103	.199	.11102	.252	.15528
.041	.01093	.094	.03782	.147	.07174	.2	.11182	.253	.15615
.042 .048	.01133	.095	.03791 .03850	.148	.07245	.201	.11262	,254	.15702
.048	.01178	.096	.03850	.149	.07316	.202	.11343	.255	.15789
.044	.01214	.097	.03909	.15	.07387	.208	.11423	.256	.15876
.045	.01255	.098	.03968	.151	.07459	.204	.11504	.257	.15964
.044 .045 .046 .047	.01297	.099	.01028	.152	.07531 .07603 .07675	.205	.11584	.258	.16061
.047	.01339	.1	.04087	.158	.07603	.206	.11665	.259	.16139
.048	.01382	.101	.04148	.154	.07675	.207	.11746	.26	.16226
.049	.01425	.102	.04208	.155	.07747	.208	.11827	.261	.16314
.05	.01468	.103	.04269	.156	.07819	.209	.11908	.262	.16402
.051	.01512	.104	.04330	.157	.07892	.21	.11990	.268	.16490
.052	.01556	.105	.04391	.158	.07965	.211	.12071	.264	.16578
.058	.01601	.106	.04452	159	.08038	.212	.12158	.265	.16666

Rise	·	Rise		Rise		Rise		Rise	
+	Area.	+	Area.	+ 1	Area	+	Area	+	Area.
Diam	ì	Diam.		Diam.		Diam.		Diam	
		i		\ <u>'</u>		III			
.266	.16755	.313	.21015	.36	.25455	.407	.30024		0.4000
.200 .267	.16843	.314	.21108	.361	.25551	.408	.30122	.454	.34676
.268	16932	.315	.21201	.862	.25647	.409	.30220	.456	.347 76 .34876
269	.17020	.316	.21294	.363	.25743	.41	.30319	.457	.34975
.27	17109	317	21387	.864	.25839	.411	.30417	.458	.85075
.271	.17198	.318	21480	.365	.25936	412	.30516	.459	.35175
.272	.17287	.319	.21573	.866	.26032	.413	.30614	.46	.85274
.273	.17376	.32	.21667	.367	26128	.414	.30712	.461	.25374
274	.17465	.321	,21760	.368	.26225	.415	30811	.462	.35474
275	.17554	.322	.21853	.869	.26321	.416	.30910	.463	35578
276	.17644	.323	.21947	.87	.26418	417	.31008	.464	.35678
.277	.17733	.324	.22040	.871	.26514	.418	.31107	.465	.85778
.278 .279	.17823	.325	.22184	.872	.26611	.419	.31205	.466	.35873
.279	.17912	.826	.22228	.373	.26708	.42	.31304	.467	.35972
.28	.18002	.327	.22322	.874	.26805	.421	.31403	.468	.36072
.281	.18092	.328	.22415	.375	.26901	.422	.31502	.469	.36172
.282	.18182	.329	.22509	.376	.26998	.423	.31600	.47	.36272
.283	.18272	.83	.22603	.377	.27095	.424	.81699	.471	.36872
.284	.18362	.831	.22697	.378	.27192	.425	.31798	.472	.36471
.285	.18452	.832	.22792	.379	.27289	.426	.31897	.473	.36571
.286	.18542	.883	.22886	.88	.27386	.427	.81996	.474	.36671
.287	.18633	.334	.22980	.381	.27483	.428	.82095	.475	.36771
.288 .299	18728	.335	.28074	.882	.27580	.429	.32194	.476	.36871
.29	.18814 .18905	.337	.23169 .23263	.383	.27678	.43	.32293	.477	.86971
.291	.18996	.338	.23358	.385	.27775 .27872	.431 .482	32392	.478	.37071
.292	.19086	.339	.23453	.386	.27969	.433	.32491 .32590	.479	.87171
.293	.19177	.34	.23547	.387	.28067	.434	.32689	.48 .481	.87270 .37370
.294	.19268	.841	.28642	388	.28164	.435	32788	.482	.37470
295	.19360	342	.23737	389	28262	.436	.32897	.483	.37570
296	.19451	.843	.23832	.89	.28359	.437	32987	.484	.37670
.297	.19542	.344	23927	.391	.28457	438	33086	.485	.87770
.298	.19634	.845	24022	392	28554	.439	.33185	.486	.37870
.299	.19725	.846	.24117	.393	.28652	.44	.88284	.487	.37970
.8	.19817	.817	.24212	.394	.28750	.441	.33384	.488	.38070
.301	.19906	.848	.24307	.395	.28848	.442	.33483	.489	.38170
.302	.20000	.849	.24403	.396	.28945	.448	.33582	.49	.38270
.303	.20092	.85	.24498	.897	.29043	.444	.33682	.491	.38370
.304	,20184	· .851	.24593	.398	.29141	.445	.33781	.492	.38470
.305	.20276	.852	.24689	.399	.29239	.446	.33880	.493	.88570
.306	.20368	.853	.24784	.4	.29337	.447	.33980	.494	.38670
.307	.20460	.854	.24880	.401	.29435	.448	.34079	.495	.38770
.308	.20553	.355	.24976	.402	.29538	.449	.34179	.496	38870
.909	.20645	.356	.25071	.408	.29631	.45	.34278	.497	.38970
.81	.20738	.857	.25167	.404	.29729	.451	.34378	.498	.39070
.811	.20830	.858	.25268	.405	.29827	.452	.84477	.499	.39170
.812	.20923	.359	.25859	.406	.29926	.453	.34577	1.5	.39270

For rules for finding the area of a segment see Mensuration, page 59.

SPHERES.

(Some errors of 1 in the last figure only. From TRAUTWINE.)

Diam.	Sur- face.	Vol- ume.	Diam.	Sur- face.	Vol- ume.	Diam.	Sur- face.	Vol- ume.
1-32	.00307	.00002	8 1/4	33.183	17.974	9 3/6	306.36	504.21
1-16	.01227	.00018	5-16	84.472	19.031	9 % 10.	814.16	523.60
3-32	.02761	.00043	7-16	35.784	20.129		322.06	543.48
5–32	.04909	.00102	7-16	37.122	21.268	24	330.06	563.86
5-32	.07670	.00200	9-18	88.484	22.449	76	338.16	584.74
3–16 7–32	.11045	.00345	9-10	39.872	28.674 24.942	XXXXXX	346.86	606.13
7-82	.15033 .19685	.00548 .00818	56 11-16	41.283 42.719	26.254	3 9	354.66 363.05	628.04 650.46
o_33	.24851	.01165	8/	44.179	27.611	72	971 54	673.42
9-32 5-16 11-82	.30680	.01598	18-16	45.664	29.016	11.	371.54 380.13	696.91
11-82	.37123	.02127	76	47.173	30.466		388.83	720.95
56 13-32 7-16	.44179	.02761	15-16	48.708	31.965	**************************************	897.61	745.51
13-32	.51848	.03511	4.	50.265	38.510	946	406.49	770.64
7–16	.60132	.04385		53.456	36.751	14	415.48	796.33
15-32 16 9-16	.69028 .78540	.05393 .06545	1 3	56.745 60.133	40.195 48.847	29	424.50	822.58
6 18	.99403	.00345	1 ?9	63.617	47.718	33	433.73 443.01	849.40
5-10 5-4	1.2272	.12783	22	67.201	51.801	12. 78	452.89	876.79 904.78
56 11-16	1.4849	.17014	82	70.883	56.116	14	471.44	962.52
3/4	1.7671	22089	XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	74.663	60.663	13	490.87	1022.7
34 13–16	2.0739	.28084	5.	78.540	65.450	\$4	510.71	1085.3
% 15–16	2.4058	35077	1/6	82.516	70.482	13.	580.93	1150.3
15-16	2.7611	.43143	1 14	86.591	75.767	133	551.55 572.55	1218.0
1	3.1416	.52360	19	90.763	81.308	29	572.55	1288.8
1-16	8.5466 8.9761	.62804 .74551	l 29	95.033 99.401	87.113 98.189	14. %	593.95	1361.2 1436.8
3-16	4.4301	.87681	29	103.87	99.541	14.	615.75 637.95	1515.1
1/4	4.9088	1.0227	XXXXXXXX	108.44	106.18	14	660,52	1596.8
5-16	5.4119	1.1839	6. ^{^8}	113.10	118.10	\$2	683.49	1680.8
36 7-16	5.9396	1.8611		117.87	120.81	15.	706 85	1767.3
7-16	6.4919	1.5558	XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	122.72	127.83	14.14.34	730.63	1857.0
9-16	7.0686	1.7671	₹	127.68	185.66	14	754.77	1949.8
9-16	7.6699	1.9974	29	182.78	143.79	%	779.32	2045.7
11-16	8.2957 8.9461	2.2468 2.5161	29	137.89 143.14	152.25 161.03	16.	804.25 829.57	2144.7
11-10	9.6211	2.8062	32	148.49	170.14	14.53	855.29	2246.8 2352.1
13–16	10.321	8.1177	7. 78	153.94	179.59	₹ 2	881.42	2460.6
26	11.044	3.4514		159.49	189.39	17.	907.98	2578.4
₹6 15-16	11.793	3.8083	1 12	165.13	199.53	133	934.88	2687.6
2.	12.566	4.1888	I %∻	170.87	210.08	1,4	962.12	2806.2
1-16	13.364	4.5939	<u>}</u>	176.71	220.89	40 %	989.80	2928.2
3-16	14.186	5.0248	XXXXXXXX	182.66 188.69	282.18	18.	1017.9	3058.6
δ-10 1/2	15.033 15.904	5.4809 5.9641	72	194.83	248.78 255.72	14 14 14 10	1046.4 1075.2	8182.6 8815.8
5-16	16.800	6.4751	8.	201.06	268.08	2	1104.5	3451.5
86	17.721	7.0144		207.39	280.85	19.	1134.1	3591.4
3/8 7-16	18.666	7.5829	12	213.82	294.01	1/4	1164.2	3735.0
9-16	19.635	8.1813	8 ₹	220.36	307.58	14	1194.6	3882.5
9-16	20.629	8.8103	1 1/4	226.98	321.56	- 34	1225.4	4033.7
96 11-16	21.648	9.4708	XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	233.71	885.95	20.	1256.7	4188.8
11-16	22.691	10.164 10.889	1 %	240.58	350.77	14	1288.8	4847.8
34 13–16	23.758 24.850	11.649	9. 18	247.45 254.47	360.02 381.70	1 29	1320.3 1352.7	4510.9
76	25.967	12.448		261.59	397.83	21. %	1385.5	4677.9 4849.1
% 15–16	27.109	18.272	16 14 86 14	268.81	414.41	~~. 1 _{/4}	1418.6	5024.8
8.	28.274	14.137	I 5%	270.12	431.44	12	1452.2	5208.7
1-16	29.465	15.039	1 1/2	283.53	448.92	14 14 14 14	1486.2	5387.4
. 16	30.680 31.919	15.979	98	291.04	466.87	22.	1520.5	5575.3
8-16	31.919	16.957	34	298.65	1 485.31	1/4	1555.3	5787.6

SPHERES.

SPHERES-(Continued.)

Diam.	Sur- face.	Vol- ume.	Diam.	Sur- face.	Vol- ume	Diam.	Sur- face.
22 16	1590.4	5964.1	40 14	5158.1	34788	70 1/2	15615
34	1626.0	6165.2	41.	5281.1	36087	71.	15837
	1661.9	6370.6	12 1/8	5410.7	37428	¾	16061
14	1698.2	6580.6	42.	5541.9	38792	72.	16286
26 /	1735.0	6795.2	43.	5674.5	40194	⅓	16513
. 34	1772.1	7014.3	43. 1/2	5808.8 5944.7	41630 43099	78.	16742 16972
	1809.6	7238.2	44.	6082.1	44602	74. ¹ /2	17204
142	1847.5	7466.7	14	6221.2	46141	14.	17437
23	1885.8	7700.1	45. 78	6861.7	47713	75. ⁷²	17672
. 94	1924.4 1963.5	8181.3	1∕2	6503.9	49821	10.	17908
5.	2002.9	8429.2	46. "	6647.6	50965	76. ^*	18146
34 36 34	2042.8	8682.0	36	6792.9	52645	1/2	18386
22	2083.0	8939.9	47.	6939.9	54362	77.	18626
26. 94	2123.7	9202.8	₹6	7088.3	56115	1/2	18869
14	2164.7	9470.8	48.	7238.8	57906	78.	19114
12	2206.2	9744.0	1/2	7389.9	59784	1/2	19860
14	2248.0	10022	4 9	7548.1	61601	79.	19607
24.	2290.2	10306	-0 1/8	7697.7	63506	80.	19856
1/4	2332.8	10595	50.	7854.0 8011.8	65450 67483		20106 20358
1/4	2375.8	10889	51. ¹ / ₂	8171.2	69456	81.	20612
14 16 34	2419.2	11189	31.	8832.3	71519	51. 1/2	20867
20.	2463.0	11494 11805	52. ⁷⁸	8494.8	78622	82. ⁷²	21124
14 19 34	2507.2	12121	36	8658.9	75767	₩ 146	21382
1/9	2551.8	12443	53. '*	8824.8	77952	83. ^*	21642
34	2596.7	12770	16	8992.0	80178	1/2	21904
29.	2642.1 2687.8	13103	54.	9160.8	82448	84.	22167
14	2734.0	13442	1/2	9331.2	84760	1/2	22432
23	2780.5	13787	55.	9503.2	87114	85	22698
30. 74	2827.4	14137	- 1/2	9676.8	89511	⅓	22966
14	2874.8	14494	56.	9852.0	91953	86.	23235
14	2922.5	14856	57. 3/2	10029	94438 96967	87. ¹ /8	23506 28779
37	2970.6	15224	37. 16	10207 10387	99541		24058
31.	3019.1	15599	58. ⁷⁸	10568	102161	88. ¹ /2	24328
14	3068.0	15979	Jo. 3/2	10751	104826	½	24606
16	8117.3	16366 16758	59. ⁷⁸	10936	107536	89.	24885
34	3166.9	17157	36	11122	110294	1/2	25165
32.	3217.0	17568	60. ^~	11810	118098	90. ′~	25447
14	3267.4	17974	1/2	11499	115949	⅓	25780
29	3369.6	18392	61.	11690	118847	91.	26016
33. 74	3421.2	18817	. ½	11882	121794	1/2	26302
14	3473.3	19248	6 2.	12076	124789	92.	26590
14	3525.7	19685	63. ¹ / ₂	12272 12469	1278 32 130925	98. ¹ /2	26880
87	3578.5	20129		12668	134067		27172 27464
34.	1 2001.		64.	12868	137259	94.	27759
	4 3685.8	21087	14	13070	140501	34. 1/2	28055
3	2 3739.	00440	65. ⁷⁸	18278	143794	95. ⁷²	28353
35.	3848.		W. 1/8	18478	147188	30. 1/2	28652
1	3959		66. /*	13685	150533	96. 78	28953
36.	16 4071 4185		36	18893	153980	16	29255
97			67.	14103	157480	97.	29559
37.	36 4417		3/2	14314	161082	1/2	29865
38	4580	5 28781	68.	14527	164637	98.	30172
90	16 \ 465	6.7 29880	20 ½	14741	168295	· ½	30481
3	50 477	8.4 31059	69.	14957	172007	99.	80791
	16 490	1.7 32270	70.	15175	175774	, ₁₀₀ ½	81103
	40. 50	26.5 33510	= 70.	15894	179595	100.	81416

CONTENTS IN CUBIC FEET AND U. S. GALLONS OF PIPES AND CYLINDERS OF VARIOUS DIAMETERS AND ONE FOOT IN LENGTH.

1 gallon = 231 cubic inches. 1 cubic foot = 7,4805 gallons.

ä	For 1 F Leng		ä	For 1 F Leng		튄.	For 1 F	
Diameter i Inches.	Cubic Ft. also Area in Sq. Ft.	U. S. Gals., 281 Cu. In.	Diameter in Inches.	Cubic Ft. also Area in Sq. Ft.	U. S. Gals., 231 Cu. In.	Diameter in Inches.	Cubic Ft. also Area in Sq. Ft.	U. S. Gals., 231 Cu. In.
5-16 5-16 7-16 14	.0008 .0005 .0008 .001	.0025 .004 .0057 .0078 .0102	634 7 714 714 734	.2485 .2673 .2867 .8068 .8276	1.859 1.999 2.145 2.295 2.45	19 1914 20 2014 21	1.969 2.074 2.182 2.292 2.405	14.78 15.51 16.32 17.15 17.99
9-16 56 11-16 34 13-16	.0017 .0021 3 .0026 .0081 3 .0036	.0129 .0159 .0198 .0280 .0269	8 814 814 814 9	.3491 .8712 .3941 .4176 .4418	2.611 2.777 2.948 3.125 3.305	211/2 22 221/2 23 231/2	2.521 2.640 2.761 2.885 8.012	18.86 19.75 20.66 21.58 22.53
7/6 15-16 1 11/4 11/4	.0042 3 .0048 .0055 .0085 .0128	.0812 .0859 .0408 .0638 .0918	914 914 944 10 1014	.4667 .4922 .5185 .5454 .5780	8.491 3.682 3.879 4.08 4.286	24 25 26 27 28	8.142 8.409 3.687 8.976 4.276	23.50 25.50 27.58 29.74 31.99
184 2 214 214 214 234	.0167 .0218 .0276 .0341 .0412	.1249 .1682 .2066 .2550 .8085	1016 1032 11 1114 1116	.6018 .6303 .66 .6903 .7213	4.498 4.715 4.987 5.164 5.896	29 30 81 32 38	4.587 4.909 5.241 5.585 5.940	84.81 86.72 39.21 41.75 44.48
8 31/4 51/2 83/4 4	.0491 .0576 .0668 .0767	.8672 .4809 .4998 .5738 .6528	1134 12 1214 13 1814	.7530 .7854 .8522 .9218 .994	5.683 5.875 6.375 6.895 7.436	34 35 36 37 38	6.305 6.681 7.069 7.467 7.876	47.16 49.98 52.88 55.86 58.92
414 414 434 5 514	.0985 .1104 .1281 .1864 .1508	.7869 .8268 .9206 1.020 1.125	14 1416 15 1516 16	1.069 1 147 1.227 1.310 1.396	7.997 8.578 9.180 9.801 10.44	89 40 41 42 48	8.296 8.727 9.168 9.621 10.085	62.06 65.28 68.58 71.97 75.44
516 534 6 614 618	.1650 .1808 .1963 .2131 .2304	1.284 1.849 1.469 1.594 1.724	161/2 17 171/2 18 181/2	1.485 1.576 1.670 1.768 1.867	11.11 11.79 12.49 13.22 13.96	44 45 46 47 48	10.559 11.045 11.541 12.048 12.566	78.99 82.62 86.88 90.13 94.00

Given the dimensions of a cylinder in inches, to find its capacity in U. 8. gallons: Square the diameter, multiply by the length and by .0084. If $d = \frac{d^3 \times .7854 \times l}{.081} = .0084d^3l$. 281

To find the capacity of pipes greater than the largest given in the table, look in the table for a pipe of one half the given size, and multiply its capacity by 4; or one of one third its size, and multiply its capacity by 9, etc.

To find the weight of water in any of the given sizes multiply the capacity in cubic feet by 62½ or the gallons by 8½, or, if a closer approximation is required, by the weight of a cubic foot of water at the actual temperature in

CYLINDRICAL VESSELS, TANKS, CISTERNS, ETC. Diameter in Feet and Inches, Area in Square Feet, and U. S. Gallons Capacity for One Foot in Depth.

1 gallon = 281 cubic inches = $\frac{1 \text{ cubic foot}}{7.4805}$ = 0.18368 cubic feet.

Piam. Area. Gals. Diam. Area. Gals. Diam. Area. Gals.					7.4	1800			
The color of the	Diam.	Area.	Gals.	Diam.	Area.	Gals.	Diam.	Area.	Gals.
1 1	Ft. In.	Sq. ft.	1 foot	Ft. In.	Sq. ft.		Ft. In.	Sq. ft.	
1 1	1	.785	5.87	58	25.22		19	288.58	2120 9
1 2 1.069 8.00 5 10 26.73 199.92 19 6 296.65 2294.0 1 3 1.227 9.18 5 11 27.49 205.67 19 9 306.35 2291.7 1 4 1.386 10.44 6 28.27 211.51 20 314.16 2350.1 1 5 1.576 11.79 6 3 30.68 229.50 20 3 320.06 2409.2 1 6 1.767 18.22 6 6 33.18 248.23 20 6 330.06 2469.1 1 7 1.969 14.73 6 9 35.78 267.69 20 9 388.16 2529.6 1 8 2.182 16.32 7 38.48 297.88 21 346.36 2529.6 1 9 2.405 17.99 7 3 41.23 308.81 21 3 364.66 2529.6 1 1 0 2.640 19.75 7 6 44.18 330.49 21 6 383.05 2715.8 1 11 2.885 21.88 7 9 47.17 352.88 21 9 371.54 2779.3 2 1 3.142 23.50 8 50.27 376.01 22 380.13 2843.6 2 2 2 3.667 27.88 8 6 56.75 39.88 21 9 371.54 2779.3 2 4 4.276 31.99 9 63.62 477.89 23 415.48 3049.2 2 5 4.567 34.31 9 3 67.20 502.70 23 3 445.65 3175.9 2 6 4.909 36.72 9 6 70.88 590.24 23 6 438.74 3344.6 2 7 7 5.241 39.21 9 9 78.54 587.52 24 443.01 3314.0 2 8 5.585 41.78 10 88.55 647.74 24 6 471.44 826.6 21 1 6.661 49.98 10 9 90.76 678.95 24 9 481.11 3598.4 3 1 7.467 55.86 11 9 90.76 678.95 24 9 481.11 3598.9 3 1 7.467 55.86 11 9 90.76 678.95 24 9 481.11 3598.9 3 1 7.467 55.86 11 9 108.43 811.14 25 9 520.77 3895.6 3 2 1 1.065 75.44 12 9 17.68 585.09 26 550.99 27 552.07 3895.6 3 1 1.2566 94.00 14 153.94 110.8 27 76.99 25 6 510.71 3890.6 4 1 1 13.095 97.86 12 3 117.86 881.65 26 550.99 27 552.07 3895.6 4 1 1 10.38 16 12.34 110.38 15 12.048 90.18 13 13 1	ī 1	.922	6,89	59		194.25			
1 4 1.896 10.44 6 28.27 211.51 20 3 14.16 280.01 1.576 1.767 13.22 6 6 8 33.18 248.28 20 6 380.06 2409.2 1 7.9169 14.73 6 9 85.78 267.09 20 9 381.61 6 2591.0 1 7 1.969 14.73 6 9 85.78 267.09 20 9 381.61 6 2591.0 1 9 2.405 17.99 7 8 41.28 306.61 21 3 364.66 2655.0 1 1 0 2.640 19.75 7 6 44.18 330.49 21 6 383.06 2715.8 1 11 2.885 21.58 7 9 47.17 352.88 21 9 371.54 2779.3 21 1 8.409 25.50 8 5 0.27 376.01 22 380.13 244.6 22 2 8.687 27.58 8 6 56.75 424.49 22 2 9 406.49 3040.8 2 2 2 8.687 27.58 8 6 56.75 424.49 22 2 9 406.49 3040.8 2 4 4.276 31.99 9 63.62 475.89 23 415.48 31075.9 2 6 4.909 36.72 9 6 70.88 530.24 22 8 684.6 2655.0 2 7 376.0 1 22 9 406.49 3040.8 2 4 4.276 31.99 9 63.62 475.89 23 415.48 31075.9 2 6 4.909 36.72 9 6 70.88 530.24 22 6 6 4.909 36.72 9 6 70.88 530.24 22 6 4.909 36.72 9 6 70.88 530.24 22 6 4.887 34 39.21 9 9 74.66 558.51 23 9 448.01 3314.0 2 9 5.940 44.43 10 3 82.52 617.28 24 462.39 3884.1 2 9 6.305 47.16 10 6 86.59 617.28 24 462.39 3884.1 2 1 6.681 49.98 10 9 90.76 678.52 24 462.39 3884.1 2 1 6.681 49.98 10 9 90.76 678.52 24 462.39 3884.1 3 2 10 6.305 47.16 10 6 86.59 617.28 24 462.39 3884.1 3 2 10 6.305 47.16 10 6 86.59 11 9 50.03 710.90 25 490.87 3872.0 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 40.	12	1.069	8.00	5 10	26.78	199.92	19 6	298.65	2224.0
1 4 1.896 10.44 6 28.27 211.51 20 3 14.16 280.01 1.576 1.767 13.22 6 6 8 33.18 248.28 20 6 380.06 2409.2 1 7.9169 14.73 6 9 85.78 267.09 20 9 381.61 6 2591.0 1 7 1.969 14.73 6 9 85.78 267.09 20 9 381.61 6 2591.0 1 9 2.405 17.99 7 8 41.28 306.61 21 3 364.66 2655.0 1 1 0 2.640 19.75 7 6 44.18 330.49 21 6 383.06 2715.8 1 11 2.885 21.58 7 9 47.17 352.88 21 9 371.54 2779.3 21 1 8.409 25.50 8 5 0.27 376.01 22 380.13 244.6 22 2 8.687 27.58 8 6 56.75 424.49 22 2 9 406.49 3040.8 2 2 2 8.687 27.58 8 6 56.75 424.49 22 2 9 406.49 3040.8 2 4 4.276 31.99 9 63.62 475.89 23 415.48 31075.9 2 6 4.909 36.72 9 6 70.88 530.24 22 8 684.6 2655.0 2 7 376.0 1 22 9 406.49 3040.8 2 4 4.276 31.99 9 63.62 475.89 23 415.48 31075.9 2 6 4.909 36.72 9 6 70.88 530.24 22 6 6 4.909 36.72 9 6 70.88 530.24 22 6 4.909 36.72 9 6 70.88 530.24 22 6 4.887 34 39.21 9 9 74.66 558.51 23 9 448.01 3314.0 2 9 5.940 44.43 10 3 82.52 617.28 24 462.39 3884.1 2 9 6.305 47.16 10 6 86.59 617.28 24 462.39 3884.1 2 1 6.681 49.98 10 9 90.76 678.52 24 462.39 3884.1 2 1 6.681 49.98 10 9 90.76 678.52 24 462.39 3884.1 3 2 10 6.305 47.16 10 6 86.59 617.28 24 462.39 3884.1 3 2 10 6.305 47.16 10 6 86.59 11 9 50.03 710.90 25 490.87 3872.0 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 3 424.56 3 40.25 3 40.	13	1.227		5 11		205.67			
1 6 1.767 18.22 6 6 6 33.18 248.23 20 6 380.06 2469.1 1 7 1.969 14.73 6 9 8.578 207.09 20 9 388.16 5292.6 1 8 2.182 16.82 7 3 88.48 287.89 21 9 346.36 2591.0 1 10 2.640 17.99 7 3 41.28 308.81 21 3 36.86 2651.0 1 11 2.885 21.88 7 9 47.17 352.89 21 9 371.54 2779.3 2 1 8.409 25.50 8 5 5.27 376.01 22 380.13 2448.6 2 2 8.687 27.58 8 6 56.75 244.48 22 9 386.82 2908.6 2 2 8.687 27.58 8 6 56.75 244.48 22 9 406.49 3040.8 2 4 4.276 31.99 9 63.62 475.89 23 415.48 3108.0 2 2 5 4.587 34.81 9 3 67.20 502.70 23 3 424.56 3175.9 2 6 4.909 36.72 9 6 70.88 530.24 23 6 483.74 3040.8 2 2 4 4.276 31.99 9 63.62 475.89 23 445.46 3175.9 2 6 4.909 36.72 9 6 70.88 530.24 23 6 483.74 3040.8 2 2 5 5.585 41.78 10 78.54 587.52 24 46.82 34 44.83 22 29 46.49 3040.8 2 10 6.305 47.16 10 6 86.59 647.74 24 6 471.44 3526.6 2 11 6.681 49.98 10 9 90.76 678.95 24 9 480.13 3314.0 2 10 6.305 47.16 10 6 86.59 647.74 24 6 471.44 3526.6 2 11 6.681 59.88 11 95.03 710.90 25 490.87 3872.0 3 1 7.467 58.98 11 95.03 710.90 25 490.87 3872.0 3 2 7.876 58.98 11 95.03 710.90 25 490.87 3872.0 3 3 8.396 62.06 11 9 108.48 811.14 25 9 500.77 3895.6 3 3 8.296 62.06 11 9 108.48 811.14 25 9 500.77 3895.6 3 3 7.069 58.88 12 113.10 846.03 26 50.00 4204.1 3 8 10.559 78.99 13 182.73 992.91 27 782.56 4283.0 3 1 1.448 80.18 13 9 148.49 1110.8 27 9 500.48 144.81 12.566 94.00 14 153.94 1110.8 27 9 604.81 448.1 12.566 94.00 14 153.94 1110.8 27 9 9 649.18 486.2 24 4 47.84 11.30.95 97.96 14 3 159.48 1113.0 846.03 26 500.74 3745.8 4 4 11.30.95 97.96 14 3 159.48 1193.0 26 6 501.55 140.8 4 4 1 13.095 97.96 14 3 159.48 1193.0 26 6 501.57 140.8 4 14.748 110.8 215 11.786 881.65 26 3 500.77 3895.6 4 11.8 31 1 12.048 90.13 13 9 148.49 1110.8 27 9 9 649.18 486.2 24 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	14	1.396	10.44	6					
2 7 5.241 39.21 9 74.66 558.51 23 9 448.01 3314.0 2 8 5.585 41.78 10 78.54 587.52 24 452.39 3884.1 2 10 6.305 47.16 10 6 86.59 647.72 24 9 461.86 3455.0 2 11 6.681 49.98 10 9 90.76 678.95 24 9 481.11 3858.9 3 1 7.669 58.96 11 95.03 710.90 25 490.87 3875.8 3 2 7.876 58.96 11 9 108.43 811.14 25 9 26 510.71 3820.8 3 4 8.727 65.28 12 1113.10 846.03 26 500.77 3897.6 3 5 9.168 63.58 12 3 117.86 881.65 26 5	1 5	1.576	11.79	6 8			20 8	322.06	
2 7 5.241 39.21 9 74.66 558.51 23 9 448.01 3314.0 2 8 5.585 41.78 10 78.54 587.52 24 452.39 3884.1 2 10 6.305 47.16 10 6 86.59 647.72 24 9 461.86 3455.0 2 11 6.681 49.98 10 9 90.76 678.95 24 9 481.11 3858.9 3 1 7.669 58.96 11 95.03 710.90 25 490.87 3875.8 3 2 7.876 58.96 11 9 108.43 811.14 25 9 26 510.71 3820.8 3 4 8.727 65.28 12 1113.10 846.03 26 500.77 3897.6 3 5 9.168 63.58 12 3 117.86 881.65 26 5	1 5	1.707	18.22				20 0		
2 7 5.241 39.21 9 74.66 558.51 23 9 448.01 3314.0 2 8 5.585 41.78 10 78.54 587.52 24 452.39 3884.1 2 10 6.305 47.16 10 6 86.59 647.72 24 9 461.86 3455.0 2 11 6.681 49.98 10 9 90.76 678.95 24 9 481.11 3858.9 3 1 7.669 58.96 11 95.03 710.90 25 490.87 3875.8 3 2 7.876 58.96 11 9 108.43 811.14 25 9 26 510.71 3820.8 3 4 8.727 65.28 12 1113.10 846.03 26 500.77 3897.6 3 5 9.168 63.58 12 3 117.86 881.65 26 5	1 6		16.82	7 "			91		
2 7 5.241 39.21 9 74.66 558.51 23 9 448.01 3314.0 2 8 5.585 41.78 10 78.54 587.52 24 452.39 3884.1 2 10 6.305 47.16 10 6 86.59 647.72 24 9 461.86 3455.0 2 11 6.681 49.98 10 9 90.76 678.95 24 9 481.11 3858.9 3 1 7.669 58.96 11 95.03 710.90 25 490.87 3875.8 3 2 7.876 58.96 11 9 108.43 811.14 25 9 26 510.71 3820.8 3 4 8.727 65.28 12 1113.10 846.03 26 500.77 3897.6 3 5 9.168 63.58 12 3 117.86 881.65 26 5	1 9		17.99	78	41.28	808.81	21 8		
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5 19.63 146.88 17 226.98 1697.9 81 754.77 554.77 564.75 5 2 20.97 156.83 17 8 23.71 174.82 81 8 76.99 5787.5 5 2 20.97 156.83 17 6 240.53 179.93 81 6 779.31 5829.7 5 3 21.65 161.93 17 9 247.45 1851.1 31 9 791.73 5922.6 5 4 22.84 167.12 18 254.47 1903.6 82 804.25 6016.2 5 5 23.04 172.88 18 2 261.59 1956.8 32 3 16.86 8110.86 6110.8 5 6 28.76 177.73 18 6 268.80 2010.8 32 6 829.57	4 10	18.85	187.25	16 6	213.82	1599.5	80 6	730.62	
5 19.63 146.88 17 226.98 1697.9 81 754.77 554.77 564.75 5 2 20.97 156.83 17 8 23.71 174.82 81 8 76.99 5787.5 5 2 20.97 156.83 17 6 240.53 179.93 81 6 779.31 5829.7 5 3 21.65 161.93 17 9 247.45 1851.1 31 9 791.73 5922.6 5 4 22.84 167.12 18 254.47 1903.6 82 804.25 6016.2 5 5 23.04 172.88 18 2 261.59 1956.8 32 3 16.86 8110.86 6110.8 5 6 28.76 177.73 18 6 268.80 2010.8 32 6 829.57	4 11			16 9		1648.4	30 9	742.64	
5 1 20.29 101.82 17 8 233.71 1748.2 31 8 766.99 5737.5 5 2 20.97 156.83 17 6 240.53 1799.8 31 6 779.31 5829.7 5 3 21.65 161.93 17 9 247.45 1851.1 31 9 791.73 5922.6 5 4 22.34 167.12 18 254.47 1903.6 32 804.25 6016.2 5 5 23.04 172.38 18 2 261.59 1956.8 32 3 816.86 6110.6 5 6 22.76 177.73 18 6 268.80 2010.8 32 6 829.58 6205.7				17			81	754.77	
5 2 20.57 100.65 17 9 240.53 179.5 31 6 779.31 8829.7 5 3 21.65 161.93 17 9 247.45 1851.1 31 9 791.73 5929.6 5 4 228.24 167.12 18 254.47 1908.6 32 804.25 6016.2 5 5 23.76 177.73 8 6 268.80 2010.8 32 8 86.05.7 5 7 24.48 183.15 18 9 276.12 2065.5 32 9 842.39 6301.5	5 1		151.52	17 8			81 8		
5 4 22.34 167.12 18 254.47 1903.6 32 804.25 6016.2 5 5 23.04 172.88 18 2 261.59 1956.8 32 3 816.86 6110.6 5 6 23.76 177.73 18 6 268.80 2010.8 32 6 839.58 6205.7 5 7 24.48 183.15 18 9 276.12 2065.5 32 9 842.39 6301.5	5 2		161 09	17 0	240.08		81 0		5000 4
5 5 28.04 172.88 18 2 261.59 1986.8 32 3 816.86 6110.6 5 6 28.76 177.72 18 6 268.80 2010.8 32 6 829.58 6205.7 5 7 24.48 180.15 18 9 276.12 2065.5 32 9 842.39 6801.5	2 2 1	22.84			254 47				6016 9
5 6 28.76 177.73 18 6 268.80 2010.8 82 6 829.58 6205.7 5 7 24.48 188.15 18 9 276.12 2065.5 32 9 842.89 6801.5	8 3		172.88	18 8			32 3		
5 7 24.48 188.15 18 9 276.12 2065.5 32 9 842.89 6801.5	5 6	28.76	177.79	18 6	268.80	2010.8	82 6	829.58	6205.7
	5 7	24.48	188.15	18 9	276.12	2065.5	82 9	842.89	6801.5

GALLONS AND CUBIC FEET.

United States Gallons in a given Number of Cubic Feet.

1 cubic foot = 7.480519 U. S. gallons; 1 gallon = 231 cu. in. = .13368056 cu. ft.

Cubic Ft.	Gallons.	Cubic Ft.	Gallons.	Cubic Ft.	Gallons.
0.1	0.75	50	374.0	8,000	59,844.2
02	1.50	60	448.8	9,000	67,824.7
0.3	2.24	70	528.6	10,000	74,805.2
0.4	2,99	80	598.4	20,000	149,610.4
0.5	3.74	90	678.2	80,000	224,415.6
0.6	4.49	100	748.0	40,000	299,220.8
0.7	5.24	200	1,496.1	50,000	374,025.9
0.8	5.98	800	2,244.2	60,000	448,831.1
0.9	6.78	400	2,992.2	70,000	523,686.8
1	7.48	500	3,740.3	80,000	598,441.5
2	14.96	600	4,488.8	90,000	673,246.7
8	22,44	700	5,236.4	100,000	748,051.9
2 8 4 5	29.92	800	5,984.4	200,000	1,496,103.8
5	87.40	900	6,732.5	800,000	2,244,155.7
6	44.88	1,000	7,480.5	400,000	2,992,207.6
7	52.36	2,000	14,961.0	500,000	3,740,259.5
8	59.84	8,000	22,441.6	600,000	4,488,311.4
9	67.82	4,000	29,922.1	700,000	5,236,863.8
10	74.80	5,000	37,402.6	800,000	5,984,415.2
20	149.6	6,000	44,883.1	900,000	6,732,467.1
80 40	224.4 299.2	7,000	52,363.6	1,000,000	7,480,519.0

Cubic Feet in a given Number of Gallons.

Gallons.	Cubic Ft.	Gallons.	Cubic Ft.	Gallons.	Cubic Ft.
1 2	.134	1,000 2,000	133,681 267,361	1,000,000	133,680.6 267,861.1
8	.401	3,000	401.042	3,000,000	401,041.7
4	.535	4,000	584.722	4,000,000	584,722.2
5	.668	5,000	668.403	5,000,000	668,402.8
6	.802	6,000	802.083	6,000,000	802:083 3
7	.936	7,000	935.764	7,000,000	985,763.9
8	1.069	8,000	1,069.444	8,000,000	1,069,444.4
9	1.208	9,000	1,203.125	9,000,000	1,203,125.0
10	1.837	10,000	1,386.806	10,000,000	1,386,805.6

NUMBER OF SQUARE FRET IN PLATES 8 TO 35 FEET LONG, AND 1 INCH WIDE.

For other widths, multiply by the width in inches. 1 sq. in. = .00694 sq.

Ft. and In. Long.	Ins. Long.	Square Feet.	Ft. and Ins. Long.	Ins. Long.	Square Feet.	Ft. and Ins. Long.	Ins. Long.	Squar Feet
3. 0	36	.25	7.10 11	94	.6528	13. 8 9	152	1.05
1 2 8 4 5 6 7 8 9 10 11	37 38	.2569 .2639	8. 0	95 96	.6597 .6667	10	153 154	1.06 1.06
8	39 .	.2708	1	97	.6736	11	155	1.07
4	40	.2778	2	98 99	.6806 .6875	18.0	156 157	1.08 1.09
5	41 42	.2847 .2917	4	100	.6944	2	158	1.09
2	43	2986	5	101	.7014	8	159	1.10
· 8	44	.8056	2 8 4 5 6 7 8 9	102 103	.7088 .7158	98 44 56 78 9	160 161	1.11 1.11
9	45 46	.8125 .8194	ន៍	104	.7158	6	162	1.12
10	47	.8264	. 9	105	.7292	7	168	1.13
4. 0	48	.3264 .3333	10 11	106 107	.7861 .7481	8	164	1.13
1	49	.8403 .8472	9. 0	108	.7451	10	166	1.14
2	50 51	.3542	1	109	.7569	11	165 166 167	1.15 1.15
4	52 53	.3611	2	110 111	.7639 .7708	14. Ô	168 169	1.16
4. 0 1 2 8 4 5 6 7 8 9	53	.3681 .375	123456789	112	.7778	2	170	1.17 1.18
7	54 55	.8819	5	113	.7847	8 4 5 6 7 8 9	171	1.18
8	56	.3889	6	114 115	.7917 .7986	4	179 178	1.19 1.20
9	57	.3958 .4028	. ś	116	.8056	6	174	1.20
10	58 59	.4023	. 9	117	.8125	7	175	1.21
5. 0	60	.4167	10	118 119	.8194 .8264	8	176 177	1.22 1.22
1	61	.4236 .4306	10.0	120	.8333	10	178	1.23
2	62 63	4375	1	121	.8403	11	179	1.21
4	64	.4444	2	122 123	.8472	15. 0 1	180	1.25 1.25
5	65	.4514 .4583	4	124	.8542 .8611	2	181 182	1.26
6	66 67	4653	5	125	.8681	3	188	1.27
8	68	4722	10 11 10.0 1 2 3 4 5 6 7 8	126 127	.875 .8819	4	184 185	1.27 1.28
9	69	.4792 .4861	8	123	.8889	6	186	1.29
1 2 8 4 5 6 7 8 9 10	70 71	4931	. 9	129	.8958	2 3 4 5 6 7 .8 9	187	1.29
6. 0	72	.5	10 11	180 181	.9028 .9097	. 8	188 189	1.30 1.31
· 1	72 73 74	.5069 5189	11.0	182	. 9167	10	190	1.81
6. 1 28 45 67 89	74	5208	1	183	.9236	11	191	1.82
4	76	.5278	2 3 4 5 6 7 8 9 10	184 185	.9306 .9375	16.0 1	192 198	1.33 1.34
5	77	.5847 .5417	4	186	.9444		194	1.34
6	78 79	5486	5	187	.9514	8	195	1.35 1 36
ś	80 81	5556	2	188 189	.9588 .9653	4 5	196 197	1.36
ğ	81	.5625 .5694	ė ė	140	.9722	ě	198	1.87
10	82 83	5764	.9	141	.9792	7	199	1.38
7. 0	84	.5834	10	142 148	.9861 .9931	ä	200 201	1.38 1.39
· į	85	5905 5972	11 12.0	144	1.000	2 3 4 5 6 7 8 9 10	202	1.40
2	87	.6042	1	145	1.007	1,11	208	1.41
7. 0 1 2 2 3 4 5 6 7 8 9	86 87 88 89 90 91 92	L 6111	2 8 4 5 6 7	146 147	1.014	17.0 1	204 205	1.41
5	89	6181	4	148	1.021 1.028	2	206	1.43
6	90	.6319	Ď	149	1.085	2 3 4	207	1.43
ģ	92	6389	7	150 151	1.042 1.049	5	208	1.44 1.45
9	93	6458		1		ľ	1	20

SQUARE FEET IN PLATES-(Continued.)

				_				
Ft. and	- 1	~	Ft. and		g	Ft. and		~
Ins.	Ins.	Square	Ins.	Ins.	Square	Ins.	Ins.	Square
Long.	Long.	Feet.	Long.	Long.	Feet.	Long.	Long.	Feet.
	li			l				
15.0	210	1.458	22.5	269	1.868	27. 4	328	2.278
17. 6	211	1.465	22. 5	270	1.875	27.4	329	2.285
8	212	1.472	7	271	1.882	l ĕ	330	2.203
9	218	1.479	8	272	1.889	ľ	831	2.299
10	214	1.486	ğ	278	1.896	l 8	832	2.306
īĭ	215	1.498	10	274	1.903	l j	388	2.318
18. 0	216	1.5	11	275	1.91	10	884	2.319
1	217	1.507	28. 0	276	1.917	11	335	2.326
2	218	1.514	1	277	1.924	28.0	336	2.883
3	219	1.521	2 8	278	1.931	1	887	2.34
4	220 221	1.528 1.585	8 4	279 280	1.938 1.944	2 8	338 339	2.347 2.354
5 6	221	1.542	5	281	1.944	4	340	2.361
7	223	1.549	6	282	1.958	3	341	2.368
8	224	1.556	ž	283	1.965	l š	342	2.875
ğ	225	1.563	ė į	284	1.972	Ž	343	2.382
ŏ	226	1.569	ğ	285	1.979	8	844	2.389
11	227	1.576	10	286	1.986	9	345	2.396
19 . 0	228	1.588	. 11	287	1.993	10	346	2.403
1	229	1.59	24.0	288	2.	11	347	2.41
2	230	1.597	1	289	2.007	29.0	348	2.417
8	231	1.604	2 8	290	2.014 2.021	1 2	849	2.424
4 5	232	1.611 1.618	å	291 292	2.021	1 8	850 851	2.481 2.438
6	234	1.625	3	293	2.035	4	852	2.444
7	235	1.632	8	294	2.042	5	853	2.451
. Š	286	1.639	, 8	295	2.049	6	854	2.458
9	237	1.645	8	296	2.056	7	355	2.465
10	238	1.653	. 9	297	2.068	8	856	2.478
11	239	1.659	10	298	2.069	9	857	2.479
20 . 0	240	1.667	25 11	299	2.076	10	858	2.486
1	241 242	1.674 1.681	25. 0 1	300 301	2.088	30 . 0	859 860	2.498 2.5
2 8	243	1.688	2	302	2.097	30.0	361	2.507
4	244	1.694	l ŝ	303	2.104	2	862	2.514
5	245	1.701	1 4	804	2.111	2 8	863	2.521
ĕ	246	1.708	5 6	305	2.118	4	364	2.528
7	247	1.715	6	306	2.125	5	865	2.535
8	248	1.722	7	307	2.182	6	366	2.542
9	249	1.729	8	308	2.139	7 8	867	2.549
10	250	1.736	9 10	309 810	2.146 2.158		868 869	2.556
21. 0	251 252	1.743 1.75	111	811	2.155	10	870	2.568 2.569
21.0	253	1.757	26.0	812	2.167	ii	871	2.576
2	254	1.764	20. ŭ	813	2.174	81.0	872	2.588
3	255	1.771	2	814	2.181	1	878	2.59
4	256	1.778	l š	815	2.188	8	874	2.597
5	257	1.785	4	816	2.194	. 8	875	2.604
6	258	1.792	Š	817	2.201	4	876	2.611
7 8	259	1.799	6 7	818	2.208	5 6	377	2.618
9	260 261	1.806 1.818	8	819 820	2.215 2.222		378 379	2.625 2.632
10	262	1.819	l ŝ	821	2.229	l ś	880	2.639
11	263	1.826	10	822	2.236	ة ا	881	2.646
22.0	264	1.833	l ii	828	2.248	10	882	2 658
1	265	1.84	27.0	824	2.25	11	888	2.66
2 8	266	1.847	1	325	2.257	82.0	884	2.667
8	267	1.854	2	826	2.264	1 1	885	2.674
4	268	1.861	8	827	2.271	2	886	2.681
	1		•	1	1		1	1

CAPACITIES OF RECTANGULAR TANKS IN U. S. GALLONS, FOR EACH FOOT IN DEPTH.

1 cubic foot = 7.4805 U. S. gallons.

w	idth	Length of Tank.											
(of ink.	feet.	ft.	in.	feet.	ft. in.	feet.	ft. in. 4 6	feet. 5	ft. in. 5 6	feet.	ft. in.	feet.
t.	in.		_		44.00		*0.04				00.00	07.01	104 8
2 2 3 3	6	29.92		.40 3.75	44.88 56.10		59.84 74.80					97.25 121.56	
8	6			••••	67.82	78.54 91.64						145.87 170.18	
4	o			• • • •		91.04						194.49	
4	6	١	١.		l	l	l	151.48	168.31	185.14	201.97	219.80	235.61
5 6 6	_			• • • •	ļ . .			1	1			243.11	
5	6		1	••••			· · · · · ·	1				267.43 291.74	
6	6			• • • •			 	1	1			816.05	
7			1			l	1			l			366.54

w	idth					L	ength o	f Tanl	ε.			
	of ank.	ft. 7	in. 6	feet.	ft. in. 8 6	feet.	ft. in. 9 6	feet. 10	ft. in. 10 6		ft. in. 11 6	feet. 12
ft.	in.	115	.21	119.69	127,17	184.65	142 13	149.61	157.09	164.57	172.05	179.53
2 2 8 8	6 6	140 168).26 3.31 5.86	149.61 179.58 209.45	158.96 190.75	168.31 202.97 285.63	177.66 218.19	187.01 224.41	196.36 235.63	205.71 246.86	215.06 258.07	224.41 269.30
4	•	224	.41	239.37	254.34	269.30	284.26	299.22	814.18	329.14	344.10	359.06
4 5 5 6	6 6	280	2.47 0.52 3.57	269,30 299,22 329,14	817.92		355.32		392.72	411.43	430.13	
6	6	886	.62 l.67	359.06 388.98	881.50	403.94	426.39	448.83	471.27	493,71	516.15	538.59
7	6		2.72).78	418.91 448.58	476.88	504.93	532,98	561.04	589.08	617.14	645.19	628.86 673.24
7889	6		 	478.75	508.67 540.46		604.05	635.84	667 63	699.42	731.21	718.12 763.04 807.89
9. 10	6		• • • •	ļ			675.11	710.65 748.05			817.24 860.26	852.77 897.66
10 11	6		• • • •						824,78		903.26	942.56
11 12	6		• • • •								909,29	1032.3

NUMBER OF BARRELS (81 1-2 GALLONS) IN CISTERNS AND TANKS.

1 Barrel = 31\frac{4}{2} gallons = $\frac{31.5 \times 281}{1728}$ = 4.21094 cubic feet. Reciprocal = .237477.

Depth	Diameter in Feet.											
in Feet.	5	6	7	8	9,	10	11	12	18	14		
1	4.668	6.714	9.189	11.987	15.108	18.652	22.569	26.859	81.522	36 532		
	28.8	33.6	45.7	59.7	75.5	98.8	112.8	184.8	157.6	182.8		
ě	28.0	40.8	54.8	71.6	90.6	111.9	185.4	161.2	189.1	219.8		
7	82.6	47.0	64.0	88.6		180.6	158.0	188.0	220.7	255.9		
5 6 7 8	87.8	58.7	78.1	95.5	120.9	149.2	180.6	214.9	252.2	292.5		
9	42.0	60.4	82.8	107.4	136.0	167.9	203.1	241.7	283.7	329.0		
10	46.6	67.1				186.5	225.7	268.6	315.2	365.6		
11	51.8					205.2	248 8	295.4	346.7	402.1		
12	56.0	80.6				223.8	270.8	322.8	378.8	438.7		
18	60.6	87.3	118.8	155.2	196.4	242.5	293.4	849.2	409.8	478.2		
14	65.3					261.1	816.0	876.0	441.8	511.8		
15	69.9		187.1	179.1	226.6	289.8	338.5	402.9	472.8	548.4		
16						298.4	861.1	429.7	504.4	584.9		
17	79.8					317.1	883.7	456.6	585.9	621.5		
18	83.9	120.9	164.5	214.9	271.9	385.7	406.2	483.5	567.4	658.0		
19	88.6	127.6				354.4	428.8	510.8	598.9	694.6		
20	98 8	184.8	182.8	288.7	802.2	878.0	451.4	587.2	680.4	781.1		

Depth	,			Diamete	r in Feet			
in Feet.	15	16	17	18	19	20	21	22
1	41.966	47.748	53.908	60.481	67.332	74.606	82.258	90.273
5	209.8	288.7	269.5	802.2	836.7	878.0	411.8	451.4
5 6 7 8	251.8	286.5	823.4	862 6	404.0	447.6	498.5	541.6
7	298.8	884.2	877.8	428.0	471.3	522.2	575.8	631.9
8	885.7	882.0	481.2	483.4	538.7	596.8	658.0	722.2
9	877.7	429.7	485 1	543.9	606.0	671.5	740.8	812.5
10	419.7	477.5	589.0	604.8	678.8	746.1	823.5	90%.7
11	461.6	525.2	592.9	664.7	740.7	890.7	904.8	998.0
12	508.6	573.0	646.8	725.2	808.0	895.8	987.0	1083.8
18	545.6	620.7	700.7	785.6	875.8	969.9	1069.8	1178.5
14	587.5	668.5	754.6	846.0	942.6	1044.5	1151.5	1263.8
15	629.5	716.2	808.5	906.5	1010.0	1119.1	1283.8	1354.1
16	671.5	764.0	862.4	966.9	1077.8	1193.7	1316.0	1444.4
17	718.4	811.7	916.4	1027.8	1144.6	1268.3	1398.8	1584.5
18	755.4	859.5	970.3	1087.8	1212.0	1842.9	1480.6	1624.9
19	797.4	907.2	1024.2	1148.2	1279.8	1417.5	1562.8	1715.2
30	889.3	955.0	1078.1	1208.6	1346.6	1492.1	1645.1	1805.5

NUMBER OF BARRELS (31 1-2 GALLONS) IN CISTERNS AND TANKS .- Continued.

Depth				Diamete	r in Feet			
in Feet.	28	24	25	26	27	28	29	80
1	98.666	107.432	116.571	126.083	185.968	146.226	157.858	167.86
5	493.3	537.2	582.9	630.4	679.8	781.1	784.3	839.3
1 5 6	592 0	614.6	699.4	756.5	815.8	877.4	941.1	1007.2
7 8	690.7	752.0	816.0	882.6	951.8	1023.6	1098.0	1175.0
8	789.3	859.5	933.6	1008.7	1087.7	1169.8	1254.9	1342.9
9	888.0	966.9	1049.1	1134.7	1223.7	1316.0	1411.7	1510.8
10	986.7	1074.3	1165.7	1260.8	1359.7	1462.2	1568.6	1678.6
11	1085.3	1181.8	1282.8	1886.9	1495.6	1608.5	1725.4	1846.5
12	1184.0	1289.2	1398.8	1513.0	1631.6	1754.7	1882.8	2014.4
13	1282.7	1396.6	1515.4	1639.1	1767.6	1900.9	2039.2	2182.2
14	1381.3	1504 0	1632.0	1765.2	1903.6	2047.2	2196.0	2350.1
15	1480.0	1611.5	1748.6	1891.2	2039.5	2198.4	2352.9	2517.9
16	1578.7	1718.9	1865.1	2017.3	2175.5	2339.6	2509.7	2685. 8
17	1677.3	1826.3	1981.7	2143.4	2811.5	2485.8	2666.6	2853.7
18	1776.0	1933.8	2098.8	2269.5	2447.4	2632.0	2823.4	8021.5
19	1874.7	2041.2	2214.8	2895.6	2583.4	2778.3	2980.3	3189.4
20	1973.3	2148.6	2821.4	2521.7	2719.4	2924.5	8187.2	3857.8

LOGARITHMS.

Logarithms (abbreviation log).—The log of a number is the exponent The fixed number is the exponent of the power to which it is necessary to raise a fixed number to produce the given number. The fixed number is called the base. Thus if the base is 10, the log of 1000 is 8, for $10^3 = 1000$. There are two systems of logs in generatuse, the common, in which the base is 10, and the Naperian, or hyperbolic, in which the base is 2.718281828.... The Naperian base is commonly de-

noted by e, as in the equation $e^y=x$, in which y is the Nap. log of x. In any system of logs, the log of 1 is 0; the log of the base, taken in that system, is 1. In any system the base of which is greater than 1, the logs of all numbers greater than I are positive and the logs of all numbers less than

l are negative.

The modulus of any system is equal to the reciprocal of the Naperian log of the base of that system. The modulus of the Naperian system is 1, that of the common system is .4342945.

the Naperian log of the number. The hyperbolic or Naperian log of any number equals the common log $\times 2.302651$.

Every log consists of two parts, an entire part called the characteristic, or index, and the decimal part, or mantisso. The mantissa only is given in the usual tables of common logs, with the decimal point omitted. The characteristic is found by a simple rule, viz., it is one less than the number of figures to the left of the decimal point in the number whose log is to be found. Thus the characteristic of numbers from 1 to 9.99 + is 0, from 10 to 9.99 + is 1, from 10 to 9.99 + is 2, from 1 to .99 + is - 1, from .01 to .999 + is - 2, etc. Thus

> log of 2000 is 3.30103; log of .2 is - 1.80103; 200 " 2.30108; 20 " 1.30108; .02 " - 2.30103; .002 " - 8.30103; . 66 66 . . .0002 " - 4,30103. 2 " 0.30103:

The minus sign is frequently written above the characteristic thus: log 002 = 3.30103. The characteristic only is negative, the decimal part, or mantissa, being always positive.

When a log consists of a negative index and a positive mantissa, it is usual

to write the negative sign over the index, or else to add 10 to the index, and to indicate the subtraction of 10 from the resulting logarithm.

Thus $\log .2 = 7.30108$, and this may be written 9.30108 - 10. In tables of logarithmic sines, etc., the -10 is generally omitted, as being understood.

Rules for use of the table of Logarithms.—To find the log of any whole number.—For 1 to 100 inclusive the log is given complete in the small table on page 129.

For 100 to 999 inclusive the decimal part of the log is given opposite the given number in the column headed 0 in the table (including the two figures

to the left, making six figures). Prefix the characteristic, or index. 2.

For 1000 to 9999 inclusive: The last four figures of the log are found opposite the first three figures of the given number and in the vertical column headed with the fourth figure of the given number; prefix the two figures under column 0, and the index, which is 3.

For numbers over 10,000 having five or more digits: Find the decimal part of the log for the first four digits as above, multiply the difference figure in the last column by the remaining digit or digits, and divide by 10 if there be only one digit more, by 100 if there be two more, and so on; add the quotient to the log of the first four digits and prefix the index, which is 4 if there are five digits, 5 if there are six digits, and so on. The table of pro-

portional parts may be used, as shown below.

To find the log of a decimal fraction or of a whole number and a decimal.—First find the log of the quantity as if there were no decimal point, then prefix the index according to rule; the index is one less than the number of figures to the left of the decimal point.

Required log of 8,141598.

To find the number corresponding to a given log.—Find in the table the log nearest to the decimal part of the given log and take the first four digits of the required number from the column N and that on foot of the column containing the log which is the next less than the given log. To find the 5th and 6th digits subtract the log in the table from the given log, multiply the difference by 100, and divide by the figure in the Diff. column opposite the log; annex the quotient to the four digits already found, and place the decimal point according to the rule; the number of figures to the left of the decimal point is one greater than the index.

The index being 0, the number is therefore 8.14159 +.
To multiply two numbers by the use of logarithms,—
Add together the logs of the two numbers, and find the number whose log

To divide two numbers.—Subtract the log of the divisor from the log of the dividend, and find the number whose log is the difference.

To raise a number to any given power.—Multiply the log of the number by the exponent of the power, and find the number whose log is the product.

To find any root of a given number.—Divide the log of the number by the index of the root. The quotient is the log of the root.

To find the reciprocal of a number.—Subtract the decimal

part of the log of the number from 0, add 1 to the index and change the sign of the index. The result is the log of the reciprocal.

Required the reciprocal of 3.141593.

which is the log of 0.81881.

which is the log of v.o.oo..

To find the fourth term of a proportion by logarithms.

—Add the logarithms of the second and third terms, and from their sum subtract the logarithm of the first term.

when one logarithm is to be subtracted from another, it may be more convenient to convert the subtraction into an addition, which may be done by first subtracting the given logarithm from 10, adding the difference to the other logarithm, and afterwards rejecting the 10.

The difference between a given logarithm and 10 is called its arithmetical

The difference between a given logarithm and to is called its arithmetical complement, or cologarithm.

To subtract one logarithm from another is the same as to add its complement and then reject 10 from the result. For $a-b=10-b+\alpha-10$.

To work a proportion, then, by logarithms, add the complement of the logarithm of the first term to the logarithms of the second and third terms. The characteristic must afterwards be diminished by 10.

Example in logarithms with a precedity index. Solve by

Example in logarithms with a negative index.—Solve by garithms $\binom{586}{440}$, which means divide to be 1014 and 1014 logarithms 1011 to the 2.45 power.

In multiplying -1.7 by 5, we say: $5\times7=35$, 3 to carry; $5\times-1=-5$ less +3 carried =-2. In adding -2+8+3+1 carried from previous column, we say: 1+3+8=12, minus 2=10, set down 0 and carry 1; 1+4-2=3

LOGARITHMS OF NUMBERS FROM 1 TO 100.

N.	Log.	N.	Log.	N.	Log.	N.	Log.	N.	Log.
1 2 3 4 5	0.000000 0.301030 0.477121 0.602060 0.698970	21 22 23 24 24 25	1.322219 1.342423 1.361728 1.380211 1.397940	41 42 43 44 45	1.612784 1.623249 1.633468 1.643453 1.653213	61 62 63 64 65	1.785330 1.792892 1.799841 1.806180 1.812913	81 82 83 84 85	1.908485 1.918814 1.919078 1.924279 1.929419
6 7 8 9	0.778151 0.845098 0.908090 0.954248 1.000000	26 27 28 29 29	1.414978 1.481864 1.447158 1.462898 1.477121	46 47 48 49 50	1.662758 1.672098 1.681241 1.690196 1.698970	66 67 68 69 70	1.819544 1.826075 1.832509 1.838849 1.845098	86 87 88 89 90	1.934498 1.939519 1.944483 1.949390 1.954243
11 12 18 14 15	1.041898 1.079181 1.118948 1.146128 1.176091	31 32 33 34 35	1.491362 1.505150 1.518514 1.581479 1.544068	51 52 53 54 55	1.707570 1.716008 1.724276 1.732394 1.740863	71 72 73 74 75	1.851258 1.857332 1.863323 1.869232 1.875061	91 92 93 94 95	1.959041 1.968788 1.968483 1.978128 1.977724
16 17 18 19 20	1.204120 1.230449 1.255278 1.278754 1.301030	86 87 88 89 40	1.556308 1.568202 1.579784 1.591065 1.602060	56 57 58 59 60	1.748188 1.755875 1.763428 1.770852 1.778151	76 77 78 79 80	1.880814 1.886491 1.892095 1.897627 1.903090	96 97 98 99 100	1.982271 1.986772 1.991226 1.995635 2.000000

No.	100 L. 00	0.]							[N	To. 109	L. 040.
N.	0	1	2	8	4	5	6	7	8	9	Diff.
100 1 2	000000 4321 8600	0434 4751 9026	0868 5181 9451	1801 5609 9876	1734 6088	2166 6466	2598 6894	3029 7321	8461 7748	3991 8174	432 428
8 4	012887 7088	8259 7451	3680 7868	4100 8284	0900 4521 8700	0724 4940 9116	1147 5360 9582	1570 5779 9947	1998 6197	2415 6616	424 420
5 6 7	021189 5306 9884	1608 5715 9789	2016 6125	2428 6533	2841 6942	8252 7350	3664 7757	4075 8164	0361 4486 8571	0775 4896 8978	416 412 408
8 9	033424 7428	3826 7825	0195 4227 8228	0600 4628 8620	1004 5029 9017	1408 5480 9414	1812 5880 9811	2216 6230	2619 6629	8021 7028	404 400
	04				1	ll		0207	0602	0998	397

Diff.	1	2	8	4	5	6	7	8	9
134	48.4	86.8	130.2	173.6	217.0	260.4	303.8	347.2	390.
133	48.3	86.6	129.9	173.2	216.5	259.8	803.1	346.4	389.
132	43.2	86.4	129.6	172.8	216.0	259.2	302.4	345.6	388.
31	43.1	86.2	129.3	172.4	215.5	258.6	801.7	344.8	387.
131 130	43.0	86.0	129.0	172.0	215.0	258.0	301.0	344.0	387
29	42.9	85.8	128.7	171.6	214.5	257.4	800.3	848.2	386
28	42.8	85.6	128.4	171.2	214.0	256.8	299.6	342.4	885
27	42.7	85.4	128.1	170.8	213.5	256.2	298.9	841.6	384
126	42.6	85.2	127.8	170.4	213.0	255.6	298.2	340.8	383
125	42.5	85.0	127.5	170.0	212.5	255.0	297.5	840.0	382
124	42.4	84.8	127.2	169.6	212.0	254.4	296.8	339.2	881
23	42.3	84.6	126.9	169.2	211.5	253.8	296.1	838.4	380
122	42.2	84.4	126.6	168.8	211.0	258.2	295.4	837.6	879
121	42.1	84.2	126.8	168.4	210.5	252.6	294.7	336.8	378
120	42.0	84.0	126.0	168.0	210.0	252.0	294.0	836.0	878
119	41.9	83.8	125.7	167.6	209.5	251.4	293.3	335.2	377
118	41.8	83.6	125.4	167.2	209.0	250.8	292.6	834.4	376
117	41.7	88.4	125.1	166.8	208.5	250.2	291.9	888.6	375
116	41.6	88.2	124.8	166.4	208.0	249.6	291.2	832.8	374
115	41.5	88.0	124.5	166.0	207.5	249.0	290.5	832.0	373
114	41.4	82.8	124.2	165.6	207.0	248.4	289.8	331.2	372
118	41.8	82.6	123.9	165.2	206.5	247.8	289.1	330.4	871
112	41.2	82.4	123.6	164.8	206.0	247.2	288.4	829.6	870
111	41.1	82.2	123.8	164.4	205.5	246.6	287.7	328.8	369
110	41.0	82.0	123.0	164.0	205.0	246.0	287.0	898.0	369
109	40.9	81.8	122.7	163.6	204.5	245.4	286.8	827.2	368
108 107	40.8	81.6	122.4	168.2	204.0	244.8	285.6	826.4	367
107	40.7	81.4	122.1	162.8	203.5	244.2	284.9	325.6	866
106	40.6	81.2	121.8	162.4	203.0	243 6	284.2	324.8	365
105	40.5	81.0	121.5	162.0	202.5	243.0	283.5	824.0	864
104	40.4	80.8	121.2	161.6	202.0	242.4 241.8	282.8 282.1	823.2 822.4	368
108	40.8	80.6	120.9	161.2	201.5				362
102 101	40.2	80.4	120.6	160.8	201.0	241 2	281.4	321.6	361
IUI	40.1	80.2	120.8	160.4	200.5	240.6 240.0	280.7 280.0	320.8 320.0	360
400 899	40.0	80.0	120.0	160.0	200.0				360
	89.9	79.8	119.7	159.6	199.5	239.4	279.8	819.2	359
998 907	89.8	79.6	119.4	159.2	199.0	238.8	278.6	818.4	858
897	89.7	79.4	119.1	158.8	198.5	238.2	277.9	817.6	857
896 89	89.6	79.2	118.8	158.4	198.0	237.6	277.2	816.8	356.
<i>,,,</i>	89.5	79.0	118.5	158.0	197.5	237.0	276.5	816.0	855.

LOGARITHMS OF NUMBERS.

No	. 110 L.	041.]							[No	. 13
N	. •	1	2	8	4	5	6	7	8	1
110 1 2	041898 5828 9218	1787 5714 9606	2182 6105 9993	2576 6495	2969 6885	3362 7275	8755 7664	4148 8053	4540 8442	49 86
3 4	053078 6905	3463 7286	3846 7666	0380 4230 8046	0766 4613 8426	1153 4996 8805	1538 5878 9185	1924 5760 9568	2309 6142 9942	26 65
5 6 7	060698 4458 8186	1075 4832 8557	1452 5206 8 928	1829 5580 9298	2206 5958 9668	2582 6 326	2958 6699	3333 7071	3709 7448	09 40 78
8	071882 5547	2250 5912	2617 6276	2985 6640	3352 7004	0088 3718 7868	0407 4085 7731	0776 4451 8094	1145 4816 8457	15 51 86

Diff.	1	2	8	4	5	6	7	8
395 394 393 393 391 390 389 388 387 386	39.5 39.4 39.3 39.2 39.1 39.0 38.9 38.8 38.7	79.0 78.8 78.6 78.4 78.2 78.2 77.6 77.4 77.2 77.6	118.5 118.2 -117.9 117.6 117.3 117.0 116.7 116.4 116.1 115.8 115.5	158.0 157.6 157.2 156.8 156.4 156.0 155.6 155.2 154.8 154.4	197.5 197.0 196.5 196.0 195.5 195.0 194.5 194.0 198.5 198.0 192.5	287.0 236.4 235.8 235.8 234.6 234.0 233.4 232.8 232.8 231.6 231.0	276.5 275.8 275.1 274.4 273.7 273.0 272.3 271.6 270.9 270.9 270.2 269.5	816 816 816 816 816 816 816 810 800 800
384 383 389 381 380 379 378 377 376 376	38.5 38.4 38.3 38.2 38.1 38.0 37.9 37.8 37.7 37.6 37.5	76.6 76.4 76.2 76.0 75.6 75.4 75.2	115.2 114.9 114.6 114.6 114.0 118.7 118.4 118.8 112.5	158.6 158.2 152.8 152.4 152.0 151.6 151.2 150.8 150.4 150.0	192.0 191.5 191.0 190.5 190.0 189.5 189.0 188.5 188.0 187.5	230.4 229.8 229.2 228.6 228.0 227.4 226.8 226.2 225.6 225.0	268.8 268.1 267.4 266.7 266.0 265.3 264.6 263.9 263.2 262.5	30 30 30 30 30 30 30 30 30
374 373 379 371 370 369 368 367 366 565	87.4 87.8 87.2 87.1 87.0 36.9 36.8 30.7 36.6 \$6.5	74.8 74.6 74.4 74.2 74.9 73.6 73.4 73.2	112.2 111.9 111.6 111.0 110.7 110.4 110.8 109.5	149.6 149.2 148.8 148.4 148.0 147.6 147.2 146.8 146.4	187.0 186.5 186.0 185.5 185.0 184.5 184.0 183.5 183.0	224.4 223.8 223.2 222.6 222.0 221.4 220.8 220.2 219.6 219.0	261.8 261.1 260.4 259.7 259.0 258.3 257.6 256.9 256.9 256.2	29 29 29 29 29 29 29 29 29 29 29
364 363 362 361 360 350 350 350	36.4 36.3 36.2 36.1 36.0 35.9 35.9	72.6 72.4 72.2 72.3 72.0 71.6 71.4	109.2 108.9 108.6 108.8 108.0 107.7 107.4 107.1 106.8	145.6 145.2 144.8 144.4 144.0 143.6 143.2 142.8 142.4	182.0 181.5 181.0 180.5 180.0 179.5 179.0 178.5 178.0	218.4 217.8 217.2 216.6 216.0 215.4 214.8 214.2 213.6	254.8 254.1 258.4 252.7 252.0 251.3 250.6 249.9 249.2	29 28 28 28 28 28 28 28 28

No.	120 L. 0	79.]		<u> </u>					[No. 184	L. 130.
N.	0	1	2	8	4	5	6	7	8	9	Diff.
120	079181	9543	9904	0266	0626	0987	1847	1707	2067	2426	360
1 2 8	082785 6360 9905	8144 6716	3508 7071	3861 7426		4576 8136	4984 8490	5291 8845	5647 9198	6004 9552	857 855
4 5	093422 6910	0258 3772 7257	0611 4122 7604	0968 4471 7951	4820	1667 5169 8644	2018 5518 8990	2870 5866 9835	2721 6215 9681	8071 6562	352 349
6	100371 3804	0715 4146	1059 4487	1408	1747 5169	2091 5510	2484 5851	2777 6191	8119 6531	0026 8462 6871	346 343 341
8 -	7210 110590	7549 0926	7888	1599	_	8908 2270	9241 2605	9579 2940	9916 3275	0258 3609	338 335
130	8943 7271	4277 7603	4611 7934	4944 8265		5611 8926	5943 9256	6276 9586	6608 9915	6940 0245	833 830
2 3 4	120574 3852 7105	0903 4178 7429	1231 4504 7758	1560 4830 8076	5156	2216 5481 8722	2544 5806 9045	2871 6131 9368	8198 6456 9690	8525 6781	328 325
	18	. 200	1100		1	1			0000	0012	823
				PR	OPORTIC	NAL PA	RTS.		 ,		
Diff.	1	2	8		4	5	6		7	8	9 .
855 854 853 852 851 850 849 848 847 846	35.5 35.4 35.8 35.2 35.1 85.0 84.9 34.8 34.7 34.6	71.0 70.8 70.6 70.4 70.2 70.0 69.8 69.6 69.4	100 100 100 100 100 100 100 100 100	1.4 1.1 3.8	142.0 141.6 141.2 140.8 140.4 140.0 139.6 139.2 138.8 138.4	177.5 177.0 176.5 176.0 175.5 175.0 174.5 174.0 173.5	218 212. 211. 211. 210. 210. 209. 208. 208. 207.	4 24 8 24 6 24 6 24 0 24 4 24 8 24 6 24	8.5 7.8 7.1 6.4 5.7 5.0 4.3 8.6 2.9 2.2	284.0 283.2 282.4 281.6 280.8 280.0 279.2 276.4 277.6 276.8	819.5 818.6 817.7 816.8 815.9 815.0 814.1 818.2 812.8 811.4
345 344 343 342 341 340 339 338 337 336	84.5 84.4 84.8 84.2 84.1 84.0 83.9 83.8 83.7 83.6	69.0 68.8 68.6 68.4 68.2 68.0 67.8 67.6 67.4	105 106 106 106 106 107 101 101 101	3.2 2.9 2.6 2.8 2.0 1.7	188.0 187.6 187.2 136.8 136.4 136.0 185.6 185.2 184.8 134.4	172.5 172.0 171.5 171.0 170.5 170.0 169.5 169.0 168.5 168.0	207 . 206 . 205 . 205 . 204 . 204 . 208 . 202 . 201 .	4 24 8 24 2 28 6 28 0 28 4 28 8 29 2 28	1.5 0.8 0.1 9.4 8.7 8.0 7.3 6.6 5.9	276.0 275.2 274.4 273.6 272.8 272.0 271.2 270.4 269.6 268.8	810.5 809.6 808.7 807.8 806.9 806.0 805.1 804.2 808.3 802.4
335 334 333 332 331 330 829 328 327 326	33.5 33.4 33.3 33.2 83.1 33.0 32.9 32.8 32.7 82.6	67.0 66.8 66.6 66.4 66.2 66.0 65.8 65.6 65.4 65.2	99 99 96 96		134.0 133.6 133.2 132.8 132.4 132.0 131.6 131.2 130.8 130.4	167.5 167.0 166.5 166.0 165.5 165.0 164.5 164.0 163.5 163.0	201. 200. 199. 199. 198. 198. 197. 196. 196.	4 28 8 28 2 28 6 23 0 23 4 28 8 22 2 22	4.5 8.8 3.1 2.4 1.7 1.0 0.8 9.6 8.9 8.9	268.0 267.2 266.4 265.6 264.8 264.0 268.2 262.4 261.6 260.8	801.5 800.6 299.7 296.8 297.9 297.0 296.1 295.2 294.8 298.4
825 824 823 822	32.5 32.4 32.3 32.2	65.0 64.8 64.6 64.4	97	.5 .2 .9 .6	130.0 129.6 129.2 128.8	162.5 162.0 161.5 161.0	195.0 194.4 198.0 198.0	4 22 8 22	7.5 6.8 6.1 5.4	260.0 259.2 258.4 257.6	292.5 291.6 290.7 289.8

LOGARITHMS OF NUMBERS.

No. 185 L. 130.] [No. 1-												
/ 2	v.	D .	1	2	8	4	5	6	7	8	9	
13 13 7 8	3 (35)	39 21	0655 3858 7037	3 4177	1298 4496 7671	1619 4814 7987	1939 5133 8303	2260 5451 8618	2580 5769 8934	2900 6086 9249	8219 6400 956	
9	14301	-1	0194 8327	0508 3639	0822 3951	1136 4263	1450 4574	1763 4885	2076 5196	2389 5507	270 581	
40 1	612 921		6438 3527	6748 9835	7058	7867	7676 0756	7985 1068	8294 1370	8603 1676	198	
2 8	152288 5836	15	594 640	2900 5943 8965	8205 6246 9266	8510 6549 9567	8815 6852 9868	4120 7154	4424 7457	4728 7759	508 806	
5	8362 161368	10	864 367	1967 4947	2266 5244	2564 5541	2863 5838	0168 3161 6134	0469 3460 6430	0769 3758 6726	106 405 702	
7	4353 7317		50 18	7908	8203	8497	8792	9086	9380	9674	996	
8 9	170262 3186	05 84		0848 37 69	1141 4060	1434 4351	1726 4641	2019 4932	2311 5222	2603 5512	289 580	

Dropoperovit	D

Diff.	1 1	2	3	4	5	6	7	8
21 20 119 118 117 116 115	32.1 32.0 81.9 31.8 31.7 31.6 31.5 31.4 81.3	64.2 64.0 63.8 63.6 63.4 63.2 63.0 62.8 62.6	96.3 96.0 95.7 95.4 95.1 94.8 94.5 94.2 93.6	128.4 128.0 127.6 127.2 126.8 126.4 126.0 125.6 125.2 124.8	160.5 160.0 159.5 159.0 158.5 158.0 157.5 157.0 156.5 156.0	192.6 192.0 191.4 190.8 190.2 189.6 189.0 188.4 187.8 187.8	224.7 224.0 228.8 222.6 221.9 221.2 220.5 219.8 219.1 218.4	256.8 256.0 255.2 254.4 253.6 252.8 252.0 251.2 250.4
12 11 10 10 10 10 10 10 10 10 10 10 10 10	31.2 31.1 31.0 30.9 30.8 30.7 30.6 30.5 30.4 30.3	62.4 62.2 62.0 61.8 61.4 61.2 61.0 60.8	93.3 93.0 92.7 92.4 92.1 91.8 91.5 91.2 90.6	124.4 124.0 128.6 128.2 122.8 122.4 122.4 122.0 121.6 121.2 120.8	155.5 155.0 154.5 154.0 153.5 153.0 152.5 152.0 151.5 151.0	186.6 186.0 185.4 184.3 184.2 183.6 183.0 182.4 181.8 181.2	217.7 217.0 216.3 215.6 214.9 214.2 213.5 212.8 212.1 211.4	248.6 247.5 246.4 245.6 244.6 243.6 243.6 243.6
2 1 0 9 8 7 6 5 8 9 8 9 8	30.2 30.1 30.0 29.9 29.8 29.7 29.6 29.5 29.4 29.3	60.4 60.2 60.0 59.8 59.6 59.4 59.0 58.8 58.6 58.4	90.3 90.0 89.7 89.4 89.1 88.8 88.5 88.5 88.9 87.9	120.4 120.0 119.6 119.2 118.8 118.4 118.0 117.6 117.2 116.8	150.5 150.0 149.5 149.0 148.5 148.0 147.5 147.0 146.5 146.0	180.6 180.0 179.4 178.8 178.9 177.6 177.0 176.4 175.8 175.2	210.7 210.0 209.8 208.6 207.9 207.2 206.5 205.8 205.1 244.4	240.6 240.0 239.8 238.4 237.6 236.6 235.8 234.4
201 200 200 200 200 200 200 200 200 200	7 28	58.2	87.8 87.0 86.7 86.4 86.1 85.8	116.4 116.0 115.6 115.2 114.8 114.4	145.5 145.0 144.5 144.0 148.5 148.0	174.6 174.0 173.4 172.8 172.2 171.6	203.7 203.0 202.3 201.6 200.9 200.2	232.8 232.0 231.2 230.4 229.6 228.8

No.	150 Zz. 17	6.]							[3	No. 169	L. 230.
N.	0	1	2	8	4	5	6	7	8	9	Diff.
150	176091 8977	6381 9264	6670 9552	6959 9839	7248	7536	7825	8113	8401	8689	289
2	181844 4691	2129 4975	2415 5259	2700 5542	0126 2985 5825 8647	0413 3270 6108 8928	0699 3555 6391 9209	0986 8839 6674	1272 4123 6956	1558 4407 7289	287 285 283
4 5	7521 190332 3125	7803 0612 8403	8084 0892 8681	8366 1171 8959	1451 4237	1780 4514	2010 4792	9490 2289 5069	9771 2567 5846	0051 2846 5628	281 279 278
8	5900 8657	6176 8932	6458 9206	6729 9481	7005 9755	7281	7556	7832	8107	8389	276
9	201397	1670	1943	2216	2488	2761	3088	0577 8 905	0850 3577	1194 3848	274 272
160 1 2	4120 6826 9515	4391 7096 9783	4663 7365	4934 7634	5204 7904	5475 8173	5746 8441	6016 8710	6286 8979	6556 9247	271 269
8 4 5	212188 4844 7484	2454 5109 7747	0051 2720 5373 8010	0319 2986 5638 8273	0586 3252 5902 8536	0853 3518 6166 8798	1121 3783 6430 9060	1388 4049 6694 9323	1654 4314 6957 9585	1921 4579 7221 9846	267 266 264 262
6 7 8	220108 2716 5909 7887	0370 2976 5568 8144	0631 8236 5826 8400	0892 3496 6084 8657	1153 8755 6342 8913	1414 4015 6600 9170	1675 4274 6858 9426	1936 4533 7115 9682	2196 4792 7372 9938	2456 5051 7680	261 259 258
	28	0144	0100					8000	8800	0198	256
		· · · · ·	7	PRO	PORTIC	DNAL PA	RTS.	 -			
Diff	. 1	2		<u> </u>	4	5	6		7	8	9
285 284 283 282 281 280 279 278 277 276 275 274 273 272 271	28.5 28.3 28.3 28.0 27.9 27.6 27.5 27.4 27.3 27.1	57.0 56.8 56.6 56.4 56.2 56.0 55.8 55.6 55.4 55.2 54.8 54.8 54.8	84 84 84 83 83 83 82 82 82 82 81 81	.2 .9 .6 .8 .0 .7 .4 .1 .8 .5 .9 .6	114.0 118.6 118.2 112.8 112.4 112.0 111.6 111.2 110.8 110.4 110.0 109.2 108.8 108.4	142.5 141.5 141.0 140.5 140.9 139.0 138.5 138.0 137.5 136.5 136.5	171 170 169 168 168 167 166 165 165 165 164 163 163	.4	99.5 98.8 98.1 97.4 96.7 96.0 95.3 94.6 93.9 93.2 92.5 91.1 90.4 89.7	228.0 227.2 226.4 225.6 224.8 224.0 228.4 221.6 220.8 220.0 219.2 218.4 217.6 216.8	256.5 255.6 254.7 253.8 252.9 252.0 251.1 250.2 249.8 248.4 247.5 246.6 245.7 244.8
270 269 268 267 266 264 268 262	27.0 26.9 26.8 26.7 26.6 26.5 26.4 26.3 26.2	54.0 58.8 53.6 53.4 53.2 53.0 52.8 52.6 52.4	81 80 80 80 79 79 79	.0 .7 .4 .1 .8 .5 .2	108.0 107.6 107.2 106.8 106.4 106.0 105.6 105.2 104.8	135.0 134.5 134.0 135.5 138.0 132.5 132.0 131.5 131.0	162 161 160 160 159 159 158 157	0 1 8 1 8 1 6 1 0 1 4 1 8 1	89.0 88.3 87.6 86.9 86.2 85.5 84.8 84.1	216.0 215.9 214.4 218.6 212.8 212.0 211.2 210.4 209.6	248.0 249.1 241.2 240.8 239.4 238.5 237.6 236.7 285.8
261 260 259 258 257 256 256	26.1 26.0 25.9 25.8 25.7 25.6 25.5	52.2 52.0 51.8 51.6 51.4 51.2 51.0	78 78 77 77 77	.8 .0 .7	104.4 104.0 108.6 108.2 102.8 102.4 102.0	130.5 130.0 129.5 129.0 128.5 128.0 127.5	156 156 155 154 154 158 158	6 1 0 1 4 1 8 1 2 1 6 1	82.7 83.0 81.3 80.6 79.9 79.2 78.5	208.8 208.0 207.2 206.4 205.6 204.8 204.0	284.9 284.0 288.1 289.2 281.8 280.4 239.5

LOGARITHMS OF NUMBERS,

No	. 170 La	220.]							. D	io. 18
N.	. 0	1 1	2	8	4	5	-	7	8	9
170	230445 2996 5528 8046	825 578	0 8504 1 6988	1215 3757 6285 8799	1470 4014 6537 9049	1724 4264 6789 9299	1979 4517 7041 9550	2234 4770 7292 9800	2488 5028 7544	2749 5276 7798
4 5 6 7	249549 3036 5513 7978	0799 8396 5759 8219	1948 3534 6006	1297 8782 6252 8769	1546 4089 6499 8954	1795 4277 6745 9198	9044 4525 6991 9448	2293 4772 7237 9687	0050 2541 5019 7482 9982	0800 2790 5286 7726
٠ إ_	250490 2858	0664 3096	6906 3338	1151 2590	1895	1688 4064	1981 4806	2125 4548	2368 4790	9176 2610 5031
	5273 7679	5514 7918	5755 8158	5996 8596	8637 8637	8877	6718 9116	6958 9355	7198 9594	743 983
	260071 2451 4818 7172	0310 2088 5054 7406	9548 2925 5290 7641 9960	0787 \$162 5525 7875	1025 8399 5761 8110	1268 3636 5996 8344	1501 3878 6282 8578	1739 4109 6467 8812	1976 4346 6702 9046	2214 4583 6937 9278
-	9518 271842 4158 6402	9746 9074 4389 6692	2906 4620 6921	6218 258 8 485 0 7151	0446 2770 5081 7880	9679 8001 5811 7909	0912 8238 5548 7888	1144 8464 5772 8067	1877 8696 6002 8296	1609 3927 6232 8525

Diff.	1 8	3	4	5	. 6	7	8
255 554 552 552 553 553 553 553 553 553 553 553	25.5 50.6	76.2 775.6 775.7 774.1 775.5 772.8 70.8 70.8 70.8 70.8 70.8 70.8 70.8 70	102.0 101.6 101.8 110.8 1100.4 1100.0 99.6 98.8 98.4 98.6 97.6 98.8 98.4 98.6 98.8 98.4 98.6 98.8 98.8 98.8 98.8 98.8 98.8 98.8	127.5 127.0 128.0 128.0 125.5 124.5 124.5 124.5 124.5 122.0 121.5 121.0 120.5	153.0 158.4 151.2 150.6 149.4 148.2 147.6 148.4 145.8 144.6 144.4 145.8 144.6 144.6 144.6 144.6 145.8 14	176.5 177.8 177.1 176.7 177.3 173.8 172.8 172.8 172.8 170.8 170.8 170.8 166.9 166.9 166.9 166.9 166.9 166.9 166.9 166.9 166.9 166.9 166.9 166.9 166.9 166.9 166.9 166.9	204.0 903.2 202.4 201.6 200.8 200.0 199.2 198.4 198.6 198.8 192.8 192.8 192.8 193.6 19

No.	190 L. 27	78.]							[1	No. 214	L. 332.
N.	0	1	2	8	4	5	6	7	8	9	Diff.
190	278754	8982	9211	948	9667	9895	0128	0851	0578	0806	228
1 2	281083 8301	1231 3527	1488 8758	171 897	9 4205	2169 4431	2396 4656	2622 4882	2849 5107	8075 5832	227 226
8 4	5557 7802	5782 8026	6007 8249	628 847		6681 8920	6905 9148	7130 9366	7354 9589	7578 9812	225 228
5 6	290035 2256	0257 2478	0480 2699	070 292	0 8141	1147 8863	1369 8584	1591 8804	1813 4025	2084 4246	222 221
7 8 9	4466 6665 8853	4687 6884 9071	4907 7104 9289	512 732 950	3 7542	5567 7761	5787 7979	6007 8198	6226 8416	6446 8685	220 219
-				-	_	9943	0161	0878	0595	0818	218
200 1 2	301030 3196 5351	1247 3412 5566	1464 3628 5781	168 384 599	4 4059	2114 4275 6425	2331 4491 6639	2547 4706 6854	2764 4921 7068	2980 5136 7282	217 216 215
8 4	7496 9630	7710 9848	7924	818	7 8851	8564	8778	8991	9204	9417	213
Ծ	811754 8867	1966 4078	0056 2177 4289	026 236 449	9 2600	0693 2812 4920	0906 8028 5180	1118 8284 5340	1880 8445 5551	1542 8656 5760	212 211
8	5970 8068	6180 8272	6390 8481	659 868	6809	7018 9106	7227 9314	7486 9522	7646 9780	7854 9938	210 209 208
9	820146	0354	0562	076	-	1184	1891	1598	1805	2012	207
210	2219 4282	2426 4488	2683 4694	285 489	9 5105	8252 5310	8458 5516	8665 5721	8871 5926	6181	206 205
8	6336 8380	6541 8588	6745 8787	698 899		7359 9398	7563 9601	7767 980 5	7972	8176 0211	204
4	830414	0617	0819	102	_	1427	1630	1832	2034	2286	202
		,			Proport	TIONAL	PARTS.	1			
Diff	. 1	2	_	8	4	5	6		7	8	9
225 224	22.5 22.4	45.0 44.8	67	.5 .2	90.0 89.6	112.5 112.0	135 134	4 1	57.5 56.8	180.0 179.2	202.5 201.6
228 222 221	22.8 22.2 22.1	44.6 44.4 44.2	66	3.9 3.6 3.8	89.2 88.8 88.4	111.5 111.0 110.5	188 188 182	.2 1	56.1 55.4 54.7	178.4 177.6 176.8	200.7 199.8 198.9
220 219	22.0 21.9	44.0 43.8	66	.0 .7	88.0 87.6	110.0 109.5	182	0 1	54.0 58.8	176.0 175.2	198.0 197.1
218 217	21.8	43.6 43.4	64	5.4 5.1	87.2 86.8	109.0 108.5	130	.8 1	52.6 51.9	174.4 178.6	196.2 195.3
216 215	21.6 21.5	48.2 43.0	6	l.8 l.5	86.4 86.0	108.0 107.5	129 129	6 1	51.8 50.5	172.8 172.0	194.4 198.5
214 218 212	21.4 21.3 21.2	42.8 42.6 42.4	6	1.2 3.9 3.6	85.6 85.2 84.8	107.0 106.5 106.0	128 127 127	8 1	49.8 49.1 48.4	171.2 170.4 169.6	192.6 191.7 190.8
211 210	21.1 21.0	42.2 42.0	6	3.8 3.0	84.4 84.0	105.5 105.0	126 126	6 1	47.7 47.0	168.8 168.0	189.9 189.0
209 208	20.9 20.8	41.8 41.6	1 63	3.7 3.4	88.6 88.2	104.5 104.0	125 124	8 1	46.8 45.6	167.2 166 4	188.1 187.2
207 208 205	20.7 20.6 20.5	41.4 41.2 41.0	6	2.1 1.8 1.5	82.8 82.4 82.0	108.5 108.0 102.5	124 128 128	6 1	44.9 44.2 43.5	165.6 164.8 164.0	186.8 185.4 184.5
204 208	20.4 20.8	40.8 40.6	6	1. 2).9	81.6 81.2	102.0 101.5	122 121	8 1	42.8 43.1	163.2 162.4	183.6 183.7
908	20.2	40.4	6	0.6	´0.8	101.0	121	ತ 1	41.4	161.6	181.8

LOGARITHMS OF NUMBERS.

	1	1	1			1			1
N.	0	1	2	8	4	5	6	7	8
215	332438	2640	2842	8044	8246	8447	8649	3850	4051
6	4454	4655	4856	5067	5257	5458	5658	5859	6059
7	6460	6660	6860	7060	7260	7459	7659	7858	8058
8	8456	8656	8855	9054	9253	9451	9650	9849	
_			2044	1000	4000	4 105	1000	4000	0047
9	840444	0642	0841	1089	1237	1435	1632	1830	2028
20	2423	2620	2817	8014	8212	8409	3606	3802	8999
	4392	4589	4785	4981	5178	5874	5570	5766	5968
1	6353	6549	6744	6939	7135	7330	7525	7720	791
2 8	8305	8500	8694	8889	9083	9278	9472	9666	9860
٩I			<u> </u>						
4	850248	0442	0636	0829	1023	1216	1410	1603	1796
5	2183	2375	2568	2761	2954	8147	3339	8532	3724
6	4108	4801	4498	4685	4876	5068	5260	5452	5648
	6026	6217	6408	6599	6790	6981	7172	7363	7554
ġ.	7935	8125	8316	8506	8696	8886	9076	9266	945
7 8 9	9835			0404	0700				
-		0025	0215	0404	0593	0783	0972	1161	1350
	361728	1917	2105	2294	2482	2671	2859	3048	3236
330	3612	8800	3988	4176	4368	4551	4739	4926	511
1	5488	5675	5862	6049	6236	6428	6610	6796	6983
2	7356	7542	7729	7915	8101	8287	8473	8659	884
4	9216	9401	9587	9772	9958	!	<u>'</u>		
4	3210					0148	0328	0513	0698
~	871068	1253	1437	1622	1806	1991	2175	2360	2544
5 6	2912	8096	8280	8464	8647	8831	4015	4198	4382
7	4748	4932	5115	5298	5481	5664	5846	6029	6212
7 8	6577	6759	6942	7124	7306	7488	7670	7852	8034
9	8898	8580	8761	8943	9124	9306	9487	9668	9849
9	88							V	

Diff.	1 2	8	4	5	6	7
2011 22 2000 39 1199 11 198 11 197 11 196 12 195 13 192 13 191 190 11 190 12 191 188 1 188 1 188 1 188 1 188 1 188 1 188 1 188 1	0.8 40.4 40.0 1.0 39.6 1.8 39.6 1.7 59.4 239.6 1.5 39.0 1.5 39.0 1.5 39.0 1.5 38.6 1.2 38.2 38.4 38.6 37.6 8.7 37.8 8.8 37.8 8.7 37.8 8.8 37.8 8.8 37.8 8.8 37.8 8.8 38.4 18.1 38.2 18.1 38.2	60.6 60.3 60.0 59.7 59.4 59.1 58.8 58.5 58.2 57.9 57.6 57.3 56.1 56.4 56.1 55.8 55.8 55.9 54.9 54.9	80.8 80.4 80.0 79.2 78.8 77.2 76.8 76.0 76.0 76.2 74.8 74.8 74.0 78.6 78.6 78.6 78.6 78.6 78.6 78.6	101.0 100.5 100.0 99.0 98.5 98.0 97.5 97.5 96.0 96.5 96.0 94.5 94.0 93.5 93.5 93.5 93.5 93.5 93.5 93.5 93.5	121.2 120.6 120.0 119.4 118.8 118.2 117.0 116.4 115.2 114.0 113.4 112.2 111.0 110.4 109.8 109.8 108.6	141.4 140.0 139.3 138.6 137.9 137.2 136.5 135.8 135.1 134.4 139.7 133.0 132.3 131.6 130.9 129.5 128.8 128.1 127.4 126.7

No.	No. 240 L. 380.] [No. 260 L. 421.												
N.	0	1	2	8	4	6	•	8	8	9	Diff.		
240	390911	0393	0578	0754	0984	1115	1998	1476	1656	1887	181		
. 1	2017	2.97	2877 4174	2557 4858	2787 4588	2917 4712	8097 4891	8977 5070	8456 5240	8686 5428	180 179		
20	8815 5606	8995 5785	5964	6149	6821	6499	6677	6856	7084	7212	178		
	7390	7568	7746	7924	8101	8279	8456	8634	8811	8989	178		
5	9166	9843	9520	9698	9875	0619	0500	0004	9011	0900	110		
	3100	2020	-		20.0	0051	0228	0405	0582	0759	177		
6	890935	1112	1288	1464	1641	1817	1993	2169	2345	2521	176		
7	2697	2878	8048	3224	8400	8575	8751	3926	4101	4277	176		
7	4452	4627	4802	4977	5152	5826	5501	5676	5850	6025	175		
ğ	6199	6874	6548	0723	6696	7071	7245	7419	7592	7766	174		
250 1	7940 9674	8114 9847	8287	8461	8684	89 08	9961	9154	9328	9501	178		
-	50.2		0020	0192	0865	0538	0711	6888	1056	1228	178		
2	401401	1578	1745	1917	2089	2261	2488	2605	2777	2949	172		
ã	8121	8292	8464	3635	.3807	3978	4149	4320	4492	4668	171		
4	4884	5005	5176	5346	5517	5688	5858	6029	6199	6870	171		
5	6540	6710	6881	7051	7221 8918	7891	7561	7781	7901	8070	170		
6	8240	8410	8579	8749	8918	9087	9257	9426	9595	9764	169		
7	9933					_		4444	1000	4 154			
_	414000	0102	0271	0440	0609	0777	0946	1114	1283	1451	169		
8	411690	1788	1956	2124	2293 3970	2461	2629	2796	2964	3132	168		
9	8300	8467	3635	8608	1	4187	4805	4472	4639	4806	167		
260	4978	5140	5307	5474	5641	5808	5974	6141	6308	6474	167		
1	6641	6807	6978	7139	7306	7472 9129	7638	7804	7970	8185	106		
2	8801	8467	8633	8798	8964	9129	9295	9460	9625	9791	165		
8	9956	4404		0.54	0010		~~~			-1400			
	404.00	0121	0286	0451	0616	0781	0945	1110	1275	1439	165		
4	421604	1768	1933 8574	9097 3737	2261	2426 4065	2590 4228	2754	2918	9088 4718	164		
5 6	3246 4882	8410 5045	5208	5371	8901 5534	5697	5860	4392 6023	4555 6136	6349	164 163		
7	6511	6674	6836	6999	7161	7324	7486	7648	7811	7978	162		
8	8135	8297	8459	8621	8783	8944	9106	9268	9429	9591	162		
٥	9752	9914	0200	5001	3100	COTE	6100		0240	2001	1		
•	43	"""	0075	0236	0398	0559	0720	0881	1042	1203	161		

Diff.	1	8	8	4	5	6	7	8	9
178 177 176 176 174 178 179 171	17.8 17.7 17.6 17.5 17.4 17.8 17.2 17.1	85.6 85.4 85.2 85.0 84.8 84.6 84.4	53.4 53.1 52.8 52.5 52.2 51.9 51.6 51.8	71.2 70.8 70.4 70.0 69.6 69.2 68.8 68.4 68.0	89.0 88.5 88.0 87.5 87.0 86.5 86.0 85.5	106.8 106.2 105.6 105.0 104.4 108.8 108.2	124.6 123.9 123.2 122.5 121.8 121.1 120.4 111.7	142.4 141.6 140.8 140.0 139.2 136.4 137.6 136.8	160.2 159.8 158.4 157.5 156.6 155.7 154.8 158.9
169 168 167 166 165 164 163 168	17.0 16.9 16.8 16.7 16.6 16.5 16.4 16.3 16.3	84.0 83.8 83.6 83.4 83.2 83.0 82.8 82.6 82.4	51.0 50.7 50.4 50.1 49.8 49.5 49.2 48.9 48.5 48.8	67.6 67.2 66.8 66.4 66.0 65.6 65.2 64.8	84.5 84.0 83.5 83.0 82.5 82.0 81.5 81.0	102.0 101.4 100.8 100.9 99.6 99.0 98.4 97.8 97.2 96.6	119.0 118.8 117.6 116.9 116.2 115.5 114.8 114.1 118.4 118.7	136.0 135.2 134.4 135.6 139.8 138.0 131.9 130.4 129.6 128.8	158.0 152.1 151.2 150.8 149.4 148.5 147.5 146.7 145.8 144.9

N.	•	2	25	8	4	5	•	1	8	9
270	481364	1525	1685	1846	2007	2167	9898	2488	2649	2809
۱ĭ۱	2969	8130	8290	8450	8610	3770	2828 3930	4090	4249	4409
2	4569	4729	4888	5048	5907	5867	5526	5685	5844	600
8	6163	6322	6481	6640	6799	6957	7116	7275	7433	750
4	7751	7909	8067	8226	8884	8542	8701	8859	9017	917
5	9333	9491	9648	9806	9964					
				i 		0122	0279	0437	0594	075
6	440909	1066	1224	1381	1538	1695	1852	2009	2166	232
7	2480	2637	2798	2950	8106	8263	3419	3576	3732	3889
8	4045	4201	4357	4518	4669	4825	4981	5137	5293	5449
9	5604	5760	5915	6071	6226	6382	6537	6692	6848	7003
280	7158	7813	7468	7623	7778	7988	8088	8242	8897	8556
-i	8706	8861	9015	9170	9324	9478	9688	9787	9941	
-										0098
2	450249	0403	0557	0711	0865	1018	1172	1326	1479	1633
8	1786	1940	2093	2247	2400	2553	2706	2859	3012	3168
4	8318	3471	3624	8777	3930	4082	4235	4387	4540	4692
5	4845	4997	5150	5302	5454	5606	5758	5910	6062	6214
6	6366	6518	6670 8184	6821	6973	7125	7276	7428	7579	7731
7	7882	8033	9694	8336 9845	8487 9995	8638	8789	8940	9091	924
8	9392	9548	2024	8045	3430	0146	0296	0447	0597	0748
_	400000	1048	1198	1348	1499	1649	1799	1948	2098	2248
9	460898	1 -								
290	2398	2548	2697	2847	2997	8146	8296	8445	3594	3744
1	3893	4043	4191	4340	4490	4639	4788	4936	5085	5234
2	5383	5532	5680	5829	5977	6126	6274	6423	6571	6719
8	6868	7016	7164	7312	7460	7608	7756	7904	8052	8200
2 3 4 5	8347	8495	8643	8790	8938	9085	9233	9380	9527	9675
5	9823	9969	0116	0263	0410	0557	OFOA	0051	0000	444
	10000	1438	1585	1732	1878	2025	0704 2171	0851 2318	0998 2464	1145 2610
6 7	471292	2908	3049	8195	8341	8487	3633	8779	3925	4071
7	2756	4362	4508	4653	4799	4944	5090	5235	5381	5526
8	4216 5671	5816	5962	6107	6252	6397	6542	6687	6832	6976

Diff.	1	2	3	4	5	6	7	8
161	16.1	32.2	48.3 48.0	64.4	80.5 80.0	96.6 96.0	112.7 112.0	128.8 128.0
160	16.0	32.0	47.7	63.6	79.5	95.4	111.8	127.2
159	15.9	31.6	47.4	63.2	79.0	94.8	110.6	126.4
158	15.8	81.4	47.1	62.8	78.5	94.2	109.9	125.6
157	15.7	31.2	46.8	62.4	78.0	93.6	109.2	124.8
156	15.6	31.0	46.5	62.0	77.5	93.0	108.5	124.0
155	15.5	80,8	46.2	61.6	77.0	92.4	107.8	123.2
154	15.4 15.3	80.6	45.9	61.2	76.5	91.8	107.1	122.4
153	15.2	30.4	45.6	60.8	76.0	91.2	106.4	121.6
152 151	15.1	30.2	45.3	60.4	75.5	90.6	105.7	120 8
	15.0	80.0	45.0	60.0	75.0	90.0	105.0	120.0
150	14.9	29.8	44.7	59.6	74.5	89.4	104.3	119.2
149 148	14.8	29.6	44.4	59.2	74.0	8 8. 8	103.6	1 18.4
147	14.7	29.4	44.1	58.8	73.5	88.2	102.9	117.6
146	14 6	29.2	43.8	58.4	73.0	87.6	102.2	116.8
145	14.5	29.0	43.5	58.0	72.5	87.0	101.5	116.0
144	14.4	28.8	43.2	57.6	72.0	86.4	100.8	115.2
143	14.3	28.6	42.9	57.2	71.5	85.8	100.1	114.4
142	14.2	28.4	42.6	56.8	71.0	85.2	99.4	113.6
141	14.1	28.2	42.8	56.4	70.5	84.6	98.7	112.8
140	14.0	28.0	42.0	56.0	70.0	84.0	98.0	112.0

00 L. 47	7.]							[N	o. 839	L. 531.
0	1	2	8	4	5	6	7	8	9	Diff.
477121 8566	7266 8711	7411 8855	7555 8999	7700 9143	7844 9287	7989 9431	8133 9575	8278 9719	8422 9868	145 144
480007	0151	0294	0438	0582	0725	0869	1012	1156	1299	144
1443	1586	1729	1872	2016	2159	2302	2445	2588	2731	148
2874 4300	3016 4442	3159 4585	3302 4727	3445 4869	3587 5011	3730 5153	3872 5295	4015 5437	4157 5579	143 142
5721	5863	6005	6147	6289	6430	6572	6714	6855	6997	142
7138	7280	7421	7563	7704	7845	7986	8127	8269	8410	141
8551 9958	8692	8833	8974	9114	9255	9396	9537	9677	9818	141
	0099	0239	0380	0520	0661	0801	0941	1081	1222	140
491362	1502	1642	1782	1922	2062	2201	2341	2481	2621	140
2760	2900 4294	3040	8179	8319	8458	3597	3737	8876	4015	189
4155 5544	5683	4433 5822	4572 5960	4711	4850 6238	4989 6376	5128 6515	5267 6653	5406 6791	139 139
6930	7068	7206	7344	6099 7483	7621	7759	7897	8035	8173	138
8311	8448	8586	8724	8862	8999	9137	9275	9412		188
9687	9824	9962		-	\ <u>-</u>	 			-	
501059	1196	1333	0099 1470	0236 1607	0374 1744	0511 1880	0648 2017	0785 2154	0922 2291	137 137
2427	2564	2700	2837	2973	8109	3246	8382	3518	3655	186
3791	3927	4063	4199	4335	4471	4607	4743	4878		136
5150	5286	5421	5557	5698	5828	5964	6099	6284	6370	136
6505	6640	6776	6911	7046	7181	7316	7451	7586	7721	135
7856 9203	7991 9337	8126 9471	8260 9606	8395 9740	8530 9874	8664	8799	8934	9068	185
				-		0009 1349	0143	0277 1616	0411	184
510545 1883	0679 2017	0813 2151	0947 2284	1081 2418	1215 2551	9684	1482 2818	2951	1750 3084	184 183
3218	8351	3484	3617	8750	3883	4016	4149	4282	4415	183
4548	4681	4818	4946	5079	5211	5344	5476	5609	5741	183
5874	6006	6139	6271	6403	6535	6668	6800	6932	7064	182
7196	7328	7460	7592	7724	7855	7987	8119	8251		182
8514 9828	8646 9959	8777	8909	9040	9171	9303	9484	9566	9697	181
		0090	0221	0358	0484	0615	0745	0876	1007	181
521138	1269	1400	1530	1661	1792	1922	2053	2183	2314	181
2444 3746	2575 3876	2705 4006	2835 4136	2966 4266	3096 4396	8226 4526	3356 4656	3486 4785	3616 4915	130
5045	5174	5804	5434	5563	5698	5822	5951	6081		129
6339	6469	6598	6727	6856	6985	7114	7243	7372		129
7630	7759	7888	8016	8145	8274	8402	8581	8060		129
8917	9045	9174	9302	9430	9559	9687	9815	9948		128
30200	0328	0456	0584	0712	0840	0968	1096	1228	1851	128
			Pro	PORTIO	NAL PA	ARTS.				
1	2	1 10	8	4	5	6	1	7	8	9
19.0	007 6		77	55.6	60 K	83.		~ 0	111 0	125.
13.9 13.8	27.8	41	.7	55.2	69.5 69.0	82.		77.8 16.6	111.2 110.4	124.
18.7	27.4	41	.1	54.8	68.5	82.	2 9	5.9	109.6	123.
13.6	27.2	40	.8	54.4	68.0	81.	6 8	5.2	108.8	122.
18.5	27.0	40	0.5	54.0	67.5	81.		4.5	108.0	121.
18.4	26.8	40	.2	58.6	67.0	80.		3.8	107.2	120.
18.3	26.6		.9	53.2	66.5	79.		8.1	106.4	119.
13.2 13.1	26.4 26.2).6).3	52.8 52.4	66.0 65.5	79. 78.	ا ۾	2.4	105.6 104.8	118.
18.0	26.0		.6	52.0	65.0	1 78:		1.6	104.0	117. 117.
12.9	25.8		.7	51.6	64.5	1 77.		0.8	103.2	116.
12.8	25.6	1 39	1.4	51.2	64.0	76.		9.6	102.4	115.
12 7	25.4	1 39	3.1 \	50.8	63.5	76.	2 8	8.9	101.6	114.

- 1				I	1	11		1	,		
N.	0	1	2	8	4	5	6	7	8	9	Diff
340	581479	1607	1784	1862	1990	2117	2245	2872	250 377	0 2627 2 3899	12
1	2754	2882	8009 4280	8136	3264	3391	8518	8645	377	2 3899	12
2	4026	4153	4280	4407	4534	4661	4787	4914	504	5167	12
8	5294	5421	5547	5674 6937	5800	5927	6058	6180	630	6482	18
4	6558	6685	5547 6811 8071	6937	7063	7189	7315	7441	504 630 756 882	5167 6 6482 7 7698	19
5	4026 5294 6558 7819 9076	5421 6685 7945 9202	9327	8197 9452	1990 3264 4534 5800 7063 8322 9578	4661 5927 7189 8448 9708	8518 4787 6058 7315 8574 9829	2872 8645 4914 6180 7441 8699 9954		9901	12
									007 183 257 882	9 0204	15 15 15
7 8	540329 1579	1704	1000	0/05	0000	0000	1000	1205	183	0 1454 8 2701	ניי ו
8	1948	0455 1704 2950	0580 1829 3074	0705 1953 8199	0830 2078 3323	0955 2203 3447	1080 2327 3571	2452 8696	201	2701	1 13
9	2825	2200			0020	10(10)	9911	1			1
350	4068 5307 6543	4192	4316	4440 5678 6913	4004	4000	4012	4936 6172	506 629	0 5188	15
1	5501	0901	0000	8010	2006	0860	0049	0172	023	6 6419	13
28	0040	0000	0109	8144	0007	0000	9510	0005	102	9 7652 8 8881	112
41	7775 9003	4192 5431 6666 7898 9126	5555 6789 8021 9249	9371	4564 5802 7036 8267 9494	4688 5925 7159 8389 9616	4812 6049 7282 8512 9739	7405 8635 9861	752 875 998	8881	ı
٦				OEOE					I	∩1∩@	15 15
2	1450	1579	1604	1916	1099	9080	9121	1004	120	1323	12
21	9888	9700	0473 1694 2911	3033	2155	8976	8908	2510	964	0 2047	1 46
5 6 7 8	2000	anna	4128	0595 1816 3033 4247	4368	0840 2060 8276 4489	4610	4731	485	9 4029	1 46
9	550228 1450 2668 3883 5094	0351 1572 2790 4004 5215	4126 5336	5457	0717 1938 3155 4368 5578	5699	0962 2181 8398 4610 5820	1084 2308 8519 4731 5940	120 242 864 485 606	1 6182	15 15 15
360	6909	6428 7627 8829	6544	6664 7868 9068	6785 7988 9188	6905	7026 8228 9428	7146	726 846	7 7387	15
	7507	7627	7748	7868	7988	8108	82:28	8349 9548	846	9 8589	12
1 2 8	7507 8709 9907	8829	8948		9188	9308	9428	9548	966	7 7387 9 8589 7 9787	12
°		0026 1221 2412 8600 4784 5966 7144	0146 1340 2531 8718 4908 6084 7262	0265 1459 2650 3837 5021 6202 7879	0385 1578 2769 3955	0504 1698 2887 4074	0624 1817 8006 4192 5376 6555 7782	0748	086 205 824 442 561	3 0982	1 11
4	561101 2298	1221	1340	1459	1578	1698	1817	1936 8125 4311	205	3 0982 5 2174 4 3362 9 4548 2 5730 1 6909 7 8084	11
5	2293	2412	2531	2650	2769	2887	8006	8125	824	4 8362	111
6	8481	8600	8718~	3837	3955	4074	4192	4311	442	9 4548	11
4 5 6 7 8 9	8481 4666 5848 7026	4784	4908	5021	5139 6320 7497	5257 6437 7614	5376	5494 6678 7849	561	2 5730	11 11 11
8 (5848	5966	6064	6202	6820	6437	6555	6678	1 078	1 6909	11
						7614			796		
70	8202 9374	831 9 9491	8436 9608	8554 9725	8671 9842	9788 9959	8905	9023	914	0 9257	11
_							0076 1243 2407 8568 4726 5880 7032	0198 1359 2523 3684 4841 5996 7147	030	9 0426	11
28	570548	0660	0776	0893	1010 2174	1126	1243	1859	147	8 1592	11
8	1709	1825	1942	2058 8220	2174	2291	2407	2523	263	2755	11
4	570548 1709 2872 4081 5188	0660 1825 2988 4147	0776 1942 8104 4268 5419	4977	8336	2291 8452 4610	8568	3684	1470 2633 8800 4950 6111	9 0426 6 1592 9 2755 0 8915 7 5072 1 6226 2 7377	11 11 11 11
2	4081 4190	4147	5/10	4379 5534	#494 #8#0	4010 E70F	4120	4841	495	5072	11
2	6341	5808 6457 7607	4570	8807	4494 5650 6802 7951	5765 6917	0880	5990	726	6228	111
6	7492	7607	6572 7722	6687 7836	7051	8066	8181	8295		1017	11 11 11
5 6 7 8 9	8639	8754	8868	8983	9097	9212	9326	9441	8410 955		11
				Рво	PORTIO	NAL PA	RTS.				<u>' </u>
Diff.	1 1	2	1 8		4	5	6		7	8	9

Diff.	1	2	3	4	5	6	7	8	9
128	12.8	25.6	38.4	51.2	64.0	76.8	89.6	102.4	115.2
127 126	12.7	25.4 25.2	38.1 37.8	50.8	63.5	76.2	88.9	101.6	114.3
125	12.5	25.0	87.5	50.4	63.0 62.5	75.6 75.0	88.2 87.5	100.8	113.4 112.5
124	12.4	24.8	37.2	49.6	62.0	74.4	86.8	99.2	111.6
123	12.3	24.6	86.9	49.2	61.5	73.8	86.1	98.4	110.7
122 121	12.2	24.4	36.6	48.8	61.0	73.2	85.4	97.6	109.8
121	12.1	24.2	36.3	48.4	60.5	72.6	84.7	96.8	108.9
120	12.0	24.0	36.0	48.0	6 0.0	72.0	84.0	96.0	108.0
119	11.9	23.8	35.7	47.6	59.5	71.4	83.3	95.2	107.1

	380. I. 5	19.]							Tr.	io. 414	Pr 014
N.	0	1	8	8	4	5	6	7	8	9	Diff.
80	579784	9898	0018	0126	0941	0855	0469	0588	0697	0811	114
1	580925	1039	1153	1267	1881	1495	1608	1722	1836	1950	111
2	2063	2177	2291	2404	2518	2631	2745	2858	2972	8085	
3	8199	3312	2291 3426	8539	2518 3652	3765	3879	8992	4105	4218	İ
4 1	4331	4444	4557	4670	4783	4896 6024	5009	5122	5235 6362	5348	11
5 6 7 8	5461 6587	5574 6700 7823	5686 6812	5799	5912 7037	7149	6137	6250 7374	7486	6475	
7	7711	7829	7985	6925 8047	8160	8272	7262 8384	8496	8608	8720	11
8	7711 8832 9950	8944	9056	9167	8160 9279	9391	9508	9615	9726	7599 8720 9838	
9	9950		0100	0004	0006	0507	0619	0780	0842	0958	l
	BOLOGE	0061	0178	0284	0396	11					1
390 1	591065	1176 2288	1287 2399	1399 2510	1510 2621	1621 2732	1732 2843	1848 2954	1955 8064	2066 8175	11
2	2177 3286	3397	3508	3618	8729	3840	8950	4061	4171	4282	٠,
2	4393	4503	4614	3618 4724	4834	4945	5055	5165	5276	5386	l
4 1	5496	5606 6707 7805 8900	5717	5827 6927	5937 7087	6047	6157	6267	6377 7476	6487	11
507	6597	6707	6817	6927	7087	7146 8243	7256 8358	7366 8462	7476	7586	l "
ည္အ	7695 9701	8000	7914 9009	8024 9119	8134 9228	9337	9446	9556	8572 9665	8681 9774	1
8	8791 9883	9992		0119	- Banks	2001			-		10
- [0101	0210	0319	0428	0537	0646	0755	0864	ľ
9	600978	1089	1191	1299	1408	1517	1625	1784	1848	1951	l
400	2060	2169	2277	2386	2494	2603	2711	2819 3902 4982	2928	3036	l
1	3144	3253	3361	8469	3577	3686	8794	8902	4010	4118	10
2	4226	4334	4442 5521	4550 5628	4658	4766 5844	4874 5951	6059	5089 6166	5197 6274	l
2	5305 6381	5418 6489	6596	6704	5736 6811	6919	7026	7133	7241	7348	1
2 8 4 5	7455	7562	7669	7777	7884	7991	8098	8205	8312	8419	10
6	8526	8633	8740 9808	7777 8847	8954	9061	9167	9274	9381	9488	۱ - ۲
7	9594	9701	9808	9914	0021	0128	0234	0841	0447	0554	1
8	610660	0767	0878	0979	1086	1192	1298	1405	1511	1617	1
8	1728	1829	1986	2043	2148	2254	1298 2360	9466	1511 2572	1617 2678	10
410	2784	2890	2996	8102	3207	8313	8419	8525	8680	8736	~``
1	8842	8947	4058	4159	4264	4370	4475	4581	4686	4792 5845	1
3	4897	5008	5108	5218	5319	5424	5529	5634 6686	5740	8845	10
3 4	5950 7000	6055 7105	6160 7210	6265 7315	6370 7420	6476 7525	6581 7629	7734	6790 7839	6895 7948	"
		·	<u> </u>		PORTIO	NAL PA	RTS.				
Dif	r. 1]	2	1	в	4	5	6		7	8	9
118	11.8 11.7	23.6	85	.4	47.2	59.0	70.	8 8	8.6	94.4	106
117	11.7	23.4	85	.1	46.8	58.5	70.5	8 8	1.9 I	98.6	105
116 115	11.6 11.5	23.2 23.0		.8	46.4 46.0	58.0 57.5	69.0		1.2	92.8 92.0	104
114	11.4	22.8	84	.2	45.6	57.0	68.4	1 2	9.8	91.2	108 102
113	11.8	22.6 22.4	88	.9	45.2	56.5	67.8	3 71	9.1	90.4	101
112	11.2			.6	44.8	56.0	67.5	3 20	3.4	89.6	100
111	11.1 11.0	22.9			44.4	55.5	66. 66.	3 7	7.7	88.8 88.0	99
110 109 108	11.0	22.0		.0	44.0	55.0	66.) 7	7.0	88.0	99
109	10.9	21.8 21.6	82	.7	43.6	54.5 54.0	65.	1 7	3.8	87.2	98
107	10.8 10.7	21.4		1	43.2 42.8	53.5	64.6	7	5.6	86.4 85.6	97
107 106	10.6	21.2	81	.8 l	42.4	5 8.0	63.6	3 84	1.9	84.8	96
105	10.5	21.0	81	.5	42.0	K2 5	68.0) 1 7	3.8	84.0	94
104	10.4	20.8			41.6	52.0	62.		8.5	83.2	98

1101	415 L. 6	18.]								[N	e. 4
N.	0	1		2	8	4	6	6	7	8	8
15	618048 9098	8158 9198		9257 9802	8962 9406	8466 9511	8571 9615	8676 9719	8780 9824	8884 9928	89
7 8 9	620186 1176 2214	0240 1280 2818	1	0844 1884 2421	0448 1488 2525	0552 1592 2628	0656 1695 2788	0760 1799 2885	0864 1903 2089	0968 2007 8042	10 2:
20 1 2 3	8249 4282 5812 6840	3353 4885 5415 6448	4	3456 4488 5518 3546	8559 4591 5621 6648	8663 4695 5724 6751	8766 4798 5827 6853	3869 4901 5929 6956	8978 5004 6082 7058	4076 5107 6185 7161	55 65 75
4 5	7366 8389 9410	7468 8491 9 512	٤	7571 3593 3613	7673 8695 9715	7775 8797 9817	7878 8900 9919	7980 9002	8082 9104 0128	8185 9906 0224	88
7 8 9	690428 1444 2457	0530 1545 2559	1	3631 1647 2660	0733 1748 2761	0835 1849 2862	0986 1951 2963	0021 1038 2052 8064	1139 2159 8165	1241 2255 8266	12 22 8
1 2 8 4 5	8468 4477 5484 6488 7490 8489	8569 4578 5584 6588 7590 8589	4.4	9670 1679 5685 6688 7690 8689	8771 4779 5785 6789 7790 8789	3872 4880 5886 6889 7890 8888	8978 4981 5986 6989 7990 8988	4074 5081 6087 7089 8090 9088	4175 5182 6187 7189 8190 9188	4276 5288 6287 7290 8290 9287	44 56 78 88
6 7 8 9	9486 640481 1474 2465	9586 0581 1573 2563	-	9686 0680 1672 2662	9785 0779 1771 2761	9885 0879 1871 2860	9984 0978 1970 2959	0084 1077 2069 3058	0188 1177 2168 8156	0283 1276 2267 8255	0 1 2 8
10 1 2 3 4 5	8458 4489 5422 6404 7383 8360 9335	8551 4537 5521 6508 7481 8458 9432		3650 4636 5619 6600 7579 8555 9530	8749 4734 5717 6698 7676 8653 9627	8847 4832 5815 6796 7774 8750 9724	8946 4931 5913 6894 7872 8848 9821	4044 5029 6011 6992 7969 8945 9919	4148 5127 6110 7089 8067 9043	4242 5226 6208 7187 8165 9140	56 67 88 98
6 7 8 9	650306	0400 1373 234	5 8	0502 1472 2440	0599 1569 25 36	0696 1666 2633	0798 1762 2780	0890 1859 2826	0016 0987 1956 2928	0118 1084 2058 3019	2 8
450 1 2 2 4	617 618 609 1 708 5 801	7 427 6 523 6 619 6 715 11 810	8 4 2 7	8405 4869 5881 6290 7247 8202 9155	8502 4465 5427 6386 7343 8298 9250	8598 4562 5528 6482 7438 8393 9346	8695 4658 5619 6577 7534 8488 9441	8791 4754 5715 6673 7629 8584 9586	8888 4850 5810 6769 7725 8679 9631	8984 4946 5906 6864 7820 8774 9726	44 56 66 77 88 98
	8 6608	16 001	1	0106 1055 2002	0201 1150 2096	0296 1245 2191	0891 1339 2286	8486 1434 2380	0581 1529 2475	0676 1623 2569	0 1 2
[_			200		1	PORTIO	170	1	-1-	S. T	
1	Diff.	1	8		3	4	5	6	1	7	
/	104 108 103	0.8 2 0.2 2 10.1 2 10.0 2	1.0 0.8 0.6 0.4 0.2 0.0	81 81 80 80 80 80 29	.6 .8	42.0 41.6 41.2 40.8 40.4 40.0 89.6	52.5 52.0 51.5 51.0 50.5 50.0 49.5	63.6 62.4 61.5 60.6 60.6 59.4	1 77 3 77 3 77 3 70	3.5 2 8 2 1 1.4 0 7 0 0	84 88 82 81 80 80 79

N.	0	1	2	8	4	5	6	7	8	9	Diff.
160	662758	2852	2947	3041	8135	3230	3324	8418	3512	3607	
1	8701	3795	3889	3983	4078	4172	4266	4360 5299	4454	4548	1
2	4642	4736	4830	4924	4078 5018	5112	5206	5299	5393	5487	94
8	5581 6518	5675	5769 6705	5862 6799	5956 6892	6050 6986	6148 7079	6237 7178	5393 6331 7266	6424	1
4	6518	6612	6705	6799	6892	6986	7079	7178	7266	7360	!
5	7453	7546	7640	7788	7826 8759	7920	8018	8106	8199	8293	i i
6	8386	8479	8572	8665	8759	8852	8945	9038	9181	9224	1
7	9317	9410	9503	9596	9689	9782	9875	9967	0060	0153	98
8	670246	0339	0431	0524	0617	0710	0802	0895	0988	1080	~
ğ	1178	1265	1358	1451	1543	1636	1728	1821	1913	2005	1
470		2190				2560	2652	2744		2929	l
1	2098 3021	8118	2283 3205	8297	2467 3390	3482	8574	3666	2836 3758	3850	
	8942	4034	4126	2375 3297 4218	4310 5228	4402	4494	4586	4677	4769	92
2 8	4861	4953	5045	5137	5228	5320	5412	5503	5595	5687	
4	4861 5778	5870	5962	6053	6145	6236	6328	6419	6511	6602	1
- 5	6694	6785	6876	6968 7881 8791	7059 7972	7151	7242	7333	7424	7516	
6	7607	7698	7789	7881	7972	8063	8154	8245	8336	8427	1 .
7	8518	8609	8700	8791	8882 9791	8973 9882	9064	9155	9246	9337	91
8	9428	9519	9610	9700	9791	9882	9973	0000	0174	2045	1
9	680336	0426	0517	0607	0698	0789	0879	0063 0970	0154 1060	0245 1151	l
480	1241	1332 2235 3137	1422 2326 8227 4127	1518	1603	1693	1784	1874	1964	2055	
1	2145	2235	2326	2416	2506	2596	2686	2777	2867	2957	l
2 8	8047	8137	3227	8317	3407	8497	3587	3677	3767	8857 4756	90
8	8947	1 40337	4127	4217	4307 5204 6100	4396	4486	4576	4666	4756	ł
4	4845	4935 5831	0020	5114	5204	5 894 6189	5383 6279	5473	5563	5652	l
5	5742	5831	5921	6010	6100	6189	6279	6368	6458	6547	l
ě	6636	6726	6815	6904	6994	7083	7172	7261	7851	7440	ı
7	7529 8420	7618	7707 8598	7796	7886 8776	7975	8064 8953	8153	8242 9131	8331 9220	89
8	9309	8509 9398	9486	8687 9575	9664	8865 9753	9841	9042 9930	8191	8220	i .
y	8008	8080	8400	8015	9004	9100	9031	8800	0019	0107	1
490	690196	0285	0878	0462	0550	0639	0728	0816	0905		
1	1081	1170	0873 1258	1347	1435	1524	1612	1700	1789	0993 1877	l
2	1965	2053 2935 3815 4693	2142	1847 2230	0550 1435 2318	2406	2494	1700 2583	1789 2671	2759	1
ã	1965 2847	2935	3023	3111	3199	3287	3375	8463	8551	3639	86
4	3727	3815	8903	8991	4078	4166	4254	4342	4430	4517	
	4605	4693	8903 4781	4868	4956	5044	5181	5219	5307	5394	ı
5 6	5482 6356	5559	5657	5744	5832	5919	6007	6094	6182	6269	l
8	6356	6444	6531	6618	6706	6793	6880	6968	7055	7142	ı
8	7229 8100	7817	7404	7491	7578	7665	7752	7839	7926	8014	87
9	8100	8188	8275	8362	8449	8585	8622	8709	8796	8883	1 57

·									Î
Diff.	1	2	8	4	5	6	7	8	9
98 97 96 95 94 98 92 91	9.8 9.7 9.6 9.5 9.4 9.8 9.2 9.1	19.6 19.4 19.2 19.0 18.8 18.6 18.4	29.4 29.1 28.8 28.5 28.2 27.9 27.6 27.8	39.2 38.5 38.4 38.0 37.6 87.2 86.8 36.4	49.0 48.5 48.0 47.5 47.0 46.5 46.0 45.5	58.8 58.2 57.6 57.0 56.4 55.8 55.2 54.6	68.6 67.9 67.2 66.5 65.8 65.1 64.4 63.7	78.4 77.6 76.8 76.0 75.2 74.4 78.6 72.8	88.2 87.3 86.4 85.5 84.6 83.7 89.8 81.9
90 89 88	9.0 8.9 8.8 8.7	18.0 17.8 17.6 17.4	27.0 26.7 26.4 26.1	86.0 85.6 85.2 84.8	45.0 44.5 44.0 43.5	54.0 58.4 52.8 52.2	63.0 62.3 61.6 60.9	72.0 71.2 70.4 69.6	81.0 80.1 79.2 78.8
	8.6	17.2	25.8	84.4	43.0	51.6	60.2	68.8	77.4

No.	500	L. 6	6.]							[]	No.
N.		0	1	2	8	4	5	6	7	8	
500		8970 9638	9057 9924	9144	9231	9317	9404	9491	9578	9664	9
2	<u> </u>	0704	0790	0011 0877	0098 0963		0271 1136	0858 1222	0444 1809	0531 1395	0
8		1568	1654	1741	1827	1918	1999	2086	2172	2258	2
4		2431 3291	2517 3377	2603 3463	2689 3549		2861 8721	2947 3807	3083 3893	3119 3979	3 4
5 6		1151	4236	4322	4408	4494	4579	4665	4751	4837	4
7 1		5008	5094	5179 6085	5265 6120		5486	5522	560?	5693	5
8 9	ē	8864 3718	5949 6808	6888	6974		6291 7144	6876 7229	6462 7815	6547 7400	6
510	7	570	7655	7740	7826		7996	8081	8166	8251	8
1 2		270	8506 9855	8591 9440	8676 9524		8846 9694	8931 9779	9015 9863	9100 9948	9
	7716	117	0202	0287	0371	0456	0540	0625	0710	0794	0
3 4	710	963	1048	1132	1217	1301	1385	1470	1554	1639	1
5	1	807	1892 2734	1976	2060		2229	2313	2897	2481	2
6		650 491	8575	2818 3659	2902 3742	2986 3826	3070 3910	8154 3994	3238 4078	8323 4162	8
8	4	1330	4414	4497	4581	4665	4749	4833	4916	5000	5
9	_	5167	5251 6087	5335 6170	5418 6254		5586 6421	5669 6504	5758 6588	.5836	5
520		3003 3838	6921	7004	7088		7254	7888	7421	6671 7504	6
2 1	•	7671	7754	7837	7920	8003	8086	8169	8258	8836	8
8		3502 9331	8585 9414	8668 9497	8751 9580	8834 9663	8917 9745	9000 9828	9083 9911	9165 9994	8
5	72	0159	0242	0325	0407	0490	0578	0655	0738	0821	- 0
6	(0986	1068 1893	1151 1975	1233 2058	1816	1398	1481	1568	1646	1
7		1811 2634	2716	2798	2881	2140 2963	8045	2305 8127	2387 3209	2469 3291	28
9	1	8456	8538	8620	3702	3784	8866	8948	4030	4112	4
530	1	4276 5095	4858 5176	4440 5258	4522 5340	4604 5422	4685 5508	4767 5585	4849 5667	4931 5748	5
1 2	1	5912	5993	6075	6156	6238	6820	6401	6483	6564	6
3	1	6727	6809 7623	6890 7704	6972 7785	7053	7184	7216 8029	7297	7379 8191	7
5	1	7541 8854	8485	8516	8597	8678	8759	8841	8110 8922	8003	8
1 6		9165 9974	9246	9827	9408	9489	9570	9651	9732	9813	9
3	I —		0055	0186	0217	0298	0378	0459	0540	0621	0
1 8	3 7	30782 1589	0863 1669	0944 1750	1024 1830	1105 1911	1186	1266 2072	1347 2152	1428 2233	11
54		2394	2474	2555	2685	2715	2796	2876	2956	3037	8
i i	1 (8197	8278	8358	8438	8518	8598	8679	8759	3839	8
1	2	8999 4800	4079 4880	4160 4960	4240 5040	4320 5120	4400 5200	4480 5279	4560 5859	4640 5489	4' 5!
1	4	5599	5679	5759	5838	5918	5998	6078	6157	6237	6
\-	<u>- </u>		1		-	1					<u>-</u>
Ì					PR	PORTIC	NAL PA	LRTS.			
1	Diff	. 1	2	8		4	5	6		7	8
1	87 86 85	8.7 8.6 8.5	17.4 17.2 17.0	26 25 25	8	34.8 34.4 84.0	48.5 48.0 42.5	52.2 51.6 51.0	60 59	.9 .2 .5	69 68 68
	84	8.4	16.8	25.	.z	88.6	42.0	50.4	\ 58	.8	67.

		4		8	_ <u> </u>	1 .				9	
N.	0	1	8	•	4	5	•	7	8		Diff.
545	736897	6476	6556	6685	6715	6795	6874	6954	7084	7113	
6	7198	7272	7858	7481	7511	7590	7670	7749	7829	7908	1
8	7987	8067	8146	8225	8805	8884	8468	8548	8622	8701	
8	9781 9572	8860 9651	8989 9781	9018 9810	9097 9689	9177	9256	9885	9414	9498	
y	9012	8001	8191	8010	8008	8800	0047	0126	0905	0284	79
550	740363	0442	0591	0600	0678	0757	0886	0915	0994	1078	
~ĭ	1152	1280	0521 1309 2096	0600 1888 2175	1467	1546	1624	1703	1782	1860	1
2	1939	1280 2018	2006	2175	2254	2332	2411	2489	2568	2647	1
8	2725	2804	2882	2961	2020	3118	8196	8275	8353	3431	
4	3510	2804 3588	3667	8745	3039 3823	8902	8980	4058	4136	4215	
š	4293	4371	4449	4528 5309	4606 5887	4684	4762	4840	4919	4997	}
5	5075	5158	5231	K900	K887	5465	5548	5621	5699	5777	78
7	5855	5988	6011	6089	6167	6245	6828	6401	6479	6556	
ė	6634	6712	6790	6868	6945	7023	7101	7179	7956	7884	
ğ	7412	7489	7567	7645	7722	7800	7878	7955	8033	8110	
560	8188	8266	8343	8421	8498	8576	8658	8731	8808	8885	1
1	8963	9040	9118	9195	9272	9350	9427	9504	9582	9659	l
2	8963 9736	9814	9891	9968							ł
_					0045 0817	0123	0200	0277	0854	0431	1
8	750508	0586	0663	0740	0817	0894	0971	1048 1818	1125	1202	1
4	1279	1356	1488 2202	1510	1587	1664	1741	1818	1895	1972	77
5	2048	2125 2893	2202	2279	2356 3128	2433	2509	2586	2663	2740	١
6	2816	2893	2970	8047	3123	8900	8277	8358	8480	8506	1
7	8588	8660	8786	3818	8889	8966	4042	4119	4195	4272	l
8	4848	4425	4501	4578	4654	4780	4807	4888	4960	5096	
9	5112	5189	5265	5841	5417	5494	5570	5646	5722	5799	ŀ
570	5875 6686	5951	6027	6103	6180	6256	6332	6408	6484	6560	
1	6636	6712	6788	6864	6940	7016	7092	7168	7244	7820	76
2	7396 8155	7472	7548	7624 8382	7700	7775	7851	7927	8003	8079	
8	8100	8230	8306	8082	8458	8533	8609	8685	8761	8886	ł
4 5	8912 9668	8988 9743	9063 9819	9139 9894	9214 9970	9290	9366	9441	9517	9592	l
Đ	9000	9740	AOTA	9094	8810	0045	0121	0196	0272	0347	1
6	760422	0498	0573	0649	0724	0799	0875	0950	1095	1101	l
7	1176	1251	1326	1402	1477	1552	1627	1702	1095 1778	1858	ı
8	1928	2008	2078	2153	2228	2808	2378	2458	2529	2604	Ι.
9	2679	2754	2829	2904	2978	3053	8128	8203	8278	8358	75
580	3428	3508	8578	3658	8727	3802	8877	8952	4027	4101	1
ĭ	4176	4251	4396	4400	4475	4550	4694	4699	4774	4848	l
ż	4923	4998	4326 5072	5147	5221	4550 5296	4624 5870	5445	5520	5594	ŀ
8	5669	5743	5818	5892	5966	6041	6115	6190	6964	6338	i i
4	6413	6487	6562	6686	6710	6785	6859	6933	7007	7082	1

Diff.	1	2	8	4	5	6	7	8	9
83 82 81 80 79 78 77 76 75	8.8 8.2 8.1 8.0 7.9 7.8 7.7 7.6 7.5	16.6 16.4 16.2 16.0 15.8 15.6 15.4 15.9 15.0 14.8	24.9 24.6 24.3 24.0 23.7 23.4 23.1 22.8 22.5 22.2	83.2 32.8 32.4 32.0 31.6 31.2 80.8 80.4 30.0 29.6	41.5 41.0 40.5 40.0 39.5 89.0 88.5 88.0 87.5 87.0	49.8 49.2 48.6 48.0 47.4 46.8 46.2 45.6 45.0 44.4	58.1 57.4 56.7 56.0 55.3 54.6 53.9 58.2 52.5 51.8	66.4 65.6 64.8 64.0 63.2 62.4 61.6 60.8 60.0 50.8	74.7 73.8 72.9 78.0 71.1 70.2 69.3 68.4 67.5

									[]
N.	0	1	2		4	5	6	7	8
585	767156	7290	7804	7879	7458	7527	7601	7675	7749
6	7898	7972	8046	8120	8194	8268	8342	8416	8490
7	8636	8712	8786	8860 9599	9934 9678	9008 9746	9082	9156 9894	9230 9968
8	9977	9451	9525	8099	9010	9/40	8020	9009	3600
9	770115	0189	0263	0836	0410	0484	0557	0681	0705
590	0652	0926	0999	1073	1146	1220	1293	1367	1440
1	1587	1661	1734	1808	1881	1955	2028	2102	2175
2	2322	2395	2468	2542	2615	2688	2763	2835	2908
3	3055	3128	8201	3274	8348	3421 4152	8494 4225	8567 4298	3640
4	3786	3860	3933 4663	4006 4786	4079 4809	4882	4955	5028	4371
5	4517	4590 5819	5892	5465	5538	5610	5683	5756	5100 5829
6	5246	6047	6120	6193	6265	6336	6411	6483	6556
7	5974	6774	6846	6919	6992	7064	7187	7209	7282
8	6701 7427	7499	7572	7644	7717	7789	7862	7984	8006
- 1	8151	8224	8296	8368	8441	8513	8585	8658	8730
600		8947	9019	9091	9163	9236	9308	9380	9452
1	9596	9669	9741	9813	9885	9957			-
2	3030						0029	0101	0173
	780317	0389	0461	0533	0605	0677	0749	0821	0893
3 4	1037	1109	1181	1253	1324	1396	1468	1540	1612
	1755	1827	1899	1971	2042	2114	2186	2258	2329
5 6 7	2473	2544	2616	2688	2759	2831	2902	2974	8046
7	3189	8260	3333	3408	3475	8546	3618	3689	8761
8	3904	3975	4046	4118	4189	4261	4332	4408	4475
9 (4617	4689	4760	4881	4902	4974	5045	5116	5187
610	5330	5401	5472	5543	5615	5686	5757	5828	5899
1 1	6041	6112	6183	6254	6325	6396	6467	6538	6609
2 2	6751	6822	6893	6964	7035	7106	7177	7248	7319
8 1	7460	7581	7602	7673	7744	7815 8522	7885	7956 8663	8027
4	8168	8239	8310	8381 9087	8451 9157	9228	8593	9869	8734
5	8875	8946 965 1	9016 9722	9792	9863	9933	9299	8006	9440
6	9561	9001	81.64	8182	8000	8800	0004	0074	0144
		0856	0496	0496	0567	0637	0707	0778	0848
7	790285 0988	1059	1129	1199	1269	1840	1410	1480	1550
8	1691	1761	1831	1901	1971	2041	2111	2181	2252
9	-		2532	2602	2672	2742	2812	2882	2952
620	2392	2462 3162	8231	8301	3371	8441	3511	8581	3651
1	3092	3860	3930	4000	4070	4139	4209	4279	4349
2	8790	4558	4627	4697	4767	4836	4906	4976	5045
8	4488	5254	5324	5393	5463	5532	5602	5672	5741
4	5185 5880	5949	6019	6088	6158	6227	6297	6366	6436
5	6574	6644	6718	0782	6852	6921	6990	7060	7129
1 2	7268	7887	7406	7475	7545	7614	7688	7752	7821
1 %	7960	8029	8008	8167	8236	8305	8374	8443	8518
6789	8651	8720	8789	8858	8927	8996	9065	9184	9203
1 2	, , , , , , , , , , , , , , , , , , , ,) .	ı	١.					

nia.	1	2	3	4	5	6	7
75	7.5	15.0	22.5	30.0	87.5	45.0	52.5
74	7.4	14.8	22.2	29.6	87.0	44.4	51.8
78	7.8	14.6	21.9	29.2	86.5	43.8	51.1
72	7.9	14.4	21.6	28.8	86.0	43.2	50.4
71	7.1	14.2	21.8	28.4	85.5	42.6	49.7
70	7.0	14.0	21.0	28.0	85.0	42.0	49.0
69	6.9	13.8	20.7	27.6	84.5	41.4	48.8

N.	0	1	2	8	4	5	6	7	8	9	Diff.
630	799841	9409	9478	9547	9616	9685	9754	9823	9892	9961	
1	800029	0098	0167	0236	0305	0373	0442	0511	0580	0643	l
2	0717	0786	0854	0923	0992	1061	1129	1198	1266	1335	1
8	1404	1472	1541	1609	1678	1747	1815	1884	1952	2021	1
4	2089	2158	2226	2295	2363	2432	2500	2568	2637	2705	ł
5	2774	2842	2910	2979	3047	3116	3184	3252	3321	3389	1
6	8457	3525	3594	3662	3730	3798	3867	8935	4008	4071	ı
7	4139	4208	4276	4344	4412	4480	4548	4616	4685	4758	l
7 8	4821	4889	4957	5025	5093	5161	5229	5297	5365	5433	68
ğ	5501	5569	5637	5705	5778	5841	5908	5976	6044	6112	"
- 1	806180	6248	6316	6384	6451	6519	6587	6655	6723		
40		6926	0010		7129			7332		6790	
1 {	6858	7603	6994	7061		7197	7264		7400	7467	1
2	7535		7670	7738	7806	7878	7941	8008	8076	8143	
8	8211	8279 8953	8846	8414	8481	8549	8616	8684	8751	8818	1
4	8886	0800	9021	9088	9156	9223	9290	9358	9425	9492	l
5	9560	9627	9694	9762	9829	9896	9964	0001	0000	0402	1
_	040000			0404	2504	0000		0031	0098	0165	i
6	810283	0300	0867	0434	0501	0569	0636	0703	0770	0837	
7	0904	0971	1039	1106	1173	1240	1307	1874	1441	1508	67
8	1575	1642	1709	1776	1843	1910	1977	2044	2111	2178	1
9	2245	2312	2379	2445	2512	2579	2646	2718	2780	2847	l
50 l	2916	2980	8047	8114	8181	8247	8314	8381	3448	8514	{
~ĭ l	8581	3648	8714	8781	3848	8914	3981	4048	4114	4181	l
	4248	4314	4381	4447	4514	4581	4647	4714	4780	4847	1
2 3	4913	4980	5046	5118	5179	5246	5812	5878	5445	5511	•
7	5578	5644	5711	5777	5843	5910	5976	6042	6109	6175	l
4	6241	8900	6374	6440	6506	6573	6639	6705	6771	6838	1
2	6904	6398 6970	7036	7102	7169	7235	7301	7367	7433	7499	ı
6	7565	7631	7698	7764	7830	7896	7962	8028	8094	8160	1
61	8226	8292	8358	8424	8490		8622	8688	8754	8820	1
8	8885	8951	9017	9083	9149	8556 9215	9281	9346	9412	9478	66
360	9544	9610	9676	9741	9807	9873	9989	8040	9419	9210	1
		 						0004	0070	0186	ĺ
1	820201	0267	0888	0399	0464	0530	0595	0661	0727	0792	1
2	0658	0924	0989	1055	1120	1186	1251	1817	1382	1448	l
8	1514	1579	1645	1710	1775	1841	1906	1972	2087	2108	1
4	2168	2288	2299	2364	2480	2495	2560	2626	2691	2756	ł
5	2822	2887	2952	8018	3083	8148	8213 8865	8279	8344	8409	I
6	8474	3539	8605	3670	8735	8800	8865	3930	8996	4061	ı
7	4126	4191	4256	4321	4386	4451	4516	4581	4646	4711	65
8	4776	4841	4906	4971	5036	5101	5166	5231	5296	5361	٠.
9	5426	5491	5556	5621	5686	5751	5815	5880	5945	6010	l
70	6075	6140	6204	6269	6334	6399	6464	6528	6598	6658	l
"i l	6723	6787	6852	6917	6981	7046	7111	7175	7240	7305	l
2	7869	7434	7499	7563	7628	7692	7757	7821	7884	7951	ĺ
ã	8015	8080	8144	8209	8278	8338	8402	8467	7886 8531	8595	l
4	8660	8724	8789	8853	8918	8982	9046	9111	9175	9239	l
-						0				1	
				Pro	PORTIO	nal Pa	RTS.				
Diff	. 1	2	1 8	3	4	5	6		7	8	9
68	6.8	18.6	20	_ -	27.2	84.0	40.8		.6	54.4	61.5
67	6.7	18.4	20	1	26.8	83.5	40.2		. ŭ	53.6	60.
66	6.6	13.2	19		26.4	83.0	89.6	140	.2	52.8	59.4
65	6.5	18,0	19		26.0	82.5	89.0	a a	.5	52.0	58.

N.	0	1	2	2	4	5	6	7	8	9	Diff.
75	829304	9368	9482	9497	9561	9625	9690	9754	9818	9882	
6	9947			0139	0204	0268	0332	0396	0460	0525	
7	830589	0011 0653	0075 0717	0781	0845	0909	0973	1037 1678	1102 1742	1166 1806	64
8	1230	1294	1358	1422 2062	1486 2126	1550 2189	1614 2253	2817	2381	2445	٧.
9	1870	1984	1998	2700	2764	2828	2892	2956		3083	l
180	2509 8147	2573 3211	2637 8275	3338	3402	8466	3530	8598	3657 4294	3721 4857	
2	3784	3848	3912	3975	4039	4103 4739	4166 4802	4230 4866	4929	4993	1
8	4421	4484	4548	4611	4675 5310	5373	5487	5500		5627	l
4	5056	5120	5183	5247	5944	6007	6071	6134	6197	6261	1
5	5691	5754	5817	5881 6514	6577	6641	6704	6767		6894	1
6	6324 6957	6387 7020	6451 7083	7146	7210	7273	7336	7399	7462 8098	7525 8156	I
8	7588	7652	7715	7778	7841	7904	7967	8030		8786	63
9	8219	8282	8345	8408	8471	8534	8597	1		9415	1
390	8849	8912	8975	9038	9101 9729	9164 9792	9227 9855	9289		-	
1	9478	9541	9604	9667						- 0043	ł
_	040400	2400	0000	0294	0357	0420	0482	054		0671	l
2	840106	0169	0232 0859	0921	0984	1046	1109	1172		1297 1922	1
8 4	0733 1359	0796 1422	1485	547	1610	1672 2297	1735 2360	1797		2547	ı
3	1985	2047	2110	2172	2235 2859	2921	2983	3046			1
6	2609	2672	2784	2790	3452	3544	3606	3669	3731	8798	1 ′
7	8233	8295	3357	3420	4104	4166	4229	429	l 4353	4415	1
8	3855	8918	8980	4042 4664	4726	4788	4850	4919			1
9	4477	4539	4601		5346	5408	5470	558		5656	62
700	5098	5160	5222	52 84 5904	5966	6028	6090	615			ı
1	5718	5780 6399	5842 6461	6523	6585	6646	6708 7326	738			1
2 8	6337 6955	7017	7079	141	7202 7819	7264 7881	7943	800			1
4	7578	7684	7696	7758	8435	8497	8559	862			1
5	8189	8251	8312	8374	9051	9112	9174	923		9358	1
6	8805	8866	8928	8989 9604	9665	9726	9788	984	9 9911	9972	1
7	9419	9481	9542		0279	0340	0401	046			1
8		0095	0156	0217 0830	0891	0952	1014	107	- 1	1	1
9				1442	1508	1564		168		1809 2419	
710		1320	1381	2053	2114	2175		229	7 2968	3029	6:
	1870 2 2480		2602	2665	2724 8333	2785 3394	3455	851			1
1	8090			3275	3941	4002		412		4245	1
	4 8696		3820	3881	4549	4610	4670	478	1 4792		ļ.
	5 430	8 436	4428		5156	5216	5277	533		5459	i
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(9 67				6970	1051	1001	1.10		1.2.2	1
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1				P	OPORTI	ONAL I	PARTS.				
1	Diff.	1 \	2	8	4	5	-	3	7	8	9
1				-\- <u></u>	26.0	32.5	39	.0	45.5	52.0	58
ı	65	6.5	18.0	19.5	1 25.6	1 32.0	1 38	.4	44.8	51.2	57
1	64	6.4	12.8 12.6	19.2	25.2	81.5	87	.8	44.1 43.4	50.4	56
١	68	6.2	12.	4 \ 18.6	24.8	31.0 30.5		.6	43.4 42.7	49.6 48,8	55
- 1	6 <u>1</u>	6.1	12.		24.4	80.0			42.0	48.0	1 54

1 2 7393 5 7995 6 9196 9 9196 9 7996 7 0996 4 1594 1 2191 1 2191 8 2787 3 3882 7 3977 1 4570 4 5705 6 6346 6 6357 7 7 7526 6 4 8703 8 9290 9 8 9877	7453 8056 8657 9258 9859 0458 1056 1654 2951 9847 3449 4036 4630 5222 5814 6405 6998 87585 8174 8768	7513 8116 8718 9318 9918 9918 1116 1214 2810 2906 3501 4096 4689 5283 5874 6465 7644 8828	7574 8176 8778 9879 9978 1176 11773 2870 2966 8561 4155 4748 5343 5343 7114 7708	7634 8236 8238 9439 0038 0687 1236 1838 2430 3025 3620 4214 4806 5400 5992 6583 7178	7694 8397 8898 9499 0098 0097 1295 1893 2489 3085 3680 4274 4867 5459 6051	77755 8357 8958 9559 0158 0757 1355 1953 2549 3144 3739 4325 5519	7815 8417 9018 9619 0218 0817 1415 2012 2608 3204 3799 4392 4985	7875 8477 9078 9679 0877 1475 2072 2668 3263 3858 4459 5045	Diff.
5 7995 5 7996 5 7996 9 9198 9 9799 8 0996 7 1594 1 2191 2191 2 3927 8 3832 7 3977 1 4570 4 5163 6 5755 6 6967 7 7526 8 615 4 8703 8 9290 8 9677	8056 8657 9258 9859 0458 1056 1654 2351 3847 8443 4036 4630 5322 5814 6405 6996 7585 8174 8768	8116 8718 9318 9918 0518 1114 2810 2906 3501 4096 4689 5289 5287 6465 7066 7644 8828	8176 8778 9279 9978 0578 1176 1176 1276 28670 2966 3561 4155 4748 5341 5933 6524 7114	8236 8838 9439 0038 0637 1236 1838 2430 3025 3620 4214 4806 5400 5992 6588	8297 8896 9499 0098 0697 1295 1893 2489 3085 9680 4274 4867 5459 6051	8357 8958 9559 0158 0757 1355 1953 2549 3144 3739 4383 4926	8417 9018 9619 0218 0617 1415 2012 2608 3204 8799 4392 4985	8477 9078 9679 0278 0877 1475 2072 2668 3263 3858 4452	60
5 7995 5 7 8597 8 9198 9 9799 8 0996 4 1594 1 2191 2191 2 3 3882 7 3977 1 4 5163 6 5755 6 6987 7 7 7526 8 815 4 8703 8 9290 8 9877	9258 9859 0458 1056 1654 2351 3847 3442 4036 4630 5232 5814 6405 6996 7585 8174 8768	8116 8718 9318 9918 0518 1114 2810 2906 3501 4096 4689 5289 5287 6465 7066 7644 8828	8176 8778 9279 9978 0578 1176 1176 1276 28670 2966 3561 4155 4748 5341 5933 6524 7114	8236 8838 9439 0038 0637 1236 1838 2430 3025 3620 4214 4806 5400 5992 6588	8898 9499 0098 0697 1295 1893 2489 3085 3680 4274 4867 5459 6051	8958 9559 0158 0757 1855 1958 2549 3114 9789 4383 4926	8417 9018 9619 0218 0617 1415 2012 2608 3204 8799 4392 4985	8477 9078 9679 0278 0877 1475 2072 2668 3263 3858 4452	60
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9877		9408	9466	9525	9584	9642	9701	9760	
	9935	9994							
		<u> </u>	0053	0111	0170	0228	0287	0345	
1 0462	0521	0579	0638	0696	0755	0813	0872	0990	
1047	1106	1164	1223	1281	1339	1398	1456	1515	
3 1631 3 2215	1690 2278	1748 9381	1806 9389	1865	1923	1981	2040 2623	2008 2681	
2797	2855	2918	2972	2448 8080	2506 3088	2564 8146	9904	8262	
8879	8437	8495	8558	8611	8669	8727	8204 8785	8844	
8960	4018	4076	4184	4192	4250	4308	4366	4424	58
4540	4598	4656	4714	4772	4890	4888	4945	5008	•
5119	5177	5225	5209	5351	5400	KARR	REGME	KK89	
	6333			6507	6564	6622	6680	6787	
6858	6910	6968	7026	7083	7141	7199	7256	7814	
	7487	7544		7659	7717	7774	7832		
							8407		
			0208	0888			OFFE		
					074U	Sept (2000	801%	
0100	0101	0011	8080	8800	0018	0070	0127	0185	
0299	0856	0418	0471	0528	0585	0642	0699	0756	
1	1000			1000					
									_
2012	2069	2126	2188	2240	2297	2854	2411	2468	57
9591	2688	2695	2752			2923	2980	8087	
	3207	3264	3321	8377	8484	8491	8548	8605	
	5 6858 1 7429 7 8004 2 8579 8 9153 9 9736 2 0299 4 0871 1442	5 6858 6910 7429 7487 7 8004 8062 2 8579 8637 9 798 9794 2 0299 0856 4 0871 0928 5 1442 1499 5 2012 2069	5 6858 6910 6968 1 7429 7467 7544 7 8004 8062 8119 2 8579 6637 6694 6 9153 9211 9268 9 9786 9784 9841 2 0299 0856 0418 4 0671 0928 0985 5 1442 1499 1556 5 2012 2069 2126	5 6858 6910 6968 7038 1 7429 7487 7544 7602 7 8004 8062 8119 8177 2 8579 8037 8604 8752 9 9736 9784 9641 9898 2 0299 0856 0418 0471 4 0871 0928 0985 1042 5 1442 1499 1556 1613 5 2881 2088 2095 2752	5 6858 6910 6968 7028 7082 5 6858 6910 6968 7022 7082 7 804 8062 8119 8177 8234 8 8579 8037 8904 8752 8609 8 9153 9211 9268 9285 9888 9 9736 9744 9641 9898 9956 2 0299 0856 0418 0471 0528 4 0671 0928 0965 1042 1099 5 1442 1499 1556 1613 1670 5 2012 2069 2126 2183 2240 5 2581 2688 2696 2752 2809	5 6858 6910 6968 7026 7083 7141 1 7429 7487 7544 7602 7659 7717 7 8004 8062 8119 8177 8234 8202 8 8579 8937 8944 8752 8909 886 9 9736 9744 9841 9888 9440 9 9736 9784 9841 9898 9926 2 0299 0856 0418 0471 0528 0585 4 0671 0928 0985 1042 1099 1156 5 1442 1499 1556 1613 1670 1727 5 2012 2069 2126 2183 2240 2297 5 2881 2388 2366 2752 2809 2866	5 6858 6910 6968 7026 7083 7141 7199 1 7429 7487 7544 7602 7659 7717 7774 7 8004 8062 8119 8177 8234 8202 8349 8 8579 8937 8944 8752 8909 8866 8924 9 9736 9744 9641 9898 9856 0138 0070 2 0299 0856 0418 0471 0528 0585 0642 4 0671 0928 095 1042 1099 1156 1218 5 1442 1499 1556 1613 1670 1727 1784 5 2801 2808 2838 2240 2297 2854 5 2831 2838 2366 2923 2866 2923	5 6858 6910 6968 7028 7083 7141 7199 7286 1 7429 7487 7544 7602 7659 7717 7774 7882 7 8004 8062 8119 8177 8234 8202 8349 8407 8 8579 8937 8944 860 866 8924 8961 9 9786 9711 9268 9325 9888 9440 9497 9555 9 9786 9784 9641 9898 9966 9038 0685 0642 0690 0127 2 0299 0856 0418 0471 0528 0585 0642 0690 0127 0690 0127 1727 1734 1841 1841 1841 1841 1841 1841 1841 1841 1841 1841 1858 2860 2823 2860 2884 2960	5 6858 6910 6968 7068 7068 7141 7199 7256 7814 7 7429 7487 7544 7602 7659 7717 7774 7882 7889 7 8004 8002 8119 8177 8234 8202 8849 8407 8464 8 8579 8637 8640 8782 8609 8666 8924 8961 9039 9 9736 9744 9841 9898 9956 0013 0070 0127 0185 2 0290 0356 0418 0471 0528 0686 0642 0690 0755 9612 4 0871 0928 0965 1042 1099 1156 1218 1271 1328 5 1442 1499 1556 1613 1670 1727 1784 1641 1898 5 28012 2689 2280 2297 2854<
	7429 8004 8579 9153 9736 0299 0871 1442 2012 2581	5698 5756 6270 6333 6910 7429 7487 8004 8062 9510 9736 9734 9736 9734 1442 1499 9012 2069 5581 2688	5696 5756 5818 6276 6333 6910 6968 6910 6968 6910 8567 6904 8004 8062 8119 8579 9637 9604 9637 9604 9637 9636 6910 9289 0985 0418 1442 1499 1556 2012 2009 2136 2561 2868 2668 2688	5698 5756 5818 5871 6276 6333 6391 6449 6853 6910 6968 7026 7429 7487 7544 7602 8004 8062 8119 8177 8579 9637 9604 8752 9153 9211 9268 9325 9734 9841 0471 0871 0928 0985 1042 1442 1499 1556 1613 2012 2069 2126 2183 20561 2868 2666 9752	5696 5756 5813 5871 5929 6276 6333 6391 6449 6507 6283 6910 6968 7023 7083 7429 7467 7544 7602 7659 8004 8028 8119 8177 834 8570 9637 9604 8752 8909 9153 9211 9208 9325 988 9736 9794 9641 96471 0528 0871 0928 0965 1042 1099 1442 1459 1556 1613 1670 2012 2069 2126 2123 2240 2561 2638 2605 2752 2809	5696 5756 5813 5871 5929 5987 6276 6333 6391 6449 6507 6564 6808 6910 6968 7026 7083 7141 7429 7467 7544 7602 7659 7717 8004 8028 8119 8177 834 8292 8570 9637 9604 8752 8909 866 9153 9211 9268 9282 9285 9440 9726 9784 9641 9871 0528 0585 0871 0928 0965 1042 1099 1156 1442 1499 1556 1613 1670 1727 2012 2069 2126 2123 2240 2297 2561 2638 2695 2752 2890 2865	5696 5756 5813 5871 5929 5987 6045 6276 6333 6391 6449 6507 6564 6622 6808 6910 6968 7023 7083 7141 7199 7429 7467 7544 7602 7659 7717 7777 8004 8028 8119 8177 834 8392 8349 8703 9637 9604 8752 8909 8865 8924 9153 9211 9208 9252 3888 9440 9407 9726 9744 9641 9689 9956 0013 0070 0299 0856 0418 0471 0528 0585 0642 0671 0928 0965 1042 1099 1155 1218 1442 1499 1556 1613 1670 1727 1784 2012 2069 2126 2752 2809 2865	5696 5756 5813 5871 5929 5987 9045 9102 6276 6333 6391 6449 6507 6564 6622 6690 6808 6910 6968 7063 7083 7141 7199 7256 7429 7447 7544 7602 7659 7717 7774 7832 8004 8028 8118 8272 8809 8866 8924 8961 9153 9211 9208 9325 8889 8400 9497 9555 9736 9744 9641 9689 9956 0013 0070 0127 0299 0856 0418 0471 0528 0585 0642 0699 0871 0928 0965 1042 1099 1156 1218 1271 1442 1499 1556 1613 1670 1727 1784 1841 2012 2068 2688 2695 <th>5696 5756 5813 5871 5929 5987 8045 8102 8117 8177 8787 7711 7774 7832 7889 7889 7889 8800 802 8118 827 8890 8868 8924 8961 9089 913 921 9288 9825 9839 9440 9407 9555 9613 9613 9604 8752 8909 8868 8924 8961 9089 963 9613 9689 9632 9613 9639 9632 9613 9632 9632 9632 9632 9633 9641 9639 9636 9632 9633 9641 9639 9636 9632 9633 9642 9690</th>	5696 5756 5813 5871 5929 5987 8045 8102 8117 8177 8787 7711 7774 7832 7889 7889 7889 8800 802 8118 827 8890 8868 8924 8961 9089 913 921 9288 9825 9839 9440 9407 9555 9613 9613 9604 8752 8909 8868 8924 8961 9089 963 9613 9689 9632 9613 9639 9632 9613 9632 9632 9632 9632 9633 9641 9639 9636 9632 9633 9641 9639 9636 9632 9633 9642 9690

n.	0	1	2	8	4	5	6	7	8	9	Diff.
65 6 7 8	888661 4229 4795 5361 5926	8718 4285 4852 5418	8775 4342 4909 5474	8882 4399 4965 5531 6096	3888 4455 5022 5587 6152	8945 4512 5078 5644 6209	4002 4569 5135 5700 6265	4059 4625 5192 5757 6321	4115 4683 5248 5813 6378	2 4739 5 5305 3 5870	
9 0128456	6491 7054 7617 8179 8741 9302 9862	5983 6547 7111 7674 8236 8797 9358 9918	6089 6604 7167 7780 8292 8853 9414 9974	6660 7228 7786 8348 8909 9470	6716 7280 7842 8404 8965 9526	6773 7896 7898 8460 9021 9582	6829 7392 7955 8516 9077 9638	6885 7449 8011 8573 9134 9694	6945 7506 8067 8629 9190 9750	6998 5 7561 7 8128 9 8685 0 9246 0 9806	56
8	890421 0980 1537	0477 1035 1598	0533 1091 1649	0030 0589 1147 1705	0086 0645 1203 1760	0141 0700 1259 1816	0197 0756 1314 1872	0253 0812 1370 1928	0309 0868 1426 1988	3 0924 3 1482	
780 1 2 8 4 5 6 7 8	2095 2651 3807 3769 4316 4870 5423 5975 6526 7077	2150 2707 3263 3817 4371 4925 5478 6030 6581 7132	2906 2762 3818 3878 4427 4980 5533 6085 6636 7187	2262 2813 3873 3923 4482 5038 5558 6612 7242	2817 2878 3429 3984 4538 5091 5644 6195 6747 7297	2878 2989 3484 4089 4593 5146 5699 6251 6802 7352	2429 2985 3540 4094 4648 5201 5754 6306 6857 7407	2484 3040 3595 4150 4704 5257 5809 6361 6912 7462	2540 3096 3651 4206 4759 5312 5864 6416 6967 7517	3151 3706 5 4261 9 4814 2 5367 4 5920 3 6471 7 7022	
790 1 2 3 4	7627 8176 8725 9273 9821	7682 8231 8780 9328 9875	7737 8286 8835 9683	7792 8841 8890 9437 9985	7847 8896 8944 9498	7902 8451 8999 9547	7957 8506 9054 9602	8012 8561 9109 9656	8067 8615 9164 9711	8670 9218 9766	55
56789	900367 0913 1458 2008 2547	0422 0968 1518 2057 2601	9980 0476 1022 1567 2112 2655	0531 1077 1622 2166 2710	0039 0586 1131 1676 2221 2764	0094 0640 1186 1731 2275 2818	0149 0695 1240 1785 2329 2873	0208 0749 1295 1840 2384 2927	0258 0804 1349 1894 2438 2981	0859 1404 1948 2492	
800 1 2 3 4 5 6 7	8090 8683 4174 4716 5256 5796 6335 6874 7411	8144 8687 4229 4770 5810 5850 6389 6927 7465	3199 3741 4283 4824 5364 5904 6443 6981 7519	8258 8795 4337 4878 5418 5958 6497 7035 7573 8110	3307 3849 4391 4982 5472 6012 6551 7089 7626 8163	3361 3904 4445 4966 5526 6066 6604 7143 7680 8217	8416 8958 4499 5040 5580 6119 6658 7196 7734 8270	8470 4012 4558 5094 5634 6173 6712 7250 7787 8824	353.1 4066 4607 5148 5688 6227 6766 7304 7841 8878	4190 4861 5202 5742 6281 6820 7358 7895	54
				Pro	PORTIO	MAL PA	RTS,				
1	Diff.	1 \	2 \	8	4	5	6		7	8	9
	57 56 56 54	5.7 5.6 5.5 5.4	11.4 11.2 11.0 10.8	17.1 16.8 18.5 16.2	22.8 22.4 22.0 21.6	28.5 28.0 27.5 27.0	34.2 33.6 33.0 82.4	39	9.9 9.2 3.5 7.8	45.6 44.8 44.0 48.2	51.5 50.4 49.4

N.	0	1	2	8	4	5	6	7	8	9	Diff.
10	908485	8589	8592	8646	8699	8758	8807	8860	8014	8967	
2	9021 9556	9074 9610	9128 9668	9181 9716	9235 9770	9289 9823	9342 9877	9396 9930	9449 9984	9508	
8	910091	0144 0678	0197 0781	0251 0784	0304 0838 1371 1903 2435	0858 0891 1424	0411	0464	0518	0037 0571	
4	0624	0678	0781	0784	0838	0891	0944	0998	1051 1584	1104	
5	1158	1211 1748	1264 1797 2328	1317 1850 2381	1009	1424	1477 2009	1530 2063	1584 2116	1687	
7	1690 2222	2275	2828	2381	2435	1956 2488	2541	9504	2647	2169 2700	
8	2753	2806	2859	2913	2966	3019	3072	3125	8178	3231	l
ğ	8284	3337	3390	3443	8496	8549	3602	3655	3708	8761	58
30 J	8814	3867 4396 4925 5453 5980	3920	3973 4502 5030 5558 6085 6612 7138	4026 4555 5083 5611 6138 6664 7190	4079	4132	4184 4718	4237 4766	4290	1
1	4979	4095	4449 4977	5030	5083	4608 5136	4660 5189	5241	5294	5347	l
2 8	4343 4872 5400	5453	5505 6033 6559 7085	5558	5611	5664	5716	5769	5822	4819 5847 5875	i
4	5927 6454	5980	6033	6085	6138	6191	6243	6296	5822 6849	6401	l
4 5 6 7 8	6454	6507 7033	6559	6612	6664	6717	6770	6822	6875	6927	l
6	6980	7033	7085	7188	7190	7248	7295	7348	7400	7453 7978	
7	7506	7558	7611 8135	7668 8188	7716 8240	7768 8293	7820 8345	7878 8397	7925 8450	8502	l
9	8030 8555	8083 8607	8659	8712	8764	8816	8869	8921	8978	9026	1
30 1	9078 9601	9130 9653	9183 9706	9235 9758	9287 9810	9340 9862	9892 9914	9444 9967	9496	9549	
_									0019	0071	1
28456789	920123 0645 1166	0176 0697 1218	0228 0749 1270	0280 0801 1322 1842 2362	0332 0853 1374	0384	0436	0489	0541 106.2	0598	1
8	0645	0697	0749	0801	0858	0906 1426	0958 1478	1010 1530	1582	1114 1694	5.8
4	1686	1788	1200	1822	1904	1946	1000	2050	2102	2154	l
ĕ	9906	2258	1790 2310 2829	2262	1894 2414 2938	2466	1998 2518	2570	2622	2674	1
7	2206 2725	2777	2829	2881	2933	2985	3037	2570 3089	8140	3192	1
Š.	8244 8762	8296 8814	3348 3865	2881 3399	8451	3503	3555	3607	3658	3710	
-				8917	8969	4021	4072	4124	4176	4228	
40	4279 4796	4331 4848 5364 5879	4383	4484	4486	4538 5054	4589	4641	4698	4744	1
1	5812	4848	4899 5415	4951 5467	5008 5518	5570	5106 5621	5157 5678	5209 5725	5261 5776	i
2 8 4 5 6 7 8	6898	5870	5981	5982	6034	6085	6137	6188	6240	6291	1
4	5828 6342 6857 7870	1 63344	6445	6497	6548	6600	6651	6702	6754	6805	1
5	6857	6908 7422	6959	7011	7062 7576	7114	7165	7216	7268	7819	1
6	7870	7422	7478	7524 8037	7576	7627	7678	7780	7781	7882	1
7	7888	7935	7986	8037	8088 8601	8140	8191	8242	8298	8345	1
8	7888 8396 8908	8447 8959	8498 9010	8549 9061	9112	8652 9163	8708 9215	9266	8805 9317	9857 9868	{
50	9419	9470	9521	9572	9623	9674	9725	9776	9827	9879	١.,
ĭ	9930	9981								-	51
0	930440	0491	0032 0542	0083	0134 0643 1158	0185 0694	0236 0745	0287 0796	0338	0889	
8	0949	1000	1051	0592 1102 1610	1158	1204	1254	1305	1356	1407	1
2 8 4	1458	1509	1560	1610	1661	1712	1763	1814	1865	1915	1

Diff.	1	2	8	4	5	6	7	8	9
58	5.3	10.6	15.9	21.2	26.5	81.8	87.1	42.4	47.7
52	5.2	10.4	15.6	20.8	26.0	81.2	86.4	41.6	46.8
51	5.1	10.2	15.8	20.4	25.5	80.6	85.7	40.8	45.9
50	5.0	10.0	15.0	20.0	25.0	80.0	85.0	40.0	45.0

No.	855 L. 9	81.]							DN	io. 1
N.	0	1	2	8	4	5	6	7	8	
55	931966	2017	2068	2118	2169	2220	2271	2322	2372	24
6	2474	2524	2575	2626	2677	2727	2778	2829	2879	29
7	2981	3031	3082	8133	8188	3234	8285	8335	8386	84
8	3487	3538	8589	8639	8690	8740	8791	8841	3892	38
او	3993	4044	4094	4145	4195	4246	4296	4347	4397	44
· 1	4498	4549	4599	4650	4700	4751	4801	4852	4902	49
60	5003	5054	5104	5154	5205	5255	5306	5356	5406	5
1	5507	5558	5608	5658	5709	5759	5809	5860	5910	59
8	6011	6061	6111	6162	6212	6262	6313	6363	6413	64
4 1	6514	6564	6614	6665	6715	6765	6815	6865	6916	69
	7016	7066	7116	7167	7217	7267	7317	7367 7869	7418 7919	74
6	7518	7568	7618	7668	7718	7769	7819 8320	8370	8420	8
5 6 7	8019	8069	8119	8169 8670	8219 8720	8269 8770	8820	8870	8920	8
8	8520	8570	8620 9120	9170	9220	9270	9820	9369	9419	8
9	9020	9070								
870	9519	9569	9619	9669	9719	9769	9819	9869	9918	99
	040018	0068	0118	0168	0218	0267	0317	0367	0417	0
1	940018	0566	0616	0666	0716	0765	0815	0865	0915	0
2	.0516 1014	1064	1114	1163	1218	1263	1313	1362	1412	14
3	1511	1561	1611	1660	1710	1760	1809	1859	1909	19
5	2008	2058	2107	2157	2207	2256	2306	2355	2405	2
6	2504	2554	26 03	2653	2702	2752	2801	2851	2901	2
1 7	3000	3049	8099	8148	8198	8247	8297	8346	3396	8
8	3495	3544	8593	8643	8692	3742	8791	3841	8890	3
9	3989	4038	4068	4187	4186	4236	4285	4335	4384	(-
1 -	4483	4532	4581	4631	4680	4729	4779	4828	4877	4
880	4976	5025	5074	5124	5173	5222	5272	5321	5370	5
1 2	5469	5518	5567	5616	5665	5715	5764	5813	5862	5
8	5961	6010	6059	6108	6157	6207	6256	6305	6354	6
4	6452	6501	6551	6600	6649	6698	6747	6796	6845	6
K	6943	6992	7041	7090	7189	7189	7238 7728	7287	7336 7826	77
5	7434	7483	7582 8022	7581 8070	7630 8119	7679 8168	8217	7777 8266	8315	8
7	7924	7975	8511	8560	8608	8657	8706	8755	8804	8
8	8413	8462	8999	9048	9097	9146	9195	9244	9292	94
ğ	8902	8951				1				1
- 1	9390	9439	9488	9536	9585	9634	9683	9731	9780	94
890	9878	9926	9975			-	0400	0040	0000	-
1	20.0		0400	0024	0073	0121	0170	0219	0267	0
2	950365	0414	0462	0511	0560	0608	0657 1148	0706 1192	0754 1240	12
3	0851	0900	0949	0997	1046	1095	1629	1677	1726	17
4	1338	1386	1435	1483 1969	1532 2017	1580 2066	2114	2163	2211	25
5	1823	1872	2405	2453	2502	2550	2599	2647	2696	2
6	2308	2356	2889	2988	2986	8034	3083	8131	3180	3
7	2792	2841	8378	8421	3470	8518	3566	8615	3663	8
678	3276	8325	3856	8905	3958	4001	4049	4098	4146	41
ĕ	3760	1 2000	1	. 5000			1	1		

Diff.	1	2	8	4	5	6	7	8
51	5.1	10.2	15.8	20.4	25.5	30.6	85.7	40.8
50	5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0
49	4.9	9.8	14.7	19.6	24.5	29.4	34.8	89.2
48	4.8	9.6	14.4	19.2	24.0	28.8	83.6	88.4

No. 990 L. 995.]

No. 999 L. 999.

N.	0	1	2	8	4	5	6	7	8	9	Diff.
990 1 2 8 4 5 6 7 8	995635 6074 6513 6949 7386 7823 8259 8095 9131 9565	5679 6117 6555 6998 7480 7867 8308 8789 9174 9609	5728 6161 6599 7087 7474 7910 8847 8782 9218 9652	5767 6205 6643 7080 7517 7954 8890 8826 9261 9696	5811 6249 6687 7124 7561 7998 8434 8869 9305 9789	5854 6298 6781 7168 7605 8041 8477 8918 9848 9788	5898 6337 6774 7212 7648 8085 8521 8956 9392 9826	5942 6380 6818 7255 7692 8129 8564 9000 9485 9870	5986 6424 6862 7299 7736 8172 8608 9043 9479 9918	6030 6468 6906 7343 7779 8216 8652 9087 9522 9967	44

HYPERBOLIC LOGARITHMS.

No.	Log.	No.	Log.	No.	Log.	No.	Log.	No.	Log.
1.01	.0099	1.45	.3716	1.89	.6366	2.33	.8458	2.77	1.0188
1.02	.0198	1.46	.3784	1.90	.6419	2.34	.8502	2.78	1.0225
1.03	.0296	1.47	.3853 .3920	1.91	.6471	2.35 2.36	.8544	2.79	1.0260
1.04 1.05	.0488	1.49	.3988	1.92 1.93	.6528 .6575	2.37	.8587 .8629	2.81	1.0296
1.06	.0588	1.50	.4055	1.94	.6627	2.38	.8671	2.82	1.0367
1.07	.0677	1.51	.4121	1.95	.6678	2.39	.8713	2.88	1.0408
1.08	.0770	1.52	.4187	1.96	.6729	2.40	.8755	2.84	1.0488
1.08 1.09	.0862	1.53	.4258	1.97	.6780	2.41	8796	2.85	1.0478
1.10	.0958	1.54	.4318	1.98	.6831	2.42	.8838	2.86	1.0508
1.11 1.12 1.18	.1044	1.55	4388	1.99	.6881	2.43	.8879	2.87	1.0543
1.12	.1183	1.56	.4447	2.00	.6981	2,44	.8920	2.88	1.0578
1.18	.1222	1.57	.4511	2.01	.6981	2,45	.8961	2.89	1.0618
1.14	.1810	1.58	.4574	2.02	.7081	2.46	.9002	2.90	1.0647
1.14 1.15	.1398	1.59	.4637	2.03	.7080	2,47	.9042	2.91	1.0682
1.16	.1484	1.60	.4700	2.04	.7129	2,48	.9083	2.92	1.0716
1.17	.1570	1.61	.4762	2.05	.7178	2,49	.9128	2.93	1.0750
1.16 1.17 1.18 1.19	.1655	1.62	.4824	2.06	.7227	2,50	.9168	2.94	1.0784
1.19	.1740	1.63	.4824 .4886	2.07	.7275	2,51	.9203	2.95	1.0818
1.20	.1823	1.64	.4947	2.08	.7824	2,52	.9248	2.96	1.0852
1.20 1.21	.1906	1.65	.5008	2.09	.7372	2.58	.9282	2.97	1.0886
1.22 1.28	.1988	1.66	.5068	2.10	.7419	2.54	.9822	2.98	1.0919
1.28	.2070	1.67	.5128	2.11	.7467	2.55	.9361	2.99	1.0953
1.24 1.25	.2151	1.68	.5188	2.12	.7514	2.56	.9400	8.00	1.0986
1.25	.2231	1.69	.5247	2.13	.7561	2.57	.9439	3.01	1.1019
1.26	.2311	1.70	.5806	2.14	.7608	2.58	.9478	8.02	1.1053
1.27	.2390	1.71	.5365	2.15	.7655	2.59	.9517	3.03	1.1086
1.28 1.29	.2469	1.72	.5423	2.13	.7701	2.60	.9555	8.04	1.1119 1.1151
1.29	.2546	1.73	.5481	2.17	.7747	2.61	.9594	3.05	1.1151
1.30	.2624	1.74	.5589	2.18	.7798	2.62	.9632	8.06	1.1184
1.81 1.82 1.33	.2700	1.75	.5596	2.19	.7889	2.63	.9670	8.07	1.1217
1.82	.2776	1.76	.5653	2.20	.7885 .7930	2.64	.9708	8.08	1.1249
1.33	.2852	1.77	.5710	2.21		2.65	.9746	8.09	1.1288
1.84	.2927	1.78	.5766	2.22	.7975	2.66	.9788	8.10	1.1814
1.35 1.36		1.79	.5822	2.28	.8620	2.67	.9821	8.11	1.1846
1.87	.8075	1.80	.5878	2.24	.8065	2.68	.9858	8.12	1.1878
1.00	.3221	1.82	.0903	2.25	.8109	2.69 2.70	.9895	8.18	1.1410
1.88 1.89	.3298	1.88	.5988		.8154		-9938	8.14	1.1442
1.40	.3365	1.84	.6098	2.27	.8198 .8242	2.71	1 9969	8.15	1.1474
1 41	.3436	1.85	.6152	2.29	.8286	2.72	1.0006	8 16 8.17	1.1506 1.1587
1.41 1.42	.8507	1.86	.6206	2.30	.8329	2.74	1.0080	3.18	1.1569
1.48	.3577	1.87	.6259	2.81	.8372	2.75	1.0116	8.19	1.1600
1.44	.8646	1.88	.6818	2.82	.8416	2.76	1.0152	8.20	1.1688
	1	*	.5010	~	.0410	~	1.0100	0.20	1.100%
		''	·	·		-			

No. Log. No. Log.	No.	Log.	No.
3.21 1.1663 3.87 1.3533	4.53	1.5107	5.19
3.22 1.1694 3.88 1.3558	4.54	1.5129	5.20
3.23 1.1725 3.89 1.3584	4.55	1.5151	5.21
3.24 1.1756 3.90 1.3610	4.56	1.5173	5.22
3.25 1.1787 3.91 1.3635	4.57	1.5195	5.23
3.26 1.1817 3.92 1.3661 3.27 1.1848 3.93 1.3686	4.58	1.5217	5.24 5.25
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	4.60	1.5261	5.26
3.29 1.1909 3.95 1.3737	4.61	1.5282	5.27
9 90 4 4090 9 00 1 3762	4.62	1.5304	5.28
3 21 1 1060 3 97 1 3 180	4.63	1.5326	5.29
9 00 4 4000 9 00 1 3813	4.64	1.5347	5.30
3.33 1.2030 3.99 1.3838	4.65	1.5369	5.31
3.34 1.2060 4.00 1.3868	4.66	1.5390 1.5412	5.32
3.35 1.2090 4.01 1.3888	4.68	1.5433	5.34
3.36 1.2119 4.02 1.3313	4.69	1.5454	5.35
3.51 1.2193 3 2062	4.70	1.5476	5.36
3.38 1.2119 3.05 3 3987	4.71	1.5497	5.37
3.39 1.2200 1.06 1.4012	4.71	1.5518	5.38
3,40 1.2200 1.4036	4.73	1.5539	5.39
3.41 1.2307 1.08 1.4061	4.74	1.5560	5.40
3.42 1.2290 1 1 4085	4.75	1.5581	5.41
	4.76	1.5602	5.42
0.41 1 0004 4 11 1 1 -415	4.77	1.5623	5.43
3.45 1.2384 4.11 1.4159 3.46 1.2413 4.12 1.4183	4.79	1.5665	5.45
4 0440 4 4 10	4.80	1.5686	5.46
3.47 1.2442 4.14 1.4207 3.48 1.2470 4.14 1.4231	4.81	1.5707	5.47
9 40 1 2499 4.15 1 4255	4.82	1.5728	5.48
0 50 / 1 2528 // 3 3 4 4279	4.83	1.5748	5.49
0 51 1 9556 4.1.	4.84	1.5769	5.50
1 1 9585 4 4324	4.85	1.5790 1.5810	5.51
	4.87	1.5831	5.52
54 1.2641 4 21 1.4370	4.88	1.5851	5.54
55 1.2008 4.22 1.4422	4.89	1.5872	5.55
56 1.2006 4.23 1.4446	4.90	1.5892	5.56
57 1 0754 4.24 1 4469	4.91	1.5913	5.57
00 1 9782 4.20 1 4493	4.92	1.5933	5.58
80 1.2809 4.37 1.4510	4.93	1.5953	5.59
0007 1 4.~ 1 4 1540	4.95	1.5974	5.60
02 1 1 200	4.96	1,6014	5.62
63 1 1.200 1 4.30 1 2 4600	4.97	1.6034	5.63
	4.98	1,6054	5.64
65 1 2975 4.82 1.4656	4.99	1,6074	5.65
00 1 2002 4.35 1 4679	5.00	1.6094	5.66
1 3029 4 4702	5.01	1,6114	5.67
	5.02	1.6134 1.6154	5.68
70 1.3083 4 97 1.4748	5.04	1.6174	5.70
71 1.01 4.38	5.05	1,6194	5.71
72 1 1.010	5.06	1.6214	5.72
101 4.40 1 4839	5.07	1.6233	5.73
74 1 9918 4.41 1 4861	5.08	1.6253	5.74
1 2944 4.45 1 4884	5.09	1.6273	5.75
10	5.10	1.6292	5.76
78 1.3297 1 4.45 1.4929	5.11	1.6312	5.77
	5.12 5.13	1.6332 1.6351	5.78 5.79
	5.14	1.6371	5.80
	5.15	1.6390	5.81
	5.16	1.6409	5.82
BASS AND A BORR	5.17	1.6429	5.83
3.84 1.3481 4.51 1.5085	5.18	1.6448	5.84

No.	Log.	No.	Log.	No.	Log.	No.	Log.	No.	Log.
6.51	1.8788	7.15	1.9671	7.79	2.0528	8.66	2.1587	9.94	2.2966
6.52	1.8749	7.16	1.9685	7.80	2.0541	8.68	2.1610	9.96	2.2986
6.53	1.8764	7.17	1.9699	7.81	2.0554	8.70	2.1688	9.98	2.8006
6.54	1.8779	7.18	1.9718	7.82	2.0567	8.78	2.1656	10.00	2.3026
6.55	1.8795	7.19	1.9727	7.88	2.0580	8.74	2.1679	10.25	2.8279
6.56	1.8810 1.8825	7.20	1.9741	7.84 7.85	2.0592 2.0605	8.76	2.1702 2.1725	10.50 10.75	2.8518 2.8749
6.57 6.58	1.8840	7.22	1.9769	7.86	2.0618	8.78 8.80	2.1748	11.00	2.8979
6.59	1.8856	7.28	1.9782	7.87	2.0681	8.82	2.1770	11.25	2.4201
6.60	1.8871	7.94	1.9796	7.88	2.0648	8.84	2.1798	11.50	2.4430
6.61	1.8886	7.25	1.9810	7.89	2.0656	8.86	2.1815	11.75	2.4636
6.62	1.8901	7.26	1.9824	7.90	2.0669	8.88	2.1838	12.00	2.4849
6.63	1.8916	7.27	1.9888	7.91	2.0681	8.90	2.1861	12.25	2.5052
6.64	1.8981	7.28	1.9851	7.92	2.0694	8.99	2.1888	18.50	2.5262
6.65	1.8946 1.8961	7.29	1.9865 1.9879	7.98	2.0707 2.0719	8.94 8.96	2.1905 2.1928	12.75 13.00	2.5455 2.5649
6.66 6.67	1.8976	7.81	1.9892	7.95	2.0788	8.98	2.1950	18.25	2.5840
6.68	1.8991	7.32	1.9906	7.96	2.0744	9.00	2.1972	13.50	2.6027
6.69	1.9006	7.88	1.9920	7.97	2.0757	9.02	2.1994	18.75	2.6211
6.70	1.9021	7.84	1.9938	7.98	2.0769	9.04	2.2017	14.00	2.6891
6.71	1.9036	7.85	1.9947	7.99	2.0782	9.06	2.2039	14.25	2.6567
6.72	1.9051	7.86	1.9961	8.00	2.0794	9.08	2.2061	14.50	2.6740
6.78 6.74	1.9068 1.9081	7.87	1.9974 1.9988	8.01	2.0807 2.0819	9 10 9.12	2.2088 2.2105	14.75 15.00	2.6918 2.7081
6.75	1.9095	7.89	2.0001	8.03	2.0832	9.14	2.2127	15.50	2.7408
6.76	1.9110	7.40	2.0015	8.04	2.0844	9.16	2.2148	16.00	2.7726
6.77	1.9125	7.41	2.0028	8.05	2.0857	9.18	2.2170	16.50	2.8034
6.78	1.9140	7.42	2.0041	8.06	2.0869	9.20	2.2192	17.00	2.8832
6.79	1.9155	7.43	2.0055	8.07	2.0682	9.22	2.2214	17.50	2.8521
6.80	1.9169	7.44	2.0069	8.08	2.0894	9.24	2.2235	18.00	2.8904
6.81 6.82	1.9184 1.9199	7.45 7.46	2.0082	8.09 8.10	2.0906 2.0919	9.26 9.28	2.2257 2.2279	18.50 19.00	2.9178 2.9444
6.83	1.9218	7.47	2.0108	8.11	2.0931	9.30	2.2800	19.50	2.9703
6.84	1.9228	7.48	2.0122	8.12	2.0948	9.82	2,2322	20.00	2.9957
6.85	1.9242	7.49	2.0136	8.18	2.0956	9.34	2.2348	21	8.0445
6.86	1.9257	7.50	2.0149	8.14	2.0968	9.36	2.2364	22	8.0910
6.87	1.9272	7.51	2.0162	8.15	2.0980	9.88	2.2886	28	8.1855
6.88	1.9286 1.9801	7.52	2.0176 2.0189	8.16	2.0992 2.1005	9.40	2.2407 2.2428	24 25	8.1781 8.2189
6.89 6.90	1.9815	7.54	2.0202	8.18	2.1017	9.44	2.2450	26	8.2581
6.91	1.9830	7.55	2.0215	8.19	2.1029	9.46	2.2471	27	3.2958
6.92	1.9844	7.56	2.0239	8.90	2.1041	9.48	2.2492	28	8.8822
6.93	1.9359	7.57	2.0242	8.22	2.1066	9.50	2.2518	29	8.8678
6.94	1.9378	7.58	2.0255	8.24	2.1090	9.52	2.2534	30	8.4012
6.95	1.9387	7.59	2.0268	8.26	2.1114	9.54	2.2555	81	3.4840
6.96 6.97	1.9402	7.60 7.61	2.0295	8.28 8.30	2.1138 2.1168	9.56 9.58	2.2576 2.2597	82 83	8.4657 8.4965
6.98	1.9430	7.62	2.0308	8.32	2.1187	9.60	2.2618	84	3.5968
6.99	1.9445	7.68	2.0321	8.84	2.1211	9.62	2.9638	85	8.5558
7.00	1.9459	7.64	2.0834	8.86	2.1235	9.64	2.2659	86	8.5835
7.01	1.9478	7.65	2.0347	8.88	2.1258	9.66	2.2680	87	8.6109
7.02	1.9488	7.66	2.0860	8.40	2.1282	9.68	2.2701	38	8.6876
7.08 7.04	1.9502	7.67	2.0378 2.0886	8.42	2.1306 2.1330	9.70	2.2721 2.2748	89 40	3.6636 3.6889
7.04	1.9530	7.69	2.0899	8.46	2.1358	9.74	2.2768	41	3.7136
7.06	1.9544	7.70	2.0412	8.48	2.1377	9.76	2.2788	49	8.7877
7.07	1.9559	1 7.71	2.0425	8.50	2.1401	9.78	2.2808	48	8.7612
7.08	1.9578	7.72	2.0438	8.52	2.1424	9.80	2.2824	44	8.7842
7.09	1.9587	7.78	2.0451	8.54	2.1448	9.88	2.2844	45	8.8067
7.10	1.9601	7.74	2.0464	8.56	2.1471	9.84	2.2865	46	8.8986
7.11	1.9615	7.75	2.0477	8.58	2.1494	9.86	2.2885	47	8.8501
7.12 7.18	1.9629	7.76	2.0490 2.0508	8.68	2.1518 2.1541	9.88	2.2905 2.2925	48 49	3.8718 3.8918
7.14	1.9657	7.78	2.0516	8.64	2.1564	9.92	2.2946	50	8.9120
		11		1		1	1	11 -5	1

NATURAL TRIGONOMETRICAL FUNCTIONS.

0	M.	Sine.	Co-Ver	8.	Cosec.	Tang.	Cotan.	Secant.	Ver. Sir.,	Cosine.	
0	0	.00000	1.0000	In	finite	.00000	Infinite	1.0000	,00000	1,0000	90
7	15	.00436	.9956		9.18		229.18	1,0000	.00001	.99999	77
	30	.00873	.9912		4.59		114.59	1.0000	.00004	.99996	
	45	.01309	.9869		6.397	.01309	76.390	1.0001	.00009	.99991	
1	10	.01745	.9825	5 5	7.299	.01745	57,290	1.0001	.00015	.99985	89
•	15	.02181	,9781	9 4	5.840	.02182	45.829	1.0002	.00024	.99976	00
	30	.02618	.9738	32 3	8.202	.02618	38.188	1.0003	.00034	.99966	
1	45	.03054	.9694	16 3	8.202	.03055	32.730	1.0005	.00047	.99953	- 1
	0	.03490	.965	10 2	8.654	.03492	28.636	1.0006	.00061	.99939	88
1	15	.03926	.960			.03929	25.452	1.0008	.00077	.99923	00
-1		.04362	.956			.04366	22,904	1.0009	.00095	.99905	
1		.04798	.952			.04803	20.819	1.0011	.00115	.99885	
1		.05234	.947			.05241	19.081	1.0014	.00137	,99863	87
ı		.05669		21 1	7.639	.05678	17.611	1.0016	.00161	.99839	0.
L	30	.06105	.938			.06116	16.350	1.0019		.99813	
1						.06554	15.257	1.0021	.00214	.99786	
ı	45	.06540	,930	24	4.336	.06993	14.301	1.0024	.00244	.99756	86
1		.06976	.925	580		.07431	13.457	1.0028	.00275	.99725	30
1		.07411			12.745	.07870	12.706	1.0031	.00308	.99692	
1	30	.07846	1 .91			.08309	12.035	1.0034	.00343	.99656	
1	45	0971		284		.08749	11.430	1.0038	.00381	.99619	85
1	0	.0871		850		.09189	10.883	1.0042	.00420	.99580	00
1	15	.0915		415	10.433	.09629	10.385	1.0046	.00460	.99540	
١	30	.0958		981		.10069	9.9310	1.0051	.00503	.99497	
. 1	45	.1001		9547		.10510	9.5144	1.0055		.99452	84
4	0	.1045		3119	9.1855		9.1309	1.0060	.00594	.99406	94
1	15	.108		9118		.11393	8.7769	1.0065			
	30			8680	8.5079		8.4490	1.0000	.00643	.99357	
_	45	1.117	04 .8	8246	8.2055				.00693	.99307	00
7	15			7813			8.1443	1.0075	.00745	.99255	83
	1		520 .8	37380	7.9240		7.8606	1.0081	.00800	.99200	
				36947	7.6613		7.5958	1.0086	.00856	.99144	
	14			36515	7.4156		7,3479	1.0092	.00913	.99086	00
2	8	0 1.13	3917 .	36083	7.1853		7.1154	1.0098	.00973	.99027	82
	-1	15 1.1	1349	85651	6.9690		6.8969	1.0105		.98965	
	1	30 1.1		85219	6.7655	•14945	6,6912	1.0111	.01098	.98902	
			5212 .	84788	6.5736	15391	6.4971	1.0118		.98836	
	9			84357	6.3924		6.3138	1.0125		.98769	81
				.83926	6.2211		6.1402	1.0132		.98700	
				.83495	6.0589		5.9758	1.0139		.98629	
		45 -		.83065	5.9049	.17183	5.8197	1.0147	.01444		
	10			.82635	5.7588	-17633	5.6713	1.0154	.01519		80
		15	17794	.82206	5.6198		5,5301	1.0162			
			18224	.81776	5.4874		5.3955	1.0170		.98325	
			.18652	.81348	5.3612		5.2672	1.0179			4/4
	11	0	.19081	.80919	5.2408		5.1446	1.0187	.01837	,98163	79
		15	.19509	.80491	5.1258	-19891	5.0273	1.0196		.98079	
		30	.19937	.80063	5.0158			1.0205			
	53	45	.20364	.79636	4.9106			1.0214			
	L		.20791	.79209	4.8097	.21256	4,7046	1.0223		.97815	78
		15	.21218	.78782	4.7130	-21712	4.6057	1.0233		.97723	
		30	.21644	.78356	4.6202	.22169		1.0243	.02370	.97630	
		45	.22070	.77930	4.5311	.22628		1.0253		.97534	
	1		.22495	.77505	4.4454		4.3315	1.0263		.97437	77
		15	.22920	.77080	4.3630	.23547	4.2468	1.0273	.02662		
		30	.23345	.76655	4.2837	-24008	4.1653	1.0284			
		45	.23769	.76231	4.2072	.24470		1.0295			
	1	4 0	.24192	.75808	4.1336						76
	15	15	.24615	.75385	4.0625					.96923	
		30	.25038	.74962	3.9939			1.0329			
		45	.25460	.74540	3.9277						
	1	5 0	.25882	.74118	3.8637						75
	-	-				-			-	-	-
				Ver. Sin.	Secant.	Cotan.	Tang.	Cosec,	Co-Vers.	Sine,	0

From 75° to 90° read from bottom of table upwards.

•	M.	Sine.	Co-Vers.	Cosec,	Tang.	Cotan.	Secant,	Ver. Sin.	Cosine,		
15	0	.25882	.74118	8.8687	.26795	8.7820	1.0358	.08407	.96598	75	0
	15	.26303	.73697	8.8018	.27263	3.6680	1.0865	.08521	.96479		45
	80	.26724	.78276	8.7420	.27732	8.6059	1.0377	.08687	.96868		80
	45	.27144	.72856	3.6840	.28203	8.5457	1.0390	.08754	.96246		15
16	0	.27564	.72436	8.6280	.28674	3.4874	1.0408	.03874	.96126	74	0
	15	.27988	.72017	8.5736	.29147	8.4308	1.0416	.03995	.96005		45
	30	.28402	.71598	8.5209	.29621	3.3759	1.0429	.04118	.95882		80
	45	.28820	.71180	8.4699	.30096	3.3226	1.0448	.04248	.95757		15
17	0	.29237	.70768	3.4203	.80573	8.2709	1.0457	.04870	.95630	78	0
	15	.29654	.70846	8.3722	.81051	3.2205	1.0471	.04498	.95502		45
	80	.30070	.69929	3.3255	.81530	8.1716	1.0485	.04638	.95372		80
	45 0	.80486	.69514	3.2801	.82010	3.1240	1.0500	.04760	.95240		15
18	.0	.80902	.69098	3.2361	.32492	8.0777	1.0515	.04894	.95106	72	0
	15	.81816	68684	8.1932	.82975	3.0326	1.0530	.05030	.94970	i l	45
	30	.81730	.68270	8.1515	.33459	2.9887	1.0545	.05168	.94882		30
	45	.32144	.67856	8.1110	.33945	2.9459	1.0560		.94693		15
19	0	. 32557	.67443	8.0715	.84433	2.9042	1.0576	.05448	.94552	71	0
	15	.32969	.67081	8.0831	.34921	2.8636	1.0592		.94409		45
	80	.33381	.66619	2.9957	.35412	2.8239	1.0608	.05736	.94264		80
	45	.88792	.66208	2.9593	.35904	2.7852	1.0625	.05882	.94118		15
20	0	.84202	65798	2.9238	.86397	2.7475	1.0642	.06031	.93969	70	0
	15	.84612	·65888	2.8892	.36892	2.7106	1.0659 1.0676	.06181 .06338	.93819		45
	30	.85021	.64979	2.8554	.87388	2.6746	1.0676	.06338	98667		80
	45	.85429	.64571	2.8225	.37887	2.6395	1.0694	.06486	.93514		15
21	0	.85837	.64163	2.7904	.38386	2.6051	1.0711	.06642	.98858	69	0
	15	.36244	.63756	2.7591	·38888	2.5715	1.0729	.06799	.93201		45
	30	.86650	.68350	2.7285	.39391	2.5886	1.0748	.06958	.98042		80
	45	.37056	.62944	2.6986	.39896	2.5065	1.0766	.07119	.92881		15
22	0	.87461	.62539	2.6695	·40408	2.4751	1.0785	.07282	.92718	68	0
	15	.87865	.62135	2.6410	.40911	2.4448	1.0804	.07446	.92554		45
	80	.88268	.61782	2.6131	.41421	2.4142	1.0824	.07612	.92388		80
	45	.38671	.61829	2.5859	.41983	2.3847	1.0844	.07780	.92220		15
28	0	.89073	.60927	2.5593	.42447	2.3559	1.0864	.07950	.92050	67	0
-	15	.39474	.60526	2.5383	. 42963	2.3276	1.0884	.08121	.91879		45 30
	80	.39875	60125	2.5078	.48481	2.2998	1.0904	.08294	.91706		30
	45	.40275	.59725	2.4829	.44001	2 2727	1.0925	.08469	.91531		15
24	0	.40674	.59326	2.4586	.44523	2.2460	1.0946	.08645	.91855	66	0
	15	.41072	.58928	2.4348	.45047	2.2199	1.0968	.08824	.91176		45
	30	.41469	.58531	2.4114	.45573	2.1943	1.0989	.09004	.90996		30
	45	41866	58184	2.3886	.46101	2.1692	1.1011	.09186	.90814		15
25	0	.42262	.57788	2.3662	.46631	2.1445	1.1034	.09369	.90631	65	0 45
- 1	15	.42657	.57848	2.8443	.47163	2.1203	1.1056	.09854	.90446		45
	30	.43051	.56949	2.3228	.47697	2.0965	1.1079	.09741	.90259		30
1	45	. 43445	.56555	2.3018	.48234	2.0732	1.1102	.09930	.90070		15
26	0	.43837	.56163	2.2312	.48773	2.0503	1.1126	.10121	.89679	64	0
	15	.44229	.55771	2.2610	.49314	2.0278	1.1150	.10818	.89687		45
	30	.44620	55380	2.2412	.49858	2.0057	1.1174	.10507	.89498		86
	45	.45010	.54990	2.2217	.50404	1.9840	1.1198	.10702	.89298		15
27	0	.45339	.54601	2.2027	.50952	1.9626	1.1223	.10899	.89101	68	0
	15	.45787	.54218	2.1840	.51508	1.9416	1.1248	.11098	.88902		45
	30	.46175	.53825	2.1657	.52057	1.9210	1.1274	.11299	.88701		30
	45	.46561	.53439	2.1477	.52612	1.9007 1.8807	1.1300	.11501	.88499		15
28	0	.46947	.53053	2.1800	.58171	1.8807	1.1326 1.1852	.11705	.88295	62	10
	15	.47332	.52668	2.1127	.53782	1.8611	1.1852	.11911	.88089		45
	80	.47716	.52284	2.0957	. 54295	1.8418	1.1379	.12118	.87882		30
	45	.48099	.51901	2.0790	.54862	1.8228	1.1406	.12827	.87678	!	15
29	0	. 48481	.51519	2.0627	.55481	1.8040	1.1488	.12588	.87462	61	0
	15	.48862	.51138	2.0466	.56003	1.7856	1.1461	.12750	.87250		45
	30	.49242	.50758	2.0308	.56577	1.7675	1.1490	.12964	.87036		80
	45	.49622	.50878	2.0152	.57155	1.7496	1.1518	.18180	.86820		15
80	Õ	.50000	.50000	2.0000	.57785	1.7320	1.1547	.18397	.86608	60	Ō
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From 60° to 75° read from bottom of table upwards.

•	M.	Sine.	Co-Vers.	Cosec.	Tang.	Cotan.	Secant.	Ver, Sin,	Cosine,	
30	0	.50000	.50000	2.0000	.57785	1.7320	1.1547	.13397	.86603	60
90	15	50377	49623	1.9850	.58318	1.7147	1.1576	.13616	.86384	00
	30	.50754	49246	1.9703	.58904	1.6977	1.1606	.13837	.86163	
		.51129	.48871	1.9558	.59494	1.6808	1.1656	.14059	.85941	
	45		.48496	1.9416	.60086	1.6643	1.1666	.14283	.85717	59
31	0	.51504	.48123	1.9276	.60681	1.6479				99
	15	.51877		1.9139	.61280		1.1697	.14509	.85491	
- 1	30	.52250	47750			1.6319	1.1728	.14736	.85264	
	45	.52621	.47379	1.9004	.61882	1.6160	1.1760	.14965	.85035	*0
32	0	.52992	47008	1.8871	.62487	1.6003	1.1792	.15195	.84805	58
	15	.53361	.46639	1.8740	.63095	1.5849	1.1824	.15427	.84573	
- 1	30	.53730	.46270	1.8612	.63707	1.5697	1.1857	.15661	.84339	
	45	.54097	.45903	1.8485	.64322	1.5547	1.1890	.15896	.84104	
33	0	.54464	45536	1.8361	.64941	1.5399	1 1924	.16133	.83867	57
	15	.54829	.45171	1.8238	. 65563	1.5253	1.1958	,16371	.83629	
- 1	30	.55194	.44806	1.8118	.66188	1.5108	1,1992	.16611	.83389	
- 1	45	.55557	.44443	1.7999	.66818	1,4966	1.2027	.16853	.83147	
34	0	.55919	.44081	1.7883	.67451	1.4826	1,2062	.17096	.82904	56
-	15	.56280	.43720	1.7768	.68087	1.4687	1,2098	.17341	.82659	
	30	:56641	.43359	1.7655	.68728	1.4550	1.2134	.17587	.82413	
	45	.57000	43000	1.7544	.69372	1.4415	1.2171	.17835	.82165	
35	0	.57358	.42642	1.7434	.70021	1.4281	1.2208	.18085	.81915	55
99	15	.57715	42285	1.7327	.70673	1.4150	1.2245	.18336	.81664	7.1.
		.58070	.41930	1.7230	.71329	1.4019	1.2283	.18588	.81412	
	30	.58425	.41575	1.7116	.71990	1.3891	1.2322	.18843	.81157	
	45	.58779	41221	1.7013	.72654	1.3764	1.2361	,19098	.80902	54
36	0		40869	1.6912	.73323	1.3638	1.2400	.19356	.80644	
	15	.59131	40518	1.6812	.73996	1.3514	1.2440	.19614	.80386	
- 1	30	.59482	40168	1.6713	.74673	1.3392	1.2480	.19875	.80125	
	45	.59832	39819	1.6616	.75355	1.8270	1.2521	.20136	.79864	53
7	0	.60181		1.6521	.76042	1.3151	1.2563	.20400	.79600	90
	15	.60529	.39471	1.6427	.76733	1 2020				
- 1	30	.60876	.39124			1.3032	1.2605	.20665	,79335	
	45	.61222	.38778	1.6334	.77428	1.2915	1.2647	.20931	.79069	20
18	0	.61566	.38434	1.6243	.78129	1.2799	1.2690	.21199	.78801	52
~	15	.61909	28091	1.6153	.78834	1.2685	1.2734	.21468	.78532	
	30	.62251	.37749	1.6064	.79543	1.2572	1.2778	.21739	.78261	
	45	.62592	.37408	1.5976	.80258	1.2460	1.2822	.22012	.77988	
39	0	.62932	37008	1.5890	.80978	1.2349 1.2239	1.2868	. 22285	.77715	51
,,,	15	.63271	.36729	1.5805	.81703	1.2239	1.2913	.22561	.77439	
	30	.63608	36392	1.5721	.82434	1,2131	1.2960	.22838	.77162	
	45	.63944	1 36056	1.5639	.83169	1,2024	1.3007	.23116	.76884	
10	0		35721	1.5557	.83910	1.1918	1.3054	.23396	.76604	50
40	15		2 .35388	1.5477	.84656	1.1812	1.3102	.23677	.76323	
	30		51 .35000	1.5398	.85408	1.1708	1.3151	.23959	.76041	
	43		6 .34724	1.5320	.86165	1.1606	1.3200	.24244	.75756	
			6 .34394	1.5242	.86929	1.1504	1.3250	.24529	.75471	49
41		a married		1.5166	.87698	1.1403	1.3301	.24816	.75184	
	1	0.000		1.5092	.88472	1,1303	1.3352	.25104	.74896	
	3		-20 4 4 6	1.5018	.89253	1.1204	1.3404	25394	.74606	5
			00000	1.4945	.90040	1.1106	1.3456	25686	.74314	48
45		0 .669	manage.	1.4873	.90834	1.1009	1.3509	.25978	.74022	
		5 .672		1.4802	.91633	1.0913	1.3563	.26272	.73728	
		0 .675		1.4732	.92439	1.0818	1.3618	.26568	.78432	
		5 .678		1.4663	.93251	1.0518		.26865	.73135	47
4		0 .682		1.4595			1.3673			
179		15 .685			.94071	1.0630	1.3729	.27163	.72837	
		30 .688		1.4527	.94896	1.0538	1.3786	.27463	.72587	
		45 .691		1.4461	.95729	1.0446	1.3843	.27764	.72236	10
4	14	0 .694		1.4396	.96569	1.0355	1.3902	.28066	.71934	46
100		15 .697	79 .30221	1.4331	.97416	1.0265	1.3961	.28370	.71630	-
	1	30 .700	91 .29909	1.4267	.98270	1.0176	1.4020	.28675	.71325	(-
	1	45 .704	101 .29599	1.4204	.99131	1.0088	1.4081	.28981	.71019	
	45	0 .70	711 .29289	1.4142	1.0000	1.0000	1.4142	.29289	.70711	45
	1000	_								

From 45° to 60° read from bottom of table upwards.

LOGARITHMIC SINES, ETC.

Deg.	Sine.	Cosec.	Versin.	Tangent.	Cotan.	Covers.	Secant.	Cosine.	Deg.
0	In.Neg.	Infinite.	In.Neg.	In.Neg.		10.00000			90
ì	8.24186	11.75814	6.18271	8.24192	11.75808		10.00007	9.99998	
2	8.54282	11.45718	6.78474	8.54808	11.45692	9.98457	10.00026	9.99974	88
8		11.28120	7.18687		11.28060	9.97665	10.00060	9.99940	87
4		11.15642	7.38667		11.15596		10.00106		86
	0 04000	11.05970	7.58089	9 04105	11.05805	0 08040	10.00166	9.99834	85
5							10.00239	9.99761	
6		10.98077	7.73863 7.87238		10.97838 10.91086		10.00825	9.99675	
7		10.91411	7.01200						
8		10,85644 10,80567	7.98820 8.09032		10.85220 10.80029		10.00425 10.00588	9.99575 9.99462	
y	8.18400	10.00001	0.0000	0.10011	10.000.00	0.00012	10.00000	0.00104	01
10		10.76088	8.18162		10.75868		10,00665	9.99835	
11	9.28060	10.71940	8.26418		10.71185		10.00805		79
12	9.31788	10.68212	8.33950		10.67258		10.00960	9.99040	
13	9.35209	10.64791	8.40875		10.63664		10.01128	9.98872	77
14	9.38368	10.61632	8.47282	9.89677	10.60828	9.87971	10.01810	9.98690	76
15	0.41900	10.58700	8.53248	0 49905	10.57195	0 96000	10.01506	9.98494	75
16		10.55966	8.58814				10.01716		74
17		10.53406	8.64048		10.51466		10.01940		
18		10.51002	8.68969		10.48822		10.02179		72
		10.48786	8.73625		10.46303		10.02433		71
19	8.01204	10.90100	0.10000	Ø.0000	10.4000	J. G.CO.	10,03800	0.0.00	٠.
20	9.53405	10.46595	8.78037	9.56107	10.48893	9.81821	10.02701	9.97299	70
21		10.44567	8,82290		10.41582	9.80729	10.02985	9.97015	69
22		10.42642	8.86228		10.89859	9.79615	10.03288	9.96717	68
28		10.40812	8.90034		10,87215		10.08597	9.96408	
24		10.89069			10.85142		10.03927	9.96078	66
					10 00100	0 2001.40	10.04272	9.95728	
25		10.87405	8.97170		10.88188				
26		10.35816	9.00521		10.81182		10.04684		
27		10.84295	9.03740		10.29283		10.05012	9.94988	
28		10.32839	9.06838		10.27483		10.05407	9.94593	62
29	9.68557	10.81448	9.09823	9.74875	10.25625	9.71197	10.05818	9.94182	61
30	0 60907	10.80108	9.12702	9.76144	10.23856	9 69897	10.06247	9.93753	60
81		10.28816			10.22123		10.06693		59
82	0 79491	10.27579	9.18171	0 70570	10.20421	9 67217	10 07158	9.92842	
88		10.26389			10.18748	9.65898	10.07158 10.07641	9.92859	
84		10.25244			10.17101	9.64425	10.08143	9.91857	56
	3.14.00		1	1				1	
85		10.24141	9.25781		10.15477		10.08664	9.91336	
86		10.23078	9.28099		10.18874		10.09204	9.90796	
87		10.22054	9.30398		10.12289		10.09765	9.90235	58
8 8		10.21066	9.32631	9,89281			10.10847	9.89653	
89	9.79887	10.20118	9,84802	9.90637	10.09168	9.56900	10.10950	9.89050	51
40	9 90907	10.19193	9.86918	9.92881	10.07619	9 55293	10.11575	9.88425	50
41	0.81804	10.18806	9.38968		10.06084	0 53848	10.12222	9.87778	49
42		10.17449	9.40969		10.04556		10.12893	9.87107	48
48	0.00001	10,16622	9.42918		10.08034		10.18587	9.86418	
44	9.84177	10.15828	9.44818		10.01516		10.14807	9.85693	46
45	9.84949	10.15052	9.46671	10.00000	10.00000	9.46671	10.15052	9.84949	45
	Cosine.	Secant.	Covers.	Cotan.	Tangent.	Versin.	Cosec.	Sine.	
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From 45° to 90° read from bottom of table upwards,

MATERIALS.

THE CHEMICAL ELEMENTS.

The Common Elements (42).

Chemical Symbol.	Name.	Atomic Weight.	Chemical Symbol.	Name.	Atomic Weight.	Chemical Symbol.	Name.	Atomic Weight.
Al Sb As Ba Bi B Cd Ca CC Cl Cr Co	Aluminum Antimony Arsenic Barium Bismuth Boron Bromine Cadmium Calcium Carbon Chlorine Chromium Cobalt Copper	27.1 120.4 75.1 187.4 208.1 10.9 79.9 111.9 40.1 12. 85.4 52.1 59. 63.6	F Au H Iree Pb Li Mn H Ni NO	Fluorine Gold Hydrogen Iodine Iridium Iron Lead Lithium Magnesium Manganese Mercury Nickel Nitrogen Oxygen	19. 197.2 1.01 126.8 193.1 56. 206. 207.03 24.3 55. 200. 58.7 14. 16.	Pd P Pt KSi AS Sr Ssn Ti Va Zn	Palladium Phosphorus Platinum Potassium Silicon Silver Sodium Strontium Sulphur Tin Titanium Tungsten Vanadium Zinc	106. 81. 194.9 89.1 28.4 107.9 28. 87.6 32.1 119. 48.1 184.8 51.4 65.4

The atomic weights of many of the elements vary in the decimal place as given by different authorities. The above are the most recent values referred to O = 16 and H = 1.008. When H is taken as 1, O = 15.879, and the other figures are diminished proportionately. (See Jour. Am. Chem. Soc., March, 1896.)

The Bare Elements (27).

Beryllium, Be. Cæsium, Cs. Cerium, Ce. Didymium, D. Erbium, E. Gallium, Ga. Germanium, Ge.

Glucinum, G. Indium, In. Lanthanum, La Molybdenum, Mo. Niobium, Nb. Osmium, Os. Rhodium, R.

Rubidium, Rb. Ruthenium, Ru. Samarium, Sm. Scandium, Sc. Selenium, Se. Tantalum, Ta. Tellurium, Te.

Thallium, Tl. Thorium, Th. Uranium, U. Ytterbium, Yr. Yttrium, Y. Zirconium, Zr.

SPECIFIC GRAVITY.

The specific gravity of a substance is its weight as compared with the weight of an equal bulk of pure water.

To find the specific gravity of a substance.

W = weight of body in air; w = weight of body submerged in water.

Specific gravity
$$\pm \frac{W}{W-w}$$
.

If the substance be lighter than the water, sink it by means of a heavier substance, and deduct the weight of the heavier substance.

Specific-gravity determinations are usually referred to the standard of the weight of water at 62° F., 62.355 lbs. per cubic foot. Some experimenters have used 60° F. as the standard, and others 82° and 39.1° F. There is no general agreement.

Given sp. gr. referred to water at 39.1° F., to reduce it to the standard of 62° F. multiply it by 1.00112.

Given sp. gr. referred to water at 62° F., to find weight per cubic foot m tiply by 62,355. Given weight per cubic foot, to find sp. gr. multiply 63,3657. Given sp. gr., to find weight per cubic inch multiply by .03608.

Weight and Specific Gravity of Metals.

	Specific Gravity. Range according to several Authorities.	Specific Grav- ity. Approx. Mean Value, used in Calculation of Weight.	Weight per Cubic Foot, lbs.	Weight per Cubic Inch, lbs.
Aluminum	2.56 to 2.71	2.67	166.5	.0963
Antimony	6.66 to 6.86 9.74 to 9.90	6.76 9.82	421.6 612.4	.2439
Brass: Copper + Zinc)	8.14 10 8.80	1		
80 20		(8.60 8.40	536.3 523.8	.310 3 .3081
70 30 \	7.8 to 8.6	8.36	521.8	.3017
50 50		(8.20	511.4	.2959
Bronze { Copper, 95 to 80 } Tin, 5 to 20 }	8.52 to 8.96	8.853	552.	.8195
Cadmium	8.6 to 8.7	8.65	539.	.3121
Calcium	1.58	1		
Chromium	5.0 8.5 to 8.6			
CobaltGold, pure	8.5 to 8.6 19.245 to 19.361	19,258	1200.9	.6949
Copper	8.69 to 8.92	8.853	552.	.8195
Iridíum	22.38 to 23.	0.000	1396.	.8076
Iron, Cast	6.85 to 7.48	7.218	450.	.2604
" Wrought	7.4 to 7.9	7.70	480.	.2779
Lead	11.07 to 11.44	11.38	709.7	.4106
Manganese	7. to 8.	8.	499.	.2887
Magnesium	1.69 to 1.75	1.75	109.	.0641
(82°	13.60 to 13.62	13.62	849.3	.4915
Mercury	13.58	13.58	846.8	.4900
(2120	13.87 to 13.38	13.38	834.4	.4828
Nickel	8.279 to 8.93	8.8	548.7	.3175
Platinum	20.33 to 22.07	21.5	1347.0	.7758
Potassium	0.865 10.474 to 10.511	10.505	655.1	0204
Sodium	0.97	10.505	000.1	.3791
Steel	7.69* to 7.932†	7.854	489.6	.2834
Tin	7.291 to 7.409	7.350	458.8	.2652
Titanium	5.3			2.200.0
Tungsten	17. to 17.6			
Zinc	6.86 to 7.20	7.00	436.5	.2526

Specific Gravity of Liquids at 60° F.

Acid, Muriatic	1.200	Oil, Olive	.92
" Nitrie			.97
" Sulphuric	1.849	" Petroleum	.78 to .88
Alcohol, pure	.794	" Rape	.92
Alcohol, pure	.816	" Turpentine	.87
" 50 " "	.934	" Whale	.92
Ammonia, 27.9 per cent Bromine	.891	Tar	1.
Bromine	2.97	Vinegar	1.08
Carbon disulphide	1.26	Water	1.
Ether, Sulphuric	.72	" sea	1.026 to 1.08
Oil, Linseed	.94		

Compression of the following Fluids under a Pressure of 15 lbs. per Square Inch.

Water	.00004663	Ether	.00006158
Alcohol	.0000216	Mercury	.00000265

^{*} Hard and burned.
† Very pure and soft. The sp. gr. decreases as the carbon is increased.
In the first column of figures the lowest are usually those of cast metals, which are more or less porous; the highest are of metals finely rolled or drawn into wire.

The Hydrometer.

The hydrometer is an instrument for determining the density of liquida. It is usually made of glass, and consists of three parts: (1) the upper part, a graduated stem or fine tube of uniform diameter; (2) a bulb, or enlargement of the tube, containing air; and (3) a small bulb at the bottom, containing shot or mercury which causes the instrument to float in a vertical position. The graduations are figures representing either specific gravities, or the numbers of an arbitrary scale, as in Baumé's, Twaddell's, Beck's, and other hydrometers.

There is a tendency to discard all hydrometers with arbitrary scales and to use only those which read in terms of the specific gravity directly.

Baume's Hydrometer and Specific Gravities Compared.

-								
8	Liquids Heavier	Liquids	Degrees Baumé.	Liquids Heavier	Liquids	Degrees Baumé.	Liquids Heavier	Liquids
8 6		Lighter	9 8		Lighter	9 g		Lighter
6.51	than	than	263	than	than	5.5	than	than
52	Water,	Water,	9 E	Water,	Water,	Ø 6	Water,	Water,
Degrees Baumé.	sp. gr.	sp. gr.	ПН	sp. gr.	sp. gr.	OΜ	sp. gr.	sp. gr.
0	1,000		19	1.148	.942	38	1.333	.839
1	1.007		20	1.152	.986	89	1.345	.834
2	1.018		21	1.160	.980	40	1.357	.830
8	1.020		22	1.169	.924	41	1.369	.825
4 1	1.027	1	28	1.178	.918	42	1.882	.820
5	1.034		24	1.188	.913	44	1.407	.811
6	1.041	l i	25	1.197	.907	46	1.434	.802
7	1.048		26	1.206	.901	48	1.462	.794
8	1.056		27	1.216	.896	50	1.490	.785
9	1.063		28	1.226	.890	52	1.520	.777
10	1.070	1.000	29	1.236	.885	54	1.551	.768
11	1.078	.993	30	1.246	.880	56	1.583	.760
12	1.086	.986	81	1,256	.874	58	1.617	.753
18	1.094	.980	82	1.267	.869	60	1.652	.745
14	1.101	.973	83	1.277	864	65	1.747	
15	1.109	.967	84	1.288	.859	70	1.854	
16	1.118	.960	85	1.299	854	75	1.974	
17	1.126	.954	86	1.810	.849	76	2.000	
18	1.134	.948	87	1.322	.844	ļ		1

Specific Gravity and Weight of Wood.

			Weight per Cubic Foot, lbs.		Specific Grav	rity.	Weight per Cubic Foot, lbs.
		Avge.				Avge.	
Alder	0.56 to 0.80	.68	42	Hornbeam	.76	.76	47
Apple	.78 to .79	.76	47	Juniper	.56	.56	35
Ash	.60 to .84	.72	45	Larch	.56	.56	35
Bamboo	.31 to .40	.35	22	Lignum vitæ	.65 to 1.33	1.00	62
Beech	.62 to .85	.73		Linden	.604		87
Birch	.56 to .74	.65	41	Locust	.728		46
Box ,	.91 to 1.83	1.12		Mahogany	.56 to 1.06	.81	51
Cedar	.49 to .75	.62		Maple	.57 to .79	.68	42
Cherry	.61 to .72	.66		Mulberry	.56 to .90	.73	46
Chestnut	.46 to .66	.56		Oak, Live		1.11	69
Cork	.24	.24	15	" White		.77	48
Cypress	.41 to .66	.53	88	" Red	.78 to .75	.74	46
Dogwood	.76	.76	47	Pine, White		.45	28
Ebony	1.18 to 1.38	1.23	76	" Yellow.	.46 to .76	.61	88
Elm	.55 to .78	.61		Poplar	.38 to .58	.48	36
Fir	.48 to .70	.59	87	Spruce	.40 to .50	.45	28
Gum	.84 to 1.00	.92	57	Sycamore	.59 to .62	.60	37
Hackmatack	.59	.59		Teak	.66 to .98	.82	51
Hemlock	.86 to .41	.38	24	Walnut	.50 to .67	.58	36 .
Hickory	.69 to .94	.77	48	Willow	.49 to .59	.54	84
Holly	.76	.76	47			- 1	

Weight and Specific Gravity of Stones, Brick, Cement, etc.

•	Pounds per Cubic Foot.	Specific Gravity.
Asphaltum	87	1.89
Brick, Soft	100	1.6
" Common	112	1.79
" Hard	125	2.0
" Pressed	185	2.16
" Fire	140 to 150	2.24 to 2.4
Brickwork in mortar	100	1.6
" cement	112	1.79
Cement, Rosendale, loose	60	.96
" Portland, "	78	1.25
lay	120 to 150	1.92 to 2.4
Concrete	120 to 140	1.92 to 2.24
Earth, loose	72 to 80	1.15 to 1.28
" rammed	90 to 110	1.44 to 1.76
Emery	250	4.
lass.	156 to 172	2.5 to 2.75
" flint	180 to 196	2.88 to 8.14
ineigg)		
Franite (·····	160 to 170	2.56 to 2.79
ravel	100 to 120	1.6 to 1.92
ypsum	130 to 150	2.08 to 2.4
Hornblende	200 to 220	8.2 to 8.52
Lime, quick, in bulk	50 to 55	.8 to .88
imestone	170 to 200	2.72 to 8.2
Ingnesia, Carbonate	150	2.4
farhle	160 to 180	2.56 to 2.88
farble	140 to 160	2.24 to 2.56
" dressed	140 to 180	2.24 to 2.88
fortar	90 to 100	1.44 to 1.6
itch	72	1.15
laster of Paris	74 to 80	1.18 to 1.28
Juartz	165	2.64
and.	90 to 110	1.44 to 1.76
andstone	140 to 150	2.24 to 2.4
ilate	170 to 180	2.72 to 2.88
Stone, various	185 to 200	2.16 to 3.4
rap	170 to 200	
ile	110 to 200	2.72 to 3.4
oapstone	166 to 175	1.76 to 1.92
	100 to 175	2.65 to 2.8

Specific Gravity and Weight of Gases at Atmospheric Pressure and 32° F.

(For other temperatures and pressures see pp. 459, 479.)

	Density, $Air = 1$.	Density, $H = 1$.	Grammes per Litre.		Cubic Ft. per Lb.
Air	1.0000	14.444	1.2931	.080723	12.388
Oxygen, O	1.1052	15.963	1.4291	.08921	11.209
Hydrogen, H		1.000	0.0895	.00559	178.931
Nitrogen, N	0.9701	14.012	1.2544	.07881	12,770
Carbon monoxide, CO	0.9671	13.968	1.2505	.07807	12.810
Carbon dioxide, CO	1.5197	21.950	1.9650	.12267	8.152
Methane, marsh-gas, CH,	0.5530	7.987	0.7150	.04464	22.429
Ethylene, C. H.		13.973	1.2510	.07809	12.805
Acetylene, U.H		12.978	1.1614	.07251	13.792
Ammonia, NH		8.506	0.7615	.04754	21.036
Water vapor, H ₂ O	0.6218	8.981	0.8041	.05020	19.922

PROPERTIES OF THE USEFUL METALS.

Aluminum, Al.—Atomic weight 27.1. Specific gravity 2.6 to 2.7. The lightest of all the useful metals except magnesium. A soft, duetile malleable metal, of a white color, approaching silver, but with a bluish cast. Very non-corrosive. Tenacity about one third that of wrought-iron. Formerly a rare metal, but since 1890 its production and use have greatly increased on account of the discovery of cheap processes for reducing it from the ore. Melts at about 1160° F. For further description see Aluminum, under Strength of Materials. under Strength of Materials.

Antimony (Stibium), Sb.—At. wt. 120.4. Sp. gr. 6.7 to 6.8. A brittle metal of a bluish-white color and highly crystalline or laminated structure. Melts at 842° F. Heated in the open air it burns with a bluish-white flame. tes chief use is for the manufacture of certain alloys, as type-metal (anti-mony 1, lead 4), britannia (antimony 1, tin 9), and various anti-friction metals (see Alloys). Cubical expansion by heat from 32° to 212° F., 0.0070.

Specific heat .050

Specific heat 0.50.

Bismuth, Bi.—At. wt. 208.1. Bismuth is of a peculiar light reddish color, highly crystalline, and so brittle that it can readily be pulverized. It meets at 510° F., and boils at about 2300° F. Sp. gr. 9.23 at 54° F., and 10.055 just above the melting-point. Specific heat about 0.301 at ordinary temperatures. Coefficient of cubical expansion from 32° to 212°, 0.0040. Conductivity for heat about 1.780 and for electricity only about 1.780 of that of silver. Its tensile strength is about 6400 lbs. per square inch. Bismuth expansion in cooling, and Tribe has shown that this expansion does not take place until after solidification. Bismuth is the most diamagnetic element known, a sphere of it being repelled by a magnet.

Cadminum. 601.—At. wt. 112. So. gr. 8.6 to 8.7. A bluish-white metal.

Cadmium, Cd.—At. wt. 112. Sp. gr. 8.6 to 8.7. A bluish-white metal, lustrous, with a fibrous fracture. Melts below 500° F. and volatilizes at about 680° F. It is used as an ingredient in some fusible alloys with lead, tin, and bismuth. Cubical expansion from 32° to 212° F., 0.0094.

Copper, Cu.—At. wt. 63.2. Sp. gr. 8.81 to 8.95. Fuses at about 1930° F. Distinguished from all other metals by its reddish color. Very ductile

F. Distinguished from all other metals by its reddish color. Very ductile and malleable, and its tenacity is next to iron. Tensile strength 20,000 to 30,000 lbs. per square inch. Heat conductivity 73.8% of that of silver, and superior to that of other metals. Electric conductivity equal to that of gold and silver. Expansion by heat from 32° to 212° F., 0.0051 of its volume. Specific heat .003. (See Copper under Strength of Materials: also Alloys.) Gold (Aurum), Au.—At. wt. 197.2. Sp. gr., when pure and pressed in a die, 19.34. Melts at about 1915° F. The most malleable and ductile of all metals. One ounce Troy may be beaten so as to cover 160 sq. ft. of surface. The average thickness of gold leaf is 1/282000 of an inch, or 100 sq. ft. per ounce. One grain may be drawn into a wire 500 ft. in length. The ductility is destroyed by the presence of 1/2000 part of lead, bismuth, or antimony. Gold is hardened by the addition of silver or of copper. In U. S. gold coin there are 30 parts gold and 10 parts of alloy, which is chiefly copper with a listle silver. By jewelers the fineness of gold is expressed in carats, pure gold being 24 carats, three fourths fine 18 carats, etc.

Iridium.—Iridium is one of the rarer metals. It has a white lustre, resembling that of steel; its hardness is about equal to that of the ruby; in the cold it is quite brittle, but at a white heat it is somewhat malleable. It is one of the fleaviest of metals, having a specific gravity of 22.35. It is extended infusible and almost absolutely inoxidizable.

For uses of Iridium, methods of manufacturing it, etc., see paper by W. D.

For uses of iridium, methods of manufacturing it, etc., see paper by W. D. Dudley on the "Iridium Industry," Trans. A. I. M. E. 1884.

Iron (Ferrum), Fe.—At. wt. 56. Sp. gr.: Cast, 6.85 to 7.48; Wrought, 7.4 to 7.9. Pure iron is extremely infusible, its melting point being above 3000° F., but its fusibility increases with the addition of carbon, cast iron fusing about 2500° F. Conductivity for heat 11.9, and for electricity 12 to 14.8, siver being 100. Expansion in bulk by heat: cast iron. 2033, and wrought iron. 3035, from 25° to 312° F. Specific heat: cast iron. 1298, wrought iron. 1138.

Attail 1165. Clast iron exposed to continued heat becomes permanently extend 1165. steel .1165. Cast iron exposed to continued heat becomes permanently expanded 11/2 to 3 per cent of its length. Grate-bars should therefore be allowed about 4 per cent play. (For other properties see Iron and Steel under Strength of Materials.)

Lead (Furnburg, Pb.—At. wt. 206.9. Sp. gr. 11.07 to 11.44 by different suchericles. Melta at about 625° F., softens and becomes pasty at about 61° F. If broken by a sudden blow when just below the melting-point it is quite britistle and the fracture appears crystalline. Lead is very malleable.

and ductile, but its tenacity is such that it can be drawn into wire with great difficulty. Tensile strength, 1600 to 2400 lbs. per square inch. Its elasticity is very low, and the metal flows under very slight strain. Lead dissolves some extent in pure water, but water containing carbonates or sulphates forms over it a film of insoluble salt which prevents further action.

Magnesium, Mg.—At. wt. 24. Sp. gr. 1.69 to 1.75. Silver-white, brilliant, malleable, and ductile. It is one of the lightest of metals, weighing only about two thirds as much as aluminum. In the form of filings, wire, or thin ribbons it is highly combustible, burning with a light of dazzling brilliancy, useful for signal-lights and for flash-lights for photographers. It is nearly non-corrosive, a thin film of carbonate of magnesia forming on exposure to damp air, which protects it from further corrosion. It may be alloyed with aluminum, 5 per cent Mg added to Al giving about as much increase of strength and hardness as 10 per cent of copper. Cubical expansion by heat 0.0083, from 32° to 212° F. Melts at 1200° F. Specific heat .25.

Manganese, Min.—At. wt. 55. Sp. gr. 7 to 8. The pure metal is not used in the arts, but alloys of manganese and iron, called spiegeleisen when

used in the arts, but alloys or manganese and iron, called spreguenese when containing below 25 per cent of manganese, and ferro-manganese when containing from 25 to 90 per cent, are used in the manuficture of steel. Metallic manganese, when alloyed with iron, oxidizer applidy in the air, and its function in steel manufacture is to remove the oxygen from the bath of steel whether it exists as oxide of iron or as occluded gas.

Mercury (Hydrargyrum), Hg.-At. wt. 199.8. A silver-white metal, liquid at temperatures above—39° F., and boils at 680° F. Unchangeable as gold, silver, and platinum in the atmosphere at ordinary temperatures, but oxidizes to the red oxide when near its boiling-noint. So gr.: when liquid

oxidizes to the red oxide when near its boiling-point. Sp. gr.: when liquid 13.58 to 13.59, when frozen 14.4 to 14.5. Easily tarnished by sulphur fumes, also by dust, from which it may be freed by straining through a cloth. No metal except iron or platinum should be allowed to touch mercury. The metal except from or platinum should be anowed to touch mercury. The smallest portions of tin, lead, zinc, and even copper to a less extent, cause it to tarnish and lose its perfect liquidity. Coefficient of cubical expansion from \$2° to 212° F. .0182; per deg. .000101.

Nickel, Ni.—At. wt. 58.3. Sp. gr. 8.27 to 8.98. A silvery-white metal with a strong lustre, not tarnishing on exposure to the air. Ductile, hard, and as tenacious as iron. It is attracted to the magnet and may be made

and as teneduals in the like iron. Nickel is very difficult of fusion, melting at about 3000° F. Chiefly used in alloys with copper, as german-silver, nickel-silver, etc., and recently in the manufacture of steel to increase its hardness and strength, also for nickel-plating. Cubical expansion from 32° to 212° F., 0.0038. Specific heat .109.

Platinum, Pt.—At. wt. 195. A whitish steel-gray metal, malleable, very ductile, and as unalterable by ordinary agencies as gold. When fused and refined it is as soft as copper. Sp. gr. 21.15. It is fusible only by the oxyhydrogen blowpipe or in strong electric currents. When combined with iridium it forms an alloy of great hardness, which has been used for gun-vents and for standard weights and measures. The most important uses of platinum in the arts are for vessels for chemical laboratories and manufactories, and for the connecting wires in incandescent electric lamps. Cubical expansion from 32° to 212° F., 0.0027, less than that of any other metal ex-

cept the rare metals, and almost the same as glass.

Silver (Argentum), Ag.—At. wt. 107.7. Sp. gr. 10.1 to 11.1, according to condition and purity. It is the whitest of the metals, very malleable and ductile, and in hardness intermediate between gold and copper. Melts at about 1750° F. Specific heat .056. Cubical expansion from 32° to 213° F. As a conductor of electricity it is equal to copper. As a conductor

of heat it is superior to all other metals.

Tin (Stannum) Sn.—At. wt. 118. Sp. gr. 7.298. White, lustrous, soft, maileable, of little strength, tenacity about 3500 lbs. per square inch. Fuses at 442° F. Not sensibly volatile when melted at ordinary heats. Heat conat 442° F. Not sensibly volatile when melted at ordinary heats. Heat conductivity 14.5, electric conductivity 12.4; silver being 100 in each case. Expansion of volume by heat 0069 from 82° to 212° F. Specific heat 055. Its chief uses are for coating of sheet-iron (called tin plate) and for making alloys with copper and other metals.

Zinc, Zn.-At. wt. 65. Sp. gr. 7.14. Melts at 780° F. Volatilizes and burns in the air when melted, with bluish white fumes of zinc oxide. It is ductile and malleable, but to a much less extent than copper, and its tenacity about 5000 to 6000 lbs. per square inch, is about one tenth that of wrought iron. It is practically non-corrosive in the atmosphere, a thin film of carbonate of sine former. bonate of zinc forming upon it. Cubical expansion between 32° and 212° F.

0.0068. Specific heat .096. Electric conductivity 29, heat conductivity 36, silver being 100. Its principal uses are for coating iron surfaces, called "galvanizing," and for making brass and other alloys.

Table Showing the Order of

Malleability.	Ductility.	Tenacity.	Infusibility.
Gold	Platinum	Iron	Platinum
Silver	Silver	Copper	Iron
Aluminum	Iron	Aluminum	Copper
Copper	Copper	Platinum	Gold
Tin	Gold	Silver	Silver
Lead	Aluminum	Zinc	Alum inum
Zinc	Zinc	Gold	Zinc
Platinum	Tin	Tin	Lead
Iron	Lead	Lead	Tin

WEIGHT OF RODS, BARS, PLATES, TUBES, AND SPHERES OF DIFFERENT MATERIALS.

Notation: b = breadth, t = thickness, s = side of square, d = external diameter, $d_1 = \text{internal diameter}$, all in inches.

Hameter, $a_1 =$ internal diameter, all in inches. Sectional areas: of square bars = s_1^2 ; of flat bars = bt; of round rods = .7854 d^2 ; of tubes = .7854 $(d^2 - d_1^2) = 3.1416(dt - t^2)$. Volume of 1 foot in length: of square bars = $12s_1^2$; of flat bars = 12bt; of round bars = $9.4286d^2$; of tubes = $9.4286d^2 - d_1^2 = 37.699(dt - t^2)$, in cu. in. Weight per foot length = volume × weight per cubic inch of the material. Weight of a sphere = diam. $^3 \times .5236 \times$ weight per cubic inch.

Material.	Specific Gravity.	Weight per cubic foot, ibs.	Weight of Plates I inch thick per per sq. ft., lbs.	Weight of Square Bars per foot length, ibs.	Weight of Flat Bars per foot length, ibs.	Weight per cubic inch, 15e Relative Weights.	Weight of Round Rod per foot length, lbs.	Weight of Syderes or Balls, lbs.
Cast iron Wrought Iron. Steel Copper & Bronze \{	7.854 8.855 8.393 11.88 2.67	480. 489.6 552. 523.2 709.6 166.5 163.4	46. 43.6 59.1 13.9 13.6	81/682 3.482 3.88882 3.68382 4.9382 1.1682 1.1388	3.4bt 8.833bt	.2779 1. .2883 1.0 .3195 1.1 .3029 1.0 .4106 1.4	2 2.670d ² 5 3.011d ² 9 2.854d ² 8 3.870d ² 17 0.908d ² 1 0.891d ²	.1455d* .1484d* .1678d* .1586d* .2150d* .0504d*

Weight per cylindrical in., 1 in. long, = coefficient of d^2 in ninth col. +12. **For tubes** use the coefficient of d^2 in ninth column, as for rods, and multiply it into $(d^2-d_1^2)$; or multiply it by $4(d-\ell^2)$. **For hollow spheres** use the coefficient of d^3 in the last column and

multiply it into $(d^3-d_1^3)$.

For hexagons multiply the weight of square bars by 0.866 (short diam. of hexagon = side of square). For octagons multiply by 0.8284.

MEASURES AND WEIGHTS OF VARIOUS MATERIALS (APPROXIMATE).

Erickwork.-Brickwork is estimated by the thousand, and for various thicknesses of wall runs as follows:

814-	in.	wall,	or	1 bi	ick	in	thickness.	14	bricks	per	superficial:	faat.
1292	••	••	4.	116	**	44	16	21	**			
17	44	66	66	2′~	"	"	46	28	46	44	44	~4
9114				214			44	25	44	46	66	44

An ordinary brick measures about $814 \times 4 \times 2$ inches, which is equal to 66 cubic inches, or 26.2 bricks to a cubic foot. The average weight is 414 lbs.

Fuel.—A bushel of bituminous coal weighs 76 pounds and contains 2888 cubic inches = 1.554 cubic feet. 29.47 bushels = 1 gross ton.

A bushel of coke weighs 40 lbs. (25 to 42 lbs.).

One acre of bituminous coal contains 1600 tons of 2240 lbs, per foot of thickness of coal worked. 15 to 25 per cent must be deducted for waste in

min			•	
41 to	45 cubi	c feet	bituminous coal when broken down	= 1 ton, 2240 lbs.
34 to	41 "	46	anthracite, prepared for market	= 1 ton. 2240 lbs.
128	66	46	of charcoal	= 1 ton, 2240 lbs.
70.9	44	44	" coke	= 1 ton, \$240 lbs.
1 cu	bic foot	of ant	hracite coal (see also page 625)	= 55 to 66 lbs.
1 .			minous "	
i •	(Cumbe	rland coal	
i .		Canna	coal	= 50.8 lbs.
i.		charco	al (hardwood)	= 18.5 lbs.
î '	`	CIIII, CC	(pine)	= 18 lbs.

A bushel of charcoal.—In 1881 the American Charcoal-Iron Workers' Association adopted for use in its official publications for the standard bushel of charcoal 2748 cubic inches, or 20 pounds. A ton of charcoal is to be taken at 2000 pounds. This figure of 20 pounds to the bushel was taken as a fair average of different bushels used throughout the country, and it has since been established by law in some States.

vres, Earths, etc.
13 cubic feet of ordinary gold or silver ore, in mine = 1 ton = 2000 lbs.
20 " " broken quartz = 1 ton = 2000 lbs,
18 feet of gravel in bank = 1 ton.
27 cubic feet of gravel when dry $= 1$ ton.
25 " " sand
18 " " earth in bank
27 " " " when dry
17 " " clay = 1 ton.
Cement.—English Portland, sp. gr. 1.25 to 1.51, per bbl 400 to 430 lbs. Rosendale, U. S., a struck bushel 62 to 70 lbs.
Lime. —A struck bushel
Grain.—A struck bushel of wheat = 60 lbs.; of corn = 56 lbs.; of oats =
80 lbs.

Salt.—A struck bushel of salt, coarse, Syracuse, N. Y. = 56 lbs.; Turk's Island = 76 to 80 lbs.

Weight of Earth Filling.

(From Howe's "Retaining Walls.")

	AV	erage weight in
	, lbe	per cubic foot.
Earth, common loan	, loose	. 72 to 80
	shaken	. 82 to 92
44 44 44	remmed moderately	00 to 100
Gravel	······································	. 90 to 106
Sand		. 90 to 106
Soft flowing mud	•••••••••	. 104 to 120
Sand, perfectly wet.	**********	. 118 to 129

COMMERCIAL SIZES OF IRON BARS.

Wlate.

Width.	Thickness.	Width.	Thickness.	Width.	Thickness
11/6 11/6 11/6 11/6 11/6 11/6 11/6	16 to 56 16 to 34 16 to 15/16 16 to 1 16 to 1	17/6 2 21/4 23/6 21/4 25/6 25/6 25/4 81/4	14 to 14 14 to 194 14 to 194 14 to 194 15 to 194 14 to 196 14 to 196 14 to 2	4 41/4 5 51/4 6 61/4 71/4	14 to 2 14 to 2 14 to 2 14 to 2 14 to 2 14 to 2 14 to 2

Evands: 14 to 134 inches, advancing by 16ths, and 134 to 5 inches by 8ths. Squares: 5/16 to 11/4 inches, advancing by 16ths, and 11/4 to 8 inches by

8th

Half rounds: 7/16, 14, 56, 11/16, 34, 1, 114, 114, 114, 134, 3 inches.

Hexagons: 34 to 114 inches, advancing by 8ths.

Ovals: 14 × 14, 56 × 5/16, 54 × 36, 56 × 7/16 inch.

Half ovals: 14 × 14, 56 × 5/82, 34 × 8/16, 36 × 7/82, 114 × 14, 134 × 56, 13% × % inch.

Round-edge flats: 1½ × ½, 1¾ × 56, 1% × 56 inch.

Bands: ½ to 1½ inches, advancing by 8ths, 7 to 16 B. W. gauge.
1½ to 5 inches, advancing by 4ths, 7 to 16 gauge up to 3 inches, 4 to 14 gauge, 314 to 5 inches.

WEIGHTS OF SQUARE AND ROUND BARS OF WROUGHT IRON IN POUNDS PER LINEAL FOOT.

Iron weighing 480 lbs. per cubic foot. For steel add 2 per cent.

Thickness or Diameter in Inches.	Weight of Square Bar One Foot Long.	1 5 1	Thickness or Diameter in Inches.	Weight of Square Bar One Foot Long.	5	Thickness or Diameter in Inches.	Veight of Square Bar One Foot Long.	5
hickness of Diameter in Inches.	_맺 麻엉	Veight of Round Bar One Foot Long.	hickness Diameter in Inches.	が扱い	Feight of Round Bar One Foot Long.	hickness Diameter in Inches.	Veight of Square Book One Foot Long.	of Bar of
hickness Diameter In Inches	္တစ္	Weight of Round B One Foot Long.	hickness Diameter in Inches	Weight of Square B One Foot Long.		hickness Diameter in Inches.	Weight of Square B One Fool Long.	
8 8 8	2 3 " S	E 24 %	888	26 4 80	H 2 H 80	888	12 F. W. 95	4 5 F 7
중교그	\$0.25 E	30 S S		765 ± 5 ±	56 S S S	[종료교	76 5 5 5	750 S €
프즈르	Weight Squary One F Long.	Veight Bound One F Long.	255 S	Veight Squar One F Long.	Weight Bound One Fo Long.	222	Weight Square One F Long.	Weight Round One Fo
H	P	S	E	*	*	H	×	5
0	}	1 1	11/16 34 18/16 15/16	24.08	18.91	3/6 7/16	96.30	75.64
1/16	.013 .052 .117 .208 .326 .469 .638 .833 1.055	.010	8/4	25.21	19.80	7/16	98.55	77.40
1/4	.053	.041	18/16	96.87	20.71	1,6	100.8	79.19
3/16	.117	.041	76	96.87 27.55	21.64	9/16	100.8 103.1	81.00
5/16 5/16 7/16	.208	1 164	15/16	28.76	22.59	56 11/16	105.5 107.8	82.83
5716	.326	.256	8	80.00	23.56	11/16	107.8	84.69
86	.469	.256 .368 .501	1/16	30.00 81.26 32.55	24.55	13/16 76 15/16	110.2 112.6	86.56
7/16	.638	.501	16	82.55	25.57	13/16	112.6	88.45
16	.893	654	3/16	1 23.87	26.60	76	115.1 117.5	90.36
9716	1.055	.828	14	35.21	27.65	15/16	117.5	92.29
56	1.302	1.023	5/16	35.21 86.58	27.65 28.73	6	120.0	94.25
9/16 11/16 13/16	1 1.576	.828 1.023 1.237	1/16 1/6 3/16 1/4 5/16 1/6 7/16 1/2 9/16	37.97	29.82		125.1	98.22
2/	1.875	1 1 472 1	7/16	39.39 40.83	80.94	12	130.2	102.3
13/16	2.201	1.728	12	40.88	82.07	l á2	135.5	106,4
74	2.201 2.552	2.004	9/16	42.30	33.23	12	140.8	110.6
15/16	2.930	1.728 2.004 2.801	1 66	43.80	84.40	l 62	146.3	114.9
1 10, 10	8.333	2.618	11/16 34 13/16	45.83	85.60	1914 3914 3914	151 0	119.3
17/16	3.763	2.955	1 22	46.88	36.82	1 62	157.6 163.8 169.2	123.7
1/16 1/6 3/16	4.219	3.313	18/16	48.45	88.05	7 /8	163.8	128.3
3/16	4.701	3.692	1076	50.05	89.81		169.2	182.9
14	5.208	4.091	15/16	51.68	40.59	12	175.2	187.6
5/16	5.208 5.742	4.510	4	51.68 53.38	40.59 41.89	62	181.8	142.4
36	A 900	4.950	* 1/18	55.01	43.21	19143814381418	175.2 181.8 187.5	147.3
7/16	6.888 7.500 8.138 8.802	5.410	1/16 1/6 3/16	56.72	44.55	62	193.8	152.2
14	7.500	5.890	3/16	58.45	45.91	1 62	200.2	157.2
9/16	8.188	6.392	1 32	60.21 61.99	47.29	12	206.7	162.4
56	8.802	6.913	5/18	61.99	48.69	8	213.8	167.6
56 11/16	9.492	7.455	84	63.80	50.11	14	226.9	178.2
34	10.21	7.455 8.018	7/16	63.80 65.64	51.55	12	240.8	178.2 189.2
13/16	10.95 11.72	8.601 9.204	5/16 5/16 3/6 7/16 1/6 9/16 5/6	67.50	58.01	14 14 14 14 14	255.2	200.4
7.6	11.72	9.204	9/16	69.39	54.50	9 13	270.0	212.1
15/16	12.51	9.828	1 86	71.80	56.00		285.2	224.0
2	18.98	10.47	11/18	78.24	57.52	14	300.8	236.3
1/16	1 14 18	11.14	82	75.21	59.07	82	316.9	248.9
12.0	15.05	11 00	13/16	77.20	60.63	10	333.8	261.8
9716	15.95	12.58	86	77.20 79.22	62.22	14	350.2	275.1
14.0	16.88	18.25	15/16	81.26	63.82	12	367.5	288.6
5716	15.05 15.95 16.88 17.88	12.58 13.25 14.00 14.77	5	81.26 83.83	63.82 65.45	14	385.2	302.5
	18.80	14.77	1/16	85.49	67.10	111	403.3	316.8
7716	19.80	15.55	122	87.55	68.76	14	421.9	331.3
3/16 3/16 5/16 5/16	20.88	16.36	1/16 1/6 3/16	89.70	70.45	12	440.8	346.2
9716 %	31.89	17.19	1 32	91.88	72.16	14	460.2	361.4
2/10	22.97	18.04	5/16	94.08	72.16 73.89	12	480.	377
78	~~~	10.04	1 37.0	1 53.00	1 .5.65	1	1	

WEIGHTS OF FLAT BOLLED IRON IN POUNDS PER LINEAL FOOT. WIdths from 1 In. to 12 In.

Iron weighing 480 lbs. per cubic foot. For steel add 2 per cent.

	4%".	98	88	2.92	8. 8.	8.8	25.5	88.9	2.85	8.91	8.8	0.80	 88	2.86	8.8	28.4	88.98	8.88	18.2	8.8	10.70	8	Z.	8. 29.	88 13	2.2	89 29	8. 8.	7.7	8.3 2.3	89	89.08	29.15
	4,8″.		92	=	æ	g	22	92	8	4	œ	=	28	<u> </u>	<u>∞</u>	×	8	×	88	=	ĸ	2	8	8	8	I	98	=	ß	9	2	8.8	8
	4%".	88.																														27.45	
	<u>*,</u>	88	1.67	8 2 2	85 85	4.17	8.8	88	6.67	2.2	86 88	9.17	10.00	10.83	11.67	12.50	13.33	14.17	15.00	15.83	16.6	2.20	18.83	19.17	8.8	88.	21.67	3 3	88 88	24.12	8	86.8 86.8	20.67
	8%".	₽.	1.56	8. 8.	8.18	8.91	4.69	5.47	6	8	7.81	8.59	88.6	10.16	20.02	11.72	12.50	18.28	14.08	14.84	15.68	18.41	17.19	17.97	18.75	19.53	20.31	8 등	88. 88.	83 83	8 4.	81 S	8.6
	37%,	82.	1.46	2.19	88	3.65	88.	5.10	88	6.56	2.8	8.08	8.75	9.48	10.21	10.92	11.67	12.40	18.18	18.85	14.58	15.31	16.04	16.77	17.50	18.88	18.96	19.69	8 3.	21.15	윤 88:	88	23. 25.
	814".	.677	38.	8. 8	2.7	8.80	90.	4.74	5.43	8	8.77	7.45	8.18	8.80	9.48	10.16	10.88	11.51	12.19	12.86	13.54	2.23	14.90	15.57	16.85	16.98	17.60	18.88	18.96	19.62	8.8	8.8	21.67
	%	88	8	.88	25.50	8.18	8.75	8	200	88	6.25	88.	2.50	8.13	8.73	88.6	10.00	10.63	11.85	11.88	12.50	18.18	18.75	14.38	15.00	15.63	16.25	16.88	17.50	18.18	18.73	888	30.08
Widths.	23/4".	.573	1.15	22	20.20	88	8.44	4.01	4.58	5.16	20	8.8	88.8	7.45	8.08	8.59	9.17	9.74	10.31	10.89	11.46	12.08	12.60	18.18	18.75	14.88	14.90	15.47	16.04	16.61	17.19	17.78	18.83
	27%,,	15.5	2.	1.56	80.3	2.60	8.13	65	4.17	4.69	2.51	5.78	6.25	6.77	2.20	7.81	88	88	88.6	8.8	10.42	10.94	11.46	11.88	12.50	18.08	18.54	14.06	14.58	15.10	8	16.15	16.67
	% a	469	88	1.41	88:	8	8	88	8.75	83	4.69	6.16	5.63	60.9	6.58	88.	2.2	2.82	8.44	8.91	88.6	20.00	10.81	20.78	11.85	11.73	12.19	12.66	18.18	18.59	9.7	25.53	15.00
	<u>؞ٛ</u>	.417	88	 8	1.67	508	2.50	88	88.38	20.30	4.17	4.58	8	6.42	88.9	8.25	6.67	2.08	2.50	2.82	8.8	8.78	9.17	9.28	10.00	10.42	88.01	11.25	11.67	12.08	25.50	888	18.88
	1%".	8 8.	8	8	1.46	88	2.19	20	8	88	8	4.01	88.7	4.74	5.10	5.47	88.	6.50	6.56	8.98	7.29	2.8	8.08	8.8	8.79	9.11	9.48	8.	10.21	10.57	3.5	8:	11.67
	13%".	.813	8	88	1.25	1.56	.88	2.19	23.	2.81	8.18	4.8	8.78	90.4	4.88	4.69	8.9	5.81	5.63	2.2	6.35 35	9.50	æ.	7.19	3.2	7.81	8.18	4.	œ 19	8.	88	88	10.0E
	114".	88.	.521	. Z	20.1	8.	1.56	88	80.2	20.	8.8	8. 8.	8.13	8.89	3.85	8.91	4.17	4.43	4.69	8.8	5.21	5.47	2	8.8	8.8	6.51	6.73	2.08	2.8 2.8	29.	<u>چ</u>	8.3	8.83
	1″.	808	.417	8	88	8	33	1.46	1.67	88.	80.2	83.	25.22	2.71	88	8.18	88.88	25.52	8.75	8.98	4.17	%	85.58	5	8.9	2.2	6.43	6.68	88.	3 .0	8	\$	0.67
Thick-	Inches.	1-16	×	8-16	74	91-0	*	2-16	7	9-16	Z	11-16	*	18-16	×	16-16	_	1 1-16	- x	1 8-16	77	1 5-16	- %	1 7-16	- %	1 2-16	- %	1 11-16	- %	1 18-16	%	1 12	~

Thick							Widths.								
Inobes.	53K".	.,842	5%	6″.	634".	%	69%".	۳.	7%	œ,	84%".	<i>چ</i> '.	10″.	11".	12″.
	 		114844668445112141212122222222222222222222222222		1480000000111147555588888888888 88242811465888888842888428				116461612111112828882138483 21688282882811184688388888	11875.0011275.009128888888484828 \$8862866286686686688668	11887-80344515028888888884888 F72125888474154888888888888888888888888888888	8558789558888888874488888 8558789588888888888888888888888888	8.400.514458888888888888888888888888888888888	888746788882888884844388387	%%r-131715347293829483382558 262626262626262626266666
- 13	Ι,	Wolcht of				-		- ;				-			- Indiana

Other sixes. -Weight of other sizes can easily be obtained from the above table by means of combinations or divisions. Thus, for example, 3385 8358 8358 Weight of 12 \times 14 equals weight of 12 \times 1 plus weight of 12 \times 14. Or, twee weight of 12 \times 15, as it is two sa thick.

Weight of \times 114 equals midway weight between 6 \times 174 and 6 \times 2. Weight of 8 \times 14, being twice as wide as 12 \times 14, weights.

WEIGHT OF IRON AND STEEL SHRETS, Weights per Square Foot.

(For weights by Decimal Gauge, see page 32.)

Thickne	ess by Birn	ningham	Gauge.	Thickness by American (Brown and Sharpe's) Gauge.					
No. of Gauge.	Thick- ness in Inches.	Iron.	Steel.	No. of Gauge,	Thick- ness in Inches.	Iron.	Steel.		
0000	.454	18.16	18.52	0000	.46	18.40	18.77		
000	.425	17.00	17.84	000	.4096	16.38	16.71		
00	.38	15.90	15.50	00	.8648	14.59	14.88		
0	.84	13.60	13.87	0	.3249	18.00	18.26		
1	.8	12.00	12.94	1	.2898	11.57	11.80		
2	.284	11.86	11.59	2	.2576	10.80	10.51		
8	.259	10.86	10.57	8	.2294	9.18	9.36		
4	.238	9.52	9.71	4	.2048	8.17	8.84		
5	.22	8.80	8.98	5	.1819	7.28	7.42		
6 7 8 9 10	.203 .18 .165 .148 .134	8.12 7.20 6.60 5.92 5.86	8,28 7,34 6,78 6,04 5,47	6 7 8 9	.1620 .1443 .1285 .1144 .1019	6.48 5.77 5.14 4.58 4.08	6.61 5.89 5.24 4.67 4.16		
11	.19	4.80	4.90	11	.0907	8.68	8.70		
12	.109	4.86	4.45	19	.0808	8.28	3.80		
18	.095	8.80	8.88	18	.0720	2.88	2.94		
14	.083	8.32	8.89	14	.0641	2.56	2.62		
15	.072	2.88	2.94	15	.0571	2.28	2.38		
16	.065	2.60	9.65	16	.0508	9.08	2.07		
17	.058	2.82	2.87	17	.0458	1.81	1.85		
18	.049	1.96	2.00	18	.0408	1.61	1.64		
19	.042	1.68	1.71	19	.0859	1.44	1.46		
20	.085	1.40	1.48	20	.0820	1.28	1.81		
21 22 23 24 25	.032 .028 .025 .022	1.28 1.12 1.00 .88 .80	1.31 1.14 1.02 .898 .816	21 22 28 24 25	.0285 .0258 .0226 .0201 .0179	1.14 1.01 .904 .804 .716	1.16 1.08 .922 .820 .730		
26	.018	.73	.734	26	.0159	.686	.649		
27	.016	.64	.658	27	.0142	.568	.579		
28	.014	.56	.571	28	.0196	.504	.514		
29	.018	.52	.530	29	.0118	.452	.461		
30	.012	.48	.490	30	.0100	.400	.408		
81	.01	.40	.408	81	.0089	.856	.363		
82	.009	.36	.367	88	.0080	.820	.326		
88	.008	.32	.326	83	.0071	.284	.290		
84	.007	.26	.386	84	.0068	.253	.257		
85	.005	.20	.204	85	.0056	.234	.328		

,	iron.	Steel.
Specific gravity	7.7	7.854 489.6
weight per cubic toot	.2778	.2883

As there are many gauges in use differing from each other, and even the thicknesses of a certain specified gauge, as the Birmingham, are not assumed a same by all manufacturers, orders for sheets and wires should always e the weight per square foot, or the thickness in thousandths of an inch.

OF PLATE IRON, PER LINEAL FOOT, IN POUNDS. on 480 lbs. per Cubic Foot, For Steel add 2 per cent.) WEIGHT Based

200.000 to 100 t 2000年 | 1000年 | 1000 11-18 882388388844442832888886668898852881288 887388488868888884888866688978867886 × Inches **33286888888828-644**2623228882-1468888882-158 = -48648**6**4864864868468468468468666466 X Thickness **56448864178646688888675854887780187588** 7-16 **෧෧ඁ෪෫෧෧ඁ෪෫෧෧ඁ෪෫෧෧ඁ**෪෫෧෧ඁ෪෫෧෧ඁ෪෧෪෧෪෧෪෧෪෧෪෧ 34382155888882528811488433754886874843 X 9-Inches.

WEIGHTS OF STEEL BLOOMS.

Soft steel. 1 cubic inch = 0.284 lb. 1 cubic foot = 490.75 lbs.

Sizes.		Lengths,											
		1"	6′′	12"	18"	24"	30"	86"	42"	48"	54"	60"	66"
12" 11	× 4" × 6 × 5 × 4	18.63 18.75 15.62 12.50	82 113 94 75	164 225 188 150	245 338 281 225	327 450 875 300	409 563 469 875	491 675 562 450	578 788 656 525	654 900 750 600	786 1018 848 675	818 1125 937 750	900 1238 1081 825
10	× 7	19.88	120	239	358	477	596	715	835	955	1074	1193	1312
	× 6	17.04	102	204	307	409	511	618	716	818	920	1022	1125
	× 5	14.20	85	170	256	341	426	511	596	682	767	852	937
	× 4	11.36	68	136	205	273	341	409	477	546	614	682	750
	× 3	8.52	51	102	158	204	255	806	358	409	460	511	562
9	× 7	17.89	107	215	322	430	537	644	751	859	966	1078	1181
	× 6	15.34	92	184	276	368	460	552	644	786	828	990	1012
	× 5	12.78	77	153	230	307	383	460	537	614	690	767	844
	× 4	10.22	61	123	184	245	307	368	429	490	552	618	674
8	× 8	18.18	109	218	327	436	545	655	764	878	982	1091	1200
	× 7	15.9	95	191	286	382	477	572	668	763	859	954	1049
	× 6	13.63	82	164	245	327	409	491	578	654	786	818	900
	× 5	11.36	68	186	205	273	841	409	477	546	614	682	750
	× 4	9.09	55	109	164	218	278	327	382	436	491	545	600
7	× 7	13.92	83	167	251	884	418	501	585	668	752	885	919
	× 6	11.93	72	148	215	286	358	430	501	573	644	716	788
	× 5	9.94	60	119	179	238	298	358	417	477	586	596	656
	× 4	7.95	48	96	143	191	239	286	834	882	429	477	525
	× 8	5.96	86	72	107	148	179	214	250	286	322	858	898
61 <u>/6</u>	× 61/2	12.	72	144	216	288	860	482	504	576	648	720	798
	× 4	7.88	44	89	138	177	221	266	810	854	899	443	487
	× 6	10.22	61	123	184	245	307	368	429	490	551	618	674
	× 5	8.52	51	102	158	204	255	807	856	409	460	511	562
	× 4	6.82	41	82	123	164	204	245	286	827	868	469	450
	× 8	5.11	81	61	92	123	158	184	214	245	276	307	837
51 <u>/6</u> 5	× 51/6 × 4 × 5 × 4	8.59 6.25 7.10 5.68	52 37 43 84	108 75 85 68	155 112 128 102	206 150 170 186	258 188 218 170	809 225 256 205	861 262 298 289	412 300 841 278	464 837 883 807	515 875 426 341	567 412 469 875
41/2	× 4½	5.75	35	69	104	138	178	207	242	276	811	845	380
	× 4	5.11	31	61	92	123	158	184	215	246	276	807	388
	× 4	4.54	27	55	83	109	186	164	191	218	246	272	800
	× 3½	8.97	24	48	72	96	119	143	167	181	215	288	262
	× 3	8.40	20	41	61	82	102	122	148	163	184	204	224
81 <u>%</u> 8	× 81⁄8 × 8 × 8	8.48 2.98 2.56	21 18 15	42 36 31	63 54 46	84 72 61	104 89 77	125 107 92	146 125 108	167 143 128	188 161 188	209 179 154	230 197 169

SIZES AND WEIGHTS OF STRUCTURAL SHAPES.

Minimum, Maximum, and Intermediate Weights and
Dimensions of Carnegie Steel I-Beams.

tion	Depth of Beam.	Weight per Foot.	Flange Width.	Web Thick- ness.	Sec- tion Index	of	Weight per Foot.	Flange Width.	Web Thick- ness.
B1	ins. 24	10s. 1095 99 99 88 89 75 76 55 76 55 85 55 55 43 43 55 15 55 55 15 15 15 15 15 15 15 15 15	ins. 7.25 7.19 7.19 7.19 7.10 7.00 6.83 6.25 6.18 6.10 6.10 5.75 5.55 5.50 5.00 4.95 4.86 4.71 4.48 4.48 4.47 4.48 4.37 4.18 4.37 4.18 87	ins, 50.669 0.687 0.505 0.505 0.505 0.505 0.505 0.505 0.505 0.505 0.646 0.466 0.467 0.666 0.467 0.666 0.467 0.666 0.467 0.666 0.467 0.666 0.467 0.666 0.467 0.666 0.467 0.467 0.667 0.467	B19 " " " B28 " " " " " " " " " " " " " " " " " " "	ins. 6	lbs. 17.25 14.75 12.25 14.75 12.25 9.75 10.5 7.5 6.5 5.5 100 95 85 80 95 80 95 80 95 80 85 80 85 80 85 80 85 80 85 80 85 80 85 86 86 86 86 86 86 86 86 86 86 86 86 86	ins. 8.88 8.45 8.83 8.15 8.288 2.81 8.262 2.42 8.38 6.62 6.19 6.68 6.48 6.19 6.00 5.61 5.49 5.87	ins. 0.48 0.35 0.23 0.50 0.36 0.21 0.34 0.34 0.34 0.38 0.19 0.36 0.19 0.38 0.81 0.78 0.81 0.66 0.60 0.89 0.81 0.78 0.89 0.89 0.89 0.89 0.89 0.89 0.89 0.8
**	"	17.5 15	3.76 3.66	0.85 0.25	" spe		B2, B4, I beams, t		

Sectional area = weight in lbs. per ft. + 3.4, or \times 0.2941. Weight in lbs. per foot = sectional area \times 3.4.

Maximum and Minimum Weights and Dimensions of Carnegie Steel Deck Beams.

Depth of Beam	Weight per Foot, lbs.		Flange	Width.			Increase of Web and Flange per		
inches.	Min.	Max.	Min.	Max.	Min.	Max.	lb. increase of Weight.		
10 9	27.23 26.00	35,70 30.00	5.25 4.94	5.50 5.07	.38	.63 .57	.029		
7	20.15 18.11	24.48 28.46	5.00 4.87	5.16 5.10	.31 .81	.47 .54	.087 .042 .049		
	of Beam, inches.	for Beam, inches. Min. 10 27.23 9 28.00 8 20.15 7 18.11	Foot, lbs. Beam, inches. Min. Max. 10 27.23 85.70 9 28.00 30.00 8 20.15 24.48 7 18.11 23.46	Foot, ibs. Min. Max. Min. 10 27.23 35.70 5.25 9 28.00 30.00 4.94 8 20.15 24.48 5.00	Foot, lbs. Beaun, inches. Min. Max. Min. Max. Min. Max. Min. Max. 10 27.28 35.70 5.25 5.50 9 28.00 30.00 4.94 5.07 8.20.15 24.48 5.00 5.16 7 18.11 23.46 4.87 5.10	Foot, lbs. Flange Widel Thick	Foot, lbs. Flange With Thickness. Thickness. Min. Max. Min. Min. Max. Min. Max. Min. Min. Min. Max. Min. Min. Min. Min		

Minimum, Maximum, and Intermediate Weights and Dimensions of Carnegie Standard Channels.

50 3.72 0.72 13.75 2.35 45 3.62 0.62 11.25 2.26 40 8.52 0.52 C6 7 19.75 2.51	Section Index.	Depth of Channel. Inches. Weight per Frot. Pounds.	Flange Width. Inches. Web Thick- ness. Inches.	Section Index. Depth of Channel. Inches.	Weight per foot. Pounds. Flange Width. Inches.	Web Thick- ness. Inches.
C3 10 35 3.18 0.82 " " 8 1.98 1.98 " " 8 1.99 1.98 1.98 1.99 1.98 1.99 1.98 1.99 1.98 1.99 1.98 1.99 1.98 1.99 1.98 1.99 1.98 1.98	C2	50 45 45 33 33 30 25 20 25 20 15 20 15 20 15 20 15 20 15 20 15	3.52 0.52 3.43 0.43 3.40 0.40 3.82 0.64 3.17 0.51 3.05 0.89 2.94 0.28 3.18 0.68 2.94 0.68 2.89 0.53 2.74 0.58 2.60 0.24 2.82 0.62 2.85 0.45 2.85 0.45 2.49 0.29	C6 7	18.75 2.35	0.40 0.31 0.22 0.68 0.53 0.42 0.21 0.56 0.44 0.32 0.20 0.44 0.32 0.30 0.49 0.49 0.40 0.40 0.40 0.40 0.40 0.4

Weights and Dimensions of Carnegie Steel Z-Bars.

	. .	Si	ze.	١.	l	, T	Si	ze.	
Section Index.	Thickness of Metal	Flanges.	Web.	Weight. Pounds.	Section Index.	Thickness of Metal	Flanges.	Web.	Weight. Pounds.
Z1 Z2 Z8 Z5 Z6	3/6 7/16 9/16 9/16 11/16 13/4 13/16 5/16 5/16 5/16 14/16 11/16	3 9/16 3 9/16 3 9/16 3 9/16 3 9/16 3 5/16 3 5/16 3 5/16 3 5/16 3 5/16 3 5/16	6 1/16 1/8 6 1/16 6 1/8 6 1/16 6 1/16 5 1/16 5 1/16 5 1/16 5 1/16 5 1/16 5 1/16 5 1/16 5 1/16	15.6 18.3 21.0 22.7 25.4 28.0 29.3 32.0 84.6 11.6 11.9 16.4 17.8 20.2 22.7	Z6 . Z7 Z8 Z9 Z10 Z11 Z12	34 13/16 34 5/16 36 7/16 9/16 11/16 11/16 14/16 5/16 3/6 7/16 9/16	3 5/16 3 3/6 3 1/16 3 3/6 3 3/16 5 1/16 3 1/16 3 1/16 3 1/16 2 11/16 2 11/16 2 11/16 2 11/16 2 11/16	5 1/16 5 3/6 4 1/16 4 3/6 4 1/16 4 3/6 4 1/16 4 3/6 3 1/16 3 1/16 3 1/16 3 1/16	26.0 28.8 8.8 10.8 12.4 18.8 17.9 18.9 20.9 22.9 6.7 8.4 9.7 11.4 12.5 14.3

Pencoyd Steel Angles. EVEN LEGS.

Size in Inches.		Approximate Weight in Pounds per Foot for Various Thicknesses in Inches.													
	1/8 .125	3/16 .1875	14 .25	5/16 .3125		7/16 .4375	1/9	9/16 .5625		11/16 .6875	34 .75	13/16 .8125	7/6 .875	15/16 .9375	
8 × 8 6 × 6 5 × 5 4 × 4 31 5 × 31 6 3 × 3 23 4 × 23 4 21 5 × 21 6 22 × 2 13 4 × 13 4 11 5 × 11 6 11 1 × 11	1.9 1.0 0.8	2.5 2.1 1.8	3.6 3.2 2.8 2.4 2.0	5,5 5.0 4.5 4.0 3.5 2.9	12.3 9.8 8.5 7.2 6.6 5.9 5.4 4.8 4.1	14.8 11.3 9.8 8.3 7.7 6.9	19.7 16.8 12.8 11.1 9.4 8.6		24.4 20.1 15.8 13.7	26.5 22.0	28.8 23.8	31.0 25.6	45.8 33.4 27.4	35.9	1

UNEVEN LEGS.

Size in		Approximate Weight in Pounds per Foot for Various Thicknesses in Inches.													
Inches.	1/4 .125	3/16	14	5/16	3/8 .375	7/16	16	9/16 .5625		11/16 .6875		13/16		15/16 .9375	
8		2.7 2.8 2.1 1.9	4 5 4 5 4 5 4 5 4 5 6 8 2 9 6	8.7 7.7 7.1 6.6 6.1 5.5 5.5 4.5 3.3	12.2 11.6 11.0 11.0 10.3 9.7 9.1	14.3 13.6 12.8 12.8 12.0 11.2 10.5 10.5 9.8 9.1 8.3 7.7 6.9 6.2	17.0 17.0 16.3 15.5 14.6 13.6 12.8 11.9 11.1 10.3 9.4 8.7 7.9		21.0 21.2 20.1 19.0 17.9 16.8 15.7 14.7 14.7	23.0 23.4 22.0 20.8 19.6 18.4 17.2 16.0	24.8 25.6 23.8 22.6 21.3 20.0 18.7 17.4	26.7 27.8 25.6 24.5	27.4	30.5 31.9 29,4	32.5

ANGLE-COVERS.

Size in Inches.	3/16	14	5/16	3/8	7/16	1/2	9/16	5/8
8 × 3 294 × 294 214 × 214 214 × 214 2 × 2	3.0 2.6 2.4	4.8 4.4 4.0 3.5 3.2	5.9 5.5 5.0 4.4 4.0	7.1 6.6 6.0 5.3 4.8	8.2 7.7 7.0	9.8 8.8 8.1	10.4	11.5

SQUARE-ROOT ANGLES.

Size in Inches.	Approximate Weight in Pounds per Foot for Various Thicknesses in Inches.							arious Thicknesses Various Thickness				or	
	1/4 .25	5/16 .3125	86 .375	7/16 .4375	.50	9/16 .5625	5% .625		1∕8 .125	3/16 .1875	.25	5/16 .3125	86 .875
4 × 4 31,4 × 31,4 3 × 3 25,4 × 25,4 21,4 × 21,4 21,4 × 21,4	4.9 4.5 4.1 8.6	5.6 5.1	9.8 8.5 7.2 6.7 6.1 5.4	11.4 9.9 8.3 7.8 7.1	9.4		16.2	2 ×2 134×134 114×114 114×114 1 ×1	0.82		3.3 2.9 2.4 2.04 1.53	4.1 3.6 3.0 2.55	4.9 4.4

Pencoyd Tees.

Section Number.	Size in Inches,	Weight per Foot.	Section Number.	Size in Inches.	Weight per root.			
	EVEN TEES		UNEVEN TEES.					
440T 441T 385T 386T 380T 330T 225T 226T 227T 222T 222T 220T 117T 115T 112T	4 × 4 4 × 4 31,4 × 31,4 31,4 × 31,4 31,4 × 31,4 21,4 × 21,4 21,4 × 21,4 21,4 × 21,4 21,4 × 21,4 21,4 × 11,4 11,4 × 11,4 1 × 1	10.9 18.7 7.0 9.0 11.0 6.5 7.7 5.8 6.6 4.0 8.5 2.4 2.1	48T 44T 48T 88T 88T 80T 88T 88T 38T 38T 38T 28T 28T 28T 25T	4 × 3 4 × 3 4 × 4 814 × 3 814 × 3 8 × 214 8 × 224 8 × 224	9.0 10.2 18.5 7.0 8.5 4.0 5.0 6.0 7.0 8.3 9.5 6.6 7.2 8.3 9.5			
υ	NEVEN TEE	s.	24T 20T 22T	2½ × 9/16 2 × 9/16 2 × 1 1/16 2 × 1 2 × 1	2.2 2.0 2.0			
64T 65T 58T 54T 42T	6×4 6×514 5×314 5×4 4×2	17.4 89.0 17.0 15.3 6.5	21T 22T 17T 18T 15T 12T	2 ×1 2 ×14 134×1 1/16 134×114 114×15/16 114×15/16	2.5 3.0 1.9 3.5 1.4 . 1.2			

Pencoyd Miscellaneous Shapes.

Section Number.	Section.	Size in Inches.	Weight per Foot in Pounds.
217M 210M 260M	Heavy rails. Floor-bars.	6 3 1/16×4×3 1/16×14 to 1/2 21/4×6×21/4×14 to 3/6	50.0 7.1 to 14.8 9.8 to 14.7

SIZES AND WEIGHTS OF ROOFING MATERIALS.

Corrugated Iron. (The Cincinnati Corrugating Co.) SCHEDULE OF WEIGHTS.

U.S. Gauge.	Thickness in decimal parts of an inch. Flat.	ecimal parts 100 sq. ft. of an inch.		Weight per 100 sq. ft. Corrugated and Galvanized.	Weight in oz. per sq. ft. Flat, Galvan- ized.		
No. 28 No. 26 No. 24 No. 22 No. 20	.025 .08125 .0875	621/4 lbs. 75 " 100 " 125 " 150 "	70 lbs. 84 " 111 " 138 " 165 "	86 lbs. 99 '' 127 '' 154 '' 152 ''	1214 oz. 1414 " 1814 " 2214 " 2614 "		
No. 18 No. 16	.05 .0625	200 " 250 "	220 " 275 "	296 '' 291 ''	3412 '' 4212 ''		

The above table is on the basis of sheets rolled according to the U.S. Standard Sheet-metal Gauge of 1893 (see page 31). It is also on the basis of

Standard Sheet-metal (lauge of 1833 (see page 31). It is also on the pass of 21/4 × 56 in corrugations.

To estimate the weight per 100 sq. ft. on the roof when lapped one corrugation at sides and 4 in. at ends, add approximately 12½% to the weights per 100 sq. ft., respectively, given above.

Corrugations 2½ in. wide by ½ or 5½ in. deep are recognized generally as the standard size for both roofing and siding; sheets are manufactured usually in lengths 6, 7, 8, 9, and 10 ft., and have a width of 28½ or 25 in. outside width—ten corrugations,—and will cover 2 ft. when lapped one corrugations is idea. tion at sides.

Ordinary corrugated sheets should have a lap of 1½ or 2 corrugations side-lap for roofing in order to secure water-tight side seams; if the roof is rather steep 1½ corrugations will answer.

Some manufacturers make a special high-edge corrugation on sides of sheets (The Cincinnati Corrugating Co.), and thereby are enabled to secure a water-proof side-lap with one corrugation only, thus saving from 6% to 12% of material to cover a given area.

The usual width of flat sheets used for making the above corrugated material is 28¼ inches.

No. 28 gauge corrugated iron is generally used for applying to wooden buildings; but for applying to iron framework No. 24 gauge or heavier should be adopted.

Few manufacturers are prepared to corrugate heavier than No. 20 gauge, but some have facilities for corrugating as heavy as No. 12 gauge.
Ten feet is the limit in length of corrugated sheets.
Galvanizing sheet iron adds about 2½ oz. to its weight per square foot.

Corrugated Arches.

For corrugated curved sheets for floor and ceiling construction in fireproof buildings, No. 16, 18, or 20 gauge iron is commonly used, and sheets may be curved from 4 to 10 in. rise—the higher the rise the stronger the arch.

By a series of tests it has been demonstrated that corrugated arches give the most satisfactory results with a base length not exceeding 6 ft., and t ft. or even less is preferable where great strength is required. These corrugated arches are usually made with $2\frac{1}{16} \times \frac{1}{16}$ in. corrugations, and in same width of sheet as above mentioned.

Terra-Cotta.

Porous terra-cotta roofing 3" thick weighs 16 lbs, per square foot and 2" thick, 12 lbs. per square foot.

Ceiling made of the same material 2" thick weighs 11 lbs. per square foot.

Tiles.

Flat tiles 6½" × 10½" × 5½" weigh from 1480 to 1850 lbs. per square of roof (100 square feet), the lap being one-half the length of the tile.

Tiles with grooves and fillets weigh from 740 to 295 lbs. per square of roof.

Pan-tiles 14½" × 10½" laid 10" to the weather weigh 850 lbs. per square.

Tin Plate-Tinned Sheet Steel.

The usual sizes for roofing tin are $14'' \times 20''$ and $20'' \times 28''$. Without

The usual sizes for roofing tin are 14" × 20" and 20" × 32". Without allowance for lap or waste, tin roofing weighs from 50 to 62 lbs. per square. The on the roof weighs from 62 to 75 lbs. per square. Roofing plates or terne plates (steel plates coated with an alloy of tin and lead) are made only in IC and IX thicknesses (29 and 27 Birmingham gauge). "Coke" and "charcoal" tin plates, old names used when from made with coke and charcoal was used for the tinned plate, are still used in the trade, although steel plates have been substituted for iron; a coke plate now commonly meaning one made of Bessemer steel, and a charcoal plate one of open-hearth steel. The thickness of the tin coating on the plates varies with different "brands."

For valuable information on Tin Roofing, see circulars of Merchant & Co.,

Philadelphia.

Philadelphia. The thickness and weight of tin plates were formerly designated in the trade, both in the United States and England, by letters, such as I.C., D.C., I.X., D.X., etc. A new system was introduced in the United States in 1898, known as the "American base-box system." The base-box is a package containing 32,000 square inches of plate. The actual boxes used in the trade contain 60, 120, or 240 sheets, according to the size. The number of square inches in any given box divided by 32,000 is known as the "box ratio." This ratio multiplied by the weight or price of the base-box gives the weight or price of the given box. Thus the ratio of a box of 120 sheets 14×20 in. is 33,600 + 32,000 = 1.05, and the price at \$3.00 base is \$3.00 $\times 1.05 = 3.15 . The following tables are furnished by the American Tin Plate Co., Chicago, Ill.

Comparison of Gauges and Weights of Tin Plates. (Based on II S. Standard Sheet-metal Gauge.)

(Based on U.S. Si	angara Si	ieet-metai Gauge	;.)	
AMERICAN BASE-BOX.	- 1	ENGLISH B		•
(32,000 sq. in.)		(31,360 sc	₽·10.Z	
Weight. Gau	ge. Ga	luge.	• Weigi	1t.
55 lbs No. 3	8.00 No.	. 88.00	54.44 lbs	
	8.72	87.00	57.84 "	
00 00 00	0.04	86.00	01.24	
70	1.92	85.00	00.00	
75 "	4.20 '	84.00	74.85 "	
	3.48 "	88.24	80.00 **	
	2.76	82.50	85.00 **	
		00.00		
W	6.04	81.77	80.00	
20	1.32 "	81.04	30.00	
100 " " 80	0.80 "	80.65	100.00 "	I.C.L.
	0.08	30.06	108.00 "	I.C.
	8.61 "	28.74	126.00 "	I.X.L.
		NO AA		
120	1.92	28.00	100.00	I.X.
100	0.48	26.46	197.00	I. 2X.
180 " " 2	5.52 "	25.46	178.00 "	I. 8X.
	4.80 "	24.68	199.00 "	I. 4X.
	4.08 "	28.91	220.00 "	I. 5X.
240 2	o.og	23.14	MAT.00	I. 6X.
2000	6.04		262.00 ''	I. 7X.
280 "	1.92 "	21.60	288.00 "	I. 8X.
			190 00 44	D.O.
140	1.93	27.86	1.19.00	D.C.
100	0.04	25.38	100.00	D.X.
	4.08 '	24.24	211.00 "	D. 2X.
240 " " 2	3.36 4	28.12	212.00 "	D. 3X.
	1.92 "	22.00	273.00 "	D. 4X.

American Packages Tin Plate.

Inches Wide.		Length.	Sheets Inches per Box Wide.			Length.	Sheets per Box	
17 " 2 26 " 3 9 " 1	25% 10 108∡	Square. Square. Square. All lengths.	60 240	13 1 3 14	" to	1334 1334 148	1714 and longer. To 16 in, long, incl. 1614 and longer. To 15 in, long, incl.	120 240
11 " 1 11 " 1 12 " 1	194 194 294	To 18 in. long, incl. 1814 and longer. To 17 in. long, incl.	240 190 240	15	"	1494 2594 30	151/4 and longer. All lengths. All lengths.	190 190 60

Small sizes of light base weights will be packed in double boxes.

Slate.
Number and superficial area of slate required for one square of roof.
(1 square = 100 square feet.)

Dimensions in Inches.	Number per Square.	Superficial Area in Sq. Ft.	Dim ensions in Inches.	Number per Square.	Superficial Area in Sq. Ft.
6×12	588	267	12×18	160	240
7 x 12	457	1	10×20	169	235
8 × 12	400		11×20	154	
9 x 12	855		12×20	141	!
7×14	374	254	14 × 20	121	1
8×14	827	l	16×20	137	!
9 x 14	291		12 × 22	126	281
10×14	261		14 × 22	108	
8 x 16	277	246	12 x 24	114	228
9×16	246	1	14×24	98	
10 × 16	221		16×24	86	
9×18	218	240	14×26	89	225
10 × 18	192		16×26	78	

As slate is usually laid, the number of square feet of roof covered by one slate can be obtained from the following formula:

 $\frac{\text{width} \times (\text{length} - 3 \text{ inches})}{288} = \text{the number of square feet of roof covered.}$

Weight of slate of various lengths and thicknesses required for one square of roof :

Length	Weight in Pounds per Square for the Thickness.										
in Inches.	₩"	3–16"	¼ "	36"	16"	56''	34"	1"			
12 14 16 18 20 22 24 26	483 460 445 434 425 418 412 407	724 688 667 650 637 626 617 610	967 920 890 869 851 836 825 815	1450 1379 1836 1303 1276 1254 1238 1222	1936 1842 1784 1740 1704 1675 1653 1631	2419 2801 2229 2174 2129 2098 2066 2089	2902 2760 2670 2607 2553 2508 2478 2445	8872 3683 3567 8480 3408 3350 3306 3263			

The weights given above are based on the number of slate required for one square of roof, taking the weight of a cubic foot of slate at 175 pounds.

Pine Shingles.

Number and weight of pine shingles required to cover one square of roof:

Number of Inches Exposed to Weather.	Number of Shingles per Square of Roof.	Weight in Pounds of Shingle on One-square of Roofs.	Remarks.
4 41/4 5 51/4	900 800 790 655 600	216 192 178 157 144	The number of shingles per square is for common gable-roofs. For hiproofs add five per cent. to these figures. The weights per square are based on the number per square.

Skylight Glass.

The weights of various sizes and thicknesses of fluted or rough plate-glass required for one square of roof.

Dimensions in	Thickness in	Area	Weight in Lbs. per
Inches.	Inches.	in Square Feet.	Square of Roof.
12 × 48	8-16	3.997	250
15 × 60	14	6.246	350
20 × 100	36	13.890	500
94 × 156	16	101.768	700

In the above table no allowance is made for lap.

If ordinary window-glass is used, single thick glass (about 1-16") will weigh about 82 lbs. per square, and double thick glass (about 1-6") will weigh about 164 lbs. per square, no allowance being made for lap. A box of ordinary window-glass contains as nearly 50 square feet as the size of the panes will admit of. Panes of any size are made to order by the manufacturers, but a great variety of sizes are usually kept in stock, ranging from 6×8 inches to 86×60 inches.

APPROXIMATE WEIGHTS OF VARIOUS ROOF-COVERINGS.

For preliminary estimates the weights of various roof coverings may be taken as tabulated below (a square of roof = 10 ft. square = 100 sq. ft.): Weight in Li

Name.	Square of R
Cast-iron plates (%" thick)	1500
Copper. Felt and asphalt.	100
Feit and gravel	800-1000
Iron, corrugated	100- 875 100- 850
Lath and plaster	900-1000
Sheathing, pine, 1" thick yellow, northern southern	800
Spruce, 1" thick	200
Sheathing, chestnut or maple, 1" thick	400
ash, hickory, or oak, 1" thick Sheet iron (1-16" thick)	500
" " " and laths	500
Shingles, pine	900
Skylights (glass 8-16" to 16" thick)	250- 700
Sheet lead	500-800
Thatch	
Tiles, flat	1500-2000
" (grooves and fillets)	700-1000 1000
" pan" " with mortar	2000-3000
Zinc	. 100- 200

Approximate Loads per Square Foot for Roofs of Spans under 75 Feet, Including Weight of Truss.

(Carnegie Steel Co.)

Roof covered with corrugated sheets, unboarded	8	lbs.
Roof covered with corrugated sheets, on boards	11	"
Roof covered with slate, on laths	18	- 66
Same, on boards, 11/4 in, thick	16	66
Roof covered with shingles, on laths	10	44
Add to above if plastered below rafters	10	••
Characteristic matter and authorized for the state of the	40	- 44

d when separate calculations are not made.

WEIGHT OF CAST-IRON PIPES OR COLUMNS.

WEIGHT OF CAST-IRON PIPES OR COLUMNS. In Lbs. per Lineal Foot.

Cast iron = 450 lbs. per cubic foot.

Bore.	Thick. of Metal.	Weight per Foot.	Bore.	Thick. of Metal.	Weight per Foot.	Bore.	Thick. of Metal.	Wei per I
Ins.	Ins.	Lbs.	Ins.	Ins.	Lbs.	Ins.	Ins.	Lb
8	86	12.4	10	32	79.2	22	24	167
•	12	17.2	103/6	₹	54.0		76	196
- 1	6 2	22.2		5 6	68.2	23	34	174
316	62	14.8		24	82.8		_3%6	205
078	12	19.6	11	24	56.5		1 ₀ ,	235
- 1	4Z	25.8		29	71.8	24	1/8	182
4	\$2	16.1		24	86.5 58.9		1/8	213 245
•	12	22.1	111/6	29	74.4	25	1 .	189
- 1	6Z	28.4		29	90.2	20	% %	222
436	\$2	17.9	12	73	61.3		1/8	255
278	12	24.5	12	1 29	77.5	26		197
- 1	62	81.5		78	98.9	20	24 26	230
5	\$2	19.8	121/6	1 73	68.8		1 1 78	265
٠	12	27.0	1272	1 23	80.5	27		204
1	5 2	84.4 21.6		329	97.6	~'	1/8	239
51/2	9 2	~~~	18	1 32	66.3		178	274
-/2	12	~~~	10	62	83.6	28	3/	211
- 1	9 7	23.5		1 52	101.2	~~	1	248
6	36 I	31.8	14	12	71.2		1′°	284
1	34 I	40.7	••	62	89.7	29	3/4	219
	56	25.8		§4	108.6		34	256
61/6	36	34.4	15	52	95.9		1 1	294
/~	14 I	48.7		34	116.0	30	₹ %	265
- 1	26	27.1		36	186.4		1	304
7	7 4	36.8	16	1 %	102.0		13/6	343
- 1	24	46.8		34	123.3	81	116	273
	26	29.0		1 2∕6	145.0		1	314
736	76	39.3	17	l ?%i	108.2		11/6	354
- 1	24	49.9		24	130.7	82	.76	282
	26	30.8		26	153.6		1	324
8	76	41.7	18	Rosenses es	114.3		11/6 2/8	365
- 1	29	52.9		24	188.1	83	_ 3%	291
~.		44.2		1 29	162.1		1	333
81/6		56.0	19	29	120.4		11/6 28	376
- 1		68.1		23	145.4	34	1,78	299
•		46.6		29	170.7		1 11/	343
¥		59.1	20	79	126.6 152.8	85	116	388 308
- 1	39	71.8		1 72	179.3	30	1/8	853
01/	73	49.1	21	l 29	179.5		112	899
91/6	22 \	62.1	21	39	160.1	36	11/6	316
- 1	33 9 \	75.5		1 72	187.9	30	1/8	363
10	33	51.5	22		138.8		1116	410
10 /	23 \	65.2	2.0	78	1 100.0		178	410

The weight of the two flanges may be reckoned = weight of one foot,

WEIGHTS OF CAST-IBON PIPE TO LAY 12 PEET LENGTH.

Weights are Gross Weights, including Hub.

(Calculated by F. H. Lewis.)

Thic	kness.	Inside Diameter,								
Inches.	Equiv. Decimals.	4"	6"	8"	10"	12"	14"	16"	18"	20"
86 13-82	.375 .40625	209 228	304 381	400 485						
7-16	.4375	247	858	470	581	692	804	1	1	ı
15-32	.4687	266	386	505	624	744	863	1	1	l
17-32	.5	286	414	541	668	795	922	1050	1177	
	.53125	306	443	577	712	846	983	1118	1253	
9-16	.5625	897	470	613	756	899	1043	1186	1829	l
19-32	.59875		498	649	801	951	1103 1163	1254 1322	1405 1481	1040
56 11-16	.625 .687 5	••••		686	845 935	1008	1285	1460	1635	1640 1810
34	.75	••••			1026	1216	1408	1598	1789	1980
13-16	.8125				1000	1324	1531	1738	1945	2152
36	.875					1432	1656	1879	2101	2324
15-16	.9375						1788	2021	2259	2498
1	1.	l					1909	2168	2418	2672
11/	1.125								2738	3024
178						4	١.	1	8062	3330
11/6 11/4	1.25		• • • • • •				ļ •• • • •	,,,		
114 114 186								ļ	3389	3739
15%	1.25	l::::::	<u> </u>		Insid	e Diar	neter.	1		
15%	1.25 1.375	22"	24"	27"	Insid	e Diar	meter. 86"	42"		
Thic	1.25 1.375 kness. Equiv. Decimals.	1799			i		1	42"	3389	3789
Thic Inches.	1.25 1.375 kness. Equiv. Decimals. .625 .6875	1799 1985	2160	2422	30"	33′′	86"	42"	3389	3789
Thic Inches.	1.25 1.375 kness. Equiv. Decimals. .625 .6875 .75	1799 1985 2171	2160 2362	2422 2648	2984	33"	8507		3389	3789
Thic Inches. 11-16 34 13-16	1.25 1.375 kness. Equiv. Decimals. .625 .6875 .75 .8125	1799 1985 2171 2359	2160 2362 2565	2422 2648 2875	30" 2934 3186	3221 3496	86" 8507 8806	4496	3389	3789
Thic Inches. 11-16 34 13-16	1.25 1.375 kness. Equiv. Decimals. .625 .6873 .75 .8125 .878	1799 1985 2171 2359 2547	2160 2362 2565 2769	2422 2648 2875 3103	30" 2934 3186 8437	3221 3496 3771	8507 8506 4105	4496 4773	48"	3789
Thic Inches. 54 11-16 34 13-16 76 15-16	1.25 1.375 kness. Equiv. Decimals. .625 .6875 .75 .8125 .875 .9875	1799 1985 2171 2359 2547 2737	2160 2362 2565 2769 2975	2422 2648 2875 3103 3332	2934 3186 8137 8690	3221 3496 3771 4048	8507 8506 4105 4406	4426 4773 5122	3389 48" 5442 5839	3789
Thic Inches. 54 11-16 34 13-16 15-16	1.25 1.375 kness. Equiv. Decimals. .625 .6875 .75 .8125 .875 .9375	1799 1985 2171 2359 2547 2737 2927	2160 2362 2565 2769 2975 8180	2422 2648 2875 3103 3332 3562	2934 3186 8137 8690 3942	3221 3496 3771 4048 4325	8507 3806 4105 4406 4708	4496 4773 5122 5472	48" 5442 5839 6236	3789
Thic Inches. 54 11-16 34 13-16 15-16	1.25 1.375 kness. Equiv. Decimals. .625 .6875 .75 .8125 .875 .9375 1.	1799 1985 2171 2359 2547 2737 2927 8810	2160 2362 2565 2769 2975 3180 8598	2422 2648 2875 3103 3332 3562 4027	30" 2934 8186 8137 3690 3942 4456	3221 3496 3771 4048 4325 4886	86" 8507 8806 4105 4406 4708 5316	4496 4773 5122 5472 6176	48" 5442 5839 6236 7034	60"
Thic Inches. 54 11-16 34 13-16 75 15-16	1.25 1.375 kness. Equiv. Decimals. .625 .6875 .75 .8125 .878 .9875 1.125	1799 1985 2171 2359 2547 2737 2927	2160 2362 2565 2769 2975 3180 8598 4016	2422 2648 2875 3103 3332 3562 4027 4492	30" 2934 3186 8137 3690 3942 4456 4970	3221 3496 3771 4048 4325 4886 5447	3507 3507 3806 4105 4406 4708 5316 5924	4496 4773 5122 5472	48" 5442 5839 6236	60"
Thic Inches. 54 11-16 34 13-16 75 15-16	1.25 1.375 kness. Equiv. Decimals. .625 .6875 .75 .8125 .875 .9375 1.	1799 1985 2171 2359 2547 2737 2927 8810	2160 2362 2565 2769 2975 3180 8598	2422 2648 2875 3103 3332 3562 4027	30" 2934 8186 8137 3690 3942 4456	3221 3496 3771 4048 4325 4886	86" 8507 8806 4105 4406 4708 5316	4426 4773 5122 5472 6176 6880 7591 8808	3389 48" 5442 5839 6236 7034 7838 8640 9447	974\$ 10740 11738
Thic Inches. 54 11-16 34 13-16 15-16	1.25 1.375 kness. Equiv. Decimals. .625 .6873 .75 .873 .9375 1. 1.125 1.375 1.5 1.625	1799 1985 2171 2359 2547 2737 2927 8810	2160 2362 2565 2769 2975 3180 8598 4016	2422 2648 2875 3103 3332 3562 4027 4492 4964	2934 3186 3137 3690 3942 4456 4970 5491	3221 3496 3771 4048 4325 4886 5447 6015	3507 3806 4105 4406 4708 5316 5924 6540 7158 7782	4426 4773 5122 5472 6176 6880 7591 8308 9022	5442 5839 6236 7034 7838 86447 10360	974£
Thic Inches. 54 11-16 34 13-16 15-16	1.25 1.375 kness. Equiv. Decimals. 625 .6875 .75 .8125 .875 .9375 1.125 1.25 1.375 1.5 1.625 1.75	1799 1985 2171 2359 2547 2737 2927 8810	2160 2362 2565 2769 2975 3180 8598 4016	2422 2648 2875 3103 3332 3562 4027 4492 4964	2934 3186 3137 3690 3942 4456 4970 5491 6012	3221 3496 3771 4048 4325 4886 5447 6015 6584	8507 8506 4105 4406 4708 5316 5924 6540 7158	4496 4773 5122 5472 6176 6880 7591 8308 9022 9742	5442 5839 6236 7034 7838 8640 9447 10260	974\$ 10740 11738 12744 18750
Thic Inches. 54 11-16 34 13-16 15-16	1.25 1.375 kness. Equiv. Decimals. .625 .6873 .75 .8125 .875 .9875 1. 1. 125 1. 25 1. 375 1. 625 1. 75 1. 75 1. 75	1799 1985 2171 2359 2547 2737 2927 8810	2160 2362 2565 2769 2975 3180 8598 4016	2422 2648 2875 3103 3332 3562 4027 4492 4964	2934 3186 3137 3690 3942 4456 4970 5491 6012	3221 3496 3771 4048 4325 4886 5447 6015 6584 7159	3507 3806 4105 4406 4708 5316 5924 6540 7158 7782	4496 4773 5122 5472 6176 6880 7591 8303 9022 9742 10468	5442 5839 6236 7034 7833 8640 9447 10360 11076 11076	9742 10740 11738 12744 13750 14762
Thic Inches. 54 11-16 34 13-16 15-16	1.25 1.375 kness. Equiv. Decimals. .625 .6875 .75 .875 .9875 1. 1.25 1.375 1.5 1.625 1.75 1.878 2.	1799 1985 2171 2359 2547 2737 2927 8810	2160 2362 2565 2769 2975 3180 8598 4016	2422 2648 2875 3103 3332 3562 4027 4492 4964	2934 3186 3137 3690 3942 4456 4970 5491 6012	3221 3496 3771 4048 4325 4886 5447 6015 6584 7159	3507 3806 4105 4406 4708 5316 5924 6540 7158 7782	4496 4773 5122 5472 6176 6880 7591 8308 9022 9742	5442 5839 6236 7034 7838 8640 9447 10360 11076 11976 11978	974\$ 10740 11738 12744 18750 14762 15776
Thic Inches. 54 11-16 34 13-16 76 15-16	1.25 1.375 kness. Equiv. Decimals. .625 .6873 .75 .8125 .875 .9875 1. 1. 125 1. 25 1. 375 1. 625 1. 75 1. 75 1. 75	1799 1985 2171 2359 2547 2737 2927 8810	2160 2362 2565 2769 2975 3180 8598 4016	2422 2648 2875 3103 3332 3562 4027 4492 4964	2934 3186 3137 3690 3942 4456 4970 5491 6012	3221 3496 3771 4048 4325 4886 5447 6015 6584 7159	3507 3806 4105 4406 4708 5316 5924 6540 7158 7782	4496 4773 5122 5472 6176 6880 7591 8303 9022 9742 10468	5442 5839 6236 7034 7833 8640 9447 10360 11076 11076	9742 10740 11738 12744 13750 14762

CAST-IRON PIPE FITTINGS. Approximate Weight.

(Addyston Pipe and Steel Co., Cincinnati, Ohio.)

	(Audy	ston Pipe	and Ste	er Co., Ci	ncin nati,	Onto.)	
Size in	Weight	Size in	Weight	Size in	Weight	Size in	Weight
Inches.	in Lbs.	Inches.	in Lbs.	Inches.	in Lbs.		in Lbs.
CROS	SES	TEE	28	SLEE	TES	REDUC	TPPQ
	40		220	_			
2 3	110	8×4 8×3	220	2 3	10 25	8×3 10×8	116
3×2	90	10 × 3	390	4	45	10×6	212 170
4	120	10×8	330	6	65	10×4	160
4×3	114	10×6	370	8	80	12×10	320
4×2	90	10 × 4	850	10	140	12×8	250
6	200	10×3	810	12	190	12×6	250
6×4	160	12	600	14	208	12 × 4	250
6×3	160	12×10	555	16	350	14 × 12	475
8	325	12×8	515	18	375	14×10	440
8×6	280	12 × 6	550	20	500	14×8	390
8 × 4	265	12 × 4	525	24	710	14×6	285
8×3	225	14 × 12	650	30	965	16 × 12	475
10	575	14×10	650	86	1200	16 × 10	435
10×8	415	14×8	575	90° ELI	BOWS.	20×16	690
10 × 6 10 × 4	450 300	14×6	545	2	1 14	20×14	575
10 × 8	350	14×4	525 490	3	34	20 × 12	540
12	740	14 × 3 16	790	4	55	20 × 8 24 × 20	400 990
12×10	650	16×14	850	6	120	30 × 24	1305
12×8	620	16 × 12	850	š	150	30 × 18	1385
12×6	540	16 × 10	850	1Ŏ	260	36 × 30	1730
12 × 4	525	16×8	755	12	370		
12 × 3	495	16×6	680	14	450		REDUC-
14×10	750	16×4	655	16	660	ERS FO	
14×8	635	18	1235	18	850	6×4	95
14×6	570	20	1475	20	900	6×8	70
16	1100	20×16	1115	24	1400	S PII	PES
16 × 14	1070	20 × 12	1025	80	8000		105
16 × 12	1000	20×10	1090	1/8 or 45° I	BENDS.	6	190
16 × 10 16 × 8	1010 825	20×8	900	8	1 80		
16×6	700	20×6 20×4	875 845	4	~~~	PLU	GS.
16 × 4	650	20 × 4 20 × 10	1465	è	95	2	3
18	1560	20 × 10	2000	š	150	8	10
20	1790	24 × 12	1425	10	200	4	10
20 × 12	1370	24 × 8	1875	12	290	6	15
20 × 10	1225	24×6	1450	16	510	8	30
20×8	1000	30	8025	18	580	10	46
20×6	1000	30 × 24	2640	20	780	12	66
20 × 4	1000	30×20	2200	24	1425	14	90
24	2400	30 × 12	2035	- 80	2000	16 18	100
24 × 20	2020	80 × 10	2050	1/16 or	22160	20	180 150
24 × 6	1840 2635	80×6	1825	BEN	DS.~	24	185
80 × 20 80 × 12	2030 2250	86	5140	6	150	30	370
30 × 12	1995	36 × 30	4200 4050	8	155		
		86 × 18	4000	1Ŏ	205	CAI	
TEE	28.	45° BR.	ANCH	12	260	3	20
2	28	PIPE		16	450	4	25
8	80			24	1280	. 6	60
3×2	76	8	90	30	2000	.8	75
4	100	4	125	REDUC	ERS	10	100
4 × 3	90	6	205			12	120
4×2	87	6×6×4	145	8×2	25	DRIP B	OXES.
6	150 145	8 8× 6	830 830	4×3 4×2	42 40	4	295
6×4	145 145	24 D	2765	4 × 2 6 × 4	95	6	330
6×8 6×2	75	24 × 24 × 20	2145	6×3	70	8	375
8 × 8	300	80	4170	8×6	126	10	875
8×6	270	86	10300	8×4	116	20	1420
0 × 0	210	- 00	.0000	U A 12	120	. ~	4 744

WEIGHTS OF CAST-IRON WATER- AND GAS-PIPE.

(Addyston Pipe and Steel Co., Cincinnati, Ohio.)

e ii	Stand	ard Wate	r-pipe,	in es.	Stan	dard Gas	-pipe.
Size in Inches.	Per Foot.	Thick- ness.	Per Length.	Size	Per Foot.	Thick- ness.	Per Length.
2 3	7 15	5/16	63 180	2 8	6 1214	1/4 5/16	48 150
2 3 4 6 8 10	17 22 83	12	204 264 396	4 6 8	17 80	36 7/16 7/16	204 . 360
8	49 45	12	504 540	-	40		480
12 12 14	60 75 117	9/16	720 900 1400	10 12 14	50 70 84	7/16 16 9/16	600 840 1000
16 18	125 167	34	1500 2000	16 18	100 134	9/16 11/16	1200 1600
20 24	200 250	15/16	2400 3000	20 24	150 184 250	11/16	1800 2200
30 86 42	350 475 600	11/6 18/6 18/6	4200 5700 7200	30 36 42	350 417	24 28 15/16	3000 4200 5000
48 60	775 1330	11/2	9300 15960	48 60	542 900	11/6 19/6	6500 10800
72	1835	21/4	22030	72	1250	112	15000

THICKNESS OF CAST-IRON WATER-PIPES.

- P. H. Baermann, in a paper read before the Engineers' Club of Philadelphia in 1882, gave twenty different formulas for determining the thickness of cast-iron pipes under pressure. The formulas are of three classes:
- Depending upon the diameter only.
 Those depending upon the diameter and head, and which add a constant.
- 3. Those depending upon the diameter and head, contain an additive or subtractive term depending upon the diameter, and add a constant. The more modern formulas are of the third class, and are as follows:

о н	HOLE WORLD LOLLINGING WILL OF MIC ATTIC	creeps' enter er c es T	OITO M P.
ŧ	$= .00008hd + .01d + .86 \dots$	Shedd,	No. 1.
t	$= .00006hd + .0183d + .296 \dots$	Warren Foundry.	No. 2.
ŧ	= .000058hd + .0152d + .312	Francis.	No. 3.
t	= .000048hd + .013d + .32	.Dupuit,	No. 4.
ŧ	$= .00004hd + .1 \sqrt{d} + .15$	Box,	No. 5.
t	= .000135hd + .40011d	. Whitman.	No. 6.
t	$= .00006(h + 230)a + .3330033a \dots$	Fanning.	No. 7.
ŧ	= 00015hd + 25 - 0052d	Meggs.	No 8

In which t = thickness in inches, h = head in feet, d = diameter in inches.

Rankine, "Civil Engineering," p. 721, says: "Cast-iron pipes should be made of a soft and tough quality of iron. Great attention should be paid to moulding them correctly, so that the thickness may be exactly uniform all round. Each pipe should be tested for ir-bub-les and flavs by ringing it with a hammer, and for trength by exposing 't to 'ou at the intended greatest working pressure." The rule for computing the hickness of a pipe

to resist a given working pressure is $t = \frac{rp}{f}$, where r is the radius in inches,

p the pressure in pounds per square inch, and f the tenacity of the iron ver square inch. When f=18000, and a factor of safety of 5 is used, the above expressed in terms of d and h becomes

$$t = \frac{.5d .433h}{3600} = \frac{dh}{16628} = .00006dh$$

[&]quot;There are limitations, however, arising from difficulties in casting, and by the strain produced by shocks, which cause the thickness to be made reater than that given by the above formula."

Thickness of Metal and Weight per Length for Different Sizes of Cast-iron Pipes under Various Heads of Water.

(Warren Foundry and Machine Co.)

	Ft. I	0 Iead.	1(Ft. I	00 Iead.	15 Ft. H	o ead.	20 Ft. F		2! Ft. I	50 Head.	8(Ft. I	
Size.	Thickness of Metal.	Weight per Length.	Thickness of Metal.	Weight per Length.	Thickness of Metal.	Weight per Length.						
		_		-		_	_				-	
8 4 5 6 8 10 12 14 16 18 20	.344 .361	144 197	.853 .878	149 204	.862 .385	158 211	.871 .397	157 218	.880	161 226	.390 .421	166 235
5	.361 .378	254	.393	265	.408	275	.428	286	.409 .438 .465 .522	298 377	.453	309
6	.893 .422	315 445	.411 .450	830 475	.429 .474	845 502	.447 .498	861 529	.465	877 557	.483 .546	393 584
10	.459	600	.489	641	.519	682	.549	723	.579	766	.609	808
12	.491	768	.527	826	.563	885	.599	944	.635 .692	1004	.671	1064
14	.524	952	.566	1031	.608	1111	.650	1191	.692	1272	.734	1352
16	.557 .589	1152	.604 .648	1253	.652 .697	1360 1680	.700 .751	1463 1761	.748 .805	1568 1894	.796 .859	1673 2026
19	699	1870 1603	.682	1500 1763	.742	1924	.802	2086	.862	2248	922	2412
24	687	2120	.759	2349	.831	2580	.908	2811	.975	3045	1.047	3279
80	.785	8020	.875	8876	.965	3735	1.055	4095	1.145	4458	1.235	4822
36	.622 .687 .785	4070		4581	1.098		1.206	5013	1.814	6183	1.422	6656
24 30 36 42 48	1.078	5265	1.106 1.222	5958 7521	1.232 1.366		1.858 1.510	7360 9340	1.484 1.654	8070 10269	1.610 1.798	8804 11195

All pipe cast vertically in dry sand; the 3 to 12 inch in lengths of 12 feet, all larger sizes in lengths of 12 feet 4 inches.

Safe Pressures and Equivalent Heads of Water for Castiron Pipe of Different Sizes and Thicknesses.

(Calculated by F. H. Lewis, from Fanning's Formula.)

								Si	ze of	Pip	3.							
	4	"	6	"	8	"	10	y "	19	"	14	"	16	"	18	"	20)"
Thick-	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet,	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet,	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.
7-16 1-2 9-16 5-8 11-16 3-4 13-18 7-8 15-16 1 1 1-8	119 224 336	958 516 774	49 124 199 274	112 286 458 631	18 74 130 186	300	44 89 132 177 224	101 205 304 408 516	24 62 99 137 174 212 249	55 143 228 316 401 488 574	49 74 106 138 170 202 234 266	97 170 244 316 392 465 538 612	56 84 112 140 168 196 224	129 194 258 323 387 452 516	41 66 91 116 141 166 191 216	95 152 210 267 325 382 440 497	51 74 96 119 141 164 209 256	325 378 481

Safe Pressures, etc., for Cast-iron Pipe.-(Continued.)

								Si	ze of	Pip	е.							
	25	2"	2	ç"	2	"	30	y "	3	3"	36	"	49	"	48	3"	66	y,
Thick- ness.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Foet,	Pressure in Pounds,	Head in Feet.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.
11-16 3-4 13-16 7-8 15-16 1 1 1-8 1 1-4 1 1-8 1	40 60 80 101 121 143 183 924	99 138 184 233 279 327 419 516	30 49 68 86 105 134 161 199 237	69 113 157 198 243 286 371 458 546	19 36 59 85 102 135 169 202 236	64 83 190 159 196 235 311 389 465 544	24 39 54 69 84 114 174 204 234	55 90 124 159 194 263 339 401 470 538	42 55 69 96 124 151 178 206 233	97 127 159 221 286 348 410 472 537	38 44 57 89 107 132 157 182 207	74 101 131 189 247 304 362 419 477	38 59 81 108 124 145 167 188 210	88 136 187 237 286 334 484	24 43 62 81 99 118 136 155	55 99 143 187 238 272 813 357 401	34 40 64 79	78 113 147 189 217 251
2 1-8 2 1-4 2 1-2 2 3-4	***			:::		:::		:::	:::					:::	193	445	139 154 134 214	350 450 480

Norm.—The absolute safe static pressure which may be put upon pipe is given by the formula $P=\frac{2T}{D}\times\frac{S}{E}$, in which formula P is the pressure per square inch; T, the thickness of the shell; S, the ultimate strength per square inch of the metal in tension; and D, the inside diameter of the pipe. In the tables S is taken as 18000 pounds per square inch, with a working strain of one fifth this amount or 3600 pounds per square inch. The formula for the absolute safe static pressure then is: $P=\frac{7200T}{D}$.

It is, however, usual to allow for "water-ram" by increasing the thickness enough to provide for 100 pounds additional static pressure, and, to insure sufficient metal for good casting and for wear and tear, a further increase equal to .833 $\left(1-\frac{D}{100}\right)$.

The expression for the thickness then becomes:

$$T = \frac{(P+100)D}{7900} + .833 \left(1 - \frac{D}{100}\right),$$

and for safe working pressure

$$P = \frac{7900}{D} \left(T - .888 \left(1 - \frac{D}{100} \right) \right) - 100.$$

The additional section provided as above represents an increased value under static pressure for the different sizes of pipe as follows (see table in margin). So that to test the pipes up to one fifth of the ultimate strength of the material, the pressures in the marginal table should be added to the pressure-values given in the table above.

Size of Pipe.	Lbs.
4" 6 8 10 12 14 16 18 20 23 24 49 49 60	676 476 346 316 276 248 229 196 185 176 156 143 128 116

RIVETED HYDRAULIC PIPE.

(Pelton Water Wheel Co.)

Weight per foot with safe head for various sizes of double-riveted pipe.

18	4 4 4 5 5 5 5 6 6 6 6 7 7 7 7 8 8 8 9 1 1 10 1 10 10 11 11 11 11 11 11 11 11	Diameter of Pipe, Inches.
1.05	18 16 16 14 18 16 14 18 16 14 18 16 16 14 18 16 16 14 18 16 16 16 16 16 16 16 16 16 16 16 16 16	Thick. of Metal, U.S. Stand
810 807 31 18 11 115 837 29 760 334 18 10 114 378 821/4 485 834 18 8 171 460 40 40 40 40 40 40 40 40 40 40 40 40 40	.062 .063 .063 .063 .05 .062 .078 .05 .078 .05 .078 .062 .078 .078 .078 .078 .078 .078 .078 .078	Equivalent Thickness,
	607 760 485 605 757 405 630 846 427 866 420 878 427 866 427 867 875 840 875 840 875 840 875 840 875 840 875 840 875 840 875 840 875 840 875 840 875 840 875 840 875 840 875 840 875 840 875 840 875 840 875 840 840 875 840 840 875 840 840 840 840 840 840 840 840 840 840	Head in Feet Pipe will Safely Stand.
	334 334 414 514 514 514 614 677 812 714 714 714 714 714 714 714 714	Weight per Lineal Foot, in Pounds.
	18 18 18 18 18 20 20 20 20 20 20 20 20 20 20 20 20 20	Diameter of Pipe, Inches.
Description Description	12 110 86 14 110 110 110 110 110 110 110 110 110	Thick. of Metal, U. S. Standard Gauge.
<u> </u>	.125 .14 .171 .062 .078 .109 .125 .14 .171 .062 .078 .109 .125 .14 .171 .078 .109 .125 .14 .171 .078 .109 .125 .14	Equivalent Thickness, . Inches.
2514 2914 40 11934 411 11934 4514 4514 4514 4514 4514 4514 4514 45	295 837 878 460 151 189 965 304 445 138 172 240 276 283 346 145 283 346 283 283 283 283 188 283 283 283 283 185 283 283 185 283 283 283 283 283 283 283 283 283 283	Head in Feet Pipe will Safely Stand.
	35 4514 1734 222 3014 123 3014 123 3014 123 3014 123 3014 123 3014 125 125 125 125 125 125 125 125 125 125	Weight per Lineal Foot, in Pounds.

STANDARD PIPE FLANGES.

Adopted August, 1894, at a conference of committees of the American Society of Mechanical Engineers, and the Master Steam and Hot Water Fitters' Association, with representatives of leading manufacturers and users of pipe.—Trans. A. S. M. E., xxi. 29. (The standard dimensions given have not yet, 1901, been adopted by some manufacturers on account of their unwillingness to make a change in their patterns.)

The list is divided into two groups; for medium and high pressures, the first ranging up to 75 lbs. per square inch, and the second up to 200 lbs.

Pipe size, inches.	Pipe Thickness, $\frac{P+100}{P+100}d + .833 \left(1 - \frac{d}{100}\right)$	Thickness, nearest Fraction, inches.	Stress on Pipe per square inch @ 200 lbs.	Radius of Fillet, inches.	Flange Diameters, inches.	Flange Thicknesses at edge, inches.	Width Flange Face, inches.	Bolt Circle Diameter, inches.	Number of Bolts.	Bolt Diameter, inches.	Bolt Length, inches.	Stress on each Bolt, per square inch at Bottom of Thread @ 200 lbs.
2 1/2 2 1/2 3 1/2 3 1/2 1/2 3 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2	.409 .429 .449 .466 .498 .525 .563 .60 .639 .678 .719 .864 .946 1.09 1.18 1.25 1.30 1.38 1.48 1.71	**************************************	460 550 690 700 900 11060 11290 11310 1470 1600 1690 1780 2040 2000 2130	HANNER HERE CONTROL OF THE PROPERTY OF THE PRO	6 7 7 1 6 1 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	5. 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	2 14 14 14 15 15 15 14 14 15 15 16 16 16 16 16 16 16 16 16 16 16 16 16	484 6 7 7 14 8 17 18 18 18 18 18 18 18 18 18 18 18 18 18	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	***************************************	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	825 1050 1330 2530 2100 1430 1630 2360 3200 3610 2970 2970 4280 4280 4280 4210 4540 4490 4490 4590 5030 5000 5700 6090

Notes.—Sizes up to 24 inches are designed for 200 lbs. or less.

Sizes from 24 to 48 inches are divided into two scales, one for 200 lbs., the other for less.

The sizes of bolts given are for high pressure. For medium pressures the diameters are ½ in. less for pipes 2 to 20 in. diameter inclusive, and ¼ in. less for larger sizes, except 48-in. pipe, for which the size of bolt is 1½ in. When two lines of figures occur under one heading, the single columns are for both medium and high pressures. Beginning with 24 inches, the left-hand

columns are for medium and the right-hand lines are for high pressures.

The sudden increase in diameters at 16 inches is due to the possible inser-

tion of wrought-iron pipe, making with a nearly constant width of gasket a greater diameter desirable.

When wrought-iron pipe is used, if thinner flanges than those given are sufficient, it is proposed that bosses be used to bring the nuts up to the standard lengths. This avoids the use of a reinforcement around the pipe.

Figures in the 3d, 4th, 5th, and last columns refer only to pipe for high

pressure

In drilling valve flanges a vertical line parallel to the spindles should be idway between two holes on the upper side of the flanges.

FLANGE DIMENSIONS, ETC., FOR EXTRA HEAVY PIPE FITTINGS.

Adopted by a Conference of Manufacturers, June 28, 1901.

Size of Pipe.	Diam. of Flange.	Thickness of Flange.	Diameter of Bolt Circle.	Number of Bolts.	Size of, Bolts.
Inches.	Inches.	Inches.	Inches.		Inches.
2	616	. %	5	4	5 6
21/2	736	1	57/6	4	3 4
8	81/4	11/6	696	8	5 6
31/4	9	1 3-16	71/4	8	26
4	10	11/4	77/6	8	24
41/6	1016	1 5-16	81/6	8 8 8	₹.
5	1 11 .	196	924		24
6	121/6	1 7-16	1096	12	24
7	14	11/4	11%	12	2 8
۰,8	15	196	18	12	2/8
.9	16	154	14	12	26
10	1714	1%	1514	16	28
12	20 ~	2	1794	16	29
14	221/4	278	20	20	, %
15	231/6	2 8-16	21	20	1
16	25	224	221/6	20	1
18	27	298	2416	24	1
20	2914	21/9	2094	24	11/8
22	811/6	279	2894	28	176
24	84	29/4	811/4	28	11/8

PIMENSIONS OF PIPE FLANGES AND CAST-IRON PIPES.

(J. E. Codman, Engineers' Club of Philadelphia, 1889.)

				<u> </u>				· · · · · · · · · · · · · · · · · · ·	
Diameter of Pipe.	Diamater of Flange.	Diameter of Bolt Circle.	Diameter of Bolt	Number of Bolts.	Thickness of Flange.		ripe. Dec.	Weight per foot without Flange.	Weight of Flange and Bolts.
2 8 4 5 6 8 10 12 14 16 18 20 22 24 28 20 22 28 28 30 40 44 44 44 46	614 779 944 1094 1184 1184 11794 22 24 27 2814 24 27 2814 3314 43 40 41 47 49 5114 56 56 56	45/4 57/8 8 91/6 113/4 15/4 18 20 221/4 241/4 18 33 25/4 40 42 44 46 481/4 481/4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	**************************************	4 6 6 8 8 10 12 14 16 16 18 20 22 24 24 28 30 32 32 34 36 84 36 84 36	76 76 11-16 76 13-16 1 1-16 1 1 1-16 1 1 5-16 1 7-16 1 9-16 1 11-16 1 1 1-16 1 1 1-16 1 2 1 1 1-16 1 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 5-32 1 3-16	.971 1.017	6.96 11.16 15.84 21.00 26.64 89.36 54.00 70.56 89.04 109.44 1181.76 1156.00 1182.16 210.24 240.24 240.24 272.16 306.00 341.76 879.44 419.04 460.56 504.00 549.36 596.64 645.84 665.96	4.41 5.98, 7.66 9.63 11.82 16.91 23.00 30.13 88.34 47.70 58.23 70.00 83.05 58.23 70.00 83.05 197.42 113.18 190.90 214.26 239.27 266.00 294.49 336.94 336.94

D =Diameter of pipe. All dimensions in inches.

FORMULE.—Thickness of flange = 0.033D + 0.56; thickness of pipe = 0.032D + 0.327; weight of pipe per foot = $0.24D^2 + 3D$; weight of flange $0.01D^2 + 0.1D^2 + D + 2$; diameter of flange = 1.125D + 4.25; diameter of bolt = 0.011D + 0.73; number below = 0.78D + 2.56.

Standard Dimensions of Wrought-Iron Welded Pipe.

(National Tube Works.)

Length of Perf. Thread,	집 46:8		<u> </u>	182	3	88	28	1.16	2 ×	1.46	1.57	38	88	8.10	8.3	:	:	:	
No. of Threads perinch.		222														:	: :	:	one
Weight of Water per Idn. Ft. of Pipe.	1. bg.	28	:: ::: :::: ::::::::::::::::::::::::::	88.4	20.020	4.291	5.512	8	18.508	21.664	27.166	41.158	8.07 8.07 8.07 8.07	89.080	25	101.208	158.675	188.842	Soldione
Weight of Pipe per Lin. Ft.	Lbe.																		on in
U. 8. Gallons per Ft. of Pipe.	Galls.	900	2.54	1068	888	5136	.6613	1.088	2000	2.599	80. 4 80. 5 80. 5	4.937	5.875	8.285	9.480	12.141	18.424	2002	and lone
Length of Pipe cont'g i	Feet. 2500.0	27. 28. 28.	270.016 167.246	5.75	86.8	14.567	11.812	2.802	4.08	2.876	98.	1.515	2.5	0.80	8	968	9	330	11/1/10
Area	8q. Ft.																		Die
External	8q. Ins. 1288	8. 15. 5. 15.	25.55 25.55	88.4 50.8	9	19.566	5.5 2.5 5.5 5.5 5.5 5.5 5.5 5.5 5.5 5.5	24.801	45.47.8 86.47.8	58.426	22.780	88.434	27.677	76.715	01.088	5.4.2	8.184	52.890	000
Area	2000 2000 2000 2000 2000 2000 2000 200	8.00 8.13	888	25	88	.0687	88.	1388	200	8474	4356	9	200	1.1075	1.2685	0.000	4699	8.94834	1, 60
Internal	Sq. Inc. .067	190	8.00.4 8.00.6	98. 88. 87.	4 .	9.887	5. E	19.886	88	50.027	25.55 50.55	95.083	118.098	159.485	38.68 8.68	25 25 25 25 25 25 25 25 25 25 25 25 25 2	25 - 52 - 52 - 52 - 52 - 52 - 52 - 52 -	424.658	9 45 6
Inspection of Pipe of	Feet. 9.484	82.7	8 8 8 8 8 8	010	88	0.955	.849	.88	200	4	S . S	2	8.5	8	8	Ž:	124	159	Page 1
Instant I specification of Pipe 194 (1.1) to require the contraction of the contraction o	Feet. 14.151	5. 78 188	4.00 8.25 8.25	20.872	8	1.07	9.5	757	3.7	2	3.8	2	2000	8	3	ž Š	2	2	7
Exter- nal Cir- cumfer- ence,	1	8. 5. 8. 18. 8. 18.			•	= ==	<u> </u>	-	N CI	Q.	33 ex	90	4 4	4	70.	δč	ě	7.	
Internal Chreum- ference.	H 25.	1.552	0, 00, 4 0, 00, 4 0, 00, 8 0, 00, 8	5.058	200	11.146	12.648	15.849	2 8 2 8 2 8	25.076	8.8	30	20.5 20.5 20.5 20.5 20.5 20.5 20.5 20.5	44.768	2.80	2.5 5.5 5.5 5.5 5.5 5.5 5.5 5.5 5.5 5.5	200	38.042	1
Thick- ness of Metal,	ı	88					_										•	•	11001
Actual Inside Diam.	_	200 200			1 04 6	9	4.4	43			۶	:=:	35	33	8	56	8	8	/7 maca
LantoA Outsido Amaid	!	55.3								_		-				25	88	2	0
lanimok oblani mald	13,700		x _;	, <u>,,</u>	ž.	. జే	4.5	20	6 6-	•	95	==	2 5	1	22	:		:	

Pipe from 18" to 1" inclusive is butt-welded, and proved to 300 lbs. per sq. in. Pipe 114" and larger is lap-welded, and proved to 500 lbs per sq. in.

For discussion of the Briggs Standard of Wrought-iron Pipe Dimensions, see Report of the Committee of the A. S. M. E. in "Standard Pipe and Pipe Threads," 1886. Trans., Vol. VIII, p. 29. The diameter of the bottom of the thread is derived from the formula $D = (0.05D + 1.9) \times \frac{1}{n}$, in which D = outside diameter of the tubes, and n the number of threads to the inch. The diameter of the top of the thread is derived from the formula $0.8\frac{1}{n} \times 2 + d$, or $1.6\frac{1}{n} + d$, in which d is the diameter at the bottom of the thread at the end of the pipe.

The sizes for the diameters at the bottom and top of the thread at the end of the pipe are as follows:

Diam. of Pipe, Nom- ina.	Diam. at Bot- tom of Thread.	Diam. at Top of Thread.	Diam. of Pipe, Nom- inal.	Diam. at Bot- tom of Thread.	of	Nom-	Diam. at Bot- tom of Thread.	Diam. at Top of Thread.
in.	in. .384 .483 .568 .701 .911 1.144 1.488 1.727 2.223	in. .393 .522 .658 .815 1.025 1.268 1.627 1.866 2.339	in. 21/4 3 31/4 4 4 1/4 5 6 ?	in. 2.620 3.241 3.788 4.234 4.731 5.290 6.346 7.840	in. 2.820 8.441 3.938 4.434 4.931 5.490 6.546 7.540	in. 8 9 10 11 12 13 14	in. 8.384 9.827 10.445 11.439 12.488 13.675 14.669 15.663	in. 8.584 9.527 10.645 11.639 12.638 13.875 14.869 15.868

Having the taper, length of full-threaded portion, and the sizes at bottom and top of thread at the end of the pipe, as given in the table, taps and dies can be made to secure these points correctly, the length of the imperfect threaded portions on the pipe, and the length the tap is run into the fittings beyond the point at which the size is as given, or, in other words, beyond the end of the pipe, having no effect upon the standard. The angle of the thread is 60°, and it is slightly rounded off at top and bottom, so that, instead at its depth being 0.866 its pitch, as is the case with a full V-thread, it is 45 the pitch, or equal to 0.8 + n, n being the number of threads per inch.

Taper of conical tube ends, 1 in 82 to axis of tube = 34 inch to the foot total tanes.

total taper.

WROUGHT-IRON WELDED TUBES, EXTRA STRONG. Standard Dimensions.

Nominal Diameter.	Actual Out- side Diameter.	Thickness, Extra Strong.	Thickness, Double Extra Strong.	Actual Inside Diameter, Extra Strong.	Actual Inside Diameter, Double Extra Strong.
Inches. 1/6 1/4 1/4 1/4 2 2/4 3/4	Inches. 0.405 0.54 0.675 0.84 1.05 1.315 1.66 1.9 2.375 2.375 4.0	Inches, 0.100 0.123 0.127 0.149 0.157 0.183 0.293 0.291 0.290 0.304 0.321	0.298 0.314 0.364 0.388 0.406 0.442 0.560 0.608 0.642	Inches. 0.205 0.294 0.421 0.542 0.786 0.961 1.272 1.494 1.933 2.315 2.882 8.358	0.244 0.422 0.587 0.884 1.088 1.491 1.755 2.284 2.716 8.136

STANDARD SIZES, ETC., OF LAP-WELDED CHAR-COAL-IRON BOILER-TUBES.

(National Tube Works.)

External Diameter,	Internal Diam- eter,	Standard Thickness.	Internal Cir- cumference.	External Circumference.	Inter		Exter		Length of Tube per Sq. Ft. of InsideSurface	Length of Tube per Sq. Ft. of Outside Sur- face.	Length of Tube per Sq. Ft. of Mean Surface,	Weight per Lineal Foot.
in. 11-4 13-4 21-22-3-4 221-4 231-4 331-9 33-4 41-9 10 11 12 13 14 15 16 17 18 19 19 19 19 19 19 19 19 19 19	1,560 1,810 2,060 2,282 2,532 2,782 3,010 3,510 3,732 4,704 5,670 6,670 7,670 8,640 10,562 11,562 11,562 11,563 11,483 15,458 16,433 15,458	in	1n. 2,545 3,330 4,115 4,901 5,686 6,472 7,955 8,740 9,456 10,242 11,724 11,724 13,295 14,778 12,403 30,141 33,175 36,260 33,317 42,404 6,497 48,563 51,623 54,714	1n. 3.142 3.927 4.712 5.498 6.283 7.069 7.854 8.639 9.425 10.210 10.996 11.781 12.566 14.137 15.708 18.850 21.991 32.274 31.416 34.658 37.699 40.841 43.982 47.124 50.266 53.407 56.545	8q. in, 515 8822 1.348 1.348 1.348 1.348 1.948 1.957 3.333 4.090 6.035 6.079 7.116 8.347 9.376 10.939 14.066 9.35,250 72.292 87.583 104.629 123.190 143.224 164.721 187.671 1212.066 238.225	.0036 .0061 .0094 .0113 .0179 .0231 .0284 .0350 .0494 .0580 .0678 .0760 .0977 .1750 .9421 .7266 .8555 .9946 .11439 .13033 .14727 .1,6548	8q. in. 7,85 1,927 1,767 2,405 3,142 3,142 3,142 4,909 6,940 7,069 8,296 9,621 11,045 11,045 12,566 13,904 11,045 13,566 13,904 11,045 13,566 13,904 13,566 13,904 13,566 13,904 13,566 13,904 13,566 13,904 13,566 13,904 13,566 13,904 13,566 13,904 13,566 13,904 13,566 13,904 13,566 13,904 13,566 13,904 13,566 13,904 13,566 13,904 13,566 13,904 13,566 13,904 14,904 14,904 15,904	.6600 .7854 .9217 1.0090 1.9272 1.3963 1.5768 1.7671	ft. 4,479 3,604 2,916 2,916 2,110 1,854 1,674 1,508 1,273 1,088 1,024 1,024 6,73 4,98 4,12 3,98 4,12 4,12 4,13 4,14 4,14 4,14 4,14 4,14 4,14 4,14	ft. 3.806 2.547 2.183 1.919 1.698 1.528 1.923 1.1791 1.091 1.091 2.055 849 4.77 4.24 3.82 3.82 3.82 3.83 3.83 3.83 3.83 3.83	ft. 4.149 2.316 2.010 1.776 2.010 1.449 1.329 1.054 1.020 2.788 6.560 6.560 4.88 4.33 3.390 2.78 2.78 2.278 2.299 2.16 2.205	1bs
20 21	18,400 19,360 20,320	,300 ,320 ,340	57.805 60.821 63.837	59.690 62.832 65.974	294.375 324.294	2,0443	314,159 346,361	2,1817	.208 .197 .188	.201 .191 .182	.194	59.48 66.77 73.40

In estimating the effective steam-heating or boiler surface of tubes, the surface in contact with air or gases of combustion (whether internal or external to the tubes) is to be taken.

For heating liquids by steam, superheating steam, or transferring heat from one liquid or gas to another, the mean surface of the tubes is to be taken.

To find the square feet of surface, S, in a tube of a given length, L, in feet, and diameter, d, if inches, multiply the length in feet by the diameter in inches and by .2618. Or, $S = \frac{3.1416dL}{12} = .2618dL$. For the diameters in the table below, multiply the length in feet by the figures given opposite the diameter.

Inches, Diameter.	Square Feet per Foot Length.	Inches, Diameter.	Square Feet per Foot Length.	Inches, Diameter.	Square Feet per Foot Length.
11/4	.0654 .1809 .1968 .2618 .8272 .3927 .4581 .5286	214 254 254 314 314 4	.5890 .6545 .7199 .7854 .8508 .9163 .9817 1.0472	5 6 7 8 9 10 11	1.3090 1.5708 1.8326 2.0944 2.8562 2.6180 2.8798 3.1416

BIVETED IRON PIPE.

(Abendroth & Root Mfg. Co.)

Sheets punched and rolled, ready for riveting, are packed in convenient form for shipment. The following table shows the iron and rivets required for punched and formed sheets.

Number Square Feet of Iron required to make 100 Lineal Feet Punched and Formed Sheets when put together.			mate No. required 00 Linesi Funched Formed	Number Square Feet of Iron required to make 100 Lineal Feet Punched and Formed Sheets when put together.			oximate No. tivets 1 Inch rt required 100 Lines. t Punched Formed ets.
Diam- eter in Inches.	Width of Lap in Inches.	Square Feet.	Approxi of Rive apart for 10 Feet and Sheets	Diam- eter in Inches.	Width of Lap in Inches.	Square Feet.	Approxication River 10 Feet and Sheets
8 4 5 6 7 8 9 10 11 12 13	1 11/2 11/2 11/2 11/2 11/2 11/2	90 116 150 178 206 234 258 289 814 343 369	1,600 1,700 1,800 1,900 2,000 2,200 2,300 2,400 2,500 2,600 2,700	14 15 16 18 20 22 24 26 28 30 36	114 114 114 114 114 114 114 114 114 114	897 423 453 506 562 617 670 725 779 836 998	2,800 2,900 3,000 3,200 8,500 8,700 8,900 4,100 4,400 4,600 5,200

WEIGHT OF ONE SQUARE FOOT OF SHEET-IRON FOR BIVETED PIPE.

Thickness by the Birmingham Wire-Gauge.

No. of Gauge.	Thick- ness in Decimals of an Inch.	Weight in lbs., Black.	Weight in lbs., Galvan- ized.	No. of Gauge.	Thick- ness in Decimals of an Inch.	Weight in lbs., Black.	Weight in lbs., Galvan- ized.
26	.018	.80	.91	18	.049	1.82	2.16
24	.022	1.00	1.16	16	.065	2.50	2 67
22	.028	1.25	1.40	14	.083	8.12	8.84
20	.085	1.56	1.67	12	.109	4.37	4.78

SPIRAL RIVETED PIPE,

(Abendroth & Root Mfg. Co.)

Thick	Thickness.			Approximate Burst-				
B. W. G. No.	Inches.	eter, Inches.	in lbs. per Foot in ling Pre per So	ssure in lbs. luare Inch.				
26 24 22 20	.018 .022 .028	8 to 6 8 to 12 8 to 14	lbs.= "= 1/6 of diam. in ins. "= 4 ""					
18 16	.035 .049 .065	8 to 24 8 to 21 6 to 24	" = .5 " " 2700 lbs " = .6 " " 3600 " - " = .8 " " 4800 " -	diam. in ins.				
14 12	.083 .109	8 to 24 9 to 24	" =1.1 " " 6400 " = " =1.4 " " 8000 " =					

The above are black pipes. Galvanized weighs 10 to 30 % heavier.

Double Galvanized Spiral Riveted Flanged Pressure Pipe, tested to 150 lbs. hydraulic pressure.

Inside diameters, inches 3 Thickness, B. W. G 20 Nominal wt. per foot, lbs 2½	4 5	6 7	8 9 10 11 1	12(13)14[15]16[18]20]22[2
Thickness, B. W. G 20	20 20	18 18 1	8 18 16 16 1	16 16 14 14 14 14 14 14 12 1
Nominal wt. per foot, lbs 21/4	8 4	5 6	7 8 11 12 1	14 15 20 22 24 29 34 40 5

DIMENSIONS OF SPIRAL PIPE FITTINGS.

Inside Diameter.	Outside Diameter Flanges,	Number Bolt-holes.	Diameter Bolt-holes.	Diameter Circles on which Bolt- holes are Drilled.	Sizes of Bolts.
ins. 8 4 5 6 7 8 9 10 11 12 13 14 15 16 18 20 22 24	ins. 6 7 8 876 10 11 13 14 15 16 17 1778 23 24 25 34 30	4 8 8 8 8 8 8 12 12 12 12 12 12 12 16 16	ins. 16 17 16 16 16 16 16 16 16 16 16 16 16 17 16 11/16 16 16 16 16 16 16 16 16 16 16 16 16 1	ins. 454 5 15/16 6 15/16 776 9 10 1114 1214 1356 1514 1514 17 7/16 1914 2316 26 2734	ins. 7/16 × 184 7/16 × 184 7/16 × 184 184 184 184 184 184 184 184 184 184

SEAMLESS BRASS TUBE. IRON-PIPE SIZES.

(For actual dimensions see tables of Wrought-iron Pipe.)

Nominal	Weight	Nom.	Weight	Nom.	Weight	Nom.	Weight
Size.	per Foot.	Size.	per Foot.	Size.	per Foot.	Size.	per Foot.
ins.	lbs. .25 .43 .62 .90	ins. 3/4 1 11/4 11/4	lbs. 1.25 1.70 2.50 3.	ins. 2 21/2 3 31/4	lbs. 4.0 5.75 8.30 10.90	ins. 4 43/2 5	lbs. 12.70 18.90 15.75 18.81

SEAMLESS DRAWN BRASS TUBING. (Randolph & Ciowes, Waterbury, Conn.)

Outside diameter 3/16 to 73/4 inches. Thickness of walls 8 to 25 Stube' Gauge, length 12 feet. The following are the standard sizes:

Outside Diam- eter.	Length Feet.	Stubbs' or Old Gauge.	Outside Diam- eter.	Length Feet.	Stubbs' or Old Gauge.	Outside Diam- eter,	Length Feet.	Stubbs or Old Gauge.
5-16	12 12 12	20 19	136 116 167	12 12 12	14 14	256 254	12 12 12	11 11 11
78 56 54 13-16	12 12 12 12	19 18 18 17	134 1 13-16	12	14 13 13 13 13 19 19	314 316	12 12 10 to 12	11 11 11
13-16 36 15-16	12 12 12	17	1 15-16	12 19 12 12	19 12 19	5 514	10 to 12 10 to 12 10 to 12	
1116	12 12 12	17 16 16 15	214 286 912	19 12 12	12 12 12	516 594 6	10 to 12 10 to 12	11 11

BENT AND COILED PIPES. (National Pipe Bending Co., New Haven, Conn.) COILS AND BENDS OF IRON AND STEEL PIPE.

Size of pipeInches Least outside diameter of codiInches	-	36 216	1½ 31½	34 414	1 6	11/4	1½ 12	2 16	21/ <u>6</u> 24	8 82
Size of pipeInches Least outside diameter of coil		l .	41 <u>/</u> 6 52	5 58	6 66	7 80	8 92	9 105	10 180	12 156
Lengths continuous welded COILS AND BENDS OF										NG.
Size of tube, outside diameter Least outside diameter of coi		Inch Inch	ies ies	34	36 116	236	56	874	1 13:	138
Size of tube, outside diameter Least outside diameter of coi		Inch Inch	ies ies	116	156	134	2 1	214	28/4 21/4	234
Lengths continuous brazed, 90° BENDS. EXTR.									PE.	
Diameter of pipe	Inch	ies 🏖	3 24	16 2 36 3	5 6 8	6 3	7 8 8 5	0 55 8 18 8 6	9 10 60 70	12 72 84

The radii given are for the centre of the pipe. "Centre to end" means the perpendicular distance from the centre of one end of the bent pipe to a plane passing across the other end. Standard iron pipes of sizes 4 to 8 in. are bent to radii 6 in larger than the radii in the above table; sizes 9 to 12 in. to radii 12 in larger.

wolded Solid Brawn-steel Tubes, imported by P. S. Justice & Co., Philadelphia, are made in sizes from ½ to 4½ in. external diameter varying by ½ the, and with thickness of walls from 1/16 to 11/16 in.

WEIGHT OF BRASS, COPPER, AND ZINC TUBING. Per Foot.

Thickness by Brown & Sharpe's Gauge.

Brass,	Brass, No. 17.		Brass, No. 20. Lightning-ro No. 23		
Inch. 1/4 5-16 5-16 7-16 9-11 56 27 11/4 11/4 11/4 27 27 3	Lbs	Inch. 1/6 8-16 8-16 9-6 7-16 1/4 9-16 9-8 11 1/4	Lbs. .032 .039 .063 .106 .126 .158 .189 .208 .220 .252 .284 .378 .500	Inch. 3/2 9-16 9-16 11-16 94 Zinc, 1	Lbs

LEAD PIPE IN LENGTHS OF 10 FEET.

In.	8-8 Thick.		5-16 7	ľhick.	1/4 Thick.		3-16 Thick.		
2½ 3 3½ 4 4 4½ 5	lb. 17 20 22 25 31	OZ. 0 0 0 0	lb. 14 16 18 21	OZ. 0 0 0 0	lb. 11 12 15 16 18 20	oz, 0 0 0 0 0	lb. 8 9 9 12 14	oz. 0 0 8 8	

LEAD WASTE-PIPE.

11/6	in.,	2 lbs. per foot.	1	816 in.,	4 lbs. per foot.
2		3 and 4 lbs. per foot.	į,	4 "	5, 6, and 8 lbs.
3	"	316 and 5 lbs. per foot.		416 "	6 and 8 lbs.
		5 in. 8,	10, and	12 lbs.	

LEAD AND TIN TUBING.

1/4 inch. 1/4 inch.

SHEET LEAD.

Weight per square foot, $2\frac{1}{2}$, 8, $8\frac{1}{2}$, 4, $4\frac{1}{2}$, 5, 6, 8, 9, 10 lbs. and upwards. Other weights rolled to order.

BLOCK-TIN PIPE.

36 in., 414, 614, and 8 oz. per foot. 14, " 6, 714, and 10 oz. " 36 " 8 and 10 oz. " 37 " 10 and 12 oz. "	1 in., 15, and 18 oz. per foot.
16 " 6, 716, and 10 oz. "	11/4 " 11/4 and 11/4 lbs. "
5% " 8 and 10 oz. "	116 " 2 and 216 lbs. "
3¼ " 10 and 12 oz. "	11/4 " 11/4 and 11/4 lbs. " 11/4 " 2 and 21/4 lbs. " 2 " 21/4 and 3 lbs. "

LEAD AND TIN-LINED LEAD PIPE.

(Tatham & Bros., New York.)

Calibre.	Letter.	Weight per Foot and Rod.	Thickness in 1-100th In.	Calibre.	Letter.	Weight per Foot and Rod.	Thickness in 1-100th In.
% in. "" 7-16 in. "" % in. ""	E DC C B AAA AAA E DC C B AAA AAA AAA AAA AAA AAA AAA	7 lbs. per rod 10 oz. per foot 12 " " 1 lb. " 114 " " 13 oz. " 1 lb. per rod 1 lb. per foot 1 " " 1 lb. per foot 1 " " 1 lb. " " 1 lb. per foot 1 " " 1 lb. " " 1 lb. per foot 1 " " 1 lb.	6 8 12 16 19 27 7 9 1 13 16 19 23 25 8 10 12 16 20 22 3 30	1 in. "" "" "" "" "" "" "" "" "" "" "" "" ""	E D C B A AAA A E D C C B A AAA A C C B A AAA A C C B A AAA A A A	1½ lbs. per foot 2 3.4	10 11 14 17 21 24 30 10 10 12 14 16 19 25 12 14 17 19 28 27

WEIGHT OF LEAD PIPE WHICH SHOULD BE USED FOR A GIVEN HEAD OF WATER.

(Tatham & Bros., New York.)

Head or Number	Pressure		Ca	libre and	i Weigh	t per Fo	ot.	
of Feet Fall.	per sq. inch.		% inch.	⅓ inch.	⅓ inch.	¾ inch.	1 inch.	1¼ in.
80 ft. 50 ft. 75 ft. 100 ft. 150 ft. 200 ft.	15 lbs. 25 lbs. 38 lbs. 50 lbs. 75 lbs. 100 lbs.	D C B A AA AAA	10 oz. 12 oz. 1 lb. 1¼ lbs. 1¼ lbs. 1¼ lbs.	34 lb. 1 lb. 114 lbs. 134 lbs. 2 lbs. 3 lbs.	1 lb. 114 lbs. 2 lbs. 214 lbs. 234 lbs. 314 lbs.	3 lbs.	3¼ lbs. 4 lbs. 4¾ lbs.	334 lbs. 434 lbs. 6 lbs.

To find the thickness of lead pipe required when the head of water is given. (Chadwick Lead Works).

Ruls.—Multiply the head in feet by size of pipe wanted, expressed decimally, and divide by 750; the quotient will give thickness required, in one-hundredths of an inch.

Example.—Required thickness of half-inch pipe for a head of 25 feet.

WEIGHT OF COPPER AND BRASS WIRE AND PLATES.

Brown & Sharpe's Gauge.

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No. of	Sige of	Weight of Wire per 1000 Lineal Feet.	Wire per al Feet.	Weight of Plates per Square Foot,	Plates per Foot,	No. of	Size of	Weight of Wire pe 1,000 Lineal Feet	Wire per eal Feet.	Weight of Plates per Square Foot.	Plates per Foot.
ange.	Topic	Copper.	Brass.	Copper.	Brass.	S S S S S S S S S S S S S S S S S S S		Copper.	Brass.	Copper.	Brass.
8	Inch. .46000	Lbs. 640.5	Lbe. 605.28	Lbs. 20.84	Lbs. 19.69	25	Inch. .028462	Lbs. 2.45	Lbs. 2.317	Lbs. 1.29	Lbs.
§ 8	.40964 86480	508.0 408.0	258 252	25.55 52.55 52.55	17.58	81 SS	.022571	1.94	1.888	1.15	1.8
30,	38486	819.5	301	2.5	13.90	8	.020100	1.38	1.155	<u>E</u>	8
- O	50.50	200	3. S.	13.10	12.38	88	01594	692	727	E 8	88
. 60	22942	159.8	35.55	20.00	80.00	200	.014195	.610	.576	.648	8
4.10	18194	4.85	88	3 3 3	7.79	88	.011257	£ 88	.362	5.5. 5.10	¥. 84
91	16202	85 8.	8:	7.84	6.93	88	.010025	.804	782	\$	2. 2. 2. 3.
- oc	12849	2.00	88	0.00	20.20	38	007950	191	181	9.08	88
a	.11448	80.04	87.44	5.18	4.90	8	080200	.152	143	.321	8
2;	.10189	25.55 52.55	88	4.62	4.36	35 8	.006304	.120	.114	88	0,20
75	000042	12.5	8.8 8.8	. «	9.00	88	00000	0220	2000	8.00	25.6
200	021961	15.65	14.81	88	3.08	36	.004453	0000	.0567	808	191
7	.064084	12.4	11.75	8.8	2.74	38	.003965	.0476	.0450	981.	27.
2	.057068	88.	38.0	80.00	2.44	33	.008531	.0875	.0357	.160	.151
2;	060820	8 5.6	2.20	88	20.18	40	.003144	0680	.0283	. 142	.18
2	00000	38	. .	38	2	Specific g	Specific gravity	8.880	8.86	8.696	8.218
28	082890	88	88	8.4	1.54	Wolcht	Weight now on his De	***	504 16	K40 &	K10 A

WEIGHT OF BOUND BOLT COPPER. Per Foot.

Inches.	Pounds.	Inches.	Pounds.	Inches.	Pounds.
36 115 20 215 215 215 215 215 215 215 215 215 215	.425 .756 1.18 1.70 2.31	1 114 114 186 114	3.02 3.88 4.72 5.72 6.81	156 184 176 2	7.99 9.27 10.64 12.10

WEIGHT OF SHEET AND BAR BRASS,

Thickness,	Sheets	Square	Round	Thickness,	Sheets	Square	Round
Side or	per	Bars 1	Bars 1	Side or	per	Bars 1	Bars 1
Diam.	sq. ft.	ft.long.	ft.long,	Diam.	sq. ft.	ft. long.	ft.long.
Inches. 1-16 1-6 8-16 1-6 7-16 1-6 1-6 1-16 1-16 1-16 1-16	\$.72 5.45 8.17 10 90 13.62 16.35 19.07 21.80 24.52 27.25 29.97 82.70 35.42 38.15	.014 .056 .129 .227 .355 .510 .695 .907 1.15 1.42 1.72 2.04 2.40 2.78 8.19	.011 .045 .100 .178 .278 .401 .545 .712 .902 1.11 1.85 1.60 1.88 2.18 2.50	Inches. 1 1-16 11/6 11/6 11/6 11/6 11/6 11/7-16 11/6 11/6 11/1-16 11/6 11/6 11/6 11/	46.82 49.05 51.77 54.50 57.22 59.95 62.67 65.40 68.13 70.85 73.57 76.30 79.02 81.75	4.10 4.59 5.12 5.67 6.26 6.86 7.80 8.16 8.86 9.59 10.84 11.198 11.98 12.76 18.68	8,23 8,61 4,02 4,45 4,91 5,89 5,89 6,41 6,95 7,53 8,73 9,86 10,01

COMPOSITION OF VARIOUS GRADES OF ROLLED BRASS, ETC.

Trade Name.	Copper	Zinc.	Tin.	Lead.	Nickel.
Common high brass	61.5	38.5			
Yellow metal	60	40			
Cartridge brass	609/8	833/8		••••	
Clock brass		40 831/6 20 40		114	
Drill rod.	60	40		116 116 to 2	l
Spring brass	1 66%	831/6 201/6	11/6		
18 per cent German silver	611/2	201/2	1	l	18

The above table was furnished by the superintendent of a mill in Connecticut in 1894. He says: While each mill has its own proportions for various mixtures, depending upon the purposes for which the product is intended, the figures given are about the average standard. Thus, between cartridge trass with 354 per cent zinc and common high brass with 364 per cent zinc, there are any number of different mixtures known generally as "high brass," or specifically as "spinning brass," "drawing brass," etc., wherein the amount of zinc is dependent upon the amount of zero is dependent upon the amount of zero is dependent upon the amount of sero sero.

AMERICAN STANDARD SIZES OF DROP-SHOT.

	Diameter.	No. of Shot to the oz.		Diameter.	No. of Shot to the oz.		Diam- eter.	No. of Shot to the og.
Fine Dust. Dust No. 12 " 11 " 10 " 9	8-100" 4-100 5-100 6-100 Trap Shot 7-100" Trap Shot 8-100"	848	" 6 " 5 " 4	Trap Shot 9-100'' Trap Shot 10-100'' 11-100 12-100 13-100 14-100	399	No. 2 " 1 " B " BB. " BBB " T " FT " FF	15-100" 16-100 17-100 18-100 19-100 20-100 21-100 22-100 23-100	86 71 59 50 42 36 31 27

COMPRESSED BUCK-SHOT.

	Diameter.	No. of Balls to the lb.		Diameter.	No. of Balls to the lb.
No. 8		282	No. 00 " 000 Balls	84-160" :6-100 88-100 44-100	115 98 85 50

SCREW-THREADS, SELLERS OR U. S. STANDARD.

In 1864 a committee of the Franklin Institute recommended the adoption of the system of screw-threads and bolts which was devised by Mr. William Sellers, of Philadelphia. This same system was subsequently adopted as the standard by both the Army and Navy Departments of the United States, and by the Master Mechanics' and Master Car Builders' Associations, so that it may now be regarded, and in fact is called, the United States Standard.

The rule given by Mr. Sellers for proportioning the thread is as follows: Divide the pitch, or, what is the same thing, the side of the thread, into eight equal parts; take off one part from the top and fill in one part in the bottom of the thread; then the fiat top and bottom will equal one eighth of the pitch, the wearing surface will be three quarters of the pitch, and the diameter of screw at bottom of the thread will be expressed by the for mula

diameter of bolt $-\frac{1.299}{\text{no. threads per inch}}$

For a sharp V thread with angle of 60° the formula is

diameter of bolt $-\frac{1.733}{\text{no. of threads per inch}}$

The angle of the thread in the Sellers system is 60°. In the Whitworth or English system it is 55°, and the point and root of the thread are rounded.

Screw-Threads, United States Standard.

Diam.	Pitch.	Diam.	Pitch.	Diam.	Pitch.	Diam.	Pitch.	Diam.	Pitch.
5-16 58 7-16 14 9-16 9-16 11-16	20 18 16 14 13 12 11	18-16 15-16 15-16 1 1-16 11/8	10 10 9 9 8 7	11/4 1 5-16 13/6 11/6 11/6 13/4 13/4	7 6 6 5 5 5	1 15-16 2 214 2 5-16 246 219	5 414 414 4 4 4	2 13-16 3 814 3 5-16 314 4	814 814 814 814 814

Screw-Threads, Whitworth (English) Standard.

Diam.	Pitch.	Diam.	Pitch.	Diam.	Pitch.	Diam.	Pitch.	Diam.	Pitch.
5-16 36 7-16 1/2 9-16	20 18 16 14 12 12	56 11-16 34 13-16 76 15-16	11 11 10 10 9	1 11/6 11/4 13/6 11/6	8 7 6 6 5	134 176 2 214 214 234	5 41/6 41/8 4 4 31/6	3 314 314 394 4	314 314 314 3 3 3

U. S. OR SELLERS SYSTEM OF SCREW-THREADS.

В	OLT	S AN	D TH	REAL	s.	HE	X. NUT	SAND	HEA	DS.	÷.
Diam. of Bolt.	Threads per Inch.	Diam. of Root of Thread.	Width of Flat.	Area of Bolt Body in Sq. Inches.	Area at Root of Thread in Sq. Inches.	Short Diam., Rough.	Short Diam., Finish.	Long Diam., Rough.	Thickness, Rough.	Thickness, Finish.	Long Diam. Sq Nuts Rough.
Ins.		Ins.	Ins.			Ins.	Ins.	Ins.	Ins.	Ins.	Ins.
14 16 16 16 16 16 16 16 16 16 16 16 16 16	16 14 13 12 11 10 9 8 7 7 6 6 5 16 5 4 4 4 3 4 4	. 185 . 240 . 294 . 344 . 400 . 454 . 450 . 620 . 731 . 1. 665 . 1. 189 . 1. 491 . 1. 389 . 1. 491 . 1. 1962 . 2. 176 . 2. 176 . 2. 176 . 3. 3. 3. 3. 3. 3. 3. 3. 3. 3. 3. 3. 3.		077-110 150 1969 307-13-19-19-19-19-19-19-19-19-19-19-19-19-19-	.027 .045 .068 .033 .020 .020 .020 .020 .020 .020 .020	19-82 11-16 25-32 76 31-92 11-16 114 1-7-16 114 1-7-16 2 2 3-16 2 2 3-16 2 2 3-16 2 3 1 5 2 3 1 5 5 5 5 5 5 5 5 6 6 6 6 6 6 7 7 7 4 8 8 8 6 6 7 7 7 4 8 8 8 6 6 7 7 7 4 8 8 8 6 6 7 7 7 4 8 8 8 6 6 7 7 7 7 8 8 8 8 6 6 7 7 7 7 8 8 8 8	7-16 17-32 56 23-32 13-16 29-32 1 1 3-16 136 1 9-16	37-64 11-16 51-64 9-10 1 17-32 1 7-162 1 21-32 2 3-32 2 5-16 2 17-32 2 31-32 3 3-16 3 13-32 3 5-16 3 13-32 3 5-16 3 13-32 5 5-16 3 13-32 7 9-16 7 3-32 7 9-16 7 31-32 8 27-32 9 9 -82 9 9 9 9 9 9	14-16-16-16-16-16-16-16-16-16-16-16-16-16-	3-16 3-16 3-16 3-16 13-16 13-16 13-16 13-16 1 3-16 1 3-16 1 1-16 2 3-16 2 3-16 2 3-16 2 3-16 2 3-16 2 3-16 3 3-16 3 11-16 3 11-16 3 11-16 4 3-16 4 3-16 4 3-16 4 3-16 4 3-16 4 3-16	7-10 10-1 63-6 1 7-64 1 15-6 1 23-6 1 126 2 1-32 2 19-6 2 2 1-32 2 19-6 3 3-32 3 23-6 3 3-32 3 23-6 4 5-32 4 27-6 4 5-32 4 27-6 6 6 17-3: 7 1-16 8 41-6 93-4 10 49-6 11 23-6 11 23-6 11 23-6

LIMIT GAUGES FOR IRON FOR SCREW THREADS.

In adopting the Sellers, or Franklin Institute, or United States Standard, as it is variously called, a difficulty arose from the fact that it is the habit of iron manufacturers to make iron over-size, and as there are no over-size.

screws in the Sellers system, if iron is too large it is necessary to cut it away with the dies. So great is this difficulty, that the practice of making taps and dies over-size has become very general. If the Sellers system is adopted it is essential that iron should be obtained of the correct size, or very nearly so. Of course no high degree of precision is possible in rolling iron, and when exact sizes were demanded, the question arose how much allowable variationithers should be from the true size. It was proposed to make limit-gauges for inspecting iron with two openings, one larger and the other smaller than the standard size, and then specify that the iron should enter the large end and not enter the small one. The following table of dimensions for the limit-gauges was commended by the Master Car-Builders' Association and adopted by letter ballot in 1883.

Size of Iron.	Size of Large End of Gauge.	Size of Small End of Gauge.	Differ- ence.	Size of Iron.	Size of Large End of Gauge.	Size of Small End of Gauge.	Differ- ence.
14 in. 5-16 36 7-16 14 9-16	0.2550 0.8180 0.8810 0.4440 0.5070 0.5700	0.2450 0.3070 0.8690 0.4810 0.4980 0.5550	0.010 0.011 0.012 9.013 0.014 0.015	% in. % in. % in. 11/6 11/4	0.6330 0.7585 0.8840 1.0095 1.1850 1.2605	0.6170 0.7415 0.8660 0.9905 1.1150 1.2895	0.016 0.017 0.018 0.019 0.020 0.021

Caliper gauges with the above dimensions, and standard reference gauges for testing them, are made by The Pratt & Whitney Co.

THE MAXIMUM VARIATION IN SIZE OF BOUGH IRON FOR U. S. STANDARD BOLTS.

Am. Mach., May 12, 1892.

By the adoption of the Sellers or U. S. Standard thread taps and dies keep their size much longer in use when flatted in accordance with this system than when made sharp "V," though it has been found advisable in practice in most cases to make the taps of somewhat larger outside diameter than the nominal size, thus carrying the threads further towards the V-shape and giving corresponding clearance to the tops of the threads when in the nuts or tapped holes.

nuts or tapped holes.

Makers of taps and dies often have calls for taps and dies, U. S. Standard,

" for rough iron."

An examination of rough iron will show that much of it is rolled out of round to an amount exceeding the limit of variation in size allowed.

In view of this it may be desirable to know what the extreme variation in iron may be, consistent with the maintenance of U. S. Standard threads, i.e., threads which are standard when measured upon the angles, the only place where it seems advisable to have them fit closely. Mr. Chas. A. Bauer, the general manager of the Warder, Bushnell & Glessner Co., at Springfield, Ohio, in 1834 adopted a plan which may be stated as follows; All bolts, whether cut from rough or finished stock, are standard size at the bottom and at the sides or angles of the threads, the variation for fit of the nut and allowance for wear of taps being made in the machine taps. Nuts are punched with holes of such size as to give 85 per cent of a full thread, experience showing that the metal of wrought nuts will then crowd into the threads of the taps sufficiently to give practically a full thread, while if punched smaller some of the metal will be cut out by the tap at the bottom of the threads, which is of course undesirable. Machine taps are made enough larger than the nominal to bring the tops of the threads up full (sharp), plus the amount allowed for fit and wear of taps. This allows the iron to be enough above the nominal diameter to bring the threads up full (sharp) at top, while if i is small the only effect is to give a fiat at top of threads; neither condition affecting the actual size of the thread at the point at which its is mended to bear. Limit gauges are furnished to the mills, by which the iron is rolled the maximum size being shown in the third column of the table. The minimum diameter is not given, the tendency in rolling being mearly always to exceed the nominal diameter.

In making the taps the threaded portion is turned to the size given in the eighth column of the table, which gives 6 to 7 thousandths of an inch allowance for its and wear of tap. Just above the threaded portion of the tap a

place is turned to the size given in the ninth column, these sizes being the same as those of the regular U. S. Standard bolt, at the bottom of the thread, plus the amount allowed for fit and wear of tap; or, in other words, d' = U. S. Standard d + (D' - D). Sauges like the one in the cut, Fig. 72, are furnished for this sizing. In finishing the threads of the tap a tool



F1g. 72.

is used which has a removable cutter finished accurately to gauge by grinding, this tool being correct U. S. Standard as to angle, and flat at the point. It is fed in and the threads chased until the flat point just touches the portion of the tap which has been turned to size d'. Care having been taken with the form of the tool, with its grinding on the top face (a fixture being provided for this to insure its being ground properly), and also with the setting of the tool properly in the lathe, the result is that the threads of the tap are correctly sized without further attention.

It is evident that one of the points of advantage of the Sellers system is sacrificed, i.e., instead of the taps being fiatted at the top of the threads they are sharp, and are consequently not so durable as they otherwise would be; but practically this disadvantage is not found to be serious, and is far overbalanced by the greater ease of getting iron within the prescribed limits; while any rough bolt when reduced in size at the top of the threada, by filing or otherwise, will fit a hole tapped with the U.S. Standard hand taps, thus affording proof that the two kinds of bolts or screws made for the two different kinds of work are practically interchangeable. By this system \(\frac{1}{2} \) iron can be .005" smaller or .0108" larger than the nominal diameter, or, in other words, it may have a total variation of .0158", while \(\frac{1}{2} \) '' iron can be .005" smaller or .0308" larger than nominal—a total variation of .0414"—and within these limits it is found practicable to procure the iron.

STANDARD SIZES OF SCHEW-THREADS FOR BOLTS
AND TAPS.
(CMAR A RAUBE)

				(CHAB.	A. DA	EE.)			
1	2	8	4	5	6	7	8	9	10
4	2	D	d	h	f	D' - D	D'	d'	H
5-16 96 7-16 14 9-16 9-16	20 18 16 14 18 19 11 10 9	Inches2608 .2508 .3245 .5885 .4530 .5166 .5805 .6447 .7717 .8991 1.0271	Inches .1855 .2408 .2988 .8447 .4000 .4548 .5069 .6201 .7807 .8376	Inches. .0379 .0421 .0474 .0541 .0562 .0631 .0689 .0758 .0649	Inches. .0062 .0070 .0078 .0089 .0096 .0104 .0114 .0125 .0139 .0156	.006 .006 .006 .006 .006 .007 .007 .007	Inches2668 .3305 .3945 .4590 .5223 .6517 .7787 .9061 1.0341	Inches. .1915 .2468 .2998 .3507 .4060 .4618 .5189 .6271 .7877 .8446	Inches. 2024 2589 3189 3670 4236 4803 5846 6499 7680 8731
114 114	77	1.1559 1.2809	.9894 1.0644	.1088 .1088	.0179	.007	1.1629 1.2879	.9464 1.0714	.9789 1.1089

A = nominal diameter of bolt.

D =actual diameter of bolt.

d =diameter of bolt at bottom of thread.

= number of threads per inch.

f =flat of bottom of thread.

h = depth of thread.

D' and d' = diameters of tap.

H =hole in nut before tapping.

$$D = A + \frac{.2165}{n},$$

$$d = A - \frac{1.20904}{n},$$

$$h = \frac{.7877}{n} = \frac{D - d}{2},$$

$$f = \frac{.125}{n},$$

$$H = D' - \frac{1.288}{n} = D' - .85(2h)$$

STANDARD SET-SCREWS AND CAP-SCREWS.

American, Hartford, and Worcester Machine-Screw Companies. (Compiled by W. S. Dix.)

Diameter of Screw Threads per Inch Size of Tap Drill*	(A) 16 40 No. 43	(B) 3-16 24 No. 30	(C) 14 20 No. 5	5-16 18 17-64	(E) 36 16 21-64	(F) 7-16 14 36	(G) 12 12 27-64
Diameter of Screw Threads per Inch Size of Tap Drill*	(H) 9-16 12 31-64	(I) 56 11 17–32	(J) 34 10 21–32	(K) 76 9 49-64	(L) 1 8 76	(M) 13/8 7 63-64	(N) 114 116

A	Set Scre	ws.	Hex. I	Head Ca	p-screws.	Sq. H	ead Ca	p-screws.
Short Diam. of Head	Long Diam. of Head	Lengths (under Head).	Short Diam, of Head.	Long Diam, of Head.	Lengths (under Head).	Short Diam. of Head.	Long Diam. of Head.	Lengths (under Head).
(C) 14 (D) 5-16 (E) 38 (F) 7-16 (G) 14 (H) 9-16 (I) 58 (K) 78 (K) 78 (M) 114 (N) 114	.71 .80 .89 1.06 1.24 1.42 1.60	% to 3 % to 4 % to 4 % 1 to 4 % 1 to 5 1 % to 5 1 % to 5 %	7-16 16 9-16 56 34 13-16 78 1 114 138 134	.51 .58 .65 .79 .87 .94 1.01 1.15 1.30 1.45 1.59 1.73	34 to 3 34 to 334 34 to 334 34 to 334 34 to 434 1 to 434 1 to 434 114 to 5 2 to 5 2 to 5	9-16 56 11-16	.53 .62 .71 .80 .89 .98 1.06 1.24 1.60 1.77 1.95 2.13	34 to 3 34 to 334 34 to 334 34 to 334 34 to 4 34 to 4 34 to 4 41 to 4 42 to 4 43 to 4 44 to 5 45 to 5 46 to 5 56 to 5 56 to 5

	Filister Head screws.	Flat Head	Cap-screws.		head Cap- ews.
Diam. of Head.	Lengths (under Head).	Diam. of Head.	Lengths (including Head).	Diam. of Head.	Lengths (under Head).
(A) 3-16 (B) 14 (C) 36 (D) 7-16 (E) 9-16 (F) 56 (G) 34 (H) 13-16 (i) 76 (J) 1 (K) 1½6 (L) 1½4	\$4 to 214 \$4 to 294 \$4 to 314 \$4 to 314 \$4 to 314 \$4 to 314 \$4 to 414 \$1 to 414 \$1 to 414 \$1 to 494 \$1 to 45 \$2 to 5	15-32 56 15-32 56 34 13-16 76 1 11/6 13/8	% to 1% % to 2 % to 3 1 to 3 1	7-82 (.225) 5-16 7-16 9-16 56 34 18-16 15-16	% to 1% % to 2% % to 2% % to 2% % to 2% % % to 2% % % to 2% % % to 3% % to 3% % to 3 % 1½ to 3 % 1% to 3 %

^{*} For cast iron. For numbers of twist-drills see p. 29.

Threads are U. S. Standard. Cap-screws are threaded 34 length up to and including 1"diam. × 4" long, and 14 length above. Lengths increase by 14" each regular size between the limits given. Lengths of heads, except flat and button, equal diam. of screws.

The angle of the cone of the flat-head screw is 76°, the sides making angles of 52° with the top.

STANDARD MACHINE SCREWS.

No.	Threads per	Diam. of	Diam.	Diam. of	Diam. of Filister	Len	the.
но.	Inch.	Body.	Head.	Round Head.	Head.	From	То
2	56	.0842	.1681	.1544	.1882	8-16	16
3	48	.0973	.1894	.1786	.1545	8-16	57
4	32, 36, 40	.1105	.2158	.2028	.1747	8-16	• • • • • • • • • • • • • • • • • • • •
5	82, 86, 40	.1236	.2421	.2270	.1985	8-16	
6	80, 82	.1368	.2684	.2512	.2175	3-16	1
7	30, 32	.1500	.2947	.2754	.2892	3/4	11/6
23456789	30, 32	.1631	.8210	.2936	.2610	14	11/4 11/4
9	24, 30, 32	.1763	.8474	.3238	.2805	34	136 117 137 2
10	24, 30, 32	.1894	.3737	.3480	.3035	3/4	13/2
12	20, 24	.2158	.4263	.3922	.3445	36	13/4
14	20, 24	.2421	.4790	.4364	.3885	38	2
16	16, 18, 20	.2684	.5816	.4866	.4300	36	21/4
18	16, 18	.2947	.5842	.5248	.4710	16	21/4 21/4 23/4 39/4
20	16, 18	.3210	.6368	.5690	.5200	3/6	23/4
22	16, 18	.3474	.6894	.6106	.5557	1/2	8
24	14, 16	.3737	.7420	.6522	.6005	36	8
26 28	14, 16	.4000	.7420	.6938	.6425	34	8
28	14, 16	.4268	.7946	.7854	.6920	7/8	3 3 8
30	14, 16	.4520	.8473	.7770	.7240	1	8

Lengths vary by 16ths from 3-16 to 1/2, by 5ths from 1/2 to 1/2, by 4ths from 1/2 to 3.

SIZES AND WEIGHTS OF SQUARE AND HEXAGONAL NUTS.

United States Standard Sizes. Chamfered and trimmed. Punched to suit U. S. Standard Taps.

tolt.			Hole,	. Sq.	um.	Squ	are.	Hexa	gon.
Diam. of Bolt.	Width.	Thickness.	Diam, of B	Long Diam. Nuts.	Long Diam. Hex. Nuts.	No. in 100 Ibs.	Wt. each in lbs.	No. in 100 lbs.	Wt. each
56 7-16 1-6 9-16 9-16 9-16 1-1	56 13-16 3-16	\$6-16 \$6-16 \$6-16 \$7-16 \$1-16 \$115 \$115 \$115 \$115 \$115 \$115 \$115 \$1	13-64 14 19-64 11-32 25-64 29-64 33-64 39-64 47-64 59-64 1 1-16 1 5-32 1 9-32 1 13-32 114 2 3-16 2 3-16 2 7-16	11-16 13-16 11-16 11-16 11-18-16 11-18-16 11-18-16 2 13-16 2 13-16 2 13-16 2 13-16 31-16 31-16 31-16 31-16 4 15-16 51-16 6 6 11-16	9-16 11-16 13-16 78 1 11-6 13-6 13-6 13-6 2 1-16 2 5-16 2 5-16 2 5-16 39-8 39-8 39-8 4 1-16 44-6 4 15-16 5 5-16	7270 4700 4700 2350 1630 1120 640 380 280 170 130 96 70 130 96 70 130 96 70 130 96 70 130 96 70 130 96 70 71 71 71 71 71 71 71 71 71 71 71 71 71	.0138 .0231 .0426 .0613 .0893 .1124 .156 .263 .357 .588 .769 1.04 1.43 2.27 2.27 2.27 2.94 4.35 8.33 4.35 8.33 11.11	7615 5200 3000 2000 1430 1100 450 309 216 148 111 85 68 56 40 37 29 21 11 11 11 11 11 11 11 11 11 11 11 11	.013: .019: .033: .050 .070 .091 .135 .324 .463 .676 .901 1.18 1.47 2.50 2.70 2.50 3.45 4.76 6.67 9.09 11.76

WEIGHT OF 100 BOLTS WITH SQUARE HEADS, (Hoopes & Townsend.)

Inches.	1/4	5/16	8/8	2/16	1/3	9/16	2/8	%	%	1	11/8	14	13%	11/6	13%
Length.	lbs.	10	lbs.		lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.
11/2 in.	3.9	9	9.7			26.0	0	58.0		:		:			
	4.6	22.20	11.3			29.0	C3	63.2	97.7	145	:				
11 5/6	5.4	00	12.9			35 5	-	69.0	105.6	155	:	:			
3	6.5	G	14.5			85.4	00	75.9	113.8	163	240	309	350		
375 "	6.9	5	16.1			38.7	10	81.4	122.0	174	253	355	370		
	7.6	Ξ	17.7			42.0	2-	87.6	130.2	185	267	342	830	520	800
., 5/4	8.3	35	19.2		36.2	45.3	0	93.8	138.4	196	281	359	410		833
2	9.0	13.7	20.7			48.6	-	100.0	146.6	202	295	876	430		866
: 5/4	9.7	14.8	22.2	31.0	41.8	51.9	03	106.1	154.9	218	309	894	450		006
,, 9	10.4	15.9	23.7	33,1	44.6	55.2	78.4	119.2	163.2	553	85	412	470		934
,, 5/19	11.1	17.0	25.2	35.2	47.4	58.5	77.6	118.3	171.5	240	337	430	490		896
	11.8	18.1	26.7	37.3	50.5	61.8	81.8	194.4	179.8	251	351	448	510		1000
., 962	12.5	19.2	28.5	39.4	53.1	65.1	86.0	130.5	187.1	262	365	466	530		1036
. 80	13.2	20.3	29.7	41.5	56.0	68.5	0.06	136.6	195.4	273	379	484	550		1070
,, 6	***	:	33.1	45.7	61.5	75.2	-	148.8	212.0	582	407	518	590		1138
10 11	:	:	36.5	49.9	67.0	81.9	na	161.0	229.0	317	485	552	630		1206
11 ,,	:	:	40.0	54.1	72.5	88	PO.	178.2	246.0	333	463	586	670		1974
15 "	14.64	:	43.5	58.3	78.0	95.5	-	184.4	263.0	361	491	620	710		1842
13 61	:		:	:	83.5	102.3	131.2	196.6	280.0	383	519	655	751		1410
14	:	:		:	0.68	109.1	10	208.8	597 0	405	547	069	793	-	1478
12				***	94.5	116.0	0	221.0	314.0	427	575	7355	883	-	1548
,, 91	++++	:	::	::	100.0	123.0	156.5	233 2	331.0	449	603	2.60	877	-	1616
1, 21	:::	1	::	:	105.5	130.0	165.0	245.4	348.0	471	631	735	919	_	1684
18	:	:	:	:	111.0	187.0	173.5	257.6	365.0	493	629	830	961	-	1759
119 **			:	:	116.5	144.0	185.0	269.8	88.5.0	515	687	865	1003	-	1890
30 ,,	***		:	:	122.0	151.0	190.5	282.0	399.0	587	715	900	1045	-	1888
31 15		:	:				198.0	294.0	416.0	559	743	965	1080	-	1956
35 "	1	:					206.0	306.0	437.0	581	7771	1030	1199		1006
53 **	:	:	:	:			215.0	318.0	454.0	603	299	1095	177	-	6006
54 "	:						0.166	330.0	470 0	625	897	1160	1918	595	9160
25											200	1995	1988	15.75	3000
											4 74 74 74	- Section			No.

TRACK BOLTS.

With United States Standard Hexagon Nuts.

Rails used.	Bolts.	Nuts.	No. in Keg, 200 lbs.	Kegs per Mile.
45 to 85 lbs	4 × 414 4 × 4 4 × 894 4 × 814 4 × 814		230 240 254 260 268 288	6.8 6. 5.7 5.5 5.4 5.1
90 to 40 lbs	6 × 8)4	1 1-16	875	4.
	6 × 8	1 1-16	410	8.7
	6 × 294	1 1-16	485	8.8
	6 × 2)4	1 1-16	465	3.1
90 to 80 lbs	16 × 8	76	715	2.
	16 × 216	16	760	2.
	16 × 214	18	860	2.
	16 × 2	78	860	2.

CONE-HEAD BOILER RIVETS, WEIGHT PER 100.

(Hoopes & Townsend.)

Diam., in., Scant.	1/2	9/16	5/8	11/16	94	13/16	36	1	136*	134
Length.	lbs.	lbs.	lbs.	lbs.	lbs.	Ibs.	lbs.	Ibs.	lbs.	Ibs
34 inch	8,75	13.7	16.20		7-77				1	
34 "	9,85	14.4	17,22	1000	200					2
1 "	10.00	15.2	18,25	21.70	26.55					
114 "	10.70	16.0	19.28	28.10	28,00	I COLD		1000		0
114 "	11.40	16.8	20.31	24.50	29.45	37.0	46	60	1 30	
186 **	12.10	17.6	21.34	25.90	30.90	38.6	48	63	95	
116 "	12,80	18.4	22,37	27.30	32,35	40.2	50	65	98	13
198 4 198 4 198 4 134 4 176 4	13,50	19.2	23.40	28.70	33.80	41.9	52	67	101	13
134 "	14.20	20.0	24.43	30.10	35.25	43.5	54	69	104	14
176 "	14.90	20.8	25.46	31.50	36.70	45.2	56	71	107	14
2	15.60	21.6	26,49	33.90	38.15	47.0	58	74	110	14
21/8 "	16.30	22.4	27.52	34.80	39.60	48.7	60	77	114	15
214 "	17.00	23.2	28.55	35.70	41.05	50.3	62	80	118	35
236 "	17.70	24.0	29.58	37.10	42.50	51.9	64	88	121	16
214 "	18.40	24.8	30.61	38.50	43.95	53.5	66	-86	124	16
256 4	19.10	25.6	31.64	39.90	45.40	55.1	68	89	127	16
934 " 976 "	19,80	26.4	32.67	41.30	46.85	56.8	70	92	130	17
976 "	20.50	27.2	33,70	42.70	48.30	58.4	72	95	133	17
3 11	21.20	28.0	34.73	44.10	49.75	60.0	74	98	137	18
314 11	22,60	29.7	36.79	46.90	52.65	63.8	78	103	144	18
316 "	24.00	31 5	38.85	49.70	55.55	66.5	82	108	151	19
314 " 834 "	25.40	33.3	40.91	52,50	58,45	69.8	86	113	158	20
4 "	26.80	35.2	42.97	55,30	61.35	73.0	90	118	165	21
414 "	28, 20	36.9	45.03	58,10	64.25	76.8	94	124	172	22
416 4	29,60	38.6	47.09	60,90	67,15	79.5	98	130	179	92
414 " 416 " 494 "	31.00	40.3	49.15	63,70	70.05	82.8	102	136	186	23
5 "	32.40	42.0	51.21	66,50	72.95	86.0	106	142	193	24
514 14	33.80	43.7	53.27	69.20	75.85	89.3	110	148	200	25
514 " 516 " 534 "	35.20	45.4	55.33	72,00	78.75	92.5	114	154	206	26
534 54	36.60	47.1	57.39	74.80	81.65	95.7	118	160	212	27
6 "	38.00	48.8	59.45	77.60	84.55	99.0	122	166	218	28
616 "	40.80	52.0	68.57	83,30	90.35	105.5	130	177	231	29
7 "	43.60	55.2	67.69	88.90	96.15	112.0	138	188	245	31
Teads	5.50	8.40	11.50	13.20	18.00	23.0	29:0	38.0	56.0	77.

* These two sizes are calculated for exact diameter. Rivets with button heads weigh approximately the same as cone-head rivets.

TURNBUCK LES.

(Cleveland City Forge and Iron Co.)

Standard sizes made with right and left threads. D = outside diameter



of screw. A = length in clear between heads = 6 ins. for all sizes. B = length of tapped heads = $1\frac{1}{2}D$ nearly. C = 6 ins. +3D nearly.

SIZES OF WASHERS.

Diameter in inches.	Size of Hole, in inches.	Thickness, Birmingham Wire-gauge.	Bolt in inches.	No. in 100 lbs.
11/2 11/2 11/2 11/2 11/2 12/4 2 21/4 23/4 33	5-16 96 7-16 9-16 9-16 9-16 11-16 13-16 31-32 146 144 144	No. 16 10 11 11 11 11 11 11 11 11 11 11 11 11	5-16 5-16 5-16 5-16 5-16 1-16 1-16 1-16	29,300 18,000 7,600 8,300 9,180 2,350 1,680 1,140 580 470 380 360

TRACK SPIKES.

Rails used.	Spikes.	Number in Keg, 200 lbs.	Kegs per Mile, Ties 24 in. between Centres.	
45 to 85 40 ° 52 35 ° 40 24 ° 35 24 ° 30 18 ° 24 16 ° 20 14 ° 16 8 ° 10	514 × 9-16 5 × 9-16 5 × 14 414 × 7-16 4 × 7-16 4 × 7-16 814 × 34 814 × 34 214 × 36 214 × 36	880 400 490 550 735 820 1250 1350 1550 2240	20 27 23 20 15 13 9 8 7	

STREET BAILWAY SPIKES.

Spikes.	Number in Keg, 200 lbs.	Kegs per Mile, Ties 24 in. between Centres.	
5½ × 9-16	400	80	
5 × ½	575	19	
4½ × 7-16	800	18	

BOAT SPIKES. Number in Keg of 200 lbs.

Length.	34	5–16	%	36
4 inch. 5 " 6 " 7 " 8 " 9 " 10 "	2975 2050 1825	1280 1175 990 880	940 800 650 600 525 475	450 875 835 800 275

WROUGHT SPIKES. Number of Nails in Keg of 150 Pounds.

Size.	14 in.	5-16 in.	¾ in.	7–16 in.	⅓ in.
3 inches 3½ 4 4½ 4 5 4 6 6 8 4 9 8 10 4 11 4	2250 1890 1650 1464 1880 1292 1161	1208 1185 1064 930 868 669 635 578	742 570 483 455 424 391	445 884 800 270 249 236	306 256 240 222 203 180

WIRE SPIKES.

Size.	Approx. Size Ap. No. of Wire Nails. in 1 lb.	Size.	Approx. Size Ap. No. of Wire Nails. in 1 lb.
10d Spike 16d " 20d " 30d " 40d " 50d "	814 " " 6 85 4 " " 5 26 414 " 4 20 5 " 8 15	60d Spike 61/2 in 7 8 9	6 in. No. 1 10 61/2 " " 1 9 7 " " 0 7 8 " " 00 5 9 " " 00 .41/2

LENGTH AND NUMBER OF CUT NAILS TO THE POUND.

Size.	Length.	Common.	Olinch.	Fence.	Finishing.	Fine.	Barrel.	Casing.	Brads.	Tobacco.	Cut Spikes.
94 36 36 31 31 41 51 51 61 71 84 101 124 1161 201 201 301 401 501 501 501 501 501 501 501 5	34 in. 1114 22 24 22 24 23 38 34 44 44 55 56	800 480 288 200 168 124 88 70 58 44 23 18 114 10 8	95 74 62 53 46 42 38 83 20	84 64 48 36 30 24 20 16	1100 720 523 410 268 188 146 130 102 76 62 54	1000 760 368	800 500 376 224 180	398 224 128 110 91 71 54 40 83 27	126 98 75 65 55 57	130 96 82 68	28 22 141 121 91 8 6

SIZES, LENGTH, AND NUMBER TO THE POUND OF STANDARD STEEL WIRE NAILS.

(John A. Roebling's Sons Co.)

-	ezig	22 22 22 22 22 22 22 22 22 22 22 22 22
th, inches.	Leng	22 7 7 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
Spikes.	Wire	2 888 555 5
*30	niniJ	1780 1780 1800 1900
*000	RdoT	2000 20 20 20 20 20 20 20 20 20 20 20 20
gje,	upus	522821
ed Roofing.	Barb	2.64.1 2.65.1 2.65.1 2.65.1 3.
·3u	Slati	200 200 1450 1450 1450 1450 1450 1450 1450 14
ed Oval	Невуу.	\$25.55.52.25.88.88.4.25.25.25.25.25.25.25.25.25.25.25.25.25.
Barbed Head Nail		242888822482255
ring Brads.	FJOOL	: ::::::::::::::::::::::::::::::::::::
ng, and looth and rbed Box,	ms	281 282 283 283 283 283 283 283 283 283 283
Barrel.		15000 10000 10000 15000
	Fine	780
Smooth and Barbed Finishing.		155 885 885 885 128 128 128 128 128 128 128 128 128 128
Fence.		34488888888
Clinch.		::0:9::2:2:2:2:2:2:2:2:2:2:2:2:2:2:2:2:2
ed Common.	Barb	
mon Nails. I Brads.	Соти	62 18 18 18 18 18 18 18 18 18 18 18 18 18
th, inches.	gne-J	22 THE SECTION
•	sezi3	Section of the sectio

38. lbs. of 4d Common, or 38. lbs. of 3d Common, will lay 1000 shingles.

APPROXIMATE NUMBER OF WIRE NAILS PER POUND.

	=	ESSAR
	11	Acres 28.28.28.29.29.29.29.29.29.29.29.29.29.29.29.29.
	2	wers of 1200.00
	0	an average only ed the point or thick-headed
	∞	rs are
	20	umbers and he and he and he
	0	nn n. nsion sa
	0	8
	\$	20 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	•	99999888888888888888888888888888888888
	8	113 11 115 116 117 117 117 117 117 117 117 117 117
a l	•	4313888878888878888888888888888888888888
nche	32	37.8883328888834488
म् पु	C5	8 2 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
Length, inches.	*	888741588111188811
	*	288488288338838288888888888888888888888
		• • •
	72	84488883888888888888888888888888888888
•	-	28 28 28 28 28 28 28 28 28 28 28 28 28 2
	*	200 200 200 200 200 200 200 200 200 200
İ	28	1196 1197 1289 239 239 239 239 1118 11188 11403 2405 3310 11188 3310 11118
	*	2211 2211 220 230 230 230 230 230 230 230 230 230
	38	663 863 887 11096 1239 1239 11429 11429 11639 1113 1113 1113 1113 1113 1113 11
	*	
	-i	——————————————————————————————————————
Wire Gauge.	ජ	
9	}	
A P	" 	80

SIZE, WEIGHT, LENGTH, AND STRENGTH OF IRON WIRE.

(Trenton Iron Co.)

No. by Wire	Diant. in Deci- mals of	Area of Section in Decimals of	Feet to the Pound.	Weight of One Mile	proximate)	rength (Apo of Charcoal in Pounds,
Gauge.	Inch.	One Inch.	round.	in pounds.	Bright.	Annealed.
00000 0000 0000 000 000 00 0 1 1 2 3 4 4 5 6 7 7 8 9 10 11 11 12 13 14 15 16 17 18 18 19 19 19 19 19 19 19 19 19 19 19 19 19	.450 .400 .380 .383 .305 .285 .245 .225 .205 .190 .1175 .160 .01175 .080 .070 .0525 .045 .040 .0325 .040 .0325 .040 .0325	15904 12566 10179 08553 07306 08379 05515 04714 08976 03301 02805 02405 02405 02405 02011 01651 01327 01084 00866 00672 00503 00285 00216 00159 001256 0009621	1.863 2.358 2.911 3.415 5.374 6.286 7.454 8.976 10.453 12.322 14.736 22.333 27.340 34.219 44.092 58.916 76.984 101.488 187.174 196.000 34.219 44.092 36.000 37.174 38.0000 38.000 38.000 38.000 38.000 38.000 38.000 38.000 38.000 38.0000 38.000 38.000 38.000 38.000 38.000 38.000 38.000 38.000 38.0000 38.000 38.00000 38.0000 38.0000 38.0000 38.0000 38.0000 38.0000 38.0000 38.0000 38.0	2833.248 2238.878 1813.574 1523.861 1301.678 1136.678 982.555 839.942 708.365 588.139 505.084 428.472 358.3008 294.1488 236.4384 193.1424 154.2816 119.7504 89.6016 68.5872 28.3878 22.8872 17.1889 13.4429	12598 9955 8124 6880 5926 5226 4570 3948 3374 2839 2476 2136 1813 1507 1233 1010 810 631 474 372 293 222 169 137 107	9449 7466 6091 5160 4445 8920 8425 2960 2530 2130 1860 1860 1130 925 758 607 473 356 280 2105 105 107 103 80
22 23 24 25 26 27 28 29 30 31 33 34 35 36 37 88 40	.028 .025 .020 .018 .017 .016 .015 .018 .011 .010 .009 .0085 .007	.0006157 .0004909 .0008976 .0008142 .0002545 .0002270 .0002011 .0001767 .0001589 .0001827 .0001837 .0007088 .0007088 .0007088 .0006027 .0005027 .0005027	481, 234 603, 863 745, 710 943, 396 1164, 689 1305, 670 1476, 869 1925, 321 2232, 653 2620, 607 8119, 092 3773, 584 4182, 508 4657, 728 5292, 035 5896, 147 6724, 291 7698, 253	10.9718 8.7437 7.0805 5.5968 4.5334 4.0439 3.5819 3.1485 2.7424 2.3649 2.0148 1.6928 1.3992 1.2624 1.1336 1.0111 88549 78672 68587	+ HH-4.5	Swedish charcal fron is about 10 more. Mild Bessener steel is about 10 more. Ordinary cruchle steel is about 25 feel at cruchle steel is from that of charcoal from wire.

GALVANIZED IRON WIRE FOR TELEGRAPH AND TELEPHONE LINES.

(Trenton Iron Co.)
WEIGHT PER MILE-OHM.—This term is to be understood as distinguishing WEIGHT PER MILE-OHM.—Into term is to be understood as distinguishing the resistance of material only, and means the weight of such material required per mile to give the resistance of one ohm. To ascertain the mileage resistance of any wire, divide the "weight per mile-ohm" by the weight of the wire per mile. Thus in a grade of Extra Best Best, of which the weight per mile-ohm is 5000, the mileage resistance of No. 6 (weight per mile 525 lbs.) would be about 9½ ohms; and No. 14 steel wire, 6500 lbs. weight per mile-ohm (95 lbs. weight per mile), would show about 69 ohms.

Sizes of Wire used in Telegraph and Telephone Lines.

No. 4. Has not been much used until recently; is now used on important lines where the multiplex systems are applied.
No. 5. Little used in the United States.
No. 6. Used for important circuits between cities.
No. 8. Medium size for circuits of 400 miles or less.

No. 9. For similar locations to No. 8, but on somewhat shorter circuits;

until lately was the size most largely used in this country.

Nos. 10, 11. For shorter circuits, railway telegraphs, private lines, police and fire-alarm lines, etc.

No. 12. For telephone lines, police and fire-alarm lines, etc. Nos. 18, 14. For telephone lines and abort private lines: steel wire is used most generally in these sizes.

The coating of telegraph wire with zinc as a protection against oxidation

The coating of telegraph wire with zinc as a protection against oxidation is now generally admitted to be the most efficacious method.

The grades of line wire are generally known to the trade as "Extra Best Best" (E. B. B.), "Best Best" is made of the very best iron, as nearly pure as any commercial iron, soft, tough, uniform, and of very high conductivity, its weight per mile-ohm being about 5000 lbs.

The "Best Best" is of iron, showing in mechanical tests almost as good results as the E. B. B., but not quite as soft, and being somewhat lower in conductivity; weight per mile-ohm about 5700 lbs.

The Trenton "Steel" wire is well suited for telephone or short telegraph lines, and the weight per mile-ohm is about 6500 lbs.

lines, and the weight per mile-ohm is about 6500 lbs.

The following are (approximately) the weights per mile of various sizes of galvanized telegraph wire, drawn by Trenton Iron Co.'s gauge:
No. 4, 5, 6, 7, 8, 9, 10, 11, 12, 13

720, 610, 525, 450, 875, 310, 250, 200, 160,

TESTS OF TELEGRAPH WIRE.

The following data are taken from a table given by Mr. Prescott relating to tests of E. B. B. galvanized wire furnished the Western Union Telegraph Co.:

Size of	Diam. Parts of		ight.	Length. Feet	Resist Temp. 75	ance. .8° Fahr.	Ratio of Breaking Weight to
Wire.	One Inch.		Pounds per mile.	per pound.	Feet per ohm.	Ohms per mile.	Weight
4 5 6 7 8 9 10 11 12 14	.238 .220 .203 .180 .165 .148 .134 .120 .109	1043.2 891.3 758.9 596.7 501.4 408.4 830.7 265.2 218.8 126.9	886.6 678.0 572.2 449.9 878.1 804.2 249.4 240.0 165.0 95.7	6.00 7.85 9.20 11.70 14.00 17.4 21.2 26.4 82.0 55.2	958 727 618 578 409 828 269 216 179 104	5.51 7.26 8.54 10.86 12.92 16.10 19.60 24.42 29.60 51.00	3.05 3.40 3.07 3.38 3.87 2.97 3.43 3.05

JOINTS IN TELEGRAPH WIRES.—The fewer the joints in a line the better. All joints should be carefully made and well soldered over, for a bad joint may cause as much resistance to the electric current as several miles of wire.

TABLE OF DIMENSIONS, WEIGHT, AND RESISTANCE OF COPPER WIRE. (Birmingham Gauge.)

Gernere	Number.	8880mmmを表現で表現では日本には日本には日本であるようのである。 1000mmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmm
Resistance.	Ohms per Foot.	0000004 00000188 000011709 000117709 000118706 00018706 00018706 00018706 00018706 00018706 00018706 00018706
Rests	Ohms per Lb.	00000007 00010450 00010450 00010450 00010450 000105280 00100738 00140348 00140348 00140113
gth.	Feet per Ohm.	119966 55 13046 15 13046 15 13
Length	Feet per Lb.	1. 60.27 1. 60.27 1. 60.27 1. 60.28 1. 60.
rbt.	Lbs. per Ohm.	1948.73 6969-13 6969-13 8775-14 1962-03 1962-03 1962-03 1962-03 1962-03 1962-03 1962-03 1962-03 140-74 140-
Weight	Lbs. per Foot.	25.02.20 4.4716 4.47
Sectional Area	in Circular Mils. = diam².	200 116 116 116 116 116 116 116 116 116 1
Diameter	Inch	±#####################################
1-	Number.	88864888888888888888888888888888888888

WIRE.	
COPPER	
F PURE	1 100
CANCE 0	
RESIST	
HT. ANI	The state of the s
S. WEIG	1
MENSIONS	700
B OF DI	
TABLE	

d	Cfroular	Maximum Amperes.	Dlameter in	Weight, S	Sp. gr. 8.899.	Len	Length.	Kesistance, Legal	Shr.	8. G
Number.	Mils.	*(C.M.)3	Mile. Mil = .001 in.	Lbs. per Foot	Foot, Lbs. per Ohm.	Feet per Lb.	Feet per Ohm.	Ohms per Lb.	Ohms per Ft.	Number.
	3000	10.01	25.78	,000084	28.507	110.080	\$85.9	.3850405	.003497600	ωĸ
0 00	8000	19.0	25.55	.024220	18.464	41.288	768.3	.0651602	.001311780	∞
2	12000	18	109.55	.036328	41.588	27.527	1143.4	.0240743	.000874578	13
2	15000	41.6	123.48	019290	64.902	22.022	1429.2	.0154178	.000699600	92
8	50000	51.6	141.43	*0000*	116.572	16.516	1905.7	#000000°	#742000.	3
32	52000	0.19	158.12	.075682	180.378	13.213	2382.0	0/30000	/D8613000	88
90	30000	20.0	173.21	10000	203.122	0 4901	0.000	0000000	949000000	88
eg:	35000	78.6	187.09	COSONT.	26.250	9.435L	9000	0001000	000000000	3 5
90	40000	86.8	200.00	196997	201.920 584 008	0.2302	4087.7	0017100	2000000	25
90	45000	100.7	512.1% 002 £1	151357	721 096	6.6069	4763.8	0013968	000200914	2
250	22000	110.8	234, 53	106501	872.547	6.0060	5240.5	.0011467	.000190821	128
33	00009	117.7	244.95	181625	1038.258	5.5059	5716.5	.00096315	.600174931	8
92	. 00099	125.0	254.96	.196772	1218.586	2.0820	6182.9	.00083067	.000161465	3
20	20000	132.1	264.58	106118.	1413.264	4.7192	6669.4	.00070758	786671000	2
75	75000	139.1	273.87	.227043	1629.457	7	7146.0	00001630		<u>.</u>
80	80000	146.0	282 85	242176	1845.952	4. 1292	7023.3	2/14000.	.000131193	3
200	82000	152.8	291.56	2022303	2083.759	0.5800	0000	20001000	04621040	88
8	00000	109.0	300.00	1012124	9000	8 4779	9051	00036415	000110477	88
88	100000	179 6	818	302709	2884 082	30.3635	9527.6	.00034673	090104960	91
35	110000	185.4	731.67	332991	3489.968	3.0031	10480.6	.00028656	.000095410	110
181	120000	198.0	37.976	.363267	4153.433	2.7528	11433.6	.00024070	.000084460	120
130	130000	210.3	360.56	.393527	4874.226	2.6411	12386.0	.00020614	0820800	8
140	140000	555.5	874.17	423797	5652.899	25.55	13338.7	06017690	0.00000000	21;
150	150000	234.0	387.30	454061	6484.673	30.2	14201.3	401000°	ARRONAL.	2;
99	160000	245.6	8.6	454328	7883.043	7.00±	15253.V	40011000		35
170	170000	0.70%	412.32	220810.	0000.000	1 0050	17170	10741000	0404040	25
8	180000	208.9	72.52	101100	10411 941	7887	18106.1	#000000	AAAAA5549	8
38	000000	900 4	77.00	605.97	11598 681	1,6517	19055.4	00008667	000059478	500
38	000000	319.0	180	685975	13959 567	1.5016	20061.1	60007163	707740000	220
200	940000	283.0	96	796498	16612.114	1.3765	22866.0	61090000	000043733	240
2	280000	353.5	200	787068	19496.997	1.2706	24778.1	.00006129	89097000	360
98	980000	373.7	529.16	847605	22613.233	1.1798	\$677.8	223-10000	167/C0000°	\$
9	300000	303.6	547.73	041806	20967.464	1.1018	28683.1	.00003862	986750000	3
88	320000	413.1	565.69	279896	29533.696	1.6823	30488.3	.00003386	.000032799	380
95	340000	438.3	200	1.020314	23.0.181	9175	2000	.00002000	000000000	200
000	000000	7								

DIMENSIONS, WEIGHT, AND RESISTANCE OF COPPER WIRE, (Brown & Sharbe)s Gauge.)

Gauge	Diameter	Sect. Area	Wei	Weight.	Length.—Feet.	-Feet.	Resistan	Resistance.—Ohms.	Gauge
mber.	Inch.	Mils.	Lbs, per Foot,	Lbs. per Ohm.	Per Lb.	Per Ohm.	Per Foot.	Per Lb.	Number.
9000	3 .	211600.	.640525	13129.29	1.56122	2.724.7	.000048786	.0000761656	0000
8	79007	167805.	.507955	8256.95	1.9687	16255.27	.000061519	11121000	8
8	8868	133079.	+40284	5193.13	8.4824	12891.37	.0000775713	.000192563	3
۰.	38486	100034	7519457	3265.84	8.1803	1022.08	0.00097818	.0002062	>-
	95789	66873	900915	1901 80	4 07799	64.99 58	00015553	0000770118	4 01
100	5000	25824	159325	819.700	6 2765	5008.61	.000196139	.00122108	. 63
	.90431	41748.	.126357	522.839	7.9141	4043.6	.000247304	.00191263	4
-	18194	33102.	.10022	321,309	9.97983	3306.61	.000311856	.00311227	0
•	16202	28251.	0.0794616	205.062	12,5547	2542.89	.000393955	.00494898	•
	1428	SOSI7.	.0630134	127.07	15.8696	2010.01	. UNO490005	00780166	
× 0	1707	19001	1018890	79.9298	20.0097	1000	00000000	011020110	••
	20101	1000	0814956	91 6096	91 6010	1055 66	0000000	001649	•=
1	072000	7508	004005	10 880	40.1909	207	0019597	0609087	1=
72	Senanan	659	0107445	10 5094	FO 5000	690 555	0015909	0700769	12
3:	190100	2178	6154759	7 04010	00000 OF	201 00	001000	107170	32
32	700700	710	A194910	4 51099	80 4415	607 800	0008197	901719	3 ≠
12	067068	2000	0008584	9 11015	101 4965	915 490	00018078	201109	12
25	200	200	.0078179	1.95501	87.19	250.184	.00399707	2011507	22
11	.045257	8068	.0062	1.23013	161.29	198,409	.0050401	816318	11
2	040903	1624.	.004917	.773677	203.374	167.35	.0063553	1.29263	8 2
2	888		.0038991	.486524	256.468	194.7	.00801426	2.0654	2
Ri	100150	1001	2260200	100700	25.30	26.3023	010100	5.2082 F 1067	85
7 SI	025547	642	0019448	191037	514.193	60.03	0160678	8 26197	181
2	.089571	200	.0015421	.076105	648.452	49.3504	.0202633	13.13974	83
4	1080	4	.001223	10478624	817.688	38.1365	.0255516	20.89823	a
2	610.	9	6696000	.0301038	1081.088	23.0381	.0322184	28.2184	8
RS	014195		0000000	0110010	1630 40	10 5191	0519518	28.82	8 &
	019841	150.8	0004837	0074748	9067 964	16.479	0646098	133 6563	: 85
2	.011257	126.7	.0003836	.0047087	5606.969	12.2854	.081464	212.373	8
8	.010025	100.5	.0003042	₹196200.	3987.084	9.7355	.102717	337.639	8
5	.008928	2.	.0002413	.0018306	4414.49	7.72143	12961	536.7516	5
25	8	2:	.0001913	.00117133	6226.915	6.12245	163394	803.738	8
23	9/20	3.5	0001000	000736789	6090.41	4.800/0	200962	1207.281	83
51	10000	2.5	CONTROL O	0000001070	10101	0.0200	9075.1	100.001	58
3	3000	2.5	0000000	212122000	1001	0.0000	41909	KASA AK	3 %
38	90772	3 2	OUNDOUGHOUS .	200211000	10650 07	1 0000	Konen	6670	35
38	OUSDE!	15.79	00000000	172700000	10000	1 50000	AKARAK	18708 04	38
38	UNEST.	10.61	76460000	0000455998	00106 007	1 9,7777	20000	91098 11	88
3:	Tonno.	200	100000000	00000000000	200.00	10000	20170	07011	3 9

HARD-DRAWN COPPER TELEGRAPH WIRE.

(J. A. Roebling's Sons Co.)

Furnished in half-mile coils, either bare or insulated.

Size, B. & S. Gauge.	Resistance in Ohms per Mile.	Breaking Strength.	Weight per Mile.	Approximate Size of E. B. B. Iron Wire equal to Copper.
9 10 11 12 18 14 15	4.30 5.40 6.90 8.70 10.90 13.70 17.40	625 525 420 830 270 213 170	209 166 131 104 83 66 52 41	Iron-wire Gauge

In handling this wire the greatest care should be observed to avoid kinks, bends, scratches, or cuts. Joints should be made only with McIntire Connectors.

On account of its conductivity being about five times that of Ex. B. B. Iron Wire, and its breaking strength over three times its weight per mile, copper may be used of which the section is smaller and the weight less than an equivalect iron wire, allowing a greater number of wires to be strung on the poles.

the poies. Besides this advantage, the reduction of section materially decreases the electrostatic capacity, while its non-magnetic character lessens the self-induction of the line, both of which features tend to increase the possible speed of signalling in telegraphing, and to give greater clearness of enunciation over telephone lines, especially those of great length.

INSULATED COPPER WIRE, WEATHERPROOF INSULATION.

	Do	Double Braid.			iple Bra	id.	Approximate		
Num- bers, B. & S. Gauge.		Pounds.		Outside Weights, Diame- ters in			Weights, Pounds.		
	32ds Inch.	1000 Feet.	Mile.	82ds Inch.	1000 Feet.	Mile.	Reel.	Coil.	
0000 000 00 0 1 1 2 8 4 5 6	20 18 17 16 15 14 13 11 10	716 575 465 875 285 245 190 152 120	3781 8036 2455 1980 1505 1294 1003 808 634 518	24 22 18 17 16 15 14 12 11	775 630 490 400 806 268 210 164 145 112	4092 3326 2587 2112 1616 1415 1109 866 766 591	2000 2000 500 500 500 500 500 250 260 275	250 250 250 250 250 250 250 250 125 130 140	
8 10 12 14 16	8 7 6 5 4 8	66 45 80 20 14	849 238 158 106 74 53	9 8 7 6 5	78 55 85 26 20	412 290 185 137 106	200 200	100 100 25 25 25 25	

Power Cables. Lead Incased, Jute or Paper Insulated. (John A. Roebling's Sons Co.)

Nos,. B.&S.G.	Circular Mils.	Outside Diam. Inches.	Weights, 1000 feet. Pounds.	Nos., B. & S. G.	Circular Mils.		Weights, 1000 feet. Pounds.
	1000000 900000 800000 750000 700000 650000 550000 450000 450000 450000 3850000	1 13/16 1 23/32 1 21/32 156 1 19/82 1 9/16 1 17/32 1 7/16 13/6 1 11/32 1 5/16	6228 5778 5543 5315 5083 4857 4630 4278 3923	0000 000 00 0 0 1 2 3 4 6	300000 250000 211600 168100 133225 103625 83521 66564 52441 41616 26244	11/4 1 3/16 1 3/32 1 1/16 1 15/16 29/82 7/6 25/32 3/4 11/16	8060 2732 2533 2530 2021 1772 1633 1482 1360 1251

Stranded Weather-proof Feed Wire.

Circular	Outside			imate on reels.	Circular	Outside Diam.	Weights. Pounds.		imate on reels.
Mils.	Diam. Inches.	1000 feet.	Mile.	Approx length Feet.	Mils.	Inches.	1000 feet.	Mile.	Approx length Feet.
1000000 900000 800000 750000 700000 650000 600000	11/6 1 18/32 1 11/33 1 5/16 1 9/82 1/4 1 7/82		18744 16975 15206 14825 13438 12556 11668	800 850 850 900 900	850000 500000 450000 400000 350000 300000 250000	1 3/16 11/6 1 3/82 1 1/16 1 15/16 29/82	2043 1875 1703 1530 1358 1185 1012	10787 9900 8992 8078 7170 6257 5848	1200 1320 1400 1450 1500 1600

The table is calculated for concentric strands. Rope-laid strands are larger.

Approximate Bules for the Besistance of Copper Wire. The resistance of any copper wire at 20° C. or 68° F., according to Mat- $\frac{d^2}{d^2}$, in which R is the resistance in interthiesen's standard, is R =national ohms, I the length of the wire in feet, and d its diameter in mils.

(1 mll = 1/1000 inch.)
A No. 10 Wire, A.W.G., .1019 in. diameter (practically 0.1 in.), 1000 ft. in length, has a resistance of 1 ohm at 68° F. and weighs 31.4 lbs.

If a wire of a given length and size by the American or Brown & Sharpe gauge has a certain resistance, a wire of the same length and three numbers higher has twice the resistance, six numbers higher four times the resistance, etc.

Approximate rules for resistance at any temperature :

$$R_t = R_0(1 + .004t); \qquad R_t = \frac{9.6(1 + .004t)l}{d^2};$$

 R_0 = resistance at 0°, R_t = resistance at the temperature t° C., l = length in feet, d = diameter in inils. (See Copper Wire Table, p. 1034.)

GALVANIZED STEEL-WIRE STRAND. For Smokestack Guys, Signal Strand, etc.

(J. A. Roebling's Sons Co.)

This strand is composed of 7 wires, twisted together into a single strand.

Diameter.	Weight per 100 Feet.	Estimated Breaking Strength.	Diameter.	Weight per 100 Fest.	Estimated Breaking Strength.	Diameter.	Weight per 100 Feet.	Estimated Breaking Strength.
in. 15/32 7/16 35 5/16	lbs. 51 48 37 30 21	lbs. 8,320 7,500 6,000 4,700 3,300	in. 9/82 17/64 1/4 7/92 8/16	lbs. 18 15 1116 834 616	lhs. 2,600 2,250 1,750 1,300 1,000	in. 5/82 9/64 1/6 8/32	lbs. 416 812 214 2	lbs. 700 525 875 820

For special purposes these strands can be made of 50 to 100 per cent greater tensile strength. When used to run over sheaves or pulleys the use of soft-iron stock is advisable.

FLEXIBLE STEEL-WIRE CABLES FOR VESSELS.

(Trenton Iron Co., 1886.)

With numerous disadvantages, the system of working ships' anchors with chain cables is still in vogue. A heavy chain cable contributes to the holding-power of the anchor, and the facility of increasing that resistance by paying out the cable is prized as an advantage. The requisite holding-power is obtained, however, by the combined action of a comparatively fight anchor and a correspondingly great mass of chain of little service in proportion to its weight or to the weight of the anchor. If the weight and size of the anchor were increased so as to give the greatest holding noward. proportion to its weight or to the weight of the anchor. In weight an size of the anchor were increased so as to give the greatest holding-power required, and it were attached by means of a light wire cable, the combined weight of the cable and anchor would be much less than the total weight of the chain and anchor, and the facility of handling would be much greater. English shipbuilders have taken the initiative in this direction, and many of the largest and most serviceable vessels affoat are fitted with steel-wire

cables. They have given complete satisfaction.

The Trenton Iron Co.'s cables are made of crucible cast-steel wire, and guaranteed to fulfil Lloyd's requirements. They are composed of 72 wires subdivided into six strands of twelve wires each. In order to obtain great flexibility, hempen centres are introduced in the strands as well as in the completed cable.

FLEXIBLE STEEL-WIRE HAWSERS.

These hawsers are extensively used. They are made with six strands of twelve wires each, hemp centres being inserted in the individual strands as all as in the completed rope. The material employed is crucible cast steel, galvanized, and guaranteed to fulfil Lloyd's requirements. They are only one third the weight of hempen hawsers; and are sufficiently pliable to work the strand of the support rope of gaulatient strands. round any bitts to which hempen rope of equivalent strength can be applied.

18-inch tarred Russian hemp hawser weighs about 89 lbs. per fathom.

10 inch white manila hawser weighs about 20 lbs. per fathom.

14-inch stud chain weighs about 68 lbs. per fathom.

14-inch galvantsed steel hauser verighs about 12 lbs. per fathom.

Each of the above named has about the same tensile strength.

SPECIFICATIONS FOR GALVANIZED IRON WIRE. Issued by the British Postal Telegraph Authorities.

Weig	tht pe	r Mile.	I	Diamet	er.	Te	Tests for Strength and Ductility.			ad	Mile pr	Γ	
ed Standard.	All	-		Breaking Weight.	No. of Twists in 6 in	king Weight not less than—	No. of Twists in 6 in.	Breaking Weight not less than-	No. of Twists in 6 in.	Resistance per Mi of the Standard Size at 60° Fahr	t, being Standard t × Resistance.		
Required	Minimum.	Maximum.	Beguired	Minimum.	Maximum.	Minimum.	Minimum.	For Breaking less t	Minimum.	For Break	Maimum.	Maximum.	Constant, Weight
lbs. 800 600 450 400 200	lbs. 767 571 424 877 190	lbs. 888 629 477 424 218	mils. 242 209 181 171 121	mils. 237 204 176 166 118	mils. 247 214 186 176 125	lbs. 2480 1860 1390 1240 620	15 17 19 21 30	lbs. 2550 1910 1425 1270 638	14 16 18 20 28	lbs. 2620 1960 1460 1800 655	18 15 17 19 26	ohms. 6.75 9.00 12.00 18.50 27.00	5400 5400 5400 5400 5400 5400

STRENGTH OF PIANO-WIRE.

The average strength of English piano-wire is given as follows by Webster, Horsfals & Lean;

Numbers in Music- wire Gauge.	Equivalents in Fractions of Inches in Diameters.		Numbers in Music- wire Gauge.	Equivalents in Fractions of inches in Diameters.	
12 18 14 15 16 17	.029 .081 .033 .035 .037 .089	225 250 286 305 840 860	18 19 20 21 22	.041 .048 .045 .047 .052	395 425 500 540 650

These strengths range from 800,000 to 340,000 lbs. per sq. in. The composition of this wire is as follows: Carbon, 0.870; silicon, 0.090; sulphur, 0.011; phosphorus, 0.018; manganese, 0.425.

"PLOUGH"-STEEL WIRE.

The term "plough," given in England to steel wire of high quality, was derived from the fact that such wire is used for the construction of ropes used for ploughing purposes. It is to be hoped that the term will not be seed in this country, as it tends to confusion of terms. Plough-steel is known here in some steel-works as the quality of plate steel used for the mould-boards of ploughs, for which a very ordinary grade is good enough. Experiments by Dr. Percy on the English plough-steel (so-called) gave the following results: Specific gravity, 7.814; carbon, 0.828 per cent; manganese, 0.587 per cent; silicon, 0.143 per cent; sulphur, 0.009 per cent; phopophorus, nii; copper, 0.030 per cent. No traces of chromium, titanium, or tungsten were found. The breaking strains of the wire were as follows:

.159 Diameter, inch... 224,000 257,600 201,600 The elongation was only from 0.75 to 1.1 per cent.

WIRES OF DIFFERENT METALS AND ALLOYS.

(J. Bucknall Smith's Treatise on Wire.)

Brass Wire is commonly composed of an alloy of 13/4 to 2 parts of sopper to 1 part of zinc. The tensile strength ranges from 20 to 40 tons per square inch, increasing with the percentage of zinc in the alloy.

German or Nickel Silver, an alloy of copper, zinc, and nickel, is practically brass whitened by the addition of nickel. It has been drawn into

practically orass wintened by the audition to mean. It has seen a summer wire as fine as .002" diam.

Platinum wire may be drawn into the finest sizes. On account of its high price its use is practically confined to special scientific instruments and electrical appliances in which resistances to high temperature, oxygen, and acids are essential. It expands less than other metals when heated, which reads the being could in class without fear of cracking. It is property permits its being sealed in glass without fear of cracking. It is therefore used in incandescent electric lamps.

Phosphor-bronze Wire contains from 2 to 6 per cent of tin and from 1/20 to 1/8 per cent of phosphorus. The presence of phosphorus is

derimental to electric conductivity.

**Delta-metal ** wire is made from an alloy of copper, iron, and zinc.

Its strength ranges from 45 to 63 tons per square inch. It is used for some kinds of wire rope, also for wire gauze. It is not subject to deposits of verdigirs. It has great toughness, even when its tensile strength is over 60 tons per square inch.

tons per square inch.

Aluminum Wire.— Specific gravity .268. Tensile strength only alout 10 tons per square inch. It has been drawn as fine as 11,400 yards to the cunce, or .042 grains per yard.

Aluminum Bronze, 50 copper, 10 aluminum, has high strength and ductility; is inoxidizable, sonorous. Its electric conductivity is 12.6 per cent.

Silicon Bronze, patented in 1882 by L. Weiler of Paris, is made as follows: Fluosilicate of potash, pounded glass, chloride of sodium and calcium, carbonate of soda and lime, are heated in a plumbago crucible, and after the reaction takes place the contents are thrown into the molten bronze to be treated. Silicon-bronze wire has a conductivity of from 40 to 38 per cent of that of copper wire and four times more than that of iron, while its tensile strength is nearly that of steel, or 28 to 55 tons per square while its tensile strength is nearly that of steel, or 28 to 55 tons per square inch of section. The conductivity decreases as the tensile strength increases. Wire whose conductivity equals 95 per cent of that of pure copper gives a tensile strength of 28 tons per square inch, but when its conductivity is 34 per cent of pure copper, its strength is 50 tons per square inch. It is

being largely used for telegraph wires. It has great resistance to oxidation.

Ordinary Brawn and Annealed Copper Wire has a strength of from 15 to 20 tons per square inch.

SPECIFICATIONS FOR HARD-DRAWN COPPER WIRE.

The British Post Office authorities require that hard-drawn copper wire supplied to them shall be of the lengths, sizes, weights, strengths, and conductivities as set forth in the annexed table.

Weig	Weight per Statute Mile.			Approximate Equiva- lent Diameter.				Resist- Mile of an hard)	Veight ece (or ire.
Required Standard.	Minimum.	Maximum	Standard.	Minimum.	Maximum.	Minimum Breaking Weight,	Minimum No. c Twists in 3 Inche	Maximum ance per Wire (who	Minimum of each Pi Coil) of W
lbs, 100 150 200 400	lbs. 9714 14614 195 890	lbs. 10214 15334 205 410	mils. 79 97 112 158	mils. 78 9514 11014 15514	mils. 80 98 11314 16014	lbs. 330 490 650 1300	30 25 20 10	ohms. 9.10 6.05 4.53 2.27	Îbs. 50 50 50 50

WIRE ROPES.

List adopted by manufacturers in 1892. See pamphlets of John A. Roebling's Sons Co., Trenton Iron Co., and other makers.

Pliable Hoisting Bope.
With 6 strands of 19 wires each.

			. 1	ROM.			
Trade Number.	Di a meter.	Circumference in inches.	Weight per foot in pounds. Rope with Hemp Cen- tre.	Breaking Strain, tons of 2000 lbs.	Proper Working Load in tons of 2000 lbs.	Circumference of new Manila Rope of equal Strength.	Min. Size of Drum or Sheave in feet.
1 2 3 4 5 5 5 6 7 8 9 10 10 10 10 10 10 10 10 10 10 10 10 10	24 154 156 1156 1156 1156 1156 1156 1156	634 6 516 516 434 4 316 3194 214 214 214 214 214	8 00 6.30 5.25 4.10 3.65 3.00 2.50 2.00 1.58 1.20 0.88 0.60 0.48 0.39 0.29	74 65 54 44 47 59 83 27 20 16 11.50 8.64 5.18 4.27 3.48 3.00 2.50	15 13 11 9 8 61,79 4 3 21,74 11,74 11,74 11,74 11,74	14 13 12 11 10 914 815 715 612 612 434 334 334 335 214	13 12 10 81,6 77,5 6 6 51,4 41,9 41,9 21,4 21,4 21,4
			CAST	STEEL.			
1 2 3 4 5 5 5 6 7 8 9 10 10 4 10 10 4 10 10 2 10 7 8	234 154 155 1156 1146 1148 1156 1156 1156 1156 1156 1156 1156 115	694 614 614 484 4814 814 814 224 215 114	8.00 6.30 5.35 4.10 3.65 3.00 2.50 2.50 2.00 1.58 1.20 0.88 0.48 0.39 0.29	155 125 106 86 77 63 52 43 38 25 18 12 9	31 25 21 15 12 10 8 6 8 14 14 14 14 13 18	15 14 13 12 11 11 904 814 7 54 414 334 334	814 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8

Cable-Traction Ropes.

According to English practice, cable-traction ropes, of about 3½ in. in circumference, are commonly constructed with six strands of seven or affecten wires, the lays in the strands varying from, say, 3 in. to 3½ in., and the lays in the ropes from, say, 7½ in. to 9 in. In the United States, however, strands of nineteen wires are generally preferred, as being more flexible; but, on the other hand, the smaller external wires wear out more rapidly. The Market-street Street Railway Company, San Francisco, has used ropes 1½ in. in diameter, composed of six strands of nineteen steel wires, weighing 2½ lbs. per foot, the longest continuous length being 24,125 ft. The Chicago City Railroad Company has employed cables of identical construction, the longest length being 27,700 ft. On the New York and Brooklyn Bridge cablealiway steel ropes of 11,500 ft. long, containing 114 wires, have been used.

Transmission and Standing Rope.

With 6 strands of 7 wires each.

IRON.

Trade Number.	Diameter.	Circumference.	Weight per footin pounds of Rope with Hemp Cen- tre.	Breaking Strain in tons of 2000 lbs	Proper Working Load in tons of 2000 Ibs.	Chrumference of new Manila Rope of equal Strength.	Min. Size of Drum or Sheave in feet,
11 12 13 14 15 16 17 18 19 20 21 22 23 24 25	114 136 114 115 116 11-16 96 9-16 12-16 55-16 9-32	484 448 4 814 814 814 814 814 814 814 81	3.37 2.77 2.28 1.82 1.50 0.92 0.70 0.57 0.41 0.93 0.23 0.21 0.16 0.125	36 30 25 20 16 12.3 8.8 7.6 5.8 4.1 2.83 2.13 1.65 1.38	9 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	10 9 816 719 614 434 434 434 214 214 214	18 12 103 103 103 103 103 103 103 103 103 103
			CAST	STEEL.			
11 12 18 14 15 16 17 18 19 20 21 22 23	11/6 11/8 11/8 11/8 11/16 5/8-16 14/16 5/8-16	4344 438 4 318 214 214 218 114 114	3.37 2.77 2.28 1.89 1.50 1.12 0.92 0.70 0.57 0.41 0.23 0.23	62 52 44 86 30 22 17 14 11 8 6 41 4	13 10 9 714 6 414 314 214 114 114 114	13 12 11 10 9 8 7 6 5 14 4 4 4 4 4 3 14 3 14 3 3	814 8 714 614 534 54 4 316 316 316 316 316 316 316

Plough-Steel Rope.

214

116

0.12

25

9-39

36

Wire ropes of very high tensile strength, which are ordinarily called "Plough-steel Ropes," are made of a high grade of crucible steel, which, when put in the form of wire, will bear a strain of from 100 to 150 tons per square inch.
Where it is necessary to use very long or very heavy ropes, a reduction of

the dead weight of ropes becomes a matter of serious consideration.

It is advisable to reduce all bends to a minimum, and to use somewhat larger drums or sheaves than are suitable for an ordinary crucible rope having a strength of 60 to 80 tons per square inch. Before using Plough-stee Ropes it is best to have advice on the subject of adaptability.

Plough-Steel Rope.

With 6 strands of 19 wires each.

Trade Number.	Diameter in inches.	Weight per foot in pounds.	Breaking Strain in tons of 2000 lbs.	Proper Working Load.	Min. Size of Drum or Sheave in feet.
1 2 8	21/4 2 13/4 15/2	8.00 6.30 5.25 4.10	240 189 157 128	46 87 81 25	9 8 71/6
5 53/ 6 6	178 178 196 114	8.65 8.00 2.50 2.00	110 90 75 60	22 18 15	514 514 5
8 9 10 1014	1.78 1.76 3.6 3.7 2.7	1.58 1.20 0.88 0.60	47 87 27 18	9 7 5 81/2	414 414 834 314
1012	9-16 1/2	0.44	13 10	21/2	214

With 7 Wires to the Strand.

15	1 76	1.50 1.12	45 83 25	9 6 ⅓	53/6
16 17	\$4.0	0.92	25	5	4
18 19	11-16 %	0.92 0.70 0.57 0.41	21 16	4 884	81/6
20	98 9–16	0.41	12	212	23/
21 22 23	79 7–16	0.31 0.23 0.21	5	178	2) 2 2 1) 4
23	% ₹	0.21	4	1	13/6

Galvanized Iron Wire Rope.

For Ships' Rigging and Guys for Derricks.

CHARCOAL ROPE.

Circum- ference in inches.	Weight per Fath- om in pounds.	Cir. of new Manila Rope of equal Strength.	Break- ing Strain in tons of 2000 pounds	Circum- ference in inches	Weight per Fathom in pounds.	Cir. of new Manila Rope of equal Strength.	Break- ing Strain in tons of 2000 pounds
51/4 51/4 54/4 41/4 41/4 41/4 81/4 81/4 81/4 81/4	261/4 241/2 22 21 19 161/4 123/4 109/4 91/4 6	11 101/2 10 91/2 9 81/4 8 71/4 61/2 65/4 51/4	43 40 35 38 80 26 23 20 16 14 12	214 214 214 114 114 116	514	5 43/4 41/4 83/4 82/4 22/4 21/4 11/4 11/8	9 8 7 5 31 21 21 21 21 21 21 21 21 21 21 21 21 21

Galvanized Cast-steel Yacht Rigging.

Circum- ference in inches.	Weight per Fath- om in pounds.	Cir. of new Manilla Rope of equal Strength.	Break- ing Strain in tons of 2000 pounds	Circum- ference in inches	Weight per Fathom in pounds.	Cir. of new Manilia Rope of equal Strength.	Break- ing Strain in tons of 2000 pounds
4 81/4 8 23/4 21/4	141/4 109/4 8 69/4 51/4 41/4	18 11 916 814 87	66 43 32 27 22 18	28 194 114 114 114 1	814 214 2 176 184	616 514 484 414 884 8	14 10 8 616 512 314

Steel Hawsers. For Mooring, Sea, and Lake Towing.

	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2											
Circumfer- ence.	Breaking Strength.	Size of Manilla Haw- ser of equal Strength.	Circumfer- ence.	Breaking Strength.	Size of Manilla Haw- ser of equal Strength.							
Inches. 214 234 234 3	Tons. 15 18 22	Inches. 61/2 7 81/2	Inches, 31/6 4	Tons. 29 35	Inches. 9 10							

Steel Flat Ropes.

(J. A. Roebling's Sons Co.)

Steel-wire Flat Ropes are composed of a number of strands, alternately twisted to the right and left, laid alongside of each other, and sewed together with soft iron wires. These ropes are used at times in place of round ropes in the shafts of mines. They wind upon themselves on a narrow winding-drum, which takes up less room than one necessary for a round rope. The soft-iron sewing-wires wear out sooner than the steel strands, and then it becomes necessary to sew the rope with new iron wires.

Width and Thickness in inches.	Weight per foot in pounds.	Strength in pounds.	Width and Thickness in inches.	Weight per foot in pounds.	Strength in pounds.
36 × 2	1.19	85,700	14 × 3	2.88	71,400
36 × 21/6	1.86	55,800	14 × 31 4	2.97	89,000
36 × 3	2.00	60,000	14 × 4	8.30	99,000
36 × 31/6	2.50	75,000	14 × 4	4.00	120,000
36 × 4	2.86	85,800	14 × 5	4.27	128,000
36 × 4	8.12	93,600	14 × 5	4.82	144,600
36 × 5	3.40	100,000	14 × 6	5.10	153,000
36 × 5	8.90	110,000	14 × 7	5.90	177,000

For safe working load allow from one fifth to one seventh of the breaking stress.

"Lang Lay" Rope.

In wire rope, as ordinarily made, the component atrands are laid up into rope in a direction opposite to that in which the wires are laid into strands; that is, if the wires in the strands are laid from right to left, the strands are laid into rope from left to right. In the "Lang Lay," sometimes known as 'Universal Lay," the wires are laid into strands and the strands into rope in the same direction; that is, if the wire is laid in the strands from right to left, the strands are also laid into rope from right to left. Its use has been found desirable under certain conditions and for certain purposes, mostly for haulage plants, inclined planes, and street railway cables, although be has also been used for vertical hoists in mines, etc. Its advantages are the

GALVANIZED STREL CABLES.

For Suspension Bridges. (Roebling's.)

Diameter in inches.	Ultimate Strength in tons of 2000 pounds.	Weight per foot	Diameter in inches.	Ultimate Strength in tons of 2000 pounds.	Weight per foot.	Diameter in inches.	Ultimate Strength in tons of 2000 pounds.	Weight per foot.
25/6	220	18	21/4	155	8.64	134	95	5.6
25/6	200	11.8	2	110	6.5	154	75	4 85
25/6	180	10	13/6	100	5.8	115	65	3.7

COMPARATIVE STRENGTHS OF FLEXIBLE GAL-VANIZED STREL-WIRE HAWSERS,

With Chain Cable, Tarred Bussian Hemp, and White Manila Ropes.

Patent Flexible Steel-wire Hawsers and Cables.				Chain Cable.			Tarred Rus- sian Hemp Rope.			White Manilla Ropes.			
Size, Circumference.	Weight per Fathom.	Guaranteed Breaking Strain, tons.	Diameter of Sheave round which it may be worked, inches,	Size.	Weight per Fathom.	train	Breaking Strain, tons.	Size.	Weight per Fathom.	Breaking Strain, tons.	Size.	Weight per Fathom.	Breaking Strain, tons.
1 11/4 11/6 21/4 21/4 21/4 21/4 33/4 41/6 61/6 77/6	294 446 516 7 8 9 12 15 2346 28	216	6 716 9 1016 13 15 16 6 1916 18 1916 1916 1916 1916 1916 1	2 1-16	54 68 112 143 166 204 231 256	51-6 7 81-6 101-6 117-8 15-8-10 18 223-6 377-6 551-6 671-9 79-6	6 734 994 1284 17 8-10 23 7-10 27 3415 5554 6619 7719 107 1-10 12014 13434	294 34 5 64 64 74 84 9 10 11 12 13 15 17 10 21 22 24 25	3 314 6 8 10 13 16 19 23 28 23 39 56 67 193 134 146	116 216 314 5 7 9 1116 14 1616 20 2416 20 34 50 60 7 89 106 115 125	236 314 4 5 534 614 7 716 816 9 10 11 1234 1316	114 184 28 8446 6 7 884 1016 13 144 22 294 42	2 234 314 5 1016 1214 15 18 223 3814 51 62 7314

NOTE.—This is an old table, and its authority is uncertain. The figures in the fourth column are probably much too small for durability.

it is somewhat more flexible than rope of the same diameter and composed of the same number of wires laid up in the ordinary manner; and (especially) that owing to the fact that the wires are laid more axially in the rope, longer surfaces of the wire are exposed to wear, and the endurance of the rope is thereby increased. (Trenton fron Co.)

Notes on the Use of Wire Rope.

(J. A. Roebling's Sons Co.)

Several kinds of wire rope are manufactured. The most pliable variety contains nineteen wires in the strand, and is generally used for hoisting and running rope. The ropes with twelve wires and seven wires in the strand are stiffer, and are better adapted for standing rope, guys, and rigging. Orders should state the use of the rope, and advice will be given. Ropes are

ders should state the use of the rope, and advice will be given. Adjes are made up to three inches in diameter, upon application.

For safe working load, allow one fifth to one seventh of the ultimate strength, according to speed, so as to get good wear from the rope. When substituting wire rope for hemp rope, it is good economy to allow for the former the same weight per foot which experience has approved for the

Wire rope is as pliable as new hemp rope of the same strength; the for-mer will therefore run over the same-sized sheaves and pulleys as the latter. But the greater the diameter of the sheaves, pulleys, or drums, the longer wire rope will last. The minimum size of drum is given in the table.

Experience has demonstrated that the wear increases with the speed. It is, therefore, better to increase the load than the speed.

Wire rope is manufactured either with a wire or a hemp centre. The latter is more pliable than the former, and will wear better where there is short bending. Orders should specify what kind of centre is wanted.

Wire rope must not be coiled or amouled like hemp rope.

When mounted on a reel, the latter should be mounted on a spindle or flat turn-table to pay off the rope.

When forwarded in a small coil, without reel, roll it over the ground like a wheel, and run off the rope in that way. All untwisting or kinking must be avoided.

To preserve wire rope, apply raw linsesd-oil with a piece of sheepskin, wool inside; or mix the oil with equal parts of Spanish brown or lamp-black.

To preserve wire rope under water or under ground, take mineral or vegetable tar, and add one bushel of fresh-slacked lime to one barrel of tar, which will neutralize the acid. Boil it well, and saturate the rope with the

hot tar. To give the mixture body, add some sawdust.

The grooves of cast-iron pulleys and sheaves should be filled with wellseasoned blocks of hard wood, set on end, to be renewed when worn out. This end-wood will save wear and increase adhesion. The smaller pulleys on the same plan. When large sheaves run with very great velocity, the grooves should be cloned with leather, set on end, or with India rubber. This is done in the case of sheaves used in the transmission of power between distant points by means of rope, which frequently runs at the rate of 4000 feet per minute.

Steel ropes are taking the place of iron ropes, where it is a special object

to combine lightness with strength.

But in substituting a steel rope for an iron running rope, the object in view should be to gain an increased wear from the rope rather than to reduce the

Locked Wire Rope.
Fig. 74 shows what is known as the Patent Locked Wire Bope, made by the Trenton Iron Co. It is claimed to wear two to three times as long as an





F1g. 74.

ordinary wire rope of equal diameter and of like material. Bixes made are from 16 to 116 inches diameter.

CRANE CHAINS.

(Pencoyd Iron Works.)

:	66	D. B. G.	" Specia	l Crane.			Crane.			
Size of Chain, inches.	Pitch Approximately, inches	Weight per Foot in pounds, approximately.	Outside Width, inches.	Proof Test, pownds.	Average Breakage Strain, pounds.	Ordinary Safe Load, General Use, pounds.	Proof Test, pounds.	Average Breaking Strain, pounds.	Ordinary Safe Load, General Use, pounds.	
14 5-16 5-16 7-16 9-16 11-16 12-16 15-16 11-16 15-16 11-16 1	2 19-32	76 1 7-10 2 2 2 2 3 3 2-10 4 4 6 5 7-10 8 9 10 7-10 11 2-10 12 4 10 18 4-10 18 4-10 19 7-10 21 7-10	76 11-16 114 111-16 111-16 176 111-16 22-16 22-11-16 22-18 23-16 33-4 35-16 33-4 35-16 33-4 49-16 49-16	1932 2898 4186 5796 7728 660 11914 14490 17388 20286 22484 25872 29568 33264 87576 41880 46200 50512 55718 60368 66528	8864 5796 8372 11592 15456 19320 29828 88960 84776 40572 44968 51744 59136 66538 75152 83776 92400 101024 111496 120736 133055	1288 1932 2790 3864 5182 9660 11592 13524 14989 17248 19712 22176 25050 27925 30800 33674 87165 40245 44352	1680 2520 3640 5040 6720 8400 12600 15120 17640 20440 23520 26880 30240 39080 42000 45920 50680 50680 60480	3360 5040 7280 10080 13440 16800 20720 25200 30240 35280 4080 47040 55760 60480 60480 60480 91840 101360 1109760 120960	1120 1680 2427 3360 5600 6907 8400 10080 11780 11780 20160 22773 25387 26000 30613 33787 40320	

The distance from centre of one link to centre of next is equal to the inside length of link, but in practice 1/32 inch is allowed for weld. This is approximate, and where exactness is required, chain should be made a

FOR CHAIN SHEAVES.—The diameter, if possible, should be not less than twenty times the diameter of chain used.

EXAMPLE. - For 1-inch chain use 20-inch sheaves.

Hemlock bark, dry

SIZES OF FIRE-BRICK.

	9-inch straight $9 \times 416 \times 216$ inches.
	Soap 9×21/4×21/4 "
/ Jamb	Checker 9×3 ×3 4
// 52225	2-inch 9×41/6×2 44
0.414.014	Split 9×4½×1¼ "
9×43/4×23/4	Jamb 9 x 41/6 x 21/6 "
	No. 1 key 9 × 21/2 thick × 41/4 to 4 inches
	wide.
/	113 bricks to circle 12 feet inside diam.
Key	No. 2 key 9 × 21/6 thick × 41/6 to 31/6
(114.914)	inches wide.
9 x 21/x (41/4-21/4)	63 bricks to circle 6 ft. inside diam.
V	No. 3 key 9 x 21/4 thick x 41/4 to 3
•	inches wide,
	88 bricks to circle 8 ft. inside diam.
Wedge \	No. 4 key 9 × 21/6 thick × 41/6 to 21/4
/ / weaks /	inches wide.
0 414 (0)4 (1)6	25 bricks to circle 11/2 ft. inside diam.
9×4%× (2½:1½)	No. 1 wedge (or bullhead). $9 \times 4\frac{1}{2}$ wide $\times 2\frac{1}{2}$ to 2 in.
	thick, tapering lengthwise.
	98 bricks to circle 5 ft. inside diam.
/ Arch /	No. 2 wedge 9 × 416 × 216 to 116 in. thick.
/ >	No. 2 wedge
Øx 436× (236:136)	No. 1 arch 9×41/6×21/6 to 2 in. thick,
(/	tapering breadthwise.
V	72 bricks to circle 4 ft. inside diam.
	No. 2 arch 9×41/6×21/6 to 11/6.
	42 bricks to circle 2 ft. inside diam.
No.1 Skew	No. 1 skew 9 to 7 × 41/6 to 21/6.
1 1	Bevel on one end.
\rightarrow	No. 2 skew 9 × 21/6 × 41/6 to 21/6.
(9:7)×414×234/	Equal bevel on both edges.
	No. 3 skew 9 × 21/6 × 41/6 to 11/6.
	Taper on one edge.
\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	24 inch circle 8½ to 5½ × 4½ × 2½.
No. 2 Skew	Edges curved, 9 bricks line a 24-inch circle.
	36-inch circle 834 to 616 × 416 × 216.
9×234×(434:234)	13 bricks line a 36-inch circle.
V (3	48-inch circle
	17 bricks line a 48-inch circle.
~	1814-inch straight 1314×214×6.
\wedge	1814 inch key No. 1 1814 × 214 × 6 to 5 inch.
No. 8 Skew	90 bricks turn a 12-ft, circle.
\rightarrow	1816-inch key No. 2 1816 × 216 × 6 to 436 inch.
\ /9×2¼×(4½:1½)	52 bricks turn a 6-ft. circle.
<u> </u>	Bridge wall, No. 1
et in ou	Bridge wall, No. 218×6½×8.
36 in. Circle	Mill file
8%	Stock-hole tiles
< 4 ox \	18-inch block
34 64	Flat back
\sim \sim 7	Flat back arch
V	22-inch radius, 56 bricks to circle. Locomotive tile32 × 10 × 3.
	84 × 10 × 8.
	34 × 8 × 3.
Cupola	86× 8×3.
	40 × 10 × 8.
	Tiles slabs and blocks various sizes 12 to 30 inches
	Tiles, slabs, and blocks, various sizes 12 to 30 inches long 8 to 30 inches wide 2 to 6 inches thick.

Thes, siabs, and blocks, various sizes 12 to 30 inches long, 8 to 30 inches wide, 2 to 6 inches thick.

Cupola brick, 4 and 6 inches high, 4 and 6 inches radial width, to line shells 28 to 66 in diameter.

A 9-inch straight brick weighs 7 lbs. and contains 100 cubic inches. (=120 lbs. per cubic foot. Specific gravity 1.93.)

One cubic foot of wall requires 17 9-inch bricks, one cubic yard requires 460. Where keys, wedges, and other "shapes" are used, add 10 per cent in estimating the number required.

3

One ton of fire-clay should be sufficient to lay 3000 ordinary bricks. To secure the best results, fire-bricks should be laid in the same clay from which they are manufactured. It should be used as a thin paste, and not as mortar. The thinner the joint the better the furnace wall. In ordering bricks the service for which they are required should be stated.

NUMBER OF FIRE-BRICK REQUIRED FOR VARIOUS CIRCLES.

<u>.</u>	j.	KEY BRICKS.					A	ARCH BRICKS.			wı	WEDGE BRICKS.			
Diam. of Circle.	Circ	No. 4.	No. 8.	No. 2.	No. 1.	Total.	No. 2.	No. 1.	9,,	Total.	No. 2.	No. 1.	à	Total.	
2233445566778899	60606060606060606060606060606060606060	25 17 9	18 25 38 38 39 19 11 13 6	10 81 32 42 55 55 55 55 55 55 55 55 55 55 55 55 55	9 19 29 38 47 57 66 85 94 104 113 113	25 30 34 38 42 46 51 55 59 63 67 71 76 84 88 92 97 101 109 113 117	42 81 21 10	18 36 54 72 72 72 72 72 72 72 72 72 72 72 72 72	8 15 28 30 88 45 68 68 75 83 90 98 105 113 121	49 49 57 64 72 80 87 102 110 125 139 147 155 170 170 177 185 198	60 48 86 24 12	20 40 59 79 98 98 98 98 98 98 98 98 98 98 98 98 98	8 15 23 30 38 45 61 68 76 83 91 106	60 68 76 88 91 106 1121 128 138 144 151 166 174 181 189 196	

For larger circles than 12 feet use 113 No. 1 Key, and as many 9-inch brick as may be needed in addition.

ANALYSES OF MT. SAVAGE FIRE-CLAY.

(1)	(2)		(8)	(4)
1871	1877.		1878.	1885.
Mass. Institute of Technology.	Report Clays o New Jer Prof. G. H.	of	Second Geological Survey of Pennsylvania.	(2 samples) Dr. Otto Wuth.
50.457	56. 8 0	Silica	. 44.895	56.15
85.904	80.08	Alumina	. 83.558	88.295
	1.15	Titanic acid		• • • • •
1.504	1.18	Peroxide iron	. 1.000	0.59
0.188	••••	Lime	. trace	0.17
9.018	• • • • •	Magnesia	. 0.108	0.115
trace	0.80	Potash (alkalies)	. 0.247	•••••
12.744	10.50	Water and inorg. matter		9.68
100.760	100 450		100.498	100.000

MAGNESIA BRICKS.

"Foreign Abstracts" of the Institution of Civil Engineers, 1893, gives a paper by C. Bischof on the production of magnesia bricks. The material most in favor at present is the magnesite of Styria, which, although less pure considered as a source of magnesia than the Greek, has the property of friting at a high temperature without melting. The composition of the two substances, in the natural and burnt states, is as follows:

Magnesite.	Styrian.	Greek.		
Carbonate of magnesia	90.0 to 96.0% 0.5 to 2.0 3.0 to 6.0 1.0 0.5	94.46% 4,49 FeO 0.06 0,52 Water 0.54		
Burnt Magnesite,				
Magnesia	7.8 18.0	\$2,46 95.36 0.83 10.92 0.56 8.54 0.73 7.98		

At a red heat magnesium carbonate is decomposed into carbonic acid and caustic magnesia, which resembles lime in becoming hydrated and recarbonated when exposed to the air, and possesses a certain plasticity, so that it can be moulded when subjected to a heavy pressure. By long-continued it can be moulded when subjected to a heavy pressure. By long continued or stronger heating the material becomes dead-burnt, giving a form of magnesia of high density, sp. gr. 3.8, as compared with 3.0 in the plastic form, which is unasterable in the air but devoid of plasticity. A mixture of two volumes of dead-burnt with one of plastic magnesia can be moulded into bricks which contract but little in firing. Other binding materials that have been used are: clay up to 10 or 15 per cent; gas-tar, perfectly freed five water, sods, silica, risegas as a solution of magnesium nectate which is readily decomposed by heat, and carbolates of alkalies or time. Among magnesium compounds a weak solution of magnesium nhoride may also be used. For setting the bricks lightly burnt, caustic magnesia, with a small proportion of silica to render it iese refractory, is recommended. The strength of the bricks may be increased by adding iron, either as oxide or silicate. If a porous product is required, sawdust or starch may be added to the mixture. When deed-burnt magnesia sused alone, sods is said to be the best binding material.

See also papers by A. E. Hunt, Trans, A. I. M. E., xvi, 720, and by T. Egles-

See also papers by A. E. Hunt, Trans. A. I. M. E., xvi, 729, and by T. Egleston, Trans. A. I. M. E., xiv, 458.

Asbeston. —J. T. Donald, Eng. and M. Jour., June 27, 1891.

ANALYSIS.

		Canadian.			
	Italian.	Broughton.	Templeton.		
Silice.	. 49.80%	40.57%	49.594		
Magnesia	. 48.37	41.50	42.05		
Ferrous oxide	87	2.81	1.97		
Alumina	. 2,27	.90	2.10		
Weter	. 18.72	13.55	13.46		
	-	******			
	109,58	99.83	100.10		

Chemical analysis throws light upon an important point in connection with asbestos, i.e., the cause of the harsbness of the fibre of some varieties, Ashestos is principally a hydrous silicate of magnesis, i.e., silicate of magnesia combined with water. When harsh fibre is analyzed it is found to contain less water than the soft fibre. In fibre of very fine quality from Black Lake analysis showed 14.38; of water, while a harsh fibred sample gave only 11.70s. If soft fibre be heated to a temperature that will drive of a portion of the combined water, there results a substance so brittle that it may be crumbled between thumb and finger. There is evidently some connection between the consistency of the fibre and the amount of mater in its composition.

STRENGTH OF MATERIALS.

Stress and Strain.—There is much confusion among writers on strength of materials as to the definition of these terms. An external force applied to a body, so as to pull it apart, is resisted by an internal force, or resistance, and the action of these forces causes a displacement of the molecules, or deformation. By some writers the external force is called a stress and the internal force a strain; others call the external force a strain, and the internal force a stress: this confusion of terms is not of importance, as the words stress and strain are quite commonly used synonymously, but the use of the word strain to mean molecular displacement, deformation, or distortion, as is the custom of some, is a corruption of the language. See Engineering News, June 28, 1892. Definitions by leading authorities are given below.

Stress.-A stress is a force which acts in the interior of a body, and resists the external forces which tend to change its shape. A deformation is the amount of change of shape of a body caused by the stress. The word strain is often used as synonymous with stress and sometimes it is also used to designate the deformation. (Merriman.)

The force by which the molecules of a body resist a strain at any point is called the stress at that point.

The summation of the displacements of the molecules of a body for a given point is called the distortion or strain at the point considered. (Burr). Stresses are the forces which are applied to bodies to bring into action their elastic and cohesive properties. These forces cause alterations of the forms of the bodies upon which they act. Strain is a name given to the kind of alteration produced by the stresses. The distinction between stress and strain is not always observed, one being used for the other. (Wood.)

Stresses are of different kinds, viz.: tensile, compressive, transverse, tor-

sional, and shearing stresses.

A tensile stress, or pull, is a force tending to elongate a piece. A com-A tensite stress, or pull, is a force tending to shorten it. A transverse stress tends to bend it. A torsional stress tends to twist it. A shearing stress tends to force one part of it to slide over the adjacent part.

Tensile, compressive, and shearing stresses are called simple stresses.

Transverse stress is compounded of tensile and compressive stresses, and

torsional of tensile and shearing stresses.

To these five varieties of stresses might be added tearing stress, which is either tensile or shearing, but in which the resistance of different portions of the material are brought into play in detail, or one after the other, instead of simultaneously, as in the simple stresses.

Effects of Stresses.—The following general laws for cases of simple tension or compression have been established by experiment. (Merriman):

 When a small stress is applied to a body, a small deformation is produced, and on the removal of the stress the body springs back to its original form. For small stresses, then, materials may be regarded as perfectly elastic.

2. Under small stresses the deformations are approximately proportional to the forces or stresses which produce them, and also approximately pro-

portional to the length of the bar or body.

3. When the stress is great enough a deformation is produced which is partly permanent, that is, the body does not spring back entirely to its briginal form on removal of the stress. This permanent part is termed a set. In such cases the deformations are not proportional to the stress.

4. When the stress is greater still the deformation rapidly increases and

the body finally ruptures.
5. A sudden stress, or shock, is more injurious than a steady stress or than

a stress gradually applied.

a stress gradually applied.

Elastic Limit.—The elastic limit is defined as that point at which the deformations cease to be proportional to the stresses, or, the point at which the rate of stretch (or other deformation) begins to increase. It is also defined as the point at which the first permanent set becomes visible. The last definition is not considered as good as the first, as it is found that with some materials a set occurs with any load, no matter how small, and that with others a set which might be called permanent vanishes with lapse of time, and as it is impossible to get the point of first set without removing

the whole load after each increase of load, which is frequently inconvenient. The elastic limit, defined, however, as the point at which the extensions begin to increase at a higher ratio than the applied stresses, usually corresponds

very nearly with the point of first measurable permanent set.

Apparent Elastic Limit.—Prof. J. B. Johnson (Materials of Construction, p. 19) defines the "apparent elastic limit" as "the point on the stress diagram [a plotted diagram in which the ordinates represent loads and the abscissas the corresponding elongations] at which the rate of decorresponding elongations at which the rate of de-formation is 50% greater than it is at the origin," [the minimum rate]. An equivalent definition, proposed by the author, is that point at which the modulus of extension (length × increment of load per unit of section + in-crement of elongation) is two thirds of the maximum. For steel, with a modulus of elasticity of 30,000,000, this is equivalent to that point at which the increase of elongation in an 8-inch specimen for 1000 lbs. per sq. in. increase of load is 0,0004 in.

Yield-point.—The term yield-point has recently been introduced into the literature of the strength of materials. It is defined as that point at which the rate of stretch suddenly increases rapidly. The difference be which the rate of screen studenty increases rapatry. The unfertice between the elastic limit, strictly defined as the point at which the rate of stretch begins to increase, and the yield-point, at which the rate increases suddenly, may in some cases be considerable. This difference, however, will not be discovered in short test-pieces unless the readings of elongations are

made by an exceedingly fine instrument, as a micrometer reading to -

of an inch. In using a coarser instrument, such as calipers reading to 1/100 of an inch, the elastic limit and the yield-point will appear to be simultaneous. Unfortunately for precision of language, the term yield-point was not introduced until long after the term elastic limit had been almost universally adopted to signify the same physical fact which is now defined by the term yield-point, that is, not the point at which the first change in rate, observable only by a microscope, occurs, but that later point (more or less indefinite as to its precise position) at which the increase is great enough to seen by the naked eye. A most convenient method of determining the point at which a sudden increase of rate of stretch occurs in short specimens, when a testing-machine in which the pulling is done by screws is mens, when a testing-machine in which the pulling is done by screws is used, is to note the weight on the beam at the instant that the beam "drops." used, is to note the weight on the beam at the instant that the beam "drops. During the earlier portion of the test, as the extension is steadily increased by the uniform but slow rotation of the screws, the poise is moved steadily along the beam to keep it in equipoise; suddenly a point is reached at which the beam drops, and will not rise until the elongation has been considerably increased by the further rotation of the screws, the advancing of the poise meanwhile being suspended. This point corresponds practically to the point at which an appreciable permanent set is first found. It is also the point which an appreciable permanent set is first found. It is also the point which has hitherto been called in practice and in text-books the elastic limit and which an approximate the second of the secon able only by micrometric measurements, is more precise and scientific.

In tables of strength of materials hereafter given, the term elastic limit is used in its customary meaning, the point at which the rate of stress has begun to increase, as observable by ordinary instruments or by the drop of the beam. With this definition it is practically synonymous with yield-

point.

Coefficient (or Modulus) of Elasticity.—This is a term expressing the relation between the amount of extension or compression of a material and the load producing that extension or compression.

It is defined as the load per unit of section divided by the extension per

unit of length.

Let P be the applied load, k the sectional area of the piece, l the length of the part extended, λ the amount of the extension, and E the coefficient of elasticity. Then P + k = the load on a unit of section; $\lambda + l =$ the elongation of a unit of length.

 $E = \frac{P}{k} + \frac{\lambda}{l} = \frac{Pl}{k\lambda}.$

The coefficient of elasticity is sometimes defined as the figure expressing the load which would be necessary to elongate a piece of one square inch section to double its original length, provided the piece would not break, and the ratio of extension to the force producing it remained constant. This definition follows from the formula above given, thus: If k = one squar inch, I and k = cach = one inch, then E = P. Within the elastic limit, when the deformations are proportional to the square of the squa

stresses, the coefficient of elasticity is constant, but beyond the elastic limit it decreases rapidly.

In cast iron there is generally no apparent limit of elasticity, the deforma-tions increasing at a faster rate than the stresses, and a permanent set being produced by small loads. The coefficient of elasticity therefore is not constant during any portion of a test, but grows smaller as the load increases, The same is true in the case of timber. In wrought iron and steel, however, there is a well-defined elastic limit, and the coefficient of elasticity within that limit is nearly constant.

Resistance of a Material.—Within the elastic limit, the resistance increasing uniformly from zero stress to the stress at the elastic limit, the work done by a load applied gradually is equal to one half the product of the final stress by the extension or other deformation. Beyond the clastic limit, the extensions increasing more rapidly than the loads, and the strain diagram approximating a parabolic form, the work is approximately equal to two thirds the product of the maximum stress by the extension.

The amount of work required to break a bar, measured usually in inch-pounds, is called its resilience; the work required to strain it to the elastic

limit is called its elastic resilience. (See page 270.)
Under a load applied suddenly the momentary elastic distortion is equal

to twice that caused by the same load applied gradually.

When a solid material is exposed to percussive stress, as when a weight falls upon a beam transversely, the work of resistance is measured by the

product of the weight into the total fail.

Rievation of Ultimate Resistance and Elastic Limit,—it was first observed by Prof. B. H. Thurston, and Commander L. A. Beards-lee, U. S. N., independently, in 1878, that if wrought from be subjected to atrees beyond its elastic limit, but not beyond its ultimate resistance, and then allowed to "rest" for a definite interval of time, a considerable increase of elastic limit and ultimate resistance may be experienced. In other words, the application of stress and subsequent "rest" increases the resistance of wrought iron.

This "rest" may be an entire release from stress or a simple holding the

test-piece at a given intensity of stress.

Commander Beardslee prepared twelve specimens and subjected them to an intensity of stress equal to the ultimate resistance of the material, with-out breaking the specimens. These were then allowed to rest, entirely free from stress, from 24 to 80 hours, after which period they were again stressed until broken. The gain in ultimate resistance by the rest was found to vary from 4.4 to 17 per cent.

This elevation of elastic and ultimate resistance appears to be peculiar to

iron and steel: it has not been found in other metals.

Belation of the Elastic Limit to Endurance under Re-Meantless of the same statement to minuterance causes meaned Stresses (condensed from Baginering, August 7, 1891).—
When engineers first began to test materials, it was soon recognized that if a specimen was loaded beyond a certain point it did not recover its original dimensions on removing the load, but took a permanent set; this point was called the elastic limit. Since below this point a bar appeared to recover completely its original form and dimensions on removing the load, it appeared obvious that it had not been injured by the load, and beace the working load might be deduced from the elastic limit by using a small factor of safety.

Experience showed, however, that in many cases a har would not carry safely a stress anywhere near the elastic limit of the material as determined by these experiments, and the whole theory of any connection between the elastic limit of a bar and its working load became almost discredited, and engineers employed the ultimate strength only in deducing the safe working load to which their structures might be subjected. Still, as experience accumulated it was observed that a higher factor of safety was required for a live

load than for a dead one.

In 1871 Wöhler published the results of a number of experiments on bars of iron and steel subjected to live loads. In these experiments the stresses were put on and removed from the specimens without impact, but it was, nevertheless, found that the breaking stress of the materials was in every case much below the statical breaking load. Thus, a bar of Krupp's axle steel having a tenacity of 49 tons per square inch broke with a stress of 28.6 tons per square inch, when the load was completely removed and replaced without impact 170,000 times. These experiments were made on a large number of different brands of iron and steel, and the results were concordant in showing that a bar would break with an alternating stress of only, say, one third the statical breaking strength of the material, if the repetitions of stress were sufficiently numerous. At the same time, however, it appeared from the general trend of the experiments that a bar would stand an indefinite number of alternations of stress, provided the stress was kept below the limit.

Prof. Bauschinger defines the elastic limit as the point at which stress ceases to be sensibly proportional to strain, the latter being measured with

a mirror apparatus reading to $\frac{1}{5000}$ th of a millimetre, or about $\frac{1}{100000}$ in.

This limit is always below the yield-point, and may on occasion be zero. On loading a bar above the yield-point, this point rises with the stress, and the rise continues for weeks, months, and possibly for years if the bar is left at rest under its load. On the other hand, when a bar is loaded beyond its true elastic limit, but below its yield-point, this limit rises, but reaches a maximum as the yield-point, is approached, and then falls rapidly, reaching even to zero. On leaving the bar at rest under a stress exceeding that of its primitive breaking-down point the elastic limit begins to rise again, and may, if left a sufficient time, rise to a point much exceeding its previous

This property of the elastic limit of changing with the history of a bar has This property of the elastic limit of changing with the listory of a bar had done more to discredit it than anything else, nevertheless it now seems as if it, owing to this very property, were once more to take its former place in the estimation of engineers, and this time with fixity of tenure. It had long been known that the limit of elasticity might be raised, as we have said, to almost any point within the breaking load of a bar. Thus, in some experiments by Professor Styffe, the elastic limit of a puddled-steel bar was raised 18,000 lbs. by subjecting the bar to a load exceeding its primitive elastic

limit.

A bar has two limits of elasticity, one for tension and one for compression. Banachinger loaded a number of bars in tension until stress ceased to be sensibly proportional to strain. The load was then removed and the bar sension of the sense of the sen ceeded. This process raises the elastic limit in compression, as would be found on testing the bar in compression a second time. In place of this, however, it was now again tested in tension, when it was found that the artificial raising of the limit in compression had lowered that in tension below its previous value. By repeating the process of alternately testing in tension and compression, the two limits took up points at equal distances from the line of no load, both in tension and compression. These limits Bauschinger calls natural elastic limits of the bar, which for wrought iron correspond to a stress of about 814 tons per square inch, but this is practically the limiting load to which a bar of the same material can be strained alternated in tension and compression without breaking when the loading is nately in tension and compression, without breaking when the loading is repeated sufficiently often, as determined by Wöhler's method.

As received from the rolls the elastic limit of the bar in tension is above

the natural elastic limit of the bar as defined by Bauschinger, having been the natural elastic limit of the bar as defined by Bauschinger, having been artificially raised by the deformations to which it has been subjected in the process of manufacture. Hence, when subjected to alternating stresses, the limit in tension is immediately lowered, while that in compression is raised until they both correspond to equal loads. Hence, in Wöhler's experiments, in which the bars broke at loads nominally below the elastic limits of the material, there is every reason for concluding that the loads were really greater than true elastic limits of the material. This is confirmed by tests on the connecting-road of empines, which of course works. firmed by tests on the connecting-rods of engines, which of course work under alternating stresses of equal intensity. Careful experiments on old rods show that the elastic limit in compression is the same as that in tension, and that both are far below the tension elastic limit of the material as

received from the rolls.

The common opinion that straining a metal beyond its elastic limit injures it appears to be untrue. It is not the mere straining of a metal beyond one elastic limit that injures it, but the straining, many times repeated, beyond its two elastic limits. Sir Benjamin Baker has shown that in bending a shell plate for a boiler the metal is of necessity strained beyond its elastic limit, so that stresses of as much as 7 tons to 15 tons per square inch may obtain in it as it comes from the rolls, and unless the plate is annealed, has stresses will still exist after it has been built into the boiler. In such a case, however, when exposed to the additional stress due to the pressure inside

the boiler, the overstrained portions of the plate will relieve themselves by stretching and taking a permanent set, so that probably after a year's working very little difference could be detected in the stresses in a plate built into the boiler as it came from the bending rolls, and in one which had been annealed, before riveting into place, and the first, in spite of its having been strained beyond its elastic limits, and not subsequently annealed, would be as strong as the other.

Resistance of Metals to Repeated Shocks.

More than twelve years were spent by Wöhler at the instance of the Prussian Government in experimenting upon the resistance of Iron and steel to repeated stresses. The results of his experiments are expressed in what is known as Wöhler's law, which is given in the following words in Dubois's translation of Weyrauch:

"Rupture may be caused not only by a steady load which exceeds the carrying strength, but also by repeated applications of stresses, none of which are equal to the carrying strength. The differences of these stresses are measures of the disturbance of continuity, in so far as by their increase the minimum stress which is still necessary for rupture diminishes."

A practical illustration of the meaning of the first portion of this law may be given thus: If 50,000 pounds once applied will just break a bar of iron or steel, a stress very much less than 50,000 pounds will break it if repeated sufficiently often.

sufficiently often.

E

This is fully confirmed by the experiments of Fairbairn and Spangenberg, as well as those of Wöhler; and, as is remarked by Weyrauch, it may be considered as a long-known result of common experience. It partially ac-counts for what Mr. Holley has called the "intrinsically ridiculous factor of safety of six."

Another "long-known result of experience" is the fact that rupture may be caused by a succession of shocks or impacts, none of which alone would be sufficient to cause it. Iron axies, the piston-rods of steam hammers, and other pieces of metal subject to continuously repeated shocks, invariably break after a certain length of service. They have a "life" which is limited.

Several years ago Fairbairn wrote: "We know that in some cases wrought iron subjected to continuous vibration assumes a crystalline structure, and that the cohesive powers are much deteriorated, but we are ignorant of the causes of this change." We are still ignorant, not only of the causes of this change, but of the conditions under which it takes place. Who knows whether wrought iron subjected to very slight continuous vibration will endure forever? or whether to insure final rupture each of the continuous small shocks must amount at least to a certain percentage of single heavy shock (both measured in foot-pounds), which would cause rupture with one application? Wöhler found in testing iron by repeated stresses (not impacts) that in one case 400,000 applications of a stress of 500 centners to the square inch caused rupture, while a similar bar remained sound after 48,000,000 applications of a stress of 300 centners to the square inch (1 centner = 110.2 lbs.)

Who knows whether or not a similar law holds true in regard to repeated shocks? Suppose that a bar of iron would break under a single impact of 1000 foot-pounds, how many times would it be likely to bear the repetition of 100 foot-pounds, or would it be safe to allow it to remain for fifty years subjected to a continual succession of blows of even 10 foot-pounds each?

Mr. William Metcalf published in the Metallurgical Review, Dec. 1877, the results of some tests of the life of steel of different percentages of carbon under impact. Some small steel pitmans were made, the specifications for which required that the unloaded machine should run 4½ hours at the rate of 1200 revolutions per minute before breaking.

The steel was all of uniform quality, except as to carbon. Here are the results; The

.30 C. ran 1 h. 21 m. Heated and bent before breaking. .49 C. 1 h. 28 m., .48 C. 4 h. 57 m. Broke without heating " 8 h. 50 m. .65 C. .80 C. Broke at weld where imperfect. " 5 h. 40 m. " 18 h. .84 C. .87 C. Broke in weld near the end. Ran 4.55 m., and the machine broke down.

Some other experiments by Mr. Metcalf confirmed his conclusion, viz.

that high-carbon steel was better adapted to resist repeated shocks and vibrations than low-carbon steel.

These results, however, would scarcely be sufficient to induce any engineer to use .84 carbon steel in a car-axle or a bridge-rod. Further experiments are needed to confirm or overthrow them.

(See description of proposed apparatus for such an investigation in the author's paper in Trans. A. I. M. E., vol. viii., p. 76, from which the above

extract is taken.)

Stresses Produced by Suddenly Applied Forces and Shocks.

(Mansfield Merriman, R. R. & Eng. Jour., Dec. 1889.)

Let P be the weight which is dropped from a height h upon the end of a bar, and let y be the maximum elongation which is produced. The work performed by the falling weight, then, is

W=P(h+y),

and this must equal the internal work of the resisting molecular stresses. The stress in the bar, which is at first 0, increases up to a certain limit Q, which is greater than P; and if the elastic limit be not exceeded the elongation increases uniformly with the stress, so that the internal work is equal to the mean stress 1/2Q multiplied by the total elongation y, or

$$W = 1/2 Qy$$
.

Whence, neglecting the work that may be dissipated in heat,

$$1/2Qy = Ph + Py.$$

If e be the elongation due to the static load P, within the elastic limit $y = \frac{Q}{D}e$; whence

$$Q = P\left(1 + \sqrt{1 + 2\frac{h}{e}}\right), \quad \dots \quad \dots \quad (1)$$

which gives the momentary maximum stress. Substituting this value of O. there results

$$y = e\left(1 + \sqrt{1 + 2\frac{h}{e}}\right), \quad \dots \quad (2)$$

which is the value of the momentary maximum elongation. A shock results when the force P, before its action on the bar, is moving with velocity, as is the case when a weight P falls from a height h. This above formulas show that this height h may be small if e is a small quantity, and yet very great stresses and deformations be produced. For instance, let h = 4e, then Q = 4P and y = 4e; also let h = 12e, then Q = 6e. Or take a wrought-iron bar 1 in. square and 5 ft. long: under a steady load of 5000 lbs. this will be compressed about 0.012 in., supposmosthat to lateral flavoure occurs; but if a weight of 5000 lbs. drops upon its end that no lateral flexure occurs; but if a weight of 5000 lbs. drops upon its end from the small height of 0.048 in. there will be produced the stress of 20,000 lbs.

A suddenly applied force is one which acts with the uniform intensity P upon the end of the bar, but which has no velocity before acting upon it. This corresponds to the case of h=0 in the above formulas, and gives Q=2P and y = 2e for the maximum stress and maximum deformation. Prob ably the action of a rapidly-moving train upon a bridge produces stresses.

of this character.

Increasing the Tensile Strength of Iron Bars by Twisting them.—Ernest L. Ransome of San Francisco has obtained an English Patent, No. 16221 of 1888, for an "improvement in strengthening and testing wrought metal and steel rods or bars, consisting in twisting the same in a cold state.

Any defect in the lamination of the metal which would be a supported that the statement of the otherwise be concealed is revealed by twisting, and imperfections are shown at once. The treatment may be applied to bolts, suspension-rods or bars subjected to tensile strength of any description."

Results of tests of this process were reported by Lieutenant F. P. Gilmore, U. S. N., in a paper read before the Technical Society of the Pacific Coast, published in the Transactions of the Society for the month of December, 1888. The experiments include trials with thirty-nine bars, twenty-nine of which were variously twisted, from three-eighths of one turn to six turns per foot. The test-pieces were cut from one and the same bar, and accurate

measured and numbered. From each lot two pieces without twist were tested for tensile strength and ductility. One group of each set was twisted until the pieces broke, as a guide for the amount of twist to be given those to be tested for tensile strain.

The following is the result of one set of Lieut. Gilmore's tests, on iron bars 8 in. long, .719 in. diameter.

No. of Bars.	Conditions.	Twists in Turns.	Twists per ft.	Tensile Strength.	Tensile per sq. in,	Gain per cent.
2 2 2 1	Not twisted. Twisted cold.	0 14 1 2 21/2	0 94 11/2 8 33/4	22,000 23,900 25,800 26,300 26,400	54,180 59,020 63,500 64,750 65,000	9 17 19 20

Tests that corroborated these results were made by the University of California in 1889 and by the Low Moor Iron Works, England, in 1890.

TENSILE STRENGTH.

The following data are usually obtained in testing by tension in a testing machine a sample of a material of construction:

The load and the amount of extension at the elastic limit.

The maximum load applied before rupture.

The elongation of the piece, measured between gauge-marks placed a stated distance apart before the test; and the reduction of area at the point of fracture.

The load at the elastic limit and the maximum load are recorded in pounds per square inch of the original area. The elongation is recorded as a percentage of the stated length between the gauge-marks, and the reduction area as a percentage of the original area. The coefficient of elasticity is calculated from the ratio the extension within the elastic limit per inch of length bears to the load per square inch producing that extension.

On account of the difficulty of making accurate measurements of the frac-

tured area of a test-piece, and of the fact that elongation is more valuable than reduction of area as a measure of ductility and of resilience or work of resistance before rupture, modern experimenters are abandoning the custom of reporting reduction of area. The "strength per square inch of fractured section" formerly frequently used in reporting tests is now almost entirely abandoned. The data now calculated from the results of a tensile test for commercial purposes are: 1. Tensile strength in pounds per square inch of original area. 2. Elongation per cent of a stated length between gauge marks, usually 8 inches. 3. Elastic limit in pounds per square inch of original area.

The short or grooved test specimen gives with most metals, especially with wrought iron and steel, an apparent tensile strength much higher than the real strength. This form of test-plece is now almost entirely abandoned.

The following results of the tests of six specimens from the same 11/4" steel bar illustrate the apparent elevation of elastic limit and the changes in other properties due to change in length of stems which were turned down in each specimen to .798" diameter. (Jas. E. Howard, Eng. Congress 1898 Section G.)

Description of Stem.	Elastic Limit,	Tensile Strength,	Contraction of
	Lbs. per Sq. In.	Lbs. per Sq. In.	Area, per cent.
1.00" long	64,900	94,400	49.0
	65,320	97,800	48.4
	68,000	102,420	89.6
.4" radius	75,000	116,880	81.6
V-shaped groove	86,000, about	134,960	23.0
	90,000, about	117,000	Indeterminate.

Tests plate made by the author in 1879 of straight and grooved test-pieces of boiler-plate steel out from the same gave the following results:

5 straight pieces, 56,605 to 59,012 lbs. T. S. Aver. 57,566 lbs. 4 grooved "64,341 to 67,400 " "65,452 "

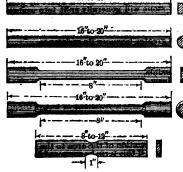
Excess of the short or grooved specimen, 21 per cent, or 12,114 lbs.

Measurement of Elongation.—In order to be able to compare records of elongation, it is necessary not only to have a uniform length of records of elongation, it is necessary not only to have a uniform length of section between gauge-marks (say 8 inches), but to adopt a uniform method of measuring the elongation to compensate for the difference between the apparent elongation when the piece breaks near one of the sauge-marks, and when it breaks midway between them. The following method is recommended (Trans. A. S. M. E., vol. xi., p. 632):

Mark on the specimen divisions of 1/2 inch each. After fracture measure from the point of fracture the length of 8 of the marked spaces on each fractured portion (or 7 + on one side and 8 + on the other if the fracture is not at one of the marks). The sum of these measurements, less 8 inches, is a superstiment of 8 trackers of the registral length 1/2 the fracture is a

the elongation of 8 inches of the original length. If the fracture is so near one end of the specimen that 7+spaces are not left on the shorter portion, then take the measurement of as many spaces (with the fractional part next to the fracture) as are left, and for the spaces lacking add the measurement of as many corresponding spaces of the longer portion as are necessary to make the 7+ spaces.

Shapes of Specimens for Tensile Tests.—The shapes shown in Fig. 75 were recommended by the author in 1882 when he was connected



-16["]to 20"--

No. 1. Square or flat bar, as rolled.

No. 2. Round bar, as rolled.

No. 8. Standard shape for flats or squares. Fillets 1/2 inch radius.

No. 4. Standard shape for rounds. Fillets 1/4 in. radius.

No. 5. Government shape for marine boiler-plates of iron. Not recommended for other tests, as results are generally in error.

Frg. 75.

the test should be stated.

with the Pittsburgh Testing Laboratory. They are now in most general use, the earlier forms, with 5 inches or less in length between shoulders, being almost entirely abandoned.

Precautions Required in making Tensile Tests.—The testing-machine itself should be tested, to determine whether its weighing apparatus is accurate, and whether it is so made and adjusted that in the test of a property made specimen the line of strain of the testing-machine is absolutely in line with the axis of the specimen.

The energinger should be a changed that it will not give an incorrect record.

The specimen should be so shaped that it will not give an incorrect record

of strength.

It should be of uniform minimum section for not less than five inches of its length.

Regard must be had to the time occupied in making tests of certain mate-Wrought iron and soft steel can be made to show a higher than their actual apparent strength by keeping them under strain for a great length

In testing soft alloys, copper, tin, zinc, and the like, which flow under constant strain their highest apparent strength is obtained by testing them rapidly. In recording tests of such materials the length of time occupied in

For very accurate measurements of elongation, corresponding to increments of load during the tests, the electric contact micrometer, described in Trans. A. S. M. E., vol. vi., p. 479, will be found convenient. When readings of elongation are then taken during the test, a strain diagram may be plotted from the reading, which is useful in comparing the qualities of different specimens. Such strain diagrams are made automatically by the new Olsen testing-machine, described in Jour. Frank. Inst. 1891.

The coefficient of elasticity should be deduced from measurement ob-served between fixed increments of load per unit section, say between 2000 and 12,000 pounds per square inch or between 1000 and 11,000 pounds instead of between 0 and 10,000 pounds.

COMPRESSIVE STRENGTH.

What is meant by the term "compressive strength" has not yet been settled by the authorities, and there exists more confusion in regard to this term than in regard to any other used by writers on strength of materials. The reason of this may be easily explained. The effect of a compressive stress upon a material varies with the nature of the material, and with the shape and size of the specimen tested. While the effect of a tensile stress is to produce rupture or separation of particles in the direction of the line of strain, the effect of a compressive stress on a piece of material may be either to cause it to fly into splinters, to separate into two or more wedge-shaped pieces and fly apart, to bulge, buckle, or bend, or to flatten out and utterly resist rupture or separation of particles. A piece of speculum metal under compressive stress will exhibit no change of appearance until rupture takes place, and then it will fly to pieces as suddenly as if blown apart by gun-powder. A piece of cast iron or of stone will generally split into wedge-shaped fragments. A piece of wrought iron will buckle or bend. A piece of wood or zinc may bulge, but its action will depend upon its shape and size.

A piece of lead will flatten out and resist compression till the last degree;

that is, the more it is compressed the greater becomes its resistance.

Air and other gaseous bodies are compressible to any extent as long as they retain the gaseous condition. Water not confined in a vessel is compressed by its own weight to the thickness of a mere film, while when confined in a vessel it is almost incompressible.

ned in a vessel it is almost incompression.
It is probable, although it has not been determined experimentally, that
It is probable, although it has not been determined experimentally, that solid bodies when confined are at least as incompressible as water. they are not confined, the effect of a compressive stress is not only to shorten them, but also to increase their lateral dimensions or bulge them.

shorten them, but also to increase their lateral dimensions or buige them. Lateral strains are therefore induced by compressive stresses.

The weight per square inch of original section required to produce any given amount or percentage or shortening of any material is not a constant quantity, but varies with both the length and the sectional area, with the shape of this sectional area, and with the relation of the area to the length. The "compressive strength" of a material, if this term be supposed to mean the weight in pounds per square inch necessary to cause rupture, may vary with every size and shape of specimen experimented upon. Still more difficult would it be to state what is the "compressive strength" of a material which does not rupture at all but flattens out. Suppose we are testiment. which does not rupture at all, but flattens out. Suppose we are testing a cylinder of a soft metal like lead, two inches in length and one inch in diameter, a certain weight will shorten it one per cent, another weight ten per cent, another fifty per cent, but no weight that we can place upon it will rupture it, for it will flatten out to a thin sheet. What, then, is its compressive strength? Again, a similar cylinder of soft wrought iron would probably compress a few per cent, bulging evenly all around; it would then commence to bend, but at first the bend would be imperceptible to the eye and neall to be measured. Soon this bend would be great enough to be noticed, and finally the piece might be bent nearly double, or otherwise distorted. What is the "compressive strength" of this piece of iron? Is it the weight per square inch which compresses the piece one per cent or five per cent, that which causes the first bending (impossible to be discovered),

per cent, that which causes the hist century impressible to be discovered, or that which causes a perceptible bend?

As showing the confusion concerning the definitions of compressive strength, the following statements from different authorities on the strength of wrought iron are of interest.

Wood's Resistance of Materials states, "comparatively few experiments

have been made to determine how much wrought iron will sustain at the point of crushing. Hodgkinson gives 65,000, Rondulet 70,800, Weisbach 72,000 Rankine 30,000 to 40,000. It is generally assumed that wrought iron will resist about two thirds as much crushing as to tension, but the experiments fail to give a very definite ratio."

Mr. Whipple, in his treatise on bridge-building, states that a bar of good

wrought iron will sustain a tensile strain of about 60,000 pounds per square inch, and a compressive strain, in pieces of a length not exceeding twice the least diameter, of about 90,000 pounds.

The following values, said to be deduced from the experiments of Major Wade, Hodgkinson, and Capt. Meigs, are given by Haswell:

American	wrough	t iroı	a	127,720	lbs.
••	"	44	(mean)	85,500	- 66
English	44	66	• •	65,200 40,000	64
Tongue			••••••	40,000	- 46

Stoney states that the strength of short pillars of any given material, all having the same diameter, does not vary much, provided the length of the piece is not less than one and does not exceed four or five diameters, and that the weight which will just crush a short prism whose base equals one aquare inch, and whose height is not less than 1 to 1½ and does not exceed 4 or 5 diameters, is called the crushing strength of the material. It would be well if experimenters would all agree upon some such definition of the term "crushing strength," and insist that all experiments which are made for the purpose of testing the relative values of different materials in compression be made on specimens of exactly the same shape and size. An arbitrary size and shape should be assumed and agreed upon for this purpose. The size mentioned by Stoney is definite as regards area of section. viz., one square inch, but is indefinite as regards length, viz., from one to five diameters. In some metals a specimen five diameters long would bend, and give a much lower apparent strength than a specimen having a length of one diameter. The words "will just crush" are also indefinite for ductile materials, in which the resistance increases without limit if the piece tested does not bend. In such cases the weight which causes a certain percentage of compression, as five, ten, or fifty per cent, should be assumed as the crushing strength.

For future experiments on crushing strength three things are desirable: First, an arbitrary standard shape and size of test specimen for comparison of all materials. Secondly, a standard limit of compression for dutilin materials, which shall be considered equivalent to fracture in brittle materials. Thirdly, an accurate knowledge of the relation of the crushing strength of a specimen of standard shape and size to the crushing strength of specimens of all other shapes and sizes. The latter can only be secured by a very extensive and accurate series of experiments upon all kinds of materials, and on specimens of a great number of different shapes

The author proposes, as a standard shape and size, for a compressive test specimen for all metals, a cylinder one inch in length, and one half square inch in sectional area, or 0.788 inch diameter; and for the limit of compression equivalent to fracture, ten per cent of the original length. The term "compressive strength," or "compressive strength of standard specimen," would then mean the weight per square inch required to fracture by compressive stress a cylinder one inch long and 0.798 inch diameter, or to reduce its length to 0.9 inch if fracture does not take place before that reduction in length is reached. If such a standard, or any standard size whatever, had been used by the earlier authorities on the strength of materials, we never would have had such discrepancies in their statements in regard to

the compressive strength of wrought iron as those given above.

The reasons why this particular size is recommended are: that the sectional area, one-half square inch, is as large as can be taken in the ordinary testing-machines of 100,000 pounds capacity, to include all the ordinary metals of construction, cast and wrought iron, and the softer steels; and that the length, one inch, is convenient for calculation of percentage of compression. If the length were made two inches, many materials would bend in testing, and give incorrect results. Even in cast iron Hodgkinson found as the mean of several experiments on various grades, tested in specimens 34 inch in height, a compressive strength per square inch of 94,730 pounds, while the mean of the same number of specimens of the same irons tested in pleese 114 inches in height was only 88,800 pounds. The best size and shape of standard specimen should, however, be settled upon only after consultation and agreement among several authorities.

The Committee on Standard Tests on the American Society of Mechanical

Engineers say (vol. xi., p. 624):
"Although compression tests have heretofore been made on diminutive sample pieces, it is highly desirable that tests be also made on on uninhuture from 10 to 20 diameters in length, corresponding more nearly with actual practice, in order that elastic strain and change of shape may be determined by using proper measuring apparatus.

The elastic limit, modulus or coefficient of elasticity, maximum and ulti-mate resistances, should be determined, as well as the increase of section at

various points, vis., at bearing surfaces and at crippling point.

The use of long compression-test pieces is recommended, because the investigation of short cubes or cylinders has led to no direct application of the constants obtained by their use in computation of actual atructures, which have always been and are now designed according to empirical for mulæ obtained from a few tests of long columns."

COLUMNS, PILLARS, OR STRUTS.

Hodgkinson's Formula for Columns.

P= crushing weight in pounds; d= exterior diameter in inches; $d_1=$ interior diameter in inches; L= length in feet.

Both ends rounded, the Both ends flat, the length of the column length of the column Kind of Column. exceeding 15 times exceeding 30 times its diameter. its diameter. Solid cylindrical col- $P = 98,920 \frac{d^{3.55}}{}$ umns of cast iron..... Hollow cylindrical col-) umns of cast iron..... \ Solid cylindrical col-) umns of wrought iron. Solid square pillar of Dantzic oak (dry).... § Solid square pillar of) red deal (dry).....

The above formulæ apply only in cases in which the length is so great that the column breaks by bending and not by simple crushing. If the column be shorter than that given in the table, and more than four or five times its diameter, the strength is found by the following formula:

$$W = \frac{PCK}{P + \frac{5}{2}CK}$$

in which P= the value given by the preceding formulæ, K= the transverse section of the column in square inches, C= the ultimate compressive resistance of the material, and W= the crushing strength of the column.

Hodgkinson's experiments were made upon comparatively short columns, the greatest length of cast-iron columns being 60½ inches, of wrought iron 90% inches.

The following are some of his conclusions:

In all long pillars of the same dimensions, when the force is applied in the direction of the axis, the strength of one which has flat ends is about

three times as great as one with roun ed ends.

2. The strength of a pillar with 'ne nd rounded and the other flat is an arithmetical mean between the two given in the preceding case of the same

3. The strength of a pillar having both ends firmly fixed is the same as one of half the length with both ends rounded.

4. The strength of a pillar is not increased more than one seventh by enlarging it at the middle.

Gordon's formula deduced from Hodgkinson's experiments are more renerally used than Hodgkinson's own. They are:

Columns with both ends fixed or flat, P =

Columns with one end flat, the other end round, $P = \frac{fS}{1 + 1.8a_{-1}^{2}}$

Columns with both ends round, or hinged, $P = \frac{fS}{1 + 4a_{-e}^{p}}$;

S = area of cross-section in inches;

P = ultimate resistance of column, in pounds;

r = least radius of gyration, in inches, r² = Moment of inertia

area of section

l = length of column in inches;

a = a coefficient depending upon the material; f and a are usually taken as constants; they are really empirical variables, dependent upon the dimensions and character of the column as well as upon the material. (Burr.)

For solid wrought-iron columns, values commonly taken are: f = 36,000 to

40,000; $\alpha = 1/96,000$ to 1/40,000. For solid east-iron columns, f = 80,000, a = 1/6400.

 $\frac{1}{1+\frac{1}{800}}\frac{l^2}{d^2}, l = \text{length and}$ For hollow cast-iron columns, fixed ends, p = -

d= diameter in the same unit, and p= strength in lbs, per square inch. The coefficient of l^2/d^2 is given various values, as 1/400, 1/500, 1/600, and 1/800, by different writers. The use of Gordon's formula, with any coefficients derived from Hodgkinson's experiments, for cast-iron columns is to be deprecated. See Strength of Cast-iron Columns, pp. 250, 251. Sir Benjamin Baker gives,

For mild steel, f = 67,000 lbs., a = 1/22,400, For strong steel, f = 114,000 lbs., a = 1/14,400

Prof. Burr considers these only loose approximations for the ultimate resistances. See his formulæ on p. 259.

For dry timber Rankine gives f = 7200 lbs., $\alpha = 1/3000$.

MOMENT OF INERTIA AND RADIUS OF GYRATION.

The moment of inertia of a section is the sum of the products of each elementary area of the section into the square of its distance from an assumed axis of rotation, as the neutral axis.

The radius of gyration of the section equals the square root of the quotient of the moment of inertia divided by the area of the section. If

R = radius of gyration, I = moment of inertia and A = area,

$$R = \sqrt{\frac{I}{A}}. \qquad \frac{I}{A} = R^2.$$

The moments of inertia of various sections are as follows:

The Homelton of Mertals of various sections are as follows: d = diameter; o outside diameter; $d_1 = \text{inside}$ diameter; b = breadth; h = depth; b_1 , h_1 , inside breadth and diameter; Solid rectangle $I = 1/12bh^2$; Hollow rectangle $I = 1/12(bh^3 - b_1h_1^3)$; Solid square $I = 1/12(bh^3 - b_1h_1^3)$; Hollow square $I = 1/12(bh^3 - b_1h_1^3)$; Solid cylinder $I = 1/64\pi d^4$; Hollow cylinder $I = 1/64\pi (d^4 - d_1^4)$.

Moments of Inertia and Radius of Gyration for Various Sections, and their Use in the Formulas for Strength of Girders and Columns.—The strength of sections to resist strains, either as girders or as columns, depends not only on the area but also on the form of the section, and the property of the section which forms the basis of the constants used in the formulas for strength of girders and columns to express the effect of the form, is its moment of inertia about its neutral axis. The modulus of resistance of any section to transverse bending is its moment of inertia divided by the distance from the neutral axis to the fibres farthest removed from that axis; or

Section modulus
$$= \frac{\text{Moment of inertia}}{\text{Distance of extreme fibre from axis}}$$
. $Z = \frac{I}{y}$

Moment of resistance = section modulus × unit stress on extreme fibre.

Moment of Inertia of Compound Shapes. (Pencoyd Iron Works.—The moment of inertia of any section about any axis is equal to the I about a parallel axis passing through its centre of gravity + (the area of the section x the square of the distance between the axes).

By this rule, the moments of inertia or radii of gyration of any single sections being known, corresponding values may be obtained for any combination of these sections.

tion of these sections.

Radius of Gyration of Compound Shapes.—In the case of a pair of any shape without a web the value of R can always be found without considering the moment of inertia.

The radius of gyration for any section around an axis parallel to another axis passing through its centre of gravity is found as follows: Let r = radius of gyration around axis through centre of gravity; R = radius of gyration around another axis parallel to above; d = distance be-

tween axes: $R = \sqrt{d^2 + r^2}$. When r is small, R may be taken as equal to d without material error. Graphical Method for Finding Hadius of Gyration.—Benj. F. La Rue, Eng. News, Feb. 2, 1893, gives a short graphical method for finding the radius of gyration of hollow, cylindrical, and rectangular columns of the radius of gyration of hollow, cylindrical, and rectangular columns of the radius of gyration of hollow, cylindrical, and rectangular columns of the radius of the radius of gyration of hollows. umns, as follows:

For cylindrical columns:

Lay off to a scale of 4 (or 40) a right-angled triangle, in which the base equals the outer diameter, and the altitude equals the inner diameter of the column, or vice versa. The hypothenuse, measured to a scale of unity (or 10), will be the radius of gyration sought.

This depends upon the formula

$$G = \sqrt{\frac{\text{Mom. of Inertia}}{\text{Area}}} = \frac{\sqrt{D^2 + d^2}}{4}$$

in which A =area and D =diameter of outer circle, a =area and d =diameter of inner circle, and G = radius of gyration. $\sqrt{D^2 + d^2}$ is the expression for the hypothenuse of a right-angled triangle, in which D and d are the base and altitude.

The sectional area of a hollow round column is $.7854(D^2-d^2)$. By constructing a right-angled triangle in which D equals the hypothenuse and dequals the altitude, the base will equal $\sqrt{D^2-d^2}$. Calling the value of this expression for the base B, the area will equal .7854 B^2 . Value of G for square columns:

Lay off as before, but using a scale of 10, a right-angled triangle of which the base equals D or the side of the outer square, and the altitude equals d, the side of the inner square. With a scale of 3 measure the hypothenuse, which will be, approximately, the radius of gyration.

This process for square columns gives an excess of slightly more than 45.

By deducting 45 from the result, a close approximation will be obtained.

A very close result is also obtained by measuring the hypothenuse with the same scale by which the base and altitude were laid off, and multiplying by the decimal 0.29; more exactly, the decimal is 0.28867. The formula is

$$G = \sqrt{\frac{\text{Mom. of inertia}}{\text{Area}}} = \frac{1}{\sqrt{12}} \sqrt{D^2 + d^2}, = 0.28867 \sqrt{D^2 + d^2}$$

This may also be applied to any rectangular column by using the lesser diameters of an unsupported column, and the greater diameters if the column is supported in the direction of its least dimensions.

ELEMENTS OF USUAL SECTIONS.

Moments refer to horizontal axis through centre of gravity. This table is intended for convenient application where extreme accuracy is not important. Some of the terms are only approximate; those marked* are correct, Values for radius of gyration in flanged beams apply to standard minimum sections only. A = area of section; b = breadth; h = depth; D = diameter.

of Section.	Moment of Inertia.	Section Modulus.	Square of Least Radius of Gyration.	Least Radius of Gyration.
Solid Rect- angle.	bh³ *	bh2 *	(Least side)2*	Least side *
Hollow Rect- angle.	bh²-b1h1² *	$\frac{bh^3-b_1h_1^{2*}}{6h}$	$\frac{h^2+h_1^2}{12}$	$\frac{h+h^1}{4.89}$
Solid Circle.	<u>AD</u> ² *	<u>AD</u> *	D2 *	<u>D</u> *
Hollow Circle. A, area of large section; a, area of small section.	$\frac{A\bar{D}^2 - ad^2}{16}$	$\frac{AD^2-ad^2}{8D}$	$\frac{D^2+d^2}{16}$	$\frac{D+d}{5.64}$
Solid Triangle.	36 Bhs	bh² 24	The least of of the two: $\frac{h^2}{18}$ or $\frac{b^2}{24}$	The least of the two; $\frac{h}{4.24}$ or $\frac{b}{4.9}$
Even Angle.	Ah² 10.2	Ah 7.2	62 25	<u>b</u>
Uneven Angle.	Ah ² 9.5	Ah 6.5	$\frac{(hb)^2}{13(h^2+b^2)}$	$\frac{hb}{2.6(h+b)}$
Even Cross.	Ah ² 19	Ah 9.5	22.5	h 4.74
Even Tee.	Ah2 11.1	<u>Ah</u>	22.5	b 4.74
I Beam.	Ah ² 6.66	Ah 8.2	<u>b³</u> 21	b 4.58
Channel.	Ah ² 7.84	Ah 8.67	b ² 12.5	8.54
Deck Beam.	Ah ² 6.9	$\frac{Ah}{4}$	bs 36.5	<u>b</u> <u>ē</u>
	Solid Rectangle. Hollow Rectangle. Solid Circle. Hollow Circle. 4, area of large section; a, area of small section. Solid Triangle. Even Angle. Uneven Angle. Even Tee. I Beam. Channel.	Solid Rectangle. Solid Rectangle. Hollow Rectangle. Solid Circle. $\frac{bh^2 - b_1h_1^2}{12}$ Solid Circle. $\frac{AD^2}{16}$ Hollow Circle. $\frac{AD^2}{16}$ Hollow Circle. $\frac{AD^2 - ad^3}{16}$ Solid Triangle. $\frac{bh^2}{36}$ Even Angle. $\frac{4h^2}{9.5}$ Even Cross. $\frac{Ah^2}{11.1}$ I Beam. $\frac{Ah^2}{6.66}$ Channel. $\frac{Ah^2}{7.34}$	of Inertia. Modulus. Solid Rectangle. $\frac{bh^3}{12} * \frac{bh^2}{6} *$ Hollow Rectangle. $\frac{bh^3 - b_1h_1^2}{12} * \frac{bh^3 - b_1h_1^{12}}{6h}$ Solid Circle. $\frac{AD^2}{16} * \frac{AD}{8} *$ Hollow Circle. $\frac{AD^2 - ad^2}{16} * \frac{AD^2 - ad^2}{8D}$ Anall section. $\frac{ab^2}{36} * \frac{bh^2}{24}$ Even Angle. $\frac{4h^2}{10.2} * \frac{Ah}{6.5}$ Even Cross. $\frac{Ah^2}{19} * \frac{Ah}{9.5}$ Even Tee. $\frac{Ah^2}{6.66} * \frac{Ah}{3.2}$ I Beam. $\frac{Ah^2}{6.66} * \frac{Ah}{3.2}$ Channel. $\frac{Ah^2}{7.34} * \frac{Ah}{3.67}$	of Section. Moment of Inertia. Section Modulus. Least Radius of Gyration. Solid Rectangle. $\frac{bh^3}{12}$ ** $\frac{bh^2}{6}$ ** $\frac{(\text{Least side})^{2*}}{12}$ Hollow Rectangle. $\frac{bh^3 - b_1 h_1^3 *}{18}$ ** $\frac{bh^3 - b_1 h_1^{2*}}{6h}$ ** $\frac{h^2 + h_1^2 *}{12}$ * Solid Circle. $\frac{AD^2 *}{16}$ ** $\frac{AD^2 - ad^2}{8D}$ ** $\frac{D^2 *}{16}$ ** Hollow Circle. $\frac{AD^2 - ad^2}{16}$ ** $\frac{AD^2 - ad^2}{8D}$ ** $\frac{D^2 + d^2 *}{16}$ ** Solid Triangle. $\frac{bh^2}{36}$ ** $\frac{bh^2}{24}$ ** $\frac{bh^2}{16}$ ** Even Angle. $\frac{4h^3}{10.2}$ ** $\frac{4h}{7.2}$ ** $\frac{b^2}{18}$ ** Unieven Angle. $\frac{4h^3}{9.5}$ ** $\frac{4h}{6.5}$ ** $\frac{b^2}{13(h^2 + b^2)}$ ** Even Cross. $\frac{4h^2}{19}$ ** $\frac{4h}{9.5}$ ** $\frac{b^2}{22.5}$ ** Even Tee. $\frac{4h^3}{6.66}$ ** $\frac{4h}{3.2}$ ** $\frac{b^2}{21}$ ** Channel. $\frac{4h^3}{7.84}$ ** $\frac{4h}{3.67}$ ** $\frac{b^2}{22.5}$ ** Deck Beam. $\frac{4h^3}{6.9}$ ** $\frac{4h}{3.67}$ ** $\frac{b^2}{22.5}$ **

Distance of base from centre of gravity, solid triangle, $\frac{h}{3}$; even angle, $\frac{h}{3.3}$; uneven angle, $\frac{h}{3.5}$; even tee, $\frac{h}{3.8}$; deck beam, $\frac{h}{2.3}$; all other shapes given in the table, $\frac{h}{2}$ or $\frac{D}{3}$.

The Strength of Cast-iron Columns.

Hodgkinson's experiments (first published in Phil. Trans. Royal Socy., 1840, and condensed in Tredgold on Cast Iron, 4th ed., 1846), and Gordon's formula, based upon them, are still used (1898) in designing cast-iron columns. That they are entirely inadequate as a basis of a practical formula suitable to the present methods of casting columns will be evident from what follows.

What follows.

Hodgkinson's experiments were made on nine "long" pillars, about 7½ ft. long, whose external diameters ranged from 1.74 to 2.23 in., and average thickness from 0.29 to 0.35 in., the thickness of each column also varying, and on 13 "short" pillars, 0.733 ft. to 2.251 ft. long, with external diameters from 1.08 to 1.28 in., all of them less than ½ in. thick. The iron used was Low Moor, Yorkshire, No. 3, said to be a good iron, not very hard, earlier experiments on which had given a tensile strength of 14,535 and a crushing strength of 109,801 lbs. per sq. in. The results of the experiments on the "long" pillars were reduced to the equivalent breaking weight of a solid pillar 1 in. diameter and of the same length, 7½ ft., which ranged from 2969 to 3987 lbs. per sq. in., a range of over 12 per cent, although the pillars were made from the same iron and of nearly uniform dimensions. From the 13 experiments on "short" pillars a formula was derived, and from the respective of the same length, 7½ ft., which ranged from 2969 to 3987 lbs. per sq. in., a range of over 12 per cent, although the pillars were made from the same iron and of nearly uniform dimensions. From the 18 experiments on "short" pillars a formula was derived, and from the vere obtained the "calculated" breaking weights, the actual breaking weights ranging from about 8 per cent above to about 8 per cent below the calculated weights, a total range of about 16 per cent. Modern cast-tron columns, such as are used in the construction of buildings, are very different in size, proportions, and quality of iron from the slender "long" pillars used in Hodgkinson's experiments. There is usually no check, by actual tests or by disinterested inspection, upon the quality of the material. The tensile, compressive, and transverse strength of cast iron varies through a great range (the tensile strength ranging from less than 10,000 to over 40,000 lbs. per sq. in.), with variations in the chemical composition of the iron, according to laws which are as yet

Another difficulty in obtaining a practical formula for the strength of castiron columns is due to the uncertainty of the quality of the casting, and the danger of hidden defects, such as internal stresses due to unequal cooling, cinder or dirt, blow-holes, "cold-shuts," and cracks on the inner surface, which cannot be discovered by external inspection. Variation in thickness, due to rising of the core during casting, is also a common defect.

In addition to the above theoretical or a priori objections to the use of Gordon's formula, based on Hodgkinson's experiments, for cast-iron columns, we have the data of recent experiments on full-sized columns, made by the Building Department of New York City (Eng'n News, Jan. 18 and 20, 1898). Ten columns in all were tested, six 15-inch, 1904 inches long, two 8-inch, 196 inches long, and two 6-inch, 120 inches long. The tests were made on the large hydraulic machine of the Phoenix Bridge Co., of 2,000,000 pounds capacity, which was calibrated for frictional error by the repeated testing within the elastic limit of a large Phoenix column, and the comparison of these tests with others made on the government machine at the Watertown Arsenal. The average frictional error was calculated to be 15.4 per cent, but Engineering News, revising the data, makes it.1, per cent, with a variation of 3 per cent either way from the average with different loads. The results of the tests of the volumes are given on the opposite page.

page.

Column No. 6 was not broken at the highest load of the testing machine.
Columns Nos. 3 and 4 were taken from the Ireland Building, which collapsed on August 8, 1895; the other four 15-inch columns were made from drawings prepared by the Building Department, as nearly as possible duplicates of Nos. 3 and 4. Nos. 1 and 2 were made by a foundry in New York with no knowledge of their ultimate use. Nos. 5 and 6 were made by a foundry in Brooklyn with the knowledge that they were to be tested. Nos. 7 to 10 were made from drawings furnished by the Department.

Trano	$\Delta \mathbf{r}$	CART	TDON	COLUMNS

	Diam.		Thickness	3.	Breakii	g Load.
Number.	Inches.	Max.	Min.	Average.	Pounds.	Pounds per sq. in.
1 2 8 4 5 6 7 8 9	15 15 15 15 15 15 15 7% to 814 8 6 1/16 6 3/32	1 5/16 11/4 1 7/32 1 11/16 11/4 11/4 1 3/32 1 5/32 11/8	1 1 1 1 1 1 1 1 5 8 1 1 1 1 1 1 1 1 1 1	1 11/6 11/6 11/6 1 11/64 1 3/16 1 3/64 1 9/64 1 7/64	1,356,000 1,380,000 1,198,000 1,246,000 1,632,000 2,082,000 651,000 612,800 400,000 455,200	80,630 27,700 24,900 25,200 32,100 40,400 + 31,900 26,800 22,700 26,300

Applying Gordon's formula, as used by the Building Department, $S = \frac{80000a}{1 + \frac{1}{4000a^2}}$, to these columns gives for the breaking strength per square

inch of the 15-inch columns 57,143 pounds, for the 8-inch columns 40,000 pounds, and for the 6-inch columns 40,000. The strength of columns Nos. 3 and 4 as calculated is 128 per cent more than their actual strength; their actual strength is less than 44 per cent of their calculated strength; and the factor of safety, supposed to be 5 in the Building Law, is only 2.2 for central loading, no account being taken of the likelihood of eccentric loading.

factor of safety, supposed to be 5 in the Building Law, is only 2.2 for central loading, no account being taken of the likelihood of eccentric loading. Prof. Lanza, in his Applied Mechanics, p. 872, quotes the records of 14 tests of cast-iron mill columns, made on the Watertown testing-machine in 1857-88, the breaking strength per square inch ranging from 25,100 to 63,310 pounds, and showing no relation between the breaking strength per square inch and the dimensions of the columns. Only 3 of the 14 columns had a strength exceeding 28,500 pounds per square inch. The average strength of the other 11 was 29,600 pounds per square inch. Prof. Lanza says that it is evident that in the case of such columns we cannot rely upon a crushing strength of greater than 25,000 or 30,000 pounds per square inch of area of section.

He recommends a factor of safety of 5 or 6 with these figures for crushing strength, or 5000 pounds per square inch of area of section as the highest allowable safe load, and in addition makes the conditions that the length of the column shall not be greatly in excess of 20 times the diameter, that the thickness of the metal shall be such as to insure a good strong casting, and that the sectional area should be increased if necessary to insure that the extreme fibre stress due to probable eccentric loading shall not be greater than 5000 nounds per source inch

extreme fibre stress due to probable eccentric loading shall not be greater than 5000 pounds per square inch.

Prof. W. H. Burr (Eng'g News, June 30, 1898) gives a formula derived from plotting the results of the Watertown and Phoenixville tests, above described, which represents the average strength of the columns in pounds per square inch. It is p = 30,500 - 160l/d. It is to be noted that this is an average value, and that the actual strength of many of the columns was much lower. Prof. Burr says: "If cast-iron columns are designed with anything like a reasonable and real margin of safety, the amount of mital required dissipates any supposed economy over columns of mild steel."

required dissipates any supposed economy over columns of mild steel."

Transverse Strength of Cast-iron Water-pipe. (Technology Quarterly, Sept. 1897.)—Tests of 31 cast-iron pipes by transverse stress gave a maximum outside fibre stress, calculated from maximum load, assuming each half of pipe as a beam fixed at the ends, ranging from 12,800 lbs. to 26,300 lbs. per sq. in.

Bars 2 in. wide cut from the pipes gave moduli of rupture ranging from 28,400 to 51,400 lbs. per sq. in. Four of the tests, bars and pipes:

 Moduli of rupture of bar
 28,400
 34,400
 40,000
 51,400

 Fibre stress of pipe
 18,300
 12,800
 14,500
 26,800

These figures show a great variation in the strength of both bars and pipes, and also that the strength of the bar does not bear any definite relation to the strength of the pipe.

Safe Load, in Tons of 2000 Lbs., for Round Cast-iron Columns, with Turned Capitals and Bases.

Loads being not eccentric, and length of column not exceeding 20 times the diameter. Based on ultimate crushing strength of 25,000 lbs. per sq. in. and a factor of safety of 5. (For eccentric loads see page 254.)

Thick-						Dian	neter,	inches	•			
nches.	6	7	8	9	10	11	12	18	14	15	16	18
56	26.4	31.3	_									
56 54 78		36.8				7	Dec 2					
36		42.1				69.6	76.5	House P	70000	200		
1	39.2	47.1				78.5	86.4	91.2	102.1	110.0	- 4	
11/6	1	ا ا	60.8	69.6	78.4	87.2	96.1	104.9	118.8	122.6	181.4	
11/4	1	1 '		76.1	85.9	95.7	105.5	115.3	125.2	135.0	144.8	164
11/6 11/4 13/6 11/4 13/4		1			93.1	103.9	114.7	125.5	136.3	147.1	157.9	179
112							128.7	135.5	147.8	159.0	170.8	194
187	1				1				168.4	182.1	195.8	228
2	1									204.2	219.9	251

For lengths greater than 20 diameters the allowable loads should be decreased. How much they should be decreased is uncertain, since sufficient data of experiments on full-sized very long columns, from which a formula for the strength of such columns might be derived, are as yet lacking. There is, however, rarely, if ever, any need of proportioning castion columns with a length exceeding 20 diameters.

Safe Loads in Tons of 2000 Pounds for Cast-iron Columns.

(By the Building Laws of New York City, Boston, and Chicago, 1897.)

a = sectional area in square inches; l = unsupported length of column in inches; d = side of square column or thickness of round column in inches.

The safe load of a 15-inch round column 1; inches diameter, 16 feet long, according to the laws of these cities would be, in New York, 361 tons; in Boston, 264 tons; in Chicago, 250 tons.

The allowable stress per square inch of area of such a column would be, in New York, 11,850 pounds; in Boston, 8300 pounds; in Chicago, 7850 pounds. A safe stress of 5000 pounds per square inch would give for the safe load on the column 150 tons.

Strength of Brackets on Cast-iron Columns.—The columns tested by the New York Building Department referred to above had brackets cast upon them, each bracket consisting of a rectangular shelf supported by one or two triangular ribs. These were tested after the columns had been broken in the principal tests. In 17 out of 22 cases the brackets broke by tearing a hole in the body of the column, instead of by shearing or transverse breaking of the bracket itself. The results were surprisingly low and very irregular. Reducing them to strength per square inch of the total vertical section through the shelf and rib or ribs, they ranged from 2450 to 5600 lbs., averaging 4800 lbs., for a load concentrated at the end of the shelf, and 4100 to 10,900 lbs., averaging 8000 lbs., for a distributed load. (Eng'g News, Jan. 20, 1898.)

Safe Loads, in Tons, for Round Cast Columns. (In accordance with the Building Laws of Chicago.*)

Diame- ter in	Thick- ness in				Un	supp	orte	d Le	ngth	in F	eet.			
Inches.	Inches.	6	8	10	12	14	16	18	20	22	24	26	28	80
6{	34 34 36	50 57 62	43 50 56	37 42 49	32 36 43	27 31 38	33		For	mul	a: w	= -	5a	13.
7 { 8 {	% %	71 75 86	64 69 79	57 62 71	49 56 64	48 50 57	38 44 50	89 44		2 cro	e loa 000 p	ound	ton	
9	1 76 1 11/6	97 101 118 126	89 94 105 117	81 86 97 107	72 78 88 97	68 70 79 88	56 68 71 79	50 57 64 71	_	una i	mn; suppe n inc mete	hes;		ngth es.
10	7/6 1 11/6 11/4	116 130 145 158	109 122 136 149	101 114 126 139	93 105 117 128	85 96 107 117	78 88 97 107	71 80 88 97	64 72 80 88					
11	1 11/6 11/4 11/6	147 168 179 195	139 155 170 185	131 146 160 174	122 136 149 162	113 126 138 150	104 116 127 138	96 106 117 127	88 97 107 117	80 89 98 106				
12	11/6 11/4 19/6 19/6	181 199 217 234	174 191 207 224	165 181 197 212	155 170 185 200	145 159 173 187	135 148 161 178	125 187 149 161	115 127 188 149	106 117 127 187	98 108 117 126			
18	11/6 18/4 18/6 11/8	200 219 239 258	192 211 230 248	184 202 220 237	174 191 208 225	164 180 196 212	154 169 184 199	144 158 172 186	184 147 160 173	125 137 149 161	116 127 138 149	107 117 128 138		
14	11/4 19/6 11/2 15/8		287 258 278 298	223 243 263 282	218 232 251 269	202 220 238 255	191 207 224 241	180 195 211 227	168 183 198 212	157 171 185 198	147 160 173 185	187 149 161 173	128 139 150 161	
15	186 116 156 184			266 287 309 329	255 276 296 816	243 263 283 301	231 250 268 286	219 236 254 271	206 223 289 255	194 210 225 240	182 197 211 225	171 185 198 211	160 178 186 198	150 162 174 185
16	114 198 194	·			301 323 345	288 310 331	275 296 316	262 282 800	248 267 285	235 253 270	222 239 254	209 225 239	197 212 225	195 199 212
18	156 184 178					866 391 415	351 375 399	337 360 383	322 344 866	307 328 349	295 813 383	279 298 317	264 282 300	251 268 285
20	184 176 2 216						435 463 490 517	420 417 473 499	404 431 456 481	389 414 438 462	373 397 420 413	357 380 409 425	341 363 384 406	326 347 367 387
22	13/4 13/6 2 21/6							480 511 541 581	464 494 524 562	448 478 506 548	432 461 488 524	416 443 470 504	400 426 452 485	384 409 434 465
24	276 234 234 234 234								626 668 691 724	608 639 671 703	589 620 650 681	570 600 629 659	550 579 608 637	531 559 587 614

From tables published by The Expanded Metal Co., Chicago, 1897.)

ECCENTRIC LOADING OF COLUMNS.

In a given rectangular cross-section, such as a masonry joint under pressure, the stress will be distributed uniformly over the section only when the resultant passes through the centre of the section; any deviation from such a central position will bring a maximum unit pressure to one edge and a minimum to the other; when the distance of the resultant from one edge is one third of the entire width of the joint, the pressure at the nearer edge is twice the mean pressure, while that at the farther edge is zero, and that when the resultant approaches still nearer to the edge the pressure at the when the resultant approaches still nearer to the edge the pressure at the farther edge becomes less than zero; in fact, becomes a tension, if the material (mortar, etc., there is capable of resisting tension. Or, if, as usual in masonry joints, the material is practically incapable of resisting tension, the pressure at the nearer edge, when the resultant approaches it nearer than one third of the width, increases very rapidly and dangerously, becoming the pressure of the property of the p ing theoretically infinite when the resultant reaches the edge.

With a given position of the resultant relatively to one edge of the joint or section, a similar redistribution of the pressures throughout the section may be brought about by simply adding to or diminishing the width of the section.

Let P = the total pressure on any section of a bar of uniform thickness.

w = the width of that section = area of the section, when thickness = 1.

p = P/w = the mean unit pressure on the section. M = the maximum unit pressure on the section.

m = the minimum unit pressure on the section. d = the eccentricity of the resultant = its distance from the centre of

Then
$$M = p \left(1 + \frac{6d}{w}\right)$$
 and $m = p \left(1 - \frac{6d}{w}\right)$.

When $d = \frac{1}{6}w$ then M = 2p and m = 0.

When d is greater than 1/6w, the resultant in that case being less than one third of the width from one edge, p becomes negative. (J. C. Trautwine, Jr., Engineering News, Nov. 23, 1893.)

wine, Jr., Engineering News, Nov. 23, 1883.)

Eccentric Loading of Cast-Iron Columns. — Prof. Lanza writes the author as follows: The table on page 252 applies when the resultant of the loads upon the column acts along its central axis, i.e., passes through the centre of gravity of every section. In buildings and other constructions, however, cases frequently occur when the resultant load does not pass through the centre of gravity of the section; and then the pressure is not evenly distributed over the section, but is greatest on the side where the resultant acts. (Examples occur when the loads on the floors are not uniformly distributed.) In these cases the outside fibre stresses of the column should be computed as follows, viz.: Let P = total pressure on the section;

Let P = total pressure on the section; d = eccentricity of resultant = its distance from the centre of gravity

of the section;

A = area of the section, and I its moment of inertia about an axis in its plane, passing through its centre of gravity, and perpendicular to d (see page 267); $c_1 = d$ istance of most compressed and $c_2 = t$ hat of least compressed fibre from above stated axis; $s_1 = m$ aximum and $s_2 = m$ inimum pressure per unit of area. Then

$$s_1 = \frac{P}{A} + \frac{(Pd)c_1}{I} \quad \text{and} \quad s_2 = \frac{P}{A} - \frac{(Pd)c_2}{I}.$$

Having assumed a certain trial section for the column to be designed, s, should be computed, and, if it exceed the proper safe value, a different

should be computed, and, if it exceed the proper safe value, a different section should be used for which s, does not exceed this value.

The proper safe value, in the case of cast-iron columns whose ratio of length to diameter does not greatly exceed 20, is 5000 pounds pre square into when the eccentricity used in the computation of s, is liable to occur frequently in the ordinary uses of the structure; but when it is one which can only occur in rare cases the value 8000 pounds per square inch may be used.

A long cap on a column is more conducive to the production of eccentricity of loading than a short one, hence a long cap is a source of weakness in a column.

in a column.

ULTIMATE STRENGTH OF WROUGHT-IRON COLUMNS.

(Pottsville Iron and Steel Co.)

Computed by Gordon's formula,
$$p = \frac{f}{1 + C(\frac{l}{r})^2}$$

p = ultimate strength in lbs. per square inch;

l = length of column in inches;

r = least radius of gyration in inches;

C = 1/40,000; C = 1/40,000 for square end-hearings; 1/30,000 for one pin and one square bearing; 1/20,000 for two pin-bearings.

bearing: 1/20,000 for two pin-bearings.

For safe working load on these columns use a factor of 4 when used in buildings, or when subjected to dead load only; but when used in bridges the factor should be 5.

WROUGHT-IRON COLUMNS.

ı		e Strength square inc		<u>1</u>	Safe Stre square in	ength in Ib nch—Facto	s per or of 5.
1 r	Square Ends.	Pin and Square End.	Pin Ends.	7	Square Ends.	Pin and Square End.	Pin Ends.
10 15 20 25 30 85 40 45 50 65 70 75 80 85 90 95 106	39944 39776 39604 39318 39318 38810 38460 38072 37686 36697 36182 36697 36182 3634 48076 34482 3883 3264 33636 3366 366 36	39866 89702 39472 39182 38884 88430 37974 87470 36928 36896 35714 84478 34384 34384 32966 82266 82266 82750 30000 29250	89800 89554 89214 38788 85278 87690 86382 35582 35582 35788 39024 32128 8128 81088 29884 28470 27562 26666 25786	10 15 80 25 80 85 40 45 50 65 70 75 80 85 90 95 100 105	7989 7955 7921 7877 7821 7762 7614 7529 7437 7339 7226 7127 7015 6896 6777 6653 6527 6400 6271	7973 7940 7894 7896 7896 7767 7686 7595 7494 7386 7267 7186 6897 6736 6593 6447 6290 6150 6000 5850	7960 7911 7843 7758 7656 7588 7407 7264 7105 6949 6780 6005 6424 6058 5877 5694 5513 33157

Maximum Permissible Stresses in columns used in buildings. (Building Ordinances of City of Chicago, 1898.)

For riveted or other forms of wrought-iron columns:

$$S = \frac{12000n}{19}$$
.

l = length of column in inches;

$$1 + \frac{l^2}{80000^{-8}}$$

r = least radius of gyration in inches; a = area of column in square inches.

For riveted or other steel columns, if more than 60r in length:

$$B = 17,000 - \frac{60}{r}$$

If less than 60r in length:

S = 13.500a. For wooden posts:

$$S = \frac{ac}{1 + \frac{l^2}{250d^2}}.$$

a = area of post in square inches;
d = least side of rectangular post in inches;
l = length of post in inches;
600 for white or Norway pine;

800 for oak; 900 for long-leaf yellow pine.

BUILT COLUMNS.

From experiments by T. D. Lovett, discussed by Burr, the values of f and a in several cases are determined, giving empirical forms of Gordon's formula as follows: p = pounds crushing strength per square inch of section, l = length of column in inches, r = radius of gyration in inches.

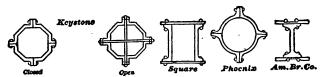


Fig. 76.

Flat Ends.

$$p = \frac{\frac{39,000}{1 + \frac{1}{18,300} \frac{l^2}{r^2}}}{1 + \frac{1}{18,300} \frac{l^2}{r^2}} (1) = \frac{\frac{39,000}{1 + \frac{1}{18,000} \frac{l^2}{r^2}}}{1 + \frac{1}{18,000} \frac{l^2}{r^2}} (2) = \frac{\frac{36,000}{1 + \frac{1}{18,000} \frac{l^2}{r^2}}}{1 + \frac{1}{18,000} \frac{l^2}{r^2}} (2) = \frac{\frac{36,000}{1 + \frac{1}{18,000} \frac{l^2}{r^2}}}{1 + \frac{1}{18,000} \frac{l^2}{r^2}} (2) = \frac{\frac{36,000}{1 + \frac{1}{18,000} \frac{l^2}{r^2}}}{1 + \frac{1}{18,000} \frac{l^2}{r^2}} (3) = \frac{\frac{36,000}{1 + \frac{1}{18,000} \frac{l^2}{r^2}}}{1 + \frac{1}{18,000} \frac{l^2}{r^2}} (3) = \frac{\frac{36,000}{1 + \frac{1}{18,000} \frac{l^2}{r^2}}}{1 + \frac{1}{18,000} \frac{l^2}{r^2}} (3) = \frac{\frac{36,000}{1 + \frac{1}{18,000} \frac{l^2}{r^2}}}{1 + \frac{1}{18,000} \frac{l^2}{r^2}} (3)$$

Round Ends.

$$p = \frac{42,000}{1 + \frac{1}{12000}} (8) \frac{86,000}{1 + \frac{1}{11500}} \frac{1}{120} (11)$$

With great variations of stress a factor of safety of as high as 6 or 8 may be used, or it may be as low as 8 or 4, if the condition of stress is uniform or essentially so.

Burr gives the following general principles which govern the resistance of built columns:

The material should be disposed as far as possible from the neutral axis of the cross-section, thereby increasing r;
There should be no initial internal stress;
The individual portions of the column should be mutually supporting;
The individual portions of the column should be so firmly secured to each

The individual portions of the column should be so firmly secured to each other that no relative motion can take place, in order that the column may fail as a whole, thus maintaining the original value of r. Stoney says: "When the length of a rectangular wrought-iron tubular column does not exceed 30 times its least breadth, it fails by the bulging or buckling of a short portion of the plates, not by the flexure of the pillar as a

In Trans. A. S. C. E., Oct. 1880, are given the following formulæ for the ultimate resistance of wrought-iron columns designed by C. Shaler Smith:

Flat Ends.

$$p = \frac{38,500}{1 + \frac{1}{5890}} \frac{l^3}{d^3}$$
(12)
$$\frac{42,500}{1 + \frac{1}{4500}} \frac{l^3}{d^3}$$
(15)
$$\frac{36,500}{1 + \frac{1}{8750}} \frac{l^3}{d^3}$$
(18)
$$\frac{36,500}{1 + \frac{1}{18750}} \frac{l^3}{d^3}$$
(18)
$$\frac{36,500}{1 + \frac{1}{2700}} \frac{l^3}{d^3}$$
(11)

One Pin End.

$$p = \frac{38,500}{1 + \frac{1}{8000} \frac{l^3}{d^3}} (13) \frac{40,000}{1 + \frac{1}{2250} \frac{l^3}{d^3}} (16) \frac{36,500}{1 + \frac{1}{2250} \frac{l^3}{d^3}} (19) \frac{36,500}{1 + \frac{1}{1500} \frac{l^3}{d^3}} (22)$$

Two Pin Ends.

$$p = \frac{37,500}{1 + \frac{1}{1900}} \frac{1}{d^3} (14) \frac{36,600}{1 + \frac{1}{1500}} \frac{17}{d^3} (17) \frac{36,500}{1 + \frac{1}{1750}} \frac{7}{d^3} (20) \frac{36,500}{1 + \frac{1}{1200}} \frac{1}{d^3} (23)$$

The "common" column consists of two channels, opposite, with flanges outward, with a plate on one side and a lattice on the other.

The formula for "square" columns may be used without much error for

the common-chord section composed of two channel-bars and plates, with the axis of the pin passing through the centre of gravity of the crosssection. (Burr).

Compression members composed of two channels connected by zigzag bracing may be treated by formulæ 4 and 5, using f = 36,000 instead of

Experiments on full-sized Phoenix columns in 1873 showed a close agreement of the results with formulæ 6-8. Experiments on full-sized Phoenix columns on the Watertown testing-machine in 1881 showed considerable discrepancies when the value of l+r became comparatively small. The following modified form of Gordon's formula gave tolerable results through the whole range of experiments:

Phoenix columns, flat end,
$$p = \frac{40,000 \left(1 + \frac{2r}{l}\right)}{\frac{1}{1 + 50,000} \frac{l^2}{r^2}}$$
. (34)

Plotting results of three series of experiments on Phoenix columns, a more simple formula than Gordon's is reached as follows:

Phoenix columns, flat ends, $p = 39,640 - 46^{l}$, when l + r is from 30 to 140;

$$p = 64,700 - 4600 \sqrt{\frac{1}{r}}$$
 when $l + r$ is less than 30.

Dimensions of Phænix Columns.

(Phœnix Iron Co.)

The dimensions are subject to slight variations, which are unavoidable in

rolling iron shapes.

rouning iron snapes.

The weights of columns given are those of the 4, 6, or 8 segments of which they are composed. The rivet heads add from 2% to 5% to the weights given. Rivets are spaced 3, 4, or 6 in, apart from centre to centre, and somewhat more closely at the ends than towards the centre of the column. G columns have 8 segments, E columns 6 segments, C, B^2 , B^1 , and A have 4 segments. Least radius of guration = $D \times .3858$.

The seta leads given are computed as being one fourth of the breeking

The safe loads given are computed as being one-fourth of the breaking load, and as producing a maximum stress, in an axial direction, on a squareend column of not more than 14,000 lbs. per sq. in. for lengths of 90 radii and under.

Dimensions of Phonix Steel Columns.

(Least radius of gyration equals $D \times .3636$.)

One Se	gment.	Diame	ters in In	ches.	0	ne Colun	nn.	t t
Thickness in Inches.	Weight in Lbs.	d Inside.	D Outside.	D¹ over Flanges.	Area of Cross Section, Sq. Inches.	Weight per Ft.	Least Radius of Gyration in Inches.	Safe Load in Net Tons for 16-feet Lengths.
3/16 14 5/16 3/8	9.7 12.2 14.8 17.3	A 35/6	4 41/8 41/4 41/8	6 1/16 6 3/16 6 5/16 6 7/16	3.8 4.8 5.8 6.8	12.9 16.8 19.7 23.1	1.45 1.50 1.55 1.59	18.2 23.9 30.0 35.9
7/16 7/16 7/16 1/5 0/16	16.3 19.9 23.5 27.0 30.6 34.2 87.7	B.1 47/6	596 519 558 534 558 616	51.6 8 3/16 8 5/16 8 7/16 8 9/16 8 11/16	6.4 7.8 9.2 10.6 12.0 13.4 14.8	21.8 26.5 31.3 36.0 40.8 45.6 50.3	1.95 2.09 2.04 2.09 2.13 2.18 2.23	36.4 45.1 54.4 63.9 73.8 83.2 93.1
5/16 5/16 7/16 1/6 9/16 9/16	18.9 22.9 27.0 31.1 35.2 39.3 43.3	B.2 6 1/16	6 9/16 6 11/16 6 13/16 6 15/16 7 1/16 7 3/16 7 5/16	914 936 9 7/16 914 956 934 9 13/16	7.4 9.0 10.6 12.2 18.8 15.4 17.0	25.2 30.6 36.0 41.5 46.9 52.4 57.8	2.39 2.43 2.48 2.52 2.57 2.61 2.66	48.3 59.5 70.7 82.3 93.9 105.8 111.9
5/16 5/16 3/6 7/16 1/6 9/16 3/4 13/16 3/4 11/6 11/6	251/2 31 36 41 46 51 56 62 68 73 78 89 99	C 7%	8 7/16 8 9/16 8 11/16 8 13/16 8 15/16	11 11/18 1134 11 13/16 1176 11 15/16 12 1/16 12 3/16 12 5/16 12 5/16 12 5/16 12 12/16 12 12/16 12/16 12/16 12/16 12/16 12/16 13/16 13/16 13/16 13/16	10.0 12.1 14.1 16.0 18.0 19.9 21.9 24.8 26.6 28.6 30.6 34.8 38.8 42.7	34.0 41.8 48.0 54.6 61.8 68.0 74.6 82.6 90.6 97.3 104.0 118.6 182.0 145.3	2.64 2.88 2.93 2.97 3.01 3.16 3.20 3.24 8.29 3.34 3.48 8.57	70.0 85.1 98.8 112.5 126.3 140.0 153.7 170.2 186.7 200.3 214.4 244.3 271.7
14 5/16 5/16 5/16 5/16 5/16 5/16 5/16 1/16	28 8234 37 42 47 52 57 62 68 73 78 88 98	11 E 11 1/16	11 9/16 11 11/16 11 18/16 11 15/16 12 1/16 12 3/16 12 5/16 12 7/16 12 11/16 12 13/16 13 1/16 13 1/16 13 5/16 13 9/16	151/5 159/5 159/5 153/4 157/6 16 1/16 16 3/16 16 5/16 16 7/18 16 7/18 16 11/16 17 1/16 17 1/16	16.5 19.1 21.7 24.7 37.6 30.6 33.5 36.4 40.0 43.0 45.9 51.7 57.6 63.5	56.0 65.0 74.0 84.0 94.0 104.0 114.0 124.0 136.0 146.0 176.0 196.0 216.0	4.20 4.25 4.29 4.34 4.38 4.48 4.48 4.52 4.56 4.61 4.66 4.73 4.84 4.93	115.3 133.8 152.4 178.0 198.6 214.1 284.7 255.3 280.0 800.6 821.2 362.4 403.6 444.7
5/16 56 7/16	31 36 41 46	G 14%	1514 1536 1516 1596	1934 1914 1958 19 11/16	24.2 28.1 32.0 86.0	82.6 96.0 109.3 122.6	5.54 5.59 5.64 5.68	170.2 197.7 225.1 252.6

One Se	gment.	Diamet	ers in In	ches.	O:	ıe Colun	מו.	Zet Get
Thickness in Inches.	Weight in Lbs. per Yard.	d Inside.	D Outside.	D over Flanges.	Area of Cross Section, Sq. Inches.	Weight per Ft. in Pounds.	Least Radius of Gyration in Inches.	Safe Load in Net Tons for 16-feet Lengths.
9/16 56 11/16 34 13/16 76 1 11/6 11/4	51 56 61 66 71 76 86 96 106	G 1456	15% 15% 16\% 16\% 16\% 16\% 16\% 16\% 17\% 17\%	1934 1978 20 2014 2014 2036 2076 2078 21	39.9 43.8 47.7 51.7 55.6 59.6 67.4 75.3 83.1 90.9	186.0 149.3 162.6 176.0 189.3 202.6 229.3 256.0 252.6 309.8	5.78 5.77 5.89 5.98 5.91 5.95 6.04 6.13 6.27 6.32	280.0 807.4 834.9 862.4 389.8 417.8 472.1 527.8 582.0 636.9

Working Formulæ for Wrought-iron and Steel Struts of various Forms.—Burr gives the following practical formulæ, which he believes to possess advantages over Gordon's:

he believes to possess advantages over	Gordon's:	
Kind of Strut.	 p = Ultimate Strength, lbs. per sq. in. of Section. 	p ₁ = Working Strength = 1/5 Ultimate, lbs. per sq. in. of Section.
Flat and fixed end iron angles and tees	$44000-140\frac{l}{r}$ (1)	$8800 - 28 \frac{l}{r}$ (2)
Hinged-end iron angles and tees	$.46000 - 175 \frac{l}{r}$ (8)	$9200 - 85 \frac{1}{r}$ (4)
Flat-end iron channels and I beams	.40000-110 $\frac{l}{r}$ (5)	$8000-22\frac{l}{r}$ (6)
Flat-end mild-steel angles	.59000—180 $\frac{l}{r}$ (7)	$10400 - 86 \frac{l}{r}$ (8)
Flat-end high-steel angles	•	•
Pin-end solid wrought iron columns	.82000 - 80 $\frac{1}{r}$	$6400-16\frac{l}{r}$ (12)
	$32000-277 \frac{l}{d} $	$6400-55\frac{l}{d}$
Equations (1) to (4) are to be used o	aly between $\frac{l}{r} = 4$	$0 \text{ and } \frac{l}{r} = 900$
(1) and (6) (1) (4) (4) (4) (7) to (10) (10) (11) (12) (13) (14) (15) (15) (15) (15) (15) (15) (15) (15	•	0 " " = 200 0 " " = 200 0 " " = 200

Steel columns, properly made, of steel ranging in specimens from 65,000 to 73,000 lbs. per square inch should give a resistance 25 to 33 per cent in excess of that of wrought-iron columns with the same value of l+r, provided that ratio does not exceed 140.

The unsupported width of a plate in a compression member should not exceed 30 times its thickness.

In built columns the transverse distance between centre lines of rivets securing plates to angles or channels, etc., should not exceed 35 times the plate thickness. If this width is exceeded, longitudinal buckling of the

plate takes place, and the column ceases to fail as a whole, but yields in

The same tests show that the thickness of the leg of an angle to which latticing is riveted should not be less than 1/9 of the length of that leg or side if the column is purely and wholly a compression member. The above limit may be passed somewhat in stiff ties and compression members designed to carry transverse loads. The panel points of latticing should not be separated by a greater distance than 60 times the thickness of the angle-leg to which the latticing is riveted,

if the column is wholly a compression member.

The rivet pitch should never exceed 16 times the thickness of the thinnest metal pierced by the rivet, and if the plates are very thick it should never nearly equal that value.

Merriman's Rational Formula for Columns (Eng. News.

July 19, 1894).

$$C = \frac{B}{1 - \frac{nB}{\pi^2 E} \frac{l^2}{r^2}}. \qquad (1)$$

$$B = \frac{C}{1 + \frac{nC}{\pi^2 E} \frac{P}{r^2}}. \qquad (2)$$

B = unit-load on the column = total load P + area of cross-section A: C = maximum compressive unit-stress on the concave side of the column: l= length of the column; r= least radius of gyration of the cross-section E= coefficient of elasticity of the material; n= 1 for both ends round and one fixed: n=4/9 for one end round and one fixed: n=4/9 for both ends fixed. This formula is for use with strains within the elastic limit only: it does not

hold good when the strain C exceeds the elastic limit. Prof. Merriman takes the mean value of E for timber = 1,500,000, for cast iron = 15,000,000, for wrought-iron = 25,000,000, and for steel = 30,000,000, and $\pi^2 = 10$ as a close enough approximation. With these values he com-

putes the following tables from formula (1):

I .- Wrought-iron Columns with Round Ends.

Unit- load.		M	aximum	Compre	essive Un	it-stress	C.	
$\frac{P}{A}$ or B .	$\frac{l}{r} = 20$	$\frac{l}{r} = 40$	$\frac{l}{r} = 60$	$\frac{l}{r} = 80$	$\frac{l}{r} = 100$	$\frac{l}{r} = 120$	$\frac{l}{r} = 140$	$\frac{l}{r} = 160$
5.000 6,000 7,000 8,000 9,000 10,000 11,000 12,000 18,000	5,040 6,055 7,080 8,100 9,180 10,160 11,200 12,240 18,280	5,170 6,240 7,330 8,430 9,550 10,680 11,750 13,000 14,180	5,890 6,560 7,780 9,040 10,840 11,680 13,070 14,500 15,990	5,780 7,090 8,580 10,060 11,690 13,440 15,810 17,820 19,480	6,250 7,890 9,720 11,660 14,060 16,670 19,640 23,080	6,980 9,090 11,610 14,640 18,380 23,090	8,220 11,330 15,510 21,460	10,250 15,560 24,720

II.-Wrought-iron Columns with Fixed Ends.

Unit- load.		М	aximum	Compre	essive Ur	nit-stress	c.	
$\frac{P}{A}$ or B .	$\frac{l}{r} = 20$	$\frac{l}{r} = 40$	$\frac{l}{r} = 60$	$\frac{l}{r} = 80$	$\frac{l}{r} = 100$	$\frac{l}{r} = 120$	$\frac{l}{r} = 140$	$\frac{l}{r} = 160$
6,000	6,010	6,060	6,130	6,240	6,380	6,570	6,800	7,090
7,000	7,020	7,080	7,180	7,330	7,580	7,780	8,110	8,530
8,000	8,025	8,100	8,240	8,430	8,700	9,040	9,490	10,060
9,000	9,030	9,180	9,300	9,550	9,890	10,840	10,930	11,690
10,000	10,040	10,160	10,870	10,710	11,110	11,680	12,440	13,440
11,000	11,050	11,200	11,450	11,880	12,360	18,070	14,020	15,310
12,000	12,060	12,240	12,540	13,000	18,640	14,510	15,690	17,320
18,000	18,070	18,280	18,640	14,210	14,940	15,990	17,440	19,480
14,000	14,080	14,820	14,740	15,380	16,280	17,580	19,290	21,820

III.-Steel Columns with Bound Ends.

Unit- load.		M	axi mum	Compre	ssive Un	it-stress	C.	
$\frac{P}{A}$ or B .	$\frac{l}{r}=20$	$\frac{l}{r} = 40$	$\frac{l}{r} = 60$	$\frac{l}{r} = 80$	$\frac{l}{r} = 100$	$\frac{l}{r} = 120$	$\frac{l}{r} = 140$	$\frac{l}{r} = 160$
6,000 7,000 8,000 9,000 10,000 11,000 12,000 13,000	6,050 7,070 8,090 9,110 10,130 11,160 12,200 18,830	6,200 7,270 8,380 9,450 10,560 11,690 12,820 13,970	6,470 7,650 8,770 10,090 11,860 12,670 14,020 15,400	6,880 8,230 9,650 11,140 12,710 14,370 16,130 18,000	7,500 9,180 10,870 12,850 15,000 17,370 20,000 22,940	8,430 10,540 12,990 15,850 19,230 23,300 28,300	9,870 12,900 16,760 20,930 28,850	12,800 17,400 24,590

IV.-Steel Columns with Fixed Ends.

Unit- load.		Maximum Compressive Unit-stress C.								
$\frac{P}{A}$ or B .	$\frac{l}{r} = 20$	$\frac{l}{r} = 40$	$\frac{l}{r} = 60$	$\frac{l}{r} = 80$	$\frac{l}{r} = 100$	$\frac{l}{r} = 120$	$\frac{l}{r} = 140$	$\frac{l}{r} = 160$		
7,000	7,020	7,070	7,150	7,270	7,480	7,650	7,900	8,280		
8,000	8,020	8,090	8,200	8,880	8,570	8,770	9,200	9,650		
9,000	9,030	9,110	9,250	9,450	9,730	10,090	10,550	11,140		
10,000	10,080	10,130	10,310	10,560	10,910	11,860	11,810	12,710		
11,000	11,040	11,160	11,380	11,690	12,110	12,670	18,410	14,370		
12,000	12,050	12,900	12,450	12,820	13,330	14,020	14,980	16,180		
18,000	18,060	18,230	18,530	18,970	14,580	15,400	16,500	17,990		
14,000	14,070	14,250	14,610	15,130	15,850	16,830	18,150	19,960		
15,000	15,080	15,810	15,710	16,310	17,140	18,290	19,870	22,060		

The design of the cross-section of a column to carry a given load with maximum unit-stress C may be made by assuming dimensions, and ther

computing C by formula (1). If the agreement between the specified and computed values is not sufficiently close, new dimensions must be chosen, and the computation be repeated. By the use of the above tables the work will be snortened.

The formula (1) may be put in another form which in some cases will abbreviate the numerical work. For B substitute its value P + A, and for Ar^2 write I, the least moment of inertia of the cross-section; then

in which I and r^2 are to be determined. For example, let it be required to find the size of a square oak column with fixed ends when loaded with 24,000 lbs. and 16 ft loag, so that the maximum compressive stress C shall be 1000 lbs. per square inch. Here I=24,000, C=1000, $n=\frac{1}{4}$, $\pi^2=10$, E=1,500,000, I=10 × 12, and (3) becomes comes

$$I \rightarrow 94r^2 = 14.75$$
.

Now let x be the side of the square; then

$$I = \frac{x^4}{12}$$
 and $r^2 = \frac{x^2}{12}$,

so that the equation reduces to $x^4-24x^2=177$, from which x^3 is found to be 29.92 sq. in., and the side x=5.47 in. Thus the unit-load B is about 802 lbs. per square inch.

WORKING STRAINS ALLOWED IN BRIDGE MEMBERS.

Theodore Cooper gives the following in his Bridge Specifications: Compression members shall be so proportioned that the maximum load shall in no case cause a greater strain than that determined by the following formula :

$$P \approx \frac{8000}{1 + \frac{14}{40,000r^3}}$$
for aquare-end compression members;

$$P = \frac{8000}{l^3}$$
 for compression members with one pin and one square end; $1 + \frac{1}{30,000r^3}$

$$P = \frac{8000}{1 + \frac{l^2}{80,000r^2}}$$
 for compression members with pin-bearings;

(These values may be increased in bridges over 180 ft. span. See Cooper's Specifications.)

P= the allowed compression per square inch of cross-section; l= the length of compression member, in inches; r= the least radius of gyration of the section in inches. No compression member, however, shall have a length exceeding 45 times its least width.

Tension Members.—All parts of the structure shall be so proportioned that the maximum loads shall in no case cause a greater tension than the following (except in spans exceeding 150 feet): Pounds ner

10	unde ber
	sq. in.
On Interal bracing	15,000
On solid rolled beams, used as cross floor-beams and stringers.	9,000
On bottom chords and main diagonals (forged eye-bars) On bottom chords and main diagonals (plates or shapes), net	10,000
Section	
On counter rods and long verticals (forged eye-bars)	8,000
On counter and long verticals (plates or shapes), net section	6,500
On bottom flange of riveted cross-girders, net section	8,000
On bottom flange of riveted longitudinal plate girders over	
90 ft. long, net section	8,000

On bottom flange of riveted longitudinal plate girders under	
	P 000
90 ft. long, net section	7,000
On floor-beam hangers, and other similar members liable to	
sudden loading (bar iron with forged ends)	WANT
On floor beam haugers, and other similar members liable to	
sudden loading (plates or shapes), net section	6,000

Members subject to alternate strains of tension and compression shall be proportioned to resist each kind of strain. Both of the strains shall, however, be considered as increased by an amount equal to 8/10 of the least of 8

the two strains, for determining the sectional area by the above allowed
The Phœnix Bridge Co. (Standard Specifications, 1895) gives the follow-
ng:
The greatest working stresses in pounds per square inch shall be as fol- ows:
Tension.
Steel. Iron.
$P = 9,000 \left[1 + \frac{\text{Min. stress}}{\text{Max. stress}} \right]$ For bars, $P = 7,500 \left[1 + \frac{\text{Min. stress}}{\text{Max. stress}} \right]$
$P = 8,500 \left[1 + \frac{\text{Min. stress}}{\text{Max. stress}} \right]$ Plates or $P = 7,000 \left[1 + \frac{\text{Min. stress}}{\text{Max. stress}} \right]$
8,500 pounds. Floor-beam hangers, forged ends
section
10,000 Lower nanges of rolled beating 8,000
20,000 Outside notes of pills
30,000 " Pins for wind-breoing
Shearing.
9,000 pounds. Pins and rivets
6,000 pounds. Webs of plate girders 5,000 pounds.
Bearing.
16,000 pounds. Projection semi-intrados pins and rivets 12,000 pounds. Hand-driven rivets 20% less unit stresses. For bracing increase unit stresses 50%.
A

Compression.

Lengths less than forty times the least radius of gyration, P previously found. See Tension.
Lengths more than forty times the least radius of gyration, Preduced by following formulæ:

For both ends fixed,
$$b = \frac{P}{1 + \frac{16}{36,0007^5}}$$
For one end hinged,
$$b = \frac{P}{1 + \frac{18}{24,0007^4}}$$
For both ends hinged,
$$b = \frac{P}{1 + \frac{18}{18,0007^4}}$$

P= permissible stress previously found (see Tension); b= allowable working stress per square inch; l= length of member in inches; r= least radius of gyration of section in inches. No compression member, however, shall have a length exceeding 45 times its least width.

·	Pounds per
	sq. in.
In counter web members	10,500
In long verticals	10,000
In all main-web and lower-chord eye-bars	18.200
In plate hangers (net section)	9,000
In tension members of lateral and transverse bracing	
In steel-angle lateral ties (net section)	
For spans over 200 feet in length the greatest allowed	working stresse

per square inch, in lower-chord and end main-web eye-bars, shall be taken at

$$10,000 \left(1 + \frac{\text{min. total stress}}{\text{max. total stress}}\right)$$

whenever this quantity exceeds 18,200.

The greatest allowable stress in the main-web eye-bars nearest the centre of such spans shall be taken at 13,200 pounds per square inch; and those for the intermediate eye-bars shall be found by direct interpolation between the preceding values.

The greatest allowable working stresses in steel plate and lattice girders and rolled beams shall be taken as follows:

•	Pounas pe
	sq. in.
Upper flange of plate girders (gross section)	10,000
Lower flange of plate girders (net section)	10,000
In counters and long verticals of lattice girders (net section) In lower chords and main diagonals of lattice girders (n	9,000
section)	10,000
In bottom flanges of rolled beams	10,000
In top flanges of rolled beams	

RESISTANCE OF HOLLOW CYLINDERS TO COLLAPSE.

Fairbairn's empirical formula (Phil. Trans. 1858) is

where p = p ressure in lbs. per square inch, t = t hickness of cylinder, d = d diameter, and l = l ength, all in inches; or,

$$p = 806,300 \frac{t^{2\cdot 19}}{Ld}$$
, if L is in feet. (2)

He recommends the simpler formula

as sufficiently accurate for practical purposes, for tubes of considerable diameter and length.

The diameters of Fairbairn's experimental tubes were 4", 6", 8", 10", and 12", and their lengths, between the cast-iron ends, ranged between 19 inches and 60 inches.

His formula (3) has been generally accepted as the basis of rules for ascertaining the strength of boiler-flues. In some cases, however, limits are fixed to its application by a supplementary formula.

Lloyd's Register contains the following formula for the strength of circular

boiler-flues, viz.,

The English Board of Trade prescribes the following formula for circular flues, when the longitudinal joints are welded, or made with riveted buttstraps, viz.,

For lap-joints and for inferior workmanship the numerical factor may be reduced as low as 60,000.

The rules of Lloyd's Register, as well as those of the Board of Trade, prescribe further, that in no case the value of P must exceed the amount given by the following equation, viz.,

In formulæ (4), (5), (6) P is the highest working pressure in pounds per square inch, t and d are the thickness and diameter in inches, L is the length of the flue in feet measured between the strengthening rings, in case it is fitted with such. Formula (4) is the same as formula (3), with a factor of safety of 9. In formula (6) the length L is increased by 1; the influence which this addition has on the value of P is, of course, greater for short tubes than for long ones.

Nystrom has deduced from Fairbairn's experiments the following formula for the collapsing strength of flues :

$$p = \frac{4Tt^2}{d\sqrt{L}}, \dots \dots \dots \dots (7)$$

where p, t, and d have the same meaning as in formula (1), L is the length in feet, and T is the tensile strength of the metal in pounds per square inch. If we assign to T the value 50,000, and express the length of the flue in inches, equation (7) assumes the following form, viz.,

$$p = 692,800 \frac{t^2}{d\sqrt{l}}$$
 (8)

Nystrom considers a factor of safety of 4 sufficient in applying his formula. (See "A New Treatise on Steam Engineering," by J. W. Nystrom, p. 106.)
Formula (1), (4), and (8) have the common defect that they make the collapsing pressure decrease indefinitely with increase of length, and vice versa. M. Love has deduced from Fairbairn's experiments an equation of a different form, which, reduced to English measures, is as follows, viz.,

$$p = 5,358,150 \frac{t^2}{td} + 41,906 \frac{t^2}{d} + 1328 \frac{t}{d}, \dots$$
 (9)

where the notation is the same as in formula (1).

D. K. Clark, in his "Manual of Rules," etc., p. 696, gives the dimensions of stues, selected from the reports of the Manchester Steam-Users Association, 1862-69, which collapsed while in actual use in boilers. These flues varied from 24 to 60 inches in diameter, and from 3-16 to 35 inch in thickness. varies from \$100 of mines in diameter, and from \$-100 yg inch in linexhess. They consisted of rings of plates riveted together, with one or two longitudinal seams, but all of them unfortified by intermediate flanges or strength ening rings. At the collapsing pressures the flues experienced compressions ranging from 1.58 to 2.17 tons, or a mean compression of 1.82 tons per square inch of section. From these data Clark deduced the following formula "for the average resisting force of common boiler-flues," viz.,

where p is the collapsing pressure in pounds per square inch, and d and t are the diameter and thickness expressed in inches.

C. R. Roelker, in Van Nostrand's Magazine, March, 1881, discussing the above and other formnise, shows that experimental data are as yet insufficient to determine the value of any of the formule. He says that Nystrom's formula, (8), gives a closer agreement of the calculated with the actual collapsing the constraints of the calculated with the actual collapsing the constraints of the calculated with the actual collapsing the constraints of the calculated with the actual collapsing the constraints. lapsing pressures in experiments on flues of every description than any of the other formulæ.

Collapsing Pressure of Plain Iron Tubes or Flues.

The resistance to collapse of plain-riveted flues is directly as the square of the thickness of the plate, and inversely as the square of the diameter. The support of the two ends of the flue does not practically extend over a length of tube greater than twice or three times the diameter. The collapsing pressure of long tubes is therefore practically independent of the length.

Instances of collapsed flues of Cornish and Lancashire boilers collated by Ciark, showed that the resistance to collapse of flues of %-inch plates, 18 to 48 feet long, and 30 to 50 inches diameter, varied as the 1.75 power of the diameter. Thus,

inches. lbs. per sq. in: for 7-16-inch plates the collapsing pressures were 60 49 42

For collapsing pressures of plain iron flue-tubes of Cornish and Lauca shire steam-boilers, Clark gives:

$$P = \frac{900,000t^2}{d^{1.78}}.$$

P = collapsing pressure, in pounds per square inch;
 t = thickness of the plates of the furnace tube, in inches.

d = internal diameter of the furnace tube, in inches.

For short lengths the longitudinal tensile resistance may be effective in augmenting the resistance to collapse. Flues efficiently fortified by flangejoints or hoops at intervals of 8 feet may be enabled to resist from 50 lbs. to 60 lbs. or 70 lbs. pressure per square inch more than plain tubes, according to the thickness of the plates.

ing to the thickness of the plates.

Strength of Small Tubes.—The collapsing resistance of solid-drawn tubes of small dameter, and from .134 inch to .109 inch in thickness, nas been tested experimentally by Messrs. J. Russell & Sons. The results for wrought-iron tubes varied from 14.33 to 30.07 tons per square-inch section of the metal, averaging 18.30 tons, as against 17.57 to 24.38 tons, averaging 22.40 tons, for the bursting pressure.

(For strength of Segmental Crowns of Furnaces and Cylinders see Clark, S. E., vol. 1, pp. 649-651 and pp. 627, 628.)

Formula for Corrugated Furnaces (Eng'g, July 24, 1891, p. 102).—As the result of a series of experiments on the resistance to collapse of Fox's corrugated furnaces, the Board of Trade and Lloyd's Registry altered their formulas for these furnaces in 1891 as follows:

Board of Trade formula is altered from

$$\frac{19,500 \times T}{D} = WP \text{ to } \frac{14,000 \times T}{D} = WP.$$

T = thickness in inches; D = mean diameter of furnace;

 $WP \Rightarrow$ working pressure in pounds per square inch. Lloyd's formula is altered from

$$\frac{1000 \times (T-?)}{D} = WP$$
 to $\frac{1284 \times (T-2)}{D} = WP$.

T =thickness in sixteenths of an inch:

D = greatest diameter of furnace;
 WP = working pressure in pounds per square inch.

TRANSVERSE STRENGTH.

In transverse tests the strength of bars of rectangular section is found to vary directly as the breadth of the specimen tested, as the square of its depth, and inversely as its length. The deflection under any load varies as the cube of the length, and inversely as the breadth and as the cube of the depth. Represented algebraically, if S= the strength and D the deflection, t the langth, t the breadth, and t the depth,

S varies as
$$\frac{bd^3}{l}$$
 and D varies as $\frac{l^3}{hd^3}$.

For the purpose of reducing the strength of pieces of various sizes to a common standard, the term modulus of rupture (represented by E) is used. Its value is obtained by experiment on a bar of rectangular section

supported at the ends and loaded in the middle and substituting numerical values in the following formula:

$$R = \frac{8}{3} \frac{Pl}{hd3},$$

in which P = the breaking load in pounds, l = the length in inches, b the

breadth, and d the depth.

The modulus of rupture is sometimes defined as the strain at the instant of rupture upon a unit of the section which is most remote from the neutral axis on the side which first ruptures. This definition, however, is based upon a theory which is yet in dispute among authorities, and it is better to define it as a numerical value, or experimental constant, found by the ap-

plication of the formula above given.

From the above formula, making l 12 inches, and b and d each 1 inch, if follows that the modulus of rupture is 18 times the load required to break a bar one inch square, supported at two points one foot apart, the load being

applied in the middle.

Coefficient of transverse strength = $\frac{\text{span in feet} \times \text{load at middle in lbs.}}{\text{breadth in inches} \times (\text{depth in inches})^2}$. $= \frac{1}{18}$ th of the modulus of rupture.

Fundamental Formulæ for Flexure of Beams (Merriman).

Resisting shear = vertical shear; Resisting moment = bending moment;

Sum of tensile stresses = sum of compressive stresses; Resisting shear = algebraic sum of all the vertical components of the in-

ternal stresses at any section of the beam.

If A be the area of the section and Ss the shearing unit stress, then resist-

ing shear = AS_c , and if the vertical shear = V, then $V = AS_c$.

The vertical shear is the algebraic sum of all the external vertical forces on one side of the section considered. It is equal to the reaction of one support, considered as a force acting upward, minus the sum of all the vertical downward forces acting between the support and the section.

The resisting moment = algebraic sum of all the moments of the internal horizontal stresses at any section with reference to a point in that sec-8I $\frac{2A}{C}$, in which S = the horizontal unit stress, tensile or compressive as the case may be, upon the fibre most remote from the neutral axis, c = the shortest distance from that fibre to said axis, and I = the moment of inertia of the cross-section with reference to that axis.

The bending moment M is the algebraic sum of the moment of the external forces on one side of the section with reference to a point in that section = moment of the reaction of one support minus sum of moments of loads between the support and the section considered.

$$M = \frac{SI}{c}$$

the bending moment is a compound quantity = product of a force by the cistance of its point of application from the section considered, the distance being measured on a line drawn from the section perpendicular to the lirection of the action of the force.

Concerning the above formula, Prof. Merriman, Eng. News, July 21, 1894. says: The formula just quoted is true when the unit-stress S on the part of the beam farthest from the neutral axis is within the elastic limit of the material. It is not true when this limit is exceeded, because then the neutral axis does not pass through the centre of gravity of the cross-section, and because also the different longitudinal stresses are not proportional to their distances from that axis, these two requirements being involved in the de-distances from that axis, these two requirements being involved in the dis-distances of the formula. But in all cases of design the permissible unit-stresses should not exceed the elastic limit, and hence the formula applies rationally, without regarding the ultimate strength of the material or any of the circumstances regarding rupture. Indeed so great reliance is placed upon this formula that the practice of testing beams by rupture has been almost entirely abandoned, and the allowable unit-stresses are mainly derived from tensile and compressive tests.

GENERAL FORMULÆ FOR TRANSVERSE STRENGTH OF BEAMS OF UNIFORM CROSS-SECTION.

	ALC:	SECTION.			
	Rectang	Rectangular Beam.	Beam	Beam of any Section.	tion,
Beam,	Breaking Load.	Deflection for Load P or W.	Maximum Moment of Stress. Rupture.	Moment of Rupture.	Deflection.
Fixed at one end, load at the other	$P = \frac{1}{6} \frac{Rbd^3}{l}$	4Pl3	Pt =	RI	1 Pls
Same with load distributed uniformly	$W = \frac{1}{8} \frac{Rbd^3}{l}$	8 W78 2 Ebds	1 m =	RI	1 W 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
Supported at ends, loaded in middle	$P = \frac{2}{3} \frac{Rbd^3}{l}$	Pis 4Ebd3	1 4 P2 ==================================	R .	1 Pis
Same loaded uniformly	$W = \frac{4}{8} \frac{Rbd^3}{l}$	5 W78	1 m =	RI	11 12 13 13 13 13 13 13 13 13 13 13 13 13 13
Same, loaded at middle, and also } with uniform load,	$\frac{2P + W = \frac{4}{8} \frac{Rbd^3}{l}}{l}$	$\frac{1}{4} \left(P + \frac{1}{8}W\right) \frac{l^3}{Ebd^3}$	$\left(\frac{1}{4}P + \frac{1}{8}W\right)l =$	S IEI o	$\frac{1}{48}(P+\frac{5}{8}W)\frac{l^3}{El}$
Fixed at both ends, loaded in middle	$P = \frac{4 Rbd^3}{3 l}$	1 Pts 16 Ebds	1 Pl	RI	2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
Same, Barlow's Experiments	$P = \frac{Rbd^3}{l}$		$\frac{1}{6}Pl$	RI	77
Same, uniformly loaded	$W = \frac{2Rbd^2}{l}$	1 W73 32 Ebd3	$\frac{1}{12}W7 =$	RI	84 m
Fixed at one end, supported at the) other, loaded at .684l from fixed end, }			$\frac{3}{8}(2\sqrt{3}-3)Pl =$	RI	P 13
Same uniformly loaded	$W = \frac{4}{3} \frac{Rbd^3}{l}$.0648 W7s	$\frac{1}{8}m_l$	RI	$\frac{\text{(nearly)}}{185}.$
					(nearly).

Formulæ for Transverse Strength of Beams,-Referring to table on preceding page, P = load at middle;

W= total load, distributed uniformly;

l = length, b = breadth, d = depth, in inches:

E = modulus of elasticity;

R =modulus of rupture, or stress per square inch of extreme fibre:

I = moment of inertia;

c = distance between neutral axis and extreme fibre.

For breaking load of circular section, replace bd^2 by 0.52 d^2 . For good wrought iron the value of R is about 80,000, for steel about 120,000, the percentage of carbon apparently having no influence. (Thurston, Iron and Steel, p. 491).

For cast fron the value of R varies greatly according to quality. Thurston found 45,740 and 67,980 in No. 2 and No. 4 cast fron, respectively.

For beams fixed at both ends and loaded in the middle, Barlow, by experi-

ment, found the maximum moment of stress = 1/8Pl instead of $\frac{1}{2}Pl$, the result given by theory. Prof. Wood (Resist, Matls, p. 185) says of this case: The phenomena are of too complex a character to admit of a thorough and exact analysis, and it is probably safer to accept the results of Mr. Barlow in practice than to depend upon theoretical results.

APPROXIMATE GREATEST SAFE LOADS IN LBS. ON STEEL BEAMS. (Pencovd Iron Works.)

Based on fibre strains of 16,000 lbs. for steel. (For iron the loads should be one-eighth less, corresponding to a fibre strain of 14,000 lbs. per square inch.)

L =length in feet between supports; A =sectional area of beam in square

a = interior area in square inches; d = interior depth in inches.

inches;

D = depth of beam in inches.

w = working load in net tons.

D as dopin	or beam in inci	108.	W = WOLKING IC	MEGI III II OF COIRS.		
Mana of	Greatest Safe	Load in Pounds.	Deflection in Inches.			
Shape of Section.	Load in Middle.	Load Distributed.	Load in Middle.	Load Distributed.		
Solid Rect- angle.	890AD L	1780AD L	$\frac{wL^3}{82AD^3}$	wL ³ 52AD ²		
Hollow Rect- angle.	890(AD-ad) L	1780(AD-ad) L	$\frac{wL^2}{32(AD^2-ad^2)}$	wL^{3} $52(AD^{2}-ad^{3})$		
Solid Cylin- der.	667AD L	1388 A D L	wL ³ 24AD ²	wL ⁹ 88AD ²		
Hollow Cylinder.	667(AD-ad) L	1883(AD-ad) L	$\frac{wL^3}{24(AD^2-ad^2)}$	$\frac{wL^{2}}{88(AD^{2}-ad^{2})}$		
Even-legged Angle or Tee.	885AD L	1770AD	10L ² 82AD ²	wL ³ 52AD ²		
Channel or Z bar.	1595AD L	8050AD L	wL ³ 58AD ²	wL³ 85AD²		
Deck Beam.	1380AD L	2760AD	$\frac{wL^3}{50AD^2}$	$\frac{wL^3}{80AD^2}$		
I Beam.	1695 <i>AD</i>	3390AD L	wL ³ 58.AD ²	wL ³ 98 A D ²		
1	II	III	17	V		

The above formulæ for the strength and stiffness of rolled beams of various sections are intended for convenient application in cases where

strict accuracy is not required.

The rules for rectangular and circular sections are correct, while those for the flanged sections are approximate, and limited in their application to the standard shapes as given in the Pencoyd tables. When the section of any beam is increased above the standard minimum dimensions, the flanges remaining unaltered, and the web alone being thickened, the tendency will be for the load as found by the rules 20 be in excess of the actual; but within the limits that it is possible to vary any section in the rolling, the rules will apply without any serious inaccuracy.

will apply without any serious inaccuracy.

The calculated safe loads will be approximately one half of loads that would injure the elasticity of the materials.

The rules for deflection apply to any load below the elastic limit, or less than double the greatest safe load by the rules.

anan double the greatest sate load by the raise.

If the beams are long without lateral support, reduce the loads for the ratios of width to span as follows:

		h of Be	am.	Proportion forming G	of Calcula reatest Sa	
20	times	flange	width.	Whole	calculated	load.
80	66	44	66	9-10	44	66
40		46	4	8-10	44	66
50		66	64	7-10	44	44
60	- 44	44	44	6-10	44	44
70		44	44	5-10	44	**

These rules apply to beams supported at each end. For beams supported otherwise, after the coefficients of the table as described below, referring to the respective columns indicated by number.

Changes of Coefficients for Special Forms of Beams.

Kind of Beam.	Coefficient for Safe Load.	Coefficient for Deflection.
Fixed at one end, loaded at the other.	One fourth of the coeffi- cient, col. II.	One sixteenth of the co- efficient of col. IV.
Fixed at one end, load evenly distributed.	One fourth of the coeffi- cient of col. III.	Five forty-eighths of the coefficient of col. V.
Both ends rigidly fixed, or a continuous beam, with a load in middle.	Twice the coefficient of col. II.	Four times the coeffi- cient of col. IV.
Both ends rigidly fixed, or a continuous beam, with load evenly dis- tributed.	One and one-half times the coefficient of col.	

RLASTIC RESILIENCE.

In a rectangular beam tested by transverse stress, supported at the ends and loaded in the middle,

$$P = \frac{2}{3} \frac{Rbd^2}{l};$$

$$\Delta = \frac{1}{4} \frac{Pl^3}{Eod^2};$$

in which, if P is the load in pounds at the elastic limit, R = the modulus of transverse strength, or the strain on the extreme fibre, at the elastic limit, E = modulus of elasticity, Δ = deflection, I, b, and d = length, breadth, and depth in inches. Substituting for P in (2) its value in (1), we have

The clastic resilience = half the product of the load and deflection = 14PA, and the elastic resilience per cubic inch

$$=\frac{1}{9}\frac{P\Delta}{B\omega}$$

Substituting the values of P and A, this reduces to elastic resilience per enbic inch = $\frac{1}{18}\frac{L}{E}$, which is independent of the dimensions; and therefore 1 R2 the elastic resilience per cubic inch for transverse strain may be used as a modulus expressing one valuable quality of a material. Similarly for tension:

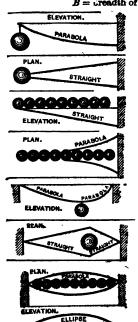
Let P = tensile stress in pounds per square inch at the elastic limit;

e = elongation per unit of length at the elastic limit; E = modulus of elasticity = P + e; whence e = P + E.

Then elastic resilience per cubic inch = $\frac{1}{2}P_0 = \frac{1}{2}\frac{T}{R}$.

BEAMS OF UNIFORM STRENGTH THROUGHOUT THEIR LENGTH.

The section is supposed in all cases to be rectangular throughout. The beams shown in plan are of uniform depth throughout. Those shown in alevation are of uniform breadth throughout. B = creadth of beam. D = depth of beam.



Fixed at one end, loaded at the other; curve parabola, vertex at loaded end; BD² proportional to distance from loaded end. The beam may be reversed, so that the upper edge is parabolic, or both edges may be parabolic.

Fixed at one end, loaded at the other; triangle, apex at loaded end; BD* proportional to the distance from the loaded end.

Fixed at one end; load distributed; triangle, apex at unsupported end; BD^q proportional to square of distance from unsupported end.

Fixed at one end; load distributed; curves two parabolas, vertices touching each other at unsupported end; BD^a proportional to distance from unsupported end.

Supported at both ends; load at any one point; two parabolas, vertices at the points of support, bases at point loaded; BD² proportional to distance from nearest point of support. The upper edge or both edges may also be parabolic.

Supported at both ends; load at any one point; two triangles, apless at points of sup-port, bases at point loaded; BD⁰ propor-tional to distance from the nearest point of support.

Supported at both ends: load distributed: curves two parabolas, vertices at the middle of the beam; bases centre line of beam; BD^2 proportional to product of distances from points of support.

Supported at both ends; load distributed; curve semi-ellipse; BD^3 proportional to the product of the distances from the points of support.

-- -- 1

PROPERTIES OF ROLLED STRUCTURAL STEEL.

Explanation of Tables of the Properties of I Beams, Channels, Angles, Deck-Beams, Bulb Angles, Z Bars, Tees, Trough and Corrugated Plates.

(Tae Carnegie Steel Co., Limited.)

The tables for I beams and channels are calculated for all standard weights to which each pattern is rolled. The tables for deck-beams and angles are calculated for the minimum and maximum weights of the various shapes, while the properties of Z bars are given for thicknesses differing by 1/16 inch.

For tees, each shape can be rolled to one weight only. Column 12 in the tables for I beams and channels, and column 9 for deck-beams, give coefficients by the help of which the safe, uniformly distributed load may be readily determined. To do this, divide the coefficient given by the span or distance between supports in feet. If the weight of the deck-beams is intermediate between the minimum and maximum weights given, add to the coefficient for the minimum weight the value given for one pound increase of weight multiplied by the number of pounds the section is heavier than the minimum.

If a section is to be selected (as will usually be the case), intended to carry a certain load for a length of span already determined on, ascertain the coefficient which this load and span will require, and refer to the table for a section having a coefficient of this value. The coefficient is obtained by multiplying the load, in pounds uniformly distributed, by the span length in feet. In case the load is not uniformly distributed, but is concentrated at the middle of the span, multiply the load by 2, and then consider it as uniformly distributed. The deflection will be 8/10 of the deflection for the latter load. For other cases of loading obtain the hending moment in tells. This

For other cases of loading obtain the bending moment in ft.-lbs.; this

multiplied by 8 will give the coefficient required.

If the loads are quiescent, the coefficients for a fibre stress of 16,000 lbs. per square inch for steel may be used; but if moving loads are to be provided for, a coefficient of 12,500 lbs. should be taken. Inasmuch as the effects of impact may be very considerable (the stresses produced in an unylelding inelastic material by a load suddenly applied being double those produced by the same load in a quiescent state), it will sometimes be advisable to use still smaller fibre stresses than those given in the tables. In such cases the coefficients may be determined by proportion. Thus, for a fibre stress of 8,000 lbs. per square inch the coefficient will equal the coefficient for 16,000

lbs. fibre stress, from the table, divided by 2.

The section moduli, column 11, are used to determine the fibre stress per square inch in a beam, or other shape, subjected to bending or transverse stresses, by simply dividing the bending moment expressed in inch-pounds

by the section modulus.

In the case of T shapes with the neutral axis parallel to the flange, there will be two section moduli, and the smaller is given. The fibre stress calculated from it will, therefore, give the larger of the two stresses in the extreme fibres, since these stresses are equal to the bending moment divided by the section modulus of the section.

For Z bars the coefficients (C) may be applied for cases where the bars are

subjected to transverse loading, as in the case of roof-purlins.

For angles, there will be two section moduli for each position of the neutral axis, since the distance between the neutral axis and the extreme fibres has a different value on one side of the axis from what it has on the other. The

section modulus given in the table is the smaller of these two values.

Column 12 in the table of the properties of standard channels, giving the distance of the center of gravity of channel from the outside of web, is used to obtain the radius of gyration for columns or strute consisting of two channels latticed, for the case of the neutral axis passing through the centre of the cross-section parallel to the webs of the channels. This radius of gyration is equal to the distance between the centre of gravity of the channel and the centre of the section, i.e., neglecting the moments of inertia of the channels around their own axes, thereby introducing a slight error on the side of safety.

(For much other important information concerning rolled structural shapes, see the "Pocket Companion" of The Carnegie Steel Co., Limited,

Pittsburg, Pa., price \$2.)

Properties of Carnegie Standard I Beams-Steel.

1	2	3	4	5	6	7	8	9	10	11	12
		t.		ep.	е.	Inertia, xis Per- to Web	Axis Coin- ith Centre	Gyration, Axis Per- r to Web	adius of Gyration, Neutral Axis Coin- cident with Centre Line of Web.	Section Modulus, Neu- tral Axis Perpendic- ular to Web at Cen- tre.	Coefficient of Strength for Fibre Stress of 16,000 lbs. per sq. in.
	H	Foot.	on	×	ng	oment of In Neutral Axis pendicular to at Centre.	b. xis	Gyrs Axis r to	b d d	ction Modulus, tral Axis Perpe ular to Web at tre.	or Fibre Stre 6,000 lbs. per
jes	ea	H	cti	of	718	of A lar	Neutral Ax cident with Line of Web	Neutral A. pendicular at Centre.	Adius of Gy Neutral Axis cident with Line of Web.	A P	o o
E	E	be	S	88	-	755	7 5	of all	of Wila	Mc xis	hr
	0	t l	30	ne	0	oment o Neutral pendicula at Centre	oment Neutral cident Line of	adius of Neutral pendicula at Centre	s true	- A -	for Fibre 16,000 lbs.
tio	th	500	63	S.	IT.	en en	de	en	Hinden de	ctio	£ 70
Section Index.	Depth of Beam.	Weight per	Area of Section.	Thickness of Web.	Width of Flange.	Moment Neutra pendic at Cent	Moment Neutra cident Line of	Radius Neutra pendic at Cen	Radius Neutr cident Line o	Sec	500
	in.	lbs.	sq. in.	in.	in,	I	I'	r	2"	S 198.4	C
BI	24	100	29.41	0.75		2380.3	48.56	9.00	1.28	198.4	211580
44	1 44	95	27.94 26.47	0.69	7.19	2309.6 2239.1	47.10	9.09	1.30	192.5 186.6	205290
64	1 44	85	25 00	0.57	7.07	2168.6	45.70 44.35	9.20 9.31	1.33	180.7	199030 192760
		80	25.00 23.32	0.50	7.00	2087.9	42.86	9.46	1.36	174.0	185590
B 3	50	75	22.06	0.65	6.40	1268.9	30.25	7.58	1.17	126.9	135850
**	6	70	20.59			1219.9	29.04	7.70	1.19	122.0	130120
380	18	65	19.08 20.59	0.50	6.25	1169.6	27.86 24.62	7.83 6.69	1.21	117.0 102.4	124760
11	10	65	19.12	0.64	6.18	921.3 881.5	28.47	6.79	1.11	97.9	109190
44	44	60	17.65	0.55	6.09	841.8	22.38	6.91	1.13	93.5	9977
44	**	55	15,93	0.46	6.00	795.6	21.19	7.07	1.15	88.4	94300
B7	15	55	16.18	0.66	5.75	511.0	17.06	5.23	0.95	68.1	72680
44	16	50	14.71 13.24	0.56	5 65	483.4	16.04	5.73	1.04	64.5	68750
44	46	45	12.48	0.40	5 50	455.8	15.09 14.62	5.87 5.95	1.07	60.8 58.9	64820
B9	12	35	10.29	0.44	5.09	228.3	10.07	4.71	0.99	38.0	40580
**	4.	31.5	9.26	0.35	5.00	215.8	9 50	4.83	1.01	36.0	38370
311	10	40	11.76	0.75	5.10	158.7	9.50	3.67	0.90	31.7	33850
**	1.	35 30	10.29	0.60	4.95	146.4	8.52	3 77	0.91	29.3	3124
46	44	25	7 97	0.31	4 66	184.2 122.1	7.65 6.89	3.90 4.07	0.98	26.8 24.4	28630 26050
313	9	35	10.29	0.73	4.77	111.8	7.31	3.20	0.84	24.8	2650
**	**	30	8.82	0.57	4.61	101.9	7.31 6.42	3.29 3.40	0.85	22.6	24150
*	16	25	7.35	0.41	4.45	91.9	5.65	3.54	0.88	20.4	2179
**	8	21	6.31	0.29	4.33	84.9	5.16	3.67	0.90	18.9	2013
315	0	25.5 23		$0.54 \\ 0.45$		68.4 64.5	4.75 4.39	3.02	0.80	17.1 16 1	1825 1720
**	-	20.5		0.36		60.6	4 07	8 17	0.82	15.1	1616
	*	18	5,33	0.27	4.00	56.9	3.78	3.27	0.84	14.2	15170
317	7	20	5.88	0.46	4.00 3.87	42.2	3.24 2.94	2.68	0.84 0.74	12.1	1286
**		17.5	5.15	0.35	3.76	39.2	2.94	2.76	0.76	11.2	1194
319	6	15 1714	5.07	0.25	3 59	36.2 26.2	2.67 2.36	2.86 2.27	0.78	10.4 8.7	931
44.	*	1434		0.35		24.0	2.09	2.35	0.69	8.0	853
	40	121/4	3.61	0.23	3.33	21.8	1.85	2.46	0.72	7.3	775
321	5	1434	4.34	0.50	3.29	15.2	1.70	1.87	0.63	6.1	646
44	44	1214	3.60	0.36	3.15	13.6	1.45	1.94	0.63	5.4	581
323	4	934	8 00	0.21	9 89	12.1 7.1	1.23	2.05 1.52	0.65	4.8 3.6	5160 3810
543	16	9.5	2.79	$0.41 \\ 0.34 \\ 0.26$	2.80	6.7	0.93	1.55	0.58	3.4	360
**	44	8.5	2.50	0.26	2.73	6.4	0.85	1.59	0.58	3.2	339
44	46	7.5	2.21	0.19	2.66	6.0	0.77	1.64	0.59	3.0	318
377	3	7.5				2.9 2.7	0.60	1.15	0.52	1.9	207
	44	6.5		0.26		2.7	0.53	1.19	0.52	1.8	1910
		5.5	1,63	0.17	2.33	2.5	0.46	1.23	0.53	1.7	176

 $\begin{array}{l} L = \text{safe loads in lbs., uniformly distributed; } l = \text{span in feet;} \\ \textbf{\textit{M}} = \text{moment of forces in ft.-lbs.; } C = \text{coefficient given above.} \\ L = \frac{C}{l}; \qquad \textbf{\textit{M}} = \frac{C}{8}; \qquad C = Ll = 8M = \frac{8fS}{12}; \qquad f = \text{fibre stress.} \end{array}$

Properties of Special I Beams - Steel.

1	2	8	4	5	6	7	8	9	10	11	12
Section Index.	Depth of Beam.	Weight per Foot.	Area of Section.	Thickness of Web.	Width of Flange.	Moment of Inertia, Neutral Axis Per- pendicular to Web at Centre.	Moment of Inertia, Neutral Axis Coin- cident with Centre Line of Web.	Radius of Gyration, Neutral Axis Per- pendicular to Web at Centre.	Radius of Gyration, Nentral Axis Coin- cident with Centre Line of Web.	Section Modulus, Neu- tral Axis Perpendic- ular to Web at Cen- tre,	Coefficient of Strength for Fibre Stress of 16,000 lbs. per sq. in.
	in.	lbs.	sq. in.	in.	in.	I	I'	r	r'	8	C
B2	20	100	29.41	$0.88 \\ 0.81 \\ 0.74$	7.28 7.21 7.14 7.06	1655.8	52.65	7.50 7.58 7.67 7.77 7.86 5.53	1.84	165.6	1766100
11	1.	95	27.94	0.81	7.21	1606.8 1557.8	50.78 48.98	7.08	1.35	160.7 155.8	1718900
11	u	90 85	26.47 25.00	0.44	7.14	1508.7	48.98 47.25	7.07	1.36	155.8 150.9	1661600 1609300
41.	a	80	23.73	0.66	7.00	1466.5	45.81	7 96	1.39	146.7	1564300
Bŧ	15	100	29,41	1 18	6.77	900.5	50.98	5 53	1.31	120.1	1280700
Die	144	95	27.94	1 08	6 67	900.5 872.9	48.37	5,59	1.31	116.4	1241500
841	64	90	26.47	0.99	6.58	845.4	45.91	5.65	1.32	112.7	1202300
36	44	85	25.00	0.89	6.48	817.8	43.57	5.65 5.72	1.32	109.0	1163000
44	34	80	23.81	0.81	6.40	795.5	41.76	5.78	1.32	106.1	1131300
B5	15	75	22,06	0.88	6.29	691.2	80.68	5.60	1.18	92.9	988000
4.8	8.5	70	20.59	0.78	6.19	663.6	29.00	5.68	1.19	88.5	943800
14	16	65	19,12			636.0	27.42	5 77	1.20	84.8	904600
45	46	60	17.67	0.59	6.00	609.0	25.96	5.87	1.21	81.2	866100
BS.	12	55		0.82	5.61	321.0	17.46	4.45	1.04	58.5	570600
56	44	50	14.71	0.70	5.49	303.3	16.12	4.54	1.05	50.6	539200
4.6	46	45	18.24	0,58	5.37	285.7	14.89	4.65	1.06	47.6	507900
KX.	10	40	11.84	0.46	5.25	268.9	13.81	4.77	1.08	44.8	478100

Properties of Carnegie Trough Plates-Steel,

Section Index.	Size, in Inches,	Weight per Foot.	Area of Sec- tion.	Thick- ness in Inches.	Moment of Inertia, Neutral Axis Parallel to Length.	Section Modulus, Axis as before.	Radius of Gyra- tion, Axis as before.
M10 M11 M12 M13 M14	916 × 334 916 × 334 916 × 334 916 × 334 916 × 334	lbs, 16,32 18.02 19.72 21.42 23.15	sq. in. 4.8 5.8 5.8 6.8 6.8	9/16 9/16 56 11/16	8.68 4.13 4.57 5.02 5.46	8 1.38 1.57 1.77 1.96 2.15	7 0.91 0.91 0.90 0.90 0.90

Properties of Carnegie Corrugated Plates-Steel,

Section Index.	Size, in Inches.	Weight per Foot,	Area of Sec- tion.	Thick- ness in Inches.	Moment of Inertia, Neutral Axis Parallel to Length.	Section Modulus, Axis as before.	Radius of Gyra- tion, Axis as before.
	894 × 114 834 × 114 934 × 114 12 8/16 × 214 19 8/16 × 234 12 3/16 × 234	19.04 17.75 20.71	sq. in. 2.4 8.0 8.5 5.9 6.1 7.0	14 5/16 84 84 7/16	1 0.64 0.95 1,26 4.79 5.81 6.82	S 0.80 1.13 1.42 9.88 8.90 4.46	7 0.52 0.57 0.62 0.96 0.98 0.99

finite Londa, Uniformly Distributed, for Standard and Special I Beams. (The Carnegle Steel Co., Ltd.)

In Tons of 2000 Lbs.

	3″I.	5.5 lbs.	2.1.1.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.
	4″ I.	7.5 lbs.	8.6. % 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1.
	5″ I.	9.75 lbs.	7.4.8.8.8.9.9.9.9.1.1.1.1.1.1.1.1.1.1.1.1.1
	6″ L	12.25 lbs.	5.4.4.4.8.8.8.8.9.9.9.9.9.9.1.1. 5.4.7.4.8.8.8.8.9.9.9.9.9.9.1.1.
	7", I.	15 lbs.	- 1.0 c c c c c c 4 4 c c c c c c c c c c c
	8″ I.	18 lbs.	7.5.00 7.000 7.5.00 7.00 7
	αəə	steiU wted gqu8 eq ni	28584465
	9″ I.	21 lbs.	ఇంగారం లే బాబాబాబ్ 44444255252
	10" I.	25 lbs.	50000000
	H	81.5 1bs.	2421 1 1 1 1 1 1 9 8 9 1 1 1 1 1 1 1 1 1 1
TOTE OF SOM TOR	12,	40 lbs. Special.	988.00 - 1 4 4 4 8 8 1 1 1 1 1 1 1 1 1 1 1 1 1 1
7 111	8310	Dietar Detw Suppe In Fe	######################################
		42 lbs.	844486487754448881 8111100 0 0 0 0 0 0 0 0 0 0 0 0 0 0
	15" I.	60 lbs. Special.	88888242823608887 555444 8888 8888 8888 8888 8888 888
į		80 lbs. Special.	744088888888888888888888888888888888888
	18'. I.	55 lbs.	88 88 88 88 88 88 88 88 88 88 88 88 88
)	Ť.	65 lbs.	774418887888888888888888888888888888888
	,0 8	80 lbs. Special.	88888844428888888888888888888888888888
	24" I.	80 lbs.	F1808724444688 82888 8888 888 888 888886872444685 87198 888 888
	8110	wted qqu8 qq ni	######################################

Spacing of Carnegie I-Beams for Uniform Load of 100 lbs. per Square Foot.

STEEL. (Proper distance in feet, centre to centre of beams.)

Distance	%√. I.	क्रे	30' I.	18'' I.		16″ I.		15//	T	10'' I.	Distance	9′ I.	% I.	7″ I.	6′′ I.	5″ I.	4″ I.	8′ I.
_	801bs.	801bs. Special.	651bs.	551bs,	8015a. Special.	601 bg. Special.	421bs.	401bs. Special,	81.5 Ibs.	251bs.	Supports in Feet.	21 lbs.	181bs.	15 lbs.	12.25 lbs.	9.75 lbs.	7.5 lbs.	5.5 lbs.
<u>es</u>	128.9	108.6	86.6	65.5	78.6	60.1	43.6	38.3	26.6	18.1	ص	90.8	60.7	2.4	81.0	90.0	12.7	7.0
8	109.8	95.8	73.8	85.8	67.0	51.8	87.2	28.3	200	15.4	9	55.9	42.1	30.7	21.5	14.8	8.8	4
14	2.	79.8	63.7	48.1	57.7	44.2	3 8.1	24.4	19.6	13.3	~	41.1	81.0	22.5	15.8	10.5	6.5	8.8
15	88.5	69.5	56.5	41.9	50.8	88.5	6.78	21.3	17.1	11.6	80	31.5	83.7	17.8	12.1	8.1	5.0	8.8
<u> </u>	78.5	61.1	48.7	8.98	44.2	83.8	24.5	18.7	15.0	10.8	a	8.5	18.7	18.6	9.6	6.4	8.9	2.2
2	64.2	22	48.2	83.6	39.3	30.0	21.7	16.5	13.3	9.0	2	20.1	15.2	11.1	8.2	50	8	1.8
18	87.8	48.8	38.5	29.1	84.9	28.7	19.4	14.8	11.8	8.0	=	16.6	12.5	9.1	6.4	8.4	2.6	1.5
8	51.4	₩.	\$	8	81.8		17.4	13.5	10.6	2.50	12	14.0	10.5	7.7	5.4	3.6	65	H
8	46.4			83.6 6.		21.7	15.7	15.0	9.6	6.5	13	11.9	0.6	6.5	4.6	8.1	1.9	1.0
=	42.1	88 5.	83. 83.	21.4	33.7	19.6	14.2	8.01	8.3	5.9	14	10.8	7.7	5.6	4.0	8.8	1.6	0.0
83	88.4	88.3	終	19.5	23.4	17.9	13.0	6.6	7.9	5.4	ŧ	0	6.7	4.9	3.4	60	1.4	
88 2	88	88	83 8	8:23	21.4	16.4	6.6	9.0	200	9.0	£	64	8	4		0 6	- 6	
38.28	80.00	38	20.0	15.4	18.0	13.9	20.5	200	6.1	0.03	12	2.0	8.	8.8			11	
*	27.5	83 T.	18.5	18.9	16.7	12.8	8.8	7.1	5.7	3.9	82	6.2	4.7	8.4	2.4	1.6	88	:
23	50	21.5	17	12.9	15.5	11.9	8.6	6.6	100	60	10	5.6	4.2	8.1	63	1.4		_
92	88	80.0	2	12.0	14.4	1.0	8.0	6.1	4.9	83	೩	2.0	8.8	80.	1.9	1.8		
8	3	18.6	14 8	11.2	18.5	10.8	2.0	5.7	4.6	8.1	25	4.6	8.4	2.5	1.8	1.2	:	:
2	8	17.4	∞.	10.5	12.6	9.6	0.2	10 00	7	6.6	왏	œ œ	8.1	es es	1.6	1:1	:	:

For any other load than 100 lbs. per square foot, divide the specing given by the Fatio tha given to lad per square foot bears to 100.
Thus for a load of 150 lbs. per square foot divide by 1.5. Maximum fibe atress, 16,000 lbs. per square inch.
Only figures above the cross-lines should be used for plastered cellings, so that the deflection will not cause cracking of the plaster.

Properties of Standard Channels-Steel.

A B	16,000 bs. per sq. in. Distance of Centre of Gravity from Outside of Web.
in. lbs. aq. in. in. in. I I' r r' S C 15 55 16 18 0.82 3.82 430 2 12 19 5 16 868 57.4 6118 " 50 14 71 0.72 3.72 402 7 11 22 5 23 873 53.7 5727 " 45 12 24 6.82 20 275 1 10 29 5 39 392 50 10 10 20 " 45 12 24 6.82 20 275 1 10 29 5 39 392 50 10 10 20 " 45 15 15 15 15 15 15 15	00 .823
*** 40. 11.76 0.52 3.52 347.5	000 784 000 7722 000 6894 000 687 000 6876 000 6896 000 6896

L= safe load in lbs., uniformly distributed; l= span in feet; M= moment of forces in ft.-lbs.; C= coefficient given above.

$$L = \frac{C}{l}$$
; $M = \frac{C}{8}$; $C = Ll = 8M = \frac{8fS}{12}$; $f = \text{fibre stress.}$

					Carneg	te ne	CK-Des	ıms.		
1	2	3	4	5	6	7	8	9	10	11
Depth of Beam.	Weight per Foot.	Area of Section.	Thickness of Web.	Width of Flange.	Moment of Incrtia, Neutral Axis Per- pendicular to Web.	Section Modulus, Neutral Axis Per- pendicular to Web.	Radius of Gyration. Neutral Axis Per- pendicular to Web.	Coefficient of Strengthfor Fibre Stress of 16,000 lbs. per eq. in.	Moment of Inertia, Neutral Axis Co- incident with Centre Line of Web.	Radius of Gyration. Neutral Axis Co- incident with Centre Line of Web.
in. 10 10	lbs.	sq.in.	in. .68	in.	I	8 25.7	7.	\overline{c}	7.41	<u>r'</u>
10	35.70	10.5	.68	5.50	189.9	25.7	3.64 3.88	274100	7.41	0.84
10	27.23	8.0	.38	5.25	118.4	21.2	3.88	226100	6.12	0.87
9	30 00	8.8	.57	5.07	93.2	19.6	8.25	208500	5.18	0.75
9	26.00	7.6	. 44	4.94	85.2	17.7	8.35	189100	4.61	0.76
8	24.48	7.2	.47	5.16	62.8	14.1	2.97	150100	4.45	0.79
8	24.48 20.15	5.9	.81	5.00	55.6	12.2	2.97 3.08	129800	8.90	0.82
9 8 8 7	23.46	6.9	.54	5.10	45.5	11.7	2.57 2.70	124600	4.80	0.79
7	18.11	5.3	.81	4.87	38.8	9.7	2.70	103000	3.55	0.82
6	18.36	5.4	.48	4.58	26.8	8.2	2.25	87700	2.78	0.72
6	15.8C	4.5	.28	4.38	24.0	11.7 9.7 8.2 7.8	2.33	77400	2.38	0.78

Add to coefficient C for every lb. increase in weight of beam, for 10-in. beams, 4900 lbs.; 7-in., 4500 lbs.; 8-in., 4000 lbs.; 7-in., 3400 lbs., 6-in., 3000 lbs.

				arneg	ie Bu	IIb A	ngles.		
10.	[26.50]	7.80 .48	3.5	104.2	19.9	3.66	211700		
9	21.80	6.41 .44	3.5	69.3	14.5	3.33	154200		
8	19.23	5.66 .41	3.5	48.8	11.7	2.95	124800		
7	18.25	5.37 .44	3.0	34.9	9.6	2.56	102300	********	
6	17.20	5.06 .50	3.0	23.9	7.6	2.16	80500		
6	13.75	4.04 .38	3.0	20.1	6.6	2.21	70400		
6	12,30	3.62 .31	3.0	18.6	5.7	2.28	60400		
5	10.00	2.94 .31	2.5	10.2	4.1	1.86	43300	,,,,,,,,,,	

Carnegie T Shapes	Cari	regie	T	Sha	Des
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1	2	3	4	5	6_	7	8	9	10	11
Size : Flange by Stem.	Weight per foot	Area of Section.	Distance of C. of G. from Outside of Flange	Mom. of Inertia, Neutral Axis through C. of G. Parallel to Flange.	Least Section Modulus Neut. Axis through C. of G. Parallel to Flange.	Radius of Gyration, Neut. Axis through C. of G. Parallel to Flange.	Mom. of Inertia, Neutral Axis through C. of G. Coincident with Stem.	Section Modulus, Neut. Axis through C. of G. Coincident with Stem.	Radius of Gyration, Neut. Axis through C. of G. Coincident with Stem.	Coefficient of Strength for Fibre Stress of 13,000 lbs. per sq. in., Neutral Axis through C. of G. Parallel to Flange.
in.	lbs. 13.6 11.0 15.8 8.5 10.0	sq.in. 8.99	in. 0.75	1 2.6	8	r	1' 5.6 4.3 3.77 2.6 8.1 2.6 8.1 2.8 2.1 2.8 2.1 2.8 2.1	8"	7'	7 9410
5 ×3 5 ×21/4 41/4×31/4	13.6	8.99	0.75 0. 6 5	2.6	1.18 0.86 2.13	0.82	5.6	2.22	1.19	9410
5 ×216	11.0	2.24 4.65	0. 6 5 1.11	1.6	0.80	0.71	9.0	1.70 1.65	1.16	6900
414×314 414×3 414×3 414×3	10.0	2.55	1.11 0.73	5.1 1.8	0.81	1.04 0.87 0.86	9.6	1.16	0.90 1.03	17090 6490
416×3	10.0	8.00	0.75	2.1	0.94	0.88	8 1	1.88	1.04	7540
412012	8.0	8.00 2.40 2.79 4.56	0.58	1.1	0.56	0.69	2.6	1.16	1 07	4520
412×216 412×216	9.3	2.79	0.60	1.2	0.65	0.68	8.1	1.88	1.08 0.79 0.78	5230
	9.3 15.6	4.56	1.56		3.10	1.54	2.8	1.41	0.79	24800
4 ×5 4 ×5	112.0	3.54	1.51	8.5	2.43	1.56 1.37	2.1	1.41 1.06	0.78	19410
4 ×416	14.6	4.29	1.37	8.0	2.55	1.37	2.8	1.41 1.06	0.81	20400
4 ×5 4 ×5 4 ×41/4 4 ×4 4 ×4 4 ×8	11.4	8.86	1.81	8.0 6.8 5.7	1.98	1.38	2.1	1.06	0.80	15840
4 ×4	118.7	4.02	1.18	5.7	2.02	1.20	2.8	1.40	0.84	16190
4 ×4 4 ×3 ×21,6	10.9	3.21	1.15	4.7	1.64	1.23	2.2	1.09	0.84	18100
4 ×8	9.8	2.78	0.78	2.0	0.88	0.86	2.1	1.05	0.88	7070
×814	8.6	2.52	0.68	1.2	0.62	0.69	2.1	1.05	0.92	4980

1	2	3	4	5	6	7	8	9	10	11
Size : Flange by Stem.	Weight per foot.	Area of Section.	Distance of C. of G. from Outside of Flange.	Mom. of Inertia, Neutral Axis through C. of G. Parallel to Flange.	Least Section Modulus, Neut, Axis through C. of G. Parallel to Flange.	Axis through C. of G. Parallel to Flange.	Mom. of Inertia, Neutral Axis through C. of G. Coincident with Stem.	Section Modulus, Neutral Axis through C, of G. Coincident with Stem.	Radius of Gyration, Neut. Axis through C. of G. Coincident with Stem.	Coeffi. of Strength for Fibre Stress of 12,000 lbs. per sq. in., Neutral Axis through C. of G. Par-
10. XXX 22 24 4 556 62 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	10.8. 7.3.8 7.9.8 7.9.8 7.9.8 7.9.8 9.9.9 11.73 10.6.6 10.9.8	3.455 3.211 2.494 2.284 3.483 3.213 2.884 2.944 2.677 2.180 2.180 1.95 2.160 1.95 2.160 1.95 1.91 1.91 1.92 1.93 1.93 1.93	Inc.	1.0 0.81	8 0.55 6 0.42 0.40 0.40 0.34 1.75 1.19 0.88 0.72 1.19 1.21 1.10 1.21 1.10 0.86 0.76 0.76 0.76 0.76 0.76 0.77 0.76 0.77 0.77	7 0.70 0.52 0.51 1.21 1.22 1.04 1.05 0.88 0.89 0.92 0.88 1.23 1.25 1.26 1.06 1.09 0.88 0.89 0.90 0.72 0.73 0.73 0.73 0.74 0.83 0.74 0.83 0.74 0.83 0.67 0.60 0.67 0.60 0.67 0.60 0.67 0.67	1.89 1.42 1.89 1.42 1.89 1.42 1.89 1.42 1.07 1.74 1.88 1.41 1.09 1.30 1.30 1.30 1.30 1.30 1.30 1.30 1.30	8' 0.88 0.71 1.05 0.88 0.81 1.08 1.08 1.08 1.08 1.08 1.08	0.91 0.91 0.96 0.96 0.72 0.70 0.73 0.73 0.75 0.76 0.60 0.60 0.68 0.61 0.64 0.63 0.62 0.65 0.55 0.55 0.55 0.55 0.55 0.55 0.55	C 4380 3350 3180 2700 15870 12380 112000 9530 7450 11470 9050 7040 15480 14270 12540 14270 12540 14270 12540 14270 12540 6900 4

Properties of Standard and Special Angles of Minimum and Maximum Thicknesses and Weights.

ANGLES WITH EQUAL LEGS.

1	2	8	4	5	6	7	8	9
Dimensions.	Thickness.	Weight per Foot.	Area of Section.	Distance of Centre of Gravity from Back of Flange.	Moment of Inertia, Neutral Axis through Centre of Gravity Parallel to Flange.	Section Modulus, Neutral Axis through Centre of Gravity Parallel to Flange.	Radius of Gyration, Neutral Axis through Centre of Gravity Parallel to Flange.	Least Radius of Gyration, Neutral Axis through Centre of Gravity at Angle of 45° to Flanges.
in. 6 ×6 6 ×6 *5 ×5 *5 ×5	in. 3/6 7/16 3/6 3/8	88.1 17.2 27.2 12.3	sq. in. 9.74 5.06 7.99 3.61	in. 1.82 1.66 1.57 1.39	I 81.92 17.68 17.75 8.74	8 7.64 4.07 5.17 2.42	r 1.81 1.87 1.49 1.56	1.17 1.19 0.98 0.99
4 × 4	13/16	19.9	5.84	1.29	8.14	8.01	1.18	0.80
4 × 4	5/16	8.2	2.40	1.12	3.71	1.29	1.24	0.82
814 × 814	13/16	17.1	5.03	1.17	5.25	2.25	1.02	0.69
814 × 814	5/8	8.5	2.48	1.01	2.87	1.15	1.07	0.70
8 × 8	144	11.4	8.36	0.98	2.62	1.30	0.88	0.59
8 × 3		4.9	1.44	0.84	1.24	0.58	0.93	0.60
*23/4 × 23/4		8.5	2.50	0.87	1.67	0.89	0.82	0.54
*23/4 × 23/4		4.5	1.81	0.78	0.93	0.48	0.85	0.55
214 × 214	14	7.7	2.25	0.81	1.23	0.78	0.74	0.49
214 × 214		4.1	1.19	0.72	0.70	0.40	0.77	0.50
*214 × 214		6.8	2.00	0.74	0.87	0.58	0.66	0.48
*214 × 214		3.7	1.06	0.66	0.51	0.32	0.69	0.46
2 × 2	7/16	5.3	1.56	0.66	0.54	0.40	0.59	0.89
2 × 2	8/16	2.5	0.72	0.57	0.28	0.19	0.62	0.40
134 × 134	7/16	4.6	1.80	0.59	0.35	0.30	0.51	0.35
154 × 154	3/16	2.1	0.62	0.51	0.18	0.14	0.54	0.36
114 × 114	3/16	3.4	0.99	0.51	0.19	0.19	0.44	0.81
114 × 114	3/16	1.8	0.53	0.44	0.11	0.104	0.46	0.82
114 × 114	5/16	2.4	0.69	0.42	0.09	0.109	0.36	0.25
114 × 114	1/8	1.0	0.30	0.35	0.044	0.049	0.88	0.26
*11/6 × 11/6	5/16	2.1	0.61	0.39	0.063	0.087	0.82	0.24
*11/6 × 11/8	16	0.9	0.27	0.32	0.032	0.039	0.84	0.23
1 × 1	14	1.5	0.44	0.34	0.037	0.056	0.29	0.20
1 × 1	18	0.8	0.24	0.30	0.022	0.031	0.81	0.21
*76 × 76 *76 × 36 \$4 × \$4 \$4 × \$4 *56 × \$6	3/16 3/16 3/16 1/6	1.0 0.7 0.8 0.6 0.5	0.29 0.21 0.25 0.17 0.14	0.29 0.26 0.26 0.23 0.20	0.019 0.014 0.012 0.009 0.005	0.033 0.028 0.024 0.017 0.011	0.26 0.26 0.22 0.28 0.18	0.18 0.19 0.16 0.17 0.18

Properties of Standard and Special Angles of Minimum and Maximum Thickness and Weights.

ANGLES WITH UNEQUAL LEGS.

1	2	3	4	5	6	7	8	9	10	11
		ıt.	ď	Mome	nts of rtia. I	Mod	tion ulus.	Radii	of Gyra	tion.
Dimensions.	Thickness,	Weight per Foot.	Area of Section.	Neutral Axis Parallel to Longer Flange.	Neutral Axis Par- allel to Shorter Flange.	Neutral Axis Par- allel to Longer Flange.	Neutral Axis Par- allel to Shorter Flange.	Neutral Axis Par- allel to Longer Flange.	Neutral Axis Par- allel to Shorter Flange.	Least Radius. Axis diagonal.
inches. *7 ×3½ *7 ×3½ 6 ×4 6 ×4	inch. 7/16 7/8 3/8	lbs. 32 8 15.0 27.2 12.3	sq. in. 9.50 4.40 7.99 3.61	7.53 8.95 9.75 4.90	45.87 22.56 27.73 13.47	2.96 1.47 3.39 1.60	10.58 5.01 7.15 8.32	0.89 0.95 1.11 1.17	2.19 2.26 1.86 1.98	.88 .89 .88
6 ×31/6 6 ×31/6 *5 ×4 *5 ×4	7/8 8/8 7/8 8/8	25.7 11.7 24.9 11.0	7.55	6.55 3.84 9.28 4.67	26.38 12.86 16.42 8.14	2.59 1 23 3.31 1.57	6.98 8.25 4.99 2.84	0.93 0.99 1.14 1.20	1.87 1.94 1.52 1.59	.78 .77 .88 .86
5 ×81/6 5 ×31/6 5 ×3 5 ×3	76 38 13/16 5/16	22.7 10.4 19.9 8.2	6 67 3.05 5.84 2.40	6.21 8.18 3.71 1.75	15.67 7.78 13.98 6.26	2.52 1.21 1.74 0.75	4.88 2.29 4.45 1.89	0.96 1.02 0.80 0.85	1.58 1.60 1.55 1.61	.77 .76 .66
*41/6×3 *41/6×3 *4 ×31/6 *4 ×31/6	13/16 3/8 13/16 3/8	18.5 9 1 18.5 9.1	5.48 2.67 5.48 2.67	3.60 1.98 5.49 2.99	10.33 5.50 7.77 4.18	1.71 0.88 2.30 1.18	3.62 1.83 2.92 1.50	0.81 0.86 1.01 1.06	1.88 1.44 1.19 1.25	.67 .66 .74 .73
4 ×3 4 ×3 316×3 316×3	13/16 5/16 13/16 5/16	17.1 7.1 15.7 6.6	5.08 2.09 4.62 1.98	3.47 1.65 3.33 1.58	7 34 3.38 4.98 2.33	1.68 0.74 1.65 0.72	2.87 1.23 2.20 0.96	0.83 0.89 0.85 0.90	1.21 1.27 1.04 1.10	.66 .65 .65
814×214 314×214 *314×2 *814×2	11/16 14 9/16 14	12.4 4.9 9.0 4.8	3.65 1.44 2.64 1.25	1.72 0.78 0.75 0.40	4.13 1.80 2.64 1.36	0.99 0.41 0.53 0.26	1.85 0.75 1.30 0.63	0.67 0.74 0.58 0.57	1.06 1.12 1.00 1.04	.58 .55 .45 .44
3 ×21/6 3 ×21/2 *3 ×2 *3 ×2	9/16 14 13 14	9.5 4.5 7.7 4.0	2.78 1.81 2.25 1.19	1.42 0.74 0.67 0.89	2.28 1.17 1.92 1.09	0.82 0.40 0.47 0.25	1.15 0.56 1.00 0.54	0.72 0.75 0.55 0.56	0.91 0.95 0.92 0.95	.54 .53 .47 .46
216×2 216×2 *214×116 *214×176	3/16 3/16 3/16 3/16	6.8 2.8 5.5 2.3	2.00 0.81 1.63 0.67	0.64 0.29 0.26 0.12	1.14 0.51 0.82 0.34	0.46 0.20 0.26 0.11	0.70 0.29 0.59 0.23	0.56 0.60 0.40 0.43	0.75 0.79 0.71 0.72	.44 .43 .89 .40
*2 ×1% *2 ×1% *1%×1 *1%×1	3/16 1/4 1/8	2.7 2 1 1.8 1.0	0.78 0.60 0.53 0.28	0.12 0 09 0.04 0.02	0.37 0.24 0.09 0.05	0.12 0.09 0.05 0.03	0.23 0.18 0.09 0.06	0.89 0.40 0.27 0.29	0.63 0.63 0.41 0.44	.30 .29 .25

Properties of Carnegie E Bars.

(For dimensions see table on rage 178.)

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1	2	3	4	5	6	7	8	9	10	11	12
Section Index.	Weight per Foot,	Area of Section.	Mom. of Inertia. Neutral Axis through C. of Gr. Perpendicular to Web.	Mom. of Inertia, Neutral Axis through C. of Gr. Coincident with Web.	Section Modulus, Neutral Axis through C. of Gr. Perpendicular to Web.	Section Modulus, Neutral Axis through C. of Gr. Colneident with Web.	Radii of Gyration, Neut. Axis through C. of Gr. Perpendicular to Web.	Radii of Gyration. Neut. Axis through C. of Gr. Coincident with Web.	Radii of Gyration. Least Radius, Neutral Axis Diagonal.	Coeff. of Strength for Fibre Stress of 16,000 lbs. per sq. in., Axis Perpen- dicular to Web at Centre.	Coeff. of Strength for Fibre Stress of 12,000 bs. per 8q. in Axis Perpen- dicular to Web at Centre,
Z1	15.6 18.3 21.0	sq. in. 4.59 5.89 6.19	I 25.32 29.80 34.36	9.11 10.95 12.87	8 8.44 9.88 11.22	\$ 2.75 3.27 3.81	r 2.35 2.35 2.36	r 1.41 1.43 1.44	0.83 0.84 0.84	C 90,000 104,800 119,700	C' 67,500 78,600 89,800
Z2	22.7 25.4 28.0	6.68 7.46 8.25	34.64 38.86 48.18	12.59 14.42 16.34	11.55 12.82 14.10	3.91 4.43 4.98	2,28 2,28 2,29	1.37 1.39 1.41	0.81 0.82 0.84	123,200 136,700 150,400	92,400 102,600 112,800
Z3	29.3 32.0 34.6	8.63 9.40 10.17	42.12 46.13 50.22	15.44 17.27 19.18	14.04 15.32 16.40	4.94 5.47 6.03	2.21 2.22 2.22	1.34 1.36 1.37	0.81 0.82 0.83	149,800 162,300 174,900	112,300 121.500 181,200
Z4	11.6 13.9 16.4	3.40 4.10 4.81	18.36 16.18 19.07	6.18 7.65 9.20	5.34 6.39 7.44	2.00 2.45 2.92	1.98 1.99 1.99	1.35 1.37 1.38	0.75 0.76 0.77	57,000 68,200 79,400	42,700 51,100 59,500
Z5	17.8 20.2 22.6	5.25 5.94 6.64	19.19 21.83 24.53	9.05 10.51 12.06	7.68 8.62 9.57	3.02 3.47 3.94	1.91 1.91 1.92	1.31 1.33 1.35	0.74 0.75 0.76	81,900 91,900 102,100	61,400 69,000 76,600
Z6	28.7 26.0 28.3	6,96 7.64 8.38	23.68 26.16 28.70	11.37 12.83 14.36	9.47 10.34 11.20	3.91 4.87 4.84	1.84 1.85 1.86	1.28 1.30 1.31	0.78 0.75 0.76	101.000 110,300 119,500	75,800 82,700 89,600
Z7	8.9 10.3 12.4	2.41 8.03 3.66	6.28 7.94 9.63	4.28 5.46 6.77	3.14 3.91 4.67	1.44 1.84 2.26	1.62 1.62 1.62	1.33 1.34 1.36	0.68 0.69	33,500 41,700 49,800	25,100 81,800 37,400
Z8	18.8 15.8 17.9	4.05 4.66 5.27	9.66 11.18 12.74	6.78 7.96 9.26	4.83 5.50 6.18	2.37 2.77 3.19	1,55 1,55 1,55	1.29 1.31 1.33	0.66 0.67 0.69	51,500 58,700 65,900	38,600 44,000 49,400
Z9	18.9 20.9 22.9	5.55 6.14 6.75	12.11 13.59 14.97	8.73 9.95 11.24	6.05 6.65 7.26	3.18 3.58 4.00	1.48 1.48 1.49	1.25 1.27 1.29	0.66 0.67 0.69	61,500 70,900 77,400	48,400 53,200 58,100
Z10	8.7 8.4	1.97 2.48	2.87 3.64	2.81 3.64	1.92 2.38	1.10 1.40	1.21 1.21	1.19 1.21	0.55	20 500 25,400	15,400 19,000
Z11	9.7	2.86 8.36	3.85 4.57	3.92 4.75	2.57 2.98	1.57 1.88	1.16 1.17	1.17 1.19	0.55 0.56	27,400 31,800	20,600 28,800
Z12	12.5 14.3	3.69 4.18	4.59 5.26	4 85 5.70	3.00	1.99 2.31	1.12 1.12	1.15 1.17	0.55	32,600 36,600	24,500 27,400

Dimensions of lightest weight bars of each size: Z1, Z2, and Z3, depth of web 6 in., width of flange 3½ in., thickness of metal respectively 3%, 9/16, and 3½ in.; Z4, Z5, Z6, 5 × 3½ × 5/16, ½, and 11/16 in.; Z7, Z8, Z9, 4 × 3 1/16 × ½, 37, 10, and 3½ in.; Z10, Z11, Z12, 3 × 2 11/16 × ½, 3%, and ½ in. Each mension is increased 1/16 in. in the next heavier weight.

FLOORING MATERIAL.

For fire-proof flooring, the space between the floor-beams may be spanned with brick arches, or with hollow brick made especially for the purpose, the latter being much lighter than ordinary brick.

latter being much lighter than ordinary brick.

Arches 4 inches deep of solid brick weigh about 70 lbs. per square foot, including the concrete levelling material, and substantial floors are thus made up to 6 feet span of arch, or much greater span if the skew backs at the springing of the arch are made deeper, the rise of the arch being preferably not less than 1/10 of the span. Hollow brick for floors are usually in depth about ½ of the span, and are used up to, and even exceeding, spans of 10 feet. The weight of the latter material will vary from 20 lbs. per square foot for 3-foot spans up to 60 lbs. per square foot for spans of 10 feet. square foot for 3-foot spans up to 60 lbs. per square foot for spans of 10 feet. Full particulars of this construction are given by the manufacturers. For supporting brick floors the beams should be securely tied with rods to resist the lateral pressure.

In the following cases the loads, in addition to the weight of the floor

itself, may be assumed as:

For street bridges for general public traffic	80 lbs. p	er sq. ft.
For floors of dwellings	80 lbs. po 40 lbs. 80 lbs	" - "
For churches, theatres, and ball-rooms	80 lbs.	** **
For hay-lofts	80 lbs	66 66
For storage of grain		** **
For warehouses and general merchandise	OKO Iba	66 46
For warehouses and general merchandise	400 108.	16 66
For factories 200 to		
For snow thirty inches deep	16 lbs.	
For maximum pressure of wind	50 lbs.	46 46
For brick walls	112 lbs. pe	er cu. ft.
For masonry walls 116-		"
Roofs, allowing thirty pounds per square foot for win	nd and sn	ow:
For corrugated iron laid directly on the purlins For corrugated iron laid on boards	87 lbs. pe	er sa. ft.
For corrugated iron laid on boards	40 lbs.	
For slate nailed to laths	48 lbg	66 66
For clote neiled on hoards	46 lbg	46 66

If plastered below the rafters, the weight will be about ten pounds per square foot additional.

TIE-RODS FOR BEAMS SUPPORTING BRICK ARCHES.

The horizontal thrust of brick arches is as follows:

$$\frac{1.5WS^2}{R} = \text{pressure in pounds. per lineal foot of arch:}$$

W =load in pounds. per square foot; S =span of arch in feet;

R = rise in inches.

Place the tie-rods as low through the webs of the beams as possible and spaced so that the pressure of arches as obtained above will not produce a greater stress than 15,000 lbs. per square inch of the least section of the bolt.

TORSIONAL STRENGTH.

Let a horizontal shaft of diameter = d be fixed at one end, and at the other or free end, at a distance = l from the fixed end, let there be fixed a horizontal lever arm with a weight = P acting at a distance = a from the axis of the shaft so as to twist it; then Pa = moment of the applied force.

Resisting moment = twisting moment = $\frac{SJ}{SJ}$ $\frac{c}{c}$, in which S = unit shearingresistance, J = polar moment of inertia of the section with respect to the axis, and c = distance of the most remote fibre from the axis, in a crosssection. For a circle with diameter d.

$$J = \frac{\pi d^4}{32}; \qquad c = \frac{1}{16}d;$$

$$P_3 = \frac{SJ}{c} = \frac{\pi d^3S}{16} = \frac{d^3S}{5.1} = .1968d^3S; \quad d = \sqrt[3]{\frac{5.1Pa}{8}}.$$

For hollow shafts of external diameter d and internal diameter d_1 ,

$$Pa = .1963 \frac{d^4 - d_1^4}{d}S;$$
 $d = \sqrt[3]{\frac{5.1Pa}{\left(1 - \frac{d_1^4}{d^4}\right)S}}.$

For a square whose side = d,

$$J = \frac{d^4}{6};$$
 $c = d\sqrt{\frac{1}{16}};$ $\frac{SJ}{c} = Pa = \frac{d^3S}{4.2426} = 0.236d^3S.$

For a rectangle whose sides are b and d,

$$J = \frac{bd^3}{12} + \frac{b^3d}{12}; \qquad c = \frac{1}{2}\sqrt{b^2 + d^3}; \qquad \frac{8J}{c} = Pa = \frac{(bd^3 + b^3d)S}{8J\sqrt{b^2 + d^3}}.$$

The above formulæ are based on the supposition that the shearing resistance at any point of the cross-section is proportional to its distance from the axis; but this is true only within the elastic limit. In materials capable of flow, while the particles near the axis are strained within the elastic limit those at some distance within the circumference may be strained nearly to those at some distance within the circumference may be strained nearly to the ultimate resistance, so that the total resistance is something greater than that calculated by the formulæ. (See Thurston, "Matls. of Eng.," Part II. p. 527.) Saint Venant finds for square shafts $Pa = 0.208d^3S$ (CotterIII. "Applied Mechanics," pp. 348, 355). For working strength, however, the formulæ may be used, with S taken at the safe working unit resistance. For a rectangle, sides b (longer) and d (shorter) and area A, $Pa = \frac{SA^2}{8b+1.8d}.$

$$Pa = \frac{SA^2}{2b + 18d}.$$

The ultimate torsional shearing resistance S is about the same as the direct shearing resistance, and may be taken at 20,000 to 25,000 lbs. per square inch for cast iron, 45,000 lbs. for wrought iron, and 50,000 to 150,000 lbs. for steel, according to its carbon and temper. Large factors of safety should be taken, especially when the direction of stress is reversed, as in reversing engines, and when the torsional stress is combined with other stresses, as is usual in shafting. (See "Shafting.") **Elastic Resistance to Torsion.**—Let l = length of bar being twisted, d = diameter, P = force applied at the extremity of a lever arm of length = a, Pa = t wisting moment, G = t torsional modulus of elasticity, $\theta = angle through which the free end of the shaft is twisted, measured in arc of radius <math>= 1$.

arc of radius = 1.
For a cylindrical shaft
$$Pa = \frac{\pi\theta Gd^4}{32l}; \qquad \theta = \frac{32Pal}{\pi d^4G}; \qquad G = \frac{32Pal}{\theta\pi d^4}; \qquad \frac{32}{\pi} = 10.186.$$

If a =angle of torsion in degrees,

$$\theta = \frac{a\pi}{180};$$
 $a = \frac{180\theta}{\pi} = \frac{180 \times 32 Pal}{\pi^2 d^4 G} = \frac{583.6 Pal}{d^4 G}.$

The value of G is given by different authorities as from $\frac{1}{4}$ to $\frac{2}{5}$ of E, the modulus of elasticity for tension.

COMBINED STRESSES.

(From Merriman's "Strength of Materials.")

Combined Tension and Flexure.—Let A = the area of a bar subjected to both tension and flexure, P = tensile stress applied at the ends, But yet the unit tensile stress, S = unit stress at the fibre on the tensile side most remote from the neutral axis, due to flexure alone, then maximum tensile unit stress = (P + A) + S. A beam to resist combined tension and flexure should be designed so that (P + A) + S shall not exceed the proper allowable working unit stress.

Combined Compression and Flexure.—If P+A= unit stress due to compression alone, and S= unit compressive stress at fibre most remote from neutral axis, due to flexure alone, then maximum compressive unit stress = $(P + A) + \dot{S}$, Combined Tension (or Compression) and Shear.—If ap-

plied tension (or compression) unit stress = p, applied shearing unit stress = v, then from the combined action of the two forces

Max.
$$S = \pm \sqrt{v^2 + \frac{1}{4}p^2}$$
, Maximum shearing unit stress;

Max. $t = \frac{1}{2}p + \sqrt{v^2 + \frac{1}{4}p^2}$, Maximum tensile (or compressive) unit stress.

Combined Flexure and Torsion.—If S = greatest unit stress due to flexure alone, and $S_0 =$ greatest torsional shearing unit stress due to torsion alone, then for the combined stresses

Max. tension or compression unit stress $t = \frac{1}{2}S + \sqrt{Ss^2 + \frac{1}{4}S^2}$;

Max. shear
$$s = \pm \sqrt{Ss^2 + \frac{1}{4}S^2}$$
.

Formula for diameter of a round shaft subjected to transverse load while transmitting a given horse-power (see also Shafts of Engines):

$$d^{3} = \frac{16M}{\pi t} + \frac{16}{t} \sqrt{\frac{M^{2}}{\pi^{2}} + \frac{402,500,000H^{2}}{n^{2}}},$$

where $M=\max$ innum bending moment of the transverse forces in pound-inches, H= horse-power transmitted, n= No. of revs. per minute, and t= the safe allowable tensile or compressive working strength of the material. **Combined Compression and Torsion.**—For a vertical round shaft carrying a load and also transmitting a given horse-power, the result-

ant maximum compressive unit stress

$$t = \frac{4P}{\pi d^2} + \sqrt{321,000^2 \frac{H^2}{n^2 d^6} + \frac{16P^2}{\pi^2 d^4}},$$

in which P is the load. From this the diameter d may be found when t and

Stress due to Temperature.—Let l = length of a bar, A = its sectional area, c = coefficient of linear expansion for one degree, t = rise or fall in temperature in degrees, t = modulus of elasticity, $t = \text{the change of length due to the rise or fall <math>t$; if the bar is free to expand or contract, t = the change of length due to the rise or fall t; if the bar is free to expand or contract, t = the change of length due to the rise or fall t; if the bar is free to expand or contract, t = the change of length due to the rise or fall t; if the bar is free to expand or contract. ctl

If the bar is held so as to prevent its expansion or contraction the stress produced by the change of temperature = S = ActE. The following are average values of the coefficients of linear expansion for a change in temperature of one degree Fahrenheit:

For brick and stone....a = 0.0000050, For cast iron......a = 0.0000062, For wrought iron.....a = 0.0000067,

The stress due to temperature should be added to or subtracted from the stress caused by other external forces according as it acts to increase or to

relieve the existing stress.

What stress will be caused in a steel bar 1 inch square in area by a change of temperature of 100° F.? $S = ActE = 1 \times .0000065 \times 100 \times 30.000,000 = 19,500$ lbs. Suppose the bar is under tension of 19,500 lbs. between rigid abutments before the change in temperature takes place, a cooling of 100° F, will double the tension, and a heating of 100° will reduce the tension to zero,

STRENGTH OF FLAT PLATES.

For a circular plate supported at the edge, uniformly loaded, according to Grashof.

$$f = \frac{5}{6} \frac{r^2}{t^2} p;$$
 $t = \sqrt{\frac{5r^2p}{6f}};$ $p = \frac{6ft^2}{5r^2}.$

For a circular plate fixed at the edge, uniformly loaded,

$$f = \frac{2}{3} \frac{r^2}{t^2} p;$$
 $t = \sqrt{\frac{2}{3} \frac{r^2 p}{f}};$ $p = \frac{8ft^2}{2r^2};$

in which f denotes the working stress; r, the radius in inches; t, the thick ness in inches; and p, the pressure in pounds per square inch.

For mathematical discussion, see Lanza, "Applied Mechanics," p. 900, etc. Lanza gives the following table, using a factor of safety of 8, with tensile strength of cast iron 20,000, of wrought iron 40,000, and of steel 80,000:

	Supported.	Fixed.
Cast iron t	$= .0182570r \sqrt{p}$	$t = .0163300r \sqrt{p}$
Wrought iront	$= .0117850r \sqrt{p}$	$t = .0105410r \sqrt{p}$
Steelt	$= .0091287r \sqrt{p}$	$t = .0081649r \sqrt{p}$

For a circular plate supported at the edge, and loaded with a concentrated load P applied at a circumference the radius of which is r_a :

$$f = \left(\frac{4}{3}\log\frac{r}{r_0} + 1\right) \frac{P}{\pi t^2} = c \frac{P}{\pi t^2};$$
for $\frac{r}{r_0} = 10$ 20 30 40 50;
 $c = 4.07$ 5.00 5.58 5.92 6.22;
 $t = \sqrt{\frac{cP}{\pi f}};$ $P = \frac{\pi t^2 f}{c}.$

The above formulæ are deduced from theoretical considerations, and give thicknesses much greater than are generally used in steam-engine cylinderheads. (See empirical formulæ under Dimensions of Parts of Engines.) The theoretical formulæ seem to be based on incorrect or incomplete hypotheses, but they err in the direction of safety.

theoretical formulæ seem to be based on incorrect or incomplete hypotheses, but they err in the direction of safety.

The Strength of Unetayed Flat Surfaces.—Robert Wilson (Eng'g, Sept. 24, 1877) draws attention to the apparent discrepancy between the results of theoretical investigations and of actual experiments on the strength of unstayed flat surfaces of boiler-plate, such as the unstayed flat crowns of domes and of vertical boilers.

strength of unstayed hat surfaces of coller-plate, such as the unstayed hat rowns of domes and of vertical boilers.

Rankine's "Civil Engineering" gives the following rules for the strength of a circular plate supported all round the edge, prefaced by the remark that "the formula is founded on a theory which is only approximately true, but which nevertheless may be considered to involve no error of practical importance:"

$$M = \frac{Wb}{6\pi} = \frac{Pb^3}{94}$$
.

Here

M =greatest bending moment;

 $W = \text{total load uniformly distributed} = \frac{Pb^2\pi}{4}$;

b = diameter of plate in inches;

P =bursting pressure in pounds per square inch.

Calling t the thickness in inches, for a plate supported round the edges,

$$M = \frac{1}{6} 42,000bt^2;$$
 $\therefore \frac{Pb^3}{24} = 7000t^2.$

For a plate fixed round the edges,

$$\frac{2}{8} \frac{Pb^2}{24} = 7000t^2$$
; whence $P = \frac{t^2 \times 63,000}{t^2}$,

where r = radius of the plate.

Dr. Grashof gives a formula from which we have the following rule:

$$P = \frac{t^9 \times 72,000}{t^{-2}}.$$

This formula of Grashof's has been adopted by Professor Unwin in his "Elements of Machine Design." These formulæ by Rankine and Grashof may be regarded as being practically the same.

may be regarded as being practically the same.

On trying to make the rules given by these authorities agree with the results of his experience of the strength of unstayed flat ends of cylindrical bollers and domes that had given way after long use, Mr. Wilson was led to believe that the above rules give the breaking strength much lower than it

actually is. He describes a number of experiments made by Mr. Nichols of Kirkstall, which gave results varying widely from each other, as the method of supporting the edges of the plate was varied, and also varying widely from the calculated bursting pressures, the actual results being in all cases

very much the higher. Some conclusions drawn from these results are:

1. Although the bursting pressure has been found to be so high, boiler-makers must be warned against attaching any importance to this, since the plates deflected almost as soon as any pressure was put upon them and sprang back again on the pressure being taken off. This springing of the plate in the course of time inevitably results in grooving or channelling, which, especially when aided by the action of the corrosive acids in the water or steam, will in time reduce the thickness of the plate, and bring about the destruction of an unstayed surface at a very low pressure.

2. Since flat plates commence to deflect at very low pressures, they should never be used without stays; but it is better to dish the plates when they are

not stayed by flues, tubes, etc.

3. Against the commonly accepted opinion that the limit of elasticity should never be reached in testing a boiler or other structure, these experi-ments show that an exception should be made in the case of an unstayed flat end-plate of a boiler, which will be safer when it has assumed a permanent set that will prevent its becoming grooved by the continual variation of pressure in working. The hydraulic pressure in this case simply does what should have been done before the plate was fixed, that is, dishes it.

4. These experiments appear to show that the mode of attaching by flange or by an inside or outside angle-iron exerts an important influence on the manner in which the plate is strained by the pressure.

When the plate is secured to an angle-iron, the stretching under pressure is, to a certain extent, concentrated at the line of rivet-holes, and the plate partakes rather of a beam supported than fixed round the edge. Instead of the strength increasing as the square of the thickness, when the plate is attached by an angle-iron, it is probable that the strength does not increase even directly as the thickness, since the plate gives way simply by stretching at the rivet-holes, and the thicker the plate, the less uniformly is the strain borne by the different layers of which the plate may be considered to be made up. When the plate is flanged, the flange becomes compressed by the pressure against the body of the plate, and near the rim, as shown by the contrary flexure, the inside of the plate is stretched more than the outside, and it may be by a kind of shearing action that the plate gives way along

the line where the crushing and stretching meet.

5. These tests appear to show that the rules deduced from the theoretical investigations of Lamé, Rankine, and Grashof are not confirmed by experi-

ment, and are therefore not trustworthy.

The rules of Lamé, etc., apply only within the elastic limit. (Eng'g, Dec. 13, 1895.)

Unbraced Wrought-iron Heads of Boilers, etc. (The Locomotive, Feb. 1890).-Few experiments have been made on the strength of flat heads, and our knowledge of them comes largely from theory. Experi-ments have been made on small plates 1-16 of an inch thick, yet the data so obtained cannot be considered satisfactory when we consider the far thicker heads that are used in practice, although the results agreed well with Ran-kine's formula. Mr. Nichols has made experiments on larger heads, and from them he has deduced the following rule: "To find the proper thickness for a flat unstayed head, multiply the area of the head by the pressure per square inch that it is to bear safely, and multiply this by the desired factor of safety (say 8); then divide the product by ten times the tensile strength of the material used for the head." His rule for finding the bursting pressure when the dimensions of the head are given is: "Multiply the thickness of the end-plate in inches by ten times the tensile strength of the material used, and divide the product by the area of the head in inches."

In Mr. Nichols's experiments the average tensile strength of the iron used for the heads was 44,800 pounds. The results he obtained are given below, with the calculated pressure, by his rule, for comparison.

1. An unstayed flat boiler-head is $34\frac{1}{2}$ inches in diameter and 9-16 inch thick. What is its bursting pressure? The area of a circle $34\frac{1}{2}$ inches in diameter is 935 square inches; then $9-16 \times 44.800 \times 10 = 252.000$, and $252.000 \times 935 = 270$ pounds, the calculated bursting pressure. The head actually burst at 930 rounds. at 280 pounds.

2. Head 3414 inches in diameter and 36 inch thick. The area = 33 square inches; then, $\frac{5}{2}$ × 44,800 × 10 = 188,000, and $\frac{168,000}{2}$ + $\frac{935}{2}$ = 180 pound-calculated bursting pressure. This head actually burst at 200 pounds. The area = 935 3. Head 2614 inches in diameter, and 36 inch thick. The area 541 square inches. Then, $36\times44,800\times10=168,000$, and 168,000+541=311 pounds. This head burst at 370 pounds.

4. Head 28½ inches in diameter and 36 inch thick. The area = 638 square inches; then, $\frac{9}{6} \times 44,800 \times 10 = 168,000$, and 168,000 + 638 = 263 pounds. The actual bursting pressure was 300 pounds. In the third experiment, the amount the plate bulged under different

pressures was as follows:

At pounds per sq. in.... 10 20 Plate bulged.........1/32 1/16 120 140 170 200 1/8 14 34

The pressure was now reduced to zero, "and the end sprang back 8-18 inch, leaving it with a permanent set of 9-16 inch. The pressure of 200 lbs, was again applied on 86 separate occasions during an interval of five days, the bulging and permanent set being noted on each occasion, but without any appreciable difference from that noted above.

The experiments described were confined to plates not widely different in their dimensions, so that Mr. Nichols's rule cannot be relied upon for heads

that depart much from the proportions given in the examples.

Thickness of Flat Cast-iron Plates to resist Bursting Pressures.—Capt. John Ericsson (Church's Life of Ericsson) gave the following rules: The proper thickness of a square cast-iron plate will be obtained by the following: Multiply the side in feet (or decimals of a foot) by 14 of the pressure in pounds and divide by 850 times the side in inches; the westignt is the cause of the thickness in inches.

quotient is the square of the thickness in inches.

For a circular plate, multiply 11-14 of the diameter in feet by 1/4 of the pressure on the plate in pounds. Divide by 850 times 11-14 of the diameter

in inches. [Extract the square root.]
Prof. Wm. Harkness, Eng of News, Sept. 5, 1895, shows that these rules can be put in a more convenient form, thus:

For square plates $T = 0.00495S \sqrt{p_s}$ and

For circular plates $T = 0.00439D \sqrt{p}$,

where T= thickness of plate, S= side of the square, D= diameter of the circle, and p= pressure in lbs. per sq. in. Professor Harkness, however, doubts the value of the rules, and says that no satisfactory theoretical solution has yet been obtained.

Strength of Stayed Surfaces.—A flat plate of thickness t is supported uniformly by stays whose distance from centre to centre is a, uniform load p lbs. per square inch. Each stay supports pa^2 lbs. The greatest stress on the plate is

 $f = \frac{2}{9} \frac{a^2}{t^2} p. \text{ (Unwin)}.$

SPHERICAL SHELLS AND DOMED BOILER-HEADS.

To find the Thickness of a Spherical Shell to resist a given Pressure,—Let d = diameter in inches, and p the internal pressure per square inch. The total pressure which tends to produce rupture around the great circle will be $\frac{1}{2}\pi d^2p$. Let S = safe tensile stress per square inch, and t the thickness of metal in inches; then the resistance to the pressure will be #dtS. Since the resistance must be equal to the pressure.

$$\frac{1}{4}\pi d^2p = \pi dtS$$
. Whence $t = \frac{pd}{4S}$.

The same rule is used for finding the thickness of a hemispherical head

The same rule is used for intaining the which we say to a cylinder, as of a cylindrical boiler.

Thickness of a Domed Head of a boiler,—If S =safe tensile stress per square inch, d =diameter of the shell in inches, and t =thickness of the shell, t = pd + 2S; but the thickness of a kemispherical head of the same diameter is t = pd + 4S. Hence if we make the radius of curvature of a domed head equal to the diameter of the boiler, we shall have t = $\frac{2pd}{4S} = \frac{pd}{2S}$, or the thickness of such a domed head will be equal to the thick-

ess of the shell.

Stresses in Steel Plating due to Water-pressure, as in plating of vessels and bulkheads (Engineering, May 22, 1891, page 629).

Mr. J. A. Yates has made calculations of the stresses to which steel plates

are subjected by external water-pressure, and arrives at the following con-

Assume 2a inches to be the distance between the frames or other rigid supports, and let d represent the depth in feet, below the surface of the water, of the plate under consideration, t = thickness of plate in inches, D the deflection from a straight line under pressure in inches, and P = stress per square inch of section.

For outer bottom and ballast tank plating, $a = 420\frac{t}{a}$, D should not be greater than .05 $\frac{2a}{12}$, and $\frac{P}{2}$ not greater than 2 to 3 tons; while for bulkheads, etc., $a = 2352 \frac{t}{d}$, D should not be greater than $.1\frac{2n}{12}$, and $\frac{P}{2}$ not greater than 7 tons. To illustrate the application of these formulæ the following cases have been taken:

For	Outer Bo	ttom, etc.	For Bulkheads, etc.					
Thick- ness of Plating.	ss of below Water. Frames shown to exceed in. in. 20 About 21	Spacing of Frames should not exceed	Thick- ness of Plating	Depth of Water.	Maximum Spacing of Rigid Stiffeners.			
XXXXXX	ft. 20 10 18 9 10	About 21 " 42 " 18 " 36	in.	ft. 20 20 10 20 10	ft. in. 9 10 7 4 14 8 4 10 9 8 4 10			

It would appear that the course which should be followed in stiffening bulkheads is to fit substantially rigid stiffening frames at comparatively wide intervals, and only work such light angles between as are necessary for making a fair job of the bulkhead.

THICK HOLLOW CYLINDERS UNDER TENSION.

Burr, "Elasticity and Resistance of Materials," p. 36, gives

$$t = r \left\{ \left(\frac{h+p}{h-p} \right)^{\frac{1}{2}} - 1 \right\} \cdot \begin{array}{l} t = \text{thickness}; \ r = \text{interior radius}; \\ h = \text{maximum allowable hoop tension at the} \\ \text{interior of the cylinder}; \\ p = \text{intensity of interior pressure}. \end{array}$$

Merriman gives

s = unit stress at inner edge of the annulus; r = interior radius; t = thickness; t = length.

The total stress over the area
$$2tl = 2sl \frac{rt}{r+t}$$
. (1)

The total interior pressure which tends to rupture the cylinder is $2rl \times p$. If p be the unit pressure, then $p = \frac{st}{r+t}$, from which one of the quantities s, p, r, or t can be found when the other three are given.

$$s = \frac{p(r+t)}{t};$$
 $r = \frac{(s-p)t}{p};$ $t = \frac{rp}{s-p}.$

In eq. (1), if t be neglected in comparison with r, it reduces to 2sit, which is the same as the formula for thin cylinders. If t=r, it becomes sit, or

is one same as the formula for thin cylinders. If t=r, it becomes st, or only half the resistance of the thin cylinder.

The formulæ given by Burr and by Merriman are quite different, as will be seen by the following example: Let maximum unit stress at the inner edge of the annulus = 8000 lbs. per square inch, radius of cylinder = 4 inches, interior pressure = 4000 lbs. per square inch. Required the thickness.

By Burr,
$$t = 4 \left\{ \left(\frac{8000 + 4000}{8000 - 4000} \right)^{\frac{1}{2}} - 1 \right\} = 4 (\sqrt{3} - 1) = 2.928 \text{ inches.}$$

By Merriman,
$$t = \frac{4 \times 4000}{8000 - 4000} = 4$$
 inches.

Limit to Useful Thickness of Hollow Cylinders (Eng'g, Jan. 4, 1884).—Professor Barlow lays down the law of the resisting powers

of thick cylinders as follows:
"In a homogeneous cylinder, if the metal is incompressible, the tension on every concentric layer, caused by an internal pressure, varies inversely as the square of its distance from the centre."

Suppose a twelve-inch gun to have walls 15 inches thick.

Pressure on exterior
$$=$$
 $\frac{6^2}{21^2} = 1:12.25.$

So that if the stress on the interior is 1214 tons per square inch, the stress on the exterior is only 1 ton.

Let s = the stress on the inner layer, and s, that at a distance x from the axis; r = internal radius, R = external radius.

$$s_1:s::r^2:x^2$$
, or $s_1=s\frac{r^2}{x^2}$.

The whole stress on a section 1 inch long, extending from the interior to the exterior surface, is $S = sr \times \frac{R-r}{R}$.

In a 12-inch gun, let s = 40 tons, r = 6 in., R = 21 in.

$$S = 40 \times 6 \times \frac{21 - 6}{21} = 172 \text{ tons.}$$

Suppose now we go on adding metal to the gun outside: then R will become so large compared with r, that R-r will approach the value R, so that the fraction $\frac{R-r}{R}$ becomes nearly unity.

Hence for an infinitely thick cylinder the useful strength could never exceed Sr (in this case 240 tons).

Barlow's formula agrees with the one given by Merriman.

Another statement of the gun problem is as follows: Using the formula

$$p=\frac{st}{r+t},$$

 $s = 40 \text{ tons}, t = 15 \text{ in.}, r = 6 \text{ in.}, p = \frac{40 \times 15}{21} = 289 \text{ tons per sq. in.}, 289 \times$ radius = 172 tons, the pressure to be resisted by a section 1 inch long of the thickness of the gun on one side. Suppose thickness were doubled, making t = 30 in.: $p = \frac{40 \times 30}{26} = 38\%$ tons, or an increase of only 16 per cent.

For short cast-iron cylinders, such as are used in hydraulic presses, it is doubtful if the above formulæ hold true, since the strength of the cylindrical portion is reinforced by the end. In that case the bursting strength would be higher than that calculated by the formula. A rule used in practice for such presses is to make the thickness = 1/10 of the inner circumference, for pressures of 3000 to 4000 lbs. per square inch. The latter pressure would bring a stress upon the inner layer of 10,350 lbs. per square inch, as calculated by the formula; which would necessitate the use of the best charged licen to make the pressure reacceptable as best charcoal iron to make the press reasonably safe.

THIN CYLINDERS UNDER TENSION.

Let p = safe working pressure in lbs. per sq. in.; d = diameter in inches; T = tensile strength of the material, lbs. per sq. in.;

t =thickness in Inches;

f = factor of safety;

c = ratio of strength of riveted joint to strength of solid plate.

$$fpd = 2Ttc; p = \frac{2Ttc}{df}; t = \frac{fpd}{2Tc}$$

If T = 50000, f = 5, and c = 0.7; then

$$p = \frac{14000t}{d}$$
; $t = \frac{dp}{14000}$

The above represents the strength resisting rupture along a longitudinal seam. For resistance to rupture in a circumferential seam, due to pressure on the ends of the cylinder, we have $\frac{p\pi d^2}{4} = \frac{Tt\pi dc}{f}$;

whence
$$p = \frac{4Ttc}{dt}$$
.

Or the strength to resist rupture around a circumference is twice as great as that to resist rupture longitudinally; hence boilers are commonly singleriveted in the circumferential seams and double-riveted in the longitudinal seams.

HOLLOW COPPER BALLS.

Hollow copper balls are used as floats in boilers or tanks, to control feed and discharge valves, and regulate the water-level.

They are spun up in halves from sheet copper, and a rib is formed on one half. Into this rib the other half fits, and the two are then soldered or brazed together. In order to facilitate the brazing, a hole is left on one side of the ball, to allow air to pass freely in or out; and this hole is made use of afterwards to secure the float to its stem. The original thickness of the metal may be anything up to about 1-16 of an inch, if the spinning is done on a hand lathe, though thicker metal may be used when special machinery on a hand lathe, though thicker metal may be used when special machiners is provided for forming it. In the process of spinning, the metal is thinned down in places by stretching; but the thinnest place is neither at the equator of the ball (i.e., along the rib) nor at the poles. The thinnest points lie along two circles, passing around the ball parallel to the rib, one on each side of it, from a third to a balf of the way to the poles. Along these lines the thickmess may be 10, 15, or 20 per cent less than elsewhere, the reduction depending somewhat on the skill of the workman.

The Locomotive for October, 1891, gives two empirical rules for determining the thickness of a copper ball which is to work under an external

pressure, as follows:

These rules give the same result for a pressure of 166 lbs. only. Example: Required the thickness of a 5-inch copper ball to sustain

250 lbs. per sq. in.

HOLDING-POWER OF NAILS, SPIKES, AND SCREWS.

(A. W. Wright, Western Society of Engineers, 1881.) Spikes.-Spikes driven into dry cedar (cut 18 months):

Size of spikes	5×14 in. sq.	6 × 14	6 × 1/4	5 × 36
Size of spikes	414 in.	5 in.	5 in.	4¼ in.
104440100000000000000000000000000000000	1159	928	2129	1556
From 6 to 9 tests each Min. "	766	766	1120	687

A. M. Wellington found the force required to draw spikes $9/16 \times 9/16$ in., driven 414 inches into seasoned oak, to be 4281 lbs.; same spikes, etc., in un-

seasoned oak, 6523 lbs.

"Professor W. R. Johnson found that a plain spike % inch square driven 3% inches into seasoned Jersey yellow pine or unseasoned chestnut required about 2000 lbs. force to extract it; from seasoned white oak about 4000 and from well-seasoned locust 6000 lbs."

Experiments in Germany, by Funk, give from 2465 to 3940 lbs. (mean of many experiments about 3000 lbs.) as the force necessary to extract a plain 44 inches one property of the structure of the ariven 446 inches into white or yellow pine. When driven 5 inches the force required was about 1/10 part greater. Similar spikes 9/16 inches square, 7 inches long, driven 6 inches deep, required from 3700 to 6745 lbs. to extract them from pine; the mean of the results being 4873 lbs. In all cases about twice as much force was required to extract them from oak. The spikes were all driven across the grain of the wood. When driven with the grain, spikes or nails do not hold with more than half as much force.

Boards of oak or pine nailed together by from 4 to 16 tenpenny common cut nails and then pulled apart in a direction lengthwise of the boards, and across the nails, tending to break the latter in two by a shearing action, averaged about 300 to 400 lbs. per nail to separate them, as the result of

many trials.

Resistance of Drift-bolts in Timber.—Tests made by Rust and Coolidge, in 1878.

	_												Pounds.
1st	Test.	1 in.	square	iron	drove				white	pine,	15/16-in.	hole	26,400
2d		1 in.	round	**	44		••		"		18/16-in.	**	16,800
8d	44	1 in.	square	66	46			"	"	44	15/16-in.		14,600
4th	4.6	1 in.	round	46			44			44	18/16-in.	"	13,200
5th	66	1 in.	round	46	66	84	64	"	Norw'y	pine	18/16-in.		18,720
6th	64	1 in.	square	44	**	80	"	"	"		15/16-in.		19,200
7th	66		square	44				"	**	46	15/16-in.		15,600
8th	66		round	66	66	22	**	"	+ 6	44	18/16-in.	"	14,400

Note -In test No. 6 drift-bolts were not driven properly, holes not being in line, and a piece of timber split out in driving.

Force required to draw Screws out of Norway Pine.

16"	diam.	drive screw	4 in. in w	ood.	Power	required,	average	2424	lbs
. 11	44	4 threads pe	er in. 5 ir	ı. in w	ood. "		"	2748	"
66	44	D'ble thr'd, 8	per in., 4	in. in	"	"	66	2730	**
66	66	Lag-screw, 7	per in 1	136 "	"	**	44	1465	**
66	66		6 " " 2	12 "		**	66	2026	46
16 i	nch R.	R. spike		5° "		**	44	2191	44

Force required to draw Wood Screws out of Dry Wood, Tests made by Mr. Bevan. The screws were about two inches in length, .22 diameter at the exterior of the threads, .15 diameter at the bottom, the depth of the worm or thread being .035 and the number of threads in one inch equal 12. They were passed through pieces of wood half an inch in thickness and drawn out by the weights stated: Beech, 460 lbs.: ash, 790 lbs.: oak, 760 lbs.; mahogany, 770 lbs.; elm, 665 lbs.; sycamore, 830 lbs.

Tests of Lag-screws in Various Woods were made by A. J.
Cox, University of Iowa, 1891:

Kind of Wood.	Size Screw.	Size Hole bored.	Length in Tie.	Max. Resist. lbs.	No. Tests.
Seasoned white oak	% in. 9/16 "	16 in. 7/16 "	416 in.	8037 6480	3
" " "	16 "	86 "	416 "	8780	2
Yellow-pine stick	\$3 ··	12	4 "	8800 8405	2 2

In figuring area for lag-screws, the surface of a cylinder whose diameter is

equal to that of the screw was taken. The length of the screw part in each case was 4 inches.—Engineering News, 1891.

Cut versus Wire Nails.—Experiments were made at the Watertown Arsenal in 1893 on the comparative direct tensile adhesion, in pine and spruce, of cut and wire nails. The results are stated by Prof. W. H. Burr as follows:

There were 58 series of tests, ten pairs of nails (a cut and a wire nail in each) being used, making a total of 1160 nails drawn. The tests were made in spruce wood in most instances, but some extra ones were made in white pine, with "box nails." The nails were of all sizes, varying from 1½ inches to 6 inches in length. In every case the cut nails showed the superior holding strength by a large percentage. In spruce, in nine different sizes of nails, both standard and light weight, the ratio of tenacity of cut to wire nail was about 3 to 2, or, as he terms it, "a superiority of 47.45% of the former." With the "finishing" nails the ratio was roughly 3.5 to 2; superiority 72%. With box nails (1½ to 4 inches long) the ratio was roughly 3 to 2; superiority 71%. The mean superiority in spruce wood was 61%. In white pine, cut nails, driven with taper along the grain, showed a superiority of 100%, and with taper across the grain of 185%. Also when the nails were driven in the end of the stick, i.e., along the grain, the superiority of cut nails was 100%, or the ratio of cut to wire was 2 to 1. The total of the results showed the ratio of tenacity to be about 3.2 to 2 for the harder wood, and about 2 to 1 for the softer, and for the whole taken together the ratio was 3.5 to 2. We are led to conclude that under these circumstances the cut nail is superior to the wire nail in direct tensile holding-power by 72.74%.

Nail-holding Power of Various Woods.

(Watertown Experiments.)
Holding-power per square inch of

Kind of Wood.	f Wood. Size of Nail. Surface in Wood				
		Wire Nail.	Cut Nail.	Mean.	
White pine	8d 9 '' 20 '' 50 ''	- 167 -	450 455 477 847 863 840	405	
Yellow pine	8 " 10 " 50 " 60 "	818	695 755 596 604	662	
White oak	8 · · 20 · · 60 · ·	940	1340 1292 1018	1216	
Chestnut	50 '' 60 ''		664 702	683	
Laurel	9"	651 {	1179	1200	

Nail-holding Power of Various Woods.

(F. W. Clav's Experiments. Eng'g News, Jan. 11, 1894.)

Wood.	Tenacity of 6d				
wood.	Plain.	Barbed.	Blued.	Mean.	
White pine	106	94	185	111	
Yellow pine	190	180	270	196	
Basswood	78	182	219	148	
White oak	226	300	555	360	
Hemlock	141	201	819	220	

Tests made at the University of Illinois gave the resistance of a 1-in. round rod in a 15/16-inch hole perpendicular to the grain, as 6000 lbs. per lin. ft. in pine and 15,600 lbs. in oak. Experiments made at the East River Bridge gave resistances of 12.000 and 15,000 lbs. per lin. ft. for a 1-in. round rod in holes 15/16-in. and 14/16-in. diameter, respectively, in Georgia pine.

Holding-power of Bolts in White Pine.

(Eng'g News, September 26, 18)],)	
, , , , , , , , , , , , , , , , , , , ,	Round.	Square.
	Lbs.	Ĺbs.
Average of all plain 1-in, bolts	8224	8200
Average of all plain bolts, % to 11/2 in	7805	8110
A warrage of all holts	6369	QKOQ

Round drift-bolts should be driven in holes 18/16 of their diameter, and square drift-bolts in holes whose diameter is 14/16 of the side of the square

STRENGTH OF WROUGHT IRON BOLTS.

(Computed by A. F. Nagle.)

	Stress upon Bolt upon Basis of											
Diameter of Bolt, Inches.	Number of Threads.	Diameter of Bottom of Thread, Inches	Area at Bottom of Thread, Square Inches.	s sq. inch.	eq 4000 lbs. per sq. inch.	eg 5000 lbs. per sq. inch.	g 7000 lbs, per sq. inch.	sq 10000 lbs. per sq. inch.	Probable Breaking Load.			
9-16	18 12 11 10 9 8 7 7 6 6 5 5 5 4 4 4 4 4 4 4 8 8 8 8 8 8 8 8 8 8	.88 .44 .49 .60 .71 .81 .91 1.12 1.25 1.35 1.45 1.57 1.66 2.12 2.37 2.57 3.50	.12 .15 .19 .28 .89 .52 .65 .84 1.03 1.44 1.95 2.18 2.88 3.55 4.43 5.20 7.25	350 450 560 850 1180 1550 2520 3000 4930 5840 6540 8650 10840 113290 11580 21760 22860	460 600 750 1180 1570 2070 2600 3360 4000 7800 8720 7800 8720 11530 20770 29070 29070	580 750 930 1410 1970 2600 5000 6140 7180 8250 9800 10900 11400 17730 222150 26000 80260 48100	810 1050 1310 1980 2760 3680 5900 7000 8600 10000 11560 13640 20180 24830 34830 34830 36360 50760	1160 1500 1870 2880 3940 5180 6510 8410 10000 12280 14360 16510 21800 22800 35500 52000 72500 72500	5800 7508 9000 14000 19000 25000 80000 39000 46000 65000 65000 125000 125000 1180000 218000 218000 218000			

When it is known what load is to be put upon a bolt, and the judgment of the engineer has determined what stress is safe to put upon the iron, look down in the proper column of said stress until the required load is found. The area at the bottom of the thread will give the equivalent area of a flat bar to that of the bolt.

Effect of Initial Strain in Bolts.—Suppose that bolts are used to connect two parts of a machine and that they are screwed up tightly before the effective load comes on the connected parts. Let $P_1 =$ the initial tension on a bolt due to screwing up, and $P_2 =$ the load afterwards added. The greatest load may vary but little from P_1 or P_2 , according as the former or the latter is greater, or it may approach the value $P_1 + P_2$, depending upon the relative rigidity of the bolts and of the parts connected. Where rigid flanges are bolted together, metal to metal, it is probable that the extension of the bolts with any additional tension relieves the initial tension, and that the total tension is P_1 or P_2 , but in cases where elastic packing, as india rubber, is interposed, the extension of the bolts may very little affect the initial tension, and the total strain may be nearly $P_1 + P_2$. Since the latter assumption is more unfavorable to the resistance of the bolt, this contingency should usually be provided for. (See Unwin, "Elements of Machine Design" for demonstration.)

STAND-PIPES AND THEIR DESIGN.

(Freeman C. Coffin, New England Water Works Assoc., Eng. News, March 16, 1893.) See also papers by A. H. Howland, Eng. Club of Phil. 1887; B. F. Stephens, Amer. Water Works Assoc., Eng. News, Oct. 6 and 13, 1888; Kiersted, Rensselaer Soc. of Civil Eng., Eng. Record. April 25 and May 2, 1891, and W. D. Pence, Eng. News, April and May, 1894.

The question of diameter is almost entirely independent of that of height. The question of diameter is almost entirely independent of that of height. The efficient capacity must be measured by the length from the high-water line to a point below which it is undesirable to draw the water on account of loss of pressure for fire-supply, whether that point is the actual bottom of the stand-pipe or above it. This allowable fluctuation ought not to exceed tt., in most cases. This makes the diameter dependent upon two condi-

tions, the first of which is the amount of the consumption during the ordinary interval between the stopping and starting of the pumps. This should never draw the water below a point that will give a good fire stream and leave a margin for still further draught for fires. The second condition is the maximum number of fire streams and their size which it is considered. necessary to provide for, and the maximum length of time which they are liable to have to run before the pumps can be relied upon to reinforce

Another reason for making the diameter large is to provide for stability

against wind-pressure when empty.

The following table gives the height of stand-pipes beyond which they are not safe against wind pressures of 40 and 50 lbs. per square foot. The area of surface taken is the height multiplied by one half the diameter.

Heights of Stand-pipe that will Resist Wind-pressure by its Weight alone, when Empty.

Diameter,	Wind, 40 lbs.	Wind, 50 lbs
feet.	per sq. ft.	per sq. ft.
20	45	85
25	70	55
80		80
85		160

To have the above degree of stability the stand-pipes must be designed

with the outside angle-iron at the bottom connection.

Any form of auchorage that depends upon connections with the side plates near the bottom is unsafe. By suitable guys the wind-pressure is resisted by tension in the guys, and the stand-pipe is relieved from wind strains that tend to overthrow it. The guys should be attached to a band of angle or other shaped iron that completely encircles the tank, and rest upon some sort of bracket or projection, and not be riveted to the tank. They should be anchored at a distance from the base equal to the height of the point at which they are attached, if possible.

The best plan is to build the stand-pipe of such diameter that it will resist

the wind by its own stability.

Thickness of the Side Plates.

The pressure on the sides is outward, and due alone to the weight of the ne pressure on the sides is douward, and due alone to the weight of the water, or pressure per square inch, and increases in direct ratio to the height, and also to the diameter. The strain upon a section 1 inch in height at any point is the total strain at that point divided by two—for each side is supposed to bear the strain equally. The total pressure at any point is equal to the diameter in inches, multiplied by the pressure per square inch, due to the height at that point. It may be expressed as follows:

$$H = \text{height in feet, and } f = \text{factor of safety;}$$
 $d = \text{diameter in inches;}$
 $p = \text{pressure in lbs. per square inch;}$
 $434 = p$ for 1 ft. in height;
 $s = \text{tensile strength of material per square inch;}$
 $T = \text{thickness of plate.}$

Then the total strain on each side per vertical inch

$$=\frac{.484Hd}{2}=\frac{pd}{2};$$
 $T=\frac{.434Hdf}{2s}=\frac{pdf}{2s}.$

Mr. Coffin takes f = 5, not counting reduction of strength of joint, equivalent to an actual factor of safety of 3 if the strength of the riveted joint is taken as 60 per cent of that of the plate.

The amount of the wind strain per square inch of metal at any joint can be found by the following formula, in which

H = height of stand-pipe in feet above joint; T = thickness of plate in inches;p = wind pressure per square foot: W = wind pressure per foot in height above joint; W = Dp where D is the diameter in feet; m = average leverage or movement about neutral axis or central points in the circumference; or, $m = \text{sine of } 45^{\circ}$, or .707 times the radius in feet.

Then the strain per square inch of plate

$$=\frac{(Hw)\frac{H}{2}}{\text{circ. in ft.}\times mT}$$

Mr. Coffin gives a number of diagrams useful in the Jesign of stand-pipes, together with a number of instances of failures, with discussion of their probable causes.

Mr. Kiersted's paper contains the following: Among the most prominent strains a stand-pipe has to bear are; that due to the static pressure of the water, that due to the overturning effect of the wind on an empty stand-pipe, and that due to the collapsing effect, on the upper rings, of violent wind storms.

For the thickness of metal to withstand safely the static pressure of water, let

t =thickness of the plate iron in inches; H = height of stand-pipe in feet;

D =diameter of stand-pipe in feet.

Then, assuming a tensile strength of 48,000 lbs. per square inch, a factor of safety of 4, and efficiency of double-riveted lap-joint equalling 0.6 of the strength of the solid plate,

$$t = .00036H \times D;$$
 $H = \frac{10,000t}{3.6D};$

which will give safe heights for thicknesses up to % to % of an inch. The same formula may also apply for greater heights and thicknesses within practical limits, if the joint efficiency be increased by triple riveting.

The conditions for the severest overturning wind strains exist when the

stand-pipe is empty.

Formula for wind-pressure of 50 pounds per square foot, when

d = diameter of stand-pipe in inches;

x =any unknown height of stand-pipe;

 $x = \sqrt{80\pi dt} = 15.85 \sqrt{dt}$.

The following table is calculated by these formulæ. The stand-pipe is intended to be self-sustaining; that is, without guys or stiffeners.

Heights of Stand-pipes for Various Diameters and Thicknesses of Plates.

Thickness of	Diameters in Feet.												
Plate in Frac- tions of an Inch.	5	6	7	8	9	10	12	14	15	16	18	20	25
3-16	50	55	60	65	55	50	35					х.	
7-32	55	2.00	25.06	2000	65	60	50		40		2000	100	12.0
4-16	60	65	70	75	75	70	55	50	45	40	35	35	25
5-16	70	75	80	85	90	85	70	60	55	50	45	40	35
6-16	75	80	90	95	100	100	85	75	70	65	55	50	40
7-16	80	90	95	100	7:0	115	100	85	80	75	65	60	45
8-16	85	95	100	110	115	120	115	100	90	85	75	70	55
9-16				115	125	130	130	110	100	95	85	80	60
10-16					130	135	145	120	115	105	95	85	65
11-16		V 5 4				145	155	135	125	120	105	95	75
12-16						150	165	145	135	130	115	105	80
13-16						144	100	160	150	140	125	110	90
14-16	10000	100			9000	221	1222		160	150	135	120	95
15-16	10,000	Sec.	1.7	355		***	1444	0.500	la a	160	145	130	105
16-16	4.74									100	155	200.00	110
10-10	100	***			4.5 -	1.64	149.4	5.4.4	***	1(4(4)	199	140	110

Heights to nearest 5 feet. Rings are to build 5 feet vertically.

Failures of Stand-pipes have been numerous in recent years. list showing 23 in portant failures inside of nine years is given in a paper by Prof. W. D. Pence, Eng'g. News, April 5, 12, 19 and 26, May 3, 10 and 24, and June 7, 1894. His discussion of the probable causes of the failures is most valuable.

Kenneth Allen, Engineers Club of Philadelphia, 1886, gives the following rules for thickness of plates for stand pipes.

Assume: Wrought iron plate T. S. 48,000 pounds in direction of fibre, and T. S. 45,000 pounds across the fibre. Strength of single riveted joint 4 that of the plate, and of double riveted joint, 7 that of the plate; wind pressure = 50 pounds per square foot; safety factor = 3. Let h = total height in feet; r = outer radius in feet; r' = inner radius

in feet; p = pressure per square inch; t = thickness in inches; d = outer diameter in feet.

Then for pipe filled and longitudinal seams double riveted

$$t = \frac{pr \times 12}{48,000 \times .7 \times 16} = \frac{hd}{4801}$$
;

and for pipe empty and lateral seams, single riveted, we have by equating moments:

$$50 \times 2r \left(\frac{h}{2}\right)^2 = 144 \times 6000 \left(r^4 - r'^4\right) \cdot \frac{.7854}{r}$$
, whence $r^4 - r'^4 = \frac{h^2 r^2}{27144}$.

Table showing required Thickness of Bottom Plate.

Height in	Diameter.							
Feet.	5 feet.	10 feet.	15 feet.	20 feet.	25 feet.	30 feet		
50 60 70 80 90 100 125 150 175 200	, + 7-64* +11-64* + 7-32 +19-64 + \$6 +29-64	7/6 * 9-64* 11-64* 8-16 7-32 †15-64 †28-64 †28-64 †11-16 †29-32	11-64* 7-32 14 9-32 5-16 28-64 7-16 17-32 89-64 45-64	77 15-64 9-32 21-64 94 27-64 15-32 87-64 45-64 18-16 15-18	"" 19-64 28-64 13-32 15-32 17-32 37-64 47-64 76 1 1-32 11-64	28-64 27-64 81-64 9-16 9-6 45-64 7-64 1 3-64 1 7-32 1 25-64		

^{*} The minimum thickness should = 3-16".

Water Tower at Yonkers, N. Y.—This tower, with a pipe 122 feet high and 20 feet diameter, is described in Engineering News, May 18, 1892.

The thickness of the lower rings is 11-16 of an inch, based on a tensile strength of 60,000 lbs. per square inch of metal, allowing 65% for the strength of riveted joints, using a factor of safety of 31% and adding a constant of 16 inch. The plates diminish in thickness by 1-16 inch to the last four plates at the top, which are 14 inch thick.

The contract for steel requires an elastic limit of at least 33,000 lbs. per square inch; an ultimate tensile strength of from 56,000 to 66,000 lbs. per square inch; an elongation in 8 inches of at least 20%, and a reduction of square inch; an elongation in a inches of at least 20%, and a reduction of area of at least 48%. The inspection of the work was made by the Pittsburgh Testing Laboratory. According to their report the actual conditions developed were as follows: Elastic limit from 34,020 to 39,420; the tensite strength from 58,330 to 65,390; the elongation in 8 inches from 29,420 to 71.82%; reduction in area from 52.72 to 71.82%; 17 plates out of 141 were rejected in the inspection.

WROUGHT-IRON AND STEEL WATER-PIPES.

Eiveted Steel Water-pipes (Engineering News, Oct. 11, 1890, and Aug. 1, 1891.)—The use of riveted wrought-iron pipe has been common in the Pacific States for many years, the largest being a 44-inch conduit in connection with the works of the Spring Valley Water Co., which supplies San Francisco. The use of wrought iron and steel pipe has been necessary in the West, owing to the extremely high pressures to be withstood and the difficulties of transportation. As an example: In connection with

N.B.—Dimensions marked t determined by wind-pressure.

the water supply of Virginia City and Gold Hill, Nev., there was laid in 1879 an 1116-inch riveted wrought-iron pipe, a part of which is under a head of . 720 feet.

In the East, the most important example of the use of riveted steel water pipe is that of the East Jersey Water Co., which supplies the city of Newark. The contract provided for a maximum high service supply of 25,000,000 gallons daily. In this case 21 mues of 48-inch pipe was laid, some of it under 840 feet head. The plates from which the pipe is made are about 18 feet long by 7 feet wide, open-hearth steel. Four plates are used to make one section of pipe about 27 feet long. The pipe is riveted longitudinally with a double row, and at the end joints with a single row of rivets of varying diameter, corresponding to the thickness of the steel plates. Before being rolled into the trench, two of the 27-feet lengths are riveted together, thus diminishing still further the number of joints to be made in the trench and the extra excavation to give room for jointing. All changes in the grade of the pipe-line are made by 10° curves and all changes in line by 2½, 5, 7½ and 10° curves. To lay on curved lines a standard bevel was used, and the different

certain length of pipe. The thickness of the plates varies with the pressure, but only three thicknesses are used, 14, 5-16, and 36 inches, the pipe made of these thicknesses having a weight of 160, 185, and 225 ibs. per foot, respectively. At the works all the pipe was tested to pressure 11/4 times that to which it is to be sub-

curves are secured by varying the number of beveled joints used on a

jected when in place.

Mannesmann Tubes for High Pressures.—At the Mannesmann Works at Komotau, Hungary, more than 600 tons or 25 miles of 3-inch and 4-inch tubes averaging 14 inch in thickness have been successfully tested to a pressure of 2000 lbs. per square inch. These tubes were intended

for a high-pressure water-main in a Chilian nitrate district.

This great tensile strength is probably due to the fact that, in addition to being much more worked than most metal, the fibres of the metal run spirally, as has been proved by microscopic examination. While cast-iron tubes will hardly stand more than 200 lbs. per square inch, and welded tubes are not safe above 1000 lbs. per square inch, the Mannesmann tube easily withstands 2000 lbs. per square inch. The length up to which they can be readily made is shown by the fact that a coil of 8-inch tube 70 feet long was made recently.

For description of the process of making Mannesmann tubes see Trans.

A. I. M. E., vol. xix., 384,

STRENGTH OF VARIOUS MATERIALS. EXTRACTS FROM KIRKALDY'S TESTS.

The recent publication, in a book by W. G. Kirkaldy, of the results of many thousand tests made during a quarter of a century by his father, David Kirkaldy, has made an important contribution to our knowledge concerning the range of variation in strength of numerous materials. A condensed abstract of these results was published in the American Muchinist, May 11 and 18, 1893, from which the following still further condensed extracts are

The figures for tensile and compressive strength, or, as Kirkaldy calls them, pulling and thrusting stress, are given in pounds per square into original section, and for bending strength in pounds of actual stress or original section, and for bending strength in pounds of actual stress of pounds per BD^2 (breadth × square of depth) for length of 36 inches between supports. The contraction of area is given as a percentage of the original area, and the extension as a percentage in a length of 10 inches, except when otherwise stated. The abbreviations T. S., E. L., Contr., and Ext. are used for the sake of brevity, to represent tensile strength, elastic limit, and percentage of the sake of the

centages of contraction of area, and elongation, respectively.

Cast Iron.—44 tests: T. S. 15,468 to 28,740 pounds; 17 of these were unsound, the strength ranging from 15,468 to 24,357 pounds. Average of all,

23,805 pounds.

23,805 pounds. Thrusting stress, specimens 2 inches long, 1.34 to 1.5 in, diameter; 43 tests, all sound, 94,852 to 151,912; one, unsound, 93,759; average of all, 118,825. Bending stress, bars about 1 in, wide by 2 in, deep, cast on edge. Ultimate stress 2876 to 3854; stress per $BD^2 = 725$ to 382; average, 820. Average modulus of rupture, $R_1 = 3/2$ stress per $BD^2 \times \text{length}_1 = 44,280$. Ultimate deflection, 29 to 40 in; average, 34 inch. Other tests of cast iron, 460 tests, 16 lots from various sources, gave re-

sults with total range as follows: Pulling stress, 12,688 to 33,616 pounds; thrusting stress, 66,863 to 175,950 pounds; bending stress, per BD^2 , 505 to 1128 pounds; modulus of rupture, R, 27,270 to 61,912. Ultimate deflection, .21 to .45 inch.

The specimen which was the highest in thrusting stress was also the highest in bending, and showed the greatest deflection, but its tensile strength was only 26,502.

The specimen with the highest tensile strength had a thrusting stress of 143,939, and a bending strength, per BD^2 , of 979 pounds with 0.41 deflection. The specimen lowest in T. S. was also lowest in thrusting and bending, but gave .38 deflection. The specimen which gave .21 deflection had T. S., 19,188;

thrusting, 104.291; and bending, 561.

Iron Castings.—99 tests; tensile strength, 10,416 to 31,652; thrusting stress, ultimate per square inch, 58,502 to 132,031.

Channel Irons.—Tests of 18 pieces cut from channel irons. T. S. 40,693 to 53,141 pounds per square inch; contr. of area from 8.9 to 32.5 %. Ext. in 10 in. from 2.1 to 22.5 %. The fractures ranged all the way from 100 fibrous to 100 % crystalline. The highest T. S., 58,141, with 8.1 % contr. and 5.3 % ext., was 100 % crystalline; the lowest T. S., 40,693, with 3.9 contr. and 5.3 f ext., was 75 f crystalline; the lowest T. S., 40,005, with 3.9 contr. and 2.1 f ext., was 75 f crystalline. All the fibrous irons showed from 12.2 to 22.5 f ext., 17.3 to 32.5 contr., and T. S. from 43,426 to 49,615. The fibrous irons are therefore of medium tensile strength and high ductility. The crystalline irons are of variable T. S., highest to lowest, and low ductility.

Lowmoor Iron Bars.—Three rolled bars 2½ inches diameter; tensile tests: elastic, 23,200 to 24,200; ultimate, 50,875 to 51,905; contraction, 44, to 42.5; extension, 20,20 to 24,200; ultimate, 46,810 to 49,223; contraction, 20,7 to 46.5; extension, 10.8 to 31.6. Fractures of all, 100 per cent fibrous. In the hammarch hars the lowest T. S. was accompanied by lowest ductility.

extension, 10.8 to 31.6. Fractures of all, 100 per cent fibrous. In mered bars the lowest T. S. was accompanied by lowest ductility.

Iron Bars, Various. -Of a lot of 80 bars of various sizes, some rolled and some hammered (the above Lowmoor bars included) the lowest T. S. (except one) 40,808 pounds per square inch, was shown by the Swedish "hoop L" bar 3½ inches diameter, rolled. Its elastic limit was 19,500 pounds; contraction 68.7% and extension 37.7% in 10 inches. It was also the most duclile of all the bars tested, and was 100% fibrous. The highest pounds; contraction 68.7% and extension 37.7% in 10 inches. It was also the most ductile of all the bars tested, and was 100 % fibrous. The lighest T. S., 60,780 pounds, with elastic limit, 29,400; contr., 36.6; and ext., 24.3%, was shown by a "Farnley" 2-inch bar, rolled. It was also 100 % fibrous. The lowest ductility 2.6% contr., and 4.1% ext., was shown by a 334-inch hammered bar, without brand. It also had the lowest T. S., 40,278 pounds, but rather high elastic limit, 25,700 pounds. Its fracture was 95% crystalline. Thus of the two bars showing the lowest T. S., one was the most ductile and the other the least ductile in the whole series of 80 bars.

Generally, high ductility is accompanied by low tensile strength, as in the Swedish bars, but the Farnley bars showed a combination of high ductility

and high tensile strength.

Locomotive Forgings, Iron.—17 tests: average, E. L., 30,420; T. S., 50,521; contr., 36.5; ext. in 10 inches, 28.8.

Broken Anchor Forgings, Iron.—4 tests: average, E. L., 23,825;

T. S., 40,083; contr., 3.0; ext. in 10 inches, 3.8.

Kirkaldy places these two irons in contrast to show the difference between

good and bad work. The broken anchor material, he says, is of a most treacherous character, and a disgrace to any manufacturer.

Iron Plate Girder.—Tensile tests of pieces cut from a riveted iron and the same of the same o girder after twenty years' service in a railway bridge. Top plate, average of 3 tests, E. L., 26,600; T. S., 40,806; contr. 16 1; ext. in 10 inches, 7.8. Bottom plate, average of 3 tests, E. L., 31,200; T. S., 44,288; contr., 18.3; ext. in 10 inches, 6.3. Web-plate, average of 3 tests, E. L., 28,000; T. S., 45,902; contr., 15 9; ext. in 10 inches, 8.9. Fractures all fibrous. The results of 30 tests from different parts of the girder prove that the iron has undergone

no change during twenty years of use.

Steel Plates.—Six plates 100 inches long, 2 inches wide, thickness various, .36 to .97 inch. T. S., 55,485 to 60,805; E. L., 29,600 to 33,200; contr., 52.9 to 59.5; ext., 17.05 to 18.57.

Steel Bridge Links.—40 links from Hammersmith Bridge, 1886.

				ij	Fracture.	
	T. S.	E. L.	Contr.	Ext. in 100	Silky.	Granular.
Average of all. Lowest T. S. Highest T. S. and E. L. Lowest E. L. Greatest Contraction Greatest Extension Least Contr. and Ext.	67,294 60,753 75,936 64,044 68,745 65,980 63,980	38,294 36,030 44,166 32,441 38,118 36,792 39,017	84.5% 30.1 81.2 34.7 52.8 40.8 6.0	14.11% 15.51 12.42 13.43 15.46 17.78 6.62	30% 15 30 100 35 0	70% 85 70 0 65 100

The ratio of elastic to ultimate strength ranged from 50.6 to 65.2 per cent: average, 56.9 per cent.

Extension in lengths of 100 inches. At 10,000 lbs. per sq. in., .018 to .024; mean, .020 inch; at 20.000 lbs. per sq. in. .049 to .063; mean, .085 inch; at 30,000 lbs. per sq. in., .083 to .100; mean, .090; set at 30,000 pounds per sq. in., 0 to .002; mean, 0.

The mean extension between 10,000 to 30,000 lbs. per sq. in. increased regularly at the rate of .007 inch for each 2000 lbs. per sq. in. increment of strain. This corresponds to a modulus of elasticity of 28,571,429. The least increase of extension for an increase of load of 20,000 lbs. per sq. in., .065 inch, corresponds to a modulus of elasticity of 30,769,231, and the greatest, .076 inch, to a modulus of 26,315,789.

Steel Rails.—Bending tests, 5 feet between supports, 11 tests of flange

rails 72 pounds per yard, 4.63 inches high.

	Elastic stress.	Ultimate stress.	Deflection at 50,000	Ultimate
	Pounds.	Pounds.	Pounds.	Deflection.
Hardest	34,200	60,960	3.24 ins.	8 ins.
Softest	32,000	56,740	8.76 "	8 "
Mean		59,209	3.53 "	§ " ,
All unere	cked at 8 inche	s deflection		

Pulling tests of pieces cut from same rails. Mean results.

	Elastic Stress.	Ultimate Pounds.	Contraction of area of frac-	Extension
	per sq. in.	per sq. in.	ture.	in 10 ins.
Top of rails	44,200	88,110	19.9%	13.5%
Botton of rails	40,900	77,820	80.9%	22.8%

Steel Tires. - Tensile tests of specimens cut from steel tires.

KRUPP STEEL .- 262 Tests.

TO-4 1...

Fret in

Highest Mean Lowest	E. L.	T. S.	Contr.	5 inches.
	69,250	119,079	31.9	18.1
	52,869	104,112	29.5	19.7
	41,700	90,523	45.5	23.7

Vickers, Sons & Co.-70 Tests.

	E. L.	T. S.	Contr.	5 inches.
Highest	58,600	120,789	11.8	8.4
Mean	51,066	101,264	17.6	12.4
Lowest	48,700	87,697	24.7	16.0

Note the correspondence between Krupp's and Vickers' steels as to tensile strength and elastic limit, and their great difference in contraction and elongation. The fractures of the Krupp steel averaged 22 per cent silky, 78 per cent granular; of the Vicker steel, 7 per cent silky, 93 per cent granular.

Steel Axles.-Tensile tests of specimens cut from steel axles.

PATENT SHAFT AND AXLE TREE CO.-157 Tests.

Highest Mean Lowest	E. I 49,800 86,267 81,800	T. S. 99,009 72,099 61,382	Contr. 21.1 83.0 84.8	Ext. in 5 inches. 16.0 23.6 25.3
	Vickers,	Sons & Co	125 Tests.	
Highest Mean Lowest	E. L. 42,600 87,618 30,250	T. S. 83,701 70,572 56,388	Contr. 18.9 41.6 49.0	Ext. in 5 inches. 13.2 27.5 87.2

The average fracture of Patent Shaft and Axle Tree Co. steel was 33 per cent silky, 67 per cent granular.

The average fracture of Vickers' steel was 88 per cent silky, 12 per cent granular. VICKERS' .-- 82 Tests 1879

Tensile tests of specimens cut from locomotive crank axles.

Highest Mean Lowest	E. L. 26,700 24,146 21,700	T. S. 68,057 57,922 50,195	Contr. 28.8 32.9 52.7	Ext. in 5 inches. 18.4 24.0 86.2
	Vran	ers'78 Tests.	1004	
				Ext. in
	E. L.	T. S.	Contr.	5 inches.
Highest	27.600	64,878	27.0	20.8
Mean	23,573	56,207	32.7	25.9
Lowest	17,600	47,695	85.0	27.2
	FRIED.	KRUPP43 Tes	ts, 1889.	
			•	Ext. in
	E. L.	T. S.	Contr.	5 inches.

Highest..... 31,650 66,868 48.6 85.6 Mean 29,491 21,950 82.8 61,774 47.7 55,172 85.6 Lowest 55.8 Steel Propeller Shafts. - Tensile tests of pieces cut from two shafts,

mean of four tests each. Hollow shaft, Whitworth. T. S., 61,290; E. L., 80,575; contr., 52.8; ext. in 10 inches, 28.6. Solid Shaft, Vickers', T. S., 46,870; E. L. 20,425; contr., 44.4; ext. in 10 inches, 30.7.

Thrusting tests, Whitworth, ultimate, 55,201; elastic, 29,300; set at 30,000 lbs., 0.18 per cent; set at 40,000 lbs., 2.04 per cent; set at 50,000 lbs., 3.82 per

cent. Thrusting tests, Vickers', ultimate, 44,602; elastic, 22,250; set at 30,000 lbs., 2.29 per cent; set at 40,000 lbs., 4.69 per cent.

Shearing strength of the Whitworth shaft, mean of four tests, was 40,654

Shearing strength of the Wiltworth Shalt, mean of four tests, was 40,034 lbs. per square inch, or 66.3 per cent of the pulling stress. Specific gravity of the Whitworth steel, 7.867: of the Vickers', 7.856.

Spring Steel.—Untempered, 6 tests, average, E. L., 67,916; T. S., 15,568; contr., 37.8; ext. in 10 inches, 16.6. Spring steel untempered, 15 tests, average, E. L., 38,785; T. S., 69,496; contr., 19.1; ext. in 10 inches, 29 8. These two lots were shipped for the same purpose, viz., railway carriage leaf springs.

Steel Castings.—44 tests, E. L., 31.816 to 35,567; T. S., 54,928 to 63,840; contr., 1.67 to 15.8; ext., 1.45 to 15.1. Note the great variation in ductility. The steel of the highest strength was also the most ductile.

Riveted Joints, Pulling Tests of Riveted Steel Plates, Triple Biveted Lap Joints, Machine Riveted, Holes Drilled.

Plates, width and thick $13.50 \times .25$ 13.	tness, incl. $00 \times .51$	nes:	12.25×1.01	14.00 × .77
Plates, gross sectional 8.375			12.372	10.780
Stress, total, pounds:	832,640	423,180	528,000	455,210

42,696

42,227

Stress per square inch of gross area, joint: 59,058 50,178 46,178

Stress per square inch of plates, solid:

70,765	95,300	03,000	62,280	68,045
Ratio of strength of	joint to solid	l plate :		•
83.46	76.83	72.09	6 3.8 6	62.06
Ratio net area of pl 73.4	ate to gross:	62.7	64.7	72.9
Where fractured:	W.5	02.1	04.1	14.8
plate at	plate at	plate at	plate at	rivets
holes.	plate at holes.	holes.	holes.	sheared.
Rivets, diameter, ar	rea and numb	er:		
.45, .159, 24	.64, .821, 21	.95, .708, 12	1.08, .918, 12	.95, .708, 12
Rivets, total area:	6.741	8.496	10.000	8.496
8.816			10,992	
Strength of V weld to solid bar.	veias.—Ten	sile tests to de	termine ratio o	r strength or
werd to solld bar.	Iron T	E BARS28 Te	sta.	
Strength of solid be				to 57 065 11-s
Strenth of welded b	ars varied fro	oin	17.810	3 to 44.586 lbs.
Ratio of weld to sol				87.0 to 79.1%
	Iron I	PLATES7 Test	8.	
Strength of solid nl	ate from		44.851	to 47.481 lbs.
Strength of solid pl Strength of welded	plate from		26,449	to 88,931 lbs.
Ratio of weld to sol	l id		• • • • • • • • • • • • • • • • • • • •	57.7 to 83.9%
	CHAIN I	Links.—216 Tes	sts.	
Strength of solid be	ar from		49,125	2 to 57,875 lbs.
Strength of welded	bar from	••••	39,57	5 to 48,824 lbs.
Ratio of weld to so				72.1 to 95.45
Iron l	Bars.—Hand	and Electric Ma	schine Welded.	
82 tests, solid iron,			52,	444
	ded, average		46,8	386 ratio 89.1≰
10 Hann	Omen Dana	AND Drames		899 " 89.3 %
Strength of solid	CYTEEL DAKS	AND PLATES.—	LA TERMS.	4,226 to 64,580
Strength of solid	• • • • • • • • • • • • • • • • • • •			8,558 to 46,019
Ratio weld to solid.	••••••			52.6 to 82.1%
The ratio of weld	to solid in all	the tests rangi	ing from 87.0 to	95.4 is proof
of the great variation	on of workma	nship in weldi	ng.	
Cast Copper	–4 tests, avei	rage, E. L., 590	0; T. S., 24,781;	contr., 24.5;
ext., 21.8.		00 44- 00 4	- PW in Al. !-1	TR T 0000 44
Copper Plate 18,650; T. S., 30,993 riation in elastic li	to 94 981 : gon	, 22 USUS, 20 t	O.75 III. TILICE;	E. L., V/00 to
riation in elastic li	mit is due to	difference in i	he heat at wh	ich the nietes
were finished. And	iealing reduc	es the T. S. onl	v about 1000 pc	unds, but the
E. L. from 8000 to 70	000 pounds.			
Another series, .8 to 56.7; ext. in 10	8 to .52 thick;	148 tests, T. S	., 29,099 to 81,92	4; contr., 28.7
to 55.7; ext. in 10	inches, 28.1	to 41.8. Note	tne uniform	ity in tensile
strength.	-74 toeta	(0 88 to 1 08 inc	h diameter). T	S 31 634 to
Drawn Coppe 40,557; contr., 87.5 t	o 64.1: ext. in	10 inches 5.8	to 48.2.	. 6., 01,002 10
Rranga fram	a Propall	er RiedeN	leans of two te	sts each from
centre and edge. contr., 25.4; ext. in T. S., 35,960; contr., Cast German	Central port	ion (sp. gr. 8.8	20). E. L., 7550;	T. S., 26,812;
contr., 25.4; ext. in	10 inches, 82.	Edge portion	n (sp. gr. 8550).	E. L., 8950;
T. S., 85,960; contr.	, 87.8; ext. in	10 inches, 47.9.	100 += 00 100 - 1	T C 00 8144-
48 540, contr. 2 2 to	SilverIU	tests: E. L., 13	,400 to x9,100;	1. 8., 20,714 to
46,540; contr., 3.2 to				
German silver, 2 lot	ith Sheet l	Tetal.—T en s i	ia oftenärn.	5,816 to 87,129
Bronze, 4 lots	M3	· • • • • • • • • • • • • • • • • • • •		3,380 to 92,086
Brass. 2 lots			4	4.898 to 58.188
Copper, 9 lots				0.470 to 48.450
Iron, 13 lots, length	way		4	4,881 to 59,484
Iron, 13 lots, length Iron, 18 lots, crossw Steel, 6 lots	ay		8	9,888 to 57,850
Steel, 6 lots Steel, 6 lots, crossw	· · · · · · · · · · · · · · · · · · ·	••••••		8,308 to 75,361
Groot, o sous, crossw	a y	• ••••••••		-,0 W OU,188

Wire.-Tensile Strength.

German silver, 5 lots	
Bronze, 1 lot	78,049
Brass, as drawn, 4 lots	81.114 to 98.578
Copper, as drawn, 3 lots	57,0U1 TO 40,494
Copper annealed, 8 lots	34.936 to 45.210
Copper (another lot), 4 lots	
Copper (extension 36.4 to 0.6%).	•
Iron, 8 lots	59,246 to 97,908
Iron (extension 15.1 to 0.7%).	
Steel, 8 lots	08,272 to 818,828

The Steel of 318,823 T. S. was .047 inch diam., and had an extension of only 0.8 per cent; that of 103,272 T. S. was .107 inch diam. and had an extension of 2.2 per cent. One lot of .044 inch diam. had 967,114 T. S., and 5.2 per cent extension.

Wire Hopes.
Selected Tests Showing Range of Variation.

	g u .		Strands.		of leg.		
Description.	Circumference, inches.	Weight per Fathom.	No. of Strands.	No. of Wires.	Diameter of Wires, inches	Hemp Core.	Ultimate Strength lbs.
Galvanised Ungalvanized Ungalvanized Galvanized Ungalvanized Ungalvanized Galvanized Galvanized Galvanized Ungalvanized Ungalvanized Ungalvanized Ungalvanized Galvanized Galvanized Ungalvanized Ungalvanized Galvanized Ungalvanized Ungalvanized Galvanized	7.70 7.00 6.38 7.10 6.18 6.19 4.92 5.36 4.82 3.65 3.50 4.11 3.02 2.68 2.87 2.46 1.75 2.04	58.00 42.50 37.57 40.46 40.38 20.86 21.50 12.21 11.35 7.27 8.62 5.43 3.85 2.80 2.72	677677666676666666666666666666666666666	19 19 30 19 19 80 12 7 7 12 12 12 12 12 12	.1563 .1495 .1347 .1004 .1316 .0728 .1106 .1693 .0755 .122 .135 .080 .068 .105 .0963 .0560 .0472 .0619 .0378	Main Main and Strands Wire Core Main and Strands Wire Core Main and Strands Main and Strands Main and Strands Main and Strands Main and Strands Main and Strands Main and Strands Main and Strands Main and Strands Main and Strands Main and Strands Main and Strands Main and Strands Main and Strands Main and Strands	839,780 814,860 395,990 372,750 968,470 321,820 190,890 110,180 110,180 101,440 98,670 75,110 55,095 41,205 88,555 88,555 88,075 24,552 20,415

Hemp Ropes, Untarred.—15 tests of ropes from 1.53 to 6.90 inches circumference, weighing 0.42 to 7.77 pounds per fathom, showed an ultimate strength of from 1670 to 33,808 pounds, the strength per fathom weight varying from 2672 to 5534 pounds.

varying from 2872 to 5534 pounds. **Hemp Rapes, Tarred.** -15 tests of ropes from 1.44 to 7.12 inches circumference, weighing from 0.38 to 10.39 pounds per fathom, showed an ultimate strength of from 1046 to 31,549 pounds, the strength per fathom weight varying from 1767 to 5149 pounds.

weight varying from 1767 to 5149 pounds. **Cotton Ropes.**—5 ropes, 2.48 to 6.51 inches circumference, 1.08 to 8.17 pounds per fathom. Strength 3089 to 23,258 pounds, or 2474 to 8846 pounds per fathom weight.

Manila Bopes.—35 tests: 1.19 to 8.90 inches circumference, 0.20 to 11.40 pounds per fathom. Strength 1280 to 65,550 pounds, or 3008 to 7894 pounds per fathom weight.

Belting.

No. of	Tensile strength
lots.	per square inch.
lots. 11 Leather, single, ordinary tanned	\$248 to 4824
4 Leather, single, Helvetia	5631 to 5944
7 Leather, double, ordinary tanned	2160 to 3572
8 Leather, double Helvetia	4078 to 5412
6 Cotton, solid woven	5648 to 8869
14 Cotton, folded, stitched	4570 to 7750
1 Flax, solid, woven	9946
1 Flax, folded, stitched	6389
6 Hair, solid, woven	3852 to 5159
2 Rubber, solid, woven	
Canvas35 lots: Strength, lengthwise, 113 to 408 p	ounds per inch;

crossways, 191 to 468 pounds per inch.

The grades are numbered 1 to 6, but the weights are not given. The strengths vary considerably, even in the same number.

strengths vary considerably, even in the same number. **Marbles.**—Crushing strength of various marbles. 88 tests, 8 kinds. Specimens were 6-inch cubes, or columns 4 to 6 inches diameter, and 6 and 12 inches high. Range 7542 to 13,720 pounds per square inch. **Granite.**—Crushing strength, 17 tests; square columns 4×4 and 6×4 , 4 to 24 inches high, 3 kinds. Crushing strength ranges 10,026 to 13,271 pounds per square inch. (Very uniform.) **Stones.**—(Probably sandstone, local names only given.) 11 kinds, 43 tests, 6×6 , columns 12, 18 and 24 inches high. Crushing strength ranges from 3105 to 12,122. The strength of the column 24 inches long is generally from 10 to 20 per cent less than that of the 6-inch cube.

from 10 to 20 per cent less than that of the 6-inch cube.

Stones.—(Probably sandstone) tested for London & Northwestern Railway. 16 lots, 8 to 6 tests in a lot. Mean results of each lot ranged from 3785 to 11,956 pounds. The variation is chiefly due to the stones being from different lots. The different specimens in each lot gave results which generally agreed within 80 per cent.

Bricks.—Crushing strength, 8 lots; 6 tests in each lot; mean results ranged from 1835 to 9209 pounds per square inch. The maximum variation in the specimens of one lot was over 100 per cent of the lowest. In the most uniform lot the variation was less than 20 per cent.

Wood.-Transverse and Thrusting Tests.

		2 214120 0120				
	Tests.	Sizes abt. in square.	Span, inches.	Ultimate Stress.	$\frac{S = LW}{4BD^2}.$	Thrust- ing Stress per sq. in.
Pitch pine	10	111/2 to 121/2	144	45,856 to 80,520 87,948	1096 to 1403 657	8586 to 5438 2478
Dantzic fir	12	12 to 18	144	to 54,152 82,856	to 790 1505	to 8423 2478
English oak	8	41/4 × 12	120	to 39,084 23,624	to 1779 1190	to 4487 2656
American white oak	5	41/6 × 12	120	25,024 to 26,952	to 1872	to 8899

Demerara greenheart, 9 tests (thrusting)	
Oregon pine, 2 tests	5888 and 7284
Honduras mahogany, 1 test	6769
Tobasco mahogany, 1 test	5978
Norway spruce, 2 tests	
American vellow pine, 2 tests	8875 and 8998
English ash, 1 test	8025

Portland Coment.—(Austrian.) Cross-sections of specimens 4 x 21/4 inches for pulling tests only; cubes, 8 × 8 inches for thrusting tests; weight, 98.8 pounds per imperial bushel; residue, 0.7 per cent with sieve 2500 meshes per square inch; 38.8 per cent by volume of water required for mixing; time of setting, 7 days; 10 tests to each lot. The mean results in lbs. per sq. in. were as follows:

	Cement alone.	Cement alone.	1 Cement, 2 Sand.	1 Cement, 3 Sand.	1 Cement, 4 Sand.
Age. 10 days	Pulling.	Thrusting.	Thrusting.	Thrusting.	Thrusting.
20 days	420	3342	1028	494	275
80 dava	451	2794	1179	504	994

30 days 451 3724 1172 594 838 **Portland Coment.**—Various samples pulling tests, $2 \times 21/2$ inches pross-section, all aged 10 days, 180 tests; ranges 87 to 643 pounds per square inch.

TENSILE STRENGTH OF WIRE.

(From J. Bucknall Smith's Treatise on Wire.)

	Tons per sq.	Pounds per
	in. sectional	
	area.	tional area.
Black or annealed iron wire	. 25	56,000
Bright hard drawn	. 85	78,400
Bessemer, steel wire	. 40	89,600
Mild Siemens-Martin steel wire	. 60	134,000
High carbon ditto (or "improved")	. 80	179,200
Crucible cast-steel "improved" wire	. 100	224,000
"Improved" cast-steel "plough"	. 120	268 ,800
Special qualities of tempered and improved cas	t-	•

Reports of Work of the Watertown Testing-machine in 1883.

	TES	STS OF F	RIVETED	JOINTS	, IR	ON AN	ID STEEL	PLAT	es.
	Thickness Plate.	Diameter, Rivets, inches.	Diameter, Punched Holes, inches.	Width Plate Tested, inches.	No. Rivets.	Pitch Rivets, inches.	Tensile Strength Joint in Net Sec- tion of Plate per square inch, pounds.	Tensile Strength Plate per square inch, pounds.	Efficiency of Joint, Per Cent.
***********		11-16 11-16 34 11-16 11-16 11-16 11-16 11-16 11-16 11-16 11-16 11-16 11-16 11-16	34 13-16 13-16 34 13-16 13-16 1 1-16 1 1-16 1 3-16 1 3-16 1 3-16 1 1-16 1 1-16 1 1-16 1 1-16 1 1-16 1 1-16 1 1-16 1 1-16	10/5 10/5 10 10 10 10 10 10 10 10/5 11.9 11.9 10/5 10 10 10 10 10 10 10 10 10 10 10 10 10	66555555544446655555544444	194 134 22 22 22 22 23 25 24 134 22 23 24 25 25 25 25 25 25 25 25 25 25 25 25 25	89,300 41,000 85,650 85,150 46,360 46,875 46,400 46,140 44,260 42,310 41,920 61,270 60,830 47,530 49,840 62,770 61,210 68,920 66,710 62,180 62,590 54,650 54,200	47,180 47,180 44,615 44,615 47,180 44,615 44,615 44,635 44,635 44,635 65,380 57,215 58,380 57,215 57	47.0 + 44.0 + 45.6 + 45

1 Lap-joint.

& Butt-joint.

* Iron.

† Steel.

The efficiency of the joints is found by dividing the maximum tensile stress on the gross sectional area of plate by the tensile strength of the material.

COMPRESSION TESTS OF 8 x 3 INCH WROUGHT-IRON BARS.

	Tested with Two	o Pin Ends, Pins Diameter.	Tested with One Flat and One Pin		
Length, inches.	Ultimate Com- pressive Strength pounds per square inch.	Tested with Two Flat Ends, Ulti- mate Compressive Strength, pounds per square inch.	End, Ultimate Compressive		
80	\$ 28,260 \$ 31,990 \$ 26,310				
90	26,640 524,030 25,380	{ 26,780 } 25,580	\$ 25,120 \$ 25,190		
120	(20,660) 20,200 (16,520	23,010 22,450	22,450 21,870		
180	17,840 (13,010 (15,700				

Tested with two pin-	Diameter of Pins.	Ult. Comp. Str., per sq. in., lbs.
ends. Length of bars	% inch	
200 Inches.	1/2 " 212 "	01 400

TENSILE TEST OF SIX STEEL EYE-BARS.

COMPARED WITH SMALL TEST INGOTS.

The steel was made by the Cambria Iron Company, and the eye-bar heads made by Keystone Bridge Company by upsetting and hammering. All the bars were made from one ingot. Two test pieces, 34-inch round, rolled from a test-ingot, gave elastic limit 48,040 and 42,210 pounds; tensile strength, 73,150 and 69,470 pounds, and elongation in 8 inches, 22.4 and 25.6 per cent. respectively. The ingot from which the eye-bars were made was 14 inches square, rolled to billet, 7 × 6 inches. The eye-bars were rolled to 64× 1 inch. Chemical tests gave carbon .27 to .30; manganese, .61 to .73; phosphorus, 074 to .098.

Gauged Length, inches.	Elastic limit, lbs. per sq. in.	Tensile strength per sq. in., lbs.	Elongation per cent, in Gauged Length.
160	37.480	67,800	15.8
160	36,650	64,000	6. 96
160	4	71,560	8. 6
200	87,600 .	68,720	12.8
200	8 5,810	65,850	12. 0
200	8 3,230	64,410	16. 4
200	87,640	68,290	13.9

The average tensile strength of the ¾-inch test pieces was 71,310 lbs., that of the eye-bars 67,280 lbs., a decrease of 5.7%. The average elastic limit of the test pieces was 45,150 lbs., that of the eye-bars 84,402 lbs., a decrease of 19.4%. The elastic limit of the test pieces was 63.8% of the ultimate strength, that of the eye-bars 54.2% of the ultimate strength.

COMPRESSION OF WROUGHT-IRON COLUMNS, LATTICED BOX AND SOLID WEB.

ALL TESTED WITH PIN ENDS.

Columns made of	Length, feet.	Sectional Area, square inch.	Total Weight of Column, pounds.	Ultimate Strength, per square inch, pounds.
6 inch channel, solid web	10.0	9.831	482	80,220
6 " " "	15.0	9.977	592	21,050
6 " " "	20.0	9.762	755	16,220
8 44 44 44 44	20.0	16.281	1,290	22,540
	26.8	16.141	1,645	17,570
8-inch channels, with 5-16-in. continuous plates	26.8	19.417	1,940	25,290
5-16-inch continuous plates and angles. Width of plates, 12 in., 1 in. and 7.85 in.	26.8	16.168	1,765	28,020
7-16-inch continuous plates and angles.	26.8	20.954	2,242	25,770
Plates 12 in. wide.	13.3	7.628	679	33,910
8 " " " " " " " " " " " " " " " " " " "	20.0	7.621	924	34,120
8 " "	26.8	7.673	1,255	29,870
8-inch channels, latticed, swelled sides	13.4	7.624	684	83,530
B " " " " " " " " " " " " " " " " " " "	20.0	7.517	921	83,390
8 " " " " "	26.8	7.702	1,280	80,770
10 " "	16.8	11.944	1,470	38,740
10 " " "	25.0	12.175	1.926	82,440
10-inch channels, latticed, swelled sides.	16.7	12.366	1,549	81,130
6. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6	25.0	11.932	1,962	82,740
* 10-inch channels. latticed one side; con-		1	-,	1,4
tinuous plate one side	25.0	17.622	1,849	26,190
† 10 inch channels, latticed one side; continuous plate one side	25.0	17.721	1,827	17,270

^{*} Pins in centre of gravity of channel bars and continuous plate, 1.63 inches from centre line of channel bars.

† Pins placed in centre of gravity of channel bars.

EFFECT OF COLD-DRAWING ON STEEL

Three pieces cut from the same bar of hot-rolled steel: 1. Original bar, 2,03 in, diam., gauged length 30 in., tensile strength 55,400

bs. per square in.; elongation 23.9%.

2. Diameter reduced in compression dies (one pass) .094 in.; T. S. 70,420; el. 2.7% in 20 in. .

8. " " " 2.2% in 20 in.; T. S. 81,890; el. .0.073≴ in 20 in.

Compression test of cold-drawn bar (same as No. 3), length 4 in., diam. 1.806 in.; Compressive strength per sq. in., 75,000 lbs.; amount of compression .057 iu.; set .04 iu. Diameter increased by compression to 1.821 in. in the middle; to 1.813 in. at the ends.

Tests of Cold-rolled and Cold-drawn Steel, made by the Cambria Iron Co. in 1897, gave the following results (averages of 12 tests of each):

El, in 8 in. 28.3 % 9.6 " 8.9" Red. 58.5 % Before cold-rolling, E. L. 85,890 T.S. 59,980 34.9 " After 72,530 79,830 After cold-drawing, 76,350 83,860

The original bars were 2 in. and 34 in. diameter. The test pieces cut from the bars were 34 in. diam. 18 in, long. The reduction in diameter from the hot-roiled to the cold-roiled or cold-drawn bar was 1/16 in. in each case

TESTS OF AMERICAN WOODS. (See also page 309.)

In all cases a large number of tests were made of each wood. Minimum and maximum results only are given. All of the test specimens had a sectional area of 1.575 × 1.575 inches. The transverse test specimens were 39.37 inches between supports, and the compressive test specimens were 12.60 inches long. Modulus of rupture calculated from formula $R = \frac{3}{2} \frac{Pl}{bdz}$; P = 1 load in pounds at the middle, l = 1 length in inches, l = 1 breadth, l = 1 length in inches, l = 1 length; l = 1 length; l = 1 length in inches, l = 1 length; l = 1 length; l = 1 length; l = 1 length in inches, l = 1 length; l = 1 len

Name of Wood.	Modu	rse Tests. ilus of ture.	Compression Parallel to Grain, pounds per square inch.	
	Min.	Max.	Min.	Max.
Cucumber tree (Magnolia acuminata) Yellow poplar white wood (Lirioden-		12,050	4,560	7,410
dron tulipifera)	6,560	11,756	4,150	5,790
cana) Sugar-maple, Rock-maple (Acer sac-	6,720	11,530	3,810	6,480
charinum	9,680	20,130	- 7,460	9.940
Red maple (Acer rubrum)	8,610	18,450	6,010	7.500
Locust (Robinia pseudacacia)	12,200	21,730	8,330	11,940
Wild cherry (Prunus serotina)	8,310	16,800	5,830	9,120
Sweet gum (Liquidambar styraciflua)	7,470	11,180	5,630	7,620
Dogwood (Cornus florida)	10,190	14,560	6,250	9,400
Sour gum, Pepperidge (Nyssa sylvatica).	9.830	14,300	6,240	7.480
Persimmon (Diospyros Virginiana)	10,290	18,500	6,650	8.080
White ash (Fraxunis Americana)	5,950	15,800	4,520	8,830
Sassafras (Sassafras officinale)	5,180	10,150	4,050	
Slippery elm (Ulmus fulva)	10,220	13,952	6,980	5,970 8,790
White elm (Ulmus Americana)	8,250			
	0,600	15,070	4,960	8,040
Sycamore; Buttonwood (Platanus occi- dentalis)	6,720	11,360	4,960	7,840
Butternut; white walnut (Juglans ci-	4 600		~ 400	0.040
nerea)	4,700	11,740	5,480	6,810
Black walnut (Juglans nigra)	8,400	16,320	6,940	8,850
Shellbark hickory (Carya alba)	14,870	20,710	7,650	10,280
Pignut (Carya porcina)	11,560	19,480	7,460	8,470
White oak (Quercus alba)	7,010	18,360	5,810	9,070
Red oak (Quercus rubra)	9,760	18,370	4,960	8,970
Black oak (Quercus tinctoria)	7,900	18,420	4,540	8,550
Chestnut (Castanea vulgaris)	5,950	12.870	3,680	6,650
Beech (Fagus ferruginea)	13,850	18,840	5,770	7,840
Canoe-birch, paper-birch (Betula papy-		1 1		
racea)	11,710	17,610	5,770	8,590
Cottonwood (Populus monilifera)	8,390	13,430	8,790	6,510
White cedar (Thuja occidentalis)	6,310	9,530	2,660	5,810
Red cedar (Juniperus Virginiana)	5,640	15,100	4,400	7,010
Cypress (Saxodium Distichum)	9,530	10,03 0	5,060	7,140
White pine (Pinus strobus)	5,610	11,580	8,750	5,600
Spruce pine (Pinus glabra)	3,780	10,980	2,580	4,680
Long-leaved pine, Southern pine (Pinus)		'		
palustris)	9,220	21,060	4,010	10,600
White spruce (Picea alba)	9,900	11,650	4,150	5,800
Hemlock (Tsuga Canadensis)	7,590	14,680	4,500	7,420
Red fir, yellow fir (Pseudotsuga Doug-		'		,
lasii)	8,220	17,920	4,880	9,800
Tamarack (Larix Americana)	10,080	16,770	6,810	10,700

SHEARING STRENGTH OF IRON AND STEEL.

H. V. Loss in American Engineer and Railroad Journal, March and April, 1893, describes an extensive series of experiments on the shearing of iron and steel bars in shearing machines. Some of his results are:

Depth of penetration at point of maximum resistance for soft steel bars is independent of the width, but varies with the thickness. If d= depth of penetration and t= thickness, d=.3t for a flat knife, d=.25 t for a 4° bevel knife, and $d=.16 \ \sqrt{19}$ for an 8° bevel knife. The ultimate pressure per inch of width in flat steel bars is approximately 50,000 lbs. $\times t$. The energy consumed in foot pounds per inch width of steel bars is, approximately: 1 thick, 1300 ft.-lbs.; $1\frac{1}{2}\frac{t}{t}$, 2500; $13\frac{1}{4}\frac{t}{t}$, 3700; $13\frac{t}{t}\frac{t}{t}$, 4500; the energy increasing at a slower rate than the square of the thickness. Iron angles require more energy than steel angles of the same size; steel breaks while iron has to be cut off. For hot-rolled steel the resistance per square inch for rectangular sections varies from 4400 lbs. to 20,500 lbs., depending partly upon its hardness and partly upon the size of its cross-area, which latter element indirectly but greatly indicates the temperature, as the smaller dimensions require a considerably longer time to reduce them down to size, which time again means loss of heat.

It is not probable that the resistance in practice can be brought very much below the lowest figures here given—viz., 4400 lbs. per square inch—as a decrease of 1000 lbs. will henceforth mean a considerable increase in

cross-section and temperature.

HOLDING-POWER OF BOILER-TUBES EXPANDED INTO TUBE-SHEETS.

Experiments by Chief Engineer W. H. Shock, U. S. N., on brass tubes, 2½ inches diameter, expanded into plates 3½ inch thick, gave results ranging from \$550 to 46.000 lbs. Out of 48 tests 5 gave figures under 10,000 lbs. plateween 10,000 and 20,000 lbs., 18 between 20,000 and 30,000 lbs., 100 between 30,000 and 30,000 lbs., and 3 over 40,000 lbs. Experiments by Yarrow & Co., on steel tubes, 2 to 2½ inches diameter, gave results similarly varying, ranging from 7900 to 41,715 lbs., the majority ranging from 20,000 to 30,000 lbs. In 15 experiments on 4 and 5 inch tubes the strain ranged from 20,720 to 68,040 lbs. Beading the tube does not necessarily give increased resistance, as some of the lower figures were obtained with beaded tubes. (See paper on Rules Governing the Construction of with beaded tubes. (See paper on Rules Governing the Construction of Steam Boilers, Trans. Engineering Congress, Section G, Chicago, 1893.)

CHAINS. Weight per Foot, Proof Test and Breaking Weight. (Pennsylvania Railroad Specifications, 1899.)

Nominal Diameter of Wire. Inches.	Description.	Maximum Length of 100 Links. Inches.	weight	Proof. Test. Lbs.	Breaking Weight. Lbs.
5/32 3/16	Twisted chain	103.1 96.2	0.20 0.85		
3/16 1/4 5/16	Perfection twisted chain. Straight link chain	151.25 102.0 114.7	0.266 0.70 1.10	1,500 3,000	3,000 5,500
3/8 3/8 7/16	Crane chainStraight-link chain		1.50 1.50 1.90	3,500 4,000 5,000	7,000 7,500 9,500
7/16	Crane chain Straight-link chain Crane chain	126.3 153.0	1.90 2.50 2.50	5,500 7,000 7,500	10,000 12,500 13,000
149 149 149 149 149 149 149 149 149 149	Straight-link chain Crane chain Straight-link chain	178.5 176.7	4.00	11,000	20,000 20,600 29,000
34 38	Crane chain	202.0 252.5	5.50 5.50 7.40	16,000 16,000 22,000	29,000 40,000
1 116 114	16 66	277.7 303.0 353.5	9.50 12.00 15.00	30,000 40,000 50,000	55,000 66,000 82,000
11/2	" "	416.6	21.00	70,000	116,000

Elongation of all sizes, 10 per cent. All chain must stand the proof test without deformation. A piece 2 ft. long out of each 200 ft. is tested to destruction.

British Admiralty Proving Tests of Chain Cables.—Stud-nks. Minimum size in inches and 16ths. Proving test in tons of 2240 lbs. 19 110 112 22 28. 111 113 114 115 2 21

Test, tons: 4018 4318 4718 5146 5546 5946 6946 6711 72 7611 8146 9146 Wrought-fron Chain Cables.—The strength of a chain link is less than twice that of a straight bar of a sectional area equal to that of one side of the link. A weld exists at one end and a bend at the other, each requiring at least one heat, which produces a decrease in the strength. The report of the committee of the U.S. Testing Board, on tests of wrought-iron and chain cables contains the following conclusions. That beyond doubt, when made of American bar iron, with cast-iron studs, the studded link is

inferior in strength to the unstudded one. "That when proper care is exercised in the selection of material, a variation of 5 to 17 per cent of the strongest may be expected in the resistance of cables. Without this care, the variation may rise to 25 per cent.

"That with proper material and construction the ultimate resistance of

the chain may be expected to vary from 155 to 170 per cent of that of the bar used in making the links, and show an average of about 163 per cent.

"That the proof test of a chain cable should be about 50 per cent of the ultimate resistance of the weakest link."

The decrease of the resistance of the studded below the unstudded cable is probably due to the fact that in the former the sides of the link do not remain parallel to each other up to failure, as they do in the latter. The reremain parallel to each other up to failure, as they do in the latter. The result is an increase of stress in the studded link over the unstudded in the proportion of unity, to the secant of half the inclination of the sides of the former to each other.

From a great number of tests of bars and unfinished cables, the committee considered that the average ultimate resistance, and proof tests of chain cables made of the bars, whose diameters are given, should be such as are

shown in the accompanying table.

ULTIMATE RESISTANCE AND PROOF TESTS OF CHAIN CABLES.

Diam. of Bar.	Average resist. = 168% of Bar.	Proof Test.	Diam. of Bar.	Average resist. = 168% of Bar.	Proof Test.
Inches. 1 1/16 1 1/15 1 8/16 1 5/16 1 5/16 1 7/16	Pounds. 71,172 79,544 88,445 97,731 107,440 117,577 128,129 139,103 150,485	Pounds, 33,340 87,820 42,053 46,468 51,084 55,908 60,920 66,188 71,550	Inches. 1 9/16 156 1 11/16 134 1 13/16 176 1 15/16	162,283 174,475 187,075 200,074 213,475	Pounds. 77,159 82,956 83,947 95,128 101,499 109,058 114,806 121,737

STRENGTH OF GLASS.
Second Series.)
Common Extra White
Best Common Extra White
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Com (Fairbairn's "Useful Information for Engineers," Mean specific gravity
Mean tensile strength, lbs. per sq. in., bars... 8.078 2.528 2.450 2,896 2.413 2,546 do. thin plates. 4,200 6,000 Mean crush'g strength, lbs. p. sq. in., cyl'drs. 27,582 39,876 31,003

cubes.

13,130

20,208

The bars in tensile tests were about 14 inch diameter. The crushing tests were made on cylinders about 34 inch diameter and from 1 to 2 inches high, and on cubes approximately 1 inch on a side. The mean transverse strength of glass, as calculated by Fairbairn from a mean tensile strength of 2560 ibs. and a mean compressive strength of 30,150 ibs. per sq. in., is, for a bar supported at the ends and loaded in the middle,

in which w = breaking weight in lbs., b = breadth, d = depth, and l = length, in inches. Actual tests will probably show wide variations in both directions from the mean calculated strength.

STRENGTH OF COPPER AT HIGH TEMPERATURES.

The British Admiralty conducted some experiments at Portsmouth Dockyard in 1877, on the effect of increase of temperature on the tensile strength of copper and various bronzes. The copper experimented upon was in rods .72-in. diameter.

The following table shows some of the results:

Temperature	Tensile Strength in lbs. per sq. in.	Temperature	Tensile Strength
Fahr.		Fahr.	in lbs. per sq. in.
Atmospheric.	23,115	300°	21,607
100°	23,366	400°	21,105
200°	22,110	500°	19,597

Up to a temperature of 400° F. the loss of strength was only about 10 per cent, and at 500° F. the loss was 16 per cent. The temperature of steam at 200 lbs. pressure is 382° F., so that according to these experiments the loss of strength at this point would not be a serious matter. Above a temperature of 500° the strength is seriously affected.

STRENGTH OF TIMBER.

Strength of Long-leaf Pine (Yellow Pine, Pinus Palustris) from Alabama (Bulletin No. 8, Forestry Div., Dept. of Agriculture, 1898, Tests by Prof. J. B. Johnson.)

The following is a condensed table of the range of results of mechanical tests of over 2000 specimens, from 26 trees from four different sites in

Alabama; reduced to 15 per cent moisture:

	But	t I	ogs.	Midd	ile	Logs.	Тој	p L	ogs.	Av'g of all Butt Logs.
Specific gravity	0.449	to	1.039	0,575	to	0.859	0.484	to	0.907	0.767
Transverse strength, $\frac{8}{2} \frac{WL}{bh^2}$	4,762	to	16,200	7,640	te	17,128	4,268	to	15,554	12,614
do do at elast. limit Mod. of elast., thous. lbs. Relative elast. resilience.	4,930 1,119	to	18,110	5.540	to	11,790	2.553	to		9,460
inch-pounds per cub. in. Crushing endwise, str. per	0.23	to	4.69	1.84	to	4.21	^ 09	to	4.65	2.98
sq. inlbs	4,781	to	9,850	5,030) to	9,800	4,587	to	9,100	7,452
strength per sq. in.,lbs. Tensile strength per sq. in.	675		2,094	656 6.830	to	1,445 29,500	584 4,170	to	1,766 23,280	1,598 17,359
Shearing strength (with grain), mean per sq. in.	1			1		1,230	1		•	866

Some of the deductions from the tests were as follows:

1. With the exception of tensile strength a reduction of moisture is accompanied by an increase in strength, stiffness, and toughness.

2. Variation in strength goes generally hand-in-hand with specific gravity.

3. In the first 20 or 30 feet in height the values remain constant; then occurs a decrease of strength which amounts at 70 feet to 20 to 40 per cent

of that of the butt-log.

4. In shearing parallel with the grain and crushing across and parallel with the grain, practically no difference was found.

5. Large beams appear 10 to 20 per cent weaker than small pieces.

6. Compression tests endwise seem to furnish the best average statement of the value of wood, and if one test only can be made, this is the safest, as was also recognized by Bauschinger.

7. Bled timber is in no respect inferior to unbled timber.

The figures for crushing across the grain represent the load required to cause a compression of 15 per cent. The relative elastic resilience, in inch pounds per cubic inch of the material, is obtained by measuring the area of the plotted-strain diagram of the transverse test from the origin to the point in the curve at which the rate of deflection is 50 per cent greater than point in the curve at which the rate of deflection is a per cent greater than the rate in the earlier part of the test where the diagram is a straight line. This point is arbitrarily chosen since there is no definite "elastic limit" in timber as there is in iron. The "strength at the elastic limit" is the strength taken at this same point. Timber is not perfectly elastic for any load if left on any great length of time.

The long-leaf pine is found in all the Southern coast states from North

Carolina to Texas. Prof. Johnson says it is probably the strongest timber in large sizes to be had in the United States. In small selected specimens, in large sizes to be had in the United States. In small selected specimens, other species, as oak and hickory, may exceed it in strength and toughness. The other Southern yellow pines, viz., the Cuban, short-leaf and the lobiolly pines are inferior to the long-leaf about in the ratios of their specific gravities; the long-leaf being the heaviest of all the pines. It averages (kiln-dried) 48 pounds per cubic foot, the Cuban 47, the short-leaf 40, and the loblolly 34 pounds.

Strength of Spruce Timber.—The modulus of rupture of spruce is given as follows by different authors: Hatfield, 9900 lbs. per square inch Rankine, 11,100; Laslett, 9045; Trautwine, 8100; Rodman, 6168. Trautwine advises for use to deduct one-third in the case of knotty and poor

timber.

Immer.

Prof. Lanza, in 25 tests of large spruce beams, found a modulus of rupture from 2995 to 5666 lbs.; the average being 4613 lbs. These were average beams, ordered from dealers of good repute. Two beams of selected stock, seasoned four years, gave 7562 and 8748 lbs. The modulus of elasticity ranged from 897,000 to 1,588,000, averaging 1,294,000.

Time tests show much smaller values for both modulus of rupture and modulus of elasticity. A beam tested to 5800 lbs. in a screw machine was left over night, and the resistance was found next morning to have dropped to about 3000, and it broke at 3500.

Prof. Lanza remarks that while it was necessary to use larger feators of

Prof. Lanza remarks that while it was necessary to use larger factors of safety, when the moduli of rupture were determined from tests with smaller pieces, it will be sufficient for most timber constructions, except in factories, to use a factor of four. For breaking strains of beams, he states that it is better engineering to determine as the safe load of a timber beam the load that will not deflect it more than a certain fraction of its span, say about 1/300 to 1/400 of its length.

Properties of Timber.

(N. J. Steel & Iron Co.'s Book.)

Description.	Weight per cubic foot, in lbs.	Tensile Strength per sq. inch, in lbs.	Crushing Strength per sq. inch, in lbs.	Relative Strength for Cross Breaking. White Pine = 100.	
Ash		11,000 to 17,207		130 to 180	458 to 700
		11,500 to 18,000			
Cedar	50 to 56.8	10,800 to 11,400	5,600 to 6,000		
Cherry				130	
Chestnut	83	10,500	5,350 to 5,600	96 to 123	
		13,400 to 13,489		96	
Hemlock		8,700	5,700	88 to 95	
Hickory		12,800 to 18,000	8,925	150 to 210	
Locust		20,500 to 24,800	9,113 to 11,700	132 to 227	
Maple		10,500 to 10.584		122 to 220	367 to 647
Oak, White	45 to 54.5	10,253 to 19,500	4,684 to 9,509	130 to 177	752 to 966
Oak, Live	70	1	6.850	155 to 189	
Pine, White	80	10,000 to 12,000	5,000 to 6,650	100	225 to 423
Pine, Yellow		12,600 to 19,200	5,400 to 9,500	98 to 170	286 to 415
Spruce		10,000 to 19,500	5,050 to 7,850	86 to 110	253 to 374
Walnut, Black.	42	9,286 to 16,600	7,500		l

The above table should be taken with caution. The range of variation in the species is apt to be much greater than the figures indicate. See Johnson's tests on long-leaf pine, and Lanza's on spruce, above. The weight of yellow pine in the table is much less than that given by Johnson. (W. K.)

pine in the table is much less than that given by Johnson. (W. K.)

Compressive Strengths of American Woods, when slowly
and carefully seasoned.—Approximate averages, deduced from many experiments made with the U. S. Government testing-machine at Watertown,
Mass., by Mr. S. P. Sharpless, for the Census of 1880. Seasoned woods resist
crushing much better than green ones; in many cases, twice as well. Different specimens of the same wood vary greatly. The strengths may readily
vary as much as one-third part more or less from the average.

	End- wise,* lbs. per sq. in.	lbs	de- ise,† . per . in.		End- wise,* lbs. per sq. in.	lbs.	se,+
		.01	.1			.01	.1
Ash, red and white Aspen	6800 4400 7000 8000 4400	1300 800 1100 1300 600	1400 1900	Maple: sugar and black white and red Oak: white, post (or	8000 6800		4300 2900
Butternut Buttonwood (sycamore) Cedar, red Cedar,white (arbor-	5400 6000 6000	700 1300 700	2600 1000	iron), swamp white, red, and blackscrub and basket. chestnut and live	7000 6000	1700	4000 4200 4500
vitæ)	4400	500 700 1700 900	1800	pin	6500 5400 6300	1300 • 600	3000 1200 1400
Coffee-tree, Ky Cypress, bald Elm, Am. or white red	7700	1300 500 1300 1300	1200 2600 2600	pitch and Jersey scrub Georgia Poplar	5000 8500 5000	1000 1300 60 0	2000 2600 1100
Hemlock	5300 8000 10000 5000	600 2000 1600 500	1100 4000 13000 900	Sassafras Spruce, black white Sycamore (button- wood)	5000 5700 4500	700 60 0	2100 1300 1200 2600
black and yellow. honey Mahogany Maple: broad-leafed, Ore.	9800 7000 9000 5300	1900 1600 1700 1400	4400 2600 5300 2600	Walnut: black white (butternut). Willow	8000	1300 700	2600 1600 1400

Expansion of Timber Due to the Absorption of Water.

(De Volson Wood, A. S. M. E., vol. x.)

Pieces 36×5 in., of pine, oak, and chestnut, were dried thoroughly, and then immersed in water for 37 days.

The mean per cent of elongation and lateral expansion were:

	Pine.	Oak.	Chestnut.
Elongation, per cent	0.065	0.085	0.165
Lateral expansion, per cent	2.6	3.5	3 .65

Expansion of Wood by Heat.—Trautwine gives for the expansion of white pine for 1 degree Fahr. 1 part in 440,580, or for 180 degrees 1 part in 2447, or about one-third of the expansion of iron.

^{*} Specimens 1.57 ins, square × 12.6 ins. long.
† Specimens 1.57 ins, square × 6.3 ins. long. Pressure applied at mid-length by a punch covering one-fourth of the length. The first column gives the loads producing an indentation of .01 inch, the second those producing an indentation of .1 inch. (See also page 306).

Shearing Strength of American Woods, adapted for Pins or Treenails.

J. C. Trautwine (Jour. Franklin Inst.). (Shearing across the grain.)

per sq. in. 6280	Hickory 6045
Beech	7285
Birch	Maple
Cedar (white)	Oak
Cedar (Central American) 3410	Pine (white) 2480
Cherry 2945	Pine (Northern yellow 4340
Chestnut	Pine (Southern yellow) 5785
Dogwood	Pine (very resinous yellow) 5053
Ebony	Poplar
Gum	
Hemlock 2750	Walnut (black) 4728
Locust 7176	Walnut (common) 2830

THE STRENGTH OF BRICK, STONE, ETC.

A great advance has recently been made in the manufacture of brick, in the direction of increasing their strength. Chas. P. Chase, in Engineering News, says: "Taking the tests as given in standard engineering books eight News, says: "Taking the tests as given in standard engineering books eight or ten years ago, we find in Trautwine the strength of brick given as 500 to 4200 lbs. per sq. in. Now, taking recent tests in experiments made at Watertown Arsenal, the strength ran from 5000 to 22,000 lbs. per sq. in. In the tests on Illinois paving-brick, by Prof. I. O. Baker, we find an average strength in hard paving brick of over 5000 lbs. per square inch. The average crushing strength of ten varieties of paving-brick much used in the West, I find to be 7150 lbs. to the square inch."

A recent test of brick made by the dry-clay process at Watertown Arsenal, scendiling to Paving showed an average compressive strength of 4202 lbs.

according to Paving, showed an average compressive strength of 3972 lbs, per sq. in. In one instance it reached 4973 lbs. per sq. in. A test was made at the same place on a "fancy pressed brick." The first crack developed at a pressure of 305,000 lbs., and the brick crushed at 364,300 lbs., or 11,130 lbs. per sq. in. This indicates almost as great compressive strength as grante paving-blocks, which is from 12,000 to 20,000 lbs. per sq. in.

The following notes on bricks are from Trautwine's Engineer's Pocket-

book:

Strength of Brick.—40 to 300 tons per sq. ft., 622 to 4668 lbs. per sq. in. A soft brick will crush under 450 to 600 lbs. per sq. in., or 80 to 40 tons per square foot, but a first-rate machine-pressed brick will stand 200 to 400 tons weight of Bricks.—Per cubic foot, best pressed brick, 150 lbs.; good pressed brick, 131 lbs.; common hard brick, 125 lbs.; good common brick, 181 lbs.; common hard brick, 125 lbs.; good common brick, 181 lbs.; of inferior brick, 100 lbs.

Absorption of Water.—A brick will in a few minutes absorb 1/2 lb. of water, the last being 1/7 of the weight of a hand-moulded one, or 1/2 lb. Treets of Britanes.

Tests of Bricks, full size, on flat side. (Tests made at Water-town Arsenal in 1883.)—The bricks were tested between flat steel buttresses Compressed surfaces (the largest surface) ground approximately flat. The bricks were all about 2 to 2.1 inches thick, 7.5 to 8.1 inches long, and 3.5 to 3.76 inches wide. Crushing strength per square inch: One lot ranged from 11,056 to 16,784 lbs.; a second, 12,995 to 22,851; a third, 10,390 to 12,709. Other tests gave results from 5960 to 10,250 lbs. per sq. in.

Crushing Strength of Masonry Materials. (From Howe's "Retaining-Walls.")

	ons per sq. ft.	tons per sq. ft.
Brick, best pressed	40 to 800	Limestones and marbles, 250 to 1000
Chalk	20 to 30	Sandstone 150 to 550
Granite	800 to 1200	Soapstone 400 to 800

Strength of Granite. - The crushing strength of granite is commonly rated at 12,000 to 15,000 lbs. per sq. in, when tested in two-inch cubes, and only the hardest and toughest of the commonly used varieties reach a strength above 20,000 lbs. Samples of granite from a quarry on the Con-

necticut River, tested at the Watertown Arsenal, have shown a strength of 85,995 lbs. per sq. in. (Engineering News, Jan. 12, 1898).

Strength of Avondale, Pa., Limestone—(Engineering News, Feb. 9, 1898).—Crushing strength of 2-in. cubes: light stone 12,112, gray stone 18,040, lbs. per sq. in.

Transverse test of lintels, tool-dressed, 42 in. between knife-edge bearings, load with knife-edge brought upon the middle between bearings: .. Light stone.....

Transverse Strength of Flagging.

(N. J. Steel & Iron Co.'s Book.)

EXPERIMENTS MADE BY R. G. HATFIELD AND OTHERS.

b =width of the stone in inches; d =its thickness in inches; l =distance between bearings in inches.

The breaking loads in tons of 2000 lbs., for a weight placed at the centre of the space, will be as follows:

-	$\frac{bd^2}{l} \times$	$\frac{bd^2}{l} \times$
Bluestone flagging Quincy granite Little Falls freestone Belleville, N. J., freestone. Granite (another quarry) Connecticut freestone.	.684 .576 .480 .488	Dorchester freestone .264 Aubigny freestone .216 Caen freestone .144 Glass 1,000 Slate .1.2 to 2.7

Thus a block of Quincy granite 80 inches wide and 6 inches thick, resting on beams 36 inches in the clear, would be broken by a load resting midway between the beams = $\frac{80 \times 36}{100} \times .624 = 49.92$ tons.

STRENGTH OF LIME AND CEMENT MORTAR.

(Engineering, October 2, 1891.)

Tests made at the University of Illinois on the effects of adding cement to lime mortar. In all the tests a good quality of ordinary fat lime was used, slaked for two days in an earthenware jar, adding two parts by weight of water to one of lime, the loss by evaporation being made up by fresh additions of water. The cements used were a German Portland, Black Diamond tions of water. The cements used were a cerman Portiand, place Diamond (Louisville), and Resendale. As regards fineness of grinding, 85 per cent of the Portland passed through a No. 100 sieve, as did 72 per cent of the Rosendale. A fairly sharp sand, thoroughly washed and dried, passing through a No. 18 sleve and caught on a No. 30, was used. The mortar in all cases consisted of two volumes of sand to one of lime paste. The following results were obtained on adding various percentages of cement to the mortar:

Tensile Strength, pounds per square inch.

Total building policy p								
Age	$\left. \left\{ \left \begin{array}{c} 4 \\ \text{Days.} \end{array} \right. \right. \right.$	7 Days.	Days.	21 Days.	28 Days.	Days.	84 Days	
Lime mortar	4	8	10	18	18	21	26	
20 per cent Rosendal	le 5	816	91/6	12	17	17	18	
20 " " Portland	5	816	14	20	25	24	26	
30 " Rosendal	e 7	11	13	1816	21	2216	23	
30 " " Rosendal		16	18	22	25	28	27	
40 " Rosendal		12	1616	2116	2216	24	36	
40 " Portland	27	89	38	43	47	59	57	
60 " Rosenda		13	20	16	22	2214	28	
60 " " Portland	45	13 58	55	68	67	102	78	
80 " " Rosendal		1816	2214	27	29	811/6	83	
80 " " Rosendal	97	91	103	124	94	210	145	
100 " Rosenda	le 18	23	26	81	34	46		
TO TOSCHUA	90	1 400					48	
100 " " Portland	90	120	146	152	181	205	202	

MODULI OF ELASTICITY OF VARIOUS MATERIALS.

The modulus of elasticity determined from a tensile test of a bar of any material is the quotient obtained by dividing the tensile stress in pounds per square inch at any point of the test by the elongation per inch of length produced by that stress; or if P = pounds of stress applied, K = the sectional area, l = length of the portion of the bar in which the measurement is made, and $\lambda = the$ elongation in that length, the modulus of allocations $E = \frac{P}{l}$, $\lambda = \frac{P}{l}$

elasticity $E = \frac{P}{K} + \frac{\lambda}{l} = \frac{Pl}{K\lambda}$. The modulus is generally measured within the

elastic limit only, in materials that have a well-defined elastic limit, such as elastic limit only, in materials that have a well-defined classic limit, soul a fron and steel, and when not otherwise stated the modulus is understood to be the modulus within the elastic limit. Within this limit, for such materials the modulus is practically constant for any given bar, the elongation being directly proportional to the stress. In other materials, such as cast iron, which have no well-defined elastic limit, the elongations from the beginning of a test increase in a greater ratio than the stresses, and the modulus is therefore at its maximum near the beginning of the test, and continually decreases. The moduli of elasticity of various materials have already been given above in treating of these materials, but the following table gives some additional values selected from different sources:

9,170,000 14,230,000 15,000,000 to 18,000,000 Brass, cast..... wire..... Copper..... Lead..... 1,000,000 4,600,000 Tin, cast..... 12.000,000 to 27,000,000 (?) 22,000,000 to 29,000,000 (?) Iron, cast..... Iron, wrought..... 28,000.000 to 32,000,000 (see below) Marble..... 25,000,000 14,500,000 8,000,000 1,600,000 1,300,000 Beech..... 1,250,000 to 1,500,000 869,000 to 2,191,000 Birch.... Fir..... 974,000 to 2,283,000 2,414,000 Oak Teak.. Walnut.... Pine, long-leaf (butt-logs)... 306,000 1,119,000 to 8,117,000 Avge. 1,926,000

The maximum figures given by many writers for iron and steel, viz., 40,000,000 and 42,000,000, are undoubtedly erroneous. The modulus of elasticity of steel (within the elastic limit) is remarkably constant, notwithstandthere of steer within the elastic limit) is remarkably constant, notwinstanding great variations in chemical analysis, temper, etc. It rarely is found below 29,000,000 or above 31,000,000. It is generally taken at 30,000,000 in engineering calculations. Prof. J. B. Johnson, in his report on Long-leaf Pine, 1933, says: "The modulus of elasticity is the most constant and reliable property of all engineering materials. The wide range of value of the modulus of elasticity of the various metals found in public records must be explained by erroneous methods of testing.

In a tensile test of cast iron by the author (Van Nostrand's Science Series, No. 41, page 45), in which the ultimate strength was 23,285 lbs. per sq. in., the measurements of elongation were made to .0001 inch, and the modulus of elasticity was found to decrease from the beginning of the test, as follows: At 1000 lbs. per sq. in., \$5,000,000; at 2000 lbs., 16,666,000; at 4000 lbs., 13,636,000; at 4000 lbs., 12,500,000; at 12,000 lbs., 11,200,000; at 15,000 lbs., 12,500,000; at 23,000 lbs., 12,500,000; at 20,000 at

6.140.000.

FACTORS OF SAFETY.

A factor of safety is the ratio in which the load that is just sufficient to overcome instantly the strength of a piece of material is greater than the greatest safe ordinary working load. (Rankine.)
Rankine gives the following "examples of the values of those factors

which occur in machines ":

De	ad Load.	Live Load, Greatest.	Live Load, Mean.
Iron and steel		. 6	from 6 to 40
Timber	4 to 5	8 to 10	****
THE COURT OF STREET	-	•	****

The great factor of safety, 40, is for shafts in millwork which transmit very variable efforts.

Unwin gives the following "factors of safety which have been adopted in certain cases for different materials." They "include an allowance for ordingry contingencies."

Dead Load.	In Temporary		In Structures subj. to Shocks,
Wrought iron and steel. 3	4	4 to 5	10
Cast iron 8	4	5	10
Timber	4	10	••••
Brickwork		6	••••
Masonry 20	••••	20 to 30	••••

Unwin says says that "these numbers fairly represent practice based on

experience in many actual cases, but they are not very trustworthy." Prof. Wood in his "Resistance of Materials" says: "In regard to the margin that should be left for safety, much depends upon the character of the loading. If the load is simply a dead weight, the margin may be comparatively small; but if the structure is to be subjected to percussive forces or shocks, the margin should be comparatively large on account of the indeterminate effect produced by the force. In machines which are subjected to a constant far while in use, it is very difficult to determine the proper margin which is consistent with economy and safety. Indeed, in such cases, economy as well as safety generally consists in making them excessively strong, as a single breakage may cost much more than the extra material necessary to fully insure safety."

For discussion of the resistance of materials to repeated stresses and

shocks, see pages 288 to 240.

Instead of using factors of safety it is becoming customary in designing to fix a certain number of pounds per square inch as the maximum stress which will be allowed on a piece. Thus, in designing a boiler, instead of naming a factor of safety of 6 for the plates and 10 for the stay-bolts, the ultimate tensile strength of the steel being from 50,000 to 60,000 lbs. per sq. in, an allowable working stress of 10,000 lbs. per sq. in, on the plates and 6000 lbs. per sq. in, on the stay-bolts may be specified instead. So also in Merriman's formula for columns (see page 260) the dimensions of a column of the strength of the stren are calculated after assuming a maximum allowable compressive stress per square inch on the concave side of the column. The factors for masonry under dead load as given by Rankine and by Unwin,

The factors for masonry under dead load as given by Rankine and by Unwin, viz., 4 and 20, show a remarkable difference, which may possibly be explained as follows: If the actual crushing strength of a pier of masonry is known from direct experiment, then a factor of safety of 4 is sufficient for a pier of the same size and quality under a steady load; but if the crushing strength is merely assumed from figures given by the authorities (such as the crushing strength of pressed brick, quoted above from Howe's Retaining Walls, 40 to 300 tons per square foot, average 170 tons), then a factor of safety of 20 may be none too great. In this case the factor of safety is really a "factor of ignorance."

The selection of the proper factor of safety or the proper maximum unit stress for any given case is a matter to be largely determined by the judgment of the engineer and by experience. No definite rules can be given. The customary or advisable factors in many particular cases will be found where these cases are considered throughout this book. In general the following circumstances are to be taken into account in the selection of a factor

1. When the ultimate strength of the material is known within narrow limits, as in the case of structural steel when tests of samples have been made, when the load is entirely a steady one of a known amount, and there is no reason to fear the deterioration of the metal by corrosion, the lowest

factor that should be adopted is 3.

When the circumstances of 1 are modified by a portion of the load being variable, as in floors of warehouses, the factor should be not less than 4.
 When the whole load, or nearly the whole, is apt to be alternately out on and taken off, as in suspension rods of floors of bridges, the factor should

be 5 or 6.

4. When the stresses are reversed in direction from tension to compression, as in some bridge diagonals and parts of machines, the factor should be not less than 6.

5. When the piece is subjected to repeated shocks, the factor should be not less than 10.

6. When the piece is subject to deterioration from corrosion the section should be sufficiently increased to allow for a definite amount of corrosion before the piece be so far weakened by it as to require removal.

7. When the strength of the material, or the amount of the load, or both are uncertain, the factor should be increased by an allowance sufficient to

cover the amount of the uncertainty.

8. When the strains are of a complex character and of uncertain amount, such as those in the crank-shaft of a reversing engine, a very high factor is necessary, possibly even as high as 40, the figure given by Rankine for shafts in millwork.

THE MECHANICAL PROPERTIES OF CORK.

Cork possesses qualities which distinguish it from all other solid or liquid bodies, namely, its power of altering its volume in a very marked degree in consequence of change of pressure. It consists, practically, of an aggrega-tion of minute air-vessels, having thin, water-tight, and very strong walls, and hence, if compressed, the resistance to compression rises in a manner more like the resistance of gases than the resistance of an elastic solid such as a spring. In a spring the pressure increases in proportion to the distance to which the spring is compressed, but with gases the pressure increases in a much more rapid manner; that is, inversely as the volume which the gas is made to occupy. But from the permeability of cork to air, it is evident that, if subjected to pressure in one direction only, it will gradually part with its occluded air by effusion, that is, by its passage through the porous walls of the cells in which it is contained. The gaseous man of orek constitutes 188 of its bulk. Its also that its the contained. part of cork constitutes 53% of its bulk. Its elasticity has not only a very considerable range, but it is very persistent. Thus in the better kind of corks used in bottling the corks expand the instant they escape from the bottles. This expansion may amount to an increase of volume of 75%, even after the corks have been kept in a state of compression in the bottles for ten years. If the cork be steeped in hot water, the volume continues to increase till it attains nearly three times that which it occupied in the neck of the bottle.

When cork is subjected to pressure a certain amount of permanent deformation or "permanent set" takes place very quickly. This property is common to all solid elastic substances when strained beyond their elastic limits, but with cork the limits are comparatively low. Besides the permanent set, there is a certain amount of sluggish elasticity—that is, cork on being released from pressure springs back a certain amount at once, but

the complete recovery takes an appreciable time.

Cork which had been compressed and released in water many thousand times had not changed its molecular structure in the least, and had continued perfectly serviceable. Cork which has been kept under a pressure of three atmospheres for many weeks appears to have shrunk to from 80% to 85% of its original volume.—Van Nostrand's Eng'g Mag. 1886, xxxv. 307.

TESTS OF VULCANIZED INDIA-RUBBER.

Lieutenant L. Vladomiroff, a Russian naval officer, has recently carried out a series of tests at the St. Petersburg Technical Institute with a view to establishing rules for estimating the quality of vulcanized india-rubber. The following, in brief, are the conclusions arrived at, recourse being had to physical properties, since chemical analysis did not give any reliable result: 1. India-rubber should not give the least sign of superficial cracking when bent to an angle of 180 degrees after five hours of exposure in a closed air-bath to a temperature of 125° C. The test-pieces should be 2,4 inches 2. Rubber that does not contain more than half its weight of metallic oxides should stretch to five times its length without breaking. 3. Rublic oxides should stretch to five times its length without used in vulcanizing it, ber free from all foreign matter, except the sulphur used in vulcanizing it, the first length without rupture. 4. The should stretch to at least seven times its length without rupture. extension measured immediately after rupture should not exceed 125 of the original length, with given dimensions. 5. Suppleness may be determined by measuring the percentage of ash formed in incineration. This may form the basis for deciding between different grades of rubber for certain purposes. 6. Vulcanized rubber should not harden under cold. These rules have been adopted for the Russian navy.—Iron Age, June 15, 1893.

XYLOLITH, OR WOODSTONE

is a material invented in 1883, but only lately introduced to the trade by Otto Serrig & Co., of Pottschappel, near Dresden. It is made of magnesia cement, or calcined magnesite, mixed with sawdust and saturated with a solution of chloride of calcium. This pasty mass is spread out into sheets and submitted to a pressure of about 1000 lbs. to the square inch, and then simply dried in the air. Specific gravity 1.558. The fractured surface shows a uniform close grain of a yellow color. It has a tensional resistance when dry of 100 lbs. per square inch, and when wet about 66 lbs. When immersed dry of 100 lbs. per square inch, and when wet about 66 lbs. When immersed in water for 12 hours it takes up 2.1% of its weight, and 8.8% when immersed 216 hours.

When treated for several days with hydrochloric acid it loses 2.3% in weight, and shows no loss of weight under boiling in water, brine, soda-lye, and solution of sulphates of iron, of copper, and of ammonium. In hardness the material stands between feldspar and quartz, and as a non-conductor of

heat it ranks between asbestos and cork.

It stands fire well, and at a red heat it is rendered brittle and crumbles at the edges, but retains its general form and cohesion. This xylolith is supplied in sheets from 1/4 in. to 11/4 in. thick, and up to one metre square. It is extensively used in Germany for floors in railway stations, hospitals, etc., and for decks of vessels. It can be sawed, bored, and shaped with ordinary woodworking tools. Putty in the joints and a good coat of paint make it entirely water-proof. It is sold in Germany for flooring at about 7 cents per square foot, and the cost of laying adds about 4 cents more.—Eng'g News, July 28, 1892, and July 27, 1893.

ALUMINUM-ITS PROPERTIES AND USES. (By Alfred E. Hunt, Pres't of the Pittsburgh Reduction Co.)

The specific gravity of pure aluminum in a cast state is 2.58; in rolled bars of large section it is 26; in very thin sheets subjected to high compression under chilled rolls, it is as much as 2.7. Taking the weight of a given bulk of cast aluminum as 1, wrought iron is 2.90 times heavier; structural steel, 2.95 times; copper, 3.60; ordinary high brass, 3.45. Most wood suitable for use in structures has about one third the weight of aluminum, which weighs 0.092 lb. to the cubic inch.

Pure aluminum is practically not acted upon by boiling water or steam. Carbonic oxide or hydrogen sulphide does not act upon it at any temperature under 600° F. It is not acted upon by most organic secretions.

Hydrochloric acid is the best solvent for aluminum, and strong solutions of caustic alkalies readily dissolve it. Ammonia has a slight solvent action, and concentrated sulphuric acid dissolves aluminum upon heating, with evolution of sulphurous acid gas. Dilute sulphuric acid acts but slowly on the metal, though the presence of any chlorides in the solution allow rapid decomposition. Nitric acid, either concentrated or dilute, has very little action upon the metal, and sulphur has no action unless the metal is at a red heat. State has very little effect on aluminum. Strips of the metal placed on the sides of a wooden ship corroded less than 1/1000 inch after six months' exposure to sea-water, corroding less than copper sheets similarly placed.

In malleability pure aluminum is only exceeded by gold and silver. In ductility it stands seventh in the series, being exceeded by gold, silver, platinum, iron, very soft steel, and copper. Sheets of aluminum have been rolled down to a thickness of 0.0005 inch, and beaten into leaf nearly as rolled down to a thickness of 1,0005 inch, and beaten into lear nearly as thin as gold leaf. The metal is most malleable at a temperature of between 400° and 600° F., and at this temperature it can be drawn down between rolls with nearly as much draught upon it as with heated steel. It has also been drawn down into the very finest wire. By the Mannesmann process aluminum tubes have been made in Germany.

Aluminum stands very high in the series as an electro-positive metal, and contact with other metals should be avoided, as it would establish a galvanic

couple.

The electrical conductivity of aluminum is only surpassed by pure copper, silver, and gold. With silver taken at 100 the electrical conductivity of aluminum is 54.20; that of gold on the same scale is 78; zinc is 29.90; iron is only 16, and platinum 10.60. Pure aluminum has no polarity, and the metal in the market is absolutely non-magnetic.

Sound castings can be made of aluminum in either dry or "green" sand moulds, or in metal "chills." It must not be heated much beyond its melting point, and must be poured with care, owing to the ready absorption of occluded gases and air. The shrinkage in cooling is 17.64 inch per foot or a little more than ordinary brass. It should be melted in plumbago crucibles, and the metal becomes molten at a temperature of 1120° F. according to Professor Roberts-Austen, or at 1300° F. according to Richards

The coefficient of linear expansion, as tested on \(\frac{3}{2} \)-inch round aluminum rods, is 0.00002295 per degree centigrade between the freezing and boiling point of water. The mean specific heat of aluminum is higher than that of any other metal, excepting only magnesium and the alkali metals. From zero to the melting-point it is 0.2185; water being taken as 1, and the latent heat of fusion at 28.5 heat units. The coefficient of thermal conductivity of unannealed aluminum is 37.96; of annealed aluminum, 38.37. As a conductor of heat aluminum ranks fourth, being exceeded only by silver, copper, and

Aluminum, under tension, and section for section, is about as strong as cast iron. The tensile strength of aluminum is increased by cold rolling or cold forging, and there are alloys which add considerably to the tensile strength without increasing the specific gravity to over 3 or 3.25.

The strength of commercial aluminum is given in the following table as

the result of many tests:

	Elastic Limit per sq. in. in	Ultimate Strength per sq. in. in	Percentage of Reduct'n
Form.	Tension,	Tension,	of Area in
	lbs.	lbs.	Tension.
Castings	6.500	15,000	15
Sheet	12,000	24,000	35
Wire	16,000-80,000	80,000-65,000	60
Bars		28,000	40

The elastic limit per square inch under compression in cylinders, with length twice the diameter, is 3500. The ultimate strength per square inch under compression in cylinders of same form is 12,000. The modulus of elasticity of cast aluminum is about 11,000,000. It is rather an open metal in its texture, and for cylinders to stand pressure an increase in thickness must

its texture, and for cylinders to stand pressure an increase in thickness must be given to allow for this porceity. Its maximum shearing stress in castings is about 12,000, and in forgings about 16,000, or about that of pure copper. Pure aluminum is too soft and lacking in tensile strength and rigidity for many purposes. Valuable alloys are now being made which seem to give great promise for the future. They are alloys containing from 2% to 7% or 8% of copper, manganese, iron, and nickel. As nickel is one of the principal constituents, these alloys have the trade name of "Nickel-aluminum." Plates and bars of this nickel alloy have a tensile strength of from 40,000 to 50,000 pounds per square inch, an elastic limit of 55% to 60% of the ultimate tensile strength an elongation of 3% in 2 inches and a reduction of area of 25%

sile strength, an elongation of 20% in 2 inches, and a reduction of area of 25%.

This metal is especially capable of withstanding the punishment and distortion to which structural material is ordinarily subjected. Nickelaluminum alloys have as much resilience and spring as the very hardest of hard-drawn brass.

Their specific gravity is about 2.80 to 2.85, where pure aluminum has a

specific gravity of 2.72

In castings, more of the hardening elements are necessary in order to give the maximum stiffness and rigidity, together with the strength and ductility of the metal; the favorite alloy material being zinc, iron manganese, and copper. Tin added to the alloy reduces the shrinkage, and alloys of aluminum and tin can be made which have less shrinkage than cast iron.

The tensile strength of hardened aluminum-alloy castings is from 20,000

to 25,000 pounds per square inch.

Alloys of aluminum and copper form two series, both valuable. The first is aluminum bronze, containing from 5% to 111% of aluminum; and the second is copper hardened aluminum, containing from 2% to 15% of copper. Aluminum-bronze is a very dense, fine-grained, and strong alloy, having good ductility as compared with tensile strength. The 10% bronze in forged bars will give 100,000 lbs. tensile strength per square inch, with 60,000 lbs. elastic limit per square inch, and 10% elongation in 8 inches. The 5% to 75% bronze has a specific gravity of 8 to 8.30, as compared with 7.50 for the 10% to 1136% bronze, a tensile strength of 70,000 to 80,000 lbs., an elastic limit of 40,000 lbs. an elastic limit of 40,000 lbs.

lbs, per square inch, and an elongation of 30% in 8 inches.

Aluminum is used by steel manufacturers to prevent the retention of the occluded gases in the steel, and thereby produce a solid ingot. The proportions of the dose range from 1/2 lb. to several pounds of aluminum per ton of steel. Aluminum is also used in giving extra fluidity to steel used in castings, making them sharpen and sounder. making them sharper and sounder. Added to cast iron, aluminum causes the iron to be softer, free from shrinkage, and lessens the tendency to "chill,"

With the exception of lead and mercury, aluminum unites with all metals,

though it unites with antimony with great difficulty. A small percentage of silver whitens and hardens the metal, and gives it added strength; and or silver whitens and narcens the metal, and gives it added strength; and this alloy is especially applicable to the manufacture of fine instruments and apparatus. The fc!!owing alloys have been found recently to be useful in the arts: Nickel-aluminum, composed of 20 parts nickel to 80 of aluminum; rosine, made of 40 parts nickel, 10 parts silver, 30 parts aluminum, and 20 parts tin, for jewellers' work; metaline, made of 85 parts cobalt, 25 parts aluminum, 10 parts iron, and 30 parts copper. The aluminum-bourbounz metal shown at the Paris Exposition of 1889, has a specific gravity of 2.9 to 2.96, and can be cast in very solid shapes, as it has very little shrinkage. From analysis the following composition is deduced: Aluminum, 85.74%; tin, 12 94%; silicon 1.38%; iron none 12.94%; silicon, 1.32%; iron, none.

The metal can be readily electrically welded, but soldering is still not sat-

isfactory. The high heat conductivity of the aluminum withdraws the heat of the molten solder so rapidly that it "freezes" before it can flow suffior the motion solder so rapidly that it "freezes" before it can flow sufficiently. A German solder said to give good results is made of 80% tin to 20% zinc, using a flux composed of 80 parts stearic acid, 10 parts chloride of zinc, and 10 parts of chloride of tin. Pure tin, fusing at 250° C., has also been used as a solder. The use of chloride of silver as a flux has been patented, and used with ordinary soft solder has given some success. A pure nickel soldering-bit should be used, as it does not discolor aluminum

as copper bits do.

ALLOYS. ALLOYS OF COPPER AND TIN.

(Extract from Report of U. S. Test Board,*) Test Strength, er sq. in. l" sq. Torsion Mean Com-蒀 Tests. position by Elastic Limit, lbs. per sq. i Elongation, per cent in Number. Transverse J Modulus of Rupture, Bď. Deflection, 1 Rar 22 in. 1 SQ Crushing Strength, Ibs per sq Analysis. Mom-ft,-lbs, aximum Tensile St Ibs. per s per Angle of Torsion, degrees. Bar 22 i nches. Crp. Tor. Tin. per. 100. 27,800 1 14,000 29,848 bent. 153 6.4742,000 143 100. 12,760 24,58011,000 0.47 21,251 2.31 39,000 10 65 40 97.89 96.06 1.90 10,000 16,000 04.00 34,000 150 317 32,000 33,232 14.29 bent. 42,048 157 247 38,659 43,731 4 94.11 5.43 28,540 19,000 .. 7.80 5 92.11 5.53 42,0001 160 126 90.27 88.41 87.15 82.70 9.58 11.59 12.73 17.34 49,400 60,403 84,531 6 26,860 15,750 3.66 44 38,000 114 7 44 8 29,430 20,000 3.33 4.00 53,000 182 100 9 67,930 0.63 10 80.95 18.84 32,980 0.04 56,715 0.4978,000 190 16 11 77.56 76.68 22.25 23.24 0. 29,926 0.16 22,010 0.19 12 22,010 0. 32,210 114,000 3.472.89 26.85 0. 9,512 13 0.05 69.84 14 29.88 5,585 5,585 0. 12,076 0.06 147,000 18 1.5 15 68.58 31,26 0. 9,152 0.04 ... 67.87 65.84 56.70 16 32.10 34.47 0. 0,477 0.05 2,201 2,201 1,4554,776 2,126 17 0. 0.0284,700 16 1 0. 18 43.17 1,455 0.02 19 44.52 55.28 3,010 3,010 0. 4,776 0.03 35,800 23 1 0. 5,224 34, 22 65,80 3,371 3,371 19,600 20 2 0 04 21 23.35 76.29 6,775 6,775 12,408 0. 0.27 15.08 22 84.62 9,063 0.86 6,500 23 25 10,706 23 11.49 88.47 6,390 8,500 5.85 4.10 10,100 62 6,450 4,780 24 8.57 91.89 8,500 6.87 5,305 bent. 9,800 23 132 25 2,750 12.32 6,925 3.72 96.81 9,800 23 " 557 3.505 35.51 3.740 6,400 12

^{*} The tests of the alloys of copper and tin and of copper and zinc, the results of which are published in the Report of the U.S. Board appointed to test Iron, Steel, and other Metals, Vols. I and II, 1879 and 1881, were made by the author under direction of Prof. R. H. Thurston, chairman of the Committee on Alloys. See preface to the report of the Committee, in Vol.

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Nos. 1a and 2 were full of blow-holes.

Tests Nos. 1 and 1a show the variation in cast copper due to varying conditions of casting. In the crushing tests Nos. 12 to 20, inclusive, crushed and broke under the strain, but all the others bulged and flattened out. In these cases the crushing strength is taken to be that which caused a decrease of 10% in the length. The test-pieces were 2 in. long and 5% in. diameter. The torsional tests were made in Thurston's torsion-machine, on pieces 5% in. diameter and 1 in. long between heads.

chameter and 1 in. long between heads.

Specific Gravity of the Copper-tin Alloys.—The specific gravity of copper, as found in these tests, is 8.674 (tested in turnings from the ingot, and reduced to 39.1° F.). The alloy of maximum sp. gr. 8.956 contained 62.42 copper, 37.48 tin, and all the alloys containing less than 37 tin varied irregularly in sp. gr. between 8.65 and 8.93, the density depending not on the composition, but on the porosity of the casting. It is probable that the actual sp. gr. of all these alloys containing less than 37% tin is about 8.95, and any smaller fleure indicates porosity in the specimen 8.95, and any smaller figure indicates porosity in the specimen.

From 37% to 100% tin, the sp. gr. decreases regularly from the maximum of 8,956 to that of pure tin, 7.293.

Note on the Strength of the Copper-tin Alloys.

The bars containing from 2% to 24% tin, inclusive, have considerable strength, and all the rest are practically worthless for purposes in which strength is required. The dividing line between the strong and brittle alloys is precisely that at which the color changes from golden yellow to silver-white, viz., at a composition containing between 34% and 30% of tin.

It appears that the tensile and compressive strengths of these alloys are in no way related to each other, that the torsional strength is closely proportional to the tensile strength, and that the transverse strength may depend in some degree upon the compressive strength, but it is much more nearly related to the tensile strength. The modulus of rupture, as obtained by the transverse tests, is, in general, a figure between those of tensile and compressive strengths per square inch, but there are a few exceptions in

which it is larger than either.

The strengths of the alloys at the copper end of the series increase rapidly with the addition of tin till about 4% of tin is reached. The transverse strength continues regularly to increase to the maximum, till the alloy constrength continues regularly to increase to the maintain the state and torsional strengths also increase, but irregularly, to the same point. This irregularly is probably due to porosity of the metal, and might possibly be removed by any means which would make the castings more compact. The maximum is reached at the alloy containing 82.70 copper, 17.34 tin, the transverse strength, however, being very much greater at this point than the tensile or torsional strength. From the point of maximum strength the figures drop rapidly to the alloys containing about 27.5% of tin, and then more slowly to 37.5%, at which point the minimum (or nearly the minimum) strength, by all three methods of test, is reached. The alloys of minimum strength are found from 37.5% tin to 52.5% tin. The absolute minimum is probably about 45% of tin.

From 52.5% of tin to about 77.5% tin there is a rather slow and irregular increase in strength. From 77.5% tin to the end of the series, or all tin, the

strengths slowly and somewhat irregularly decrease.

The results of these tests do not seem to corroborate the theory given by some writers, that peculiar properties are possessed by the alloys which are compounded of simple multiples of their atomic weights or chemical equivalents, and that these properties are lost as the compositious vary more or less from this definite constitution. It does appear that a certain percentage composition gives a maximum strength and another certain percentage a minimum, but neither of these compositions is represented by simple multiples of the atomic weights.

There appears to be a regular law of decrease from the maximum to the minimum strength which does not seem to have any relation to the atomic

proportions, but only to the percentage compositions.

Hardness.—The pieces containing less than 24% of tin were turned in the lathe without difficulty, a gradually increasing hardness being noticed, the last named giving a very short chip, and requiring frequent sharpening of the tool.

With the most brittle alloys it was found impossible to turn the test-pieces in the lathe to a smooth surface. No. 18 to No. 17 (26.85 to 84.47 tin) could not be cut with a tool at all. Chips would fly off in advance of the tool and

beneath it, leaving a rough surface; or the tool would sometimes, apparently, crush off portions of the metal, grinding it to powder. Beyond 40% tin the hardness decreased so that the bars could be easily turned.

ALLOYS OF COPPER AND ZINC. (U. S. Test Board).

	Mean	Com-	Tensile	Elastic Limit	on %	Trans- verse	, kg .	Crush-		ional sts.
No.	Ana	lysis.	Strength, lbs. per	Break- ing	Elongation ; in 5 inches.	Test Modu- lus of	본부	ing Str'gth per sq.	Moment ftlbs.	e of sion,
	Cop- per.	Zinc.	sq. in.	Load, lbs. per sq. in.	B	Rup- ture.	Peffect rq. ba long.	in., lbs.	Max. Tor Momen ftlbs.	Angle Torsic deg.
1	97.83	1.88	27,240				-		180	357
1 2 8	82.93			26.1	26.7	23,197	Bent		155	829
8	81.91	17.99		80.6	81.4	21,193			166	845
4	77.89		35,630	20.0	35.5		l "		169	811
5 6 7 8	76.65	23.08		24.6	35.8	22,325	"	42,000	165	267
6	73.20			23.7	38.5) 16 66		168	293
7	71.20			29.5	29.2		;;	· · · · • • • •	164	269
8	69.74			28.7	20.7	26,030	1	· · · · · • • • •	143	202
10	66.27		37,800 48,300	25.1 82.8	87.7 81.7			· • • • • • • • • • • • • • • • • • • •	176 202	257 230
11	60.94	88.66	41,065	40.1	20.7		14	75,000	194	202
75	58.49			54.4	10.1		1 "	10,000	227	93
÷ิลั	55.15	44.44		44.0	15.3		- "	78,000	209	109
	54.86			53.9	8.0	47,955		1	223	72
15	49,66			54.5	5.0		1.26	117,400	172	88
16	48.99			100.	0.8		0.61	l 	176	16
17	47.56			100.	0.8		1.17	121,000	155	18
18	43.86			100.		17,691	0.10		88	18 2 2 1
19	41.80			100.	• • • •	7,761	0.04		18	2
20 21	32.94	66.28		100.		8,296	0.04	· • • · • • • •	29	1
21	29,20			100.		16,579	0.04		40	2
22	20.81	77.68		100. 100.	0.2	22,972 85,026	0.13	52,152	65	1
23 24	12.12 4.85			100.	0.4		0.81	·····	82 81	8 22
25		Zinc.	18,065 5,400	75.	0.7		0.12	22,000	87	142
~	Casu	Zille.	1100,400	1 10.	0.1	143700	. 0.14	, ~~,000	. 01	140

Variation in Strength of Gun-bronze, and Means of Improving the Strength.—The figures obtained for alloys of from 7.8% to 12.7% tin, viz., from 26.680 to 29.430 pounds, are much less than are usually given as the strength of gun-metal. Bronze guns are usually cast under the pressure of a head of metal, which tends to increase the strength under the pressure of a head of metal, which tends to increase the strength and density. The strength of the upper part of a gun casting, or sinking head, is not greater than that of the small bars which have been tested in these experiments. The following is an extract from the report of Major Wade concerning the strength and density of gun-bronze (1850):—Extreme variation of six samples from different parts of the same gun (a 32-pounder howitzer): Specific gravity, 8.487 to 8.835; tenacity, 23,428 to 52,192. Extreme variation of all the samples specific gravity, 8.308 to 8.850; tenacity, 23,108 to 54,531. Extreme variation of all the samples from the gun heads: Specific gravity, 8.308 to 8.756; tenacity, 23,529 to 85,484.

Major Wade says: The general results on the quality of bronze as it is found in guns are mostly of a negative character. They expose defects in density and strength, develop the heterogeneous texture of the metal in different parts of the same gun, and show the irregularity and uncertainty of quality which attend the casting of all guns, although made from a milar materials, treated in like manner.

materials, treated in like manner.

Navy ordnance bronze containing 9 parts copper and 1 part tin, tested at Washington, D. C., in 1875-6, showed a variation in tensile strength from 29,800 to 51,400 lbs. per square inch, in elongation from 3% to 58%, and in specific gravity from 8.39 to 8.88.

That a great improvement may be made in the density and tenacity of gun-bronze by compression has been shown by the experiments of Mr. S. B. Dean in Boston, Mass., in 1869, and by those of General Uchatius in Austria 1873. The former increased the density of the metal next the bore of the gun from 8.321 to 8.875, and the tenacity from 27,238 to 41,471 pounds per

square inch. The latter, by a similar process, obtained the following figures for tenacity:

	Pounds per sq. in.
Bronze with 10% tin	72,053
Bronze with 8% tin	78,958
Bronze with 64 tin	77.656

ALLOYS OF COPPER, TIN, AND ZINC. (Report of U. S. Test Board, Vol. II, 1881.)

72 90 5 5 41,834 2.68 22.60 30,740 2.34 9.6 5 88.14 1.86 10 31,986 3.67 32,000 33,000 17.6 19.5 70 85 5 10 44,457 2.85 28,840 28,560 6.80 5.2 89 85 12.5 2.5 62,405 2.83 34,000 32,800 1.29 2.7 88 88 2.5 12.5 5 6.960 1.61 86,000 34,000 .86 .9 77 82.5 15 2.5 69,045 1.09 33,000 33,800	No.	Analysis, Original Mixture,			Transverse Strength.		Tensile Strength per square inch.		Elongation per cent in 5 inches.	
6 88.14 1.86 10 31,986 3 67 32,000 33,000 17.6 19.5 70 85 10 5 10 44,457 2.85 28.60 38,600 2.85 5.2 89 85 12.5 2.5 62,470 2.85 38.60 38,000 2.80 1.29 2.7 88 89.5 12.5 5 66,960 1.61 36,000 38,000 38,000 .80 9.9 77 82.5 15 2.5 69,045 1.09 38,000 33,800 6.6 68 80 10 10 67,117 2.45 38,80 31,950 1.1.6 8.5 68 77.5 10 12.5 56,476 .44 32,50 30,760 .55 .4 86 77.5 10 12.5 56,355 2.91 38,00 33,950 1.56 3.1 63 75 5 <t< th=""><th></th><th>Cu.</th><th>Sn.</th><th>Zn.</th><th>of</th><th>tion,</th><th>Α.</th><th>В.</th><th>A.</th><th>В.</th></t<>		Cu.	Sn.	Zn.	of	tion,	Α.	В.	A.	В.
4 57.5 21.25 21.25 2 52 .02 25 1,300	5 771 898 77 658 696 873 854 655 668 834 922 601 622 874 75 555 557 89 553 542	88.55 88.55 88.86 88.55 88.86 88.55 88 88.55 88 88 88 88 88 88 88 88 88 88 88 88 8	1.86 50 12.5 15 15 10 11.0 5 5 5 5 10 15 20 5 5 7 5 5 10 15 20 5 5 7 5 5 10 15 20 5 5 10 15 20 5 10	10 10 10 10 10 10 10 10 10 10 10 10 10 1	41, 834 41, 457 62, 470 62, 470 66, 960 66, 960 66, 170 66, 17	2.68 3.67 2.85 2.85 2.88 1.61 1.88 2.44 1.19 1.39 3.11 2.91 2.91 3.88 2.45 1.61 3.88 2.45 3.81 3.81 3.81 3.81 3.81 3.81 3.81 3.81	32, 000 28, 400 38, 600 38, 600 38, 500 38, 500 38, 500 38, 500 38, 500 38, 14	33,000 28,560 36,000 32,800 34,000 31,950 30,780 30,780 30,780 30,900 32,500 34,000 32,500 34,000 32,400 36,000 27,660 32,400 36,000 22,500 36,000 22,500 36,000 22,500 36,000 22,500 36,000 22,500 36,000 22,500 36,000 22,500 36,000 22,500 36,000 22,500 36,000 22,500 36,000 36	17.6 6.80 2.51 1.29 .86 	9.63 19.5 5.28 5.28 2.25 2.25 .92 .68 8.59 1.67 1.40 .59 1.83 1.25 .54 8.78 .99 .40 8.09 .43 .20 .61 .19 8.02 .40
	4	57.5	21.25	21.25	2.752	.02	725	1,800	l	2.88
. א. ו מות ועל ו על 127, ו און מון על ו על ו על ו על ו על ו	50	55		40	88.174	.22	27,400	80,500	.46	.48
			1ŏ							.10
										.45

The transverse tests were made in bars 1 in. square, 22 in. between supports. The tensile tests were made on bars 0.798 in. diam. turned from the two halves of the transverse-test bar, one half being marked A and the other B.

Ancient Bronzes.—The usual composition of ancient bronze was the same as that of modern gun-metal—90 copper, 10 the; but the proportion of tin varies from 5% to 15%, and in some cases lead has been found. Some ancient Egyptian tools contained 88 copper, 12 tin.—The alloys containing less than 15% of zinc by original mixture were generally defective. The bars were full of blow-holes, and the metal showed signs of oxidation. To insure good cestings it appears that copper-zinc alloys should contain more than good castings it appears that copper-zinc alloys should contain more than 18% of zinc.

From No. 2 to No. 8 inclusive, 16.98 to 80.06% zinc the bars show a remarkable similarity in all their properties. They have all nearly the same strength and ductility, the latter decreasing slightly as zinc increases, and are nearly alike in color and appearance. Between Nos. 8 and 10, 30.06 and 36.86% zinc, the strength by all methods of test rapidly increases. Between No. 10 and No. 15, 38.36 and 50.14% zinc, three is another group, distinguished by high strength and diminished ductility. The alloy of maximum tensile, transverse and torsional strength contains about 41% of zinc.

The alloys containing less than 55% of zinc are all yellow metals. Beyond 55% the color changes to white, and the alloy becomes weak and brittle. Between 70% and pure zinc the color is bluish gray, the brittleness decreases and the strength increases, but not to such a degree as to make them useful

for constructive purposes.

Difference between Composition by Mixture and by Analysis.—There is in every case a smaller percentage of zinc in the average analysis than in the original mixture, and a larger percentage of copper. The loss of zinc is variable, but in general averages from it ozy.

Liquation or Separation of the Mctals.—In several of the

bars a considerable amount of liquation took place, analysis showing a difference in composition of the two ends of the bar. In such cases the change in composition was gradual from one end of the bar to the other, the upper end in general containing the higher percentage of copper. A notable instance was bar No. 13, in the above table, turnings from the upper end containing 40.88% of zinc, and from the lower end 48.52%.

Specific Gravity.—The specific gravity follows a definite law. varying with the composition, and decreasing with the addition of zinc. From the plotted curve of specific gravities the following mean values are taken:

80 60 70 Per cent zinc..... 10 20 40 50 80 Specific gravity...... 8.80 8.72 8.60 8.40 8.36 8.20 8.00 7.72 7.40 7.20 7.14.

Graphic Representation of the Law of Variation of Strength of Copper-Tin-Zinc Alloys.—In an equilateral triangle the sum of the perpendicular distances from any point within it to the three sides is equal to the altitude. Such a triangle can therefore be used to show graphically the percentage composition of any compound of three parts, such as a triple alloy. Let one side represent 0 copper, a second 0 tin, and the third 0 zinc, the vertex opposite each of these sides repreo tin, and the third o zinc, the vertex opposite each of these sides representing 100 of each element respectively. On points in a triangle of wood representing different alloys tested, wires were erected of lengths proportional to the tensile strengths, and the triangle then built up with plaster to the height of the wires. The surface thus formed has a characteristic topography representing the variations of strength with variations of composition. The cut shows the surface thus made, The vertical section to the left represents the law of tensile strength of the copper-tin alloys, the one to the right that of tin-zinc alloys, and the one at the rear that of the copper-zinc alloys. The high point represents the strongest possible ealloys of the three metals. If a composition is copper to the three metals. alloys of the three metals. Its composition is copper 55, zinc 43, tin 2, and its strength about 70,000 lbs. The high ridge from this point to the point of maximum height of the section on the left is the line of the strongest alloys,

represented by the formula zinc + (8 \times tin) = 55. All alloys lying to the rear of the ridge, containing more copper and less tin or zinc are alloys of greater ductility than those on the line of maximum strength, and are the valuable commercial alloys; those in front on the declivity toward the central valley are brittle, and those in the valley are both brit-tle and weak. Passing from the valley toward the section at the right the alloys lose their brittleness and become soft, the maximum softness being at tin = 100, but they remain weak, as is shown by the low elevation of the surface. This model was planned and constructed by Prof. Thurston in 1877. (See Trans. A. S. C. E. 1881 B.port of the U. S. Board appointed to

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test Iron, Steel, etc., vol. ii., Washington, 1881, and Thurston's *Materials of Engineering*, vol. iii.)

The best alloy obtained in Thurston's research for the U. S. Testing Board has the composition, Copper 55, Tin 0.5, Zinc 44.5. The tensile strength in a cast bar was 68,900 lbs. per sq. in., two specimens giving the same result; the elongation was 47 to 51 per cent in 5 inches. Thurston's formula for coppertin-zinc alloys of maximum strength (Trans. A. S. C. E., 1881) is z+3t=55,

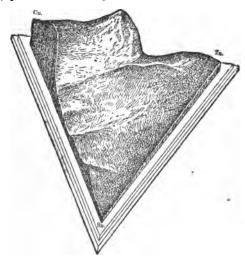


Fig. 77.

in which z is the percentage of zinc and t that of tin. Alloys proportioned according to this formula should have a strength of about 40,000 lbs, per sq. in. +500z. The formula fails with alloys containing less than 1 per cent of tin.

The following would be the percentage composition of a number of alloys made according to this formula, and their corresponding tensile strength in

castings:

Tin.	Zînc.	Copper.	Tensile Strength, Ibs. per sq. in.	Tin.	Zinc.	Copper.	Tensile Strength, lbs. per sq. in.
「123456F	52 49 46 43 40 87	47 49 51 53 55 57 59	66,000 64,500 68,000 61,500 60,000 58,500 57,000	8 9 10 19 14 16 18	81 28 25 19 18 7	61 63 65 69 78 77 81	55,500 54,000 52,500 49,500 46,500 43,500

These alloys, while possessing maximum tensile strength, would in general be too hard for easy working by machine tools. Another series made on the formula z+4 t=50 would have greater ductility, together with considerable strength, as follows, the strength being calculated as before, tensile strength in ibs, per sq. in. =40,000+500z.

Tin.	Zine.	Copper.	Tensile Strength, lbs. per sq. in.	Tin.	Zinc.	Copper.	Tensile Strength, lbs. per sq. in.
1	46	53	63,000	7	22	71	51,000
2	42	56	61,000	8	18	74	49,000
8	88	59	59,000	9	14	77	47,000
4	34	62	57,000	10	10	80	45,000
5	80	65	55,000	11	6	83	49,000
6	26	68	58,000	12	Ř	88	41,000

Composition of Alloys in Every-day Use in Brass Foundries. (American Machinist.)

l

	Cop- per.	Zinc.	Tin.	Lead.	
	lbs.	lbs.	lbs.	lbs.	
Admiralty metal	87	5	8	•••••	For parts of engines on board naval vessels.
Bell metal	16		4		Bells for ships and factories.
Brass (yellow)	16	8	ļ	1/6	For plumbers, ship and house brass work.
Bush metal	64 82	8	l 4	4	For bearing bushes for shafting.
Gun metal	82	1	8	- 	For pumps and other hydraulic purposes.
Steam metal	20	1	11/6	1	Castings subjected to steam pressure.
Hard gun metal	16	I	21/6	l. 	For heavy bearings.
Muntz metal	60	40			Metal from which bolts and nuts are forged, valve spindles, etc.
Phosphor bronze	93		8 ph	os. tin	For valves, pumps and general work.
i	90		10 4	66	For cog and worm wheels,
••	"	l		1	bushes, axle bearings, slide valves, etc.
Brazing metal	16	8	Ī	l	Flanges for copper pipes.
" solder	50	50	l	∤	Solder for the above flanges.
, aoidei	, .,	, 50	1	1	politici iti ulic above nanges.

Gurley's Bronze.—16 parts copper, 1 tin, 1 zinc, 1/4 lead, used by W. & L. E. Gurley of Troy for the framework of their engineer's transita, Tensile strength 41,114 lbs. per sq. in., elongation 27% in 1 inch, sp. gr. 8.696. (W. J. Keep, Trans. A. I. M. E. 1890.)

Useful Alloys of Copper, Tin, and Zinc.

(Selected from numerous sources.)

U. S. Navy Dept. journal boxes and guide-gibs	Copper.	Tin. 1 13.8 2.30	Zinc. 14 parts. 8.4 per cent. 39.48 " " "
Composition, U. S. Navy	88	10	2 " "
Brass bearings (J. Rose)	164 87.7	8 11.0	1 parts. 1.3 per cent.
Gun metal	92.5 91	5	2.5 " " " 2
4 44	87.75	9,75	2.5 " "
64 64 special section 1.00 sect	85	5	10 4 4
	88 13	2 2	15 " " 2 parts.
Tough brass for engines	76.5	11.8	11.7 per cent.
Bronze for rod-boxes (Lafond)	. 83	16	2 slightly malicable
" " pieces subject to shock	83 20	15	1.50 0.50 lead.
Red brass parts	20 87	4.4	4.3 4.8 **
Brenze for pump casings (Lafond)	88	10	2
" eccentric straps. "	84	14	2
shrill whistles	80	18	2.0 antimony.
" Low-toned whistles	81	17	2.0 "

		Copper.	Tin.	Zinc.	
Art bronz	e, dull red fracture	97	2	1	
Gold bron	ze	89.5	2.1	5.6	2.8 lead.
Bearing m	ne tal	89	8 .	8	
•	64	89	216	814	
*	4	86	14	-/-	
44		OE1/	1284	9	
44	4	On' =	18	2	
44	46	79	18	914	14 load
44	4	74	914	õíZ	7 lead.
English b	rass of A.D. 1504	64	8 8	2912	316 lead.

Tobin Bronze.—This alloy is practically a sterro or delta metal with the addition of a small amount of lead, which tends to render copper softer and more ductile. (F. L. Garrison, J. F. I., 1891.)

The following analyses of Tobin bronze were made by Dr. Chas. B. Dudley:

Din Makal

	Lig metal	Test Dar (Roll
	per cent.	per cent.
Copper		61.20
Zinc		87.14
Tin		0.90
Iron	0.11	0.18
Lead		0.35

Dr. Dudley writes, "We tested the test bars and found 78,500 tensile Dr. Dudley writes, "We tested the test bars and found '8,500 tensite strength with 15\$ elongation in two inches, and 4016\$ in eight inches. This high tensile strength can only be obtained when the metal is manipulated, Such high results could hardly be expected with cast metal."

The original Tobin bronze in 1875, as described by Thurston, Trans. A. S. C. E 1881, had, composition of copper 88.22, tin 2.30, zinc 39.48. As cast it had a tenacity of 68,000 lbs. per sq. in., and as rolled 79,000 lbs.; cold

A circular of Ansonia Brass & Copper Co. gives the following:—The tensile strength of six Tobin bronze one-inch round rolled rods, turned down to a diameter of \$\frac{9}{5}\$ of an inch, tested by Fairbanks, averaged 79,600 lbs. per sq. in., and the elastic limit obtained on three specimens averaged 54,257 lbs. per sq. in.

At a cherry-red heat Tobin bronze can be forged and stamped as readily as seen. Bous and nuts can be forged from it, either by hand or by machinery, with a marked digree of economy. Its great tensile strength, and resistance to the corrosive action of sea-water, render it a most mitable metal for condenser plates, steam-launch shafting, ship sheathing and fastenings, nails, hull plates for steam yachts, torpedo and life boats, and ship deck fittings. as steel. Bolts and nuts can be forged from it, either by hand or by ma-

The Navy Department has specified its use for certain purposes in the machinery of the new cruisers. Its specific gravity is 8.071. The weight of a cubic inch is .291 lb.

Special Alloys. (Engineer, March 24, 1898.)

JAPANESE ALLOYS for art work:

	Copper.	Silver.	Gold.	Lead.	Zinc.	Iron.
Shaku-do Shibu-ichi		1.55 82.07	8.73 traces.	0.11 .52	trace.	trace.

GILBERT'S ALLOY for cera-perduta process, for casting in plaster-of-paris. Copper 91.4 Tin 5.7 Lead 2.9 Very fusible.

COPPEE-ZINC-IRON ALLOYS.

(F. L. Garrison, Jour. Frank. Inst., June and July, 1891.)

Delta Metal.—This alloy, which was formerly known as sterro-metal, is composed of about 60 copper, from 34 to 44 zinc, 2 to 4 iron, and 1 to 2 tin. The peculiarity of all these alloys is the content of iron, which appears to have the property of increasing their strength to an unusual degree. In making delta metal the iron is previously alloyed with zinc in known and definite proportions. When ordinary wrought-iron is introduced into moltan ging the latter readily discolves or obscribe the former and will take molten zinc, the latter readily dissolves or absorbs the former, and will take

it up to the extent of about 5% or more. By adding the zinc-iron alloy thus obtained to the requisite amount of copper, it is possible to introduce any definite quantity of iron up to 5% into the copper alloy. Garrison gives the following as the range of composition of copper-zinc-iron, and copper-zinc-tin-iron alloys: I. II.

Per cent. Per cent. Iron..... 0.1 to 5 Iron..... 0.1 to 5 Copper 50 to 65 Tin 0.1 to 10 Zinc..... 1.8 to 45 Copper..... 98 to 40

The advantages claimed for delta metal are great strength and toughness. It produces sound eastings of close grain. It can be rolled and forged hot, and can stand a certain amount of drawing and hammering when cold. It takes a high polish, and when exposed to the atmosphere tarnishes less than hrass

When cast in sand delta metal has a tensile strength of about 45,000 pounds per square inch, and about 10% elongation; when rolled, tensile strength of 60,000 to 75,000 pounds per square inch, elongation from 9% to 17% on bars 1.138 inch in diameter and 1 inch area.

Wallace gives the ultimate tensile strength 33,600 to 51,520 pounds per

square inch, with from 10% to 20% elongation.

Delta metal can be forged, stamped and rolled hot. It must be forged at a dark cherry-red heat, and care taken to avoid striking when at a black

According to Lloyd's Proving House tests, made at Cardiff, December 2 1887, a half-inch delta metal-rolled bar gave a tensile strength of 88,400 pounds per square inch, with an elongation of 80% in three inches.

PHOSPHOR-BRONZE AND OTHER SPECIAL

BRONZES.

Phosphor-bronze.—In the year 1868, Monteflore & Kunzel of Liège, Belgium, found by adding small proportions of phosphorus or "phosphoret of tin or copper" to copper that the oxides of that metal, nearly always

83,40 Elongation, per cent..... 1.50

The strength of phosphor-bronze varies like that of ordinary bronze according to the percentages of copper, tin, zinc, lead, etc., in the alloy.

Deoxidized Bronze.—This alloy resembles phosphor bronze some-

what in composition and also delta metal, in containing zinc and iron. The following analysis gives its average composition:

Copper			0.10 0.07
Zinc	3.23	Phosphorus	0.005
Lead	2.14		100.615

Comparison of Copper, Silicon-bronze, and Phosphorbronze Wires. (Engineering, Nov. 23, 1883.)

Description of Wire.	Tensile Strength.	Relative Conductivity.
Pure copper	108,080 ** ** ** **	100 per cent, 96 " " 84 " " 26 " "

Penn. R. R. Co.'s Specifications for Phosphor-Bronze (1902).—The metal desired is homogeneous alloy of copper, 79.70; lead, 9.0; phosphorus, 0.80. Lots will not be accepted if samples do not show tin, between 9 and 11%; lead, between 8 and 11%; bhosphorus, between 0.7 and 1%; nor if the metal contains a sum total of other substances than copper, tin, lead, and phosphorus in greater quantity than 0.50 per cent. (See also p. 334.)

Silicon Bronze. (Aluminum World, May, 1897.)

The most useful of the silicon bronzes are the 3% (97% copper, 3% silicon) and the 5% (95% copper, 5% silicon), although the hardness and strength of the alloy can be increased or decreased at will by increasing or decreasing silicon. A 3% silicon bronze has a tensile strength, in a casting, of about 55,000 lbs. per sq. in, and from 50% to 60% elongation. The 5% bronze has a tensile strength of about 75,000 lbs. and about 8% elongation. More than 5% or 54% of silicon in copper makes a brittle alloy. In using silicon, either as a flux or for making silicon bronze, the rich alloy of silicon and copper which is now on the market should be used. It should be free from iron and other metals if the best results are to be obtained. Ferro-silicon is not suitable for use in copper or bronze mixtures.

ALUMINUM ALLOYS.

Aluminum Bronze. (Cowles Electric Smelting and Al. Co.'s circular.)
The standard A No. 2 grade of aluminum bronze, containing 10% of aluminum and 90% of copper, has many remarkable characteristics which distinguish it from all other metals.

The tenacity of castings of A No. 2 grade metal varies between 75,000 and 90,000 lbs. to the square inch, with from 4% to 14% elongation.

Increasing the proportion of aluminum in bronze beyond 11% produces a brittle alloy; therefore nothing higher than the A No. 1, which contains 11%, is made.

The B, C, D, and E grades, containing 71/48, 58, 21/48, and 11/48 of aluminum, respectively, decrease in tenacity in the order named, that of the former being about 65,000 pounds, while the latter is 25,000 pounds. While there is also a proportionate decrease in transverse and torsional strengths, elastic limit, and resistance to compression as the percentage of aluminum is lowered and that of copper raised, the ductility on the other hand increases in the same proportion. The specific gravity of the A No. 1 grade is 7.56. Bell Bros., Newcastle, gave the specific gravity of the aluminum bronzes

as follows: 3%, 8.601;

4%, 8.621:

5%, 8,369; 10%, 7.689.

Tests of Aluminum Bronzes. (By John H. J. Dagger, in a paper read before the British Association, 1889.)

Per cent	Tensile	Strength.	Elonga-		
of	Tons per	Pounds per square inch.	tion,	Specific	
Aluminum.	square inch.		per cent.	Gravity.	
11	40 to 45	89,600 to 100,800	8	7.23	
10	83 " 40	73,920 " 89,600	14	7.69	
714	25 " 30	56,000 " 67,200	40	8.00	
5-514	15 " 18	33,600 " 40,320	40	8.37	
217	18 " 15	29,120 " 33,600	50	8.69	
117	11 " 13	24,640 " 29,120	55		

Both physical and chemical tests made of samples cut from various secnoun physical and chemical tests made or samples cut from various sections of 245, 58, 7155, or 108 aluminized copper eastings tend to prove that the aluminum unites itself with each particle of copper with uniform proportion in each case, so that we have a product that is free from liquation and highly homogeneous. (R. C. Cole, from Age, Jan. 16, 1890.)

Casting.—The melting point of aluminum bronze varies slightly with the amount of aluminum contained, the higher grades melting at a somewhat lower temperature than the lower grades. The A No. 1 grades melting at about 1700° F., a little higher than ordinary bronze or brass.

Aluminum bronze shrinks more than ordinary brass. As the metal soliding

at about 1700° F., a little higher than ordinary bronze or brass.

Aluminum bronze shrinks more than ordinary brass. As the metal solidifies rapidly it is necessary to pour it quickly and to make the feeders amply large, so that there will be no "freezing" in them before the casting is properly fed. Baked-sand moulds are preferable to green sand, except for small castings, and when fine skin colors are desired in the castings. (See paper by Thos. D. West, Trans. A. S. M. E. 1886, vol. viii.)

All grades of aluminum bronze can be rolled, swedged, spun, or drawn cold except A 1 and A. 2. They can all be worked at a bright red heat.

In rolling, swedging, or spinning cold, it should be annealed very often, and at a brighter red heat than is used for annealing brass.

Brazing.—Aluminum bronze will braze as well as any other metal.

Brazing.-Aluminum bronze will braze as well as any other metal, using one quarter brass solder (zinc 500, copper 500 (and three quarters borax, or, better, three quarters cryolite.

Soldering.—To solder aluminum bronze with ordinary soft (pewter) solder: Cleanse well the parts to be joined free from grease and dirt. place the parts to be soldered in a strong solution of sulphate of copper and place in the bath a rod of soft iron touching the parts to be joined. After a while a coppery-like surface will be seen on the metal. Remove from bath, rinse quite clean, and brighten the surfaces. These surfaces can then be tinned by using a fluid consisting of zinc dissolved in hydrochloric acid, in

the ordinary way, with common soft solder.

Mierzinski recommends ordinary hard solder, and says that Hulot uses an alloy of the usual half-and-half lead-tin solder, with 12.5%, 25% or 50% of

zinc amalgam.

Aluminum-Brass (E. H. Cowles, Trans. A. I. M. E., vol. xviii.)—Cowles aluminum-brass is made by fusing together equal weights of A 1 aluminum-braze, copper, and zinc. The copper and braze are first thoroughly melted and mixed, and the zinc is finally added. The material is left in the furnace until small test-bars are taken from it and broken. When these bars show a tensile strength of 80,000 pounds or over, with 2 or 3 per cent ductility, the metal is ready to be poured. Tests of this brass, on small bars, have at times shown as high as 100,000 pounds tensile strength.

The screw of the United States gruphost Pettel is cast from this brass,

The screw of the United States gunboat Petrel is cast from this brass,

mixed with a trifle less zinc in order to increase its ductility.

Tests of Aluminum-Brass. (Cowles E. S. & Al. Co.)

(01.11.11.11.11.11.11.11.11.11.11.11.11.1									
Specimen (Castings.)	Diameter of Piece, Inch.	Area. sq. in.		Elastic Limit, lbs. per sq. in.		Remarks.			
15% A grade Bronze. 17% Zinc	.465	.1698	41,225	17,668	411/6	pieces long the			
1 part A Bronze } 1 part Zinc } 1 part Copper	.465	.1698	78,327		21/6	test ali 6 reen ruide			
1 part A Bronze) 1 part Zinc 1 part Copper	.460	.1661	72,246		21/4	These were bet			

The first brass on the above list is an extremely tough metal with low elastic limit, made purposely so as to "upset" easily. The other, which is called Aluminum-brass No 2, is very hard.

We have not in this country or in England any official standard by which to judge of the physical characteristics of cast metals. There are two conditions that are absolutely necessary to be known before we can make a fair comparison of different materials: namely, whether the casting was made in dry or green sand or in a chill, and whether it was attached to a larger casting or cast by itself. It has also been found that chill castings give higher results than sand-castings, and that bars cast by themselves purposely for testing almost invariably run higher than test-bars attached to castings. It is also a fact that bars cut out from castings are generally weaker than bars cost alone. (E. H. Cowles.)

Caution as to Reported Strength of Alloys.—The same variation in strength which has been found in tests of gun-metal (copper and tin) noted above, must be expected in tests of aluminum bronze and in fact of all alloys. They are exceedingly subject to variation in density and in grain, caused by differences in method of molding and casting, temperature of pouring, size and shape of casting, depth of "sinking head," etc.

Aluminum Hardened by Addition of Copper. Rolled Sheets .04 inch thick. (The Engineer, Jan. 2, 1891.)

Al. Per cent.	Cu. Per cent.	Sp. Gr. Calculated.	Sp. Gr. Determined.	Tensile Strength in pounds per square inch.
100 98	•• 9	2.78	2.67 2.71	26,535 43,563
96	4	2.90	2.77	44,180
94 92	ŝ	8.02 8.14	2.82 2.85	54,778 50,87 4

330

Tests of Aluminum Alloys.

(Engineer Harris, U. S. N., Trans, A. I. M. E., vol. xviii.)

Composition.			Tensile	Elastic	Elonga-	Reduc		
Cop- per.	Alumi- num.	Silicon.	Zinc.	Iron.	Strength, per sq. in. lbs.		tion, per ct.	tion of Area per ct.
91.50% 88.50 91.50 90.00 63.00 63.00 91.50 93.00 88.50	6.50% 9.33 6.50 9.00 3.83 8.33 6.50 6.50 9.33	1.75% 1.66 1.75 1.00 0.33 0.83 1.75 0.50 1.66	83.83% 83.83	0.25% 0.50 0.25 0.25	60,700 66,000 67,600 72,830 82,200 70,400 59,100 58,000 69,930	18,000 27,000 24,000 83,000 60,000 55,000 19,000 19,000 83,000	23.2 3.8 13. 2.40 2.33 0.4 15.1 6.2 1.33	80.7 7.8 21.62 5.78 9.88 4.38 23.59 15.5 3.80
92.00	6.50	0.50			46,530	17,000	7.8	19.19

For comparison with the above 6 tests of "Navy Yard Bronze," Cu 88, Sn 10, Zn 2, are given in which the T. S. ranges from 18,000 to 24,590, E. L. from 10,000 to 18,000 El. 2.5 to 5.8%, Red. 4 7 to 10.89.

Alloys of Aluminum, Silicon and Iron.

M. and E. Bernard have succeeded in obtaining through electrolysis, by treating directly and without previous purification, the aluminum earths (red and white bauxites) the following:

Alloys such as ferro-aluminum, ferro-silicon-aluminum and silicon-aluminum, where the proportion of silicon may exceed 10% which are employed in the metallurgy of iron for refining steel and cast-iron.

Also silicon aluminum, where the proportion of silicon does not exceed 10%, which may be employed in mechanical constructions in a rolled or hammered condition, in place of steel, on account of their great resistance, especially where the lightness of the piece in construction constitutes one of the main conditions of success.

The following analyses are given:

1. Alloys applied to the metallurgy of iron, the refining of steel and cast

1. Alloys applied to the metallurgy of iron, the refining of steel and cash fron: No. 1. Al, 70%; Fe, 25%; Si, 5%. No. 2. Al, 70; Fe, 20; Si, 10. No. 3. Al, 70; Fe, 15; Si, 15. No. 4. Al, 70; Fe, 10; Si, 20. No. 5. Al, 70; Fe, 10; Si, 10; Mn, 10. No. 6. Al. 70; Fe, trace; Si, 10; Mn, 10.

2. Mechanical alloys: No. 1. Al, 92; Si, 6.75; Fe, 1.25. No. 2. Al, 90; Si, 9.25; Fe, 0.75. No. 3. Al, 90; Si, 10; Fe, trace. The best results were with alloys where the proportion of iron was very low, and the proportion feillion in the neighborhood of 10%. Above that proportion the alloy becomes crystalline and can no longer be employed. The density of the alloys of silicon in approximately the same as that of aluminum — In Metallurois of silicon is approximately the same as that of aluminum.—La Metallurgie.

Tungsten and Aluminum.—Mr. Leinhardt Mannesmann says that the addition of a little tungsten to pure aluminum or its alloys communicates a remarkable resistance to the action of cold and hot water, salt water and other reagents. When the proportion of tungsten is sufficient the alloys offer great resistance to tensile strains.

Aluminum, Copper, and Tin.—Prof. R. C. Carpenter, Trans. A. S. M. E., vol. xix., finds the following alloys of maximum strength in a series in which two of the three metals are in equal proportions:

Al. 85; Cu. 7.5; Sn. 7.5; tensile strength, 30,000 lbs. per sq. in.; elongation in 6 in. 4%; sp. gr., 3.02. Al. 6.25; Cu. 87.5; Sn. 6.25; T. S., 63,000; El., 3.8; sp. gr., 735. Al. 5; Cu. 5: Sn. 90; T. S., 11,000; El., 10.1; sp. gr., 6.82.

Aluminum and Zinc.—Prof. Carpenter finds that the strongest

alloy of these metals consists of two parts of aluminum and one part of zinc. Its tensi'e strength is 24,000 to 26,000 lbs. per sq. in.; has but little ductility, is readily cut with machine-tools, and is a good substitute for hard cast brass.

Aluminum and Tin.—M. Bourbouze has compounded an alloy of aluminum and tin, by fusing together 100 parts of the former with 10 parts of the latter. This alloy is paler than aluminum, and has a specific gravity of 2.85. The alloy is not as easily attacked by several reagents as aluminum is, and it can also be worked more readily. Another advantage is that it can be soldered as easily as bronze, without further preliminary prepara-

tions.

Aluminum-Antimony Alloys.—Dr. C. R. Alder Wright describes aluminum-antimony alloys in a communication read before the Society of Chemical Industry. The results of his researches do not disclose the existence of a commercially useful alloy of these two metals, and have greater scientific than practical interest. A remarkable point is that the alloy with the chemical composition Al Sb has a higher melting point than althoral manifester and the statement of the statement either aluminum or antimony alone, and that when aluminum is added to pure antimony the melting-point goes up from that of antimony (450° C.) to a certain temperature rather above that of silver (1000° C.).

ALLOYS OF MANGANESE AND COPPER.

Various Manganese Alloys.—E. H. Cowles, in Trans. A. I. M. E., vol. xviii, p. 495, states that as the result of numerous experiments on mixtures of the several metals, copper, zinc, tin, lead, aluminum, iron, and manganese, and the metalloid silicon, and experiments upon the same in ascertaining tensile strength, ductility, color, etc., the most important determinations appear to be about as follows:

1. That pure metallic manganese exerts a bleaching effect upon copper more radical in its action even than nickel. In other words, it was found that 18% of manganese present in copper produces as white a color in the resulting alloy as 25% of nickel would do, this being the amount of each required to remove the last trace of red.

2. That upwards of 20% or 25% of manganese may be added to copper with-

out reducing its ductility, although doubling its tensile strength and chang-

ing its color.

3. That manganese, copper, and zinc when melted together and poured into moulds behave very much like the most "yeasty" German silver, producing an ingot which is a mass of blow-holes, and which swells up above the mould before cooling.

4. That the alloy of manganese and copper by itself is very easily

oxidized.

i

5. That the addition of 1.25% of aluminum to a manganese-copper alloy converts it from one of the most refractory of metals in the casting process

converts it from one of the most refractory of metals in the casting process into a metal of superior casting qualities, and the non-corrodibility of which is in many instances greater than that of either German or nickel silver.

A "silver-bronze" alloy especially designed for rods, sheets, and wire has the following composition: Manganese, 18; aluminum, 1.20; silicon, 0.5; zinc, 13; and copper, 67.5%. It has a tensile strength of about 57,000 pounds on small bars, and 20% elongation. It has been rolled into thin plate and drawn into wire. 008 inch in diameter. A test of the electrical conductivity of this wire (of size No. 32) shows its resistance to be 41.44 times that of pure copper. This is far lower conductivity than that of German silver.

copper. This is far lower conductivity than that of German silver.

Manganese Bronze. (F. L. Garrison, Jour. F. I., 1891.)—This alloy has been used extensively for casting propeller-blades. Tests of some made by B. H. Cramp & Co., of Philadelphia, gave an average elastic limit of 80,000 pounds per square inch, tensile strength of about 60,000 pounds per square inch, with an elongation of 8% to 10% in sand castings. When rolled, the elastic limit is about 80,000 pounds per square inch, tensile strength \$5,000 to 106,000 pounds per square inch, with an elongation of 12% to 15%.

Compression tests made at United States Navy Department from the metal in the pouring-gate of propeller-hub of U. S. S. Maine gave in two tests crushing stress of 126,450 and 135,750 lbs. per sq. in. The specimens were 1 inch high by 0.7 × 0.7 inch in cross-section = 0.49 square inch. Both specimens gave way by shearing, on a plane making an angle of nearly 45° with the direction of stress.

the direction of stress.

the direction of stress. A test on a specimen $1\times 1\times 1$ inch was made from a piece of the same pouring-gate. Under stress of 150,000 pounds it was flattened to 0.72 inch high by about $1\frac{1}{4}\times 1\frac{1}{4}$ inches, but without rupture or any sign of distress. One of the great objections to the use of manganese bronze, or in fact any alloy except iron or steel, for the propellers of iron ships is on account of the galvanic action set up between the propeller and the stern-posts. This difficulty has in great measure been overcome by putting strips of rolled zinc around the propeller apertures in the stern-frames. The following analysis of Parsons' manganese bronze No. 2 was made from a chip from the propeller of Mr. W. K. Vanderbilt's yacht Alva.

Copper	88.644
Zinc	1.570
Tin	
Iron	
Lead	
Phosphorus	
	00 000

It will be observed there is no manganese present and the amount of zinc is very small.

E. H. Cowles, Trans. A. I. M. E., vol. xviii, says: Manganese bronze, so called, is in reality a manganese brass, for zinc instead of tin is the chief element added to the copper. Mr. P. M. Parsons, the proprietor of this brand of metal, has claimed for it a tensile strength of from 24 to 28 tons on small bars when cast in sand. Mr. W. C. Wallace states that brass-founders of high repute in England will not admit that manganese bronze has more than from 12 to 17 tons tensile strength. Mr. Horace See found tensile strength of 45,000 pounds, and from 6% to 121/2% elongation.

GERMAN-SILVER AND OTHER NICKEL ALLOYS.

German Silver.—The composition of German silver is a very uncertain thing and depends largely on the honesty of the manufacturer and the price the purchaser is willing to pay. It is composed of copper, zinc. and nickel in varying proportions. The best varieties contain from 18% to 25% of nickel and from 20% to 30% of zinc, the remainder being copper. The more expensive nickel silver contains from 25% to 33% of nickel and from 75% to 66% of copper. The nickel is used as a whitening element; it also strengthens the alloy and renders it harder and more non-corrodible than the brass made without it, of copper and zinc. Of all troublesome alloys to handle in the foundry or rolling mill, German silver is the worst. It is unmanageable and refractory at every step in its transition from the crude elements into rods, sheets, or wire. (E. H. Cowles, Trans. A. I. M. E., vol. xviii, p. 494.)

			Copper.	Nickel.	Tin.	žinc.
German	silve	r	51.6	25.8	22.6	
66	60	***************************************	50.2	14.8	8,1	81.9
".	66	*******	51.1	13.8	8.2	31.9
66	66	***************************************	52 to 55	18 to 25		20 to 80
Nickel	66	4	75 to 66	25 to 88		

A refined copper-nickel alloy containing 50% copper and 40% nickel, with very small amounts of iron, silicon and carbon, is produced direct from Bessemer matte in the Sudbury (Canada) Nickel Works. German silver manufacturers purchase a ready-made alloy, which melts at a low heat and requires simple addition of zinc, instead of buying the nickel and copper separately. This alloy, "50-50" as it is called, is almost indistinguishable from pure nickel. Its cost is less than nickel, its melting point much lower, it can be cast solid in any form desired, and furnishes a casting which works easily in the lathe or planer, yielding a silvery white surface unchanged by air or moisture. For bullet casings now used in various British and continental rifles, a special alloy of 80% copper and 20% nickel is made.

	Copper.	Nickel.	Zinc.	
Chinese packfong	40.4	31. A	6.5	parts.
" tutenag		8	6.5	- 44
German silver	2	1	1	**
" (cheaper)		2	8.5	44
" (closely resembles s	11). 8	8	8.5	66

ALLOYS OF BISMUTH.

By adding a small amount of bismuth to lead that metal may be hardened and toughened. An alloy consisting of three parts of lead and two of bismuth has ten times the hardness and twenty times the tenacity of lead. The alloys of bismuth with both tin and lead are extremely fusible, and take fine impressions of casts and moulds. An alloy of one part bismuth, two parts tin, and one part lead is used by pewter-workers as a soft solder, and by soap-makers for moulds. An alloy of five parts bismuth, two parts tin, and three parts lead melts at 199° F., and is somewhat used for stereotyping, and for metallic writing pencils. Thorpe gives the following proportions for the better-known fusible metals:

Name of Alloy.	Bismuth.	Lead.	Tin.	Cad- mium	Mer- cury.	Melting- point,
Newton's. Rose's. D'Arcet's. D'Arcet's with mercury. Wood's. Lipowitz's. Guthrie's "Entectic".	50 50 50 50 50	81.25 28.10 25.00 25.00 25.00 26.90 20.55	18.75 24.10 25.00 25.00 12.50 12.78 21.10	12.50 10.40		202° F. 203° '' 201° '' 118° '' 149° '' "Yery low.'

The action of heat upon some of these alloys is remarkable. Thus, Lipowitz's alloy, which solidifies at 149° Fah., contracts very rapidly at first, as it cools from this point. As the cooling goes on the contraction becomes slower and slower, until the temperature falls to 101.3° Fah. From this point the alloy expands as it cools, until the temperature falls to about 77° Fah., after which it again contracts, so that at 32° F. a bar of the alloy has the same length as at 115° F.

Alloys of bismuth have been used for making fusible plugs for boilers, but it is found that they are altered by the continued action of heat, so that one cannot rely upon them to melt at the proper temperature. Pure Banca tin

is used by the U.S. Government for fusible plugs.

FUSIBLE ALLOYS. (From various sources.)

Sir Isaac Newton's, bismuth 5, lead 3, tin 2, melts at	9190	T.
Rose's, bismuth 2, lead 1, tin 1, melts at		
Wood's, cadmium 1, bismuth 4, lead 2, tin 1, melts at	165	"
Guthrie's, cadmium 13.29, bismuth 47.88, lead 19.36, tin 19.97, melts at.	160	"
Lead 3, tin 5, bismuth 8, melts at	208	44
Lead 1, tin 8, bismuth 5, melts at	212	
Lead 1, tin 4, bismuth 5, melts at	240	"
Tin 1, bismuth 1, melts at	286	
Lead 2, tin 3, melts at		
Tin 2, bismuth 1, melts at	336	
Lead 1, tin 2, melts at	860	::
Tin 8, bismuth 1, melts at	392	
Lead 2, tin 1, melts at	4(0	
Lead 1, tin 1, melts at	400	44
Lead 1, tin 3, melts at	900	66
Tin 3, bismuth 1, melts at. Lead 1, bismuth 1, melts at	084	66
Lead 1, Tin 1, bismuth 4, melts at	901	"
Lead 5, tin 3, bismuth 8, melts at	909	66
Tin 3, bismuth 5, melts at.	202	"
THE O'S DISTRICTED OF THE CONTRACTOR OF THE CONT	~~~	

BEARING-METAL ALLOYS.

(C. B. Dudley, Jour. F. I., Feb. and March, 1892.)

Alloys are used as bearings in place of wrought iron, cast iron, or steel, partly because wear and friction are believed to be more rapid when two metals of the same kind work together, partly because the soft metals are more easily worked and got into proper shape, and partly because it is desirable to use a soft metal which will take the wear rather than a hard metal, which will wear the journal more rapidly.

A good bearing-metal must have five characteristics: (1) It must be strong

A good bearing-metal must have five characteristics: (1) It must be strong enough to carry the load without distortion. Pressures on car-journals frequently as high as 350 to 400 lbs. per square inch.

(2) A good bearing-metal should not heat readily. The old copperation hearing, made of seven parts copper to one part tin, is more apt to heat than some other alloys. In general, research seems to show that the harder the bearing-metal, the more likely it is to heat.

(3) Good bearing-metal should work well in the foundry. Oxidation while melting causes spongy castings. It can be prevented by a liberal use of powdered charcoal while melting. The addition of 1% to 2% of zinc or a small amount of phosphorus greatly aids in the production of sound castings. This is a principal element of value in phosphor-bronze.

(4) Good bearing-metals should show small friction. It is true that friction is almost wholly a question of the lubricant used; but the metal of the bearing has certainly some influence.

(5) Other things being equal, the best bearing-metal is that which wears slowest.

The principal constituents of bearing-metal alloys are copper, tin, lead, ginc, antimony, iron, and aluminum. The following table gives the constituents of most of the prominent bearing-metals as analyzed at the Pennsylvania Railroad laboratory at Altoona.

Analyses of Bearing-metal Alloys.

Metal.	Cop- per.	Tin.	Lead.	Zinc.	Anti- mony.	Iron.
Camelia metal	70.20					0.55
Anti-friction metal	1.60	98.13				trace
White metal	. 			• • • • • •		۱
Car-brass lining	. 	trace			15.10	
Salgee anti-friction	4.01	9.91		85.57		
Graphite bearing-metal		14.38				7 (1)
Antimonial lead			80.69		18.83	l
Carbon bronze		9.72			. 	(2)
Cornish bronze	77.83	9.60				trace(3)
Delta metal	92.39	2.37				0.07
*Magnolia metal	trace		83.55	trace	16.45	trace(4)
American anti-friction metal			78.44	0.98	19.60	0.65
Tobin bronze	59.00	2.16				
Graney bronze	75.80	9.20	15.06			
Damascus bronze	76.41	10.60		. 		
Manganese bronze	90.52	9.58			. 	(5)
Ajax metal	81.24	10.98				(6)
Anti-friction metal						l
Harrington bronze		0.97		42.67		0.68
Car-box metal					14.38	
Hard lead		1	94.40		6.03	.
Phosphor-bronze	79.17	10.22	9.61		l. .	(უ
Ex. B. metal		8.00	15.00			l (8)

Other constituents:

No graphite.
 Possible trace of carbon.

(3) Trace of phosphorus.(4) Possible trace of bismuth.

(5) No manganese.

(6) Phosphorus or arsenic, 0.37.

(7) Phosphorus, 0.94. (8) Phosphorus, 0.20.

*Dr. H. C. Torrey says this analysis is erroneous and that Magnolia metal always contains tin.

As an example of the influence of minute changes in an alloy, the Harrington bronze, which consists of a minute proportion of iron in a copperminc alloy, showed after rolling a tensile strength of 75,000 lbs. and 20% elongation in 2 inches.

In experimenting on this subject on the Pennsylvania Railroad, a certain number of the bearings were made of a standard bearing-metal, and the same number were made of the metal to be tested. These bearings were placed on opposite ends of the same axle, one side of the car having the standard bearings, the other the experimental. Before going into service the bearings were carefully weighed, and after a sufficient time they were

again weighed.

The standard bearing-metal used is the "S bearing-metal" of the Rhosphor-bronze Smelting Co. It contains about 79.70% copper, 9.50% lead, 19% tin, and 0.80% phosphorus. A large number of experiments have shown that the loss of weight of a bearing of this metal is 1 lb. to each 18,000 to 25,000 miles travelled. Besides the measurement of wear, observations were made on the frequency of "hot boxes" with the different metals. The results of the tests for wear, so far as given, are condensed into the

following table :

Metal.		Composition.						
Meual.	Copper.	Tin.	Lead.	Phos.	Arsenic. V	of Tear.		
Standard	79.70	10.00	9.50	0.80		100		
Copper-tin		12.50			•••••	148		
Copper-tin, secon						153		
Copper-tin, third	experiment,	same met	al			147		
Arsenic-bronze	89.20	10.00	•••	••••	0.80	142		
Arsenic-bronze	79.20	10.00	7.00		0.80	115		
Arsenic-bronze	79.70	10.00	9.50	****	0.80	101		
"K" bronze	77.00	10.50	12.50			92		
"K" bronze, seco	ond experim	ent. same	metal			92.7		
Alloy "B"		8.00	15.00	••••	••••	86.5		

The old copper-tin alloy of 7 to 1 has repeatedly proved its inferiority to the phosphor-bronze metal. Many more of the copper-tin bearings heated than of the phosphor-bronze. The showing of these tests was so satisfactory that phosphor-bronze was adopted as the standard bearing-metal of the Penusylvania R.R., and was used for a long time.

The experiments, however, were continued. It was found that arsenic practically takes the place of phosphorus in a copper-tin alloy, and three tests were made with arsenic bronzes as noted above. As the proportion to lead is increased to correspond with the standard, the durability increases as well. In view of these results the "K" bronze was tried, in which neither phosphorus nor arsenic were used, and in which the lead was increased above the proportion in the standard phosphor-bronze. The result was that the metal wore 7.30% slower than the phosphor-bronze. No trouble from heating was experienced with the "K" bronze more than with the standard. No trouble from

Dr. Dudley continues:

At about this time we began to find evidences that wear of bearing-metal alloys varied in accordance with the following law: "That alloy which has when the greatest power of distortion without rupture (resilience), will best resist wear." It was now attempted to design an alloy in accordance with this law, taking first the proportions of copper and tin, 9½ parts copper to 1 of tin was settled on by experiment as the standard, although some evidence since that time tends to show that 12 or possibly 15 parts copper to 1 of tin might have been better. The influence of lead on this copper tin alloy seems to be much the same as a still further diminution of the However than to be much the same as a still further diminution of tin. However, the tendency of the metal to yield under pressure increases as the amount of tin is diminished, and the amount of the lead increased, so a limit is set to the use of lead. A certain amount of tin is also necessary to keep the lead

the use of lead. A certain amount of tin is also necessary to keep the lead alloyed with the copper.

Bearings were cast of the metal noted in the table as alloy "B," and it wore 18.5% slower than the standard phosphor-bronze. This metal is now the standard bearing-metal of the Pennsylvania Railroad, being slightly changed in composition to allow the use of phosphor-bronze scrap. The formula adopted is: Copper, 105 lbs.; phosphor-bronze, 60 lbs.; tin, 9% lbs.; lead, 25% lbs. By using crdinary care in the foundry, keeping the metal well covered with charcoal during the melting, no trouble is found in casting good bearings with this metal. The copper and the phosphor-bronze can be put in the pot before putting it in the melting-hole. The tin and lead should be added after the pot is taken from the fire.

It is not known whether the use of a little zinc, or possibly some other

It is not known whether the use of a little zinc, or possibly some other combination, might not give still better results. For the present, however, this alloy is considered to fulfil the various conditions required for good bearing-metal better than any other alloy. The phosphor-bronze had an ultimate tensile strength of 80,000 lbs., with % elongation, whereas the alloy "B" had 24,000 lbs. tensile strength and 11% elongation.

White Metal for Engine Bearings. (Report of a British Naval Committee, Eng'g, July 18, 1902.)—For lining bearings, crankpin bushes, and other parts exclusive of cross-head bushes: Tin 12, copper 1, antimony 1. Melt 6 tin 1 copper, and 6 tin 1 antimony separately and mix the two together.

For cross head bushes a harder alloy, viz., 85% tin, 5% copper, 10% antimony, has given good results.

(For other bearing metals, see Alloys containing antimony, on next page.)

ALLOYS CONTAINING ANTIMONY.

VARIOUS ANALYSES OF BABBITT METAL AND OTHER ALLOYS CONTAINING ANTIMONY.

	Tin.	Copper	Antimony.	Zinc.	Lead.	Bismuth.
Babbitt metal	50	1	3 parts			
for light duty (:	=89.3	1.8	8.9 per ct.			
Harder Babbitt	96	4	8 parts			
	=88.9		7.4 per ct.			
Britannia	85.7		10.1	2.9		l .
"	81.9		16.2	1.9	. . 	 .
"	81.0		16.	1.		
"	70.5		25.5	• • • • <u>•</u> • • • • • •		
	22	10	62.	6. i		
"Babbitt"	45.5		13.	· • • • • • • • • • • • • • • • • • •	40.0	
Plate pewter	89.3		7.1			1.8
White metal	85	5	10.	Bearings	on Ger. lo	comotives.

* It is mixed as follows: Twelve parts of copper are first melted and then This mixed as follows: Twelve parts of copper are first melted and then 36 parts of tin are added; 24 parts of antimony are put in, and then 36 parts of tin, the temperature being lowered as soon as the copper is melted in order not to oxidize the tin and antimony, the surface of the bath being protected from contact with the air. The alloy thus made is subsequently remelted in the proportion of 50 parts of alloy to 100 tin. (Joshus Rose.)

White-metal Alloys.—The following alloys are used as lining metals by the Factor Religious of France (1990):

by the Eastern Railroad of France (1890):

Number.	Lead.	Antimony.	Tin.	Copper.
1	65	25	0	10
2	0	11.12	83.33	5.55
8		20	10	0
4		8	12	0

No. 1 is used for lining cross-head slides, rod-brasses and axle-bearings; No. 2 for lining axle-bearings and connecting-rod brasses of heavy engines; No. 8 for lining eccentric straps and for bronze slide-valves; and No. 4 for metallic rod-packing.

Some of the best-known white-metal alloys are the following (Circular of Hoveler & Dieckhaus, London, 1893):

	Tin.	Antimony.	Lead.	Copper.	Zinc.
1. Parsons'	86	1	2	- 2	27
2. Richards'	70	15	1016	416	0
8. Babbitt's	55	18	2312	312	0
4. Fentons'	16	0	0′~	5 ~	79
5. French Navy	716	Ò	7	7	8716
6. German Navy	85	716	Ò	716	o´-

"There are engineers who object to white metal containing lead or zinc. This is, however, a prejudice quite unfounded, inasmuch as lead and zinc often have properties of great use in white alloys." It is a further fact that an "easy liquid" alloy must not contain more than 18% of antimony, which is an invaluable ingredient of white metal for improving its hardness; but in no case must it exceed that margin, as this would reduce the plasticity of the compound and make it brittle.

Hardest alloy of tin and lead: 6 tin, 4 lead. Hardest of all tin alloys (?): 74 tin 18 antimony, 8 conver

tin, 18 antimony, 8 copper.

Alloy for thin open-work, ornamental castings: Lead 2, antimony 1. White metal for patterns: Lead 10, bismuth 6, antimony 2, common brass 8, tin 10.

Type-metal is made of various proportions of lead and antimony, from 17% to 20% antimony according to the hardness desired.

Babbitt Metals. (C. R. Tompkins, Mechanical News, Jan. 1891.)

The practice of lining journal-boxes with a metal that is sufficiently fusible to be melted in a common ladle is not always so much for the purpose of securing anti-friction properties as for the convenience and cheapness of forming a perfect bearing in line with the shaft without the necessity of boring them. Boxes that are bored, no matter how accurate, require great

boring them. Boxes that are borea, no matter now accurate, require greate are in fitting and attaching them to the frame or other parts of a machine. It is not good practice, however, to use the shaft for the purpose of casting the bearings, especially if the shaft be steel, for the reason that the hot metal is apt to spring it; the better plan is to use a mandrel of the same size or a trifle larger for this purpose. For slow-running journals, where the load is moderate, alm at any metal that may be conveniently melted. and will run free will answer the purpose. For wearing properties, with a moderate speed, there is probably nothing superior to pure zinc, but when not combined with some other metal it shrinks so much in cooling that it cannot be held firmly in the recess, and soon works loose; and it lacks those

anti-friction properties which are necessary in order to stand high speed.

For line-shafting, and all work where the speed is not over 300 or 400 r. pm., an alloy of 8 parts zinc and 2 parts block-tin will not only wear longer than any composition of this class, but will successfully resist the force of a heavy load. The tin counteracts the shrinkage, so that the metal, if not overheated, will firmly adhere to the box until it is worn out. But this mixture does not possess sufficient anti-friction properties to warrant its use

in fast-running journals.

Among all the soft metals in use there are none that possess greater anti-Allong an the soft means in use there are none that possess greater anti-friction properties than pure lead; but lead alone is impracticable, for it is so soft that it cannot be retained in the recess. But when by any process lead can be sufficiently hardened to be retained in the boxes without materially injuring its anti-friction properties, there is no metal that will wear longer in light feat-running journals. With most of the best and most popular anti-friction metals in use and sold under the name of the Babbitt metal,

the basis is lead.

Lead and antimony have the property of combining with each other in all proportions without impairing the anti-friction properties of either. The antimony hardens the lead, and when mixed in the proportion of 80 parts lead by weight with 20 parts antimony, no other known composition of metals possesses greater anti-friction or wearing properties, or will stand a higher speed without heat or abrasion. It runs free in its melted state, has no shrinkage, and is better adapted to light high-speeded machinery than any other known metal. Care, however, should be manifested in using it, and it should never be heated beyond a temperature that will scorch a dry pine stick.

Many different compositions are sold under the name of Babbitt metal. Some are good, but more are worthless; while but very little genuine Babbitt metal is sold that is made strictly according to the original formula. Most of the metals sold under that name are the refuse of type-foundries and other smelting-works, melted and cast into fancy ingots with special brands,

and sold under the name of Babbitt metal.

It is difficult at the present time to determine the exact formulas used by the original Babbitt, the inventor of the recessed box, as a number of differ. ent formulas are given for that composition. Tin, copper, and antimony were the ingredients, and from the best sources of information the original proportions were as follows:

Another writer gives:

50 parts tin =	=	89.3%	83.3%
2 parts copper =	=	8.6%	8.3%
A norte entimony	_	7 14	8 94

The copper was first melted, and the antimony added first and then about ten or fifteen pounds of tin, the whole kept at a dull-red heat and constantly ten or fifteen pounds of the, the whole kept at a dull-red heat and constantly stirred until the metals were thoroughly incorporated, after which the balance of the tin was added, and after being thoroughly stirred again it was then east into ingots. When the copper is thoroughly melted, and before the antimony is added, a handful of powdered charcoal should be thrown into the crucible to form a flux, in order to exclude the air and prevent the antimony from vaporizing; otherwise much of it will escape in the form of a vapor and consequently be wasted. This metal, when carefully prepared, is probably one of the best metals in use for lining boxes that are subjected to a heavy weight and wear; but for light fast running internals. subjected to a heavy weight and wear; but for light fast-running journals the copper renders it more susceptible to friction, and it is more liable theat than the metal composed of lead and antimony in the proportions just given.

SOLDERS.

Common solders, equal parts tin and lead; fine solder, 2 tin to 1 lead; chear solder, 2 lead, 1 tin.

Fusing-point of tin-lead alloys:

		25558° F.	Tin 11/4 to lead 1 834 F.
		10541	" 2 [~] " 1840
"1"		5511	48 44 44 1 856
"1"		3482	" 4 " " 1 365
" 1 "		2441	" 5 " " 1 878
"1"	**	1870	" 6 " " 1881

Common pewter contains 4 lead to 1 tin.

Common pewter contains 4 lead to 1 tin.
Gold solder: 14 parts gold, 6 silver, 4 copper.
Gold solder for 14-carat
gold: 25 parts gold, 25 silver, 12½ brass, 1 zinc.
Silver solder: Yellow brass 70 parts, zinc 7, tin 11½. Another: Silver 145
parts, brass (8 copper, 1 zinc) 73, zinc 4.
German-silver solder: Copper 88, zinc 54, nickel 8.
Variable solder: See and we have a solder.

Novel's solders for aluminum: Tin 100 parts, lead 5; " 100 " zinc 5; melts at 536° to 572° F. 586 to 612

" 1000 " " copper 10 to 15; 662 to 842 4 1000 66 nickel 10 to 15; Ģ 662 to 842

Novel's solder for aluminum bronze: Tin 900 parts, copper 100, bismuth 2 to 8. It is claimed that this solder is also suitable for joining aluminum to copper, brass, zinc, iron, or nickel.

ROPES AND CABLES.

STRENGTH OF ROPES.

(A. S. Newell & Co., Birkenhead. Klein's Translation of Weisbach, vol. iii. part 1, sec. 2.)

Hemp.		Iron.		St	eel.	
Girth.	Weight per Fathom.	Girth.	Weight per Fathom.	Girth.	Weight per Fathom.	Tensile Strength,
Inches.	Pounds.	Inches.	Pounds.	Inches.	Pounds.	Gross tons.
		11/4	11/6	1	1 1	8
894	4	196	214	11/6	134	5
416	5	1%	21/6	l .		6
51/6	7	21.6	81/6	156 154	21/6	5 6 7 8 9 10
		214	41/6		1	ğ
6	9	284	5	17/6	8	10
61/6	10	252	5½ 6	2	814	12 13
7	12	28/4	616	2 21/6 21/4	4	18 14
7	12	878	716	274	41/6	15
71/6	14	31/6	8	23%	5	16
8	16	81/4	716 8 816 9	91.2	514	17 18 20 22 24 26 28 30 33 86
_		818	10	252	51/6 6	20
81/6	18	853	11	994	63/6	22
914 10 11	22	872	19 18	81/4	8	26
10	26	1 4°	14	-/-	1	28
11	22 26 30	41/4	15	8%	9	80
	1	456	16	1		32
19	84	1 129	18 20	1 375.	10 12	86

Flat Ropes.

Hemp.		Iron	n.	St		
Girth.	Weight per Fathom.	Girth.	Weight. per Fathom.	Girth.	Weight per Fathom.	Tensile Strength.
Inches. 4 × 11/6 5 × 11/4 51/4 × 11/6 × 11/4 6 × 11/4 7 × 11/6 81/4 × 21/6	Pounds. 20 24 26 28 30 36 40 45 50	Inches. 2½ × ½ 2½ × ½ 2½ × ½ 8 × 56 8½ × 56 3½ × 56 3½ × 56	Pounds. 11 18 15 16 18 20 22	2 × 1/4 21/4 × 1/4 21/4 × 1/4 21/4 × 1/4	Pounds. 10 11 12 13	Gross tons, 20 23 27 28 32 36 40
812 × 214 9 × 214 914 × 234 10 × 214	55	4 × 11/16 414×34 416×34 456×34	22 25 28 32 34	294 × 96 8 × 94 814 × 96 816 × 96	15 16 18 20	45 50 56 60

Working Load, Diameter, and Weight of Ropes and Chains. (Klein's Weisbach, vol. iii, part 1, sec. 2, p. 561.)

Hemp ropes: d= diam. of rope. Wire rope: d= diam. of wire, n= number of wires, G= weight per running foot, k= permissible load in pounds per square inch of section, P= permissible load on rope or chain. Oval chains: d= diam of iron used; inside dimensions of oval 1.5d and 2.6d. Each link is a piece of chain 2.6d long. $G_0=$ weight of a single link = 2.10d9 lbs.; G= weight per running foot = 2.73d9 lbs.

	Hempen	Wire Rope.	
	Dry and Untarred. Wet or Tarred.		
k (lbs.) =	1420	1160	17000
d (ins.) =	0.03 √P	0.083 √P	$0.0087\sqrt{\frac{P}{n}}$
P (lbs.) = G (lbs.) =	$\begin{array}{c} 1120d^2 = 2855G \\ 1.28d^2 = 0.00085P \end{array}$	$\begin{array}{c} 916d^2 = 1975G \\ 1.54d^2 = 0.0005P \end{array}$	$\begin{array}{c} 13350nd^2 = 4590G \\ 2.91nd^2 = 0.000218P \end{array}$

	Open-link Chain.	Stud-link Chain.
k (lbs.) = d (ins.) = P (lbs.) = G (lbs.) =	$\begin{array}{c} 8500 \\ 0.0087 \sqrt{P} \\ 18350 d^2 = 1360 G \\ 9.73 d^2 = 0.000737 P \end{array}$	$ \begin{array}{c c} 11400 \\ 0.0076 \sqrt{P} \\ 17800d^2 = 1660G \\ 10.65d^2 = 0.0006P \end{array} $

Stud Chains 4/3 times as strong as open-link variety. [This is contrary to the statements of Capt. Beardslee, U. S. N., in the report of the U. S. Test Board. He holds that the open link is stronger than the studded link. See D. 308 antel.

STRENGTH AND WEIGHT OF WIRE ROPE, HEMPEN ROPE, AND CHAIN CABLES. (Klein's Weisbach.)

Breaking Load in tons of 2240 lbs.	Kind of Cable.	Girth of Wire Rope and of Hemp Rope Diameter of Iron of Chain, inches.	Weight of One Foot in length. Pounds.
1 Ton	Wire Rope	1.0	0.125
	Hemp Rope	2.0	0.177
	Chain	34	0.500
8 Tons	Wire Rope Hemp Rope Chain	2.0° 5.0 1/2 2.5°	0.488 0.978 2.667
12 Tons	Wire Rope	2.5	0.758
	Hemp Rope	7.0	2.036
	Chain	11/16	4.502
16 Tons,	Wire Rope	8.0	1.186
	Hemp Rope	8.0	2.865
	Chain	18/16	6.169
20 Tons	Wire Rope	8.5	1.546
	Hemp Rope	9.0	3.225
	Chain	29/32	7.674
24 Tons	Wire Rope	4.0	2,043
	Hemp Rope	10.0	4,166
	Chain	81/32	8,836
80 Tons	Wire Rope	4.5	2.725
	Hemp Rope	11.0	5.000
	Chain	1.1/16	10.385
86 Tons	Wire Rope	5.0	8.728
	Hemp Rope	12.5	5.940
	Chain	1.3/16	18.01
44 Tons	Wire Rope	5.5	4.50
	Hemp Rope	14.0	6.94
	Chain	1.5/16	16.00
54 Tons	Wire Rope	6.0	5.67
	Hemp Rope	15.0	7.92
	Chain	1.7/16	19.16

Length sufficient to provide the maximum working stress:

Hempen rope, dry and untarred wet or tarred	2855	feet.
Wire rope Open-link chain Stud chain	4590	44
Open-link chain	1360	46
Stud chain	1660	66

Sometimes, when the depths are very great, ropes are given approximately the form of a body of uniform strength, by making them of separate pieces, whose diameters diminish towards the lower end. It is evident that by this means the tensions in the fibres caused by the rope's own weight can be considerably diminished.

considerably diminished.

Rope for Hoisting or Transmission. Manila Rope
(C. W. Hunt Company, New York.)—Rope used for hoisting or for transmission of power is subjected to a very severe test. Ordinary rope chafes
and grinds to powder in the centre, while the exterior may look as though
it was little worn.

In bending a rope over a sheave, the strands and the yarns of these strands slide a small distance upon each other, causing friction, and wear the rope internally.

The "Stevedore" rope used by the C. W. Hunt Co. is made by lubricating the fibres with plumbago, mixed with sufficient tallow to hold it in position. This lubricates the yarns of the rope, and prevents internal chafing and wear. After running a short time the exterior of the rope gets compressed and coated with the lubricant.

In manufacturing rope, the fibres are first spun into a yarn, this yarn being twisted in a direction called "right hand." From 20 to 80 of these yarns, depending on the size of the rope, are then put together and twisted in the opposite direction, or "left hand," into a strand. Three of these

strands, for a 8-strand, or four for a 4-strand rope, are then twisted together, the twist being again in the "right hand" direction. When the strand is twisted, it untwists each of the threads, and when the threatstrands are twisted together into rope, it untwists the strands, but again twists up the threads. It is this opposite twist that keeps the rope in its proper form. When a weight is hung on the end of a rope, the tendency is for the rope to untwist, and become longer. In untwisting the rope, it would twist the threads up, and the weight will revolve until the strain of the untwisting strands just equals the strain of the threads being twisted tighter. In making a rope it is impossible to make these strains exactly balance each other. It is this fact that makes it necessary to take out the rurns" in a new rope, that is, untwist it when it is put at work. The proper twist that should be put in the threads has been ascertained approximately by experience. imately by experience.

The amount of work that the rope will do varies greatly. It depends not only on the quality of the fibre and the method of laying up the rope, but also on the kind of weather when the rope is used, the blocks or sheaves over which it is run, and the strain in proportion to the strain put upon the rope. The principal wear comes in practice from defective or badly set

sheaves, from excess of load and exposure to storms.

The loads put upon the rope should not exceed those given in the tables, for the most economical wear. The indications of excessive load will be the twist coming out of the rope, or one of the strands slipping out of its proper position. A certain amount of twist comes out in using it the first day or two, but after that the rope should remain substantially the same. If it does not, the load is too great for the durability of the rope. If the rope wears on the outside, and is good on the inside, it shows that it has been chafed in running over the pulleys or sheaves. If the blocks are very small, it will increase the sliding of the strands and threads, and result in a more rapid internal wear. Rope made for hoisting and for rope transmission is usually made with four strands, as experience has shown this to be the most serviceable.

The strength and weight of "stevedore" rope is estimated as follows:

Breaking strength in pounds = ?20 (circumference in inches)2; Weight in pounds per foot = .032 (circumference in inches)2.

The Technical Words relating to Cordage most frequently heard are:

YARN.—Fibres twisted together.

THREAD.—Two or more small yarns twisted together. STRING.—The same as a thread but a little larger yarns. STRAND.—Two or more large yarns twisted together. CORD.—Several threads twisted together. ROPE.—Several strands twisted together. HAWSER.-A rope of three strands. SHROUD-LAID .- A rope of four strands. CABLE -Three hawsers twisted together. YARNS are laid up left-handed into strands. STRANDS are laid up right-handed into rope.

HAWSERS are laid up left-handed into a cable. A rope is:

LAID by twisting strands together in making the rope.

SPLICED by joining to another rope by interweaving the strands.

WHIPPED.—By winding a string around the end to prevent untwisting. SERVED. -When covered by winding a yarn continuously and tightly around it.

PARCELED.—By wrapping with canvas.

PAYED.—When two parts are bound together by a yarn, thread or string.

PAYED.—When painted, tarred or greased to resist wet.

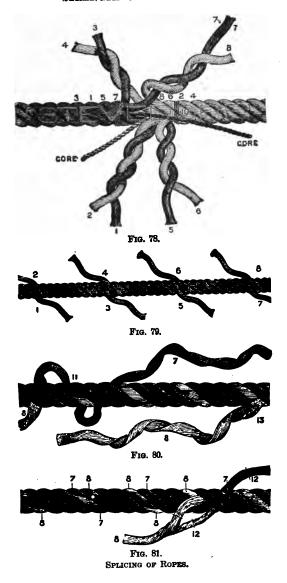
HAUL.—When painted, tailed of greated to tests now.

HAUL.—To pull on a rope.

TAUT.—Drawn tight or strained.

Splicing of Ropes.—The splice in a transmission rope is not only the weakest part of the rope but is the first part to fail when the rope is worn out. If the rope is larger at the splice, the projecting part will wear on the "Visual data was fail from the outling off of the strands. The following pulleys and the rope fail from the cutting off of the strands. The following directions are given for splicing a 4-strand rope.

The engravings show each successive operation in splicing a 1% inch manila rope. Each engraving was made from a full-size specimen.



Tie a piece of twine, 9 and 10, around the rope to be spliced, about 6 feet from each end. Then unlay the strands of each end back to the twine.

Butt the ropes together and twist each corresponding pair of strands loosely, to keep them from being tangled, as shown in Fig. 78.

The twine 10 is now cut, and the strand 8 unlaid and strand 7 carefully laid

in its place for a distance of four and a half feet from the junction

The strand 6 is next unlaid about one and a half feet and strand 5 laid in

its place. The ends of the cores are now cut off so they just meet.

Unlay strand 1 four and a half feet, laying strand 2 in its place. Unlay strand 3 one and a half feet, laying in strand 4.

Cut all the strands off to a length of about twenty inches, for convenience in manipulation.

The rope now assumes the form shown in Fig. 79 with the meeting points of the strands three feet apart.

Each pair of strands is successively subjected to the following operation: From the point of meeting of the strands 8 and 7, unlay each one three turns; split both the strand 8 and the strand 7 in halves as far back as they are now unlaid and "whip" the end of each half strand with a small piece of twine.

The half of the strand 7 is now laid in three turns and the half of 8 also laid in three turns. The half strands now meet and are tied in a simple

laid in three turns. The name strangs now meet and are used in a simple knot, 11, Fig. 80, making the rope at this point its original size.

The rope is now opened with a marlin spike and the half strand of 7 worked around the half strand of 8 by passing the end of the half strand of 7 through the rope, as shown in the engraving, drawn taut and again worked around this half strand until it reaches the half strand 13 that was not laid in. This half strand 13 is now split, and the half strand 7 drawn through the opening thus made, and then tucked under the two adjacent strands, as shown in Fig. 81. The other half of the strand 8 is now wound around the other half strand 7 in the same manner. After each pair of strands has been treated in this manner, the ends are cut off at 12, leaving them about four inches long. After a few days' wear they will draw into the body of the rope or wear off, so that the locality of the splice can scarcely be detected.

Coal Hoisting. (C. W. Hunt Co.).—The amount of coal that can be

hoisted with a rope varies greatly. Under the ordinary conditions of use a rope hoists from 5000 to 8000 tons. Where the circumstances are more favorable, the amounts run up frequently to 12,000 or 15,000 tons, occasionally to 20,000 and in one case 32,400 tons to a single fall.

When a hoisting rope is first put in use, it is likely from the strain put upon it to twist up when the block is loosened from the tub. This occurs in the first day or two only. The rop "turns" taken out of the rope. no further trouble until worn out. The rope should then be taken down and the erope. When put up again the rope should give

It is necessary that the rope should be much larger than is needed to bear

the strain from the load.

Practical experience for many years has substantially settled the most economical size of rope to be used which is given in the table below.

Hoisting ropes are not spliced, as it is difficult to make a splice that will

not pull out while running over the sheaves, and the increased wear to be

obtained in this way is very small.

Coal is usually hoisted with what is commonly called a "double whip;" that is, with a running block that is attached to the tub which reduces the strain on the rope to approximately one half the weight of the load hoisted. The following table gives the usual sizes of hoisting rope and the proper working strain:

Stevedore Hoisting-rope.

C. W. Hunt Co.

Circumference of the rope in ins.	Proper Working Strain on the Rope in lbs.	Nominal size of Coal tubs. Double whip.	Approximate Weight of a Coil, in lbs.
8	850	1/6 to 1/5 tons.	860
81/4 4	500 650	14 " 12 "	480 650
41/6	800	13 " 14 "	830
Hoisting rope is o	l 1000 ordered by circumfer	94 1	960 rope by diameter

Weight and Strength of Manila Rope.

Spencer Miller (Eng'g News, Dec. 6, 1890) gives a table of breaking strength of manila rope, which he considers more reliable than the strength computed by Mr. Hunt's formula: Breaking strength=720×(circumference in inches)². Mr. Miller's formula is: Breaking weight lbs. = circumference²×a coefficient which varies from 900 for ½" to 700 for 2" diameter rope, as below:

Circumference ... 11/2 2 21/4 23/4 3 31/4 33/4 41/4 41/4 5 51/4 Coefficient 900 845 820 790 780 765 760 745 735 725 712

The following table gives the breaking strength of manila rope as calculated by Mr. Hunt's formula, and also by Mr. Miller's, using in the latter the coefficient 900 for sizes below 114 in. circumference and 700 for sizes above 6 in. The differences between the figures for any given size are probably not greater than the difference in actual strength of samples from different makers. Both sets of figures are considerably lower than those given in tables published by some makers of rope, but they are believed to be more reliable. The figures for weight per 100 ft. are from manufacturers' tables.

Diameter in inches.	Circumfer- ence in inches.	ght of 0 Feet Rope 1bs.	Stren	mate gth of in lbs.	Diameter in inches.	Circumfer- ence in inches.	ght of Feet Rope Ibs.	Ultimate Strength of Rope in lbs.	
Dia. ip	Signal Brig	Wei 10 in	Hunt.	Miller.	Diar	S a a	Weigh 100 of in It	Hunt.	Miller.
3/16 5/16 7/16 9/16 9/16 9/16 13/1; 78 1 1/16 11/4	9/16 9/4 1 11/4 11/4 11/4 11/4 21/4 21/4 21/4 21/4 21/4 31/4 31/4 31/4 31/4	2 3 4 5 6 776 11 1916 1820 2375 2815 3835 38	290 400 630 900 1,240 1,620 2,050 2,880 3,610 4,500 5,440 7,600 8,820 10,120	280 500 790 1,140 1,550 2,020 2,480 3,380 4,150 5,030 5,970 7,020 8,160 9,870 10,690	1 5/16 13/6 13/6 11/9/16 11/9/16 13/4 21/6 21/4 21/6 21/6 33/6 33/4	4 414 414 414 5 5 6 6 6 7 7 14 8 8 8 9 9 9 10	52 58 65 721/2 80 97 113 133 153 153 184 211 227 262 298 325	11,500 13,000 14,600 16,200 18,000 21,800 25,900 35,300 40,500 46,100 58,300 65,000 72,000	12,000 13,500 14,900 16,500 18,100 21,500 25,200 29,600 39,400 44,800 50,600 63,200 70,000

For rope-driving Mr. Hunt recommends that the working strain should not exceed 1/20 of the ultimate breaking strain. For further data on ropes see "Rope-driving."

Knots.-A great number of knots have been devised of which a few only are illustrated, but those selected are the most frequently used. In the cuts, Fig. 82, they are shown open, or before being drawn taut, in order to show the position of the parts. The names usually given to them are:

- Bight of a rope.
- B. Simple or Overhand knot.
- č. Figure 8 knot.
- Double knot.
- Ď. F. G. Boat knot.
- Bowline, first step.
- Bowline, second step. Bowline completed.
- H. I. J.
 - Square or reef knot. Sheet bend or weaver's knot.
- Sheet bend with a toggle.
- K. L. Carrick bend.
- M. N. Stevedore knot completed.
 - Stevedore knot commenced.
- Slip knot.

- Flemish loop.
- Q. R. Chain knot with toggle.
- Half-hitch.
- Timber-hitch.
- Clove hitch.
- U. Rolling-hitch.
- Timber-hitch and half-hitch.
- Blackwall-hitch.
- V. W. X. Y. Z. Fisherman's bend.
- Round turn and half-hitch.
- Wall knot commenced. " completed.
- AA.
- Wall knot crown commenced. BB.
- completed.

The principle of a knot is that no two parts, which would move in the same direction if the rope were to slip, should lay along side of and touching each other.

The bowline is one of the most useful knots, it will not slip, and after being strained is easily untied. Commence by making a bight in the rope, then put the end through the bight and under the standing part as shown in G. then pass the end again through the bight, and haul tight.

The square or reef knot must not be mistaken for the "granny" knot that slips under a strain. Knots H. K and M are easily untied after being under strain. The knot M is useful when the rope passes through an eye and is held by the knot, as it will not slip and is easily untied after being strained.

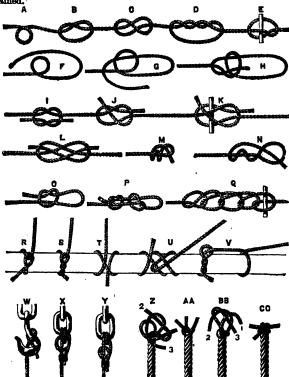


Fig. 82,-Knots.

The timber hitch S looks as though it would give way, but it will not; the greater the strain the tighter it will hold. The wall knot looks complicated, but is easily made by proceeding as follows: Form a bight with strand 1 and pass the strand 2 around the end of it, and the strand 3 round the end of 2 and then through the bight of 1 as shown in the cut Z. Haul the ends taut when the appearance is as shown in AA. The end of the strand 1 is now laid over the centre of the knot, strand 2 laid over 1 and 3 over 2, when the end of 3 is passed through the bight of 1 as shown in BB. Haul all the strands taut as shown in CG.

To Splice a Wire Rope.—The tools required will be a small marline spike, nipping cutters, and either clamps or a small hemp-rope sling with which to wrap around and untwist the rope. If a bench-vise is accessible it will be found convenient.

In splicing rope, a certain length is used up in making the splice. An allowance of not less than 16 feet for 1/2 inch rope, and proportionately longer for larger sizes, must be added to the length of an endless rope in

ordering.

Having measured, carefully, the length the rope should be after splicing, and marked the points M and M', Fig. 83, unlay the strands from each end E and E' to M and M' and cut off the centre at M and M', and then:

end E and E to M and M and cut off the centre at M and M, and then:

(1). Interlock the six unlaid strands of each end alternately and draw
them together so that the points M and M meet, as in Fig. 84.

(2). Unlay a strand from one end, and following the unlay closely, lay into
the seam or groove it opens, the strand opposite it belonging to the other
end of the rope, until within a length equal to three or four times the length
of one lay of the rope, and cut the other strand to about the same length
from the point of meeting as at 4, Fig. 85.

(3). Unlay the adjacent strand in the opposite direction, and following the
unlay closely lay in its place the corresponding opposite strand, cutting the

unlay closely, lay in its place the corresponding opposite strand, cutting the ends as described before at B, Fig. 85.

There are now four strands laid in place terminating at A and B, with the eight remaining at MM', as in Fig. 85.

It will be well after laying each pair of strands to tie them temporarily at

the points A and B. Pursue the same course with the remaining four pairs of opposite strands,

F1G. 88. F1G. 84. Fig. 85. Fig. 86. Fig. 87.

SPLICING WIRE ROPE. stopping each pair about eight or ten turns of the rope short of the preceding pair, and cutting the ends as before.

We now have all the strands laid in their proper places with their respect-

ive ends passing each other, as in Fig. 86.
All methods of rope-splicing are identical to this point; their variety consists in the method of tucking the ends. The one given below is the one

most generally practiced.

Clamp the rope either in a vise at a point to the left of A, Fig. 86, and by a champ the rope either in a vise at a point to the left of A, Fig. 30, and by and-clamp applied near A, open up the rope by untwisting sufficiently to cut the core at A, and seizing it with the nippers, let an assistant draw it out slowly, you following it closely, crowding the strand in its place until it is all laid in. Cut the core where the strand ends, and push the end back into its place. Remove the clamps and let the rope close together around it. Draw out the core in the opposite direction and lay the other strand in the centre of the rope, in the same manner. Repeat the operation at the five remaining points, and hammer the rope lightly at the points where the ends pass each other at A, A, B, B, etc., with small wooden mallets, and the splice is complete, as shown in Fig. 87.

If a clamp and vise are not obtainable, two rope slings and short wooden

levers may be used to untwist and open up the rope. A rope spliced as above will be nearly as strong as the original rope and smooth everywhere. After running a few days, the splice, if well made, cannot be found except by close examination.

The above instructions have been adopted by the leading rope manufac-

turers of America.

SPRINGS.

Definitions.—A spiral spring is one which is wound around a fixed point or centre, and continually receding from it like a watch spring. A helical spring is one which is wound around an arbor, and at the same time advancing like the thread of a screw. An elliptical or laminated spring is made of flat bars, plates, or "leaves," of regularly varying lengths, superposed one upon the total Sections.

Laminated Steel Springs.—Clark (Rules, Tables and Data) gives the following from his work on Railway Machinery, 1855:

$$\Delta = \frac{1.66L^8}{bt^2n};$$
 $s = \frac{bt^2n}{11.3L};$ $n = \frac{1.66L^8}{\Delta bt^8};$

 Δ = elasticity, or deflection, in sixteenths of an inch per ton of load, s = working strength, or load, in tons (2240 lbs.), L = span, when loaded, in inches, b = breadth of plates, in inches, taken as uniform, t = thickness of plates, in sixteenths of an inch, t = number of plates.

Note.-The span and the elasticity are those due to the spring when weighted.

weighted.

2 When extra thick back and short plates are used, they must be replaced by an equivalent number of plates of the ruling thickness, prior to the employment of the first two formulæ. This is found by multiplying the number of extra thick plates by the cube of their thickness, and dividing by the cube of the ruling thickness. Conversely, the number of plates of the ruling thickness given by the third formula, required to be deducted and replaced by a given number of extra thick plates, are found by the same calculation.

3. It is assumed that the plates are similarly and regularly formed, and that they are of uniform breadth, and but slightly taper at the ends. Reuleaux's Constructor gives for semi-elliptic springs:

$$P = \frac{8nbh^2}{6l} \quad \text{and} \quad f = \frac{6Pl^2}{Enbh^3};$$

 $S = \max$. direct fibre-strain in plate;

b = width of plates; n =number of plates in spring; h = thickness of plates;

l =one half length of spring; P =load on one end of spring; f = deflection of end of spring; E = modulus of direct elasticity.

The above formula for deflection can be relied upon where all the plates of the spring are regularly shortened; but in semi-elliptic springs, as used, there are generally several plates extending the full length of the spring, and the proportion of these long plates to the whole number is usually about one fourth. In such cases $f = \frac{5.5P!^3}{1.5P!^3}$ (G. R. Henderson, Trans. A. S. M. E.

one fourth. In such cases $f = \frac{5.5Ft^2}{Enbh^2}$ (G. R. Henderson, Trans. A. S. M. E.,

vol. xvi.) In order to compare the formulæ of Reuleaux and Clark we may make the following substitutions in the latter: s in tons = P in lbs. + 1120; Δs = 16f: L = 2i: t = 16h; then

$$\Delta s = 16f = \frac{1.66 \times 8l^3 \times P}{4096 \times 1120 \times nbh^3}, \text{ whence } f = \frac{Pl^3}{5,527,133},$$

which corresponds with Reuleaux's formula for deflection if in the latter we take E = 83,162,800.

Also
$$s = \frac{P}{1120} = \frac{256nbh^2}{11.3 \times 2l}$$
, whence $P = \frac{12,687nbh^2}{l}$,

which corresponds with Reuleaux's formula for working load when S in the

latter is taken at 76,120.

The value of E is usually taken at 30,000,000 and S at 80,000, in which case Reuleaux's formulæ become

$$P = \frac{13,333nbh^2}{l}$$
 and $f = \frac{Pl^2}{5,000,000nbh^2}$

Helical Steel Springs.—Clark quotes the following from the report on Safety Valves (Trans. Inst. Engrs. and Shipbuilders in Scotland, 1874-5):

$$E = \frac{d^3 \times w}{D^4 \times C}.$$

E =compression or extension of one coil in inches,

d = diameter from centre to centre of steel bar constituting the spring, in inches.

w =weight applied, in pounds,

D = diameter, or side of the square, of the steel bar, in sixteenths of an

C = a constant, which may be taken as 22 for round steel and 30 for square steel.

Norm.—The deflection E for one coil is to be multiplied by the number of

free coils, to obtain the total deflection for a given spring.

The relation between the safe load, size of steel, and diameter of coil, may be taken for practical purposes as follows:

$$D = \sqrt[3]{\frac{vol}{8}}, \text{ for round steel;}$$

$$D = \sqrt[3]{\frac{vol}{4.29}}, \text{ for square steel.}$$

Rankine's Machinery and Millwork, p. 390, gives the following:

$$\frac{W}{\Psi} = \frac{ed^4}{64nr^3}; \quad W_1 = \frac{.196/d^2}{r}; \quad v_1 = \frac{12.566n/r^2}{cd};$$

$$\frac{W_1}{2} = \text{greatest safe sudden load.}$$

In which d is the diameter of wire in inches; c a co-efficient of transverse elasticity of wire, say 10,500,000 to 12,000,000 for charcoal iron wire and steel; r radius to centre of wire in coll; n effective number of colls; f greatest safe shearing stress, say 30,000; W any load not exceeding greatest safe load; v corresponding extension or compression; W_1 greatest safe load; and v_1

v corresponding extension or compression: W_1 greatest safe load; and v_1 greatest safe steady extension or compression. If the wire is square, of the dimensions $d \times d$, the load for a given deflection is greater than for a round wire of the diameter d in the ratio of 2.81 to 1.96 or of 1.43 to 1, or of 10 to 7, nearly. Wilson Hartnell (Proc. Inst. M. E., 1882, p. 426), says: The size of a spiral spring may be calculated from the formula on page 304 of "Rankine's Useful Rules and Tables"; but the experience with Salter's springs has shown that the safe limit of stress is more than twice as great as there given, namely 60,000 to 70,000 lbs. per square inch of section with $\frac{1}{2}$ inch wire, and about 50,000 with $\frac{1}{2}$ inch wire. Hence the work that can be done by springs of wire is four or five times as great as Rankine allows.

For % inch wire and under,

Maximum load in lbs. =
$$\frac{12,000 \times (\text{diam. of wire})^3}{\text{Mean radius of springs}}$$
;

Weight in lbs. to deflect spring 1 in. =
$$\frac{180,000 \times (diam.)^4}{Number of coils \times (rad.)^4}$$
.

The work in foot-pounds that can be stored up in a spiral spring would lift it above 50 ft.

In a few rough experiments made with Salter's springs the coefficient of rigidity was noticed to be 12.600,000 to 13.700,000 with ½ luch wire; 11,000,000 for 11/32 inch; and 10,600,000 to 10,900,000 for 36 inch wire.

Helical Springs.—J. Begtrup, in the American Machinist of Aug. 18, 1892, gives formulas for the deflection and carrying capacity of helical springs of cound and course the low follows:

springs of round and square steel, as follow:

$$W = .3927 \frac{Sd^3}{D - d'}$$

$$E' = 8 \frac{P(D - d)^3}{Ed^4},$$
for round steel,
$$W = .471 \frac{Sd^3}{D - d},$$

$$F = 4.712 \frac{P(D - d)^3}{E^{3/4}},$$
for square steel.

F = carrying capacity in pounds, S = greatest tensile stress per square inch of material, d = diameter of steel,

D = outside diameter of coil

F = deflection of one coil,

E = torsional modulus of elasticity.

P = load in pounds.

From these formulas the following table has been calculated by Mr. Begtrup. A spring being made of an elastic material, and of such shape as to allow a great amount of deflection, will not be affected by sudden shocks or blows to the same extent as a rigid body, and a factor of safety very much less than for rigid constructions may be used.

HOW TO USE THE TABLE.

When designing a spring for continuous work, as a car spring, use a greater factor of safety than in the table; for intermittent working, as in a steam-engine governor or safety valve, use figures given in table; for square steel multiply line W by 1.2 and line F by .59.

Example 1.—How much will a spring of \$6" round steel and 3" outside diameter carry with safety? In the line headed D we find 3, and right underneath 473, which is the weight it will carry with safety. How many coils must this spring have so as to deflect \$" with a load of 400 pounds? Assuming a madulus of elegibity of 13 millions we find in the entry line and must this spring have so as to deflect 8" with a load of 400 pounds? Assuming a modulus of elasticity of 12 millions we find in the centre line headed F the figure .0610; this is deflection of one coil for a load of 100 pounds; therefore .061 \times 4 = .344" is deflection of one coil for 400 pounds load, and 3 + .244 = 12½ is the number of coils wanted. This spring will therefore be 43" long when closed, counting working coils only, and stretch to 734". Example 2.—A spring 334" outside diameter of 7,16" steel is wound close; how much can it be extended without exceeding the limit of safety? We find maximum safe load for this spring to be 709 pounds, and deflection of one coil for 100 pounds load .0405 inches; therefore 7.02 \times .0405 = .384" is the greatest admissible opening between coils. We may thus, without knowing the load, ascertain whether a spring is overloaded or not.

Carrying Capacity and Deflection of Helical Springs of Round Steel.

d = diameter of steel. D = outside diameter of coil. W = safe workingload in pounds—tensile stress not exceeding 60,000 pounds per square inch. F = deflection by a load of 100 pounds of one coil, and a modulus of elasticity of 10, 12 and 14 millions respectively. The ultimate carrying capacity will be about twice the safe load.

065′, 16.	D W	.25 85	.50 15	.75	1.00	1.25	1.50 4.5	1.78 8.8	2.00 3.8			
g No.	F	.0276	.3588 .3075	1.483 1.228	8.562 8.053	7.950 6.914	19.88 11.04	90.85 17.87	81.57 27.06			
	$\frac{1}{D}$.0197	.2562 .75	1.023	2.544 1.25	5.178 1.50	9.200	2.00	22.55 2.25	8.50		_
= .120'	W F	.0206 .0176	.0987 .0904	.2556 .2191	.5412 .4639	.9856 .8448	25 1.624 1.892	22 2.492 2.136	19 8.625 8.107			
N.S.	- 1	.0147	.0670	.182	.8866	.7040	1.160	1.780	2.589	8.612		
= .180" No. 7.	D W	75 941 .0187	1.00 167 .0408	1.25 198 .0907	1.50 104 .1703	1.75 88 .9866	2.00 75 .4466	9.25 66 .6571	2.50 59 .9249	9.75 58 1.956	3.00 49 1.660	
E Z	₽┤	.0118 .0098	.0950 .0992	.0778 .0648	.1460 .1917	.9457 .9048	.8828 .8190	.5632 .4693	.7928	1.077 .8075	1.428	
***	$\frac{D}{W}$	1.25 \$68	1.50 294	1.75 245	2,00 210	2.25 184	2.50 164	2.75 147	8.00 134	8.25 123	3.50 113	
E E	F	.0199 .0171 .0142	.0389 .0333 .0278	.0672 .0576 .0480	.1067 .0914 .0762	.1593 .1365 .1187	.2270 .1944 .1610	.3109 .2665 .2221	.3548	.5875 .4607 .3889	.5859	

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Carrying Capacity and Deflection of Helical Springs of Round Steel.—(Continued).

					~					_		
a = 5/16"	$F_{\{F\}}$	1.50 605 .0136 .0117 .0097	1.75 500 .0242 .0207 .0173	2.00 426 .0392 .0386 .0280	2.25 871 .0593 .0508 .0424	2.50 329 .0854 .0732 .0610	2.75 295 .1187 .1012 .0853	3.00 267 .1583 .1857 .1181	3.25 245 .2066 .1771 .1476	8.50 226 .2640 .2263 .1886	3.75 209 .3312 .2839 .2366	4.00 195 .4089 .3505 .2921
d = 36"	$F \left\{ egin{array}{l} D \\ W \\ F \end{array} ight.$	2.00 765 .0169 .0145 .0120	2.25 663 .0259 .0222 .0185	2.50 589 .0377 .0323 .0269	2.75 528 .0528 .0452 .0376	3.00 473 .0711 .0610 .0508	3.25 433 .0935 .0801 .0668	3.50 398 .1200 .1029 .0858	3.75 368 .1513 .1297 .1081	4.00 843 .1874 .1606 .1338	4.25 321 .2290 .1963 .1635	4.50 801 .2761 .2367 .1972
d = 7/16''	$F \left\{ egin{array}{c} D \\ W \\ F \left\{ ight. \end{array} ight.$	2.00 1263 .0081 .0069 .0058	2.25 1089 .0126 .0108 .0090	2.50 957 .0186 .0160 .0133	2.75 853 .0262 .0225 .0187	8.00 770 .0357 .0306 .0255	8.25 702 .0472 .0405 .0837	8.50 644 .0617 .0529 .0441	3.75 596 .0772 .0661 .0551	4.00 544 .0960 .0823 .0686	4.50 486 .1423 .1220 .1017	5.00 432 .2016 1728 .1440
d = 1/8"	F	2.00 1963 .0042 .0036 .0030	2.25 1688 .0067 .0057 .0048	2.50 1472 .0099 .0085 .0071	2.75 1309 .0141 .0121 .0101	8.00 1178 .0194 .0167 .0139	3.25 1071 .0259 .0222 .0185	3.50 982 .0336 .0288 .0240	3.75 906 .0427 .0366 .0305	4.00 841 .0534 .0457 .0381	4.50 735 .0796 .0683 .0569	5.00 654 .1134 .0973 .0810
d = 9/16"	F	2.50 2163 .0056 .0048 .0040	2.75 1916 .0081 .0070 .0058	3.00 1720 .0112 .0096 .0080	8.25 1560 .0151 .0129 .0108	3.50 1427 .0197 .0169 .0141	8.75 1815 .0252 .0216 .0180	4.00 1220 .0316 .0271 .0225	4.25 1137 .0390 .0334 .0278	4.50 1065 .0474 .0406 .0839	5.00 945 .0679 .0582 .0485	5.50 849 .0035 .0801 .0668
',% = p	F	2.50 8068 .0034 .0029 .0024	2.75 2707 .0049 .0042 .0035	3.00 2422 .0068 .0058 .0049	3.25 2191 .0092 .0079 .0066	3.50 2001 .0121 .0104 .0086	8.75 1841 .0155 .0133 .0111	4.00 1704 .0196 .0168 .0140	4.25 1587 .0243 .0208 .0173	4.50 1484 .0297 .0254 .0212	5.00 1815 .0427 .0866 .0305	5.50 1180 .0591 .0506 .0422
d = 11/16"	$F_{\{F\}}$	3.00 8311 .0043 .0037 .0030	3.25 2988 .0058 .0050 .0042	8.50 2723 .0077 .0066 .0055	8.75 2500 .0100 .0086 .0071	4.00 2311 .0127 .0108 .0090	4.25 2151 .0157 .0185 .0112	4.50 2009 .0193 .0165 .0138	4.75 1885 .0233 .0200 .0167	5.00 1776 .0279 .0239 .0199	5.50 1591 .0%88 .0833 .0277	6.00 1441 .0522 .0447 .0373
d = 3%"	$F \left\{ egin{array}{c} D \ W \ F \end{array} ight.$	8.00 4418 .0028 .0024 .0020	8.25 8976 .0088 0033 .0027	8.50 8615 .0051 .0044 .0086	3.75 8318 .0066 .0057 .0047	4.00 3058 .0084 .0072 .0060	4.25 2840 .0105 .0090 .0075	4.50 2651 .0129 .0111 .0093	4.75 2485 .0157 .0185 .0113	5.00 2339 .0189 .0162 .0135	5.50 2093 .0264 .0226 .0188	6.00 1898 .0356 .0305 .0254
d = 76"	$F \left\{ egin{array}{c} D \ W \ F \left\{ ight. \end{array} ight.$	8.50 6013 .0021 .0018 .0015	8.75 5490 .0027 .0024 .0020	4.00 5051 .0035 .0030 .0025	4.25 4676 .0045 .0038 .0032	4.50 4854 .0055 .0047 .0089	4.75 4073 .0067 .0058 .0048	5.00 3826 .0081 .0070 .0058	5.25 3607 .0097 .0083 .0069	5.50 3413 .0115 .0098 .0082	6.00 8080 .0156 .0184 .0112	6.50 2806 .0207 .0177 .0148
d = 1"	$F_{\mathbf{F}}^{D}$	8.50 9425 .0012 .0010 .0008	8.75 8568 .0016 .0014 .0011	4.00 7854 .0021 .0018 .0015	4.25 7250 .0026 .0023 .0019	4.50 6732 .0033 .0028 .0023	4.75 6283 .0041 .0085 .0029	5.00 5890 .0049 .0043 .0085	.0051	5.50 5286 .0071 .0061 .0051	6.00 4712 .0097 .0088 .0069	6.50 4284 .0129 .0111 .0092

The formulæ for deflection or compression given by Clark, Hartnell, and Begtrup, although very different in form, show a substantial agreement when reduced to the same form. Let d= diameter of wire in inches, $D_1=$ mean diameter of coil, n the number of coils, w the applied weight in pounds, and C a coefficient, then

Compression or extension of one coil = $\frac{wD_1^3}{Cd^4}$;

Weight in pounds to cause comp. or ext. of 1 in. = $\frac{Cd^4}{mD^{\frac{3}{2}}}$.

The coefficient C reduced from Hartnell's formula is $8\times180,000=1,440,000$; according to Clark, $16^4\times2^2=1,441,79^2$, and according to Begtrup (using 12,000,000 for the torsional modulus of elasticity) = 12,000,000 + 8 = 1,500,000.

Rankine's formula for greatest safe extension, $v_1 = \frac{12,566n/r^2}{may}$ may take

the form $v_1 = \frac{.7854nD_1^2}{100d}$ if we use 30,000 and 12,000,000 as the values for f and c respectively.

The several formulæ for safe load given above may be thus compared letting d= diameter of wire, and $D_1=$ mean diameter of coil, Ranking. $W=\frac{.196fd^3}{r}$; Clark, $W=\frac{8(d\times 16)^3}{D_1}$; Begtrup, $W=\frac{.39278d^3}{D_1}$; Hartnell

 $W = \frac{12000a^3}{a}$. Substituting for f the value 30,000 given by Rankine, and for S, 60,000 as given by Begtrup, we have $W = 11,760 \frac{d^3}{D}$ Rankine; 12,298 $\frac{d^3}{D}$

Clark; 23,562 $\frac{d^3}{D_1}$ Begtrup; 24,000 $\frac{d^3}{D_1}$ Hartnell.

Taking from the Pennsylvania Railroad specifications the capacity when closed of the following springs, in which d = diameter of wire, D diameter outside of coil. $D_1 = D - d$, c capacity, H height when free, and h height when closed, all in inches.

and substituting the values of c in the formula $c = W = x \frac{d^3}{D}$ we find x, the

coefficient of $\frac{d^3}{D}$ to be respectively 32,000; 38,000; 32,400; 24,888; 34,560; 42,140, average 34,000.

Taking 12,000 as the coefficient of $\frac{d^3}{D_1}$ according to Rankine and Clark for safe load, and 24,000 as the coefficient according to Begtrup and Hartnell, we have for the safe load on these springs, as we take one or the other coefficient.

5,400 lbs. 10,800 " Rankine and Clark...... 150 600 1,012 300 1.200 2,021 7.500 Capacity when closed, as above 400 1,900 2,100 8,100 10,000

J. W. Cloud (Trans. A. S. M. E., v. 173) gives the following:

$$P = \frac{S\pi d^3}{16R}$$
 and $f = \frac{32PR^2l}{G\pi d^4}$;

P = load on spring;

 $S = \max \lim shearing fibre-strain in bar;$ $d = \operatorname{diameter} of sieel of which spring is made;$

R = radius of centre of coil;
 l = length of bar before coiling;
 G = modulus of shearing elasticity;

f =deflection of spring under load.

Mr. Cloud takes S = 80,000 and G = 12,600,000. The stress in a helical spring is almost wholly one of torsion. For method of deriving the formulæ for springs from torsional formula see Mr. Cloud's paper, above quoted.

ELLIPTICAL SPBINGS, SIZES, AND PROOF TESTS.

Pennsylvania Railroad Specifications, 1896.

	betw'n	er all		Tests.					
Class.	Length betwo	Width over inches.	Plates. No. Size, in.	Ins. (a)	high.	lbs.	Ins.	lbs.	e p.t. (a) ine.
E 1, Triple E 2, Quadruple £ 3, Triple E 4, Single + E 5, " † E 6. " † E 7, Triple E 8, Double E 11, " E 12, " E 13, Double E 14, " E 15, Quadruple E 16, Guadruple E 17, Double E 19, Bingle † E 19, Double E 20, " E 21, "	36 40 40 42 36 82 36 40 40 84 30 40	1134 1534 1134 1134 1134 1534 1534 1534	5 8 × 11/32 5 8 × 96 6 8 × 11/32 7 8 8 × 96 8 8 × 11/32 7 8 8 × 96 8 8 × 11/32 5 3 × 96 5 4 × 11/32 5 3 × 96 6 4 × 96 6 4 × 96 6 4 × 96 6 4 × 96 6 4 × 96 6 4 × 96 6 4 × 96 6 6 × 96 6 7 7 126 6 8 7 7 126 6 8 7 7 126 6 8 7 7 126 6 8	334 4 5* 14* 116* 22' 334 334 334 334 334 115 13/16 13/16	956 954 958 — 958 — 954 10 954 1056 8 756	4800 6650 6000 free 3000 4875 11,800 8000 8000 10,600 13,100 6840 11,820 8900 8970 5-250 13,890 15,890 15,750	3 3 3 3 3 0 0 3 3 3 3 3 3 3 3 3 3 3 3	5500 6000 8000 24350 4970 6380 — 6000 10,000 12,200 15,780 10,600 8600 9540 7800 — 28,800	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
E 22, " E 28, " E 24, "	24 36 36	1056 1056 10	5 4×86 5	1 214 214	81/2 8 8 8	18.000 8750 7500	0 11/4 11/4	82,980 10,750 9500	=

(a) Between bands; (b) over all; s.p.t., auxiliary plates touching.

*Between bottom of eye and top of leaf. †semi-elliptical.

Tracings are furnished for each class of spring.

PHOSPHOR-BRONZE SPRINGS.

Wilfred Lewis (Engineers' Club, Philadelphia, 1837) made some tests with phosphor-brouze wire, 12 in. diameter, coiled in the form of a spiral spring, 1½ in. diameter from centre to centre, making 52 coils.

Such a spring of steel, according to the practice of the P. R. R., might be used for 40 lbs. A load of 30 lbs. gradually applied gave a permanent set. With a load of 21 lbs. in 30 hours the spring engthened from 20% inches to 21½ inches, and in 200 hours to 21½ inches. It was concluded that 21 lbs. was too great for durability. For a given load the extension of the bronze spring was just double the extension of a similar steel spring, that is, for the same extension the steel applier is two as a trong extension the steel spring is twice as strong.

D RESIST TORSIONAL FORCE. (Reuleaux's Constructor.) SPRINGS TO

Flat spiral or helical spring... $P = \frac{S bh^3}{2}$ $f = R\vartheta = \frac{64}{\pi} \frac{Pl}{E} \frac{R^2}{\bar{d}^4}.$ $f = R\vartheta = \frac{32}{\pi} \frac{P}{G} \frac{R^2l}{\bar{d}^4}.$ Round helical spring $P = \frac{S\pi}{32} \frac{d^3}{R}$; Round bar, in torsion...... $P = \frac{8\pi}{16} \frac{d^3}{R};$ $f = R\vartheta = \frac{32}{\pi} \frac{P}{G} \frac{R^2 l}{d^4}.$ Flat bar, in torsion..... $P = \frac{S}{3R} \frac{b^3 h^3}{\sqrt{b^2 + h^2}};$ $f = R\vartheta = \frac{3P k^2 l}{G} \frac{b^2 + h^2}{b^3 h^3}.$

P =force applied at end of radius or lever-arm R; $\vartheta =$ angular motion at end of radius R; S = permissible maximum stress, = 4/5 of permissible stress in flexure; E = modulus of elasticity in tension; G = torsional modulus, = 2/5 E; l = developed length of spiral, or length of bar; d = diameter of wire; b = breadth of flat bar; h = thickness.

HELICAL SPRINGS-SIZES AND CAPACITIES.

(Selected from Specifications of Penna. R. R. Co., 1899.)

	ins,			ıt.	Jo.	Test.	Heigh	t and l	Loads.	Single
P, R. R. Co.'s Class.	Diam. of Bar,	Length of Bar, ins.	Tapered to ins.	Normal Weight	Outside Diam. Coll, ins.	Free, ins.	Solid, ins.	Ins. with	Load of lbs.	Capacity of Si Coil, Ibs.
H 185 H	9/64 11/64 3/16 3/16 3/16 3/16 7/32 1/4 5/16 5/16 3/8 13/82 7/16 15/32 17/32 17/32 17/32 17/32 17/32 11/16 5/8 \$1/4 13/16 11/16 13/16 15/16 11/16 15/16 11/16 15/16 11/1	571/4 426 426 426 426 426 426 426 426 426 426 426	59 764 46 44 74 74 14 14 14 14 14 14 14 14 14 14 14 14 14	22 279 14 12 15 7 12 29 14 7 15 27 13 15 10 13 15 10 13 15 14 16 10 24 12 38 9 9 15 14 14 4 31 1 23 0 9 14 4 31 1 23 0 9 12 0 9 14 7 16 10 17 10 18 14 12 18 15 14 18 16 10 18 16 10 18 16 10 18 17 10 18 18 18 18 18 18 18 18 18 18 18 18 18 1	111122144445555555555555555555555555555	58 44 4 8 8 8 8 9 9 9 9 1 5 1 1 1 1 1 1 1 1 1 1 1 1 1 1	3 5 3 2 3 4 5 4 6 6 6 6 5 5 5 5 4 6 6 6 6 5 5 5 5	36 4 5 1836 5 4 4664 6 4 17 8 18446 18 18 18 18 18 18 18 18 18 18 18 18 18	110 170 103 45 110 250 250 6766 380 450 1350 330 810 532 1200 2100 2100 2100 2100 2100 2100 3260 1400 2750 3600 1700 3540 250 3600 450 3600 450 3600 450 3600 450 3600 450 3600 450 3600 4600 4600 4600 4600 4600 4600 460	188 270 244 188 200 500 500 497 700 700 700 700 11.400 11.300 11.

^{*}The subscript 1 means the outside coil of a concentric group or cluster: 2 and 3 are inner coils.

RIVETED JOINTS.

Fairbairn's Experiments. (From Report of Committee on Riveted Joints, Proc. Inst. M. E., April, 1881.)

The carliest published experiments on riveted joints are contained in the memoir by Sir W. Fairbairn in the Transactions of the Royal Society. Making certain empirical allowances, he adopted the following ratios as expressing the relative strength of riveted joints:

Solid plate	100
Double-riveted joint	70
Single-riveted joint.	56

These well-known ratios are quoted in most treatises on riveting, and are still sometimes referred to as having a considerable authority. It is singular, however, that Sir W. Fairbairn does not appear to have been aware that the proportion of metal punched out in the line of fracture ought to be different in properly designed double and single liveted joints. These celebrated ratios would therefore appear to rest on a very unsatisfactory analysis of the experiments on which they were based.

ratios would therefore appear to rest on a very unastistactory analysis of the experiments on which they were based.

Loss of Strength in Punched Plates.—A report by Mr. W. Parker and Mr. John, made in 1878 to Lloyd's Committee, on the effect of punching and drilling, showed that thin steel plates lost comparatively little from punching, but that in thick plates the loss was very considerable. The following table gives the results for plates punched and not annealed

or reamed:

Thickness of Plates.	Material of Plates.	Loss of Tenacity, per cent.
1/4	Steel	8
82	**	18
12	44	26
82	**	88
\$ 2	Iron	18 to 23

The effect of increasing the size of the hole in the die-block is shown in the following table:

Total Taper of Hole in Plate, inches.	Material of Plates.	Loss of Tenacity due to Punching, per cent.
1-16	Steel	17.8
14	44	12.3
16 12	44	(Hole ragged) 24.5

The plates were from 0.675 to 0.712 inch thick. When 3/-in. punched holes were reamed out to 11/6 in. diameter, the loss of tenacity disappeared, and the plates carried as high a stress as drilled plates. Annealing also restores to punched plates their original tenacity.

Strength of Perforated Plates.

(P. D. Bennett, Eng'g, Feb. 12, 1886, p. 155.)

Tests were made to determine the relative effect produced upon tensile strength of a flat bar of iron or steel: 1. By a ½-inch hole drilled to the required size: 2. by a hole punched ½ inch smaller and then drilled to the size of the first hole; and, 3, by a hole punched in the bar to the size of the drilled bar. The relative results in strength per square inch of original area were as follows:

	1.	2.	8.	4.
	Iron.	Iron.	Steel.	Steel.
Unperforated bar	1.000	1.000	1.000	1.000
Perforated by drilling	1.029	1.012	1.068	1.108
" punching and drilling.	1.030	1.008	1.059	1.110
" " nunching only	0.795	0.894	0.935	0.997

In tests 2 and 4 the holes were filled with rivets driven by hydraulic pressure. The increase of strength per square inch caused by drilling is a phenomenon of similar nature to that of the increased strength of a grooved barrover that of a straight bar of sectional area equal to the smallest section of the grooved bar. Mr. Bennett's tests on an iron bar 0.84 in. diameter, 10 in.

long, and a similar bar turned to 0.84 in. diameter at one point only, showed that the relative strength of the latter to the former was 1.823 to 1.000.

Riveted Joints.—Drilling versus Punching of Holes.

The Report of the Research Committee of the Institution of Mechanical Engineers, on Riveted Joints (1881), and records of investigations by Prof. A. B. W. Kennedy (1881, 1882, and 1885), summarize the existing information regarding the comparative effects of punching and drilling upon iron and steel plates. From an examination of the voluminous tables given in Professor Unwin's Report, the results of the greatest number of the experiments made on iron and steel plates lead to the general conclusion that, while thin plates, even of steel, do not suffer very much from punching, yet in those of ½ inch thickness and upwards the loss of tenacity due to punching ranges from 10% to 23% in iron plates, and from 11% to 33% in the case of hild steel. In drilled plates there is no appreciable loss of strength. It is mild steel. In drilled plates there is no appreciable loss of strength. It is possible to remove the bad effects of punching by subsequent reaming or annealing; but the speed at which work is turned out in these days is not favorable to multiplied operations, and such additional treatment is seldom practised. The introduction of a practicable method of drilling the plating of ships and other structures, after it has been bent and shaped, is a matter of great importance. If even a portion of the deterioration of tenacity can be prevented, a much stronger structure results from the same material and the same scanting. This has been fully recognized in the modern English practice (1887) of the construction of steam-bollers with steel plates; punching in such cases being almost entirely abolished, and all rivet-holes being drilled after the plates have been bent to the desired form.

Comparative Efficiency of Riveting done by Different Methods.

The Reports of Professors Unwin and Kennedy to the Institution of Mechanical Engineers (Proc. 1881, 1882, and 1885) tend to establish the four following points:

1. That the shearing resistance of rivets is not highest in joints riveted by

means of the greatest pressure;

2. That the ultimate strength of joints is not affected to an appreciable extent by the mode of riveting; and, therefore,

8. That very great pressure upon the rivets in riveting is not the indispen-

sable requirement that it has been sometimes supposed to be;

4. That the most serious defect of hand-riveted as compared with machineriveted work consists in the fact that in hand-riveted joints visible slip commences at a comparatively small load, thus giving such joints a low value as regards tightness, and possibly also rendering them liable to failure under sudden strains after slip has once commenced.

The following figures of mean results, taken from Prof. Kennedy's tables (Proceedings 1886, pp. 218-225), give a comparative view of hand and hydraulic riveting, as regards their ultimate strengths in joints, and the periods

at which in both cases visible slip commenced.

Total Brea	king Load.	Load at which Visible Slip began.				
Hand-riveting.	Hydraulic Rivet- ing.	Hand-riveting.	Hydraulic Rivet-			
Tons. 86.01	Tons. 85.75	Tons. 21.7	- Tons.			
82.16	77.00 82.70 78.58	25.0	85.0 53.7 54.0			
149.2	145.5 140.2	81.7	49.7 46.7			
198.3	188.1 183.7	25.0	56.0			

In these figures hand-riveting appears to be rether better than hydraulic riveting, as far as regards ultimate strength of joint; but is very much inferior to hydraulic work, in view of the small proportion of load borne be it before visible slip commenced.

Some of the Conclusions of the Committee of Research on Riveted Joints.

(Proc. Inst. M. E., Apl. 1885.)
The conclusions all refer to joints made in soft steel plate with steel rivets, the holes all drilled, and the plates in their natural state (unannealed). In every case the rivet or shearing area has been assumed to be that of the holes, not the nominal (or real) area of the rivets themselves. Also, the strength of the metal in the joint has been compared with that of strips cut from the same plates, and not merely with nominally similar material.

The metal between the rivet-holes has a considerably greater tensile resistance per square inch than the unperforated metal. This excess tenacity amounted to more than 20%, both in %-inch and %-inch plates, when the pitch of the rivet was about 1.9 diameters. In other cases %-inch plate gave an excess of 15% at fracture with a pitch of 2 diameters, of 10% with a pitch of 8.6 diameters, and of 6.6%, with a pitch of 3.9 diameters; and 34-inch plate gave 7.8% excess with a pitch of 2.8 diameters.

In single-riveted joints it may be taken that about 22 tons per square inch is the shearing resistance of rivet steel, when the pressure on the rivets does not exceed about 40 tons per square inch. In double-riveted joints, with rivets of about % inch diameter, most of the experiments gave about 24 tons per square inch as the shearing resistance, but the joints in one series went at 22 tons.

The ratio of shearing resistance to tenacity is not constant, but diminishes

very markedly and not very irregularly as the tenacity increases.

The size of the rivet heads and ends plays a most important part in the strength of the joints—at any rate in the case of single-riveted joints. An increase of about one third in the weight of the rivets (all this increase, of course, going to the heads and ends) was found to add about 81/4 to the resistance of the joint, the plates remaining unbroken at the full shearing resistance of 22 tons per square inch, instead of tearing at a shearing stress of only a little over 20 tons. The additional strength is probably due to the prevention of the distortion of the plates by the great tensile stress in the rivets.

The intensity of bearing pressure on the rivet exercises, with joints proportioned in the ordinary way, a very important influence on their strength. So long as it does not exceed 40 tons per square inch (measured on the pro-So long as it does not exceed 40 tons per square inch (measured on the projected area of the rivets), it does not seem to affect their strength; but pressures of 50 to 55 tons per square inch seem to cause the rivets to shear in most cases at streases varying from 16 to 18 tons per square inch. For ordinary joints, which are to be made equally strong in plate and in rivets, the bearing pressure should therefore probably not acceed 42 or 43 tons per square inch. For double-riveted butt-joints perhaps, as will be noted later, a higher pressure may be allowed, as the shearing stress may probably not be more than 15 or 18 tons per square inch when the plate tears.

A margin (or net distance from outside of holes to edge of plate) equal to the disputer of the drilled hole has been found sufficient in all cases hither to the

diameter of the drilled hole has been found sufficient in all cases hitherto tried. To attain the maximum strength of a joint, the breadth of lap must be such as to prevent it from breaking zigzag. It has been found that the net metal measured zigzag should be from 30% to 35% in excess of that measured straight across, in order to insure a straight fracture. This corresponds to a diagonal pitch of 2/3 p + d/3, if p be the straight pitch and d the diameter of the rivet-hole.

Visible slip or "give" occurs always in a riveted joint at a point very much below its breaking load, and by no means proportional to that load. A collation of the results obtained in measuring the slip indicates that it depends upon the number and size of the rivets in the joint, rather than upon anything else; and that it is tolerably constant for a given size of rivet in a given type of joint. The loads per rivet at which a joint will commence to

slip visibly are approximately as follows:

Diameter of Rivet.	Type of Joint.	Riveting.	Slipping Load per Rivet.
inch inch inch inch	Single-riveted Double-riveted Double-riveted Single-riveted Double-riveted Double-riveted	Hand Hand Machine Hand Hand Machine	2.5 tons 3.0 to 3.5 tons 7 tons 8.2 tons 4.8 tons 8 to 10 tons

To find the probable load at which a joint of any breadth will commence to slip, multiply the number of rivets in the given breadth by the proper figure taken from the last column of the table above. It will be understood that the above figures are not given as exact; but they represent very well the results of the experiments.

The experiments point to simple rules for the proportioning of joints of maximum strength. Assuming that a bearing pressure of 43 tons per square inch may be allowed on the rivet, and that the excess tenacity of the plate is 10% of its original strength, the following table gives the values of the ratios of diameter d of hole to thickness t of plate (d+t), and of pitch p to diameter of hole (p+d) in joints of maximum strength in $\frac{3}{6}$ -inch plate,

For Single-riveted Plates.

Original T Pla		Shearing River	esistance of vets.		Ratio.	Ratio. Plate Area	
Tons per sq. in.	Lbs. per sq. in.	Tons per sq. in.	Lbs. per sq. in.	d+t		Rivet Area	
30	67,200	22	49,200	2.48	2.80	0.667	
28	62,720	22	49,200	2.48	2.40	0.785	
8 0	67,900	94	53,7 60	2.28	2.27	0.718	
28	62,720	24	53,760	2.28		0.690	

This table shows that the diameter of the hole (not the diameter of the rivet) should be 2% times the thickness of the plate, and the pitch of the rivets 2% times the diameter of the hole. Also, it makes the mean plate area

71% of the rivet area.
If a smaller rivet be used than that here specified, the joint will not be of uniform, and therefore not of maximum, strength; but with any other size of rivet the best result will be got by use of the pitch obtained from the simple formula

$$p=a\frac{d^2}{t}+d,$$

where, as before, d is the diameter of the hole.

The value of the constant α in this equation is as follows:

For	30-ton	plate and	22-ton	rivets.	a =	0.524
**	28	- "	22	"	**	0.558
44	80	66	94	44	**	0.570
44	28	44	24	"	**	0.606

Or, in the mean, the pitch $p = 0.56 \frac{d^3}{dt} + d$.

It should be noticed that with too small rivets this gives pitches often con-

siderably smaller in proportion than 2% times the diameter.

For deuble-riveted lap-joints a similar calculation to that given above, but with a somewhat smaller allowance for excess tenacity, on account of the large distance between the rivet-holes, shows that for joints of maximum strength the ratio of diameter to thickness should remain precisely as in single-riveted joints; while the ratio of pitch to diameter of hole should be 8.64 for 30-ton plates and 22 or 24 ton rivets, and 3.88 for 28-ton plates with the same tivets.

Here, still more than in the former case, it is likely that the prescribed size of rivet may often be inconveniently large. In this case the diameter of rivet should be taken as large as possible; and the strongest joint for a given thickness of plate and diameter of hole can then be obtained by using the pitch given by the equation

 $p=a\,\frac{d^2}{4}+d,$

where the values of the constant a for different strengths of plates and rivets may be taken as follows:

Table of Proportions of Double-riveted Lap-joints,

in which
$$p = a \frac{d^2}{t} + d$$
.

Thickness of Plate.	Original tenacity of Plate, Tons per sq. in.	Shearing Resist- ance of Rivets. Tons per sq. in.	Value of Constant.
3% inch	30	24	1.15
8/4 ''	28	24	1.22
8% ''	80	22	1.05
86 "	28	22	1.12
3 /4 ''	80	24	1.17
82 ''	28	24	1.25
8½ "	30	22	1.07
% "	28	23	1.14

Practically, having assumed the rivet diameter as large as possible, we can fix the pitch as follows. for any thickness of plate from % to % inch;

For 30-ton plate and 24-ton rivets
$$\begin{cases} p = 1.16 \frac{d^2}{t} + d; \\ w = 30 \text{ " " 22 " " } p = 1.06 \frac{d^2}{t} + d; \\ w = 28 \text{ " " 24 " " } p = 1.24 \frac{d^2}{t} + d. \end{cases}$$

In double-riveted butt-joints it is impossible to develop the full shearing resistance of the joint without getting excessive bearing pressure, because the shearing area is doubled without increasing the area on which the pressure acts. Considering only the plate resistance and the bearing pressure, and taking this latter as 45 tons per square inch, the best pitch would be about 4 times the diameter of the hole. We may probably say with some certainty that a pressure of from 45 to 50 tons per square inch on the rivets will cause shearing to take place at from 16 to 18 tons per square inch. Working out the equations as before, but allowing excess strength of only 5% on account of the large pitch, we find that the proportions of double-riveted butt-joints of maximum strength, under given conditions, are those or the following table:

Double-riveted Butt-joints.

Original Ten- acity of Plate, Tons per sq. in.	Shearing Resistance of Rivets, Tons per sq. in.	Bearing Pressure, Tons per sq. in.	Ratio $\frac{d}{t}$	Ratio p d
30	16	45	1.80	3.85
28	16	45	1.80	4.06
30	18	48	1.70	4.03
28	18	48	1.70	4.27
80	16	50	2.00	4.20
28	16	50	2.00	4.42

Practically, therefore, it may be said that we get a double-riveted butt-joint of maximum strength by making the diameter of hole about 1.8 times the thickness of the plate, and making the pitch 4.1 times the diameter of the hole.

hole.

The proportions just given belong to joints of maximum strength. But in a boiler the one part of the joint, the plate, is much more affected by time than the other part, the rivets. It is therefore not unreasonable to estimate the percentage by which the plates might be weakened by corrosion, etc., before the boiler would be unfit for use at its proper steam-pressure, and to add correspondingly to the plate area. Probably the best thing to do in this case is to proportion the joint, not for the actual thickness of plate, but for a nominal thickness less than the actual by the assumed p reentage. In this case the joint will be approximately one of uniform strength by the time it has reached its final workable condition; up to which time the joint as a whole will not really have been weakened, the corrosion only gradually bringing the strength of the plates down to that of rivets.

Efficiencies of Joints.

The average results of experiments by the committee gave: For double-riveted lap-joints in 36-inch plates, efficiencies ranging from 67.1% to 81.2%. For double-riveted bytt-joints (in double shear) 61.4% to 71.3%. These low resuits were probably due to the use of very soft steel in the rivets. For singleriveted lap-joints of various dimensions the efficiencies varied from 54.8% to

The experiments showed that the shearing resistance of steel did not increase nearly so fast as its tensile resistance. With very soft steel, for instance, of only 26 tons tenacity, the shearing resistance was about 80% of the tensile resistance, whereas with very hard steel of 52 tons tenacity the shearing resistance was only somewhere about 65% of the tensile resistance.

Proportions of Pitch and Overlap of Plates to Diameter of Bivet-Hole and Thickness of Plate.

(Prof. A. B. W. Kennedy, Proc. Inst. M. E., April, 1885.)

t = thickness of plate; d = diameter of rivet (actual) in parallel hole;

p = pitch of rivets, centre to centre;
 s = space between lines of rivets;

l =overlap of plate.

The pitch is as wide as is allowable without imparing the tightness of the joint under steam.

For single-riveted lap-joints in the circular seams of boilers which have double-riveted longitudinal lap joints,

$$d = t \times 2.25;$$

 $p = d \times 2.25 = t \times 5$ (nearly);
 $l = t \times 6.$

For double-riveted lap-joints:

$$d = 2.25t;$$

 $p = 8t;$
 $s = 4.5t;$
 $l = 10.5t.$

Sin	Single-riveted Joints.				Double-riveted Joints.				
t	đ	p	ı	t	đ	p		ı	
8-16 34 5-16 36 7-16 34 9-16	7-16 9-16 11-18 13-16 1 114 114	15-16 1¼ 1 9-16 136 2 3-16 216 2 13-16	11/6 11/4 17/8 21/4 25/8 8 83/8	3-16 14 5-16 36 7-16 14 9-16	7-16 9-16 11-16 13-16 1 1146	11/6 2 21/6 8 31/6 4 41/6	76 1 3-16 114 184 2 214 214	2 23/4 33/8 4 45/6 51/4 57/8	

With these proportions and good workmanship there need be no fear of

leakage of steam through the riveted joint.

The net diagonal area, or area of plate, along a zigzag line of fracture should not be less than 80% in excess of the net area straight across the

ioint, and 35% is better.

Mr. Theodore Cooper (R. R. Gazette, Aug. 22, 1890) referring to Prof. Kennedy's statement quoted above, gives as a sufficiently approximate rule for the proper pitch between the rows in staggered riveting, one half of the pitch of the rivets in a row plus one quarter the diameter of a rivet-hole.

Apparent Excess in Strength of Perforated over Unperforated Plates. (Proc. Inst. M. E., October, 1888.)

The metal between the rivet-holes has a considerably greater tensile resistance per square inch than the unperforated metal. This excess tenselty amounted to more than 20%, both in 36-inch and 3-inch plates, when che pitch of the rivets was about 1.9 diameters. In other cases 36-inch plate gave an excess of 15% at fracture with a pitch of 2 diameters, of 10% with a pitch of 3.6 diameters, and 36-inch plate gave 7.86 excess with a pitch of 3.9 diameters; and 36-inch plate gave 7.86 excess with a pitch of 2.8 diameters. plate gave 7.8% excess with a pitch of 2.8 diameters.

(1) The "excess strength due to perforation" is increased by anything which tends to make the stress in the plate uniform, and to diminish the effect of the narrow strip of metal at the edge of the specimen.

(2) It is diminished by increase in the ratio of p/d, of pitch to diameter of hole, so that in this respect it becomes less as the efficiency of the joint

increases.

increases. (3) It is diminished by any increase in hardness of the plate. (4) For a given ratio p/d, of pitch to diameter of hole, it is also apparently diminished as the thickness of the plate is increased. The ratio of pitch to thickness of plate does not seem to affect this matter directly, at least within the limits of the experiments.

Test of Double-riveted Lap and Butt Joints. (Proc. Inst. M. E., October, 1888.)

Steel plates of 25 to 26 tons per square inch T. S., steel rivets of 24.6 tons shearing-strength per square inch.

SHOW! IN B. BVI CHE	on per square r	HCH.		~
Kind of Joint.	Thickness of Plate.		Ratio of Pitch to Diameter.	Comparative Efficiency of Joint.
Lap	3 6″	0.8"	8.62	75.2
Butt	%	0.7	8.93	76.5
Lap	%	1.1	2.82	68.0
	¾	1.6	8.41	78.6
Butt	*	1.1	4.00	72.4
_ "	%	1.6	8.94	76.1
Lap	1 -	1.8	2.42	63.0
_"	1	1.75	3.00	70.2
Butt	1	1.3	8.92	76.1
of the	Rivet in Si	ngle Shear	posed for the	e Diameter 8, 1880.)
Browne	d =	= 2t (with doub	ole covers 11(t)	
Fairbairn	d =	= 2t for plates	less than % in.	(1) (2)
"	d =	= $116t$ for plate	s greater than 🦠	ś in. (8)
Lemaitre	d =	= 1.5t + 0.16		(4)
Antoine	d =	= 1.1 4/t		(5)
Pohlig	d =	2t for boiler	riveting	(6)
	d =	= 3t for extra	strong riveting	(7)
Redtenbacher	d =	= 1.5t to 2t		(8)
Unwin	d =	$= \frac{34}{4}t + \frac{5}{16}$ to	%t + %	(9)

 $\dots \qquad d = 1.2 \sqrt{t}$ The following table contains some data of the sizes of rivets used in practice, and the corresponding sizes given by some of these rules.

(10)

Diameter of Rivets for Different Thicknesses of Plates.

		Diameter of Rivets, in inches.										
Thick- ness of plate. Inches.	Lloyd's Rules.	Liverpool Rules.	English Dock-yards.	French Veritas.	Browne Eq. (1).	Fairbairn (2) and (3).	Lemaitre (4).	Antoine (5).	Unwin (10).	Wilson.		
5/16 5/6 7/18	*5 *5 *5 *4	% % % 18/16	16,004,34	% %	5% 3% 3%	56 84 21/82 34	28/32 18/16 15/16	56 11/16 34 34	11/16 % 18/16 76	56 11/16		
9/16 56 11/16 94	343436	13/16 76 98 15/16	7/8 5/8 1	3/4 18/16 3/8	11/4	27/32 15/16 1 1/83 11/6	1 1½ 1 3/16 1¼	13/16 76 15/16 15/16	15/16 1 1/16	7.6 7.6 1.6 1.6		
18/16 36 15/16	% 1 1 1	1 11/4 1 8/16 11/4	1 11/6 11/6 11/6	1 1 1/16		1 7/32	1%	1 1 1 1/16 11/8	1 8/82 11/6 1 8/16 11/4	1 1 116 116		

strength of Double-riveted Seams, Calculated.—W. B. Ruggles, Jr., in Power for June, 1890, gives tables of relative strength of rivets and parts of sheet between rivets in double-riveted seams, compared with strength of shell, based on the assumption that the shearing strength of rivets and the tensile strength of steel are equal. The following figures show the sizes in his tables which show the nearest approximation to equality of strength of rivets and parts of plates between the rivets, together with the percentage of each relative to the strength of the solid plate.

rnesss of inches.	Pitch of Rivets, inches.	Size of Rivet- holes,	Percen Streng Pla		Thickness of Plate, inches,	Pitch of Rivets,		Percen Streng Pla	th of
Thick plate	inches.	inches.	Rivets. Plate.	inches.	Rivets.	Plate.			
14 14 14 14 15/16 16/16 16/16 16/16 16/16 16/16 16/16 16/16 16/16 16/16 16/16 16/16 16/16 16/16	21/24/24/24/24/24/24/24/24/24/24/24/24/24/	14 9/16 9/16 11/16 9/16 54 11/16 34 58 11/16 34 13/16	.739 .795 .785 .819 .749 .748 .761 .780 .755 .754 .702 .777	.765 .775 .800 .810 .735 .762 .780 .793 .722 .738 .760 .776 .788 .776	7/16 7/16 7/16 7/16 7/10 16 16 16 16 9/16 9/16 9/16	25/4 31/6 35/6 41/6 21/6 81/4 41/6 3 3 41/6 3 41/6 3 41/6 3 41/6 3 41/6 3 41/6 3 41/6 3 41/6 3 41/6 3 41/6 3 41/6 3 41/6 3 41/6 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	34 13/16 78 15/16 34 13/16 76 15/16 13/16 78 15/16	.734 .758 .758 .765 .707 .721 .740 .761 .701 .714 .727 .745 .742	.728 .740 .759 .773 .700 .718 .731 .750 .708 .708 .708 .729 .733 .750

H. De B. Parsons (Am. Engr. & R. R. Jour., 1893) holds that it is an error to assume that the shearing strength of the rivet is equal to the tensile strength. Also, referring to the apparent excess in strength of perforated over unperforated plates, he claims that on account of the difficulty in properly matching the holes, and of the stress caused by forcing, as is too often the case in practice, this additional strength cannot be trusted much more than that of friction.

Adopting the sizes of iron rivets as generally used in American practice for steel plates from 1/2 to 1 inch thick: the tensile strength of the plates as 60,000 lbs.; the shearing strength of the rivets as 40,000 for single-shear and 35,500 for double-shear, Mr. Parsons calculates the following table of pitches, so that the strength of the rivets against shearing will be approximately equal to that of the plate to tear between rivet-holes. The diameter of the rivets has in all cases been taken at 1/16 in. larger than the nominal size, as the rivet is assumed to fill the hole under the power riveter.

Riveted Joints.

Lap or Butt with Single Welt—Steel Plates and Iron Rivets.

Thickness	Diameter	Pi	tch.	Efficiency.		
Plates.	of Rivets.	Single.	Double.	Single.	Double.	
in. 1/4	in. 168	in. 1 3/16 1 11/16 176 1 11/16 176 174 2 3/16	in. 176 2 11/16 234 2 7/16 256 2 7/16 256	55.7% 52.7 49.0 43.6 42.0 38.6 38.1	70.0% 68.6 65.9 60.4 59.5 55.4 54.9	

Calculated Efficiencies—Steel Plates and Steel Bivets.—The differences between the calculated efficiencies given in the two tables above are notable. Those given by Mr. Ruggles are probably too high, since he assumes the shearing strength of the rivets equal to the tensile strength of the plates. Those given by Mr. Parsons are probably lower than will be obtained in practice, since the figure he adopts for shearing strength is rather low, and he makes no allowance for excess of strength of the perforated over the unperforated plate. The following table has been calculated by the author on the assumptions that the excess strength of the perforated plate is 10%, and that the shearing strength of the rivets per square inch is four fifths of the tensile strength of the plate. If t= thickness of plate, d= diameter of rivet-hole, p= pitch, and T= tensile strength per square inch, then for single-riveted plates

$$(p-d)t \times 1.10T = \frac{\pi}{4}d^2 \times \frac{4}{5}T$$
, whence $p = .571\frac{d^2}{t} + d$.
For double-riveted plates, $p = 1.142\frac{d^2}{4} + d$.

The coefficients .571 and 1.142 agree closely with the averages of those given in the report of the committee of the Institution of Mechanical Engineers, quoted on pages 357 and 358, ante.

# Dia		Pitch.		Efficiency.			Diam	Pitch.		Efficiency.	
Thickness.	Diam, of Rivet- hole.	Single Riveting.	Double Riveting.	Single Riveting.	Double Riveting.	Thickness.	Diam. of Rivet- hole.	Single Riveting.	Double Riveting.	Single Riveting.	Double Riveting.
in. 8/16 1/4 5/16 7/16	in. 7/16 1/2 9/16 9/16 9/16 9/16 9/16 9/16 9/16 11/16	in. 1.020 1.261 1.071 1.285 1.137 1.339 1.551 1.218 1.607 2.041 1.136 1.484 1.869 2.305	in. 1.603 2.023 1.642 2.008 1.712 2.053 2.415 1.810 2.463 3.206 1.647 2.218 2.864 3.610	57.1 60.5 53.3 56.5 50.5 53.3 55.7 48.7 53.3 57.1 45.0 49.5 53.2 56.6	72.7 75.8 69.6 72.0 67.1 69.5 71.5 65.5 69.5 72.7 62.0 66.2 69.4 72.8	in. 1/28 9/16 5/5	in. \$4.28 1146 1144 1144 1144 1144 1144 1144 114	in. 1.292 1.749 2.142 2.570 1.821 1.652 2.015 2.410 2.836 1.264 1.575 1.914 2.281 2.678	in. 2.085 2.624 8.284 4.016 1.892 2.429 2.429 2.429 2.429 2.422 2.429 2.428 2.774 2.827 2.827 2.827 4.438 4.105	\$46.1 50.0 58.3 56.2 43.2 47.0 50.4 53.3 55.9 40.7 44.4 47.7 50.7 58.8	\$ 63.1 66.6 70.0 73.0 60.3 64.0 69.5 71.5 57.8 61.6 67.8 69.5

Riveting Pressure Required for Bridge and Boiler Work,

(Wilfred Lewis, Engineers' Club of Philadelphia, Nov., 1893.)

A number of \$4-inch rivets were subjected to pressures between 10,000 and 60,000 lbs. At 10,000 lbs. the rivet swelled and filled the hole without forming a head. At 20,000 lbs. the head was formed and the plates were slightly pinched. At 30,000 lbs. the rivet was well set. At 40,000 lbs. the metal in the plate surrounding the rivet began to stretch, and the stretching became more and more apparent as the pressure was increased to 50,000 and 60,000 lbs. From these experiments the conclusion might be drawn that the pressure required for cold riveting was about 300,000 lbs. per squareinch of rivet section. In hot riveting, until recently there was never any call for a pressure exceeding 60,000 lbs., but now pressures as high as 150,000 lbs. a prenot uncommon, and even 300,000 lbs. have been contemplated as desirable.

Apparent Shearing Resistance of Rivet Iron and Steel.

(Proc. Inst. M. E., 1879, Engineering, Feb. 20, 1880.)

The true shearing resistance of the rivets cannot be ascertained from experiments on riveted joints (1) because the uniform distribution of the load to all the rivets cannot be insured; (2) because of the friction of the plates, which has the effect of increasing the apparent resistance to shearing in an element uncertain in amount. Probably in the case of single riveted joints the shearing resistance is not much affected by the friction.

•	Ultimate Sh	earing Stress	
T	ons per sq. in.	Lbs. per sq. in.	
Iron, single shear (12 bars)	24.15	54.09 6	Clarke.
" double shear (8 bars)	22.10	49.504	CIBIKO.
	22.62	50,669	Barnaby.
" " "	22.80	49.952	Rankine.
" 3/4-in. rivets	23.05 to 25.57	51.682 to 57.277)	
" %-in. rivets	24.32 to 27.94	54.477 to 62.362	Riley.
" mean value	25.0	56,000	
" 5%-in, rivets	19.01	42.582	Greig and Eyth.
Steel	17 to 26	38.080 to 58.240	Parker.
Landore steel, %-in, rivets			
" %-in rivets	80.45 to 85.73	68.208 to 80.035	Riley.
" " mean value	33.8	74.592	
Brown's steel	22.18	49.688	Greig and Eyth.

Fairbairn's experiments show that a rivet is 64% weaker in a drilled than in a punched hole. By rounding the edge of the rivet-hole the apparent shearing resistance is increased 12%. Mr. Maynard found the rivets 4% weaker in drilled holes than in punched holes. But these results were obtained with riveted joints, and not by direct experiments on shearing. There is a good deal of difficulty in determining the true diameter of a punched hole, and it is doubtful whether in these experiments the diameter was very accurately ascertained. Messrs. Greig and Eyth's experiments also indicate a greater resistance of the rivets in punched holes than in drilled holes.

If, as appears above, the apparent shearing resistance is less for double than for single shear, it is probably due to unequal distribution of the stress on the two rivet sections.

The shearing resistance of a bar, when sheared in circumstances which prevent friction, is usually less than the tenacity of the bar. The following results show the decrease:

	Tenacity of Bar.	Shearing Resistance.	Ratio.
Harkort, iron	26.4	16.5	0.62
	25.4	20.2	0.79
	22.2	19.0	0.85
	28.8	22.1	0.77

In Wöhler's researches (in 1870) the shearing strength of iron was found to be four-fifths of the tenacity. Later researches of Bauschinger confirm this result generally, but they show that for iron the ratio of the shearing resistance and tenacity depends on the direction of the stress relatively to the direction of rolling. The above ratio is valid only if the shear is in a plane perpendicular to the direction of rolling, and if the tension is applied parallel to the direction of rolling. The shearing resistance in a plane parallel to the direction of rolling is different from that in a plane perpendicular to that direction, and again different from that in a plane perpendicular or parallel to the breadth of the bar. In the former case the resistance is 18 to 20% greater than in a plane perpendicular to the fibres, or is equal to the tenacity. In the latter case it is only half as great as in a plane perpendicular to the fibres.

CLASSIFICATION OF IRON AND STEEL.
(W. Kent, Railroad & Engineering Journal, April, 1887.)

IRON AND STEEL.

CLASSIFICATION OF IRON AND STEEL.

German, shear, bits-ter, and puddled or indirect process, as (8+) WROUGHT STEEL. Obtained by direct Will Harden. Or welded from a pasty mass. steels. WROUGHT. a. Obtained by direct process from ores, as Catalan, Chenot, and Obtained by indirect process from cast iron, as finery-hearth Will Not Harden. WROUGHT IRON other process irons. and puddled irons. 3 IRON. Open-hearth (3) Crucible, (4) Bessemer, CAST STEEL. steels. and (6) Mitig.* Or obtained from a fluid mass. Malleable. <u>છ</u> Malleable cast iron, ob-1 by annealing In oxides. CAST, (2) cast CAST IRON. (1) Ordinary Non-malleable. castings. Distinguishing How Obtained. Generic Term. Varieties. Quality. Species.

• No. 6. Mitis is the name given to a new product (having the same general properties and produced by the same processes as soft cast steels) made by adding an alloy of aluminum to melted wrought iron or soft steel before pouring.
+ No. 8. Wrought steel is almost an obsolete product, having been replaced in commerce by cast steel.
Sub-varieties of Nos. 3. 4, and 5, soft, mild, medium, and hard steels, according to percentage of carbon, the divisions between them not being well defined.

Cast from usually contains over 3% of carbon; cast steel anywhere from 0.06% to 1.50%, according to the purpose for which it is used; wrought from from 0.02% to 0.10%. The quality of hardening and tempering which formerly distinguished steel from wrought from is now no longer the dividing line between them, since soft steels are now produced which, by the ordinary blacksmith's tests, will not harden. All products of the crucible, Bessemer, and open-hearth processes are now commercially known as steel.

CAST IRON.

Grading of Pig Iron.—Pig iron is commonly graded according to its fracture, the number of grades varying in different districts. In Eastern Pennsylvania the principal grades recognized are known as No. 1 and 2 foundry, gray forge or No. 3, mottled or No. 4, and white or No. 5. Intermediate grades are sometimes made, as No. 2 X, between No. 1 and No. 2, and special names are given to irons more highly silicized than No. 1, as No. 1 X, silver-gray, and soft. Charcoal foundry pig iron is graded by numbers in anthracite and coke pig. Southern coke pig iron is graded into ten or more grades. Grading by fracture is a fairly satisfactory method of grading irons made from uniform ore mixtures and fuel, but is unreliable as means of determining quality of irons produced in different sections or from different ores. Grading by chemical analysis, in the latter case, is the only satisfactory method. The following analyses of the five standard grades of northern foundry and mill pig irons are given by J. M. Hartman grades of northern foundry and mill pig irons are given by J. M. Hartman (Bull. I. & S. A., Feb., 1892):

	No. 1.	No. 2.	No. 8.	No. 4.	No. 4 B.	No. 5.
Iron	92.37	92.31	94.66	94.48	94.08	94.68
Graphitic carbon	8.52	2.99	2.50	2.02	2.02	
Combined carbon	.18	.37	1.52	1.98	1.43	8.83
Silicon	2.44	2.52	.72	.56	.92	.41
Phosphorus	1.25	1.08	.26	.19	.04	.04
Sulphur	.02	.02	trace	.08	.04	.02
Manganese	.28	.72	.34	.67	2.02	.9 8

CHARACTERISTICS OF THESE IRONS.

No. 1. Gray.—A large dark, open-grain iron, softest of all the numbers and used exclusively in the foundry. Tensile strength low. Elastic limit low. Fracture rough. Turns soft and tough.

No. 2. Gray.—A mixed large and small dark grain, harder than No. 1 iron, and used exclusively in the foundry. Tensile strength and elastic limit higher than No. 1. Fracture less rough than No. 1. Turns harder, less tough, and more brittle than No. 1.

No. 8. Gray.—Small, gray, close grain, harder than No. 2 iron, used either than No. 1 iron will be dether than No. 2 iron, used either than N

in the rolling-mill or foundry. Tensile strength and elastic limit higher than No. 2. Turns hard, less tough, and more brittle than No. 2. No. 4. Mottled.—White background, dotted closely with small black spots

of graphitic carbon: little or no grain. Used exclusively in the rolling-mill. Tensile strength and elastic limit lower than No. 8. Turns with difficulty; less tough and more brittle than No. 3. The manganese in the B pig iron replaces part of the combined carbon, making the iron harder and closing

the grain, notwithstanding the lower combined carbon.

No. 5. White.—Smooth, white fracture, no grain, used exclusively in the rolling mill. Tensile strength and elastic limit much lower than No. 4. Too

hard to turn and more brittle than No. 4.

Southern pig irons are graded as follows, beginning with the highest in silicon: Nos. 1 and 2 silvery, Nos. 1 and 2 soft, all containing over 3% of silicon; Nos. 1, 2, and 3 foundry, respectively about 2.75%, 2.5% and 2% silicon; No. 1 mill, or "foundry forge;" No. 2 mill, or gray forge; mottled; white

No. 1 mill, or "foundry forge;" No. 2 mill, or gray forge; mottled; white-Good charcoal chilling iron for car wheels contains, as a rule, 0.58 to 0.95 silicon, 0.08 to 0.90 manganese, 0.06 to 0.75 phosphorus. The following is an analysis of a remarkably strong car wheel: Si, 0.784; Mn, 0.488; P. 0.428, S. 0.08; Graphitic C, 8.083; Combined C, 1.247; Copper, 0.029. The chill was very hard—14 in. deep at root of flange, 34 in. deep on tread. A good ordnance iron analysed: Si, 0.30; Graphitic C, 2.20; Combined C, 1.70; P, 0.44; Mn, 8.55 (!). Its specific gravity was 7.24 and tenacity 81,734 lbs. per sq. in

Influence of Silicon, Phosphorus, Sulphur, and Manganese upon Cast Iron.—W. J. Keep, of Detroit, in several papers (Trans. A I. M.E., 1898 to 1898), discusses the influence of various chemical elements on the quality of cast iron. From these the following notes have

been condensed:

SILICON.—Pig iron contains all the carbon that it could absorb during its reduction in the blast-furnace. Carbon exists in cast iron in two distinct forms. In chemical union, as "combined" carbon, it cannot be discerned. except as it may increase the whiteness of the fracture, in so-called whit

iron. Carbon mechanically mixed with the iron as graphite is visible, varying in color from gray to black, while the fracture of the iron ranges from a light to a very dark gray.

Silicon will expel carbon, if the iron, when melted, contains all the carbon

that it can hold and a portion of silicon be added.

Prof. Turner concludes from his tests that the amount of silicon producing the maximum strength is about 1.80%. But this is only true when a white base is used. If an iron is used as a base which will produce a sound casting to begin with, each addition of silicon will decrease strength. Silicon itself is a weakening agent. Variations in the percentage of silicon added to a pig iron will not insure a given strength or physical structure, but these results will depend upon the physical properties of the original iron.

After enough silicon has been added to cause solid castings, any further

addition and consequent increase of graphite weakens the casting.

As strength decreases from increase of graphite and decrease of combined corbon, deflection increases; or, in other words, hending is increased by graphite. When no more graphite can form and silicon still increases, deflection diminishes, showing that high silicon not only weakens iron, but makes it stiff. This stiffness is not the same strength-stiffness which is caused by compact iron and combined carbon. It is a brittle-stiffness.

Silicon of itself, however small the quantity present, hardens cast-iron; but the decrease of hardness from the change of the combined carbon to graphite, caused by the slicon, is so much more rapid than the hardening produced by the increase of silicon, that the total effect is to decrease hard-

ness, until the silicon reaches from 8 to 5%

As practical foundry-work does not call for more than 3% of silicon, the ordinary use of silicon does reduce the hardness of castings; but this is produced through its influence on the carbon, and not its direct influence on the

When the change from combined to graphite carbon has ceased to diminish hardness, say at from 2% to 5% of silicon, the hardening by the silicon it-

self becomes more and more apparent as the silicon increases.

The term "chilling" irons is generally applied to such as, cooled slowly, would be gray, but cooled suddenly become white either to a depth sufficient for practical utilization (e.g., in car-wheels) or so far as to be detrimental. Many irons chill more or less in contact with the cold surface of the mould in which they are cast, especially if they are thin. Sometimes this is a valuable quality, but for general foundry purposes it is desirable to have all parts of a casting an even gray.

Silicon exerts a powerful influence upon this property of irons, partially

or entirely removing their capacity of chilling.

When silicon is mixed with irons previously low in silicon the fluidity is

It is not the percentage of silicon, but the state of the carbon and the action of silicon through other elements, which causes the iron to be fluid. Silicon irons have always had the reputation of imparting fluidity to other

irons. This comes, no doubt, from the fact that up to 8% or 4% they increase the quantity of graphite in the resulting casting.

A white iron which will invariably give porous and brittle castings can be made solid and strong by the addition of silicon; a further addition of sili made solid and strong by the addition of sincon; a further addition of sincon will turn the iron gray; and as the grayness increases the iron will grow weaker. Excessive silicon will again lighten the grain and cause a hard and brittle as well as a very weak iron. The only softening and shrinkage-lessening influence of silicon is exerted during the time when graphite is being produced, and silicon of itself is not a softener or a lessener of shrinkage; but through its influence on carbon, and only during a certain stage, does it produce these effects.

PHOSPHORUS.—While phosphorus of itself, in whatever quantity present, weakens cast-iron, yet in quantities less than 1.5% its influence is n t sufficiently great to overbalance other beneficial effects, which are exerted before the percentage reaches 1%. Probably no element of itself weakens cast iron as much as phosphorus, especially when present in large quantities.

Shrinkage is decreased when phosphorus is increased. All high-phosphorus pig irons have low shrinkage. Phosphorus does not ordinarily harden cast iron, probably for the reason that it does not increase combined carbon.

The fluidity of the metal is slightly increased by phosphorus, but not to

any such great extent as has been ascribed to it.

The property of remaining long in the fluid state must not be confounded with fluidity, for it is not the measure of its ability to make sharp castings,

or to run into the very thin parts of a mould. Generally speaking, the state ment is justified that, to some extent, phosphorus prolongs the fluidity of the ron while it is filling the mould.

The old Scotch irons contained about 1% of phosphorus. The foundry-irons which are most sought for for small and thin castings in the Eastern States

contain, as a general thing, over 1% of phosphorus. Certain irons which contain from 4% to 7% silicon have been so much used on account of their ability to soften other irons that they have come to be known as "softeners" and as lesseners of shrinkage. These irons are valuable as carriers of silicon; but the irons which are sold most as softeners and shrinkage lesseners are those containing from 1% to 2% of phosphorus. We must therefore ascribe the reputation of some of them largely to the phosphorus and not wholly to the silicon which they contain.

From 1/48 to 1% of phosphorus will do all that can be done in a beneficial

way, and all above that amount weakens the iron, without corresponding benefit. It is not necessary to search for phosphorus-irons. Most irons contain more than is needed, and the care should be to keep it within limits. SULPHUR.—Only a small percentage of sulphur can be made to remain

Soll-Phon.—Only a small percentage of sulphur can be made to remain in carbonized iron, and it is difficult to introduce sulphur into gray cast iron or into any carbonized iron, although gray cast iron often takes from the fuel as much more sulphur as the iron originally contained. Percentages of sulphur that could be retained by gray cast iron cannot materially injure the iron except through an increase of shrinkage. The higher the carbon the iron except through an increase of shrinkage. or the higher the silicon, the smaller will be the influence exerted by sulphur.

The influence of sulphur on all cast iron is to drive out carbon and silicon and to increase chill, to increase shrinkage, and, as a general thing, to decrease strength; but if in practice sulphur will not enter such iron, we shall not have any cause to fear this tendency. In every-day work, how ever, it is found at times that iron which was gray when put into the cupola comes out white, with increased shrinkage and chill, and often with decreased strength. This is caused by decreased silicon, and can be remedied by an increase of silicon.

Mr. Keep's opinion concerning the influence of sulphur, quoted above, is

disagreed with by J. B. Nau (Iron Aye, March 29, 1894). He says:
"Sulphur, in whatever shape it may be present, has a deleterious influence on the iron. It has the tendency to render the iron white by the influence it exercises on the combination between carbon and iron. Pig iron containing a certain percentage of it becomes porous and full of holes, and castings made from sulphurous iron are of inferior quality. This happens especially when the element is present in notable quantities. With foundry-iron containing as high as 0.1% of sulphur, castings of greater strength may be obtained than when no sulphur is present.

That the sulphur contents of pig iron may be increased by the sulphur contained in the coke used, is shown by some experiments in the cupola, reported by Mr. Nau. Seven consecutive heats were made.

The sulphur content of the coke was 1%, and 11.7% of fuel was added to the

Before melting, the silicon ranged from 0,320 to 0,830 in the seven heats after melting, it was from 0.110 to 0.584, the loss in melting being from .100 to .875. The sulphur before melting was from .076 to .090, and after melting from .132 to .174, a gain from .044 to .098.

From the results the following conclusions were drawn:

1. In all the charges, without exception, sulphur increased in the pig iron after its passage through the cupola. In some cases this increase more than doubled the original amount of sulphur found in the pig iron.

The increase of the sulphur contents in the iron follows the elimination of a greater amount of silicon from that same iron. A larger amount of limestone added to these charges would have produced a more basic cinder, and undoubtedly less sulphur would have been incorporated in the iron

3. This coke contained 1% of sulphur, and if all its sulphur had passed into the iron there would have been an average increase of 0.12 of sulphur for the seven charges, while the real increase in the pig iron amounted to only 0.031. This shows that two thirds of the sulphur of the coke was taken up by the iron in its passage through the cupola.

MANGANESE.—Manganese is a nearly white metal, having about the same appearance when fractured as white cast iron. As produced commercially, it is combined with iron, and with small percentages of silicon, phosphorus,

and sulphur.

If the manganese is under 40%, with the remainder mostly iron, and silic

not over 0.50%, the alloy is called spiegeleisen, and the fracture will show flat reflecting surfaces, from which it takes its name.

With manganese above 50%, the iron alloy is called ferro-manganese.

As manganese increases beyond 50%, the mass cracks in cooling, and when

it approaches 98% the mass crumbles or falls in small pieces.

Manganese combines with iron in almost any proportion, but if an iron containing manganese is remelted, more or less of the manganese will escape by volatilization, and by exidation with other elements present in the iron. If sulphur be present, some of the manganese will be likely to unite with it and escape, thus reducing the amount of both elements in the casting.

Cast iron, when free from manganese, cannot hold more than 4.50% of carbon, and 8.50% is as much as is generally present; but as manganese increases, carbon also increases, until we often find it in spiegel as high as 5%, and in ferro-manganese as high as 6%. This effect on capacity to hold carbon is

peculiar to manganese.

Manganese renders cast iron less plastic and more brittle.

Manganese increases the shrinkage of cast iron. An increase of 1% raised the shrinkage 26%. Judging from some test records, manganese does not influence chill at all; but other tests show that with a given percentage of selicon the carbon may be a little more inclined to remain in the combined form, and therefore the chill may be a little deeper. Hence, to cause the chill to be the same, it would seem that the percentage of silicon should be a little higher with manganese than without it.

An increase of 1% of manganese increased the hardness 40%. If a hard chill is required, manganese gives it by adding hardness to the whole casting.

J. B. Nau (Iron Age, March 29, 1894), discussing the influence of manga-

nese on cast iron, says:

Manganese favors the combination between carbon and iron. Its influence, when present in sufficiently large quantities, is even great enough no only to keep the carbon which would be naturally found in pig iron combined, but it increases the capacity of iron to retain larger amounts of car-

bon and to retain it all in the combined state.

Manganese iron is often used for foundry purposes when some chill and hardness of surface is required in the casting. For the rolls of steel-rail mills we always put into the mixture a large amount of manganiferous iron, and the rolls so obtained always presented the desired hardness of surface and in general a mottled structure on the outside. The inside, which always probably any objects of the structure of the control of the structure of the ways cooled much slower, was gray iron. One of the standard mixtures that

invariably gave good results was the following:
50% of foundry iron with 1.3% silicon and 1.5% manganese;

85% of foundry iron with 1% silicon and 1.5% manganese; 15% steel (rail ends) with about 0.85% to 0.40% carbon.

The roll resulting from this mixture contained about 1% of silicon and 1% of manganese

Another mixture, which differed but little from the preceding, was as follows:

45% foundry iron with about 1.3% silicon and 1.5% manganese; 80% foundry iron with about 1% silicon and 1.5% manganese

10% white or mottled iron with about 0.5% to 0.6% Si. and 1.2% Mn.

15% Bessemer steel-rail ends with about 0.35% to 0.40% C. and 0.6% to 1% Mn.

The pix from used in the preceding mixtures contained also invariably from 1.5% to 1.8% of phosphorus, so that the rolls obtained therefrom carried about 1.3% to 1.4% of that element. The last mixture used produced rolls containing on the average 0.8% to 1% of silicon and 1% of manganese. When ever we tried to make those rolls from a mixture containing but 0.2% to 0.3% manganese our rolls were invariably of inferior quality, grayer, and consequently softer. Manganese iron cannot be used indiscriminately for foundry purposes. When greater softness is required in the castings manganese has to be avoided, but when hardness to a certain extent has to be

obtained manganese iron can be used with advantage.

Manganese decreases the magnetism of the iron. This characteristic increases with the percentage of manganese that enters into the composition of the iron. The iron loses all its magnetism when manganese reaches 25% of its composition. For this reason manganese iron has to be avoided in castings of dynamo fields and other pieces belonging to electric machinery,

where magnetic conductibility is one of the first considerations.

Shrinkage of Cast Iron.—Mr. Keep gives a series of curves showing that shrinkage depends on silicon and on the cross-section of the casting, decreasing as the silicon and the section increase. The following "tures are obtained by inspection of the curves:

نبن	Size of Square Bars.	ند.	1	Size of	Squar	e Bars	
Silicon, Per Cent.	in. 1 in. 2 in. 3 in. 4 in.	Silicon, Per Cent.	in.	1 in.	2 in.	3 in.	4 in.
A	Shrinkage, In. per Foot.	ш <u>ч</u>	Sh	rinkag	e, In.	per Fo	ot.
1.00 1.50 2.00	.178 .158 .129 .112 .102 .166 .145 .116 .099 .088 .154 .133 .104 .086 .074	2.50 3.00 3.50	.142 .130 .118	.121 .109 .097	.091 .078 .065	.072 .058 .045	.060 .046 .032

Mr. Keep says. "The measure of shrinkage is practically equivalent to a

mr. neep says. The measure of surinkage is practically equivalent to a chemical analysis of silicon. It tells whether more or less silicon is needed to bring the quality of the casting to an accepted standard of excellence."

Strength in Helation to Silicon and Cross-section.—
In castings one half-inch square in section the strength increases as silicon increases from 1.00 to 3.50; in castings 1 in. square in section the strength is practically independent of silicon, while in larger castings the strength decreases as silicon increases.

The following table shows values taken from Mr. Keep's curves of the approximate transverse strength of 1-in. × 12-in. cast bars of different sizes.

ņ.	Siz	e of S	quare (Cast B	ars.	اند.	Siz	e of So	quare (Cast B	urs.
Silicon, Per Cent.	∦ in.	1 in.	2 in.	3 in.	4 in.	Silicon, Per Cent.	in.	1 in.	2 in.	3 in,	4 in.
<i>а</i> гд,	Stre	ngth c	of a 4-in ection,	ı. × 1 lbs.	2-in.	Pe	Stre	ngth o Se	falir		2-in,
1.00 1.50 2.00	290 324 358	260 272 278	232 228 220	222 212 202	220 208 196	2.50 3.00 3.50	392 426 446	278 276 264	212 202 192	190 180 168	184 172 160

Irregular Distribution of Silicon in Pig Iron.—J. W. Thomas (Iron Aye, Nov. 12, 1891) finds in analyzing samples taken from every other bed of a cast of pig Iron that the silicon varies considerably, the iron coming first from the furnace having generally the highest percentage. In one series of tests the silicon decreased from 2.040 to 1.713 from the first bed to the eleventh. In another case the third bed had 1.250 Si., the seventh 1.718, and the eleventh 1.101. He also finds that the silicon varies in each pig, being higher at the point than at the butt. Some of his figures are: point of pig 2.328 Si., butt of same 1.787.

Some Tests of Cast Iron. (G. Lanza, Trans. A. S. M. E., x., 187.)—The chemical analyses were as follows:

	Gun Iron,	Common from
	per cent.	per cent.
Total carbon	8.51	• • • • • • • • • • • • • • • • • • • •
Graphite	2.80	****
Sulphur	0.138	0.173
Phosphorus	0.155	0.418
Silicon	1.140	1.89

The test specimens were 26 inches long and square in section; those tested with the skin on being very nearly one inch square, and those tested with the skin removed being cast nearly one and one quarter inches square, and afterwards planed down to one inch square.

			Tensile Strength.	Elastic Limit.	of Elas- ticity.
Unplaned common Unplaned gun Planed gun	20,300 to 20,800 27,000 to 28,775	•• ••	= 22,066 = 20,520 = 28,175 = 30,500	6,500 5,833 11,000 8,500	13,194,233 11,943,953 16,130,300 15,932,8

The elastic limit is not clearly defined in cast iron, the elongations increasing faster than the increase of the loads from the beginning of the test. The modulus of elasticity is therefore variable, decreasing as the loads in-

crease. For example, see the results of test of a cast-iron bar on p. 314.

The Strength of Cast Iron depends on many other things besides to chemical composition. Among them are the size and shape of the casting, the temperature at which the metal is poured, and the rapidity of cooling. Internal stresses are apt to be induced by rapid cooling, and slow cooling tends to cause segregation of the chemical constituents and opening of the grain of the metal, making it weak. The relation of these variable conditions to the strength of cast iron is a complex one and as yet but imperfectly understood. (See "Cast-iron Columns," p. 250.)

The author recommends that in making experiments on the strength of cast iron, bars of several different sizes, such as 16, 1, 116, and 2 in. square (or round), should be taken, and the results compared. Tests of bars of one size only do not furnish a satisfactory criterion of the quality of the iron of which they are made. See Trans. A. I. M. E., xxvi., 1017.

CHEMISTRY OF FOUNDRY IRONS.

(C. A. Meissner, Columbia College Q'ly, 1890; Iron Age, 1890.)

Silicon is a very important element in foundry irons. Its tendency when not above 216% is to cause the carbon to separate out as graphite, giving the casting the desired benefits of graphitic iron. Between 216% and 316% silicon is best adapted for iron carrying a fair proportion of low silicon scrap and close iron, for ordinarily no mixture should run below 11/5 silicon to get good castings.

From 3% to 5% silicon, as occurs in silvery iron, will carry heavy amounts scrap. Castings are liable to be brittle, however, if not handled carefully

as regards proportion of scrap used.

From 11/6% to 2% silicon is best adapted for machine work; will give strong

clean castings if not much scrap is used with it.

Below 1% silicon seems suited for drills and castings that have to stand great variations in temperature.

Silicon has the effect of making castings fluid, strong, and open-grained; also sound, by its tendency to separate the graphite from the total carbon, and consequent slight expansion of the iron on cooling, causing it to fill out thoroughly. Phosphorus, when high, has a tendency to make iron fluid, retain its heat longer, thereby helping to fill out all small spaces in casting. retain its nest longer, thereby neighbor to the strong so in castings. It is excellent then high to use in a mixture of low-phosphorus irons, up to 11/28 giving good results, but as said before, the casting should be below \$4.5. It has a good results, but, as said before, the casting should be below 34%. It has a strong tendency when above 1% in pig to make the iron less graphitic, pre-

venting the separation of graphite.

Sulphur in open iron seldom bothers the founder, as it is seldom present to any extent. The conditions causing open iron in the furnace cause low sulphur. A little manganese is an excellent antidote against sulphur in the furnace. Irons above 1% manganese seldom have any sulphur of any con-

sequence.

Graphite is the all-important factor in foundry irons; unless this is present in sufficient amount in the casting, the latter will be liable to be poor. Graphite causes iron to slightly expand on cooling, makes it soft, tough and fluid. (The statement as to expansion on cooling is denied by W. J. Keep.)

Relation of the Appearance of Fracture to the Chemical Composition.—S. H. Chauvenet says when run [from the blast-furnace] the lower bed is almost always close grain, but shows practically the same analysis as the large grain in the rest of the cast. If the iron runs rapidly, the lower bed may have as large grain as any in the cast. If the iron runs rapidly, for, say six beds and some obstruction in the tap-hole causes the seventh bed to fill up slowly and sluggishly, this bed may be close-grain, although the eighth bed, if the obstruction is removed will be open-grain. Neither the graphitic carbon nor the silicon seems to have any influence on the fracture in these cases, since by analysis the graphite and silicon is the same in each. The question naturally arises whether it would not be better to be guided by the analysis than by the fracture. The fracture is a guide, but it is not an infallible guide. Should not the open- and the close-grain iron of the same cast be numbered under the same grade when they have the same analysis?

Mr. Meissner had many analyses made for the comparison of fracture

with analysis, and unless the condition of furnace, whether the iron ran fast or slow, and from what part of pig bed the sample is taken, are known, the fracture is often very misleading. Take the following analyses:

	Α.	В.	C.	D.	E.	F.
Silicon Sulphur Graphitic car Comb. carbon .	4.315 0.008 3.010	4.818 0.008 2.757	4.270 0.007 2.680	3.328 0.083 2.243	3.869 0.006 3.070 0.108	3.861 0.006 3.100 0.096

- A. Very close-grain iron, dark color, by fracture, gray forge.
- B. Open-grain, dark color, by fracture, No. 1.
 C. Very close-grain, by fracture, gray forge.
 D. Medium-grain, by fracture, No. 2, but much brighter and more open

b. Mentuin-grain, by fracture, No. 2, but much originer and more open than A. C, or F.

E. Very large, open-grain, dark color, by fracture, No. 1.

E. Very close-grain, by fracture, gray forge.

By comparing analyses A and B, or E and F, it appears that the close-grain iron is in each case the highest in graphitic carbon. Comparing A and E, the graphite is about the same, but the close-grain is highest in silicon.

Analyses of Foundry Irons. (C. A. Meissner.) SCOTCH IRONS.

Name.	Grade.	Sil icon .	Phos- phorus.	Manga- nese.	Sul- phur.	Graph- ite.	Com. Carbon.
Summerlee	1 1	2.70 2.47	0.545 0.760 1.000	1.80 2.51 1.70	0.01 0.015 0.015	8.09	0.25
Eglinton	2 1 1	3.44 2.70 2.15 2.59	0.810 0.618 0.840	2.90 2.80 1.70	0.013 0.02 0.025 0.010	2.00 8.76 3.75	0.80 0.21 8.75
CarnbroeGlengarnockGlengarnock said	1	1.70 3.08	1.100	1.83	0.008	8.50	0.40
to carry % scrap		4.00	0.900	3.41	0.010	1.78	0.90

AMERICAN SCOTCH IRONS.

No. Sample	Silicon.	Phos- phorus.	Manganese	Sulphur.	No. Grade.	
1 2 8 4 5 5 6 6 6 7	6.00 1.67 2.40 1.28 3.50 2.90 8.44 8.35 8.68	0.430 1.920 1.000 0.690 0.613 0.733 1.000 1.300 0.503	1.00 1.90 1.70 1.40 2.51 1.40 1.70 1.50 2.96	0.015 0.012	1 2 2 2 1	casting.

DESCRIPTION OF SAMPLES .- No. 1. Well known Ohio Scotch iron, almost silvery, but carries two-thirds scrap; made from part black-band ore. Very successful brand. The high silicon gives it its scrap-carrying capacity.

No. 2. Brier Hill Scotch castings, made at scale works; castings demanding more fluidity than strength.

No. 3. Formerly a famous Ohio Scotch brand, not now in the market Made mainly from black-band ore.

No. 4. A good Ohio Scotch, very soft and fluid; made from black-band ore-mixture.

Nos. 5a and 5b. Brier Hill Scotch iron and casting; made for stove purposes; 350 lbs. of iron used to 150 lbs. scrap gave very soft fluid iron; worked well.

No. 6a. Shows comparison between Summerlee (Scotch) (6a) and Brier Hill Scotch (6b). Drillings came from a Cleveland foundry, which found both irone closely alike in physical and working quality. No. 7. One of the best southern brands, very hard to compete with, owing to its general qualities and great regularity of grade and general working.

MACHINE IRONS.

Sample No.	Silicon.	Phos- phorus.	Manga- nese.	Sulphur.	Graphite.	Comb. Carbon.	Grade No.
8	2.80	0.492	0.61	0.015			1
0	1.80	0.262	0.70	0.030			8
10a	2.66	0.770	1.20	0.020	2.51		2
106	8.68	0.411	1.25	0.014	3.05		1
11	2.10	0.415	0.60	0.050			2
12	1.87	0.294	1.51	0.080	2.31	0.78	2 2 2
13	8.10	0.124	trace	0.021			2
14	2.12	0.610	0.80	l	.		
15	1.70	0.682	1.60	1			
16a	1.45	0.470	1.25	0.009			2
16b	1.40	0.316	1.37	0.008			l
17	3.26	0.426	0.25				1
18	0.80	0.164	0.90	0.015	l		1

DESCRIPTION OF SAMPLES.-No. 8. A famous Southern brand noted for fine machine castings.

No. 9. Also a Southern brand, a very good machine iron. Nos. 10a and 10b. Formerly one of the best known Ohio brands. Does not shrink; is very fluid and strong. Foundries having used this have reported very favorably on it.

No. 11. Iron from Brier Hill Co., made to imitate No. 3; was stronger

than No. 3; did not pull castings; was fluid and soft.
No. 13. A Pennsylvania iron, very tough and soft. This is partially Bessemer iron, which accounts for strength, while high silicon makes it soft.
No. 14. Castings made from Brief Hill Co.'s machine brand for scale works,

very satisfactory, strong, soft and fluid.
No. 15. Castings made from Brier Hill Co.'s one half machine brand, one half Scotch brand, for scale works, castings desired to be of fair strength, but very fluid and soft.

No. 16a. Brier Hill machine brand made to compete with No. 8.

No. 18b. Castings (clothes-hooks) from same, said to have worked badly, castings being white and irregular. Analysis proved that some other fron too high in manganese had been used, and probably not weil mixed.

No. 17. A Pennsylvania iron, no shrinkage, excellent machine iron, soft

and strong.

No. 18. A very good quality Northern charcoai iron.

"Standard Grades" of the Brier Hill Iron and Coal Company,

Brier Hill Scotch Iron.—Standard Analysis, Grade Nos. 1 and 2.

 Silicon
 9.00 to 3.00

 Phosphorus
 0.50 to 0.75

 Manganese 2.00 to 2.50

Used successfully for scales, mowing-machines, agricultural implements, novelty hardware, sounding-boards, stoves, and heavy work requiring no special strength.

Brier Hill Silvery Iron.—Standard Analysis	Grade	No.	1.
Silioon			
Phosphorus	1.00	to 1.	50
Managanaga	9 00	+~ 0	or.

Used successfully for hollow-ware, car-wheels, etc., stoves, bumpers, and similar work, with heavy amounts of scrap in all cases. Should be mainly used where fluidity and no great strength is required, especially for heavy work. When used with scrap or close pig low in phosphorus, castings of considerable strength and great fluidity can be made

	Iron.—Standard	Grade No.	1.
Phognhorug		0.50 tr. 0.60	

The best iron for machinery, wagon-boxes, agricultural implements, pump-works, hardware specialties, lathes, stoves, etc., where no large amounts of scrap are to be carried, and where strength, combined with great fluidity and softness, are desired. Should not have much scrap with it.

Regular Machine Iron,-Standard Analysis, Grade Nos. 1 and 2.

Silicon		1.50 to 2.00
Phosphorus	••••••	0.30 to 0.50
Manganese		0.80 to 1.00

Used for hardware, lawn-mowers, mower and reaper works, oil-well machinery, drills, fine machinery, stoves, etc. Excellent for all small fine castings requiring fair fluidity, softness, and mainly strength. Cannot be well used alone for large castings, but gives good results on same when used with above mentioned heavy machine grade; also when used with the Scotch in right proportion. Will carry but little scrap, and should be used alone for good strong castings.

For Axles and Materials Requiring Great Strength, Grade No. 2.

Silicon	. .	1.50
Phosphorus		0.200 and less.
Manganese		. 0.80

This gave excellent results.

A good neutral iron for guns, etc., will run about as fol Silicon	lows:
Phosphorus	0.25
Sulphur Manganese	none,

It should be open No. 1 iron.

This gives a very tough, elastic metal. More sulphur would make tough but decrease elasticity.

For fine coastings demanding elegance of design but no strength, phosphorus to 3.0% is good. Can also stand 1.0% to 2.0% manganese. For work of a hard, abrasive character manganese can run 2.00% in casting.

Analyses of Castings.

Sample No.	Silicon.	Phos- phorus.	Manganese	Sulphur.	Graphite.	Comb. Carbon.
81 32 88	9.50 0.85 1.58 1.84	1.400 0.351 0.397 0.577	2.20 0.92 1.08	0.090 0.040	8.10	0.58
84a 34b 84c 85a	2.50 2.80 2.80	0.749 1,208 0.418	1.04 1.10 1.16 0.54			
35b 35c 35d 35e	8.10 8.80 9.88 4.50	1.880 0.879 0.408 0.660	1.14 0.80 1.10 0.78			
36 87a 87b	8.48 9.66 1.90	1.489 0.900 0.980	0.90 1.30 1.90	0.025		

No. 81. Sewing-machine casting, said to be very fluid and good casting. This is an odd analysis. I should say it would have been too hard and brittle, yet no complaint was made.

No. 32. Very good machine casting, strong, soft, no shrinkage. No. 33. Drillings from an annealer-box that stood the heat very well.

No. 34a. Drillings from door-hinge, very strong and soft. No. 34b. Drillings from clothes-hooks, tough and soft, stood severe hammering

No. 34c. Drillings from window-blind hinge, broke off suddenly at light strain. Too high phosphorus.

No. 35a. Casting for heavy ladle support, very strong.

Nos 35b and 35c. Broke after short usage. Phosphorus too high. Car-

bumpers

No. 35d. Elbow for steam heater, very tough and strong. No. 36. Cog-wheels, very good, shows absolutely no shrinkage. No. 27. Heater top network, requiring fluidity but no strength.

No. 37a. Gray part of above. No. 37b. White, honeycombed part of above. Probably bad mixing and got chilled suddenly.

STRENGTH OF CAST IBON.

Rankine gives the following figures:

13,400 to 29,000, average 16,500 Various qualities, T. S...... 145,000, Compressive strength..... 82,000 to 145,000, Modulus of elasticity..... 14,000,000 to 22,900,000, 112,000 17,000,000

Specific Gravity and Strongth. (Major Wade, 1856.) Third-class guns: Sp. Gr. 7.087, T. S. 20,148. Another lot: least Sp. Gr. 7.163.

T. S. 22,402.

Second-class guns: Sp. Gr. 7.154, T. S. 24,767. Another lot: mean Sp. Gr. 7.302, T. S. 27,232.

First class guns: Sp. Gr. 7.204, T. S. 28,805. Another low greatest Sp. Gr. 7.402, T. S. 31,027.

Strength of Charcoal Pig Iron.—Pig iron made from Salisbury ores, in furnaces at Wassaic and Millerton, N. Y., has shown over 40,000 lbs. T. S. per square inch, one sample giving 42,281 lbs. Muirkirk, Md., iron tested at the Washington Navy Yard showed: average for No. 2 iron, 21,601 lbs.; No. 3, 23,959 lbs.; No. 4, 41,329 lbs.; average density of No. 4, 7.336 (J. C. I. W., v. p. 44.)

I. W.. v. p. 44.)

Nos. 3 and 4 charcoal pig iron from Chapinville, Conn., showed a tensile strength per square inch of from 34,761 lbs. to 41,882 lbs. Charcoal pig iron from Shelby, Ala. (tests made in August, 1891), showed a strength of 34,800 lbs, for No. 3; No. 4, 39,675 lbs.; No. 5, 46,450 lbs.; and a mixture of equal parts of Nos. 2, 3, 4, and 5, 41,470 lbs. (Bull. I. & S. A.)

Variation of Density and Tenacity of Gum-irons.—An increase of density invariably follows the rapid cooling of cast iron, and as general rule the tenacity is increased by the same means. The tenacity generally increases quite uniformly with the density, until the latter ascends to some given point, after which an increased density is accommanded by a to some given point; after which an increased density is accompanied by a diminished tenacity.

The turning-point of density at which the best qualities of gun-iron attain their maximum tenacity appears to be about 7.30. At this point of density, or near it, whether in proof-bars or gun-heads, the tenacity is greatest.

As the density of iron is increased its liquidity when melted is diminished.

This causes it to congeal quickly, and to form cavities in the interior of the casting. (Pamphlet of Builders' Iron Foundry, 1893.)

Specifications for Cast Iron for the World's Fair Build-

ings, 1892.—Except where chilled iron is specified, all castings shall be of tough gray iron, free from injurious cold-shuts or blow-holes, true to pattern, and of a workmanlike finish. Sample pieces I in. square, cast from the same heat of metal in sand moulds, shall be capable of sustaining on a crear span of 4 feet 6 inches a central load of 500 lbs. when tested in the

Specifications for Tests of Cast Iron in 12" B. L. Mortars, (Pamphlet of Builders Iron Foundry, 1893.)—Charcoal Gun Iron.—The tensile strength of the metal must average at each end at least 30,000 lbs. per square inch; no specimen to be over 37,000 lbs. per square inch; but one specimen from each end may be as low as 28,000 lbs. per square inch. The long extension specimens will not be considered in making up these averages, but must show a good elongation and an ultimate strength, for each specimen, of not less than 24,000 lbs. The density of the metal must be such as to indicate that the metal has been sufficiently refined, but not carried so

high as to impair the other qualities.

Specifications for Grading Pig Iron for Car Wheels by Chill Tests made at the Furnace. (Penna. R. R. Specifications, 1883.)—The chill cup is to be filled, even full, at about the middle of every cast from the furnace. The test-piece so made will be 7½ inches long, 3½ inches wide, and 1¾ inches thick, and is to be broken across the centre when entirely cold. The depth of chill will be shown on the bottom of the testentirely cold. The depth of chill will be shown on the bottom of the test-piece, and is to be measured by the clean white portion to the point where gray specks begin to show in the white. The grades are to be by eighths of an inch, viz., 36, 34, 36, 36, 38, 34, 36, etc., until the iron is mottled; the lowest grade being 36 of an inch in depth of chill. The pigs of each cast are to be marked with the depth of chill shown by its test-piece, and each grade is to be kept by itself at the furnace and in forwarding.

Mixture of Cast Iron with Steel.—Car wheels are sometimes

made from a mixture of charcoal iron, anthracite fron, and Bessemer steel. The following shows the tensile strength of a number of tests of wheel mixtures, the average tensile strength of the charcoal iron used being

22,000 lbs.:

				. per sq	. in.
Charcoal i	iron	with	21/6% steel	22,467	
**	• 6	6.	834% steel	26,738	
64	44	66	614% steel and 614% anthracite	24,400	
66	• 6		7165 steel and 7165 anthracite	28 150	
4	**		216% steel, 216% wro't iron, and 61/1% anth		
**	46	• 6	5 % steel, 5% wro't iron, and 10% anth	26,500	
			(Tour C I W	iii n	184 \

Cast Iron Partially Bessemerized .- Car wheels made of parchartes and the restaurable bessementation.—Car wheels made of partially Bessementated iron (blown in a Bessement converter for 3% minutes), chilled in a chill test mould over an inch deep, just as a test of cold blast charcoal iron for car wheels would chill. Car wheels made of this blown iron have run 250,000 miles. (Jour.C. I. W., vl. p. 77.)

Bad Cast Iron.—On October 15, 1891, the cast iron fly-wheel of a large

pair of Corliss engines belonging to the Amoskeag Mfg. Co., of Manchester, N. H., exploded from centrifugal force. The fly-wheel was 30 feet diameter and 110 inches face, with one set of 12 arms, and weighed 116,000 lbs. After the accident, the rim castings, as well as the ends of the arms, were found to be full of flaws, caused chiefly by the drawing and shrinking of the metal. Specimens of the metal were tested for tensile strength, and varied from 15,000 lbs. per square inch in sound pieces to 1000 lbs. in spongy ones. None of these flaws showed on the surface, and a rigid examination of the parts before they were erected failed to give any cause to suspect their true nature. Experiments were carried on for some time after the accident in the Amoskeag Company's foundry in attempting to duplicate the flaws, but with no success in approaching the badness of these castings.

MALLEABLE CAST IRON.

Malleableized cast iron, or malleable iron castings, are castings made of ordinary cast iron which have been subjected to a process of decarbonization, which results in the production of a crude wrought iron. Handles, latches, and other similar articles, cheap harness mountings, plowshares, iron handles for tools, wheels, and pinious, and many small parts of machinery, are made of malleable cast iron. For such pieces charcoal cast iron of the best quality (or other iron of similar chemical composition), should be selected. Coke irons low in silicon and sulphur have been used in place of charcoal irons. The castings are made in the usual way, and are then imbedded in oxide of iron, in the form, usually, of hematite ore, or in peroxide of manganese, and exposed to a full red-heat for a sufficient length of time, to insure the nearly complete removal of the carbon. This decarbonization is conducted in cast-iron boxes, in which the articles, if small, are packed in alternate layers with the decarbonizing material. The largest pieces require the longest time. The fire is quickly raised to the maximum temperature, but at the close of the process the furnace is cooled very slowly. The operation requires from three to five days with ordinary small castings, and may take two weeks for large pieces.

Rules for Use of Malleable Castings, by Committee of Master Carbuilders' Ass'n, 1880.

1. Never run abruptly from a heavy to a light section.

2. As the strength of malleable cast iron lies in the skin, expose as much surface as possible. A star-shaped section is the strongest possible from which a casting can be made. For brackets use a number of thin ribs instead of one thick one.

3. Avoid all round sections; practice has demonstrated this to be the

weakest form. Avoid sharp angles.

4. Shrinkage generally in castings will be 3/16 in. per foot.

Strength of Malleable Cast Iron.—Experiments on the strength of malieable cast iron, made in 1891 by a committee of the Master Carbuilders' Association. The strength of this metal varies with the thickness, as the following results on specimens from ½ in, to 1½ in. in thickness show:

Dimensions.	Tensile Strength.	Elongation.	Elastic Limit.	
in. in, 1.52 by .25 1.52 ' .39 1.53 ' .5 1.53 ' .64 2. ' .78 1.54 ' .88 1.06 '' 1.02 1.38 '' 1.5 1.52 '' 1.54	1b, per sq, in. 34,700 33,700 32,800 32,100 25,100 33,600 30,600 27,400 28,200	per cent in 4 in. 2 2 2 2 114 114 114	lb, per sq. in. 21,100 15,260 17,000 19,400 15,400 19,300 17,600	

The low ductility of the metal is worthy of notice. The committee gives the following table of the comparative tensile resistance and ductility of malleable cast iron, as compared with other materials:

	Ultimate Strength, lb. per sq. in	Comparative Strength; Cast Iron = 1.	Elongation Per Cent in 4 in.	Comparative Ductility; Malleable Cast Iron = 1.
Cast iron	82,000 50,000	1 1.6 2.5 8	0.35 2.00 20.00 10.00	0.17 1 10 5

Another series of tests, reported to the Association in 1892, gave the following:

Thick- ness.	Width.	Area.	Elastic Limit.	Ultimate Strength.	Elongation in 8 in.
in.	in.	sq in.	lb. per sq.	lb. per sq. in.	percent.
.271	2.81	.7615	28,520	82,620	
.293 .89 .41	2.78 2.82 2.79	.8145 1.698 1.144	22,650 20,595 20,280	28,160 82,060 28,650	1.5 1.0
,529	2.76	1.46	19.520	27,875	1.1
.661	2.81	1.857	18,840	25,700	.7
.8	2.76	2.508	18,890	25,120	1.1
1.025	2.89	2.890	18,220	28,720	1.5
1.117	2.81	8.188	17,050	25,510	1.8
1.021	2.83	2.879	18,410	26,950	1.8

WROUGHT IRON.

Influence of Chemical Composition on the Properties of Wrought Iron, (Beardslee on Wrought Iron and Chain Cables, Abridgement by W. Kent. Wiley & Sons, 1879.)—A series of 2000 tests of specimens from 14 brands of wrought iron, most of them of high repute, was made in 1877 by Capt. L. A. Beardslee, U.S.N., of the United States Testing Read | Properties Chamical analyses were made of these income. Testing Board. Forty-two chemical analyses were made of these irons, with a view to determine what influence the chemical composition had upon the strength, ductility, and welding power. From the report of these tests by A. L. Holley the following figures are taken:

	Average Chemical Composition.						
Brand.	Tensile Strength.	8.	P.	Si.	C.	Mn.	Slag.
L	66,598	trace	{ 0.065 { 0.084	0.080 0.105	0.212 0.512	0.005 0.029	0.192 0.452
P	54,363	\$0.009 10.001	0.250	0.182	0.038	0.033	0.848
В	52,764	0.008	0.231	0.156	0.015	0.017	
J	51,754	{0.008 {0.005	0.140 0.291	0.182 0.321	0.027 0.051	trace 0.053	0.678 1.724
0	51,134	{0.004 }0.005	0.067	0.065 0.073	0.045 0.042	0.007	1.168
C	50,765	`0.007	0.169	0.154	0.042	0.021	

Where two analyses are given they are the extremes of two or more analyses of the brand. Where one is given it is the only analysis. Brand L should be classed as a puddled steel.

ORDER OF QUALITIES GRADED FROM No. 1 TO No. 19.

Brand.	Tensile Strength.	Reduction of Area.	Elongation.	Welding Power,
L	1	18	19	most imperfect.
P	6	6	8	badly.
В	12	16	15	best.
J	16	19	18	rather badly.
o	18	1	.4	very good.
Ω	19	12	16	

The reduction of area varied from 54.2 to 25.9 per cent, and the elongation from 29.9 to 8.8 per cent.

tion from 29.9 to 8.3 per cent.

Brand O, the purest iron of the series, ranked No. 18 in tensile strength, but was one of the most ductile; brand B, fquite impure, was below the average both in strength and ductility, but was the best in welding power?, also quite impure, was one of the best in every respect except welding, while L, the highest in strength, was not the most pure, it had the least ductility, and its welding power was most imperfect. The evidence of the influence of chemical composition upon quality, therefore, is quite contra dictory and confusing. The irons differing remarkably in their mechanical properties, it was found that a much more marked influence unchair. properties, it was found that a much more marked influence upon their qualities was caused by different treatment in rolling than by differences in composition.

In regard to slag Mr. Holley says: "It appears that the smallest and most worked iron often has the most slag. It is hence reasonable to con-

clude that an iron may be dirty and yet thoroughly condensed."

In his summary of "What is learned from chemical analysis," he says: "So far, it may appear that little of use to the makers or users of wrought iron has been learned. . . . The character of steel can be surely pred-The character of steel can be surely pred-

in the second control. . . . The character of second and estably predicated on the analyses of the materials; that of wrought iron is altered by subtle and unobserved causes."

Influence of Reduction in Rolling from Pile to Bar on the Strength of Wrought Iron.—The tensile strength of the irons used in Beardske's tests ranged from 45,000 to 62,700 lbs. per sq. in., brank by the property of the pr L. which was really a steel, not being considered. Some specimens of L gave figures as high as 70,000 lbs. The amount of reduction of sectional area in rolling the bars has a notable influence on the strength and elastic limit; the greater the reduction from pile to bar the higher the strength. The following are a few figures from tests of one of the brands:

Size of bar, in. diam. Area of pile, sq. in.:	4 80	8 80	2 72	1 25	16 9	1/4 3
Bar per cent of pile:	15.7	8.83	4.86	8.14	2.17	3 1.6
Tensile strength, lb.:	46,322	47,761	48,280	51,128	52,275	59,585
Elastic limit, lb.:	23 430	96 400	21 200	86 467	90 196	

Specifications for Wrought Iron (F. H. Lewis, Engineers' Club of Philadelphia, 1891).—1. All wrought from must be tough, ductile, fibrous, and of uniform quality for each class, straight, smooth, free from cinderpockets, flaws, buckles, blisters, and injurious cracks along the edges, and must have a workmanlike finish. No specific process or provision of manufacture will be demanded, provided the material fulfils the requirements of these specifications.

2. The tensile strength, limit of elasticity, and ductility shall be determined from a standard test-piece not less than ¼ inch thick, cut from the full sized bar, and planed or turned parallel. The area of cross-section shall not be less than ½ square inch. The elongation shall be measured after breaking on an original length of 8 inches.

3. The tests shall show not less than the following results:

For bar iron in tension	T.S.	= 50,000;	E. L.	= 26,000;	E. L. in 8 in., 18	6
For snape iron in tension	**	= 48,000;	44	= 26,000;	" 159	
For plates under 36 in. wide	**	=48,000;	**	= 26,000;	" 129	
For plates over 36 in. wide	**	= 46,000;	"	= 25,000;	⁶⁴ 109	

4. When full-sized tension members are tested to prove the strength of their connections, a reduction in their ultimate strength of (500 x width of

bar) pounds per square inch will be allowed.

5. All iron shall bend, cold, 180 degrees around a curve whose diameter is twice the thickness of piece for bar iron, and three times the thickness

for plates and shapes.

6. Iron which is to be worked hot in the manufacture must be capable of bending sharply to a right angle at a working heat without sign of

7. Specimens of tensile iron upon being nicked on one side and bent shall show a fracture nearly all fibrous.

8. All rivet iron must be tough and soft, and be capable of bending cold until the sides are in close contact without sign of fracture on the convex side of the curve. Penna. R. R. Co.'s Specifications for Merchant-bar Iron

(1902).-One bar will be selected for test from each 100 bars in a pile. All the iron of one size in the shipment will be rejected if the average tensile strength of the specimens representing it falls below 47.000 lbs. or exceeds 53,000 lbs per sq. in., or if any single specimens show less than 45,000

In the case of flat bars which have to be reduced in width for test an allow. ance of 1,000 lbs per sq. in. will be made, making the rejection limit 46,000 lbs. per sq. in. All the iron of one size in the shipment will be rejected if the average elongation in 8 ins. falls below the following limits: Rounds, 1/4 in. and over, 20%; less than 1/4 in., 16%. Flats pulled as rolled. 20%; flats reduced, 16%.

Nicking and Bending Tests —When necessary to make nicking and bending tests the iron will be held firmly in a vise, nicked lightly on one side and then broken by a succession of light blows on the nicked side. It must

then broken by a succession of light blows on the nicked side. It must when thus broken show a generally fibrous structure, not more than 25¢ crystalline, and must be free from admixture of steel.

Stay-bott Iron. (Penna. R. R. Co.'s specifications, 1900.)—Sample bars must show a tensile strength of not less than 48,000 lbs, per sq. in. and an elongation of not less than 25% in 8 ins. One piece from each lot will be threaded in dies with a sharp V thread, 12 to 1 in. and firmly screwed through two holders having a clear space between them of 5 ins. One holder will be rigidly secured to tre bed of a suitable machine and the other vibrated at right angles to the axis over a space of ½ in. or ½ in. each side of the centre line. Acceptable iron should stand 2,200 double vibrations before breakage.

Specifications for Wrought Iron for the World's Fair Buildings. (Eng'g News, March 26, 1892.)—All iron to be used in the tensile members of open trusses, laterals, pins and bolts, except plate iron over 8 inches wide, and shaped iron, must show by the standard test-pieces a tensile strength in lbs. per square inch of:

52 000 - 7,000 × area of original bar in sq. in.

52,000 circumference of original bar in inches

with an elastic limit not less than half the strength given by this formula, and an elongation of 20% in 8 in.

Plate iron 24 inches wide and under, and more than 8 inches wide, must show by the standard test-pieces a tensile strength of 48,000 lbs. per sq in. with an elastic limit not less than 28,000 lbs. per square inch, and an elementary of the strength not less than 28,000 lbs. per square inch, and an elementary of the strength not less than 48,000 lbs. with an elastic limit not less than 28,000 lbs. per square inch. Plates from 24 inches to 36 inches in width must have an elongation of not less than 10%; those from 36 inches to 48 inches in width the control of the strength of width, 8%; over 48 inches in width, 5%.

All shaped iron, flanges of beams and channels, and other iron not hereinbefore specified, must show by the standard test-pieces a tensile strength in lbs. per square inch of :

$$50,000 - \frac{7,000 \times \text{area of original bar}}{\text{circumference of original bar}}$$

with an elastic limit of not less than half the strength given by this formula, and an elongation of 15% for bars 5% inch and less in thickness, and of 12% for bars of greater thickness. For webs of beams and channels, specifications

for plates will apply.

All rivet iron must be tough and soft, and pieces of the full diameter of the rivet must be capable of bending cold, until the sides are in close contact, without sign of fracture on the convex side of the curve.

Stay-bolt Iron.—Mr. Vauclain, of the Baldwin Locomotive Works, at a meeting of the American Railway Master Mechanics' Association, in 1892, says: Many advocate the softest iron in the market as the best for the riverbule. He helicard in an Iron as hard as was consistent with beging stay-bolts. He believed in an iron as hard as was consistent with heading stay-botts. He believed in an iron as nard as was consistent with neating the bolt nicely. The higher the tensile strength of the iron, the more vibrations it will stand, for it is not so easily strained beyond the yield-point. The Baldwin specifications for stay-bolt iron call for a tensile strength of 50,000 to 52,000 lbs. per square inch, the upper figure being preferred, and the lower being insisted upon as the minimum.

FORMULÆ FOR UNIT STRAINS FOR IRON AND STEEL IN STRUCTURES.

(F. H. Lewis, Engineers' Club of Philadelphia, 1891.) The following formulæ for unit strains per square inch of net sectional area shall be used in determining the allowable working stress in each member of the structure. (For definitions of soft and medium steel see Specifications for Steel.)

Tension Members.						
•	Wrought Iron.	Soft Steel.	Medium Steel.			
Floor-beam hangers or suspenders, forged bars Counter-ties Suspenders, hangers and counters, riveted	Will not be used 6000	Will not be used	7000 7000			
members, net sec- tion	5000 8000	5500 8000	7000 Will not be used			
and tension flanges of girders, net sec- tion	$7000(1 + \frac{\min}{1})$	8% greater than iron	9000(1+)			
Forged eyebars	Will not be used	Will not be used	$9000 \left(1 + \frac{\min}{\max}\right)$			
Lateral or cross-sec- tion rods	1	16,000	(For eyebars only, 17,000)			

Shearing.

	Wrought Iron,	Soft Steel.	Medium Steel.
On pins and shop rivets	1800	6600	7200
On field rivets		5900	Will not be used
In webs of girders		5000	6000

Bearing.

	Wrought Iron.	Soft Steel.	Medium Steel.
On projected semi- intrados of main-pin holes. On projected semi-in- trados of rivet-holes* On lateral pins. Of bed-plates on ma- soury.	12,000 12,000 15,000 250 lbs. per sq. in.	13,200 13,200 16,500	14,500 14,500 18,000

^{*} Excepting that in pin-connected members taking alternate stresses, the bearing stress must not exceed 9000 lbs. for iron or steel.

Bending.

On extreme fibres of pins when centres of bearings are consider d as points of application of strains:

Wrought Iron, 15,000. Soft Steel, 16,000. Medium Steel, 17,000.

	mbression weinne	1 176	
	Wrought Iron.	Soft Steel.	Medium Steel.
One flat and one pin end Chords with pin ends and all end-posts	$7000 \left(1 + \frac{\min}{\max}\right) - 40 \frac{l}{r}$ $7000 \left(1 + \frac{\min}{\max}\right) - 35 \frac{l}{r}$ $7500 - 40 \frac{l}{r}$	10% greater than iron	20% greater than iron

In which formulæ l= length of compression member in inches, and r= least radius of gyration of member in inches. No compression member shall have a length exceeding 45 times its least width, and no post should le used in which l+r exceeds 125.

Members Subject to Alternate Tension and Compression.

			FICOLIO II.
	Wrought Iron.	Soft Steel.	Medium Steel.
For compression only	Use the formulæ above		
gor compressed cary	max. lesser	8% prester	204 oreaton
For the greatest stress	$7000 \left(1 - \frac{\text{max. lesser}}{2 \text{ max. greater}}\right)$	than iron	20% greater than iron

Use the formula giving the greatest area of section.

The compression fianges of beams and plate girders shall have the same cross-section as the tension fianges.

W. H. Burr, discussing the formulæ proposed by Mr. Lewis, says: "Taking the results of experiments as a whole, I am constrained to believe that they indicate at least 15% increase of resistance for soft-steel columns over those of wrought iron, with from 20% to 25% for medium steel, rather than 10% and

of wrongut from, what it is a way of the seem to show that its it eminently for alternate and combined stresses, and for that reason I would give it 15% increase over iron, with about 22% for medium steel.

two grades respectively, are amply justified.
"I should not hesitate to assign 15% and 22% increases over values for iron for bearing and bending of soft and medium steel as being within the safe limits of experience. Provision should also be made for increasing pinshearing, bending and bearing stresses for increasing ratios of fixed to moving loads."

Maximum Permissible Stresses in Structural Materials used in Buildings. (Building Ordinances of the City of Chicago. 1898.) Cast iron, crushing stress: For plates, 15,000 lbs. per square inch; for lintels, brackets, or corbels, compression 13,500 lbs. per square inch, and tension 8000 lbs. per square inch. For girders, beams, corbels, brackets, and trusses, 16,000 lbs. per square inch for steel and 12,000 lbs. for iron.

For plate girders:

girders:

Flange area =
$$\frac{\text{maximum bending moment in ft.-lbs.}}{CD}$$

D = distance between centre of gravity of flanges in feet.

 $C = \begin{cases} 18,500 \text{ for steel.} \\ 10,000 \text{ for iron.} \end{cases}$

Web area =
$$\frac{\text{maximum shear}}{C}$$
. $C = \begin{cases} 10,000 \text{ for steel,} \\ 6,000 \text{ for iron.} \end{cases}$

For rivets in single shear per square inch of rivet area:

For timber girders:

$$S = \frac{cbd^3}{l}.$$

$$b = \text{breadth of beam in inches.}$$

$$d = \text{depth of beam in feet.}$$

$$l = \text{length of beam in feet.}$$

$$l = \text{length of beam in feet.}$$

$$l = \text{longth of beam in feet.}$$

$$l = \text{longth of beam in inches.}$$

$$l =$$

Proportioning of Materials in the Memphis Bridge (Geo. S. Morison, Trans. A. S. C. E., 1898).—The entire superstructure of the Memphis bridge is of steel and it was all worked as steel, the rivet-holes being drilled in all principal members and punched and reamed in the lighter members.

The tension members were proportioned on the basis of allowing the dead load to produce a strain of 20,000 lbs. per square inch, and the live load a strain of 10,000 lbs. per square inch. In the case of the central span, where the dead load was twice the live load, this corresponded to 15,000 lbs. total strain per square inch, this being the greatest tensile strain.

The compression members were proportioned on a somewhat arbitrary basis. No distinction was made between live and dead loads. A maximum

strain of 14,000 lbs. per square inch was allowed on the chords and other large compression members where the length did not exceed 16 times the least transverse dimension, this strain being reduced 750 lbs. for each additional unit of length. In long compression members the maximum length was limited to 30 times the least transverse dimension, and the strains limited to 6,000 lbs. per square inch, this amount being increased by 200 lbs. for each unit by which the length is decreased.

Wherever reversals of strains occur the member was proportioned to resist the sum of compression and tension on whichever basis (tension or compression) there would be the greatest strain per square inch; and, in addition, the net section was proportioned to resist the maximum tension, and the gross section to resist the maximum compression.

The floor beams and girders were calculated on the strain being limited to 10,000 lbs. per square inch in extreme fibres. Rivet-holes in cover-plates and flanges were deducted.

The rivets of steel in drilled or reamed holes were proportioned on the basis of a bearing strain of 15,000 lbs. per square inch and a shearing strain or five lbs. per square inch, and special pains were taken to get the double shear in as many rivets as possible. This was the requirement for shop rivets. In the case of field rivets, the number was increased one-half. The plus were proportioned on the basis of a bearing strain of 18,000 lbs. per square inch and a bending strain of 20,000 lbs. per square inch in expensions the properties of the pine being payer made more than one inch

treme fibre, the diameters of the pins being never made more than one inch

The weight on the rollers of the expansion joint on Pier II is 40,000 lbq. per linear foot of roller, or 3,333 lbs. per linear inch, the rollers being 15 ins. in diameter.

As the sections of the superstructure were unusually heavy, and the strains from dead load greatly in excess of those from moving load, it was thought best to use a slightly higher steel than is now generally used for lighter structures, and to work this steel without punching, all holes being drilled. A somewhat softer steel was used in the floor-system and other lighter

The principal requirements which were to be obtained as the results of

tests on samples cut from finished material were as follows:

	Max. Ultimate Strength, lbs. per sq. inch.	• Min. Ultimate Strength, lbs. per sq. inch.	Min. Elastic Limit, lbs, per sq. in.	Elongation	Min. Per- centage of Reduction at Fracture
High-grade steel.	78,500	69,000	40,000	18	88
Eye-bar steel	75,000	66,000	38,000	20	40
Medium steel	72,500	64,000	37,000	22	44
Soft steel	63,000	55,000	30,000	28	50

TENACITY OF METALS AT VARIOUS TEMPERATURES.

The British Admiralty made a series of experiments to ascertain what loss of strength and ductility takes place in gun-metal compositions when raised to high temperatures. It was found that all the varieties of gun-metal suffer a gradual but not serious loss of strength and ductility up to a certain temperature, at which, within a few degrees, a great change takes place, the strength falls to about one half the original, and the ductility is wholly gone. At temperatures above this point, up to 500, there is little, if any, further loss of strength; the temperature at which this great change and loss of strength takes place, although uniform in the specimens cast from the same pot, varies about 100° in the same composition cast at different temperatures, or with some varying conditions in the foundry process. The temperature at which the change took place in No. 1 series was ascertained to be about 370°, and in that of No. 2, at a little over 250°. Whatever may be the cause of this important difference in the same composition, the fact stated may be taken as certain. Rolled Muntz metal and copper are satisfactory up to 500°, and may be 'used as securing-bolts with safety. Wrought iron, Yorkshire and remanufactured, increase in strength up to 500°, but lose slightly in ductility up to 300°, where an increase begins and continues up to 500°, where it is still less than at the ordinary temperature of the atmosphere. The strength of Landore steel is not affected by temperature up to 500° that its ductility is reduced more than one helf. (Iron Oct.) ature up to 500°, but its ductility is reduced more than one half. (Iron, Oct.

Tensile Strength of Iron and Steel at High Temperatures.—James E. Howard's tests (Iron Age, April 10, 1890) show that the tensile strength of steel diminishes as the temperature increases from 0° until a minimum is reached between 200° and 300° F., the total decrease between 200° and 300° F., the total decrease being about 4000 lbs. per square inch in the softer steels, and from 6000 to 8000 lbs. in steels of over 80,000 lbs. tensile strength. From this minimum point the strength increases up to a temperature of 400° to 650° F, the maximum being reached earlier in the harder steels, the increase amounting to from 10,000 to 20,000 lbs. per square inch above the minimum strength at from 200°

to 300°. From this maximum, the strength of all the steel decreases steadily at a rate approximating 10,000 lbs, decrease per 100° increase of temperature. A strength of 30,000 lbs, per square inch is still shown by .10 C. steel at about 1000° F., and by. 60 to 7.00 C. steel at about 1600° F.

The strength of wrought iron increases with temperature from 0° up to a maximum at from 400 to 600° F., the increase being from 8000 to 10,000 lbs. per square inch, and then decreases steadily till a strength of only 6000 lbs.

per square inch is shown at 1500° F.

Cast iron appears to maintain its strength, with a tendency to increase, until 900° is reached, beyond which temperature the strength gradually diminishes. Under the highest temperatures, 1500° to 1600° F., numerous cracks on the cylindrical surface of the specimen were developed prior to cracks on the cylindrical surface of the specimen were developed prior to rupture. It is remarkable that cast fron, so much inferior in strength to the steels at atmospheric temperature, under the highest temperatures has nearly the same strength the high-temper steels ther have.

Strength of Iron and Steel Boiler-plate at High Temperatures. (Chas. Huston, Jour. F. I., 1877.)

AVERAGE OF THREE TESTS OF EACH.

Temperature F.	68°	575°	925°
Charcoal iron plate, tensile strength, lbs	55,866	68,080	65,343
" " contr. of area	26	23	21
Soft open-hearth steel, tensile strength, lbs	54,600	66,083	64,850
" contr. \$		38	83
" Crucible steel, tensile strength, lbs	64,000	69.266	68,600
" " contr. \$		30	21

Strength of Wrought Iron and Steel at High Temperatures. (Jour. F. I., cxii., 1881, p. 241.) Kollmann's experiments at Oberhausen included tests of the tensile strength of iron and steel at temperatures ranging between 70° and 2000° F. Three kinds of metal were tested, viz., fibrous iron having an ultimate tensile strength of 52,464 lbs., an elastic viz., norous from naving an ultimate tensile strength of 0.2,404 108., an elastic strength of 38,280 lbs., and an elongation of 17.5%; fine-grained iron having for the same elements values of 55.892 lbs., 38,118 lbs., and 20%; and Bessemer steel having values of 84,893 lbs., 55,029 lbs., and 14.5%. The mean ultimate tensile strength of each material expressed in per cent of that at ordinary atmospheric temperature is given in the following table, the fifth column of which exhibits, for purposes of comparison, the results of experiments carried on by a committee of the Franklin Institute in the years 1890 82 1832-86.

out-uv.	Fibrous	Fine-grained	Bessemer	Franklin
Temperature	Wrought	Iron,	Steel,	Institute,
Degrees F.	Iron, p. c.	per cent.	per cent.	per cent.
- 0	100.0	100.0	100.0	96.0
100	100.0	100.0	100.0	102.0
200	100.0	100.0	100.0	105.0
800	97.0	100.0	100.0	106.0
400	95.5	100.0	100.0	106.0
500	92.5	98.5	98.5	104.0
600	88.5	95.5	92.0	99.5
700	81.5	90.0	68.0	92.5
800	67.5	77.5	44.0	75.5
900	44.5	51.5	36.5	53.5
1000	26.0	36.0	81.0	86.0
1100	20.0	30.5	26.5	••••
1200	18.0 16.5	28.0 23.0	22.0 18.0	••••
1800 1400	18.5	19.0	15.0	. •••••
1500	10.0	15.5	12.0	•••••
1600	7.0	12.5	10.0	•••••
1700	5.5	10.5	8.5	••••
1800	4.5	8.5	7.5	· •••••
1900	8.5	7.0	6.5	••••
2000	8.5	5.0	5.0	• • • • •
~000	4.0	5.0	0.0	••••

The Effect of Cold on the Strength of Iron and Steel.— The following conclusions were arrived at by Mr. Styffe in 1865:

⁽¹⁾ That the absolute strength of iron and steel is not diminished by cold, but that even at the lowest temperature which ever occurs in Sweden it is at least as great as at the ordinary temperature (about 60° F.).

(9) That neither in steel nor in iron is the extensibility less in severe cold than at the ordinary temperature.

(3) That the limit of elasticity in both steel and iron lies higher in severe cold.

(4) That the modulus of elasticity in both steel and iron is increased on reduction of temperature, and diminished on elevation of temperature; but that these variations never exceed 0.05 % for a change of temperature of 1.8° F., and therefore such variations, at least for ordinary purposes, are of no special importance.

Mr. C. P. Sandberg made in 1867 a number of tests of iron rails at various temperatures by means of a falling weight, since he was of opinion that, although Mr. Styffe's conclusions were perfectly correct as regards tensile strength, they might not apply to the resistance of iron to impact at low temperatures. Mr. Sandberg convinced himself that "the breaking strain" of iron, such as was usually employed for rails, "as tested by sudden blows or shocks, is considerably influenced by cold; such iron exhibiting at 10° F. only from one third to one fourth of the strength which it possesses at 84° F." Mr. J. J. Webster (Inst. C. E., 1880) gives reasons for doubting the accuracy of Mr. Sandberg's deductions, since the tests at the lower temperature were nearly all made with 21-ft. lengths of rail, while those at the higher temperatures were made with short lengths, the supports in every case being the same distance apart.

the nigher temperatures were made with sold angular, and consequent, where the same distance apart.

W. H. Barlow (Proc. Inst. C. E.) made experiments on bars of wrought iron, cast iron, malleable cast iron, Bessemer steel, and tool steel. The bars were tested with tensile and transverse strains, and also by impact; one half of them at a temperature of 50° F, and the other half at 5° F. The lower temperature was obtained by placing the bars in a freezing mixture, care being taken to keep the bars covered with it during the whole time of

the experiments.

The results of the experiments were summarized as follows:

 When bars of wrought iron or steel were submitted to a tensile strain and broken, their strength was not affected by severe cold (6° F.), but their ductility was increased about 1% in iron and 3% in steel.

When bars of cast iron were submitted to a transverse strain at a low temperature, their strength was diminished about 8% and their flexibility

about 164

8. When bars of wrought iron, malleable cast iron, steel, and ordinary cast iron were subjected to impact at a temperature of 5° F., the force required to break them, and the extent of their flexibility, were reduced as follows, viz.:

	Reduction of Force of Impact, per cent.	Reduction of Flexi- bility, per cent.
Wrought iron, about	8	18
Steel (best cast tool), about Malleable cast iron, about		17 15
Cast iron, about		not taken

The experience of railways in Russia, Canada, and other countries where the winter is severe is that the breakages of rails and tires are far more numerous in the cold weather than in the summer. On this account a softer class of steel is employed in Russia for rails than is usual in more temperate climates.

The evidence extant in relation to this matter leaves no doubt that the capability of wrought iron or steel to resist impact is reduced by cold. Ou the other hand, its static strength is not impaired by low temperatures.

Effect of Low Temperatures on Strength of Railroad Axles. (Thos. Andrews, Proc. Inst. C. E., 1891.)—Axles 6 ft 6 in. long between centres of journals, total length 7 ft. 3½ im., diameter at middle 4½ in., at wheel-sets 5½ im., journals 3¾ × 7 in. were tested by impact at temperatures of 0° and 100° F. Between the blows each axle was half turned over, and was also replaced for 15 minutes in the water-bath.

The mean force of concussion resulting from each impact was ascertained

as follows:

Let h = height of free fall in feet, w = weight of test ball, hw = W = "energy," or work in foot-tons, x = extent of deflections between bearings,

then
$$F$$
 (mean force) = $\frac{W}{x} = \frac{hw}{a}$.

The results of these experiments show that whereas at a temperature of 0° F. a total average mean force of 179 tons was sufficient to cause the breaking of the axies, at a temperature of 100° F. a total average mean force of 428 tons was requisite to produce fracture. In other words, the resistance to concussion of the axies at a temperature of 0° F. was only about 428 of what it was at a temperature of 100° F.

The average total deflection at a temperature of 0° F. was 6.48 in., as against 15.06 in. with the axles at 100° F. under the conditions stated; this represents an ultimate reduction of flexibility, under the test of impact, of about 57% for the cold axles at 0° F., compared with the warm axles at 100° F.

EXPANSION OF IRON AND STEEL BY HEAT.

James E. Howard, engineer in charge of the U.S. testing-machine at Watertown, Mass., gives the following results of tests made on bars 85 inches long (from Age, April 10, 1890);

		Chemical composition,				Coefficient of Expansion.
Metal.	Marks.	c.	Mn.	Si.	Fe by difference.	Per degree F. per unit of length.
Wrought iron Steel	1a 2a 3a 4a 5a 6a 7a 8a 9a 10a	.09 .20 .81 .87 .51 .57 .71 .89	.11 .45 .57 .70 .58 .98 .56 .57 .80	.02 .07 .08 .17 .19	90.80 99.85 99.13 96.93 98.89 96.48 98.63 98.45 98.35 97.95	.0000087803 .0000087861 .0000080859 .000008149 .000008897 .000008891 .000008187 .000008187 .000008187 .000008187 .000008187

DURABILITY OF IRON, CORROSION, ETC.

Durability of Cast Iron.—Frederick Graff, in an article on the Philadelphia water-supply, says that the first cast-iron pipe used there was laid in 1820. These pipes were made of charcoal iron, and were in constant use for 53 years. They were uncoated, and the inside was well filled with tubercles. In sait water good cast iron, even uncoated, will last for a century at least; but it often becomes soft enough to be cut by a knife, as is shown in iron cannon taken up from the bottom of harbors after long submersion. Close-grained, hard white metal lasts the longest in sea water.—

Rugia News. April 23. 1887, and March 26. 1892.

mersion. Close-grained, hard white metal lasts the longest in sea water.—
Engly News. April 23, 1887, and March 26, 1892.
Tests of Iron after Forty Years' Service.—A square link 12
inches broad, I inch thick and about 12 feet long was taken from the Kieff
bridge, then 40 years old, and tested in comparison with a similar link which
had been preserved in the stock-house since the bridge was built. The following is the record of a mean of four longitudinal test-pieces, 1 × 1½ × 8

inches, taken from each link (Stahl und Eisen, 1890):

•	Old Link taken from Bridge.	New Link from Store-house.
Tensile strength per square inch, tons. Elastic limit	21.8	22.2
Elastic limit "	11.1	11.9
Elongation, per cent	14.00	18.49
Contraction, per cent	17.85	18.75

Durability of Iron in Bridges. (G. Lindenthal, Eng'g, May 2, 1881, p. 139.)—The Old Monongahela suspension bridge in Pittsburgh, built in 1815, was taken down in 1822. The wires of the cables were frequently trained to half of their ultimate strength, yet on testing them after 37 years.

use they showed a tensile strength of from 72,700 to 100,000 lbs. per square inch. The elastic limit was from 67,100 to 78,600 lbs. per square inch. Reduction at point of fracture, 35% to 75%. Their diameter was 0.13 inch. A new ordinary telegraph wire of same gauge tested for comparison showed: T. S., of 100,000 lbs.; E. L., 81,550 lbs.; reduction, 57%. Iron rods used as stays or suspenders showed: T. S., 48,770 to 49,720 lbs. per square inch; E. L., 26,880 to 29,200. Mr. Lindenthal draws these conclusions from big tester. his tests:

"The above tests indicate that iron highly strained for a long number of years, but still within the elastic limit, and exposed to slight vibration, will

not deteriorate in quality.

"That if subjected to only one kind of strain it will not change its texture even if strained beyond its elastic limit, for many years. It will stretch and

behave much as in a testing-machine during a long test.

"That iron will change its texture only when exposed to alternate severe straining, as in bending in different directions. If the bending is slight but very rapid, as in violent vibrations, the effect is the same."

Corrosion of Iron Bolts.—On bridges over the Thames in London. bolts exposed to the action of the atmosphere and rain-water were eaten away in 25 years from a diameter of 1/8 in. to 1/2 in., and from 1/8 in. diameter to 5/16 inch.

Wire ropes exposed to drip in colliery shafts are very liable to corrosion. Corrosion of Iron and Steel.—Experiments made at the Riverside Corrosion of Iron and Steel.—Experiments made at the kiverside Iron Works, Wheeling, W. Va., on the comparative liability to rust of iron and soft Bessemer steel: A piece of iron plate and a similar piece of steel, both clean and bright, were placed in a mixture of yellow loam and sand, with which had been thoroughly incorporated some carbonate of soda, nitrate of soda, ammonium chloride, and chloride of magnesium. The earth as prepared was kept moist. At the end of 33 days the pieces of metal were taken out, cleaned, and weighed, when the iron was found to have lost 0.84% of its weight and the steel 0.72%. The pieces were replaced and after 28 days weighed again when the iron was found to have lost 2.06% of its original

or its weight and the steel 0.12%. The pieces were replaced and after 22 days weighed again, when the iron was found to have lost 2.06% of its original weight and the steel 1.73%. (Eng'g, June 28, 1891.)

Corrosive Agents in the Atmosphere.—The experiments of F. Crace Calvert (Chemical News, March 3, 1871) show that carbonic acid, in the presence of moisture, is the agent which determines the oxidation of iron in the atmosphere. He subjected perfectly cleaned blades of iron and steel to the action of different gases for a period of four months, with results as follows:

results as follows:

Dry oxygen, dry carbonic acid, a mixture of both gases, dry and damp oxygen and ammonia: no oxidation. Damp oxygen: in three experiments

one blade only was slightly oxidized.

Damp carbonic acid: slight appearance of a white precipitate upon the iron, found to be carbonate of iron. Damp carbonic acid and oxygen oxidation very rapid. Iron immersed in water containing carbonic acid oxidized rapidly.

Iron immersed in distilled water deprived of its gases by boiling rusted the iron in spots that were found to contain impurities.

Galvanic Action is a most active agent of corrosion. It takes place when two metals, one electro-negative to the other, are placed in contact

and exposed to dampness.

Sulphurous acid (the product of the combustion of the sulphur in coal) is an exceedingly active corrosive agent, especially when the exposed iron is coated with soot. This accounts for the rapid corrosion of iron in railway bridges exposed to the smoke from locomotives. (See account of experiments by the author on action of sulphurous acid in *Jour Frank Inst.*, June, 1875, p. 487.) An analysis of sooty iron rust from a railway bridge showed the presence of sulphurous, sulphuric, and carbonic acids, chlorine, and ammonia. Bloxam states that ammonia is formed from the nitrogen of the air during the process of rusting.

Corrosion in Steam-boilers.-Internal corrosion may be due either to the use of water containing free acid, or water containing sulphate or chloride of magnesium, which decompose when heated, liberating the acid, or to water containing air or carbonic acid in solution. External corrosion rarely takes place when a boiler is kept hot, but when cold it is apt to corrode rapidly in those portions where it adjoins the brickwork or where it may be covered by dust or ashes, or wherever dampuess may lodge. (See Impurities of Water, p. 551, and Incrustation and Corrosion, p. 716.)

PRESERVATIVE COATINGS.

(The following notes have been furnished to the author by Prof. A. H. Sabin.)

Cement.—Iron-work is sometimes protected by bedding in concrete. in which case it is first cleaned and then washed with neat cement before

being imbedded.

Asphaltum.—This is applied hot either by dipping (as water-pipe) or by pouring it on (as bridge floors). The asphalt should be slightly elastic when cold, with a high melting-point, not softening much at 100° F., applied at 800° to 400°; surface must be dry and should be hot; coating should be of considerable thickness.

Paint.—Composed of a vehicle or binder, usually linseed oil or some inferior substitute, or varnish (enamel paints); and a pigment which is a more or less inert solid in the form of powder, either mixed or ground together. The principal pigments are white lead (carbonate) and white zinc (oxide), red lead (peroxide), oxides of iron, hydrated and dehydrated, graphite, lamp-black, chrome yellow, ultramarine and Prussian blue, and various tinting colors. White lead has the greatest body or opacity of white pigments; three coats of it equal five of white zinc; zinc is more brilliant and permanent, but it is liable to peel, and it is customary to mix the two. These are the standard white paints for all uses and the basis of all light colored paints. These are the standard white paints for all uses and the basis of all light colored paints. Anhydrous iron oxides are brown and purplish brown. hydrated iron oxides are yellowish red to reddish yellow, with more or less brown; most iron oxides are mixtures of both sorts. They also contain frequently manganese and clay. They are cheap, and are serviceable paints for wood, and are often used on iron, but for the latter use are falling into disrepute. Graphite used for painting iron contains from 10 to 90% foreign matter, usually silicates and iron oxides. It is very opaque, hence has great covering power, and may be applied in a very thin coat which should be avoided. It retards the drying of oil, hence the necessity of using dryers; these are lead and manganese compounds dissolved in oil which should be avoided. It retards the drying of oil, hence the necessity of using dryers; these are lead and manganese compounds dissolved in oil and turpentine or benzine, and act as carries of oxygen; they are necessary in most paints, but should be used as little as possible. There are many grades of lamp-black; as a rule the cheaper sorts contain oily matter and are especially hard to dry; all lamp-black is slow to dry in oil. It is the principal black on wood, and is used some on iron, usually in combination with varnish or varnish-like compounds. It is very permanent on wood. A gallon of oil takes only a pound of lamp-black to make a paint, while the same amount of oil requires about 40 lbs. of red lead. On this account red-lead paint, which weighs about 30 lbs. per gallon, is the most expensive of all comon paints. It does not dry slowly like other oil paints, but combines with the oil to make a sort of cement; on this account it is used on the joints of steam-pipes, etc. To prevent the mixture of red lead and oil the joints of steam-pipes, etc. To prevent the mixture of red lead and oil setting into a cake, and also to cheapen it, it is often adulterated with whiting or sometimes with white zinc, the proportion of adulterant being sometimes double the lead. Red lead has long had a high reputation as a paint for iron and steel and is still used very extensively; but of late years some of the new paints and varnish-like preparations have displaced it to some extent even on the most important work.

Varnishes.—These are made by melting fossil resin, to which is then added from half its weight to three times its weight of refined linseed oil, and the compound is thinned with turpentine; they usually contain a little dryer. They are chiefly used on wood, being more durable and more brilliant than oil, and are often used over paint to preserve it. Asphaltum is sometimes substituted in part or in whole for the fossil resin, and in this way are made varnishes which have been applied to iron and steel with good results. Asphaltum and animal and vege able tar and pitch have also been simply dissolved in solvents, as benzine or carbon disulphide, and used

for the same purpose.

All these preservative coatings are supposed to form impervious films, keeping out air and moisture; but in fact all are somewhat porous. On this account it is necessary to have a film of appreciable thickness, best formed by successive coats, so that the pores of one will be closed by the next. pigment is used to give an agreeable color, to help fill the pores of the oil film, to make the paint harder so that it will resist abrasion, and to make a thicker film. In varnishes these results are sought to be attained by the reain which is dissolved in the oil. There is no sort of agreement among practical men as to which is the best coating for any particular case; this is probably because so much depends on the preparation of the surface and the care with which the coating is applied, and also because the conditions

of exposure vary so greatly.

Methods of Application.—Too much care cannot be given to the preparation of the surface. If it is wood, it should be dry, and the surface of knots should be coated with some preparation which will keep the tarry matter in the wood from the coating. All old paint or varnish should be removed by burning and scraping. Metallic surfaces should be cleaned by wire brushes and scrapers, and if the permanence of the work is of much importance the scale and oxide should be completely removed by acid pickling or by the sand blast or some equally efficient means. Pickling is usually done with a 10% solution of sulphuric acid; as the solution becomes exhausted it may be made more active by heating. All traces of acid must be removed by washing and the metal must be rapidly dried and painted before it becomes in the slightest degree oxidized. The rand-blast, which has been applied to large work recently and for many years to small work with good results, leaves the surface perfectly clean and dry; the paint must be applied immediately. Plenty of time should always be allowed, usually about a week, for each coat of paint to dry before the next coat is applied; less than two coats should never be used. Two will last three times as long as one coat. Benzine should not be an ingredient in coatings for iron-work, because its rapid evaporation lowers the temperature of the fron and may cause formation of dew on the surface adjacent to the paint which is immediately to be painted.

Cast from water-pipes are usually coated by dipping in a hot mixture of coal-tar and coal-tar pitch; riveted steel pipes by dipping in hot asphalt or by a japan enamel which is baked on at about 400° F. Ships' bottoms are usually coated with some sort of paint to prevent rusting, over which is apread, hot, a poisonous, slowly soluble compound, usually a copper soap, to prevent a duesion of marine constitue.

to prevent adhesion of marine growths.
Galvanized from and tin surfaces should be thoroughly cleaned with benzine and scrubbed before painting. When new they are covered with grease and chemicals used in coating the plates, and these must be removed or the paint will be destroyed.

Quantity of Paint for a Given Surface.—One gallon of paint will cover 250 to 350 sq. ft. as a first coat, depending on the character of the

surface, and from 350 to 450 sq. ft. as a second coat.

Qualities of Paints.—The Railroad and Engineering Journal, vols. liv and iv, 1890 and 1891, has a series of articles on paint as applied to wooden structures, its chemical nature, application, adulteration, etc., by Dr. C. B. Dudley, chemist, and F. N. Pease, assistant chemist, of the Penna, R. R. They give the results of a long series of experiments on paint as applied to

They give the results of a long stree of experiments on parameter approximation proposes.

Bustless Coatings for Iron and Steel.—Tinning, enamelling, lacquering, galvanizing, electro-chemical painting, and other preservative methods are discussed in two important papers by M. P. Wood, in Trans. A. S. M. E., vols, xv and xvi.

A Method of Producing an Inoxidizable Surface on iron and steel by means of electricity has been developed by M. A. de Meritens (Engineering). The article to be protected is placed in a bath of ordinary or distilled water, at a temperature of from 155 to 176 Ft., and an nary or distilled water, at a temperature of from 153° to 176° k., and an electric current is sent through. The water is decomposed into its elements, oxygen and hydrogen, and the oxygen is deposited on the metal, while the hydrogen appears at the other pole, which may either be the tank in which the operation is conducted or a plate of carbon or metal. The current has only sufficient electromotive force to overcome the resistance of the circuit and to decompose the water; for if it be stronger than this, the oxygen combines with the iron to produce a pulverulent oxide, which has no adherence. If the conditions are as they should be, it is only a few minutes after the oxygen appears at the metal before the darkening of the surface shows oxygen appears at the metal nearons the darkening of the surface shows that the gas has united with the iron to form the magnetic oxide Fe₃O₄, which will resist the action of the air and protect the metal beneath it. After the action has continued an hour or two the coating is sufficiently solid to resist the scratch-brush, and it will then take a brilliant polish. If a piece of thickly rusted iron be piaced in the bath, its sasquioxide (Fe₃O₃) is rapidly transformed into the magnetic oxide. This outer layer

has no adhesion, but beneath it there will be found a coating which is actually a part of the metal itself.

In the early experiments M. de Meritens employed pieces of steel only, but in wrought and cast iron he was not successful, for the coating came off with the alightest friction. He then piaced the iron at the negative pole of the apparatus, after it had been already applied to the positive pole. Here the oxide was reduced, and hydrogen was accumulated in the pores of the metal. The specimens were then returned to the anode, when it was found that the oxide appeared quite readily and was very solid. But the result was not quite perfect, and it was not until the bath was filled with distilled water, in place of that from the public supply, that a perfectly satisfactory result was attained.

Manganese Plating of Iron as a Protection from Rust,
-According to the Italian Progress, articles of iron can be protected against

rust by sinking them near the negative pole of an electric bath composed of 10 litres of water, 50 grammes of chloride of manganese, and 200 grammes of nitrate of ammonium. Under the influence of the current the bath deposits on the articles a protecting film of metallic manganese.

A Non-oxidizing Process of Annealing is described by H. P. Jones, in Ring's News, Jan. 2, 1892. The new process uses a non-oxidizing gas, and is the invention of Mr. Horace K. Jones, of Hartford, Coun. Its principal feature consists in keeping the annealing retort in communication with the gas-holder or gas-main during the entire process of heating and cooling, the gas thus being allowed to expand back into the main, and being, therefore, kept at a practically constant pressure.

The retorts are made from wrought-iron tubes. The gas is taken directly

from the mains supplying the city with illuminating gas. If metal which has been blued or slightly oxidized is subjected to the annealing process it comes out bright, the oxide being reduced by the action of the gas.

Comparative tests were made of specimens of steel wire annealed in illuminating gas, in nitrogen, and in an open fire and cooled in ashes, and of specimens of the unannealed metal. The wires were .188 in, in diameter and were turned down to .150 in.

The average results were as follows:

Unannealed, two lots, 5 pieces each, tensile strength av. 97,120 and 80,790 lbs. per sq. in., elongation 7.12% and 8.80%. Annealed in open fire, 8 tests, av. t. s. 63,090, el. 26.76%. Annealed in nitrogen, av. of 3 lots, 13 pieces, t. s. 59,820, el. 29.33%. Annealed in illuminating gas, av. of 3 lots, 13 pieces, t. s. 60,180, el. 28.29%. The elongations are referred to an original length of 1.15 ins.

STEEL.

BELATION BETWEEN THE CHEMICAL COMPOSITION AND PHYSICAL CHARACTER OF STEEL.

W. R. Webster (see Trans. A. I. M. E., vols. xxi and xxii, 1898-4) gives resuits of several hundred analyses and tensile tests of basic Bessemer steel plates, and from a study of them draws conclusions as to the relation of chemical composition to strength, the chief of which are condensed as follows:

The indications are that a pure iron, without carbon, phosphorus, manganese, silicon, or sulphur, if it could be obtained, would have a tensile strength of 34,750 lbs. per square inch, if tested in a 36-inch plate. With this as a base, a table is constructed by adding the following hardening effects, as shown by increase of tensile strength, for the several elements named.

Carbon, a constant effect of 800 lbs. for each 0.01%. Sulphur, 500 0.01%.

Phosphorus, the effect is higher in high-carbon than in low-carbon steels. With carbon hundreths \$\(\text{\chi} \) ... 9 10 11 12 18 14 15 16 17 With carbon hundreths ≴.... 9 10 11 12 18 14 15 16 17 Each .01≴ P has an effect of lbs. 900 1000 1100 1200 1300 1400 1500 1500 1500 Manganese, the effect decreases as the per cent of manganese increases.

.00 .15 .20 .25 .30 .85 .40 .45 .50 .55 Mn being per cent..... to to to to to to to to to to 1.15 .20 .25 .80 .85 .40 .45 .50 .55 .65 Str'gth increases for .01\$ 240 240 220 200 180 160 140 120 100 100 lbs. Total incr. from 0 Mn... 8600 4800 5900 6900 7800 8600 9300 9900 10,400 11,400

390

STEEL. Silicon is so low in this steel that its hardening effect has not been considered.

With the above additions for carbon and phosphorus the following table has been constructed (abridged from the original by Mr. Webster). To the figures given the additions for sulphur and manganese should be made as above.

Estimated Ultimate Strengths of Basic Bessemer Steel Plates.

For Carbon, .06 to .24; Phosphorus, .00 to .10; Manganese and Sulphur, .00 in all cases.

Carl	on.	.06	.08	.10	.12	.14	.16	.18	.20	.22	.24
Phos.	.005	39,950	41,550	48,250	44,950	46,650	48,300	49,900	51.500	53,100	54,700
15	.01	40,350	41,950	43,750	45,550	47,350	49,050	50,650	52,250	53,850	55,450
44	.02	41, 150	42,750							55,350	56,950
	.03	41,950	43,550							56,850	58,450
	.04		41,350							58,350	59,950
44	.05		45,150							59,850	61,450
44	.06		45,950							61.350	62,950
44	.07		46,750							62,850	64,450
44	.08		47,550							64,350	65,950
64	.09		48,350							65,850	67,450
-66	.10		49,150							67,350	68,950
001 Pl		80 lbs.								150 lb	150 lb

In all rolled steel the quality depends on the size of the bloom or ingot from which it is rolled, the work put on it, and the temperature at which it is finished, as well as the chemical composition.

is missied, as well as the chemical composition.

The above table is based on tests of plates \$\frac{3}{2}\$ inch thick and under 70 inches wide; for other plates Mr. Webster gives the following corrections for thickness and width. They are made necessary only by the effect of thickness and width on the finishing temperature in ordinary practice. Steel is frequently spoiled by being finished at too high a temperature.

Corrections for Size of Plates.

	Plates.	Up to 70 ins. wide.	Over 70 ins. wide.
	Inches thick.	Lbs.	Lbs.
3/4	and over		1000
11/16	"		750
56	4		500
9/16	46		250
36	46		- 0
7/16	46	— 500	± 500
36		0	+ 1000
5/16	46	+ 8000	+ 5000

Comparing the actual result of tests of 408 plates with the calculated results, Mr. Webster found the variation to range as in the table below.

Summary of the Differences Between Calculated and Actual Besults in 408 Tests of Plate Steel,

In the first three columns the effects of sulphur were not considered: in the last three columns the effect of sulphur was estimated at 500 lbs. for each .01% of S.

				Universal Mill.	Sheared.	Both Mills.	Universal Mill.	Sheared.	Both Mills.	Both Mills, Corrected for Thickness at 1 Width.
Per		1000 2000 3000 4000 5000	.: ::	23.4 40.9 62.5 75.5 89.5	32.1 48.9 71.3 81.0 91.1	28.4 45.6 67.6 78.7 90.4	24.6 48.5 67.8 82.5 98.0	27.0 54.9 73.0 85.2 92.8	26.0 52.2 70.8 84.1 92.9	55.1 74.7 89.0

The last figure in the table would indicate that if specifications were drawn ealling for steel plates not to vary more than 5000 lbs. T. S. from a specified figure (equal to a total range of 10,000 lbs.), there would be a probability of the rejection of 5% of the blooms rolled, even if the whole lot was made from steel of identical chemical analysis. In 1000 heats only 2% of the heats failed to meet the requirements of the orders on which they were graded; the loss of plates was much less than 1%, as one plate was rolled from each heat and tested before rolling the remainder of the heat.

R. A. Hadfield (Jour. Iron and Steel Inst., No. 1, 1894) gives the strength of

rery pure Swedish iron, remelted and tested as cast, 20.1 tons (45,024 lbs.) per sq. in.; remelted and forged, 21 tons (47,040 lbs.). The analysis of the cast bar was: C, 0.08; Si, 0.04; S, 0.02; P, 0.02; Mn. 0.01; Fe, 99.82.

Effect of Oxygen upon Strength of Steel.—A. Lantz, of the Peine works, Germany, in a letter to Mr. Webster, says that oxygen plays an important rôle—such that, given a like content of carbon, phosphorus, and menganese a blow with greater every content given a careful large. and manganese, a blow with greater oxygen content gives a greater hardness and less ductility than a blow with less oxygen content. The m-thod used for determining oxygen is that of Prof. Ledebur, given in Stahl und Eisen, May, 1892, p. 193. The variation in oxygen may make a difference in strength of nearly 1/2 ton per sq. in. (Jour. Iron and Steel Inst., No. 1, 1894.)

RANGE OF VARIATION IN STRENGTH OF BESSEMER AND OPEN-HEARTH STEELS.

The Carnegie Steel Co. in 1888 published a list of 1057 tests of Bessemer and open-hearth steel, from which the following figures are selected:

Kind of Steel.	Tests.	Elastic	Limit.	Ultii Strei	mate ngth.	Elong per c in 8 in	cent
	No. of	High't.	Lowest	High't.	Lowest	High't.	Lowest
(a) Bess. structural (b) "" (c) Bess. angles (d) O. H. fire-box (e) O. H. bridge	100 170 72 25 20	41,890	39,280 39,970 32,630	71,300 73,540 63,450 62,790 69,940	61,450 65,200 56,130 50,350 63,970	33.00 30.25 34.30 36.00 30.00	28.75 28.15 26.25 25.62 21.75

REQUIREMENTS OF SPECIFICATIONS.

(a) Elastic limit, 35,000; tensile strength, 62,000 to 70,000; elong. 22% in 8 in.
(b) Elastic limit, 40,000; tensile strength, 67,000 to 75,000.
(c) Elastic limit, 30,000; tensile strength, 56,000 to 64,000; elong. 20% in 8 in.
(d) Tensile strength 50,000 to 62,000; elong. 28% in 4 in.
(e) Tensile strength, 64,000 to 70,000; elong. 20% in 8 in.

Strength of Open-hearth Structural Steel. (Pencoyd Iron Works.)—As a general rule, the percentage of carbon in steel determines its hardness and strength. The higher the carbon the harder the steel, the hardness and strength. higher the tenacity, and the lower the ductility will be. The following list exhibits the average physical properties of good open-hearth basic steel:

Per cent Carbon.	Ultimate Strength, lbs. per sq. in.	Elastic Limit, lbs. per sq. in.	Stretch in 8 in., %.	Red. of Area, %	Per cent Carbon.	Ultimate Strength, lbs per sq. in.	Elastic Limit, lbs. per sq. in.	Stretch in e in., g.	Red. of Area, g.
.08	54000	82500	82	60	.17	61600	87000	27	50
.09	54800	83000	31	58	.18	62500	37500	27	49
.10	55700	33500	81	57	.19	63300	38000	26	48
.11	56500	84000	80	56	.20	64200	38500	26	47
.12	57400	84500	30	55	.21	65000	. 39000	25	46
.18 .14	58200	85000	29	54	.22	65800	89500	25	45
.14	59100	85500	29	53	.23	66600	40000	24	44
.15	60000	86000	28	52	.24	67400	40500	24	43
.15	60600	86500	28	51	.25	68200	41000	23	42

The coefficient of elasticity is practically uniform for all grades, and is the same as for iron, viz., 29,000,000 lbs. These figures form the average of a numerous series of tests from rolled bars, and can only serve as an

proximation in single instances, when the variation from the average may be considerable. Steel below .10 carbon should be capable of doubling flat without fracture, after being chilled from a red heat in cold water. Steel of .15 carbon will occasionally submit to the same treatment, but will usually bend around a curve whose radius is equal to the thickness of the specimen; about 90% of specimens stand the latter bending test without fracture. fracture. As the steel becomes harder its ability to endure this bending test becomes more exceptional, and when the carbon ratio becomes .20, little over 25% of specimens will stand the last-described bending test. Steel having about .40% carbon will usually harden sufficiently to cut soft iron and maintain an edge

Mehrtens gives the following tables in Stahl und Eisen (Iron Age, April 90, 1893) showing the range of variation in strength, etc., of basic Bessemer and of basic open-hearth structural steel. The figures in the columns headed Per Cent show the per cent of the total number of charges which came within the range given.

BASIC BESSEMER STEEL, 680 CHARGES.

Elastic Limit, Per pounds per So. in.	80. In.	Elongation, per cent.	Per Cent.
85,500 to 88,400 15.0 88,400 to 39,800 81.6	55,600 to 56,900 18.67 56,900 to 58,300 88.67	21 to 25	
89,800 to 41,200 27.5	58,300 to 59,700 23.53 59,700 to 61,200 15.60	27 to 29	50.44
42,700 to 46,400 9.9		80 to 82.5	

BASIC OPEN-HEARTH STRUCTURAL STEEL, 489 CHARGES.

84,400 to 87,000 12.8	55,800 to 56,900 8.0	20 to 25 21.7
57,000 to 89,800 85.9	56,900 to 59,700 51.8	25 to 26 7.7
89,800 to 42,700 80.2	59,700 to 61,200 19.6	26 to 28 21.3
	61,200 to 62,600 11.2	
44,100 to 48,400 8.5	62,600 to 65,100 9.4	80 to 87.1 24.3

Rivet steel, 19 charges, showed a total range from 51,800 to 56,900 lbs. tensile strength, and 25.3 to 29.8 per cent elongation.

In the basic Bessemer steel over 90% was below 0.08 phosphorus, and a were below 0.10; manganese was below 0.6 in over 90% and below 0.9 in all, sulphur was below 0.05 in 84%, the maximum being 0.071; carbon was below 0.10 in all. In the basic open-hearth steel phosphorms was below 0.06 in 98%, the maximum being 0.08; manganese below 0.06 in 97%; sulphur below 0.07 in 88%, the maximum being 0.12. The carbon ranged from 0.09 to 0.14.

Low Tensile Strength of Very Pure Steel.—Swedish nail-rod open-hearth steel, tested by the author in 1881, showed a tensile strength of only 42,591 lbs. per sq. in. A piece of American nail-rod steel showed 45,021

only 42,591 lbs. per sq. in. A piece of American nail-rod steel showed 45,021 lbs. per sq. in. Both steels contained about 10 carbon and .015 phosphorus, and were very low in sulphur, manganese, and silicon. The pieces tested were bars about 2 × 36 in. section.

Low Strength Due to Insufficient Work. (A. E. Hunt, Trans. A. I. M. E., 1886.)—Soft steel inguts, made in the ordinary way for boiler plates, have only from 10,000 to 20,000 lbs. tensile strength per sq. in., an elongation of only about 10% in 8 in., and a reduction of area of less than 20%. Such ingots, properly heated and rolled down from 10 in. to 14 in. thickness, w.m. give from 50,000 to 65,000 lbs. tensile strength, an elongation in 8 in., of from 23% to 33%, and a reduction of area of from 55% to 70%. Any work stopping short of the above reduction in thickness ordinarily yields intermediate results in its tensile tests. intermediate results in its tensile tests.

Rifect of Finishing Temperature in Bolling.—The strength and ductility of steel depend to a high degree upon fineness of grain, and this may be obtained by having the temperature of the steel rather low, say at a dull red heat, 1300° to 1400° F., during the finishing stage of rolling. In the manufacture of steel rails a great improvement in quality has been obtained by finishing at a low temperature. An indication of the finishing Obtained by missing as a low superscale. At indication of the missing temperature is the amount of shrinkage by cooling after leaving the rolls, The Philadelphia and Reading Railway Company's specification for rails (1902) says, "The temperature of the ingot or bloom shall be such that with rapid rolling and without holding before or in the finishing passes or subsequently, and withoutarificial cooling after leaving the last pass, the distance between hot saws shall not exceed 80 ft. 6 in, for a 30-ft. rail."

Fining the Grain by Annealing,—Steel which is coarse-grained

on account of leaving the rolls at too high a temperature may be made fine-grained and have its ductility greatly increased without lowering its tensile strength by reheating to a cherry red and cooling at once in air. (See paper on "Steel Rails," by Robert Job, Trans. A. I. M. E., 1902.)

Effect of Cold Holling,—Cold rolling of iron and steel increases the elastic limit and the ultimate strength, and decreases the ductility. Major Wade's experiments on bars rolled and polished cold by Lauth's process showed an average increase of load required to give a slight permanent set as follows: Transverse, 162%; torsion, 180%; compression, 181% on short columns 1½ in. long, and 64% on columns 8 in. long; rension, 96%. The hardness, as measured by the weight required to produce equal indentations, was increased 50%; and it was found that the hardness was as great in the centre of the bars as elsewhere. Sir W. Fairbairn's experiments showed an increase in ultimate tensile strength of 50%, and a reduction in the elongation in 10 in. from 2 in. or 20% to 0.79 in. or 7.9%.

Hardening of Soft Steel.—A. E. Hunt (Trans. A. I. M. E., 1888, vol. xii), says that soft steel, no matter how low in carbon, will harden to a certain extent upon being heated red-hot and plunged into water, and that it hardens more when plunged into brine and less when quenched in oil.

An illustration was a heat of open-hearth steel of 0.15% carbon and 0.29% of manganese, which gave the following results upon test-pieces from the same

1/4 in. thick plate.

	Maximum Load.	Elongation in 8 in.	
	lbs. per sq. in.		of Area. Per cent.
Unhardened	55.000	27	62
Hardened in water	74.000	25	50
Hardened in brine		22	48
Hardened in oil	67,700	26	49

While the ductility of such hardened steel does not decrease to the extent that the increased tenacity would indicate, and is much superior to that of normal steel of the high tenacity, still the greatly increased tenacity after hardening indicates that there must be a considerable molecular change in the steel thus hardened, and that if such a hardening should be created locally in a steel plate, there must be very dangerous internal strains caused thereby.

Comparison of Tests of Full-size Eye-bars and Sample Test-pieces of Same Steel Used in the Memphis Bridge. (Geo. S. Morison, Trans. A. S. C. E., 1893.)

Full-Sized Eyebars, Sections $10^{\prime\prime}$ wide $\times1$ to $23/16^{\prime\prime}$ thick.			Sample Bars from Same Melts about 1 in. area.					
Reduc- tion of	Elong			Reduc-	Elon- gation,	Elastic Limit,	Max.	
p.c.	Inches.	p.c.	lbs. per	sq. in.	p. c.	in 8 ins. p. c.	lbs. per	sq. in.
39.6	20.2	16.8	35,100	67,490	47.5	27.5	41,580	73.070
39.7 44.4 88.5	26.6 36.8 38.5	8.2 11.8 17.3	87,680 89,700 88,140	70,160 65,500 65,060	52.6 47.9 47.5	24.4 28.8 27.5	42,650 40,280 41,580	75,6 0 70,280 78,050
40.0 89.4	82.5 36.8	13.5	32,860 31,110	65,600	44.5	20.0	43,750 42,210	75,000 69,730
84.6 82.6	32.9 13.0	13.7	33,990 29,380	63,220 63,100	52.2 48.3	28.1 28.8	40,230 39,090	69,720 71,300
7.3 38.1 31.8	20.8 28.9 24.0	6.9 14.1 11.8	28,080 29,670 32,700	55,160 62,140 65,400	43.2 59.6 40.3	24.2 26.3 25.0	88.320 40,200 39,360	70,220 71,080 69,300
48.6	39.4	19.3	30,500 33,360	58,870 73,550	40.3	25.0 25.5	40,910	70,360 69,900
44.6	32.0 35.8	15.7 14.9	82,520 28,000	60,710 58,720	43.6 44.4	27.0 29.5	40,400	70,490 66,800
41.8	23.5 47.1	13.1 15.1	32,290 29,970	62,270 58.680	42.8 45.7	21.3	40,530	72,240 70,480

The average strength of the full-sized eye-bars was about 8000 lbs. per sq. in., or about 12%, less than that of the sample test-pieces.

TREATMENT OF STRUCTURAL STEEL.

(James Christie, Trans. A. S. C. E., 1893.)

Effect of Punching and Shearing.—There is no doubt that steel of higher tensile strength than is now accepted for structural purposes should not be punched or sheared, or that the softer material may contain elements prejudicial to its use however treated, but especially if punched. But extensive evidence is on record indicating that steel of good quality, in bars of moderate thickness and below or not much exceeding 80,000 lbs. tensile strength, is not any more, and frequently not as much, injured as wrought iron by the process of punching or shearing.

The physical effects of punching and shearing as denoted by tensile test

are for iron or steel:

Reduction of ductility; elevation of tensile strength at elastic limit; reduc-

tion of ultimate tensile strength.

In very thin material the superficial disturbance described is less than in thick; in fact, a degree of thinness is reached where this disturbance practically ceases. On the contrary, as thickness is increased the injury Leco:nes more evident.

The effects described do not invariably ensue; for unknown reasons there

are sometimes marked deviations from what seems to be a general result.

By thoroughly annealing sheared or punched steels the ductility is to a large extent restored and the exaggerated elastic limit reduced, the change being modified by the temperature of reheating and the method of cooling.

It is probable that the best results combined with least expenditure can be obtained by punching all holes where vital strains are not transferred by the rivets; and by reaming for important joints where strains on riveted joints are vital, or wherever perforation may reduce sections to a minimum. The reaming should be sufficient to thoroughly remove the material dis-

turbed by punching; to accomplish this it is best to enlarge punched holes at least 1/4 in diameter with the reamer. **Eiveting.**—It is the current practice to perforate holes 1/16 in. larger than the rivet diameter. For work to be reamed it is also a usual requirement to punch the holes from 1/4 to 8/16 in. less than the finished diameter, the holes being reamed to the proper size after the various parts are

assembled.

It is also excellent practice to remove the sharp corner at both ends of the reamed holes, so that a fillet will be formed at the junction of the body

and head of the finished rivets.

The rivets of either iron or mild steel should be heated to a bright red or yellow heat and subjected to a pressure of not less than 50 tons per square

inch of sectional area.

For rivets of ordinary length this pressure has been found sufficient to completely fill the hole. If, however, the holes and the rivets are exceptionally long, a greater pressure and a slower movement of the closing tool than is used for shorter rivets has been found advantageous in compelling the more sluggish flow of the metal throughout the longer hole.

Welding.-No welding should be allowed on any steel that enters into

Upsetting.—Enlarged ends on tension bars for screw-threads, eyebars, etc. are formed by upsetting the material. With proper treatment and a sufficient increment of enlarged sectional area over the body of the bar the result is entirely satisfactory. The upsetting process should be performed so that the properly heated metal is compelled to flow without folding or

Annealing.—The object of annealing structural steel is for the purpose of securing homogeneity of structure that is supposed to be impaired by un-equal heating, or by the manipulation necessarily attendant on certain processes. The objects to be annealed should be heated throughout to a uniform temperature and uniformly cooled.

The physical effects of annealing, as indicated by tensile tests, depend on the grade of steel, or the amount of hardening elements associated with it: also on the temperature to which the steel is raised, and the method or rate of cooling the heated material.

The physical effects of annealing medium-grade steel, as indicated by ten-The physical enects of addressing meeting from the sale test, are reported very differently by different observers, some claiming directly opposite results from others. It is evident, when all the attendant conditions are considered, that the obtained results must vary both in kind and degree.

The temperatures employed will vary from 1000° to 1500° F.; possibly even a wider range is used. In some cases the heated steel is withdrawn at full temperature from the furnace and allowed to cool in the atmosphere; in others the mass is removed from the furnace, but covered under a muffle, to lessen the free radiation; or, again, the charge is retained in the furnace, and the whole mass cooled with the furnace, and more slowly than by either of the other methods.

The best general results from annealing will probably be obtained by introducing the material into a uniformly-heated oven in which the temperature is not so high as to cause a possibility of cracking by sudden and unequal changing of temperature, then gradually raising the temperature of the material until it is uniformly about 1200° F., then withdrawing the material after the temperature is somewhat reduced and cooling under shelter of a muffle, sufficiently to prevent too free and unequal cooling on

shelter of a nume, smeltently to prevent too free and unequal cooling on the other.

G. G. Mehrtens, Trans. A. S. C. E. 1893, says: "Annealing is of advantage to all steel above 64,000 lbs. strength per square inch, but it is questionable whether it is necessary in softer steels. The distortions due to heating cause trouble in subsequent straightening, especially of thin plates.

"In a general way all unannealed mild steel for a strength of 56,000 lbs. The control of the strength of the st

61,000 lbs. may be worked in the same way as wrought iron. Rough treatment or working at a blue heat must, however, be prohibited. Shearing is to be avoided, except to prepare rough plates, which should afterwards be smoothed by machine tools or files before using. Drifting is also to be avoided, because the edges of the holes are thereby strained beyond the yield point. Reaming drilled holes is not necessary, particularly when yield point. Reaming drilled noies is not necessary, particularly when sharp drills are used and neat work is done. A slight countersinking of the edges of drilled holes is all that is necessary. Working the material while heated should be avoided as far as possible, and the engineer should bear this in mind when designing structures. Upsetting, cranking, and bending ought to be avoided, but when necessary the material should be annealed

after completion.

"The riveting of a mild-steel rivet should be finished as quickly as possible, before it cools to the dangerous heat. For this reason machine work is the best. There is a special advantage in machine work from the fact that the pressure can be retained upon the rivet until it has cooled suffi-

that the pressure can be retained upon the rivet until it has cooled sufficiently to prevent elongation and the consequent loosening of the rivet."

Punching and Drilling of Steel Plates. (Proc. Inst. M. E., Aug. 1887, p. 3:46.)—In Prof. Unwin's report the results of the greater number of the experiments made on iron and steel plates lead to the general conclusion that, while thin plates, even of steel, do not suffer very much from punching, yet in those of 1/4 in. thickness and upwards the loss of tenacity due to punching ranges from 10/8 to 23% in iron plates and from 11/8 to 33% in the case of mild steel. Mr. Parker found the loss of tenacity in steel plates to be as help as fully one third of the original strength of the plate. plates to be as high as fully one third of the original strength of the plate. In drilled plates, on the contrary, there is no appreciable loss of strength. It is even possible to remove the bad effects of punching by subsequent reaming or annealing.

Working Steel at a Blue Heat.—Not only are wrought iron and working steel at a Bille Heat.—Not only are wrought from an oxide coating ranging from light straw to blue on bright steel, 430° to 600° F.), but while they are probably not seriously affected by simple exposure to blueness, even if prolonged, yet if they be worked in this range of temperature they remain extremely brittle after cooling, and may indeed be more brittle than when at blueness; this last point, however, is not certain. (Howe, "Metallurgy of Steel," p. 534.)

Tests by Prof. Krohn, for the German State Railways, show that working

at blue heat has a decided influence on all materials tested, the injury done being greater on wrought iron and harder steel than on the softer steel. The fact that wrought iron is injured by working at a blue heat was reported

by Stromeyer. (Engineering News, Jan. 9, 1892.)

A practice among boiler-makers for guarding against failures due to working at a blue heat consists in the cessation of work as soon as a plate which had been red-hot becomes so cool that the mark produced by rubbing a had been red-not becomes so cool that the mark produced by rutoning shammer-handle or other piece of wood will not glow. A plate which is not hot enough to produce this effect, yet too hot to be touched by the hand, is most probably blue hot, and should under no circumstances be hammered or hent. (C. E. Stroneyer, Proc. Inst. C. E. 1886.)

Welding of Steel.—A. E. Hunt (A. I. M. E., 1892) says: I have neverseen so-called "welded" pieces of steel Julied apart in a testing-machine

otherwise broken at the joint which have not shown a smooth cleavage-plane, as it were, such as in iron would be condemned as an imperfect wold. My experience in this matter leads me to agree with the position taken by Mr. William Metcalf in his paper upon Steel in the Trans. A. S. C. E., vol. xvi., p. 301. Mr. Metcalf says, "I do not believe steel can be welded."

Oil-tempering and Annealing of Steel Forgings,—H. F. J. Porter says (1867) that all steel forgings above 0.1% carbon should be annealed, to relieve them of forging and annealing strains, and that the process of annealing reduces the elastic limit to 4% of the ultimate strength. Oil-tempering should only be practised on this sections, and large forgings should be hollow for the purpose. This process raises the elastic limit above 50% of the ultimate tensile strength, and in some alloys of steel, notably nickel steel, will bring it up to 60% of the ultimate.

Hydraulic Forging of Steel. (See pages 618 and 619.)

INFLUENCE OF ANNEALING UPON MAGNETIC CAPACITY.

Prof. D. E. Hughes (Eng'g, Feb. 8, 1884, p. 180) has invented a "Magnetic Balance," for testing the condition of iron and steel, which consists chiefly of a delicate magnetic needle suspended over a graduated circular index, and a magnet coil for magnetizing the bar to be tested. He finds that the following laws hold with every variety of iron and steel:

1. The magnetic capacity is directly proportional to the softness, or mo-

lecular freedom.

2. The resistance to a feeble external magnetizing force is directly as the

2. The resistance to a feeble external magnetizing loves is unrectly as case hardness, or molecular rigidity.

The magnetic balance shows that annealing not only produces softness in iron, and consequent molecular freedom, but it entirely frees it from all strains previously introduced by drawing or hammering. Thus a bar of iron drawn or hammered has a peculiar structure, say a fibrous one, which gives a greater mechanical strength in one direction than another. This bar, if thoroughly annealed at high temperatures, becomes homogeneous in all directions and has no lower aren traces of its previous strains provides. all directions, and has no longer even traces of its previous strains, provided that there has been no actual separation into a distinct series of fibres.

Effect of Annealing upon the Magnetic Capacity of Different Wires; Tests by the Magnetic Balance.

Decembrica	Magnetic Capacity.			
Description.	Bright as sent.	Annealed.		
Best Swedish charcoal iron, first variety. " " second " third " Swedish Siemens-Martin iron	deg. on scale. 280 236 275 165 218 150 115	deg. on scale. 525 510 508 430 340 391		

Bright-yellow heat, cooled completely in cold water. Yellow-red heat, cooled completely in cold water. Bright yellow, let down in cold water to straw color. " " cooled completely in off	Magnetic Capacity.
" cooled completely in oil	28 32 83
Reheat, cooled completely in water	43 51
the state of the s	58
Annealed, " " ofi	66 72 . 84

STANDARD SPECIFICATIONS FOR STEEL.

The following specifications are abridged from those adopted Aug. 10. 1901, by the American Section of the International Association for Testing Materials.*

Kinds of Steel Used for Different Purposes .- O, open-

hearth; B, Bessemer; C, crucible.

(1) Castings, O, B, C. (2) Azles, O. (3) Forgings, O, B, C. (4) Tires, O, C. (5) Rails, O, B. (6) Splice-bars, O. B. (7) Structural Steel for buildings, O, B. (8) Structural steel for ships, O. (9) Boiler-plate and rivets, O.

CHEMICAL REQUIREMENTS FOR THE ABOVE NINE CLASSES.

(The minus sign after the figures means "or less.")

(The minus sign after the figures means "or less.")

(1) ordinary, P, 0.8a; C, 0.40-; tested castings, P, 0.05-; S, 0.05-.

(2) P, 0.06-; S, 0.06-. Nickel steel, Ni, 3.00 to 4.00; P, 0.04-; S, 0.04-. (3) soft or low carbon, P, 0.10-; S, 0.10-; Class B (see below), P, 0.06-; S, 0.06-. Classes C and D, P, 0.04-; S, 0.04-. (4) P, 0.05-; S, 0.05-; Mn, 0.80-; Si, 0.20+. (5) P, 0.10-; Si, 0.20-; C, a, 0.35 to 0.45; b, 0.38 to 0.48; c, 0.40 to 0.50; d, 0.43 to 0.53; e, 0.45 to 0.55; Mn, a, b, 0.70 to 1.00; c, 0.75 to 1.05; d, e, 0.80 to 1.10. [a, 50 to 59+ lbs. per yard; b, 60 to 69+ lbs.; c, 70 to 79+lbs.; d, 80 to 89+ lbs.; c, 90 to 10bs.] (6) P, 0.10-; C, 0.15-; Mn, 0.30 to 0.60. (7) P, 0.10-. (8) acid, P, 0.08-; S, 0.06-; basic, P, 0.06-; S, 0.06-. (9) a, P, 0.06-; b, c, c, P, 0.C4-; d, P, 0.03-; a, b, S, 0.05-; Mn, 0.30 to 0.60; c, d, e, S, 0.04-; Mn, 0.30 to 0.50. [a, flange or boiler steel, acid; b, do. basic; c, fire-box, acid; d, do. basic; e, extra soft.]

"Where the physical properties desired are clearly and properly specified,

"Where the physical properties desired are clearly and properly specified, the chemistry of the steel, other than prescribing the limits of the injurious impurities, P and S, may in the present state of the art of making steel be safely left to the manufacturer."

PHYSICAL REQUIREMENTS.

(1) Castings subjected to physical tests.

Quality.	Hard.	Medium.	Soft.
Tensile strength, lbs. per sq. in	85,000	70,000	60,000
Yield-point, lbs. per sq. in	38,250	31,500	27,000
Elongation, per cent in 2 ins	15	18	22
Contr. of area, per cent	20	25	30

The above are the minimum requirements. Test-piece 1 in. diam. ing test: Specimen $1 \times 1\frac{1}{2}$ ins. to bend cold around a diam. of 1 in. through 120° for soft and 90° for medium castings.

120° for soft and 90° for medium castings.

(2) Axles.—For car, engine-truck, and tender-truck axles no tensile test is required. For driving-axles, minimum requirements: T. S. 80,000; Y. P. 40,000 for carbon steel (a), 50,000 for nickel steel, 3 to 4 per cent Ni, oil-tempered or annealed (b). Elongation in 2 ins., 18 per cent for a, 25 per cent for b. Contraction of area, 45 per cent for b. Test-piece \(\frac{1}{2}\) in. diam.

Drop-test..--Not required for driving-axles. For other axles one axle from each melt to be tested on a standard R.R. drop-testing apparatus, with supports 3 ft. april 17,500 lbs., supported on prings. The axle shall stand the number of blows named below without rupture and without exceeding at the first blow the deflection stated. It is to be turned over after the first, third, and fifth blows.

Diam. of axle at centre, ins	41	41	4 7	45	48	5	57
No. of blows	5	5	5	5	5.	5	7
Height of drop, ft	24	26	28 1	31	3 4	43	43
Deflection, ins	81	81	8 1	8	8	7	5 1

(3) Steel Forgings.—Classification: A, soft or low carbon; B, carbon steel, not annealed; C, do., annealed; D, do., oil-tempered; E, nickel-steel, annealed; F, do., oil-tempered. Sub-classes: a, solid or hollow forgings, diam. or thickness not over 10 ins.; b, solid forgings, diam. not over 20 ins., or thickness of section not over 15 ins.; c, solid, over 20 ins. diam.; d, solid

^{*}The complete specifications may be found in book form in "American Standard Specifications for Steel," by Albert Ladd Colby (Chemical Publishing Co., Easton, Pa., 1902).

or hollow, a.c.m. or thickness not over 3 ins.; e, do., not over 6 ins. Minimum requirements of test-piece \(\frac{1}{2} \) in. diameter, 2 ins. between gauge-marks:

Kind.	Ten- sile St'gth.	Elastic Limit.	El. in 2 ins., Per Ct.	Contr., Per Ct.	Kind.	T. S.	E. L.	El. in 2 ins., Per Ct	Contr., Per Ct.
Aa Ba Ca Cb Cc Dd De	75,000 80,000 75,000 70,000 90,000	29,000 Y.P. 37,500 Y.P. 40,000 37,500 35,000 55,000 50,000	28 18 22 23 24 20 22	35 30 35 35 30 45 45	Da Ea Eb Ec Fd Fe Fa	80,000 80,000 80,000 95,000 90,000	45,000 50.000 45,000 45,000 65,000 60,000 55,000	25 25 24 21	40 45 45 40 50 50 45

The number and location of test specimens to be taken from a melt, blow. or forging depend upon its character and importance, and must therefore be regulated by individual cases. The yield-point (in steels A and B) shall be determined by observation of the drop of the beam or halt in the gauge of the testing-machine. The elastic limit shall be determined by means of an extensometer, and will be taken at that point where the proportionality changes.

Bending Test.—A specimen 1×1; ins. shall bend cold 180° without fracture on outside of bent portion, as follows. The test may be made by bending or

Around a diam. of ins..... Cc For kind Cab D

(4) Tires.—Physical requirements of test-piece 1 in. diam.; Tires for passenger engines: T.S., 100,000; El. in 2 ins., 12 per cent. Tires for freight engines and car wheels: T.S., 110,000; El., 10 per cent. Tires for switching engines: T.S., 120,000; El., 8 per cent.

*Drop-test.—If a drop-test is called for, a selected tire shall be placed verti-

cally under the drop on a foundation at least 10 tons in weight and subjected to successive blows from a tup weighing 2240 lbs. falling from increasing heights until the required deflection is obtained, without breaking or cracking. The minimum deflection must equal $D^2 + (40T^2 + 2D)$, D being intering. The minimum deflection must equal $D^2 + (4017)$ nal diameter and T thickness of tire at centre of tread.

(5) **Rails.**—One drop-test shall be made on a piece of rail not more than 6 ft. long, selected from every fifth blow of steel. The rail shall be placed head upwards on solid supports 3 ft. apart, which are part of, or firmly secured to, an anvil-block weighing at least 20,000 lbs., and subjected to the following impact tests.

Weight of rails, lbs. per yd. 45 to 55 55 to 65 65 to 75 75 to 85 85 to 100

latter tests fail, all the rails of the blow which they represent will be rejected, but if both tests meet the requirements, all the rails of the blow will be accepted.

(6) **Splice-bars.**—Tensile strength of a specimen cut from the head of the bar, 54,000 to 64,000 lbs.; yield-point, 32,000 lbs. Elongation in 8 ins., not less than 25 per cent. A test specimen cut from the head of the bar shall bend 180° flat on itself without fracture on the outside of the bent portion. If preferred, the bending test may be made on an unpunched splice-bar, which shall be first flattened and then bent. One tensile test and one bending test to be made from each blow or melt of steel.

(7) Structural Steel for Buildings.

Class.	Rivet-steel.	Medium Steel.
Tensile strength, lbs. per sq. in. Yield-point, not less than. Elongation in 8 ins., not less than.	1 T.S.	60,000-70,000 † T. S. 22 per cent.

Modifications in elongation requirements: For each increase of 1 in. in thickness above 1 in., a deduction of 1 per cent in the specified elongation. For each decrease of $\frac{1}{16}$ in. in thickness below $\frac{1}{16}$ in., a deduction of $2\frac{1}{1}$ per

For pins the required elongation shall be 5 per cent less than that specified, as determined on a test specimen the centre of which shall be 1 in.

from the surface.

Bending Tests.—Rivet-steel shall bend cold 180° flat on itself, and medium steel 180° around a diameter equal to the thickness of the specimen, without fracture on the outside of the bent portion.

One tensile and one bending-test specimen shall be taken from the finished

material of each melt or blow.

(8) Structural Material for Bridges and Ships.

Class.	Rivet-steel.	Soft Steel.	Medium Steel.
Tens. str., lbs. per sq. in	} T. S.	52,000-62,000	60,000-70,000
Y. P., not less than		½ T. S.	½ T. S.
El. in 8 ins. not less than.		25 per cent.	22 per cent.

Modifications in elongation: Same as in structural steel for buildings. Eyebars.—Full-sized tests: T. S. not less than 55,000 lbs.; El., 12} per cent. in 15 ft. of the body.

Bending Tests.—Rivet and soft steel, 180° flat on itself, and medium steel 180° around a diameter equal to the thickness of the specimen, without fracture on the outside of the bent portion.

(9) Boiler-plate and Rivet-steel.

Class.	Flange- or Boiler-steel.	Fire-box Steel.	Extra-soft Steel.
T. S., lbs per sq. in	55,000-65,000	52,000-62,000	45,000-55,000
Y. P., not less than	½ T. S.	½ T. S.	† T. S.
El. in 8 ins. not less than	25 per cent.	26 per cent.	28 per cent.

Modifications in elongation requirements for thin and thick material same

as in structural steel for buildings.

Bending Tests.—A specimen cut from the rolled material, both before and after quenching, shall bend cold 180° flat on itself without fracture on the outside of the bent portion. For the quenched test the specimen shall be heated to a light cherry-red as seen in the dark and quenched in water of a temperature between 80° and 90° F. Number of test-pieces: One tensile, one cold-bending, and one quenched-bending specimen will be furnished from each plate as it is rolled, and two specimens for each kind of test from each melt of rivet-rounds.

Homogeneity Test for Fire-box Steel.—This test is made on one of the

broken tensile-test specimens, as follows:

broken tensile-test specimens, as follows:
A portion of the test-piece is nicked with a chisel, or grooved on a machine, transversely about a sixteenth of an inch deep, in three places about 2 in. apart. The first groove should be made on one side, 2 in. from the square end of the piece; the second, 2 in. from it on the opposite side; and the third, 2 in. from the last, and on the opposite side from it. The test-piece is then put in a vise, with the first groove about \(\frac{1}{2}\) in above the jaws, care being taken to hold it firmly. The projecting end of the test-piece is then broken off by means of a hammer, a number of light blows being used, and the bending being away from the groove. The piece is broken at the other two grooves in the same way. The object of this treatment is to open and render visible to the eve any seams due to failure to weld up. or to and render visible to the eye any seams due to failure to weld up, or to foreign interposed matter, or cavities due to gas bubbles in the ingot. After rupture, one side of each fracture is examined, a pocket lens being used if necessary, and the length of the seams and cavities is determined. The sample shall not show any single seam or cavity more than 1 in long in either of the three fractures.

VARIOUS SPECIFICATIONS FOR STEEL.

Structural Steel.—There has been a change during the ten years from 1890 to 1890, in the opinions of engineers, as to the requirements in specifications for structural steel, in the direction of a preference for metal of low tensile strength and great ductility. The following specifications of different dates are given by A. E. Hunt and G. H. Clapp, Trans. A. I. M. E. 1390 xix, 926:

TENSION MEMBERS.	1879.	1881.	1882.	1885.	1887.	1889.
Elastic limit	50,000	40@45,000	40,000	40,000	40,000	38,000
Tensile strength	80,000	70@80,000	70,000	70,000	67@.75,000	63@70,000
Elongation in 8 in	12%	18%	18%	18%	20%	22%
Reduction o. area	20%	80%	45%	42%	424	45%

F. H. Lewis (Iron Age, Nov. 8, 1892) says: Regarding steel to be used under the same conditions as wrought iron, that is, to be punched without reaming, there seems to be a decided opinion (and a growing one) among engineers, that it is not safe to use steel in this way, when the ultimate tensile strength is above 65,000 lbs. The reason for this is, not so much because there is any marked change in the material of this grade, but because all steel, especially Bessemer steel, has a tendency to segregations of carbon and phosphorus, producing places in the metal which are harder than they normally should be. As long as the percentages of carbon and phosphorus are kept low, the effect of these segregations is inconsiderable; but when these percentages are increased, the existence of these hard spots in the metal becomes more marked, and it is therefore less adapted to the treatment to which wrought iron is subjected.

There is a wide consensus of opinion that at an ultimate of 64,000 to 65,000 lbs. the percentages of carbon and phosphorus (which are the two hardening elements) reach a point where the steel has a tendency to become tender, and to crack when subjected to rough treatment.

A grade of steel, therefore, running in ultimate strength from 54,000 to 62,000 lbs., or in some cases to 64,000 lbs., is now generally considered a proper material for this class of work.

proper material for this class of work.

A. E. Hunt, Trans. A. I. M. E. 1892, says: Why should the tests for steel be so much more rigid than for iron destined for the same purpose? Some of the reasons are as follows: Experience shows that the acceptable qualities of one melt of steel offer no absolute guarantee that the next melt to it, even though made of the same stock, will be equally satisfactory. Again, good wrought iron, in plates and angles, has a narrow range (from \$6,000 to \$7,000 lbs.) in elastic limit per square inch, and a tensile strength of elastic limit is from \$7,000 to \$0,000 lbs., and in tensile strength from 48,000 to 130,000 lbs. per square inch, with corresponding variations in ductility. Moreover, steel is much more susceptible than wrought iron to widely vary. Moreover, steel is much more susceptible than wrought iron to widely varying effects of treatment, by hardening, cold rolling, or overheating.

It is now almost universally recognized that soft steel, if properly made

and of good quality, is for many purposes a safe and satisfactory substitute for wrought iron, being capable of standing the same shop-treatment as wrought iron. But the conviction is equally general, that poor steel, or an unsuitable grade of steel, is a very dangerous substitute for wrought iron even under the same unit strains.

For this reason it is advisable to make more rigid requirements in selecting material which may range between the brittleness of glass and a duc-

tility greater than that of wrought iron.

Boller, Ship, and Tank Plates.—Different specifications are the following (189):

United States Navy.—Shell: Tensile strength, 58,000 to 67,000 lbs. per sq. in.; elongation, 22% in 8-in. transverse section, 25% in 8-in. longitudinal section, Flange: Tensile strength, 56,000 bts.; elongation, 26% in 8 inches. Chemical requirements: P. not over .035%; S. not over .040%.

Chemical requirements: P. not over .030; S. not over .040%.
Cold-bending test: Specimen to stand being bent flat on itself.
Quenching test: Steel heated to cherry-red, plunged in water 83° F., and
to be bent around curve 1½ times thickness of the plate.
British Admirulty.—Tensile strength, 83,40 to 67,200 lbs.; elongation in
8 in., 20%; same cold-bending and quenching tests as U. S. Navy.
American Bofter-makers' Association.—Tensile strength, 55,000 to 65,000
bs.; elongation in 8 in., 20% for plates ¾ in. thick and under; \$2% for plates
¾ in. to ¾ in.; 25% for plates ¾ in. and over.

Cold-bending test: For plates 1/4 in. thick and under, specimen must bend back on itself without fracture; for plates over 1/4 in. thick, specimen must withstand bending 180° around a mandril 11/4 times the thickness of the plate.

Chemical requirements: P not over .040%; S not over .030%.

American Shipmasters' Association.—Tensile strength, 62,000 to 72,000

lbs.: elongation, 16% on pieces 9 in. long.

Strips cut from plates, heated to a low red and cooled in water the temperature of which is 82° F., to undergo without crack or fracture being doubled over a curve the diameter of which does not exceed three times the thickness of the piece tested.

thickness of the piece tested.

Steel Plate Used in the Construction of Cars. (Penna. R. R., 1899.*)—The material desired has the following composition: C, 0.12; Mn, 0.85; Sl, 0.05; P, not above 0.04; S, not above 0.08. It will be rejected if P exceeds 0.05, or if it shows a tensile strength below \$2,000 or above 62,000 lbs. per sq. in., or if the percentage of elongation in 8 ins. is less than the quotient of 1,500,000 + the tensile strength.

Steel Billets for Main and Parallel Rods. (Penna. R. R., 1893.)

One billet from each lot of 25 billets or smaller shipment of steel for main a parallel rods for locomotives will layer a nice drawn from it under the

or parallel rods for locomotives will have a piece drawn from it under the hammer and a test-section will be turned down on this piece to % in. in diameter and 2 in. long. Such test-piece should show a tensile strength of 85,000 lbs. and an elongation of 15%.

No lot will be acceptable if the test shows less than 80,000 lbs. tensile

strength or 19% elongation in 2 in.

Strength or 13% clougation in z in.

Bar Spring Steel. (Penna. R. R., 1901.)—Bars which vary more than 0.01 in. in thickness, or more than 0.02 in. in width, from the size ordered, or which break where they are not nicked, or which, when properly nicked and held, fall to break square across where they are nicked, will be returned. The metal desired has the following composition: Carbon, 1.00%; manganese, 0.85%; phosphorus, not over 0.08%; silicon, not over 0.15%; sulphur, not over 0.08%; copper, not over 0.08%.

Shipments will not be accepted which show on analysis less than 0.90% or over 1.10% of carbon, or over 0.50% of manganese, 0.05% of phosphorus, 0.25%

of silicon, 0.05% of sulphur, and 0.05% of copper.

Steel for Crank=pins. (Penna R. R., 1897.)—The metal desired has the following composition: 0, 0.45; Mn, not above 0.05; Si, not above 0.05; P, not above 0.08; S, not above 0.04. The tensile strength should be 85,000 lbs. per sq. in., and the elongation 18% in 8 in. Borings for analysis will be taken from one axle out of 3 lot of 51. They will be drilled parallel with the axis with a \(\frac{1}{2}\)-in. drill, starting from a punch-march located on the end, 40 per cent of the distance from the centre to the circumference. Two pieces from this pin will also be tested physically. The lot will be rejected if the

from this pin will also be tested physically. The lot will be rejected if the P is above 0.05%, or if either test-piece shows less than 80,000 lbs. or above 95,000 lbs. T. S., less than 12% elongation, or if the T. S. of the two test-pieces differs more than 5,000 lbs. or the elongation more than 5%. Dr. Chas. B. Dudley, chemist of the P. R. R. (Trans. A. I. M. E. 1892), referring to tests of crank-pins, says: In testing a recent shipment, the piece from one side of the pin showed 88,000 lbs. strength and 22% elongation, and the piece from the opposite side showed 108,000 lbs. strength and 14% elongation. Each piece was above the specified strength and ductility, but the lack of uniformity between the two sides of the pin was so marked that it was finally determined not to put the lot of 50 pins in use. To rurard against was finally determined not to put the lot of 50 pins in use. To guard against trouble of this sort in future, the specifications are to be amended to require that the difference in ultimate strength of the two specimens shall not be more than 3000 lbs.

Steel Bivets. (H. C. Torrance, Amer. Boiler Mfrs. Assn., 1990.)-The Government requirements for the rivets used in boilers of the cruisers built in 1890 are: For longitudinal seams, 88,000 to 67,000 lbs. tensile strength; elongation, not less than 36% in 8 in., and all others a tensile strength of \$6,000 to 58,000 lbs., with an elongation of not less than 30%. They shall be capable of being flattened out cold under the hammer to a thickness of one half the diameter, and of being flattened out hot to a thickness of one third

^{*} The Penna. R. R. specifications of the several dates given are still in force, July, 1902.

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the diameter without showing cracks or flaws. The steel must not contain more than .035 of 1% of phosphorus, nor more than .04 of 1% of sulphur.

A lot of 20 successive tests of rivet steel of the low tensile strength quality and 12 tests of the higher tensile strength gave the following results:

	Low Steel.	Higher.
Tensile strength, lbs. per sq. in	51.230 to 54,100	59,100 to 61,850
Elastic limit, lbs. per sq. in	31,050 to 3 3,190	32,080 to 83,070
Elongation in 8 in., per cent	80.5 to 35.25	28.5 to 31,75
Carbon, per cent	.11 to .14	.16 to .18
Phosphorus	.027 to .029	.08
Sulphur	.038 to .035	.033 to .035

The safest steel rivets are those of the lowest tensile strength, since they are the least liable to become hardened and fracture by hammering, or to break from repeated concussive and vibratory strains to which they are subjected in practice. For calculations of the strength of riveted joints the tensile strength may be taken as the average of the figures above given, or 52,665 lbs., and the shearing strength at 45,000 lbs. per sq. in.

MISCELLANEOUS NOTES ON STEEL.

May Carbon be Eurned Out of Steel?—Experiments made at the Laboratory of the Penna. Railroad Co. (Specifications for Springs, 1889) with the steel of spiral springs, show that the place from which the borings are taken for analysis has a very important influence on the amount of carbon found. If the sample is a piece of the round bar, and the borings are taken from the end of this piece, the carbon is always higher than if the borings are taken from the fide of the piece. It is common to find a difference of 0.10% between the centre and side of the bar, and in some cases the difference is as high as 0.23%. Furthermore, experiments made with samples taken from the drawn out end of the bar show, usually, less carbon than samples taken from the round part of the bar, even though the borings may be taken out of the side in both cases.

Apparently during the process of reducing the metal from the ingots to the round bar, with successive heatings, the carbon in the outside of the bar is burned out.

"Recalescence" of Steel.—If we heat a bar of copper by a flame of constant strength, and note carefully the interval of time occupied in passing from each degree to the next higher degree, we find that these intervals increase regularly, i.e., that the bar heats more and more slowly, as its temperature approaches that of the flame. If we substitute a bar of steel for one of copper, we find that these intervals increase regularly up to a certain point, when the rise of temperature is suddenly and in most cases greatly retarded or even completely arrested. After this the regular rise of temperature is resumed, though other like retardations may recur as the temperature is greatly retarded when it reaches a certain point in dull redness. If the steel contains much carbon, and it certain favoring conditions be maintained, the temperature, after descending regularly, suddenly rises spontaneously vary abruptly, remains stationary a while, and then redescence."

These retardations indicate that some change which absorbs or evolves

These retardations indicate that some change which absorbs or evolves heat occurs within the metal. A retardation while the temperature is rising points to a change which absorbs heat; a retardation during cooling points to some change which evolves heat. (Henry M. Howe, on "Heat Treatment of Steel," Trans. A. I. M. E., vol. xxii.)

Effect of Nicking a Steel Bar.—The statement is sometimes made that, owing to the homogeneity of steel, a bar with a surface crack or nick in one of its edges is liable to fail by the gradual spreading of the nick, and thus break under a very much smaller load than a sound bar. With iron it is contended this does not occur, as this metal has a fibrous structure. Sir Benjamin Baker has, however, shown that this theory, at least so far as statical stress is concerned, is opposed to the facts, as he purposely made nicks in specimens of the mild steel used at the Forth Bridge, but found that the tensile strength of the whole was thus reduced by only about one ton per square inch of section. In an experiment by the Union Bridge Company a full-sized steel counter-bar, with a screw-turned buckle connection, was tested under a heavy statical stress, and at the same time a weight weighing 1040 lbs. was allowed to drop on it from various heights. The bar was first broken by ordinary statical strain, and showed a breaking stress of

66,800 lbs. per square inch. The longer of the broken parts was then placed in the machine and put under the following loads, whilst a weight, as already mentioned, was dropped on it from various heights at a distance of five feet from the sleeve-nut of the turn-buckle, as shown below:

The weight was then shifted so as to fall directly on the sleeve-nut, and the test proceeded as follows:

It will be seen that under this trial the bar carried more than when originally tested statically, showing that the nicking of the bar by screwing had not appreciably weakened its power of resisting shocks.—Engly News.

Electric Conductivity of Steel.—Louis Campredon reports in Le

Receive Conditions of Steel,—Louis campreson reports in Learning form 0.094 to 1.14 C; 0.21 to 0.54 Mn; Si, S, and P low. The figures show that the purer and softer the steel the better is its electric conductivity, and, furthermore, that manganese is the element which most influences the conductivity. The results may be expressed by the formula $R=5.2+6.28\pm0.3$; in which R= relative resistance, copper being taken as 1, and S= the sum of the percentages of C, P, S, Si, and Mn. The conclusions are confirmed by J. A. Capp, in 1903, Trans. A. I. M. E., vol. xxxiv, who made forty-five experiments on steel of a wide range of composition. His results may be expressed by the formula $R=5.5+4S\pm1$. High manganese increases the resistance at an increasing rate. Mr. Capp proposes the following specification for steel to make a satisfactory third rail, having a resistance eight times that of copper: C, 0.15; Mn, 0.30; P, 0.06; Si, 0.05; none of these figures to be exceeded.

Specific Gravity of Soft Steel. (W. Kent, Trans. A. I. M. E., xiv. 585.)—Five specimens of boiler-plate of C. 0.14, P. 0.03 gave an average sp. gr. of 7.932, maximum variation 0.008. The pieces were first planed to remove all possible scale indentations, then filed smooth, then cleaned in dilute sulphuric acid, and then boiled in distilled water, to remove all traces

of air from the surface.

The figures of specific gravity thus obtained by careful experiment on bright, smooth pieces of steel are, however, too high for use in determining the weights of rolled plates for commercial purposes. The actual average thickness of these plates is always a little less than is shown by the calipers, on account of the oxide of iron on the surface, and because the surface is not perfectly smooth and regular. A number of experiments on commercial plates, and comparison of other authorities, led to the figure 7.854 as the average specific gravity of open-hearth boiler-plate steel. This figure is easily remembered as being the same figure with change of position of the decimal point (.7854) which expresses the relation of the area of a circle to that of its circumscribed square. Taking the weight of a cubic foot of water at 62° F. as 62.36 lbs. (average of several authorities), this figure gives 489.75 lbs. as the weight of a cubic foot of steel, or the even figure, 490 lbs., may be taken as a convenient figure, and accurate within the limits of the error of observation.

A common method of approximating the weight of iron plates is to consider them to weigh 40 lbs. per square foot one inch thick. Taking this weight and adding 2π gives almost exactly the weight of steel boiler-plate given above $(40 \times 12 \times 1.02 = 489.6 \, \text{lbs.}$ per cubic foot).

Occasional Failures of Bessemer Steel.—G. H. Clapp and A. E. Hunt, in their paper on "The Inspection of Materials of Construction in

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the United States" (Trans. A. I. M. E., vol. xix), say: Numerous instances could be cited to show the unreliability of Bessemer steel for structural purposes. One of the most marked, however, was the following: A 12-in, 1-beam weighing 30 lbs. to the foot, 20 feet long, on being unloaded from a car broke in two about 6 feet from one end.

The analyses and tensile tests made do not show any cause for the failure. The cold and quench bending tests of both the original ¾-in, round test-pieces, and of pieces cut from the finished material, gave satisfactory results; the cold-bending tests closing down on themselves without sign of

fracture.

Numerous other cases of angles and plates that were so hard in places as to break off short in punching, or, what was worse, to break the punches, have come under our observation, and sithough makers of Bessemer steel claim that this is just as likely to occur in open-hearth as in Besseme. steel, we have as yet never seen an instance of failure of this kind in open-hearth

we have as yet never seen an instance of failure of this kind in open-hearth steel having a composition such as C 0.25%, Mn 0.70%, P 0.80%.

J. W. Walles, in a paper read before the Chemical Section of the British Association for the Advancement of Science, in speaking of mysterious failures of steel, states that investigation shows that "these failures occur in steel of one class, viz., soft steel made by the Beasemer process."

Segregation in Steel Imgots. (A. Pourcel, Trans. A. I. M. E. 208, H. M. We, in his "Metallurgy of Steel," gives a résumé of observations with the results of numerous analyses, bearing upon the phenomena of seg.

regation.
In 1881 Mr. Stubbs, of Manchester, showed the heterogeneous resultr of analyses made upon different parts of an ingot of large section.
A test-piece taken 24 inches from the head of the ingot 7.5 feet in length gave by analysis very different results from those of a test-piece talici. 80 inches from the bottom.

Mn. Si. 0.043 0.92 0.5350.1610.261Top. 0.498 0.87 0.006 0.025 0.096 Bottom....

Windsor Richards says he had often observed in test-pieces taken from

Windsor Richards says he had often observed in test-pleces taken from different points of one plate variations of 0.05% of carbon. Begregation is specially pronounced in an ingot in its central portion, and around the space of the piping.

It is most observable in large ingots, but in blocks of smaller weight and limited dimensions, subjected to the influence of solidification as rapid as casting within thick walls will permit, it may still be observed distinctly. An ingot of Martin steel, weighing about 1000 lbs., and having a height of 1.10 feet and a section of 10.24 inches square, gave the following:

1. Upper section:	U.	, D	F.	MD.
Border	0.380	0.040	0.088	0.420
Centre	0.580	0.077	0.057	0.480
2. Lower section:	C.	8.	P.	Mn.
Border	0.280	0.029	0.016	0.890
Centre	0.880	0.080	0.038	0.890
3. Middle section:	Č.	R.	P	Mn.
3. Middle section.	0.390	0.025	0.025	0.400
Border	0.000	0.048	0.023	0.400
Centre	v.azu	U.U40	0.055	U.414"

Segregation is less marked in ingots of extra-soft metal cast in cast-iron moulds of considerable thickness. It is, however, still important, and explains the difference often shown by the results of tests on pieces taken from different portions of a plate. Two samples, taken from the sound part of a flat ingot, one on the outside and the other in the centre, 7.9 inches from the upper edge, gave:

- ·	U.	ъ.	Р.	Mn.
Centre	0.14	0.058	0.072	0.576
Exterior	0.11	0.036	0.027	0.610

Manganese is the element most uniformly disseminated in hard or soft

For cannon of large calibre, if we reject, in addition to the part cast in sand and called the masselotte (sinking-head), one third of the upper part sanu and cancer the massecure (analog acad), one that of the upper part of the ingot, we can obtain a tube practically homogeneous in composition, because the central part is naturally removed by the boring of the tube. With extra-soft steels, destined for ship-or boiler-plates, the solution for practically perfect homogeneity lies in the obtaining of a metal more closely decoration to page of arter-soft metal. deserving its name of extra soft metal.

The injurious consequences of segregation must be suppressed by reduc-

ing, as far as possible, the elements subject to liquation.

Earliest Uses of Steel for Structural Purposes. (G. G. ehrtens, Trans. A. S. C. E. 1893).—The Pennsylvania Railroad Company first introduced Bessemer steel in America in locomotive boilers in the year 1863, but the steel was too hard and brittle for such use. The first plates made for steel boilers had a tenacity of 85,000 to 92,000 lbs, and an elongation of but 7% to 10%. The results were not favorable, and the steel works were soon forced to offer a material of less tenacity and more ductility. The requirements were therefore reduced to a tenacity of 78,000 lbs. or less, and the elongation was increased to 15% or more. The use of Bessemer steel in bridge-building was tried first on the Dutch State railways in 1868-64, then in England and Austria. The first use of cast steel for bridges was in America, for the St. Louis Arch Bridge and for the wire of the East River Bridge. Before 1880 the Glasgow and Plattsmouth bridges over the Missouri River were also built of ingot metal. Steel eyebars were applied for the first time in the Glasgow Bridge. Since 1880 the introduction of mild steel in all kinds of engineering structures has steadily increased.

Messrs. Joseph Adamson & Co., of Hyde, England, in a letter to the author say: "The first steel for boiler purposes was used for a locomotive firebox sent to Africa in 1859. The first steel steamships were built in Liverpool for 'blockade-running' during the American Civil War about 1862, and at least 5000 tons of Bessemer steel plates were rolled at Penistone by Benson, Adamson & Garnett for this purpose. The first Bessemer steel bollers were made in this neighborhood in 1858. Drilling the rivet holes was adopted in 1859. Some of these boilers built in 1862 worked 29 years night and day. We have lost trace of these boilers now, but we know that after working this length of time they were found good enough to be worth resetting and were set to work again for a time. Between 1870 and 1880 about 2000 steel land boilers were working in this country. The pressures ranged up to 150 lbs."

STEEL CASTINGS.

(E. S. Cramp, Engineering Congress, Dept. of Marine Eng'g, Chicago, 1893.)

In 1891 American steel-founders had successfully produced a considerable variety of heavy and difficult castings, of which the following are the most noteworthy specimens:

Bed-plates up to 24,000 lbs.; stern-posts up to 54,000 lbs.; stems up to 21,000 lbs.; hydraulic cylinders up to 11,000 lbs.; shaft-struts up to 32,000 lbs.;

hawse-pipes up to 7500 lbs.; stern-pipes up to 8000 lbs.

The percentage of success in these classes of castings since 1890 has ranged from 65% in the more difficult forms to 90% in the simpler ones; the tensile strength has been from 62,000 to 78,000 lbs., elongation from 15% to 25%. The best performance recorded is that of a guide, cast in January, 1893, which developed 84,000 lbs. tensile strength and 15.6% elongation.

The first steel castings of which anything is generally known were crossing frogs made for the Philadelphia & Reading R. R. in July, 1867, by the William Butcher Steel Works, now the Midvale Steel Co. The moulds were made of a mixture of ground fire-brick, black-lead crucible-pots ground fine, and fire-clay, and washed with a black-lead wash. The steel was melted in crucibles, and was about as hard as tool steel. The surface of these castings was very smooth, but the interior was very much honeycombed. This was before the days when the use of silicon was known for solidifying steel. The sponginess, which was almost universal, was a great obstacle to their general adoption.

The next step was to leave the ground pots out of the moulding mixture and to wash the mould with finely ground fire-brick. This was a great improvement, especially in very heavy castings; but this mixture still clung so strongly to the casting that only comparatively simple shapes could be made with certainty. A mould made of such a mixture became almost as hard as fire-brick, and was such an obstacle to the proper shrinkage of castings, that, when at all complicated in shape, they had so great a tendency to crack as to make their successful manufacture almost impossible. By this time the use of silicon had been discovered, and the only obstacle in the way of making good castings was a suitable moulding mixture. This was ultimately found in mixtures having the various kinds of silica sand as the principal constituent.

One of the most fertile sources of defects in castings is a bad design Very intricate shapes can be cast successfully if they are so designed as

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cool uniformly. Mr. Cramp says while he is not yet prepared to state that anything that can be cast successfully in iron can be cast in steel, indications seem to point that way in all cases where it is possible to put on suit-

while sinking heads for feeding the casting.

H. L. Gantt (Trans. A. S. M. E., xii. 710) says: Steel castings not only shrink much more than iron ones, but with less regularity. The amount of shrinkage varies with the composition and the heat of the metal; the hotter the metal the greater the shrinkage; and, as we get smoother castings from the metal the greater the shrinkage; and, as we get smoother castings from hot metal, it is better to make allowance for large shrinkage and pour the metal as hot as possible. Allow 3/16 or ½ in. per ft. in length for shrinkage, and ½ in. for finish on machined surfaces, except such as are cast "up." Cope surfaces which are to be machined should, in large or hard castings, have an allowance of from ½ to ½ in. for finish, as a large mass of metal slowly rising in a mould is apt to become crusty on the surface, and such a crust is sure to be full of imperfections. On small, soft castings it is not drag side and ½ in on cope side will be sufficient. castings ¼ in, on drag side and ¼ in, on cope side will be sufficient. No core should have less than ¼ in, fluish on a side and very large ones should have as much as 1/2 in, on a side. Blow-holes can be entirely prevented in castings by the addition of manganese and silicon in sufficient quantities; but both of these cause brittleness, and it is the object of the conscientious steelmaker to put no more manganese and silicon in his steel than is just suffi-cient to make it solid. The best results are arrived at when all portions of

the castings are of a uniform thickness, or very nearly so.

The following table will illustrate the effect of annealing on tensile

strength and elongation of steel castings:

Carbon.	Unannea	led.	Anneal	ed.
	Tensile Strength.	Elongation.	Tensile Strength.	Elongation.
.23% .37 .58	68,738 85,540 90,121	22.40% 8.20 2.35	67,210 82,228 106,415	81.40% 21.80 9.80

The proper annealing of large castings takes nearly a week.

The proper steel for roll pinions, hammer dies, etc., seems to be that containing about .60% of carbon. Such castings, properly annealed, have worn well and seldom broken. Miscellaneous gearing should contain carbon .40% to 60%, gears larger in diameter being softest. General machinery castings should, as a rule, contain less than .40% of carbon, those exposed to great blocks. shocks containing as low at 20% of carbon. Such castings will give a tensile strength of from 60,000 to 80,000 lbs. per sq. in. and at least 15% extension in a 2 in. long specimen. Machinery and hull castings for war-vessels for the United States Navy, as well as carriages for naval guns, contain from 20% to .30% of carbon.

The following is a partial list of castings in which steel seems to be rapidly taking the place of iron: Hydraulic cylinders, crossheads and pistons for large engines, roughing rolls, rolling-mill spindles, coupling-boxes, roll pinions, gearing, hammer-heads and dies, riveter stakes, castings for ships, car couplers, etc.

For description of methods of manufacture of steel castings by the Bessemer, open-hearth, and crucible processes, see paper by P. G. Salom, Trans. A. I. M. E. xiv, 118.

Specifications for steel castings issued by the U. S. Navy Department, 1889 (abridged): Steel for castings must be made by either the open-hearth or the crucible process, and must not show more than .06% of phosphorus. All castings must be annealed, unless otherwise directed. The tensile strength of steel castings shall be at least 60,000 lbs., with an elongation of at least 15% in 8 in. for all castings for moving parts of the machinery, and at least 10% in 8 in. for other castings. Bars 1 in. sq. shall be capable of bending cold, without fracture, through an angle of 90°, over a radius not greater than 1½ in. All castings must be sound, free from injurious roughness,

sponginess, pitting, shrinkage, or other cracks, cavities, etc.

Pennsylvania Railroad specifications, 1888: Steel castings should have a tensile strength of 70,000 lbs. per sq. in. and an elongation of 15% in section or

fails below 60,000 lbs., nor if the elongation is less than 12%, nor if castings have blow-holes and shrinkage cracks. Castings weighing 80 lbs. or more must have cast with them a strip to be used as a test-piece. The dimensions of this strip must be 34 in. sq. by 12 in. long.

MANGANESE, NICKEL, AND OTHER "ALLOY" STÉELS.

Manganese Steel. (H. M. Howe, Trans. A. S. M. E., vol. xii.)—Manganese steel is an alloy of iron and manganese, incidentally, and probably

unavoidably, containing a considerable proportion of carbon.

The effect of small proportions of manganese on the hardness, strength, and ductility of iron is probably slight. The point at which mangane-se begins to have a predominant effect is not known: it may be somewhere aregains to have a precommant effect is not known; it may be somewhere about 2.5%. As the proportion of manganese rises above 2.5% the the proportion and ductility diminish, while the hardness increases. This effect reaches a maximum with somewhere about 6% of manganese. When the proportion of this element rises beyond 6% the strength and ductility both increase, while the hardness diminishes slightly, the maximum of both strength and ductility helm regular with about 14% of maximum. ductility being reached with about 14% of manganese. With this proportion the metal is still so hard that it is very difficult to cut it with steel tools. As the proportion of manganese rises above 15% the ductility falls off abruptly, the strength remaining nearly constant till the manganese passes 18%, when

it in turn dininishes suddenly.

Steel containing from 4% to 6.5% of manganese, even if it have but 0.37% of carbon, is reported to be so extremely brittle that it can be powdered under

a hand-hammer when cold; yet it is ductile when hot.

Manganese steel is very free from blow-holes; it welds with great difficulty; its toughness is increased by quenching from a yellow heat; its electric resistance is enormous, and very constant with changing temperature; iris low in thermal conductivity. Its remarkable combination of great hard-aces, which cannot be materially lessened by annealing, and great tensile strength, with astonishing toughness and ductility, at once creates and limits its usefulness. The fact that manganese steel cannot be softened, that it ever remains so hard that it can be machined only with great difficulty, sets up a barrier to its usefulness.

The following comparative results of abrasion tests of manganese and

other steel were reported by T. T. Morrell:

ABRABION BY PRESSURE AGAINST A REVOLVING HARDENED-STEEL SHAFT.

Loss of weight of	manganese steel	1.0
"	blue-tempered hard tool steel	0.4
44	annealed hard tool steel	7.5
44	hardened Otis boiler-plate steel	7.0
**	annealed " " "	
AB	RASION BY AN EMERY-WHEEL	
Loss of weight of	hard manganese-steel wheels	1.00
64	softer " "	1.19
44	hardest carbon-steel wheels	1.28
**	soft " "	

The hardness of manganese steel seems to be of an anomalous kind. The alloy is hard, but under some conditions not rigid. It is very hard in its resistance to abrasion; it is not always hard in its resistance to impact.

Manganese steel forges readily at a yellow heat, though at a bright white heat it crumbles under the hammer. But it offers greater resistance to deformation, i.e., it is harder when hot, than carbon steel.

The most important single use for manganese-steel is for the pins which hold the buckets of elevator dredges. Here abrasion chiefly is to be resisted.

Another important use is for the links of common chain-elevators.

As a material for stamp-shoes, for horse-shoes, for the knuckles of an automatic car-coupler, manganese steel has not met expectations.

Manganese steel has been regularly adopted for the blades of the Cyclone

pulverizer. Some manganese-steel wheels are reported to have roun over 300,000 miles each without turning, on a New England railroad.

Nickel Steel.—The remarkable tensile strength and ductility of nickel steel, as shown by the test-bars and the behavior of nickel-steel armorplate under shot tests, are witness of the valuable qualities conferred upon steel by the addition of a few per cent of nickel.

The following tests were made on nickel steels by Mr. Maunsel White of the Bethlehem Iron Company (Eng. & M. Jour., Sept. 16, 1893.):

	Specimen from—	Diam., in.	Length, in.	Tensile Str'gth, lbs. per sq. in.		Elonga- tion,	Reduction of Area,	
steel.	Forged bars, *	.635	4	276,800 246,595		2.75 4.25	6.0	Special treatment.
	ours,	1.564	4	105,300 142,800 143,200	74,000 74,000	19.25 13.0 12.32	55.0 28.2 27.6	Annealed.
3Mg mckel	134-in.	10	46	117,600	64,000 65,000	17.0 16.66	46.0 42.1	
348	round rolled bar.t	11	45	91,600	51,000 51,000	22.25	58.9 58.4	
		.798	8	85,200 86,000 115,464	53,000 48,000 51,820	21.82 21.25 36.25	49.5 47.4 66.28	
steel	1¼-in. sq. bar, rolled.;	1 44	15	112,600 102,010	60,000 29,180	37.87 41.37	62.82 69.59	Annealed.
nickel	1,2,5,3	.500	2	102,510 114,590	40,200 56,020	44.00 47.25	68.34	
Brg ni	1-in, round bar, rolled.§	1 11	16	115,610 105,240 106,780	59,080 45,170 45,170	45.25 49.65 55.50	62.3 72.8 63.6	Annealed.

* Forged from 6-in. ingot to % in. diam., with conical heads for holding.

+Showing the effect of varying carbon.

‡ Rolled down from 14-in. ingot to 11/4-in. square billet, and turned to size. Rolled down from 14-in. ingot to 1-in. round, and turned to size.

Nickel steel has shown itself to be possessed of some exceedingly valuable properties; these are, resistance to cracking, high elastic limit, and homogeneity. Resistance to cracking, a property to which the name of non fissibility has been given is shown more remarkably as the percentage of nickel increases. Bars of 27% nickel illustrate this property. A 1¼-in, square bar was nicked ¼ in, deep and bent double on itself without further fracture than the splintering off, as it were, of the nicked portion. Sudden failure or rupture of this steel would be impossible; it seems to possess the toughness of rawhide with the strength of steel. With this percentage of nickel the steel is practically non-corrodible and non-magnetic. The resistance to cracking shown by the lower percentages of nickel is best illustrated in the many trials of nickel-steel armor.

The elastic limit rises in a very marked degree with the addition of about 3% of nickel, the other physical properties of the steel remaining unchanged

or perhaps slightly increased.

In such places (shafts, axles, etc.) where failure is the result of the fatigue of the metal this higher elastic limit of nickel steel will tend to prolong indefinitely the life of the piece, and at the same time, through its superior

toughness, offer greater resistance to the sudden strains of shock.

Howe states that the hardness of nickel steel depends on the proportion of nickel and carbon jointly, nickel up to a certain percentage increasing the hardness, beyond this lessening it. Thus while steel with % of nickel and 0.90% of carbon cannot be machined, with less than 5% nickel it can be worked cold readily, provided the proportion of carbon be low. As the proportion of nickel rises higher, cold-working becomes less easy. It forges easily whether it contain much or little nickel.

The presence of manganese in nickel steel is most important, as it appears that without the aid of manganese in proper proportions, the conditions of

treatment would not be successful.

Tests of Nickel Steel. -Two heats of open hearth steel were made by the Cleveland Rolling Mill Co., one ordinary steel made with 9000 lbs. each scrap and pig, and 185 lbs. ferro-manganese, the other the same with the addition of 8%, or 540 lbs. of nickel. Tests of six plates rolled from each heat., 0.24 to 0.3 in. thick, gave results as follows:

Ordinary steel, T. S. 52,500 to 56,500; E. L. 32,800 to 37,900; elong. 26 Nickel steel. "68,370 to 67,100; "47,100 to 48,200; "28 to 32≰ 281/4 to 26%. The nickel steel averages 31% higher in elastic limit, 20% higher in ultimate tensile strength, with but slight reduction in ductility. (Eng. & M. Jour.,

Feb. 25, 1893.)

Aluminum Steel.—R. A. Hadfield (Trans. A. I. M. E. 1890) says: Aluminum appears to be of service as an addition to baths of molten iron or steel unduly saturated with oxides, and this in properly regulated steel manufacture should not often occur. Speaking generally, its rôle appears to be similar to that of silicon, though acting more powerfully. The statement that aluminum lowers the melting-point of iron seems to have no foundation in fact. If any increase of heat or fluidity takes place by the addition of small amounts of aluminum, it may be due to evolution of heat, owing to exidation of the aluminum, as the calorific value of this metal is very high—in fact, higher than silicon. According to Berthollet, the conversion of aluminum to A_1O_2 equals 7900 cal.; silicon to SiO_2 is stated as 7800. The action of aluminum may be classed along with that of silicon, sulphur,

phosphorus, arsenic, and copper, as giving no increase of hardness to iron, phosphorus, areemo, and copper, as giving no increase or naturess to more in contradistinction to carbon, manganese, chromium, tungsten, and nickel. Therefore, whilst for some special purposes aluminum may be employed in the manufacture of iron, at any rate with our present knowledge of its properties, this use cannot be large, especially when taking into consideration the fact of its comparatively high price. Its special advantage seems to be that it combines in itself the advantages of both silicon and manganese, but as long as allows containing these matels are so cheen and aluminum. but so long as alloys containing these metals are so cheap and aluminum

dear, its extensive use seems hardly probable.

J. E. Stead, in discussion of Mr. Hadfield's paper, said: Every one of our trials has indicated that aluminum can kill the most flery steel, providing, of course, that it is added in sufficient quantity to combine with all the oxygen which the steel contains. The metal will then be absolutely dead, and will pour like dead-melted silicon steel. If the aluminum is added as metals aligned and in the steel contains and if the adultion is made into the lic aluminum, and not as a compound, and if the addition is made just be-

lio aluminum, and not as a compound, and if the acquiron is made just nefore the steel is cast, 1/10% is ample to obtain perfect solidity in the steel.

Ohrome Steel. (F. L. Garrison, Jour. F. I., Sept. 1891.)—Chromium
increases the hardness of iron, perhaps also the tensile strength and elastic
limit, but it lessens its weldibility.

Ferro chrome, according to Berthier, is made by strongly heating the
mixed oxides of iron and chromium in brasqued crucibles, adding powdered
charcoal if the oxide of chromium is in excess, and fluxes to scorify the
earthy matter and prevent oxidation. Chromium does not appear to give
steel the power of becoming harder when quenched or chilled. Howe states
that chrome steels force more readily than tungsten steels, and when not that chrome steels forge more readily than tungsten steels, and when not that chrome steels forgething reaching than tangents seems, and which are containing over 0.5 of chronium nearly as well as ordinary carbon steels of like percentage of carbon. On the whole the status of chrome steel is not satisfactory. There are other steel alloys coming into use, which are so much better, that it would seem to be only a question of time when it will drop entirely out of the race. Howe states that many experienced chemists have found no chromium, or but the merest traces, in chrome steel sold in the markets.

J. W. Langley (Trans. A. S. C. E. 1892) says: Chromium, like manganese, is a true hardener of iron even in the absence of carbon. The addition of 1% is a true natural of it roll even in the absence of carbon. The addition of its or 2s of chromium to a carbon steel will make a metal which gets excessively hard. Hitherto its principal employment has been in the production of chilled shot and shell. Powerful molecular stresses result during cooling, and the shells frequently break spontaneously months after they are made.

Tungsten Steel-Mushet Steel. (J. B. Nau, Iron Age, Feb. 11, 1892.)

-By incorporating simultaneously carbon and tungsten in iron, it is possible to obtain a much harder steel than with carbon alone, without danger of an extraordinary brittleness in the cold metal or an increased difficulty in the working of the heated metal.

When a special grade of hardness is required, it is frequently the custom to use a high tungsten steel, known in Eugland as special steel. A specimen from Sheffield, used for chisels, contained 9.8% of tungsten, 0.7% of sliver; and 0.6% of carbon. This steel, though used with advantage in its untempered state to turn chilled rolls, was not brittle; nevertheless it was hard enough to scratch glass.

A sample of Mushet's special steel contained 8.8% of tungsten and 1.78% of

manganese. The hardness of tungsten steel cannot be increased by the or-

dinary process of hardening.

The only operation that it can be submitted to when cold is grinding. It has to be given its final shape through hammering at a red heat, and evthen, when the percentage of tungsten is high, it has to be treated very carefully; and in order to avoid breaking it, not only is it necessary to reheat it several times while it is being hammered, but when the tool has acquired the desired shape hammering must still be continued gently and with numerous blows until it becomes nearly cold. Then only can it be cooled en-

Tungsten is not only employed to produce steel of an extraordinary hardness, but more especially to obtain a steel which, with a moderate hardness, allies great toughness, resistance, and ductility. Steel from Assailly, used for this purpose, contained carbon, 0.52%; silicon, 0.04%; tungsten, 0.3%; phosphorus, 0.04%; sulphur, 0.005%.

Mechanical tests made by Styffe gave the following results:

Breaking load per square inch of original area, pounds.. 172,424 Reduction of area, per cent Average elongation after fracture, per cent

According to analyses made by the Duc de Luynes of ten specimens of the celebrated Oriental damasked steel, eight contained tungsten, two of them in notable quantities (0.518% to 1%), while in all of the samples analyzed nickel was discovered ranging from traces to nearly 4%.

Stein & Schwartz of Philadelphia, in a circular say: It is stated that tungsten sheel is suitable for the manufacture of steel magnets, since it retains its magnetism longer than ordinary steel. Mr. Kniesche has made tungsten up to 98 fine a specialty. Dr. Heppe, of Leipsig, has written a number of articles in German publications on the subject. The following instructions are given concerning the use of tungster. In order to produce cast iron possessing great hardness an addition of one half to one and one half of tungster is all that is needed. For bar iron it must be carried up to 1% to 2%, but should not exceed 2½%. For puddled steel the range is larger, but an addition beyond 3½% only increases the hardness, so that it is brought to the contraction of the product of the contraction of the contract up to 114% only for special tools, coinage dies, drills, etc. For tires 214% to 5% have proved best, and for axles 14 to 114%. Cast steel to which tungsten has been added needs a higher temperature for tempering than ordinary steel, and should be hardened only between yellow, red, and white. Chisels made of tungsten steel should be drawn between cherry-red and blue, and stand well on iron and steel. Tempering is best done in a mixture of 5 parts of yellow rosin, 3 parts of tar, and 2 parts of tallow, and then the article is once more heated and then tempered as usual in water of about 15° C.

Fluid-compressed [Steel by the "Whitworth Process." (Proc. Inst. M. E., May, 1887, p. 107.)—In this system a gradually increasing pressure up to 6 or 8 tons per square inch is applied to the fluid ingot, and within half an hour or less after the application of the pressure the column of fluid steel is shortened 11/2 inch per foot or one-eighth of its length; the pressure is then kept on for several hours, the result being that the metal is compressed into a perfectly solid and homogeneous material, free frem blow-holes.

In large gun-ring ingots during cooling the carbon is driven to the centre, the centre containing 0.8 carbon and the outer ring 0.3. The centre is bored out until a test shows that the inside of the ring contains the same percentage of carbon as the outside.

Fluid-compressed steel is made by the Bethlehem Iron Co. for gun and other heavy forgings.

CRUCIBLE STEEL.

Selection of Grades by the Eye, and Effect of Heat Treatment. (J. W. Langley, Amer. Chemist, November, 1876.)—In 1874, Miller, Metcalf & Parkin, of Pittsburgh, selected eight samples of steel which were believed to form a set of graded specimens, the order being based on the quantity of carbon which they were supposed to contain. They were numbered from one to eight. On analysis, the quantity of carbon was found to follow the order of the numbers, while the other elements present—silicon, phosphorus, and sulphur—did not do so. The method of selection is described as follows:

The steel is melted in black-lead crucibles capable of holding about eighty pounds; when thoroughly fluid it is poured into cast-iron moulds, and when cold the top of the ingot is broken off, exposing a freshly-fractured surface. The appearance presented is that of confused groups of crystals, all appearance presented is that of confused groups of crystals, all appearance presented is that of confused groups of crystals, all appearance presented is that of confused groups of crystals, all appearance presented is that of confused groups of crystals, all appearance presented in the confused groups of crystals. ing to have started from the outside and to have met in the centre; this veral form is common to all ingots of whatever composition, but to the ned eye, and only to one long and critically exercised, a minute but in-

describable difference is perceived between varying samples of steel, and this difference is now known to be owing almost wholly to variations in the amount of combined carbon, as the following table will show. Twelve samples selected by the eye alone, and analyses of drillings taken direct from the ingot before it had been heated or hammered, gave results as below:

Ingot Nos.	Iron by Diff.	Carbon.	Diff. of Carbon.	Silicon.	Phos.	Sulph.
1	99.614	.302		.019	.047	.018
2	99.455	.490	.188	.034	.005	.016
2	99.363	.529	.039	.043	.047	.018
4	99.270	.649	.120	.039	.030	.012
5 6	99.119	.801	.152	.029	.085	.016
6	99.086	.841	.040	.039	.024	.010
7	99.044	.867	.026	.057	.014	.018
8 9	99.040	.871	.004	.053	.024	.012
9	98.900	.955	.084	.059	.070	.016
10	98.861	1.005	.050	.088	.034	.012
11	98.752	1.058	.053	.120	.064	.006
12	98.834	1.079	.021	.039	.044	.004

Here the carbon is seen to increase in quantity in the order of the numbers, while the other elements, with the exception of total iron, bear no rela-tion to the numbers on the samples. The mean difference of carbon is .071.

In mild steels the discrimination is less perfect.

The appearance of the fracture by which the above twelve selections were made can only be seen in the cold ingot before any operation, except the original one of casting, has been performed upon it. As soon as it is hammered, the structure changes in a remarkable manner, so that all trace

of the primitive condition appears to be lost.

Another method of rendering visible to the eye the molecular and chemical changes which go on in steel is by the process of hardening or tempercal changes which go on in steel is by the process of hardening or tempering. When the metal is heated and plunged into water it acquires an increase of hardness, but a loss of ductility. If the heat to which the steel has been raised just before plunging is too high, the metal acquires intense hardness, but it is so brittle as to be worthless; the fracture is of a bright, granular, or sandy character. In this state it is said to be burned, and it cannot again be restored to its former strength and ductility by annealing; it is ruined for all practical purposes, but in just this state it again shows differences of structure corresponding with its content in carbon. The nature of these changes can be illustrated by plunging a bar highly heated at one end and cold at the other into water, and then breaking it off in nature of these changes can be industrated by plunging a bar highly heater at one end and cold at the other into water, and then breaking it off in pieces of equal length, when the fractures will be found to show appear-ances characteristic of the temperature to which the sample was raised. The specific gravity of steel is influenced not only by its chemical analy-sis, but by the heat to which it is subjected, as is shown by the following

table (densities referred to 60° F.):

Specific gravities of twelve samples of steel from the ingot; also of six hammered bars, each bar being overheated at one end and cold at the other, in this state plunged into water, and then broken into pieces of equal length.

	1	2	8	4	5	6	7	8	9	10	11	12
Ingot Bar:	1		i .				1		i .			
*Burned 1.			7.818 7.814	7.791 7.811		7.789 7.784		7.752 7.755	.,	7.744 7.749		7.690 7.741 7.769
4.			17.826	7.849	l	17.808		7.773		17.789	l .	17.798
Cold 6.			7.831 7.844	7.806 7.824		7.812 7.829		7.790 7.825		7.812	••••	7.811

^{*} Order of samples from bar.

Effect of Heat on the Grain of Steel. (W. Metcalf,-Jeans on Steel, p. 642.)—A simple experiment will show the alteration produced in a high carbon steel by different methods of hardening. If a bar of such steel be nicked at about 9 or 10 places, and about half an inch apart, a suitable specimen is obtained for the experiment. Place one end of the bar in a good fire, so that the first nicked piece is heated to whiteness, while the rest of the bar, being out of the fire, is heated up less and less as we approach the other end. As soon as the first piece is at a good white heat, which of course burns a high carbon steel, and the temperature of the rest of the bar gradually passes down to a very dull red, the metal should be taken out of the fire and suddenly plunged in cold water, in which it should be left till quite cold. It should then be taken out and carefully dried. An examination with a file will show that the first piece has the greatest hardness, while the last piece is the softest, the intermediate pieces gradually passing from one condition to the other. On now breaking off the pieces at each nick it will be seen that very considerable and characteristic changes have been produced in the appearance of the metal. The first burnt piece is very open or crystalline in fracture; the succeeding pieces become closer and closer in the grain until one piece is found to possess that perfectly even grain and velvet-like appearance which is so much prized by experienced steel users. The first pleces also, which have been too much hard-ened, will probably be cracked; those at the other end will not be hardened through. Hence if it be desired to make the steel hard and strong, the temperature used must be high enough to harden the metal through, but

temperature used must be high enough to harden the metal through, but not sufficient to open the grain.

Changes in Vitimate Strength and Elasticity due to Hammering, Annealing, and Tempering. (J. W. Langley, Trans. A. S. C. E. 1892.)—The following table gives the result of tests made on some round steel bars, all from the same ingot, which were tested by tensile stresses, and also by bending till fracture took place:

er.	Treatment.	of cold degrees.	Carl	bon.	ter, in.	ic limit, ds per re inch.	square ch.	Elongation, per cent.	area, cent,
Number.	Treatment,	Angle bend,	Total.	Sem	Diameter,	Elastic pounds square	Tensile, per s inc	Elon	Red
1 2 3	Cold-hammered bar Bar drawn black Bar annealed Bar hardened and	75	1.25 1.25 1.31	.47 .47 .70	.575 .577 .580	92,420 114,700 68,110	141,500 188,400 98,410	2.00 6.00 10.00	2.42 12.45 11.69
4	Bar hardened and drawn black	80	1.09	.86	.578	159,800	248,700	8.33	17.9

The total carbon given in the table was found by the color test, which is affected, not only by the total carbon, but by the condition of the carbon. The analysis of the steel was:

Silicon		Manganese	.94
Phosphorus	.02	Carbon (true total carbon, by combustion)	
Sulphur	.009	combustion)	1.81

Heating Tool Steel. (Crescent Steel Co., Pittsburg, Pa.)-There are three distinct stages or times of heating: First, for forging; second. for

hardening; third, for tempering.

The first requisite for a good heat for forging is a clean fire and plenty of fuel, so that jets of hot air will not strike the corners of the piece; next, the fire should be regular, and give a good uniform heat to the whole part to be forged. It should be keen enough to heat the piece as rapidly as may be, and allow it to be thoroughly heated through, without being so flerce as to

overheat the corners.

Steel should not be left in the fire any longer than is necessary to heat it clear through, as "soaking" in fire is very injurious; and, on the other hand, it is necessary that it should be hot through, to prevent surface cracks.

By observing these precautions a piece of steel may always be heated safely, up to even a bright yellow heat, when there is much forging to be deverant.

done on it

The best and most economical of welding fluxes is clean, crude borax, which should be first thoroughly melted and then ground to fine powder.

After the steel is properly heated, it should be forged to shape as quickly as possible; and just as the red heat is leaving the parts intended for cutting edges, these parts should be refined by rapid, light blows, continued until

the red disappears.

For the second stage of heating, for hardening, great care should be used: first, to protect the cutting edges and working parts from heating more rapidly than the body of the piece; next, that the whole part to be hardened be heated uniformly through, without any part becoming visibly hotter than the other. A uniform heat, as low as will give the required hardness,

than the other. A uniform neat, as low as whi give the required naruness, is the best for hardening.

For every variation of heat, which is great enough to be seen, there will result a variation in grain, which may be seen by breaking the piece: and for every such variation in temperature, there is a very good chance for a crack to be seen. Many a costly tool is ruined by inattention to this point. The effect of too high heat is to open the grain; to make the steel coarse. The effect of an irregular heat is to cause irregular grain, irregular strains,

and cracks.

As soon as the piece is properly heated for hardening, it should be promptly and thoroughly quenched in plenty of the cooling medium, water,

brine, or oil, as the case may be.

An abundance of the cooling bath, to do the work quickly and uniformly

all over, is very necessary to good and safe work.

To harden a large piece safely a running stream should be used.

Much uneven hardening is caused by the use of too small baths.

For the third stage of heating, to temper, the first important requisite is again uniformity. The next is time; the more slowly a piece is brought down to its temper, the better and safer is the operation.

When expensive tools are to be made it is a wise precaution to try small

pieces of the steel at different temperatures, so as to find out how low a heat will give the necessary hardness. The lowest heat is the best for any steel.

Heating to Forge.—The trouble in the forge fire is usually neven heat, and not too high heat. Suppose the piece to be forged has been put into a very hot fire, and forced as quickly as possible to a high yellow heat, so that it is almost up to the scintillating point. If this be done, in a few minutes the outside will be quite soft and in a nice condition for forging, while the middle parts will not be more than red-hot. Now let the piece be placed under the hammer and forged, and the soft outside will yield so much more readily than the hard inside, that the outer particles will be torn asunder, while the inside will remain sound.

Suppose the case to be reversed and the inside to be much hotter than the outside; that is, that the inside shall be in a state of semi-fusion, while the outside is hard and firm. Now let the piece be forged, and the outside will be all sound and the whole piece will appear perfectly good until it is cropped, and then it is found to be hollow inside.

In either case, if the piece had been heated soft all through, or if it had been

In either case, it the piece has been heated solvan through, or it has been only red-hot all through, it would have forged perfectly sound.

In some cases a high heat is more desirable to save heavy labor but in every case where a fine steel is to be used for cutting purposes it must be borne in mind that very heavy forging refines the bars as they slowly cool, and if the smith heats such refined bars until they are soft, he raises the grain, makes them coarse, and he cannot get them fine again unless he has a very heavy steam-hammer at command and knows how to use it well.

Annealing. (Crescent Steel Co.)—Annealing or softening is accomplished by heating steel to a red heat and then cooling it very slowly.

to prevent it from getting hard again.

The higher the degree of heat, the more will steel be softened, until the

limit of softness is reached, when the steel is melted.

It does not follow that the higher a piece of steel is heated the softer it will be when cooled, no matter how slowly it may be cooled; this is proved by the fact that an ingot is always harder than a rolled or hammered bar made from it.

Therefore there is nothing gained by heating a piece of steel hotter than a good, bright, cherry-red; on the contrary, a higher heat has several disadvantages: First. If carried too far, it may leave the steel actually harder than a good red heat would leave it. Second. If a scale is raised on the steel, this scale will be harsh, granular oxide of iron, and will spoil the tools used to cut it. Third. A high scaling heat continued for a little tim changes the structure of the steel, makes it brittle, liable to crack in hardening, and impossible to refine.

To anneal any piece of steel, heat it red-hot; heat it uniformly and heat it

through, taking care not to let the ends and corners get too hot,

As soon as it is hot, take it out of the fire, the sooner the better, and cool that showly as possible. A good rule for heating is to heat it at so low a red that when the piece is cold it will still show the blue gloss of the oxide that was put there by the hammer or the rolls.

Steel annealed in this way will cut very soft; it will harden very hard, without cracking; and when tempered it will be very strong, nicely refined,

and will hold a keen, strong edge.

Tempering.—Tempering steel is the act of giving it, after it has been shaped, the hardness necessary for the work it has to do. This is done by first hardening the piece, generally a good deal harder than is necessary and then toughening it by slow heating and gradual softening until it is just right for work.

A piece of steel properly tempered should always be finer in grain than the bar from which it is made. If it is necessary, in order to make the piece as hard as is required, to heat it so hot that after being hardened the grain will be as coarse as or coarser than the grain in the original bar, then the steel itself is of too low carbon for the desired work.

If a great degree of hardness is not desired, as in the case of taps, and most tools of complicated form, and it is found that at a moderate heat the tools are too hard and are liable to crack, the smith should first use a lower heat in order to save the tools already made, and then notify the steelmaker

that his steel is too high, so as to prevent a recurrence of the trouble.

For descriptions of various methods of tempering steel, see "Tempering of Metals," by Joshua Rose, in App. Cyc. Mech., vol. ii, p. 863; also, "Wrinkles and Recipes," from the Scientific American. In both of these works Mr. Rose gives a "color scale," lithographed in colors, by which the Scientific as the first of the tools in their order on the color scale to greater with following is a list of the tools in their order on the color scale, together with the approximate color and the temperature at which the color appears on brightened steel when heated in the air:

Hand-plane irons.

Scrapers for brass; very pale yellow, 430° F. Steel-engraving tools. Slight turning tools. Hammer faces. Planer tools for steel. Ivory-cutting tools. Planer tools for iron. Paper-cutters. Wood-engraving tools. Bone cutting tools. Milling-cutters; straw yellow, 460° F. Wire-drawing dies. Boring-cutters. Leather-cutting dies. Screw-cutting dies. Inserted saw-teeth. Taps.

Punches and dies. Penknives. Reamers. Half-round bits. Planing and moulding cutters. Stone-cutting tools; brown yellow, 500° F.

Gouges.

Rock-drills.

Chasers.

Twist-drills. Flat drills for brass. Wood-boring cutters. Drifts. Coopers' tools. Edging cutters; light purple, 530° F. Augers. Dental and surgical instruments. Cold chisels for steel. Axes ; dark purple, 550° F. Gimlets. Cold chisels for cast iron. Saws for bone and ivory. Needles. Firmer-chisels. Hack-saws. Framing-chisels. Cold chisels for wrought iron. Moulding and planing cutters to be filed. Circular saws for metal. Screw-drivers. Springs. Saws for wood.

Dark blue, 570° F. Pale blue, 610°. Blue tinged with green, 630°.

MECHANICS.

FORCE, STATICAL MOMENT, EQUILIBRIUM, ETC.

MECHANICS is the science that treats of the action of force upon bodies. A Force is anything that tends to change the state of a body with respect to rest or motion. If a body is at rest, anything that tends to put it in motion is a force; if a body is in motion, anything that tends to change either its direction or its rate of motion is a force.

A force should always mean the pull, pressure, rub, attraction (or repulsion) of one body upon another, and always implies the existence of a simultaneous equal and opposite force exerted by that other body on the first body, i.e., the reaction. In no case should we call anything a force unless we can conceive of it as capable of measurement by a spring-balance, and are able to say from what other body it comes. (I. P. Church.)

Forces may be divided into two classes, extraneous and molecular: extraneous forces act on bodies from without; molecular forces are exerted be-

tween the neighboring particles of bodies.

Extraneous forces are of two kinds, pressures and moving forces: pressures simply tend to produce motion; moving forces actually produce motion. Thus, if gravity act on a fixed body, it creates pressure; if on a free

motion. Thus, it gravity act on a fixed body, it creates pressure; it on a free body, it produces motion.

Molecular forces are of two kinds, attractive and repellent: attractive forces tend to bind the particles of a body together; repellent forces tend to thrust them asunder. Both kinds of molecular forces are continually exerted between the molecules of bodies, and on the predominance of one or the other depends the physical state of a body, as solid, liquid, or gaseous.

The Unit of Force used in engineering, by English writers, is the pound avoirdupois. (For some scientific purposes, as in electro-dynamics, forces are sometimes expressed in "absolute units." The absolute unit of force is that force which acting on a unit of mass during a unit of time produces a unit of velocity: in English measures, that force which acting on

duces a unit of velocity; in English measures, that force which acting on the mass whose weight is one pound in London will in one second produce a velocity of one foot per second = 1 + 32.187 of the weight of the standard pound avoirdupois at London. In the French C. G. S. or centimetre-gramme second system it is the force which acting on the mass whose weight is one gramme at Paris will produce in one second a velocity of one centimetre per second. This unit is called a "dyne" = 1,981 gramme at Paris.)

Inertia is that property of a body by virtue of which it tends to continue in the state of rest or motion in which it may be placed, until acted on by

some force.

Newton's Laws of Motion.—1st Law. If a body be at rest, it will remain at rest; or if in motion, it will move uniformly in a straight line till

acted on by some force.

2d Law. If a body be acted on by several forces, it will obey each as though the others did not exist, and this whether the body be at rest or in motion.

3d Law. If a force act to change the state of a body with respect to rest or motion, the body will offer a resistance equal and directly opposed to the

or motion, the body with other a resistance equal and directly opposed to force. Or, to every action there is opposed an equal and opposite reaction.

Graphic Representation of a Force.—Forces may be represented geometrically by straight lines, proportional to the forces. A force is given when we know its intensity, its point of application, and the direction in which it acts. When a force is represented by a line, the length of the line represents its intensity; one extremity represents the point of applica-tion; and an arrow-head at the other extremity shows the direction of the force.

Composition of Forces is the operation of finding a single force whose effect is the same as that of two or more given forces. The required

force is called the resultant of the given forces.

Resolution of Forces is the operation of finding two or more forces whose combined effect is equivalent to that of a given force. The required

forces are called components of the given force.

The resultant of two forces applied at a point, and acting in the same direction, is equal to the sum of the forces. If two forces act in opposite directions, their resultant is equal to their difference, and it acts in the direction of the greater.

If any number of forces be applied at a point, some in one direction and others in a contrary direction, their resultant is equal to the sum of those that act in one direction, diminished by the sum of those that act in the opposite direction; or, the resultant is equal to the algebraic sum of the components.

Parallelogram of Forces.—If two forces acting on a point be represented in direction and intensity by adjacent sides of a parallelogram, their resultant will be represented by that diagonal of the parallelogram, which passes through the point. Thus OR, Fig. 88, is the resultant of OQ and OP.

Polygon of Forces.—If several forces are applied at a point and act in a single plane, their resultant is found as follows:

Through the roll of the polygon of the propresenting the

F1g. 88.

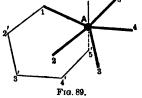
Through the point draw a line representing the first force; through the extremity of this draw a line representing the second force; and so on, throughout the system; finally, draw a line from the starting-point to the extremity of the last line

drawn, and this will be the resultant required.

Suppose the body A, Fig. 89, to be urged in the directions A1, A2, A3, A4, and A5 by forces which are to each other as the lengths of those lines. Suppose these forces to act successively and the body to first move from A to 1; the second force A2 then acts and finding the body at 1 would take it to 2; the third force would then carry it to 8', the fourth to 4', and the fifth to 5'. The line A5' represents in magnitude and direction the resultant of

all the forces considered. If there had been an additional force, Az, in the group, the body would be returned by that force to its original position, supposing the forces to act successively, but if they had acted simultaneously the body would never a bear a mend at all; the teach and acted as the supposition of the have moved at all; the tendencies to motion balancing each other.

It follows, therefore, that if the several forces which tend to move a body can be represented in magnitude and direction by the sides of a closed polygon taken in order, the body will remain at rest; but if the forces are represented by the sides of an open polygon, the body will move and the direction will be represented



by the straight line which closes the polygon.

Twisted Polygon.—The rule of the polygon of forces holds true even when the forces are not in one plane. In this case the lines A1, 1-2', 2'-3', etc., form a twisted polygon, that is, one whose sides are not in one plane.

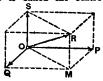
Parallelopipedon of Forces.—If three forces acting on a point be

rarallelopipedon of Forces.—It three forces acting on a point be represented by three edges of a parallelopipedon which meet in a common point, their resultant will be represented by the diagonal of the parallelopipedon that passes through their common point.

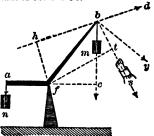
Thus OR, Fig. 90, is the resultant of OQ, OS, and OP. OM is the resultant of OP and OQ, and OR is the resultant of OM and OS.

Moment of a Force.—The moment of a force (sometimes called statical moment), with respect to a point, is the product of the force by the perpendicular distance from the point to

pendicular distance from the point to the direction of the force. The fixed point is called the centre of mo-



F1g. 90.



F1G. 91.

ments ; the perpendicular distance is the lever-arm of the force; and the moment itself measures the tendency of the force to produce rotation about the centre of moments.

If the force is expressed in pounds and the distance in feet, the moment is expressed in foot pounds. It is necessary to observe the distinction be-tween foot-pounds of statical moment and foot-pounds of work or energy.

(See Work.)

In the bent lever, Fig. 91 (from Trautwine), if the weights n and m represent forces, their moments about the point f are respectively $n \times af$ and $m \times fc$. If instead of the weight m a pulling force to balance the weight n is applied in the direction bs, or by or bd, s, y, and d being the amounts of these forces, their respective moments are $s \times ft$, $y \times fb$, $d \times fh$. If the forces sating on the lever are in equilibrium it remains at rest, and

the moments on each side of f are equal, that is, $n \times af = m \times fc$, or $a \times ft$,

or $y \times fb$, or $d \times hf$.

The moment of the resultant of any number of forces acting together in the same plane is equal to the algebraic sum of the moments of the forces

taken separately.

Statical Moment. Stability.—The statical moment of a body is the product of its weight by the distance of its line of gravity from some assumed line of rotation. The line of gravity is a vertical line drawn from its centre of gravity through the body. The stability of a body is that resistance which its weight alone enables it to oppose against forces tending

to overturn it or to slide it along its foundation.

To be safe against turning on an edge the moment of the forces tending to overturn it, taken with reference to that edge, must be less than the statical moment. When a body rests on an inclined plane, the line of gravity being vertical, falls toward the lower edge of the body, and the condition of its not being overturned by its own weight is that the line of gravity must fall within this edge. In the case of an indined tower resting on a plane the same condition holds—the line of gravity must fall within the base. The condition of stability against sliding along a horisontal plane is that the horisontal component of the force exerted tending to cause it to slide shall be less than the product of the weight of the body into the coefficient of friction between the base of the body and its supporting plane. This coefficient of friction is the tangent of the angle of repose, or the maximum angle at

or friction is the tangent of the angle of repose, or the maximum angle at which the supporting plane might be raised from the horisontal before the body would begin to slide. (See Friction.)

The Stability of a Dam against overturning about its lower edge is calculated by comparing its statical moment referred to that edge with the resultant pressure of the water against its upper side. The horizontal pressure on a square foot at the bottom of the dam is equal to the weight of at column of water of one aquare foot in section, and of a height equal to the distance of the bottom below water-level; or, if H is the height, the pressure at the bottom per square foot = $62.4 \times H$ lbs. At the water-level the pressure at the bottom per square root = $52.4 \times H$ lbs. At the water-level the pressure is zero, and it increases uniformly to the bottom, so that the sum of the pressures on a vertical strip one foot in breadth may be represented by the area of a triangle whose base is $69.4 \times H$ and whose altitude is H, or $69.4 H^{2} + 2$. The centre of gravity of a triangle being $\frac{1}{2}$ of its altitude, the resultant of all the horizontal pressures may be taken as equivalent to the sum of the pressures acting at $\frac{1}{2}H$, and the moment of the sum of the pressures is therefore $\frac{1}{2}22 \times \frac{1}{2}22

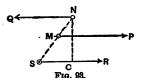
Parallel Forces.—If two forces are parallel and act in the same direction, their resultant is parallel to both, and lies between them, and the intensity of the resultant is equal to the sum of the intensities of the two forces. Thus in Fig. 91 the resultant of the forces n and m acts vertically downward at f, and is equal to n + m.

If two parallel forces act at the extremities of a straight line and in the as two parameter across across as one extremities of a straight line and in the same direction, the resultant divides the line joining the points of application of the components, inversely as the components. Thus in Fig. 91, m:n:: 2f::fo; and in Fig. 92, P::Q::SN::SM.

The resultant of two parallel forces acting in opposite directions is parallel across that the line pathons that the state of the state o

to both, lies without both, on the side and in the direction of the greater, and its intensity is equal to the difference of the intensities of the two forces.

Thus the resultant of the two forces Q and P, Fig. 93, is equal to Q-P=R. Of any two parallel forces and their



resultant each is proportional to the dis-

tance between the other two; thus in both Figs. 92 and 93, P:Q:R:SN:SM:MN. Couples.—If P and Q be equal and act in opposite directions, R=0; that is, they have no resultant. Two such forces constitute of the such that is, they have no resultant. stitute what is called a couple.

The tendency of a couple is to produce Fig. 93. rotation; the measure of this tendency, called the moment of the couple, is the product of one of the forces by the distance between the two.

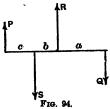
Since a couple has no single resultant, no single force can balance a couple. To prevent the rotation of a body acted on by a couple the application of two other forces is required, forming a second couple. Thus in Fig. 94, P and Q forming a couple, may be balanced by a second couple formed by R and S. The

point of application of either R or S may be a fixed pivot or axis.

Moment of the couple PQ = P(c + b + a) =moment of RS = Rb. Also, P + R = Q + S. The forces R and S need not be parallel to P.

and Q, but if not, then their components parallel to PQ are to be taken instead of the forces themselves.

Equilibrium of Forces.—A system of forces applied at points of a solid body will be in equilibrium when they have no tendency to produce motion, either of translation or of rotation.



The conditions of equilibrium are: 1. The algebraic sum of the components of the forces in the direction of any three rectangular axes must be separately equal to 0.

2. The algebraic sum of the moments of the forces, with respect to any

three rectangular axes, must be separately equal to 0. If the forces lie in a plane: 1. The algebraic sum of the components of the forces, in the direction of any two rectangular axes, must be separately

2. The algebraic sum of the moments of the forces, with respect to any

point in the plane, must be equal to 0.

If a body is restrained by a fixed axis, as in case of a pulley, or wheel and axle, the forces will be in a equilibrium when the algebraic sum of the moments of the forces with respect to the axis is equal to 0.

CENTRE OF GRAVITY.

The centre of gravity of a body, or of a system of bodies rigidly connected together, is that point about which, if suspended, all the parts will be in equilibrium, that is, there will be no tendency to rotation. It is the point through which passes the resultant of the efforts of gravitation on each of the elementary particles of a body. In bodies of equal heaviness throughout, the centre of gravity is the centre of magnitude.

(The centre of magnitude of a figure is a point such that if the figure be divided into equal parts the distance of the centre of magnitude of the

whole figure from any given plane is the mean of the distances of the centres of magnitude of the several equal parts from that plane.)

If a body be suspended at its centre of gravity, it will be in equilibrium in all positions. If it be suspended at a point out of its centre of gravity, it will swing into a position such that its centre of gravity is vertically beneath

its point of suspension.

To find the centre of gravity of any plane figure mechanically, suspend the figure by any point near its edge, and mark on it the direction of a plumb-line hung from that point; then suspend it from some other point, and again mark the direction of the plumb-line in like manner. Then the centre of gravity of the surface will be at the point of intersection of the two marks of the plumb-line.

The Centre of Gravity of Regular Figures, whether plane or solid, is the same as their geometrical centre; for instance, a straight line,

parallelogram, regular polygon, circle, circular ring, prism, cylinder, spheroid, middle frustums of spheroid, etc. Of a triangle: On a line drawn from any angle to the middle of the opposite side, at a distance of one third of the line from the side; or at the

posite side, at a distance or one third of the line from the side; of at the intersection of such lines drawn from any two angles. Of a trapezium or trapezoid: Draw a diagonal, dividing it into two trangles. Draw a line joining their centres of gravity. Draw the other diagonal, making two other triangles, and a line joining their centres. The intersection of the two lines is the centre of gravity required. Of a sector of a circle: On the radius which bisects the arc, $2cr + 3\ell$ from the centre, c being the chord, r the radius, and ℓ the arc. Of a semicircle: On the middle radius, .424r from the centre. Of a gradrant: On the middle radius, .4502r from the centre.

Of a segment of a circle; $c^3 + 12a$ from the centre. c = chord, a = area. Of a parabolic surface: In the axis, 3/5 of its length from the vertex.

Of a semi-parabola (surface): 3/5 length of the axis from the vertex, and % of the semi-base from the axis.

Of a cone or pyramid: In the axis, 14 of its length from the base. Of a paraboloid: In the axis, 16 of its length from the vertex. Of a cylinder, or regular prism: In the middle point of the axis.

Of a frustum of a cone or pyramid: Let $a = \text{length of a line drawn from the vertex of the cone when complete to the centre of gravity of the base, and$ a' that portion of it between the vertex and the top of the frustum; then distance of centre of gravity of the frustum from centre of gravity of its

base = $\frac{a}{4} - \frac{3a'^5}{4(a^3 + aa' + a'^2)^6}$ For two bodies, fixed one at each end of a straight bar, the common centre of gravity is in the bar, at that point which divides the distance between their respective centres of gravity in the inverse ratio of the weights. In this solution the weight of the bar is neglected. But it may

weights. In this solution the weight of the bar is neglected. But it may be taken as a third body, and allowed for as in the following directions:

For more than two bodies connected in one system: Find the common centre of gravity of two of them; and find the common centre of these two jointly with a third body, and so on to the last body of the group.

Another method, by the principle of moments: To find the centre of gravity of a system of bodies, or a body consisting of several parts, whose several centres are known. If the bodies are in a plane, refer their several centres to two rectangular co-ordinate axes. Multiply each weight by its distance from one of the axes, add the products, and divide the sum by the sum of the weights: the result is the distance of the centre of gravity from that axis. Do the same with regard to the other axis. If the bodies are that axis. Do the same with regard to the other axis. If the bodies are not in a plane, refer them to three planes at right angles to each other, and determine the mean distance of the sum of the weights from each of the three planes.

MOMENT OF INERTIA.

The moment of inertia of the weight of a body with respect to an axis is the algebraic sum of the products obtained by multiplying the weight of each elementary particle by the square of its distance from the axis. If the moment of inertia with respect to any axis = I, the weight of any element of the body = w, and its distance from the axis = r, we have $I = \Sigma(wr^2)$.

The moment of inertia varies, in the same body, according to the position The moment of inertia varies, in the same body, according to the position of the axis. It is the least possible when the axis passes through the centre of gravity. To find the moment of inertia of a body, referred to a given axis, divide the body into small parts of regular figure. Multiply the weight of each part by the square of the distance of its centre of gravity from the axis. The sum of the products is the moment of inertia. The value of the axis. The sum of the products is the moment of inertia. The value of the moment of inertia thus obtained will be more nearly exact, the smaller and

more numerous the parts into which the body is divided.

MOMENTS OF INERTIA OF REGULAR SOLIDS.—Rod, or bar, of uniform thickness, with respect to an axis perpendicular to the length of the rod,

$$I=W\left(\frac{l^2}{3}+d^2\right), \qquad (1)$$

 $W = \text{weight of rod}, \mathcal{Q} = \text{length}, d = \text{distance of centre of gravity from axis.}$ Thin circular plate, axis in its $I = W\left(\frac{r^2}{4} + d^2\right)$; (2)

radius of plate.

Circular ring, axis perpendicular $I = W\left(\frac{r^2 + r'^2}{2} + d^2\right)$, (4)

r and r' are the exterior and interior radii of the rin

Cylinder, axis perpendicular to $l=W(\frac{r^2}{4}+\frac{l^3}{8}+d^3)$, the axis of the cylinder,

r = radius of base, 2l = length of the cylinder

By making d=0 in any of the above formulæ we find the moment of inertia for a parallel axis through the centre of gravity.

The moment of inertia, Σwr^2 , numerically equals the weight of a body which, if concentrated at the distance unity from the axis of rotation, would which, it contentrated at the distance unity from the axis of rotation, woint require the same work to produce a given increase of angular velocity that the actual body requires. It bears the same relation to angular acceleration which weight does to linear acceleration (Rankine). The term moment of inertia is also used in regard to areas, as the cross-sections of beams under strain. In this case $I = \mathbb{Z}qr^2$, in which a is any elementary area, and r its distance from the centre. (See under Strength of Materials, p. 247.) Some writers call $\mathbb{Z}mr^2 = \mathbb{Z}wr^2 + g$ the moment of inertia.

CENTRE AND RADIUS OF GYRATION.

The centre of gyration, with reference to an axis, is a point at which, if The centre of gyratron, with retreated to an axis is a point at which, the entire weight of a body be concentrated, its moment of inertia will remain unchanged; or, in a revolving body, the point in which the whole weight of the body may be conceived to be concentrated, as if a pound of platinum were substituted for a pound of revolving feathers, the angular velocity and the accumulated work remaining the same. The distance of this point from the axis is the radius of gyration. If W = the weight of a body, $I = \Sigma wr^2 =$ its moment of inertia, and k = its radius of gyration,

$$I = Wk^2 = 2wr^2; \quad k = \sqrt{\frac{2wr^2}{W}}.$$

The moment of inertia = the weight × the square of the radius of gyration. To find the radius of gyration divide the body into a considerable number of equal small parts—the more numerous the more nearly exact is the result.—then take the mean of all the squares of the distances of the parts from the axis of revolution, and find the square root of the mean square. Or, if the moment of inertia is known, divide it by the weight and extract the square root. For radius of gyration of an area, as a cross-section of a beam, divide the moment of inertia of the area by the area and extract the square root.

The radius of gration is the least possible when the axis passes through the centre of gravity. This minimum radius is called the principal radius of gyration. If we denote it by k and any other radius of gyration by k', we have for the five cases given under the head of moment of inertia above

(1) Rod, axis perpento
$$\left\{k=l\sqrt{\frac{1}{8}}; k'=\sqrt{\frac{l^3}{8}+d^3}\right\}$$

(2) Circular plate, axis
$$k = \frac{r}{2}$$
; $k' = \sqrt{\frac{r^2}{4} + d^2}$.

(3) Circular plate, axis perpent to plane,
$$k = r\sqrt{\frac{1}{2}}$$
; $k' = \sqrt{\frac{r^2}{3} + d^2}$.

(4) Circular ring, axis perpen. to plane,
$$k = \sqrt{\frac{r^2 + r'^2}{2}}$$
; $k' = \sqrt{\frac{r^2 + r'^2}{2} + d^2}$.

(5) Cylinder, axis perpent to length,
$$k = \sqrt{\frac{r^2}{4} + \frac{15}{8}}$$
; $k' = \sqrt{\frac{r^2}{4} + \frac{15}{8} + 48}$

Principal Badii of Gyration and Squares of Badii of Gyration.

(For radii of gyration of sections of columns, see page 249.)

Surface or Solid.	Rad. of Gyration.	Square of R. of Gyration.		
Parallelogram: axis at its base height h " mid-height	.5778h	16h2		
Straight rod: axis at end	.2886h .5773i	1/12h ² 1/6l ²		
rectang. plate "mid-length Rectangular prism:	,28961	1/12/2		
axes 2a, 2b, 2c, referred to axis 2a Parallelopiped: length l, base b, axis (577 4/b2+c2	$\begin{array}{c} (b^3 + c^2) + 8 \\ 4l^2 + b^3 \end{array}$		
at one end, at mid-breadth	$.289 \sqrt{4l^2+b^2}$	12		
out. side h , inn'r h' , axis mid-length very thin, side $= h$, "	.289 $\sqrt{h^2 + h'^2}$.408 h	$(h^2 + h'^2) + 12$ $h^2 + 6$		
Thin rectangular tube: sides b, h, axis mid-length	$.289h\sqrt{\frac{\overline{h+8b}}{\overline{h+b}}}$	$\frac{h^2}{12} \cdot \frac{h+3b}{h+b}$		
Thin circ. plate: rad.r.diam.h,ax. diam.		$\frac{1}{4}r^2 = h^2 + 16$		
Flat circ. ring: diams. h , h' , axis diam. Solid circular cylinder: length l , l	1	$(h^2 + h'^2) + 16$		
axis diameter at mid-length (Circular plate: solid wheel of uni-	.289 $\sqrt{l^2 + 3l^2}$	12+4		
form thickness, or cylinder of any length, referred to axis of cyl	.7071r	1/272		
Hollow circ. cylinder, or flat ring:	.7071 $\sqrt{R^2 + r^2}$	$\begin{array}{c} (R^2 + r^2) + 2 \\ l^2 & R^2 + r^2 \end{array}$		
radii. Axis, 1, longitudinal axis; 2, diam. at mid-length	$.289 \sqrt{l^2 + 3(R^2 + r^2)}$	$\frac{1}{12}$ $\frac{1}{l^2}$ $\frac{4}{R^2}$		
Same: very thin, axis its diameter	.289 $\sqrt{l^2+6R^2}$	13+2		
" radius r; axis, longitud'l axis Circumf. of circle, axis its centre	T T	72		
Sphere: radius r. axis its diam	.7071r .6325r	1672 8/572		
Spheroid: equatorial radius r, re- volving polar axis a	.6325r	2/5r2		
Paraboloid: $r = \text{rad.}$ of base, rev.	.5773r	16r°		
Ellipsoid: semi-axes a, b, c; revolving on axis 2a	$.4472 \sqrt{b^2 + c^2}$	$\frac{b^3+c^3}{5}$		
Spherical shell: radii R, r, revolving to on its diam	$.6325 \sqrt{\frac{R^5 - r^5}{R^3 - r^5}}$	$\frac{2}{5} \frac{R^6 - r^4}{R^3 - r^3}$		
Same: very thin, radius r	8165r	361.3		
Solid cone: r = rad. of base, rev. on axis	.5477 <i>r</i>	0.3r ²		

CENTRES OF OSCILLATION AND OF PERCUSSION.

Centre of Oscillation.—If a body oscillate about a fixed horizontal axis, not passing through its centre of gravity, there is a point in the line drawn from the centre of gravity perpendicular to the axis whose motion is the same as it would be if the whole mass were collected at that point and allowed to vibrate as a pendulum about the fixed axis. This point is called the centre of oscillation.

The Radius of Oscillation, or distance of the centre of oscillation from the point of suspension = the square of the radius of gyration + distance of the centre of gravity from the point of suspension or axis. The centres of oscillation and suspension are convertible.

If a straight line, or uniform thin bar or cylinder, be suspended at one end, oscillating about it as an axis, the centre of oscillation is at % the length of

the rod from the axis. If the point of suspension is at % the length from the end, the centre of oscillation is also at % the length from the axis, that is, it is at the other end. In both cases the oscillation will be performed in the same time. If the point of suspension is at the centre of gravity, the length of the equivalent simple pendulum is infinite, and therefore the time of vibration is infinite.

For a sphere suspended by a cord, r = radius, h = distance of axis of motion from the centre of the sphere, h' = distance of centre of oscillation

from centre of the sphere, $l = \text{radius of oscillation} = h + h' = h + \frac{z}{5} \frac{r^2}{h}$

If the sphere vibrate about an axis tangent to its surface, h = r, and l = r+2/5r. If h = 10r, $l = 10r + \frac{r}{25}$

Lengths of the radius of oscillation of a few regular plane figures or thin

plates, suspended by the vertex or uppermost point.

1st. When the vibrations are flatwise, or perpendicular to the plane of the figure:

In an isosceles triangle the radius of oscillation is equal to % of the height

of the triangle.

In a circle, % of the diameter.
In a parabola, 5/7 of the height.
2d. When the vibrations are edgewise, or in the plane of the figure:

In a circle the radius of oscillation is ¾ of the diameter.

In a rectangle suspended by one angle, % of the diagonal.
In a parabola, suspended by the vertex, 5/7 of the height, plus ¼ of the

parameter. In a parabola, suspended by the middle of the base, 4/7 of the height plus

% the parameter.

Centre of Percussion.—The centre of percussion of a body oscillating about a fixed axis is the point at which, if a blow is struck by the body, the percussive action is the same as if the whole mass of the body were concentrated at the point. This point is identical with the centre of oscillation.

THE PENDULUM.

A body of any form suspended from a fixed axis about which it oscillates by the force of gravity is called a compound pendulum. The ideal body concentrated at the centre of oscillation, suspended from the centre of supension by a string without weight, is called a simple pendulum. This equivalent simple pendulum has the same weight as the given body, and also the same moment of inertia, referred to an axis passing through the point of suspension, and it oscillates in the same time.

The ordinary pendulum of a given length vibrates in equal times when the angle of the vibrations does not exceed 4 or 5 degrees, that is, 2° or 216° each

angle of the vibrations does not exceed 4 or 3 degrees, that is, x^2 or x^2/x^2 each side of the vertical. This property of a pendulum is called its isochronism. The time of vibration of a pendulum varies directly as the square root of the length, and inversely as the square root of the acceleration due to gravity at the given latitude and elevation above the earth's surface. If T = the time of vibration, l = length of the simple pendulum, g = accelerations.

eration = 32.16, $T = \pi \sqrt{\frac{l}{g}}$; since π is constant, $T = \frac{\sqrt{l}}{\sqrt{g}}$. At a given location

tion g is constant and $T \propto \sqrt{l}$. If l be constant, then for any location $T \propto \frac{1}{T}$. If T be constant, $gT^2 = \pi^2 l$; $l \propto g$; $g = \frac{\pi^2 l}{T^2}$. From this equation

the force of gravity at any place may be determined if the length of the simple pendulum, vibrating seconds, at that place is known. At New York this length is 39.1017 inches = 3.2885 ft., whence g = 32.16 ft. At London the length is 39.1393 inches. At the equator 39.0152 or 39.0168 inches, according to different authorities.

Time of vibration of a pendulum of a given length at New York

$$= t = \sqrt{\frac{l}{89.1017}} = \frac{\sqrt{l}}{6.858}$$

t being in seconds and I in inches. Length of a pendulum having a given time of vibration, $l = t^2 \times 89.1017$ inches.

The time of vibration of a pendulum may be varied by the addition of a weight at a point above the centre of suspension, which counteracts the lower weight, and lengthens the period of vibration. By varying the height of the upper weight the time is varied.

To find the weight of the upper bob of a compound pendulum, vibrating seconds, when the weight of the lower bob, and the distances of the weights

from the point of suspension are given:

$$w = W \frac{(39.1 \times D) - D^2}{(39.1 \times d) + d^2}$$

W = the weight of the lower bob, w = the weight of the upper bob; D = the distance of the lower bob and d = the distance of the upper bob from

the point of suspension, in inches.

Thus, by means of a second bob, short pendulums may be constructed to vibrate as slowly as longer pendulums.

By increasing w or d until the lower weight is entirely counterbalanced,

the time of vibration may be made infinite.

Conical Pendulum.—A weight suspended by a cord and revolving at a uniform speed in the circumference of a circular horizontal plane whose radius is r, the distance of the plane below the point of suspension being h, is held in equilibrium by three forces—the tension in the cord, the centrifugal force, which tends to increase the radius r, and the force of gravity acting downward. If v = the velocity in feet per second, the centre of gravity of the weight, as it describes the circumference, g = 82.16, and r and h are taken in feet, the time in seconds of performing one revolution is

$$t = \frac{2\pi r}{v} = 2\pi \sqrt{\frac{h}{\bar{g}}}; \quad h = \frac{gt^2}{4\pi^2} = .8146t^2.$$

If t=1 second, h=.8146 foot = 9.775 inches. The principle of the conical pendulum is used in the ordinary fly-ball governor for steam-engines. (See Governors.)

CENTRIFUGAL FORCE.

A body revolving in a curved path of radius =R in feet exerts a force, called centrifugal force, F, upon the arm or cord which restrains it from moving in a straight line, or "flying off at a tangent." If W= weight of the body in pounds, N= number of revolutions per minute, v= linear velocity of the centre of gravity of the body, in feet per second, g= 32.16,

$$v = \frac{2\pi RN}{60}$$
; $F = \frac{Wv^2}{gR} = \frac{Wv^2}{32.16R} = \frac{W4\pi^2 RN^2}{3600g} = \frac{WRN^2}{2933} = .0003410 WRN^2$ ibs.

If n = number of revolutions per second, $F = 1.2276WRn^2$. (For centrifugal force in fly-wheels, see Fly-wheels.)

VELOCITY, ACCELERATION, FALLING BODIES.

Velocity is the rate of motion, or the distance passed over by a body in

a given time.

If s = space in feet passed over in t seconds, and v = velocity in feet per second, if the velocity is uniform,

$$v = \frac{s}{t}$$
; $s = vt$; $t = \frac{s}{v}$.

If the velocity varies uniformly, the mean velocity $v_0 = \frac{v_1 + v_2}{2}$, in which v_1 is the velocity at the beginning and v_2 the velocity at the end of the time t.

Acceleration is the change in velocity which takes place in a unit of time. Unit of acceleration = a = 1 foot per second in one second. For uniformly varying velocity, the acceleration is a constant quantity, and

$$a = \frac{v_2 - v_1}{t}$$
; $v_3 = v_1 + at$; $v_1 = v_3 - at$; $t = \frac{v_3 - v_1}{a}$ (2)

If the body start from rest, $v_1 = 0$; then

$$v_0 = \frac{v^2}{2}$$
; $v_2 = 2v_0$; $\alpha = \frac{v_2}{t}$; $v_3 = at$; $v_2 - at = 0$; $t = \frac{q_1}{d}$.

Combining (1) and (2), we have

$$s = \frac{v_2^2 - v_1^2}{2a}$$
; $s = v_1 t + \frac{at^2}{2}$; $s = v_2 t - \frac{at^2}{2}$

If $v_1 = 0$, $s = \frac{v_2}{2}t$.

Retarded Motion.-If the body start with a velocity v, and come to rest, $v_2 = 0$; then $s = \frac{v_1}{2}t$.

In any case, if the change in velocity is v,

$$s = \frac{v}{2}t; \quad s = \frac{v^2}{2a}; \quad s = \frac{a}{2}t^2.$$

For a body starting from or ending at rest, we have the equations

$$v = at;$$
 $s = \frac{v}{2}t;$ $s = \frac{at^2}{2};$ $v^2 = 2as.$

Falling Bodies.—In the case of falling bodies the acceleration due to gravity is 32.16 feet per second in one second, = g. Then if v = velocity acquired at the end of t seconds, or final velocity, and h = height or space in feet passed over in the same time,

$$v = gt = 32.16t = \sqrt{2gh} = 8.02 \sqrt{h} = \frac{2h}{t};$$

$$h = \frac{gt^3}{2} = 16.08t^3 = \frac{v^2}{2g} = \frac{v^3}{64.32} = \frac{v^4}{2};$$

$$t = \frac{v}{a} = \frac{v}{32.16} = \sqrt{\frac{2h}{a}} = \frac{\sqrt{h}}{4.01} = \frac{2h}{v};$$

 $u = \text{space fallen through in the } T \text{th second} = g(T - \frac{1}{2}).$

From the above formula for falling bodies we obtain the following: During the first second the body starting from a state of rest (resistance of the air neglected) falls g + 2 = 16.08 feet; the acquired velocity is g =32.16 ft. per sec.; the distance fallen in two seconds is $h = \frac{gt^2}{2} = 16.08 \times 4 =$

64.32 ft.; and the acquired velocity is v=gt=64.32 ft. The acceleration, or increase of velocity in each second, is constant, and is 32.16 ft. per sec. Solving the equations for different times, we find for

6 Height of fall in each second, w... ... 11

Total height of fall, h...... 36

Value of g.—The value of g increases with the latitude, and decreases with the elevation. At the latitude of Philadelphia, 40°, its value is \$2.16. At the sea-level, Everett gives g=32.173-.082 cos 2 lat. -.000003 height in feet. At Paris, lat. 48° 50′ N., g=980.87 cm. =32.181 ft.

Values of $\sqrt{2g}$, calculated by an equation given by C. S. Pierce, are given in a table in Smith's Hydraulics, from which we take the following: Latitude 10° 00 20° 800 400 50°

60° Value of $\sqrt[4]{2g}$. 8.0112 8.0118 8.0137 8.0165 8.0199 8.0235 8.0269

The value of $\sqrt{2g}$ decreases about .0004 for every 1000 feet increase in elevation above the sea-level.

For all ordinary calculations for the United States, g is generally taken at 32.16, and $\sqrt{2g}$ at 8.02. In England g=32.2, $\sqrt{2g}=8.025$. Practical limiting values of g for the United States, according to Pierce, are:

Latitude 49° at sea-level g = 32.18625° 10,000 feet above the sea...... g = 32.08 Fig. 25 represents graphically the velocity, space, etc., of a body falling for

six seconds. The vertical line at the left is the time in seconds, the horizontal lines represent the acquired velocities at the end of each second = \$2.16t. The area of the small triangle at the top represents the height fallen throug in the first second = 1/2 = 16.08 feet, and each of the other triangles is an equa space. The number of triangles between each pair of horizontal lines represents he height of fall in each second, and the number of triangles between any horizontal line and the top is the total height fallen during 16 the time. The figures under h, u, and v the time. The figures under h, u, and v adjoining the cut are to be multiplied by 16.08 to obtain the actual velocities and 25 heights for the given times.

Angular and Linear Velocity of a Turning Body,—Let r = radius of a 86 11 12 turning body in feet, n = pumber of revolutions per minute, v = linear velocity of

per minute.

2" 10

a point on the circumference in feet per second, and 60v = velocity in feet

 $v = \frac{2\pi i n}{60}$, $60v = 2\pi i n$.

Angular velocity is a term used to denote the angle through which any radius of a body turns in a second, or the rate at which any point in it having a radius equal to unity is moving, expressed in feet per second. The unit of angular velocity is the angle which at a distance = radius from the centre is subtended by an arc equal to the radius. This unit angle $=\frac{180}{1}$ degrees = 57.3°. $2\pi \times 57.8^{\circ} = 360^{\circ}$, or the circumference. If A =angular $\frac{2\pi n}{60}$. The unit angle $\frac{180}{\pi}$ is called a radian. velocity, v = Ar, $A = \frac{v}{-} =$

Height Corresponding to a Given Acquired Velocity.

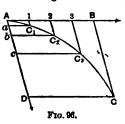
Velocity.	Height.	Velocity.	Height.	Velocity.	Heigat.	Velocity.	Height,	Velocity.	Height.	Velocity.	Height.
feet p.sec. .25	feet. .0010	feet p.sec. 18 14	feet. 2.62 3.04	feet p.sec. 8 85	feet. 17.9 19.0	feet p.sec. 55 56	feet. 47.0 48.8	feet p.sec. 76 77	feet. 89.8 92.2	feet p.sec. 97 98	feet. 146 149
p.sec. .95 .50 .75 1.00 1.25	.0087 .016 .024	15 16 17	8.49 8.98 4.49 5.03	36 87 88 39	20.1 21.8 22.4 23.6	57 50	50.5 52.8 54.1 56.	78 79 80 81	94.6 97.0 99.5 102.0	99 103 105	152 155 171
1.50 1.75 2 2.5 8 3.5	.035 .048 .062 .097	18 19 20 21	5.61 6.22 6.85	40 41 42	24.9 26.1 27.4	59 60 61 62 68	57.9 59.8 61.7	82 83 84	104.5 107.1 109.7	110 115 120 130	188 905 224 263
4 4.5	.140 .190 .248 .814	229 223 224 25	7.52 8.21 8.94 9.71	48 44 45 46	28.7 30.1 31.4 32.9	64 65 66 67	63.7 65.7 67.7 69 8	85 86 87 88	112.8 115.0 117.7 120.4	140 150 175 200	804 850 476 622
5. 6 7 8 9	.888 .559 .761 .994	26 27 28 29	10.5 11.8 12.2 13.1	47 48 49 50	34.8 35.8 37.8 38.9	69 70 71	71.9 74.0 76.2 78.4	89 90 91 92	123.2 125.9 128.7 131.6	800 400 500 600	1899 2488 3887 5597
9 10 11 19	1.26 1.55 1.88 2.24	30 81 83 88	14.0 14.9 15.9 16.9	51 52 53 54	40.4 42.0 43.7 45.3	72 78 74 75	80.6 82.9 85.1 87.5	93 94 95 96	134.5 187.4 140.3 143.8	700 800 900 1000	7618 9952 12593 15547

Falling Bodies: Velocity Acquired by a Body Falling a Given Height.

Height,	Velocity.	Height.	Velocity.	Height.	Velocity.	Height,	Velocity.	Height.	Velocity.	Height.	Velocity.
feet.	feet	feet.	feet	feet.	feet	feet.	feet	feet.	feet	feet.	feet
	p.sec.		p.sec.		p.sec.		p.sec.	0.00	p.sec.	2000	p sec
.005	.57	.39	5.01	1.20	8.79	5.	17.9 18.3	23.	38.5	72 73	68.1
.010	.80	.40	5.07	1.22	8.87	.2	18.3	.5	38.9	78	68.5
.020 .025	.98 1.13	.41	5.14	1.24 1.26	8.94	.4	18.7	24.	39.3	74	69.0
.020	1.13	.42	5.20	1.26	9.01	.6	19.0	.5	39.7	75	69.5
.025	1.27	.43	5.26	1.28	9.08	.8	19.3	25	40.1	76	69,9
.030	1.27 1.39 1.50	.44	5.32	1.30	9.15	6.	19.7	26	40.9	77	70.4
.035	1,50	.45	5.38	1.32	9.21	.2	20.0	27	41.7	78	70.9
.040	1.60	.46	5.44	1.34	9.29	.4	20.3	28	42.5 43.2	79	71.8
.045	1.70	.47	5.50	1.36	9.36	.6	20.6	29	43.2	80	71.8
.050	1.79	.48	5.56	1.38	9.43	.8	20.9	30	43.9	81	72.2
.055	1.88	.49	5.61	1.40	9.49	7.	21.2	31	44.7	82	72.6
.060	1.97	.50	5,67	1.42	9.57	.2	21.5	82	45.4	83	73.1
.065	2.04	.51	5.73	1.44	9.62	.4	21.8	33	46.1	84	73.5
.070	2.12	.52	5.78	1.46	9.70	.6	22.1	84	46.8	85	74.0
.075	2.20	.53	5.78 5.84	1.48	9.77	.8	22.4	35	47.4	86	74.4
.070 .075 .080 .085	2.27	,54	5.90	1.50	9.82	8.	22.4 22.7	36	48.1	86 87	74.8
.085	2.34	,55	5.95	1.52	9.90	.2	28.0	37	48.8	88	75.5
.090	2.41	.56	6.00	1.54	9.96	.4	23.3	88	49.4	89	75.7
.095 .100 .105	2.47	.57	6.06	1.56	10.0	.6	23.5	89	50.1	90	76.
.100	2.54	.58	6.11	1.58	10.1	.8	23.8	40	50.7	91	76.
.105	2.60	.59	6.16	1.60	10.2	9.	24.1	41	51.4	92	76.9
.110	2.66	.60	6.21	1.65	10.3	.2	24.3	42	52.0	98	77.4
.115	2.72	.62	6.32	1.70	10.5	.4	24.6	43	52.6	94	77.8
.120	2.78	.64	6.42	1.75	10.6	6	21.8	44	53.2	95	78.5
.125	2.84	.66	6.52	1.80	10.8	.8	25.1	45	53.8	96	178.€
.130	2.89	.68	6,61	1.90	11.1	10.	25.4	46	54.4	97	79.0
.14	3.00	.70	6.71	2.	11.4	.5	26.0	47	55.0	98	79.4
.15	3.11	,72	6.81	2.1	11.7	11.	26.6	48	55.6	99	79.8
.16	3.21 8.31	.74	6.90	2.2	11.9	.5	27.2	49	56.1	100	80.5
.17	8.31	.76	6.99	2.3	12.2	12.	27.8	50	56.7	125	89.7
.18	3.40	.78	7.09	2.4	12.4	.5	28.4	51	57.8	150	98.3
.19	8.50	.80	7.18	2.5	12.6	13.	28.9	52	57.8	175	106
.20	3.59	.82	7.26	2.6	12.0	.5	29.5	53	58.4	200	114
.21	3.68 8.76	.84	7.35	2.7	13.2	14.	30.0	54	59.0	225	120
99	8.76	.86	7.44	2.8	13.4	.5	3 .5	55	59.5	250	126
.28 .24 .25	1 3.85	.88	7.53	2.9	13.7	15,	31.1	56	60,0	275	133
.24	8.93 4.01	.90	7.61	3.	13.9	.5	31.6	57	60.6	300	139
.25	4.01	.92	7.69	3.1	14.1	16.	33.1	58	61.1	350	150
. 326	4.09	.94	7.78	3.2	14.3	.5	32.6	59	61.6	400	160
.27	4.17	.96	7.86	3.3	14.5	17.	83.1	60	62.1	450	170
.28	4,25	.98	7.94	3.4	14.8	.5	83.6	61	62.7	500	179
,29	4.32	1.00	8.02	3.5	15.0	18.	34.0	-62	64.2	550	188
.30	4.39	1.02	8.10	3.6	15.2	.5	34.5	63	63.7	600	197
.31	4.47	1.04	8.18	8.7	15.4	19.	85.0	64	64.2	700	212
.32	4 54	1.06	8.26	3.8	15.6	.5	35.4	65	64.7	800	227
.33	4.61	1.08	8.34	3.9	15.8	20.	85.9	66	65,2	900	241
.34	4.68	1.10	8.41	4.	16.0	.5	36.3	67	65.7	1000	254
-35	4.74	1.12	8.49	.2	16.4	21.	36.8	68	66.1	2000	859
.36	4.61 4.68 4.74 4.81	1.14	8.57	.4	16.8	.5	37.2	69	66.6	3000	439
.33 .34 .35 .36 .37 .38	4.88	1.16	8.64	.6	17.2	22.	37.6	70	67.1	4000	507
.38	4.94	1.18	8.72	8.	17.6	.5	38.1	71	67.6	5000	567

Parallelogram of Velocities.—The principle of the composition and resolution of forces may also be applied to velocities or to distances moved in given intervals of time. Referring to Fig. 88, page 416, if a body at O has a force applied to it which acting alone would give it a velocity represented by OQ per second, and at the same time it is acted on by

another force which acting alone would give it a velocity OP per second, the result of the two forces acting together for one second will carry it to



The path of a projectile is a parabola. The distance it will travel is greatest when its initial direction is at an angle 45° above the horizontal.

Mass—Force of Acceleration.—The mass of a body, or the quantity of matter it contains, is a constant quantity, while the weight varies according to the variation in the force of gravity at different places. If g = the acceleration ation due to gravity, and w = weight, then the mass $m = \frac{w}{m}$, w = mg. Weight

here means the resultant of the force of gravity on the particles of a body, such as may be measured by a spring-balance, or by the extension or deflection of a rod of metal loaded with the given weight.

Force has been defined as that which causes, or tends to cause, or to destroy, motion. It may also be defined (Kennedy's Mechanics of Machinery) as the cause of acceleration; and the unit of force as the force required to produce unit acceleration in a unit of free mass.

Force equals the product of the mass by the acceleration, or f = ma. Also, if v = the velocity acquired in the time t, ft = mv; f = mv + t; the

acceleration being uniform.

The force required to produce an acceleration of g (that is, 82.16 ft. per sec.) in one second is $f = mg = \frac{w}{a}g = w$, or the weight of the body. Also, $f = ma = m\frac{v_2 - v_1}{t}$, in which v_2 is the velocity at the end, and v_1 the velocity at the beginning of the time t, and $f = mg = \frac{w}{g} \frac{(v_2 - v_1)}{t} = \frac{w}{g} a$;

 $\frac{f}{w} = \frac{a}{a}$; or, the force required to give any acceleration to a body is to the

weight of the body as that acceleration is to the acceleration produced by gravity. (The weight w is the weight where g is measured.) Example.—Tension in a cord lifting a weight. A weight of 100 lbs. is lifted vertically by a cord a distance of 80 feet in 4 seconds, the velocity uniformly increasing from 0 to the end of the time. What tension must be maintained in the cord? Mean velocity $= v_0 = 20$ ft. per sec.; final velocity $= v_0 = 2v_0 = 40$; acceleration $a = \frac{v_0}{t} = \frac{40}{4} = 10$. Force $f = ma = \frac{va}{g} = \frac{100}{82.16} \times \frac{va}{g} = \frac{100}{82.16} \times \frac{va}{g} = \frac{100}{82.16} \times \frac{va}{g} = \frac{va}{g} = \frac{100}{82.16} \times \frac{va}{g} = \frac{$ 10 = 81.1 lbs. This is the force required to produce the acceleration only; to it must be added the force required to lift the weight without acceleration, or 100 lbs., making a total of 131.1 lbs.

The Resistance to Acceleration is the same as the force required to pro-

duce the acceleration = $\frac{w}{v_2 - v_1}$

Formulæ for Accelerated Motion.—For cases of uniformly accelerated motion other than those of falling bodies, we have the formulæ already given, $f = \frac{w}{a}a_1 = \frac{w}{a} \frac{v_2 - v_1}{b}$. If the body starts from rest, $v_1 = 0$, where = v, and $f = \frac{w}{g} \frac{v}{t}$, fgt = wv. We also have $s = \frac{vt}{2}$. Transforming and substituting for g its value 22.16, we obtain

$$f = \frac{svv^2}{64.52s} = \frac{sov}{82.16t} = \frac{sos}{16.06t^2}; \quad w = \frac{32.16ft}{v} = \frac{64.82fs}{v^2};$$

$$s = \frac{svv^2}{64.32f} = \frac{16.06ft^3}{w} = \frac{vt}{2}; \quad v = 8.02 \sqrt{\frac{fs}{w}} = \frac{32.16ft}{w};$$

$$t = \frac{svv}{32.16t} = \frac{1}{4.01} \sqrt{\frac{ts}{f}}$$

For any change in velocity $f = w \left(\frac{v_2^2 - v_1^2}{64.32s} \right)$. (See also Work of Acceleration, under Work.)

Motion on Inclined Planes.—The velocity acquired by a body descending an inclined plane by the force of gravity (friction neglected) is equal to that acquired by a body falling freely from the height of the plane. The times of descent down different inclined planes of the same height vary as the length of the planes.

The rules for uniformly accelerated motion apply to inclined planes. If a is the angle of the plane with the horizontal, $\sin a =$ the ratio of the height to the length $= \frac{b}{t}$, and the constant accelerating force is $g \sin a$. The final velocity at the end of t seconds is $v = gt \sin a$. The distance passed over in t seconds is $t = k at^2 \sin a$. The time of descent is

$$t = \sqrt{\frac{2l}{g \sin a}} = \frac{l}{4.01 \sqrt{k}}.$$

MOMENTUM, VIS-VIVA.

Momentum, or quantity of motion in a body, is the product of the mass by the velocity at any instant = $nv = \frac{tv}{-v}$.

Since the moving force = product of mass by acceleration, f = ma; and if the velocity acquired in t seconds = v, or $a = \frac{w}{t}$, $f = \frac{mv}{t}$; ft = mv; that is, the product of a constant force into the time in which it acts equals numer ically the momentum.

Since ft = mv, if t = 1 second mv = f, whence momentum might be defined as numerically equivalent to the number of pounds of force that will stop a moving body in 1 second, or the number of pounds of force which acting during 1 second will give it the given velocity.

Vis-viva, or living force, is a term used by early writers on Mechanics to denote the energy stored in a moving body. Some defined it as the product of the mass into the square of the velocity, mv^2 , $= \frac{w}{g}v^2$ others as one half of this quantity or $\frac{1}{2}mv^2$, or the same as what is now known as energy. The term is now practically obsolete, its place being taken by the word energy.

WORK, ENERGY, POWER.

Work is the overcoming of resistance through a certain distance. It is measured by the product of the resistance into the space through which it is overcome. It is also measured by the product of the moving force into the distance through which the force acts in overcoming the resistance. Thus in lifting a body from the earth against the attraction of gravity, the resistance is the weight of the body, and the product of this weight into the height the body is lifted is the work done.

resistance is the weight of the body, and the product of this weight into the height the body is lifted is the work done.

The Unit of Work, in British measures, is the fcol-pound, or the amount of work done in overcoming a pressure or weight equal to one pound through one foot of space.

The work performed by a piston in driving a fluid before it, or by a fluid in driving a piston before it, may be expressed in either of the following

> Resistance \times distance traversed = intensity of pressure × area × distance traversed ; = intensity of pressure × volume traversed.

The work performed in lifting a body is the product of the weight of the body into the height through which its centre of gravity is lifted.

If a machine lifts the centres of gravity of several bodies at once to heights

either the same or different, the whole quantity of work performed in so loing is the sum of the several products of the weights and heights; but that quantity can also be computed by multiplying the sum of all the weights into the height through which their common centre of gravity is lifted. (Rankine.)

Power is the rate at which work is done, and is expressed by the quotient of the work divided by the time in which it is done, or by units of work per second, per minute, etc., as foot-pounds per second. The most common unit of power is the horse-power, established by James Watt as the power of a strong London draught-horse to do work during a short interval, and used by him to measure the power of his steam-engines. This unit is \$3,000 foot-pounds per minute = 550 foot-pounds per second = 1,980,000 foot-pounds per hour,

Expressions for Force, Work, Power, etc.

The fundamental conceptions in Dynamics are:

Mass, Force, Time, Space, represented by the letters M, F, T, S. Mass = weight +g. If the weight of a body is determined by a spring balance standardized at London it will vary with the latitude, and the value of g to be taken in order to find the mass is that of the latitude where the weighing is done. If the weight is determined by a balance or by a platform scale, as is customary in engineering and in commerce, the London

value of $g_1 = 32.2$, is to be taken.

Velocity = space divided by time, V = S + T, if V be uniform.

Work = force multiplied by space = $FS = \frac{1}{2}MV^2 = FVT$. (V uniform.)

Power = rate of work = work divided by time = FS + T = P = product of force into velocity = FV.

Power exerted for a certain time produces work; PT = FS = FVT.

Refort is a force which acts on a body in the direction of its motion. Resistance is that which is opposed to a moving force. It is equal and opposite force.

Horse-power Hours, an expression for work measured as the product of a power into the time during which it acts = PT. Sometimes it is the summation of a variable power for a given time, or the average power

multiplied by the time.

multiplied by the time.

Energy, or stored work, is the capacity for performing work. It is measured by the same unit as work, that is, in foot-pounds. It may be either potential, as in the case of a body of water stored in a reservoir, capable of doing work by means of o water-wheel, or actual, sometimes called kinetic, which is the energy of a moving body. Potential energy is measured by the product of the weight of the stored body into the distance through which it is capable of acting, or by the product of the pressure it exerts into the distance through which that pressure is capable of acting.

Potential energy may also exist as stored best, or as stored chamical energy. Potential energy may also exist as stored heat, or as stored chemical energy, as in fuel, gunpowder, etc., or as electrical energy, the measure of these energies being the amount of work that they are capable of performing. Actual energy of a moving body is the work which it is capable of performing against a retarding resistance before being brought to rest, and is equal to the work which must be done upon it to bring it from a state of rest to its actual velocity.

The measure of actual energy is the product of the weight of the body into the height from which it must fall to acquire its actual velocity. If v= the velocity in feet per second, according to the principle of falling bodies,

 $\frac{3}{2a}$, and if w = the weight, the energy = A, the height due to the velocity =

 $\frac{1}{2}mv^2 = wv^2 + 2g = wh$. Since energy is the capacity for performing work, the units of work and energy are equivalent, or $FS = 16mv^2 = wh$. Energy exerted = work done,

The actual energy of a rotating body whose angular velocity is A and moment of inertia $\sum vv^2 = I$ is $\frac{A^2I}{2g}$, that is, the product of the moment of inertia into the height due to the velocity, A, of a point whose distance from the axis of rotation is unity; or it is equal to $\frac{wv^2}{2g}$, in which w is the weight of the body and v is the velocity of the centre of gyration.

Work of Acceleration.—The work done in giving acceleration to a body is equal to the product of the force producing the acceleration, or of the resistance to acceleration, into the distance moved in a given time. This force, as already stated equals the product of the mass into the acceleration,

or
$$f = ma = \frac{w}{g} \frac{v_2 - v_1}{t}$$
. If the distance traversed in the time $t = s$, then work $= fs = \frac{w}{a} \frac{v_2 - v_1}{t}s$.

EXAMPLE.—What work is required to move a body weighing 100 lbs. horizontally a distance of 80 ft. in 4 seconds, the velocity uniformly increasing, friction neglected?

Mean velocity $v_0 = 20$ ft. per second; final velocity $= v_2 = 2v_6 = 40$; initial velocity $v_1 = 0$; acceleration, $a = \frac{v_2 - v_1}{t} = \frac{40}{4} = 10$; force $= \frac{w}{g}a = \frac{100}{32.16} \times 10^{-3}$

10 = 31.1 lbs.; distance 80 ft.; work = fs = 31.1 \times 80 = 2488 foot-pounds. The energy stored in the body moving at the final velocity of 40 ft. per second is

$$1/6mv^2 = \frac{1}{2}\frac{w}{g}v^2 = \frac{100 \times 40^2}{2 \times 82.16} = 2488$$
 foot-pounds,

which equals the work of acceleration

$$fs = \frac{w}{g} \frac{v_2}{t} s = \frac{w}{g} \frac{v_2}{t} \frac{v_2}{2} t = \frac{1}{2} \frac{w}{g} v_2^2.$$

If a body of the weight W falls from a height H, the work of acceleration is simply WH, or the same as the work required to raise the body to the same height.

Work of Accelerated Rotation.—Let A = angular velocity of a solid body rotating about an axis, that is, the velocity of a particle whose radius is unity. Then the velocity of a particle whose radius is r is v = Ar. If the angular velocity is accelerated from A_1 to A_2 , the increase of the velocity of the particle is $v_2 - v_1 = r(A_1 - A_2)$, and the work of accelerating is $a_1 - a_2 - a_3 -$

$$\frac{w}{g} \times \frac{v_2^2 - v_1^2}{2} = \frac{wr^2}{g} \frac{A_1^2 - A_1^2}{2},$$

in which w is the weight of the particle.

The work of acceleration of the whole body is

$$\sum \left\{ \frac{w}{g} \times \frac{v_2^2 - v_1^2}{2} \right\} = \frac{A_2^2 - A_1^2}{2g} \times \Sigma wr^2.$$

The term \(\text{Z}\) is the moment of inertia of the body.

66 Force of the Blow? of a Steam Hammer or Other Falling Weight.—The question is often asked: "With what force does a failing hammer strike?" The question cannot be answered directly, and it is based upon a misconception or ignorance of fundamental mechanical laws. The energy, or capacity of doing work, of a body raised to a given height and let fall cannot be expressed in pounds, simply, but only in footpounds, which is the product of the weight into the height through which it fails, or the product of its weight + 64.32 into the square of the velocity in fast per second, which it acquires after falling through the given height. it rais, or the product of its weight + 54.32 into the square of the velocity, in feet per second, which it acquires after falling through the given height. If F = weight of the body, M its mass, g the acceleration due to gravity. S the height of fall, and v the velocity at the end of the fall, the energy in the body just before striking, is $FS = \frac{1}{26}Mv^2 = Wv^2 + 2g = Wv^2 + 64.32$, which is the general equation of energy of a moving body. Just as the energy of the body is a product of a force into a distance, so the work it does when it strikes is not the manifestation of a force, which can be expressed simply in pounds, but it is the overcoming of a resistance through a certain distance, which is expressed as the product of the average resist ance into the distance through which it is exerted. If a hammer weighing 100 lbs. falls 10 ft., its energy is 1000 foot-pounds. Before being brought to rest it must do 1000 foot-pounds of work against one or more resistances. These are of various kinds, such as that due to motion imparted to the body These are of various kinds, such as that due to motion imparted to the body struck, penetration against friction, or against resistance to shearing or other deformation, and crushing and heating of both the falling body and the body struck. The distance through which these resisting forces act is generally indeterminate, and therefore the average of the resisting forces, which themselves generally vary with the distance, is also indeterminate.

Impact of Bodies.—If two inelastic bodies collide, they will move on together as one mass, with a common velocity. The momentum of the combined mass is equal to the sum of the momenta of the two bodies before income.

pact. If m_1 and m_2 are the masses of the two bodies and v_1 and v_2 their respective velocities before impact, and v their common velocity after impact, $(m_1 + m_2)v = m_1v_1 + m_2v_2$

 $v = \frac{m_1 v_1 + m_2 v_3}{m_1 + m_2}.$

If the bodies move in opposite directions $v = \frac{m_1 v_1 - m_2 v_3}{m_1 + m_2}$, or, the velocity of two inelastic bodies after impact is equal to the algebraic sum of their

momenta before impact, divided by the sum of their masses. If two inelastic bodies of equal momenta impinge directly upon one an-

other from opposite directions they will be brought to rest.

Impact of Inelastic Bodies Causes a Loss of Energy, and this loss is equal to the sum of the energies due to the velocities lost and gained by the bodies, respectively.

$$\frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2 - \frac{1}{2}(m_1 + m_2)v^2 = \frac{1}{2}m_1(v_1 - v)^2 + \frac{1}{2}m_2(v_2 - v)^2.$$

In which $v_1 - v$ is the velocity lost by m_1 and $v - v_2$ the velocity gained by m_2 .

Example—Let $m_1 = 10$, $m_2 = 8$, $v_1 = 12$, $v_3 = 15$.

If the bodies collide they will come to rest, for $v = \frac{10 \times 12 - 8 \times 15}{10 + 8} = 0$.

The energy loss is

 $\frac{1}{6}10 \times 144 + \frac{1}{6}8 \times 225 - \frac{1}{6}18 \times 0 = \frac{1}{6}10(12 - 0)^2 + \frac{1}{6}8(15 - 0)^2 = 1620 \text{ ft. lbs.}$

Note that $v_1v_2 = v_3 = v_4 = v_3 = v_4 = v_3 = v_4 = v_3 = v_4 = v_3 = v_4 = v_3 = v_4$

$$\begin{split} v_1' &= \frac{m_1 v_1 + m_2 v_2}{m_1 + m_2} - \frac{m_2 e(v_1 - v_2)}{m_1 + m_2}; \\ v_3' &= \frac{m_1 v_1 + m_2 v_2}{m_1 + m_2} + \frac{m_1 e(v_1 - v_2)}{m_1 + m_3}. \end{split}$$

If the bodies are perfectly elastic, their relative velocities before and after impact are the same. That is: $v_1' - v_3' = v_2 - v_1$.

In the impact of bodies, the sum of their momenta after impact is the

same as the sum of their momenta before impact.

$$m_1v_1' + m_2v_2' = m_1v_1 + m_2v_2.$$

For demonstration of these and other laws of impact, see Smith's Mechanics; also, Weisbach's Mechanics.

Energy of Recoil of Guns.—(Eng'g, Jan. 25, 1884, p. 72.)

Let W= the weight of the gun and carriage; V= the maximum velocity of recoil; v= the weight of the projectile; v= the muzzle velocity of the projectile.

Then, since the momentum of the gun and carriage is equal to the momentum of the projectile, we have WV = wv, or V = wv + W.

^{*}The statement by Prof. W. D. Marks, in Nystrom's Mechanics, 20th edition, p. 454, that this formula is in error is itself erroneous.

Taking the case of a 10-inch gun firing a 400-lb. projectile with a muzzle velocity of 1400 feet per second, the weight of the gun and carriage being 22 tons = 49,280 lbs., we find the velocity of recoil =

$$V = \frac{1400 \times 400}{49,280} = 11$$
 feet per second.

Now the energy of a body in motion is $WV^2 + 2a$.

Therefore the energy of recoil = $\frac{49,280 \times 11^2}{2 \times 32.2}$ = 92,593 foot-pounds.

The energy of the projectile is $\frac{400 \times 1400^3}{2 \times 82.2} = 12,173,918$ foot-pounds.

Conservation of Energy.—No form of energy can ever be produced except by the expenditure of some other form, nor annihilated except by being reproduced in another form. Consequently the sum total of energy in the universe, like the sum total of matter, must always remain the same. (S. Newcomb.) Energy can never be destroyed or lost; it can be transformed, can be transferred from one body to another, but no matter what transformations are undergone, when the total effects of the

exertion of a given amount of energy are summed up the result will be exactly equal to the amount originally expended from the source. This law is called the Conservation of Energy. (Cotterill and Slade.)

A heavy body sustained at an elevated position has potential energy. When it falls, just before it reaches the earth's surface it has actual or kinetic energy, due to its velocity. When it strikes it may penetrate the earth a certain distance or may be crushed. In either case friction results by which the energy is converted into heat which is gradually redisted. by which the energy is converted into heat, which is gradually radiated into the earth or into the atmosphere, or both. Mechanical energy and heat are mutually convertible. Electric energy is also convertible into heat or mechanical energy, and either kind of energy may be converted into the

other.

other.

Sources of Energy.—The principal sources of energy on the earth's surface are the muscular energy of men and animals, the energy of the wind, of flowing water, and of fuel. These sources derive their energy from the rays of the sun. Under the influence of the sun's rays vegetation grows and wood is formed. The wood may be used as fuel under a steam boiler, its carbon being burned to carbonic acid. Three tenths of its heat energy escapes in the chimney and by radiation, and seven tenths appears as potential energy in the steam. In the steam-engine, of this seven tenths six parts are dissipated in heating the condensing water and are wasted; the remaining one tenth of the original heat energy of the wood is converted into mechanical work in the steam-engine, which may be used to drive machinery. This work is finally, by friction of various kinds, or possibly after transformation into electric currents, transformed into heat, which is radiated into the atmosphere, increasing its temperature. Thus all the potential heat energy of the wood is, after various transformations, which is radiated into the atmosphere, increasing its temperature. Thus all the potential heat energy of the wood is, after various transformations, converted into heat, which, mingling with the store of heat in the atmosphere, apparently is lost. But the carbonic acid generated by the combustion of the wood is, again, under the influence of the sun's rays, absorbed by vegetation, and more wood may thus be formed having potential energy

equal to the original.

Perpetual Motion.—The law of the conservation of energy, than which no law of mechanics is more firmly established, is an absolute barrier ment no new of mechanics is more irring established, is an absolute barrier to all schemes for obtaining by mechanical means what is called "perpetual motion," or a machine which will do an amount of work greater than the equivalent of the energy, whether of heat, of chemical combination, of electricity, or mechanical energy, that is put into it. Such a result would be the creation of an additional store of energy in the universe, which is not received by any human agency.

possible by any human agency.

The Efficiency of a Machine is a fraction expressing the ratio of the useful work to the whole work performed, which is equal to the energy expended. The limit to the efficiency of a machine is unity, denoting the efficiency of a perfect machine in which no work is lost. The difference between the energy expended and the useful work done, or the loss, is usually expended either in overcoming friction or in doing work on bodies surrounding the machine from which no useful work is received. Thus in an engine propelling a vessel part of the energy exerted in the cylinder Joes the useful work of giving motion to the vessel, and the remainder is spent in overcoming the friction of the machinery and in making currents and eddies in the surrounding water.

ANIMAL POWER.

Work of a Man against Known Resistances. (Rankine.)

MOIT OF A PERSON					
Kind of Exertion.	R, lbs.	V, ft. per sec.	3600 (hours per day).	RV, ftlbs. per sec.	RVT, ftlbs, per day.
Raising his own weight up stair or ladder Hauling up weights with rope,	140	0.5	8	72.5	2,088,000
loaded	40 44	0.75 0.55	6	80 24.2	648,000 522,720
4. Carrying weights up-stairs	143	0.18	6	18.5	399,600
5. Shovelling up earth to a height of 5 ft. 3 in	•	1.8	10	7.8	280,800
veloc. 0.9 ft. per sec. and re-	132	0.075	10	9.9	356,400
7. Pushing or pulling horizon- tally (capstan or oar)	120.5	2.0 5.0	,8	58 62.5	1,526,400
8. Turning a crank or winch	18.0 20.0 18.2	2.5 14.4 2.5	2 min. 10	45 988 83	1,296,000 1,188,000
9. Working pump 10. Hammering	15	,	87	7	480,000
					·

Explanation.—R, resistance; V, effective velocity = distance through which R is overcome + total time occupied, including the time of moving unloaded, if any; T^{V} , time of working, in seconds per day; $T^{V} \rightarrow 3600$, same time, in hours per day; RV, effective power, in foot-pounds per second; RVT, daily work.

Performance of a Man in Transporting Loads Horizontally. (Rankiue.)

Kind of Exertion.	L, lbs.	V, ftsec.	8600 (hours per day).	LV, lbs. con- veyed 1 foot.	LVT, lbs. con- veyed 1 foot.
 Walking unloaded transporting his own weight Wheeling load L in 2 whid barrow, return unloaded. Ditto in 1-wh. barrow, ditto. Travelling with burden Carrying burden, returning unloaded Carrying burden, for 30 seconds only 	224 183 90	5 136 136 235 186 0 11.7 23.1	10 10 10 7 6	700 878 220 225 288 0 1474.2	25,200,000 18,428,000 7,920,000 5,670,000 5,082,800

EXPLANATION.—L, load; V, effective velocity, computed as before; T', time of working, in seconds per day; T'' + 8600, same time in hours per day; LV, transport per second, in lbs. conveyed one foot; LVT, daily transport

In the first line only of each of the two tables above is the weight of the man taken into account in computing the work done. Clark says that the average net daily work of an ordinary laborer at a

pump, a winch, or a crane may be taken at 3300 foot-pounds per minute, or one-tenth of a horse-power, for 8 hours a day; but for shorter periods from four to five times this rate may

be exerted.

Mr. Glynn says that a man may exert a force of 25 lbs. at the handle of a crane for short periods; but that for continuous work a force of 15 lbs. is all that should be assumed, moving through 220 feet per minute.

Man-wheel.—Fig. 97 is a sketch of a very efficient man-power hoisting-machine which the author saw in Berne, Switzerland, in 1889. The face of the wheel was wide enough for three men to walk abreast, so that nine men could work in it at one time.

F1G. 97.

Work of a Horse against a Known Resistance. (Rankine.)

Kind of Exertion.	R.	v.	T. 3600	RV.	RVT.
1. Cantering and trotting, drawing a light railway carriage (thoroughbred) 2. Horse drawing cart or boat,	min. 2214 mean 3014 max. 50	143%	4	44716	6,444,000
walking (draught-horse)	120	8.6	8	432	12,441,600
3. Horse drawing a gin or mill, walking 4. Ditto, trotting	100 66	8.0 6. 5	8 41⁄2	300 429	8,640,000 6,950,000

Explanation.—R, resistance, in lbs.; V, velocity, in feet per second; $T'' \rightarrow 800$, hours work per day; RV, work per second; RVT, work per day. The average power of a draught-horse, as given in line 2 of the above table, being 432 foot-pounds per second, is 432/550 = 0.785 of the conventional value assigned by Watt to the ordinary unit of the rate of work of prime movers. It is the mean of several results of experiments, and may be considered the average of ordinary performance under favorable circumstances.

Performance of a Horse in Transporting Loads Horizontally. (Rankine.)

Kind of Exertion.	L.	v.	T.	LV.	LVT.
5. Walking with cart, always loaded	1500	8.6	10	5400	194,400,000
	750	7.2	41/2	5400	87,480,000
ed, returning empty; V, mean velocity 8. Carrying burden, walking 9. Ditto, trotting	1500	2.0	10	3000	108,000,000
	270	8.6	10	972	34,992,000
	180	7.2	7	1296	82,659,200

Explanation.—L, load in lbs.; V, velocity in feet per second; T+3600, working hours per day; LV, transport per second; LVT, transport per day. This table has reference to conveyance on common roads only, and those evidently in bad order as respects the resistance to traction upon them.

Horse Gin.-In this machine a horse works less advantageously

than in drawing a carriage along a straight track. In order that the best

possible results may be realized with a horse-gin, the diameter of the circular track in which the horse walks should not be less than about forty

Oxen, Mules, Asses.—Authorities differ considerably as to the power these animals. The following may be taken as an approximative comof these animals. parison between them and draught-horses (Rankine):

Ox.-Load, the same as that of average draught-horse; best velocity and

work, two thirds of horse.

Mule.-Load, one haif of that of average draught-horse; best velocity, the same with horse; work one half.

Ass.-Load, one quarter that of average draught-horse; best velocity the

same; work one quarter.

Beauer, work one quarter.

Reduction of Draught of Horses by Increase of Grade of Boads. (Engineering Record, Prize Essays on Roads, 1892.)—Experiments on English roads by Gayffler & Parnell:

Calling load that can be drawn on a level 100:

The Resistance of Carriages on Roads is (according to Gen. Morin) given approximately by the following empirical formula:

$$R = \frac{W}{r}[a + b(u - 8.28)].$$

In this formula R = total resistance; r = radius of wheel in inches; W =gross load; u = velocity in feet per second; while a and b are constants, whose values are: For good broken-stone road, a = .4 to .55, b = .024 to .026; for paved roads, a = .27, b = .0884.

Rankine states that on gravel the resistance is about double, and on

sand five times, the resistance on good broken-stone roads.

ELEMENTS OF MACHINES.

The object of a machine is usually to transform the work or mechanical energy exerted at the point where the machine receives its motion into

work at the point where the final resistance The specific end may be to is overcome. change the character or direction of motion, as from circular to rectilinear, or vice versa, to change the velocity, or to overcome a great resistance by the application of a moderate force. In all cases the total energy exerted equals the total work done, the latter including the overcoming of all the frictional resistances of the machine as well as the useful work performed. No increase of power can be obtained from any machine, since this is impossible according to the law of conservation of energy. In a frictionless machine the product of the force exerted at the drivingpoint into the velocity of the driving-point, or the distance it moves in a given interval of time, equals the product of the resistance into the distance through which the resistance is overcome in the same time.

The most simple machines, or elementary machines, are reducible to three classes, viz., the Lever, the Cord, and the Inclined Plane.

The first class includes every machine consisting of a solid body capable of revolving on an axis, as the Wheel and Axle.

The second class includes every machine in which force is transmitted by means of flexi-

ble threads, ropes, etc., as the Pulley.

The third class includes every machine in which a hard surface inclined to the direc-

tion of motion is introduced, as the Wedge and the Screw.

A Lever is an inflexible rod capable of motion about a fixed point, called a fulcrum. The rod may be straight or bent at any angle, or curved. It is generally regarded, at first, as without weight, but its weight may be

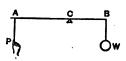
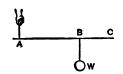


Fig. 98.



Frg. 99.



Fig. 100.

considered as another force applied in a vertical direction at its centre of gravity.

The arms of a lever are the portions of it intercepted between the force, P, and fulcrum, C, and between the weight, W, and fulcrum.

Levers are divided into three kinds or orders, according to the relative positions of the applied force, weight, and fulcrum.

In a lever of the first order, the fulcrum lies between the points at which

the force and weight act. (Fig. 98.)
In a lever of the second order, the weight acts at a point between the

fulcrum and the point of action of the force. (Fig. 99.)
In a lever of the third order, the point of action of the force is between

that of the weight and the fulcrum. (Fig. 100.)
In all cases of levers the relation between the force exerted or the pull, P, and the weight lifted, or resistance overcome, W, is expressed by the equation $P \times AC = W \times BC$, in which AC is the lever-arm of P, and BC is the lever-arm of P, or moment of the force P the moment of the resist-

ance. (See Moment.)

ance. (see moment.) In cases in which the direction of the force (or of the resistance) is not at right angles to the arm of the lever on which it acts, the "lever-arm" is the length of a perpendicular from the fulcrum to the line of direction of the force (or of the resistance). W:P::AC:BC, or, the ratio of the resistance to the applied force is the inverse ratio of their lever-arms. Also, if V^w is the velocity of W, and V_P is the velocity of W, and V_P is the V^w .

If So is the distance through which the applied force V^w .

If Sp is the distance through which the applied force acts, and Sw is the distance the weight is lifted or through which the resistance is overcome, $W:P:Sp:Sw:W\times Sw \Rightarrow P\times Sp$, or the weight into the distance it is lifted

equals the force into the distance through which it is exerted.

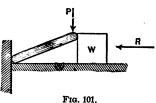
These equations are general for all classes of machines as well as for levers, it being understood that friction, which in actual machines increases

the resistance, is not at present considered.

The Bent Lever.—In the bent lever (see Fig. 91, page 416) the leverarm of the weight m is of instead of bf. The lever is in equilibrium when $n \times af = m \times cf$, but it is to be observed that the action of a bent lever may be very different from that of a straight lever. In the latter, so long as the force and the resistance act in lines parallel to each other, the ratio of the lever-arms remains constant, although the lever itself changes its inclina-tion with the horizontal. In the bent lever, however, this ratio changes: tion with the norizontal. In the bent ever, however, this ratio changes; thus, in the cut, if the arm bf is depressed to a horizontal direction that direction of af shortens, the latter becoming zero when the direction of af becomes vertical. As the arm af approaches the vertical, the weight m which may be lifted with a given force s is very great, but the distance through which it may be lifted is very small. In all cases the ratio of the weight m to the weight n is the inverse with of the beingental expensive of the properties of the temperature are arms. verse ratio of the horizontal projection of their respective lever-arms.

The Moving Strut (Fig. 101) is similar to the bent lever, except that

one of the arms is missing, and that the force and the resistance to be



overcome act at the same end of the single arm. The resistance in the case shown in the cut is not the case shown in the cut is not the weight W, but its resistance to being moved, R, which may be simply that due to its friction on the horizontal plane, or some other opposing force. When the angle between the strut and the horizontal plane changes, the ratio of the resistance to the applied force changes. When the angle becomes very small a moderate force will very small, a moderate force will overcome a very great resistance, which tends to become infinite as

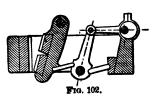
the angle approaches zero. If a= the angle, $P \times \cos a = R \times \sin a$. If a= 5 degrees, $\cos a = .9619$, $\sin a = .06716$, R=11.44 P.

The stone-crusher (Fig. 102) shows a practical example of the use of two

moving struts.

The Toggle-joint is an elbow or knee-joint consisting of two bars so connected that they may be brought into a straight line and made to produce great endwise pressure when a force is applied to bring them into this

position. It is a case of two moving struts placed end to end, the moving force being applied at their point of function, in a direction at right angles force being applied at their point of junction, in a direction at right subject to the direction of the resistance, the other end of one of the struts resting against a fixed abutment, and that of the other against the body to be moved. If a = the angle each strut makes with the straight line joining the points about which their outer ends rotate, the ratio of the resistance to the applied force is $R:P::\cos a:2\sin a$; $2R\sin a = P\cos a$. The



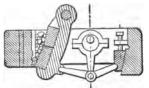


Fig. 103.

ratio varies when the angle varies, becoming infinite when the angle becomes zero.

The toggle-joint is used where great resistances are to be overcome

through very small distances, as in stone-crushers (Fig. 103).

The Inclined Plane, as a mechanical element, is supposed perfectly hard and smooth, unless friction be considered. It assists in sustaining a heavy body by its reaction. This reaction, however, being normal to the plane, cannot entirely counteract the weight of the body, which acts vertically downward Some other force must therefore

be made to act upon the body, in order that it may

be sustained.

If the sustaining force act parallel to the plane (Fig. 104), the force is to the weight as the height of the plane is to its length, measured on the incline. If the force act parallel to the base of the plane,

the power is to the weight as the height is to the base



If the force act at any other angle, let i = the angle of the plane with the horizon, and e = the angle of the direction of the applied force with the angle of the plane. $P:W:\sin i \cos e = W \sin i$. Problems of the inclined plane may be solved by the parallelogram of

Let the weight W be kept at rest on the incline by the force P, acting in the line bP', parallel to the plane. Draw the vertical line ba to represent the weight; also bb' perpendicular to the plane, and complete the parallelogram b'c. Then the vertical weight ba is the resultant of bb', the measure of gram b'c. Then the vertical weight ba is the resultant of bb', the measure of support given by the plane to the weight, and bc, the force of gravity tending to draw the weight down the plane. The force required to maintain the weight in equilible in sepresented by this force bc. Thus the force and the weight are in the ratio of bc to ba. Since the triangle of forces abc is similar to the triangle of the incline ABC, the latter may be substituted for the former in determining the relative magnitude of the forces, and

The Wedge is a pair of inclined planes united by their bases. In the application of pressure to the head or butt end of the wedge, to cause it to penetrate a resisting body, the applied force is to the resistance as the thickness of the wedge is to its length. Let t be the thickness, t the length, W the resistance, and P the applied force or pressure on the head of the

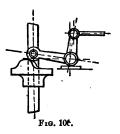
wedge. Then, friction neglected,
$$P:W::t:l; P=\frac{Wt}{t}; W=\frac{Pl}{t}$$
.

The Screw is an inclined plane wrapped around a cylinder in such a way that the height of the plane is parallel to the axis of the cylinder. If the screw is formed upon the internal surface of a hollow cylinder, it is usually called a nut. When force is applied to raise a weight or overcome a resistance by means of a screw and nut, either the screw or the nut may be fixed, the other being movable. The force is generally applied at the end of a wrench or lever-arm, or at the circumference of a wheel. If r= radius of the wheel or lever-arm, and p= pitch of the screw, or distance between threads, that is, the height of the inclined plane

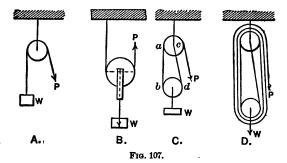
threads, that is, the height of the inclined plane for one revolution of the screw, P= the applied force, and W= the resistance overcome, then, neglecting resistance due to friction, $2\pi r \times P = Wp$; W=6.283 Fr+p. The ratio of P to W is thus independent of the diameter of the screw. In actual screws, much of the power transmitted is lost through friction.



The Cam is a revolving inclined plane. It may be either an inclined plane wrapped around a cylinder in such a way that the height of the plane is radial to the cylinder, such as the ordinary lifting-cam, used in stamp-mills



(Fig. 105), or it may be an inclined plane curved edgew'se, and rotating in a plane parallel to its base (Fig. 106). The relation of the weight to the applied force is calculated in the same manner as in the case of the screw.



Pulleys or Blocks.—P = force applied, or pull; W = weight lifted or resistance. In the simple pulley A (Fig. 107) the point P on the pulling rope descends the same amount that the weight is lifted, therefore P = W. In B and C the point P moves twice as far as the weight is lifted, therefore W = 3P. In B and C there is one movable block, and two plies of the rope engage with it. In D there are three sheaves in the movable block, each with two plies engaged, or six in all. Six plies of the rope are therefore shortened by the same amount that the weight is lifted, and the point P moves six times as far as the weight, consequently W = 6P. In general, the ratio of W to P is equal to the number of plies of the rope that are shortened, and also is equal to the number of plies that engage the lower block. If the lower block has 2 sheaves and the upper 3, the end of the rope is fastened to a hook in the top of the lower block, and then there are 5 plies shortened instead of 6, and W = 5P. If V = velocity of W, and v = velocity of P, then in all cases VW = vP, whatever the number of sheaves or their arrangement. If the hauling rope, at the pulling end, passes first around a sheave in the upper or stationary block, it makes no difference in what direction the rope is led from this block to the point at which the pull on the rope is applied; but if it first passes around the movable block, it is necessary that the pull be exerted in a direction parallel to the line of action of the resistance, or a line joining the centres of the two blocks, in order to obtain the maximum effect. If the rope pulls on the lower block at an angle, the block will be pulled out of the line drawn between the weight and the upper block, and the effective pull will be less than the actual pull

on the rope in the ratio of the cosine of the angle the pulling rope makes

en the rope in the ratio of the cosine of the angle the pulling rope makes with the vertical, or line of action of the resistance, to unity.

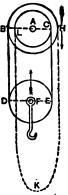
Differential Pulley. (Fig. 108.)—Two pulleys, B and C, of different radii, rotate as one piece about a fixed axis, A. An endless chain, BDECLKH, passes over both pulleys. The rims of the pulleys are shaped so as to hold the chain and prevent it from slipping. One of the bights or loops in which the chain hangs, DE, passes under and supports the running block F. The other loop or bight, HKL, hangs freely, and is called the hauling part. It is evident that the velocity of the hauling part is equal to that of the pitch-circle of the pulley B.

In order that the velocity-ratio may be exactly uniform.

pitch-circle of the pulley B. In order that the velocity-ratio may be exactly uniform, the radius of the sheave F should be an exact mean between the radii of B and C. Consider that the point B of the cord BD moves through an arc whose length =AB, during the same time the point C or the cord CE will move downward a distance =AC. The length of the bight or loop BDEC will be shortened by AB - AC, which will cause the pulley F to be raised half of this amount. If P = the pulling force on the cord HK, and W the weight lifted at F, then $P \times AB = W \times \frac{1}{2}(AB - AC)$.

To calculate the length of chain required for a differential pulley, take the following sum: Half the circumference of

pulley, take the following sum: Half the circumference of A + half the circumference of B + half the circumference of F + twice the greatest distance of F from A + theleast length of loop HKL. The last quantity is fixed



Mitte

Frg. 109.

least length of 100p 224.

according to convenience.

The Differential Windlass (Fig. 109) is identical in principle with the differential pulley, the difference in construction being that in the differential windlass the running block hangs in the bight of a rope whose two rounds and have their ends respectively. parts are wound round, and have their ends respec-tively made fast to two barrels of different radii, which rotate as one piece about the axis A. The differential windlass is little used in practice, because of the great length of rope which it requires.

The Differential Screw (Fig. 110) is a compound screw of different pitches, in which the threads wind the same way. N, and N, are the two nuts; S_1S_1 , the longer-pitched thread; S_1S_2 , the shorter-pitched thread: in the figure both these threads are left-handed. At each turn of the screw the nut N_2 advances relatively to N^2 through a distance equal to the difference of the pitch. The use of the differential screw is to combine the slowness

of advance due to a fine pitch with the strength of thread which can be

obtained by means of a coarse pitch only.

A Wheel and Axle, or Windlass, resembles two pulleys on one axis, having different diameters. If a weight be lifted by means of a rope wound

over the axle, the force being applied at the rim of the wheel, the action is like that of a lever of which the shorter arm is equal to the radius of the axle plus half the thickness of the rope, and the longer arm is equal to the radius of the wheel. A wheel and axle is therefore sometimes classed



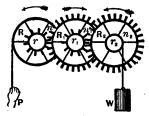
Fig. 110.

as a perpetual lever. If P = the applied force, D = diameter of the wheel, W = the weight lifted, and d the diameter of the axis + the diameter of

The rope, PD = Wd.

Toothed-wheel Gearing is a combination of two or more wheels and axies (rig. 11). If a series of wheels and pinions gear into each other, as in the cut, friction neglected, the weight lifted, or resistance over come, is to the force applied inversely as the distances through which they act in a given time. If R, R, R, be the radii of the successive wheels, measured to the pitch-line of the teeth, and r, r, r, the radii of the corresponding pinions, P the applied force, and W the weight lifted, $P \times$ $R \times R_1 \times R_2 = W \times r \times r_1 \times r_2$, or the applied force is to the weight as the product of the radii of the pinions is to the product of the radii of the wheels; or, as the product of the numbers expressing the teeth in each pinion is to the product of the numbers expressing the teeth in each

Endless Screw, or Worm-gear. (Fig. 112.)—This gear is commonly used to convert motion at high speed into motion at very slow



Frg. 111.



speed. When the handle P describes a complete circumference, the pitch-line of the cog-wheel moves through a distance equal to the pitch of the screw, and the weight W is lifted a distance equal to the pitch of the screw multiplied by the ratio of the diameter of the axle to the diameter of the pitch-circle of the wheel. The ratio of the applied force to the weight lifted is inversely as their velocities, friction not being considered; but the friction in the worm-gear is usually very great, amounting sometimes to three or four times the useful work done.

If v = the distance through which the force P acts in a given time, say 1 second, and V = distance the weight W is lifted in the same time, r = radius of the crank or wheel through which P acts, t = pitch of the screw, and also of the teeth on the cog-wheel, d = diameter of the axle.

and also of the teeth on the cog-wheel, d = diameter of the axle, 6.288 r D and D = diameter of the pitch-line of the cog-wheel, v = $\times V$: $V = v \times td + 6.283rd$. Pv = WV + friction.

STRESSES IN FRAMED STRUCTURES.

Framed structures in general consist of one or more triangles, for the reason that the triangle is the one polygonal form whose shape cannot be changed without distorting one of its sides. Problems in stresses of simple framed structures may generally be solved either by the application of the triangle, paralellogram, or polygon of forces, by the principle of the lever, or by the method of moments. We shall give a few examples, referring the student to the works of Burr, Dubois, Johnson, and others for more elaborated as the student of the works of Burr, Dubois, Johnson, and others for more elaborated as the student to the works of Burr, Dubois, Johnson, and others for more elaborated as the student to the works of Burr, Dubois, Johnson, and others for more elaborated as the student to the works of Burr, Dubois, Johnson, and others for more elaborated as the student to the works of Burr, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, Dubois, Johnson, and others for more elaborated as the student to the works of Burry, rate treatment of the subject.

rate treatment of the subject.

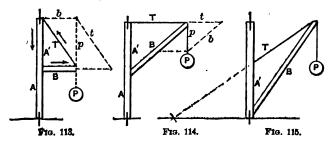
1. A Simple Crame. (Figs. 113 and 114.)—A is a fixed mast, B a brace or boom, T a tie, and P the load. Required the strains in B and T. The weight P, considered as acting at the end of the boom, is held in equilibrium by three forces: first, gravity acting downwards; second, the tension in T; and third, the thrust of B. Let the length of the line p represent the magnitude of the downward force exerted by the load, and draw a parallelogram with sides b is parallel, respectively, to B and T, such that p is the diagonal of the parallelogram. Then b and t are the components drawn to the same scale as p, p being the resultant. Then if the length p represents the load, t is the tension in the tie, and b is the compression in the brace.

Or, more simply, T, B, and that portion of the mast included between them or A' may represent a triangle of forces, and the forces are proportional to the length of the sides of the triangle; that is, if the height of the triangle A' = the load, then B = the compression in the brace, and T = the tension in the

tie; or if P = the load in pounds, the tension in $T = P \times \frac{T}{A}$, and the com-

pression in $B = P \times \frac{B}{A^{\prime}}$ **.** Also, if a = the angle the inclined member makes with the mast, the other member being horizontal, and the triangle being right-angled, then the length of the inclined member = height of the triangle \times secant a, and the strain in the inclined member = P secant a. Also, the strain in the horizontal member = P tan a.

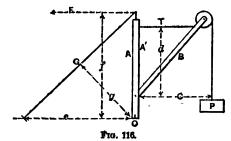
The solution by the triangle or parallelogram of forces, and the equations Tension in $T=P\times T/A'$, and Compression in $B=P\times B/A'$, hold true even if the triangle is not right-angled, as in Fig. 115; but the trigonometrical rela-



tions above given do not hold, except in the case of a right-angled triangle. It is evident that as A' decreases, the strain in both T and B increases, tending to become infinite as A' approaches zero. If the tie T is not attached to the mast, but is extended to the ground, as shown in the dotted line, the tension in it remains the same.

2. A Guyed Crame or Derrick. (Fig. 116.)—The strain in B is, as before, $P \times B/A'$, A' being that portion of the vertical included between B and T, wherever T may be attached to A. If, however, the tie T is attached to B beneath its extremity, there may be in addition a bending strain in B due to a tendency to turn about the point of attachment of T as a fulcrum.

The strain in T may be calculated by the principle of moments. The moment of P is Pc, that is, its weight × its perpendicular distance from the point of rotation of B on the mast. The moment of the strain on T is the product of the strain into the perpendicular distance from the line of its



direction to the same point of rotation of B, or Td. The strain in T therefore = Pc + d. As d decreases the strain on T increases, tending to infinity as d approaches zero.

ity as d approaches zero. The strain on the guy-rope is also calculated by the method of moments. The moment of the load about the bottom of the mast O is, as before, Pc. If the guy is horizontal the strain in it is F and its moment is Ff, and F = Fc + f. If it is inclined, the moment is the strain $G \times$ the perpendicular distance of the line of its direction from O, or Gg, and G = Fc + g.

The guy-rope having the least strain is the horizontal one F, and the str-

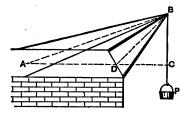


Fig. 117.

in G = the strain in $F \times$ the se cant of the angle between F and G. As G is made more nearly vertical g decreases, and the strain increases, becoming infinite when g = 0.

3. Shear-poles with Guys. (Fig. 117.)—First assume that the two masts act as one placed at BD, and the two guys as one at AB. Calculate the strain in BD and AB as in Fig. 115. Multiply half the strain in BD (or AB) by the secant of half the angle the two masts (or guys) make with each other to find the strain in each mast (or guy).

Two Diagonal Braces and a Tie-rod. (Fig. 118.)—Suppose the braces are used to sustain a single load P. Compressive stress on $AD = \frac{1}{2}P \times AD + AB$; on $CA = \frac{1}{2}P \times CA + AB$. This is true only if CB and BD are of equal length, in which case $\frac{1}{2}$ of P is supported by each abutment C and D. If they are unequal in length (Fig. 119), then, by the principle of the lever, find the re-

actions of the abutments R_1 and R_2 . If Pis the load applied at the point B on the lever CD, the fulcrum being D, then $R_1 \times CD = P \times BD$ and $R_2 \times CD = P \times BC$; $R_1 = P \times BD + CD$; $R_2 = P \times BC + CD$.

The strain on $AC = R_1 \times AC + AB$, and on $AD = R_2 \times AD + AB$.

The strain on the tie = $R_1 \times CB + AB$ $= R_2 \times BD + AB.$

Fro. 118.

When CB=BD, $R_1=R_2$. The strain on CB and BD is the same, whether the braces are of equal length or not, and is equal to $\frac{1}{2}F \times \frac{1}{2}CD + AB$. If the braces support a uniform load,

as a pair of rafters, the strains caused by such a load are equivalent to that caused by one half of the load applied at the centre. The horizontal thrust of the braces against each other at the

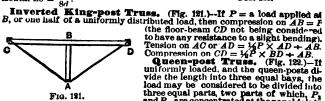
Frg. 119.

apex equals the tensile strain in the tie.

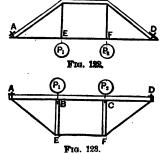
King-post Truss or Bridge. (Fig. 190.)—If the load is distributed over the whole length of the truss, the effect is the same as if half the load were placed at the centre, the other half being carried by the abutments. Let P = one half the load on the truss, then tension in the vertical tie AB = P. Compression in each of the inclined braces = $\frac{1}{2} \frac{1}{2} \frac{$ the tie. If W = the total load on one truss uniformly distributed, l = its length and d = its depth, then the tension on the hor-

Fra. 120.

izontal tie =



vide the length into three equal bays, the load may be considered to be divided into three equal parts, two parts of which, P_1 and P_2 , are concentrated at the panel joints and the remainder is equally divided between the abutments and supported by them directly. The two parts P_1 and P_2 only are considered to affect



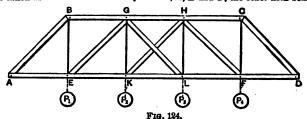
the members of the truss. Strain in the vertical ties BE and CF each equals P_1 or P_2 . Strain on AB and CD each $= P_1 \times CD + CF$. Strain on the tie AE or EF or $ED = P_1 \times CF$. Thrust on BC = tension

on EF For stability to resist heavy unequal loads the queen-post truss

should have diagonal braces from B to F and from C to E.

Inverted Queen-post
Truss. (Fig. 123.) — Compression
on EB and FC each = P_1 or P_2 .
Compression on AB or BC or CD = $P_1 \times AB + EB$. Tension on AE or $FB = P_1 \times AE + EB$. Tension on $FB = P_1 \times AE + EB$. Tension on $FB = P_1 \times AE + EB$. Tension on EF =compression on BC. For stability to resist unequal loads, ties should be run from C to E and from

Burr Truss of Five Panels. (Fig. 124.)—Four fifths of the load may be taken as concentrated at the points E, K, L and F, the other fifth being



supported directly by the two abutments. For the strains in BA and CD the truss may be considered as a queen-post truss, with the loads P_1 , P_2 concentrated at E and the loads P_3 , P_4 concentrated at E. Then, compressive strain on $AB = \{P_1 + P_2\} \times AB + BE$. The strain on CD is the same if the loads and panel lengths are equal. The tensile strain on BE or CF = P_1+P_2 . That portion of the truss between E and F may be considered as a smaller queen-post truss, supporting the loads P_2 , P_3 at E and E. The strain on EG or $HF=P_2\times EG+GE$. The diagonals GL and EG necessary of strain unless the truss is unequally loaded. The verticals GE and HL each

receive a tensile strain equal to P_2 or P_3 .

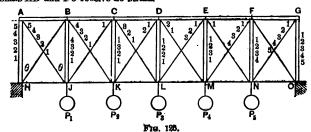
For the strain in the horizontal members: BG and CH receive a thrust For the strain in the horizontal members: BG and CH receive a thrust equal to the horizontal component of the thrust in AB or CD, $= \{P_1 + P_2\} \times AE + BE$. CH receives this thrust and also, in addition, a thrust equal to the horizontal component of the thrust in EG or HF, or, in all, $(P_1 + P_2 + P_3) \times AE + BE$. The tension in AE or FD equals the thrust in BG or HC, and the tension in EK. KL, and LF equals the thrust in GH.

Pract or Whipple Truss. (Fig. 125.)—In this truss the diagonals are ties, and the verticals are struts or columns.

Calculation by the method of distribution of strains: Canada first the

Calculation by the method of distribution of strains; Consider first the load P_1 . The truss having six bays or panels, 5/6 of the load is transmitted to the abutment H, and 1/6 to the abutment O, on the principle of the lever. As the five sixths must be transmitted through JA and AH, write on these members the figure 5. The one sixth is transmitted successively through $JA = \frac{1}{2}$ JC, CK, KD, DL, etc., passing alternately through a tie and a strut. Write on these members, up to the strut GO inclusive, the figure 1. Then consider the load P_2 , of which 4/8 goes to AH and 2/6 to GO. Write on KB, BJ, JA, and AH the figure 4, and on KD, DL, LE, etc., the figure 2. The load P_2 . transmit 3/6 in each direction; write 3 on each of the members through which this stress passes, and so on for all the loads, when the figures on the several members will appear as on the cut. Adding them up, we have the following totals:

Each of the figures in the first line is to be multiplied by $1/6P \times$ secant of angle HAJ, or $1/6P \times AJ + AH$, to obtain the tension, and each figure in the lower line is to be multiplied by 1/6P to obtain the compression. The diagonals HB and FO receive no strain.



It is common to build this truss with a diagonal strut at HB instead of the post HA and the diagonal AJ; in which case 5/6 of the load P is carried through JB and the strut BH, which latter then receives a strain = 15/6P \times secant of HBJ.

The strains in the upper and lower horizontal members or chords increase from the ends to the centre, as shown in the case of the Burr truss. AB receives a thrust equal to the horizontal component of the tension in AJ, or $15/6P \times \tan AJB$. BC receives the same thrust + the horizontal component of the tension in BK, and so on. The tension in the lower chord of each panel is the same as the thrust in the upper chord of the same panel. (For calculation of the chord strains by the method of moments, see below.)

lation of the chord strains by the method of moments, see below.)

The maximum thrust or tension is at the centre of the chords and is equal to $\frac{WL}{8D}$, in which W is the total load supported by the truss, L is the length, and D the depth. This is the formula for maximum stress in the chords

of a truss of any form whatever.

The above calculation is based on the assumption that all the loads P_1 , P_2 , etc., are equal. If they are unequal the value of each has to be taken into account in distributing the strains. Thus the tension in AJ, with unequal loads, instead of being $15 \times 1/6$ P secant θ would be see $\theta \times (5/6P_1 + 4/6$ $P_2 + 4/6$ $P_3 + 1/6$ $P_4 + 1/6$ P_4 .) Each panel load, P_1 etc., includes its fraction of the weight of the truss.

General Formula for Strains in Diagonals and Verticals.—Let n= total number of panels, x= number of any vertical considered from the nearest end, counting the end as 1, r= rolling load for each panel, P= total load for each panel,

Strain on verticals =
$$\frac{[(n-x)+(n-x)^2-(x-1)+(x-1)^2]P}{2n} + \frac{r(x-1)+(x-1)^2}{2n}$$

For a uniformly distributed load, leave out the last term,

$$[r(x-1)+(x-1)^2]+2n$$
.

Strain on principal diagonals = strain on verticals × secant 0, that is secant of the angle the diagonal makes with the vertical.

Strain on the counterbraces: The strain on the counterbrace in the first panel is 0, if the load is uniform. On the 2d, 3d, 4th, etc., it is P secant 6

$$\times \frac{1}{n}, \frac{1+2}{n}, \frac{1+2+8}{n}$$
, etc., P being the total load in one panel.

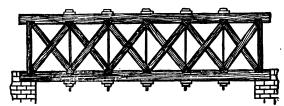
Strain in the Chords-Method of Moments.—Let the truss be uniformly loaded, the total load acting on it = W. Weight supported at each end, or reaction of the abutment = W/2. Length of the truss = L. Weight on a unit of length = W/L. Horizontal distance from the nearest abutment to the point (say M in Fig. 125) in the chord where the strain is to be determined = x. Horizontal strain at that point (tension on the lower chord, compression in the upper) = H. Depth of the truss = D. By the method of moments we take the difference of the moments, about the point M, of the reaction of the abutment and of the load between M and the abutments, and equate that difference with the moment of the resistance, or the strain in the horizontal chord, considered with reference to a point in the opposite chord, about which the truss would turn if the first chord were severed at M.

The moment of the reaction of the abutment is Wx/2. The moment of the load from the abutment to M is $W/Lx \times$ the distance of its centre of gravity from M, which is x/2, or moment = $Wx^2 + 2L$. Moment of the stress in the chord = $HD = \frac{Wx}{2} - \frac{Wx^2}{2L}$, whence $H = \frac{W}{2D} \left(x - \frac{x^2}{L}\right)$. If x = 0 or L;

H=0. If x=L/2, $H=\frac{2L}{8D}$, which is the horizontal strain at the middle

of the chords, as before given.

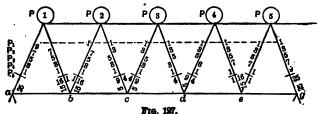
The Howe Truss, (Fig. 125.)—In the Howe truss the diagonals are struts, and the verticals are ties. The calculation of strains may be made



Frg. 126.

in the same method as described above for the Pratt truss.

The Warren Girder. (Fig. 127.)—In the Warren girder, or triangular truss, there are no vertical struts, and the diagonals may transmit either



tension or compression. The strains in the diagonals may be calculated by the method of distribution of strains as in the case of the rectangular truss. On the principle of the lever, the load P_1 being 1/10 of the length of the span from the line of the mearest support a, transmits 9/10 of its weight to a and 1/10 to g. Write 9 on the right hand of the strut 1a, to represent the compression, and 1 on the right hand of 1b, 2c, 3d, etc., to represent compression, and on the left hand of b^2 , c^2 , etc., to represent tension. The load P_1 transmits 7/10 of its weight to a and 3/10 to g. Write 7 on each member from 2 to a and 3 on each member from 2 to g, placing the figures representing compression on the right hand of the member, and those representing tension on the left. Proceed in the same manner with all the loads, then

sum up the figures on each side of each diagonal, and write the difference of each sum beneath, and on the side of the greater sum, to show whether the difference represents tension or compression. The results are as follows: Compression, 1a. 25; 2b. 15; 2c, 5: 3c, 5: 4c, 5; 4c, 15; 5g, 25. Tension, 1b, 15; 2c, 5: 4d, 5; 5e, 15. Each of these figures is to be multiplied by 1/10 of one of the loads as P_1 , and by the secant of the angle the diagonals make with a vertical line.

The strains in the horizontal chords may be determined by the method of

moments as in the case of rectangular trusses.

Roof-truss.—Solution by Method of Moments.—The calculation of strains in structures by the method of statical moments consists in taking a cross-section of the structure at a point where there are not more than three members (struts, braces, or chords).

To find the strain in either one of these members take the moment about the intersection of the other two as an axis of rotation. The sum of the moments of these members must be 0 if the structure is in equilibrium. But the moments of the two members that pass through the point of reference or axis are both 0, hence one equation containing one unknown quantity can be found for each cross-section.

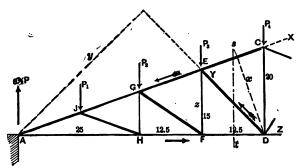


Fig. 128.

In the truss shown in Fig. 128 take a cross-section at ts, and determine the strain in the three members cut by it, viz., CE, ED, and DF. Let X = force exerted in direction CE, Y = force exerted in direction DE, Z = force ex-

erted in direction FD.

For X take its moment about the intersection of Y and Z at D = Xx. For FOR A take its moment about the intersection of X and Z at A = Yy. For Z take its moment about the intersection of X and X at A = Yy. For Z take its moment about the intersection of X and Y at E = Zz. Let z = 15, x = 18.6, y = 38.4, AD = 50, CD = 20 ft. Let P_1 , P_2 , P_3 , P_4 be equal loads, as shown, and $3\frac{1}{2}P$ the reaction of the abutment A.

The sum of all the moments taken about D or A or E will be 0 when the structure is at rest. Then $-Xx + 3.5P \times 50 - P_3 \times 12.5 - P_2 \times 25 - P_1 \times 25.5 - P_2$

87.5 = 0.

The +, signs are for moments in the direction of the hands of a watch or "clockwise" and - signs for the reverse direction or anti-clockwise. Since $P=P_1=P_2=P_3=P_3$, -18.6X+175P-75P=0; -18.6X=-100P; X=100P+18.6=5.376P.

 $-Yy + P_3 \times 37.5 + P_3 \times 25 + P_3 \times 12.5 = 0$; 38.4Y = 75P; Y = 75P + 88.4 = 1.958P.

 $-Zz + 8.5P \times 87.5 - P_1 \times 25 - P_2 \times 12.5 - P_3 \times 0 = 0$; 15Z = 93.75P; Z = 93.75P

o.207. In the same manner the forces exerted in the other members have been found as follows: EG=6.73P; GJ=8.07P; JA=9.42P; JH=1.35P; GF=1.59P; AH=8.75P; HF=7.50P.

The Fink Hoof-truss. (Fig. 129.)—An analysis by Prof. P. H. Philbrick (Van N. Mag., Aug. 1880) gives the following results:

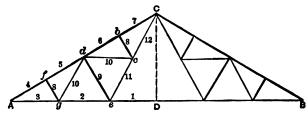


Fig. 129.

W= total load on roof; N= No. of panels on both rafters; W/N=P= load at each joint b,d,f, etc.; V= reaction at $A=\frac{1}{2}W=\frac{1}{2}NP=4P;$ AD=S; AC=L; CD=D; $t_1,t_2,t_3=$ tension on De,eg,gA, respectively; $e_1,e_2,e_3,e_4=$ compression on Cb,bd,df, and fA.

Strains in 1, or $De = t_1 = 2PS + D$; 7, or $De = t_1 = 2PS + D$; 8, " $De = t_2 = 3PS + D$; 8, " $De = t_3 = 7/2PS + D$; 9, " $De = t_3 = 7/2PS + D$; 9, " $De = t_3 = 7/2PS + D$; 10, " $Ce = t_3 = 7/2PS + D$; 10, " $Ce = t_3 = 7/2PS + D$; 11, " $Ce = t_3 = 7/2PS + D$; 11, " $Ce = t_3 = 7/2PS + D$; 12, " $Ce = t_3 = 3/2PS + D$.

Example.—Given a Fink roof-truss of span 64 ft., depth 16 ft., with four panels on each side, as in the cut; total load 32 tons, or 4 tons each at the points f, d, b, C, etc. (and 2 tons each at A and B, which transmit no strain to the truss members). Here W=32 tons, P=4 tons, S=32 ft., D=16 ft., $L=4\sqrt{S^2+D^2}=2.236\times D$. L+D=2.236, D+L=.4472, S+D=2.246, S+D=3.246. The strains on the numbered members then are as follows:

The Economical Angle.—A structure of triangular form, Fig. 129a, is supported at α and b. It sustains any load L, the elements cc being in compression and t in tension. Required the angle θ so that the total weight of the structure shall be a minimum. F. R. Honey (Sci. Am. Supp., Jan. 17, 1895) gives a solu-

F. R. Honey (Sci. Am. Supp., Jan. 17, 1895) gives a solution of this problem, with the result $\tan \theta = \sqrt{\frac{C+T}{T}}$, in which C and T represent the crushing and the ten-

sile strength respectively of the material employed. It is applicable to any material. For C=T, $\theta=543/2$. Fig. 129a. For C=0.4T (yellow pine), $\theta=493/2$. For C=0.8T (soft steel), $\theta=581/2$. For C=6T (cast iron), $\theta=691/2$.

θ

HEAT.

THERMOMETERS.

The Fahrenheit thermometer is generally used in English-speaking countries, and the Centigrade, or Celsius thermometer, in countries that use the metric system. In many scientific treatises in English, however, the Centigrade temperatures are also used, either with or without their Fahrenheit equivalents. The Réaumur thermometer is used to some extent on the Continent of Europe.

In the Fahrenheit thermometer the freezing-point of water is taken at 32°, and the holling-point of water at mean atmospheric pressure at the sea-level, 14.7 lbs. per sq. in., is taken at 212°, the distance between these two points being divided into 180°. In the Centigrade and Reagmur thermometers the freezing-point is taken at 0°. The boiling-point is 100° in the Centigrade scale, and 80° in the Réaumur.

= 5/9 deg. Centigrade = 4/9 deg. Réaumur. = 9/5 deg. Fahrenheit = 4/5 deg. Réaumur. = 9/4 deg. Fahrenheit = 5/4 deg. Centigrade. 1 Fahrenheit degree Centigrade degree

1 Réaumur degree = 9/4 deg. Fahrenheit = 5/4 deg. Cen Temperature Fahrenheit = 9/5 × temp. C. + 32° = 9/4 R. + 82°. Temperature Centigrade = 5/9 (temp. F. - 32°) = 5/4 R.

Temperature Réaumur = 4/5 temp. C. = 4/9 (F. - 32°).

Mercurial Thermometer. (Rankine, S. E., p. 234.)—The rate of expansion of mercury with rise of temperature increases as the temperature becomes higher; from which it follows, that if a thermometer showing the dilatation of mercury simply were made to agree with an air thermometer at 32° and 212°, the mercurial thermometer would show lower temperatures than the air thermometer between those standard points, and higher temperatures beyond them.

For example, according to Regnault, when the air thermometer marked 350°C. (= 662°F.), the mercurial thermometer would mark 502.16°C. (= 688.89°F.), the error of the latter being in excess 12.16°C. (= 21.89°F.).

Actual mercurial thermometers indicate intervals of temperature propor-

tional to the difference between the expansion of mercury and that of glass. The inequalities in the rate of expansion of the glass (which are very different for different kinds of glass) correct, to a greater or less extent, the errors arising from the inequalities in the rate of expansion of the mercury.

For practical purposes connected with heat engines, the mercurial thermometer made of common glass may be considered as sensibly coinciding with the air-thermometer at all temperatures not exceeding 500° F.

PYROMETRY.

Principles Used in Various Pyrometers.—Contraction of clay by heat, as in the Wedgwood pyrometer used by potters. Not accurate, as the contraction varies with the quality of the cla

Expansion of air, as in the air-thermometers, Wiborgh's pyrometer. Uchling and Steinbart's pyrometer, etc.

Specific heat of solids, as in the copper-ball, platinum-ball, and fire-clay

pyrometers. Relative expansion of two metals or other substances, as copper and fron.

as in Brown's and Bulkley's pyrometers, etc.

Melting-points of metals, or other substances, as in approximate determinations of temperature by melting pieces of zinc, lead, etc.

Measurement of strength of a thermo-electric current produced by heat-

ing the junction of two metals, as in Le Chatelier's pyrometer. Changes in electric resistance of platinum, as in the Siemens pyrometer.

Mixture of hot and com air, as in Hobson's hot-blast pyrometer. Time required to heat a weighed quantity of water enclosed in a vessel.

as in the water pyrometer.

Thermometer for Temperatures up to 950° F.—Mercury with compressed nitrogen in the tube above the mercury. Made by Queen Co., Philadelphia.

TEMPERATURES, CENTIGRADE AND FAHRENHEIT.

PARRENIE II.													
C.	F.	C.	F.	C.	F.	C.	F.	C.	F.	C.	F.	Ċ	F.
-40	-4 0.	26	78.8	92	197.6	158	316.4	224	485.2	290	554		1742
-89	-88.2	27	80.6	93	199.4	159	818.2	225	487.	300	572		1760
-38 -37	-86.4 -84 6	26 29	82.4 84.2	94 95	201.2 208.	160	820.	226 227	488.8 440.6	310 320	590		1778 1796
-36	-82.8	30	86.	96	204.8	161 162	821.8 823.6	228	442.4	330	608 626		1814
- 35	-81.	81	87.8	97	206.6	168	825.4	229	444.2	340	644	1000	
-34	-29.2	82	89.6	98	208.4	164	327.2	230	446.	350	662	1010	1850
- 33	-27.4	83	91.4	99	210.2	165	329.	231	447.8	360	680		1868
- 32	-25.6	84	98.2	100	212.	166	830.8	222	449.6	370	698	1030	
81 30	-23.8 -22.	35 36	95. 96.8	101 102	218.8 215.6	167 168	332.6 834.4	233 234	451.4 453.2	380 390	716 734	1040 1050	
-29	-20.2	87	98.6	103	217.4	169	336.2	235	455.	400	752	1060	
-28	-18.4	88	100.4	104	219.2	170	338.	236	456.8	410	770	1070	
-27	-16.6	39	102.2	105	221.	171	339.8	237	458.6	420	788	1080	
-26	-14.8	40	104.	106	222.8	172	841.6	238	460.4	430	806	1090	1994
-25	-13.	41	105.8	107	224.6	173	843.4	539	462.8	440	824	1100	2012
24 28	-11.2	42 48	107.6 109.4	108 109	226.4 228.2	174	845.8	240 241	464. 465.8	450 460	842 860	1110	2030
-23	-9.4 -7.6	44	111.2	110	230.	175 176	847. 848.8	242	467.6	470	878	1120	2048 2066
-21	- 5.8	45	113.	iii	231.8	177	350.6	243	469.4	480	896		9084
90	- 4.	46	114.8	112	233.6	178	852.4	244	471.2	490	914		2102
19	- 2.2	47	116.6	118	235.4	179	854.2	245	478.	500	885	1160	2120
-18	- 0.4	48	118.4	114	237.2	180	856.	246	474.8	510	950		2188
-17	+ 1.4	49	120.2	115	239.	181	857.8	247	476.6	520	968		2156
-16 -15	8.2 5.	50 51	192. 193.8	116 117	240.8 242.6	182 183	359.6 861.4	248 249	478.4 480.8	530 540	986 1004		2174 2192
-14	6.8	52	125.6	118	244.4	184	863.2	250	482.	550			2210
-18	8.6	58	187.4	119	246.2	185	865.	251	483.8		1040		2228
-12	10.4	54	129.2	120	248.	186	366.8	252	485.6	570	1058		2246
-11	12.2	55	181.	121	249.8	187	368.6	253	487.4	580	1076		2264
~10	14.	56	182.8	122	251.6	188	870.4	254	489.2	590	1094	1250	
- 9 - 8	15.8 17.6	57 58	184.6 186.4	128 124	253.4 255.2	189 190	872.8 874.	255 256	491. 492.8		1112		2800 2318
_ ?	19.4	50	188.2	125	257.	191	375.8	257	494.6		1148	1280	2336
_ 6	21.2	60	140.	126	258.8	192	377.6	258	496.4		1166		2354
- 5	23.	61	141.8	127	260.6	193	379.4	259	498.2	640	1184	1800	2872
4	24.8	62	143.6	128	262.4	194	381.2	260	500.		1202	1310	2390
- 8	26.6	68 64	145.4 147.2	129 130	264.2 266.	195 196	888.	261	501.8 508.6	660	1220 1238	1820	2408
- 2 - 1	28.4 80.2	65	149.	181	267.8	197	384.8 386.6	262 268	505.4	850	1256	1830	2426 2444
- ô	82.	66	150.8	132	269.6	198	888.4	264	507.2	690	1274		2462
+1	83.8	67	152.6	138	271.4	199	890.8	265	509.		1292		2480
. 8	85.6	68	154.4	134	273.2	200	392.	266	510.8		1310		2498
8	87.4	09	156.2	185	275.	201	893.8	267	512.6	720	1328		2516
4 5	89.2	70 71	158. 159.8	136 187	276.8 278.6	202 208	395.6 397.4	268 269	514.4 516.2		1346 1364	1890	2584 2552
6	49.8	72	161.6	188	280.4	204	399.2	270	518.		1382		2570
ž	44.6	78	168.4	139	282.2	205	401.	271	519.8		1400	1420	2588
8	46.4	74	165.2	140	284.	206	402.8	272	521.6	770	1418	1430	2606
.9	48.8	75	167.	141	285.8	207	404.6	278	528.4	780	1486 1454		2624
10	50. 51.8	76 77	168.8 170.6	142 148	287.6 289.4	208 209	406.4	274 275	525.2 527.	330	1454 1472		2642 \ 2660
11 12	58.6	78	178.4	140 144	291.2	210	410.	276	528.8		1490		2678
îŝ	55.4	79	174.2	145	293.	211	411.8	277	530.6		1508		2696
14	57.2	80	176.	146	294.8	212	418.6	278	532.4	880	1526	1490	2714
15	59.	81	177.8	147	296.6	218	415.4	279	534.2		1544		2782
16	60.8	83 83	179.6	148	298.4	214	417.2	280	586.		1562		2750
17 18	64.4	83 84	181.4 183.2	149 150	800.2 802.	215 216	419. 420.8	281 282	537.8 539.6		1580 1598		2768 278 6
19	66.2	85	188.	151	803.8	217	422.6	288	541.4	880	1616		2804
90	68.	86	186.8	152	805.6	218	424.4	284	543.2	890	1684	1550	2822
21	69.8	87	188.6	158	807.4	219	426.2	285	545.	900	1652	1600	2912
22	71.6	188	190.4	154	809.2	220	428.	286	546.8		1670	1650	8002
28 24	78.4	80	199.2 194.	155	811. 812.8	221 222	429.8 431.6	287 258	548.6 550.4	920 930	16 8 8 1706	1700	8092
25	75.8 77.	91	195.8	156 157	814.6	228 228	483.4	255 289	552.2	940		1800	\$162 \$162
-	_ '''	<u></u>	100,0	101	OLT.U		100.4	A00		200	2142	1000	1

F.	C.	F.	C.	F.	C.	F.	C.	F.	C.	F.	C.	F.	C.
-40	_40.	26	- 3.3	92	33.3	158	70.	224	106.7	290	143.3		182,2
-39	-39.4	27	- 2.8 - 2.2 - 1.7 - 1.1 - 0.6	93	33.9	159	70.6	225	107.2 107.8	291	143.9		187.8
-38	-38.9	28	-22	94	34.4	160	71.1	226	107.8	292	144.4		193,3
$-37 \\ -36$	-38.3	29	- 1.7	25	35.	161 162	71.7	227 228	108.3	293	145.		198.9
-35	-37.8	30 31	- 1.1	96 97	35.6 36.1	163	72.2 72.8	228	108.9 109.4	294 295	145.6 146.1		204.4
-34	$-37.2 \\ -36.7$	32	- 0.0	98	36.7	164	73.3	230	110.	295	146.7		215.6
-33	-36.1	83	+ 0.6	99	87.2	165	73.9	231	110.6	297	147.2		221.1
-32	-35.6	34	1.1	100	37.8	166	74.4	232	111.1	298	147.8		226.7
-31	-35.	85	1.7	101	88.3	167	75.	233	111.7	299	148.3		232.2
-30	-34.4	36	2.2	102	38.9	168	75.6	234	112.2	300	148.9		237.8
-29	-33.9	37	2.8	103	89.4	169	76.1	235	112.8	801	149.4	470	243.3
-28	- 33.3	38	8.8	104	40.	170	76.7	236	113.8	30.5	150.		248.9
$-27 \\ -26$	$-32.8 \\ -32.2$	39	8.9	105	40.6	171	77.2	237	113.9	303	150.6		254.4
-25		40	5.	106 107	41.1	172 178	78.3	238 239	114.4	804 805	151.1 151.7		260. 265.6
-24	$-31.7 \\ -31.1$	42	5.6	108	41.7	174	78.9	240	115.6	306	152.2		271.1
-23	-30.6	43	6.1	109	42.8	175		241	116.1	307	152.8		276.7
-22	-30.	44	6.7	110	43.3	176	80.	242	116.7	308	153.8	540	282,2
-21	-29.4	45	7.0	111	43.9	177	80.6	243	1179	809	153.9	550	287.8
-20	-28.9	46	7.8	112	44.4	178	81.1 81.7 82.2	244	117.8 118.8	310	154.4	560	293,3
-19	-28.3	47	8.3	113	45.	179	81.7	245	118.8	311	155.		298.9
-18	-27.8	48	8.9	114	45.6	180	82.2	246	118.9	812	155.6		304.4
-17	-27.2	49	9.4	115	46.1	181	82.8	247	119.4	813	156.1		310.
-16	-26.7	50	10.	116	46.7	182	83.3	248	120.	314	156.7		315.6
-15	-26.1	51	10.6	117	47.2	183	83.9	249 250	120.6	315	157.2		321.1
-14 -13	-25.6 $-25.$	52 53	11.1	118 119	47.8 48.3	184 185	84.4 85.	251	121.1 121.7	316 317	157.8 158.8		326.7 332.2
-12	-24.4	54	12.2	120	48.9	186	85.6	252	122.2	818	158.9		337.8
-11	-23.9	55	12.8	121	49.4	187	86.1	253	122.8	819	159.4		343,3
-10	-23.3	56	13.3	122	50.	188	86.7	254	123.3	320	160.		348.9
- 9	-22.8	57	13.9	123	50.6	189	87.2	255	123.9	821	160.6	670	354.4
- 8	-22.2	58	14.4	124	51.1	190	87.8	256	124.4	322	161.1	680	360.
- 7	21.7	59	15.	125	51.7	191	88.3	257	125.	323	161.7		365.6
- 6	-21.1	60	15.6	126	52.2 52.8	192	88.9	258	125.6	324	162,2		371.1
- 5	-20.6	61	16.1	127	52.8	198	89.4	259	126.1	825	162.8	710	376.7
- 4 - 3	-20. -19.4	62 63	16.7	128 129	53.3 53.9	194 195	90. 90.6	260 261	126.7 127.2	326 327	163.8 163.9	720	382.2 387.8
- 2	-18.9	64	17.2 17.8 18.3	130	54.4	196	01 1	262	197 8	328	164.4		393.3
- ĩ	-18 3	65	18.3	131	55.	197	91.7 92.2 92.8	263	127.8 128.8 128.9	829	165.	750	398.9
ō	-17.8	66	18.9	132	55.6	198	92.2	264	128.9	330	165.6		404.4
+1	-17.2	67	19 4	133	56.1	199	92.8	265	129.4	831	166.1		410.
2	-16.7	68	20.	134	56.7	200	93.3	266	130.	332	166.7		415.6
3	-16.1	69	20.6	135	57.2	201	93.9	267	130.6	333	167.2		421.1
4	-15.6	70	21.1	136	57.8	202	94.4	268	131.1	334	167.8		426,7
5	-15.	71	21.7 22.2	137 138	58.3	203 204	95. 95.6	269 270	131.7 132.2	835 836	168.3 168.9		432.2 437.8
6	-14.4 -13.9	72 73	22.8	139	59.4	205	96.1	271	182.8	337	169.4		443.3
8	-13.3	74	23.3	140	60.	206	96.7	272	133.8	838	170.		448.9
9	-12.8	75	23.9	141	60.6	207	97.2	273	133,9	839	170.6	850	454.4
10	-12.2	76	24.4	142	61.1	208	97.2 97.8	274	134.4	340	171.1	860	460.
11	-11.7	77	25.	143	61.7	209	98.3	275	135.	841	171.7	870	465.6
12	-11.1	78	25.6	144	62.2	210	98.9	276	135.6	842	172.2		471.1
13	-10.6	79	26.1	145	62.8	211	99.4	277	136.1	848	172.8		476.7
14	-10.	80	26.7	146	63.3	212	100.	278	136.7	844	173.3		482.2
15	- 9.4	81	27.2	147	63.9	213	100.6	279 280	137.2	845 846	178.9		487.8
16 17	- 8.9 - 8.3	82 83	27.8 28.3	148 149	64.4	214	101.7	280	137.8 138.3	347	174.4 175.		493.3 498.9
18	- 7.8	84	28.9	150	65.6	216	102.9	282	138.9	348	175.6		504.4
19	- 7.2	85	29.4	151	66.1	217	102.2 102.8	283	139.4	849	176.1		510.
20	- 6.7	86	30.	152	66.7	218	103.3	284	140.	350	176.7		515.6
21	-6.7 -6.1	87	80.6	153	67.2	219	103.9	285	140.6	851	177.2	970	521.1
22	- 5.6	88	81.1	154	67.2 67.8	220	104.4	286	141.1	852	177.8	980	526.7
23	- 5.	89	81.7	155	68.3	221	105.	287	141.7	353	178.8		532,2
24	- 4.4	90	82.2	156	68.9	222	105.6	288	142.2	354	178.9		537.8
25	- 3.9	91	82.8	157	69.4	223	106.1	289	142.8	355	179.4	1010	548.3

Platinum or Copper Ball Pyrometer.—A weighed piece of platinum, copper, or iron is allowed to remain in the furnace or heated chamber till it has attained the temperature of its surroundings. It is then suddenly taken out and dropped into a vessel containing water of a known weight and temperature. The water is stirred rapidly and its maximum temperature taken. Let W = weight of the water, ut the weight of the ball t = the original and T the final heat of the water, and S the specific heat of the metal; then the temperature of fire may be found from the formula

$$x = \frac{W(T-t)}{wS} + T.$$

The mean specific heat of platinum between 32° and 446° F. is .03333 or 1/30 that of water, and it increases with the temperature about .000305 for each 100° F. For a fuller description, by J. C. Hoadley, see Trans. A. M. E., vi. 702. Compare also Henry M. Howe, Trans. A. I. M. E., xviii. 728.

For accuracy corrections are required for variations in the specific heat of the water and of the metal at different temperatures, for loss of heat by radiation from the metal during the transfer from the furnace to the water, and from the appearans during the heating of the water; also for the heat-absorbing capacity of the vessel containing the water.

Fire-clay or fire-brick may be used instead of the metal ball.

Le Chatelier's Thermo-electric Pyrometer.—For a very full description see paper by Joseph Struthers, School of Mines Quarterly, vol. xii, 1891; also, paper read by Prof. Roberts-Austen before the Iron and Steel Institute, May 7, 1891.

The principle upon which this pyrometer is constructed is the measurement of a current of electricity produced by heating a couple composed of two wires, one platinum and the other platinum with 10% rhodium—the cur-rent produced being measured by a galvanometer.
The composition of the gas which surrounds the couple has no influence

on the indications.

When temperatures above 2500° F. are to be studied, the wires must have an isolating support and must be of good length, so that all parts of a furnace can be reached.

For a Siemens furnace, about 1114 feet is the general length. The wires are supported in an iron tube, 14 inch interior diameter and held in place by a cylinder of refractory clay having two holes bored through, in which the wires are placed. The shortness of time (five seconds) allows the temperature to be taken without deteriorating the tube.

Tests made by this pyrometer in measuring furnace temperatures under a great variety of conditions show that the readings of the scale uncorrected are always within 45° F. of the correct temperature, and in the majority of industrial measurements this is sufficiently accurate. Le Chatelier's pyrometer is sold by Queen & Co., of Philadelphia.

Graduation of Le Chatelier's Pyrometer.—W. C. Roberts-Austen in his Researches on the Properties of Alloys, Proc. Inst. M. E. 1892, says: The electromotive force produced by heating the thermo-junction of one of eight temperature is measured by the movement of the spot of light.

to any given temperature is measured by the movement of the spot of light on the scale graduated in millimetres. A formula for converting the divion the scale graduated in minimeters. A formula for converting the divisions of the scale into thermometric degrees is given by M. Le Chatelier; but it is better to calibrate the scale by heating the thermo-junction to temperatures which have been very carefully determined by the aid of the air-thermometer, and then to plot the curve from the data so obtained. Many fusion and boiling-points have been established by concurrent evidence of various kinds, and are now very generally accepted. The following table contains certain of these:

Deg. F.	Deg. 0).	Deg. F.	Deg. (D.
212	100	Water boils.	1783	945	Silver melts.
618	826	Lead melts.	1859 .	1015	Potassium sul-
676	358	Mercury boils.	ł		phate melts.
779		Zinc melts.	1918	1045	Gold melts.
838	448	Sulphur boils.	1929	1054	Copper melts.
1157	625	Aluminum melts.	2732	1500	Palladium melts.
1229	665	Selenium boils.	3227	1775	Platinum melts.

The Temperatures Developed in Industrial Furnaces.— M. Le Chatelier states that by means of his pyrometer he has discovered that the temperatures which occur in melting steel and in other industrial operations have been hitherto overestimated.

M. Le Chatelier finds the melting heat of white dast iron 1183° (2075° F.), and that of gray cast iron 1220° (22:26° F.). Mild steel melts at 1475° (2657° F.), semi-mild at 1455° (2657° F.), and hard steel at 1410° (2570° F.). The furnace for hard porcelain at the end of the baking has a heat of 1570° (2468° F.). The heat of a normal incandescent lamp is 1800° (8272° F.), but it may be pushed to beyond 10100° (8312° F.).

Prof. Roberts-Austen (Recent Advances in Pyrometry, Trans. A. I. M. E., Chicago Meeting, 1839) gives an excellent description of modern forms of pyrometers. The following are some of his temperature determinations.

GOLD-MELTING, ROYAL MINT.	
Degrees.	Degrees
Centigrade.	Fahr.
Temperature of standard alloy, pouring into moulds 1180 Temperature of standard alloy, pouring into moulds (on	2156
a previous occasion, by thermo-couple) 1147	2097
Annealing blanks for coinage, temperature of chamber 890	1634
SILVER-MELTING, ROYAL MINT.	
Temperature of standard alloy, pouring into mould 980	1796
TEN-TON OPEN-HEARTH FURNACE, WOOLWICH ARSENAL.	
Temperature of steel, 0.8g carbon, pouring into ladle 1645	2993
Steel, 0.3% carbon, pouring into large mould 1580	2876
Reheating furnace, interior	1706
Cupola furnace, No. 2 cast iron, pouring into ladle 1600	2912

The following determinations have been effected by M. Le Chatelier: BESSEMER PROCESS.

Six-ton Converter.		•
	Degrees.	Degrees
	Centigrade	
A. Bath of slag	1580	9876
B. Metal in ladle	1640	2984
C. Metal in ingot mould	1580	2876
D. Ingot in reheating furnace	1200	2192
E. Ingot under the hammer	1080	1976
Open-hearth Furnace (Siemens)	•	
Semi-Mild Steel.		
A. Fuel gas near gas generator		1328
B. Fuel gas entering into bottom of regenerator chamb		752
C. Fuel gas issuing from regenerator chamber		2192
Air issuing from regenerator chamber		1889
Chimney gases. Furnace in perfect condition	300	590
End of the melting of pig charge	1420	2588
Completion of conversion	1500	278 9
Molten steel. In the ladie-Commencement of casting	1580	2876
End of casting	1490	2714
In the moulds	1520	9768
For very mild (soft) steel the temperatures are higher	by 50° C.	

SIEMENS CRUCIBLE OR POT FURNACE. 1600° C., 2912° F.

ROTARY PUDDLING FURNACE.

Furnage	Degrees C. 1840-1230	Degrees F 2444-2346
Furnace	1830	2426
Blast-furnace (Gray-Bessemer F		
Opening in face of tuyere	1930	8506
Molten metal—Commencement of fusion		8506 25 52
End, or prior to tapping	1570	2858
HOFFMAN RED-BRICK KILM.		
Burning temperatures	1100	2012

Hobsen's Hot-blast Pyrometer consists of a brass chamber having three hollow arms and a handle. The hot blast enters one of the arms and induces a current of atmospheric air to flow into the second arm. The two currents mix in the chamber and flow out through the third arm, in which the temperature of the mixture is taken by a mercury thermometer. The openings in the arms are adjusted so that the proportion of hot blast to the atmospheric air remains the same.

blast to the atmospheric air remains the same.

The Wiborgh Air-pyrometer. (E. Trotz, Trans, A.I.M.E. 1892.)—The inventor using the expansion-coefficient of air, as determined by Gay-Lussac, Dulon, Rudberg, and Regnault, bases his construction on the following theory: If an air-volume, V, enclosed in a porcelain globe and connected through a capillary pipe with the outside air, be heated to the temperature T (which is to be determined) and thereupon the connection be discontinued, and there be then forced into the globe containing V another volume of air V' of known temperature t, which was previously under atmospheric pressure H, the additional pressure h, due to the addition of the air-volume V' to the air-volume V, can be measured by a manometer. But this pressure is of course a function of the temperature T. Before the introduction of V', we have the two separate air-volumes, V at the temperature T and V' at the temperature t, both under the atmospheric pressure H. After the forcing in of V' into the globe, we have, on the contrary, only the volume V of the temperature T, but under the pressure H + h.

H+h.

The Wiborgh Air-pyrometer is adapted for use at blast-furnaces, smelting-the wiborgh Air-pyrometer is adapted for use at blast-furnaces, smelting of the second state of the second se works, hardening and tempering furnaces, etc., where determinations of temperature from 0° to 2400° F. are required.

Seger's Fire-clay Pyrometer. (H. M. Howe, Eng. and Mining Jour., June 7, 1890.)—Professor Seger uses a series of slender triangular fire-clay pyramids, about 3 inches high and % inch wide at the base, and each a little less fusible than the next; these he calls "normal pyramids" ("normal-kegel"). When the series is placed in a furnace whose temperature is gradually raised, one after another will bend over as its range of plasticity is reached; and the temperature at which it has bent, or "wept," so far that its apex touches the hearth of the furnace or other level surface on which it is standing, is selected as a point on Seger's scale. These points may be accurately determined by some absolute method, or they may merely serve to give comparative results. Unfortunately, these gyramids afford no indications when the temperature is stationary or falling.

Mesuré and Nouel's Pyrometric Telescope. (*Ibid.*)—Mesuré and Nouel's pyrometric telescope gives us an immediate determination of the temperature of incandescent bodies, and is therefore much better adapted to cases where a great number of observations are to be made, and at short intervals, than Seger's. Such cases arise in the careful heating of steel. The little telescope, carried in the pocket or hung from the neck, can be used by foreman or heater at any moment.

It is based on the fact that a plate of quartz, cut at right angles to the axis, rotates the plane of polarization of polarized light to a degree nearly inversely proportional to the square of the length of the waves; and, further, on the fact that while a body at dull redness merely emits red light, as the temperature rises, the orange, yellow, green, and blue waves

successively appear.

If, now, such a plate of quartz is placed between two Nicol prisms at right angles, "a ray of monochromatic light which passes the first, or polarizer, and is watched through the second, or analyzer, is not extinguished as it was before interposing the quartz. Part of the light passes the analyzer, and, to again extinguish it, we must turn one of the Nicols a certain angle," depending on the length of the waves of light, and hence on the temperature of the incandescent object which emits this light. Hence the angle through which we must turn the analyzer to extinguish the light

is a measure of the temperature of the object observed.

For illustrated descriptions of different kinds of pyrometers see circular issued by Queen & Co., Philadelphia.

The Uchling and Steinbart Pyrometer. (For illustrated description see Engineering, Aug. 24, 1894.)—The action of the pyrometer is based on a principle which involves the law of the flow of gas through minuted and the contract of the following manner. It is closed the an absorbable minuted. apertures in the following manner: If a closed tube or chamber be supplied with a minute inlet and a minute outlet aperture and air be caused by a constant suction to flow in through one and out through the other of these apertures, the tension in the chamber between the apertures will vary with 454

the difference of temperature between the inflowing and outflowing air. If the inflowing air be made to vary with the temperature to be measured, and the outflowing air be kept at a certain constant temperature, then the tension in the space or chamber between the two apertures will be an exact measure of the temperature of the inflowing air, and hence of the temperature to be measured.

In operation it is necessary that the air be sucked into it through the first minute aperture at the temperature to be measured, through the second aperture at a lower but constant temperature, and that the suction be of a constant tension. The first aperture is therefore located in the end of a platinum tube in the bulb of a porcelain tube over which the hot blast sweeps, or inserted into the pipe or chamber containing the gas whose temperature is to be ascertained.

The second aperture is located in a coupling, surrounded by boiling water, and the suction is obtained by an aspirator and regulated by a column of water of constant height.

The tension in the chamber between the apertures is indicated by a

manometer.

The Air-thermometer. (Prof. R. C. Carpenter, Eng'g News, Jan. 5, 1893.)—Air is a perfect thermometric substance, and if a given mass of air 1893.)—Air is a perfect thermometric substance, and if a given mass of an be considered, the product of its pressure and volume divided by its absolute temperature is in every case constant. If the volume of air remain constant, the temperature will vary with the pressure; if the pressure remain constant the temperature will vary with the volume. As the former condition is more easily attained air-thermometers are usually constructed of constant volume, in which case the absolute temperature will near with the pressure. will vary with the pressure.

If we denote pressure by p and p', the corresponding absolute temperatures by T and T', we should have

$$p:p'::T:T'$$
 and $T'=p'\frac{T}{p}$.

The absolute temperature T is to be considered in every case 460 higher than the thermometer-reading expressed in Fahrenheit degrees. From the form of the above equation, if the pressure p corresponding to a known absolute temperature T be known, T can be found. The quotient T/p is a constant which may be used in all determinations with the instrument. The pressure on the instrument can be expressed in inches of mercury, and is evidently the atmospheric pressure b as shown by a barometer, plus or minus an additional amount. A shown by a manometer attached to the air

minus an additional amount k another by a manometer attached to the air thermometer. That is, in general, $p = b \pm h$. The temperature of 32° F. is fixed as the point of melting ice, in which case T = 460 + 32 = 492° F. This temperature can be produced by surrounding the bulb in melting ice and leaving several minutes, so that the temperature of the confined air shall acquire that of the surrounding ice. When the air is at that temperature, note the reading of the attached manometer h, and that of a barometer; the sum will be the value of p corresponding to the absolute temperature of 492° F. The constant of the instrument, K = 492 + p, once obtained, can be used in all future determinations.

High Temperatures judged by Color.—The temperature of a body can be approximately judged by the experienced eye unaided, and M. Pouillet has constructed a table, which has been generally accepted, giving the colors and their corresponding temperature as below:

Deg. C.	Deg. F.	Deg. C	Deg. F.
Incipient red heat 525	977	Deep orange heat 1100	2021
Dull red heat 700	1292	Clear orange heat 1200	2192
Incipient cherry-red		White heat 1300	2372
heat 800	1472	Bright white heat. 1400	2552
Cherry-red heat 900	1652) 1500	2732
Clear cherry - red		Dazzling white heat to	to
heat 1000	1832	1600	2912

The results obtained, however, are unsatisfactory, as much depends on the susceptibility of the retina of the observer to light as well as the degree of illumination under which the observation is made.

A bright bar of iron, slowly heated in contact with air, assumes the following tints at annexed temperatures (Claudel):

	Cent.	Fahr.	1	Cent.	Fahr.
Yellow at	225	487	Indigo at	288	550
Orange at	243	473	Blue at	293	559
Red at	265	509	Green at	382	630
Violet at	277	531	"Oxide-gray"	400	752

BOILING POINTS AT ATMOSPHERIC PRESSURE. 14.7 lbs. per square inch.

Ether, sulphuric		Average sea-water		F.
Carbon bisulphide	118	Saturated brine	226	
Ammonia		Nitric acid	248	
Chloroform	140	Oil of turpentine	815	
Bromine	145	Phosphorus	554	
Wood spirit		Sulphur		
Alcohol		Sulphuric acid	590	
Benzine		Linseed oil	597	
Water		Mercury		

The boiling points of liquids increase as the pressure increases. The boiling point of water at any given pressure is the same as the temperature of saturated steam of the same pressure. (See Steam.)

MELTING-POINTS OF VARIOUS SUBSTANCES.

The following figures are given by Clark (on the authority of Pouillet, Claudel, and Wilson), except those marked *, which are given by Prof. Roberts-Austen in his description of the Le Chatelier pyrometer. These latter are probably the most reliable figures.

Alloy, 1 tin, 1 lead 370 to 466° F.
Tin 442 to 446
Cadmium 442
Bismuth 504 to 507
Lead 608 to 618*
Zinc 680 to 779*
Antimony 810 to 1150
Aluminum 1157*
Magnesium 1200
Calcium Full red heat.
Bronze 1692
Silver 1733* to 1873
Potassium sulphate 1859*
Gold 1913* to 2282
Copper 1929* to 1996
Cast iron, white 1922 to 2075*
" gray 2012 to 2786 2228*
Steel 2372 to 2532
" hard 2570*; mild, 2687*
Wrought iron 2732 to 2912
Palladium 2732*
Platinum 3227*

For melting-point of fusible alloys, see Alloys. Cobalt, nickel, and manganese, fusible in highest heat of a forge. Tungsten and chromium, not fusible in forge, but soften and agglomerate. Platinum and iridium, fusible only before the oxyhydrogen blowpipe.

QUANTITATIVE MEASUREMENT OF HEAT.

Unit of Heat.—The British unit of heat, or British thermal unit (B. T. U.), is that quantity of heat which is required to raise the temperature of 1 lb. of pure water 1° Fahr., at or near 89°.1 F., the temperature of maximum and the second mum density of water.

The French thermal unit, or calorie, is that quantity of heat which is re-

quired to raise the temperature of 1 kilogramme of pure water 1° Cent., at or about 4° C., which is equivalent to 39°.1 F.

1 French calorie = 8,968 British thermal units; 1 B. T. U. = .252 calorie.
The "pound calorie" is sometimes used by English writers; it is the

tity of heat required to raise the temperature of 1 lb. of water 1° C. 1 lb. culorie = 9/5 B.T.U. = 0.4536 calorie. The heat of combustion of carbon, to CO_3 , is said to be 8080 calories. This figure is used either for French calories or for pound calories, as it is the number of pounds of water that can be raised 1° C. by the complete combustion of 1 lb. of carbon, or the number of kilogrammes of water that can be raised 1° C. by the combustion of 1 kilo. of carbon; assuming in each case that all the heat generated is transferred to the water.

The Mechanical Equivalent of Heat is the number of footpounds of mechanical energy equivalent to one British thermal unit, heat and mechanical energy being mutually convertible. Joule's experiments, 1843-50, gave the figure 772, which is known as Joule's equivalent. More recent experiments by Prof. Rowland (Proc. Am. Acad. Arts and Sciences, 1880; see also Wood's Thermodynamics) give higher figures, and the most probable average is now considered to be 778.

1 heat-unit is equivalent to 778 ft.-lbs. of energy. 1 ft. lb. = 1/778 = .0012852 heat-units. 1 horse-power = 33,000 ft.-lbs. per minute = 2545 heat-unit beat-unit be

Heat of Combustion of Various Substances in Oxygen.

	Heat units. Cent. Fahr.		A suth omiter
			Authority.
	(34,462	62,032	Favre and Silbermann.
Hydrogen to liquid water at 0° C	₹ 33,808	60,854	Andrews.
" to steam at 100° C	(34,842 28,732	51,717	Thomsen. Favre and Silbermann.
Carbon (wood charcoal) to carbonic	8,080		Andrews.
acid, CO ₃ ; ordinary temperatures.	8,137	14,647	Berthelot.
Carbon, diamond to CO ₂ black diamond to CO ₂	7,859 7,861		
" graphite to CO ₂	7,901 2,473	14,222	
	2,403	4,325	
Carbonic oxide to CO ₂ , per unit of CO	2,431 2,385		Andrews. Thomsen.
CO to CO ₂ per unit of $C = 2\frac{1}{8} \times 2403$	5.607	10,093	Favre and Silbermann.
Marsh-gas, Methane, CH ₄ to water	13,120 13,108		Thomsen. Andrews.
and CO ₂	(13,063 (11,858		Favre and Silbermann.
Oleflant gas, Ethylene, C ₂ H ₄ to water and CO ₂	11,942	21,496	Andrews.
-	11,957	21,528 18,184	Thomsen.
Benzole gas, C ₆ H ₆ to water and CO ₂	9,915	17,847	Favre and Silbermann.

In burning 1 pound of hydrogen with 8 pounds of exygen to form 9 pounds of water, the units of heat evolved are 62,032 (Favre and 8.); but if the resulting product is not cooled to the initial temperature of the gases, part of the heat is rendered latent in the steam. The total heat of 1 bf of steam at 212° F. is 1146.1 heat-units above that of water at 32° , and $9 \times 1146.1 = 10,315$ heat-units, which deducted from 62,032 gives 51,717 as the heat evolved by the combustion of 1 lb. of hydrogen and 8 lbs. of oxygen at 32° F, to form steam at 212° F.

By the decomposition of a chemical compound as much heat is absorbed or rendered latent as was evolved when the compound was formed. If 11b of carbon is burned to CO₂, generating 14,544 B.T.U., and the CO₂ thus formed is immediately reduced to CO in the presence of glowing carbon, by the reaction $\text{CO}_2 + \text{C} = 2\text{CO}$, the result is the same as if the 2 bs. C had been burned directly to 2CO, generating 2 × 4451 = 8903 heat-units; consequently 14,544 — 8902 = 5642 heat-units have disappeared or become latent, and the

"unburning" of CO_2 to CO is thus a cooling operation. (For heats of combustion of various fuels, see Fuel.)

SPECIFIC HEAT.

Thermal Capacity.—The thermal capacity of a body is the quantity of heat required to raise its temperature one degree. The ratio of the heat or near required to raise its temperature one degree. The rand of the heat required to raise the temperature of a certain weight of a given substance one degree to that required to raise the temperature of the same weight of water one degree from the temperature of maximum density 39.1 is commonly called the specific heat of the substance. Some writers object to the tern as being an inaccurate use of the words "specific" and "heat." A more correct name would be "coefficient of thermal capacity"

Determination of Specific Heat.—Method by Mixture.—The body whose specific heat is to be determined is raised to a known temperature, and is then immersed in a mass of liquid of which the weight, specific heat, and temperature are known. When both the body and the liquid have attained the same temperature, this is carefully ascertained.

Now the quantity of heat lost by the body is the same as the quantity of heat elsewhed by the liquid

heat absorbed by the liquid.

Let c, w, and t be the specific heat, weight, and temperature of the hot body, and c', w', and t' of the liquid. Let T be the temperature the mixture assumes.

Then, by the definition of specific heat, $c \times w \times (t-T) =$ heat-units lost by the hot body, and $c' \times w' \times (T-t') =$ heat-units gained by the cold liquid. If there is no heat lost by radiation or conduction, these must be

$$cw(t-T)=c'w'(T-t') \quad \text{or} \quad c=\frac{c'w'\left(T-t'\right)}{w(t-T)}.$$

Specific Heats of Various Substances.

The specific heats of substances, as given by different authorities, show considerable lack of agreement, especially in the case of gases.

The following tables give the mean specific heats of the substances named according to Regnault. (From Rontgen's Thermodynamics, p. 134.) These specific heats are average values, taken at temperatures which usually come under observation in technical application. The actual specific heats of all substances, in the solid or liquid state, increase slowly as the body expands or as the temperature rises. It is probable that the specific heat of a body when liquid is greater than when solid. For many bodies this has been verified by experiment. The following tables give the mean specific heats of the substances named

votinou by captilinous				
	Solids.			
Antimony 0 Copper 0 Gold 0 Wrought iron 0 Glass 0 Cast iron 0 Lea-i 0 Platinum 0 Silver 0 Tin 0	.0951 Steel (hard) 0 .0624 Zine 0 .1188 Brass 0 .1897 Ice 0 .1298 Sulphur 0 .0314 Charcoal 0 .0334 Alumina 0 .0570 Phosphorus 0	1175 0966 0989 5040 2026 2410 1970		
Liquins.				
	0000 1 36	0000		

		Mercury 0.0333			
Lead (melted)	0.0402	Alcohol (absolute) 0.7009			
Sulphur "	0.2340	Fusel oil 0.5640			
Bismuth "		Benzine 0.4500			
Tin "		Ether			
Sulphuric soid	0.3350	1			

GASES.

Constant Pressure. Constant Volume.

	0.23751 0. 16847
Oxygen	0.21751 2.15507
Hydrogen	3.40900 2.41226 0.24380 0.17278
Superheated steam	0,4805 0,346
Carbonic acid	0.217 0.1585
Oleflant Gas (CH ₂)	
Carbonic oxide Ammonia	0.2479 0.1758 0.508 0.299
Ether	0.4797 0.8411
Alcohol	0.4534 0.3200
Acetic acid	0.4500
Chloroform	
(Selected from various sources.)	wing are given by other authorities.
	'ALS.
Platinum, 32° to 446° F0833	Wrought iron (Petit & Dulong).
(increased .000305 for each 100° F.)	" 32° to 212°
Cadmium	" 32° to 392°
Conner 200 to 0100 F	" 32° to 572°1218 " 32° to 662°1255
32° to 572° F 1018	Wrought iron (J. C. Hoadley,
Brass	ASME Vi718)
52° 10 572° F	l Wrought iron, 32° to 200°
Nickel	Wrought iron, 32° to 200°1129 22° to 600°1327 32° to 2000°2619
Nickel	32° 10 2000°,, ,2019
- OTHER	Source
Brickwork and masonry, about20	Coal
Marble	Coke
Chalk	Graphite
Quicklime	Sulphate of lime
Magnesian limestone	Magnesia222
Silica	Soda
Stones generally	River sand
- · · · · · · · · · · · · · · · · · · ·	
Wood Annual Annu	
	Oa.k
	Pear
	Pear
Liot	IIDS.
Liot	IIDS.
Alcohol, density .793	NDS. Olive oil
Alcohol, density .793	NDS. Olive oil
Liqu Alcohol, density .793	Olive oil
Liqu Alcohol, density .793	Olive oil
Liqu Alcohol, density .793	Olive oil
Liqu Alcohol, density .793	Olive oil
Alcohol, density .793	Olive oil
Alcohol, density .793	Olive oil
Alcohol, density .793	Olive oil
Alcohol, density .793	Olive oil
Alcohol, density .793622 Sulphuric acid, density 1.87385	Olive oil
Alcohol, density .793	Olive oil
Liqu Alcohol, density .793 .622 Sulphuric acid, density 1.87 .335 Mydrochloric acid .130 .661 Hydrochloric acid .600 Gas Sulphurous acid .126 Light carburetted hydrogen, ma Blast-furnace gases .126 Specific Heat of Sali Per cent salt in solution .5 Specific heat .93 Specific Heat of Air. Regna Between -30° C. and 10° C.	Olive oil
Liqu Alcohol, density .793 .622 Sulphuric acid, density 1.87 .335 Mydrochloric acid .130 .661 Hydrochloric acid .600 Gas Sulphurous acid .126 Light carburetted hydrogen, ma Blast-furnace gases .126 Specific Heat of Sali Per cent salt in solution .5 Specific heat .93 Specific Heat of Air. Regna Between -30° C. and 10° C.	Olive oil
Liquid	Olive oil
Liquid	Olive oil
Liquid	Olive oil

the specific heat of a fixed gas at constant pressure to the sp. ht. at constant volume is given as follows by different writers (Eng'g, July 12, 1889): Beguault, 1.3953; Moll and Beck, 1.4085; Szathmari, 1.4027; J. Macfarlane Gray, 1.4. The first three are obtained from the velocity of sound in air. The fourth is derived from theory. Prof. Wood says: The value of the ratio for air, as found in the days of La Place, was 1.41, and we have 0.3377 + 1.41 = 0.1886, the value used by Clausius, Hansen, and many others. But this ratio is not definitely known. Rankine in his later writings used 1.408, and Tait in a recent work gives 1.404, while some experiments gives less than 1.4 and others more than 1.41. Prof. Wood uses 1.406.

Specific Heat of Gases.—Experiments by Mallard and Le Chateller indicate a continuous increase in the specific heat at constant volume of steam, CO₂, and even of the perfect gases, with rise of temperature. The

steam, CO₃, and even of the perfect gases, with rise of temperature. The variation is inappreciable at 100° C., but increases rapidly at the high temperatures of the gas-engine cylinder. (Robinson's Gas and Petroleum Engines.)

1

Specific Heat and Latent Heat of Fusion of Iron and Steel. (H. H. Campbell, Trans. A. I. M. E., xix. 181.)

					_	Akerman.	Troilius.
Specific	heat	pig iron,	0 to	1200°	C	0.16	
- "	**	- 0	1200 to	1800°	Ċ	0.21	
**	44	"	0 to	1500°	C	****	0.18
"	44	44	1500 to	1800°	C	••••	0.20
Calculating by both sets of data we have:							

Akerman. Troilius. 330 calories per kilo. soft iron....

T.atent	heat	of fusion	Akerman. pig iron, calories per kilo 46	Troilius.	
***	1000		gray pig	83	
44	46	46	white pig	. 23	
 		. -			

From which we may assume that the truth is about: Steel, 20; pig iron, 30.

EXPANSION BY HEAT.

In the centigrade scale the coefficient of expansion of air per degree is of 1° C. In Farrenheit units it increases 1/491.2 = .002036 of its volume at 32° F. for every increase of 1° F.

Expansion of Gases by Heat from 32° to 212° F. (Regnault.)

	Increase in Volume, Pressure Constant. Volume at 32° Fahr. = 1.0, for		Volume Press	in Pressure, e Constant. sure at 32° = 1.0, for
	100° C.	1° F.	100° ℃.	1° F.
Hydrogen. Atmospheric air. Nitrogen Carbonic oxide Carbonic acid Sulphurous acid	0.3661 0.3670 0.3670 0.3669 0.3710 0.3908	0.002084 0.002089 0.002089 0.002088 0.002061 0.002168	0.3667 0.3665 0.3668 0.3667 0.3688 0.3845	0.002087 0.002086 0.002089 0.002037 0.002039 0.002186

If the volume is kept constant, the pressure varies directly as the absolute temperature.

Lineal Expansion of Solids at Ordinary Temperatures.

(British Board of Trade; from CLARE.)

	For 1° Fahr,	For 1° Cent.	Coef- ficient of Expan- sion from 32° to 212° F.	According to Other Authorities.
•	Length=1	Length=1		1
Aluminum (cast)	.00001234	.00002221	.002221	
Antimony (cryst.)	.00000627	.00001129	.001129	.001088
Brass, cast	.00000957	.00001722	.001722	.001868
" plate	.00001052	.00001894	.001894	•••••
Brick Bronze (Copper, 17; Tin, 2½; Zinc 1).	.00000308	.00000330	.000550	•••••
Bismuth	.00000975	.00001755	.001774	.001892
Cement, Portland (mixed), pure	.00000594	.00001070	.001070	.001082
Concrete: cement, mortar, and pebbles	.00000795	.00001430	.001430	
Copper	.00000887	.00001596	.001596	.001718
Ebonite	.00004278	.00007700	007700	
Glass, English flint	.00000451	.00000812	.000812	
" thermometer	.00000499	.00000897	.000897	
naru	.00000397	.00000714	.000714	
Granite, gray, dry	.00000438	.00000789	.000789	
" red, dry	.00000786	.00001415	.000897	•••••
Gold, pure	.00000786	.00000641	.000641	
Iron, wrought	.00000648	.00001166	.001166	.001285
" cast	.00000556	.00001001	.001001	.001110
Lead	.00001571	.00002828	.002828	
Magnesium		1		.002694
Marbles, various { from	.00000308	.00000554	000554	
) to	.00000786	.00001415	.001415	
Masonry, brick from	.00000256	.00000460	.000460	
Manager (and to	.00000494	.00000890	.000890	
Mercury (cubic expansion)	.00000695	.00011911	.0017971	.018018
Nickel Pewter	.000001129	.00001231	.002088	.001279
Plaster, white	.00000922	.00001660	.001660	
Platinum	.00000479	.00000863	.000868	
Platinum, 85 per cent { Iridium, 15 " " }	.00000453	.00000815		
Iridium, 15 " " \			.000815	.000884
PorcelainQuartz, parallel to major axis, t 0° to	.000000200	.000000860	.000360	
Quartz, parallel to major axis, $t 0^{\circ}$ to	00000484	00000000		1
40° C	.00000434	.00000781	.000781	
Quartz, perpendicular to major axis, t 0° to 40° C	.00000788	.00001419	.001419	Í
Silver, pure	.00001079	.00001943	.001419	.001908
Slate	.00000577	.00001038	.001038	.001800
Steel, cast	.00000636	.00001144	.001144	.001079
"tempered	.00000689	.00001240	.001240	.001019
Stone (sandstone), dry	.00000652	.00001174	.001174	1
	.00000417	.00000750	.000750	
<u>Tin</u>	.00001168	.00002094	.002094	.001938
Wedgwood ware	.00000489	.00000881	.000881	•••••
Wood, pine	.00000276	.00000496	.000496	
Zinc	.00001407	.00002582	.002532	.002942
Zinc, 8 t	.00001496	.00002692	.002692	•••••
1 m, 1)	l	l	l	

Cubical expansion, or expansion of volume \Rightarrow linear expansion \times 8.

Absolute Temperature-Absolute Zero. - The absolute zero of a gas is a theoretical consequence of the law of expansion by heat, assuming that it is possible to continue the cooling of a perfect gas until its volume is

diminished to nothing.

If the volume of a perfect gas increases 1/278 of its volume at 0° C, for If the volume of a perfect gas increases 1/2/3 of its volume at 0° C, for every increase of temperature of 1° C., and decreases 1/2/3 of its volume for every decrease of temperature of 1° C., then at -278° C. the volume of the imaginary gas would be reduced to nothing. This point -278° C., or 491.2° F. below the melting-point of ice on the air thermometer, or 492.6° F, below on a perfect gas thermometer $=-459.2^{\circ}$ F. (or -460.66°), is called the absolute zero; and absolute temperatures are temperatures measured, on either the Fahrenheit or centigrade scale, from this zero. The freezing point, 32° F., corresponds to 491.2° F. absolute. If p_0 be the pressure and v_0 the volume of a gas at the temperature of 32° F. = 491.2° on the absolute scale = T_0 , and p the pressure, and v the volume of the same quantity of gas at any other absolute temperature T, then

 $\frac{pv}{p_0v_0} = \frac{T}{T_0} = \frac{t + 459.8}{491.2}$ $\frac{pv}{T} = \frac{p_0 v_0}{T}.$

The value of $p_0v_0=T_0=\frac{1}{T_0}=\frac{1}{491.2}$; $\frac{p_0v_0}{T}=\frac{p_0v_0}{T_0}$. The value of $p_0v_0+T_0$ for air is 53.37, and pv=53.37T, calculated as follows by Prof. Wood:

A cubic foot of dry air at 32° F. at the sea-level weighs 0.080728 lb. The volume of one pound is $v_0 = \frac{1}{080728} = 12.387$ cubic feet. The pressure per square foot is 2116.2 lbs.

 $\frac{p_0 v_0}{r} = \frac{2116.2 \times 12.387}{401.18} = \frac{26214}{491.13} = 53.37.$

The figure 491.18 is the number of degrees that the absolute zero is below the figure 34.15 is the fluther of degrees that the absolute scale, whose divisions would be indicated by a perfect gas thermometer, the calculated value approximately is 492.66, which would make pv = 53.21T. Prof. Thomson considers that -273.1° C., $= -459.4^{\circ}$ F., is the most probable value of the absolute zero. See Hent in Ency. Brit.

Expansion of Liquids from 32° to 212° F.—Apparent expansion in glass (Clark). Volume at 212°, volume at 32° being 1:

Water	Nitrie acid	1.11
Water saturated with salt 1.05	Olive and linseed oils,	1.08
Mercury 1.0182	Turpentine and ether	1.07
Alcohol 1.11	Hydrochlor, and sulphuric acids	1.06

For water at various temperatures, see Water. For air at various temperatures, see Air.

LATENT HEATS OF FUSION AND EVAPORATION.

Latent Heat means a quantity of heat which has disappeared, having been employed to produce some change other than elevation of temperature. By exactly reversing that change, the quantity of heat which has dis appeared is reproduced. Maxwell defines it as the quantity of heat which must be communicated to a body in a given state in order to convert it into

another state without changing its temperature.

Latent Heat of Fusion.—When a body passes from the solid to the liquid state, its temperature remains stationary, or nearly stationary, at a certain melting point during the whole operation of melting; and in order to make that operation go on, a quantity of heat must be transferred to the

substance melted, being a certain amount for each unit of weight of the substance. This quantity is called the latent heat of fusion.

When a body passes from the liquid to the solid state, its temperature remains stationary or nearly stationary during the whole operation of freezing; a quantity of heat equal to the latent heat of fusion is produced in the body and rejected into the atmosphere or other surrounding bodies.

The following are examples in British thermal units per pound, as given

in Landolt & Börnstein's Physikalische-Chemische Tabellen (Berlin, 1894).

Substances. Latent Heat of Fusion.	Substances. Latent Heat of Fusion.
Bismuth22.75	Silver 37.93
Cast Iron, gray 41.4	Beeswax 76.14
Cast Iron, white 59.4	Paraffine 63.27
Lead 9.66	Spermaceti 66,56
Tin 25.65	Phosphorus 9.06
Zinc 50.68	Sulphur

Prof. Wood considers 144 heat units as the most reliable value for the latent heat of fusion of ice. Person gives 142 65.

Latent Heat of Evaporation.—When a body passes from the solid or liquid to the gaseous state, is temperature during the operation remains stationary at a certain boiling point, depending on the pressure of the vapor produced; and in order to make the evaporation go on, a quantity of heat must be transferred to the substance evaporated, whose amount for each unit of weight of the substance evaporated depends on the temperature. That heat does not raise the temperature of the substance, but disappears in causing it to assume the gaseous state, and it is called the latent heat of evaporation.

When a body passes from the gaseous state to the liquid or solid state, its

When a body passes from the gaseous state to the liquid or solid state, its temperature remains stationary, during that operation, at the boiling point corresponding to the pressure of the vapor: a quantity of heat equal to the latest heat of evaporation at that temperature is produced in the body; and in order that the operation of condensation may go on, that heat must be transferred from the body condensed to some other body.

The following are examples of the latent heat of evaporation in British thermal units, of one pound of certain substances, when the pressure of the vapor is one atmosphere of 14.7 lbs. on the square inch:

Subst	tance. Boiling-poin one atm. I	t under Laten Fahr. Briti	t Heat in sh units.
Water		965.7	(Regnault.)
Alcohol		864.3	(Andrews,)
Ether	95.0	1 6 2.8	"
Bisulphide of carbo	on 114.8	156.0	44

The latent heat of evaporation of water at a series of boiling-points extending from a few degrees below its freezing-point up to about 375 degrees Fahrenheit has been determined experimentally by M. Regnault. The results of those experiments are represented approximately by the formula. in British thermal units per pound,

$$l \text{ nearly} = 1091.7 - 0.7(t - 82^\circ) = 965.7 - 0.7(t - 212^\circ).$$

The Total Heat of Evaporation is the sum of the heat which disappears in evaporating one pound of a given substance at a given temperature (or latent heat of evaporation) and of the heat required to raise its temperature, before evaporation, from some fixed temperature up to the temperature of evaporation. The latter part of the total heat is called the sensible heat.

In the case of water, the experiments of M. Regnault show that the total heat of steam from the temperature of melting ice increases at a uniform rate as the temperature of evaporation rises. The following is the formula in British thermal units per pound:

$$h = 1091.7 + 0.305(t - 82^{\circ}).$$

For the total heat, latent heat, etc., of steam at different pressures, see table of the Properties of Saturated Steam. For tables of total heat, latent heat, and other properties of steams of ether, alcohol, acetone, chloroform, chloride of carbon, and bisulphide of carbon, see Rontgen's Thermodynamics (Dubois's translation.) For ammonia and sulphur dioxide, see Wood's Thermodynamics; also, tables under Refrigerating Machinery, in this book.

EVAPORATION AND DRYING.

In evaporation, the formation of vapor takes place on the surface; in boiling, within the liquid: the former is a slow, the latter a quick, method of evaporation.

If we bring an open vessel with water under the receiver of an air-pump and exhaust the air the water in the vessel will commence to boil, and if we keep up the vacuum the water will actually boil near its freezing-point. The formation of steam in this case is due to the heat which the water takes out of the surroundings.

Steam formed under pressure has the same temperature as the liquid in which it was formed, provided the steam is kept under the same pressure. By properly cooling the rising steam from boiling water, as in the multiple-

By properly cooling the rising steam from boiling water, as in the multipleeffect evaporating systems, we can regulate the pressure so that the water boils at low temperatures. Evaporation of Water in Reservoirs.—Experiments at the Mount Hope Reservoir, Rochester, N. Y., in 1891, gave the following results:

	July.	Aug.	Sept.	Oct.
Mean temperature of air in shade	70.5	70.8	68.7	53.8
" water in reservoir	68.2	70.2	66.1	54.4
" humidity of air, per cent	67.0	74.6	75.2	74.7
Evaporation in inches during month	5.59	4.98	4.05	8.28
Rainfall in inches during month	8.44	2.95	1.44	2.16

Evaporation of Water from Open Channels. (Flynn's Irrigation Canals and Flow of Water.)—Experiments from 1881 to 1885 in Tulare County, California, showed an evaporation from a pan in the river equal to an average depth of one eighth of an inch per day throughout the

wear. When the pan was in the air the average evaporation was less than 3/16 of an inch per day. The average for the month of August was 1/8 inch per day, and for March and April 1/12 of an inch per day. Experiments in Colorado show that evaporation ranges from .088 to .16 of an inch per day

during the irrigating season.

In Northern Italy the evaporation was from 1/12 to 1/9 inch per day, while in the south, under the influence of hot winds, it was from 1/6 to 1/5 irch

In the hot season in Northern India, with a decidedly hot wind blowing, the average evaporation was 1/2 inch per day. The evaporation increases

with the temperature of the water.

Evaporation by the Multiple System.—A multiple effect is a series of evaporating vessels each having a steam chamber, so connected that the heat of the steam or vapor produced in the first vessel heats the second, the vapor or steam produced in the second heats the third, and so on. The vapor from the last vessel is condensed in a condenser. Three vessels are generally used, in which case the apparatus is called a Triple Effect. In evaporating in a triple effect the vacuum is graduated so that the

liquid is boiled at a constant and low temperature.

Resistance to Boiling.—Brine. (Rankine.)—The presence in a liquid of a substance dissolved in it (as salt in water) resists ebullition, and raises the temperature at which the liquid boils, under a given pressure; but unless the dissolved substance enters into the composition of the vapor, the relation between the temperature and pressure of aturation of the vapor remains unchanged. A resistance to ebuilition is also offered by a vessel of remains unchanged. A resistance to ebullition is also offered by a vessel of a material which attracts the liquid (as when water beils in a glass vessel), and the boiling take place by starts. To avoid the errors which causes of this kind produce in the measurement of boiling-points, it is advisable to place the thermometer, not in the liquid, but in the vapor, which shows the true boiling-point, freed from the disturbing effect of the attractive nature of the vessel. The boiling-point of saturated brine under one atmosphere is 226° Fahr., and that of weaker brine is higher than the boiling-point of pure water by 1,2° Fahr., for each 1/32 of salt that the water contains 1/32° and the brine in marine boilers is not suf-Average sea-water contains 1/32; and the brine in marine boilers is not suffered to contain more than from 2/32 to 8/32.

Methods of Evaporation Employed in the Manufacture of Salt. (F. E. Engelhardt, Chemist Onondaga Salt Springs; Report for 1889.)—1. Solar heat—solar evaporation. 2. Direct fire, applied to the heating surface of the vessels containing br.ne—kettle and pan methods. 3. The steam-grainer system-steam-pans, steam-kettles, etc. 4. Use of steam and a reduction of the atmospheric pressure over the boiling brine-vacuum

system.

When a saturated salt solution boils, it is immaterial whether it is done under ordinary atmospheric pressure at 228° F., or under four atmospheres with a temperature of 320° F., or in a vacuum under 1/10 atmosphere, the result will always be a fine-grained salt.

The fuel consumption is stated to be as follows: By the kettle method, 40 to 45 bu. of salt evaporated per ton of fuel, anthractic dust burned on perfect of the salt evaporation. 5.53 lbs. of water per pound of coal. By the for ated grates; evaporation, 5.53 lbs. of water per pound of coal. By the pan method, 70 to 75 bu. per ton of fuel. By vacuum pans, single effect, 36 bu. per ton of anthracite dust (2000 lbs.). With a double effect nearly double that amount can be produced.

Solubility of Common Salt in Pure Water. (Andree.)

	82	50	86	104	140	176
100 parts water dissolve parts	35.63	85.69	36.03	36.82	37.06	88.00
100 parts brine contain salt	26.27	26.30	26.49	26.64	27.04	27.54

According to Poggial, 100 parts of water dissolve at 229.66° F., 40.85 parts of salt, or in per cent of brine, 28.749. Gay Lussac found that at 229.72° F., 100 parts of pure water would dissolve 40.88 parts of salt, in per cent of brine 28.741 parts.

brine, 28,764 parts.

The solubility of salt at 229° F. is only 2.5% greater than at 32°. Hence we cannot, as in the case of alum, separate the salt from the water by allowing a saturated solution at the boiling point to cool to a lower temperature.

Solubility of Sulphate of Lime in Pure Water. (Marignac.)

Temperature F. degrees.	82	64,5	89.6	100.4	105.8	127.4	186.8	212
Parts water to dissolve 1 part gypsum	415	386	871	868	870	875	417	452
1 part gypsum { Parts water to dissolve 1 { part anhydrous CaSO ₄ }	525	488	470	466	468	474	528	572

In sait brine sulphate of lime is much more soluble than in pure water. In the evaporation of salt brine the accumulation of sulphate of lime tends to stop the operation, and it must be removed from the puns to avoid waste of fuel.

The average strength of brine in the New York salt districts in 1889 was 69.38 degrees of the salinometer.

Strength of Salt Brines.—The following table is condensed from one given in U.S. Mineral Resources for 1888, on the authority of Dr. Englehardt.

Belations between Salinometer Strength, Specific Gravity, Solid Contents, etc., of Brines of Different Strengths.

Salinometer, degrees.	Baumé, degrees.	Specific gravity.	Per cent of salt,	Weight of a gallon of this brine in pounds.	Pounds of salt in a gal- lon of brine of 231 cubic inches.	Gallons of brine required for a bushel of salt.	Pounds of water to be evaporated to produce a bushel of salt,	Lbs. of coal required to produce a bushel of salt, 1 lb. coal evapo- rating 6 lbs. of water.	Bushels of salt that can be made with a ton of coal of 2000 pounds.
1	.26 .52	1.002	.265 .580	8.347 8.356	.022	2,531	21,076 10,510	3,513	.569
4	1.04	1.007	1,060	8.389	.099	1,264 629.7	5,927	1,752 871.2	1.141 2.295
6	1.56	1.010	1.590	8.414	.133	418.6	8,466	577.7	3.462
0	1.56 2.08	1.014	2.120	8.447	.179	812.7	2,585	430.9	4.641
10	2.60	1.017	2 650	8.472	.088 .133 .179 .224 .270 .316	249.4	2.057	342.9	5 888
12	8.12	1.021	8.180	8.506	.270	207.0	1,705	284.2	7.088
14	3.64	1.025	3.710	8.589	.316	176.8	1,453	242.2	9.256
16	4.16	1 028	4.240	8.564	.864	154.2	1,265	210.8	9 488
18	4.68 5.20	1.032		8.597	.410	136.5	1,118	186.8	10.78
20	7.80	1.054	5,300 7,950	8.622 8.781	.698	122.5 80.21	1,001	176.8	11.99
40	10.40	1.078	10,600	8.939	.947	59.09	648.4 472.3	108.1 78.71	18.51 25,41
50	13.00	1.093	13.250	9.105	1,206	46 41	366.6		82 78
60	15 60	1.114	15,900	9.280	1.475	37.94	296,2	49.86	40.51
70	18.20	1,136	18,550	9,464	1.755	31,89	245.9	40,98	48.80
80	20.80	1.158	21,200	9.647	2.045	27.38	208.1	84.69	57.65
90	23.40	1.182	23.850	9 847	2.348	23,84	178,8	29,80	67 11
100	26.00	1.200	26,500	10.089	2.660	21.04	155.3	25,88	77.26

Concentration of Sugar Solutions.* (From "Heating and Concentrating Liquids by Steam," by John G. Hudson; The Engineer, June 18, 1890.)—In the early stages of the process, when the liquor is of low density, the evaporative duty will be high, say two to three (British) gallons per square foot of heating surface with 10 lbs. steam pressure, but will gradually fall to an almost nominal amount as the final stage is approached. As a generally safe basis for designing, Mr. Hudson takes an evaporation of one gallon per hour for each square foot of gross heating surface, with steam of the pressure of about 10 lbs.

As examples of the evaporative duty of a vacuum pan when performing the earlier stages of concentration, during which all the heating surface

can be employed, he gives the following:

Coil Vacuum Pan.—434 in. copper coils, 528 square feet of surface; steam in coils, 15 lbs.; temperature in pan, 141° to 148°; density of feed, 25° Beaumé, and concentrated to 81° Beaumé.

First Trial.—Evaporation at the rate of 2000 gallons per hour = 3.8 gallons per square foot; transmission, 876 units per degree of difference of tem-

perature.

Second Trial.—Evaporation at the rate of 1503 gallons per hour = 2.8 gal-

lons per square foot; transmission, 265 units per degree.

As regards the total time needed to work up a charge of massecuite from As regards the total time needed to work up a charge of masseculité from liquor of a given density, the following figures, obtained by plotting the results from a large number of pans, form a guide to practical working. The pans were all of the coil type, some with and some without jackets, the gross heating surface probably averaging, and not greatly differing from, .25 square foot per gallon capacity, and the steam pressure 10 lbs, per square inch. Both plantation and refining pans are included, making various grades of sugar:

ANTIOUS BISHIOS OF BURGET!					
	Density 10°	of Feed	(degs.	Beaun 25°	né). 80°
Evaporation required per gallon masse- cuite discharged	6.128	8.6	2.26	1.5	.97
Average working hours required per charge	12,	9.	63/6	5.	4.
per square foot of gross surface, as- suming .25 sq. ft. per gallon capacity	2.04	1.6	1.89	1.2	.97
Fastest working hours required per charge		5.5	8.8	2.75	2.0
Equivalent average evaporation per hour per square foot	2.88	2.6	2.88	2.18	1.9

The quantity of heating steam needed is practically the same in vacuum as in open paus. The advantages proper to the vacuum system are primarily the reduced temperature of boiling, and incidentally the possibility of using heating steam of low pressure.

In a solution of sugar in water, each pound of sugar adds to the volume of the water to the extent of .061 gallon at a low density to .0638 gallon at

high densities.

aign densities.

A Method of Evaporating by Exhaust Steam is described by Albert Steams in Traus. A. S. M. E., vol. viii. A pan $17'6'' \times 11' \times 1'6''$, fitted with east-iron condensing pipes of about \$50 of. ft. of surface, evaporated 130 gallons per hour from clear water, condensing only about one half of the steam supplied by a plain slide-valve engine of $14'' \times 32''$ cylinder. making 65 revs. per min., cutting off about two thirds stroke, with steam at 75 lbs. boiler pressure.

It was found that keeping the pan-room warm and letting only sufficient

air in to carry the vapor up out of a ventilator adds to its efficiency, as the average temperature of the water in the pan was only about 165° F.

Experiments were made with coils of pipe in a small pan, first with no agitator, then with one having straight blades, and lastly with troughed blades; the evaporative results being about the proportions of one, two, and three respectively.

In evaporating liquors whose boiling point is 220° F., or much above that of water, it is found that exhaust steam can do but little more than bring them up to saturation strength, but on weak liquors, syrups, glues, etc., it should be very useful.

^{*} For other sugar data see Bagasse as Fuel, under Fuel.

466 HEAT.

Drying in Vacuum.—An apparatus for drying grain and other substances in vacuum is described by Mr. Emil Passburg in Proc. Inst. Mech. Engrs., 1889. The three essential requirements for a successful and economical process of drying are: 1. Cheap evaporation of the moisture; 2. Quick drying at a low temperature; 3. Large capacity of the apparatus employed.

The removal of the moisture can be effected in either of two ways: either

by slow evaporation, or by quick evaporation—that is, by boiling.

Slow Evaporation.—The principal idea carried into practice in machines acting by slow evaporation is to bring the wet substance repeatedly into contact with the inner surfaces of the apparatus, which are heated by steam, while at the same time a current of hot air is also passing through the substances for carrying off the moisture. This method requires much heat, because the hot-air current has to move at a considerable speed in order to shorten the drying process as much as possible; consequently a great quantity of heated air passes through and escapes unused. As a carrier of moisture hot air cannot in practice be charged beyond half its full saturation; and it is in fact considered a satisfactory result if even this proportion be attained. A great amount of heat is here produced which is

not used; while, with scarcely half the cost for fuel, a much quicker removal of the water is obtained by heating it to the boiling point. Quick Evaporation by Boiling.—This does not take place until the water is brought up to the boiling point and kept there, namely, 212° F., under atmospheric pressure. The vapor generated then escapes freely. Liquids are easily evaporated in this way, because by their motion consequent on built by vary is continuously. bolling the heat is continuously conveyed from the heating surfaces through the liquid, but it is different with solid substances, and many more difficulties have to be overcome, occause convection of the heat ceases entirely in The substance remains motionless, and consequently a much greater quantity of heat is required than with liquids for obtaining the

Evaporation in Vacuum.-All the foregoing disadvantages are avoided if the boiling-point of water is lowered, that is, if the evaporation is carried out under vacuum.

This plan has been successfully applied in Mr. Passburg's vacuum drying apparatus, which is designed to evaporate large quantities of water con-

tained in solid substances.

The drying apparatus consists of a top horizontal cylinder, surmounted by a charging vessel at one end, and a bottom horizontal cylinder with a discharging vessel beneath it at the same end. Both cylinders are encased in steam-jackets heated by exhaust steam. In the top cylinder works a revolving cast-iron screw with hollow blades, which is also heated by exhaust steam. The bottom cylinder contains a revolving drum of tubes, consisting of one large central tube surrounded by 24 smaller ones, all fixed in tube-plates at both ends; this drum is heated by live steam direct from the boiler. The substance to be dried is fed into the charging vessel through two manholes, and is carried along the top cylinder by the screw creeper to the back end, where it drops through a valve into the bottom cylinder, in which it is lifted by blades attached to the drum and travels forwards in the reverse direction; from the front end of the bottom cylinder it falls into a discharg-ing vessel through another valve, having by this time become dried. The vapor arising during the process is carried off by an air-pump, through a dome and air-valve on the top of the upper cylinder, and also through a throttle-valve on the top of the lower cylinder; both of these valves are supplied with strainers

As soon as the discharging vessel is filled with dried material the valve connecting it with the bottom cylinder is shut, and the dried charge taken out without impairing the vacuum in the apparatus. When the charging vessel requires replenishing, the intermediate valve between the two cylinders is shut, and the charging vessel filled with a fresh supply of wet material; the vacuum still remains unimpaired in the bottom cylinder, and has to be restored only in the top cylinder after the charging vessel has been

closed again.

In this vacuum the boiling-point of the water contained in the wet material is brought down as low as 110° F. The difference between this temperature and that of the heating surfaces is amply sufficient for obtaining good results from the employment of exhaust steam for heating all the surfaces except the revolving drum of tubes. The water contained in the solid substance to be dried evaporates as soon as the latter is heated to about 110° F.: and as long as there is any moisture to be removed the solid substance is not heated above this temperature.

Wet grains from a brewery or distillery, containing from 75% to 78% of water, have by this drying process been converted in some localities from a worthless incumbrance into a valuable food-stuff. The water is removed

a worthless incumbrance into a valuable food-stuff. The water is removed by evaporation only, no previous mechanical pressing being resorted to. At Messrs. Guinness's brewery in Dublin two of these machines are employed. In each of these the top cylinder is 20' 4" long and 2' 8" diam., and the screw working inside it makes 7 revs. per min.; the bottom cylinder is 19' 2" long and 5' 4" diam., and the drum of the tubes inside it makes 5 revs. per min. The drying surfaces of the two cylinders amount together to a total area of about 1000 sq. ft., of which about 49's is heated by exhaust steam direct from the boiler. There is only one air-pump, which is made large enough for three machines; it is horizontal, and has only one air-cylinder, which is double-acting, 173', in. diam. and 173', in. stroke; and it is driven at about 45 revs. per min. As the result of about eight months' experience, the two machines have been drying the wet grains from about 500 cwt. of malt per day of 24 hours. per day of 24 hours.

Roughly speaking, 8 cwt. of malt gave 4 cwt. of wet grains, and the latter yield 1 cwt. of dried grains; 500 cwt. of malt will therefore yield about 670 cwt. of wet grains, or 385 cwt. per machine. The quantity of water to be evaporated from the wet grains is from 75% to 78% of their total weight, or

say about 512 cwt. altogether, being 256 cwt. per machine.

BADIATION OF HEAT.

Radiation of heat takes place between bodies at all distances apart, and follows the laws for the radiation of light.

The heat rays proceed in straight lines, and the intensity of the rays radiated from any one source varies inversely as the square of their distance from the source.

This statement has been erroneously interpreted by some writers, who have assumed from it that a boiler placed two feet above a fire would receive by radiation only one fourth as much heat as if it were only one four above. In the case of boiler furnaces the side walls reflect those rays that are received at an angle—following the law of optics, that the angle of including dence is equal to the angle of reflection,—with the result that the intensity of heat two feet above the fire is practically the same as at one foot above,

of ness two only one-fourth as much.

The rate at which a hotter body radiates heat, and a colder body absorbs heat, depends upon the state of the surfaces of the bodies as well as on their temperatures. The rate of radiation and of absorption are increased by darkness and roughness of the surfaces of the bodies, and diminished by smoothness and polish. For this reason the covering of steam pipes and boilers should be smooth and of a light color: uncovered pipes and steam-

cylinder covers should be polished.

The quantity of heat radiated by a body is also a measure of its heatabsorbing power, under the same circumstances. When a polished body is struck by a ray of heat, it absorbs part of the heat and reflects the rest. The reflecting power of a body is therefore the complement of its absorbing power, which latter is the same as its radiating power.

The relative radiating and reflecting power of different bodies has been determined by experiment, as shown in the table below, but as far as quandetermined by experiment, as shown in the table below, but as far as quantities of heat are concerned, says Prof. Trowbridge (Johnson's Cyclosedia, art. Heat), it is doubtful whether anything further than the said relative determinations can, in the present state of our knowledge, be depended upon, the actual or absolute quantities for different temperatures being still uncertain. The authorities do not even agree on the relative radiating powers. Thus, Leslie gives for tin plate, gold, silver, and copper the figure 12, which differs considerably from the figures in the table below, given by Clark, stated to be on the authority of Leslie, De La Provostaye and Desains and Molloni. sains, and Melloni.

Relative Radiating and Reflecting Power of Different Substances.

	Radiating or Absorbing Power.	Reflecting Power.		Radiating or Absorbing Power.	Reflecting Power.
Lampblack	100 100 100 98 98 to 98		Zinc, polished, Steel, polished Platinum, polished " in sheet Tin	19 17 24 17 15	81 83 76 83 85
Ordinary glass Ice	85 79 27	10 15 28 78	Brass, cast, dead polishedBrass, bright polished	11	89 93
Cast iron, bright pol- ished	25 23	75 77	Copper, varnished hammered Gold, plated on polished	14 7 5	86 98 95
ished	23	77	steel Silver, polished bright	3	97 97

Experiments of Dr. A. M. Mayer give the following: The relative radiations from a cube of cast iron, having faces rough, as from the foundry, planed, "drawfiled," and polished, and from the same surfaces oiled, are as below (Prof. Thurston, in Trans. A. S. M. E., vol. xvi.):

Surface.	Oiled.	Dry.
Rough	60 49	100 32 20 18

It here appears that the oiling of smoothly polished castings, as of cylinder heads of steam-engines, more than doubles the loss of heat by radiation, while it does not seriously affect rough castings.

CONDUCTION AND CONVECTION OF HEAT.

Conduction is the transfer of heat between two bodies or parts of a body which touch each other. Internal conduction takes place between the parts of one continuous body, and external conduction through the surface of contact of a pair of distinct bodies.

The rate at which conduction, whether internal or external, goes on, being proportional to the area of the section or surface through which it

takes place, may be expressed in thermal units per square foot of area per

Internal Conduction varies with the heat conductivity, which depends upon the nature of the substance, and is directly proportional to the difference between the temperatures of the two faces of a layer, and inversely as its thickness. The reciprocal of the conductivity is called the internal thermal resistance of the substance. If r represents this resistance x the thickness of the layer in inches, x and x the two faces, and x the quantity in thermal units transmitted per hour per square

foot of area,
$$q = \frac{T' - T}{rx}$$
. (Rankine.)

Péclet gives the following values of r: Gold, platinum, silver..... 0.0016 Lead...... 0.0090 Copper..... 0.0018 Marble..... 0.0716 Iron..... 0.0043 Brick..... 0.1500 Zinc..... 0.0045

Belative Heat-conducting Power of Metals.

(* Calvert & Johnson ; † Weidemann & Franz.)								
Metals.	C. & J.	tW. & F. 1			†W. & F.			
Bilver	. 1000	1000	Cadmium		••••			
Gold	. 981	532	Wrought iron	486	119			
Gold, with 1% of silve	er 840		Tin	422	145			
Copper, rolled	. 845	736	Steel	897	116			
Copper, cast	. 811		Platinum	3⊱0	84			
Mercury	. 677	••••	Sodium		••••			
Mercury, with 1.2	5%		Cast iron		***			
of tin		****	Lead	287	85			
Aluminum,	. 665	••••	Antimony:					
Zinc:			cast horizonta		••••			
cast vertically	628		cast vertically		••••			
cast horizontally.	608	• • • • •	Bismuth	61	18			
rolled	641	• • • • •						

Influence of a Non-metallic Substance in Combination on the CONDUCTING POWER OF A METAL.

Influence of carbon on iron:	Cast copper 811
Wrought iron	Copper with 1% of arsenic 570
Steel 397	with .5% of arsenic 669
Cast iron 359	" with .25% of arsenic 771

The Bate of External Conduction through the bounding surface between a solid body and a fluid is approximately proportional to the difference of temperature, when that is small; but when that difference is

the rate of conduction increases faster than the simple ratio of that difference. (Rankine.)

If r, as before, is the coefficient of internal thermal resistance, e and e' the coefficient of external resistance of the two surfaces, x the thickness of the plate, and T' and T' the temperatures of the two fluids in contact with the two surfaces, the rate of conduction is $q = \frac{T' - T}{T}$. According to

two surfaces, the rate of conduction is $q = \frac{1-1}{e+e'+rx}$. According to

 $\overline{A[1+B(T-T)]}$, in which the constants A and B have Peclet, e + e' = the following values:

B for polished metallic surfaces B for rough metallic surfaces and for non-metallic surfaces. A for polished metals, about A for glassy and varnished surfaces. A for dull metallic surfaces for dull metallic surfaces for lamp-black	.90 1.34 1.58 1.78

When a metal plate has a liquid at each side of it, it appears from experiments by Peclet that $B=.058,\,A=8.8$.

The results of experiments on the evaporative power of boilers agree very well with the following approximate formula for the thermal resistance of boiler plates and tubes :

$$e+e'=\frac{a}{(T'-T)},$$

which gives for the rate of conduction, per square foot of surface per hour,

This formula is proposed by Rankine as a rough approximation, near enough to the truth for its purpose. The value of a lies between 160 and 200. Convection, or carrying of heat, means the transfer and diffusion of the heat in a fluid mass by means of the motion of the particles of that

The conduction, properly so called, of heat through a stagnant mass of fluid is very slow in liquids, and almost, if not wholly, inappreciable in gases. It is only by the continual circulation and mixture of the particles of the fluid that uniformity of temperature can be maintained in the fluid mass, or heat transferred between the fluid mass and a solid body.

The free circulation of each of the fluids which touch the side of a solid plate is a necessary condition of the correctness of Rankine's formulæ for the conduction of heat through that plate; and in these formulæ it is ir

plied that the circulation of each of the fluids by currents and eddies is such as to prevent any considerable difference of temperature between the fluid particles in contact with one side of the solid plate and those at considerable distances from it.

When heat is to be transferred by convection from one fluid to another, through an intervening layer of metal, the motions of the two fluid masses should, if possible, be in opposite directions, in order that the hottest particles of each fluid may be in communication with the hottest particles of the other, and that the minimum difference of temperature between the adjacent particles of the two fluids may be the greatest possible.

Thus, in the surface condensation of steam, by passing it through metal tubes immersed in a current of cold water or air, the cooling fluid should

be made to move in the opposite direction to the condensing steam.

Steam-pipe Coverings.

(Experiments by Prof. Ordway, Trans. A. S. M. E., vi. 168; also Circular No. 27 of Boston Mfrs. Mutual Fire Ins. Co., 1890.)

Substance 1 inch thick. Heat applied, 810° F.	Pounds of Water heated 10° F., per hour, through 1 sq. ft.	British Thermal Units per sq. ft. per minute.	Solid Matter in 1 sq. ft. 1 inch thick, parts in 1000.	Air included, parts in 1000.
1. Loose wool. 2. Live-gese feathers 3. Carded cotton wool. 4. Hair felt. 5. Loose lampblack. 6. Compressed lampblack.	8.1 9.6 10.4 10.3 9.8 10.6	1.35 1.60 1.73 1.72 1.63 1.77	56 50 20 185 56	944 950 980 815 944 756
7. Cork charcoal. 8. White-pine charcoal. 9. Anthracite-coal powder. 10. Loose calcined magnesia. 11. Compressed calcined magnesia. 12. Light carbonate of magnesia.	11.9 13.9 35.7 12.4 42.6 13.7	1.98 2.32 5.95 2.07 7.10 2.28	53 119 506 28 285 60	947 881 494 977 715 940
13. Compressed carb. of magnesia 14. Loose fossil-meal 15. Crowded fossil-meal 16. Ground chalk (Paris white) 17. Dry plaster of Paris 18. Fine asbestos	15.4 14.5 15.7 20.6 30.9 49.0	2.57 2.42 2.62 3.43 5.15 8.17	150 60 112 258 868 81	859 940 888 747 682 919
19. Air alone	48.0 62.1 13. 14. 21.	8.00 10.35 2.17 2.33 3.50 8.62	529	1000 471
25. Cork strips bound on	14.6 18. 18.7 16.7 22.	2.48 3. 3.12 2.78 8.67 8.50		
81. Loose anthracite coal ashes82. Paste of clay and vegetable fibre	27.	4.50 5.15		

It will be observed that several of the incombustible materials are nearly as efficient as wool, cotton, and feathers, with which they may be compared in the preceding table. The materials which may be considered wholly free from the danger of being carbonized or ignited by slow contact with pipes or boilers are printed in Roman type. Those which are more or less liable to be carbonized are printed in italics.

The results Nos. 1 to 20 inclusive were from experiments with the various non-conductors each used in a mass one inch thick, placed on a flat variace of iron kept heated by steam to 310° F. The substances Nos. 21 to

** were tried as coverings for two-inch steam pipe; the results being reduced to the same terms as the others for convenience of comparison.

Experiments on still air gave results which differ little from those of Nos. 3, 4, and 6. The bulk of matter in the best non-conductors is relatively too small to have any specific effect except to trap the air and keep it stagnant. These substances keep the air still by virtue of the roughness of their fibre or particles. The asbestos, No. 18, had smooth fibres. Asbestos with exceedingly fine fibre made a somewhat better showing, but asbestos is really one of the poorest non-conductors. It may be used advantageously to hold together other incombustible substances, but the less of it the better. A "magnesia" covering, made of carbonate of magnesia with a small percentage of good asbestos fibre and containing 0.25 of solid matter, transmitted 2.5 B. T. U. per square foot per minute, and one containing 0.396 of solid matter transmitted 3.38 B. T. U.

Any suitable substance which is used to prevent the escape of steam heat

should not be less than one inch thick.

Any covering should be kept perfectly dry, for not only is water a good carrier of heat, but it has been found that still water conducts heat about

eight times as rapidly as still air.

Tests of Commercial Coverings were made by Mr. Geo. M. Brill and reported in Trans. A. S. M. E., xvi. 827. A length of 60 feet of 8-th steam pipe was used in the tests, and the heat loss was determined by the condensation. The steam pressure was from 109 to 117 lbs. gauge, and the temperature of the air from 58° to 81° F. The difference between the temperature of steam and air ranged from 283° to 286°, averaging 272°.

The following are the principal results:

Kind of Covering.	Thickness of Covering. inches.	Lbs. Steam condensed per sq. ft. per hour.	B. T. U. per sq ft. per minute.	B. T. U. per sq. ft. per hour per degree of average difference of temperature.	Saving due to cover- ing lbs. steam per hour per sq. ft.	Ratio of Heat lost, Bare to Covered Pipe, \$.	H. P. lost per 100 sq. ft. of pipe (30 lbs. per hour = 1 H. P.).
Bare pipe. Magnesia Rock wool. Mineral wool Fire-felt. Manville sectional Manv. sect. & hair-felt.	1.25 1.60 1.30 1.30 1.70 2.40 2.20	.846 .120 .080 .089 .157 .109 .066	12.27 1.74 1.16 1.29 2.28 1.59 0.96 1.56	.212	.726 .766 .757 .689 .797 .780	100. 14.2 9.5 10.5 18.6 12.9 7.8 12.7	2.819 .400 .267 .297 .523 .564 .221
Manville wool-cement. Champion mineral wool Hair-felt	1.44 .82 .75	.108 .099 .183 .298 .275	1.44 1.91 4.32 3.99	.317 .422 .953	.747 .714 .548 .571	11.7 15.6 85.2 32.5	.839 .830 .439 .998 .916

Transmission of Heat, through Solid Plates, from Water to Water. (Clark, S.E.).—M. Péclet found, from experiments made with plates of wrought iron, cast iron, copper, lead, zinc, and tin, that when the fluid in contact with the surface of the plate was not circulated by artificial means, the rate of conduction was the same for different thicknesses. But when the water was thoroughly circulated over the surfaces, and when these were perfectly clean, the quantity of transmitted heat was inversely proportional to the thickness, and directly as the difference in temperature of the two faces of the plate. When the metal surface became dull, the rate of transmission of heat through all the metals was very nearly the same.

It follows, says Clark, that the absorption of heat through metal plates is more active whilst evaporation is in progress—when the circulation of the water is more active—than while the water is being heated up to the boiling point.

Transmission from Steam to Water.—M. Péclet's principle is supported by the results of experiments made in 1867 by Mr. Isherwood on the conductivity of different metals. Cylindrical pots, 10 inches in diameter, 31½ inches deep inside, and ½ inch, ½ inch, and ¾ inch thick, turned and bored, were formed of pure copper, brass (60 copper and 40 zinc), rolled wrought iron, and remelted cast iron. They were immersed in a steam bath, which was varied from 220° to 320° F. Water at 212° was supplied to the pots, which were kept filled. It was ascertained that the rate of evaporation was in the direct ratio of the difference of the temperatures inside and outside of the pots; that is, that the rate of evaporation per degree of difference of temperatures was the same for all temperatures; and that the rate of evaporation was exactly the same for different thicknesses of the metal. The respective rates of conductivity of the several metals were as follows, expressed in weight of water evaporated from and at 212° F. per square foot of the interior surface of the pots per degree of difference of temperature per hour, together with the equivalent quantities of heat-units:

7	Water at 212°.	Heat-units.	Ratio.	
Copper	665 lb.	642.5	1.00	
Brass		556.8	.87	
Wrought iron	387 "	873 6	.58	
Cast iron		815.7	.49	

Whitham, "Steam Engine Design," p. 283, also Trans. A. S. M. E. ix, 425, in using these data in deriving a formula for surface condensers calls these figures those of perfect conductivity, and multiplies them by a coefficient C, which he takes at 0.323, to obtain the efficiency of condenser surface in ordinary use, i.e., coated with saline and greasy deposits.

ordinary use, i.e., coated with saline and greasy deposits.

Transmission of Heat from Steam to Water through
Coils of Iron Pipe.—H. G. C. Kopp and F. J. Meystre (Stevens Indicator, Jan, 1894), give an account of some experiments on transmission of heat through coils of pipe. They collate the results of earlier experiments as follows, for comparison:

Experimenter.	er of Surface.	dense Square degree ence of ature p	con- d per foot per differ- temper- er hour.	mitte square degree ence of	differ-	Remarks.
Experi	Character	Heating, pounds.	Evapo- rating, pounds.	Heating, B. T. U.	Evapo- rating B. T. U.	
Havrez Perkins.	Copper colls 2 Copper colls. Copper coll Iron coll	.268	.981 1.20 1.26 .24	815 280 	974 1120 1200 215 208.2	Steam pressure = 100. Steam pressure = 10.
"	Iron tube " " Cast-iron boil- er	.285 .196 .206	.105	290 207 210 82	100	, = 200

From the above it would appear that the efficiency of iron surfaces is less

than that of copper coils, plate surfaces being far inferior.

In all experiments made up to the present time, it appears that the temperature of the condensing water was allowed to rise, a mean between the initial and final temperatures being accepted as the effective temperature. But as water becomes warmer it circulates more rapidly, thereby causing the water surrounding the coil to become agitated and replaced by cooler water, which allows more heat to be transmitted.

Again, in accepting the mean temperature as that of the condensing medium, the assumption is made that the rate of condensation is in direct proportion to the temperature of the condensing water.

In order to correct and avoid any error arising from these assumptions

and approximations, experiments were undertaken, in which all the conditions were constant during each test.

The pressure was maintained uniform throughout the coil, and provision was made for the free outflow of the condensed steam, in order to obtain at all times the full efficiency of the condensing surface. The condensing water was continually stirred to secure uniformity of temperature, which was regulated by means of a steam-pipe and a cold-water pipe entering the tank in which the coil was placed.

The following is a condensed statement of the results

HEAT TRANSMITTED PER SQUARE FOOT OF COOLING SURFACE, PER HOUR, PER DEGREE OF DIFFERENCE OF TEMPERATURE. (British Thermal Units.)

Temperature of Condens- ing Water.	1-in. Iron Pipe; Steam inside, 60 lbs. Gauge Pressure.	1½ in. Pipe; Steam inside, 10 lbs. Pressure.	11/2 in. Pipe; Steam outside, 10 lbs. Pressure.	1½ in. Pipe; Steam inside, 60 lbs. Pressure.
80	265	128	200	
100	269	180	230	239
100 120	272	187	260	247
140	277	145	267	276
160	281	158	271	306
180	299	174	270	849
200	813			419

The results indicate that the heat transmitted per degree of difference of temperature in general increases as the temperature of the condensing water is increased.

The amount transmitted is much larger with the steam on the outside of the coil than with the steam inside the coil. This may be explained in part by the fact that the condensing water when inside the coll flows over the surface of conduction very rapidly, and is more efficient for cooling than when contained in a tank outside of the coil.

This result is in accordance with that found by Mr. Thomas Craddock, which indicated that the rate of cooling by transmission of heat through metallic surfaces was almost wholly dependent on the rate of directation of

the cooling medium over the surface to be cooled.

Transmission of Heat in Condenser Tubes. (Eng'g, Dec. 10, 1875, p. 449.).—In 1874 B. C. Nichol made experiments for determining the rate at which heat was transmitted through a condenser tube. The results went to show that the amount of heat transmitted through the walls of the tube per estimated degree of mean difference of temperature increased considerably with this difference. For example:

Estimated mean difference of temperature between inside and	Ve	rtical T	ube.		zontal 1	
outside of tube, degrees Fahr Heat-units transmitted per hour	128	151.9	152.9		146.2	
per square foot of surface per degree of mean diff. of temp	422	581	561	610	737	823

These results seem to throw doubt upon Mr. Isherwood's statement that the rate of evaporation per degree of difference of temperature is the same

for all temperatures.

Mr. Thomas Craddock found that water was enormously more efficient than air for the abstraction of heat through metallic surfaces in the process of cooling. He proved that the rate of cooling by transmission of heat through metallic surfaces depends upon the rate of circulation of the cool-, ing medium over the surface to be cooled. A tube filled with hot water, moved by rapid rotation at the rate of 59 ft. per second, through air, lost as much heat in one minute as it did in still air in 12 minutes. In water, at a velocity of 3 ft. per second, as much heat was abstracted in half a minute as was abstracted in one minute when it was at rest in the water. Mr. Craddock concluded, further, that the circulation of the cooling fluid became of

greater importance as the difference of temperature on the two sides of the plate became less. (Clark, R. T. D., p. 461.)

Heat Transmission through Cast-Iron Plates Pickled in Nitric Acid.—Experiments by R. C. Carpenter (Trans. A. S. M. E., xii 179) show a marked change in the conducting power of the plates (from steam to water), due to prolonged treatment with dilute nitric acid. The action of the nitric acid, by dissolving the free iron and not attacking the carbon, forms a protecting surface to the iron, which is largely composed of carbon. The following is a summary of results:

Character by 5.4 in.	of Plates, , exposed s	each plate 8.4 in. urface 27 sq. ft.	Increase in Tempera- ture of 8.125 lbs. of Water each Minute.	Transmitted for	Rela- tive Trans- mission of Heat.
		d skin on, but	18.90	118.9	100.0
		. 1% sol., 9 days	11.5	97.7	86.8
Cast II OII -	-minic acid	1% sol., 18 days.		80.08	70.7
66	66	1% sol., 40 days.	9.6	77.8	68.7
44	44	5% sol., 9 days	9.93	87.0	76.8
44	44	5% sol., 40 days.	10.6	77.4	68.5
Dieta of m	hoom ani	same dimensions			J 00.5
as the	plate of ca	st iron	0.88	1.9	1.6

The effect of covering cast-iron surfaces with varnish has been investigated by P. M. Chamberlain. He subjected the plate to the action of strong acid for a few hours, and then applied a non conducting varnish. One surface only was treated. Some of his results are as follows:

170. As finished—greasy.
152. " washed with benzine and dried. 3.5 ft. per hour, i each degree, r - r'. 169. Oiled with lubricating oil. 162. After exposure to nitric acid sixteen hours, then oiled (linseed oil.) After exposure to hydrochloric acid twelve hours, then oiled 166 (linseed oil.) After exposure to sulphuric acid 1, water 2, for 48 hours. then oiled, varnished, and allowed to dry for 24 hours.

Transmission of Heat through Solid Plates from Air or other Dry Gases to Water. (From Clark on the Steam Engine.)

—The law of the transmission of heat from hot air or other gases to water, through metallic plates, has not been exactly determined by experiment. The general results of experiments on the evaporative action of different transmission of the evaporative action of different transmissions. portions of the heating surface of a steam boiler point to the general law that the quantity of heat transmitted per degree difference of temperature is practically uniform for various differences of temperature.

The communication of heat from the gas to the plate surface is much

accelerated by mechanical impingement of the gaseous products upon the

Clark says that when the surfaces are perfectly clean, the rate of transmission of heat through plates of metal from air or gas to water is greater for copper, next for brass, and next for wrought iron. But when the surfaces are dimmed or coated, the rate is the same for the different metals.

With respect to the influence of the conductivity of metals and of the thickness of the plate on the transmission of heat from burnt gases to water, Mr. Napier made experiments with small bollers of iron and copper placed over a gas-flame. The vessels were 5 inches in diameter and 2½ inches deep. From three vessels, one of iron, one of copper, and one of iron sides and copper bottom, each of them 1/30 inch in thickness, equal quantities of water water appropriate to drawers, in the times as followed. ties of water were evaporated to dryness, in the times as follows:

Water.	Iron Vessel.	Copper Vessel.	Iron and Copper Vessel.
4 ounces	19 minutes 83 "	18.5 minutes 3 0.75	•••••
514 "	50 " 85.7 "	44 "	86.83 minutes.

Two other vessels of iron sides 1/30 inch thick, one having a 1/4-inch copper ottom and the other a 4-inch lead bottom, were tested against the iron and copper vessel, 1/30 inch thick. Equal quantities of water were evaporated in 54, 55, and 634 minutes respectively. Taken generally, the results of these experiments show that there are practically but slight differences between iron, copper, and lead in evaporative activity, and that the activity is not affected by the thickness of the bottom.

Mr. W. B. Johnson formed a like conclusion from the results of his observations of two boilers of 160 horse-power each, made exactly alike, except that one had iron flue-tubes and the other copper flue-tubes. No dif-

ference could be detected between the performances of these boilers.

Divergencies between the results of different experimenters are attributable probably to the difference of conditions under which the heat was transmitted, as between water or steam and water, and between gaseous transmitted, as between water or steam and water, and other matter and water. On one point the divergence is extreme: the rate of transmission of heat ner degree of difference of temperature. Whilst from 400 to 600 units of heat are transmitted from water to water through iron plates, per degree of difference per square foot per hour, the quantity of heat transmitted between water and air, or other dry gas, is only about from 2 to 5 units, according as the surrounding air is at rest or in movement. In a locomotive boiler, where radiant heat was brought into play, 17 units of heat were transmitted through the plates of the fire-box per degree of difference of temperature per square foot per hour.

Transmission of Heat through Plates and Tubes from Steam or Hot Water to Air.—The transfer of heat from steam or

water through a plate or tube into the surrounding air is a complex operation, in which the internal and external conductivity of the metal, the radiating power of the surface, and the convection of heat in the surrounding air are all concerned. Since the quantity of heat radiated from a surface varies with the condition of the surface and with the surroundings, according to laws not yet determined, and since the heat carried away by convection varies with the rate of the flow of the air over the surface, it is evident that

no general law can be laid down for the total quantity of heat emitted. The following is condensed from an article on Loss of Heat from Steam-

pipes, in The Locomotive, Sept. and Oct., 1892.

A hot steam pipe is radiating heat constantly off into space, but at the same time it is cooling also by convection. Experimental data on which to base calculations of the heat radiated and otherwise lost by steam-pipes are

neither numerous nor satisfactory.
In Box's Practical Treatise on Heat a number of results are given for the amount of heat radiated by different substances when the temperature of the air is 1° Fahr. lower than the temperature of the radiating body. A portion of this table is given below. It is said to be based on Péclet's experiments.

HEAT UNITS RADIATED PER HOUR, PER SQUARE FOOT OF SURFACE, FOR 1° FAHRENHEIT EXCESS IN TEMPERATURE.

Copper, polished	Sheet-iron, ordinary
Tin, polished	Glass
Zinc and brass, polished	Cast iron, new
Tinned iron, polished	Common steam-pipe, inferred 6400
Sheet-iron, polished	Cast and sheet iron, rusted 6868
Sheet lead	Wood, building stone, and brick .7358

When the temperature of the air is about 50° or 60° Fahr., and the radiating body is not more than about 30° hotter than the air, we may calculate the radiation of a given surface by assuming the amount of heat given off by it in a given time to be proportional to the difference in temperature be-tween the radiating body and the air. This is "Newton's law of cooling." But when the difference in temperature is great, Newton's law does not hold good; the radiation is no longer proportional to the difference in temperature, but must be calculated by a complex formula established experiment, ally by Dulong and Petit. Box has computed a table from this formula, which greatly facilitates its application, and which is given below:

FACTORS FOR REDUCTION TO DULONG'S LAW OF RADIATION.

Differences in Tem- perature between	Temperature of the Air on the Fahrenheit Scale.											
Radiating Body and the Air.	320	50°	590	68°	86°	104°	1220	140°	1580	176°	1940	2120
Deg, Fahr,							-	7			-	
18	1.00	1.07	1.12	1.16	1.95	1.86	1.47	1.58	1.70	1 85	1 00	9.15
36	1.03	1.08	1.16	1.21	1.30	1.40	1.52	1.68	1.76	1.91	2 06	2 99
54				1.25								
72	1.12	1.20	1.25	1.30	1.40	1.59	1.64	1.76	1.90	2 07	9.98	2 40
90	1.16	1.25	1.31	1.36	1.46	1.58	1.71	1.84	1.98	2.15	2.83	2.51
108				1.42								
126				1.48								
144				1.54								
162	1.87	1.48	1.54	1.60	1.73	1.86	2.02	2.17	2.34	2.54	2.74	2.96
180				1.68								
198	1.50	1.62	1.69	1.75	1.89	2.04	2.21	2.38	2.56	2.78	3.00	3.24
216	1.58	1.69	1.76	1.83	1.97	2.13	2.32	2.48	2.68	2.91	3.13	3.38
234				1.90								
252				2.00								
270	1.79	1.93	2.01	2.09	2,22	2.44	2.64	2.84	3.06	3.32	8.58	3.87
288	1.89	2.03	2.12	2.20	2.37	2.56	2.78	2.99	3.22	3.50	3.77	4.07
306	1.98	2.18	2.22	2.31	2.49	2.69	2.90	3,12	3.37	3.66	3.95	4.26
324				2.42								
342				2.54								
360	2.27	2,45	2,56	2.66	2.86	3.09	3.35	3,60	8.88	4.22	4.55	4.91
378				2.79								
306				2.93								
414	2.68	2.84	2.95	3.07	3.31	3.51	3.87	4.12	4.48	4.87	5,26	5.67
432	2.76	2.98	3.10	3.23	3.47	3.76	4.10	4,32	4.61	5.12	5.33	6.04

The loss of heat by convection appears to be independent of the nature of the surface, that is, it is the same for iron, stone, wood, and other materials. It is different for bodies of different shape, however, and it varies with the position of the body. Thus a vertical steam-pipe will not lose so much heat by convection as a horizontal one will; for the air heated at the lower part of the vertical pipe will rise along the surface of the pipe, protecting it to some extent from the chilling action of the surrounding cooler air. For a similar reason the shape of a body has an important influence on the result, those bodies losing most heat whose forms are such as to allow the cool air free access to every part of their surface. The following table from Box gives the number of heat units that horizontal cylinders or pipes lose by convection per square foot of surface per hour, for one degree difference in temperature between the pipe and the air.

HEAT UNITS LOST BY CONVECTION FROM HORIZONTAL PIPES, PER SQUARE FOOT OF SUBFACE PER HOUR, FOR A TEMPERATURE DIFFERENCE OF 1° FAHR.

External Diameter of Pipe in inches.	Heat Units Lost.	External Diameter of Pipe in inches.	Heat Units Lost.	External Diameter of Pipe in inches.	Heat Units Lost.
9 8 4 5	0.728 0.626 0.574 0.544 0.528	7 8 9 10 12	0.509 0.498 0.489 0.482 0.472	18 24 86 48	0.455 0.447 0.438 0.434

The loss of heat by convection is nearly proportional to the difference in temperature between the hot body and the air; but the experiments of

Dulong and Péclet show that this is not exactly true, and we may here also resort to a table of factors for correcting the results obtained by simple proportion.

FACTORS FOR REDUCTION TO DULONG'S LAW OF CONVECTION.

Difference in Temp. between Hot Body and Air.	Factor.	Difference in Temp. between Hot Body and Air.	Factor.	Difference in Temp. between Hot Body and Air.	Factor.
18° F. 36° 54° 72° 90° 108° 126° 144° 162°	0.94 1.11 1.22 1.30 1.37 1.48 1.49 1.53 1.58	180° F. 198° 216° 234° 252° 270° 288° 306° 324°	1.62 1.65 1.68 1.78 1.74 1.77 1.80 1.83 1.85	342° F. 360° 376° 396° 414° 432° 460° 468°	1.87 1.90 1.92 1.94 1.96 1.98 2.00 8.08

EXAMPLE IN THE USE OF THE TABLES.—Required the total loss of heat by both radiation and convection, per foot of length of a steam-pipe 2 11/82 in. external diameter, steam pressure 60 lbs., temperature of the air in the room 68º Fahr.

Temperature corresponding to 60 lbs. equals 307°; temperature difference

 $= 307 - 68 = 239^{\circ}$ Area of one foot length of steam-pipe = $211/39 \times 3.1416 + 12 = 0.614$ sq.

Heat radiated per hour per square foot per degree of difference, from

table, 0.64. Radiation loss per hour by Newton's law = $289^{\circ} \times .614$ ft. $\times .64 = 93.9$ heat units. Same reduced to conform with Dulong's law of radiation: factor from table for temperature difference of 239° and temperature of air 68° = 1.93. $93.9 \times 1.93 = 181.2$ heat units, total loss by radiation.

1.53. $83.9 \times 1.53 = 181.2$ neat units, total loss by radiation. Convection loss per square foot per hour from a 211/32-inch pipe: by interpolation from table, 2'' = .728, 3'' = .626, 211/32'' = .693. Area, $.614 \times .693 \times 239^\circ = 101.7$ heat units. Same reduced to conform with Dulong's law of convection: 101.7×1.73 (from table) = 175.9 heat units per hour. Total loss by radiation and convection = 181.2 + 175.9 = 357.1 heat units per hour. Loss per degree of difference of temperature per linear foot of pipe per hour = 357.1 + 239 = 1.494 heat units = 2.433 per sq. ft.

It is not claimed, says The Locomotive, that the results obtained by this

nethod of calculation are strictly accurate. The experimental data are not sufficient to allow us to compute the heat-loss from steam-pipes with any great degree of refinement; yet it is believed that the results obtained as indicated above will be sufficiently near the truth for most purposes. An experiment by Prof. Ordway, in a pipe 2 11/32 in. diam. under the above conditions (Trans. A. S. M. E., v. 73), showed a condensation of steam of 181 grammes per hour, which is equivalent to a loss of heat of 358.7 heat units per hour, or within half of one per cent of that given by the above relowless. per hour, or within half of one per cent of that given by the above calculation.

According to different authorities, the quantity of heat given off by steam and hot-water radiators in ordinary practice of heating of buildings by direct radiation varies from 1.8 to about 3 heat units per hour per square

foot per degree of difference of temperature.

The lowest figure is calculated from the following statement by Robert Briggs in his paper on "American Practice in Warming Buildings by Steam" (Proc. Inst. C. E., 1882, vol. lxxi): "Each 100 sq. ft. of radiating surface will give off 3 Fahr. heat units per minute for each degree F. of difference in temperature between the radiating surface and the air in which

the figure 2 1/2 heat units is given by the Nason Manufacturing Company in their catalogue, and 2 to 3 1/4 are given by many recent writers.

For the ordinary temperature difference in low-pressure steam-heating, say 212° - 70° = 142° F., 1 lb. steam condensed from 212° to water at the

same temperature gives up 965.7 heat units. A loss of 2 heat units per sq. ft. per hour per degree of difference, under these conditions, is equivalent to 2 × 142+965 = 0.3 lbs, of steam condensed per hour per sq. ft. of heating surface. (See also Heating and Ventilation.)

Transmission of Heat through Walls, etc., of Buildings (Nason Manufacturing Co.). (See also Heating and Ventilation.)—that has the remarkable property of passing through moderate thicknesses of air and gases without appreciable loss, so that air is not warmed by radiant heat but by contact with surfaces that have absorbed the radiation. heat, but by contact with surfaces that have absorbed the radiation,

POWERS OF DIFFERENT SUBSTANCES FOR TRANSMITTING HEAT.

Window-glass	1	000	Bricks, rough	200 to	250
Oak or walnut		66	Bricks, whitewashed		200
White pine		80	Granite or slate		250
Pitch-pine		100	Sheet iron	1030 to	1110
Lath or plaster	75 to	100	•		

A square foot of glass will cool 1.279 cubic feet of air from the temperature inside to that outside per minute, and outside wall surface is generally

estimated at one fifth of the rate of glass in cooling effect.

Box, in his "Practical Treatise on Heat," gives a table of the conducting powers of materials prepared from the experiments of Péclet. It gives the quantity of heat in units transmitted per square foot per hour by a plate 1 inch in thickness, the two surfaces differing in temperature 1 degree:

Fine-grained gray marble	28.00
Coarse-grained white marble	22.4
Stone, calcareous, fine	16.7
Stone, calcareous, ordinary	. 13.68
Baked clay, brickwork	4.83
Brick-dust, sifted	1.33

Hood, in his "Warming and Ventilating of Buildings," p. 249, gives the results of M. Depretz, which, placing the conducting power of marble at 1.00, give .483 as the value for firebrick.

THERMODYNAMICS.

Thermodynamics, the science of heat considered as a form of energy, is useful in advanced studies of the theory of steam, gas, and air englines, refrigerating machines, compressed air, etc. The method of treatment adopted by the standard writers is severely mathematical, involving constant application of the calculus. The student will find the subject thoroughy treated in the recent works by Rontgen (Dubois's translation),

thoroughy treated in the recent with a symmetry word, and Peabody.

First Law of Thermodynamics.—Heat and mechanical energy are mutually convertible in the ratio of about 778 foot-pounds for the British thermal unit. (Wood.) Heat is the living force or vis viva due to certain molecular motions of the molecules of bodies, and this living force may be written and the processor of heat in foot-pounds, a unit of heat in stated or measured in units of heat or in foot-pounds, a unit of heat in British measures being equivalent to 772 [778] foot-pounds. (Trowbridge, Trans. A. S. M. E., vil. 727.)

Second Law of Thermodynamics.—The second law has by dif-

ferent writers been stated in a variety of ways, and apparently with ideas so diverse as not to cover a common principle. (Wood, Therm., p. 389.)
It is impossible for a self-acting machine, unaided by any external agency

to convert heat from one body to another at a higher temperature. (Clau-

sius.)

If all the heat absorbed be at one temperature, and that rejected be at one lower temperature, then will the heat which is transmuted into work be to the entire heat absorbed in the same ratio as the difference between the to the entire near absorbed in the same ratio as the difference between the absolute temperature of the source. In other words, the second law is an expression for the efficiency of the perfect elementary engine. (Wood.) The living force, or vis viva, of a body (called heat) is always proportional to the absolute temperature of the body. (Trowbridge.)

The expression $\frac{Q_1 - Q_2}{Q_2} = \frac{T_1 - T_2}{T}$ may be called the symbolical or al-

gebraic enunciation of the second law,—the law which limits the efficiency of heat engines, and which does not depend on the nature of the working medium employed. (Trowbridge.) Q_1 and T_2 = quantity and absolute

temperature of the heat received, Q_2 and T_2 = quantity and absolute temperature of the heat rejected.

The expression $\frac{T_1 - T_2}{T_1}$ represents the efficiency of a perfect heat engine which receives all its heat at the absolute temperature T_1 , and rejects heat at the temperature T_2 , converting into work the difference between the quantity received and rejected.

EXAMPLE. - What is the efficiency of a perfect heat engine which receives heat at 388° F. (the temperature of steam of 200 lbs. gauge pressure) and rejects heat at 100° F. (temperature of a condenser, pressure 1 lb. above

vacuum).

$$\frac{388 + 459.2 - (100 + 459.2)}{388 + 459.2} = 34\%, \text{ nearly.}$$

In the actual engine this efficiency can never be attained, for the difference between the quantity of heat received into the cylinder and that rejected into the condenser is not all converted into work, much of it being lost by radiation, leakage, etc. In the steam engine the phenomenon of cylinder condensation also tends to reduce the efficiency.

PHYSICAL PROPERTIES OF GASES.

(Additional matter on this subject will be found under Heat, Air, Gas, and

When a mass of gas is enclosed in a vessel it exerts a pressure against the walls. This pressure is uniform on every square inch of the surface of the vessel; also, at any point in the fluid mass the pressure is the same in every direction.

In small vessels containing gases the increase of pressure due to weight may be neglected, since all gases are very light; but where liquids are con-cerned, the increase in pressure due to their weight must always be taken into account.

Expansion of Gases, Marriotte's Law.—The volume of a gas diminishes in the same ratio as the pressure upon it is increased.

This law is by experiment found to be very nearly true for all gases, and is known as Boyle's or Mariotte's law.

If p =pressure at a volume v_1 , and $p_1 =$ pressure at a volume v_1 , $p_1v_1 =$ $pv; p_1 = \frac{v}{v}p; pv = a \text{ constant.}$

The constant, C, varies with the temperature, everything else remaining the same.

Air compressed by a pressure of seventy-five atmospheres has a volume

Ar compressed by a pressure of seventy-rive atmospheres has a volume about \mathscr{X} less than that computed from Boyle's law, but this is the greatest divergence that is found below 160 atmospheres pressure.

Law of Charles.—The volume of a perfect gas at a constant pressure is proportional to its absolute temperature. If v_b be the volume of a gas at 32° F., and v_1 the volume at any other temperature, t_1 , then

$$v_1 = v_0 \left(\frac{t_1 + 459.2}{491.2} \right); \quad v_1 = \left(1 + \frac{t_1 - 32^\circ}{491.2} \right) v_0,$$
or
$$v_1 = [1 + 0.002036(t_1 - 32^\circ)] v_0.$$

If the pressure also change from p_0 to p_1 ,

$$v_1 = v_0 \frac{p_0}{p_1} \left(\frac{t_1 + 459.2}{491.2} \right).$$

The Densities of the elementary gases are simply proportional to their atomic weights. The density of a compound gas, referred to hydrogen as 1, is one-half its molecular weight; thus the relative density of CO_2 is $\frac{1}{12}(12 + 32) = 22.$

Avogadro's Law.—Equal volumes of all gases, under the same conditions of temperature and pressure, contain the same number of molecules.

To find the weight of a gas in pounds per cubic foot at 32° F., multiply half the molecular weight of the gas by .00559. Thus 1 cu. ft. marsh-gas, CH₄,

$$= \frac{1}{4}(12 + 4) \times .00559 = .0447 \text{ lb.}$$

When a certain volume of hydrogen combines with one half its volume of oxygen, there is produced an amount of water vapor which will occupy the same volume as that which was occupied by the hydrogen gas when at the

same temperature and pressure.

Saturation-point of Vapors.—A vapor that is not near the saturasaturation-point to a vapor size A vapor size in the saturation-point behaves like a gas under changes of temperature and pressure; but if it is sufficiently compressed or cooled, it reaches a point where it begins to condense; it then no longer obeys the same laws as a gas, but its pressure cannot be increased by diminishing the size of the vessel containing it, but remains constant, except when the temperature is changed. The only gas that can prevent a liquid evaporating seems to be its own vapor.

Dalton's Law of Gaseous Pressures.—Every portion of a mass of gas inclosed in a vessel contributes to the pressure against the sides of the vessel the same amount that it would have exerted by itself had no

other gas been present.

Mixtures of Vapors and Gases.—The pressure exerted against the interior of a vessel by a given quantity of a perfect gas enclosed in it is the sum of the pressures which any number of parts into which such quantity might be divided would exert separately, if each were enclosed in a vessel of the same bulk alone, at the same temperature. Although this law vessel of the same bulk alone, at the same temperature. Although this law is not exactly true for any actual gas, it is very nearly true for many. Thus if 0.080728 lb. of air at 32° F., being enclosed in a vessel of one cubic foot capacity, exerts a pressure of one atmosphere or 14.7 pounds, on each square inch of the interior of the vessel, then will each additional 0.080728 lb. of air which is enclosed, at 32°, in the same vessel, produce very nearly an additional atmosphere of pressure. The same law is applicable to mixtures of gases of different kinds. For example, 0.12344 lb. of carbonic-acid gas, at 32°, being enclosed in a vessel of one cubic foot in capacity, exerts a pressure of one atmosphere; consequently, if 0.080728 lb. of air and 0.12344 lb. of carbonic acid, mixed, be enclosed at the temperature of 32°, in a vessel of one cubic foot of capacity, the mixture will exert a pressure of two atmospheres. As a second example: Let 0.080728 lb. of air, at 212°, be enclosed in As a second example: Let 0.080728 lb. of air, at 212°, be enclosed in a vessel of one cubic foot; it will exert a pressure of

 $\frac{212+459.2}{32+459.2}$ = 1.366 atmospheres.

Let 0.03797 lb. of steam, at 212°, be enclosed in a vessel of one cubic foot; it will exert a pressure of one atmosphere. Consequently, if 0.080728 lb. of air and 0.08797 lb. of steam be mixed and enclosed together, at 212°, in a vessel of one cubic foot, the mixture will exert a pressure of 2.366 atmospheres. It is a common but erroneous practice, in elementary books on physics, to describe this law as constituting a difference between mixed and homogeneous gases; whereas it is obvious that for mixed and homogeneous gases the law of pressure is exactly the same, viz., that the pressure of the whole of a gaseous mass is the sum of the pressures of all its parts

This is one of the laws of mixture of gases and vapors.

A second law is that the presence of a foreign gaseous substance in con-

tact with the surface of a solid or liquid does not affect the density of the vapor of that solid or liquid unless there is a tendency to chemical combination between the two substances in which case the density of the vapor is slightly increased. (Rankine, S. E., p. 239.)

Flow of Gases. —By the principle of the conservation of energy, it may be shown that the velocity with which a gas under pressure will escape into a vacuum is inversely proportional to the square root of its density; that is, oxygen, which is sixteen times as heavy as hydrogen, would, under exactly the same circumstances, escape through an opening only one fourth as fast as the latter gas.

Absorption of Gases by Liquids.—Many gases are readily absorbed by water. Other liquids also possess this power in a greater or less degree. Water will for example, absorb its own volume of carbonic-acid gas, 430 times its volume of ammouia, 21/4 times its volume of chlorine, and

only about 1/20 of its volume of oxygen.

The weight of gas that is absorbed by a given volume of liquid is proportional to the pressure. But as the volume of a mass of gas is less as the pressure is greater, the volume which a given amount of liquid can absorb at a certain temperature will be constant, whatever the pressure. Water, for example, can absorb its own volume of carbonic-acid gas at atmospheric pressure; it will also dissolve its own volume if the pressure is twice as great, but in that case the gas will be twice as dense, and consequently twice the weight of gas is dissolved.

AIR.

Properties of Air.—Air is a mechanical mixture of the gases oxygen and nitrogen; 20.7 parts O and 79.3 parts N by volume, 23 parts O and 77 parts N by weight.

The weight of pure air at 32° F, and a barometric pressure of 29.9? inches of mercury, or 14.6963 lbs. per sq. in., or 2116.3 lbs. per sq. it., is. 060728 lb. per cubic foot. Volume of 1 lb. = 12.387 cu. ft. At any other temperature and barometric pressure its weight in lbs. per cubic foot is $W = \frac{1.3253 \times B}{459.2 + T}$, where B = height of the barometer, T = temperature Fahr., and 12.253 = weight in lbs. of 459.2 c. ft. of air at 0° F, and one inch barometric pressure. Air expands 1/491.2 of its volume at 32° F, for every increase of 1° F., and its volume varies inversely as the pressure.

Volume, Density, and Pressure of Air at Various Temperatures. (D. K. Clark.)

0 11 32 13 40 13 50 18 62 18 70 18 80 18 90 18 100 14 110 14 120 14	ic Feet	Compara- tive Vol.	per Cubic Foot at Atmos. Pressure.		
82 13 40 13 50 12 63 12 70 18 80 18 90 18 100 14 110 14 120 14 140 15		tive vot.		Lbs. per Sq. In.	Compara- tive Pres.
82 13 40 13 50 12 63 12 70 18 80 18 90 18 100 14 110 14 120 14 140 15	1.583	.881	.086381	12.96	.881
40 12 50 12 70 18 80 18 90 18 100 14 110 14 120 14 140 15	2.887	.943	.080728	13.86	.943
70 18 70 18 80 18 90 18 100 14 110 14 120 14 130 14	2.586	.958	.079439	14.08	.958
70 18 80 18 90 18 100 14 110 14 120 14 130 14	2.840	.977	.077884	14.36	.977
90 18 100 14 110 14 120 14 130 14 140 15	8.141	1.000	.076097	14.70	1.000
90 18 100 14 110 14 120 14 180 14 140 15	8.842	1.015	.074950	14.92	1.015
100 14 110 14 120 14 130 14	3.598	1.034	.073565	15.21	1.034
110 14 120 14 130 14 140 15	3.845	1.051	.072230	15.49	1.054
190 14 180 14 140 15	4.096	1.073	.070942	15.77	1.078
180 14 140 15	4.844	1.092	.069721	16.05	1.092
140 15	4.592	1.111	.069500	16.88	1.111
	4.846	1.180	.067361	16.61	1.130
150 I 15	5.100	1.149	.066221	16.89	1.149
	5.351	1.168	.065155	17.19	1.168
160 15	5.608	1.187	.064088	17.50	1.187
	5.864	1.206	.063089	17.76	1.206
	5.106	1.226	.062090	18.02	1.226
	6.696 i	1.264 1.283	.059318	18.58	1.264
210 16 212 16	6.860	1.287	.059185	18.86 18.92	1.288

The Air-manemeter consists of a long vertical glass tube, closed at the upper end, open at the lower end, containing air, provided with a scale, and immersed, shong with a thermometer, in a transparent liquid, such as water or oil, contained in a strong cylinder of glass, which communicates with the vessel in which the pressure is to be ascertained. The scale shows the volume occupied by the air in the tube.

Let v_0 be that volume, at the temperature of 32° Fahrenheit, and mean pressure of the atmosphere, p_0 ; let v_i be the volume of the air at the temperature t_i , and under the absolute pressure to be measured p_1 ; then

$$p_1 = \frac{(t + 459.2^{\circ})p_0v_0}{491.2^{\circ}v_1}.$$

Pressure of the Atmosphere at Different Altitudes.

At the sea-level the pressure of the air is 14.7 pounds per square inch; at % of a mile above the sea-level it is 14.02 pounds; at ½ mile, 18.33; at 9, mile, 12.66; at 1 mile, 12.62; at 1½ mile, 11.42; at 1½ mile, 10.65; and at 2

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miles, 9.80 pounds per square inch. For a rough approximation we may assume that the pressure decreases ½ pound per square inch for every 1000 feet of ascent.

It is calculated that at a height of about 3½ miles above the sea-level the weight of a cubic foot of air is only one half what it is at the surface of the earth, at seven miles only one fourth, at fourteen miles only one sixteenth, at twenty-one miles only one sixty-fourth, and at a height of over forty-five miles it becomes so attenuated as to have no appreciable weight.

The pressure of the atmosphere increases with the depth of shafts, equal to about one inch rise in the barometer for each 900 feet increase in depth: this may be taken as a rough-and-ready rule for ascertaining the depth of shafts.

Pressure of the Atmosphere per Square Inch and per Square Foot at Various Readings of the Barometer.

RULE.—Barometer in inches × .4908 = pressure per square inch; pressure per square inch × 144 = pressure per square foot.

Barometer.	Pressure per Sq. In.	Pressure per Sq. Ft.	Barometer.	Pressure per Sq. In.	Pressure per Sq. Ft.
in. 28.00 28.25 28.50 28.75 29.00 29.25 29.50	lbs. 13.74 13.86 13.98 14.11 14.28 14.35 14.47	lbs.* 1995 2013 2031 2049 2066 2083	in. 29.75 80.00 80.25 80.50 30.75 81.00	lbs. 14.60 14.72 14.84 14.96 15.09	lbs.* 2102 2119 2186 2154 2173 2190

* Decimals omitted.

For lower pressures see table of the Properties of Steam.

Barometric Beadings corresponding with Different Altitudes, in French and English Measures.

Alti- tude.	Read- ing of Earom- eter.	Altitude.	Reading of Barom- eter.	Alti- tude.	Reading of Barom- eter.	Altitude,	Reading of Barom- eter.
meters. 0 21 127 234 342 453 564 678 793 909 1027	mm. 762 760 750 740 730 720 710 700 690 680 670	feet. 0. 68.9 416.7 767.7 1122.1 1486.2 1850.4 2224.5 2599.7 2962.1 3369.5	inches. 30. 39.92 29.52 29.13 28.74 28.35 27.95 27.16 25.77 26.38	meters. 1147 1269 1393 1519 1647 1777 1909 2043 2180 2318 2460	mm. 660 650 640 630 620 610 600 590 580 570	feet. 3763.2 4163.8 4568.8 4963.1 5408.2 5830.2 6243. 6702.9 7152.4 7605.1 8071.	inches. 25.96 25.59 25.19 24.80 24.41 24.01 28.62 23.83 22.44 22.04

Levelling by the Barometer and by Boiling Water. (Trautwine.)—Many circumstances combine to render the results of this kind of levelling unreliable where great accuracy is required. It is difficult to read off from an aneroid (the kind of barometer usually employed for engineering purposes) to within from two to five or six feet, depending on its size. The moisture or dryness of the air affects the results; also winds, the vicinity of mountains, and the daily atmospheric tides, which cause incessant and irregular fluctuations in the barometer. A barometer hanging quietly in a room will often vary 1/4 of an inch within a few hours, corresponding to a difference of elevation of nearly 100 feet. No formula can possibly be devised that shall embrace these sources of error,

To Find the Difference in Altitude of Two Places.—Take from the table the altitudes opposite to the two boiling temperatures, or the two barometer readings. Subtract the one opposite the lower reading from that opposite the upper reading. The remainder will be the required height, as a rough approximation. To correct this, add together the two thermometer readings, and divide the sum by 2, for their mean. From table of corrections for temperature, take out the number under this mean. Multiply the approximate height just found by this number.

At 70° F. pure water will boil at 1° less of temperature for an average of about 550 feet of elevation above sea-level, up to a height of 1/2 a mile. At the height of 1 mile, 1° of boiling temperature will correspond to about 560 feet of elevation. In the table the mean of the temperatures at the two stations is assumed to be 32° F., at which no correction for temperature is necessary in using the table. To Find the Difference in Altitude of Two Places.—Take

necessary in using the table.

Bolling- point in deg. Fah.	Barom. fn.	Altitude above Sea-level, feet.	Bolling- point in deg. Fah.	Barom, in.	Altitude above Sea-level, feet.	Boiling- point in deg. Fab.	Barom. in.	Altitude above Sea-level, feet.
184° 195 186 187 188 189 190 191	16.79 17.16 17.54 17.98 18.32 18.72 19.13 19.54 19.96	15,221 14,649 14,075 13,498 12,984 12,367 11,799 11,243 10,685	196 197 198 190 200 201 202 203 204	21.71 22.17 22.64 23.11 23.59 24.08 24.58 25.08 25.59	8,481 7,982 7,381 6,843 6,804 5,764 5,225 4,697 4,169	208 208.5 209 209.5° 210 210.5 211 211.5 212	27.78 28.00 28.29 28.56 28.85 29.15 29.42 29.71 30.00	2,063 1,809 1,539 1,539 1,025 754 512 255 S, L. = 0
198 194 195	20.89 20.82 21.26	10,127 9,579 9,081	205 206 207	26.11 26.64 27.18	8,642 8,115 2,589	212.5 213	30.30 30.59	-261 -511

CORRECTIONS FOR TEMPERATURE.

Mean temp. F. in s Multiply by	hada Al Mai Ma	9001 400	KAO I KAO	1 700 181	no ione	1000
Mean comb. t. in a	Haue. 0 10-1 20-	10U MEU	100	1 10 10	0 80	100.
Multiply has	000 054 075	I DOGI 1 DIG	11 1028 11 1150	1 07011	100 1 101	1 1/0
atuinpiy uy	.000 .004 .010	1.990 1.010	1.000 1.000	11.010 1.	. 100 1.121	1.146

Moisture in the Atmosphere.—Atmospheric air always contains a small quantity of carbonic acid (see Ventilation, p. 528) and a varying quantity of aqueous vapor or moisture. The relative humidity of the air at any time is the percentage of moisture contained in it as compared with the amount it is capable of holding at the same temperature.

The degree of saturation or relative humidity of the air is determined by the use of the dry and wet bulb thermometer. The degree of saturation for a number of different readings of the thermometer is given in the following table condensed from the Hydrometric Tables of the U.S. Westher Bursay.

table, condensed from the Hygrometric Tables of the U.S. Weather Bureau:

RELATIVE HUMIDITY, PER CENT.

er.	Difference between the Dry and Wet Thermometers, Deg. F.
nomet Deg. F.	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 28 24 26 28
PER	Relative Humidity, Saturation being 100. (Barometer = 30 ins.)
32	89 79 69 59 49 39 30 20 11 2
40	92 83 75 68 60 52 45 37 29 23 15 7 0
50	93 87 80 74 67 61 55 49 43 38 32 27 21 16 11 5 0
60	94 89 83 78 78 68 63 58 53 48 43 39 34 30 26 21 17 18 9 5 1
70 80 90	95 90 86 81 77 72 68 64 59 55 51 48 44 40 36 38 29 25 22 19 15 12 9 6
80	96 91 87 83 79 75 72 68 64 61 57 54 50 47 44 41 38 35 32 29 26 23 20 18 12 7
90	96 92 89 85 81 78 74 71 68 65 61 58 55 52 49 47 44 41 39 36 34 31 29 26 22 17 1
100	96 93 89 86 83 80 77 73 70 68 65 62 59 56 54 51 49 46 44 41 39 37 35 33 28 24 2
110	97 93 90 87 84 81 78 75 73 70 67 65 62 60 57 55 52 50 48 46 44 42 40 88 34 30 2
120	97 94 91 88 85 82 80 77 74 72 69 67 65 62 60 58 55 53 51 49 47 45 43 41 38 34 3
140	97 95 92 89 87 84 82 79 77 75 73 70 68 66 64 62 60 58 56 54 53 51 49 47 44 41 3

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Weights of Air, Vapor of Water, and Saturated Mixtures of Air and Vapor at Different Temperatures, under the Ordinary Atmospheric Pressure of 29,921 inches of Mercury.

			incinca o				
	n it	F.	MIXTUE	RES OF AII	R SATURAT	ED WITH	APOR.
gʻ.	Cubic Ft. t Different res, 1bs.	force of Vapor, of Mercury.	Elastic Force of the Air in		of Cubic F of Air an	oot of the d Vapor.	Weight
Temperature, Fahrenheit. Weight of a Cul of Dry Air at Dif Temperatures,		Elastic Force Inches of M	Mixture of Airand Vapor, Inches of Mercury.	Weight of the Air, lbs.	Weight of the Vapor, pounds.	Total W'ght of Mixture, pounds.	Vapor mixed with 1 lb, of Air, pounds.
0° 12 22 32 42 52 62 72 82 102 1122 1322 1422	.0864 .0842 .0824 .0807 .0791 .0776 .0761 .0747 .0738 .0720 .0707 .0694 .0682 .0671 .0660	.044 .074 .118 .181 .267 .388 .556 .785 1.092 1.501 2.036 2.731 3.621 4.752 6.165	29.877 29.849 29.808 39.740 29.654 29.533 29.365 29.136 28.829 27.885 27.190 26.300 25.169 23.756	.0863 .0840 .0821 .0822 .0784 .0766 .0747 .0727 .0706 .0684 .0659 .0631 .0599 .0564 .0524	.000079 .000130 .000202 .000304 .000440 .000627 .000881 .001221 .001667 .002250 .002997 .003946 .005142 .006639 .008473 .001716	.086379 .084180 .082302 .080504 .077327 .077581 .073921 .072967 .070717 .068897 .067046 .065042 .063039 .060873 .058416	.00092 .00155 .00245 .00379 .00561 .00819 .01179 .01680 .02361 .08289 .04547 .06253 .08584 .11771 .16170 .22465
162 172 182	.0638 .0628 .0618	10.099 12.758 15.960	19.822 17.163 13.961	.0423 .0360 .0288	.013415 .016682 .020536	.055715 .052682 .049386	.31713 .46338 .71800
192 202 212	.0609 .0600 .0591	19.828 24.450 29.921	10.093 5.471 0.000	.0205 .0109 .0000	.025142 .030545 .036820	.045642 .041445 .036820	1.22643 2.80230 Infinite.

The weight in lbs. of the vapor mixed with 100 lbs. of pure air at any given temperature and pressure is given by the formula

$$\frac{62.3 \times E}{29.92 - E} \times \frac{29.92}{p}$$

where E = elastic force of the vapor at the given temperature, in inches of mercury, p = absolute pressure in inches of mercury, = 29.92 for ordinary atmospheric pressure.

Specific Heat of Air at Constant Volume and at Constant Pressure.—Volume of 1 lb. of air at 32° F. and pressure of 14.7 lbs. per sq. in. = 12.387 cu. ft. = a column 1 sq. ft. area × 12.387 ft. high. Raising temperature 1° F. expands it $\frac{1}{491.2}$, or to 12.4122 ft. high—a rise of .02522 foot.

Work done = 2116 lbs. per sq. ft. \times .02522 = 53.37 foot-pounds, or 53.37 + 778 = .0686 heat units.

The specific heat of air at constant pressure, according to Regnault, is 0.2375; but this includes the work of expansion, or .0686 heat units; hence the specific heat at constant volume = 0.2375 - .0686 = 0.1689.

Ratio of specific heat at constant pressure to specific heat at constant volume = .2375 + .1689 = 1.406. (See Specific Heat, p. 458.)

Flow of Air through Orifices.—The theoretical velocity in feet per second of flow of any fluid, liquid, or gas through an orifice is v = $\sqrt{2gh} = 8.02 \sqrt{h}$, in which h =the "head" or height of the fluid in feet required to produce the pressure of the fluid at the level of the orifice. (For gases the formula holds good only for small differences of pressure on the two sides of the orifice.) The quantity of flow in cubic feet per second

is equal to the product of this velocity by the area of the orifice, in square feet, multiplied by a "coefficient of flow," which takes into account the contraction of the vein or flowing stream, the friction of the orifice, etc. For air flowing through an orifice or short tube, from a reservoir of the pressure p_1 into a reservoir of the pressure p_2 . Weisbach gives the following values for the coefficient of flow, obtained from his experiments.

FLOW OF AIR THROUGH AN ORIFICE.

	Coefficient c in formula	$v = c \sqrt{2}$	Egh.			
Diameter	Ratio of pressures p_1+p_2	1.05 1.0	9 1.43	1.65	1.89	2.15
1 centimetre.	Coefficient	.555 .5	89 .692	.724	.754	.788
Diameter	Ratio of pressures	1.05 1.0	0 1.98	1 67	2.01	
	Coefficient					
a.14 Continuen ob	Coemcient	.000 .0	10 .001	.010		• • • •
	Wasan A	C	n			

FLOW OF AIR THROUGH A SHORT TUBE.

Diam. 1 cm.,	Ratio of pressures p_1+p_2 Coefficient	1.05	1.10	1.30		••••	
Length 3 cm.	Coefficient	.730	.771	.830	• • • •		••••
	Ratio of pressures						
Longth 4.242 cm.	Coefficient	.818	.822		• • • •	• • • • •	••••
Longth 1 6 am	Ratio of pressures	1.24	1.38	1.59	1.85	2.14	• • • •
Orifice rounded.	Ratio of pressures	.979	.986	.965	.971	.978	• • • •

FLIEGNER'S EQUATION FOR FLOW OF AIR FROM A RESERVOIR THROUGH AN ORIFICE. (Proc. Inst. C. E., lv, 379.)

$$G = (3465 - 10000D)F\sqrt{\frac{p_1^2 - p_0^2}{T}};$$

G = the flow in kilogrammes per second; p_1p_0 = the internal and external pressures in atmospheres of 10,000 kg, per sq. metre; D = diameter of the orifice in metres; F = its cross-section in sq. metres; T = absolute temperature, Centigrade, of the air in the reservoir. The experiments were made with six orifices from 3.17 to 11.86 mm. diameter, in brass plates 12 mm. thick, drilled cylindrically for about $\frac{1}{2}$ mm., and conically enlarged towards the outside et an explanation of $\frac{1}{2}$ m.

outside at an angle of 45°.

Clark (Rules, Tables, and Data, p. 891) gives, for the velocity of flow of air through an orifice due to small differences of pressure,

$$V = C \sqrt{\frac{2gh}{12} \times 773.2 \times \left(1 + \frac{t - 82}{493}\right) \times \frac{29.92}{p}},$$
 or, simplified,
$$V = 352 C \sqrt{\left(1 + .00203(t - 32)\frac{h}{p}\right)};$$

in which V = velocity in feet per second; 2g = 64.4; k = height of the column of water in inches, measuring the difference of pressure; t= the temperature Fahr.; and p= barometric pressure in inches of mercury. 773,2 is the volume of air at 32 under a pressure of 29.93 inches of mercury when that of an equal weight of water is taken as 1.

For 62° F., the formula becomes $V = 363C \sqrt{\frac{h}{c}}$, and if p = 29.92 inches V =

66.35C √ħ The coefficient of efflux C, according to Weisbach, is:

For conoidal mouthpiece, of form of the contracted vein, with pressures of from .23 to 1.1 atmospheres..... C = .97 to .99 with pressures of 170 m. 25 to 11 atmospheres. C = .56 to .79 Circular orifices in thin plates. C = .56 to .79 Short cylindrical mouthpieces. C = .81 to .84 The same rounded at the inner end C = .92 to .93 Conical converging mouthpieces C = .90 to .99

Flow of Air in Pipes.—Hawksley (Proc. Inst. C. E., xxxiii, 55) states that his formula for flow of water in pipes $v=48 \sqrt{\frac{\overline{HD}}{L}}$ may also

be employed for flow of air. In this case H = height in feet of a column ofair required to produce the pressure causing the flow, or the loss of head for a given flow; v= velocity in feet per second, D= diameter in feet, L= length in feet.

If the head is expressed in inches of water, h, the air being taken at 62° F., its weight per cubic foot at atmospheric pressure = .0761 lb. Then $H = \frac{62.86}{.0761 \times 12} = 68.3h$. If d = diameter in inches, $D = \frac{d}{19}$ and the formula

becomes $v = 114.5 \sqrt{\frac{\hbar d}{L}}$, in which h = inches of water column, d = diam-

eter in inches and L = length in feet; $h = \frac{Lv^2}{13110d}$; $d = \frac{Lv^2}{13110h}$.

The quantity in cubic feet per second is

$$Q = .7854 \frac{d^2}{144} v = .6245 \sqrt{\frac{h d^2}{L}}; \quad d = \sqrt[4]{\frac{Q^2 L}{.39h}}; \quad h = \frac{Q^2 L}{.39d^2}.$$

The horse-power required to drive air through a pipe is the volume Q in cubic feet per second multiplied by the pressure in pounds per square foot and divided by 550. Pressure in pounds per square foot = P = inches of water column \times 5.196, whence horse-power =

$$HP. = \frac{QP}{550} = \frac{Qh}{105.9} = \frac{Q^3L}{41.8d^3}$$

If the head or pressure causing the flow is expressed in pounds per square inch = p, then h = 27.71p, and the above formulæ become

$$v = 602.7 \sqrt{\frac{pd}{L}}; \quad p = \frac{Lv^3}{363,300d}; \quad d = \frac{Lv^3}{363,800p};$$

$$Q = 3.287 \sqrt{\frac{pd^5}{L}}; \quad p = \frac{Q^9L}{10.806d^5}; \quad d = \sqrt[5]{\frac{Q^9L}{10.806p}};$$

$$HP. = \frac{Q144p}{550} = .2618Qp = .02421 \frac{Q^3L}{d^5}.$$

/olume of Air Transmitted in Cubic Feet per Minute in Pipes of Various Diameters.

Formula
$$Q = \frac{.7854}{144}d^2v \times 60.$$

Veloc'y	Actual Diameter of Pipe in Inches.												
Feet p. sec	1	2	8	4	5	6	8	10	12	16	20	24	
1	.827	1.81	2,95		8.18		20.94	32.73	47.12		130.9	188.5	
3 4	.655	2.62			16.36			65,45	94.25		261.8	377	
3	.982	8.98			24.5	35.3	62.8	98.2	141.4	251,3	392,7	565.5	
	1.31		11.78		82.7	47.1	83.8	181	188	335	523	754	
5	1.64		14.7	26.2	41	59	104	163	235	419	654	942	
6	1.96		17.7	81.4	49.1	70.7	125	196	283	502	785	1131	
7	2,29		20.6	36,6	57.2	82.4	146	229	830	586	916	1319	
8	2.62	105	23.5	41.9	65.4	94	167	262	877	670	1047	1508	
9	2.95	11.78	26.5	47	78	106	188	294	424	754		1696	
10	3,27	18.1	29,4	52	83	118	209	327	471	838	1309	1885	
12	8,93	15.7	35.3	63	98	141	251	393	565	1005	1571	2262	
15	4.91	19.6	44.2	78	155	177	314	491		1256	1963	2827	
18	5,89	23.5	53	94	147	212	377	589		1508	2356	3393	
20	6.54	26.2	59	105	164	235	419	654	942	1675	2618	3770	
24	7.85	31.4	71	125	196	288	502	785		2010	3141	4524	
25	8.18	32,7	73	131	204	294	528	818	1178	2094	3272	4712	
28	9.16	36.6	82	146	229	330	586	916	1319	2346	3665	5278	
30	9.8	39,3	88	157	245	353	628	982	1414	2513	3927	5655	

In Hawksley's formula and its derivatives the numerical coefficients are constant. It is scarcely possible, however, that they can be accurate except within a limited range of conditions. In the case of water it is found that the coefficient of friction, on which the loss of head depends, varies with the length and diameter of the pipe, and with the velocity, as well as with the condition of the interior surface. In the case of air and other gases we have, in addition, the decrease in density and consequent increase in volume and in velocity due to the progressive loss of head from one end of the pipe to the other.

'Clark states that according to the experiments of D'Aubuisson and those of a Sardinian commission on the resistance of air through long conduits or pipes, the diminution of pressure is very nearly directly as the length, and as the square of the velocity and inversely as the diameter. The resistance is not varied by the density.

not varied by the density.

If these statements are correct, then the formulæ $h = \frac{Lv^2}{cd}$ and $h = \frac{Q^2L}{c'd^3}$ and their derivatives are correct in form, and they may be used when the numerical coefficients c and c' are obtained by experiment.

If we take the forms of the above formulæ as correct, and let C be a variable acceptations.

It we take the forms of the above formings as correct, and let C be a variable coefficient, depending upon the length, diameter, and condition of surface of the pipe, and possibly also upon the velocity, the temperature and the density, to be determined by future experiments, then for k = head in inches of water, d = diameter in inches, L = length in feet, v = velocity in feet per second, and Q = quantity in cubic feet per second:

$$v = C \sqrt{\frac{hd}{L}};$$
 $d = \frac{Lv^2}{C^2h};$ $h = \frac{Lv^2}{C^2d};$ $Q = .005454C \sqrt{\frac{hd^5}{L}};$ $d = \sqrt[4]{\frac{33663Q^2L}{C^2h}};$ $h = \frac{38683Q^2L}{C^2d^5}.$

For difference or loss of pressure p in pounds per square inch.

$$\begin{split} h &= 27.71p & \sqrt{h} = 5.264 \sqrt{p}; \\ v &= 5.264 C \sqrt{\frac{pd}{L}}; & d &= \frac{Lv^2}{27.71C^2p}; & p &= \frac{Lv^2}{27.71C^2d}; \\ Q &= .02871 C \sqrt{\frac{pd^3}{L}}; & d &= \sqrt[4]{\frac{1218Q^2L}{C^2p}}; & p &= \frac{1218Q^2L}{C^2d^3}. \end{split}$$

(For other formulæ for flow of air, see Mine Ventilation.)

Loss of Pressure in Ounces per Square Inch.-B. F. Sturtevant Company uses the following formulæ:

$$p_1 = \frac{Lv^2}{25000d}$$
; $v = \sqrt{\frac{25000dp_1}{L}}$; $d = \frac{Lv^2}{25000p_1}$;

in which $p_1 =$ loss of pressure in ounces per square inch, v =velocity of air in feet per second, and L =length of pipe in feet. If p is taken in pounds per square inch, these formulæ reduce to

$$p = .0000025 \frac{Lv^3}{d}; \quad v = 632.5 \sqrt{\frac{dp_1}{L}}; \quad d = \frac{.0000025 Lv^2}{p}.$$

These are deduced from the common formula (Weisbach's), $p = f \frac{l}{d} \frac{v^2}{2a}$, in which f = .0001608.

The following table is condensed from one given in the catalogue of B. F.

Sturtevant Company.

Loss of pressure in pipes 100 feet long, in ounces per square inch. For any other length, the loss is proportional to the length.

Air,				Dian	neter o	of Pipe	in In	ches.			0	
Velocity of Air feet per min.	1	2	3	4	5	6	7	8	9	10	11	19
Veloc				Los	s of Pr	essure	in O	unces				
600 1200 1800 2400 3000 3600 4200 4800 6000		.200 .800 1.800 3.200 5. 7.2 9.8 12.8 20.	.133 .533 1,200 2,133 3,333 4.8 6,553 8,533 13,388	-	.080 .320 .720 1.280 2. 2.88 3.92 5.12 8.0	_	5.714	2.45 3.2 5.0	.044 ,178 ,400 ,711 1.111 1.6 2.178 2.844 4.444	.040 .169 .360 .640 1.000 1.44 1.96 2.56 4.0	.036 .145 .327 .582 .909 1.309 1.782 2.327 3.636	.033 .183 .300 .533 .833 1.200 1.633 2.138 8.333
	14	16	18	20	23	24	28)	32	36	40	44	48
				Los	s of Pr	essure	in O	inces.				
600 1200 1800 2400 3600 4200 4800	.029 .114 .257 .457 1.029 1.400 1.829 2.857	.026 .100 .225 .400 .900 1.225 1.600 2.500	.022 .089 .200 .356 .800 1.089 1.422 2.222	.020 .080 .180 .320 .720 .980 1.280 2.000	.018 .073 .164 .291 .655 .891 1.164 1.818	.017 .067 .156 .267 .600 .817 1.067	.014 .057 .129 .239 .514 .700 .914	.012 .050 .112 .200 .450 .612 .800 1 .250	.011 .044 .100 .178 .400 .544 .711	.010 .040 .090 .160 .360 .490 .640	.009 .036 .082 .145 .327 .445 .582	.008 .033 .075 .133 .300 .408 .533 .833

Effect of Bends in Pipes. (Norwalk Iron Works Co.)

Radius of elbow, in diameter of pipe = 5 3 2 11/6 11/4 1 3/4 1 Equivalent lgths. of straight pipe, diams 7.85 8.24 9.03 10.36 12.72 17.51 36.09 121.2

Compressed-air Transmission. (Frank Richards, Am. Mach., March 8, 1894)—The volume of free air transmitted may be assumed to be directly as the number of atmospheres to which the air is compressed. Thus, if the air transmitted be at 75 pounds gauge-pressure, or six atmospheres, the volume of free air will be six times the amount given in the table (page 486). It is generally considered that for economical transmission the velocity in main pipes should not exceed 20 feet per second. In the smaller distributing pipes the velocity should be decidedly less than this. The loss of power in the transmission of compressed air in general is not

a serious one, or at all to be compared with the losses of power in the operation of compression and in the re-expansion or final application of the air. The formulas for loss by friction are all unsatisfactory. The statements

of observed facts in this line are in a more or less chaotic state, and selfevidently unreliable.

A statement of the friction of air flowing through a pipe involves at least all the following factors: Unit of time, volume of air, pressure of air, diamthe pipe or the head required to maintain the flow. Neither of these factors can be allowed its independent and absolute value, but is subject to modifican be allowed as independent and absolute value, but is subject to modinacations in deference to its associates. The flow of air being assumed to be uniform at the entrance to the pipe, the volume and flow are not uniform after that. The air is constantly losing some of its pressure and its volume is constantly increasing. The velocity of flow is therefore also somewhat accelerated continually. This also modifies the use of the length of the pipe as a constant factor.

Then, besides the fluctuating values of these factors, there is the condition of the pipe itself. The actual diameter of the pipe, especially in the smaller sizes, is different from the nominal diameter. The pipe may be straight, or it may be crooked and have numerous elbows. Mr. Richards

considers one elbow as equivalent to a length of pipe.

Formulæ for Flow of Compressed Air in Pipes.—The formulæ on pages 485 and 487 are for air at or near atmospheric pressure. For compressed air the density has to be taken into account. A common formula for the flow of air, gas, or steam in pipes is

$$Q = c \sqrt{\frac{pd^{5}}{wL}},$$

in which Q= volume in cubic feet per minute, p= difference of pressure in lbs, per sq. in. causing the flow, d= diameter of pipe in in., L= length of pipe in tt., w= density of the entering gas or steam in lbs per cu. tt., and c= a coefficient found by experiment. Mr. F. A. Halsey in calculating a table for the Rand Drill Co's Catalogue takes the value of c at 58, basing it upon the experiments made by order of the Italian government preliminary to boring the Mt. Cenis tunnel. These experiments were made with pipes of 3231 feet in length and of approximately 4, 8, and 14 in. diameter. The volumes of compressed air passed ranged between 16.64 and 1200 cu. ft. per minute. The value of c is quite constant throughout the range and shows little disposition to change with the varying diameter of the pipe. It is of course probable, says Mr. Halsey, that c would be smaller if determined for smaller sizes of pipe, but to offset that the actual sizes of small commercial pipe are considerably larger than the nominal sizes, and as these calculations are commonly made for the nominal diameters it is probable that in those small sizes the loss would really be less than shown by the table. The formula is of course strictly applicable to fluids which do not change their density, but within the change of density admissible in the transmission of air for power purposes it is probable that the errors introduced by this change are less than those due to errors of observation in the present state of knowledge of the subject. Mr. Halsey's table is condensed below.

Pipe,	Cu	bic fee			compr throu				essure inute.	of 80	lbs.
Diameter of Pipe, in inches.	50	100	200	400	800	1000	1500	2000	3000	4000	5000
Diame in in		Loss	of pres	sure i	n lbs. p of st	er squ raight	are in pipe.	ch for	each 1	000 ft.	
114 114 2 2 2 3 8 4 5 6 8 10 12 14	8.61 1.45 0.20 0.12	5.8 1.05 0.35 0.14	4.80 1.41 0.57 0.26 0.14	5.80 2.28 1.05 0.54 0.18	4.16 2.12 0.68 0.28 0.07	6.4 8.27 1.08 0.43 0.10	7.60 2.43 1.00 0.24 0.08	4.32 1.75 0.42 0.14	9.6 3.91 0.93 0.30 0.12	7.10 1.68 0.55 0.22 0.10	10.7 2.59 0.84 0.16

To apply the formula given above to air of different pressures it may be given other forms, as follows:

Let Q = the volume in cubic feet per minute of the compressed air; $Q_1 =$ the volume before compression, or "free air," both being taken at mean atmospheric temperature of 62° F; $w_1 =$ weight per cubic foot of $Q_1 =$ 0.076! b.; r = atmospheres, or ratio of absolute pressures, = (gauge-pressure + 14.7) + 14.7; w = weight per cu. ft. of Q; p = difference of pressure, in lbs. per sq. in., causing the flow; d = diam. of pipe in in.; L = length of pipe in ft.; c = experimental constant. Then

$$Q = c\sqrt{\frac{pd^{5}}{vL}}; \qquad Q_{1} = rQ; \qquad w = rrr_{1} = .0761r;$$

$$Q = 3.625c\sqrt{\frac{pd^{5}}{rL}}; \qquad Q_{1} = 5.625c\sqrt{\frac{pd^{5}r}{L}};$$

$$d = \sqrt[6]{.0761\frac{LQ^{2}r}{c^{2}p}} = 0.597\sqrt[6]{\frac{LQ^{2}r}{c^{2}p}} = \sqrt[6]{.0761\frac{LQ_{1}^{2}}{c^{2}pr}} = 0.597\sqrt[6]{\frac{LQ_{1}^{2}}{c^{2}pr}};$$

$$p = .0761\frac{LQ^{2}r}{c^{2}d^{5}} = .0761\frac{LQ_{1}^{2}}{c^{2}d^{5}}.$$

The value of c according to the Mt. Cenis experiments is about 58 for pipes 4, 8, and 14 in. diameter, 3281 ft. long. In the St. Gothard experiments it ranged from 62.8 to 78.2 (see table below) for pipes 5.91 and 7.87 in. diameter, 1713 and 15,092 ft. long. Values derived from D'Arcy's formula for flow of water in pipes, ranging from 45.3 for 1 in. diameter to 63.2 for 24 in., are given under "Flow of Steam," p. 671. For approximate calculations the value 60 may be used for all pipes of 4 in. diameter and upwards. Using c=60, the above formulæ become

$$Q = 217.5 \sqrt{\frac{pd^{5}}{rL}};$$
 $Q_{1} = 217.5 \sqrt{\frac{pd^{5}r}{L}};$
$$[d = 0.1161 \sqrt[6]{\frac{\overline{LQ^{2}r}}{p}} = 0.1161 \sqrt[6]{\frac{\overline{LQ_{1}^{2}}}{p^{r}}};$$

$$p = 0.00002114 \frac{\overline{LQ^{2}r}}{d\delta} = 0.00002114 \frac{\overline{LQ_{1}^{2}}}{r^{2}}.$$

Loss of Pressure in Compressed Air Pipe-main, at St. Gothard Tunnel.

(E. Stockalper.)

				٠,	D. Divi	Laipe	٠.,				
	eter.	second or equi- ime at c pres-	second sed air nsity.	of Bir.	d-	_ <u></u>	Obse	rved 1	Pressu	res.	nula
Experiment.	. Main Diameter	olume per seco of free air. or eq valent volume atmospheric pr sure and 32° F.	ompres mean de	density pressed ter = 1.)	Weight of air flow ing per second.	ean velocity in feet per second	Pressure at beginning of pipe.	Pressure at end of pipe.	Loss Press	of sure.	$= c \sqrt{\frac{pd^6}{wL}}.$
	Air	20 2 E E	Volu e f	Mean com (Wa	Wei	Mean feet	Pre be pi	Pre			Value Q=
									lbs. per		
No.	in.	cu.ft.	cu.ft.	den.	lbs.	feet.	at.	at.	sq.in.	*	1
1}	7.87 5.91	83.056	6.534 7.063	.00650	2.669 2.669	19.32 37.14	5.60 5.24	5.24 5.00	5.292 3.528	6.4 4.6	73.2
ازه	7.87	22.002	5.509	.00514	1.776	16.30	4.35	4.18	8.234	5.1	63.9 70.7
~ / /	5.91	} 22.002 {	5.863	.00482	1.776		4.18 i				
8	7.87 5.91	18.364	5,262 5,580	.00449	1.483 1.483	15.58	3.84	8.65	2.793	5.0	67.6
- 9	J. 81	, (0.000	.00425	1.485	29.34	8.65	8.54	1.617	8.0	62.8
	!										

The length of the pipe 7.87 in diameter was 15,092 ft., and of the smaller pipe 1712.6 ft. The mean temperature of the air in the large pipe was 70° F, and in the small pipe 80° F.

Equation of Pipes.—It is frequently desired to know what number of pipes of a given size are equal in carrying capacity to one nipe of a larger size. At the same velocity of flow the volume delivered by two pipes of different sizes is proportional to the squares of their diameters; thus, one 4-inch pipe will deliver the same volume as four 2-inch pipes. With the same head, however, the velocity is less in the smaller pipe, and the volume delivered varies about as the square root of the fifth power (i.e., as the 2.5 power). The following table has been calculated on this basis. The figures opposite the intersection of any two sizes is the number of the smaller-sized pipes required to equal one of the larger. Thus, one 4-inch pipe is equal to 5.7 2-inch pipes.

Diam.	1	2	3	4	5	6	7	8	9	10	12	14	16	18	20	24
2 3	5.7	1 2.8														
4	15.6	5.7	2.1	4							111			1		
5	55.9		3.6	1.7	1											
6	88.2		5.7	2.8	1.6	1									- 1	
7	130	22.9	8.3	4.1	2.3	1.5	1	0.5								
Ř	181	32	11.7	5.7	3.2	2.1	1.4	1								
8 9	248	43.	15.6		4.3	2.8	1.9	1.3	1	1				0.0		
10	216				5.7	3.6	2.4	1.7	1.8	1	(I					
11	401	70.9		12.5		4.6	3.1	2.2	1.7	1.3	100	m		. 11		
12 18	499	88.2	32	15.6		5.7	3.8	2.8	2.1	1.6	1			14		
18	609	108	39.1	19	10.9	7.1	4.7	8.4	2.5	1.9	1,2	1				
14	733	130	47	22.9	13.1	8.3	6.7	4.1	3.0	2.3	1.5	1				
15	871	154	55.9	27.2	15.6	9.9	6.7	4.8	3.6	2.8	1.7	1.2			1	
16	Na.	181	65.7	32	18.3	11.7	7.9	5.7	4.2	3.2	2.1	1.4	1			
17		211	76.4	37.2	21.3		9.2	6.6	4.9	3.8	2.4	1.6	1.2			
18		243	88.2	43	24.6	15.6	10.6	7.6	5.7	4.3	2.8	1.9	1.3	1		
17 18 19		278	101	49.1	28.1	17.8	12.1	8.7	6.5	5	3.2	2.1	1.5	1.1		
20		316	115		32	20.3	13.8	9.9	7.4	5.7	3.6	2.4	1.7	1.3	1	
20		401	146	70.9	40.6	25.7	17.5	12.5	9.3	7.2	4.6	3.1	2.2	1.7	1.3	1
24	Jees.	499	181	88.2		32	21.8	15.6	11.6	8.9	5.7	3.8		2.1	1.6	1
26		609	221	108	61.7	39.1	26.6	19.	14.2	10.9	7.1	4.7	8.4	2.5	1.9	1.2
28		733	266	130	74.2	47	32	22.9	17.1	13.1	8.3	5.7	4.1	3	2.3	1.5
30	244	871	316	154	88.2		38		20.3	15.6	9.9	6.7	4.8		2.8	1.7
36	110		499	243	130		60	43	32	24.6	15.6	10.6	7.6		4.8	2.8
42	11	15.98	733	357	205	130	88.2		47	36.2	19	15.6	11.2	8.8	6.4	4.1
48	Acres 1	200	2500	499	286	181	123	88.2	62.7	50.5	35	21.8		11.6		5.7
20 22 24 26 28 30 36 42 48 54 60	+++	1 31	100	670	383	243	165			67.8		23.2		15.6	12	7.6
60	Line		-	871	499	316	215	154	115	88.2	55.9	38	27.2	20.3	15.6	9.9

Measurement of the Velocity of Air in Pipes by an Anemometer,—Tests were made by B. Donkin, Jr. (Inst. Civil Engrs. 1892), to compare the velocity of air in pipes from 8 in, to 24 in, diam., as shown by an anemometer 234 in. diam. with the true velocity as measured by the time of descent of a gas-holder holding 1622 cubic feet. A table of the results with discussion is given in Eng'g News, Dec. 22, 1892. In pipes from 8 in. to 20 in. diam. with air velocities of from 140 to 690 feet per minute the anemometer showed errors varying from 14.5% fast to 10% slow. With a 24-inch pipe and a velocity of 73 ft. per minute, the anemometer gave from 44 to 63 feet, or from 13.6 to 39.6% slow. The practical conclusion drawn from these experiments is that anemometers for the measurement of velocities of air in pipes of these diameters should be used with great caution. The percentage of error is not constant, and varies considerably with the diameter of the pipes and the speeds of air. The use of a baffle, consisting of a perforated plate, which tended to equalize the velocity in the centre and at the sides in some cases diminished the error.

The impossibility of measuring the true quantity of air by an anemometer held stationary in one position is shown by the following figures, given by Wm. Daniel (Proc. Inst. M. E., 1875), of the velocities of air found at different points in the cross-sections of two different airways in a mine.

DIFFERENCES OF ANEMOMETER READINGS IN AIRWAYS.

	8 ft. sq	uare.	
1712	1795	1859	1329
1622	1695	1782	1091
1477	1844	1524	1049
1262	1856	1293	1333

Average	e 1469.	

	5 × 8 ft.										
1170	1209	1288									
948	1104	1177									
1134	1049	1106									

Average 1182.

WIND.

Force of the Wind.—Smeaton in 1759 published a table of the velocity and pressure of wind, as follows:

VELOCITY AND FORCE OF WIND, IN POUNDS PER SQUARE INCH.

			ND 1 01001 01 11111111			7 4920 1	ACT 10:11
Miles per hour.	Feet per second.	Force per sq. ft. pounds.	Common Appella- tion of the Force of Wind.	Miles per Hour.	Feet per second.	Force per sq. ft. pounds.	Common Appella- tion of the Force of Wind.
1 2 3 4 5 6 7 8 9 10 12 14 15 16	1.47 8.93 4.4 5.87 7.83 8.8 10.25 11.75 18.2 14.67 17.6 90.5 22.00 23.45	0.044 0.079 0.123 0.177 0.241 0.315 0.400 0.492 0.708 0.964	Just perceptible. Gentle pleasant wind. Pleasant brisk gale.	20	80.7 88.02 95.4 102.5	3.075 4.429 6.627 7.873 9.963 12.80 14.9 17.71 20.85 24.1 27.7 81.49	Very brisk. High wind. Very high storm. Great Storm. Hurricane. Immense hurricane.

The pressures per square foot in the above table correspond to the formula $P=0.005\,V^{\circ}$, in which V is the velocity in miles per hour. Engly News, Feb. 9, 1838, says that the formula was never well established, and has floated chiefly on Smeaton's name and for lack of a better. It was put forward only for surfaces for use in windmill practice. The trend of modern evidence is that it is approximately correct only for such surfaces, and that for large solid bodies it often gives greatly too large results. Observations by others are thus compared with Smeaton's formula:

Old Smeaton formula $P =$.005 778
As determined by Prof. Martin $P =$.004 P3
" Whipple and Dines $P =$.002977

At 60 miles per hour these formulas give for the pressure per square foot, 18, 14.4 and 10.44 ibs., respectively, the pressure varying by all of them as the square of the velocity. Lieut. Crosby's experiments (Bug'g, June 18, 1890), claiming to prove that P = fV instead of $P = fV^2$, are discredited. A. R. Wolff (The Windmill as a Prime Mover, p. 9) gives as the theoretical pressure per sq. ft. of surface, $P = \frac{dQv}{a}$, in which d = density of air in pounds $\frac{.018748(p+P)}{r}$; p being the barometric pressure per square foot at any level, and temperature of 33° F., t any absolute temperature. Q =volume of air carried along per square foot in one second, v =velocity dv^a of the wind in feet per sec., y = 82.18. Since Q = v cu. ft. per sec., P =Multiplying this by a coefficient 0.98 found by experiment, and substituting 0.017431 × p t × 33.16 ___,018 the above value of d, he obtains P = -—, and when o

= 2116.5 lbs. per sq. ft. or average atmospheric pressure at the sea-level, 86.8929 $P = \frac{1}{t \times 32.16}$ -, an expression in which the pressure is shown to vary

with the temperature; and he gives a table showing the relation between velocity and pressure for temperatures from 0° to 100° F., and velocities velocity and pressure for temperatures from 0° to 100° F., and velocities from 1 to 80 miles per hour. For a temperature of 45° F. the pressures agree with those in Smeaton's table, for 0° F. they are about 10 per cent greater, and for 100° 10 per cent less. Prof. H. Allen Hazen, Engly News, July 5, 1890, says that experiments with whirling arms, by exposing plates to direct wind, and on locomotives with velocities running up to 40° miles per hour, have invariably shown the resistance to vary with V^3 . In the formula $P = .9055 V^3$, in which P = pressure in pounds, S = surface in square feet, V = velocity in miles per hour, the doubtful question is that regarding the accuracy of the first two factors in the second member of this equation. The first factor has been variously determined from .03 ft. 0.05 ft has been

The first factor has been variously determined from .003 to .005 [It has been determined as low as .0014.—Ed. Eng'g News].

The second factor has been found in some experiments with very short whirling arms and low velocities to vary with the perimeter of the plate, but this entirely disappears with longer arms or straight line motion, and the only question now to be determined is the value of the coefficient. Perhaps some of the best experiments for determining this value were tried in France in 1886 by carrying flat boards on trains. The resulting formula in this case was, for 44.5 miles per hour, p = .00558547.

Mr. Crosby's whirling experiments were made with an arm 5.5 ft. long.

It is certain that most serious effects from centrifugal action would be set up by using such a short arm, and nothing satisfactory can be learned with arms less than 20 or 30 ft. long at velocities above 5 miles per hour.

Prof. Kernot, of Melbourne (Engineering Record, Feb. 20, 1894), states that

experiments at the Forth Bridge showed that the average pressure on surfaces as large as railway carriages, houses, or bridges never exceeded two thirds of that upon small surfaces of one or two square feet, such as have been used at observatories, and also that an inertia effect, which is frequently overlooked, may cause some forms of anemometer to give false results enormously exceeding the correct indication. Experiments of Mr. O. T. Crosby showed that the pressure varied directly as the velocity, whereas all the early investigators, from the time of Smeaton onwards, made it vary as the square of the velocity. Experiments made by Prof. Kernot at speeds varying from 2 to 15 miles per hour agreed with the earlier authorities, and tended to negative Crosby's results. The pressure upon one side of a cube, or of a block proportioned like an ordinary carriage, was found to be 9 of that upon a thiu plate of the same area. The same result was obtained for a square tower. A square pyramid, whose height was three times its base, experienced .8 of the pressure upon a thin plate equal to one of its sides, but if an angle was turned to the wind the pressure was increased by fully 20%. A bridge consisting of two plate-girders connected by a deck at the top was found to experience 9 of the pressure on a thin plate equal in size to one girder, when the distance between the girders was equal to their depth, and this was increased by one fifth when the distance between the girders was 494 AIR.

double the depth. A lattice-work in which the area of the openings was 55% of the whole area experienced a pressure of 80% of that upon a plate of the same area. The pressure upon cylinders and cones was proved to be equal to half that upon the diametral planes, and that upon an octagonal prism to be 20% greater than upon the circumscribing cylinder. A sphere was subject to a pressure of .86 of that upon a thin circular plate of equal diameter. A hemispherical cup gave the same result as the sphere; when its concavity was turned to the wind the pressure was 1.15 of that on a flat plate of equal diameter. When a plane surface parallel to the direction of the wind was brought nearly into contact with a cylinder or sphere, the pressure on the latter bodies was augmented by about 20%, owing to the lateral escape of the air being checked. Thus it is possible for the security of a tower or chimney

to be impaired by the erection of a building nearly touching it on one side.

Pressures of Wind Registered in Storms.—Mr. Frizell has examined the published records of Greenwich Observatory from 1849 to 1869, and reports that the highest pressure of wind he finds recorded is 41 lbs. per sq. ft., and there are numerous instances in which it was between 30 and 40 lbs. per sq. ft. Prof. Henry says that on Mount Washington, N. H., a velocity of 150 miles per hour has been observed, and at New York 150 miles an hour, and that the highest winds observed in 1870 were of 72 and 63

miles per hour, respectively.

Lieut. Dunwoody, U.S. A., says, in substance, that the New England coast is exposed to storms which produce a pressure of 50 lbs. per sq. ft. Engineering News, Aug. 20, 1880.

WINDMILLS.

Power and Efficiency of Windmills.—Rankine, S. E., p. 215, gives the following: Let $Q = \text{volume of air which acts on the sail, or part of a sail, in cubic feet per second, <math>v = \text{velocity of the wind in feet per second, } s = \text{sectional area of the cylinder, or annular cylinder of wind, through which the sail, or part of the sail, sweeps in one revolution, <math>c = \mathbf{a}$ coefficient to be found by experience; then Q = cvs. Rankine, from experience by Smeath and taking c to include an allowance for mental data given by Smeaton, and taking c to include an allowance for friction, gives for a wheel with four sails, proportioned in the best manner, c = 0.75. Let $A = \text{weather angle of the sail at any distance from the axis, i.e., the angle the portion of the sail considered makes with its plane of$ revolution. This angle gradually diminishes from the inner end of the sail to the tip; u= the velocity of the same portion of the sail, and E= the efficiency. The efficiency is the ratio of the useful work performed to whole energy of the stream of wind acting on the surface s of the wheel, which energy is $\frac{Dsv^s}{2g}$, D being the weight of a cubic foot of air. Rankine's formula for efficiency is

$$E = \frac{Ru}{\frac{Dsv^3}{v}} = c \left\{ \frac{u}{v} \sin 2A - \frac{u^2}{v^2} \left(1 - \cos 2A + f \right) - f \right\},$$

in which c=0.75 and f is a coefficient of friction found from Smeaton's data = 0.016. Rankine gives the following from Smeaton's data:

Rankine gives the following as the best values for the angle of weather at different distances from the axis:

Distance in sixths of total radius... 18• Weather angle.....

But Wolff (p. 125) shows that Smeaton did not term these the best angles, but simply says they "answer as well as any," possibly any that were in existence in his time. Wolff says that they "cannot in the nature of things be the most desirable angles." Mathematical considerations, he says, conclusively show that the angle of impulse depends on the relative velocity of each point of the sail and the wind, the angle growing larger as the ratio becomes greater. Smeaton's angles do not fulfil this condition. Wolff developments

ops a theoretical formula for the best angle of weather, and from it calculates a table for different relative velocities of the blades (at a distance of one seventh of the total length from the centre of the shaft) and the wind, from which the following is condensed:

Ratio of the	Dis	tance	e fro	m tl	10 83	is of	the	wh	eel i	n se	entl	18 O	' rad	lius.
Speed of Blade at 1/7 of Radius to Velocity of Wind.		1		2		3	1	•		3	1	3		7
***************************************					Bes	t an	gles	of w	eath	er.		•	•	
0.10 0.15	42° 40	9' 44	89°	21' 39	36°	89' 53	34° 29	6' 31	81° 26	43' 84	29°	81'	97° 21	30' 48
0.15 0.20 0.25	89 37	21 59	84 36	6 43	29 26	81 84	25 22	40 30	22 19	30 20	19	54 51	17	46 52
0.30 0.35	36 35	89 21	29 27	81 80	24 21	0 48	19 17	54 46	16 14	51 52	14 12	32 44	12 11	44
0.40 0.45 0.50	34 32 31	6 58 43	25 24 22	40 0 30	19 18 16	54 16 51	16 14 13	0 32 17	18 11 10	17 59 54	11 10 9	19 10 13	8 7	50 48 58

The effective power of a windmill, as Smeaton ascertained by experiment. varies as s, the sectional area of the acting stream of wind; that is, for simi-

lar wheels, as the squares of the radii. The value 0.75, assigned to the multiplier c in the formula Q = cvs, is rine value 0.70, assigned to the multiplier c in the formula Q = cvs, assortance by Smeaton, that the effective power of a windmill with sails of the best form, and about 15\(\frac{1}{2}\) ft. radius, with a breeze of 13 ft. per second, is about 1 horse-power. In the computations founded on that fact, the mean angle of weather is made = 18°. The efficiency of this wheel, according to the formula and table given, is 0.29, at its best speed, when the tips of the sails move at a velocity of 2.6 times that of the wind.

Merivale (Notes and Formulæ for Mining Students), using Smeaton's coefficient of efficiency, 0.29, gives the following:

 U = units of work in foot lbs. per sec.;
 W = weight, in pounds, of the cylinder of wind passing the sails each second, the diameter of the cylinder being equal to the diameter of the sails:

V = velocity of wind in feet per second;

H.P. = effective horse-power 0.29 WV $\mathcal{U} = \frac{77}{64}; \text{ H.P.} =$ 64 × 550°

A. R. Wolff, in an article in the American Engineer, gives the following (see also his treatise on Windmills):

Let c =velocity of wind in feet per second;

n = number of revolutions of the windmill per minute;

 b_0 , b_1 , b_2 , b_3 be the breadth of the sail or blade at distances l_0 , l_1 , l_2 ,

la. and l, respectively, from the axis of the shaft;

 l_0 = distance from axis of shaft to beginning of sail or blade proper; l = distance from axis of shaft to extremity of sail proper; $v_0, v_1, v_2, v_3, v_x =$ the velocity of the sail in feet per second at dis-

tances l_0 , l_1 , l_2 , l, respectively, from the axis of the shaft; a_0 , a_1 , a_2 , a_3 , a_2 = the angles of impulse for maximum effect at dis-

tances l_0 , l_1 , l_2 , l_3 , l respectively from the axis of the shaft; a = the angle of impulse when the sails or blocks are plane surfaces, so that there is but one angle to be considered;

N =number of sails or blades of windmill; K = .93.

d = density of wind (weight of a cubic foot of air at average temperature and barometric pressure where mill is erected);

W = weight of wind-wheel in pounds;
 f = coefficient of friction of shaft and bearings;

 \dot{D} = diameter of bearing of windmill in feet.

The effective horse-power of a windmill with plane sails will equal

$$\frac{(l-l_{\theta})Kc^{2}dN}{550g} \times \text{mean of} \left(v_{\theta}(\sin a - \frac{v_{\theta}}{4}\cos a)b_{\theta}\cos a\right)$$

$$v_{x}(\sin a - \frac{v_{x}}{6}\cos a)b_{x}\cos a - \frac{fW \times .05236nD}{550}.$$

The effective horse-power of a windmill of shape of sail for maximum effect equals

$$\frac{N(l-l_0)Kdc^3}{\cdot 2200g} \times \text{mean of} \left(\frac{2\sin^2 a_0 - 1}{\sin^2 a_0} b_0, \quad \frac{2\sin^2 a_1 - 1}{\sin^2 a_1} b_1 \dots \right) \\ \cdot \cdot \cdot \frac{2\sin^2 a_x - 1}{\sin_0 a_x} b_x \right) - \frac{fW \times .05286nD}{550}.$$

The mean value of quantities in brackets is to be found according to Simpson's rule. Dividing l into 7 parts, finding the angles and breadths corresponding to these divisions by substituting them in quantities within brackets will be found satisfactory. Comparison of these formulæ with the only fairly reliable experiments in windmills (Coulomb's) showed a close agreement of results.

Approximate formulæ of simpler form for windmills of present construction can be based upon the above, substituting actual average values for a,

tion can be based upon the above, substituting actual average values for a, c, d, and e, but since improvement in the present angles is possible, it is better to give the formulæ in their general and accurate form.

Wolff gives the following table based on the practice of an American manufacturer. Since its preparation, he says, over 1500 windmills have been sold on its guaranty (1885), and in all cases the results obtained did not vary sufficiently from those presented to cause any complaint. The actual results obtained are in close agreement with those obtained by theoretical analysis of the impulse of wind upon windmill blades.

Capacity of the Windmill.

Designation of Mill.	of Wind, in per hour.	ons of Wheel minute.	Gallor	ns of W	Equivalent Actual Use- ful Horse-power de- veloped.	No. of Hours during which ult will be ob-				
Designati	Velocity miles	Revolutions per mi	25 feet.	50 feet.	75 feet.	100 feet.	150 feet.	200 feet.	Equivaler ful Hor veloped	Average per Day this Res tained.
wheel 8½ ft. 10 " 18 " 14 " 16 " 20 " 25 "	16 16 16 16 16	70 to 75 60 to 85 55 to 60 50 to 55 46 to 50 40 to 45 30 to 85	83,941 45,139 64 600 97,682 124,950	22.569 31.654	6.638 11.851 15.304 19.542 32.518 40.800 71.604	4.750 8.485 11.246 16.150 24.421 81.248 49.725			0.61	8888888888

These windmills are made in regular sizes, as high as sixty feet diameter of

These windmills are made in regular sizes, as high as sixty feet diameter of wheel; but the experience with the larger class of mills is too limited to enable the presentation of precise data as to their performance.

If the wind can be relied upon in exceptional localities to average a higher velocity for eight hours a day than that stated in the above table, the performance or horse-power of the mill will be increased, and can be obtained by multiplying the figures in the table by the ratio of the cube of the higher average velocity of wind to the cube of the velocity above recorded He also gives the following table showing the account of the wind.

He also gives the following table showing the economy of the windmill. All the items of expense, including both interest and repairs, are reduced to the hour by dividing the costs per annum by $365 \times 8 = 2920$; the interest,

etc., for the twenty-four hours being charged to the eight hours of actual work. By multiplying the figures in the 5th column by 584, the first cost of the windmill, in dollars, is obtained.

Economy of the Windmill.

	raised r.	tual Useful developed.	of uring	Expense of Developed	Actual U	sefu , per	l Po	wer ir.	1 2
Designation of Mill.	hou	Equivalent Actual I Horse-power devel	Average Number of Hours per Day d which this Quant will be raised.	For Interest on First Cost (First Cost, including Cost of Wind-mill, Pump, and Tower, 55 per annum).	For Repairs and Depreciation (5% of First Cost per annum).	For Attendance.	For Oil.	Total.	Expense per Horse power, in cents, in bour.
816 ft. whee		0.04	8	0.25	0.25	0.06	0.04		
10 " "	1151	0.12	8	0.30	0.80		0.04		
12 " "	2036	0.21	8	0.36	0.86		0.04		
	2708	0.28	8	0.75	0.75		0.07	1.68	
16 " " 18 " " 20 " "	3876	0.41	8	1.15	1.15				
90 44 44	5861	0.61		1.85	1.35				4.6
25 " "	7497	0.79	****	1.70	1.70 2.05		0.10		4.5 8.2
KU .	12748	1.54	1 8	2.05	7.00	0.00	0.10	4.20	0.2

Lieut. I. N. Lewis (Eng'g Mag., Dec. 1894) gives a table of results of experiments with wooden wheels, from which the following is taken:

	Velocity of Wind, miles per hour.													
Diameter of wheel, Feet.	8	10	12	16	20	25	30							
reet.		Actual Useful Horse-power developed.												
12	0	14	14	112	1 214	136	2							
12 16 20 25 80	114	12	2 3	8 ⁷³ 416	6	512	10							
80	2	3	14	51%	7	9	12							

The wheels were tested by driving a differentially wound dynamo. The "useful horse-power" was measured by a voltmeter and ammeter, allowing 500 watts per horse-power. Details of the experiments, including the means used for obtaining the velocity of the wind, are not given. The results are so far in excess of the capacity claimed by responsible manufacture. rers that they should not be given credence until established by further experiments.

A recent article on windmills in the Iron Age contains the following: According to observations of the United States Signal Service, the average velocity of the wind within the range of its record is 9 miles per hour for the year along the North Atlantic border and Northwestern States, 10 miles

on the plains of the West, and 6 miles in the Gulf States.

The horse-powers of windmills of the best construction are proportional to the squares of their diameters and inversely as their velocities; for example, a 10-ft. mill in a 16-mile breeze will develop 0.15 horse-power at 65 revolutions per minute; and with the same breeze

A 20-ft. mill, 40 revolutions, 1 horse-power.

A 25-ft. mill, 35 revolutions, 134 horse-power, A 30-ft. mill, 28 revolutions, 334 horse-power, A 40-ft. mill, 22 revolutions, 74 horse-power. A 50-ft. mill, 18 revolutions, 12 horse-power.

The increase in power from increase in velocity of the wind is equal to the square of its proportional velocity; as for example, the 25-ft, mill rated 498

above for a 16-mile wind will, with a 32-mile wind, have its horse-power increased to $4 \times 1\frac{1}{4} = 7$ horse-power, a 40-ft. mill in a 32-mile wind will run up to 30 horse-power, and a 50-ft. mill to 48 horse-power, with a small deduction for increased friction of air on the wheel and the machinery.

The modern mill of medium and large size will run and produce work in a 4-mile breeze, becoming very efficient in an 8 to 16-mile breeze, and increase

4-mile breeze, becoming very efficient in an 8 to 16-mile breeze, and increase its power with safety to the running-gear up to a gale of 45 miles per hour Prof. Thurston, in an article on modern uses of the windmill, Engineering Magazine, Feb. 1898, says: The best mills cost from about \$60 for the 10-ft, wheel of ½ horse-power to \$1200 for the 25-ft, wheel of ½ horse-power or less. In the estimates a working-day of 8 hours is assumed; but the machine, when used for pumping, its most common application, may actually do its work 24 hours a day for days, weeks, and even months together, whenever the wind is "stiff" enough to turn it. It costs, for work done in situations in which its irregularity of action is no objection, only one half or one third as much as steam hot air, and gas engines of similar power. one third as much as steam, hot-air, and gas engines of similar power. At Faversham, it is said, a 15-horse-power mill raises 2,000,000 gallons a month from a depth of 100 ft., saving 10 tons of coal a month, which would otherwise be expended in doing the work by steam.

Electric storage and lighting from the power of a windmill has been tested on a large scale for several years by Charles F. Brush, at Cleveland, Ohio. In 1887 he erected on the grounds of his dwelling a windmill 56 ft. in diameter, that operates with ordinary wind a dynamo at 500 revolutions per minute, with an output of 12,000 watts—16 electric horse-power—charging a storage system that gives a constant lighting capacity of 100 16 to 20 candle-power lamps. The current from the dynamo is automatically regulated to commence charging at 330 revolutions and 70 volts, and cutting the circuit at 75 volts. Thus, by its 24 hours' work, the storage system of 408 cells in 12 parallel series, each cell having a capacity of 100 ampère hours, is kept in constant readiness for all the requirements of the establishment, it being fitted up with 350 incandescent lamps, about 100 being in use each evening. The plant runs at a mere nominal expense for oil, repairs, and attention. (For a fuller description of this plant, and of a more recent one at Marblehead Neck, Mass., see Lieut. Lewis's paper in Engineering Magazine, Dec. 1894, p. 475.)

COMPRESSED AIR.

Heating of Air by Compression.—Kimball, in his treatise on Physical Properties of Gases, says: When air is compressed, all the work which is done in the compression is converted into heat, and shows itself in the rise in temperature of the compressed gas. In practice many devices are employed to carry off the heat as fast as it is developed, and keep the temperature down. But it is not possible in any way to totally remove this difficulty. But, it may be objected, if all the work done in compression is converted into heat, and if this heat is got rid of as soon as possible, then the work may be virtually thrown away, and the compressed air can have no more energy than it had before compression. It is true that the compressed gas has no more energy than the gas had before compression, if its temperature is no higher, but the advantage of the compression lies in bringing its energy into more avail-

The total energy of the compressed and uncompressed gas is the same at the same temperature, but the available energy is much greater in the former.

When the compressed air is used in driving a rock-drill, or any other piece

of machinery, it gives up energy equal in amount to the work it does, and its temperature is accordingly greatly reduced.

Causes of Loss of Energy in Use of Compressed Air.

(Zahuer, on Transmission of Power by Compressed Air.)—1. The compression of air always develops heat, and as the compressed air always cools down to the temperature of the surrounding atmosphere before it is used, the me-chanical equivalent of this dissipated heat is work lost.

2. The heat of compression increases the volume of the air, and hence it is necessary to carry the air to a higher pressure in the compressor in order that we may finally have a given volume of air at a given pressure, and at the temperature of the surrounding atmosphere. The work spent in effect-

ing this excess of pressure is work lost.

Friction of the air in the pipes, leakage, dead spaces, the resistance of-fered by the valves, insufficiency of valve area, inferior workmanship, and slovenly attendance, are all more or less serious causes of loss of power.

The first cause of loss of work, namely, the heat developed by compression, is entirely unavoidable. The whole of the mechanical energy which the compressor-piston spends upon the air is converted into heat. This heat is dissipated by conduction and radiation, and its mechanical equivalent is work lost. The compressed air, having again reached thermal equilibrium with the surrounding atmosphere, expands and does work in virtue of its intringic energy.

The intrinsic energy of a fluid is the energy which it is capable of exerting against a piston in changing from a given state as to temperature and volume to a total privation of heat and indefinite expansion.

Adiabatic and Isothermal Compression.—Air may be compressed either adiabatically, in which all the heat resulting from compression is retained in the air compressed, or isothermally, in which the heat is removed as rapidly as produced, by means of some form of refrig-

Volumes, Mean Pressures per Stroke, Temperatures, etc., in the Operation of Air-compression from I Atmosphere and 60° Fahr. (F. Richards, Am. Mach., March 30, 1898.)

- Gauge-pressure.	Atmospheres.	Volume with Air at Constant Temp.	Volume with Air not cooled.	Mean Pressure per Stroke; Air Con- stant Temp.	Mean Pressure per Stroke; Air not cooled.	Temp. of Air; not	Gauge-pressure.	Atmospheres.	Volume with Air at Constant Temp.	Volume with Air not cooled.	Mean Pl Stroke stan	Mean Pressure per Stroke; Air not cooled.	Temp. of Air; not cooled.
	2		4.	5	6	7	1	2	8	4	5	6	7
2 8 4 5 10 15 20 25 30 35 40 45 50 65 70	1 1.068 1.196 1.204 1.272 1.34 1.68 2.02 2.36 2.37 3.04 3.381 3.721 4.061 4.741 5.081 5.422 5.762 6.102	1 .9363 .8808 .8308 .7861 .7462 .5952 .495 .4237 .8708 .8289 .2957 .2462 .2272 .2109 .1968 .1844 .1735 .1639	1 .95 .91 .876 .84 .81 .69 .606 .543 .494 .4588 .37 .3144 .301 .288 .276	0 .96 1.87 2.72 8.53 4.3 7.62 10.83 12.63 14.59 16.34 17.92 20.57 21.69 22.76 23.78 24.75 25.67 26.55	14.4 17.01 19.4 21.6 23.66 25.59 27.89 29.11 30.75 32.82 33.88	60° 71 80.4 88.9 98 106 145 178 207 234 252 281 302 3821 3857 375 389 405 420	150 160 170	6.442 6.782 7.122 7.802 8.142 8.483 8.823 9.163 9.503 9.843 10.523 10.864 11.204 11.28 12.56 13.24 18.93 14.61	.1228 .1178 .1132 .1091 .1052 .1015 .0981 .095	.2566 .248 .24 .2324 .2129 .2129 .2073 .2020 .1969 .1922 .1878 .1876 .1796 .1792 .1657 .1595	27.38 28.16 28.89 29.57 30.21 30.81 31.98 32.54 33.07 33.57 34.05 34.57 35.09 35.48 36.29 37.2 37.96 38.68 39.42	86.64 87.94 89.18 40.4 41.6 42.78 43.91 44.98 46.04 47.06 48.1 49.1 50.02 51. 51.89 53.65 55.399 57.01 58.57 60.14	507 518 529 540 550 560 570 580 589 607 624 640 657

Column 3 gives the volume of air after compression to the given pressure and after it is cooled to its initial temperature. After compression air loses its heat very rapidly, and this column may be taken to represent the volume of air after compression available for the purpose for which the air has been compressed.

Column 4 gives the volume of air more nearly as the compressor has to deal with it. In any compressor the air will lose some of its heat during compression. The slower the compressor runs the cooler the air and the

smaller the volume.

Column 5 gives the mean effective resistance to be overcome by the aircylinder piston in the stroke of compression, supposing the air to remain constantly at its initial temperature. Of course it will not so remain, but this column is the ideal to be kept in view in economical air-compression 500 AIR.

Column 6 gives the mean effective resistance to be overcome by the piston, supposing that there is no cooling of the air. The actual mean effective tive pressure will be somewhat less than as given in this column; but for computing the actual power required for operating air-compressor cylinders the figures in this column may be taken and a certain percentage addedsay 10 per cent-and the result will represent very closely the power required

by the compressor.

The mean pressures given being for compression from one atmosphere upward, they will not be correct for computations in compound compression or for any other initial pressure.

Loss Due to Excess of Pressure caused by Heating in the Compression-cylinder.—If the air during compression were kept at a constant temperature, the compression-curve of an indicator-diagrain taken from the cylinder would be an isothermal curve, and would follow the law of Boyle and Marriotte, pv = a constant, or $p_1v_1 = p_0v_0$, or

 $p_1 = p_0 \frac{v_0}{v_1}$, p_0 and v_0 being the pressure and volume at the beginning of compression, and p_1v_1 the pressure and volume at the end, or at any intermediate point. But as the air is heated during compression the pressure increases faster than the volume decreases, causing the work required for any given pressure to be increased. If none of the heat were abstracted by radiation or by injection of water, the curve of the diagram would be an adiabatic curve, with the equation $p_1 = p_0 \left(\frac{v_0}{v_0}\right)^{1.405}$. Cooling the air dur-

adiabatic curve, with the equation $p_1 = p_0 \left(\frac{r_0}{v_0} \right)$

ing compression, or compressing it in two cylinders, called compounding, and cooling the air as it passes from one cylinder to the other, reduces the exponent of this equation, and reduces the quantity of work necessary to effect a given compression. F. T. Gause (Am. Mach., Oct. 20, 1892), describing the operations of the Popp air compressors in Paris, says: The greatest saving realized in compressing in a single cylinder was 33 per cent of that theoretically possible. In cards taken from the 2000 H.P. compound compressor at Quai De La Gare, Paris, the saving realized is 85 per cent of the theoretical amount. Of this amount only 8 per cent is due to cooling during compression, so that the increase of economy in the compound compressor is mainly due to cooling the air between the two stages of compression. A compression-curve with exponent 1.25 is the best result that was obtained for compression in a single cylinder and cooling with a very fine spray. The curve with exponent 1.15 is that which must be realized in a single cylinder to equal the present economy of the compound compressor at Quái De La Gare.

lorse-power required to compress and deliver one cubic foot of Free Air per to Horse-power Horse-power minute to a given pressure with no cooling of the air during the compression; also the horse-power required, supposing the air to be main-tained at constant temperature at constant temperature during the compresion.

required compress and deliver one cubic foot of Compressed Air per minute at a given pressure with no cooling of the air during the compression; also the horsepower required, supposing the air to be maintained at constant temperature during the compression.

Gauge- bressure.	Air not cooled.	Air constant temperature.		Air not cooled.	Air constant temperature.
5	.0196	.0188	5	.0268	.0251
10	.0361	.0333	l 10	.0606	.0559
20	.0628	.0551	20	.1483	.1300
80	.0846	.0718	30	.2578	.2168
40	.1082	.0843	40	.8842	.8188
50	.1195	.0946	50	.5261	.4166
60	.1842	.1036	60	.6818	.5266
70	.1476	.1190	10	.8508	.6456
80	.1599	.1195	80	1.0308	.7700
90	.1710	.1261	90	1.2177	.8979
100	.1815	.1318	100	1.4171	1.0291

The horse-power given above is the theoretical power, no allowance being made for friction of the compressor or other losses, which may amount to 10 per cent or more.

Formulæ for Adiabatic Compression or Expansion of Air (or other sensibly perfect gas).

Let air at an absolute temperature T_1 , absolute pressure p_1 , and volume v_1 be compressed to an absolute pressure p_2 and corresponding volume v_3 and absolute temperature T_2 ; or let compressed air of an initial pressure volume, and temperature p_2 , v_3 , and T_2 be expanded to p_1 , v_1 , and T_3 , there being no transmission of heat from or into the air during the operation. Then the following equations express the relations between pressure, volume, and temperature (see works on Thermodynamics):

$$\begin{split} &\frac{v_1}{v_3} = \left(\frac{p_3}{p_1}\right)^{0.71}; & \frac{p_2}{p_1} = \left(\frac{v_1}{v_3}\right)^{1.41}, & \frac{v_1}{v_2} = \left(\frac{T_2}{T_1}\right)^{2.46}; \\ &\frac{T_2}{T_1} = \left(\frac{v_1}{v_2}\right)^{0.41}; & \frac{T_2}{T_1} = \left(\frac{p_2}{p_1}\right)^{0.29}; & \frac{p_2}{p_1} = \left(\frac{T_2}{T_1}\right)^{3.46}. \end{split}$$

The exponents are derived from the ratio cp + cv = k of the specific heats of air at constant pressure and constant volume. Taking k = 1.406, 1 + k = 0.711; k - 1 = 0.406; 1 + (k - 1) = 2.463; k + (k - 1) = 3.463; (k - 1) + k = 0.711

Work of Adiabatic Compression of Air.—If air is compressed in a cylinder without clearance from a volume v_1 and pressure p_1 to a smaller volume v_2 and higher pressure p_3 , work equal to p_1v_1 is done by the external air on the piston while the air is drawn into the cylinder. Work is then done by the piston on the air, first, in compressing it to the pressure p_3 and volume v_2 , and then in expelling the volume v_2 from the cylinder against the pressure p_2 . If the compression is adiabatic, $p_1v_1^k =$ $p_2 v_2^k = \text{constant.}$ k = 1.41.The work of compression of 1 pound of air is

$$\frac{p_1v_1}{k-1}\left\{\left(\frac{v_1}{v_2}\right)^{k-1}-1\right\} = \frac{p_1v_1}{k-1}\left\{\left(\frac{p_2}{p_1}\right)^{\frac{k-1}{k}}-1\right\}$$

or

$$2.463p_1v_1\left\{ \left(\frac{v_1}{v_2}\right)^{0.41} - 1 \right\} = 2.463p_1v_1\left\{ \left(\frac{p_2}{p_1}\right)^{0.39} - 1 \right\}.$$

The work of expulsion is $p_2v_2 = p_1v_1\left(\frac{p_2}{n_1}\right)^{\frac{n_1}{n_2}}$.

The total work is the sum of the work of compression and expulsion less the work done on the piston during admission, and it equals

$$p_1v_1\left\{\frac{k}{k-1}\right\}\left(\frac{p_2}{p_1}\right)^{\frac{k-1}{k}}-1\right\} = 3.463 \ p_1v_1\left\{\left(\frac{p_2}{p_1}\right)^{\frac{q_1-2q}{k}}-1\right\}.$$

The mean effective pressure during the stroke is

$$p_1 \frac{k}{k-1} \left\{ \left(\frac{p_2}{p_1} \right)^{\frac{k-1}{k}} - 1 \right\} = 8.468 \, p_1 \, \left\{ \left(\frac{p_2}{p_1} \right)^{0.29} - 1 \right\}.$$

 p_1 and p_2 are absolute pressures above a vacuum in atmospheres or in pounds per square inch or per square foot.

EXAMPLE.—Required the work done in compressing 1 cubic foot of air per second from 1 to 6 atmospheres, including the work of expulsion from the

 $p_3 + p_1 = 6$; $\theta^{\bullet \cdot 20} - 1 = 0.681$; $3.463 \times 0.681 = 2.358$ atmospheres, $\times 14.7 = 34.66$ ibs. per sq. in. mean effective pressure, $\times 144 = 4991$ ibs. per sq. ft., $\times 1$ ft. stroke = 4991 ft.-lbs., + 550 ft.-lbs. per second = 9.08 H.P.

If R= ratio of pressures $=p_2+p_1$, and if $v_1=1$ cubic foot, the work done in compressing 1 cubic foot from p_1 to p_2 is in foot-pounds

$$8.463p_1(R^{0.29}-1),$$

 p_1 being taken in lbs. per sq. ft. For compression at the sea-level p_1 may be taken at 14 lbs. per sq. in. = 2016 lbs. per sq. ft., as there is some loss of pressure due to friction of valves and passages.

Indicator-cards from compressors in good condition and under workingspeeds usually follow the adiabatic line closely. A low curve indicates piston leakage. Such cooling as there may be from the cylinder-jacket and the re-expansion of the air in clearance-spaces tends to reduce the mean effective pressure, while the "camel-backs" in the expulsion-line, due to resistance to opening of the discharge-valve, tend to increase it.

Work of one stroke of a compressor, with adiabatic compression, in foot-

pounds.

$$W = 8.463P_1 V_1 (R^{0.29} - 1),$$

in which $P_1=$ initial absolute pressure in lbs. per sq. ft. and $V_1=$ volume traversed by piston in cubic feet.

The work done during adiabatic compression (or expansion) of 1 pound of

air from a volume v_1 and pressure p_1 to another volume v_2 and pressure p_3 is equal to the mechanical equivalent of the heating (or cooling). If t_1 is the higher and t_2 the lower temperature, Fahr., the work done is $c_yJ(t_1-t_2)$ foot-pounds, c_v being the specific heat of air at constant volume = 0.1689 and $J = 778, c_{ef}J = 131.4.$

The work during compression also equals

$$\frac{c_{v^{J}}}{Ra}p_{1}v_{1}\left[\left(\frac{p_{2}}{p_{1}}\right)^{0\cdot2\theta}-1\right]=2.468\,p_{1}v_{1}\left\{\left(\frac{p_{2}}{p_{1}}\right)^{0\cdot2\theta}-1\right\},$$

 R_a being the value of pv + absolute temperature for 1 pound of air = 53.37. The work during expansion is

$$2.463 \ p_1 v_1 \left[1 - \left(\frac{p_2}{p_1} \right)^{0.29} \right] = 2.463 \ p_2 v_2 \left[\left(\frac{p_1}{p_2} \right)^{0.29} - 1 \right],$$

in which p_1v_1 are the initial and p_2v_2 the flual pressures and volumes. Compressed-air Engines, Adiabatic Expansion. — Let the initial pressure and volume taken into the cylinder be p_1 lbs, per q_1 ft. and v_1 cubic feet; let expansion take place to p_2 and v_3 according to the adiabatic law $p_1v_1^{1+41} = p_2v_2^{1+41}$; then at the end of the stroke let the pressure drop to the back-pressure p_3 at which the air is exhausted Assuming no clearance, the work done by one pound of air during ad mission, measured above vacuum, is p_1v_1 , the work during expansion is 2.463 $p_1v_1\Big[1-\Big(\frac{p_2}{p_1}\Big)^{0.29}\Big]$, and the negative or back pressure work is $-p_3v_3$.

The total work is $p_1v_1 + 2.463p_1v_1 \left[1 - \left(\frac{p_2}{p_1}\right)^{0.29}\right] - p_2v_2$, and the mean effec-

tive pressure is the total work divided by v_2 .

If the air is expanded down to the back-pressure p_2 the total work is

$$3.468p_1v_1 \left\{ 1 - \left(\frac{p_3}{p_1} \right)^{0.29} \right\}$$

or, in terms of the final pressure and volume

$$3.463p_3v_2\left\{\left(\frac{p_1}{p_3}\right)^{0.29}-1\right\}$$
,

and the mean effective pressure is

$$3.463p_3\left\{\left(\frac{p_1}{p_3}\right)^{0.29}-1\right\}.$$

The actual work is reduced by clearance. When this is considered, the product of the initial pressure p_1 by the clearance volume is to be subtracted from the total work calculated from the initial volume v_1 including clearance. "See p. 744, under "Steam-engine.")

Mean Effective Pressures of Air Compressed Adiabatically. (F. A. Halsey, Am. Mach., Mar. 10, 1898.)

R	R0 ·20	MEP from 14 lbs. Initial.	R	R0.20	MEP from 14 lbs. Initial.
1.25	1.067	3.24	4.75	1.570	27.5
1.50	1.125	6.04	5.	1.594	28.7
1.75	1.176	8.51	5.25	1.617	29.8
2.	1.223	10.8	5.5	1.639	30.8
2.25	1.265	12.8	5.75	1.660	31.8
2.5	1.304	14.7	6.	1.681	32.8
2.75	1.841	16.4	6.25	1.701	33.8
3.	1.375	18.1	6.5	1.720	34.7
8.25	1.407	19.6	6.75	1.739	35.6
8.5	1.488	21.1	7.	1.757	36.5
8.75	1.467	22.5	7.25	1.775	87.4
4.	1.495	23.9	7.5	1.798	38.8
4.25	1.521	25.2	8.	1.827	89.9
4.5	1.546	26.4			

R = flual + initial absolute pressure.

MEP = mean effective pressure, lbs. per sq. in., based on 14 lbs. initial.

Compound Compression, with Air Cooled between the Two Cylinders. (Am. Mach., March 10 and 31, 1898.)—Work in low-pressure cylinder W_1 , in high-pressure cylinder W_3 . Total work

$$W_1 + W_2 = 3.46P_1V_1[r_1^{29} + R^{29}r_1 - 29 - 2].$$

 $r_1=$ ratio of pressures in 1. p. cyl., $r_2=$ ratio in h. p. cyl., $R=r_1r_2$. When $r_1=r_2=\sqrt{R}$, the sum W_1+W_2 is a minimum. Hence for a given total ratio of pressures, R, the work of compression will be least when the ratios of the pressures in each of the two cylinders are equal.

The equation may be simplified, when $r_1 = \sqrt{R}$, to the following:

$$W_1 + W_2 = 6.92 P_1 V_1 [R^{0.148} - 1].$$

Dividing by V_1 gives the mean effective pressure reduced to the low-pressure cylinder $MEP=6.92P_1[E^{0.145}-1]$.

In the above equation the compression in each cylinder is supposed to be adiabatic, but the intercooler is supposed to reduce the temperature of the air to that at which compression began.

Mean Effective Pressures of Air Compressed in Two Stages, assuming the Intercooler to Reduce the Temperature to That at which Compression Began. (F. A. Halsey, Am. Mach., Mar. 31, 1898.)

R	Rº-145	MEP from 14 lbs. Initial.	Ultimate Saving by Com- pound- ing, %	R	Rº-145	MEP from 14 lbs. Initial.	U.timate Saving by Com- pound- ing, %
5.0 5.5 6.0 6.5 7.0 7.5 8.0 8.5	1.263 1.280 1.296 1.312 1.326 1.336 1.352 1.364	25.4 27.0 28.6 30.1 81.5 82.8 84.0 85.2	11.5 12.8 12.8 13.2 13.7 14.3 14.8	9.0 9.5 10 11 12 18 14 15	1.375 1.386 1.396 1.416 1.434 1.451 1.466 1.481	36.3 37.3 38.3 40.2 41.9 43.5 45.0 46.4	

R = final + initial absolute pressure.

MEP = mean effective pressure lbs. per sq. in. based on 14 lbs. absolute initial pressure reduced to the low-pressure cylinder.

To Find the Index of the Curve of an Air-diagram.—
If P_1V_1 be pressure and volume at one point on the curve, and PV the pressure and volume at another point, then $\frac{P}{P_1} = \left(\frac{V_1}{V}\right)^x$, in which x is the index to be found. Let $P+P_1 = R$, and $V_1 + V = r$; then $R = r^x \log R = x \log r$ whence $x = \log R + \log r$.

Table for Adiabatic Compression or Expansion of Air. (Proc. Inst. M.E., Jan. 1881, p. 123.)

Absolute	Pressure.	Absolute T	emperature.	Volume.			
Ratio of Greater to Less. (Expan- sion.)	Ratio of Less to Greater. (Compres- sion.)	Ratio of Greater to Less. (Expan- sion.)	Ratio of Less to Greater. (Compres- sion.)	Ratio of Greater to Less. (Compres- sion.)	Ratio of Less to Greater. (Expan- sion.)		
1.2 1.4 1.6 1.8 2.2 2.4 2.6 8.8 8.2 3.4 4.6 4.8 6.0 7.0 9.0 9.0 9.0 9.0 9.0 9.0 9.0 9.0 9.0 9	.883 .714 .625 .566 .500 .454 .417 .385 .887 .387 .383 .312 .294 .278 .283 .283 .293 .293 .297 .217 .208 .217 .208 .217 .217 .208 .217 .217 .217 .218 .217 .217 .217 .217 .217 .217 .217 .217	1.054 1.102 1.146 1.186 1.1257 1.257 1.259 1.319 1.348 1.375 1.401 1.473 1.495 1.516 1.557 1.557 1.557 1.557 1.557 1.558 1.681 1.758 1.888 1.891	.948 .907 .873 .848 .848 .796 .776 .758 .749 .727 .714 .690 .679 .669 .660 .651 .642 .635 .627 .589 .589 .589 .589	1.138 1.970 1.296 1.518 1.536 1.750 1.862 1.971 2.077 2.189 2.294 2.483 2.580 2.580 2.770 2.885 3.046 3.785 3.046 3.759 4.779 4.779 4.779	.979 .788 .716 .659 .6611 .571 .587 .507 .481 .498 .498 .498 .388 .419 .403 .388 .374 .361 .389 .329 .329 .329 .220 .220 .220 .220 .220 .220 .220 .2		

Mean Effective Pressures for the Compression Part only of the Stroke when compressing and delivering Air from one Atmosphere to given Gauge-pressure in a Single Cylinder. (F. Richards, Am. Mack., Dec. 14, 1893.)

Gauge- pressure.	Adiabatic Compression.	Isothermal Compression.	Gauge- pressure.	Adiabatic Compression.	Isothermal Compression
1	.44	.48 .95	45	13.95	12.62
8	1.41 1.86	1.4 1.84	50 55	15.05 15.98 16.89	13.48 14.8 15.05
5 10	2,26 4,26	2.29 4.14	60 65 70	17.88 18.74	15.76 16.48
15 20	5.99 7.58	5.77 7.2	75 80 85	19.54 20.5	17.09 17.7
25 80 85	9.05 10.89	8.49 9.66	85 90	21.22 22.	18.8 18.87
85 40	11.59 12.8	10.72 11.7	95 100	22.77 28.43	19.4 19.99

The mean effective pressure for compression only is always lower than the mean effective pressure for the whole work.

Mean and Terminal Pressures of Compressed Air used Expansively for Gauge-pressures from 60 to 100 lbs.
(Frank Richards, Am. Mach., April 18, 1893.)

Initial Pres- sure.	6	0.	7	0.	8	0.	90	0.	100.		
Point of Cut-off.	Mean Air- pressure.	Terminal Air- pressure.	Mean Air- pressure.	Terminal Air- pressure.	Mean Afr- pressure.	Terminal Air- pressure.	Mean Air- pressure.	Terminal Air- pressure,	Mean Air- pressure.	Terminal Afr- pressure.	
.95 .90 .95 .85 .85 .86 .40 .45 .50 .60 .75 .80 .75 .80	28.6 28.9 32.13 33.66 35.85 87.93 41.75 45.14 50.75 51.92 53.67 54.93 56.52 57.79	2.83 3.85 5.64 10.71 13.26 21.53 23.69 27.94 30.39 35.01	28.74 34.75 88.41 40.15 42.68 44.99 49.31 58.16 59.51 60.84 62.83 64.25 66.05 67.5	8,09 4,38 6,36 8,39 12,61 17, 26,4 28,85 33,03 36,44	33.89 40.61 44.69 46.64 49.41 52.05 56.9 61.18 68.28 69.76 71.99 73.57 75.59 77.2	13.49 2.44 5.22 6.66 7.88 11.14 15.86 20.81 31.27 34.01 38.68 42.49 48.35 54.38	39 04 46,46 50.98 53.13 56.2 59,11 64 45 69.19 77.05 78.69 81.14 82.9 85.12 86.91		44.19 58.32 57.26 59.62 62.98 66.16 72.02 77.21 85.82 87.61 90.32 94.66 96.61	1.83 6.11 9.48 11.43 16.64 22.36 28.38 41.01 44.39 49.97 54.59 61.69	

The pressures in the table are all gauge-pressures except those in italics, which are absolute pressures (above a vacuum).

Mountain or High-altitude Compressors.

(Norwalk Iron Works Co.)

	(NOI WAIL HOIL WOLKS CO.)												
Air-		of ssing	b .	ns ute.	At 8	Bea- rel.		2000 eet.	At 6000 feet.	At 10),000 et.		
Diameter . cylinder	Length of Stroke.	Diameter Compre Cylinder	Diameter Steam- cylinder	Revolutions per minut	Capacity. cubic feet.	Horse- power:	Capacity.	Horse- power.	Capacity. Horse-	Capacity.	Horse. power,		
12 16 20 22 26	12 16 20 24 30	7 914 1814 1814 1714	10 14 18 20 24	190 150 120 110 90	298 558 872 1160 1659	35 70 110 145 215	280 524 819 1090 1560	34 68 107 140 207	244 82 462 64 722 100 960 132 1373 195	405 634 848	80 60 94 124 184		

As the capacity decreases in a greater ratio than the power necessary to compress, it follows that operations at a high altitude are more expensive than at sea-level. At 10,000 feet this extra expense amounts to over 20 per cent.

Compressors at High Altitudes. (Ingersoll-Sergeant Drill Co.)

Alt, above sea-level, ft											
Barometer, in, mercury.	30.0	28.9	27.8	26.8	25.8	24.8	23.9	23.0	22.1	21.3	20.5
" lbs.per sq.in.	14.7	14.2	13.7	13.2	12.7	12.2	11.7	11.3	10.9	10.5	10.1
Air delivered, %	100	97	98	90	87	84	81	78	76	73	70
Loss of capacity, %	0	3	7	10	13	16	19	23	24	27	30
Decreased power re- quired, %	0	1.8	3.5	5.2	6.9	8.5	10.1	11.6	13.1	14.6	16.1

Air-compressors. Rand Drill Co.

RAND-CORLISS, CLASS "BB-3" (COMPOUND | CLASS "E" (STRAIGHT-STEAM, CONDENSING; COMPOUND AIR). FOR STEAM-PRESSURE OF 125 LBS. AND TERMINAL FOR TERMINAL PRESSURES AIR-PRESSURES OF 80 AND 100 LBS.

LINE, BELT-DRIVEN). OF 80 AND 100 LBS.PER SQ IN.

							'					
in Cu. ree Air ute.	Cyline	ler Dia	ameter	s, Ins.	Ins.	per Min.	Indicated Horse-power.*	ity in Cu. Free Air inute.	ind	Cyl- ler, bes.	Ä	Indi- cated H.P.
75	Ste	Steam. Air.				<u>ē</u>	1 5 5	56.5		1 .	per	Air-
305	l		23.11.2		S.		8 8	of M	ä	1 2		pres- sure
Capacity in C Ft. of Free 2 per Minute.	h, p.	l. p.	h. p.	1. p.	Stroke,	Revs.	Hol	Capacit Ft. of I per Mi	Diam.	Stroke	Revs.	80 lbs.
670	10	18	101	17	30	85	102	97	8	12	140	17
1196	12	2:2	13	21	36	83	182	165	10	14	130	
1562	14	26	15	24	36	83	238	251	12	16	120	45
1650	14	26	15	24	42	75	252	392	14	23	100	69
1920	16	30	171	28	36	75	298	527	16	24	95	94
2343	16	30	173	28	42	75	342	633	173	24	95	112
2395	16	30	171	28	48	70	865	l				
2520	18	34	20	32	36	75	384	l				
2897	18	34	20	32	43	75	442	l .				
3128	18	31	20	32	48	70	475	ļ				
396 0	20	39	221	36	48	70	604	1				
4100	22	40	24	38	48	65	625	l				
4530	23	4:3	25	40	48	65	690	1				
5000	24	44	261	42	48	65	763	l				
6000	26	48	29	46	48	65	915	l				
6820	28	52	30	48	48	65	1040					

In the first four sizes (Class "BB-3") the air-cylinders have poppet inlet and outlet valves; in the next six the low-pressure air-cylinders have mechanical inlet-valves and poppet outlet-valves; and in the last six the low-pressure air-cylinders have Corliss inlet-valves and poppet outlet-valves. All high-pressure air-cylinders have poppet inlet and outlet valves. * Terminal air-pressure at 80 pounds.

CONDENSING, COMPOUND AIR).

CLASS "B-2" (DUPLEX STEAM, NON- CLASS "C" (STRAIGHT-LINE. STEAM-DRIVEN).

FOR STEAM- AND TERMINAL AIR-PRESSURES | FOR STEAM- AND TERMINAL AIR-OF 80 AND 100 LBS. PRESSURES OF 100 LBS. PER SQ. IN.

							1					~ q
y in Cu. Free Air nute.	eters, Inches.			Ins.	per Min.	and Air at 80 lbs.	y in Cu. Free Air nute.	Die	yl. ım., ns.	Ins.	per Min.	od power.
Capacit Ft. of J per Mi	Duplex Steam cyls.	h. p.	l. p.	Stroke,	Revs. p	Ind. H. Steam Press. a	Capacit Ft. of J per Mi	Steam.	Air.	Stroke,	Revs. p	Indicated Horse-pov
220 300 893 565 770 882 1152 1812 2085	8 9 10 12 14 14 16 18 20	7½ 9 9½ 11 13 13 15 17½ 19	12 14 15 18 21 21 21 24 28 30	12 12 16 16 16 22 22 22 30 30	140 140 120 120 120 100 100 85 85	35 47 62 89 121 139 182 285	97 165 251 392 527 671 950 1335	8 10 12 14 16 18 20 24	8 10 12 14 16 18 20 24	12 14 16 22 24 24 80 80	140 130 120 100 95 95 87 85	20 35 52 82 110 140 200 280
2356 2848	20 22	19 21	30 33	48 48	60 60	870 446	iulet a	ind c	utlet	t val	ves.	opper

The first six sizes (Class "B-2") have both air-cylinders fitted with poppetvalves (inlet and discharge). The last four have low-pressure air-cylinders fitted with mechanical inlet-valve; high-pressure air-cylinders fitted with poppet inlet and discharge valves.

STANDARD AIR COMPRESSORS.

(The Ingersoll-Sergeant Drill Co., New York City.)

	Di	am.	of C	yl.		e.	Air.	. Fe	g _n	ace	r:
Class	Stea	ım.	A	ir.		per min.	Free Air.	ing Air- pressure		pied.	оме
and Type.	High.	Low.	Low.	High.	Stroke.	Revs. pe	Cap'y,F Cu.ft.p	Working Air- pressur	Length.	Width.	Horse-power,
A.* Straight- line, Steam- driven.	10 12 14 16 18 20 22 24		10¼ 12¼ 14¼ 16¼ 16¼ 20¼ 20¼ 22¼ 24¼		12 14 18 18 24 24 24 24 24	160 155 120 120 94 94 94 94 80	177 285 382 498 657 809 960 1225	50-100 50-100 50-100 50-100 50-100 50-100 50-100 50-100	10' 2"' 12 6 15 8 15 3 19 1 19 1 19 1 22 0	3' 0'' 3 9 4 3 4 3 5 3 5 3 5 3 6 0	25-35 40-56 50-76 66-100 86-131 113-160 126-192 160-245
B. Straig	tht-li	ne, l	elt-c	irive	n, 8	Same	as 2	4 in size		$16 \times 16\frac{1}{4}$	\times 18 ins.
C.† Duplex Corliss steam, Duplex air.	10½ 16 20 24 30 32		111/4 161/4 201/4 241/4 301/4 321/4		30 36 42 42 48 60	75 75 65	576 1346 2239 3208 4932 6717	100 100 100 100 100 100	31' 0" 36 6 41 0 43 0 41 0 60 0	10' 6'' 12 6 13 6 14 6 16 6 19 6	115 274 454 646 1011 1375
Compound Corliss steam, Compound air.‡	10½ 14 16 18 22 24	18 26 30 34 40 44	161/4 221/4 241/4 281/4 341/4 361/4	1714 2014	30 36 42 48 48 48	90 85 78 75 72 70	$\frac{1668}{2137}$	100 100 100 100 100 100	39 6 43 0 49 6 55 6 56 6 58 0	14 0 14 6 15 6 15 6 18 6 19 6	97 225 284 367 604 664
F.§ Small straight- line.	6 8 10 12 12		6 8 10 12 1614		6 8 10 12 12	150 150 150 150 150	28 69 134 287 415	50-80 50-80 50-80 50-80 15-40	5 8 6 8 7 10 8 6 10 10	22 25 30 30 30 35	4-51/4 93/4-13 183/4-25 831/4-44 243/4-50
E. Belt-	driv	en.	Sam	e as	$oldsymbol{F}$ in	size	s up	to 141/4	diam. by	10 ins. s	troke.
G. Steam- actuated, duplex or half duplex.	 	10 12 14 16 18 20		10¼ 12¼ 14¼ 16¼ 18¼ 20¼	12 14 18 18 24 24		570 764	100 100 100 100 100 100	14' 6'' 16 6 20 0 20 0 25 6 25 6	7' 0'' 9 0 10 0 10 0 11 6 12 0	75 121 163 212 280 844
G. Duplex st., comp. air.	10 16 20	16¼ 24¼ 30¼	::::	10¼ 15¼ 18¼ 18¼	12 18 24		446 1130 1963	80-100 80-100 100	16 3 23 0 30 0	7 3 10 0 12 0	71-80 180-208 353
G. Comp. st., comp. air.	10 16 20	17 26 32	141/4 221/4 281/4	91/4 141/4 171/4	12 18 24	160 120 100	344 950 1710	80-100 80-100 80-100	16 3 23 0 30 0	7 6 10 0 12 0	55-62 152-171 274-308
H. Duplex st., duplex air.		8 10 12		8 10 12	8 10 12	150 150 150	138 268 474	60-100 70-100 80-100	8 6 10 0 11 8	4 6 4 9 5 10	20-28 43-54 83-95
H. Duplex st., comp. sir.		8 10 12	14 16 18	9 10 12	8 10 12	150 150 150	342	80-100 80-100 80-100	8 6 10 2 11 10	5 8 5 9 6 9	32-36 52-58 78-88
J. Belte	d du	plex	or c	omp	oun	1. 8	to 98	H.P.;	56 to 1059	eu. ft. 1	per m.

^{*} Classes A, C, G, and H are also built in intermediate sizes for lower pressures. † Furnished either duplex or half duplex. † Most economical form of compressor. Compound air-cylinders are two-stage. § Self-contained steam-compressor.

Cubic Feet of Free Air Required to Run from One to Forty Machines with 60 ibs. Pressure. (Ingersoll-Sergeant Drill Co.)

For 75 lbs. Pressure add 1/5. For 90 lbs. add 2/5.	For 75 1	hs Pressure	add 1/5.	For 90 lbs.	add 2/5.
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No. of A Machines 2 in	В	1 0	Rock-drills.												
	n. 236 in	254 in.	D 3 iu.	E 8¼ in.	F 316 in.	G 4¼ in.	H 5 in.	814 in.	4 in.						
	5 70	95	110	115	125	140	165	70	98						
2 11		160	190	200	230	250	280	140	186						
8 15		294	279 356	294 372	888 428	860	405	210 280	279 873						
5 2		370	425	445	510	460 555	524 635	250 350	465						
5 23 6 26		426	486	516	588	642	788	420	558						
7 26		476	546	581	658	781	826	490	651						
		590	600	640	720	800	920	560	744						
8 88 9 86		585	675	720	810	900	1085	680	887						
10 40		650	750	800	900	1000	1150	700	980						
12 48		780	900	960	1080	1200	1890	840	1116						
15	675	975	1125	1200	1850	1500	1725	1050	1895						
20		1300	1500	1600	1800	2000	2800	1400	1860						
25	[1625	1875	2000	2250	2500	2775	1750	2825						
3 0		1950 2600	2250 8000	2400 3200	2700 3600	3000 4000	8450 4600	2100 2800	2790 8720						

Compressed-air Table for Pumping Plants.

(Ingersoll-Sergeant Drill Co.)

For the convenience of engineers and others figuring on pumping plants to be operated by compressed air, we subjoin a table by which the pressure and volume of air required for any size pump can be readily ascertained. Reasonable allowances have been made for loss due to clearances in pump and friction in pipe.

Ratio of Diam-		Per	Perpendicular Height, in Feet, to which the Water is to Pumped.										
e ters .		25	50	75	100	125	150	175	200	250	300	400	
1 to 1 {	AB	13.75 0.21		41.25		68.25 0.89	82.5 1.04		110.0				
116 to 1	AB		12.22 0.65	18.33	24.44	30.33	36.66 1.24				78.32 2.12		
194 to 1	AB			18.75 0.94	1.14		97.5 1.80			45.88 1.99	55.0 2.39		
2 to 1	A B			· · · ·	1.23		20.63 1.52	1.66		2.11			
234 to 1	A B					13.75 1.533				2.96			
21/2 to 1 {	A B						13.2 1.79	15.4 1.98	17.6 2.06			85.2 8.18	

A = air-pressure at pump. B = cubic feet of free air per gallon of water.

A = air-pressure at pump. Be clustered to rees air per gain of water. To find the amount of air and pressure required to pump a given quantity of water a given height, find the ratio of diameters between water and air cylinders, and multiply the number of gallons of water by the figure found in the column for the required lift. The result is the number of colic feet of free air. The pressure required on the pump will be found directly above in the same column. For example: The ratio between cylinders being 2 to 1, required to pump 100 gallons, height of lift 250 feet. We find under 250 feet at ratio 2 to 1 the figures 2.11; 2.11 × 100 = 211 cubic feet of free air. The pressure required is 34.38 pounds,

Compressed-air Table for Hoisting-er vines.

(Ingersoll-Sergeant Drill Co.)

The following table gives an approximate idea of the volume of free air required for operating hoisting-engines, the air being delivered at 60 being auge-pressure. There are so many variable conditions to the operation of hoisting-engines in common use that accurate computations can only be hoisting-engines in common use that accurate computations can only be offered when fixed data are given. In the table the engine is assumed to actually run but one-half of the time for hoisting, while the compressor, of course, runs continuously. If the engine runs less than one-half the time, as it usually does, the volume of air required will be proportionately less, and vice versa. The table is computed for maximum loads, which also in practice may vary widely. From the intermittent character of the work of a hoisting-engine the parts are able to resume their normal temperature between the hoists, and there is little probability of the annoyance of freezing the applications of the control of the con ing up the exhaust-passages.

VOLUME OF FREE AIR REQUIRED FOR OPERATING HOISTING-ENGINES, THE AIR COMPRESSED TO 60 POUNDS GAUGE ENGINES, PRESSURE.

SINGLE-CYLINDER HOISTING-ENGINE.

Diam, of Cylinder, Inches.	Stroke, Inches.	Revolu- tions per Minute.	Normal Horse- power.	Actual Horse- power.	Weight Lifted, Single Rope.	Cubic Ft. of Free Air Required.
5 5 614 7 814 814	6 8 8 10 10 12 12	200 160 160 125 125 110	3 4 6 10 15 20 25	5.9 6.8 9.9 12.1 16.8 18.9 26.2	600 1,000 1,500 2,000 3,000 5,000 6,000	75 80 125 151 170 238 330
		DOUBLE-GY	LINDER HO	i əting-en g	INE.	
5 614 7 814 815 10 1214	6 8 8 10 10 19 19 12 15	200 160 160 125 125 110 110 100 90	6 8 12 90 30 40 50 75	11.8 12.6 19.8 24.2 83.6 87.8 52,4 89.2 125.	1,000 1,650 9,500 8,500 6,000 8,000 10,000	150 160 250 302 340 476 660 1,125 1,587

Practical Besults with Compressed Air.—Compressed air System at the Chapin Mines, Iron Mountain, Mich.—These mines are three miles from the falls which supply the power. There are four turbines at the falls, one of 1000 horse-power and three of 900 horse-power each. The pressure is 60 pounds at 60° Fahr. Each turbine runs a pair of compressors. The pipe to the mines is 24 ins. diameter. The power is applied at the mines to Corliss engines, running pumps, hoists, etc., and direct to rock-drills. A test made in 1888 gave 1480.27 H.P. at the compressors, and 890.17 H.P. as the sum of the horse-power of the engines at the mines. Therefore, only 27% of the power generated was recovered at the mines. This includes the loss due to leakage and the loss of energy in heat, but not the friction in the engines or compressors. (F. A. Pocock, Trans. A. I. M. E., 1890.)

W. L. Saunders (Jour. F. I. 1893) says: "There is not a properly designed compressed-air installation in operation to-day that losse over 65 by trans-

compressed-air installation in operation to-day that loses over 5% by transmission alone. The question is altogether one of the size of pipe; and if the

mission alone. The question is a logether one of the size of pipe; and if the pipe is large enough, the friction loss is a small item.

"The loss of power in common practice, where compressed air is used to drive machinery in mines and tunnels, is about 70%. In the best practice, with the best air-compressors, and without reheating, the loss is about 60%. These losses may be reduced to a point as low as 20% by combining the best systems of reheating with the best air-compressors."

Gain due to Heheating.-Prof. Kennedy says compressed air transmission system is now being carried on, on a large commercial scale, in such a fashion that a small motor four miles away from the central station can indicate in round numbers 10 horse-power, for 20 horse-power at the station itself, allowing for the value of the coke used in heating the air. The limit to successful reheating lies in the fact that air-engines cannot

work to advantage at temperatures over 350°.

The efficiency of the common system of reheating is shown by the results obtained with the Popp system in Paris. Air is admitted to the reheater at about 83°, and passes to the engine at about 315°, thus being increased in volume about 42%. The air used in Paris is about 11 cubic feet of free air per minute per horse-power. The ordinary practice in America with cold air is from 15 to 25 cubic feet per minute per horse-power. When the Paris engines were worked without reheating the air consumption was increased to about 15 cubic feet per horse-power per minute. The amount of fuel consumed during reheating is trifling.

Efficiency of Compressed-air Engines.—The efficiency of an air-engine, that is, the percentage which the power given out by the air-engine bears to that required to compress the air in the compressor, depends on the loss by friction in the pipes, valves, etc., as well as in the engine itself. This question is treated at length in the catalogue of the Norwalk Iron Works This duestion is treated at length in the catalogue of the Not walk from the Co., from which the following is condensed. As the friction increases the most economical pressure increases. In fact, for any given friction in a pipe, the pressure at the compressor must not be carried below a certain limit. The following table gives the lowest pressures which should be used at the compressor with varying amounts of friction in the pipe:

An increase of pressure will decrease the bulk of air passing the pipe and its velocity. This will decrease the loss by friction, but we subject ourselves to a new loss, i.e. the diminishing efficiencies of increasing pressures. Yet as each cubic foot of air is at a higher pressure and therefore carries more power, we will not need as many cubic feet as before, for the same work. With so many sources of gain or loss, the question of selecting the proper pressure is not to be decided hastily.

The losses are, first, friction of the compressor. This will amount ordinarily to 15 or 20 per cent, and cannot probably be reduced below 10 per cent. Second, the loss occasioned by pumping the air of the engine-room, rather than the air drawn from a cooler place. This loss varies with the season and amounts from 3 to 10 per cent. This can all be saved. The third loss, or series of losses, arises in the compressing cylinder, viz., insufficient supply, difficult discharge, defective cooling arrangements, poor lubrication, etc. The fourth loss is found in the pipe. This loss varies with the situation, and is subject to somewhat complex influences. The fifth loss is chargeable to fall of temperature in the cylinder of the air-engine. Losses arising from leaks are often serious.

Effect of Temperature of Intake upon the Discharge of a Compressor.—Air should be drawn from outside the engine-room, and from as cool a place as possible. The gain amounts to one per cent for every five degrees that the air is taken in lower than the temperature of the engine-The inlet conduit should have an area at least 50% of the area of the air-piston, and should be made of wood, brick, or other non-conductor of

Discharge of a compressor having an intake capacity of 1000 cubic feet per minute, and volumes of the discharge reduced to cubic feet at atmospheric pressure and at temperature of 62 degrees Fahrenheit:

Requirements of Bock-drills Driven by Compressed Air. (Norwalk Iron Works Co.)—The speed of the drill, the pressure of

Air. (Norwalk Iron Works Co.)—The speed of the drull, the pressure of air, and the nature of the rock affect the consumption of power of drills.

A three-inch drill using air at 30 lbs. pressure made 300 blows per minute and consumed the equivalent of 64 cubic feet of free air per minute. The same drill, with air of 58 lbs. pressure, made 450 blows per minute and consumed 160 cubic feet of free air per minute. At Hell Gate different

machines doing the same work used from 80 to 150 cubic feet free air per

An average consumption may be taken generally from 80 to 100 cubic feet

per minute, according to the nature of the work.

The Popp Compressed air System in Paris.—A most extensive system of distribution of power by means of compressed air is that of M. Popp, in Paris. One of the central stations is laid out for 24,000 horse-power. For a very complete description of the system, see Engineering, Feb. 15, June 7, 21, and 29, 1889, and March 18 and 20, April 10, and May 1, 1891. Also Proc. Inst. M. E., July, 1839. A condensed description will be found in Modern Mechanism, p. 12.

Italization of Compressed Air in Small Motors.—In the

Utilization of Compressed Air in Small Motors.—In the earliest stages of the Popp system in Paris it was recognized that no good results could be obtained if the air were allowed to expand direct into the motor; not only did the formation of ice due to the expansion of the air rapidly accumulate and choke the exhaust, but the percentage of useful work obtained, compared with that put into the air at the central station,

was so small as to render commercial results hopeless.

was so sman as to render connectant results nopeless.

After a number of experiments M. Popp adopted a simple form of castiron stove lined with fire-clay, heated either by a gas jet or by a small coke fire. This apparatus answered the desired purpose until some better arrangement was perfected, and the type was accordingly adopted throughout the whole system. The economy resulting from the use of an improved form was very marked, as will be seen from the following table.

Transcriptor on Arnauma Const

DEFICIENCY OF MIN-HEATING	LITOARG		
		on Box ves.	Wrought- iron Coiled Tubes.
Heating surface, sq. ft. Air heated per hour, cu. ft Temp. of air admitted to oven, deg. F " " at exit, deg. F Total heat absorbed per hour, calories Do, per sq. ft. of heating surface per hour, cals Do. per lb. of coke	20,342 45 215 17,900 1,278	14 11,054 45 364 17,200 1,228 2,058	46.3 38,428 41 347 39,200 830 2,545

The results given in this table were obtained from a large number of trials. From these trials it was found that more than 70% of the total number of calories in the fuel employed was absorbed by the air and transformed into useful work. Whether gas or coal be employed as the fuel, the amount required is so small as to be scarcely worth consideration; according to the experiments carried out it does not exceed 0.2 lb. per horse-power per hour, but it is scarcely to be expected that in regular practice this quantity is not largely exceeded. The efficiency of fuel consumed in this way is at least six times greater than when utilized in a boiler and steam-engine.

According to Prof. Riedler, from 15% to 20% above the power at the central station can be obtained by means at the disposal of the power users, and it has been shown by experiment that by heating the air to 480° F. an in-

creased efficiency of 30% can be obtained.

A large number of motors in use among the subscribers to the Compressed Air Company of Paris are rotary engines developing 1 horse-power and less, and these in the early times of the industry were very extravagant in their consumption. Small rotary engines, working cold air without expansion, used as high as 2330 cu. ft. of air per brake horse-power per hour, and with heated air 1624 cu. ft. Working expansively, a 1 horse-power rotary engine used 1469 cu. ft. of cold air, or 360 cu. ft. of heated air, and a 2-horse-power rotary engine 1059 cu. ft. of cold air, or 847 cu. ft. of air, heated to about 50° C.

The efficiency of this type of rotary motors, with air heated to 50° C., may now be assumed at 43%. With such an efficiency the use of small motors in many industries becomes possible, while in cases where it is necessary to have a constant supply of cold air economy ceases to be a matter of the first

importance.

Tests of a small Riedinger rotary engine, used for driving sewing-machines and indicating about 0.1 H.P. showed an air-consumption of 1877 cu. ft. per H.P. per hour when the initial pressure of the air was 88 lbs. per sq. in. and its temperature 54° F., and 988 cu. ft. when the air was heated to 338° F., its pressure being 72° lbs. With a one-half horse-power variable-expansion rotary engine the air-consumption was from 800 to 900 cu. ft. per H.P. per hour for initial pressures of 54 to 85 lbs. per sq. in. with the air heated from 336° to 388° F., and 1148 cu. ft. with cold air, 40° F., and an initial pressure of 72 lbs. The rollways of air were all taken at expression pressure of 72 lbs. The volumes of air were all taken at atmospheric pressure.

Trials made with an old single-cylinder 80-horse-power Farcot steam-engine, indicating 72 horse-power, gave a consumption of air per brake horse-power as low as 465 cu. ft. per hour. The temperature of admission was 200 F., and of exhaust 95° F.

Prof. Elliott gives the following as typical results of efficiency for various systems of compressors and air-motors:

Simple compressor and simple motor, efficiency	89.1%
Compound compressor and simple motor, "compound motor, efficiency	44.9
" compound motor, efficiency	. 50.7
Triple compressor and triple motor.	8 88

The efficiency is the ratio of the indicated horse-power in the motor cylinders to the indicated horse-power in the steam-cylinders of the compressor. The pressure assumed is 6 atmospheres absolute, and the losses are equal to those found in Paris over a distance of 4 miles.

Summary of Efficiencies of Compressed-air Transmission at Paris, between the Central Station at St. Fargeau and a 10-horse-power Motor Working with Pressure Beduced to 4½ Atmospheres.

(The figures below correspond to mean results of two experiments cold and two heated.)

1 indicated horse-power at central station gives 0.845 indicated horse-power in compressors, and corresponds to the compression of 848 cubic feet of air per hour from atmospheric pressure to 6 atmospheres absolute. (The weight of this air is about 25 pounds.)
0.845 indicated horse-power in compressors delivers as much air as will do

0.52 indicated horse-power in adiabatic expansion after it has fallen in tem-

perature to the normal temperature of the mains.

The fall of pressure in mains between central station and Paris (say 5 kilometres) reduces the possibility of work from 0.52 to 0.51 indicated horsepower.

The further fall of pressure through the reducing valve to 416 atmospheres

(absolute) reduces the possibility of work from 0.51 to 0.50.

Incomplete expansion, wire-drawing, and other such causes reduce the actual indicated horse-power of the motor from 0.50 to 0.89.

By heating the air before it enters the motor to about 320° F., the actual

indicated horse-power at the motor is, however, increased to 0.54. The ratio

of gain by heating the air is, therefore, 0.54 + 0.39 = 1.88,

In this process additional heat is supplied by the combustion of about 0.89 pounds of coke per indicated horse-power per hour, and if this be taken indecedent, the real indicated efficiency of the whole process becomes 0.47 instead of 0.54.

Working with cold air the work spent in driving the motor itself reduces the available horse-power from 0.39 to 0.26.

Working with heated air the work spent in driving the motor itself reduces the available horse-power from 0.54 to 0.44.

A summary of the efficiencies is as follows:

Efficiency of main engines 0.845.

Efficiency of compressors 0.52 + 0.845 = 0.61. Efficiency of transmission through mains 0.51 + 0.52 = 0.98.

Efficiency of reducing valve $0.50 \div 0.51 = 0.98$.

The combined efficiency of the mains and reducing valve between 5 and 4½ atmospheres is thus $0.98 \times 0.98 = 0.96$. If the reduction had been to 4, 8½, or 3 atmospheres, the corresponding efficiencies would have been 0.98, 0.89, and 0.85 respectively.

Indicated efficiency of motor 0.39 + 0.50 = 0.78. Indicated efficiency of whole process with cold air 0.39. Apparent indicated efficiency of whole process with heated air 0.54.

Real indicated efficiency of whole process with heated air 0.47.

Mechanical efficiency of motor, cold, 0.67.

Mechanical efficiency of motor, hot, 0.81.

Most of the compressed air in Paris is used for driving motors, but the work done by these is of the most varied kind. A list of motors driven from St. Fargeau station shows 225 installations, nearly all motors working at 8t. Fargeau station shows 225 installations, nearly all motors working at from ½ horse-power to 50 horse-power, and the great majority of them more than two miles away from the station. The new station at Quai de la Gare is much larger than the one at St. Fargeau. Experiments on the Riedler air-compressors at Parls, made in December, 1991, to determine the ratio between the indicated work done by the air-pistons and the indicated work in the steam-cylinders, showed a ratio of 0.8997. The compressors are driven by four triple-expansion Corliss engines of 2000 horse-power each.

Shops Operated by Compressed Air.—The Iron Age, March 2, 1893, describes the shops of the Wuerpei Switch and Signal Co. East St. Louis, the machine tools of which are operated by compressed air each of the

the machine tools of which are operated by compressed air, each of the larger tools having its own air engine, and the smaller tools being belied from shatting driven by an air engine. Power is supplied by a compound compressor rated at 55 horse-power. The air engines are of the Kriebei

compressor rated at 55 horse-power. The air engines are of the Kriebei make, rated from 2 to 8 horse-power. The air engines are of the Kriebei make, rated from 2 to 8 horse-power.

Pneumatic Postal Transmission.—A paper by A. Falkenau, Eng'rs Club of Philadelphia, April 1894, entitled the "First United States Pneumatic Postal System," gives a description of the system used in London and Paris, and that recently introduced in Philadelphia between the main post-office and a substation. In London the tubes are 2½ and 3 inch lead pipes laid in cast-iron pipes for protection. The carriers used in 2½-inch tubes are but 1½ inches diameter, the remaining space being taken up by packing. Carriers are despatched singly. First, vacuum alone was used; later, vacuum and compressed air. The tubes used in the Continental cities in Europe are wrought iron, the Paris tubes being 2½ inches diameter. There the carriers are despatched in trains of six to ten, propelled by being of cast iron bored to size. The lengths of the outgoing and return ubes are 2998 feet each. The pressure at the main station is 7 lbs., at the substation 4 lbs., and at the end of the return pipe atmospheric pressure. The compressor has two air-cylinders 18 × 24 in. Each carrier holds about 50 letters, but 100 to 150 are taken as an average. Eight carriers may be despatched in a minute, giving a delivery of 48,000 to 72,000 letters per hour, The time required in transmission is about 57 seconds.

Pneumatic postal transmission tubes were laid in 1898 by the Batcheller

Pneumatic postal transmission tubes were laid in 1898 by the Batcheller Preumatic Tobe Co. between the general post-offices in New York and Brooklyn, crossing the East River on the bridge. The tubes are cast iron, 12-tt. lengths, bored to 8½ in. diameter. The joints are bells, calked with lead and yarn. There are two tubes, one operating in each direction. Both lines are operated by air-pressure above the atmospheric pressure. One tube is operated by an air-compressor in the New York office and the other

by one located in the Brooklyn office.

The carriers are 24 in. long, in the form of a cylinder 7 in. in diameter, and are made of steel, with fibrous bearing-rings which fit the tube. Each carrier will contain about 600 ordinary letters, and they are despatched at intervals of 10 seconds in each direction, the time of transit between the two offices being 81/2 minutes, the carriers travelling at a speed of from 80 to 85

miles per hour.

The air-compressors were built by the Rand Drill Co, and the Ingersoll-Sergeant Drill Co. The Rand Drill Co, compressor is of the duplex type and has two steam-cylinders 10 × 20 in. and two air-cylinders 24 × 20 in. delivering 1870 cu. ft. of free air per minute, at 75 revolutions, the power being about 50 H.P. Corliss valve-gear is on the steam-cylinders and the Rand mechanical valve-gear on the air-cylinders.

The Ingersoll-Sergeant Drill Co, furnished two duplex Corliss air-compressors, with mechanically moved valves on air-cylinders. The steam-cylinders are 14 × 18 in. and the air-cylinders 26½ × 18 in. They are designed for 30 to 90 revs. per min. and to compress to 20 lbs. per sq. in. Another double line of pneumatic tubes has been laid between the main office and Postal Station H, Lexington Ave. and 44th St., in New York City. This line is about 3½ miles in length. There are three intermediate stations: Third Ave. and 8th St., Madison Square, and Third Ave. and 28th St. The carriers can be so adjusted when they are put into the tube that the yill traverse the line and be discharged automatically from the tube at the statraverse the line and be discharged automatically from the tube at the sta-tion for which they are intended. The tubes are of the same size as those of the Brooklyn line and are operated in a similar manner. The initial aircompression is about 12 to 15 lbs. On the Brooklyn line it is about 7 lbs.

510 AIR.

There is also a tube system between the New York Post-office and the Produce Exchange. For a very complete description of the system and its machinery see "The Pneumatic Despatch Tube System," by B. C. Batcheller. J. B. Lippincott Co., Philadelphia, 1897.

The Mekarski Compressed air Tramway at Berne,

Switzerland. (Eng'y News, April 20, 1893.)—The Mekarski system has been introduced in Berne, Switzerland, on a line about two miles long, with grades of 0.25% to 3.7% and 5.2%. The air is heated by passing it through superheated water at 330° F. It thus becomes saturated with steam, which subsequently partly condenses, its latent heat being absorbed by the expanding air. The pressure in the car reservoirs is 440 lbs. per sq. in.

The engine is constructed like an ordinary steam tramway locomotive, and drives two coupled axles, the wheel-base being 5.2 ft. It has a pair of outside horizontal cylinders, 5.1×8.6 in.; four coupled wheels, 27.5 in. diameter. The total weight of the car including compressed air is 7.25 tons,

and with 30 passengers, including the driver and conductor, about 9.5 tons.

The authorized speed is about 7 miles per hour. Taking the resistance due to the grooved rails and to curves under unfavorable conditions at 30 lbs. per ton of car weight, the engine has to overcome on the steepest grade, 5%, a total resistance of about 0.63 ton, and has to develop 25 H.P. At the maximum authorized working pressure in cylinders of 176 lbs. per sq. in. the motors can develop a tractive force of 0.64 ton. This maximum is, therefore, just sufficient to take the car up the 5.2% grade, while on the flatter sections of the line the working pressure does not exceed 78 to 147 lbs. per sq. in. Sand has to be frequently used to increase the adhesion on the 2% to

5% grades.

Between the two car frames are suspended ten horizontal compressed-air storage-cylinders, varying in length according to the available space, but of storage-cylinders, varying in length according to the available space, but of uniform inside diameter of 1.7.7 in., composed of riveted 0.27-in. sheet iron, and tested up to 588 lbs. per sq. in. These cylinders have a collective capacity of 64.25 cu. ft., which, according to Mr. Mekarski's estimate, should have been sufficient for a double trip, 5% miles. The trial trips, however, showed this estimate to be inadequate, and two further small storage-cylinders had therefore to be added of 5.3 cu. ft. capacity each, bringing the total cubic contents of the 12 storage-cylinders per car up to 75 cu. ft. divided into two groups the working and the reserve hettary the 75 cu. ft., divided into two groups, the working and the reserve battery, the former of 49 cu. ft. the latter of 26 cu. ft. capacity.

From the results of six official trips, the pressure and the mean consump-

tion of air during a double journey per motor car are as follows:

Pressure of air in storage-cylinders at starting 440 lbs. per sq. in.; at end of up-journey 176 lbs., reserve 260 lbs.; at end of down-journey 103 lbs., reserve 176 lbs. Consumption of air during up-journey 92 lbs., during downjourney 81 lbs.

The working experience of 1891 showed that the air consumption per motor car for a double journey was from 103 to 154 lbs., mean 123 lbs., and

per car mile from 28 to 42 lbs., mean 35 lbs.

The principal advantages of the compressed-air system for urban and suburban tramway traffic as worked at Berne consist in the smooth and noiseless motion; in the absence of smoke, steam, or heat, of overhead or underground conductors, of the more or less grinding motion of most electric cars, and of the jerky motion to which underground cable traction is subject. On all these grounds the system has vindicated its claims as being preferable to any other so far known system of mechanical traction for street tramways. Its disadvantages, on the other hand, consist in the extremely delicate adjustment of the different parts of the system, in the comparatively small supply of air carried by one motor car, which necessitates the car returning to the depot for refilling after a run of only four miles or 40 minutes, although on the Nogent and Paris lines the cars, which are, moreover, larger, and carry outside passengers on the top, run seven miles, and the loading pressure is 547 lbs. per sq. in. as against only 440 lbs. at Berne

Longer distances in the same direction would involve either more powerful motors, a larger number of storage-cylinders, and consequently heavier cars, or loading stations every four or seven miles; and in this respect the system is manifestly inferior to electric traction, which easily admits of a line of 10 to 15 miles in length being continuously fed from one central station without the loss of time and expense caused by reloading.

The cost of working the Berne line is compared in the annexed table

with some other tramways worked under similar conditions by horse and mechanical traction for the year 1891.

For description of the Mekarski system as used at Nantes, France, see

paper by Prof. D. S. Jacobus, Trans. A. I. M. E., xix. 558.

American Experiments on Compressed Air for Street Railways.—Experiments have been made recently in Washington, D.C., and in New York City on the use of compressed air for street-railway traction. The air was compressed to 2000 lbs. per sq. in, and passed through a tion. The air was compressed to 2000 lbs. per sq. in, and passed through a reducing-valve and a heater before being admitted to the engine. For an extended discussion of the relative merits of compressed air and electric traction, with an account of a test of a four-stage compressor giving a pressure of 2500 lbs. per sq. in., see Eng'g News, Oct. 7 and Nov. 4, 1897. A summarized statement of the probable efficiency of compressed-air traction is given as follows: Efficiency of compression to 2000 lbs. per sq. in. 65%. By wire-drawing to 100 lbs. 57.5% of the available energy of the air will be lost, leaving $65 \times .425 = 27.65\%$, as the net efficiency of the air. This may be doubled by heating, making 55.25%, and if the motor has an efficiency of 80% the net efficiency of traction by compressed air will be 55.25%, 30 = 44.2%. For a description of the Hardie compressed air locomotive. desired for

80% the net efficiency of traction by compressed air will be 55.25 × .80 = 44.3%. For a description of the Hardie compressed-air locomotive, designed for street-railway work, see Eng'g News, June 24, 1897. For use of compressed air in mine haulage, see Eng'g News, Feb. 10, 1898.

Compressed Air for Working Underground Pumps in Mines.—Eng'g Record, May 19, 1894, describes an installation of compressors for working a number of pumps in the Nottingham No. 15 Mine, Plymouth, Pa., which is claimed to be the largest in America. The compressors develop above 2300 H.P., and the piping, horizontal and vertical, is 6000 feet in length. About 25,000 gallons of water per hour are raised.

FANS AND BLOWERS.

Contrifugal Fans.—The ordinary centrifugal-fan consists of a number of blades fixed to arms, revolving on a shaft at high speed. The width of the blade is parallel to the axis of the shaft. Most engineers' reference books quote the experiments of W. Buckle, Proc. Inst. M.E., 1847, as still standard. Mr. Buckle's conclusions are given below, together with data of more recent experiments.

Experiments were made as to the proper size of the inlet openings and on Experiments were insue as we have the proper proportions to be given to the vane. The inlet openings in the sides of the fan-chest were contracted from 17½ in., the original diameter,

to 12 and 6 in. diam., when the following results were obtained:

First, that the power expended with the opening contracted to 12 in. diam. was as 214 to 1 compared with the opening of 1714 in. diam.; the velocity of the fan being nearly the same, as also the quantity and density of air delivered.

Second, that the power expended with the opening contracted to 6 in. diam. was as 2½ to 1 compared with the opening of 17½ in. diam.; the velocity of the fan being nearly the same, and also the area of the effiux pipe, but the density of the air decreaced one fourth.

These experiments show that the inlet openings must be made of sufficient

size, that the air may have a free and uninterrupted action in its passage to the blades of the fan; for if we impede this action we do so at the expense

of power.
With a vane 14 in. long, the tips of which revolve at the rate of 236.8 ft. with a vane 14 in. long, the tips of which revolve at the rate of 233.5 it.

per second, air is condensed to 9.4 ounces per square inch above the pressure of the atmosphere, with a power of 9.6 H. P.; but a vane 8 inches long, the diameter at the tips being the same, and having, therefore, the same velocity, condenses air to 6 ounces per square inch only, and takes 12 H. P.

Thus the density of the latter is little better than six tenths of the former,

Thus the density of the latter is little better than six tenths of the former, while the power absorbed is nearly 1.25 to 1. Although the velocity of the tips of the vanes is the same in each case, the velocities of the heels of the respective blades are very different, for, while the tips of the blades in each case move at the same rate, the velocity of the heel of the 14-inch is in the ratio of 1 to 1.67 to the velocity of the heel of the 8-inch blade. The longer blades approaching nearer the centre, strikes the air with less velocity, and allows it to enter on the blade with greater freedom, and with considerably less force than the shorter one. The inference is, that the short blade must take more power at the same time that it accumulates a less quantity of air. These experiments lead to the conclusion that the length of the vane demands as great a consideration as the proper diameter of the inlet opening. If there were no other object in view would be useless to make the vanes of the fan of a greater width than the inlet opening can freely supply. On the proportion of the length and width of the vane and the diameter of the inlet opening rest the three most im-

portant points, viz., quantity and density of air, and expenditure of power. In the 14-inch blade the tip has a velocity 2.6 times greater than the heel; and, by the laws of centrifugal force, the air will have a density 2.6 times greater at the tip of the blade than that at the heel. The air cannot enter on the heel with a density higher than that of the atmosphere; but in its passage along the vane it becomes compressed in proportion to its centrifugal force. The greater the length of the vane, the greater will be the difference of the centrifugal force between the heel and the tip of the blade; consequently the greater the density of the air.

Reasoning from these experiments, Mr. Buckle recommends for easy reference the following proportions for the construction of the fan:

1. Let the width of the vanues be one fourth of the diameter; 2. Let the diameter of the inlet openings in the sides of the fan-chest be one half the diameter of the fan; 8. Let the length of the vanes be one fourth of the diameter of the fan.

In adopting this mode of construction, the area of the inlet openings in the sides of the fan-chest will be the same as the circumference of the heel of the blade, multiplied by its width; or the same area as the space described by the heel of the blade,

Best Proportions of Fans. (Buckle.)

PRESSURE FROM 3 OUNCES TO 6 OUNCES PER SQUARE INCH; OR 5.2 INCHES TO 10.4 INCHES OF WATER.

	neter Fan,		V a:	nes.		of	meter Inlet sen-		meter Fan.		Vai	nes.		of	meter Inlet
		Wi	dth.	Lei	igth.	ir	gs.			Wi	dth.	Let	igth.	ji	igs.
ft.	ins.	ft.	ins.	ft.	ius.	ft.	ins.	ft.	ins.	ft.	ins.	ft.	ins.	££.	ins.
8	0 6	8	9 1016	8	9 1016	1	6	4 5	6 0	1	13/6	1	11/6	2	8
4	ŏ	ĭ	Ŏ,	ĭ	0	Ž	ŏ	6	ŏ	i	6	i	6	8	ŏ

PRESSURE FROM 6 OUNCES TO 9 OUNCES PER SQUARE INCH, AND UPWARDS, OR 10.4 INCHES TO 15.6 INCHES OF WATER.

8 8	b 6	0 0	7 814 912	1 1	0 116 812	1	9	4 5 6	6	0	1016	1	41.6 6	1 2	9 0
4	v	10	878	1	872	1	•	ь	Ψ,	1	2	1	10	×	4

The dimensions of the above tables are not laid down as prescribed limits. but as approximations obtained from the best results in practice.

Experiments were also made with reference to the admission of air into Experiments were also made with reference to the admission of air this pipe was varied from 12 to 4 inches. The object of this was to proportion the opening to the quantity of air required, and thereby to lessen the power necessary to drive the fan. It was found that the less this opening is made, provided we produce sufficient blast, the less noise will proceed from the fan; and by making the tops of this opening level with the tips of the vane, the nellymp of air has little out to provide the value of the selection of the vane. the column of air has little or no reaction on the vanes.

The number of blades may be 4 or 6. The case is made of the form of an arithmetical spiral, widening the space between the case and the revolving blades, circumferentially, from the origin to the opening for discharge.

The following rules deduced from experiments are given in Spretson's

treatise on Casting and Founding:
The fan-case should be an arithmetical spiral to the extent of the depth

of the blade at least.

The diameter of the tips of the blades should be about double the diameter of the hole in the centre; the width to be about two thirds of the radius of the tips of the blades. The velocity of the tips of the blades should be rather

more than the velocity due to the air at the pressure required, say one

eighth more velocity.

In some cases, two fans mounted on one shaft would be more useful than one wide one, as in such an arrangement twice the arra of inlet opening is obtained as compared with a single wide fan. Such an arrangement may be adopted where occasionally half the full quantity of air is required, as one of them may be put out of gear, thus saving power.

Pressure due to Velocity of the Fan-blades.—"By increasing the number of revolutious of the fan the head or pressure is increased.

the law being that the total head produced is equal (in centrifugal fans) to twice the height due to the velocity of the extremities of the blades, or

 $H = \frac{v^2}{c}$ approximately in practice " (W. P. Trowbridge, Trans. A. S. M. E.,

vii. 536.) This law is analogous to that of the pressure of a jet striking a plane surface. T. Hawksley, Proc. Inst. M. E., 1882, vol. $\ln x$. asys: "The pressure of a fluid striking a plane surface perpendicularly and then escaping at right angles to its original path is that due to twice the height h due the velocity."

(For discussion of this question, showing that it is an error to take the ressure as equal to a column of air of the height $h = v^2 + 2g$, see Wolff on

pressure as equal to a column of all of the longer pressure as equal to a column of all of the longer pressure as that the velocity of the tips of the fan is equal to nine tenths of the velocity a body would acquire in falling the height of a homogeneous column of air equivalent to the density." D. K. Clark (R. T. & D., p. 924), paraphrasing Buckle, apparently, says: "It further appears that the pressure generated at the circumferternoe is one ninth greater than that which is due to the actual circumferential velocity of the fan." The two statements, however, are not in harmony, for if $v = 0.9 \sqrt{2gH}$, $H = \frac{v^2}{0.81 \times 2g} = 1.284 \frac{v^2}{2g}$ and not $1\frac{v^2}{2g}$.

If we take the pressure as that equal to a head or column of air of twice the height due the velocity, as is correctly stated by Trowbridge, the paradoxical statements of Buckle and Clark—which would indicate that the actual pressure is greater than the theoretical-are explained, and the formula becomes $H = .617 \frac{v^2}{-}$ and $v = 1.278 \sqrt{gH} = 0.9 \sqrt{2gH}$, in which H is the head of a column producing the pressure, which is equal to twice the theoretical head due the velocity of a falling body (or $h = \frac{v^2}{2g}$), multiplied by the coefficient .617. The difference between 1 and this coefficient expresses the loss of pressure due to friction, to the fact that the inner portions of the blade have a smaller velocity than the outer edge, and probably to other causes. The coefficient 1.273 means that the tip of the blade must be given a velocity 1.273 times that theoretically required to produce the head H.

To convert the head H expressed in feet to pressure in lbs. per sq. in multiply it by the weight of a cubic foot of air at the pressure and temperature of the air expelled from the fan (about .08 lb. usually) and divide by 144. Multiply this by 16 to obtain pressure in ounces per sq. in, or by 2.085 to obtain inches of mercury, or by 27.71 to obtain pressure in inches of water column. Taking .08 as the weight of a cubic foot of air,

> = .00001066 v^2 ; $v = 810 \sqrt{p}$ nearly; p lbs. per sq. in. p_1 ounces per sq. in. = .0001706 v^2 ; $v = 80 \sqrt[4]{p_1}$ p_2 inches of mercury = .00002169 v^2 ; v = 220 4 p_2 inches of water = .0002954 v^2 ; v = 60

in which v = velocity of tips of blades in feet per second.

Testing the above formula by the experiment of Buckle with the vane 24 inches long, quoted above, we have $p = .00001066v^2 = 9.56$ oz. The experiment gave 9.4 oz.

Testing it by the experiment of H. I. Snell, given below, in which the circumferential speed was about 150 ft. per second, we obtain 3.85 ounces, while the experiment gave from 2.88 to 8.50 ounces, according to the amount of opening for discharge. The numerical coefficients of the above formulæ are all based on Buckle's statement that the velocity of the tips of the fan is equal to nine tenths of the velocity a body would acquire in falling the

height of a homogeneous column of air equivalent to the pressure. Should other experiments show a different law, the coefficients can be corrected accordingly. It is probable that they will vary to some extent with different proportions of fans and different speeds.

Taking the formula v=80 $\sqrt{p_1}$, we have for different pressures in ounces per square inch the following velocities of the tips of the blades in feet per second:

A rule in App. Cyc. Mech., article "Blowers," gives the following velocities of circumference for different densities of blast in ounces: 8, 170; 4, 180; 5, 185; 6, 205; 7, 215.

The same article gives the following tables, the first of which shows that the density of blast is not constant for a given velocity, but depends on the ratio of area of nozzle to area of blades:

QUANTITY OF AIR OF A GIVEN DENSITY DELIVERED BY A FAN.

Total area of nozzles in square feet × velocity in feet per minute corresponding to density (see table) = air delivered in cubic feet per minute.

Density, ounces per sq. in.	Velocity, feet per minute.	Density, ounces per sq. in.	Velocity, feet per min.	Density, ounces per sq. in.	Velocity, feet per minute.
1	5000	5	11,000	9	15,000
2	7000	6	12,250	10	15,800
8	8600	7	18,200	11	16,500
4	10,000	8	14.150	12	17,800

Experiments with Blowers. (Henry I. Snell, Trans. A. S. M. E. ix. 51.)—The following tables give velocities of air discharging through an aperture of any size under the given pressures into the atmosphere. The volume discharged can be obtained by multiplying the area of discharged opening by the velocity, and this product by the coefficient of contraction: .65 for a thin plate and .93 when the orifice is a conical tube with a convergence of about 3.5 degrees, as determined by the experiments of Weisbach. The tables are calculated for a barometrical pressure of 14.69 lbs. (=

235 oz.), and for a temperature of 50° Fahr., from the formula $V=\sqrt{2gh}$. Allowances have been made for the effect of the compression of the air,

but none for the heating effect due to the compression.

At a temperature of 50 degrees, a cubic foot of air weighs .078 lbs., and calling g = 82.1602, the above formula may be reduced to

$$V_1 = 60 \sqrt{31.5812 \times (285 + P) \times P_1}$$

where V_1 = velocity in feet per minute. P= pressure above atmosphere, or the pressure shown by gauge, in ozper square inch.

Pressure per sq. in. in inches of water.	Corresponding Pressure in oz. per sq. inch.	Velocity due the Pressure in feet per minute.	Pressure per sq. in. in inches of water.	Corresponding Pressure in oz. per sq. inch.	Velocity due the Pressure in feet per minute.
1/32 1/16 1/6 3/16 14 5/16	.01817 .03634 .07268 .10902 .14536 .18170 .21804	696.78 987.66 1393.75 1707.00 1971.30 2204.16 2414.70 2788.74	568 1144 1144 1144 1144 1144 1144	.36340 .43608 .50870 .58140 .7267 .8721 1.0174 1.1628	3118.38 3416.64 3690.62 8946.17 4362.63 4836.06 5224.98 5587.58

1462,20

1550.70 1635.00

Pressure in oz. per sq. inch.	Velocity due the Pressure in ft. per minute.		Velocity due the Pressure in ft. per minute.		Velocity due the Pressure in ft. per minute.	Pressure	Velocity due the Pressure in ft. per minute.
.25 .50 .75 1.00 1.25 1.50 1.75 2.00	2,582 3,658 4,482 5,178 5,792 6,349 6,801 7,838	2.25 2.50 2.75 3.00 3.50 4.00 4.50 5.00	7,787 8,213 8,618 9,006 9,739 10,421 11,065 11,676	5.50 6.00 6.50 7.00 7.50 8.00 9.00 10.00	12,259 12,817 13,354 13,878 14,874 14,861 15,795 16,684	11.00 12.00 13.00 14.00 15.00 16.00	17,534 18,350 19,138 19,901 20,641 21,360
Pressure per squ	e in ounce uare inch.	per n	y in feet ninute.	Pressure per squ	e in ounce pare inch.		in feet per nute.

Experiments on a Fan with Varying Discharge-opening. Revolutions nearly constant.

895.26

1033.86

Revolutions per minute.	Area of Discharge in square inches.	Observed Pressure in ounces.	Volume of Air dis- charged per min., cubic feet.	Horse-power.	Actual Number of cu. ft. of Air de- livered per H.P.	Theoret. Vol. per min. that may be discharged with 1H.P. at corresp. Pressure.	Efficiency of Blowers as per Experiment.
1519 1479 1480 1471 1485 1485 1465 1468 1500 1426	0 6 10 20 28 86 40 44 48 89.5	3.50 3.50 3.50 3.50 3.50 3.40 3.25 3.00 2.38	0 406 676 1353 1894 2400 2605 2752 3002 3972	.80 1.15 1.30 1.95 2.55 3.10 3.30 3.55 3.80 4.80	353 520 694 742 774 790 775 790 827	1048 1048 1048 1048 1048 1078 1126 1222 1222 1544	.337 .496 .66 .709 .718 .70 .635 .646

The fan wheel was 23 inches in diameter, 65% inches wide at its periphery,

The fan wheel was 23 inches in diameter, 6% inches wide at its periphery, and had an inlet of 12½ inches in diameter on either side, which was partially obstructed by the pulleys, which were 5 9/16 inches in diameter. It had eight blades, each of an area of 45.49 square inches.

The discharge of air was through a conical tin tube with sides tapered at an angle of 3½ degrees. The actual area of opening was 7% greater than given in the tables, to compensate for the vena contracta.

In the last experiment, 89.5 sq. in. represents the actual area of the mouth of the blower less a deduction for a narrow strip of wood placed across it for the purpose of holding the pressure-gauge. In calculating the volume of air discharged in the last experiment the value of vena contracta is taken at

Experiments were undertaken for the purpose of showing the results obtained by running the same fan at different speeds with the discharge-opening the same throughout the series.

The discharge-pipe was a conical tube 814 inches inside diameter at the end, having an area of 56.74, which is 7% larger than 58 sq. inches; therefore 58 square inches, equal to 368 square feet, is called the area of discharge, as that is the practical area by which the volume of air is computed.

Experiments on a Fan with Constant Discharge-opening and Varying Speed.—The first four columns are given by Mr. Snell, the others are calculated by the author.

Revs. per min.	Pressure in ounces, p	Vol. of Air in cu. ft. per minute, V.	Horse-power.	Velocity of Tips of Blades, ft. per sec.	Velocity due Pressure from Formula $v = 80 \ Vp$.	Coefficient of Formula $v = x \sqrt{p}$ from Experiment.	Velocity of Air per minute in Efflux Pipe, V + .368.	Theoretical Horse- power.	Efficiency per cent.
600 800 1000 1200 1400 1600 1800 2000	.50 .88 1.38 2.00 2.75 8.80 4.80 5.95	1886 1787 2245 2712 3177 8670 4172 4674	.25 .70 1.85 2.20 8.45 5.10 8.00 11.40	60.2 80.8 100.4 120.4 140.5 160.6 180.6 200.7	56.6 75.0 94. 118. 138. 156. 175.	85.1 85.6 85.4 85.1 84.8 82.4 82.4 85.6	3,630 4,856 6,100 7,870 8,633 9,978 11,337 12,701	.182 .429 .845 1.479 2.288 3.803 5.462 7.586	73 61 63 67 66 74 68 67

Mr. Snell has not found any practical difference between the efficiencies of blowers with curved blades and those with straight radial ones.

From these experiments, says Mr. Snell, it appears that we may expect to receive back 65% to 75% of the power expended, and no more.

The great amount of power often used to run a fan is not due to the fan itself, but to the method of selecting, erecting, and piping it.

(For opinions on the relative merits of fans and positive rotary blowers, see discussion of Mr. Snell's paper, Trans. A. S. M. E., ix. 66, etc.)

Comparative Efficiency of Fans and Positive Blowers.—
(H. M. Howe, Trans. A. I. M. E., x. 482.)—Experiments with fans and positive (Baker) blowers working at moderately low pressures, under 20 ounces, show that they work more efficiently at a given pressure when delivering large volumes (i.e., when working nearly up to their maximum capacity) than when delivering comparatively small volumes. Therefore, when great varieties in the cutostic results and resource of bloot required entire the ations in the quantity and pressure of blast required are liable to arise, the highest efficiency would be obtained by having a number of blowers, always driving them up to their full capacity, and regulating the amount of blast by altering the number of blowers at work, instead of having one or two very large blowers and regulating the amount of blast by the speed of the il blowers.

There appears to be little difference between the efficiency of fans and of Baker blowers when each works under favorable conditions as regards

Baker blowers when each works under favorable conditions as regards quantity of work, and when each is in good order.

For a given speed of fan, any diminution in the size of the blast-orifice decreases the consumption of power and at the same time raises the pressure of the blast; but it increases the consumption of power per unit of orifice for a given pressure of blast. When the orifice has been reduced to the normal size for any given fan, further diminishing it causes but slight elevation of the blast pressure; and, when the orifice becomes comparatively small, further diminishing it causes no sensible elevation of the blast pressure, which remains practically constant, even when the orifice is entirely closed. entirely closed.

Many of the failures of fans have been due to too low speed, to too small pulleys, to improper fastening of belts, or to the belts being too nearly vertical; in brief, to bad mechanical arrangement, rather than to inherent defects in the principles of the machine.

If several fans are used, it is probably essential to high efficiency to provide a separate blast pipe for each (at least if the fans are of different size or speed), while any number of positive blowers may deliver into the same pipe without lowering their efficiency.

Capacity of Fans and Blowers.

The following tables show the guaranteed air-supply and air-removal of leading forms of blowers and exhaust fans. The figures given are often exceeded in practice, especially when the blowers and fans are driven at higher speeds than stated. The ratings, particularly of the blowers, are below those generally given in catalogues, but it was the desire to present only conservative and assured practice. (A. R. Wolff on Ventilation.)

QUANTITY OF AIR SUPPLIED TO BUILDINGS BY BLOWERS OF VARIOUS SIZES.

Diam- eter of Wheel in feet.		power to Drive	Capacity cu, ft. per min. against a Pressure of 1 ounce per sq. in.	Diam- eter of Wheel in feet.	of Revs.	power to Drive Blower.	Capacity cu. ft. per min, against a Pressure of 1 ounce per sq. in.
4 5 6 7	850 325 275 230 200	6. 9.4 18.5 18.4 24	10,635 17,000 29,618 42,700 46,000	9 10 12 14 15	175 160 180 110 100	29 85.5 49.5 66	56,800 70,340 102,000 189,000 160,000

If the resistance exceeds the pressure of one ounce per square inch, of above table, the capacity of the blower will be correspondingly decreased, or power increased, and allowance for this must be made when the distributing ducts are small, of excessive length, and contain many contractions and bends.

QUANTITY OF AIR MOVED BY AN APPROVED FORM OF EXHAUST FAN, THE FAN DISCHARGING DIRECTLY FROM ROOM INTO THE ATMOSPHERE.

eter of Wheel	Ordinary Number of Revs. per min.	power to Drive		eter of Wheel	Ordinary Number of Bevs, per min.	power to Drive	Capacity in cu. ft. per min.
2.0	600	0.50	5,000	4.0	475	8.50	28,000
2.5	550	0.75	8,000	5.0	850	4.50	85,000
3.0	500	1.00	12,000	6.0	800	7.00	50,000
8.5	500	2.50	20,000	7.0	250	9.00	80,000

The capacity of exhaust fans here stated, and the horse-power to drive them, are for free exhaust from room into atmosphere. The capacity decreases and the horse-power increases materially as the resistance, resulting from lengths, smaliness and bends of ducts, enters as a factor. The difference in pressures in the two tables is the main cause of variation in the respective records. The fan referred to in the second table could not be used with as high a resistance as one ounce per square inch, the rated resistance of the blowers.

Caution in Regard to Use of Fan and Blower Tables.— Many engineers report that manufacturers' tables overrate the capacity of their fans and underestimate the horse-power required to drive them. In some cases the complaints may be due to restricted air outlets, long and crooked pipes, slipping of belts, too small engines, etc.

. . .

CENTRIFUGAL FANS. Flow of Air through an Orifice.

VELOCITY, VOLUME. AND H P. REQUIRED WHEN AIR UNDER GIVEN PRESSURE IN OUNCES PER SQ. IN. IS ALLOWED TO ESCAPE INTO THE ATMOSPHERE.

(B. F. Sturtevant Co.)

Pressure in ounces per sq. in.	Velocity, ft. per min.	Volume through 1 sq. in. Effec- tive Area, cu. ft. per min.	Horse-power to move the Given Volume of Air.	Horse-power per 1000 cu. ft. per min.	Pressure in ounces per sq. in.	Velocity, ft. per min.	Volume through 1 sq. in. Effec- tive Area, cu. ft. per min.	Horse-power to move the Given Volume of Air.	Horse-power per 1000 cu. ft. per min.
TO THE PERSON OF	1,828 2,585 3,165 3,654 4,084 4,473 4,330 5,478 5,768 6,048 6,315 6,571 6,818 7,055	12.69 17.95 21.98 25.87 28.36 81.06 33.54 35.85 88.01 40.06 42.00 43.86 45.63 47.34 49.00	.00043 .00122 .00225 .00346 .00483 .00635 .00600 .00978 .01166 .01366 .01575 .01794 .02022 .02260	.0840 .0680 .1022 .1263 .1703 .2044 .2385 .2728 .3068 .3410 .3750 .4090 .4431 .4772 .5112	**************************************	7,284 7,507 7,722 7,982 8,136 8,528 8,718 8,528 8,718 9,084 9,262 9,485 9,606 9,773 9,938 10,100	55.08 56.50 57.88 59.22 60.54 61.83 63.08 64.32 65.52 66.71 67.87 69.01	.02759 .03021 .03291 .03568 .03852 .04144 .04442 .04747 .05058 .05376 .05701 .06031 .06368 .06710 .07058	.5454 .5795 .6186 .6476 .6818 .7160 .7500 .7841 .8180 .8522 .8863 .9205 .9546 .9887 1.0567

The headings of the 2d and 3d columns in the above table have been abridged from the original, which read as follows: Velocity of dry air, 50° F., escaping into the atmosphere through any shaped orifice in any pipe or reservoir in which the given pressure is maintained. Volume of air in cubic feet which may be discharged in one minute through an orifice having an effective area of discharge of one square inch. The 5th column, not in the original, has been calculated by the author. The figures represent the horse-power theoretically required to move 1000 cu. ft. of air of the given pressures through an orifice, without allowance for the work of compression or for friction or other losses of the fan. These losses may amount to from 60% to 100% of the given horse-power.

60% to 100% of the given horse-power.

The change in density which results from a change in pressure has been taken into account in the calculations of the table. The volume of air at a given velocity discharged through an orifice depends upon its shape, and is always less than that measured by its full area. For a given effective area the volume is proportional to the velocity. The power required to move air through an orifice is measured by the product of the velocity and the total resisting pressure. This power for a given orifice varies as the cube of the velocity. For a given volume it varies as the square of the velocity. In the movement of air by means of a fan there are unavoidable resistances which, in proportion to their amount, increase the actual power consider-

ably above the amount here given.

For any size of centrifugal fan there exists a certain maximum area over which a given pressure may be maintained, dependent upon and proportional to the speed at which it is operated. If this area, known as its "capacity area," or square inches of blast, be increased, the pressure is lowered (the volume being increased), but if decreased the pressure remains constant. The revolutions of a given fan necessary to maintain a given pressure under these conditions are given in the table on p. 519, which is based upon the abve table. The pressure produced by a given fan and its effective capacity area being known, its nominal capacity and the horse-power required, without allowance for frictional losses, may be determined from the table above.

In practice the outlet of a fan greatly exceeds the capacity area; hence the volume moved and the horse-power required are in excess of the

amounts determined as above.

Steel-plate Full Housing Fans. (Buffalo Forge Co.)

Capacities in cubic feet of air per minute. (See also table on p. 525.)

Size,	Revolutions per Minute.												
in.	100	150	200	250	300	850	400	450	500	550	600		
50	1650	2475	3300	4125	4950	5775	6600	7425	8250	9075	9900		
60	2480	37:20	4960	6200	7440	8680	9920	11160	12400	18640	14880		
70	4500	6750	9000	11250	13500	15750	18000	20250	22500				
80	7070	10605	14140	17675	21210	24745	28280	31815					
90	10400	15600	20800	26000	31200	36400	41600						
100	14280	21420	28560	35700	42840	49980	57120						
110	18960	28440	37920	47400	56880	66360							
120	24800	37200	49600	65000	74400	'		- 1					
130	31200	46800	62400		109200		i I						
140	38354	57531	76708	95885									
150	49260	73890	98520	123150									

The Sturtevant Steel Pressure-blower Applied to Cupola Furnaces and Forges.

		Cupola l	Furnaces.		Fo	rges.
Number of Blower.	Diameter of Cupola inside of Lining, in.	Melting Capacity of Cupola per hour in lbs.		produce required	Number of Forges supplied by Blower.	Rev. per min.Blower necessary to produce pressure for forge fire.
4/0 2/0				-	1 2 3	5,548 4,294 8,645
1 2 3	22 26 30	1,200 1,900 2,900	5 6 7	3,569 3,282 3,030	4 6 8 10	3,199 2,691 2,305
· 4 5 6	35 40 46 53	4,200 6,200 8,900 12,500	8 10 12 14	2,818 2,690 2,670 2,316	10 14 19 25	2,009 1,722 1,567 1,264
8 9 10	60 72 84	16,500 24,000 34,000	14 16 16	2,023 1,854 1,627	35 45 60	1,104 950 834

The above table relates to common cupolas under ordinary conditions and to forges of medium size. The diameter of cupola given opposite each size blower is the greatest which is recommended; in cases where there is a surplus of power one size larger blower may be used to advantage. The melting capacity per hour is based upon an average of tests on some of the best cupolas found, and is reliable in cases where the cupola is well constructed and carefully operated. The blast-pressure required in wind-box is the maximum under ordinary conditions when coal is used as fuel. When coke is employed the pressure may be lower.

The cupola pressures given are those in the wind-box, while the basis pressure for forges is 4 ounces in the tuyere pipe. The corresponding revolutions of fan given are in each case sufficient to maintain these pressures at the fan outlet when the temperature is 50°. The actual speed must be higher than this by an amount proportional to the resistance of pipes and the increase of temperature, and can only be determined by a knowledge of

the existing conditions.

(For other data concerning Cupolas see Foundry Practice.)

Diameters of Blast-pipes Required for Steel Pressureblowers, (B. F. Sturtevant Co.)

Based on the loss of pressure resulting from transmission being limited to one-half ounce per square inch.

Pres-	Length of Pipe													
sure per sq. in.	in ft.		2/0	0	1	2	3	4	5	6	7	8	9	10
4 02.	100 200 300 400	494 596 578 618	5% 6% 7% 7%	61/4 73/4 81/4	656 758 814 8%	71/8 81/8 87/8 95/8	814 914 1016 1034	836 958 1098 11	1016	1134	1416 1514	1616	1514 1714 19 2018	231/3 251/3
8 oz.	100 200 300 400	53/8 61/8 65/8 71/8	61/6 71/6/8 85/8	71/6 81/4 87/8 91/6	936	816 938 10 1058	1056	1176	1036 12 13 1334	1314 1414	161/6 171/6	1876	215%	2614
12 02.	100 200 300 400	534 696 754 756	71/6 81/6 84/4 93/8	794 876 996 10]4	1016	107/8	1116	1174	127/8	1436	1756	20%	1876 2156 2356 2476	284
16 oz.	100 200 300 400	616 7 756 818	896 936		978	914 1058 1116 1214	1216	1356	1356	1596	1836	2116 2337	1976 2278 2478 2614	301

"The above table has been constructed on the following basis: Allowing a loss of pressure of ½ oz. in the process of transmission through any length of pipe of any size as a standard, the increased friction due to lengthening the pipe has been compensated for by an enlargement of the pipe sufficient to keep the loss still at ½ oz. Thus if air under a pressure of 8 oz. is to be delivered by a No. 6 blower, through a pipe 100 ft. in length, with a loss of ½ oz. pressure, the diameter of the pipe must be 11¾ in. If its length is increased to 400 ft. its diameter should also be increased to 15¼ in., or if the pressure be increased to 12 oz. the pipe, if 100 ft. long, must be 11.5½ in., in diameter, providing the loss of ½ oz. is not to be exceeded. This loss of ½ oz. is to be added to the pressure to be maintained at the fan if the tabulated pressure is to be secured at the other end of the pipe."

Efficiency of Fans.—Much useful information on the theory and practice of fans and blowers, with results of tests of various forms, will be found in Heating and Ventilation, June to Dec. 1897, in papers by Prof. R. C. Carpenter and Mr. W. G. Walker. It is shown by theory that the volume of air delivered is directly proportional to the speed of rotation, that the pressure varies as the square of the speed, and that the horse-power varies as the cube of the speed. For a given volume of air moved the horse-power varies as the square of the speed, showing the great advantage of large fans at slow speeds over small fans at high speeds delivering the same volume. The theoretical values are greatly modified by variations in practical conditions. Prof. Carpenter found that with three fans running at a speed of 6200 ft. per minute at the tips of the vanes, and an air pressure of 2½ in. of water column, the mechanical efficiency, or the horse-power of the air delivered divided by the power required to drive the fan, ranged from 3% to 47%, under different conditions, but with slow speeds it was much less, in some cases being under 20%. Mr. Walker in experiments on disk fans found efficiencies ranging all the way from 7.4% to 40%, the size of the fans and the speed being constant, but the shape and angle of the blades varying. It is evident that there is a wide margin for improvements in the forms of fans and blowers, and a wide field for experiment to determine the conditions that will give maximum efficiency.

Centrifugal Ventilators for Mines.—Of different appliances for ventilating mines various forms of centrifugal machines having proved their efficiency have now those completely replaced all others. Most if not all of the machines in use in this country are of this class, being either open-periphery fans, or closed, with chimney and spiral casing, of a more or less modified Guibal type. The theory of such machines has been demonstrated by Mr. Daniel Murgue in "Theories and Practices of Centrifugal Ventilating Machines," translated by A. L. Stevenson, and is discussed in a paper by R. Van A. Norris, Trans. A. I. M. E. xx. 687. From this paper the following formules are taken: mulæ are taken:

Let a =area in sq. ft. of an orifice in a thin plate, of such area that its resistance to the passage of a given quantity of air equals the

ensume to the passage of a given quantity of air equals the resistance of the mine;

o = orifice in a thin plate of such area that its resistance to the passage of a given quantity of air equals that of the machine;

Q = quantity of air passing in cubic feet per minute;

V = velocity of air passing through a in feet per second;

V = velocity of air passing through o in feet per second;

b = head in feat air column to produce valcating V.

h = head in feet air-column to produce velocity V; $h_0 = \text{head}$ in feet air-column to produce velocity V_0 .

$$Q=0.65aV; \quad V=\sqrt{2gh}; \quad Q=0.65a\sqrt{2gh};$$

$$a=\frac{Q}{0.65\sqrt{2gh}}=\text{equivalent orifice of mine};$$

or, reducing to water-gauge in inches and quantity in thousands of feet per minute,

$$\alpha = \frac{.408Q}{\sqrt{W.G.}}; \quad Q = 0.65oV_0; \quad V_0 = \sqrt{2gh_0}; \quad Q = 0.65o\sqrt{2gh_0};$$

$$o = \sqrt{\frac{Q^2}{0.65^3h_0^2g}} = \text{equivalent orifice of machine.}$$

The theoretical depression which can be produced by any centrifugal ventilator is double that due to its tangential speed. The formula

$$H = \frac{T^2}{2q} - \frac{V^2}{2q},$$

in which T is the tangential speed, V the velocity of exit of the air from the space between the blades, and H the depression measured in feet of air-column, is an expression for the theoretical depression which can be produced by an uncovered ventilator; this reaches a maximum when the air leaves the blades without speed, that is, V=0, and $H=T^2+2g$. Hence the theoretical depression which can be produced by any uncovered ventilator is equal to the height due to its tangential speed, and one halfthat which can be produced by a covered ventilator with expanding sellower.

So long as the condition of the mine remains constant:

The volume produced by any ventilator varies directly as the speed of rotation. The depression produced by any ventilator varies as the square of the

speed of rotation.

For the same tangential speed with decreased resistance the quantity of air increases and the depression diminishes.

The following table shows a few results, selected from Mr. Norris's paper, giving the range of efficiency which may be expected under different circumstances. Details of these and other fans, with diagrams of the results are given in the paper.

Experiments on Mine-ventilating Fans.

-	h l	ਰਂ.	l •.	Air	· t	per-	(.	1 4	نە ئە	8	l÷.
i	Revolutions per Minute, Fan.	eriphery Speed, Feet per Min.	Air e.	Subic Feet A per Revolution	Cubical Contents of Fan-blades.	Sub. Feet Air per 100 Feet Periph- ery Motion.	Water-gauge, Inches.	1	Horse- Engine.	Efficiency Engine and Fan.	nt Ori- Mine, Feet.
- 1	Fe	Sp	Cubic Feet A per Minute.	E 25	15.0	b. Feet Air Feet Perip ery Motion	2 %	- power	ĦĞ	Enga	quivalent O fice of Mine, Square Feet.
- 1	e,	F 5	∳.∄	Feet	25	55.5	ter-gau Inches.	- po Air.	고픈	P	Equivalent fice of M Square F
- 1	evolutic Minute,	Periphery Feet per	52	_ 5	2 G	9 9 A	a a	- F	Indicated power of	gă	E 2 E
ایا	o u	<u> </u>	5 5	Cubic per R	-2g-E-	HE E	, a,	Horse	1 5 5 E	5 ₹	5 6 5.
Fan.	ĕ.⊠	96	5™	≱દ્ર	ap of	Cub. 100 F	=	ē	5 8	8	£ co
124		<u> </u>		07	0_	0-		<u> </u>	iπα	B	<u> </u>
را	84	5517	286,684	2818	3040	4290	1.80	67.13	88.40	75.9) &
A {]	100	6282 6978	836,862	3369	3040	5398	2.50	132.70	155.43	85.4	1 8
- 11	111	6978	847,396	8180	8040	5002	8.20	175.17	209.64	83.6	Av'ge
- 9	128	7727	894,100	8204	8040	. 5100	8.60	223.56	295.21	75.7	112
Β {	100 130	6282 8167	188,888 274,876	1889 2114	1520 1520	3007 3366	1.40 2.00	41.67 86.63	97.99 194.95	42.0	22
- 1	59	8702	59,587	1010	1520	1610	1.20	11.27	16 76	67.83	22
C }	83	5208	82,969	1000	1520	1593	2.15	27.86	48.54	57 38	
511	40	8140	49,611	1240	3096	1580	0.87	6.80	13.82	49.2	32
D {	70	5495	137.760	1825	3096	2507	2.55	55.35	67.44	82.07	
- (I	50	2749	147,232 205,761	2944	1522	5356	0.50	11.60	67.44 28.55	40.68	
E {	69	8793	205,761	2982	1522	5451	1.00	32.42	45.98	70.50	83
- 9	96	5278	299,600	3121	1522	5676	2.15 3.35	101.50	120.64	84.10	
-11	200	7540	133,198	666 904	746	1767	8.35	70.30	102.79	68.40	26.9
\mathbf{F}	200	7540	180,909	904	746	2398	3.05 2.80	86.89	129.07	67.80	38.8
- 51	200 10	7010	209,150 28,896	1046 2890	746 3022	2774	0.10	0.45	150.08 1.30	61.70	46.3
- 11	20	1570	57,120	2856	90-20	3680 3637	0.20	1.80	8.70	40	l
- 11	25	7540 785 1570 1962	66,640	2665	3022 3022	8399	0.29	2.90	6.10	18	l
- 11	30	2355	73,080	2486	8022	8103	0.40	4.60	9.70	47.	52
~ 11	85	2747	94,080	2688	8022	3425	0.50	7.40	15.00	48.	
G {	40	8140	119,000	2800	8022	3567	0.70	12.30	24.90	49.	
- 11	50	8925	132,700	2654	8022	8381	0.90	18.80	38.80	48.	ļ
- 11	60	4710	173,600	2893	3022	3686	1.35	36.90	66.40	55.	
- 11	70	5495	203,280	2904	8022	8718	1.80	57.70	107.10	54.	
<u> U</u>	80	6280	222,320	2779	3022	3540	2.25	78.50	152.60	52.	

	Type of Fan.	Diam.	Width.	No. Inlets.	Diam. Inlets	š,
Α.	Guibal, double	20 ft.	6 ft.	4	8 ft. 10 in.	
	Same, only left hand running.		6	4	8 10	
C.	Guibal	20	6	2	8 10	
	Guibal		8	1	11 6	
	Guibal, double		4	4	8	
	Capell		10	2	7	
G.	Guìbal	25	8	1	12	

An examination of the detailed results of each test in Mr. Norris's table shows a mass of contradictions from which it is exceedingly difficult to draw any satisfactory conclusions. The following, he states, appear to be more or less warranted by some of the figures:

1. Influence of the Condition of the Airways on the Fan.—Mines with varying equivalent orifices give air per 100 feet periphery-motion of fan, within limits as follows, the quantity depending on the resistance of the mine:

mine:

	Cu. Ft. Air per 00 ft. Periphery- speed.	Aver- age.		Cu. Ft. Air per 100 ft. Periphery- speed.	Aver- age.
Under 20 sq. ft. 20 to 80	1100 to 1700 1800 to 1800	1300 1600	60 to 70 70 to 80	8300 to 5100 4000 to 4700	4000 4400
80 to 40 40 to 50 50 to 60	1500 to 2500 2300 to 3500 2700 to 4800	2100 2700 3500	80 to 90 90 to 100 100 to 114	3000 to 5600 5200 to 6200	4800 5700

The influence of the mine on the efficiency of the fan does not seem to be very clear. Eight fans, with equivalent orifices over 50 square feet, give efficiendes over 70%; four, with smaller equivalent mine-orifices, give about the same figures; while, on the contrary, six fans, with equivalent orifices of over 50 square feet, give lower efficiencies, as do ten fans, all drawing from mines with small equivalent orifices.

It would seem that, on the whole, large airways tend to assist somewhat

in attaining large efficiency.

2. Influence of the Diameter of the Fan.—This seems to be practically nil, the only advantage of large fans being in their greater width and the lower speed required of the engines.

3. Influence of the Width of a Fan.—This appears to be small as regards the efficiency of the machine; but the wider fans are, as a rule, exhausting

more air.

4. Influence of Shape of Blades.—This appears, within reasonable limits, to be practically nil. Thus, six fans with tips of blades curved forward, three fans with flat blades, and one with blades curved back to a tangent with the circumference, all give very high efficiencies—over 70%.

Influence of the Shape of the Spiral Casing.—This appears to be considerable. The shapes of spiral casing in use fall into two classes, the first presenting a large spiral, beginning at or near the point of cut-off, and the second a circular casing reaching around three quarters of the circumference second a circular casing reaching around three quarters of the circumference of the fan, with a short spiral reaching to the evasée chimney.

Fans having the first form of casing appear to give in almost every case

large efficiencies.

Fans that have a spiral belonging to the first class, but very much contracted, give only medium efficiencies. It seems probable that the proper shape of spiral casing would be one of such form that the air between each pair of blades could constantly and freely discharge into the space between pair or olders could constantly and freely discharge into the space between the fan and casing, the whole being swept along to the evasée chimney. This would require a spiral beginning near the point of cut-off, enlarging by gradually increasing increments to allow for the slowing of the air caused by its friction against the casing, and reaching the chimney with an area such that the air could make its exit with its then existing speed—somewhat less than the periphery-speed of the fan.
6. Influence of the Shutter.—This certainly appears to be an advantage, as

by it the exit area can be regulated to suit the varying quantity of air given by the fan, and in this way re-entries can be prevented. It is not uncommon to find shutterless fans into the chimneys of which bits of paper may be dropped, which are drawn into the fan, make the circuit, and are again thrown out. This peculiarity has not been noticed with fans provided with

7. Influence of the Speed at which a Fan is Run.—It is noticeable that most of the fans giving high efficiency were running at a rather high periphery velocity. The best speed seems to be between 5000 and 6000 feet

The fans appear to reach a maximum efficiency at somewhere about the speed given, and to decrease rapidly in efficiency when this maximum point

In discussion of Mr. Norris's paper, Mr. A. H. Storrs says: From the "cubic feet per revolution" and "cubical contents of fan-blades," as given in the table, we find that the enclosed fans empty themselves from one half to twice per revolution, while the open fans are emptied from one and three-quarter to nearly three times. This for fans of both types, on mines cover-ing the same range of equivalent orifices. One open fan, on a very large ing the same range of equivalent ornices. One open ran, on a sery larger orifice, was emptided nearly four times, while a closed fan, on a still larger orifice, only shows one and one-half times. For the open fans the "cubic feet per 100 ft. motion" is greater, in proportion to the fan width and equivalent orifice, than for the enclosed type. Notwithstanding this apparently free discharge of the open fans, they show very low efficiencies.

As illustrating the very large capacity of centrifugal fans to pass air, if the conditions of the mine are made favorable, a 16-ft. diam. fan, 4 ft. 6 in. wide, at 180 revolutions, passed 860,000 cu. ft. per min., and another, of same diameter, but slightly wider and with larger intake circles, passed 500,000 cu. ft., the water-gauge in both instances being about 1/4 in.

T. D. Jones says: The efficiency reported in some cases by Mr. Norris is larger than I have ever been able to determine by experiment. My own experiments, recorded in the Pennsylvania Mine Inspectors' Reports from 1875 to 1881, did not show more than 604 to 654 to 1881, did not show more than 60% to 65%.

DISK FANS.

Experiments made with a Blackman Disk Fan, 4 ft. diam., by Geo. A. Suter, to determine the volumes of air delivered under various conditions, and the power required; with calculations of efficiency and ratio of increase of power to increase of velocity, by G. H. Babcock. (Trans. A. S. M. E., vii. 547):

Rev. per min.	Cu. ft. of Air delivered per min., V .	Horse-power, HP.	Water- gauge, in.,	Ratio of In- crease of Speed.	Ratio of Increase of Delivery.	Ratio of Increase of Power.	Exponent x , $HP \propto V^x$.	Exponent y,	Efficiency of Fan.
350 440 534 612	25,797 82,575 41,929 47,756 For	0.65 2.29 4.42 7.41 series		1.257 1.186 1.146 1.749	1.262 1.287 1.139 1.851	8.523 1.848 1.677 11.140	5.4 2.4 8.97 4.		1.682 .9553 1.062 .9358
340 453 536 627	20,372 26,660 81,649 86,548 For	0.76 1.99 8.86 6.47 series		1.832 1.183 1.167 1.761	1.308 1.187 1.155 1.794	2.618 1.940 1.676 8.518	8.55 8.66 8.59 8.68		.7110 .6068 .5205 .4802
840 480 534 570	9,988 13,017 17,018 18,649 For	1.12 8.17 6.07 8.46 series	0.28 0.47 0.75 0.87	1.265 1.242 1.068 1.676	1.804 1.807 1.096 1.704	2.837 1.915 1.894 7.554	8.98 2.25 8.68 8.24	1.95 1.74 1.60 1.81	.8989 .8046 .3319 .8027
830 437 516	8,899 10,071 11,157 For	1.81 8.27 6.00 series	0.26 0.45 0.75	1.824 1.181 1.568	1.199 1.108 1.329	8.142 1.457 4.580	6.81 8.66 5.85	8.06 4.96 8.72	.2681 .2198 .2202

Nature of the Experiments.—First Series: Drawing air through 80 ft. of 48-in. diam. pipe on inlet side of the fan.

Second Series: Forcing air through 80 ft. of 48-in. diam. pipe on outlet side of the fan.

Third Series: Drawing air through 30 ft. of 48-in, pipe on inlet side of the fan—the pipe being obstructed by a diaphragm of cheese-cloth.

Fourth Series: Forcing air through 30 ft. of 48-in, pipe on outlet side of fan

the pipe being obstructed by a diaphragm of cheese cloth.

Mr. Babcock says concerning these experiments: The first four experiments are evidently the subject of some error, because the efficiency is such as to prove on an average that the fan was a source of power sufficient to overcome all losses and help drive the engine besides. The second series is less questionable, but still the efficiency in the first two experiments is larger than might be expected. In the third and fourth series the resistance of the cheese-cloth in the pipe reduces the efficiency largely, as would be expected. In this case the value has been calculated from the height equivalent to the water pressure, rather than the actual velocity of the air.

This record of experiments made with the disk fan shows that this kind of fan is not adapted for use where there is any material resistance to the flow of the air. In the centrifugal fan the power used is nearly proportioned to the amount of air moved under a given head, while in this fan the power required for the same number of revolutions of the fan increases very materially with the resistance, notwithstanding the quantity of air moved is at the same time considerably reduced. In fact, from the inspection of the third confiderably reduced to the proper that the proper poulsed is presented. and fourth series of tests, it would appear that the power required is very nearly the same for a given pressure, whether more or less air be in motion. It would seem that the main advantage, if any, of the disk fan over the centrifugal fan for slight resistances consists in the fact that the delivery is the full area of the disk, while with centrifugal fans intended to move the same quantity of air the opening is much smaller. It will be seen by columns 8 and 9 of the table that the power used increased much more rapidly than the cube of the velocity, as in centrifugal and the different experiments do not agree with each other, but a general average may be assumed as about the cube root of the eleventh power.

Full and Three-quarter Heusing Fans. (Buffalo Forge Co.) Capacities at different velocities and pressures. (See also table on p. 519.)

50 Size, in.	Size of Outlet.	of Inlet.		·			Velocities in cubic feet per minute; Pressures in ounces at Fan Outlets.							
50 18 60 22 70 22 90 33 100 37	Cano.				3654 ft min, 3	. per	4482 ft min.,	per oz.	5175 ft. per min., 1 oz.					
60 22 70 22 80 23 90 53 100 87			Diam.	Face.	Capac-	Revs. per min.	Capac-	Revs. per min.	Capac- ity.	Revs. per min.				
120 44 130 45 140 54 150 56 160 56	954 × 2054 856 × 3314 1714 × 3714 11 × 41 1454 × 4454 1816 × 4814 1814 × 5214	243/4 265/6 341/4 391/8 43 453/4 511/6 545/6 613/4 691/9 741/4	9 10 11 12 14 16 18 20 22 24 26 28 30	7 8 9 10 11 12 13 14 15 16 17 18	8,140 11,470 16,280 21,460 27,750 84,410 41,540 58,460 67,710 77,700 88,800 100,270	492 462 861 803 266 242 217 195 187 172 161 149	9,900 18,860 19,900 26,100 83,750 41,850 50,000 71,100 82,850 94,000 108,000 112,950	600 563 441 369 325 294 265 248 227 214 196 181	11,440 16,130 22,860 30,160 39,000 48,360 58,240 69,660 82,160 95,160 109,200 124,800 140,920	698 650 509 426 376 340 307 280 263 248 227 209 197				

For 14 oz. pressure, speed 2584 ft. per minute, the capacity and the revolutions are each one-half of those for 1 oz. pressure.

Efficiency of Disk Fans.—Prof. A. B. W. Kennedy (Industries, Jan. 17, 1890) made a series of tests on two disk fans, 2 and 3 ft. diameter, known as the Verity Silent Air-propeller. The principal results and conclusions are condensed below.

In each case the efficiency of the fan, that is, the quantity of air delivered per effective horse-power, increases very rapidly as the speed diminishes, so that lower speeds are much more economical than higher ones. On the other hand, as the quantity of air delivered per revolution is very nearly ronstant, the actual useful work done by the fan increases almost directly with its speed. Comparing the large and small fans with about the same air delivery, the former (running at a much lower speed, of course) is much the more economical. Comparing the two fans running at the same speed, however, the smaller fan is very much the more economical. The delivery of air per revolution of fan is very nearly directly proportional to the area of the fan's diameter.

The air delivered per minute by the \$-ft. fan is nearly 12.5R cubic feet. The being the number of revolutions made by the fan per minute). For the \$2-ft. fan the quantity is 5.7R cubic feet. For either of these or any other similar fans of which the area is A square feet, the delivery will be about 1.8AR cubic feet. Of course any change in the pitch of the blades might entirely change these figures.

The net H.P. taken up is not far from proportional to the square of the number of revolutions above 100 per minute. Thus for the 3-ft. fan the net H.B. $(R-100)^2$ while the 3-ft. fan the net

H.P. is $\frac{(2k-100)^2}{200,000}$, while for the 2-ft. fan the net H.P. is $\frac{(R-100)^2}{1.000.000}$.

The denominators of these two fractions are very nearly proportional inversely to the square of the fan areas or the fourth power of the fan diameters. The set H. P. required to drive a fan of diameter D feet or area A square feet, at a speed of R revolutions per minute, will therefore be approximately $\frac{D'(R-100)^3}{17,000,000} \text{ or } \frac{A'(R-100)^3}{10,400,000}.$

The 2-ft. fan was noiseless at all speeds. The 3-ft. fan was also noiseless up to over 450 revolutions per minute.

			ropelle ft. dia			ropelle ft. dia	
Speed of fan, revolutions per minut		750	676		576		
Net H.P. to drive fan and belt Cubic feet of air per minute		0.42 4,183					
Mean velocity of air in 8-ft. flue, fe		7,100	0,000	0,410	1,200	0,000	4,410
per minute	. 1	593	543	482	1,046	820	632
Mean velocity of air in flue, san	ne	1,880	1,220		1		ŀ
Cu.ft.of air per min.per effective H.		9,980			7 950	10.020	13,800
Motion given to air per rev. of fan,	ft.	1.77	1.81	1.88	1.82	1.79	
Cubic feet of air per rev. of fan		5.58	5.66	5.90	12.8	12.6	12.0
POSITIVE ROTARY B	LO	WE	RS.	(P. H.	& F. 1	M. Roo	ts.)
Size number	114 114 250	1 3	2 5	8 8		5 6 2 87	
		225			50 12		
	to 300	to 275			o to		
1	6	10	16			7 70	
Furnishes blast for Smith	to	to	to	to 1	o t	o to	to
4	8	14	20			7 100	
Revolutions per minute for)	•••	275 to	275 to		85 17 o t		
cupola, melting iron)		875			75 25		
Size of cupola, inches, in-	•••	18	24			2 50	
side lining		to	to		o to		
\\{	•••	24 11/2	30 21 ⁄2			0 60 8 1214	2.55's
Will melt iron per hour, tons	•••	to	to		78 O to		

The amount of iron melted is based on 30,000 cubic feet of air per ton of iron. The horse-power is for maximum speed and a pressure of 34 pound, ordinary cupola pressure. (See also Foundry Practice.)

Horse-power required.....

BLOWING-ENGINES.

Corliss Horizontal Cross-compound Condensing
Blowing-cugines. (Philadelphia Engineering Works.)

	ated power.	Revs.	Cu. Ft.		Cyl-	. in.	25. in.	of in.	ing ht.	H of
125 lbs.	13Exp. 100 lbs. Steam.	per min.	Free Air per min.	sure per sq.in., lbs.	H. P. (inder,	L. P. C. Inder Diam	Blast C der, S Diam	Stroke All, i	Approx. Shippir Weight	Approx Shipp Weigh Vert.
	1,572 2,280	40 60	80,400 45,600	} 15	44	78	(2) 84	со	505,000	605,000
	1,290 2,060	40 60	80,400 45,600	12	42	72	(2) 84	60	475,000	550,000
1,050 1,596	,	40 60	30,400 45,600	10	32	60	(2) 84	co	355,000	486,000
	1,340 1,950	40 60	26,800 39,600	15	40	72	(2) 78	60	445,000	545,000
	1,152 1,702	40 60	26,800 39,600	12	38	70	(2) 78	60	425,000	491,000
	938 1,386	40 60	26,800 39,600	} 10	3 6	66	(2) 78	60	415,000	450,000
	780 1,175	40 60	15.680 23,500	15	34	со	(2) 72	60	340,000	4:30,000
	548 822	40 60	15.680 23,500	10	28	50	(2) 72	60	270,000	300,000

Vertical engines are built of the same dimensions as above, except that the stroke is 48 in. instead of 60, and they are run at a higher number of revolutions to give the same piston-speed and the same I. H. P.

The calculations of power, capacity, etc., of blowing-engines are the same as those for air-compressors. They are built without any provision for cooling the air during compression. About 400 feet per minute is the usual piston-speed for recent forms of engines, but with positive air-valves, which have been introduced to some extent, this speed may be increased. The efficiency of the engine, that is, the ratio of the LH.P. of the air cylinder to that of the steam-cylinder, is usually taken at 90 per cent, the losses by friction, leakage, etc., being taken at 10 per cent.

STEAM-JET BLOWER AND EXHAUSTER.

A blower and exhauster is made by L. Schutte & Co., Philadelphia, on the principle of the steam-jet ejector. The following is a table of capacities:

Size	Quantity of Air per hour	Diameter of Pipes in inches.		Dize	Quantity of Air per hour	Diameter of Pipes in inches.		
NO.	No. in cubic feet.	Steam.	Air.	No.	cubic feet.	Steam.	Air.	
000 00 0 1 2 8 4	1,000 2,000 4,000 6,000 12,000 18,000 24,000	14 14 114 115 2	1 11/4 2 21/4 8 31/4 4	5 6 7 8 9 10	30,000 36,000 42,000 48,000 54,000 60,000	21/2 21/2 3 31/2 31/2 81/2	5 6 6 7 7 8	

The admissible vacuum and counter pressure, for which the apparatus is constructed, is up to a rarefaction of 20 inches of mercury, and a counterpressure up to one sixth of the steam-pressure.

The table of capacities is based on a steam-pressure of about 60 lbs., and a counter-pressure of about 8 lbs. With an increase of steam-pressure or decrease of counter-pressure the capacity will largely increase.

Another steam-jet blower is used for boiler-fiving, ventilation, and similar

purposes where a low counter-pressure or rarefaction meets the requirements.

The volumes as given in the following table of capacities are under the supposition of a steam-pressure of 45 lbs, and a counter-pressure of, say, 2 inches of water:

Size	Cubic feet of Air	Diameter of Steam-	Diameter in inches of—		Size No.	Cubic feet of Air de-	Diam. of Steam-		eter in
No.	delivered per hour.	pipe in inches.	Inlet	Disch.	NO.	livered per hour	pipe in inches.		Disch.
00 0 1 2 3	6,000 12,000 30,000 60,000 125,000	\$6 1/2 1/2 1/3 5/4	4 5 8 11 14	8 4 6 8 10	4 6 8 10	250,000 500,000 1,000,000 2,000,000	11/4 11/6	17 24 32 42	14 20 27 36

The Steam-jet as a Means for Ventilation.—Between 1810 and 1850 the steam-jet was employed to a considerable extent for ventilating English collieries, and in 1852 a committee of the House of Commons reported that it was the most powerful and at the same time the cheapest method for the ventilation of mines; but experiments made shortly afterwards proved that this opinion was erroneous, and that furnace ventilation was less than half as expensive, and in consequence the jet was soon abandened as a permanent method of ventilation.

For an account of these experiments see Colliery Engineer, Feb. 1890. The jet, however, is sometimes advantageously used as a substitute, for instance, in the case of a fan standing for repairs, or after an explosion, when the furnace may not be kept going, or in the case of the fan having

been rendered useless.

HEATING AND VENTILATION.

Ventilation. (A. R. Wolff, Stevens Indicator, April, 1890.)—The popular impression that the impure air falls to the bottom of a crowded room ular impression that the impure air falls to the bottom of a crowded room is erroneous. There is a constant mingling of the fresh air admitted with the impure air due to the law of diffusion of gases, to difference of temperature, etc. The process of ventilation is one of dilution of the impure eir by the fresh, and a room is properly ventilated in the opinion of the hygienists when the dilution is such that the carbonic acid in the air does not exceed from 6 to 8 parts by volume in 10,000. Pure country air contains about 4 parts Co₂ in 10,000, and badly-ventilated quarters as high as 80 parts.

An ordinary man exhales 0.6 of a cubic foot of CO₂ per hour. New York gas gives out 0.75 of a cubic foot of CO₂ for each cubic foot of gas burnt. An ordinary lamp gives out 1 cu. ft. of CO₂ per hour. An ordinary candle gives out 0.3 cu. ft. per hour. One ordinary gaslight equals in vitiating effect about 5½ men, an ordinary lamp 1½ men, and an ordinary candle ½ man.

To determine the quantity of air to be supplied to the inmates of an unlighted room, to dilute the air to a desired standard of purity, we can establish equations as follows:

Let v = cubic feet of fresh air to be supplied per hour; r = cubic feet of CO₂ in each 10,000 cu. ft. of the entering air; R = cubic feet of CO₂ which each 10,000 cu. ft. of the air in the room may contain for proper health conditions; n = number of persons in the room;

.6 = cubic feet of CO, exhaled by one man per hour.

Then $\frac{v \times r}{10,000}$ + .6n equals cubic feet of CO₂ communicated to the room dur ing one hour.

This value divided by v and multiplied by 10,000 gives the proportion of CO_2 in 10,000 parts of the air in the room, and this should equal R, the standard of purity desired. Therefore

If we place
$$r$$
 at 4 and R at 6, $v = \frac{6000}{6-4}n = 3000n$, (2)

or the quantity of air to be supplied per person is 3000 cubic feet per hour. If the original air in the room is of the purity of external air, and the cubic contents of the room is equal to 100 cu. ft. per inmate, only 3000 - 100 = 2900 cu. ft. of fresh air from without will have to be supplied the first hour to keep the air within the standard purity of 6 parts of CO_8 in 10,000. If the cubic contents of the room equals 200 cu. ft. per inmate, only 3000 - 2000 cu. ft. will have to be supplied the first hour to keep the air within the standard purity and so on

standard purity, and so on.

Again, if we only desire to maintain a standard of purity of 8 parts of carbonic acid in 10,000, equation (1) gives as the required air-supply per hour

$$v = \frac{6000}{8-4}n = 1500n$$
, or 1500 cu. ft. of fresh air per inmate per hour.

Cubic feet of air containing 4 parts of carbonic acid in 10,000 necessary per person per hour to keep the air in room at the composition of

If the original air in the room is of purity of external atmosphere (4 parts of carbonic acid in 10,000), the amount of air to be supplied the first hour, for given cubic spaces per inmate, to have given standards of purity not exceeded at the end of the hour is obtained from the following table:

Cubic Feet	Proportion of Carbonic Acid in 10,000 Parts of the Air, not to be Exceeded at End of Hour.										
of Space in Room per	6	7	8	9	10	15	20				
individual.	Cubic Fe	et of Air, o 10,000,	of Compos to be Supp	ition 4 P	arts of C First Ho	arbonic our.	Acid i				
100	2900	1900	1400	1100	900	445	275				
900	2800	1800	1300	1000	800	845	175				
800	2700	1700	1200	900	700	245	75				
400	2600	1600	1100	800	600	145	Non				
500	2500	1500	1000	700	500	45	.				
600	2400	1400	900	600	400	None					
700	2300	1300	800	500	800						
800	2200	1200	700	400	200						
900	2100	1100	600	800	_100	· • • · · · · ·					
1000	2000	1000	500	200	None		• • • • • •				
1500	1500	500	None	None							
2000	1000	None	•••••	. .							
2500	500										

It is exceptional that systematic ventilation supplies the 8000 cubic feet per inmate per hour, which adequate health considerations demand. Large auditoriums in which the cubic space per individual is great, and in which the atmosphere is thoroughly fresh before the rooms are occupied, and the occupancy is of two or three hours' duration, the systematic air-supply may be reduced, and 2000 to 2500 cubic feet per inmate per hour is a satisfactory

Hospitals where, on account of unhealthy excretions of various kinds, the air-dilution must be largest, an air-supply of from 4000 to 6000 cubic feet per inmate per hour should be provided, and this is actually secured in some

hospitals. A report dated March 15, 1882 by a commission appointed to examine the public schools of the District of Columbia, says:

"In each class-room not less than 15 square feet of floor-space should be allotted to each pupil. In each class-room the window-space should not be less than one fourth the floor-space, and the distance of desk most remote from the window should not be more than one and a half times the height of from the window should not be more than one and a half white should not be the top of the window from the floor. The height of the class-room should never exceed 14 feet. The provisions for ventilation should be such as to provide for each person in a class-room not less than 30 cubic feet of fresh air per minute (1800 per hour), which amount must be introduced and thoroughly distributed without creating unpleasant draughts, or causing any two parts of the room to differ in temperature more than 2° Fahr., or the maximum temperature to exceed 70° Fahr."

When the air enters at or near the floor, it is desirable that the velocity of inlet should not exceed 2 feet per second, which means larger sizes of register openings and flies than are usually obtainable, and much higher velocities of inlet than two feet per second are the rule in practice. The velocity of current into vent-flues can safely be as high as 6 or even 10 feet

per second, without being disagreeably perceptible.

The entrance of fresh air into a room is co-incident with, or dependent on, the removal of an equal amount of air from the room. The ordinary means of removal is the vertical vent-duct, rising to the top of the building. Sometimes reliance for the production of the current in this vent-duct is placed solely on the difference of temperature of the air in the room and that of the external atmosphere; sometimes a steam coil is placed within the flue near its bottom to heat the air within the duct; sometimes steam pipes (risers and returns) run up the duct performing the same functions; or steam jets within the flue, or exhaust fans, driven by steam or electric power, act directly as exhausters; sometimes the heating of the air in the flue is accomplished by gas-jets.

The draft of such a duct is caused by the difference of weight of the

heated air in the duct, and a column of equal height and cross-sectional area of weight of the external air.

Let d = density, or weight in pounds, of a cubic foot of the external air. Let $d_1 = \text{density}$, or weight in pounds, of a cubic foot of the heated air within the duct.

Let h = vertical height, in feet, of the vent-duct.

 $h(d-d_1)$ = the pressure, in pounds per square foot, with which the air is forced into and out of the vent-duct.

This pressure can be expressed in height of a column of the air of density within the vent-duct, and evidently the height of such column of equal presesure would be $h(d-d_1)$.

Or, if t = absolute temperature of external air, and $t_1 =$ absolute temperature of the air in vent-duct in the form, then the pressure equals

The theoretical velocity, in feet per second, with which the air would travels through the vent-duct under this pressure is

$$v = \sqrt{\frac{2gh(t_1 - t)}{t}} = 8.02 \sqrt{\frac{h(t_1 - t)}{t}} \cdot \dots \cdot \dots \cdot (5)$$

The actual velocity will be considerably less than this, on account of loss due to friction. This friction will vary with the form and cross-sectional area of the vent duct and its connections, and with the degree of smoothness of its interior surface. On this account, as well as to prevent leakage of air through crevices in the wall, tin lining of vent-flues is desirable. The loss by friction may be estimated at approximately 50%, and so we find for the actual velocity of the air as it flows through the vent-duct.

$$v = \frac{1}{2}\sqrt{\frac{2gh\frac{(t_1-t)}{t}}{t}}$$
, or, approximately, $v = 4\sqrt{\frac{h\frac{(t_1-t)}{t}}{t}}$. . (6)

If V = velocity of air in vent-duct, in feet per minute, and the external air be at 32° Fahr., since the absolute temperature on Fahrenheit scale equals thermometric temperature plus 459.4,

$$V = 240 \sqrt{h \frac{(t_1 - t)}{491.4}}, \dots$$
 (7)

from which has been computed the following table:

Quantity of Air, in Cubic Feet, Discharged per Minute through a Ventilating Duct, of which the Cross-sec-tional Area is One Square Foot (the External Tempera-ture of Air being 32° Fahr.).

Height of Vent-duct in	Excess of Temperature of Air in Vent-duct above that of External Air.									
feet.	50	10•	15°	20°	25°	80°	500	1000	150°	
10	777	108	138	153	171	188	242	342	419	
15	94	133	162	188	210	230	297	419	514	
20	108	153	188	217	242	265	842	484	593	
25	121	171	210	242	271	297	383	541	663	
80	183	188	230	265	297	825	419	593	726	
85	148	203	248	286	820	851	458	640	784	
40	153	217	265	306	842	375	484	656	888	
45	162	230	282	825	363	896	514	476	889	
50	171	242	297	842	383	419	541	278	937	

Multiplying the figures in above table by 60 gives the cubic feet of air discharged per hour per square foot of cross-section of vent-duct. Knowing the cross-sectional area of vent-ducts we can find the total discharge; or for a desired air-removal, we can proportion the cross-sectional area of

for a desired air-removal, we can proportion the cross-sectional area of vent-ducts required.

Artificial Cooling of Air for Ventilation. (Engineering News, July 7, 1892.)—A pound of coal used to make steam for a fairly efficient refrigerating-machine can produce an actual cooling effect equal to that produced by the melting of 16 to 46 lbs. of ice, the amount varying with the conditions of working. Or, 855 heat-units per lb. of coal converted into work in the refrigerating plant (at the rate of 3 lbs. coal per horse-power hour) will abstract 2275 to 6545 heat-units of heat from the refrigerated body. If we allow 2000 cu. ft. of fresh air per hour per person as sufficient for fair ventilation, with the air at an initial temperature of 80° F., its weight per cubic foot will be .0736 lb.; hence the hourly supply per person will weigh 2000 × .0736 lb. = 147.2 lbs. To cool this 10°, the specific heat of air being 0.238, will require the abstraction of 147.2 × 0.238 × 10 = 350 heat-units per person per hour.

air being 0.238, will require the abstraction of 14.2 × 0.250 × 10 = 500 measurates per person per hour.

Taking the figures given for the refrigerating effect per pound of coal as above stated, and the required abstraction of 350 heat-units per person per hour to have a satisfactory cooling effect, the refrigeration obtained from a pound of coal will produce this cooling effect for 2275 + 350 = 6½ hours with the least efficient working, or 6545 + 350 = 18.7 hours with the most efficient working. With ice at \$5 per ton, Mr. Wolff computes the cost of cooling with hee at about \$5 per hour per thousand persons, and concludes that this is too expensive for any general use. With mechanical refrigeration, however, if we assume 10 hours' cooling per person per pound of coal as a fair practical service in regular work, we have an expense of only 15 cts. per thousand service in regular work, we have an expense of only 15 cts. per thousand persons per hour, coal being estimated at \$3 per short ton. This is for fuel alone, and the various items of oil attendance, interest, and depreciation on the plant, etc., must be considered in making up the actual total cost of

mechanical refrigeration.

Mine-ventilation-Friction of Air in Underground Passages.—In ventilating a mine or other underground passage the resistance to be overcome is, according to most writers on the subject, proportional to the extent of the frictional surface exposed; that is, to the product be of the length of the gangway by its perimeter, to the density of the air in circulation, to the square of its average speed, v, and lastly to a coefficient k, whose numerical value varies according to the nature of the sides of the gangway and the irregularities of its course.

The formula for the loss of head, neglecting the variation in density as unimportant, is $p = \frac{ksv^2}{a}$, in which p = loss of pressure in pounds per square foot, s =square feet of rubbing-surface exposed to the air, v the velocity of

the air in feet per minute, a the area of the passage in square feet, and k the coefficient of friction. W. Fairley, in Colliery Engineer, Oct. and Nov. 1898, gives the following formulæ for all the quantities involved, using the same notation as the above, with these additions: h = horse-power of ventilation; l = length of air-channel; o = perimeter of air-channel; $g = \text{quantity of air circulating in cubic feet per minute; <math>u = \text{units of work, in toot-pounds, applied to circulate the air: <math>w = \text{water-gauge in inches.}$ Then,

1.
$$a = \frac{ksv^2}{p} = \frac{ksv^3}{u} = \frac{ksv^3}{pv} = \frac{q}{pv} = \frac{q}{v}$$
.
2. $h = \frac{u}{33,000} = \frac{q}{33,000} = \frac{5.2qw}{33,000}$.
3. $k = \frac{p\alpha}{sv^2} = \frac{u}{sv^3} = \frac{p}{sv^2 + a} = \frac{5.2w}{sv^2 + a}$.
4. $l = \frac{s}{o} = \frac{p\alpha}{kv^2o}$.
5. $o = \frac{s}{l} = \frac{p\alpha}{kv^3l}$.
6. $p = \frac{ksv^2}{a} = \frac{u}{q} = 5.2w = \left(\sqrt[3]{\frac{u}{ks}}\right)^2 \frac{ks}{a} = \frac{ksv^3}{q} = \frac{u}{av}$.

7.
$$pa = ksv^3 = \left(\sqrt[4]{\frac{u}{ks}}\right)^8 ks = \frac{u}{v}; \quad pa^3 = ksq^3.$$
8. $q = va = \frac{u}{p} = \frac{ksv^3}{p} = \sqrt{\frac{pa}{ks}} a = \sqrt{\frac{u}{ks}} a.$
9. $s = \frac{pa}{kv^2} = \frac{u}{kv^3} = \frac{qp}{kv^3} = \frac{vpa}{kv^3} = lo.$
10. $u = qp = vpa = \frac{ksv^3q}{a} = ksv^3 = 5.2qw = 33,000h.$
11. $v = \frac{u}{pa} = \frac{q}{a} = \sqrt[3]{\frac{u}{ks}} = \sqrt{\frac{pa}{ks}} = \sqrt{\frac{pa}{ks}}.$
12. $v^2 = \frac{pa}{ks} = \left(\sqrt[3]{\frac{u}{ks}}\right)^2.$
13. $v^3 = \frac{u}{ks} = \frac{qp}{ks} = \frac{vpa}{ks}.$
14. $w = \frac{p}{5.2} = \frac{ksv^3}{5.2a}.$

To find the quantity of air with a given horse-power and efficiency (e) of engine:

$$q = \frac{h \times 33,000 \times e}{p}.$$

The value of k, the coefficient of friction, as stated, varies according to the nature of the sides of the gangway. Widely divergent values have been given by different authorities (see Colliery Engineer, Nov. 1893), the most generally accepted one until recently being probably that of J. J. Atkinson, 0000000217, which is the pressure per aquare foot in decimals of a pound for each square foot of rubbing-surface and a velocity of one foot per minute. Mr. Fairley, in his 'Theory and Practice of Ventilating Coal-mines,' gives a value less than half of Atkinson's, or. 00000001; and recent experiments by D. Murgue show that even this value is high under most conditions. Murgue's results are given in his paper on Experimental Investigations in the Loss of Head of Air-currents in Underground Workings, Trans. A. I. M. E., 1893. vol. xxiii. 63. His coefficients are given in the following table, as determined in twelve experiments:

Coefficient of Loss of

		Head	by Friction.
		French.	British.
	(Straight, normal section	\$2000.	.000,000,00486
Rock.	Straight, normal section	.00094	.000,000,00497
gangways.	Straight, large section		.000,000,00549
	Straight, normal section	.00122	.000,000,00645
	[Straight, normal section	.00030	.000,000,00158
Brick-lined	Straight, normal section	.00036	.000,000,00190
arched	{ Continuous curve, normal section	.00062	.000,000,00328
gangways.	Sinuous, intermediate section		.009,000,00269
00	Sinuous, small section	.00055	.000,000,00291
Wineh and	(Straight, normal section	.00168	.000,000,00888
Timbered	≺ Straight, normal section		.000.000.00761
gangways.	Slightly sinuous, small section		.000,000,01257

The French coefficients which are given by Murgue represent the height of water-gauge in millimetres for each square metre of rubbing-surface and a velocity of one metre per second. To convert them to the British measure of pounds per square foot for each square foot of rubbing-surface and a velocity of one foot per minute they have been multiplied by the factor of conversion, .00002828. For a velocity of 1000 feet per minute, since the loss of head varies as v^2 , move the decimal point in the coefficients six places to the right.

Equivalent Orifice.—The head absorbed by the working-chambers sequivalent Orinee.—The nead absorbed by the working-chambers of a mine cannot be computed a priori, because the openings, cross-passages, irregular-shaped gob-piles, and daily changes in the size and shape of the chambers present much too complicated a network for accurate analysis. In order to overcome this difficulty Murgue proposed in 1872 the method of equivalent orifice. This method consists in substituting for the mine to be considered the equivalent thin-lipped orifice, requiring the same height of head for the discharge of an equal volume of air. The area of this orifice is obtained when the head and the discharge are known, by means of the following formulæ, as given by Fairley:

Let Q = quantity of air in thousands of cubic feet per minute; to = inches of water-gauge;

A = area in square feet of equivalent orifice.

$$A = \frac{0.37Q}{\sqrt{w}} = \frac{Q}{2.7\sqrt{w}}; \Phi \quad Q = \frac{A \times \sqrt{w}}{0.37}; \quad w = 0.1369 \times \left(\frac{Q}{A}\right)^{3}.$$

Motive Column or the Head of Air Due to Differences of Temperature, etc. (Fairley.)
Let M = motive column in feet;

T = temperature of upcast;f = weight of one cubic foot of the flowing air;

t = temperature of downcast; D = depth of downcast.

$$M = D \frac{T - t}{T \times 459}$$
 or $\frac{5.2 \times w}{f}$; $p = f \times M$; $w = \frac{f \times M}{5.2} = \frac{p}{5.2}$.

To find diameter of a round airway to pass the same amount of air as a square airway the length and power remaining the same:

Let D= diameter of round airway, A= area of square airway; O= perimeter of square airway. Then $D^3=\sqrt[3]{\frac{A^3\times 3.1416}{.7854^3\times O}}$.

meter of square airway. Then
$$D^3 = \sqrt[5]{\frac{A^3 \times 3.1416}{.7854^3 \times O}}$$

If two fans are employed to ventilate a mine, each of which when worked separately produces a certain quantity, which may be indicated by A and B then the quantity of air that will pass when the two fans are worked together will be $\sqrt[3]{A^3 + B^3}$. (For mine-ventilating fans, see page 521.)

Relative Efficiency of Fans and Heated Chimneys for Ventilation.—W. P. Trowbridge, Trans. A. S. M. E. vii. 531, gives a theoretical solution of the relative amounts of heat expended to remove a given volume of impure air by a fan and by a chinney. Assuming the total efficiency of a fan to be only 1/25, which is made up of an efficiency of 1/10 for the engine, 5/10 for the fan itself, and 8/10 for efficiency as regards friction, the fan requires an expenditure of heat to drive it of only 1/38 of the amount that would be required to produce the same ventilation by a chinney 100 ft. high. For a chinney 500 ft. high the fan will be 7.6 times more efficient. In all cases of moderate ventilation of rooms or buildings where the air is heated before it enters the rooms and spontaneous ventilation is pro-

is heated before it enters the rooms, and spontaneous ventilation is produced by the passage of this heated air upwards through vertical fluer, no special heat is required for ventilation; and if such ventilation be sufficient, the process is faultless as far as cost is concerned. This is a condition of things which may be realized in most dwelling houses, and in many halls, schoolrooms, and public buildings, provided inlet and outlet flues of ample cross-section be provided, and the heated air be properly distributed.

If a more active ventilation be demanded, but such as requires the smallest amount of power, the cost of this power may outweigh the advantages of the fan. There are many cases in which steam-pipes in the base of a chimney, requiring no care or attention, may be preferable to mechanical ventilation, on the ground of cost, and trouble of attendance, repairs, etc.

^{*} Murgue gives $A = \frac{0.38Q}{4\sqrt{n}}$, and Norris $A = \frac{0.403Q}{\sqrt{n}}$. See page 521, ante.

The following figures are given by Atkinson (Coll. Engr., 1889), showing the minimum depth at which a furnace would be equal to a ventilatingmachine, assuming that the sources of loss are the same in each case, i.e., that the loss of fuel in a furnace from the cooling in the upcast is equivalent to the power expended in overcoming the friction in the machine, and also assuming that the ventilating-machine utilizes 60% of the engine-power. The coal consumption of the engine per I.H.P. is taken at 8 lbs. per hour:

100° F. 150° F. 200° F. Average temperature in upcast...... Minimum depth for equal economy... 960 yards. 1040 yards. 1180 yards.

Heating and Ventilating of Large Buildings. (A. R. Wolff, Jour. Frank: Inst., 1893.)—The transmission of heat from the interior to the exterior of a room or building, through the walls, ceilings, windows, etc., is calculated as follows:

S = amount of transmitting surface in square feet;

 $t = \text{temperature F. inside}, t_0 = \text{temperature outside};$ K = a coefficient representing, for various materials composing buildings,the loss by transmission per square foot of surface in British thermal units per hour, for each degree of difference of temperature on the two sides of the material;

 $Q = \text{total heat transmission} = SK(t - t_0).$

This quantity of heat is also the amount that must be conveyed to the room in order to make good the loss by transmission, but it does not cover the additional heat to be conveyed on account of the change of air for purposes of ventilation. The coefficients K given below are those prescribed by law by the German Government in the design of the heating plants of its public buildings, and generally used in Germany for all buildings. They have been converted into American units by Mr. Wolff, and he finds that they agree well with good American practice:

Value of K for Each Square Foot of Brick Wali.

Thickness of (12" 16" 20" 24" 36" 40" brick wall. $K = 0.68 \quad 0.46 \quad 0.32 \quad 0.26 \quad 0.23 \quad 0.20 \quad 0.174$ 0.15 0.1290.115

1 sq. ft., wooden-beam construction,	}	 as floo	ring,	K = 0.0)83
planked over or ceiled.	٠٠٠٠ ک	 .as ceil	ling.	K = 0.1	104
planked over or ceiled, 1 sq. ft., fireproof construction,	٠٠٠٠ غ	 as floc	ring,	K = 0.1	24
floored over,	٠	 . as ceil	ling,	K = 0.1	45
floored over, 1 sq. ft., single window	. .	 		K = 1.0	130
1 sq. ft., single skylight		 		K = 1.1	118
1 sq. ft., double window		 		K = 0.5	518
1 sq. ft., double skylight					
1 sq. ft., door					

These coefficients are to be increased respectively as follows: 10% when the exposure is a northerly one, and winds are to be counted on as important factors; 10% when the building is heated during the daytime only, and the location of the building is not an exposed one; 30% when the building is heated during the daytime only, and the location of the building is exposed; 50% when the building is heated during the winter months intermittently, with long intervals (say days or weeks) of non-heating.

The value of the radiating-surface is about as follows: Ordinary bronzed cast-iron radiating-surfaces, in American radiators (of Bundy or similar type), located in rooms, give out about 250 heat-units per hour for each square foot of surface, with ordinary steam-pressure, say 3 to 5 lbs, per sq. in., and about 0.6 this amount with ordinary hot-water heating.

Non-panted radiating-surfaces, of the ordinary "indirect" type (Climax or pin surfaces), give out about 400 heat-units per hour for each square foot

of heating-surface, with ordinary steam-pressure, say 8 to 5 lbs. per sq. in.;

and about 0.6 this amount with ordinary hot-water heating.

A person gives out about 400 heat-units per hour; an ordinary gas-burner

about 4800 heat-units per hour; an incandescent electric (16 candle-power) light, about 1600 heat-units per hour.
The following example is given by Mr. Wolff to show the application of the formula and coefficients:

Lecture-room 40 × 60 ft., 20 ft. high, 48,000 cubic feet, to be heated to 69° F.; exposures as follows: North wall, 60 × 20 ft., with four windows, each 14 × 8 feet, outside temperature 0° F. Room beyond west wall and

HEATING AND VENTILATING OF LARGE BUILDINGS. 535

room overhead heated to 69°, except a double skylight in ceiling, 14 × 24 ft., exposed to the outside temperature of 0° . Store-room beyond east wall at 86° . Door 6×12 ft. in wall. Corridor beyond south wall heated to 59° . Two doors, 6×12 , in wall. Cellar below, temperature 36° .

The following table shows the calculation of heat transmission:

$t-t_{\phi}$ (Fahr.) degrees).	Kind of Transmitting Surface,	Thickness of Wall in inches.	Calculation of Area of Transmitting Surface.	Square feet of Surface.	$K(t-t_0)$.	Thermal Units.
69° 69 33 83 10 10 10 10 69 69	Outside wall. Four windows (single). Inside wall (store-room). Door Inside wall (corridor). Door Inside wall (corridor). Door Roof. Double skylight. Floor.	36" 86" 24" 86"	63 × 22 - 448 4 × 8 × 14 42 × 22 - 72 6 × 13 17 × 22 - 72 6 × 13 17 × 22 - 72 6 × 13 32 × 42 - 336 14 × 24 62 × 43	448 852 78 918 72 302 72	9 72 4 19 2 5 1 5 10 43	8,442 82,256 8,408 1,868 1,836 360 302 360 10,080 14,448 10,416
	Supplementary allowance, r "" Exposed location and intern Total thermal units	north (outside wall, 10 outside window	% 78, 10%	• • • • •	88,276 844 8,226 87,346 26,204 118,550

If we assume that the lecture-room must be heated to 69 degrees Fahr. in If we assume that the fecture-room must be heated to be degrees rain. In the daytime when unoccupied, so as to be at this temperature when first persons arrive, there will be required, ventilation not being considered, and bronzed direct low-pressure steam-radiators being the heating media, about 118,550 + 250 = 455 sq. ft. of radiating-surface. (This gives a ratio of about 405 cu. ft. of contents of room for each sq. ft. of heating-surface.)

If we assume that there are 160 persons in the lecture-room, and we provide that the content of the persons in the lecture-room, and we provide that the content of the persons in the lecture-room, and we provide that the content of the persons in the lecture-room, and we provide the content of the persons in the lecture-room, and we provide the content of the persons in the lecture-room, and we provide the content of the persons in the lecture-room and we provide the content of the persons in the lecture-room and we provide the persons in the lecture-room and we provide the persons in the lecture-room and we provide the persons in the lecture-room and we provide the persons in the lecture-room and we provide the persons in the lecture-room and we provide the persons in the lecture-room and we provide the persons in the lecture-room and the persons in the lecture-room and the persons in the lecture-room and the persons in the lecture-room and the persons in the lecture-room are persons and the persons in the lecture-room and the persons in the lecture-room are persons and the persons in the lecture-room are persons and the persons in the lecture-room are persons are persons and the persons are pe

vide 2500 cubic feet of fresh air per person per hour, we will supply $160 \times 2500 = 400,000$ cubic feet of air per hour (i.e., $\frac{400,000}{48,000} =$ over eight changes of

contents of room per hour).

To heat this air from 0° Fahr, to 69° Fahr, will require 400,000 × 0.0189 × 10 near time air from o' rain; to os' rain; will require success X colors 95 = 521,640 thermal units per hour (0.189 being the product of a weight of a cubic foot by the specific heat of air). Accordingly there must be provided 521,640 + 400 = 1804 sq. ft. of indirect surface, to heat the air required for ventilation, in zero weather. If the room were to be warmed entirely indirectly, that is, by the air supplied to room (including the heat to be conveyed to cover less by the specific of the cover to be a transmission through walls etc.) there would have to be to cover loss by transmission through walls, etc.), there would have to be conveyed to the fresh air supply \$21,640 + 113,550 = 635,190 heat-units. This would imply the provision of an amount of indirect heating-surface of the "Climax" type of 635,190 + 400 = 1589 sq. ft., and the fresh air entering the room would have to be at a temperature of about 84° Fahr., viz., 69° = 118,550

113,550

100,000 \times 0.0189, or 69 + 15 = 84° Fahr.

The above calculations do not, however, take into account that 160 persons in the lecture-room give out 160 \times 400 = 64,000 thermal units per hour; and that, say, 50 electric lights give out 50 \times 1600 = 80,000 thermal units per hour; or, say, 50 gaslights, 50 \times 4800 = 240,000 thermal units per hour. The presence of 160 people and the gas-lighting would diminish considerably the amount of heat required. Practically, it appears that the heat generated by the presence of 160 people, 64,000 heat-units, and by 60 electric lights, 80,000 heat-units, a total of 144,000 heat-units, more than covers the amount of heat transmitted through walls, etc. Moreover, that if the 50 gaslights of heat transmitted through walls, etc. Moreover, that if the 50 gaslights give out 240,000 thermal units per hour, the air supplied for ventilation must enter considerably below 69° Fahr., or the room will be heated to an unbearably high temperature. If 400,000 cubic feet of fresh air per hour

are supplied, and 240,000 thermal units per hour generated by the gas must be abstracted, it means that the air must, under these conditions, enter 240,000

 $\frac{240,000}{400,000 \times .0189}$ = about 32° less than 84°, or at about 52° Fahr. Furthermore, the additional vitiation due to gaslighting would necessitate a much larger supply of fresh air than when the vitiation of the atmosphere by the people alone is considered, one gaslight vitiating the air as much as five men.

Various Rules for Computing Radiating-surface.—The following rules are compiled from various sources. They are more in the nature of "rule-of-thumb" rules than those given by Mr. Wolff, quoted above, but they may be useful for comparison.

Divide the cubic feet of space of the room to be heated, the square feet of wall surface, and the square feet of the glass surface by the figures given under these headings in the following table, and add the quotients together; the result will be the square feet of radiating-surface required. (F. Schumann.)

SPACE, WALL AND GLASS SURFACE WHICH ONE SQUARE FOOT OF RADIATING-SURFACE WILL HEAT.

	lå .	cubic			Exposure	of Rooms	L		
nge.	ressu	lno t	All 8	Sides.	North	west.	Southeast.		
Air Change.	Steam-p in pou	Space ir feet.	Wall Surface, sq. ft.	Glass Surface, sq. ft.	Wall Surface, sq. ft.	Glass Surface, sq. ft.	Wall Surface, sq. ft.	Glass Surface, sq. ft.	
Once per hour.	1 8 5	190 210 225	15.0	7 7.7 8.5	15.87 17.25 18.97	8.05 8.85 9.77	16.56 18.00 19.80	8.4 9.24 10.20	
Twice per hour.	1 8 5	75 82 90	11.1 12.1 18.0	5.7 6.2 6.7	12.76 13.91 14.52	6.55 7.13 7.60	13.22 14.52 15.60	6.84 7.44 8.04	

Emission of Heat-units per square foot per Hour from Cast-iron Pipes or Radiators, Temp. of Air in Room, 70° F. (F. Schumann.)

Mean Temperature of	By Co	ontact.	By Radi-	By Radiation and Contact.		
Heated Pipe, Radia- tor, etc.	Air quiet	Air moving.	ation.	Air quiet.	Air moving.	
Hot water 140° 150° 160° 170°	55.51 65.45 75.68 86.18	92.52 109.18 126.18 143.30	59.68 69.69 80.19 91.12	115.14 185.14 155.87 177.80	152.15 178.87 206.82	
" " 180° " " 190°	96,93 107,90 119,13	161.55 179.83 198.55	102.15 114.45 127.00	199.48 222.85 246.13	234.48 264.05 294.28 825.55	
or steam 210° Steam 220° 230° 4 240°	180,49 149,20 153,95 165,90	217.48 237.00 256.58 279.83	139.96 155.27 169.56 184.58	270.49 297.47 828.51 850.48	857.48 892.27 426.14 464.41	
250° 260° 270°	178.00 189.90 202.70	296.65 816.50 887.88	200.18 214.36 233.42	878.18 404.26 486.18	496.81 530.86 571.25	
4	215.30 228.55 240.85	858.85 880.91 401.41	251.21 267.78 279.12	466.51 496.98 519.97	610.06 648,64 680.58	

RADIATING-SURFACE REQUIRED FOR DIFFERENT KINDS OF BUILDINGS.

The Nason Mfg. Co.'s catalogue gives the following: One square foot of surface will heat from 40 to 100 cu ft. of space to 75° in -10° latitudes. This range is intended to meet conditions of exposed or corner rooms of buildings, and those less so, as intermediate ones of $\mathbbm{1}$ block. As a general rule, 1 sq. ft. of surface will heat 70 cu. ft. of air in outer or front rooms and 100 cu. ft. in inner rooms. In large stores in cities, with buildings on each side, 1 to 100 is ample. The following are approximate proportions:

One square foot radiating-surface will heat:

by direct radiation by indirect radiation.	schoolrooms, offices, etc. 60 to 80 ft. 40 to 50 "	lofts, factories, etc. 75 to 100 ft. 50 to 70 "	auditoriums, etc. 150 to 200 ft. 100 to 140 "
7			

Isolated buildings exposed to prevailing north or west winds should have

Isolated buildings exposed to prevailing north or west winds should have a generous addition made to the heating-surface on their exposed sides. The following rule is given in the catalogue of the Babcock & Wilcox Co., and is also recommended by the Nason Mfg. Co.:
Radiating surface may be calculated by the rule: Add together the square feet of glass in the windows, the number of cubic feet of air required to be changed per minute, and one twentieth the surface of external wall and roof; multiply this sum by the difference between the required temperature of the room and that of the external air at its lowest point, and divide the product by the difference in temperature between the steam in the pipes and the required temperature of the room. The quotient is the required radiating-surface in source feet.

radiating-surface in square feet.
Prof. R. C. Carpenter (Heating and Ventilation, Feb. 15, 1897), gives the following handy formula for the amount of heat required for heating buildings by direct radiation:

$$h = \frac{n}{55}C + G + \frac{1}{4}W_{\bullet}$$

in which W= wall-surface, G= glass- or window-surface, both in sq. ft., C= contents of building in cu. ft., n= number of times the air must be changed per hour, and h= total heat units required per degree of difference of temperature between the room and the surrounding space. To heat the building to 70° F. when the outside temperature is 0°, 70 times the above quantity of heat will be required. Under ordinary conditions of pressure and temperature 1 sq. ft. of steam-heating surface will supply 280 heat units per hour, and 1 sq. ft. of hot-water heating surface 175 heat units per hour. The square feet of radiating-surface required under these conditions will be R=0.25h for steam-heating, and R=0.4h for hot-water heating. Prof. Carpenter says that for residences it is safe to assume that the air of the Carpenter says that for residences it is safe to assume that the air of the principal living-rooms will change twice in an hour, that of the halls three times and that of the other rooms once per hour, under ordinary condi-

Overhead Steam-pipes. (A. R. Wolff, Stevens Indicator, 1887.)—When the overhead system of steam-heating is employed, in which system direct radiating pipes, usually 1½ in. in diam, are placed in rows overhead, suspended upon horizontal racks, the pipes running horizontally, and side by side, around the whole interior of the building, from 2 to 8 ft. from the walls, and from 2 to 4 ft. from the ceiling, the amount of 1½ in. pipe required, according to Mr. C. J. H. Woodbury, for heating mills (for which use this system is deservedly much in vogue), is about 1 ft. in length for every 90 cu. ft. of space. Of course a great range of difference exists, due to the special character of the operating machinery in the mill, both in respect to the amount of air circulated by the machinery, and also the aid to warming the room by the friction of the journals.

warming the room by the friction of the journals.

Indirect Heating surface.—J. H. Kinealy, in Heating and Ventilation, May 15, 1894, gives the following formula, deduced from results of experiments by C. B. Richards, W. J. Baldwin, J. H. Mills, and others, upon indirect heaters of various kinds, supplied with varying amounts of air per hour per square foot of surface:

were square root of surface:

$$N = \frac{35.04}{\frac{T_2 - T_1}{T_0 - T_1} - 0.369}; \quad T_2 = (T_0 - T_1) \left(0.369 + \frac{35.04}{N}\right) + T_2.$$

N = cubic feet of air, reduced to 70° F., supplied to the heater per square foot of heating-surface per hour; T_0 = temperature of the steam or water in the heater; T_1 = temperature of the air when it enters the heater;

 T_2 = temperature of the air when it leaves the heater.

As the formula is based upon an average of experiments made upon all sorts of indirect heaters, the results obtained by the use of the equation may in some cases be slightly too small and in others slightly too large, although the error will in no case be great. No single formula ought to be expected to apply equally well to all dispositions of heating-surface in indirect heaters, as the efficiency of such heater can be varied between such wide limits by the construction and arrangement of the surface.

In indirect heating, the efficiency of the radiating-surface will increase, and the temperature of the air will diminish, when the quantity of the air caused to pass through the coil increases. Thus I sq. ft. radiating-surface, with steam at 212°, has been found to heat 100 cu. ft. of air per hour from zero to 150°, or 300 cu. ft. from zero to 100° in the same time. The best resuits are attained by using indirect radiation to supply the necessary venti-

lation, and direct radiation for the balance of the heat. (Steam.)

In indirect steam-heating the least flue area should be 1 to 1½ sq. in to every square foot of heating surface, provided there are no long horizontal reaches in the duct, with little rise. The register should have twice the area of the duct to allow for the fretwork. For hot water heating from 25%

to 30% more heating-surface and flue area should be given than for low-pressure steam. (Engineering Record, May 28, 1894.)

Bellor Heating-surface Bequired. (A. R. Wolff, Stevens Indi-cator, 1887.)—When the direct system is used to heat buildings in which the street floor is a store, and the upper floors are devoted to sales and stockrooms and to light manufacturing, and in which the fronts are of stone or iron, and the sides and the rear of building of brick—a safe rule to follow is to supply 1 sq. ft. of boiler heating-surface for each 700 cu. ft., and 1 sq. ft. of

radiating surface for each 100 cu. ft. of contents of building.

For heating mills, shops, and factories, 1 sq. ft. of boller heating-surface should be supplied for each 475 cu. ft. of contents of building; and the same allowance should also be made for heating exposed wooden dwellings. For heating foundries and wooden shops, 1 sq. ft. of boiler heating-surface should be provided for each 400 cu. ft. of contents; and for structures in which glass enters very largely in the construction—such as conservatories, exhibition buildings, and the like—1 sq. ft. of boiler heating surface should be provided for each 275 cu. ft. of contents of building.

When the indirect system is employed, the radiator-surface and the boiler

capacity to be provided will each have to be, on an average, about 25% more than where direct radiation is used. This percentage also marks approximately the increased fuel consumption in the indirect system.

Steam (Babcock & Wilcox Co.) has the following: 1 sq. ft. of boiler-surface will supply from 7 to 10 sq. ft. of radiating surface, depending upon the size of boiler and the efficiency of its surface, as well as that of the radiating surface. Small boilers for house use should be much larger proportionately than large plants. Each horse-power of boiler will supply from 240 to 360 ft. of 1-in. steam-pipe, or 80 to 120 sq. ft. of radiating surface. Cubic feet of space has little to do with amount of steam or surface required, but is a convenient factor for rough calculations. Under ordinary conditions 1 horse-power will heat, approximately, in—

Brick dwellings, in blocks, as in cities	15,000	to	20,000	cu. ft.
" stores " "	10,000	**	15,000	46
" dwellings, exposed all round	10,000	**	15,000	66
" mills, shops, factories, etc			10,000	44
Wooden dwellings, exposed	7.000	44	10,000	44
Foundries and wooden shops			10,000	44
Exhibition buildings, largely glass, etc			15,000	46

Steam-consumption in Car-heating.

C., M. & St. Paul Railway Tests. (Engineering, June 27, 1890, p. 764.)

	er of Condensation er Car per Hour. 70 lbs. 85 300
--	--

Internal Diameters of Steam Supply-mains, with Total Resistance equal to 2 inches of Water-column.*

Steam, Pressure 10 lbs. per square inch above atm., Temperature 289° F.

Formula, $d = 0.5374_{4}$ where d = internal diameter in inches:

Q = 9.3 cubic feet of steam per minute per 100 sq. ft. of radiating-surface; l = length of mains in feet; h = 159.3 feet head of steam to produce flow.

adiating- surface.	Internal Diameters in inches for Lengths of Mains from 1 ft. to 600 ft.											
Radiating surface.	1 ft.	10 ft.	20 ft.	40 ft.	60 ft.	80 ft.	100 ft.	200 ft.	300 ft.	400 f t,	600 ft.	
sq.ft.	inch.	inch.	inch.	inch.	inch.	inch.	inch.	inch.	inch.	inch.	inch.	
- 1	0.075	0.119	0.136	0.157	0.170	0.180	0.189	0.216	0.234	0.248	0.276	
10	0.19	0.30	0.84	0.39	0.43	0.45	0.47	0.54	0.59	0.62	0.68	
20	0.25	0.39	0.45	0.52	0.56	0.60	0.62	0.72	0.78	0.82	0.89	
40	0.83	0.52	0.60	0.69	0.74	0.79	0.82	0.95	1.03	1.09	1.18	
60	0.89	0.61	0.71	0.81	0.87	0.98	0.97	1.11	1.21	1.28	1.39	
80	0.48	0.68	0.79	0.90	0.98	1.04	1.09	1.25	1.35	1.48	1.55	
100	0.47	0.75	0.86	0.99	1.07	1.14	1.19	1.36	1.48	1.57	1.70	
200	0 62	0.99	1.14	1.30	1.41	1.50	1.57	1.80	1.95	8.07	2.24	
300 i	0.78	1.16	1.34	1.53	1.66	1.76	1.84	2.12	2.80	2.48	2.64	
400	0.82	1.30	1.50	1.72	1.86	1.98	2.07	2.37	2.57	2.78	2.96	
. 500	0.90	1.43	1.64	1.88	2.04	2.16	2.26	2.60	2.81	2.98	8.28	
600	0.97	1.58	1.76	2.03	2.20	2.33	2.43	2.79	8.03	8.21	8.48	
800	1.09	1.72	1.98	2.27	2 46	2.61	2.78	3.13	8.40	8.60	8.90	
1,000	1.19	1.88	2.16	2.48	2.69	2.85	2.98	8.43	8.71	8.94	4.27	
1,200	1.28	2.04	2.38	2.67	2.90	8.07	3.21	8.68	4.00	4.28	4.59	
1,400	1.36	2.15	2.47	2.84	8.08	8.26	8.41	3.92	4.25	4.50	4.88	
1,600	1.48	2.27	2.61	8.00	8.25	8.44	3.60	4.18	4.49	4.75	5.15	
1,800	1.50	2.88	2.74	8.14	8.41	8.61	3.78	4.34	4.70	4.98	5.40	
2,000	1.57	2.48	2.85	8.28	8.55	8.76	8.98	4.52	4.90	5.19	5.68	
8,000	1.84	2.92	8.36	3.85	4.18	4.48	4.63	5.82	5.77	6.11	6.63	
4,000	2.07	8.28	8.76	4.82	4.69	4.96	5.19	5.96	6.47	6.85	7.44	

^{*} From Robert Briggs's paper on American Practice of Warming Buildings by Steam (Proc. Inst. C. E., 1882, vol. lxxi). For other resistances and pressures above atmosphere multiply by the

respective factors below:

24 in. | Press. ab. atm. 0 lbs. 3 lbs. 30 lbs. 60 lbs. 0.6084 | Multiply by 1.023 1.015 0.973 0.948 Water col. 6 in. 12 in. Multiply by 0.8027 0.6988

Begisters and Cold-air Ducts for Indirect Steam Heating.

The Locomotive gives the following table of openings for registers and cold-air ducts, which has been found to give satisfactory results. The cold air boxes should have 14 sq. in, area for each square foot of radiator sufface, and never less than 34 the sectional area of the hot air ducts. The hot air ducts should have 2 sq. in. of sectional area to each square foot of radiator surface on the first floor, and from 11/2 to 2 inches on the second floor.

Heat	ing S	urface ks.	Cold-	air St	ipply,	First Floor.	Size Register.	Cold-air Supply, 2d Floor.
						luches	inches	inches
3 0 s	quar	e feet	45 s	quare	inche	s == 5 by 9	9 by 12	4 by 10
40	**	**	60	• "	**	= 6 by 10	10 by 14	4 by 14
50	44	44	75	64	46	= 8 by 10	10 by 14	5 by 15
60	66	46	90	**	64	= 9 by 10	12 by 15	6 by 15
70	44	66	108	44	46	= 9 by 12	12 by 19	6 by 18
80	44	44	120	44	66	= 10 by 12	12 by 22	8 by 15
90	46	46	135	64	66	= 11 by 12	14 by 24	9 by 15
100	44	**	150	4.	66	= 12 by 12	16 by 20	12 by 12

The sizes in the table approximate to the rules given, and it will be found that they will allow an easy flow of air and a full distribution throughout the room to be heated.

Physical Properties of Steam and Condensed Water, under Conditions of Ordinary Practice in Warming by Steam. (Briggs.)

_							
A	Steam pressure j above atm per square inch { total	lbs. lbs.	0 14.7	3 17.7	10 24.7	80 44.7	60 74.7
C	Temperature of steam Temperature of air Difference $= B - C$	Fahr. Fahr. Fahr.	212° 60° 152°	222° 60 162°	289° 60° 179°	274° 60° 214°	307° 60° 247°
E	Heat given out per minute per 100 sq. ft. of radiating-sur-	units	456	488	537	642	741
F	(face $=$ D \times 3 Latent heat of steam	Fahr.	965°	958°	946°	921•	898•
	Volume of 1 lb. weight of steam Weight of 1 cubic foot of steam	cu. ft.	26.4 0.0380	22.1 0.0452		9.24 0.1082	5.70 0.1752
J	Volume Q of steam per minute to give out E units $= E \times G + F$.	cu. ft.	12.48	11.21	9.20	6.44	4.70
ĸ	Weight of 1 cubic foot of con- densed water at tempera- ture B.		59.64	59.51	59.05	58.07	57.03
L	Volume of condensed water to return to boiler per minute $= J \times H + K$,	cu. ft.	0.0079	0.0085	0.0096	0.0120	0.0144
M	Head of steam equivalent to 12 inches water-column = K + H.	feet	1569	1817	955.5	586.7	825.5
	STEAM-SUPPLY MAINS.						
N	Head h of steam, equivalent to assumed 2 inches water- column for producing steam flow $Q_1 = M + 6$,	feet	261.5	219.5	-159.8	89.45	54.25
P	Internal diameter d of tube* for flow Q when $l = 1$ foot,	1 men	0.484		0.474	0.461	0.449
R	Do. do. when $l = 100$ feet, Ratios of values of d .	inch ratio	1.217 1.023		1.190 1.000		
	WATER-RETURN MAINS.						
T	Head h assumed at 1/2-inch water-column for producing full-bore water-flow Q.	foot	0.0417	0.0417	0.0417	0.0417	0.0417
U V W	Internal diameter d of tube* for flow Q when $l = 1$ foot, Do. do. when $l = 100$ feet, Ratios of values of d	\ men	0.147 0.868 0.926	0.379	0.898	0.178 0.484 1.092	0.468
				1 0.000	, 2.300		

^{*} P, R, U, V are each determined from the formula d = 0.5374

Size of Steam Pipes for Steam Heating. (See also Flow of Steam in Pipes.)—Sizes of vertical main pipes. Direct radiation. (J. R. Willett, Heating and Ventilation, Feb., 1894.)

Diameter of pipe, inches. 1 Sq. ft. of radiator surface 40 11/4 70 116 2 216 8 816 4 5 6 110 220 860 560 810 1110 2000 8000 A horizontal branch pipe for a given extent of radiator surface should be one size larger than a vertical pipe for the same surface.

not be as large as given above: under very favorable circumstances and conditions a 4-inch pipe may supply from 2000 to 2500 sq. ft. of surface, a 6-inch pipe for 5000 sq. ft., and a 10-inch pipe for 15,000 to 20,000 sq. ft., if the distance of run from boiler is not too great. Less than 1½-inch pipe should not be used horizoutally in a main unless for a single radiator connection

not be used horizoutally in a main unless for a single radiator connection.

Steam, by the Babcock & Wilcox Co., says: Where the condensed water is returned to the boiler, or where low pressure of steam is used, the diameter of mains leading from the boiler to the radiating-surface should be equal in inches to one tenth the square root of the radiating-surface mains included, in square feet. Thus a 1-inch pipe will supply 100 square feet of surface, itself included. Return-pipes should be at least ¾ inch in diameter, and never less than one half the diameter of the main—longer returns requiring larger pipe. A thorough drainage of steam-pipes will effectually prevent all cracking and pounding noises therein.

A. R. Wolf's Practice.—Mr. Wolff gives the following figures showing his

A. R. Wolff's Practice.—Mr. Wolff gives the following figures showing his present practice (1897) in proportioning mains and returns. They are based on an estimated loss of pressure of 2% for a length of 100 ft. of pipe, not including allowance for bends and valves (see p. 678). For longer runs divide the thermal units given in the table by 0.1 Vlength in ft. Besides giving the thermal units the table also indicates the amount of direct radiating surface which the steam-pipes can supply, on the basis of an emission of 250 thermal units per hour for each square foot of direct radiating surface.

Size of Pipes for Steam Heating.

46	of u.	2 lbs. Pr	essure	5 lbs. Pr	essure	10 K	of.	21bs Pr	essure	5 lbs. Pr	essure
E Diam.	Hetur	Chermal Units per Hr., Phous'ds	Heating- surface, Sq. Ft.	Units Units per Hr., Thous'ds	Heating- surface, Sq. Ft.	ddng In.	H Diam.	Chermal Units, per Hr Thous'ds	Heating- surface, Sq. Ft.	Thermal Units, per Hr., Thous'ds	Heating- surface, Sq. Ft.
1	1	9	36	15	60	5	314	930	3720	1550	6500
134	1	18	72	30	120	6	33/6		6000		10000
112	11/4	30	120	50	200	7	4	2250	9000	3750	15000
2	116	1 200	280	120	480	8	4	3200-	12800	5400	21600
216	2	132	528	220	880	9	416	4450	17800	7500	30000
3	216	225	900	375	1500	10	5	5800	23200	9750	39000
31.6	912	330	1320	550	2200	12	6	9250	37000	15500	62000
4	9	480	1920	800	3200	14	7	13500	54000	23000	92000
416	3	690	2760	1150	4600	16	B	19000	76000	32500	130000

Heating a Greenhouse by Steam.—Wm. J. Baldwin answers a question in the American Machinist as below: With five pounds steampressure, how many square feet or inches of heating-surface is necessary to heat 100 square feet of glass on the roof, ends, and sides of a greenhouse in order to maintain a night heat of 55° to 65°, while the thermometer outside ranges at from 15° to 20° below zero; also, what boiler-surface is necessary? Which is the best for the purpose to use—2" pipe or 1½" pipe?

Ans.—Reliable authorities agree that 1.25 to 1.50 cubic feet of air in an enclosed space will be cooled per minute per sq. ft. of glass as many degrees as the internal temperature of the house exceeds that of the air outside. Between + 65° and - 20° there will be a difference of 85°, or, say, one cubic foot of air cooled 127.5° F. for each sq ft. of glass for the most extreme condition mentioned. Multiply this by the number of square feet of glass and by 60, and we have the number of cubic feet of air cooled 1° per hour within the building or house. Divide the number thus found by 43, and it gives the units of heat required, approximately. Divide again by 83, and it will give the number of pounds of steam that must be condensed from a pressure and temperature of five pounds above atmosphere to water at the same temperature in an hour to maintain the heat. Each square foot of surface of pipe will condense from ½ to nearly ½ lb. of steam per hour, according as the coils are exposed or well or poorly arranged, for which an average of ½ lb. may be taken. According to this, it will require 3 sq. ft. of pipe surface per lb. of steam to be condensed. Proportion the heating-surface of the boiler to have about one fifth the actual radiating-surface, if you wish to keep steam over night, and proportion the grate to burn not more than six pounds of coal per sq. ft. of grate per hour. With very slow combustion, such as takes place in base-burning boilers, the grate might be proportioned for four to five pounds of coal per hour. It is cheaper to make coils of 1½" pipe than of 2", and there is nothing to be gained by using 2" pipe unless the coils are very long. The pipes in a greenhouse should be

under or in front of the benches, with every chance for a good circulation of air. "Header" coils are better than "return-bend" coils for this purpose. Mr. Baldwin's rule may be given the following form: Let H = heat-units transferred per hour, T = temperature inside the greenhouse, t = temperature outside, S = sq. ft. of glass surface; then $H = 1.58(T - t) \times 60 + 48 = 1.8758(T - t)$. Mr. Wolff's coefficient K for single skylights would give H=1.118S(T-t).

Heating a Greenhouse by Hot Water.—W. M. Mackay, of the Richardson & Boynton Co., in a lecture before the Master Plumbers' Association, N. Y., 1889, says: I find that while greenhouses were formerly heated by 4-inch and 3-inch cast-iron pipe, on account of the large body of heated by 4-inch and 3-inch cast-ivon pipe, on account of the targe cody of water which they contained, and the supposition that they gave better satisfaction and a more even temperature, florists of long experience who have tried 4-inch and 3-inch cast-iron pipe, and also 2-inch wrought-iron pipe for a number of years in heating their greenlouses by hot water, and who have also tried steam-heat, tell me that they get better satisfaction, greater economy, and are able to maintain a more even temperature with 2-inch wrought-iron pipe and hot water than by any other system they have used. They attribute this result principally to the fact that this size pipe contains less water and on this account the heat can be raised and lowered quicker than by any other arrangement of pipes, and a more uniform temperature maintained than by steam or any other system.

HOT-WATER HEATING.

(Nason Mfg. Co.)

There are two distinct forms or modifications of hot-water apparatus, de-

pending upon the temperature of the water.

In the first or open-tank system the water is never above 212° temperature, and rarely above 200°. This method always gives satisfaction where the surface is sufficiently liberal, but in making it so its cost is considerably greater than that for a steam-heating apparatus.

In the second method, sometimes called (erroneously) high-pressure hot-

water heating, or the closed-system apparatus, the tank is closed. If it is provided with a safety-valve set at 10 lbs. it is practically as safe as the open-

tank system.

Law of Velocity of Flow.—The motive power of the circulation in a hot-water apparatus is the difference between the specific gravities of the water in the ascending and the descending pipes. This effective pressure is very small, and is equal to about one grain for each foot in height for each degree difference between the pipes; thus, with a height of 12" in "up" pipe, and a difference between the temperatures of the up and down pipes of 8°, the difference in their specific grawities is equal to 8.16 grains on each square inch of the section of return-pipe, and the velocity of the circulation is proportioned to these differences in temperature and height.

To Calculate Velocity of Flow.—Thus, with a height of ascending pipe equal to 10' and a difference in temperatures of the flow and return pipes of 8° , the difference in their specific gravities will equal 81.6 grains, or +7000 = .01166 lbs., or $\times 2.81$ (feet of water in one pound) = .0269 ft., and by the law of falling bodies the velocity will be equal to $8\sqrt{.0269} = 1.312$ ft. per second, or \times 60 = 78.7 ft. per minute. In this calculation the effect of friction is entirely omitted. Considerable deduction must be made on this account. Even in apparatus where length of pipe is not great, and with pipes of larger areas and with few bends or angles, a large deduction for friction must be made from the theoretical velocity, while in large and complex apparatus with small head, the velocity is so much reduced by friction that sometimes as much as from 50% to 90% must be deducted to obtain the true rate of circulation.

Main flow-pipes from the heater, from which branches may be taken, are

to be preferred to the practice of taking off nearly as many pipes from the heater as there are radiators to supply.

It is not necessary that the main flow and return pipes should equal in capacity that of all their branches. The hottest water will seek the highest level, while gravity will cause an even distribution of the heated water if the surface is properly proportioned.

It is good practice to reduce the size of the vertical mains as they ascend,

say at the rate of one size for each floor.

As with steam, so with hot water, the pipes must be unconfined to allow

for expansion of the pipes consequent on having their temperatures increased.

An expansion tank is requ'red to keep the apparatus filled with water, which latter expands 1/24 of its bulk on being heated from 40° to 212°, and the cistern must have capacity to hold certainly this increased bulk. It is recommended that the supply cistern be placed on level with or above the highest pipes of the apparatus, in order to receive the air which collects in the mains and radiators, and capable of holding at least 1/20 of the water in the entire apparatus,

Approximate Proportions of Radiating-surfaces to Cubic Capacities of Space to be Heated.

One Square Foot of Ra- diating-surface will heat with—	In Dwellings, School-rooms, Offices, etc.	In Halls, Stores, Lofts, Facto- ries, etc.	In Churches, Large Audito- riums, etc.
High temperature di- rect hot-water radi- ation	50 to 70 cu. ft.	65 to 90 cu. ft.	130 to 180 cu. ft.
Low temperature di- rect hot-water radi- ation	80 to 50 " "	85 to 65 " "	70 to 130 " "
High temperature in- direct hot-water ra- diation	80 to 60 " "	85 to 75 " "	70 to 150 " "
Low temperature in- direct hot-water ra- diation	20 to 40 " "	25 to 50 " "	50 to 100 " "

Diameter of Main and Branch Pipes and square feet of coil surface they will supply, in a low-pressure hot-water apparatus (212°) for direct or indirect radiation, when coils are at different altitudes for direct radiation or in the lower story for indirect radiation:

Diam. of Pipe, in inches.	Indirect Radiation	Dir	ect Ra	diatio	n. He	ight of in f	Coil a	bove I	Bottom	of Bo	ile r ,
ğ	0	10	20	30	40	50	60	70	80	90	100
	sq. ft.		sq. ft.	sq. ft.	sq. ft.	sq. ft.	sq. ft.	sq. ft.	sq.ft.	sq. ft.	sq. ft.
34	49	50	52	58	55	57	59	61	68	65	68
1	87	89	92	95	98	101	103	108	112	116	121
11/4 11/6	136	140	144	149	153	158	161	169	175	182	169
11/2	196	202	209	214	222	228	235	243	252	261	271
2	349	859	370	380	393	405	413	433	449	465	483
216	546	561	577	595	613	633	643	678	701	727	755
3	785	807	835	856	888	912	941	974	1009	1046	1086
31/6	1069	1099	1182	1166	1202	1241	1283	1327	1374	1425	1480
4	1395	1436	1478	1520	1571	1621	1654	1783	1795	1861	1933
416	1767	1817	1871	1927	1988	2052	2120	2193	2272	235€	2445
5	2185	2244	2309	2376	2454	2531	2574	2713	2805	2907	3019
5 6 7	8140	3228	3341	3424	8552	3648	3768	3897	4036	4184	4344
7	4276	4396	4528	4664	4808	4964	5132	5308	5496	5700	5920
8 9	5580	5744	5912	6080	6284	6484	6616	6932	7180	7444	7785
9	7068	7268	7484	7708	7952	8208	8482	8774	9088	9424	9780
10	8740	8976	9236	9516	9816	10124	10296	10852	11220	11628	12076
11	10559	10860	11180	11519	11879	12262	12666	13108	13576	14078	14620
12	12560	12912	13364	13696	14208	14592	15052	15588	16144	16736	17376
18	14748	15169	15615	16090	16591	17126	17697	18307	18961	19633	20420
14	17104	17584	18109	18656	19282	19856	20528	21232		22800	23680
15	19684	20195		21419	22089	22801	23561	24373	25244	26179	27168
16	22320	22978	28643	24320	25136	25936	26464	27728	28720	29776	30928
			_								

The best forms of hot-water-heating boilers are proportioned about as

1 sq. ft. of grate-surface to about 40 sq. ft. of boiler-surface.
1 " boiler " 5 " radiating-surfa
1 " grate- " 900 " " " 5 " " radiating surface.
" 200 " " " grate-

Rules for Hot-water Heating.—J. L. Saunders (Heating and Ventilation. Dec 15, 1894) gives the following: Allow 1 sq. ft. of radiating surface for every 3 ft. of glass surface, and 1 sq. ft. for every 30 sq. ft. of wall surface, also 1 sq. ft. for the following numbers of cubic feet of space in the several cases mentioned.

In dwelling-bouses: Libraries and dining-rooms, first floor.. 35 to 40 cu. ft. Public-school rooms 60 to 85 "
Offices 50 to 65 "
Ractories and stores 65 to 90 "
Assembly halls and churches 90 to 150 " " 44

To find the necessary amount of indirect radiation required to heat a room: Find the required amount of direct radiation according to the foregoing method and add 50%. This if wrought-iron pipe coil surface is used; if castiron pin indirect-stack surface is used it is advisable to add from 70% to 80%.

Sizes of hot air flues, cold-air ducts, and registers for indirect work.—
Hot-air flues, first floor: Make the net internal area of the flue equal to

Hot-air flues, first floor: Make the n-t internal area of the flue equal to \$4 sq. in. to every square foot of radiating surface in the indirect stack. Hot-air flues, second floor: Make the n-t internal area of the flue equal to \$6 sq. in. to every square foot of radiating surface in the indirect stack.

Cold-air ducts, first floor: Make the net internal area of the duct equal to \$6 sq. in to every square foot of radiating surface in the indirect stack. Cold air ducts, second floor: Make the net internal area of the duct equal to \$6 sq. in. to every square foot of radiating surface in the indirect stack.

Hot-air registers should have their net area equal in full to the area of the hot-air flues. Multiply the length by the width of the register in inches; \$6 of the product is the net area of register.

of the product is the net area of register.

Arrangement of Mains for Hot-water Heating. (W. M. Mackay, Lecture before Master Plumbers' Assoc., N. Y., 1889.)—There are two different systems of mains in general use, either of which, if properly placed, will give good satisfaction. One is the taking of a single large-flow main from the beater to supply all the radiators on the several floors, with a corresponding return main of the same size. The other is the taking of a number of 2 inch wrought-iron mains from the heater, with the same number of return mains of the same s ze, branching off to the several radiators or coils with 1¼-inch or 1-inch pipe, according to the size of the radiator or coil. A 2 inch main will supply three 1¼-inch or four 1-inch branches and these branches should be taken from the top of the horizontal main with a nipple and elbow, except in special cases where it is found necessary to retard the flow of water to the near radiator, for the purpose of assisting the circulation in the far radiator; in this case the branch is taken from the side of the horizontal main. The flow and return mains are usually run side by side, suspended from the basement ceiling, and should have a gradual ascent from the heater to the radiators of at least 1 inch in 10 feet. It is customary, and an advantage where 2-inch mains are used, to reduce the size of the main at every point where a branch is taken off.

The single or large main system is best adapted for large buildings; but there is a limit as to size of main which it is not wise to go beyond -gener-

ally 6-inch, except in special cases.

The proper area of cold-air pipe necessary for 100 square feet of indirect radiation in hot water heating is 75 square inches, while the hot air pipe should have at least 100 square inches of area. There should be a damper in the cold-air pipe for the purpose of controlling the amount of air admitted to the radiator, depending on the severity of the weather,

THE BLOWER SYSTEM OF HEATING AND VENTILATING.

The system provides for the use of a fan or blower which takes its supply of fresh air from the outside of the building to be heated forces it over steam coils, located either centrally or divided up into a number of indepen-

steam coils, located either centrally or divided up into a number of independent groups, and then into the several ducts or flues leading to the various rooms. The movement of the warmed air is positive, and the delivery of the air to the various points of supply is certain and entirely independent of atmospheric conditions. For engines, fans, and steam-coils used with the lower system, see page 519.

Experiments with Hadiators of 60 sq. ft. of Surface. (Mech. News, Dec., 1893.—After having determined the volume and temperature of the warm air passing through the flues and radiators from natural causes, a fan was applied to each flue, forcing in air, and new sets of measurements were made. The results showed that more than two and one-third times as much air was warmed with the fans in use, and the falling off in the temperature of this greatly increased air-volume was only about 12.6%. The condensation of steam in the radiators with the forced-air circulation The condensation of steam in the radiators with the forced-air circulation also was only 66% greater than with natural-air draught. One of the several sets of test figures obtained is as follows:

	Natural	Forc∩d-
	Draught	
i	n Flue.	Circulation.
Cubic feet of air per minute	. 457.5	1227
Condensation of steam per minute in ounces	. 11.7	19.6
Steam pressure in radiator, pounds	. 9	9
Temperature of air after leaving radiator	. 142°	124°
" before passing through radiator.	. 61°	61°
Amount of radiating surface in square feet	. 6 0	60
Size of flue in both cases	. 12 ×	18 inches.

There was probably an error in the determination of the volume of air in these tests, as appears from the following calculation. (W. K.) Assume that 1 lb. of steam in condensing from 9 lbs. pressure and cooling to the temperature at which the water may have been discharged from the radiator gave up 1000 heat-units, or 62.5 h. u. per ounce; that the air weighed .076 lb, per cubic foot, and that its specific heat is .238. We have

	Natural Draught.	
Heat given up by steam, ounces \times 62.5 = Heat received by air, cu. ft. \times .076 \times diff. of tem. \times .288 =	781 678	1225 H.U. 1899 ''

Or, in the case of forced draught the air received 14% more heat than the steam gave out, which is impossible. Taking the heat given up by the steam as the correct measure of the work done by the radiator, the temperature of the steam at 237°, and the average temperature of the air in the case of natural draught at 102° and in the other case at 33°, we have for the temperature difference in the two cases 135° and 144° respectively; dividing these into the heat-units we find that each square foot of radiating surface transmitted 5.4 heat-units per hour per degree of difference of temperature, in the case of natural draught, and 8.5 heat-units in the case of forced draught (= 8.5 × 144° = 1224 heat-units per square foot of surface). In the Women's Homeopathic Hospital in Philadelphia, 2000 feet of

In the Women's Homeopathic Hospital in Philadelphia, 2000 feet of one-inch pipe heats 250,000 cubic feet of space, ventilating as well; this equals one square foot of pipe surface for about 350 cubic feet of space, or I is than 3 square feet for 1000 cubic feet. The fan is located in a separate building about 100 feet from the hospital, and the air, after being heated to about 135°, is conveyed through an underground brick duct with a loss of only five or six degrees in cold weather. (H. I. Snell, Trans. A. S. M. E. ix. 106.

Heating a Building to 70° F. Inside when the Outside Temperature is Zero.—It is customary in some contracts for heating to guarantee that the apparatus will heat the interior of the building to 70° in zero weather. As it may not be practicable to obtain zero weather.

in zero weather. As it may not be practicable to obtain zero weather for the purpose of a test, it may be difficult to prove the performance of the guarantee. E. E. Macgovern, in Engineering Record, Feb. 3, 1894, gives a calculation tending to show that a test may be made in weather of a higher temperature than zero, if the heat of the interior is raised above 70°. The higher the temperature of the rooms the lower is the efficiency of the radiating-surface, since the efficiency depends upon the difference between the

temperature inside of the radiator and the temperature of the room. He concludes that a heating apparatus sufficient to heat a given building to 70° in zero weather with a given pressure of steam will be found to heat the same building, steam-pressure constant, to 110° at 60°, 35° at 50°, 82° at 40°, and 74° at 32° outside temperature. The accuracy of these figures, however has not been tested by experiment.

The following solution of the question is proposed by the author. It gives results quite different from those of Mr. Macgovern, but, like them, lacks ex-

perimental confirmation.

Let S = sq. ft. of surface of the steam or hot-water radiator;
W = sq. ft. of surface of exposed walls, windows, etc.;
Ts = temp. of the steam or hot water, T₁ = temp. of inside of building or room,
a = heat-units transmitted per sq. ft. of surface of radiator per hour per degree of difference of temperature;
b = average heat-units transmitted per sq. ft. of walls per hour, per degree of difference of temperature;

degree of difference of temperature, including allowance for ventilation.

It is assumed that within the range of temperatures considered Newton's law of cooling holds good, viz., that it is proportional to the difference of temperature between the two sides of the radiating-surface.

Then
$$aS(T_s - T_1) = bW(T_1 - T_0)$$
. Let $\frac{bW}{aS} = C$; then
$$T_s - T_1 = C(T_1 - T_0); \quad T_1 = \frac{T_s + CT_0}{1 + C}; \quad C = \frac{T_s - T_1}{T_1 - T_0}.$$
If $T_1 = 70$, and $T_0 = 0$, $C = \frac{T_s - 70}{70}$.

Let $T_s = 140^\circ$, 213.5°, 308°; Then $C = 1$, 2.05, 3.4.

From these we derive the following:

Temperature of		Out	side Te	mperatu	res, Ta.		
Steam or Hot	20°	10°	0°	710°	20°	80°	40°
Water, Ts.		Insid	e Temr	eratures	s. T1.		
140°	60	65	70	75	60	85	90
213.5	56.6	63.3	70	76.7	83.4	90.2	96.9
308	54.5	62.3	70	77.7	85.5	93.2	100.9

Heating by Electricity.—If the electric currents are generated by a dynamo driven by a steam-engine, electric heating will prove very expensive, since the steam-engine wastes in the exhaust-steam and by radiation about 90% of the heat-units supplied to it. In direct steam heating, with a good boiler and properly covered supply-pipes, we can utilize about 60% of the total heat value of the fuel. One pound of coal, with a heating value of 18,000 heat-units, would supply to the radiators about $13,000 \times .60 = 7800$ heat-units. In electric heating, suppose we have a first-class condensing-engine developing 1 H.P. for every 2 lbs. of coal burned per hour. This would be equivalent to 1,980,000 ft.-lbs. + 7.78 = 2545 heat-units or 1272 heat-units for 1 lb. of coal. The friction of the engine and of the dynamo and the loss by electric leakage, and by heat radiation from the conducting wires, might reduce the heat-units delivered as electric current to the electric radiator, and these converted into heat to 50% of this, or only 686 heat-units, or less than one twelfth of that delivered to the steam-radiators in direct steam-heating. Electric heating therefore, will prove uneconomical unless the electric current is derived from water or wind power, which would otherwise be wasted. (See Electrical Engineering.)

WATER.

Expansion of Water.—The following table gives the relative volumes of water at different temperatures, compared with its volume at 4° C. according to Kopp, as corrected by Porter.

Cent.	Fahr.	Volume.	Cent.	Fahr.	Volume.	Cent.	Fahr.	Volume.
4° 5 10 15 20 25 80	89.1°	1.00000	85°	95°	1.00586	70°	158°	1.02241
	41	1.00001	40	104	1.00767	75	167	1.02548
	50	1.00025	45	113	1.00967	80	176	1.02872
	59	1.00088	50	122	1.01186	85	185	1.08213
	68	1.00171	55	131	1.01423	90	194	1.03570
	77	1.00286	60	140	1.01678	95	203	1.03943
	86	1.00425	65	149	1.01951	100	212	1.04832

Weight of 1 cu. ft. at 89.1° F. = 62.4245 lb. +1.04832 = 59.833, weight of 1 cu. ft. at 212° F.

Weight of Water at Different Temperatures.—The weight of water at maximum density, 39.1°, is generally taken at the figure given by Rankine, 62.425 lbs. per cubic foot. Some authorities give as low as 62.379. The figure 62.5 commonly given is approximate. The highest authoritative figure is 62.425. At 62° F. the figures range from 62.291 to 62.360. The figure 62.355 is generally accepted as the most accurate. At 32° F. figures given by different writers range from 62.379 to 62.418. Clark gives the latter figure, and Hamilton Smith, Jr., (from Rosetti,) gives

62,416.

Weight of Water at Temperatures above 212° F.—Porter (Richards' "Steam-engine Indicator," p. 52) says that nothing is known about the expansion of water above 212°. Applying formulæ derived from experiments made at temperatures below 212°, however, the weight and volume above 212° may be calculated, but in the absence of experimental data we are not certain that the formulæ hold good at higher temperatures.

Thurston, in his "Engine and Boiler Trials," gives a table from which we take the following (neglecting the third decimal place given by him):

Tempera-	Weight, 108.	Tempera-	Weight, lbs.	Tempera-	Weight, Ibs.	Tempera-	Weight, lbs.	Tempera-	Weight, lbs.
ture,	per cubic	ture,	per cubic	ture,	per cubic	ture,	per cubic	ture,	per cubic
deg. F.	foot.	deg. F.	foot.	deg. F.	foot.	deg. F.	foot.	deg. F.	foot,
212	59.71	280	57.90	850	55.52	420	52.86	490	50.03
220	59.64	290	57.59	860	55.16	430	52.47	500	49.61
230	59.87	800	57.26	870	54.79	440	52.07	510	49.20
240	59.10	810	56.93	880	54.41	450	51.66	520	48.78
250	58.81	820	56.58	890	54.03	460	51.26	530	48.36
260	58.52	830	56.24	400	58.64	470	50.85	540	47.94
270	58.21	840	55.88	410	58.26	480	50.44	550	47.52

Box on Heat gives the following:

400° Temperature F..... 212° 2500 8000 8500 4500 5000 Lbs. per cubic foot.... 59.82 58.85 57.42 55.94 54.84 52.70 51.02 47.64

At 212º figures given by different writers (see Trans. A. S. M. E., xiii. 409) range from 59.56 to 59.845, averaging about 59.77.

Weight of Water per Cubic Foot, from 82° to 213° F., and heatunits per pound, reckoned above 32° F.: The following table, made by interpolating the table given by Clark as calculated from Rankine's formula, with corrections for apparent errors, was published by the author in 1884, Trans. A. S. M. E., vi. 90. (For heat units above 212° see Steam Tables.)

Temp., deg. F.	Weight, lbs. per cubic foot.	Heat-units.	Tempera- ture, deg. F.	Weight, lbs. per cubic foot.	Heat-units.	Tempera- ture, deg. F.	Weight, lbs. per cubic foot.	Heat-units.	Tempera- ture, deg. F.	Weight, Ibs. per cubic foot.	Heat-units.
32	62.42	0.	78 79	62.25	46.03	123	61.68	91.16	168		136.44
83 84	62.42 62.42	1.	80	62.24 62.23	47.03 48.04	124 125	61.67 61.65	92.17 93.17	169 170	60.79	137.45 138.45
85	62.42	2. 3.	81	62.22	49.04	126	61.68	94.17	171	60.75	189.46
36	62.42	4.	82	62 31	50.04	127	61.61	95.18	172	60.78	140,47
87	62.42	5.	83	62 20	51.04	128	61.60	96.18	173	60.70	141.48
88 89	62.42	6. 7.	84 98	62.19 62.18	52.04 53.05	129 180	61.58 61.56	97.19 98.19	174 175	80.68	142.49
40	62.42	8.	85 86	62 7	54.05	131	61.54	99.20	176		144.51
41	62.42	9.	87	62.16	55.05	182	61.52	100.20	177	60.62	145.52
42	62.42	10.	88 89	62.15	56.05	133	61.51	101.21	178		146.52
43 44	62.42	11. 12.	90	62 14 62 13	57.05 58.06		61.49	102.21 103.22	179 180		147.58 148.54
45	62.42	13.	91	62 12	59.06			104.22	181		149.55
46	62.42	14.	92	62.11	60.06	137	61.43	105.23	182	60.50	150.56
47	62.42	15.	93	62.10	61.06		61.41	106.23	188		151.57
48 49	62.41 62.41	16. 17.	94 95	62.09 62.08	62.06 63.07	139 140		107.24 108.25	184 185		152,58
50	62.41	18.	96	62.07	64.07			109.25			153.59
51	62.41	19.	97	62 06	65.07		61.84	110.26	187	60.89	155.61
52 58 54	62.40	20.	98	62.05	66.07	143	61 82	111.26	188	60.87	156.62
58	62.40	21.01	99 100	62.03	67.08	144	61.80	112.27 113.28	189	60.34	157.63
54 55	62.40 62.89	22.01 28.01	100 101	62 02 62 01	68.08 69.08	145 146	61.28	113.28 114.28	190 191		158.64 159.65
56	62.39	24.01	102	62 00	70.09	147	61 24	115.29	192	60.27	160.67
56 57 58 59 60 61 62	62.89	25.01	103	61.99	71.09		61.22	116.29	198	60.25	161.68
58	62.38	26.01	104	61 97	72.09	149	61.20	117.80	194		162.69
59	62.38	27.01	105	61.96	78.10	150	61.18	118.81	195 196		163.70
60	62.37 62.37	28.01 29.01	106 107	61.95 61.93	74.10 75.10	151 152	61.10	119.31 120.83	196 197		164.71
62	62 36	30.01	108	61 92	76.10	153	61.12	121.83	198	60 1	166.73
68	62.36	81.01	109	61 91	77.11	154	61.10	122.33	199	60.10	167.74
64	68.55	82.01	110	61.89	78.11	155	61.08	123.34	200	60.07	168.75
65	62.34 62.34	83.01	111	61.88 61.86	79.11	156	61.06	121.85 125.85	201 202	60 03	169.77
66 67	62.88	84.02 85.02	112 113	61 36	80.12 81.12	157 158		125.85	202	60.00	
68	62.33	86.02	114	61 33	82.13		61.00	127.87	204		172.80
69	62.32	87.02	115	61.82	83.13	160	60.98	128.37	205	59,95	173.81
70	62.81	88.02	116	61 30	84.18		60 96	129.38	206	59,9	2 174.83
71	62.31	39.02	117	61.78 61.77	85.14		60.94	130.39 131.40	207 208	59.89	175.8
72 73	62.30 62.29	40.02 41.02	118 119	61.75	86.14 87.15	164	60.90	132.41	209	59.84	176.82 177 St
74	62.28	42.03	120	61 .74	88.15	165	60.87	1:3.41	210		178.87
75	62.28	43.03	121	61 72	89.15	166	60 85	134.42	211	59.73	179.89
76 77	62.27	44.03	122	61.70	90.16	167	1 60.88	135.43	212	59.70	180.90

Comparison of Heads of Water in Feet with Pressures in Various Units.

One foot of water at 39°.1 Fahr. = 62.425 lbs. on the square foot;
= 0.4335 lbs. on the square inch;
= 0.0995 atmosphere;
= 0.8826 inch of mercury at 32°;
= 773.3 feet of air at 32° and atmospheric pressure;

	One lb, on the square foot, at 89°.1 Fahr	=	0.01602	foot	of	water:	
	One lb. on the square inch "	=		feet	of '	water:	
	One atmosphere of 29.922 inches of mercury	=	83.9	• •		44	
	One inch of mercury at 82°.1	=	1.138	44		44	
	One foot of air at 32 deg., and one atmosphere	=	0.001293	64	44	44	
	One foot of average sea-water	=	1.026 foot	t of r	our	e water	•
	One foot of water at 62° F	=	62.855 lbs	ı, per	. ed	. foot;	•
	" " " 62° F	=	0.43302 1	b. pe	rs	q. inch:	:
•	One inch of water at 62° F = 0.5774 ounce :	=	0.036085	lb, p	er	sa. incl	í:
	One pound of water on the square inch at 62° F. :	=	2.3094 fe	et of	Wε	iter.	•
	One ounce of water on the square inch at 62° F. :	=	1.782 inc	hes c	of v	vater.	

Pressure in Pounds per Square Inch for Different Heads of Water.

At 62° F. 1 foot head = 0.438 lb. per square inch, $.433 \times 144 = 62.352$ lbs. per cubic foot.

Head, feet.	0	1	2	8	4	5	6	7	8	9
	I	0.433	0.866	1.299	1.732	2.165	2.598	8.031	8.464	3.897
10	4.830	4.763	5.196		6.062	6.495	6.928	7.861		8.227
20	8.660								12.124	
30									16.454	
40									20.784	
50									25.114	
60	25.980	26.413	26.846	27.279	27.712	28.145	28.578	29.011	29.444	29.877
70									88.774	
80									38.104	
90	38.970	39.408	39.836	40.269	40.702	41.135	41.568	42.001	42.436	42.867
	1				1	1)

Head in Feet of Water, Corresponding to Pressures in Pounds per Square Inch.

1 lb. per square inch = 2.30947 feet head, 1 atmosphere = 14.7 lbs. per sq. inch = 33.94 ft. head.

Pressure.	0	1	2	8	4	5	6	7	8	9
0)	2.309	4.619	6.928	9.238	11.547	13.857	16.166	18.476	20 785
10	23.0947	25.404	27.714	30.023	32.333	34.642	86.952	89.261	41.570	48.880
20	46,1894									
3 0	69.2841	71.594	73.903	76.213	78.522	80.881	88.141	85.450	87.760	90.069
40	92.3788									
50	115.4735	117.78	120.09	122.40	124.71	127.02	129.33	131.64	133.95	136.26
60	138.5682									
70	161.6629	163.97	166.28	168.59	170.90	178 21	175.52	177.83	180,14	182.45
80	184.7576	187.07	189.38	191.69	194 00	196.31	198.61	200.92	203.23	205.54
90	207.8523	210.16	212.47	214.78	217.09	219.40	221.71	224.02	226.33	228.64
					l			.		

Pressure of Water due to its Weight.—The pressure of still water in pounds per square inch against the sudes of any pipe, channel, or vessel of any shape whatever is due solely to the "head," or height of the level surface of the water above the point at which the pressure is considered, and is equal to .43302 lb. per square inch for every foot of head, or 62.855 lbs. per square foot for every foot of head (at 62° F).

The pressure per square inch is equal in all directions, downwards, upwards, or sideways, and is independent of the shape or size of the containing vessel.

The pressure against a vertical surface, as a retaining-wall, at any point is in direct ratio to the head above that point, increasing from 0 at the level surface to a maximum at the bottom. The total pressure against a vertical strip of a unit's breadth increases as the area of a right-angled triangle

550 WATER.

whose perpendicular represents the height of the strip and whose base represents the pressure on a unit of surface at the bottom; that is, it increases as the square of the depth. The sum of all the horizontal pressures is represented by the area of the triangle, and the resultant of this sum is equal to this sum exerted at a point one third of the height from the bottom.

(The centre of gravity of the area of a triangle is one third of its height.)

The horizontal pressure is the same if the surface is inclined instead of

vertical.

(For an elaboration of these principles see Trautwine's Pocket-Book, or the chapter on Hydrostatics in any work on Physics. For dams, retainingwalls, etc., see Trautwine.)

The amount of pressure on the interior walls of a pipe has no appreciable

The amount of pressure on the interior wans of a pipe has no appreciative effect upon the amount of flow.

Bueyancy.—When a body is immersed in a liquid, whether it float or sink, it is buoyed up by a force equal to the weight of the bulk of the liquid displaced by the body. The weight of a floating body is equal to the weight of the bulk of the liquid that it displaces. The upward pressure or buoyancy of the liquid may be regarded as exerted at the centre of gravity of the displaced water, which is called the centre of pressure or of buoyancy. A vertical line drawn through it is called the axis of buoyancy or of floating the desired by at each align industry the centre of gravity and the tion. In a floating body at rest a line joining the centre of gravity and the centre of buoyancy is vertical, and is called the axis of equilibrium. When an external force causes the axis of equilibrium to lean, if a vertical line be drawn upward from the centre of buoyancy to this axis, the point where it cuts the axis is called the metacentre. If the metacentre is above the centre of gravity the distance between them is called the metacentric height, and the body is then said to be in stable equilibrium, tending to return to its

original position when the external force is removed.

Bolling-point,—Water boils at 212° F. (100° C.) at mean atmospheric pressure at the sea-level, 14.696 lbs. per square inch. The temperature at which water boils at any given pressure is the same as the temperature of saturated steam at the same pressure. For boiling-point of water at other pressure than 14.696 lbs. per square inch, see table of the Properties of

Saturated Steam.

The Boiling-point of Water may be Baised,—When water is entirely freed of air, which may be accomplished by freezing or boiling, the cohesion of its atoms is greatly increased, so that its temperature may be raised over 50° above the ordinary boiling-point before ebullition taker place. It was found by Faraday that when such air-freed water did boil the rupture of the liquid was like an explosion. When water is surrounded by a film of oil, its boiling temperature may be raised considerably above its normal standard. This has been applied as a theoretical explanation in the instance of boiler-explosions.

The freezing-point also may be lowered, if the water is perfectly quiet, to 10° C., or 18° Fahrenheit below the normal freezing-point. (Hamilton

mith, Jr., on Hydraulics, p. 13.) The density of water at 14° F. is .99814, its density at 39°. 1 being 1, and at 32°, .99987.

Freezing=point.—Water freezes at 32° F. at the ordinary atmospheric pressure, and ice melts at the same temperature. In the melting of 1 pound of ice into water at 32° F. about 142 heat-units are absorbed, or become latent: and in freezing 1 lb. of water into ice a like quantity of heat is given

out to the surrounding medium.

Sea-water freezes at 27° F. The ice is fresh. (Trautwine.)

Ice and Snow. (From Clark.)—1 cubic foot of ice at 32° F. weighs

57.50 lbs.; 1 pound of ice at 32° F. has a volume of .0174 cu. ft. = 30.067 cu. in. Relative volume of ice to water at 32° F., 1.0855, the expansion in passing into the solid state being 8.55%. Specific gravity of ice = 0.922, water at 62º F. being 1.

At high pressures the melting point of ice is lower than 82° F., being at the rate of .0183° F. for each additional atmosphere of pressure

The specific heat of ice is .504, that of water being 1

1 cubic foot of fresh snow, according to humidity of atmosphere; 5 lbs. to 12 lbs. I cubic foot of snow moistened and compacted by rain: 15 lbs. to 50 lbs. (Trautwine).

Specific Heat of Water. (From Clark's Steam-engine.)—Calculated by means of Regnault's formula, $c=1+0.00004t+0.0000000t^3$, in which c is the specific heat of water at any temperature t in centig; ale degrees, the specific heat at the freezing-point being 1.

Tem		sh Ther- Units pound, ve 32° F.	ific Heat he given nperature.	Specific t between r. and the n Temp.	Tem;	pera- res.	sh Ther- Units pound, ve 32° F.	fic Heat le given perature.	Specific t between F. and the
Cent.	Fahr.	13 2 1 0	Speci at th Tem	Mean Heat 32° F. given	Cent.	Fahr.	British mal U per po above	Specific at the Temper	Mean Heat 32° F given
0° 10 20 30 40	32° 50 68 86 104	0.000 18.004 36.018 54.047 72.090		1.0002 1.0005 1.0009 1.0013	120° 130 140 150 160	248° 266 284 302 320	217.449 235.791 254.187 272.628 291.132	1.0177 1.0204 1.0232 1.0262 1.0294	1.0067 1.0076 1.0087 1.0097 1.0109
50 60 70 80 90 100	122 140 158 176 194 212 230	90.157 108.247 126.378 144.508 162.686 180.900 199.152	1.0042 1.0056 1.0072 1.0089 1.0109 1.0130 1.0153	1.0017 1.0023 1.0030 1.0035 1.0042 1.0050 1.0058	170 180 190 200 210 220 230	838 856 874 892 410 428 446	309.690 328.320 347.004 365.760 384.588 403.188 422.478	1.0328 1.0864 1.0401 1.0440 1.0481 1.0524 1.0568	1.0121 1.0188 1.0146 1.0160 1.0174 1.0189 1.0204

Compressibility of Water.—Water is very slightly compressible. Its compressibility is from .000010 to .000051 for one atmosphere, decreasing with increase of temperature. For each foot of pressure distilled water will be diminished in volume .0000015 to .0000013. Water is so incompressible that even at a depth of a mile a cubic foot of water will weigh only about half a pound more than at the surface.

THE IMPURITIES OF WATER.

(A. E. Hunt and G. H. Clapp, Trans. A. I. M. E. xvii. 338.)

Commercial analyses are made to determine concerning a given water: (1) its applicability for making steam; (2) its hardness, or the facility with which it will "form a lather" necessary for washing; or (3) its adaptation to other manufacturing purposes.

At the Buffalo meeting of the Chemical Section of the A. A. A. S. it was decided to report all water analyses in parts per thousand, hundred-thousand,

and million.

To convert grains per imperial (British) gallons into parts per 100,000, di-ride by 0.7. To convert parts per 100,000 into grains per U. S. gallon, mul-

tiply by 7/12 or .588.

The most common commercial analysis of water is made to determine its fitness for making steam. Water containing more than 5 parts per 100,000 of free sulphuric or nitric acid is liable to cause serious corrosion, not only of the metal of the boiler itself, but of the pipes, cylinders, pistons, and valves with which the steam comes in contact.

The total residue in water used for making steam causes the interior lin-ings of boilers to become coated, and often produces a dangerous hard

scale, which prevents the cooling action of the water from protecting the metal against burning.

Lime and magnesia bicarbonates in water lose their excess of carbonic acid on boiling, and often, especially when the water contains sulphuric acid, produce, with the other solid residues constantly being formed by the evaporation, a very hard and insoluble scale. A larger amount than 100 parts per 100,000 of total solid residue will ordinarily cause troublesome scale, and should condemn the water for use in steam-boilers, unless a better supply cannot be obtained.

The following is a tabulated form of the causes of trouble with water for steam purposes, and the proposed remedies, given by Prof. L. M. Norton.

CAUSES OF INCRUSTATION.

1. Deposition of suspended matter.

Deposition of deposed salts from concentration.

3. Deposition of carbonates of lime and magnesia by boiling off carbonic acid, which holds them in solution.

4. Deposition of sulphates of lime, because sulphate of lime is but slightly soluble in cold water, less soluble in hot water, insoluble above 270° F.

5. Deposition of magnesia, because magnesium salts decompose at high

temperature.

6. Deposition of lime soap, iron soap, etc., formed by saponification of grease.

MEANS FOR PREVENTING INCRUSTATION.

Filtration.
 Blowing off.

3. Use of internal collecting apparatus or devices for directing the circulation.

4. Heating feed-water.5. Chemical or other treatment of water in boiler.

6. Introduction of zinc into boiler.

7. Chemical treatment of water outside of boiler.

TABULAR VIEW.

Troublesome Substance. Sediment, mud, clay, etc.	Trouble. Incrustation.	Remedy or Palliation. Filtration; blowing off.
Readily soluble salts.		Blowing off.
Bicarbonates of lime, magnesia, iron.		Heating feed. Addition of caustic soda, lime, or magnesia, etc.
Sulphate of lime.	" .	Addition of carb. soda, barium hydrate, etc.
Chloride and sulphate of magne- sium.	Corrosion.	Addition of carbonate of soda, etc.
Carbonate of soda in large	Priming.	Addition of barium chlo- ride, etc.
Acid (in mine waters).	Corrosion.	Alkali.
Dissolved carbonic acid and and oxygen.	Corrosion.	Feed milk of lime to the boiler, to form a thin internal coating.
Grease (from condensed water).	Corrosion or incrustation.	Different cases require dif-
Organic matter (sewage).	Priming, corrosion, or incrustation.	ferent remedies. Consult a specialist on the subject.

The mineral matters causing the most troublesome boiler-scales are bicarbonates and sulphates of lime and magnesia, oxides of iron and alumina, and silica. The analyses of some of the most common and troublesome boiler-scales are given in the following table:

Analyses of Boiler-scale. (Chandler.)

							Sul- phate of Lime.	Mag- nesia.	Silica.	Per- oxide of Iron.	Water.	Car- bonate of Lime.
N. Y.	C.	& E	I.R.	Ry.,	No.	1	74.07	9.19	0.65	0.08	1.14	14.78
**		44	**		No.	2	71.87	1	1.76	1	1	. .
44		46	44		No.	8		18.95	2.60	0.92	1.28	12.62
**		46	66		No.	4	58.05	1	4.79	1	1	
44		44	66		No.	5			5.32		l	·
66		46	**		No.	6	30.80	81.17	7.75	1.08	2.44	26.98
46		66	44		No.	~	4.95	2.61	2.07	1.08	0.68	86.25
"		**	46		No.	8		2.84	0.65	0.36	0.15	93.19
"		66	**		No.	9	4.81	1	2.92	1		
44		**	66		No.				8.24	J	l	

Analyses	in	Parts	per	100,000	of	Water	giving	Bad

Results In	Ste	TAIL.	DOL	ters	• 14	L. Par	Hui	10.)	_	
	Bicarbonate of Lime deposited on Boiling.	Bicarbonate of Mag- nesia depos'd on Boil'g	Total Lime.	Total Magnesia.	Sulphuric Acid.	Chlorine,	Iron.	Organic Matter.	Alumina.	Chloride of Sodium.
Coal-mine water	110 151 75	25 38 89	119 190 95	39 48 120	890 860 310	590 990 21	780 38 75	30 21 10	640 30 80	1310
Monongahela River	130 80 82	21 70	161 94	81	210 219	38 210	70 90 38	****	::::	
Allegheny R., near Oil-works		82 50	61 41	104 68	28 800	190	38 23	116	741	13,45

Many substances have been added with the idea of causing chemical action which will prevent boiler-scale. As a general rule, these do more harm than good, for a boiler is one of the worst possible places in which to carry on chemical reaction, where it nearly always causes more or less corrosion of the metal, and is liable to cause dangerous explosions.

In cases where water containing large amounts of total solid residue is necessarily used, a heavy petroleum oil, free from tar or wax, which is not acted upon by acids or alkalies, not having sufficient wax in it to cause acted upon by acids or alkalies, not having sufficient wax in it to cause saponification, and which has a vaporizing-point at nearly 600° F., will give the best results in preventing boiler-scale. Its action is to form a thin greasy film over the boiler linings, protecting them largely from the action of acids in the water and greasing the sediment which is formed, thus preventing the formation of scale and keeping the solid residue from the evaporation of the water in such a plastic suspended condition that it can be easily ejected from the boiler by the process of "blowing off." If the water is not blown off sufficiently often, this sediment forms into a "putty" that will necessitate cleaning the boilers. Any boiler using bad water should

be blown off every twelve hours.

Hardness of Water.—The hardness of water, or its opposite quality, indicated by the ease with which it will form a lather with soap, depends almost altogether upon the presence of compounds of lime and magnesia. Almost all soaps consist, chemically, of cleate, stearate, and palmitate, of an alkaline base, usually soda and potash. The more lime and magnesia in a sample of water, the more soap a given volume of the water will decompose, so as to give insoluble cleate, pulmitate, and stearate of lime and magnesia, and consequently the more soa; must be added to a gallon of water in order that the necessary quantity of soap may remain in solution to form the lather. The relative hardness of samples of water is generally expressed in terms of the number of standard soap-measures consumed by a gallon of water in

yielding a permanent lather.

The standard soap-measure is the quantity required to precipitate one

grain of carbonate of lime.

It is commonly reckoned that one gallon of pure distilled water takes one soap-measure to produce a lather. Therefore one is deducted from the total number of soap-measures found to be necessary to use to produce a lather in a gallon of water, in reporting the number of soap-measures. or "degrees" of hardness of the water sample. In actually making tests for hardness, the "miniature gallon," or seventy cubic centimetres, is used rather than the inconvenient larger amount. The standard measure is made by completely disadying ten grapmes of nurse eastle soap (containing there by completely dissolving ten grammes of pure castile soap (containing 60 per cent olive-oil) in a litre of weak alcohol (of about 35 per cent alcohol). This yields a solution containing exactly sufficient soap in one cubic centimeter of the solution to precipitate one milligramme of carbonate of lime, or, in other words, the standard soap solution is reduced to terms of the "miniature gallon" of water taken. If a water charged with a bicarbonate of lime, magnesia, or iron is boile?

it will, on the excess of the carbonic acid being expelled, deposit a considerable quantity of the lime, magnesia, or iron, and consequently the water will be softer. The hardness of the water after this deposit of lime, after long boiling, is called the permanent hardness and the difference between it and the total hardness is called temporary hardness.

Lime salts in water react immediately on soap-solutions, precipitating the cleate, palmitate, or stearate of lime at once. Magnesia salts, on the contrary, require some considerable time for reaction. They are, however, more powerful hardeners; one equivalent of magnesia salts consuming as much soap as one and one-half equivalents of lime.

The presence of soda and potash salts softens rather than hardens water. Each grain of carbonate of lime per gallon of water causes an increased expenditure for soap of about 2 ounces per 100 gallons of water. (Engly.

News, Jan. 31, 1885.)

Purifying Feed-water for Steam-boilers. (See also Incrustation and Corrosion, p. 716.)—When the water used for steam-boilers contains a large amount of scale-forming material it is usually advisable to purify it before allowing it to enter the boiler rather than to attempt the prevention of scale by the introduction of chemicals into the boiler. Carbonates of lime and magnesia may be removed to a considerable extent by promotes or time and magnesia may be removed to a considerable extent by simple heating of the water in an exhaust-steam feed-vater heater or, still better, by a live-steam heater. (See circular of the Hoppes Mfg. Co., Springfield, O.) When the water is very bad it is best treated with chemicalshime, soda-ash, caustic soda, etc.—in tanks, the precipitates being separated by setting or filtering. For a description of several systems of water purification see a series of articles on the subject by Albert A. Cary in Eng'g Mag., 1897.

Mr. W. B. Coggswell, of the Solvay Process Co.'s Soda Works in Syracuse,

Mr. W. B. Coggswell, of the Solvay Process Co.'s Soda works in Syracuse, N. Y., thus describes the system of purification of boiler feed-water in use at these works (Trans. A. S. M. E., xiii. 255):

For purifying, we use a weak soda liquor, containing about 18 to 15 grams Na_2Co_3 per litre. Say 114 to 2 M^3 (or 397 to 530 gals.) of this liquor is run into the precipitating tank. Hot water about 60° C. is then turned in, and the reaction of the precipitation goes on while the tank is filling, which requires about 15 minutes. When the tank is full the water is filtered through the Hyatt (4), 5 feet diameter, and the Jewell (1), 10 feet diameter, filters in 30 minutes. Forty tanks treated per 24 hours.

 Soda in purifying reagent
 15 kgs. Na₂CO₃.

 Soda used per 1,000 gallons
 3.5 lbs.

A sample is taken from each boiler every other day and tested for deg. Baumé, soda and salt. If the deg. B. is more than 2, that boiler is blown to reduce it below 2 deg. B.

The following are some analyses given by Mr. Coggswell:

	Lake Water, grams per litre.	Mud from Hyatt Filter.	Scale from Boiler- tube.	Scale found in Pump,
Calcium sulphate	.261 .186	8.70	51.24	10.9
Calcium carbonate	.091	63.87 1.11	19.76 25.21	87.
Magnesium chloride	.087 .68		.14	
Silica Iron and aluminum oxide		15.17 8.75	2.29 1.10	.8 1.2
Total	1.270	87,10	99.74	99.9

Softening Hard Water for Locomotive Use.—A water-soft-ening plant in operation at Fossil, in Western Wyoming, on the Union Pa-cific Railway, is described in *Eng'g News*, June 9, 1892. It is the invention

of Arthur Pennell, of Kansas City. The general plan adopted is to first dissolve the chemicals in a closed tank, and then connect this to the supply main so that its contents will be forced into the main tank, the supply-pipe being so arranged that thorough mixture of the solution with the water is obtained. A waste-pipe from the bottom of the tank is opened from time to time to draw off the precipitate. The pipe leading to the tender is arranged to draw the water from near the surface.

A water-tank 24 feet in diameter and 16 feet high will contain about 46,600 gallons of water. About three hours should be allowed for this amount of water to pass through the tank to insure thorough precipitation, giving a permissible consumption of about 15,000 gallons per hour. Should more than this be required, auxiliary settling tanks should be provided.

The chemicals added to precipitate the scale-forming impurities are so-dium carbonate and quicklime, varying in proportions according to the rela-tive proportions of sulphates and carbonates in the water to be treated. Sufficient sodium carbonate is added to produce just enough sodium sulphate to combine with the remaining lime and magnesia sulphate and produce glauberite or its corresponding magnesia salt, thereby to get rid of the sodium sulphate, which produces foaming, if allowed to accumulate.

For a description of a purifying plant established by the Southern Pacific R. R. Co. at Port Los Angeles, Cal., see a paper by Howard Stillmann in Trans. A. S. M. E., vol. xix, Dec. 1897.

HYDRAULICS—FLOW OF WATER.

Formulæ for Discharge of Water though Orifices and Weirs,—For rectangular or circular orifices, with the need measured from centre of the orifice to the surface of the still water in the feeding reservoir.

$$Q = C \sqrt{2gH} \times a. \qquad (1)$$

For weirs with no allowance for increased head due to velocity of approach:

$$Q = C \frac{3}{6} \sqrt{2gH} \times LH. \qquad (2)$$

For rectangular and circular or other shaped vertical or inclined orifices; formula based on the proposition that each successive horizontal layer of water passing through the orifice has a velocity due to its respective head:

$$Q = cL\% \sqrt{2g} \times (\sqrt{Hb^2} - \sqrt{Ht^2}). \qquad (8)$$

For rectangular vertical weirs:

$$Q = c \% \sqrt{2gH} \times Lh. \qquad (4)$$

Q =quantity of water discharged in cubic feet per second; C =approximate coefficient for formulas (1) and (2); c =correct coefficient for (3) and (4).

Values of the coefficients c and C are given below.

g=32.16; $\sqrt{2g}=8.02$; H= head in feet measured from centre of orifice to level of still water; $H_0=$ head measured from bottom of orifice; $H_1=$ head measured from top of orifice; h = H, corrected for velocity of approach, $Va_1 = H + \frac{\pi}{3} \frac{c}{2a}$ -; a =area in square feet; L =length in feet.

Flow of Water from Orifices. - The theoretical velocity of water flowing from an orifice is the same as the velocity of a falling body which has fallen from a height equal to the head of water, = $\sqrt{2gH}$. The actual velocity at the smaller section of the vena contracta is substantially the same as the theoretical, but the velocity at the plane of the orifice is $C\sqrt{2gH}$, in which the coefficient C has the nearly constant value of .62. The smallest diameter of the vena contracta is therefore about .79 of that of the orifice. If C be the approximate coefficient = .62, and c the correct coefficient, the ratio $\frac{C}{c}$ varies with different ratios of the head to the diameter of the vertical orifice, or to $\frac{H}{D}$. Hamilton Smith, Jr., gives the following:

For
$$\frac{H}{D} = .5$$
 .875 1 1.5 2 2.5 5. 10. $\frac{C}{C} = .9604$.9849 .9918 .9965 .9980 .9987 .9997 1.

For vertical rectangular orifices of ratio of head to width W:

For
$$\frac{H}{W} = .5$$
 .6 .8 1 1.5 2. 8. 4. 5. 8. $\frac{C}{c} = .9428$.9657 .9823 .9890 .9953 .9974 .9988 .9998 .9996 .9996 For $H + D$ or $H + W$ over 8, $C = c$, practically.

Weisbach gives the following values of c for circular orifices in a thin wall. H = measured head from centre of orifice.

D ft.				H ft.			
D 11.	.066	.83	.82	2.0	8.0	45.	840.
.033 .066 .10	.711	.665	.637 .629 .622 .614	.628 .621 .614 .607	.641	.682	.600

For an orifice of D=.033 ft. and a well-rounded mouth piece, H being the effective head in feet,

$$H = .066$$
 1.64 11.5 56 888 $c = .959$.967 .975 .994 .994

Hamilton Smith, Jr., found that for great heads, 312 ft. to 336 ft., with converging mouthpieces, c has a value of about one, and for small circular orifices in thin plates, with full contraction, c = about .60. Some of Mr. Smith's experimental values of c for orifices in thin plates discharging into air are as follows. All dimensions in feet.

For the rectangular orifice, L, the length, is horizontal. Mr. Smith, as the result of the collation of much experimental data of others as well as his own, gives tables of the value of c for vertical orifices, with full contraction, with a free discharge into the air, with the inner face of the plate, in which the orifice is pierced, plane, and with sharp inner corners, so that the escaping vein only touches these inner edges. These tables are abridged below. The coefficient c is to be used in the formulæ (3) and (4) above. For formulæ (1) and (2) use the coefficient C found from the values of the ratios $\frac{C}{c}$ above.

Values of Coefficient c for Vertical Orifices with Sharp Edges, Full Contraction, and Free Discharge into Air. (Hamilton Smith, Jr.)

lead from Centre of Orifice H.		Square Orifices. Length of the Side of the Square, in feet.											
Head	.02	.03	.04	.05	.07	.1v	. 12.	. 15	.20	.40	.60	.80	1.0
.4 .6 1.0 3.0 6.0 10. 20. 100.(?)	.660 .648 .632 .623 .616 .606	.645 .686 .622 .616 .611 .605		.630 .622 .612 .609 .606	.628 .623 .618 .609 .607 .605 .602	.621 .617 .613 .607 .605 .604 .602	.616 .613 .610 .606 .605 .604 .602	.611 .610 .608 .606 .605 .603 .602	.605 .605 .604 .603 .602	.601 .603 .605 .604 .603 .601	.598 .601 .604 .603 .602 .601	.596 .600 .603 .602 .602 .601	.599 .603 .602 .601 .600
Н.)rifice				n feet			
	.02	.08	.04	.05	.07	.10	.12	.15	.20	.40	.60	.80 ———	1.0
.4 .6 1.0 2. 4. 6. 10. 20. 50.(?)	.655 .644 .682 .623 .618 .611 .601 .596	.640 .631 .621 .614 .611 .606 .600 .596			.628 .618 .612 .607 .603 .599 .597 .594	.618 .618 .608 .604 .602 .600 .598 .596 .591	.612 .609 .605 .601 .600 .599 .596 .594 .592	.606 .605 .603 .600 .599 .597 .596 .594	.601 .599 .599 .598 .597 .596 .594 .592	.596 .598 .599 .598 .598 .597 .596 .594	.598 .595 .597 .597 .597 .596 .596 .594	.590 .593 .596 .597 .596 .595 .593 .592	.591 .595 .596 .596 .595 .594 .593

HYDRAULIC FORMULE.-FLOW OF WATER IN OPEN AND CLOSED CHANNELS.

Flow of Water in Pipes.—The quantity of water discharged through a pipe depends on the "head;" that is, the vertical distance between the level surface of still water in the chamber at the entrance end of the pipe and the level of the centre of the discharge end of the pipe: also upon the length of the pipe, upon the character of its interior surface as to smoothness, and upon the number and sharpness of the bends; but it is independent of the position of the pipe, as horizontal, or inclined upwards or downwards.

The head, instead of being an actual distance between levels, may be caused by pressure, as by a pump, in which case the head is calculated as a vertical distance corresponding to the pressure 1 lb. per sq. in. = 2.309 ft. head, or 1 ft. head = .438 lb. per sq. in.

The total head operating to cause flow is divided into three parts: 1. The

velocity-head, which is the height through which a body must fall in vacuo rounded entrance the entry-head is inappreciable; 3. the friction-head, due to the frictional resistance to flow within the pipe.

In ordinary cases of pipes of considerable length the sum of the entry and velocity heads required scarcely exceeds 1 foot. In the case of long pipes with low heads the sum of the velocity and entry heads is generally so small that it may be neglected.

General Formula for Flow of Water in Pipes or Conduits. Mean velocity in ft. per sec. = $c\sqrt{\text{mean hydraulic radius}} \times \text{slope}$

Do, for pipes running full =
$$c_1 / \frac{\text{diameter}}{4} \times \text{slope}$$
,

in which c is a coefficient determined by experiment. (See pages 559-564.)

The mean hydraulic radius = area of wet cross-section wet perimeter.

In pipes running full, or exactly half full, and in semicircular open channels running full it is equal to 1/4 diameter.

The slope = the head (or pressure expressed as a head, in feet)
+ length of pipe measured in a straight line from end to end.
In open channels the slope is the actual slope of the surface, or its fall per unit of length, or the sine of the angle of the slope with the horizon.

Chezy's Formula: $v = c \sqrt[r]{v}s = c \sqrt[r]{s}$; r = mean hydraulic radius, s = slope = head + length, v = velocity in feet per second, all dimensions in feet.

Quantity of Water Discharged. -If Q = discharge in cubic feetper second and a =area of channel, $Q = av = ac \sqrt{rs}$.

 $a\sqrt{r}$ is approximately proportional to the discharge. It is a maximum at 308°, corresponding to 19/20 of the diameter, and the flow of a conduit 19/20 full is about 5 per cent greater than that of one completely filled.

Table giving Fall in Feet per Mile, the Distance on Slope corresponding to a Fall of 1 Ft., and also the Values of s and \sqrt{s} for Use in the Formula $v = c \sqrt{rs}$.

s = H + L = sine of angle of slope = fall of water-surface(H), in any distance (L), divided by that distance.

Fall in Feet per Mi.	Slope, 1 Foot in	Sine of Slope,	√ 8.	Fall in Feet per Mi.	Slope, 1 Foot in	Sine of Slope,	√ s.
0.25	21120	.0000478	.006881	17	810.6	.0032197	.056742
.30	17600	.0000568	.007538	18	293.8	.0034091	.058388
.40	18200	.0000758	.008704	19	277.9	.0035985	.059988
.50	10560	.0000947	.009731	20	264	.0087879	.061546
.60	8800	.0001186	.010660	22	240	.0041667	.064549
.702	7520	.0001330	.011532	24	220	.0045455	.067419
.805	6560	.0001524	.012847	26	203.1	.0049242	.070178
.904	5840	.0001712	.013085	28	188.6	.0058030	.072822
1.	5280	.0001894	.013762	80	176	.0056818	.075378
1.25	4224	.0002367	.015386	85.20	150	.0066667	.081650
1.5	3520	.0002841	.016854	40	· 182	.0075758	.087089
1.75	3017	.0003314	.018205	44	120	.0083333	.091287
2.	2640	.0003788	.019463	48	110	.0090909	.095346
2.25	2347	.0004261	.020641	52.8	100	.010	.1
2.5	2112	.0004785	.021760	60	88	.0113636	.1066
2.75	1920	.0005208 (.022822	66	80	.0125	.111808
8.	1760	.0005682	.023837	70.4	75	.0183333	.115470
3.25	1625	.0006154	.024807	80	66	.0151515	123091
8.5	1508	.0006631	.025751	88	60	.0166667	.1291
3.75	1408	.0007102	.026650	96	55	.0181818	134889
4	1320	.0007576	.027524	105.6	50	.02	141421
5	1056	.0009470	.080778	120	44	.0227278	150756
6	880	.0011364	.08371	132	40	.025	.158114
6	754.8	.0013257	.036416	160	88	.0303030	.174077
8	660	.0015152	.088925	220	24	.0416667	.204124
ğ	586.6	.0017044	.041286	264	20	.05	.223607
1Ö	528	.0018939	.048519	830	16	.0625	.25
ii l	443.6	.0020833	.045648	440	12	.0833388	.288675
12	440	.0022727	.047678	528	10	.1	.816228
18 I	406.1	.0024621	.04962	660	- 8	.125	.858553
14	877.1	.0026515	.051493	880	ĕ	1666667	408248
15	352	.0028409	.0533	1056	8	.2	447214
16	330	.0030303	.055048	1320	4	.25	.5

Values of \sqrt{r} for Circular Pipes, Sewers, and Conduits of different Diameters.

 $r = \text{mean hydraulic depth} = \frac{\text{area}}{\text{perimeter}} = \frac{1}{4} \text{ diam. for circular pipes running full or exactly half full.}$

Diam., ft. in.	$\sqrt[4]{r}$ in Feet.	Diam., ft. in.	$\sqrt[4]{r}$ in Feet.	Diam., ft. in.	$\sqrt[4]{r}$ in Feet.	Diam., ft. in.	$\sqrt[4]{r}$ in Feet.
35	.088	2 1 2 2 2 3 4 5 6 7 8 9 9 10 2 2 11 1 2 3 3 4 5 6 6 7 8 9 9 10 2 3 3 5 5 6 7 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	.707	4 6	1.061	9	1.500
1 3/6	.102	2 1	.722	4 7	1.070	9 8 9 6 9 9	1.521
' ¾	.125	2 2 2 2 3	.736	4 8	1.080	96	1.541
1	.144	2\ 8	.750	4 9 4 10 4 11 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	1.089		1.561
11/4	.161	2 4	.764 .777	4 10	1.099	10	1.581
11/2	.177	2 5	.777	4 11	1.109	10 3	1.601
134	·191	2 6	.790	5	1.118	10 6	1:620
11434 11434 222 84 45 67 89	.204	2 7	.804 .817	5 1	1.127	10 9	1.639
21/4	.228	2 8	.817	5 2	1.137	11	1.658
8 ~	.251	2 9	.829	5 3	1.146	11 3	1.677
4	.290	2 10	.842	5 4	1.155	11 6	1.696
5	.323	2 11	.854	5 5	1.164	11 9	1.714
6	.354	8	.866	5 6	1.178	12	1.732
7	.382	8 1	.878	5 7	1.181	12 8	1.750
8	.408	3 2	.890	5 8	1.190	12 6	1.768
9	.433	3 3	.901	5 9	1.199	19 9	1.785
10	.456	8 4	.913	5 10	1.208	18	1.803
11	.479	3 5 3 6	.924	5 11	1.216	18 8	1.820
1	.500	3 6	.935	6	1.225	13 6	1.837
1 1	.520	3 7	.946	6 8	1.250	14	1.871
1 2 1 3	.540	3 8	.957	5 9 5 10 5 11 6 8 6 9 7 8	1.275	14 6	1.904
1 3	.559 .577	89	.968	6 9	1.299	15	1 936
1 4	.577	3 10	.979	7	1 828	15 6	1.968
15	.595	8 11	.990	7 8	1.346	16	2.
16	.612	4	1.	76	1.869	16 6	2.031
1 7	.629	4 1	1.010	7 9	1.392	17	2.061
1 8	.646	4 2	1.021	8 3	1.414	17 6	2.091
1 9	.661	4 8	1.031	8 3	1.436	18	2,121
1 10	.677	4 4	1.041	8 6	1.458	19	2.180
1 11	.692	4 5	1.051	8 9	1.479	20	2.236

Values of the Coefficient c. (Chiefly condensed from P. J. Flynn on Flow of Water.)—Almost all the old hydraulic formulæ for finding the mean velocity in open and closed channels have constant coefficients, and are therefore correct for only a small range of channels. They have often been found to give incorrect results with disastrous effects. Ganguillet and Kutter thoroughly investigated the American, French, and other experiments, and they gave as the result of their labors the formula now generally known as Kutter's formula. There are so many varying conditions affecting the flow of water, that all hydraulic formulæ are only approximations to the correct result.

When the surface-slope measurement is good, Kutter's formula will give results seldom exceeding 71/2% error, provided the rugosity coefficient of the formula is known for the site. For small open channels D'Arcy's and Bazin's formulæ, and for cast-iron pipes D'Arcy's formulæ, are generally accepted as being approximately correct.

Kutter's Formula for measures in feet is

$$v = \left\{ \frac{\frac{1.811}{n} + 41.6 + \frac{.00281}{s}}{1 + \left(41.6 + \frac{.00281}{s}\right) \times \frac{n}{\sqrt{r}}} \right\} \times \sqrt{rs},$$

in which v = mean velocity in feet per second; $r = \frac{a}{b} = \text{hydraulic mean}$

depth in feet = area of cross-section in square feet divided by wetted perimeter in lineal feet; s = fall of water-surface (h) in any distance (l) divided

by that distance, $=\frac{h}{l}$, = sine of slope; n= the coefficient of rugosity, de-

pending on the nature of the lining or surface of the channel. If we let the first term of the right-hand side of the equation equal c, we have Chezy's formula, $v = c \sqrt{rs} = c \times \sqrt{r} \times \sqrt{s}$.

Values of n in Kutter's Formula.—The accuracy of Kutter's formula depends, in a great measure, on the proper selection of the coefficient of roughness n. Experience is required in order to give the right value to this coefficient, and to this end great assistance can be obtained, in making this selection, by consulting and comparing the results obtained from ex-periments on the flow of water already made in different channels.

In some cases it would be well to provide for the contingency of future deterioration of channel, by selecting a high value of n, as, for instance, where a dense growth of weeds is likely to occur in small channels, and also where channels are likely not to be kept in a state of good repair.

The following table, giving the value of n for different materials, is compiled from Kutter, Jackson, and Hering, and this value of n applies also in

each instance, to the surfaces of other materials equally rough,

Value of n in Kutter's Formula for Different Channels. n = .009, well-planed timber, in perfect order and alignment; otherwise,

perhaps .01 would be suitable.

n = .010, plaster in pure cement; planed timber; glazed, coated, or enamelled stoneware and iron pipes; glazed surfaces of every sort in perfect

n = .011, plaster in cement with one third sand, in good condition; also for iron, cement, and terra cotta pipes, well joined, and in best order.

n = .012, unplaned timber, when perfectly continuous on the inside; flumes.

n=018, ashlar and well-laid brickwork; ordinary metal; earthen and stoneware pipe in good condition, but not new; cement and terra-cotta pipe not well jointed nor in perfect order, plaster and planed wood in imperfect or inferior condition; and generally, the materials mentioned with n=.010, when in imperfect or inferior condition.

n=0.05, second class or rough-faced brickwork; well-dressed stonework; foul and slightly tuberculated iron; cement and terra-cotta pipes, with imperfect joints and in bad order; and canvas lining on wooden frames.

n=017, brickwork, ashlar, and stoneware in an inferior condition; tuberculated iron pipes; rubble in cement or plaster in good order; fine gravel, well rammed, $\frac{1}{2}$ to $\frac{2}{3}$ inch diameter; and, generally, the materials mentioned with n=018 when in bad order and condition.

n = .020, rubble in cement in an inferior condition; coarse rubble, rough set in a normal condition; coarse rubble set dry; ruined brickwork and masonry; coarse gravel well rammed, from 1 to 1½ inch diameter; canals with beds and banks of very firm, regular gravel, carefully trimmed and rammed in defective places; rough rubble with bed partially covered with silt and mud; rectangular wooden troughs, with battens on the inside two inches apart; trimmed earth in perfect order.

n=.0225, canals in earth above the average in order and regimen. n=.025, canals and rivers in earth of tolerably uniform cross-section; slope and direction, in moderately good order and regimen, and free from stones and weeds.

n = .0275, canals and rivers in earth below the average in order and regi-

n = .030, canals and rivers in earth in rather bad order and regimen, having stones and weeds occasionally, and obstructed by detritus.

n=.035, suitable for rivers and canals with earthen beds in bad order and regimen, and having stones and weeds in great quantities. n = .65, torrents encumbered with detritus.

Kutter's formula has the advantage of being easily adapted to a change in the surface of the pipe exposed to the flow of water, by a change in the value of n. For cast-iron pipes it is usual to use n = .013 to provide for the future deterioration of the surface.

Reducing Kutter's formula to the form $v = c \times \sqrt[4]{r} \times \sqrt[4]{s}$, and taking n, the coefficient of roughness in the formula = .011, .012, and .013, and s = .001, we have the following values of the coefficient c for different diameters of

conduit.

Values of c in Formula $v=c\times\sqrt{r}\times\sqrt{s}$ for Metal Pipes and Moderately Smooth Conduits Generally.

By Kutter's Formula (9 = .001 or greater.)

Dian	neter.	n = .011	n = .012	n = .013	Diameter.	n = .011	n = .012	n = .018
ft. 0	in. 1 2	c = 47.1 61.5 77.4	c =	c =	ft. 7 8 9	c = 152.7 155.4 157.7	c = 139.2 141.9 144.1	c = 127.9 130.4 132.7
1	6	87.4 105.7	77.5 94.6	69.5 85.3	10 11 12	159.7 161.5	146 147.8	134.5 136.2
1 2 3 4	6	116.1 123.6 133.6 140.4	104.8 111.3 120.8 127.4	94.4 101.1 110.1 116.5	14 16 18	168 165.8 168 169.9	149.8 152 154.2 156.1	137.7 140.4 142.1 144.4
5 6		145.4 149.4	132.3 136.1	121.1 124.8	20	171.6	157.7	·146

For circular pipes the hydraulic mean depth r equals 14 of the diameter. According to Kutter's formula the value of c, the coefficient of discharge, is the same for all slopes greater than 1 in 1000; that is, within these limits c is constant. We further find that up to a slope of 1 in 2640 the value of c is, for all practical purposes, constant, and even up to a slope of 1 in 5000 the difference in the value of c is very little. This is exemplified in the following:

Value of c for Different Values of \sqrt{r} and s in Kutter's Formula, with n=.013. $v=c\sqrt{r}\times\sqrt{s}$

		v =	Slopes.		
\sqrt{r}	1 in 1000	1 in 2500	1 in 3883.3	1 in 5000	1 in 10,000
.6 1 2	98.6 116.5 142.6	91.5 115.2 142.8	90.4 114.4 143.0	88.4 113.2 143.1	83.8 109.7 143.8

The reliability of the values of the coefficient of Kutter's formula for pipes of less than 6 in. diameter is considered doubtful. (See note under table on page 564.)

Values of c for Earthen Channels, by Kutter's Formula, for Use in Formula $v = c \sqrt{rs}$.

	Co	efficie n	nt of R = .022		Co		$\begin{array}{l} \text{nt of R} \\ = .03 \end{array}$		ess,		
		1	$ar{r}$ in te	et.		√r in feet.					
	0.4	1.0	1.8	2.5	4.0	0.4	1.0	1.8	2.5	4.0	
Slope, 1 in	c	C	c	c	c	С	c	c	C	c	
1000	85.7	62.5	80.3	89.2	99.9	19.7	37.6	51.6	59.3	69.2	
1250	85 5	62.3	80.3	89.3	100.2	196	37.6	51.6	59 4	69.4	
1667	35.2	62.1	80.3	89.5	100 6	19.4	37.4	51.6	59.5	69.8	
2500	34.6	61.7	80.3	89.8	101.4	19.1	37.1	51.6	59.7	70.4	
8833	34.	61.2	80.3	90.1	102.2	18.8	36.9	51.6	59.9	71.0	
5000	33.	60.5	80.3	90.7	103.7	18.8	36.4	51.6	60.4	72.2	
7500	81.6	59.4	80.3	91.5	106.0	17.6	35.8	51.6	60.9	73.9	
10000	80.5	58.5	80.3	92.3	107.9	17.1	35.3	51.6	60.5	75.4	
15840	28.5	56.7	80.2	93.9	112.2	16.2	84.3	51.6	62.5	78.6	
20000	27.4	55.7	80.2	94.8	115.0	15.6	83.8	51.5	63.1	80.4	

Mr. Molesworth, in the 22d edition of his "Pocket-book of Engineering Formulæ," gives a modification of Kutter's formula as follows: For flow in cast-iron pipes, $v = c \sqrt{rs}$, in which

$$c = \frac{181 + \frac{.00281}{8}}{1 + \frac{.026}{4\sqrt{d}} \left(41.6 + \frac{.00281}{8}\right)},$$

in which d =diameter of the pipe in feet.

(This formula was given incorrectly in Molesworth's 21st edition.)

Molesworth's Formula. $-v = \sqrt{krs}$, in which the values of k are as follows:

	Values of k for Velocities.			
Nature of Channel.	Less than 4 ft. per sec.	More than 4 ft. per sec.		
Brickwork	8800 7200	8500 6800		
Shingle	6400 5800	5900 4700		

In very large channels, rivers, etc., the description of the channel affects the result so slightly that it may be practically neglected, and k assumed = from 8500 to 9000.

Flynn's Formula.—Mr. Flynn obtains the following expression of the value of Kutter's coefficient for a slope of .001 and a value of n = .018:

$$c = \frac{183.72}{1 + \left(44.41 \times \frac{.018}{\sqrt{r}}\right)}$$

The following table shows the close agreement of the values of c obtained from Kutter's, Molesworth's, and Flynn's formulæ:

Diameter.	Slope.	Kutter.	Molesworth.	Flynn.
6 inches	1 in 40	71.50	71.48	69.5
6 inches	1 in 1000	69.50	69.79	69.5
4 feet	1 in 400	117.	117.	116.5
4 feet	1 in 1000	116.5	116.55	116.5
8 feet	1 in 700	180.5	130.68	180.5
8 feet	1 in 2600	129.8	129.98	180.5

Mr. Flynn gives another simplified form of Kutter's formula for use with different values of n as follows:

$$v = \left(\frac{K}{1 + \left(44.41 \times \frac{n}{\sqrt{r}}\right)}\right) \sqrt{rs}.$$

In the following table the value of K is given for the several values of n:

n	K	n	K	n	K	n	K	n	K
.009 .010 .011	245.63 225.51 209.05	.018	183.72	.016	165.14 157.6 150.94	.019	189.78	.022	126.78

If in the application of Mr. Flynn's formula given above within the limits of n as given in the table, we substitute for n, K, and \sqrt{r} their values, we have a simplified form of Kutter's formula.

For instance, when n = .011, and d = 3 feet, we have

$$v = \frac{209.05}{1 + \left(44.41 \times \frac{.011}{.866}\right)} \times \sqrt{rs}.$$

Razin's Formulæ:

For very even surfaces, fine plastered sides and bed, planed planks, etc.,

$$v = \sqrt{1 + .0000045 \left(10.16 + \frac{1}{r}\right)} \times \sqrt{rs}$$

For even surfaces such as cut-stone, brickwork, unplaned planking, mortar, etc.:

$$v = \sqrt{1 + .000018(4.354 + \frac{1}{r})} \times \sqrt{re}$$
.

For slightly uneven surfaces, such as rubble masonry:

$$v = \sqrt{1 + .00006 \left(1.219 + \frac{1}{r}\right)} \times \sqrt{rs}$$
.

For uneven surfaces, such as earth:

$$v = \sqrt{1 + .00085 \left(0.2438 + \frac{1}{r}\right)} \times \sqrt{rs}$$

A modification of Bazin's formula, known as D'Arcy's Bazin's:

$$v = r \sqrt{\frac{1000s}{.08534r + 0.35}}.$$

For small channels of less than 20 feet bed Bazin's formula for earthen channels in good order gives very fair results, but Kutter's formula is superseding it in almost all countries where its accuracy has been investigated. The last table on p. 561 shows the value of c, in Kutter's formula, for a wide range of channels in earth, that will cover anything likely to occur in the

ordinary practice of an engineer.

D'Arcy's Formula for clean iron pipes under pressure is

$$v = \left\{ \frac{rs}{.00007726 + \frac{.00000162}{r}} \right\}^{\frac{1}{2}}$$

Flynn's modification of D'Arcy's formula is

$$v = \left(\frac{155256d}{12d+1}\right)^{\frac{1}{2}} \times \sqrt{rs}$$

in which d = diameter in feet

D'Arcy's formula, as given by J. B. Francis, C.E., for old cast-iron pipe, lined with deposit and under pressure, is

$$v = \left(\frac{144d^2s}{.0082(12d+1)}\right)^{\frac{1}{2}}.$$

Flynn's modification of D'Arcy's formula for old cast-iron pipe is

$$v = \left(\frac{70243.9d}{12d+1}\right)^{\frac{1}{2}} \times \sqrt{rs}$$
.

For Pipes Less than 5 inches in Diameter, coefficients (c) in the formula $v = c \sqrt{rs}$, from the formula of D'Arcy, Kutter, and Fanning.

Diam. in inches.	D'Arcy, for Clean Pipes.	Kutter, for n = .011 s = .001	Fanning, for Clean Iron Pipes	Diam. in inches	for Clean	Kutter, for n = .011 s = .001	Fanning, for Clean Iron Pipes.
\$6 15 24 1 114 115	59.4 65.7 74.5 80.4 84.8 88.1	82. 36.1 42.6 47.4 51.9 55.4	80.4 88.	184 2 214 8 4 5	90.7 92.9 96.1 98.5 101.7 103.8	58.8 61.5 66. 70.1 77.4 82.9	92.5 94.8 96.6 103.4

Mr. Flynn, in giving the above table, says that the facts show that the co-Mr. Flynn, in giving the above table, says that the facts show that the coefficients diminish from a diameter of 5 inches to smaller diameters, and it is a safer plan to adopt coefficients varying with the diameter than a constant coefficient. No opinion is advanced as to what coefficients should be used with Kutter's formula for small diameters. The facts are simply stated, giving the results of well-known authors.

Older Formulæ.—The following are a few of the many formulæ for flow of water in pipes given by earlier writers. As they have constant coefficients, they are not considered as reliable as the newer formulæ.

Prony,
$$v = 97 \sqrt{rs} - .08$$
;
Eytelwein, $v = 50 \sqrt{\frac{dh}{l + 50d}}$, or $v = 108 \sqrt{rs} - 0.18$;
Hawksley, $v = 48 \sqrt{\frac{dh}{l + 50d}}$; Neville, $v = 140 \sqrt{rs} - 11 \sqrt[3]{rs}$.

In these formulæ d = diameter in feet; h = head of water in feet; l = diameterlength of pipe in feet; $s = \text{sine of slope} = \frac{h}{l}$; r = mean hydraulic depth,

= area + wet perimeter =
$$\frac{d}{4}$$
 for circular pipe.

Mr. Santo Crimp (Eng'g, August 4, 1893) states that observations on flow in brick sewers show that the actual discharge is 83% greater than that calculated by Eytelwein's formula. He thinks Kutter's formula not superior D'Arcy's for brick sewers, the usual coefficient of roughness in the former, viz., 013, being too low for large sewers and far too small in the case of small sewers.
D'Arcy's formula for brickwork is

$$v = \frac{\sqrt{2g}}{m}rs$$
; $m = a\left(1 + \frac{B}{r}\right)$; $a = .0037285$; $B = .229663$.

VELOCITY OF WATER IN OPEN CHANNELS.

Irrigation Canals.—The minimum mean velocity required to prevent the deposit of silt or the growth of aquatic plants is in Northern India taken at 1½ feet per second. It is stated that in America a higher velocity is required for this purpose, and it varies from 2 to 3½ feet per second. The maximum allowable velocity will vary with the nature of the soil of the bed. A sandy bed will be disturbed if the velocity exceeds 3 feet per second. Good loam with not too much sand will bear a velocity of 4 feet per second. The Cavour Canal in Italy, over a gravel bed, has a velocity of about 5 per second. (Flynn's "Irrigation Canals.")

Mean Surface and Bottom Velocities,-According to the formula of Bazin,

$$v = v_{\text{max}} - 25.4 \sqrt{rs}; \ v = v_b + 10.87 \sqrt{rs}.$$

 $v = v - 10.87 \sqrt{rs}$, in which v = mean velocity in feet per second, wax = maximum surface velocity in feet per second, vb = bottom velocity in feet per second, r = hydraulic mean depth in feet = area of cross-section

In square feet divided by wetted perimeter in feet, $s = \sin e$ of slope.

The least velocity, or that of the particles in contact with the bed, is almost as much less than the mean velocity as the greatest velocity is

greater than the mean.

Rankine states that in ordinary cases the velocities may be taken as bearing to each other nearly the proportions of 3, 4, and 5. In very slow currents they are nearly as 2, 3, and 4.

Safe Bottom and Mean Velocities.—Ganguillet & Kutter give

the following table of safe bottom and mean velocity in channels, calculated from the formula $v = vb + 10.87 \sqrt{rs}$:

Material of Channel.	Safe Bottom Veloc ity vb, in feet per second.	Mean Velocity v, in feet per second.
Soft brown earth	0.249	0.828
Soft loam	0.499	0.656
Sand	1,000	1.812
Gravel	1.998	2.625
Pebbles		3.938
Broken stone, flint		5.579
Conglomerate, soft slate	4.988	6.564
Stratified rock	6.006	8.204
Hard rock		18.127

Ganguillet & Kutter state that they are unable for want of observations to judge how far these figures are trustworthy. They consider them to be rather disproportionately small than too large, and therefore recommend them more confidently.

Water flowing at a high velocity and carrying large quanties of silt is very

destructive to channels, even when constructed of the best masonry.

Resistance of Soils to Erosion by Water.—W. A. Burr, Eng'g News, Feb. 8, 1894, gives a diagram showing the resistance of various soils to

erosion by flowing water.

Experiments show that a velocity greater than 1.1 feet per second will erode sand, while pure clay will stand a velocity of 7.35 feet per second. The greater the proportion of clay carried by any soil, the higher the permissible velocity. Mr. Burr states that experiments have shown that the line describing the power of soils to resist erosion is parabolic. From his diagram the following figures are selected representing different classes of soils:

Pure sand resists erosion by flow of	1.1	feet ver	second.
Sandy soil, 15% clay	1.2	46	44
Sandy loam, 40% clay	1.8	61	**
Loamy soil, 65% clay	8.0	"	44
Clay loam, 85% clay	4.8	"	"
Clay loam, 85% clay	6.2	44	
Clav	7.3	5 "	44

Abrading and Transporting Power of Water.—Prof. J. LeConte, in his "Elements of Geology," states:

The erosive power of water, or its power of overcoming cohesion, varies as the square of the velocity of the current.

The transporting power of a current varies as the sixth power of the velocity. * * * If the velocity therefore be increased ten times, the transporting power is increased 1,000,000 times. A current running three feet per second, or about two miles per hour, will bear fragments of stone of the size of a hen's egg, or about three ounces weight. A current of ten miles an hour will bear fragments of one and a half tons, and a torrent of twenty miles an hour will carry fragments of 100 tons.

The transporting power of water must not be confounded with its erosive power. The resistance to be overcome in the one case is weight, in the other, cohesion; the latter varies as the square: the former as the sixth

power of the velocity.

In many cases of removal of slightly cohering material, the resistance is

mixture of these two resistances, and the power of removing material will

vary at some rate between v^2 and v^4 .

Baldwin Latham has found that in order to prevent deposits of sewage silt in small sewers or drains, such as those from 6 inches to 9 inches diameter, a mean velocity of not less than 3 feet per second should be produced. Sewers from 12 to 24 inches diameter should have a velocity of not less than 21/4 feet per second, and in sewers of larger dimensions in no case should the

while stones of a sp. gr. of 2.82 to 8.00 required a velocity of 2.5 to 2.75 ft. per

second.

Chailly gives the following formula for finding the velocity required to move rounded stones or shingle:

$$v = 5.67 \sqrt{aq}$$

in which v =velocity of water in feet per second. a =average diameter in

feet of the body to be moved, g = its specific gravity. Geo. Y. Wisner, $Eng^{i}g$ News, Jan 10, 1895, doubts the general accuracy of statements made by many authorities concerning the rate of flow of a current and the size of particles which different velocities will move. He says:

The scouring action of any river, for any given rate of current, must be an inverse function of the depth. The fact that some engineer has found that a given velocity of current on some stream of unknown depth will move sand or gravel has no bearing whatever on what may be expected of currents of the same velocity in streams of greater depths. In channels 3 to 5 ft. deep a mean velocity of 8 to 5 ft. per second may produce rapid scouring, while in depths of 18 ft. and upwards current velocities of 6 to 8 ft. per second often have no effect whatever on the channel bed.

Grade of Sewers.—The following empirical formula is given in Baumeister's "Cleaning and Sewerage of Cities," for the minimum grade for a sewer of clear diameter equal to d inches, and either circular or oval in

section:

Minimum grade, in per cent,
$$=\frac{100}{5d+50}$$
.

As the lowest limit of grades which can be flushed, 0.1 to 0.2 per cent may be assumed for sewers which are sometimes dry, while 0.3 per cent is allowable for the trunk sewers in large cities. The sewers should run dry as

rarely as possible

Relation of Diameter of Pipe to Quantity Discharged.-In many cases which arise in practice the information sought is the diame-In many cases which arise in practice the information sought is the diameter necessary to supply a given quantity of water under a given head. The diameter is commonly taken to vary as the two-fifth power of the discharge. This is almost certainly too large. Hagen's formula, with Prof. Unwin's coefficients, give $d = c \left(\frac{Q}{Q} \right)^{387}$, where c = .339 when d and Q

Unwin's coefficients, give $d = c \left(\frac{Q}{\left(\frac{h}{I} \right)^{\frac{1}{2}}} \right)$, where c = .239 when d and Q

are in feet and cubic feet per second.

Mr. Thrupp has proposed a formula which makes d vary as the .383 power of the discharge, and the formula of M. Vallot, a French engineer, makes d vary as the .375 power of the discharge. (Engineering.)

FLOW OF WATER-EXPERIMENTS AND TABLES.

The Flow of Water through New Cast-iron Pipe was measured by S. Bent Russell, of the St. Louis, Mo. Water-works. The pipe was 12 inches in diameter, 1631 feet long, and laid on a uniform grade from end to end. Under an average total head of 3.36 feet the flow was 43,200 cubic feet in seven hours; under an average head of 3.37 feet the flow was the same; under an average total head of 3.41 feet the flow was 46,700 cubic feet in 8 hours and 35 minutes. Making allowance for loss of head due to entrance and to curves, it was found that the value of c in

the formula $v=c\sqrt{rs}$ was from 88 to 98. (Eng'g Record, April 14, 1894. Flow of Water in a 20-inch Pipe 75,000 Feet Long.—A comparison of experimental data with calculations by different formulæ is

given by Chas. B. Brush, Trans. A. S. C. E., 1888. The pipe experimented with was that supplying the city of Hoboken, N. J.

RESULTS OBTAINED BY THE HACKENSACE WATER COMPANY, FROM 1882-1887, IN PUMPING THROUGH A 20-IN. CAST-IRON MAIN 75,000 FEET LONG.

Pressure in lbs. per sq. in. at pumping-station: 95 100 105 110 115 ر د. 190 125 120 Total effective head in feet: 100 112 192 88 66 Discharge in U.S. gallons in 24 hours, 1 = 1000: 8,165 8,854 8,566 2,904 4.116 4.265 Actual velocity in main in feet per second: 2.24 2.36 2.52 2.68 2.76 2.92 Cost of coal consumed in delivering each million gals. at given velocities. \$8.40 \$8.15 \$8.00 \$8.10 \$8.80 \$8.60 \$9.00 **\$**9.60 Theoretical discharge by D'Arcy's formula: 2,748 8.004 8.244 8,488 8,699 8,915 4.102 4.297

Velocities in Smooth Cast-iron Water-pipes from 1 Foot to 9 Feet in Diameter, on Hydraulic Grades of 0.5 Foot to 8 Feet per Mile; with Corresponding Values of c in V = c \(\sqrt{rs}. \) (D. M. Greene, in Eng'g News, Feb. 24, 1894.)

Diame.	Hydrau- lic Mean Radii.	1	Hydraulic Grade; Feet per Mile = h .											
D. ters	. E E E	h = 0.5 $s = 0.0000947$	1.0 0.0001894	1.5 0.0002841	2.0 0.0003788	3.0 0.0005682	4.0 0.0007576							
1.	0.25	V = 0.4542 $c = 92.7$	97.0	0.8356 99.1	0.9808 100.7	1.2277	1.4402 104.7							
2.	0.5	V = 0.7359 $c = 106.6$	1.0798 110.9	1.3516 113.4	1.5856 115.2	1.9857 117.9	2.3294 119.7							
8.	0.75	V = 0.9783 $c = 115.5$	1.4298 119.9	1.7906 122.6	2.1017 124.4	2.6806 127.5	8.0860 129.5							
4.	1.0 {	V = 1.1883 $c = 122.1$	1.745 6 126.8	2.1861 129.7	2.5645 181.8	8.2116 184.7	8.7676 136.9							
5.	1.25	V = 1.3872 $c = 127.5$	182.4	2.5521 185.5	2.9939 187.6	3.7498 140.7	4.3988 142.9							
6.	1.5	V = 1.5742 $c = 132.1$	137.8	2.8961 140.3	8.8975 142.6	4.2548 145.8	4.9918 148.1							
٧.	1.75	V = 1.7518 $c = 135.9$ $V = 1.9218$	141.4	3.2230 146.0 3.5858	8.7809 146.8 4.1479	4.7850 150.2	5.5546 152.5							
8.	2.0	c = 139.7 $V = 2.0854$	2.0234 145.1 8.0638	148.4 3.8368	150.7 4.5010	5.1945 154.1 5.6368	6 0936 156.5 6.6125							
9.	2.25 }	c = 142.9	148.4	151.7	154.2	157.6	160.1							

The velocities in this table have been calculated by Mr. Greene's modification of the Chexy formula, which modification is found to give results which differ by from 1.29 to -2.65 per cent (average 0.9 per cent) from very carefully measured flows in pipes from 16 to 48 inches in diameter, on grades from 1.68 feet to 10.296 feet per mile, and in which the velocities ranged from 1.577 to 6.195 feet per second. The only assumption made is that the modified formula for V gives correct results in conduits from 4 feet to 9 feet in diameter, as it is known to do in conduits less than 4 feet in diameter. Other stricks on Flow of Water in long tubes are to be found in Flow's

Other articles on Flow of Water in long tubes are to be found in Eng'g News as follows: G. B. Pearsons, Sept. 23, 18:6; E. Sherman Gould, Feb. 16, 28, March 9, 16, and 23, 1889; J. L. Fitzgerald, Sept. 6 and 13, 1880; Jas. Duane, Jan. 2, 1892; J. T. Fanning, July 14, 1892; A. N. Talbot, Aug. 11, 1892.

Flow of Water in Circular Pipes, Sewers, etc., Flowing Full. Based on Kutter's Formula, with n=.018.

Discharge in cubic feet per second.

Diam-		Slope	o, or Hea	d Divid	ed by Le	ngth of	Pipe.	
eter.	1 in 40	1 in 70	1 in 100	1 in 200	1 in 800	1 in 400	1 in 500	1 in 600
5 in. 6 " 7 " 8 " 9 "	.456 .762 1.17 1.70 2.87		.288 .482 .744 1.08 1.50	.204 .841 .596 .765	.278 .480	.144 .241 .872 .54 .75	.137 ,280 .855 .516 .717	.80‡ .441
Slope	1 in 60	1 in 80	1 in 100	1 in 200	1 in 800	1 in 400	1 in 500	1 in 600
10 in,	2.59	2.24	2.01	1.42	1.16	1.00	.90	.82
11 "	8.89	8.94	9.68	1.86	1.52	1.81	1.17	1.07
12 "	4.82	8.74	3.35	2.37	1.98	1.67	1.5	1.37
13 "	5.38	4.66	4.16	2.95	2.40	2.08	1.86	1.70
14 "	6.60	5.72	5.15	8.68	9.95	2.57	8.29	2.09
Slope 15 in 16 '' 18 '' 20 ''	1 in 100 6.18 7.28 10.21 18.65 17.71	1 in 200 4.37 5.22 7.22 9.65 12.52	1 in 800 8.57 4.26 5.89 7.88 10.22	1 in 400 3.09 3.69 5.10 6.82 8.85	1 in 500 2.77 3.30 4.56 6.10 7.92	1 in 600 2.52 3.01 4.17 5.57 7.28	1 in 700 2.34 2.79 3.86 5.16 6.69	1 in 800 2.19 2.61 8.61 4.83 6.26
Slope 2 ft. 2 fr. 2 in. 2 " 4 " 2 " 6 " 2 " 8 "	1 in 200 15.88 19.78 94.15 29.08 84.71	1 in 400 11.23 18.96 17.07 20.56 24.54	1 in 600 9.17 11.39 13.94 16.79 20.04	1 in 800 7.94 9.87 12.07 14.54 17.35	1 in 1000 7.10 8.82 10.80 18,00 15.52	1 in 1250 6.35 7.89 9.66 11.68 13.88	1 in 1500 5 80 7.20 8.82 10.62	1 in 1800 5.29 6.58 8.05 9.69 11.57
Slope	1 in 500	1 in 750	1 in 1000	1 in 1250	1 in 1500	1 in 1750	1 in 2000	1 in 2500
	\$5.84	\$1.10	18.27	16.84	14.93	18.81	12.92	11.55
	30.14	24.61	21.31	19.06	17.40	16.11	15.07	13.48
	84.90	\$8.50	24.68	22.07	20.15	18.66	17.45	15.61
	40.08	82 72	28.84	95.85	28.14	21.42	20.04	17.93
	45.66	87.98	32.28	28.87	26.36	24.40	22.83	20.41
Slope 3 ft. 8 in. 8 " 10 " 4 " 6 in. 5 "	1 in 500	1 in 750	1 in 1000	1 in 1250	1 in 1500	1 in 1750	1 in 2000	1 in 2500
	51.74	42.52	\$6.59	82.72	29.87	27.66	25.87	28.14
	58.86	47.65	41.37	36.91	33.69	31.20	29.18	26.10
	65.47	53.46	46.30	41.41	37.80	84.50	82.74	29.28
	89.75	78.28	63.47	56.76	51.82	47.97	44.88	40.14
	116.9	97.09	\$4.08	75.21	68.65	63.56	59.46	53.18
Slope 5 ft, 6 in. 6 " 6 " 6 " 7 " 6 "	1 in 750	1 in 1000	1 in 1500	1 in 2000	1 in \$500	1 in 3000	1 in 8500	1 in 4000
	125.2	108.4	88.54	76.67	68.58	69.60	57.96	54.:1
	157.8	136.7	111 6	96.66	86.45	78.92	73.07	68 85
	195.0	168.8	187.9	119.4	106.8	97.49	90.26	84 48
	237.7	205.9	168.1	145.6	180.2	118.8	110.00	102.9
	285.3	247.1	201.7	174.7	156.8	142.6	132.1	123.5
Slope 8 ft. 6 in. 9 " 6 " 10 "	1 in 1500	1 in 2000	1 in 2500	1 in 8000	1 in 8500	1 in 4000	1 in 4500	1 in 5000
	239.4	207.3	195.4	169.3	156.7	146.6	138.2	131.1
	281.1	243.5	217.8	198.8	184.0	172.2	162.3	154 0
	827.0	288.1	258.3	231.2	214.0	200.2	188.7	179.1
	376.9	326.4	291.9	266.5	246.7	230.8	217.6	209.4
	431.4	373.6	334.1	305.0	282.4	264.2	249.1	206.8

For U. S. gallons multiply the figures in the table by 7,4905.

For a given diameter the quantity of flow varies as the square root of the sine of the slope. From this principle the flow for other slopes than those

given in the table may be found. Thus, what is the flow for a pipe 8 feet diameter, slope 1 in 125? From the table take Q=207.8 for alope 1 in 2000, The given slope 1 in 125 is to 1 in 2000 as 16 to 1, and the square root of this ratio is 4 to 1. Therefore the flow required is $207.3 \times 4 = 829.2$ cu, ft.

Circular Pipes, Conduits, etc., Flowing Full.

Values of the factor $ac \sqrt{r}$ in the formula $Q=ac \sqrt{r} \times \sqrt{s}$ corresponding to different values of the coefficient of roughness, n. (Based on Kutter's formula.)

Diam.		Value of ac √r.										
ft.		n = .010.	n = .011.	n = .012.	n = .018.	n = .015.	n = .017.					
	6	6.906	6.0627	5.8800 16.708	4.8216 15.029	8.9604	8 339					
	v	21.25	18.742 41.487	87.149	15.029 88.497	12.421 27.803	10.50					
1	8	46.98 86.05	76.347	68.44	61.867	51.600	23 60 43.93					
1	6	141.2	125.60	112.79	109.14	85.496	72.99					
;	9	214.1	190.79	171.66	155.68	180.58	111.8					
ņ	۰	807.6	274.50	247.38	224.68	188.77	164					
õ	8	421. 9	8:7.07	840.10	809.28	260.47	223.9					
2	6	559.6	500.78	452.07	411.27	847.28	299.3					
111222288884455666778899	ğ	722.4	647.18	584.90	582.76	451.23	388.8					
ã	- 1	911.8	817.50	789.59	674.09	570.90	493.3					
8	8	1128.9	1013.1	917.41	836.69	709.56	618.9					
8	6	1874.7	1234.4	1118.6	1021.1	866.91	750.8					
8	9	1652.1	1484.8	1845.9	1229.7	1045	906					
4		1962.8	1764.8	1600.9	1468.9	1245.8	1080.7					
4	6	2682.1	2418.3	2198	2007	1711.4	1487.8					
5		8 543	8191.8	2908.6	2659	2272.7	1977					
5	6	4557.8	4111.9	8742.7	8429	2934.8	2557.2					
6	_	5781.5	5176.3	4718.9	4322	3702.8	8232.5					
6	6	7075.2	6394.9	5825.9	5389	4588.8	4010					
7		8595.1	7774.8	7087 8501.8	6510	5591.6	4893					
7	6	10296	9318.8 11044	10083	7814 9272	6717	5884.2					
ğ	6	12196 14298	12954	11832	10889	7978.8 9877.9	6995.3 8226.8					
8	יי	16604	15049	18751	12668	10917	9580.7					
ď	6	19118	17388	15847	14597	12594	11061					
10	۰	21858	19834	18134	16709	14426	12678					
iŏ	6	24823	22534	20612	18996	16412	14484					
iĭ	٠,	28020	25444	28285	21464	18555	16383					
ii	6	31482	28593	26179	24189	20879	18395					
12	- 1	85156	81987	29254	26981	23352	20584					
12	6	89104	85529	82558	80041	26012	22938					
18		48307	89358	86077	33301	28850	25451					
18	6	47751	48412	89802	3.752	81860	28117					
14	_	52491	47739	43778	40432	85078	30965					
14	5	57496	52908	47969	44322	88454	88975					
15	1	62748	57108	52882	48418	42040	87147					
16		74191	67557 79050	6200 8 72594	57348 67140	4982 8 58 38 7	44078					
17		86769	91711	72594 84247	77982	67839	51669					
18 19	- 1	100617 115769	105570	96991	89759	78201	60067 69301					
20	- 1	132183	120570	110905	102559	89423	79259					

Flow of Water in Circular Pipes, Conduits, etc., Flowing under Pressure.

Based on D'Arcy's formulæ for the flow of water through cast-iron pipes. With comparison of results obtained by Kutter's formula, with n=.018. (Condensed from Flynn on Water Power.)

Values of a, and also the values of the factors $c\sqrt{r}$ and $ac\sqrt{r}$ for use in the formulas Q = av; $v = c\sqrt{r} \times \sqrt{s}$, and $Q = ac\sqrt{r} \times \sqrt{s}$.

Q= discharge in cubic feet per second, a= area in square feet, v= velocity in feet per second, r= mean hydraulic depth, 1/4 diam. for pipes running full, s= sine of slope,

(For values of \sqrt{s} see page 558.)

- (101.14	1405 02 70	Clean	Cast-iron		Old Cout	iron Pipes
Size o	f Pipe.		pes.	Value of		h Deposit.
d= diam. in ft. in.	a = area in square feet.	For Velocity, $c \sqrt{r}$.	For Discharge,	$ac \sqrt[4]{r}$ by Kutter's Formula, when $n = .013$.	For Velocity, c √r.	For Discharge, ac Vr.
96 16 94	.00077 .00136 .00307	5.251 6.702 9.809	.00403 .00914 .02855		8.532 4.507 6.261	.00272 .00613 .01922
1 114 114 182	.00545 .00852 .01227 .01670 .02182	11.61 13.68 15.58 17.32 18.96	.06884 .11659 .19115 .28986 .41857		7.811 9.255 10.48 11.65 12.75 14.76	.04257 .07885 .12855 .19462 .27824
22 4 23 4 5 6 7 8 9	.0341 .0491 .0873 .136	21.94 24.63 29.87 83.54 37.28	.74786 1.2089 2.5680 4.5610 7.3068	4.822	14.76 16.56 19.75 22.56 25 07 27.34	.50321 .81338 1.7246 3.0651 4.9147
8 9 10 11 1	.267 .849 .442 .545 .660 .785	40.65 43.75 46.73 49.45 52.16 54.65	10.852 15.270 20.652 26.952 34.428 42.918	15.03 88.50	29.43 31.42 33.26 35.09 86.75	7.2995 10.271 13.891 18.129 23.158 28.867
1 /2 1 4 1 6	1.000 1.396 1.767 2.182 2.640	59.34 63.67 67.75 71.71 75.82	63,435 88,886 119,72 156,46 198,83	100.54	39 91 42.83 45.57 48.34 50.65\$	42 668 59.789 80.531 105.25 188.74
2 2 2 2 4 2 6 2 8	8.142 8.687 4.276 4.909 5.585	78.80 82.15 85.39 88.39 91.51	247.57 302.90 365.14 433.92, 511.10	224.63 411.87	52.961 55.258 57.486 59.455 61.55	166.41 203.74 245.60 291.87 843.8
2 10 3 3 2 3 4 8 6	6.305 7.068 7.875 8.726 9.621	94.40 97.17 99.93 102.6 105.1	595.17 686.76 786.94 895.7 1011.2	674.09 1021.1	63.49 65.85 67.21 69 70.70	400.3 461.9 529.3 602 680.2
8 8 8 10 4 4 8 4 6	10.559 11.541 12.566 14.186 15.904	107.6 110.2 112.6 116.1 119.6	1186.5 1271.4 1414.7 1647.6 1901.9	1463 9 2007	72.40 74.10 75.73 78.12 80.43	764.5 855.2 951.6 1108.2 1279.2
4 9 5 5 8 5 6 6 5 9	17.721 19.635 21.648 23.758 25.967	122.8 126.1 129.8 182.4 185.4	2176.1 2476.4 2799.7 8146.8 8516	2659 8 42 9 .	82,20 84,85 86,99 89,07 91,08	1456.8 1665.7 1883.2 2116.2 2365
869 369 6 6 6 6 6 778899	98.274 83.183 38.485 44.179	138.4 144.1 149.6 154.9	8912.8 4782.1 5757.5 6841.6	4322 5839 6510 7814	93.0° 96.93 100.6 104.1°	2681.7 8216.4 8872.5 4601.9
8 8 9 9 6	50.266 56.745 68.617 70.882 78.540	160 165 169.8 174.5 179.1	8043 9364.7 10804 12870 14066	9272 10889 12668 14597 16709	107.61 111 114.2 117.4 120.4	5409.9 6299.1 7267.8 8890.6 9460.9

	Size o	f Pipe.		Cast-iron pes.	Value of	Old Cast-iron Pipes Lined with Deposit.			
	diam. in in.	a = area in square feet.	For Velocity,	For Discharge,	ac √r by Kutter's Formula, when n = .018	For Velocity,	For Discharge, ac Vr.		
10	6	86.590	183.6	15893	18996	123.4	10690		
11		95.038	187.9	17855	21464	126.8	12010		
11	6	103.869 113.098	192.2 196.8	19966 22204	24139 26981	129.3 182	13429 14935		
12	6	122 719 132 783	200.4 204.4	24598 27184	30041 83801	134.8 137.5	16545 18252		
13	6	143.139 153.938	208.3	29818 32664	86752 40432	140.1 142.7	20056 21971		
11	6	165.130	216.0	35660	44822	145.2	23986		
15		176.715	219.6	38807	48418	147.7	26108		
15	6	188.692	223.8	42125	52753	150.1	28335		
16		201.062	226.9	45621	57843	152.6	30686		
16	6	213.825	230.4	49273	62132	155	33144		
17		226.981	233.9	53082	67140	157.8	35704		
17	6	240.529	237.8	57074	72409	159.6	38389		
18		254.470	240.7	61249	77932	161.9	41199		
19		283.529	247.4	70154	89759	166.4	47186		
20		814.159	253.8	79736	102559	170.7	53633		

Flow of Water in Circular Pipes from % inch to 12 inches Diameter.

Based on D'Arcy's formula for clean cast-iron pipes. $Q = ac \sqrt{r} \sqrt{s}$.

Value of	Dia.		Slope,	or Head	Divide	d by Le	ngth of	Pipe.	
ac Vr.	in.	1 in 10.	1 in 20.	1 in 40.	1 in 60.	1 in 80.	1 in 100.	1 in 150.	1 in 200,
-	910	THE Y	Quan	tity in	cubic	feet p	er sec	ond.	
.00403	3.6	.00127	.00090	.00064	.00052	.00045	.00040	.00033	.00028
.00914	12	.00289		.00145		.00102		.00075	.00065
.02855	3/8 1/9 3/4	.00903		.00451	.00369	.00319		.00233	.00205
.06334	1	.02003		.01001	.00818	.00708	.00633	.00517	.00448
.11659	134	.03687	.02607	.01843	.01505	.01303	.01166	.00952	.00824
.19115	116	.06044	.04274				.01912	.01561	.01359
.28936	134	.09140	.06470	.04575	.03736	.03235	.02894	.02363	.02046
.41357	2	.13077	.09247	.06539	.05339	.04624	.04136	.03377	.02927
.74786	216	.23647	.16722			.08361	.07479	.06106	.05288
1.2089	3	.38225	.27031	.19118		.13515	.12089	.09871	.08548
2.5630	4	.81042	.57309						.18123
4.5610	5	1.4422	1.0198	.72109		.50992	.45610	.37241	*8:55
7.3068	6	2.3104	1.6338	1.1552	.94331			.59660	.51666
10.852	17	3,4314	2.4265	1.7157	1.4110	1.2132	1.0852	.88607	.7673
15.270	8	4.8284	3.4143	2.4141	1.9713	1.7072	1.5270	1.2468	1.0797
20.652	9	6.5302	4.6178	3.2651	2.6662	2.3089	2.0652	1.6862	1,4603
26.952	10	8.5222	6.0265	4.2611	3.4795	3.0132	2.6952	2.2006	1.9058
34,428	11	10.886	7.6981	5.4481	4.4447	3.8491	3.4428	2.8110	2 4344
42.918	12	13.571	9,5965	6.7853	5.5407	4.7982	4.2918	3.5043	8.0347
Value of	Vs=	.3162	.2236	.1581	.1291	.1118	.1	.08165	.0707

Value of	Dia.		Slope,	or Head	Divide	d by Le	ngth of	Pipe.	
ac Vr.	in.	1 in 250,	1 in 800.	1 in 350.	1 in 400.	1 in 450.	1 in 500.	1 in 550.	1 in 600.
.00403	86	,00025	.00023	.00022	.00020	.00019	.00018	.00017	.00016
.00914	3/8 1/2 3/4	.00058	.00053			.00043	.00041		.00033
.02855	34	.00181	.00165	.00153	.00143	.00134	.00128	.00122	.00117
.06334	1 1	,00400	.00366	.00339	.00317	.00:298	.00283	.00270	.00259
.11659	11/4 11/6 13/4	.00737	.00678	.00623	.00583	.00549	.00521	.00497	.0047
.19115	116	.01209	.01104	.01022	.00956	.00901	.00855	.00815	.0078
.28936	134	.01830	.01671	.01547	.01447	.01368	.01294	.01234	.0118
.41357	12	.02615	.02388		.02068		.01849	.01763	.0168
.74786	21/2		.04318				.03344		.03053
1.2089	3	.07645					.05406		.0493
2.5630	4	.16208	.14799			.12074	.11461	.10929	.1046
4.5610	5	,28843	.26335				.20397		.1962
7.3068	6	.46208				.34422	.32676		,2983
10.852	7	.68628	.62660				.48530		.4430
15.270	8	.96567	.88158		.76350		.68286		.6234
20.652	9	1.3060	1.1924		1.0326	.97292	,92356		.8431
26.952	10	1.7044	1.5562	1.4405	1.3476	1.2697	1 2053	1.1492	1.1003
34.428	11	2.1772	1.9878	1.8402		1.6219	1.5396	1.4680	1.4055
42.918	12	2.7141	2.4781	2.2940	2.1459	2.0219	1.9193	1.8300	1.7521
Value of	Vs=	.06324	.05774	.05345	.05	.04711	.04472	.04264	.04085

For	U.S.	gals.	pe	r sec.,	multiply	the figures in	the	table	by	7.4805
**	66	- 66	**	min.	• • •	a	66	66	*****	448.88
**	44	66	44	hour.	64	44	66	44	*****	26929.8
• 6	44	66	44	24 hr.	66	••	4	44	*****	646315.

For any other slope the flow is proportional to the square root of the slope; thus, flow in slope of 1 in 100 is double that in slope of 1 in 400.

Flow of Water in Pipes from ¾ Inch to 12 Inches Diameter for a Uniform Velocity of 100 Ft. per Min.

Diameter in Inches.	Area in Square Feet.	Flow in Cubic Feet per Minute.	Flow in U.S. Gallons per Minute.	Flow in U. S. Gallons per Hour.
34	.00077 .00186 .00807 .00545	0.077 0.186 0.307 0.545 0.852	.57 1.02 2.30 4.08 6.38	34 61 138 245 388
173 193 814	.01227 .0127 .01670 .02182 .0841	1.227 1.670 2.183 3.41 4.91	9.18 12.50 16.32 25.50	551 750 979 1,580
4 5 6 7	.0678 .135 .196 .267	8.73 13.6 19.6 26.7	86.73 65.28 102.00 146.88 199.92	2,208 8,917 6,120 8,818 11,995
9 10 11 12	.849 .449 .545 .660 .785	84.9 44.3 54.5 66.0 78.5	261.12 830.48 408.00 498.68 587.52	15,667 19,829 24,480 29,621 35,251

Given the diameter of a pipe, to find the quantity in gallons it will deliver, the velocity of flow being 100 ft. per minute. Square the diameter in inches and multiply by 4.08.

If Q' = quantity in gallons per minute and d = diameter in inches, then

$$Q' = \frac{d^2 \times .7854 \times 100 \times 7.4805}{144} = 4.08d^3.$$

For any other velocity, V', in feet per minute, $Q' = 4.08d^3\frac{V'}{100} = .0408d^3V'$.

Given diameter of pipe in inches and velocity in feet per second, to find discharge in cubic feet and in gallons per minute.

$$Q' = \frac{d^2 \times .7854 \times v \times 60}{144} = 0.32725 d^2v \text{ cubic feet per minute.}$$

 $= .32725 \times 7.4805$ or 2.448d2v U. S. galions per minute.

To find the capacity of a pipe or cylinder in gallons, multiply the square of the diameter in inches by the length in inches and by .0034. Or multiply the square of the diameter in inches by the length in feet and by .0408.

$$Q = \frac{.7854d^{3}l}{281} = .0084d^{3}l \text{ (exact) } .0084 \times 12 = .0468.$$

LOSS OF HEAD.

The loss of head due to friction when water, steam, air, or gas of any kind flows through a straight tube is represented by the formula

$$h = f \frac{4l}{d} \frac{v^2}{2g}; \quad \text{whence } v = \sqrt{\frac{64.4}{4f} \frac{hd}{l}},$$

in which l = the length and d = the diameter of the tube, both in feet; v = velocity in feet per second, and f is a coefficient to be determined by experiment. According to Weisbach, f = .00644, in which case

$$\sqrt{\frac{64.4}{4f}} = 50$$
, and $v = 50\sqrt{\frac{hd}{l}}$,

which is one of the older formulæ for flow of water (Downing's). Prof. Unwin says that the value of f is possibly too small for tubes of small bore, and he would put f = .006 to .01 for 4-inch tubes, and f = .0064 to .012 for 2-inch tubes. Another formula by Weisbach is

$$h = \left(.0144 + \frac{.01716}{\sqrt{a}}\right) \frac{l}{d} \frac{v^a}{20}.$$

Rankine gives

$$f = .005 \left(1 + \frac{1}{12d}\right)$$
.

From the general equation for velocity of flow of water $v = c \sqrt[4]{t}$, = t for round pipes $c \sqrt{\frac{d}{4}} \sqrt{\frac{h}{l}}$, we have $v^a = c^a \frac{d}{4} \frac{h}{l}$ and $h = \frac{4lv^a}{c^a d}$, in which

c is the coefficient c of D'Arcy's, Bazin's, Kutter's, or other formula, as found by experiment. Since this coefficient varies with the condition of the inner surface of the tube, as well as with the velocity, it is to be expected that values of the boss of head given by different writers will vary as much as those of quantity of flow. Two tables for loss of head per 100 ft, in length in pipes of different diameters with different velocities are given below. The first is given by Clark, based on Ellis' and Howland's experiments; the second is from the Pelton Water-wneel Co.'s catalogue, based on Cox's formula, see p. 575, with the divisor 1000 instead of 1200, as it is for riveted steel pipe. The loss of head as given in these two tables for any given diameter and velocity differs considerably. Either table should be used with caution and head as given in the tables of flow based on Kutter's and D'Arcy's formulas.

Relative Loss of Head by Friction for each 100 Feet Longth of Clean Cast-iron Pipe,

(Based on Ellis and Howland's experiments.)

Velocity			D	famete	r of P	ipes in	Inche	e.		
in Feet per	3	4	8	6	7	8	9	10	12	14
Second.		1	os of	Head	in Fee	t, per 1	00 Fee	t Long	<u>-</u>	
Teet	Feet of Head	Feet of Head	Feet of Head	of	Peet of Head	ol	of	of	of	of
2 2.5 3 8.5 4 4.5 5	.97 1.49 1.9 2.6 8.3	.55 .92 1.2 1.6 2.2	.41 .64 .82 1.2 1.7	.32 .50 .72 1.0 1.3 1.6	.27 .43 .61 .7 .9 1.2	.23 .36 .51 .71 .92 1.2	.19 .30 .44 .61 .79 1.01 1.2	.18 .27 .39 .52 .69 .87 1.1	.15 .27 .83 .45 .59 .75	.12 .19 .27 .37 .49 .61 .76
	15	18	21	24	27	80	38	36	42	46
2 2.5 8.5 4.4 4.5 5.5	.11 .17 .25 .34 .44 .56 .70	.095 .147 .21 .29 .36 .46 .58	.075 .117 .17 .23 .31 .39 .48	.065 .109 .15 .20 .27 .84 .41 .50	055 .088 .13 .18 .23 .80 .87 .44	.052 .085 .12 16 .22 .28 .84 .89	.049 .076 .108 .15 .90 .25 .30 .36	.047 .067 .10 .14 .17 .22 .27	.036 .066 .081 .111 .14 .18 .22 .27	.030 .046 .067 .092 .116 .15 .18 .22

Loss of Head in Pipe by Friction.—Loss of head by friction in each 100 feet in length of different diameters of pipe when discharging the following quantities of water per minute (Pelton Water-wheel Co.):

*				Inside	Diame	ter of	Pipe i	Inch	28.			_
به م	1	1	1	2	1	В	•	4	1	5	(5
Telocity in Fee	Loss of Head in Feet.	Cubic Feet per Minute.	Loss of Head	Cubic Feet per	Loss of Head in Feet.	Cubic Feet per & Minute.	Loss of Head in Feet.	Cubic Feet per Minute.	Loss of Head in Feet.	Ouble Feet per Minute.	Loss of Head in Feet,	Cubic Feet per Minute.
2.0 3.0 4.0 5.0 6.0 7.0	2.87 4.89 8.20 12.88 17.23 22.89	.65 .99 1.82 1.65 1.98 9.81	1.185 2.44 4.10 6.17 8.61 11.45	2.62 8.92 5.28 6.54 7.85 9.16	.791 1.62 2.78 4.11 5.74 7.68	5.89 8.88 11.80 14.70 17.70 90.6	.598 1.29 2.05 8.06 4.81 5.78	26.2 81.4	.474 .978 1.64 9.46 8.45 4.57	82.7 40.9	.815 1.87 2.05 2.87	28.5 85.8 47.1 58.9 70.7 88.4

Flow of Water in Biveted Steel Pipes.—The laps and rivets tend to decrease the carrying capacity of the pipe. See paper on "New Formulas for Calculating the Flow of Water in Pipes and Channels," by W. E. Foss, Jour. Assoc. Eng. Soc., xili, 285. Also Clemens Herschel's book on "115 Experiments on the Carrying Capacity of Large Riveted Metal Conduits," John Wiley & Sons, 1897.

_[7	<u>'</u> i	8	3	. 1	9	1	0	1	1	1	2
١	h	Q	h	Q	h	Q	h	Q	h	6	h	Q
	.838	82.0	.296	41.9	.264	53	.297	65.4	.216	79.2		94.2
	.698	48.1	.611	62.8	.544	79.5	.488	98.2	.444			
	1.175 1.76	64.1 80.2	1.027	83.7	.918	106	.822	131 163		158	.685	
	2.46	96.2		105 125	1.37 1.92	132 159	1.23 1.71	196	1.122 1.56	287	1.028 1.48	283
	3.26	112.0		146	2.52	185	2 28		2.07	277	1.91	330
				Inside	Diam	eter of	Pipe i	n Inch	es.			·
J	1	8	1	4	1	15	1	6	;	18	٤	20
	h	Q	h	Q	h	Q	h	Q	h	6	h	Q
	.183	110	.169	128	.158	147	.147	167	.132	212	.119	262
	. 375	166	.849	192	.325	221	. 306	251	.271	318	.245	
	.632	221	.587	256	.548	294	.518	835	.456	424	.410	
	.949 1.825	276 832	.881 1.229	821 885	.822 1.148	368 442	.770 1.076	419 502	.685 .957	580 686	.617 .861	654 785
١	1.75	887	1.68	449	1.52	516	1.43	586	1.27	742	1.143	
١				Inside	Diame	ter of	Pipe i	n Inch	es.			
١	2	2	2	4	2	:6	2	8	8	10	8	6
	h	Q	h	Q	h	Q	h	Q	h	Q	h	6
1	.108	816	.098	377	.091	442	.084	513	.079	589	.066	
l	.222	475	.204	565	.188	663	.174	770	.163	888	.185	848 1278
l	.873	688	.342	754	.315	885	.298	1026	.278	1178	228	1697
۱	.561	792	.518	942	.474	1106	.440	1283	.411	1472	.842	2121
j	.782 1.040	950 1109	.717 .953	1181 1319	.662 .879	1327 1548	.615 .817	1539 1796	.574 .762	1767 2061	.479 .686	2545 2868

under 11-inch pipe, find 119 cubic ft.; opposite this will be found the loss by friction in 100 ft. of length for this amount of water, which is .444. Multiply this by the number of hundred feet of pipe, which is 6, and we have 2.66 ft., which is the loss of head. Therefore the effective head is 200 - 2.66 = 197.34.

EXPLANATION.—The loss of head by friction in pipe depends not only upon diameter and length, but upon the quantity of water passed through it. The head or pressure is what would be indicated by a pressure-gauge attached to the pipe near the wheel. Readings of gauge should be taken while the water is flowing from the nozzle.

To reduce heads in feet to pressure in pounds multiply by .433. To reduce pounds pressure to feet multiply by 2.309.

Cox's Formula. Weisbach's formula for loss of head caused by the friction of water in pipes is as follows:

Friction-head =
$$\left(0.0144 + \frac{0.01716}{\sqrt{V}}\right) \frac{L.V^2}{5.367d}$$

where L = length of pipe in feet; V = velocity of the water in feet per second; d =diameter of pipe in inches.

William Cox (Amer. Mach., Dec. 28, 1893) gives a simpler formula which gives almost identical results:

$$H = \text{friction-head in feet} = \frac{L}{d} \frac{4V^2 + 5V - 2}{1200}.$$
 (1)
$$\frac{Hd}{L} = \frac{4V^2 + 5V - 2}{1200}.$$
 (2)

He gives a table by means of which the value of $\frac{4V^2 + 5V - 2}{1200}$ is at once obtained when V is known, and vice versa.

VALUES OF
$$\frac{4V^2 + 5V - 2}{1200}$$
.

_										
V	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
1 2	.00588	.00695	.00818	.00938	.01070	,01208	.01353	.01505	.01663	.01828
2	.02000	.02178	.02363	.02555		.02958	.03170			.08845
3	.04083	.04329	.04540		.05103				.06230	.06528
4	.06833	.07145	.07468		.08120				.09513	.09878
5	.10250		.11013			.12208	.12620		.13463	.13895
6	.14333	.14778	15230	.15688	.16158	.16625	.17108	.17588	.18080	. 18578
7	.19083	.19595	.20113	.20638	.21170	.21708	.22253	.22805	.22363	.28928
8	.24500	.25078	.25663	.26255	.26853	.27458	,28070	.28688	.29313	.29945
9	.30583	.31228	.31890	.32538	.33203	.33875	.34553	.35238	.35930	. 36628
10	.37333	.38045	.38763	.39488	.40220	.40958	.41703	.42455	.48218	.43978
11	.44750	.45528	.46318	.47105	.47903	.48708	.49520	.50338	.51163	.51995
12	.52883	.53678	.54530	.55388	.56253	.57125	.58003	.58888	.59780	.60678
13	.61583	. 62495	.63413	.64338	.65270		.67153	.68105	.69063	.70028
14	.71000	.71978	.72963	.78955	.74953	.75958	.76970	.77988	.79013	
15	.81083	.82128	.83180	.84288	.85302	.86375	.87453	.88538	.89630	.90728
16	.91833	.92945							1.00918	1.02079
17	1.03250	1.04428	1.05612	1.06805	1.08003	1.09208	1.10420	1.11638	1.12863	1.14095
						1.21625				
19						1.34708				
20						1.48458				
21						1.62875				

The use of the formula and table is illustrated as follows:

Given a pipe 5 inches diameter and 1000 feet long, with 49 feet head, what will the discharge be?

If the velocity V is known in feet per second, the discharge is 0.32725d²V

cubic foot per minute. By equation 2 we have

$$\frac{4V^{0}+5V-2}{1200}=\frac{Hd}{L}=\frac{49\times 5}{1000}=0.245;$$

whence, by table, V= real velocity = 8 feet per second. The discharge in cubic feet per minute, if V is velocity in feet per second and d diameter in inches, is $0.32725d^{2}V$, whence, discharge

$$= 0.32725 \times 25 \times 8 = 65.45$$
 cubic feet per minute.

The velocity due the head, if there were no friction, is 8.025 $\sqrt{H} = 56.175$ feet per second, and the discharge at that velocity would be

$$0.82725 \times 25 \times 56.175 = 460$$
 cubic feet per minute.

Suppose it is required to deliver this amount, 460 cubic feet, at a velocity of 2 feet per second, what diameter of pipe will be required and what will be the loss of head by friction?

$$d = \text{diameter} = \sqrt{\frac{Q}{V \times 0.32725}} = \sqrt{\frac{460}{2 \times 0.32725}} = \sqrt{708} = 26.5 \text{ inches.}$$

Having now the diameter, the velocity, and the discharge, the friction-head is calculated by equation 1 and use of the table; thus,

$$H = \frac{L}{d} \frac{4V^2 + 5V - 2}{1200} = \frac{1000}{26.5} \times 0.02 = \frac{20}{26.5} = 0.75 \text{ foot,}$$

thus leaving 49 - 0.75 =say 48 feet effective head applicable to power-pro-

ducing purposes.

Problems of the loss of head may be solved rapidly by means of Cox's
Pipe Computer, a mechanical device on the principle of the slide-rule, for
take by Keuffel & Esser, New York.

Frictional Heads at Given Rates of Discharge in Clean Cast-iron Pipes for Each 1000 Feet of Length.

(Condensed from Ellis and Howland's Hydraulic Tables.)

	4-in Pip	ch e.	6-in Pij	ch e.	8-io Pi _l	ch ce.	10-in Pir		19-1 Pi	inch pe.	14-1 Pi	nch pe.
U. S. Gallong Discharged per Minute.	Velocity in ft. per sec.	Friction- head, feet.	Velocity in ft. per sec.	Friction- head, feet.	Velocity in ft. per sec.	Friction- head, feet.	Velocity in ft. per sec.	Friction- head, feet.	Velocity, in ft. per sec.	Friction- head, feet.	Velocity, in ft. per sec.	Friction- head, feet.
25 50 100 150 200 250 800 1000 1200 1200 2500 8000 1200 1200 1200 1200 1200 1200 12	. 64 1 28 2 55 8 88 5 11 6 37 7 . 66 8 . 94 10 . 21 12 . 77 15 . 82 17 . 87	59 2.01 7 36 16.05 28.09 49.47 62.20 84.26 109.68 170.58 244.76 3332.36	.28 .57: 1.170 2.27 2.84 3.407 4.54 5.67 6.81 7.94 9.08 10.21 11.35 13.61 15.88 18.15 20.42 22.69	.11 .32 .1.08 .3.28 .3.92 .6.00 .8.52 .11.48 .14.89 .23.01 .52.89 .44.54 .57.95 .73.12 .90.05 .129.20 .175.38 .228.62 .228.62 .228.90	.16 .82 .64 1.28 1.60 1.91 2.28 2.55 8.19 2.55 8.7 6.38 7.66 8.94 10.21 11.47 12.77 15.96	.04 .10 .80 1.01 1.52 2.13 2.85 8.68 5.64 8.03 14.05 17.68 21.74 31.17 42.13 54.84 69.22 85.27 183.70	.10 .20 .41 .61 .82 1.03 1.43 1.43 2.04 2.45 2.45 2.86 8.27 8.57 8.57 6.53 7.85 7.85 7.81 7.02 112.25	.02 .04 .111 .22 .54 .75 .99 1.27 2.72 8.66 4.73 5.28 10.38 14.02 18.22 43.87 62.95 43.87 62.95	.077.144.28 .483.577.71.188.585 .999.11.1842.27.22.555 2.2844.083.497.34.55.11.55.67.77.09	.01 .02 .05 .10 .16 .24 .82 .43 .54 .1.14 1.52 1.96 2.45 7.44 9.86 11.50 17.82 25.51		
				-				_			10.72	71.00
**	16-ii Pi	p e.	Pi	nch pe.	Pi	nch pe.	24-i Pi	ngh pe.	30- Pi	inch pe.	\$6- P	inch ipe,
U. S. Gallons Discharged per Minuts.	Velocity in It. per sec.	Friction- head, feet.					Velocity in fig. 14, 15, 15, 15, 15, 15, 15, 15, 15, 15, 15	Friction- bead, feet.	Velocity in ft. per sec. 148	pe.	Velocity in	Friction- head, feet.

Effect of Bends and Curves in Pipes, -Weisbach's rule for bends: Loss of head in feet = $\left[.131 + 1.847 \left(\frac{r}{R}\right)^{\frac{2}{3}}\right] \times \frac{v^2}{64.4} \times \frac{a}{180}$ in which r v^2 = internal radius of pipe in feet, R = radius of curvature of axis of pipe, v = velocity in feet per second, and a = the central angle, or angle subtended by the bend.

by the bend.

Hamilton Smith, Jr., in his work on Hydraulics, says: The experimental data at hand are entirely insufficient to permit a satisfactory analysis of this quite complicated subject; it fact, about the only experiments of value are those made by Bossut and Dubuat with small pipes.

Curves.—If the pipe has easy curves, say with radius not less than 5 diameters of the pipe, the flow will not be materially diminished, provided the tops of all curves are kept below the hydraulic grade-line and provision be made for escape of air from the tops of all curves. (Trautwine.)

Hydraulic Grade-line,—In a straight tube of uniform diameter throughout, running full and discharging freely into the air, the hydraulic grade-line is a straight line drawn from the discharge end to a point immediately over the entry end of the pipe and at a depth below the surface equal to the entry and velocity heads. (Trautwine.)

In a pipe leading from a reservoir, no part of its length should be above

In a pipe leading from a reservoir, no part of its length should be above

the hydraulic grade-line.

Flow of Water in House-service Pipes. Mr. E. Kuichling, C.E., furnished the following table to the Thomson Meter Co.:

Condition	in Main, per inch.		Cul	oic Fee	t per l	capable finute, pecifié	from	the Pi	pe,	
of Discharge.	Pressure in pounds pe square in	No	minal l	Diame		Iron of nches.	r Lead	Servi	ce-pipe	in
	E	1/4	56	3/4	1	11/6	2	8	4	6
Through 85 feet of service- pipe, no back pressure.	80 40 50 60 75 100 180	1.10 1.27 1.42 1.56 1.74 2.01 2.29	1.92 2.22 2.48 2.71 8.03 8.50 8.99	3.01 8.48 8.89 4.26 4.77 5.50 6.28	6.13 7.08 7.92 8.67 9.70 11.20 12.77	16.58 19.14 21.40 23.44 26.21 80.27 84.51	48.04 47.15 52.71 60.87	101.80 113.82 124.68 189.89 160.96	200.75 224.44 245.87 274.89 317.41	444.63 513.42 574.02 628.81 703.03 811.79 925.58
Through 100 feet of service- pipe, no back pressure.	80 40 50 60 75 100 180	0.66 0.77 0.86 0.94 1.05 1.22 1.89	1.16 1.34 1.50 1.65 1.84 2.18 2.42	1.84 2.12 2.37 2.60 2.91 8.86 8.88	3.78 4.36 4.88 5.34 5.97 6.90 7.86	10.40 12.01 18.43 14.71 16.45 18.99 21.66		67.19 75.18 82.30 92.01 106.24	186.41 152.51 167.06 186.78 215.68	317.28 366.30 409.54 448.68 501.58 579.18 660.36
Through 100 feet of service- pipe and 15 feet vertical rise.	80 40 50 60 75 100 180	0.55 0.66 0.75 0.88 0.94 1.10	0.96 1.15 1.81 1.45 1.64 1.92 2.20	1.52 1.81 2.06 2.29 2.59 3.02 3.48	8.11 3.72 4.24 4.70 5.82 6.21 7.14	8.57 10.24 11.67 12.94 14.64 17.10 19.66		57.20 65.18 72.28 81.79 95.55	116.01 132.20 146 61 165.90 198.82	260.56 311.09 354.49 393.18 444.85 519.72 597.81
Through 100 feet of service- pipe, and 80 feet vertical rise.	80 40 50 60 75 100 130	0.44 0.55 0.65 0.78 0.84 1.00 1.15	0.77 0.97 1.14 1.28 1.47 1.74 2.02	1.22 1.53 1.79 2.02 2.82 2.75 8.19	2.50 8.15 8.69 4.15 4.77 5.65 6.55	6.80 8.68 10.16 11.45 18 15 15.58 18.07	28.47 26.95 81.93	56.98 64.22 78.76 87.38	98 98 115.87 180.59 149.99	211.54 266.58 312.08 851.78 403.98 478.56

In this table it is assumed that the pipe is straight and smooth inside; that the friction of the main and meter are disregarded; that the lulet from the main is of ordinary character, sharp, not flaring or rounded, and that the outlet is the full diameter of pipe. The deliveries given will be increased if, first, the pipe between the meter and the main is of larger diameter than the outlet; second, if the main is tapped, say for 1-inch pipe, but is enlarged from the tap to 114 or 114 inch; or, third, if pipe on the outlet is larger than that on the inlet side of the meter. The exact details of the conditions given are rarely met in practice; consequently the quantities of the table may be expected to be decreased, because the pipe is liable to be throttled at the joints, additional bends may interpose, or stop-cocks may be used, or the

Joints, additional benes may merpess, or sup-consumar to use a pack-pressure may be increased.

Air-bound Pipes.—A pipe is said to be air-bound when, in consequence of air being entrapped at the high points of vertical curves in the line, water will not flow out of the pipe, although the supply is higher than the outlet. The remedy is to provide cocks or valves at the high points, through which the air may be discharged. The valve may be made auto-

matic by means of a float.

Vertical Jets. (Molesworth.)—H = head of water, h = height of jet, d = diameter of jet, K = coefficient, varying with ratio of diameter of jet to head; then h = KH.

4500, If $H = d \times 800$ 600 1800 1000 1500 2800 3500 K =.96 .9 .85 .25 .7 .6 .5 .8

Water Delivered through Meters. (Thomson Meter Co.).—The best modern practice limits the velocity in water-pipes to 10 lineal feet per second. Assume this as a basis of delivery, and we find, for the several sizes of pipes usually metered, the following approximate results: Nominal diameter of pipe in inches:

3/4 56 Quantity delivered, in cubic feet per minute, due to said velocity: 1.28 7.36 29.5 0.461.85 8.28 18.1

Prices Charged for Water in Different Cities (National Meter Co.): Average minimum price for 1000 gallons in 163 places...... 9.4 cents. maximum

Extremes, 21/4 cents to100 WIRE-STRUGAMS.

Discharge from Nozzles at Different Pressures.

(J. T. Fanning, Am. Water-works Ass'n, 1892, Eng'g News, July 14, 1892.)

Nozzle diam., in.	Height of stream, ft.	Pressure at Play- pipe, lbs.	Horizon- tal Pro- jection of Streams, ft.		Gallons per 24 hours.	Friction per 100 ft. Hose, lbs.	Friction per 100 ft. Hose, Net Head, ft.
: 1	70	46.5	59.5	208	292,298	10.75	24.77
	80	59.0	67.0	230	831,200	18.00	81.10
1	90	79.0	76.6	267	884,500	17.70	40.78
	100	130.0	88.0	811	447,900	22.50	54.14
116	70 80	44.5 55.5	61.3 69.5	249 281	858,520 404,700	15.50 19.40	85.71
173	90	72.0	78.5	824	466,600	25.40	44.70 58.52
114	100	108.0	89.0	876	541,500	83.80	77.88
	70	48.0	66.0	806	440,618	22.75	52.42
114	80	53.5	72.4	348	493,900	28.40.	65.48
	90	68 .5	81.0	888	558,800	85.90	82.71
134	100	98.0	92.0	460	662,500	57.75	86.98
136	70	41.5	77.0	868	530,149	82.50	74.88
132	80	51.5	74.4	410	590,500	40.00	92.16
	90	65.5	82.6	468	674,000	51.40	118.48
158	100	88.0	92.0	540	777,700	72.00	165.89

Priction Lesses in Hose. In the above table the volumes of water discharged per jet were for stated pressures at the play-pipe.

In providing for this pressure due allowance is to be made for friction

losses in each hose, according to the streams of greatest discharge which are to be used.

The loss of pressure or its equivalent loss of head (a) in the hose may be

found by the formula $h = v^2(4m) \frac{1}{8qd}$

In this formula, as ordinarily used, for friction per 100 ft. of 214 in. hose there are the following constants: 216 in. diameter of hose d=.20638 ft.; length of hose l=100 ft., and 2g=64.4. The variables are: v= velocity in feet per second; h = loss of head in feet per 100 ft. of hose; m = a coeffieient found by experiment; the velocity v is found from the given discharges of the jets through the given diameter of hose.

Head and Pressure Losses by Friction in 100-ft. Lengths of Bubber-lined Smooth 2½-in, Hose,

Discharge per minute, gallons.	Velocity per second, ft.	Coefficient,	Head Lost, ft.	Pressure Lost, lbs. per sq. in.	Gallons per 24 hours.
200	13.072	.00450	22.89	9.93	288,000
250	16.388	.00446	85.55	15.43	860,000
300 347	18.858	.00442	46.80	20.81 26.70	482,000 499,680
850	21.677 22.873	.00489	61.58 68.48	29.78	504,000
400	26.144 29.408	.00486	88.83	38.55	576,000
450		.00484	111.80	48.52	648,000
500	82.675	.00432	137.50	59.67	720,000
520	83.982	.00431	148.40	64.40	748,800

These frictions are for given volumes of flow in the hose and the velocities respectively due to those volumes, and are independent of size of nozzle. The changes in nozzle do not affect the friction in the hose if there is no change in velocity of flow, but a larger nozzle with equal pressure at the nozzle augments the dischange and velocity of flow, and thus materially increases the friction loss in the hose.

Loss of Pressure (p) and Head (h) in Rubber-lined Smooth 2½-in. Hose may be found approximately by the formula lq^2

 $\frac{4}{4150d^5}$ and $h = \frac{4}{1801d^5}$ in which p = pressure lost by friction, in 18010° pounds per square inch; l = length of hose in feet; q = gallons of water discharged per minute: d = diam of the hose in inches, $2 \le \text{lin}$; h = friction-head in feet. The coefficient of d would be decreased for rougher hose. The loss of pressure and head for a $1 \le \text{lin}$; hose, approximately 20 lbs., or 45 ft. net, or, say, including friction in the hydrant, $1 \le \text{lin}$ hose.

If we change the nozzles to 1½ or 1¾ in diameter, then for the same 80 ft. height of stream we increase the friction losses on the hose to approximately ¾ ft. and 1 ft. head, respectively, for each foot-length of hose. These computations show the great difficulty of maintaining a high stream through large nozzles unless the hose is very short, especially for a

gravity or direct-pressure system.

This single 114 in. stream requires approximately 56 lbs. pressure, equivalent to 189 ft. head, at the play-pipe, and 45 to 50 ft. head for each 100 ft. elength of smooth 214 in. hose, so that for 100, 200, and 300 ft. of hose we must have available heads at the hydrant or fire-engine of 179, 239, and 279 ft., respectively. If we substitute 11/4-in. nozzies for same height of stream we must have available heads at the hydrants or engine of 193, 259, and 225 ft., respectively, or we must increase the diameter of a portion at least of the long hose and save friction-less of head.

Rated Capacities of Steam Fire-engines, which is perhaps one third greater than their ordinary rate of work at fires, are substantially as follows :

550 gals. per min., or 792,000 gals. per 24 hours. 8d size, 1,008,000 700 46 66 ..

1st " 900 1 ext., 1,100 1,296,000 66 1.584.000

Pressures required at Nozzle and at Pump, with Quantity and Pressure of Water Necessary to throw Water Various Distances through Different-sized Nozzles— using 2½-inch Eubber Hose and Smooth Nozzles.

(From Experiments of Ellis & Leshure, Fanning's "Water Supply.")

Eize of Nozzles.		1 In	eh.			136 I	nch.	
Pressure at nozzle, lbs, per sq. in	48 155	189 142	90 97 219 168 181	186	118	240 148	80 108 277 175 187	100 185 810 198 157
A 24		114 1	nch.		!	154 1	inch.	
Size of Nozzles.	!	-/-			!	-/•		
Pressure at nozzle, lbs. per sq. in	40		80		40		80	100
Pressure at nozzle, lbs. per sq. in * Pressure at pump or hydrant with 100 feet 214 inch rubber hose	40 61	60	80 123	100 154	71	60	80 144	180
Pressure at nozzle, lbs. per sq. in * Pressure at pump or hydrant with	40	60 92 297	80 128 842	100 154 888	71	60 107 858	80 144 413	180 462

*For greater length of 214-inch hose the increased friction can be obtained by noting the differences between the above given "pressure at nozzle" and "pressure at pump or hydrant with 100 feet of hose." For instance, if it requires at hydrant or pump eight pounds more pressure than it does at nozzle to overcome the friction when pumping through 100 than it does at nozzle to overcome the friction when pumping through 100 than it does at nozzle to overcome the friction when pumping through 100 than it does at nozzle to overcome the friction when pumping through 100 than the first through 100 than the first through 100 throu feet of 2½-inch hose (using 1-inch nozzle, with 40-pound pressure at said nozzle) then it requires 16-pounds pressure to overcome the friction in forcing through 200 feet of same size hose.

Decrease of Flow due to Increase of Length of Hose. (J. R. Freeman's Experiments, Trans. A. S. C. E. 1889.)—If the static pres-sure is 80 lbs. and the hydrant-pipes of such size that the pressure at the hy-drant is 70 lbs., the hose 2½ in. nominal diam., and the nozzle 1½ in. diam., the height of effective fire-stream obtainable and the quantity in gallons per minute will be:

							Linen	Hose.		Rubber- d Hose.
							Height, feet.	Gals. per min.	Height,	Gals. per min.
With	50	ft.	of	216-in.	hose	B	. 78	261	81	282
	250		**	776	66			184	61	229
•6	500	"	66	6.6	44		97	146	48	162

With 500 ft. of smoothest and best rubber-lined hose, if diameter be exactly 2½ in., effective height of stream will be 39 ft. (177 gals.); if diameter be ½ in. larger, effective height of stream will be 46 ft. (192 gals.)

THE SIPHON.

The Siphon is a bent tube of unequal branches, open at both ends, and is used to convey a liquid from a higher to a lower level, over an intermediate point higher than elther. Its parallel branches being in a vertical plane and plunged into two bodies of liquid whose upper surfaces are at different levels, the fluid will stand at the same level both within and without each the same tevel of the tube when a vent or small opening is made at the bend. If the air be withdrawn from the siphon through this vent, the water will rise in the branches by the atmospheric pressure without, and when the two columns unite and the vent is closed, the liquid will flow from the upper reservoir as long as the end of the shorter branch of the siphon is below the surface of the liquid in the reservoir.

If the water was free from air the height of the bend above the supply level might be as great as 33 feet.

If A = area of cross-section of the tube in square feet, H = the difference in level between the two reservoirs in feet, D the density of the liquid in pounds per cubic foot, then ADH measures the intensity of the force which causes the movement of the fluid, and $V = \sqrt{2gH} = 8.02 \ \sqrt{H}$ is the theoretical velocity, in feet per second, which is reduced by the loss of head for entry and friction, as in other cases of flow of liquids through pipes. In the case of the difference of level being greater than 83 feet, however, the velocity of the water in the shorter leg is limited to that due to a height of 83 feet, or that due to the difference between the atmospheric pressure at the entrance and the vacuum at the bend.

Leicester Allen (Am. Mach., Nov. 2, 1893) says: The supply of liquid to a siphon must be greater than the flow which would take place from the discharge end of the pipe, provided the pipe were filled with the liquid, the supply end stopped, and the discharge end opened when the discharge end

is left free, unregulated, and unsubmerged.

To illustrate this principle, let us suppose the extreme case of a siphon having a calibre of 1 foot, in which the difference of level, or between the point of supply and discharge, is 4 inches. Let us further suppose this siphon to be at the sea-level, and its highest point above the level of the supply to be 27 feet. Also suppose the discharge end of this siphon to be unregulated, unsubmerged. It would be inoperative because the water in the longer leg would not be held solid by the pressure of the atmosphere against it, and it would therefore break up and run out faster than it could be replaced at the inflow end under an effective head of only 4 inches.

Long Siphons.—Prof. Joseph Torrey, in the Amer. Machinist, describes a long siphon which was a partial failure.

The length of the pipe was 1792 feet. The pipe was 3 inches diameter, and rose at one point 9 feet above the initial level. The final level was 20 feet below the initial level. No automatic air valve was provided. The highest point in the siphon was about one third the total distance from the pond and nearest the pond. At this point a pump was placed, whose mission was to fill the pipe when necessary. This siphon would flow for about two hours and then cease, owing to accumulation of air in the pipe. When in full operation it discharged 43% gallons per minute. The theoretical discharge from such a sized pipe with the specified head is 53% gallons per minute. Siphon on the Water-supply of Mount Vernon, N. V. (Eng'q News, May 4, 1893.)—A 12-inch siphon, 925 feet long, with a maximum lift. of 92 19 feet and a 45° change in alignment, was put in use in 1892 by the

lift of 22.12 feet and a 45° change in alignment, was put in use in 1892 by the New York City Suburban Water Co., which supplies Mount Vernon, N. Y. At its summit the siphon crosses a supply main, which is tapped to charge

the siphon.

The air-chamber at the siphon is 12 inches by 16 feet long. A 14-inch tap and cock at the top of the chamber provide an outlet for the collected air.

It was found that the siphon with air-chamber as desc.ibed would run until 125 cubic feet of air had gathered, and that this took place only half as soon with a 14-foot lift as with the full lift of 22.12 feet. The siphon will operate about 12 hours without being recharged, but more water can be gotten over by charging every six hours. It can be kept running 23 hours out of 24 with only one man in attendance. With the siphon as described above it is necessary to close the valves at each end of the siphon to recharge it.

It has been found by weir measurements that the discharge of the siphon before air accumulates at the summit is practically the same as through a

straight pipe.

MEASUREMENT OF FLOWING WATER.

Piezometer.—If a vertical or oblique tube be inserted into a pipe containing water under pressure, the water will rise in the former, and the vertical height to which it rises will be the head producing the pressure at the point where the tube is attached. Such a tube is called a piezometer or pressure measure. If the water in the piezometer falls below its proper pressure measure. If the water in the plezometer falls below its proper level it shows that the pressure in the main pipe has been reduced by an extension of the main pipe has been reduced by an extension of the major property of the water rises obstruction between the piezometer and the reservoir. If the water rises above its proper level, it indicates that the pressure there has been increased by an obstruction beyond the piezometer. If we imagine a pipe full of water to be provided with a number of piezometers, then a line joining the tops of the columns of water in them is

the hydraulic grade-line.

Pitot Tube Gauge.—The Pitot tube is used for measuring the velocity of fluids in motion. It has been used with great success in measuring the flow of natural gas. (S. W. Robinson, Report Ohio Geol. Survey, 1890.) (See also Van Nostrand's Mag., vol. xxxv.) It is simply a tube so bent that a short leg extends into the current of fluid flowing from a tube, with the plane of the entering orifice opposed at right angles to the direction of the current. The pressure caused by the impact of the current is transmitted the current is transmitted. through the tube to a pressure gauge of any kind, such as a column of water or of mercury, or a Bourdon spring-gauge. From the pressure thus indicated and the known density and temperature of the flowing gas is obtained the head corresponding to the pressure, and from this the velocity. In a modification of the Pitot tube described by Prof. Robinson, there are In a modification of the ricot tube described by Fol. Robinson, there are two tubes inserted into the pipe conveying the gas, one of which has the plane of the orifice at right angles to the current, to receive the static pressure plus the pressure due to impact; the other has the plane of its critical parallel to the current, so as to receive the static pressure only. These tubes are connected to the legs of a *U* tube partly filled with mercury, which then registers the difference in pressure in the two tubes, from which the velocity may be calculated. Comparative tests of Pitot tubes with gasmeters, for measurement of the flow of natural gas, have shown an agreement within 3%.

The Venturi Meter, invented by Clemens Herschel, and described in a pamphlet issued by the Builders' Iron Foundry of Providence, R. I., is named from Venturi, who first called attention, in 1796, to the relation between the velocities and pressures of fluids when flowing through converging

and diverging tubes.

It consists of two parts—the tube, through which the water flows, and the recorder, which registers the quantity of water that passes through the

The tube takes the shape of two truncated cones joined in their smallest diameters by a short throat-piece. At the up-stream end and at the throat there are pressure-chambers, at which points the pressures are taken.

The action of the tube is based on that property which causes the small section of a gently expanding frustum of a cone to receive, without material resultant loss of head, as much water at the smallest diameter as is discharged at the large end, and on that further property which causes the pressure of the water flowing through the throat to be less, by virtue of its greater velocity, than the pressure at the up-stream end of the tube, each pressure being at the same time a function of the velocity at that point and of the hydrostatic pressure which would obtain were the water motionless within the pipe.

The recorder is connected with the tube by pressure pipes which lead to it from the chambers surrounding the up-stream end and the throat of the tube. It may be placed in any convenient position within 1000 feet of the tube. It is operated by a weight and clockwork,

The difference of pressure or head at the entrance and at the throat of the meter is balanced in the recorder by the difference of level in two columns of mercury in cylindrical receivers, one within the other. The inner carries a float, the position of which is indicative of the quantity of water flowing through the tube. By its rise and fall the float varies the time of contact between an integrating drum and the counters by which the successive readings are registered.

There is no limit to the sizes of the meters nor the quantity of water that may be measured. Meters with 24-inch, 36-inch, 48-inch, and even 20-foot

tubes can be readily mcde.

Measurement by Venturi Tubes. (Trans A. S. C. E., Nov., 1887, and Jan., 1888.)—Mr. Herschel recommends the use of a Venturi tube, inserted in the force-main of the pumping engine, for determining the quantity of water discharged. Such a tube applied to a 24-inch main has a total length of about 20 feet. At a distance of 4 feet from the end nearest the engine the inside diameter of the tube is contracted to a throat having a diameter of about 8 inches. A pressure-gauge is attached to each of two chambers, the one surrounding and communicating with the entrance or main pipe, the other with the throat. According to experiments made upon two tubes of this kind, one 4 in. in diameter at the throat and 12 in. at the entrance, and the other about 36 in. in diameter at the throat and 9 feet at its entrance, the quantity of water which passes through the tube is very nearly the theoretical discharge through an opening having an area equal to that of the throat, and a velocity which is that due to the difference in head shown by the two gauges. Mr. Herschel states that the coefficient for these two widely-varying sizes of tubes and for a wide range of velocity through the pipe, was found to be within two per cent, either way, of 98%. In other words, the quantity of water flowing through the tube per second is expressed within two per cent by the formula $W=0.98\times A\times \sqrt{2gh}$, in which A is the area of the throat of the tube, h the head, in feet, correspond-

A is the area of the throat of the tube, a the head, in feet, corresponding to the difference in the pressure of the water entering the tube and that found at the throat, and g = 32.16.

Measurement of **Discharge** of **Pumping-engines** by **Means of Nozzles**. (Trans. A. S. M. E., xii. 575).—The measurement of water by computation from its discharge through orifices, or through the nozzles of fire-hose, furnishes a means of determining the quantity of water by the purping engine which one hose policy of the transplacements. nozzies of nre-nose, rurnisnes a means of determining the quantity of water delivered by a pumping-engine which can be applied without much difficulty. John R. Freeman, Trans. A. S. C. E., Nov., 1889, describes a series of experiments covering a wide range of pressures and sizes, and the results showed that the coefficient of discharge for a smooth nozzle of ordinary good form was within one half of one per cent, either way, of 0.977; the diameter of the nozzle being accurately calipered, and the pressures being determined by means of an accurate gauge attached to a suitable piezometer at the base of the play-pipe.

In order to use this method for determining the quantity of water discharged by a pumping-engine, it would be necessary to provide a pressure-box, to which the water would be conducted, and attach to the box as many nozzles as would be required to carry off the water. According to Mr. Freeman's estimate, four 1½-inch nozzles, thus connected, with a pressure receivants essumate, 1001 142-1101 nozzies, thus connected, with a pressure of 80 lbs, per square inch, would discharge the full capacity of a two-and a-half-million engine. He also suggests the use of a portable apparatus with a single opening for discharge, consisting essentially of a Siamese nozzie, so-called, the water being carried to it by three or more lines of fire-hose. To insure reliability for these measurements, it is necessary that the shut-off valve in the force-main, or the several shut-off valves, should be tight to that all the water discharged by the another may note through the another.

so that all the water discharged by the engine may pass through the nozzles.

Flow through Rectangular Orifices. (Approximate, Seep. 556.)

CUBIC FEET OF WATER DISCHARGED PER MINUTE THROUGH AN ORIFICE ONE INCH SQUARE, UNDER ANY HEAD OF WATER FROM 8 TO 72 INCHES.

For any other orifice multiply by its area in square inches. Formula, $Q' = .624 \sqrt{h''} \times a$. Q' = cu, ft. per min.; a = area in sq. in.

Heads in inches.	Cubic Feet Discharged per min.	Heads in inches.	Cubic Feet Discharged per min.	Heads in inches.	Cubic Feet Discharged per min.	Heads in inches.	Cubic Feet Discharged per min.	Heads in inches.	Cubic Feet Discharged per min.	Heads in inches.	Cubic Feet Discharged per min.	Heads in inches.	Cubic Feet Discharged per min.
8 4 5 6 7 8 9 10 11 12	1.12 1.27 1.40 1.52 1.64 1.75 1.84 1.94 2.08 2.12	18 14 15 16 17 18 19 20 21	2.20 2.28 2.36 2.43 2.51 2.58 2.64 2.71 2.78 2.84	23 24 25 26 27 28 29 80 81 82	2.90 2.97 8.08 3.08 3.14 8.20 8.25 3.81 8.36 8.41	83 84 85 86 87 38 89 40 41 42	8.47 3.52 8.57 3.62 8.67 8.72 3.77 8.61 8.86 8.91	48 44 45 46 47 48 49 50 51	8.95 4.00 4.05 4.09 4.12 4.18 4.21 4.27 4.80 4.84	58 54 56 57 58 59 60 61 62	4.89 4.42 4.46 4.53 4.55 4.63 4.65 4.72 4.74	68 64 65 66 67 68 69 70 71	4.78 4.81 4.85 4.89 4.97 5.00 5.08 5.07 5.09

Measurement of an Open Stream by Velocity and Cross-section.—Measure the depth of the water at from 6 to 12 points across the stream at equal distances between. Add all the depths in feet together the stream at equal distances between. And all the depths in feet together and divide by the number of measurements made; this will be the average depth of the stream, which multiplied by its width will give its area or cross-section. Multiply this by the velocity of the stream in feet per minute, and the result will be the discharge in cubic feet per minute of the stream.

The velocity of the stream can be found by laying off 100 feet of the bank

and throwing a float into the middle, noting the time taken in passing over the 100 ft. Do this a number of times and take the average; then, dividing

this distance by the time gives the velocity at the surface. As the top of the stream flows faster than the bottom or sides—the average velocity being about 83% of the surface velocity at the middle—it is convenient to measure a distance of 120 feet for the float and reckon it as 100.

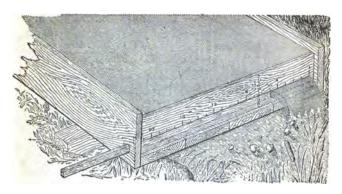


Fig. 180.

Miners' Inch Measurements. (Pelton Water Wheel Co.)

The cut, Fig. 130, shows the form of measuring-box ordinarily used, and the following table gives the discharge in cubic feet per minute of a miner's inch of water, as measured under the various heads and different lengths and heights of apertures used in California.

Length	Openin	gs 2 Inche	s High.	Openings 4 Inches High.					
of Opening in inches.	Head to Centre, 5 inches.	Head to Centre, 6 inches.	Head to Centre, 7 inches.	Head to Centre, 5 inches.	Head to Centre, 6 inches.	Head to Centre, 7 inches.			
4 6 8 10 12 14 16 18 20 22 24	Cu, ft, 1.348 1.355 1.359 1.361 1.363 1.364 1.365 1.365 1.366 1.366	Cu. ft. 1.473 1.480 1.484 1.485 1.487 1.489 1.489 1.490 1.490	Cu. ft. 1.589 1.596 1.600 1.602 1.604 1.605 1.606 1.606 1.607 1.607	Cu. ft. 1.820 1.836 1.344 1.849 1.852 1.854 1.856 1.857 1.859 1.359	Cu. ft. 1.450 1.470 1.481 1.487 1.491 1.494 1.496 1.498 1.500 1.501	Cu. ft. 1,570 1,595 1,698 1,615 1,620 1,623 1,628 1,630 1,631 1,632			
24 26 28 80 40	1.366 1.367 1.367 1.867	1.490 1.491 1.491 1.492	1.607 1.607 1.608 1.608	1.861 1.861 1.362 1.363	1.509 1.503 1.503 1.505	1.633 1.634 1.635 1.637			
50 60 70 80 90	1.368 1.368 1.368 1.368 1.869 1.369	1.498 1.493 1.498 1.493 1.493 1.494	1.609 1.609 1.609 1.609 1.610	1.364 1.365 1.365 1.366 1.866 1.366	1.507 1.508 1.508 1.509 1.509 1.509	1.689 1.640 1.641 1.641 1.641 1.642			

Note.—The apertures from which the above measurements were obtained

were through material 11/4 inches thick, and the lower edge 2 inches above

rice lottom of the measuring-box, thus giving full contraction.

Flow of Water Over Weirs. Weir Dam Measurement.
(Pelton Water Wheel Co.)—Place a board or plank in the stream, as shown

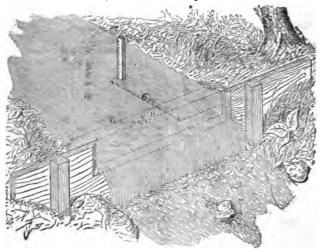


Fig. 181.

in the sketch, at some point where a pond will form above. The length of the notch in the dam should be from two to four times its depth for small quantities and longer for large quantities. The edges of the notch should be bevelled toward the intake side, as shown. The overfall below the notch should not be less than twice its depth. [Francis says a fall below the crest equal to one-half the head is sufficient, but there must be a free access of air under the sheet.]

In the pond, about 6ft. above the dam, drive a stake, and then obstruct the water until it rises precisely to the bottom of the notch and mark the stake at this level. Then complete the dam so as to cause all the water to flow through the notch, and, after time for the water to settle, mark the stake again for this new level. If preferred the stake can be driven with its top precisely level with the bottom of the notch and the depth of the water be measured with a rule after the water is flowing free, but the marks are preferable in most cases. The stake can then be withdrawn; and the distance between the marks is the theoretical depth of flow corresponding to the quantities in the table on the following page.

state Bormulo for Wairs.

Francis's For	As given by Francis.	As modified by Smith.
Weirs with both end contractions a suppressed	$Q=3.83lh^{\frac{3}{2}}$	$3.29 \left(l + \frac{h}{7}\right) h^{\frac{3}{4}}$
Weirs with one end contraction suppressed	$Q = 8.83(l1h)h^{\frac{3}{4}}$	8.29lh ³
Weirs with full contraction	$Q = 3.83(l2h)h^{\frac{3}{2}}$	$8.29\left(l-\frac{h}{10}\right)h^{\frac{3}{4}}$

The greatest variation of the Francis formulæ from the values of c given by Smith amounts to $3/6\pi$. The modified Francis formulæ, says Smith, will give results sufficiently exact, when great accuracy is not required, within the limits of h, from .5 ft. to 2 ft., l being not less than 8 h.

 $Q={
m discharge}$ in cubic feet per second, $l={
m length}$ of weir in feet, $k={
m effective}$ head in feet, measured from the level of the crest to the level of still

water above the weir.

If Q'= discharge in cubic feet per minute, and l' and h' are taken in inches, the first of the above formulæ reduces to $Q'=0.4l'h^{\frac{1}{2}}$. From this formula the following table is calculated. The values are sufficiently accurate for ordinary computations of water-power for weirs without end contraction, that is, for a weir the full width of the channel of approach, and are approximate also for weirs with end contraction when l= at least 10h, but about 6π in excess of the truth when l=4h.

Weir Table.

GIVING CUBIC FEET OF WATER PER MINUTE THAT WILL FLOW OVER A WEIR ONE INCH WIDE AND FROM 1/4 TO 201/4 INCHES DEEP.

Town o	than	widtha	multiply b	w tha	width	in inches
FOR C	tner	widths	muiudiv i	IV THE	WIGEN	in inches.

		⅓ in.	1/4 in.	₹ in.	⅓ in.	5∕8 in.	% in.	% in.
in.	cu. ft.							
0	.00	.01	.05	.09	.14	.19	.26	.32
1	.40	.47	.55	.64	.73	.82	.92	1.02
2	1.18	1.23	1.35	1.46	1.58	1.70	1.82	1.95
8	2.07	.2.21	2.34	2.48	2.61	2.76	2.90	8.05
4	3.20	8.85	3.50	3.66	8.81	3.97	4.14	4.80
5	4.47	4.64	4.81	4.98	5.15	5.33	5.51	5.69
6	5.87	6.06	6.25	6.44	6.62	6.82	7.01	7.21
7	7.40	7.60	7.80	8.01	8.21	8.42	8.63	8.83
8	9.05	9.26	9.47	9.69	9.91	10.13	10.35	10.57
9	10.80	11.02	11.25	11.48	11.71	11.94	12.17	12.41
10	12.64	12.88	13.12	13.36	18.60	13.85	14.09	14.84
11	14.59	14.84	15.09	15 84	15.59	15.85	16.11	16.86
12	16.62	16.88	17.15	17.41	17.67	17.94	18.21	18.47
18	18.74	19.01	19.29	19.56	19.84	20.11	20.39	20.67
14	20.95	21.23	21.51	21.80	22.08	22.37	22.65	22.94
15	23.23	23.52	23.82	24.11	24.40	24.70	25.00	25.30
16	25.60	25.90	26.20	26.50	26.80	27.11	27.42	27.72
17	28.03	28.34	28.65	28.97	29.28	29.59	29.91	80.22
18	30.54	80.86	31.18	31.50	31.82	32.15	82.47	82.80
19	33.12	83.45	33.78	84 11	84.44	84.77	85.10	85.44
20	35.77	36.11	36.45	36.78	87.12	37.46	37.80	88.15

For more accurate computations, the coefficients of flow of Hamilton Smith, Jr., or of Bazin should be used. In Smith's hydraulics will be found a collection of results of experiments on orfices and weirs of various shapes made by many different authorities, together with a discussion of their several formulæ. (See also Trautwine's Pocket Book.)

Baxin's Experiments.—M. Bazin (Annales des Ponts et Chaussées, Oct., 1838, translated by Marichal and Trautwine, Proc. Engrs. Club of Phila. Jan, 1890), made an extensive series of experiments with a sharp-created weir without lateral contraction, the air being admitted freely behind the falling sheet, and found values of m varying from 0.42 to 0.50, with variations of the length of the weir from 1934 to 7834 in., of the height of the creat above the bottom of the channel from 0.79 to 2.46 ft., and of the lead from 1.97 to 23.62 in. From these experiments he deduces the following formula:

$$Q = \left[0.425 + 0.21 \left(\frac{H}{P+H}\right)^2\right] LH \sqrt{2gH},$$

in which P is the height in feet of the crest of the weir above the bottom of the channel of approach, L the length of the weir, H the head, both in feet, and Q the discharge in cu. ft. per sec. This formula, says M. Bazin, is entirely practical where errors of $\mathscr L$ to $\mathscr R$ are admissible. The following table is condensed from M. Bazin's paper:

Values of the Coefficient m in the Formula $Q=mLH\sqrt{2\rho H}$, for a Share-created Weir without Lateral Contraction; the Air being Admitted Freely Behind the Falling Sheft,

Hea		Helgi	nt of (Crest C	t Wel	r Abo	ve Be	ed of (Chaur	el.	
H		Feet0.66 Inches 7.87	0.98 11.31		1.64 19.69			8.28 39.38			8 8
Ft. 1	In.	m	m	m	m	m	m	m	m	m	7)1
.164	1.97	0.458	0.453	0.451	0.450	0.449	0.449	0.449	0.448	0.448	0.4481
.280	2.76	0.455	0.448	0.445	0.443	0.442	0.441	0.440	0.440	0.439	0.4391
,295			0.447	0.442	0.440	0.438	0.436	0.436	0.435	0.434	0.4340
.394	4.72	0.462	0.448	0.442	0.438	0.436	0.433	0.432	0.480	0.430	0.4291
.525											0.4246
.656	7.87	0.480									0.4215
.787	9.45	0.488	0.465	0.452	0.444	0.438	0.432	0.428	0.424	0.422	0,4194
.919	11.02	0.496	0.472	0.457	0.448	0.441	0.433	0,429	0.424	0.422	0.4181
1.050	12,60		0.478	0.462	0.452	0.444	0.436	0.480	0.424	0.421	0.4168
1.181	14.17										0.4156
1.812	15.75										0.4144
1.444	17.82										0.4184
1,575	18,90										0.4122
1.706											0.4112
1.969	23.62			0.490	0.476	0.466	0.451	0.441	0.427	0.421	0,4092

A comparison of the results of this formula with those of experiments, says M. Bazin, justifies us in believing that, except in the unusual case of a very low weir (which should always be avoided), the preceding table will give the coefficient m in all cases within 1%; provided, however, that the arrangements of the standard weir are exactly reproduced. It is especially important that the admission of the air behind the falling sheet be perfectly assured. If this condition is not complied with, m may vary within much wider limits. The type adopted gives the least possible variation in the coefficient.

WATER-POWER.

Power of a Fall of Water-Efficiency.—The gross power of a fall of water is the product of the weight of water discharged in a unit of time into the total head, i.e., the difference of vertical elevation of the upper surface of the water at the points where the fall in question begins and ends. The term "head" used in connection with water-wheels is the difference in height from the surface of the water in the wheel-pit to the surface in the pen-stock when the wheel is running.

If Q = cubic feet of water discharged per second, D = weight of a cubis foot of water = 62.36 lbs. at 60° F., <math>H = total head in feet; then

DQH = gross power in foot-pounds per second, and DQH + 550 = .1134QH = gross horse-power. If Q' is taken in cubic feet per minute, H. P. = $\frac{Q'H \times 62.86}{33.000}$ = .00189Q'H.

A water-wheel or motor of any kind cannot utilize the whole of the head H, since there are losses of head at both the entrance to and the exit from the wheel. There are also losses of energy due to friction of the water in its passage through the wheel. The ratio of the power developed by the wheel to the gross power of the fall is the efficiency of the wheel. For TS afficiency, not horse-power = .00142Q'H = Q'H.

A head of water can be made use of in one or other of the following ways

1st. By its weight, as in the water-balance and overshot-wheel,

2d. By its pressure, as in turbines and in the hydraulic engine, hydraulic press, crane, etc.
3d. By its impulse, as in the undershot-wheel, and in the Pelton wheel.
4th. By a combination of the above.

Horse-power of a Hunning Stream.—The gross horse-power is, H. P. = $QH \times 62.36 + 550 = .1134QH$, in which Q is the discharge in cubic feet per second actually impinging on the float or bucket, and H = theoret-T S 772 ical head due to the velocity of the stream = $\frac{v}{2a} = \frac{v}{64.4}$, in which v is the velocity in feet per second. If Q' be taken in cubic feet per minute, H.P.=.00189Q'H.

Thus, if the floats of an undershot-wheel driven by a current alone be 5

Thus, it the scars of an undersnot-wheel criven by a current sione be feet \times 1 foot, and the velocity of stream = 210 ft. per minute, or 3½ ft. per sec., of which the theoretical head is .19 ft., Q = 5 sq. ft. \times 210 = 1050 cu. ft, per minute; H = .19 ft.; $H. P. = 1060 \times .19 \times .00189 = .377$ H. P. The wheels would realize only about .4 of this power, on account of friction and slip, or .161 H. P., or about .08 H. T. per square foot of float, which is equivalent to 38 sq. ft. of float per H. P.

Ourrent Motors.—A current motor could only utilize the whole power of a running stream if it could take all the relocity out of the water, so that it would leave the floats or buckets with no velocity at all; or in other words, it would require the backing up of the whole volume of the stream until the actual head was equivalent to the theoretical head due to the velocity of the stream. As but a small fraction of the velocity of the stream can be taken up by a current motor, its efficiency is very small. Current motors may be used to obtain small amounts of power from large streams, but for large powers they are not practicable.

Horse-power of Water Flowing in a Tube. - The head due to the velocity is $\frac{v^3}{2a}$ the head due to the pressure is 2; the head due to actual height above the distum plane is a feet. The total head is the sum of these = $+\lambda + \frac{f}{2}$, in feet, in which v =velocity in feet per second, f =pressure in lbs. per sq. ft., w = weight of 1 cu. ft. of water = 62.36 lbs. If <math>p = pressure in Bs. per sq. in., $\frac{f}{sn} = 2.309p$. In hydraulic transmission the velocity and the height above datum are usually small compared with the pressurehead. The work or energy of a given quantity of water under pressure = its volume in cubic feet \times its pressure in lbs. per sq. ft.; or if Q = quantity in cubic feet per second, and p = pressure in lbs. per square inch, W =144pQ, and the H. P. = $\frac{144pQ}{140}$ = .2618pQ.

Maximum Efficiency of a Long Conduit.—A. L. Adams and B.C. (emmeli (Eng's News, May 4, 1898), show by mathematical analysis that the conditions for securing the maximum amount of power through a long conduit of fixed diameter, without regard to the economy of water, is that

the spiper fall when the head there is 20 feet, or a quantity proportionate to the height at the falls. This is equal to 86.2 horse-power as a maximum.

Lowell, Mass.—The right to draw during 15 hours in the day so much water

as shall give a power equal to 25 cn. ft, a second at the great fall, when the fall there is 30 feet. Equal to 85 H. P. maximum.

Lawrence, Mass.-The right to draw during 16 hours in a day so much water as shall give a power equal to 30 cu. ft. per second when the head is 25 feet. Equal to 85 H.P. maximum.

Minneapolis, Minn.—30 cu. ft. of water per second with head of 22 feet.

Equal to 74.8 H.P.

Manchester, N. H.—Divide 725 by the number of feet of fall minus 1, and

the quotient will be the number of cubic feet per second in that fall. For 90 feet fall this equals 38.1 cu. ft., equal to 86.4 H. P. maximum.

Cohoes, N. Y.—" Mill-power" equivalent to the power given by 8 cu. ft. per second, when the fall is 20 feet. Equal to 13.6 H. P., maximum.

Passaic, N. J.—Mill-power: The right to draw 814 cu. ft. of water per sec.,

fall of 22 feet, equal to 21.2 horse power. Maximum rental \$700 per year for each mill-power = \$33.00 per H. P.

The horse-power maximum above given is that due theoretically to the weight of water and the height of the fall, assuming the water-wheel to have perfect efficiency. It should be multiplied by the efficiency of the wheel, say 75% for good turbines, to obtain the H. P. delivered by the wheel,

Value of a Water-power.—In estimating the value of a waterpower, especially where such value is used as testimony for a plaintiff whose water-power has been diminished or confiscated, it is a common custom for the person making such estimate to say that the value is represented by a sum of money which, when put at interest, would mainten a steam-plant of the same power in the same place.

Mr. Charles T. Main (Trans. A. S. M. E. xiii, 140) points out that this system of estimating is erroneous; that the value of a power depends upon a great number of conditions, such as location, quantity of water, fall or head, uniformity of flow, conditions which fix the expense of dams, canals, foundations of buildings, freight charges for fuel, raw materials and finished prod-He gives an estimate of relative cost of steam and water-power

for a 500 H. P. plant from which the following is condensed:
The amount of heat required per H. P. varies with different kinds of business, but in an average plain cotton-mill, the steam required for heating and slashing is equivalent to about 25% of steam exhausted from the highpressure cylinder of a compound engine of the power required to run that

mill, the steam to be taken from the receiver.

The coal consumption per H. P. per hour for a compound engine is taken at 134 lbs, per hour, when no steam is taken from the receiver for heating purposes. The gross consumption when 25% is taken from the receiver is about 2.06 lbs.

```
75% of the steam is used as in a compound engine at 1.75 lbs. = 1.31 lbs. 25% " high-pressure " 8.00 lbs. = .75 "
                                                                              8.00 lbs. = .75 "
```

2.06 "

The running expenses per H. P. per year are as follows;
2.06 lbs. coal per hour = 21.115 lbs. for 10½ hours or one day = 6508.42 lbs. for 808 days, which, at \$8.00 per long ton = Attendance of boilers, one man @ \$2.00, and one man @ \$1.25 =

Oil, waste, and supplies. The cost of such a steam-plant in New England and vicinity of 500 H. P. is about \$65 per H. P. Taking the fixed expenses as 4% on engine, 5% on boilers, and 2% on other portions, repairs at 2%, interest at 5%, taxes at 14% on 3% cost, an insurance at 3% on exposed portion, the total average per cent is about 121/55, or \$65 × .121/6 =

8 13

Gross cost of power and low-pressure steam per H. P. \$21 80

Comparing this with water-power, Mr. Main says: "At Lawrence the cost of dam and canals was about \$650,000, or \$65 per H. P. The cost per H. P. of wheel-plant from canal to river is about \$45 per H. P. of plant, or about \$65 per H. P. used, the additional \$20 being caused by making the plant large enough to compensate for fluctuation of power due to rise and fall of river. The total cost per H. P. of developed plant is then about \$190 per H. P. Placing the depreciation on the whole plant at 2%, repairs at 1%, innerest at 5%, taxes and issurance at 1%, or a total of 9%, gives:

> Fixed expenses per H. P. $$180 \times .09 = 1170 Running (Estimated)

"To this has to be added the amount of steam required for heating purposes, said to be about 23% of the total amount used, but in winter months the consumption is at least 371/4%. It is therefore necessary to have a boiler plant of about 371/4% of the size of the one considered with the steam-plant, costing about \$20 × .375 = \$7.50 per H. P. of total power used. The expense of running this boiler-plant is, per H. P. of the the total plant per year;

Fixed expenses 121/4% on \$7.50	\$0.94 8.26
Labor	1.28

Total \$5.48

Making a total cost per year for water-power, with the auxiliary boiler plant \$13.70+\$5.43 = \$19.13 which deducted from \$21.80 make a difference in favor of water-power of \$2.67, or for 10,000 H. P. a saving of \$26,700 per

"It is fair to say," says Mr. Main," that the value of this constant power is a sum of money which when put at interest will produce the saving; or if 6% is a fair interest to receive on money thus invested the value would be

\$26,700 -- .06 = \$445,000."

Mr. Main makes the following general statements as to the value of a water-power: "The value of an undeveloped variable power is usually nothing if its variation is great, unless it is to be supplemented by a steam-plant. It is of value then only when the cost per horse-power for the double plant is less than the cost of steam-power under the same conditions as mentioned for a permanent power, and its value can be represented in the same manner as the value of a permanent power has been represented.

"The value of a permanent power has been represented."

"The value of a developed power is as follows: If the power can be run cheaper than steam, the value is that of the power, plus the cost of plant, less depreciation. If it cannot be run as cheaply as steam, considering its cost, etc., the value of the power itself is nothing, but the value of the plant is such as could be paid for it new, which would bring the total cost of run-

ming down to the cost of steam-power, less depreciation."

Mr. Samuel Webber, Iron Age, Feb. and March, 1993, writes a series of articles showing the development of American turbine wheels, and incidentally criticises the statements of Mr. Main and others who have made comparisons of costs of steam and of water-power unfavorable to the latter. Hesays: "They have based their calculations on the cost of steam, on large compound engines of 1000 or more H. P. and 120 pounds pressure of steam in their boilers, and by careful 10-hour trials succeeded in figuring down steam to a cost of about \$20 per H. P., ignoring the well-known fact that its average cost in practical use, except near the coal mines, is from \$40 to \$50. In many instances dams, canals, and modern turbines can be all completed for a cost of \$100 per H. P.; and the interest on that, and the cost of attendance and oil, will bring water-power up to but about \$10 or \$12 per annum; and with a man competent to attend the dynamo in attendance, it can probably be safely estimated at not over \$15 per H. P."

TURBINE WHEELS.

Proportions of Turbines.-Prof. De Volson Wood discusses at length the theory of turbines in his paper on Hydraulic Reaction Motors, Trans. A. S. M. E. xiv. 266. His principal deductions which have an immediate bearing upon practice are condensed in the following:

Q = volume of water passing through the wheel per second.

 h_1 = head in the supply chamber above the entrance to the buckets, h_2 = head in the tail-race above the exit from the buckets,

 $x_1 = \text{fall}$ in passing through the buckets, $H = h_1 + x_1 - h_0$, the effective head, $\mu_1 = \text{coefficient of resistance along the guides,}$

 μ_2 = coefficient of resistance along the buckets.

 $r_1 = \text{radius of the initial rim.}$

 $r_0^* = \text{radius of the terminal rim},$ V = velocity of the water issuing from supply chamber,

v, = initial velocity of the water in the bucket in reference to the bucket,

ve = terminal velocity in the bucket,

= angular velocity of the wheel,

 γ_1 = angle between the initial element of bucket and initial rim = EAD, γ_2 = GFI, the angle between the terminal rim and terminal element of the bucket.

a = cb. Fig. 188 = the arc subtending one gate opening

 $a_1 =$ the arc subtending one bucket at entrance. (In practice a_1 is larger than a,)

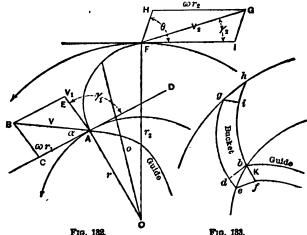
 $a_1 = gh$, the arc subtending one bucket at exit, K = bf, normal section of passage, it being assumed that the passages and buckets are very narrow.

 $k_1 = bd$, initial normal section of bucket.

 $k_3 = gi$, terminal normal section, $wr_1 = \text{velocity of initial rim}$,

 $wr_s = \text{velocity of terminal rim,}$ $\theta = HFI$, angle between the terminal rim and actual direction of the water at exit, $Y = \text{depth of } K_1, y$, of a_1 , and y_2 of K_2 , then

 $K = Ya \sin a$; $K_1 = y_1 a_1 \sin y_1$; $K_2 = y_2 a_2 \sin y_2$



Three simple systems are recognized, $r_1 < r_2$, called outward flow; $r_1 > r_2$, called inward flow; $r_1 = r_2$, called parallel flow. The first and second may be combined with the third, making a mixed system.

Value of γ_2 (the quitting angle).—The efficiency is increased as γ_2 decreases, and is greatest for $\gamma_2 = 0$. Hence, theoretically, the terminal element of the bucket should be tangent to the quitting rim for best efficiency. This, however, for the discharge of a finite quantity of water, would require an infinite depth of bucket. In practice, therefore, this angle must have a finite value. The larger the diameter of the terminal rim the smaller may be this angle for a given death of wheel and given quantity of water may be this angle for a given depth of wheel and given quantity of water

discharged. In practice γ_1 is from 10° to 20°. In a wheel in which all the elements except γ_2 are fixed, the velocity of the wheel for best effect must increase as the quitting angle of the bucket

lecreases.

Values of $a + \gamma_1$ must be less than 180°, but the best relation cannot be determined by analysis. However, since the water should be deflected from its course as much as possible from its entering to its leaving the wheel, the angle a for this reason should be as small as practicable.

In practice, a cannot be zero, and is made from 20° to 30°.

The value $r_1 = 1.4r_2$ makes the width of the crown for internal flow about the same as for $r_1 = r_2 \sqrt{\frac{1}{16}}$ for outward flow, being approximately 0.8 of the external radius.

Values of μ_1 and μ_2 .—The frictional resistances depend upon the construction of the wheel as to smoothness of the surfaces, sharpness of the angles, regularity of the curved parts, and also upon the speed it is run. These values cannot be definitely assigned beforehand, but Weisbach gives for good conditions $\mu_1 = \mu_2 = 0.05$ to 0.10. They are not necessarily equal, and μ_1 may be from 0.05 to 0.075, and μ_2 from 0.05 to 0.10 or even larger.

Values of γ_1 must be less than $180^{\circ} - a$. To be on the safe side, γ_1 may be 20 or 30 degrees less than $180^{\circ}-2a$, giving

$$\gamma_1 = 180^{\circ} - 2a - 25$$
 (say) = 155 - 2a.

Then if $a = 30^\circ$, $\gamma_1 = 95^\circ$. Some designers make γ_1 90°; others more, and still others less, than that amount. Weisbach suggests that it be less, so that the bucket will be shorter and friction less. This reasoning appears to be correct for the inflow wheel, but not for the outflow wheel. In the Tremont turbines, described in the Lowell Hydraulic Experiments, this angle is 90°, the angle a 20°, and γ_2 10°, which proportions insured a positive pressure in the wheel. Fourneyron made $\gamma_1 = 90^\circ$, and a from 30° to 33°, which values made the initial pressure in the wheel near zero.

Form of Bucket.—The form of the bucket cannot be determined analytically. From the initial and terminal directions and the volume of the water flowing through the wheel, the area of the normal sections may be found. The normal section of the buckets will be:

$$K=\frac{Q}{V}\;;\;\;k_1=\frac{Q}{v_1}\;;\;\;k_2=\frac{Q}{v_2}\;.$$

The depths of those sections will be:

$$Y = \frac{R}{a \sin a}; \quad v_1 = \frac{k_1}{a_1 \sin \gamma_1}; \quad v_2 = \frac{k_2}{a_2 \sin \gamma_2};$$

The changes of curvature and section must be gradual, and the general form regular, so that eddies and whirls shall not be formed. For the same reason the wheel must be run with the correct velocity to secure the best affect. In practice the buckets are made of two or three arcs of circles, mutually tangential.

The Value of w.—So far as analysis indicates, the wheel may run at any speed; but in order that the stream shall flow smoothly from the supply chamber into the bucket, the velocity V should be properly regulated. If $\mu_1 = \mu_2 = 0.10$, $r_2 + r_2 = 1.40$, $\alpha = 25^\circ$, $\gamma_1 = 90^\circ$, $\gamma_2 = 12^\circ$, the velocity of the *initial* rim for outward flow will be for maximum efficiency 0.614 of the

velocity due to the head, or $\omega r_1 = 0.614 \sqrt{2gH}$.

The velocity due to the head would be $\sqrt{2gH} = 1.414 \sqrt{gH}$. For an inflow wheel for the case in which $r_1^2 = 2r_2^2$, and the other dimen sions as given above, $\omega r_1 = 0.682 \sqrt{2gH}$. The highest efficiency of the Tremont turbine, found experimentally, was

9.78375, and the corresponding velocity, 0.82645 of that due to the head, and for all velocities above and below this value the efficiency was less. In the Tremont wheel $\alpha=20^{\circ}$ instead of 25° , and $\gamma_0=10^{\circ}$ instead of 13° . These would make the theoretical efficiency and velocity of the wheel some

what greater. Experiment showed that the velocity might be considerably larger or smaller than this amount without much diminution of the efficiency.

It was found that if the velocity of the initial (or interior) rim was not less than 44% nor more than 75% of that due to the fall, the efficiency was 75% or more. This wheel was allowed to run freely without any brake except its own friction, and the velocity of the initial rim was observed to be 1.335 $\sqrt{2gH}$, half of which is 0.6675 $\sqrt{2gH}$, which is not far from the velocity giving maximum effect; that is to say, when the gate is fully raised the coefficient of effect is a maximum when the wheel is moving with about half its

maximum velocity.

Number of Buckets.—Successful wheels have been made in which the distance between the buckets was as small as 0.75 of an inch, and others as tance between the buckets was as small as 0.10 of an incl., and others as much as 2.75 inches. Turbines at the Centranial Exposition had buckets from 4½ inches to 9 inches from centre to centre. If too large they will not work properly. Neither should they be too deep. Horizontal partitions are sometimes introduced. These secure more efficient working in case the gates are only partly opened. The form and number of buckets for commercial purposes are chiefly the result of experience. Ratio of Radif.-Theory does not limit the dimensions of the wheel. In

for outward flow, $r_3 + r_3$ is from 1.25 to 1.50; for inward flow, $r_3 + r_1$ is from 0.66 to 0.80.

It appears that the inflow-wheel has a higher efficiency than the outwardflow wheel. The inflow-wheel also runs somewhat slower for best effect. The centrifugal force in the outward-flow wheel tends to force the water outward faster than it would otherwise flow; while in the inward-flow wheel it has the contrary effect, acting as it does in opposition to the velocity in the buckets.

It also appears that the efficiency of the outward-flow wheel increases slightly as the width of the crown is less and the velocity for maximum efficiency is slower; while for the inflow-wheel the efficiency slightly increases for increased width of crown, and the velocity of the outer rim at the same time also increases.

Efficiency.—The exact value of the efficiency for a particular wheel must

be found by experiment.

It seems hardly possible for the effective efficiency to equal, much less exceed, 80%, and all claims of 90 or more per cent for these motors should be

exceed, 8%, and all claims of 90 or more per cent for these motors should be discarded as improbable. A turbine yielding from 75% to 80% is extremely good. Experiments with higher efficiencies have been reported. The celebrated Tremont turbine gave 79½% without the "diffuser," which might have added some 3%. A Jonval turbine (parallel flow) was reported as yielding 0.75 to 0.90, but Morin suggested corrections reducing it to 0.63 to 0.71. Weisbach gives the results of many experiments, in which the efficiency ranged from 50% to 84%. Numerous experiments give E=0.00 to 0.65. The efficiency, considering only the energy imparted to the wheel, will exceed by several per cent the efficiency of the wheel, for the latter will include the friction of the support and leakage at the joint between the sluice and wheel, which are not included in the former; also as a plant the resistances and losses in the supply-chamber are to be still further deducted.

ances and losses in the supply-chamber are to be still further deducted.

The Croums.—The crowns may be plane annular disks, or conical, or curved. If the partitions forming the buckets be so thin that they may be discarded, the law of radial flow will be determined by the form of the crowns. If the crowns be plane, the radial flow (or radial component) will diminish, for the outward flow-wheel, as the distance from the axis increases

-the buckets being full-for the angular space will be greater.

Prof. Wood deduces from the formulæ in his paper the tables on page 595, It appears from these tables: 1. That the terminal angle, a, has frequently

the appears from theses: 1. That the terminal angle, a, has frequently been made too large in practice for the best efficiency.

2. That the terminal angle, a, of the guide should be for the inflow less than 10° for the wheels here considered, but when the initial angle of the bucket is 90°, and the terminal angle of the guide is 5° 28′, the gain of efficiency is not 2% greater than when the latter is 25°.

3. That the initial angle of the bucket should exceed 90° for best effect for

outflow-wheels.

4. That with the initial angle between 60° and 120° for best effect on inflow

wheels the efficiency varies scarcely 1%.

5. In the outflow-wheel, column (9) shows that for the outflow for best effect the direction of the quitting water in reference to the earth should be nearly radial (from 76° to 97°), but for the inflow wheel the water is thrown forward in quitting. This shows that the velocity of the rim should somewhat exceed the relative final velocity backward in the bucket, as shown in columns (4) and (5).

6. In these tables the velocities given are in terms of $\sqrt{2gh}$, and the coefficients of this expression will be the part of the head which would produce that velocity if the water issued freely. There is only one case, column (5), where the coefficient exceeds unity, and the excess is so small it may be discarded; and it may be said that in a properly proportioned turbine with the conditions here given none of the velocities will equal that due to the head in the supply-chamber when running at best effect.

7. The inflow turbine presents the best conditions for construction for producing a given effect, the only apparent disadvantage being an increased first cost due to an increased depth, or an increased diameter for producing a given amount of work. The larger efficiency should, however, more than

neutralize the increased first cost,

Outward-flow Turbine.

F1 = F2 VF.	*	μ,	$\mu_1 = \mu_2 = 0.10.$	$\gamma_2=12^a.$		Parallel Crowns.	2	$v_1 = v_2$	$k_1v_1=k_2v_2=KV=Q=1.$	Q = 1.
Initial Angle.	Efficiency.	Velocity Outer Rim. r _a a'	Velocity Inner Bim. $r_1\omega'=V^{\frac{1}{4}}r_2\omega'$	Relative Velocity of Exit.	Relative Veloc. Relative Veloc. From supplyity of Exit. ity of Extrance. Chamber. v_3	Velocity of Exit from supply- Chamber, \overline{P}	Terminal nail tangle of Guide.	Direction of quitting Water.	Head Equivalent of Energy in quitting Water.	K, VOH
-	æ	80	4	20	80	2	æ	٥	10	=
99 95 55	0.804 0.828 0.839 0.921	0.872 \PsqH 0.874 \PsqH 0.798 \PsqH 0.709 \PsqH	0.687 \\ \square\ 29H \\ 0.619 \\ \square\ 29H \\ 0.565 \\ \square\ 29H \\ 0.501 \\ \square\ 29H \\ \qquare\ \qqqqqqqqqqqqqqqqqqqqqqqqqqqqqqqqqqq	1.048 \\ \sqrt{2gH} \\ 0.931 \\ \sqrt{2gH} \\ 0.931 \\ \sqrt{2gH} \\ 0.843 \\ \sqrt{2gH} \\ 0.707 \\ \sqrt{2gH} \\	0.856 \\ \sqrt{29H} \) 0.274 \\ \sqrt{29H} \) 0.278 \\ \sqrt{29H} \) 0.286 \\ \sqrt{29H} \) 0.416 \\ \sqrt{29H} \)	0.595 \\ \sqrt{2gH} \\ 0.676 \sqrt{2gH} \\ 0.749 \sqrt{2gH} \\ 0.749 \sqrt{2gH} \\ 0.886 \sqrt{2gH} \\	31° 17′ 23° 56′ 19° 5′ 18° 31′	36. 82. 87.	0.061H 0.089H 0.081H 0.022H	0.67 0.78 0.84 1.00

Inward-flow Turbine.

r1 = 4/2r2.	V2r2.	111	$\mu_1 = \mu_2 = 0.10.$	$\gamma_{1} = 12^{\circ}$.	Paral	Parallel Crowns.	28	v1 = kg	$k_1 v_1 = k_2 v_2 = KV = Q = 1.$	0=1.
- 5	Ä	Velocity Outer Rim. τ ₁ ω'	Velocity Inner Rim. ''zw'	•a	ta.	4	8	•	802 803	k, VOB
% % % % % % % % % % % % % % % % % % %	0.920 0.920 0.919 0.918	0.709 \\ \square\ 0.688 \square\ \text{V20H} \\ 0.668 \square\ \square\ \text{V20H} \\ 0.684 \square\ \square\ \text{V20H} \\ 0.684 \square\ \end{array}	0.501 \(\frac{\kappa_{2gH}}{\kappa_{2gH}}\) 0.487 \(\frac{\kappa_{2gH}}{\kappa_{2gH}}\) 0.448 \(\kappa_{2gH}\)	0.476 \(\frac{\kappa_{2gH}}{\kappa_{2gH}}\) 0.476 \(\frac{\kappa_{2gH}}{\kappa_{2gH}}\) 0.429 \(\frac{\kappa_{2gH}}{\kappa_{2gH}}\)	0.089 \\ \sqrt{2gH} \\ 0.089 \sqrt{2gH} \\ 0.089 \sqrt{2gH} \\ 0.077 \sqrt{2gH} \\ 0.126 \sqrt{2gH} \\	0.672 \\ \sqrt{29H} \\ 0.691 \\ \sqrt{29H} \\ 0.709 \\ \sqrt{20H} \\ 0.709 \\ \sqrt{29H} \\ 0.713 \\ \sqrt{29H} \\ 0.714 \\ \sqrt{29H} \\ \sqr	5 - 5 0 8 - 4 6 8 08 8 08	110° 100° 105°	0.010H 0.010H 0.010H 0.010H	1.48 1.50 1.55 1.65

Tests of Turbines. - Emerson says that in testing turbines it is a rare thing to find two of the same size which can be made to do their best at the same speed. The best speed of one of the leading wheels is invariably wide from the tabled rate. It was found that a 54-in. Leffel wheel under 12 ft. head gave much better results at 78 revolutions per minute than at 90.

Overshot wheels have been known to give 75% efficiency, but the average

performance is not over 60%.

A fair average for a good turbine wheel may be taken at 75%. In tests of 18 wheels made at the Philadelphia Water-works in 1859 and 1860, one wheel gave less than 50% efficiency, two between 50% and 60%, six between 60% and 70%, seven between 71% and 77%, two 82%, and one 87.77%. (Emerson.)

Tests of Turbine Wheels at the Centennial Exhibition, 1876. (From a paper by R. H. Thurston on The Systematic Testing of Turbine Wheels in the United States, Trans. A. S. M. E., viii. 359.)—In 1876 the judges at the International Exhibition conducted a series of trials of turbines. Many of the wheels offered for tests were found to be more or less defective in fitting and workmanship. The following is a statement of the results of all turbines entered which gave an efficiency of over 75%. Seven other wheels were tested, giving results between 65% and 75%.

Maker's Name, or Name the Wheel is Known By.	Per Cent at Full Gate or Dis- charge.	Per Cent at about 9/10 of Full Discharge.	Per Cent at about % of Full Discharge.	Per Cent at about % of Full Discharge.	Per Cent at about % of Full Discharge.	Per Cent at about 1/4 of Full Discharge.	Per Cent at about 4/10 of Full Dis- charge.
Risdon	87.68		86.20	82.41		75.85	,
NationalGeyelin (single)	88.79 88.80	•••••	••••	70.79	•••••	•••••	•••••
Thos. Tait	82.18			70.40	66.85		55.00
Goldie & McCullough	81.21		71.01	55.90			
Rodney Hunt Mach. Co	78.70	71.66		68.60	51.08	22.32	
Tyler Wheel	79.59		81.24	79.92	67,23	69.59	
Geyelin (duplex)	77.57	***		• • • • • • •			
Knowlton & Dolan	77.48	74.25	***	• • • • • •	62.75	•••••	
E. T. Cope & Sons	76.94	78.83	69.92		~~ ~~	71.74	••••
Barber & Harris	76.16 75.70	10.00	67.08	67.57	70.87 62.06	71.74	••••
York Manufacturing Co W. F. Mosser & Co	75.15	74.89	71.90	70.52	U.S.UO	66.04	•••••
W. F. MUSSET & CU	(0.10)	12,00	111.80	10.02		00.02	

The limits of error of the tests, says Prof. Thurston, were very uncertain; they are undoubtedly considerable as compared with the later work done in

they are undoubtedly considerable as compared with the later work done in the permanent flume at Holyoke—possibly as much as 4% or 5%.

Experiments with "draught-subes," or "suction-tubes," which were actually "diffusers" in their effect, so far as Prof. Thurston has analyzed them, indicate the loss by friction which should be anticipated in such cases, this loss decreasing as the tube increased in size, and increasing as its diameter approached that of the wheel—the minimum diameter tried. It was sometimes found very difficult to free the tube from air completely, and next to impossible, during the interval, to control the speed with the brokes. Every trips were often negariary before the rower due to the full brake. Several trials were often necessary before the power due to the full head could be obtained. The loss of power by gearing and by belting was variable with the proportions and arrangement of the gears and pulleys, length of belt, etc., but averaged not far from 30% for a single pair of bevelegears, uncut and dry, but smooth for such gearing, and but 10% for the same gears, well lubricated, after they had been a short time in operation. The amount of power transmitted was, however, small, and these figures are probably much higher than those representing ordinary practice. Intro-ducing a second pair—spur-gears—the best figures were but little changed, although the difference between the case in which the larger gear was the driver, and the case in which the small wheel was the driver, was perceivable, and was in favor of the former arrangement. A single straight belt gave a loss of but 2% or 3%, a crossed belt 5% to 8%, when transmitting 14

horse-power with maximum tightness and transmitting power. A "quarter turn" wasted about 10% as a maximum, and a "quarter twist" about 5%.

Dimensions of Turbines.—For dimensions, power, etc., of standard makes of turbines consult the catalogues of different manufacturers. The wheels of different makers vary greatly in their proportions for any given capacity.

The Pelton Water-wheel.—Mr. Ross E. Browne (Eng'g News, Feb. 20, 1892) thus outlines the principles upon which this water-wheel is

constructed:

The function of a water-wheel, operated by a jet of water escaping from a nozzle, is to convert the energy of the jet, due to its velocity, into useful work. In order to utilize this energy fully the wheel-bucket, after catching the jet, must bring it to rest before discharging it, without inducing turbu-

lence or agitation of the particles.

This cannot be fully effected, and unavoidable difficulties necessitate the loss of a portion of the energy. The principal losses occur as follows: First, in sharp or angular diversion of the jet in entering, or in its course through the bucket, causing impact, or the conversion of a portion of the energy into heat instead of useful work. Second, in the so-called frictional resistance offered to the motion of the water by the wetted surfaces of the buckets, causing also the conversion of a portion of the energy into heat instead of useful work. Third, in the velocity of the water, as it leaves the bucket, representing energy which has not been converted into work. Hence, in seeking a high efficiency: 1. The bucket-surface at the entrance

the bucket should be curved in such

a manner as to avoid sharp angular denection of the stream. If, for example, a jet strikes a surface at an angle and is sharply deflected, a portion of the water is backed, the smoothness of the stream is disturbed, and there results considerable loss by impact and otherwise. The entrance and deflection in the Pelton bucket are such as to avoid





Fig. 184.

Fig. 185.

these losses in the main. (See Fig. 136.)

2. The number of buckets should be small, and the path of the jet in the bucket short; in other words, the total wetted surface should be small, as

bucket short; in other words, the total wetted surface should be small, as the loss by friction will be proportional to this.

8. The discharge end of the bucket should be as nearly tangential to the wheel periphery as compatible with the clearance of the bucket which follows; and great differences of velocity in the parts of the escaping water should be avoided. In order to bring the water to rest at the discharge end of the bucket, it is shown, mathematically, that the velocity of the bucket

should be one half the velocity of the jet.

A bucket, such as shown in Fig. 185, will cause the heaping of more or less dead or turbulent water at the point indicated by dark



shading. This dead water is subsequently thrown from the wheel with considerable velocity, and represents a large loss of energy. The introduction of the wedge in the Pelton bucket (see Fig. 184) is an efficient means of avoiding this loss.

A wheel of the form of the Pelton conforms closely in construction to each of these requirements.

In a te. - made by the proprietors of the Idaho mine, near Grass Valley, Cal., the dimensions and results were as foll :s: Main supply-pipe, 22 in. diameter, 6900 ft. long, with a head of 38614 feet above centre of nozzle. The loss by friction in the pipe was 1.8 ft., reducing the effective head to 384.7 ft. The Pelton wheel used in the 1.8t was 6 ft. in diameter and the nozzle was 1.89 in. diameter. The work done was measured by a Prony brake, and the mean of 12 test showed a profile different of 27 ft. of 13 tests showed a useful effect of 87.8%.

The Petton wheel is also used as a motor for small powers. A test by M. E. Cooley of a 12-inch wheel, with a 34-inch nozzle, under 100 lbs. pressure, gave 1.9 horse-power. The theoretical discharge was .0935 cubic feet per second, and the cheoretical horse-power 2.45; the efficiency being 90 per cent. Two other types of water-motor tested at the same time each gave

efficiencies of 55 per cent.

Polton Water-wheel Tables, (Abridged.)

The smaller figures under those denoting the various heads give the spouting velocity of the water in feet per minute. The cubic-feet measurement is also based on the flow per minute.

Head	Size of	6	12	18	18	24			5	6
in ft.	Wheels.	im	in. No. 2	in.	in. No. 4	in. No. 5	ft.	ñ	ft.	ft.
20	Horse-power.	.05 1.67	.12	.20 6.62	.37	.66 20.53	1 5%	2.64 83.32		6.00
2151 97	Revolutions	684	342	228	228	171	114		70	
20	Horse-power.	.10 2.05	4.79	. 38 8.11	.69 14.76	1.22 25.51	2.76 57.44	4.88 102.04	7.69 159.66	11.04 239.75
2626.62	Revolutions	837	418	279	279	209	139	104	83	69
40	Horse-power. Cubic lest,	.15 2.37	.35 5.53	.59 9.37	1.06 16.59		4.24 66.36	7.58 107.84	11.85 184.36	16.96 265.44
3043.30	Revolutions	969	484	323	323	242	161	121	96	80
50	Horne-power. Cubic feet	.21 2.64	.49 6.18	.84 10.47	1.49 18.54	2.65 32.93		10.60 131.72	16.63 206.13	23.93 296.70
3402.61	Cubic feet Revolutions	1083	541	361	3 61	270	180	135	108	90
60	Horse-power. Cubic feet	.28	.65	1.10 11.47		3.48 36.08	7.84 81.25		21.77 225.80	31.36 325.00
8727.87	Revolutions	1195	592	895	895	296	197	148	118,	98
70	Horne-power. Cubic feet			1.39 12.39	2.47 21.94	4.39 38.97	9.88 87.76	17.58 155.88		39.52 851.04
4026.00	Revolutions	1281	640		127	3:20	213	160	130	106
80	Horse-power. Cubic feet		1.00 7.82	1.70 13 25	3.01 23.46	5.36 41.66	12.04 98 84	21.44 166.64	83.54 260.78	48.16 875.86
4303.99	Revolutions		684	456	456	842	228	171	187	114
90	Horse-power. Cubic feet		1.20 8.29	2.03 14.05	3.60 24.88	6.89 44.19		25.59 176.75	40.04 276.55	57.60 89 6.08
4565.01	Revolutions	1452	726	484	484	363	242	181	145	121
100	Horse-power.	.60	1.40		4.21 26.22	7.49	16.84	29.93	46.85	67.86
4812.00	Cubic feet Revolutions	1530	705	14.81 510	510	882 882	104.88 255	186.32 191	291.51 152	419.52 127
120	Horse-power.	.79	1 84	8.12		9.85	22.18	89.41	61.66	88.75
5271.80	Cubic feet Revolutions		9.57 838	16.21 559	28.72 559	419	114.91 279	204.10 209	319.33 167	459.64 139
140	Horse-power.	.99	2.88	8.94	6.99	12.41	27.96	49.64	77.71	111.85
5698.65	Cubic feet Revolutions	1812	906	601	81.08 604	458	124.12 3 02	226	844.92 181	496.48 151
160	Horse-power.	1.22	9.84	4.82	8.54	15.17	84.16	60.68	94.94	186.65
6096 74	Cubic feet Revolutions	4.78 1 98 8	969	646	88.17 646	484	828	235.68 242	868.73 198	580.75 161
180	Horse power.	1.45	8.89	5.75	10.19	18.10		72.41	118.80	163.08
6455.97	Cubic feet Revolutions	2049	11.72 1024	19.87 683	85.18 688	62.49 518	140.74 842		891.10 206	562.96 171
200	Horse-power.			6.74	11.98	21.20	47.75		182.70	191.00
6605.17	Cubic feet Revolutions			20.94 720		65.87 540	148.85 860			598.40 180
250	Horse-power. Cubic feet					29.63		118.54 294.59		266.96 663.45
7608.44	Revolutions	2418	1209	808						202

Pelton Water-wheel Tables.-Continued.

Head	Size of	6	12	18	18	24	8	4	5	6
in it.	Wheels.	in. No.1	in. No. 2	in. No. 3	in. No. 4	in. No. 5	ft.	ft.	ft.	ft,
800	Horse-pow'r			12.38 25.66	21.93 45.42		87.78 181.69		243.82 504.91	850.94 726.76
8334.62	Revolutions			884	884	663	442	831	265	22
850	Horse-pow'r Cubic feet				27.64 49.06			196.88 848.57	807.25 545.86	442.2 785.0
9002.43	Revolutions			955	955	716		858	285	28
400	Horse-pow'r Cubic feet	4.82	11.25	19.0	38.77 52.45			239.94 372.64	875.40 583.02	540.8 839.2
9624.00	Revolutions	3063	1531	1021	1021	765	510		806	25
450	Horse-pow'r Cubic feet				40.29 55.68		161.19	286.81 895.24	447.95	644.7 890.1
10207.79	Revolutions				1088	812		406	618.38 824	27
500	Horse-pow'r Cubic feet	6.74	15.78	26.66	47.20			335.84 416.62	524.66	755.2
10759.96	Revolutions	8426	1713	1142	1142	856		428	651.83 842	938.2 28
600	Horse-pow'r			• · · · ·				440.77 456.88	689.68 714.05	992.6
11786.94	Cubic feet Revolutions				1251					81
650	Horse-pow'r					124.25			777.62	
12268.24	Cubic feet Revolutions				1802			475.02 488		1069.7 82
700	Horse-pow'r			• • • • • • • • • • • • • • • • • • • •				555.46 492.95		1250.9 1110.1
12781.84	Revolutions		 :::: :	: ::::	1351	1018				38
750	Horse-pow'r							616.03		
13178. 19	Cubic feet Revolutions		∤∵∷ ∶		1399			510.25 524		
800	Horse-pow'r	1							1061.81	
13610.4 0	Cubic feet Revolutions	::			1444			526.99 542		86
900	Horse-pow'r								1267.02	
14486.00	Cubic feet Revolutions				1582				874.58 459	1258.8
1000	Horse-pow'r								1483.97	
15216.89	Cubic feet Revolutions		l:::::						921.83 484	

THE POWER OF OCEAN WAVES.

Albert W. Stahl, U. S. N. (Trans. A. S. M. E., xiii. 438), gives the following formulæ and table, based upon a theoretical discussion of wave motion: The total energy of one whole wave-length of a wave H feet high, L feet long, and one foot in breadth, the length being the distance between successive crests, and the height the vertical distance between the crest and the trough, is $E=8LH^2\left(1-4.935\frac{L^2}{L^2}\right)$ foot-pounds,

The time required for each wave to travel through a distance equal to its own length is $P = \sqrt{\frac{L}{5.123}}$ seconds, and the number of waves passing any

given point in one minute is $N = \frac{60}{P} = 60 \sqrt{\frac{5.128}{L}}$. Hence the total energy of an indefinite series of such waves, expressed in horse-power per foot of

breadth, is

 $\frac{E \times N}{83000} = .0329H^{2}L(1-4.935\frac{H^{2}}{I_{2}}).$

By substituting various values for H + L, within the limits of such values actually occurring in nature, we obtain the following table of

TOTAL ENERGY OF DEEP-SEA WAVES IN TERMS OF HORSE-POWER PER FOOT OF BREADTH.

Ratio of Length of Waves to			Ler	ngth of V	Vaves in	Feet.		
Height of Waves.	25	50	75	100	150	200	[300	400
50 40 80	.04 .06 .12	.28 .86 .64	.64 1.00 1.77	1.81 2.05 8.64	8.62 5.65 10.02	7.48 11.59 20.57	20.46 81.95 56.70	42.01 65.58 116.38
40 80 90 15 19 5	.25 .42 .98 8.30	1.44 2.83 5.53 18.68	8.96 6.97 15.24 51 48	8.13 14.31 81.29 105.68	21 79 39.43 86.22 291.20	45.08 80.94 177.00 597.78	120.70 223.06 487.75 1647.01	260.08 457.89 1001.25 3881.60

The figures are correct for trochoidal deep-sea waves only, but they give a close approximation for any nearly regular series of waves in deep water and a fair approximation for waves in shallow water.

The question of the practical utilization of the energy which exists in ocean waves divides itself into several parts:

1. The various motions of the water which may be utilized for power

2. The wave motor proper. That is, the portion of the apparatus in direct contact with the water, and receiving and transmitting the energy thereof; ogether with the mechanism for transmitting this energy to the machinery for utilizing the same.

. Regulating devices, for obtaining a uniform motion from the irregular and more or less spasmodic action of the waves, as well as for adjusting the

apparatus to the state of the tide and condition of the sea.

4. Storage arrangements for insuring a continuous and uniform output of

9. Storage arrangement for insuring a communication and uniform output of power during a calm, or when the waves are comparatively small.

The motions that may be utilized for power purposes are the following:
1. Vertical rise and fall of particles at and near the surface. 2. Horizontal to-and-fro motion of particles at and near the surface. 3. Varying slope of surface of wave. 4. Impetus of waves rolling up the beach in the form of breakers. 5. Motion of distorted verticals. All of these motions, except the last one mentioned, have at various times been proposed to be utilized for nower purposes; and the last is proposed to be used in apparatus described power purposes; and the last is proposed to be used in apparatus described by Mr. Stahl.

The motion of distorted verticals is thus defined: A set of particles, origi-

nally in the same vertical straight line when the water is at rest, does not remain in a vertical line during the passage of the wave; so that the line connecting a set of such particles, while vertical and straight in still water, becomes distorted, as well as displaced, during the passage of the wave, its upper portion moving farther and more rapidly than its lower portion.

Mr. Stahl's paper contains illustrations of several wave-motors designed upon various principles. His conclusions as to their practicability is as follows: "Possibly none of the methods described in this paper may ever prove commercially successful; indeed the problem may not be susceptible of a

commercially successful; indeed the problem may not be susceptible of a financially successful solution. My own investigations, however, so far as I have yet been able to carry them, incline me to the belief that wave-power

can and will be utilized on a paying basis."

Continuous Utilization of Tidal Power. (P. Decœur, Proc. Inst. C. E. 1890.)—In connection with the training-walls to be constructed in

the estuary of the Seine, it is proposed to construct large basins, by means of which the power available from the rise and fall of the tide could be utilized. The method proposed is to have two basins separated by a bank rising above high water, within which turbines would be placed. The upper basin would be in communication with the sea during the higher one third of the tidal range, rising, and the lower basin during the lower one third of the tidal range, falling. If H be the range in feet, the level in the upper basin would never fall below $\frac{9}{2}H$ measured from low water, and the level in the lower basin would never fall below $\frac{9}{2}H$ measured from low water, and the level in the lower basin would never rise above $\frac{3}{2}H$. The available head varies between 0.53H and 0.80H, the mean value being $\frac{3}{2}H$. If S square feet be the area of the lower basin, and the above conditions are fulfilled, a quantity 1/8SH cu. It. of water is delivered through the turbines in the space of $\frac{9}{2}H$ hours. The mean flow is, therefore, $\frac{9}{2}H + \frac{9}{2}9.900$ cu. ft. per sec., and, the mean fall being $\frac{9}{2}H$, the available gross horse-power is about 1/30S/H, where S' is measured in acress. This might be increased by about one third if a variation of level in the basins amounting to $\frac{1}{2}H$ were permitted. But to reach this end the number of turbines would have to be doubled, the mean head being reduced to $\frac{1}{2}H$, and it would be more difficult to trausmit to reach this end the number of thromes would have to be doubled, the mean head being reduced to $\frac{1}{2}H$, and it would be more difficult to transmit a constant power from the turbines. The turbine proposed is of an improved model designed to utilize a large flow with a moderate diameter. One has been designed to produce 800 horse-power, with a minimum head of b ft. 3 in. at a speed of 15 revolutions per minute, the vanes having 18 ft. internal diameter. The speed would be maintained constant by regulating sluices.

PUMPS AND PUMPING ENGINES.

Theoretical Capacity of a Pump.—Let Q' = cu. tt, per min.; G' = Amer. gals. per min. = 7.4805 Q'; d = diam. of pump in inches; l = stroke in inches; N = number of single strokes per min.

Capacity in cu. ft. per min. =
$$Q' = \frac{\pi}{4} \cdot \frac{d^3}{144} \cdot \frac{lN}{12} = .0004545Nd^3l_1^2$$

Capacity in cu. ft. per min.
$$Q' = \frac{\pi}{4} \cdot \frac{d^3}{144} \cdot \frac{lN}{12} = .0004545 N d^3 l;$$

Capacity in gals. per min. $G' = \frac{\pi}{4} \cdot \frac{N d^3 l}{231} \cdot \dots = .0084 N d^3 l;$

Diameter required for a diven capacity per min.
$$d = 46.9 \sqrt{\frac{Q'}{Nl}} = 17.15 \sqrt{\frac{G'}{Nl}}$$
.

If
$$v = \text{piston speed in feet per min.}$$
, $d = 13.54 \sqrt{\frac{Q'}{v}} = 4.95 \sqrt{\frac{G'}{v}}$

If the piston speed is 100 feet per min.:

$$Nl = 1200$$
, and $d = 1.854 \sqrt{Q'} = .495 \sqrt{G'}$; $G' = 4.08d^2$ per min.

The actual capacity will be from 60% to 95% of the theoretical, according to the tightness of the piston, valves, suction-pipe, etc.

Theoretical Horse-power required to raise Water to a eiven Height.-Horse-power =

Volume in cu. ft. per min. × pressure per sq. ft. Weight × height of lift 38,000 33,000

Q' = cu. ft. per min.; G' = gals, per min.; W = wt. in lbs.; P = pressure in lbs. per sq. ft.; p = pressure in lbs. per sq. in.; H = height of lift in ft.; W = 03.36Q'. P = 144p, p = .433H, H = 2.309p, G' = 7.4805Q'.

$$\begin{aligned} \mathbf{HP} &= \frac{Q'P}{83,000} = \frac{Q'H \times 144 \times .433}{39,000} = \frac{Q'H}{529.2} = \frac{G'H}{3958.7}; \\ \mathbf{HP} &= \frac{W'H}{88,000} = \frac{Q' \times 62.36 \times 2.300p}{33,000} = \frac{Q'p}{229.2} = \frac{G'p}{1714.5}. \end{aligned}$$

For the actual horse-power required an allowance must be made for the friction, slips, etc., of engine, pump, valves, and passages.

Depth of Suction.—Theoretically a perfect pump will draw water from a height of nearly 34 feet, or the height corresponding to a perfect vacuum (14.7 lbs. × 2.309 = 33.95 feet); but since a perfect vacuum cannot be obtained, on account of valve-leakage, air contained in the water, and the vapor of the water itself, the actual height is generally less than 30 feet. When the water is warm the height to which it can be lifted by suction decreases, on account of the increased pressure of the vapor. In pumping how water, therefore, the water must flow into the pump by gravity. The following table shows the theoretical maximum depth of suction for different temperatures, leakage not considered:

Temp. F.	Absolute Pressure of Vapor, lbs. per sq. in.	Vacuum	Max. Depth of Suction, feet.	Temp. F.	Absolute Pressure of Vapor, lbs. per sq. in.	in	Max. Depth of Suction, feet.
101.4	1	27.88	81.6	188.0	8	18.68	15.5
126.2	2	25.85	29.8	188.4	9	11.59	13.2
144.7	8	28.81	27.0	193.2	10	9.55	10.9
153.8	4	21.77	24.7	197.6	11	7.51	8.5
162.5	5	19.74	22.4	201.9	12	5.48	6.2
170.3	6	17.70	20.1	205.8	13	8.44	3.9
177.0	7	15.66	17.8	209.6	14	1.40	1.6

Amount of Water raised by a Single-acting Lift-pump.

—It is common to estimate that the quantity of water raised by a single-acting bucket-wave pump per minute is equal to the number of strokes in one direction per minute, multiplied by the volume trayersed by the piston in a single stroke, on the theory that the water rises in the pump only when the piston or bucket ascends; but the fact is that the column of water does not cease flowing when the bucket descends, but flows on continuously through the valve in the bucket, so that the discharge of the number if it is operated at a bigh speed may amount to perriv double that pump, if it is operated at a high speed, may amount to nearly double that calculated from the displacement multiplied by the number of single strokes in one direction.

Proportioning the Steam-cylinder of a Direct-acting **Pump.**—Let

A = area of steam-cylinder; a = area of pump-cylinder; d = diameter of pump-cylinder; d = diameter of pump-cylinder;

P = steam-pressure, lbs. per sq. in.; p = resistance per sq. in. on pumps; H = head = 2.309p; p = .433H;

 $E = \text{efficiency of the pump} = \frac{\text{work done in pump-cylinder}}{\text{work done by the steam-cylinder}}$

$$A = \frac{ap}{EP}; \quad a = \frac{EAP}{p}; \quad D = d\sqrt{\frac{p}{EP}}; \quad d = D\sqrt{\frac{EP}{p}}; \quad P = \frac{ap}{EA}; \quad p = \frac{EAP}{a}.$$

$$\frac{A}{a} = \frac{p}{EP} = \frac{.433H}{EP}; \quad H = 2.309EP \frac{A}{a}; \quad \text{If } E = 75\%, H = 1.732P \frac{A}{a}.$$

E is commonly taken at 0.7 to 0.8 for ordinary direct-acting pumps. For the highest class of pumping-engines it may amount to 0.9. The steam-pressure P is the mean effective pressure, according to the indicator-diagram; the water-pressure p is the mean total pressure acting on the pump plunger or piston, including the suction, as could be shown by an indicator-diagram of the water-cylinder. The pressure on the pump-piston is frequently much greater than that due to the height of the lift, on account of the friction of the valves and passages, which increases rapidly with velocity of flow.

Speed of Water through Pipes and Pump-passages. The speed of the water is commonly from 100 to 200 feet per minute. If 2 feet per minute is exceeded, the loss from friction may be considerable.

The diameter of pipe required is 4.95 velocity in feet per minute

For a velocity of 200 feet per minute, diameter = .35 × \(\frac{1}{2} \text{gallons per min.} \)

. 1

Sizes of Direct-acting Pumps.—The tables on this and the next page are selected from catalogues of manufacturers, as representing the two common types of direct-acting pump, viz., the single-cylinder and the duplex. Both types are now made by most of the leading manufacturers.

The Deane Single Boiler-feed or Pressure Pump.—Suitable for pumping clear liquids at a pressure not exceeding 150 lbs.

		Sizes.			Capa	acity	gi.	,	Si	zes of	Pipes	
	Steam- cylinder.	Water- cylinder.	of Stroke.	per Stroke.	at G Spe	iven	inches.	inches.				
Number.	cyllin	er- cylli	th of		kes.	ons.	çth in	표	'n.	aust.	ion.	Discharge
Num	Stea	Wat	Length	Gallons	Strokes	Gallons.	Length	Width	Steam.	Exhaust	Suction	Disc
0	3 31/6	2 21	5 5	.07	150 150	10 13	2916 3316	7 71/8	16	84 84	11/4 11/4	1 1
11/6	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	216	5 5 5	.10 .11	150 150 150	15 16 22	3314 3314 34	716	1/8	34343434	114	1 1
214 3 4	51/6	33	7	.25	125 125	31 42	4316	814 914 914	KKKKKKK	1	2	11/4 11/4 11/4 2 2
41 <u>6</u> 5	7	414	8 10 10	.49 .69	120 100 100	58 69 85	511/2 55 55	12 12 12	1 1	11/6	3 3 3	2 2 2
61 <u>6</u>	71/2 8 10	5 6	12 12	1.02	100 100	102 147	63 69	14 14 19	1116	11/6 11/6 11/6 11/6		21/6
8	12 14	7 8	12 12	2.00 2.61	100 100	200 261	69 69	19 21	11/6 2 2	214 212	4 5 5	5

The Deane Single Tank or Light-service Pump.—These pumps will all stand a constant working pressure of 75 lbs. on the water-cylinders.

	Sizes		ske.		acity min.	20		8	Sizes o	l Pipes	3.
cylinder.			er Stro	at G	iven eed.	inche	inches				
Steam- cylin	Water- cylinder.	Length of Stroke.	Gallons per Stroke.	Strokes.	Gallons.	Length in inches.	Width in inches.	Steam.	Exhaust.	Suction.	Discharge.
4 5 5 7 8 6 8 8 10 12 10 12 10 12 14 16 18	4 4 4 516 7 7 7 8 8 10 10 10 12 12 12 12 14 16 16 16 18 18	5 7 7 10 12 12 12 12 12 12 12 12 12 12 12 12 12	.27 .38 .791 1.46 2.00 2.61 2.61 2.61 4.08 4.08 4.08 4.08 7.5.87 8.79 12.00 15.66 15.66 15.66 26.42	130 125 125 1100 100 100 100 100 100 100 100 100 70 70 70 70 50	35 48 90 210 146 200 261 261 408 408 408 408 1096 616 840 1093 1096 1096 1321 1321	83 4514 4514 58 67 68 6814 6814 6814 95 95 95 95 95 95 115	91/2 15 15 17 201/2 17 201/2 30 201/2 30 201/2 30 281/2 281/2 281/2 281/2 40 40	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	3.1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	2335445558888888888888888888888888888888	11/4 21/4 21/4 4 4 4 4 4 5 5 8 8 8 8 8 8 8 10 10 10 12 12

Efficiency of Small Direct-acting Pumps.—Chas. E. Emery, in Reports of Judges of Philadelphia Exhibition, 1875. Group xx., says: "Experiments made with steam-pumps at the American Institute Exhibition of 1867 showed that average-sized steam-pumps do not, on the average, utilize more than 50 per cent of the indicated power in the steam-oylinders, the remainder being absorbed in the friction of the engine, but more particularly in the passage of the water through the pump. It may be safely stated that ordinary steam-pumps rarely require less than 120 pounds of steam per hour for each horse-power utilized in raising water, equivalent to a duty of only 15,000,000 foot-pounds per 100 pounds of coal. With larger steam pumps, particularly when they are proportioned for the work to be done, the duty will be materially increased."

The Worthington Duplex Pump. STANDARD SIZES FOR ORDINARY SERVICE.

linders.	plungers. lons per inger.			nute of ng with essure.	er Minute by stated Num-	r required in r pump to do same speed.	To	Short be ir	l Piper Lengt icrease increa	hs, d as
Diameter of Steam-cylinders.	Pr.	Length of Stroke.	Displacement in Gallons per Stroke of One Plunger.	Proper Strokes per Minute of One Plunger, varying with kind of work and pressure.	Gallons delivered per both Plungers at sts ber of Strokes,	Diameter of Plunger required in any single-cylinder punnp to do the same work at same speed.	Steam-pipe.	Exhaust-pipe.	Suction-pipe.	Discharge-pipe.
714 714 715 10 10 112 114 118 118 118 118 118 118 118 118 118	5677785588655000000000000000000000000000	3 4 5 6 6 6 10 10 10 10 10 10 10 10 10 10 10 10 10	.04 .10 .20 .53 .42 .51 .69 .93 .1.66 .1.6	100 to 250 100 to 200 100 to 200 100 to 150 100 to 150 75 to 125 75 8 to 20 to 40 to 40 to 80 to 100 to 170 to 100 to 170 to 180 to 1	276 4 5 5 5 6 7 6 7 6 7 6 7 6 7 6 7 6 7 6 7 6	81.34 \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	111222222222222222222222222222222222222	134 22 28 4 4 4 4 4 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6	11128 3 3 3 4 5 5 5 5 5 5 5 5 7 7 7 7 7 7 8 8 8 8 8 10 10 7 10	

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Speed of Piston.—A piston speed of 100 feet per minute is commonly assumed as correct in practice, but for short-stroke pumps this gives too high a speed of rotation, requiring too frequent a reversal of the valves. For long stroke pumps, 2 feet and upward, this speed may be considerably exceeded, if valves and passages are of ample area.

Number of Strokes required to Attain a Piston Speed from 50 to 125 Feet per Minute for Pumps having Strokes from 3 to 18 Inches in Length.

of Pis- n feet nin.			Le	ngth o	f Strol	ke in Inc	hes.			
in in	3	4	5	6	7	8	10	12	15	18
Speed ton, i per n			Numb	oer of s	Stroke	per Mir	ute.			
50	200	150	120	100	86	75	60	50	40	83
55	220	165	132	110	94	82.5	66	55	44	87
60	240	180	144	120	103	90	72	60	48	40
65	260	195	156	130	111	97.5	78	65	52	43
70	280	210	168	140	120	105	84	70	56	47
75	800	225	180	150	128	112.5	90	75	60	50
80	820	240	192	160	137	120	96	80	64	53
85	340	255	204	170	146	127.5	102	85	68	57
90	360	270	216	180	154	135	108	90	72	60
95	880	285	228	190	163	143.5	114	95	76	63
100	400	300	240	200	171	150	120	100	80	67
105	420	815	252	210	180	157.5	126	105	84 88	70
110	440	830	264	220	188	165	132	110	88	73
115	460	345	276	230	197	178.5	188	115	92	77
120	480	360	288	240	206	180	144	120	96	80
125	500	375	30 0	250	214	187.5	150	125	100	83

Piston Speed of Pumping-engines. (John Birkinbine, Trans. A. I. M. E., v. 459.)—In dealing with such a ponderous and unyielding substance as water there are many difficulties to overcome in making a pump work with a high piston speed. The attainment of moderately high speed is, however, easily accomplished. Well-proportioned pumping-engines of large capacity, provided with ample water-ways and properly constructed and the standard decomposity period by the property of SMIR. valves, are operated successfully against heavy pressures at a speed of 250 ft. per minute, without "thug," concussion, or injury to the apparatus, and there is no doubt that the speed can be still further increased.

Speed of Water through Valves.—If areas through valves and water passages are sufficient to give a velocity of 250 ft. per min. or less, they are ample. The water should be carefully guided and not too abruptly deflected. (F. W. Dean, Eng. News, Aug. 10, 1898.)

Boller-feed Pumps.—Practice has shown that 100 ft. of piston speed per minute is the limit of averaged and not too abruptly deflected.

per minute is the limit, if excessive wear and tear is to be avoided.

The velocity of water through the suction-pipe must not exceed 200 ft. per minute, else the resistance of the suction is too great.

The approximate size of suction-pipe, where the length does not exceed

25 ft. and there are not more than two elbows, may be found as follows:
7/10 of the diameter of the cylinder multiplied by 1/100 of the piston speed in feet. For duplex pumps of small size, a pipe one size larger is usually employed. The velocity of flow in the discharge-pipe should not exceed 500 ft. per minute. The volume of discharge and length of pipe vary so greatly in different installations that where the water is to be forced more than 50 ft. the size of discharge-pipe should be calculated for the particular conditions, allowing no greater velocity than 500 ft. per minute. The size of discharge-pipe is calculated in single-cylinder pumps from 250 to 400 ft. per minute. Greater velocity is permitted in the larger pipes.

In determining the proper size of pump for a steam-boiler, allowances must be made for a supply of water sufficient to cover all the demands of engines, steam-heating, etc., up to the capacity of generator, and should not be calculated simply according to the requirements of the engine. In pracbe calculated simply according to the requirements of the engine. In practice engines use all the way from 12 up to 50, or more, pounds of steam per H.P. per hour when being worked up to capacity. When an engine is overloaded or underloaded more water per H.P. will be required than wheroperating at its rated capacity. The average run of horizontal tubu'

boilers will evaporate from 2 to 3 lbs. of water per sq. ft. of heating-surface per hour, but may be driven up to 6 lbs. if the grate-surface is too large or the draught too great for economical working.

the draught too great for economical working.

Pump-Valves.—A. F. Nagle (Trans. A. S. M. E., x. 521) gives a number of designs with dimensions of double-beat or Cornish valves used in large pumping-engines, with a discussion of the theory of their proportions. The following is a summary of the proportions of the valves described.

SUMMARY OF VALVE PROPORTIONS.

Location of Engine.	Diam. of Valve in inches.	Weight in Water per square inch of Inside Un- balanced Area, in lbs.	Ratio of Seat- area to Inside Un- balanced Arca.	Pressure upon Seat per sq. in., in lbs.	Action.
Providence high-ser- vice engine	12	1 lb. reduced to .66 lb.	16%	877 lbs.	,Good
Providence Cornish- engine	16	1.28 1.86 .40	12 67 88	680 250 120	Good Some noise Some noise at
Chicago & &	25 15	1.41 1.81	75 85	151 140	Noisy
wood seats Chicago Water Wks.	15 8	1.16 .96	94 75	132 151	•

Mr. Nagle says: There is one feature in which the Cornish valves are necessarily defective, namely, the lift must always be quite large, unless great power is sacrificed to reduce it. It is undeniable that a small lift is preferable to a great one, and hence it naturally leads to the substitution of numerous small valves for one or several large ones. To what extreme reduction of size this view might safely lead must be left to the judgment of the engineer for the particular case in hand, but certainly, theoretically, we must adopt small valves. Mr. Corliss at one time carried the theory so far as to make them only 1% inches in diameter, but from 3 to 4 inches is the more common practice now. A small valve presents proportionately a larger surface of discharge with the same lift than a larger valve, so that whatever the total area of valve-seat opening, its full contents can be discharged with less lift through numerous small valves than with one large one.

Henry R. Worthington was the first to use numerous small rubber valves in preference to the larger metal valves. These valves work well under all the conditions of a city pumping-engine. A volute spring is generally used to limit the rise of the valve.

In the Leavitt high-duty sewerage-engine at Boston (Am. Machinist, May 81, 1884), the valves are of rubber, ¾-inch thick, the opening in valve-seat being 1814 × 4½ inches. The valves have iron face and back-plates, and form their own hinges.

CENTRIFUGAL PUMPS.

Belation of Height of Lift to Velocity.—The height of lift depends only on the tangential velocity of the circumference, every tangential velocity giving a constant height of lift—sometimes termed "head"—whether the pump is small or large. The quantity of water discharged is in proportion to the area of the discharging orifices at the circumference, or in proportion to the square of the diameter, when the breadth is kept the same. R. H. Buel (App. Cyc. Mech., ii, 606) gives the following:

proportion to the square of the diameter, when the breadth is kept the same. R. H. Buel (App. Cyc. Mech., ii, 606) gives the following:

Let Q represent the quantity of water, in cubic feet, to be pumped per minute, h the height of suction in feet, h' the height of discharge in feet, and d the diameter of suction-pipe, equal to the diameter of discharge-pipe, in

, g being the accelfeet; then, according to Fink, d = 0.36

eration due to gravity,

If the suction takes place on one side of the wheel, the inside diameter of the wheel is equal to 1.2d, and the outside to 2.4d. If the suction takes place at both sides of the wheel, the inside diameter of the wheel is equal to 0.85d, and the outside to 1.7d. Then the suction-pipe will have two branches, the area of each equal to half the area of d. The suction-pipe should be as short as possible, to prevent air from entering the pump. The tangential velocity of the outer edge of wheel for the delivery Q is equal to 1.25 $\sqrt{2a(h+h')}$ feet per second.

The arms are six in number, constructed as follows: Divide the central angle of 60°, which incloses the outer edges of the two arms, into any number of equal parts by drawing the radii, and divide the breadth of the wheel in the same manner by drawing concentric circles. The intersections of the several radii with the corresponding circles give points of the arm.

In experiments with Appold's pump, a velocity of circumference of 500 ft. per min. raised the water 1 ft. high, and maintained it at that level without discharging any; and double the velocity raised the water to four times the height, as the centrifugal force was proportionate to the square

The greatest height to which the water had been raised without discharge in the experiments with the 1-ft. pump, was 67.7 ft., with a velocity of 4153 ft. per min., being rather less than the calculated height, owing probably to leakage with the greater pressure. A velocity of 1128 ft. per min. raised the water 514 ft. without any discharge, and the maximum effect from the water 525 ft. without any discharge, and the maximum enect from the power employed in raising to the same height 5½ ft. was obtained at the velocity of 1678 ft. per min., giving a discharge of 1400 gals. per min. from the 1-ft. pump. The additional velocity required to effect a discharge of 1400 gals. per min., through a 1-ft. pump working at a dead level without any height of lift, is 550 ft. per min. Consequently, adding this number in each case to the velocity given above, at which no discharge takes place, the following substities conditions of the produced in lowing velocities are obtained for the maximum effect to be produced in each case:

Or, in general terms, the velocity in feet per minute for the circumference of the pump to be driven, to raise the water to a certain height, is equal to 550 + 500 1/height of lift in feet.

Lawrence Centrifugal Pumps, Class B-For Lifts from 15 to 35 ft.

No. of Pump.	Suction- pipe, in.	Discharge- pipe, in.	Economical Capacity, gals. per min.	H.P. for each foot of lift.	Weight, lbs.	No. of Pump.	Suction- pipe, in.	Discharge- pipe, in.	Economical Capacity, gals, per min.	H.P. for each foot of lift.	Weight, lbs.
1 11½ 2 3 4 5 6	11/6 21/6 31/6 41/6 6 6	1 11/2 2 3 4 5 6 8	25 70 100 250 450 700 1200 2000	.028 .05 .08 .15 .27 .36 .65	65 230 265 500 680 1032 1260 2460	10 12 15 18 24 30 36	10 12 15 18 24 30 36	10 12 15 18 24 30 36	3000 4200 7000 10000 18000 25000 85000	1.60 2.15 8.50 5.00 7.60 10.50 14.75	3000 6800 8840 10000 9000* 20000*

* Without base.

The economical capacity corresponds to a flow not exceeding 10 ft. per second in the delivery-pipe. Small pipes and high rate of flow cause a gr loss of power.

Size of Pulleys, Width of Belts, and Revolutions per Minute Necessary to Raise the Rated Quantity of Water to Different Heights with Pumps of Class B.

in,	iam. of Pulley, in.	Vidth of Pulley, in.	th of It, in.	Rated antity of ther.gals.	Hei	ght in	Fee	t an	d Re	volu	tions	er Mir	ute.	o, of Pump.
Size,	Diam. Pulle	Widt	Width	Bat Quant Water	6'	8'	10'	12'	10'	20'	25'	80'	35'	No. Pu
11/6 2 3	5	5	3	70	520	590	665	720	885	930	1045	1125	1200	136
2	6	5	4	100	475	540	605	660	765	850	955	1025	1100	2
3	716	7	6	250	435	500	560	610	705	790	890	945	1000	3
4	10	7	7	450	400	465	520	570	655	730	815	880	945	4
5	14	11	- 8	700	355	410	454	595	575	640	715	765	825	5
6	16	11	g	1200	315	365	400	440	510	570	635	685	745	6
5 6 8	20	12	10	2000	234	270	300	330	385	425	475	500	555	8
10	22	12	10	3000	234	270	300	330	385	425	475	500	555	10
12	30	14	12	4200	160	185	200	220	255	285	318	540	360	12
15	36	16	15	7000	140	165	180	198	228	255	285	305	330	15
18	40	10	15	10000	125	145	160	173	200	225	250	270	290	18
24		3.		18000	105	125	135	150	170	190	214	280	250	24
30				25000	95	106	118	130	148	165	185	204	215	30
36				35000	95	106	118	130	148	165	185	204	215	36

Efficiencies of Centrifugal and Heciprocating Pumps.— W. O. Webber (Trans. A. S. M. E., vii. 598) gives diagrams showing the relative efficiencies of centrifugal and reciprocating pumps, from which the following figures are taken for the different lifts stated:

5 10 15 20 25 30 25 40 50 60 80 100 120 160 200 240 280 Efficiency reciprocating pump: ..., 80 .46 .55 .61 .63 .68 .71 .75 .77 .82 .85 .87 .90 Efficiency centrifugal pump: .50 .56 .64 .68 .69 .68 .66 .62 .58 .50 .4089 .88 .85

The term efficiency here used indicates the value of W. H. P. + I. H. P. or horse-power of the water raised divided by the indicated horse-power of the steam-engine, and does not therefore show the full efficiency of the pump, but that of the combined pump and engine. It is, however, a very simple way of showing the relative values of different kinds of pumping-engines having their notive power forming a part of the plant.

The highest value of this term, given by Mr. Webber, is .9164 for a lift of

170 ft., and 3615 gals. per min. This was obtained in a test of the Leavitt pumping engine at Lawrence, Mass. July 24, 1879.
With reciprocating pumps, for higher lifts than 170 ft., the curve of efficiencies falls, and from 200 to 300 ft. lift the average value seems about cencies rais, and from 200 to 300 it. Hit the average value seems about 30 ft. Below 170 ft. the curve also falls reversely and slowly, until at about 30 ft. its descent becomes more rapid, and at 35 ft. 727 appears the best recorded performance. There are not any very satisfactory records below this lift, but some figures are given for the yearly coal consumption and total number of gallons pumped by engines in Holland under a 16-ft. lift, from which an efficiency of 44 has been deduced.

With centifying a number the lift at which the maximum efficiency is about 100 ft.

from which an efficiency of .44 has been deduced.
With centrifugal pumps, the lift at which the maximum efficiency is obtained is approximately 17 ft. At lifts from 12 to 18 ft. some makers of large experience claim now to obtain from 65% to 70% of useful effect, but. 613 appears to be the best done at a public test under 14.7 ft. head.
The drainage-pumps constructed some years ago for the Haarlem Lake were designed to lift 70 tons per min. 15 ft., and they weighed about 150 tons. Centrifugal pumps for the same work weigh only 5 tons. The weight of a centrifugal pump and engine to lift 10,000 gals. per min. 35 ft. high is

The pumps placed by Gwynne at the Ferrara Marshes, Northern Italy, in 1865, are, it is believed, capable of handling more water than other set of pumping-engines in existence. The work performed by these pumps is the lifting of 2000 tons per min—over 600,000,000 gals, per 24 hours—on a mean lift of about 10 ft. (maximum of 12.5 ft.). (See Engineering, 1876.)

The efficiency of centrifugal pumps seems to increase as the size of pump

increases, approximately as follows: A 2" pump (this designation meaning always the size of discharge-outlet in inches of diameter), giving an efficiency of 38%, a 8" pump 45%, and a 4" pump 5:%, a 5" pump 60%, and a 6" gump 64% efficiency.

Tests of Centrifugal Pumps.

W. O. Webber, Trans. A. S. M. E., ix, 237.

Maker.	An- drews.	An- drews.	An- drews.	Heald & Sisco.	Heald & Sisco.	Heald & Sisco.	Berlin. Schwartz kopff.
Size	952" 26" 191.9 1518.12 12.25 4.69 10.09	195.5	916" 984" 26" 200.5 2499.88 13.08	188.8 1673.87 12.33 5.22	10" 12" 80.5" 202.7	No. 10. 10" 12" 30.5" 2871.67 13.0 7.81 14.02 55.72	No. 9. 914" 10.8" 20.5" 500 1944.8 16.46

Vanes of Centrifugal Pumps.—For forms of pump vanes, see paper by W. O. Webber, Trans. A. S. M. E., ix. 228, and discussion thereon by Profs. Thurston, Wood, and others.

The Centrifugal Pump used as a Suction Dredge.—The Andrews centrifugal pump was used by Gen. Gillmore, U. S. A., in 1871, in deepening the channel over the bar at the mouth of the St. John's River, Florida. The pump was a No. 9, with suction and discharge pipes each 9 inches diam. It was driven at 800 revolutions per minute by belt from an engine developing 25 useful horse-power.

Although 200 revolutions of the pump disk per minute will easily raise 8000 gallons of clear water 18 ft. high, through a straight vertical 9 inch pipe, 800 revolutions were required to raise 2500 gallons of sand and water 11 ft. high, through two inclined suction-pipes having two turns each, dis-

11 ft. high, through two inclined suction-pipes having two turns each, dis-

charged through a pipe having one turn.

The proportion of sand that can be pumped depends greatly upon its specific gravity and fineness. The calcareous and argillaceous sands flow more freely than the silicious, and fine sands are less liable to choke the more freely than the silicious and time sands are less liable to choke the pipe than those that are coarse. When working at high speed, 50% to 55% of sand can be raised through a straight vertical pipe, giving for every 10 cubic yards of material discharged 5 to 5½ cubic yards of compact sand. With the appliances used on the St. John's bar, the proportion of sand seldom exceeded 45%, generally ranging from 30% to 35% when working under the most favorable conditions.

In pumping 2500 gallons, or 12.6 cubic yards of sand and water per minute, there would therefore be obtained from 3.7 to 4.3 cubic yards of sand. During the early stages of the work, before the teeth under the drag had been properly arranged to aid the flow of sand into the pipes, the yield was considerably below this average. (From catalogue of Jos. Edwards & Co., Mrs. of the Andrews Pump, New York.)

DUTY TRIALS OF PUMPING-ENGINES.

A committee of the A. S. M. E. (Trans., xii. 530) reported in 1891 on a standard method of conducting duty trials. Instead of the old unit of duty of foot-pounds of work per 100 lbs. of coal used, the committee recommend a new unit, foot-pounds of work per million heat-units furnished by the boiler. The variations in quality of coal make the old standard unit as a basis of duty ratings. The new unit is the precise equivalent of 100 lbs. of coal in cases where each pound of coal imparts 10,000 heat-units to the water in the boiler, or where the evaporation is 10,000 + 985.7 = 10.355 lbs. of water from and at 2129 per pound of fuel. This evaporative result is readily obtained from all grades of Cumberland bituminous coal, used in horizontal return tubular boilers, and, in many cases, from the best grades of anthracite coal.

The committee also recommend that the work done be determined by plunger displacement, after making a test for leakage, instead of by measurement of flow by weirs or other apparatus, but advise the use of such apparatus when practicable for obtaining additional data. The following extracts are taken from the report. When important tests are to be made the complete report should be consulted.

The necessary data having been obtained, the duty of an engine, and other quantities relating to its performance, may be computed by the use of the following formulæ:

1. Duty =
$$\frac{\text{Foot-pounds of work done}}{\text{Total number of heat-units consumed}} \times 1,000,000$$

= $\frac{A(P \pm p + s) \times L \times N}{H} \times 1,000,000$ (foot-pounds).

2. Percentage of leakage =
$$\frac{C \times 144}{A \times L \times N} \times 100$$
 (per cent).

3. Capacity = number of gallons of water discharged in 24 hours

$$=\frac{A\times L\times N\times 7.4805\times 24}{D\times 144}=\frac{A\times L\times N\times 1.24675}{D} \text{ (gallons)}.$$

Percentage of total frictions.

$$= \left[\frac{\text{I.H.P.} - \frac{A(P \pm p + s) \times L \times N}{D \times 60 \times 33,000}}{\text{I.H.P.}}\right] \times 100$$

$$= \left[1 - \frac{A(P \pm p + s) \times L \times N}{As \times \text{M.E.P.} \times Ls \times N_s}\right] \times 100 \text{ (per cent)};$$

or, in the usual case, where the length of the stroke and number of strokes of the plunger are the same as that of the steam-piston, this last formula becomes:

Percentage of total frictions =
$$\left[1 - \frac{A(P \pm p + s)}{A_s \times \text{M.E.P.}}\right] \times 100 \text{ (per cent)}.$$

In these formulæ the letters refer to the following quantities:

A =Area, in square inches, of pump plunger or piston, corrected for area of piston rod or rods;

P =Pressure, in pounds per square inch, indicated by the gauge on the

force main;

- p =Pressure, in pounds per square inch. corresponding to indication of the vacuum-gauge on suction-main (or pressure-gauge, if the suction-pipe is under a head). The indication of the vacuum-gauge, in inches of mercury, may be converted into pounds by dividing it by 2.035;
- 2.035;
 s = Pressure, in pounds per square inch, corresponding to distance between the centres of the two gauges. The computation for this pressure is made by multiplying the distance, expressed in feet, by the weight of one cubic foot of water at the temperature of the pump-well, and dividing the product by 144;
 L = Average length of stroke of pump-plunger, in feet;
 N = Total number of single strokes of pump-plunger made during the trial;
 As = Area of steam-cylinder, in square inches, corrected for area of piston-rod. The quantity As × M E.P., in an engine having more than one cylinder, is the sum of the various quantities relating to the respective cylinders:

tive cylinders; $L_8 = \text{Average length of stroke of steam-piston, in feet;}$ $N_8 = \text{Total number of single strokes of steam-piston during trial;}$

M.E.P. = Average mean effective pressure, in pounds per square inch, measured from the indicator-diagrams taken from the steam-cylin-

der; I H.P. = Indicated horse-power developed by the steam-cylinder; C = Total number of cubic feet of water which leaked by the pump-plunger during the trial, estimated from the results of the leakage test; = Duration of trial in hours:

H = Total number of heat units (B. T. U.) consumed by engine = weight of water supplied to boiler by main feed-pump × total heat of steam of boiler pressure reckoned from temperature of main feed-water + weight of water supplied by jacket-pump × total heat of steam of boiler-pressure reckoned from temperature of jacket-water + weight of any other water supplied × total heat of steam reckoned from its temperature of supplied × total heat of steam reckoned from the person of the steam of the steam is corrected for the steam of the steam is corrected from the person of the steam is corrected. temperature of supply. The total heat of the steam is corrected for the moisture or superheat which the steam may contain. No allowance is made for water added to the feed water, which is derived from any source, except the engine or some accessory of the engine. heat added to the water by the use of a flue-heater at the boiler is not to be deducted. Should heat be abstracted from the flue by means of a steam reheater connected with the intermediate receiver of the engine, this heat must be included in the total quantity supplied by the boiler.

Leakage Test of Pump.—The leakage of an inside plunger (the only type which requires testing) is most satisfactorily determined by making the test with the cylinder-head removed. A wide board or plank may be temporarily bolted to the lower part of the end of the cylinder, so as to hold back the water in the manner of a dam, and an opening made in the temporary head thus provided for the reception of an overflow-pipe. The plunger is blocked at some intermediate point in the stroke (or, if this position is not practicable, at the end of the stroke), and the water from the force main is admitted at full pressure behind it. The leakage escapes

through the overflow-pipe, and it is collected in barrels and measured. The test should be made, if possible, with the plunger in various positions. In the case of a pump so planned that it is difficult to remove the cylinderhead, it may be desirable to take the leakage from one of the openings which are provided for the inspection of the suction-valves, the head being

allowed to remain in place.

It is assumed that there is a practical absence of valve leakage. Examination for such leakage should be made, and if it occurs, and it is found to be due to disordered valves, it should be remedied before making the plunger test. Leakage of the discharge valves will be shown by water passing down into the empty cylinder at either end when they are under pressure. Leak-age of the suction-valves will be shown by the disappearance of water which covers them.

If valve leakage is found which cannot be remedied the quantity of water thus lost should also be tested. One method is to measure the amount of water required to maintain a certain pressure in the pump cylinder when this is introduced through a pipe temporarily erected, no water being allowed to enter through the discharge valves of the pump.

Table of Data and Results.—In order that uniformity may be se-

cured, it is suggested that the data and results, worked out in accordance with the standard method, be tabulated in the manner indicated in the following scheme:

DUTY TRIAL OF ENGINE.

DIMENSIONS.

1. Number of steam-cylinders	
2. Diameter of steam-cylinders	. ins.
3. Diameter of piston-rods of steam-cylinders	. ins.
4. Nominal stroke of steam-pistons	. ft.
5. Number of water-plungers	
6. Diameter of plungers	. ins.
7. Diameter of piston-rods of water-cylinders	. ins.
8. Nominal stroke of plungers	. ft.
9. Net area of steam-pistons	• sq. ins.
10. Net area of plungers	
11. Average length of stroke of steam-pistons during trial	
12. Average length of stroke of plungers during trial	. ft.
(Give also complete description of plant.)	

18. Temperature of water in pump-well	degs.
•••	

sources...... degr

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urement of	flow '	and Pamp 100.
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a a	string of rried single strokes (JUFING LIMI
-	of store in Steam	Supplied to ought of Laures. € or deg
-	of monerheating	juring trialsupplied to engine, or number supplied to engine, or number s or deg dal, determined from results of
F Jung	of pump during u	lbs.
المساد	measure measure	juring trial
N. Jeak	decure pressure,	M.E.P.
Mary Mary	PRINCIPA	ial, determined from results of lbs. ed from diagrams taken from M.E.P.
	atakara	ft, lbs.
on Duly	age of loaning	gals.
31. Capacit	of total friction	
Percent	ADDITIONA	L RESULTS.
3x -	a tamble etrokes of stee	am-piston per minute by the various steam-cylinders I.H.P.
Number	of double strokes of see	m-piston per minute by the various steam-cylinders I.H.P. nt per hour
Indicated	ter consumed by the plan	by the various steam-cylinders I.H.P., nt per hour lbs., ant per indicated horse-power
Wimber	of heat units consume	od per indicated horse-power
per hou	ur	d per indicated horse-power
39 Number	or neat units consume	a per indicated norse-power
per mi	nuve	r at cut-off and release in the
40. Steam ac	steam.evilnders	lbs.
44 Proportio	n which steam accoun	ted for by indicator bears to
the ree	a-water consumption	
49 Number	of double strokes of pur	np per minute
48. Mean effe	ctive pressure, measure	d from pump diagrams M.E.P.
44. Indicated	norse power exerted in	pump-cylinders I.H.P.
		of coal ft. lbs.
		FROM STEAM-CYLINDERS.
(Also, if no	ssible, full measuremen	t of the diagrams, embracing pressures

(Also, if possible, full measurement of the diagrams, embracing pressures at the initial point, cut-off, release, and compression; also back pressure, and the proportions of the stroke completed at the various points noted.)

SAMPLE DIAGRAM TAKEN FROM PUMP-CYLINDERS.

These are not necessary to the main object, but it is desirable to give them.

DATA AND RESULTS OF BOILER TEST.

(In accordance with the scheme recommended by the Boiler-test Committee of the Society.)

VACUUM PUMPS-AIR-LIFT PUMP.

The Pulsometer.—In the pulsometer the water is raised by suction into the pump-chamber by the condensation of steam within it, and is then forced into the delivery-pipe by the pressure of a new quantity of steam on the surface of the water. Two chambers are used which work alternately,

one raising while the other is discharging.

Test of a Pulsometer.—A test of a pulsometer is described by De Volson Wood in Trans. A. S. M. E. xiii. It had a 3½-inch suction-pipe, stood 40 in.

high, and weighed 695 lbs.

The steam-pipe was 1 inch in diameter. A throttle was placed about 2 feet

from the pump, and pressure gauges placed on both sides of the throttle, and a mercury well and thermoneter placed beyond the throttle. The wire drawing due to throttling caused superheating.

The pounds of steam used were computed from the increase of the tem

perature of the water in passing through the pump.

Pounds of steam \times loss of heat = lbs, of water sucked in \times increase of temp.

The loss of heat in a pound of steam is the total heat in a pound of saturated steam as found from "steam tables" for the given pressure, plus the heat of superheating, minus the temperature of the discharged water; or

Pounds of steam =
$$\frac{\text{lbs. water} \times \text{increase of temp.}}{H - 0.48t - T}$$

The results for the four tests are given in the following table:

Data and Results.	Number of Test.								
Dates and thooms	1	2	8	4					
Strokes per minute	71	60	57	64					
Steam press in pipe before throttl'g	114	110	127	104.3					
Steam press, in pipe after throttl'g	19	30	48.8	26.1					
Steam temp. after throttling, deg. F.	270.4	277	809.0	270.1					
Steam am'nt of superheat'g.deg.F.	8.1	8.4	17.4	1.4					
Steam used as det'd from temp., lbs.	1617	931	1518	1019.9					
Water pumped, lbs,	404,786	186.862	228,495	248,053					
Water temp. before entering pump.	75.15	90.6	76.8	70.25					
Water temp., rise of	4.47	5.5	7.49	4,55					
Water head by gauge on lift, ft	29,90	54.05	54.05	29.90					
Water head by gauge on suction	12.26	12.26	19.67	19.67					
Water head by gauge, total (H)	42.16	66.81	78.72	49.57					
Water head by measure, total (h)	82.8	57.80	66.6	41.6C					
Coeff. of friction of plant $(h) \div (H)$	0.777	0.877	0.911	0.889					
Efficiency of pulsometer	0.012	0.0155	0.0126	0.0188					
Effic. of plant exclusive of boiler	0.0098	0.0136	0.0115	0.0116					
Effic. of plant if that of boiler be 0.7									
Duty, if 1 lb. evaporates 10 lbs. water	10,511,400	18,391,000	11,059,000	12,086,800					

Of the two tests having the highest lift (54.05 ft.), that was more efficient which had the smaller suction (12.26 ft.), and this was also the most efficient of the four tests. But, on the other hand, the other two tests having the same lift (29.9 ft.), that was the more efficient which had the greater suction (19.67), so that no law in this regard was established. The pressures used, 19, 30, 438, 26.1, follow the order of magnitude of the total heads, but are not proportional thereto. No attempt was made to determine what pressure would give the best efficiency for any particular head. The pressure used was intrusted to a practical runner, and he judged that when the pump was running regularly and well, the pressure then existing was the proper one It is peculiar that, in the first test, a pressure of 19 lba of steam should pro-

duce a greater number of strokes and pump over 50% more water than 26.1 lbs., the lift being the same, as in the fourth experiment.

Chas. E. Emery in discussion of Prof. Wood's paper says, referring to tests made by himself and others at the Centennial Exhibition in 1876 (see Report of the Judges, Group xx.), that a vacuum-pump tested by him in 1871 gave a duty of 4.7 millions; one tested by J. F. Flags, at the Cincinnati Exposition in 1875, gave a maximum duty of 3.25 millions. Several vacuum to have given duties of 10 to 11 millions, the stame basis, were reported to have given duties of 10 to 11 millions, the steam-pumps doing no better than the vacuum-pumps. Injectors, when used for lifting water not required to be heated, have an efficiency of 2 to 5 millions; vacuum-pumps vary generally between 3 and 10; small steam-pumps between 8 and 15; larger steam-pumps, between 15 and 30, and pumping-engines between 30

and 140 millions.

A very high record of test of a pulsometer is given in Eng'g, Nov. 24, 1893, p. 689, viz.: Height of suction 11.27 ft.; total height of lift, 102.6 ft.; horizontal length of delivery-pipe, 118 ft.; quantity delivered per hour, 25, 188 British gallons. Weight of steam used per H. P. per hour, 92.76 lbs.; work.

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John J. Coal of Steam 91-325 foot-founds equal to a duly of $1,365.000 and $1.000 foot of it to be of steam were generated by the steam of the tendency of the steam of the tendency of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the
                                                                                        found the as to the efficiency of the evenue, the second to form pipe where the depth from which the greatest efficiency was fifth of the was about inthe depth from which the greatest efficiency was the pipe to the pipe the flow up the suction-pipe being in which having by the efficiency was described by the pipe that it is proposed in which that it is proposed in the pipe that the pipe that it is proposed in the pipe that it is proposed in the pipe that it is proposed by the pipe that it is proposed by the pipe that it is proposed by the pipe that it is proposed by the pipe that it is proposed by the pipe that it is proposed by the pipe that it is proposed by the pipe that it is proposed by the pipe that it is proposed by the pipe that it is proposed by the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe that pipe the pipe the pipe that pipe the pipe that pipe the pipe the pipe the pipe the pipe the pipe the pipe the pipe the pipe the pipe the 
                                                                                                                               The Injector when used as a pump has a very low efficiency. (See
                                      Jojector Hector when used a large of the Steam-boilers.)

All lift Per Steam-boilers.)

with its low Pund part he air lift pump consists of a very low enciency. (See into it at other boots on the rising column in the smaller pipe delivater pipe air being in bubbles of air lift pump consists of air lift 
with water, the tour.

than a column air being in bubbles of various give cousses of ar mingled is raised of water of the same of various size cousses of ar mingled was mention was proposed of the surrounding water was the level of the surrounding water was the proposed of the surrounding water was the proposed of the surrounding water in the water was by Werner Size of the water in the water was by Werner Size of the proposed of the surrounding water. This method of the surrounding was by Werner Size of the surrounding water in the water was by Werner Size of the surrounding water in the surrounding water was by Werner Size of the surrounding water in the surrounding water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water water w
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was mentioned by Collon in lectures in Paris in 1876, but its full principle in California in 1886, but its full principle in California in 1886, and to application probably was by Werner Siemens in Berlin in 1883. Provide on apparatus involving it were granted to Pohle and Hill in 1883 and U. S. paterns of the air-lift pump made by Randall, Browne and on apparatus involving it were granted to Pohle and Hill in the same year.

A paper describing tests of the air-lift pump made by Randall Browne and the Pacific Coast in Feb. 1890. A paper describing tests of the air-lift pump made by Raman and the diameter of the pump column made by Raman and the air-discharge nozzle 5g in. The air-pipe had four sharp bends and a made and the pump bends and a made air-discharge nozzle 5g in. The diameter of the pump-column was 3 in., of the air-pipe of the air-pipe of the air-pipe of the air-pipe of the air-pipe of the air-pipe of the air-pipe of the air-pipe of the air-pipe of the air-pipe of the water was pumped from a closed pipe well (55 ft. deep and 10 in. in length of 35 ft. plus the depth of submersion.

The water was pumped from a submersion.

retically regulared to compress the pump was based on the least work theory of the compress the air and deliver it to the least work theory of the efficiency of the efficiency of the pump and

retically required to compress the air and deliver it to the receiver. If the efficiency of the compressor be taken at 70%, the efficiency of the pump and for the pump and lone.
For a given submersion (h) and lift (H), the ratio of the two being kept ithin reasonable limits. (H) being not much greater than (h), the efficiency within reasonable limits, (I) and lift (II), the ratio of the two being kept was greatest when the bressure in the receiver did not greatly exceed the within reasonable limits, (H) being not much greater than (h), the efficiency head due to the submersion. The smaller the ratio H - h, the higher was the efficiency.

was greatest when the pressure in the receiver did not greatly exceed the efficiency.

The smaller the ratio H - h, the higher was

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The fact efficiency is especially that there is 50% 4.50 and action fitted there are 50% 4.50 and action fitted for handing dirty or noving 20% 25% and action fitted for handing dirty or noving parts makes the pump of 1,000,000 k, N, J, Solutions in elientical Eritty water, sewage, mine water, Newark, Chemical Work, N, J, Solutions in elientical Eritty water, sewage, mine water at George (Constant Constant Rravity. The Colorado Central Consolidated Mining Co. in one of its min For a full account of the theory of the pump, and details of the test For a full account of the theory of the pump, and details of the tests ter with a moderate fall is available, to raise a small portion of that flow

Efficiency.—The hydraulic ram is used where a considerable flow of the height exceeding that of the fall. The following are rules given by experiments (from Rankine): elwein as the results of his experiments (from Ranker).

It to be the whole supply of water in cubic feet per second, of which give clack; D, its diameter in of the supply-pipe, from the pond to the pond to the pond to the supply-pipe, from the pond to the supply-pipe, from the pond to the supply-pipe, from the pond to the supply-pipe, from the pond to the supply-pipe from the supply-pipe from the supp

Volume of air vessel = volume of feed pipe;

Efficiency,
$$\frac{Qh}{(Q-q)H}=1.12-0.2\,\sqrt{\frac{h}{H}}$$
 when $\frac{h}{H}$ does not exceed 20. or $1+\left(1+\frac{h}{10H}\right)$ nearly, when $\frac{h}{H}$ does not exceed 12. D'Aubuisson gives $\frac{\dot{q}(H+h)}{QH}=1.42-.28\,\sqrt{\frac{h}{H}}$.

Clark, using five sixths of the values given by D'Aubuisson's formula, gives: Ratio of lift to fall.... 4 6 8 10 12 14 16 18 20 22 24 26 Efficiency per cent.... 72 61 52 44 37 31 25 19 14 9 4 0

Prof. R. C. Carpenter (Eng'g Mechanics, 1894) reports the results of four tests of a ram constructed by Rumsey & Co., Seneca Falls. The ram was fitted for pipe connection for 1¼-inch supply and ½-inch discharge. The supply-pipe used was 1½ inches in diameter, about 50 feet long, with 3 elbows, so that it was equivalent to about 65 feet of straight pipe, so far as resistance is concerned. Each run was made with a different stroke for the waste or clack-valve, the supply and delivery head being constant; the object of the experiment was to find that stroke of clack-valve which would give the highest efficiency.

Length of stroke, per cent	52 5.67 19.75 297 1615	80 56 5.77 19.75 296 1567 66	60 61 5.58 19.75 301 1518 74.9	46 66 5.65 19.75 297.5 1455.5 70
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The efficiency, 74.9, the highest realized, was obtained when the clack valve travelled a distance equal to 60% of its full stroke, the full travel being 15/16 of one inch.

Quantity of Water Delivered by the Hydraulic Bam. (Chadwick Lead Works.)—From 80 to 100 feet conveyance, one seventh of supply from spring can be discharged at an elevation five times as high as the fall to supply the ram; or, one fourteenth can be raised and discharged say ten times as high as the fall applied.
Water can be conveyed by a ram 3000 feet, and elevated 200 feet. The drive-pipe is from 25 to 50 feet long.

The following table gives the capacity of several sizes of rams, the dimensions of the pipes to be used, and the size of the spring or brook to which they are adapted:

,			er of es.	Weight of Pipe (Lead), if Wrought Iron, then of Ordinary Weight.		
Size of Ram.	Quantity of Water Furnished per Min. by the Spring or Brook to which the Ram is Adapted.	Drive.	Discharge.	Drive-pipe for head or fall not over 10 ft.	pipe for not	Discharge- pipe for over 50 ft. and not ex- ceeding 100 ft. in height.
No. 2 4 3 4 4 5 6 7 10	Gals. per min. 94 to 2 112 " 4 8 " 7 6 " 14 112 " 25 20 " 40 25 " 75	inch. 3/4 1 11/4 21/4 21/4	inch	per foot. 2 lbs. 3 " 5 " 8 " 13 " 13 " 21 "	per foot. 10 ozs. 12 " 12 " 1 lb. 4 " 3 " 7 "	per foot. 1 lb. 1 ' 4 ozs. 1 ' 4 ozs. 2 ' 4 ozs 8 ' 4 ' 8 ' *

HYDRAULIC-PRESSURE TRANSMISSION.

Water under high pressure (700 to 3000 lbs. per square meh and upwards; affords a very satisfactory method of transmitting power to a distance, especially for the movement of heavy loads at small velocities, as by cranes and elevators. The system consists usually of one or more pumps capable of developing the required pressure; accumulators, which are vertical cylinders with heavily-weighted plungers passing through stuffing-boxes in the upper end, by which a quantity of water may be accumulated at the pressure to which the plungers weighted the distribution-cines; and the pressure to which the plungers are strong to the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution-cines; and the pressure of the distribution cines; and the pressure of the distribution cines; and the pressure of the distribution cines; and the pressure of the distribution cines. sure to which the plunger is weighted; the distributing-pipes; and the presses,

cranes, or other machinery to be operated.

The earliest important use of hydraulic pressure probably was in the Bramah hydraulic press, patented in 1796. Sir W. G. Armstrong in 1846 was Bramah hydraulic press, patented in 1740. Sir W. G. Armstrong in 1030 was one of the pioneers in the adaptation of the hydraulic system to cranes. The use of the accumulator by Armstrong led to the extended use of hydraulic machinery. Recent developments and applications of the system are largely due to Ralph Tweddell, of London, and Sir Joseph Whitworth. Sir Henry Beasemer, in his patent of May 18, 1856, No. 1292, first suggested the use of hydraulic pressure for compressing steel ingots while in the fluid state.

The Gross Amount of Energy of the water under pressure stored in the accumulator, measured in foot-pounds, is its volume in cubic feet × its pressure in pounds per square foot. The horse-power of a given quantity steadily flowing is H.P. = $\frac{144pQ}{2}$ = .8618pQ, in which Q is the quantity flowing 550

in cubic feet per second and p the pressure in pounds per square inch. The loss of energy due to velocity of flow in the pipe is calculated as follows (R. G. Blaine, Eng'g, May 22 and June 5, 1891):

According to D'Arcy, every pound of water loses $\frac{\lambda 4L}{L}$ times its kinetic D energy, or energy due to its velocity, in passing along a straight pipe L feet in length and D feet diameter, where λ is a variable coefficient. For clean cast-iron pipes it may be taken as $\lambda = .005 \left(1 + \frac{1}{12D}\right)$, or for diameter in inches = d.

d = 1/4 .01 .0075 .00667 .00625 .006 .00588 .00571 .00568 .00556 .00542

The loss of energy per minute is $60 \times 69.36Q \times \frac{\lambda 4L}{D} \frac{v^2}{2a}$, and the horse-

power wasted in the pipe is $W = \frac{.6868 \lambda L(H.P.)^3}{100}$, in which λ varies with the $p^3 \overline{D^6}$ diameter as above. p = pressure at entrance in pounds per square inch.Values of .63634 for different diameters of pipe in inches are: $d = \frac{1}{3} \begin{pmatrix} 1 & 2 & 3 & 4 & 4 & 4 & 4 & 4 \end{pmatrix}$

. 06400, 06800, 83800, 83800, 83800, 17800, 18800, 98800, 19400, 77400, 86800, 45600, 76400, 86800, 45600 Efficiency of Hydraulic Apparatus.—The useful effect of a direct hydraulic plunger or ram is usually taken at 98%. The following is given as the efficiency of a ram with chain-and-pulley multiplying gear properly proportioned and well lubricated: hulliplying.... 2 to 1 4 to 1 6 to 1 8 to 1 10 to 1 12 to 1 14 to 1 16 to 1

72 67 68 59 With large sheaves, small steel pins, and wire rope for multiplying gear the efficiency has been found as high as 66% for a multiplication of 20 to 1.

Henry Adams gives the following formula for effective pressure in granes and hoists:

P = accumulator pressure in pounds per square inch; m = ratio of multiplying power:

E = effective pressure in pounds per square inch, including all allowances for friction:

$$E = P(.84 - .02m).$$

J. E. Tuit (Eng'g, June 15, 1888) describes some experiments on the friction of hydraulic jacks from \$14 to 1896 inch diameter, fitted with cupped leather packings. The friction loss varied from 5.6% to 18.8% according to the condition of the leather, the distribution of the load on the ram, etc. The friction increased considerably with eccentric loads. With hemp packing a plunger, 14-inch diameter, showed a friction loss of from 11.4% to 8.4%, the load being central, and from 15.0% to 7.6% with eccentric load, the percentage of loss decreasing in both cases with increase of load.

Thickness of Hydraulic Cylinders.—From a table used by Sir W. G. Armstrong we take the following, for cast-iron cylinders, for an interior pressure of 1000 lbs. per square inch:

Diam. of cylinder, inches. 2 4 6 8 10 12 16 90 24 Thickness, inches. 0.832 1.146 1.552 1.875 2.222 2.578 8.19 3.69 4.11

For any other pressure multiply by the ratio of that pressure to 1000. These figures correspond nearly to the formula t=0.175d+0.48, in which

These figures correspond hearly to the formula $t = 0.1753 \pm 0.48$, in which t = thickness and d = diameter in inches, up to 16 inches diameter, but for 20 inches diameter the addition 0.48 is reduced to 0.19 and at 34 inches it disappears. For formulæ for thick cylinders see page 387, ante. Cast iron should not be used for pressures exceeding 3000 lbs. per square inch. For higher pressures steel castings or forged steel should be used. For working pressures of 750 lbs. per square inch the test pressure should be \$800 lbs. per square inch, and for 1500 lbs. the test pressure should not be less than 3500 lbs.

Speed of Hoisting by Hydraulic Pressure.—The maximum allowable speed for warehouse cranes is 6 feet per second; for platform cranes 4 feet per second; for passenger and wagon hoists, heavy loads, 2 feet per second. The maximum speed under any circumstances should never exceed 10 feet per second.

The Speed of Water Through Valves should never be greater

The speed of water Through Pipes.—Experiments on water at 1600 lbs. pressure per square inch flowing into a flanging-machine ram, 20-inch diameter, through a ½-inch pipe contracted at one point to ½-inch, gave a velocity of 114 feet per second in the pipe, and 456 feet at the reduced section. Through a ½-inch pipe reduced to ½-inch at one point the velocity was 218 feet per second in the pipe and 381 feet at the reduced section. In a ½-inch pipe without contraction the velocity was 256 feet per second.

For many of the above notes the author is indebted to Mr. John Platt, consulting angines of New York.

consulting engineer, of New York.

High-pressure Hydraulic Presses in Iron-works are described by R. M. Daeleu, of Germany, in Trans. A. I. M. E. 1893. The following distinct arrangements used in different systems of high-pressure hydraulic work are discussed and illustrated:

1. Steam-pump, with fly-wheel and accumulator.

2. Steam-pump, without fly-wheel and with accumulator.
3. Steam-pump, without fly-wheel and without accumulator.
In these three systems the valve-motion of the working press is operated.
In the high-pressure column. This is avoided in the following:

4. Single acting steam-intensifier without accumulator.

Steam-pump with fly-wheel, without accumulator and with pipe-circuit.
 Steam-pump with fly-wheel, without accumulator and without pipe-

eircuit.

The disadvantages of accumulators are thus stated: The weighted plungers which formerly served in most cases as accumulators, cause violent shocks in the pipe-line when changes take place in the movement of the water, so that in many places, in order to avoid bursting from this cause, the pipes are made exclusively of forged and bored steel. The seats and cones of the metallic valves are cut by the water (at high speed), and in such cases only

the most careful maintenance can prevent great losses of power.

Hydraulic Power in London.—The general principle involved is pumping water into mains laid in the streets, from which service-pipes are carried into the houses to work lifts or three-cylinder motors when rotatory power is required. In some cases a small Pelton wheel has been tried, working ander a pressure of over 700 lbs. on the square inch. Over 55

miles of hydraulic mains are at present laid (1892).

The reservoir of power consists of capacious accumulators, loaded to a pressure of 800 lbs. per square inch, thus producing the same effect as if large supply-tanks were placed at 1700 feet above the street-level. The water is taken from the Thames or from wells, and all sediment is removed therefrom by filtration before it reaches the main engine-pumps.

There are over 1750 machines at work, and the supply is about 6,500,000

gallons per week.

It is essential that the water used should be clean. The storage-tank extends over the whole boiler-house and coal store. The tank is divided, and a certain amount of mud is deposited here. It then passes through the surface condenser of the engines, and it is turned into a set of filters, eight in number. The body of the filter is a cast-iron cylinder, containing a layer

grapular flivering material resting upon a false bottom; under this is the di tributing arrangement, affording passage for the air, and under this the real bottom of the tank. The dirty water is supplied to the filters from an overhead tank. After passing through the filters the clean effluent is pumped into the clean-water tank, from which the pumping-engines derive their supply. The cleaning of the filters, which is done at intervals of 24 hours, is effected so thoroughly as situ that the filtering material never requires to be r-moved.

The engine-house contains six sets of triple-expansion engines. The cylinders are 15-inch, 22-inch, 36 inch × 24-inch. Each cylinder drives a single plunger-pump with a 5-inch ram, secured directly to the cross-head, the connecting-rod being double to clear the pump. The boiler-pressure is 130 lbs. on the square inch. Each pump will deliver 300 gallons of water per minute under a pressure of 800 lbs. to the square iach, the engines making about 61 revolutions per minute. This is a high velocity, considering the heavy pressure; but the valves work silently and without perceptible shock.

The consumption of steam is 14.1 pounds per hour.

The water delivered from the main pumps passes into the accumulators. The rams are 20 inches in diameter, and have a stroke of 23 feet. They are each loaded with 110 tons of slag, contained in a wrought-iron cylindrical box suspended from a cross-head on the top of the ram.

One of the accumulators is loaded a little more heavily than the other, so that they rise and fall successively; the more heavily loaded actuates a stop-valve on the main steam-pipe. If the engines supply more water than is wanted, the lighter of the two rams first rises as far as it can go; the other them ascends, and when it has nearly reached the top, shuts off steam and checks the supply of water automatically.

The mains in the public streets are so constructed and laid as to be per-

fectly trustworthy and free from leakage.

Every pipe and valve used throughout the system is tested to 2500 lbs. per square inch before being placed on the ground and again tested to a reduced pressure in the trenches to insure the perfect tightness of the joints. The jointing material used is gutta-percha.

The average rate obtained by the company is about 3 shillings per thousand gallons. The principal use of the power is for intermittent work in cases where direct pressure can be employed, as, for instance, passenger elevators,

cranes, presses, warehouse hoists, etc.

An important use of the hydraulic power is its application to the extinguishing of fire by means of Greathead's injector hydrant. By the use of these hydrautis a continuous fire-engine is available.

Hydraulic Riveting-machines.—Hydraulic riveting was introduced in England by Mr. R. H. Tweddell. Fixed riveters were first used about 1869. Portable riveting machines — Hydraulic riveting machines.—Hydraulic riveting machines.—Hydraulic riveting machines.—Hydraulic riveting machines were introduced in 1869.

1868. Portable riveting-machines were introduced in 1872.

The riveting of the large steel plates in the Forth Bridge was done by small portable machines working with a pressure of 1000 lbs. per square inch. In exceptional cases 3 tons per inch was used. (Proc. Inst. M. E., May, 1889.)

An application of hydraulic pressure invented by Andrew Higginson, of Liverpool, dispenses with the necessity of accumulators. It consists of a three-throw pump driven by shafting or worked by steam, and depends partially upon the work accumulated in a heavy fly-wheel. The water in its passage from the pumps and back to them is in constant circulation at a very feeble pressure, requiring a minimum of power to preserve the tube of water ready for action at the desired moment, when by the use of a tap the current is stopped from going back to the pumps, and is thrown upon the piston of the tool to be set in motion. The water is now confined, and the driving-belt or steam-engine, supplemented by the momentum of the heavy fly-wheel, is employed in closing up the rivet, or bending or forging the ob-

ject subjected to its operation.

Hydraulic Forging.—In the production of heavy forgings from cast ingots of mild steel it is essential that the mass of metal should be operated on as equally as possible throughout its entire thickness. employing a steam-hammer for this purpose it has been found that the external surface of the ingot absorbs a large proportion of the sudden impact of the blow, and that a comparatively small effect only is produced on the central portions of the ingot, owing to the resistance offered by the inertia of the mass to the rapid motion of the falling hammer—a disadvantage that antistic converse but the plant the table of the comparation of the is entirely overcome by the slow, though powerful, compression of the hydraulic forging-press, which appears destined to supersede the steam-hammer for the production of massive steel forgings.

In the Allen forging-press the force-pump and the large or main cylinder of the press are in direct and constant communication. There are no intermediate valves of any kind, nor has the pump any clack-valves, but it simply forces its cylinder full of water direct into the cylinder of the press, sniply forces its cylinder thin or water direct into the cylinder of the press, and receives the same water, as it were, back again on the return stroke. Thus, when both cylinders and the pipe connecting them are full, the large ram of the press rises and falls simultaneously with each stroke of the pump, keeping up a continuous oscillating motion, the ram, of course, travelling the shorter distance, owing to the larger capacity of the press cylinder. (Journal Iron and Steel Institute, 1891. See also illustrated article in "Modern Mechanism," page 668.)

For a very complete illustrated account of the development of the lay.

For a very complete illustrated account of the development of the hydraulic forging-press, see a paper by R. H. Tweddell in Proc. Inst. C. E., vol.

Hydraulic Forging-press.—A 2000-ton forging-press erected at the Couillet forges in Belgium is described in Eng. and M. Jour., Nov. 25, 1893.

The press is composed essentially of two parts—the press itself and the compressor. The compressor is formed of a vertical steam-cylinder and a hydraulic cylinder. The piston-rod of the former forms the piston of the latter. The hydraulic piston discharges the water into the press proper. The distribution is made by a cylindrical balanced valve; as soon as the pressure is released the steam-piston falls automatically under the action of

gravity. During its descent the steam passes to the other face of the piston to reheat the cylinder, and finally escapes from the upper end.

When steam enters under the piston of the compressor-cylinder the piston rises, and its rod forces the water into the press proper. The pressure thus exerted on the piston of the latter is transmitted through a cross-head to the forging which is upon the anvil. To raise the cross-head two small single-acting steam-cylinders are used, their piston-rods being connected to the cross-head two small single-acting steam-cylinders are used, their piston-rods being connected to the cross-head; steam acts only on the pistons of these cylinders from below. The admission of steam to the cylinders, which stand on top of the press frame, is regulated by the same lever which directs the motions of the compressor. The movement given to the dies is sufficient for all the ordinary purposes of forging.

A speed of 80 blows per minute has been attained. A double press on the

same system, having two compressors and giving a maximum pressure of 6000 tons, has been erected in the Krupp works, at Essen.

The Alken Intensifier. (Iron Age, Aug. 1890.)—The object of the machine is to increase the pressure obtained by the ordinary accumulator which is necessary to operate powerful hydraulic machines requiring very high pressures, without increasing the pressure carried in the accumulator and the general hydraulic system.

The Aiken Intensifier consists of one outer stationary cylinder and one

inner cylinder which moves in the outer cylinder and on a fixed or stationary hollow plunger. When operated in connection with the hydraulic bloom-shear the method of working is as follows: The inner cylinder having been filled with water and connected through the hollow plunger with the hydrau-lic cylinder of the shear, water at the ordinary accumulator pressure is admitted into the outer cylinder, which being four times the sectional area of the plunger gives a pressure in the inner cylinder and shear cylinder connected therewith of four times the accumulator-pressure—that is, if the accumulator-pressure—that is, if the accumulator-pressure—that is, if the accumulator-pressure—that is, if the accumulator-pressure—that is, if the accumulator-pressure—that is, if the accumulator-pressure—that is, if the accumulator-pressure is the

nected therewith of four times the accumulator-pressure—that is, it the accumulator-pressure is 500 lbs. per square inch the pressure in the intensifier will be 2000 lbs. per square inch.

Hydraulic Engine driving an Air-compressor and a Forging-hammer. (Iron Age, May 12, 1892.)—The great hammer in Terni, near Rome, is one of the largest in existence. Its falling weight amounts to 100 tons, and the foundation belonging to it consists of a block of cast iron of 1000 tons. The stroke is 16 feet 434 inches; the diameter of the cylinder 6 feet 345 inches; diameter of piston-rod 1834 inches; total height of the hammer, 62 feet 4 inches. The power to work the hammer, as well as the two cranes of 100 and 150 tons respectively, and other auxiliary applithe two cranes of 100 and 150 tons respectively, and other auxiliary appli-ances belonging to it, is furnished by four air-compressors coupled together and driven directly by water-pressure engines, by means of which the air is compressed to 73.5 pounds per square inch. The cylinders of the water-pressure engines, which are provided with a bronze lining, have a 1334 inch bore. The stroke is 4734 inches, with a pressure of water on the piston amounting to 234.6 pounds per square inch. The compressors are bored out of 3134 inches diameter, and have 4734-inch stroke. Each of the four cylinders requires a power equal to 280 horse-power. The compressed air is de620

livered into huge reservoirs, where a uniform pressure is kept up by means

of a suitable water-column.

The Hydraulic Forging Plant at Bethlehem, Pa., is described in a paper by R. W. Davenport, read before the Society of Naval Engineers and Marine Architects, 1898. It includes two hydraulic forging presses complete, with enginees and pumps, one of 1800 and one of 4800 tons capacity, together with two Whitworth hydraulic travelling forging-cranes and other necessary appliances for each press; and a complete fluid-compres-

and other necessary appliances for each press; and a complete fluid-compression plant, including a press of 7000 tons capacity and a 125 ton hydraulic travelling crane for serving it (the upper and lower heads of this press weighing respectively about 135 and 120 tons).

A new forging press has been designed by Mr. John Fritz, for the Bethlehem Works, of 14,000 tons capacity, to be run by engines and pumps of 15,000 horse-power. The plant is served by four open-hearth steel furnaces of a united capacity of 120 tons of steel per heat.

Some References on Hydraulic Transmission.—Reuleaux's Constructor;" "Hydraulic Motors, Turbines, and Pressure-engines," G. Bodiner, London, 1889; Robinson's "Hydraulic Power and Hydraulic Machinery," London, 1885; Colyer's "Hydraulic Steam, and Hand-power Lifting and Pressing Machinery," London, 1881. See also Engineering (London), Aug. 1, 1884, p. 99, March 13, 1885, p. 262; May 22 and June 5, 1891, pp. 612, 665; Feb. 19, 1892, p. 25; Feb. 10, 1898, p. 170.

FUEL.

Theory of Combustion of Solid Fuel. From Rankine, somewhat altered.)—The ingredients of every kind of fuel commonly used may be thus classed: (1) Fixed or free carbon, which is left in the form of charcoal or coke after the volatile ingredients of the fuel have been distilled away. These ingredients burn either wholly in the solid state (CO Cto CO₂) or part in the solid state and part in the gaseous state $(CO + O = CO_g)$, the latter part being first dissolved by previously formed carbonic acid by the rection $CO_g + C = 2CO$. Carbonic exide, CO, is produced when the supply of air to the fire is insufficient.

of air to the fire is insufficient.

(2) Hydrocarbons, such as oleflant gas, pitch, tar, naphtha, etc., all of which must pass into the gaseous state before being burned.

If mixed on their first issuing from amongst the burning carbon with a large quantity of hot air, these inflammable gases are completely burned with a transparent blue flame, producing carbonic acid and steam. When mixed with cold air they are apt to be chilled and pass off unburned. When raised to a red heat, or thereabouts, before being mixed with a sufficient quantity of air for perfect combustion, they disengage carbon in fine powder, and pass to the condition partly of marsh gas, and partly of free hydrogen; and the higher the temperature, the greater is the proportion of carbon gen; and the higher the temperature, the greater is the proportion of carbon thus disengaged.

If the disengaged carbon is cooled below the temperature of ignition before coming in contact with oxygen, it constitutes, while floating in the gas, smoke, and when deposited on solid bodies, soot.

But if the disengaged carbon is maintained at the temperature of ignition and supplied with oxygen sufficient for its combustion, it burns while floating in the inflammable gas, and forms red, yellow, or white flame. The flam from fuel is the larger the more slowly its combustion is effected. The flame itself is apt to be chilled by radiation, as into the heating surface of a steam-boiler, so that the combustion is not completed, and part of the gas and smoke pass off unburned.

(3) Oxygen or hydrogen either actually forming water, or existing in combination with the other constituents in the proportions which form water. Such quantities of oxygen and hydrogen are to left be out of account in determining the heat generated by the combustion. If the quantity of water actually or virtually present in each pound of fuel is so great as to make its latent heat of evaporation worth considering, that heat is to be deducted from the total heat of combustion of the fuel.

(4) Nitrogen, either free or in combination with other constituents. This

substance is simply inert.

(5) Sulphuret of iron, which exists in coal and is detrimental, as tending

to cause spontaneous combustion.

(6) Other mineral compounds of various kinds, which are also inert, and form the ash left after complete combustion of the fuel, and also the rlinker or glassy material produced by fusion of the ash, which tends to choze the grate.

Total Heat of Combustion of Fuels. (Rankine.)—The following table shows the total heat of combustion with oxygen of one pound of each of the substances named in it, in British thermal units, and also in ibs. of water evaporated from 212°. It also shows the weight of oxygen required to combine with each pound of the combustible and the weight of air necessary in order to supply that oxygen. The quantities of heat are given on the authority of MM. Favre and Silbermann.

Combustible,	Lbs.Oxy- gen per lb. Com- bustible.	Lb. Air	Total Brit- ish Heat- units.	Evapora- tive Power from 212° F., lbs.
Hydrogen gas Carbon imperfectly burned so as to make carbonic oxide Carbon perfectly burned so as to make tarbonic acid Diefiant gas, i lb	11/4	36 6 12 15 8/7	62,082 4,400 14,500 21,844	64.2 4.55 15.0 22.1
Various liquid hydrocarbons, 1 lb. Carbonic oxide, as much as is made by the imperfect combustion of 1 lb. of carbon, viz., 2½ lbs	,	6	from 21,700 to 19,000 10,000	from 2214 to 20

The imperfect combustion of carbon, making carbonic oxide, produces less than one third of the heat which is yielded by the complete combustion. The total heat of combustion of any compound of hydrogen and carbon is nearly the sum of the quantities of heat which the constituents would pro-

duce separately by their combustion. (Marsh-gas is an exception.)

In computing the total heat of combustion of compounds containing expens as well as hydrogen and carbon, the following principle is to be observed: When hydrogen and oxygen exist in a compound in the proper observed: when hydrogen and oxygen extent in a compound in the propertion to form water (that is, by weight one part of hydrogen to eight of oxygen), these constituents have no effect on the total heat of combustion. If hydrogen exists in a greater proportion, only the surplus of hydrogen above that which is required by the oxygen is to be taken into account. The following is a general formula (Dulong's) for the total heat of combus-

tion of any compound of carbon, hydrogen, and oxygen:

Let C, H, and O be the fractions of one pound of the compound, which consists respectively of carbon, hydrogen, and oxygen, the remainder being nitrogen, ash, and other impurities. Let h be the total heat of combustion of one pound of the compound in British thermal units. Then

$$h = 14,500 \left\{ C + 4.28 \left(H - \frac{O}{8} \right) \right\}$$

The following table shows the composition of those compounds which are of importance, either as furnishing oxygen for combustion, as entering into the composition, or as being produced by the combustion of fuel;

Names.	Symbol of Chemical Composition.	Proportions of Element by Weight.	Chemical Equivalent by Weight.	Proportions of Elements by Volume.
Air Water Ammonia Carbonic oxide Carbonic scid Olefiant gas Marsh-gas or fire-damp Sulphurous acid. Bulphuretted hydrogen. Sulphuret of carbon	NH, CO, CH, SH,	N 77 + O 23 H 2 + O 16 H 8 + N 14 C 12 + O 16 C 12 + O 32 C 12 + H 2 C 12 + H 4 S 32 + O 32 S 33 + H 2 S 64 + C 12	100 18 17 28 44 14 16 64 84 76	N 79 + O 21 H 2 + O H 3 + N C + O 3 C + H 4

622 FUEL.

Since each ib. of C requires 3% lbs. of O to burn it to CO₂, and air contains 23% of O, by weight, 3% + 0.23 or 11.6 lbs. of air are required to burn 1 lb. of C. Analyses of Gases of Combustion.—The following are selected from a large number of analyses of gases from locomotive boilers, to show the range of composition under different circumstances (P. H. Dudley, Trans. A. I. M. E., iv. 250):

Test.	CO2	co	0	N	
1	18.8	2.5	2.5	81.6	No smoke visible.
3	11.5		6		Old fire, escaping gas white, engine working hard,
3	8.5		8	88	Fresh fire, much black gas, " " "
4	2.3		17.2		Old fire, damper closed, engine standing still.
6 7	5.7		14.7		" smoke white, engine working hard.
6	8.4	1.2	8.4		New fire, engine not working hard.
	12	1	4.4		Smoke black, engine not working hard.
8	3.4		16.8		
9	6		13.5	81.5	" white, engine working hard.

In analyses on the Cleveland and Pittsburgh road, in every instance when the smoke was the blackest, there was found the greatest percentage of unconsumed oxygen in the product, showing that something besides the mere presence for oxygen is required to effect the combustion of the volatile carbon of fuels.

J. C. Hoadley (Trans. A. S. M. E., vi. 749) found as the mean of a great number of analyses of flue gases from a boiler using anthracite coal:

CO₁, 13.10; CO, 0.30; O, 11.94; N, 74.66.

The loss of heat due to burning C to CO instead of to CO, was 2.18%. The surplus oxygen averaged 113.3% of the O required for the C of the fuel, the

average for different weeks ranging from 88.6% to 1878.

Analyses made to determine the CO produced by excessively rapid firing gave results from 251% to 4.81% CO and 5.12 to 8.01% CO₂; the ratio of C in the CO to total carbon burned being from 43.80% to 48.55%, and the number of pounds of air supplied to the furnace per pound of coal being from 83.2 to 19.3 lbs. The loss due to burning C to CO was from 27.84% to 30.86 of the full power of the coal.

Temperature of the Fire. (Rankine, S. E., p. 288.)-By temperature of the fire is meant the temperature of the products of combustion at the instant that the combustion is complete. The elevation of that temperature above the temperature at which the air and the fuel are supplied to the furnace may be computed by dividing the total heat of combustion of one lb. of fuel by the weight and by the mean specific heat of the whole products of combustion, and of the air employed for their dilution under constant pressure. The specific heat under constant pressure of these prod

ucts is about as follows:
Carbonic-acid gas, 0.217; steam, 0.475; nitrogen (probably), 0.245; air.
0.238; ashes, probably about 0.200. Using these data, the following results are obtained for pure carbon and for oleflant gas burned, respectively, first, in just sufficient air, theoretically, for their combustion, and, second, when an equal amount of air is supplied in addition for dilution.

Fuel	Products	undiluted.	Products diluted.		
r uoi.	Carbon.	Oleflant Gas.	Carbon.	Oleflant Gas.	
Total heat of combustion, per lb Wt of products of combustion, lbs. Their mean specific heat Specific heat × weight Elevation of temperature, F	13 0.237 8.08	21,800 16.43 0.257 4.22 5050°	14,500 25 J. 288 5.94 2440°	21,800 81.86 0.248 7.9 2710°	

[The above calculations are made on the assumption that the specific heats of the gases are constant, but they probably increase with the increase of temperature (see Specific Heat), in which case the temperature would be less than those above given. The temperature would be further

reduced by the heat rendered latent by the conversion into steam of any

water present in the fuel.]

water present in the ruel.] **Hiso of Temperature in Combustion of Gases.** (Eng'g, March 12 and April 2, 1886.)—It is found that the temperatures obtained by experiment fall short of those obtained by calculation. Three theories have been given to account for this: 1. The cooling effect of the sides of the containing vessel; 2. The retardation of the evolution of heat caused by dissociation; 3. The increase of the specific heat of the gases at very high temperatures. The calculated temperatures are obtainable only as the condition that the gases shall combine instantaneously and simultaon the condition that the gases shall combine instantaneously and simultaneously throughout their whole mass. This condition is practically impossible in experiments. The gases formed at the beginning of an explosion dilute the remaining combustible gases and tend to retard or check the combustion of the remainder.

CLASSIFICATION OF SOLID FUELS.

Gruner classifies solid fuels as follows (Eng'g and M'g Jour., July, 1874):

Name of Fuel.	Ratio $\frac{O}{H}$ or $O + N +$	Proportion of Coke or Charcoal yielded by the Dry Pure Fuel
Pure cellulose Wood (cellulose and encasing matter) Peat and fossil fuel Lignite,† or brown coal Bituminous coals Anthracite	6 6 5	0.28 @ 0.30 .80 @ .35 .85 @ .40 .40 @ .50 .80 @ .90

The hituminous coals he divides into five classes as below:

		Elementary Composition.			Proportion of Coke	Nature and	
Name of Type.	C.	H.	о.	or O+N*.	yielded by Dis- tilla- tion.	Appear- ance of Coke,	
1. Long flaming dry coal, { 2. Long flaming fat}	75 @8 0	5.5@4.5	19.5@15	4@3	0.50@.60	Pulveru-	
or coking coals, or gas coals,	80@85	5.8@5	14.2@10	8@2	.60@.68	friable.	
8. Caking fat coals, or blacksmiths' coals,	84@89	5 @4.5	11 @5.5	2@1	.68@.74	Melted; some- what com- pact.	
4. Short flaming fat or caking coals, coking coals,	88@91	5.5@4.5	6.5@5.5	1	.74@.82	Melted; very com-	
5. Lean or anthra-	90 © 93	4.5@4	5.5@8	1	.82@.90	Pulveru lent.	

*The nitrogen rarely exceeds 1 per cent of the weight of the fuel.

† Not including bituminous lignites, which resemble petroleums.

Rankine gives the following: The extreme differences in the chemical composition and properties of different kinds of coal are very great. The proportion of free carbon ranges from 30 to 38 per cent; that of hydrocarbons of various kinds from 5 to 58 per cent; that of hydrocarbons of various kinds from 5 to 58 per cent; that of water, or oxygen and hydrogen in the proportions which form water, from an inappreciably small quantity to 27 per cent; that of ash, from 1½ to 28 per cent.

The numerous varieties of coal may be divided into principal classes as follows: 1, anthracite coal; 2, semi-bituminous coal; 3, bituminous coal; 4, long flaming or cannel coal; 5, lignite or brown coal.

Diminution of H and O in Series from Wood to Anthracite

(Groves and Thorp's Chemical Technology, vol. i., Fuels, p. 58.)

Substance.	Carbon.	Hydrogen.	Oxygen.
Woody fibre	52.65	5.25	42.10
Peat from Vulcaire	59.57	5.96	84.47
Lignite from Cologne	66.04	5.27	28.69
Earthy brown coal	73.18	5.88	21.14
Coal from Belestat, secondary	75.06	5:84	19.10
Coal from Rive de Gier	89.29	5.05	5.66
Anthracite, Mayenne, transition formation	91.58	8.96	4.48

Progressive Change from Wood to Graphite.

(J. S. Newberry in Johnson's Cyclopedia.)

	Wood.	Loss.	Lig- nite.	Loss.	Bitumi- nous coal	Loss.	Anthra- cite.	Loss.	Graph- ite.
Carbon	49.1	18.65	80.45	12.35	18.10	3.57	14.58	1.42	18.11
Hydrogen	6.8	8,25	8.05	1.85	1.20	0.93	0.27	0.14	0.13
Oxygen	44.6	24.40	20,20	18.13	2.07	1.32	0.65	0.65	0.00
	100.0	46.30	53,70	82.33	21.87	5.82	15.45	2.21	18.24

Classification of Coals, as Anthracite, Bituminous, etc.— Prof. Persifer Frazer (Traus. A. I. M. E., vi, 430) proposes a classifica-tion of coals according to their "fuel ratio," that is, the ratio the fixed car-bon bears to the volatile hydrocarbon.

In arranging coals under this classification, the accidental impurities, such as sulphur, earthy matter, and moisture, are disregarded, and the fuel constituents alone are considered.

	Carbon	Fixed	Volatile
	Ratio.	Carbon.	Hydrocarbon.
I. Hard dry anthracite. II. Semi-anthracite III. Semi-bituminous IV. Bituminous	100 to 12 12 to 8 8 to 5 5 to 0	100. to 92.81\$ 92.31 to 88.89 88.89 to 83.33 83.33 to 0.	0. to 7.69% 7.69 to 11.11 11.11 to 16.67 16.67 to 100

It appears to the author that the above classification does not draw the line at the proper point between the semi-bituminous and the bituminous coals, viz., at a ratio of C+V.H.C.=5, or fixed carbon 83.83%, volatile hycoals, viz., at a ratio of $C \to V$, H.C. = b, or fixed carbon 53.338, volatile rydrocarbon 16.67%, since it would throw many of the steam coals of Clearfield and Somerset counties, Penn., and the Cumberland, Md., and Pocahontas, Va., coals, which are practically of one class, and properly rated as semi-bituminous coals, into the bituminous class. The dividing line between the semi-anthracite and semi-bituminous coals, C + V. H.C. = S, would place several coals known as semi-anthracite in the semi-bituminous class. The following is proposed by the author as a better classification:

Ca	rbon Ratio.	Fixed Carbon.	Vol. H.C.
 Hard dry anthracite 	100 to 12	100 to 92.31%	0 to 7.69%
II. Semi-anthracite	12 to 7	92.81 to 87.5	7.69 to 12.5 ·
III. Semi-bituminous	7 to 8	87.5 to 75	12.5 to 25
IV. Bituminous	8 to 0	75 to 0	25 to 100

Bhode Island Graphitic Anthracite.—A peculiar graphite is found at Cranston, near Providence, R. I. It resembles both graphite and anthracite coal, and has about the following composition (A. E. Hunt. Trans. A. I. M. E., xvii., 678): Graphitic carbon, 78%; volatile matter, 2.60%; silica, 15.06%; phosphorus, .045%. It burns with extreme difficulty.

ANALYSES OF COALS.

Composition of Pennsylvania Anthracites. (Trans. A. I. M. E., xiv., 706.)—Samples weighing 100 to 200 lbs. were collected from lots of 100 to 200 tons as shipped to market, and reduced by proper methods to laboratory samples. Thirty-three samples were analyzed by McCreath, giving results as follows. They show the mean character of the coal of the more important coal-beds in the Northern field in the vicinity of Wilkesbarre, in the Peters Middle (Lablen) field in the vicinity of Hayleton in the Warner. the Eastern Middle (Lehigh) field in the vicinity of Hazleton, in the Western

Middle field in the vicinity of Shenandoah, and in the Southern field between Mauch Chunk and Tamaqua.

Name of Bed.	Name of Field.	Water.	Volatile Matter.	Fixed Carbon.	Ash.	Sulphur.	Vol. Matter. Per cent of total combustible.	Ratio, C+V.H.C.
Mammoth	W. Middle W. Middle Southern W. Middle W. Middle Southern Northern	8.71 4.18 3.54 3.16 3.01 3.04 3.41 3.09 8.42 1.30	8.08 8.08 8.72 8.72 4.13 8.95 8.98 4.28 4.38 8.10	86.40 86.38 81.59 81.14 87.98 82.66 80.87 83.81 83.27 83.34	6.22 5.92 10.65 11.08 4.88 9.68 11.23 6.18 8.20 6.23	.58 .49 .50 .90 .50 .46 .51 .64	4.69 4.85 5,00	28.07 27.99 21.93 21.88 21.82 90.98 20.82 19.62 19.00 10,29

The above analyses were made of coals of all sizes (mixed). When coal is screened into sizes for shipment the purity of the different sizes as regards ash varies greatly. Samples from one mine gave results as follows;

	Scre	eened	Anal	yses.
Name of Coal.	Through inches.	Over inches.	Fixed Carbon.	Ash.
Egg	2.5	1.75	88.49	5.66
Stove Chestnut	1.75 1.25	1,25 .75	89.67 80.72	10.17 12.67
Pea Buckwheat	.75	.50 .25	79 05 76.92	14.66 16.62
Duck wheat	.00	.40	10.84	10.02

Bernice Basin, Pa., Coals.

	Water.	Vol. H.C.	Fixed C.	Aah.	Sulphur.
Bernice Basin, Sullivan Lycoming Cos.; range o	and (0.96	8.56	82.52	8,27	0,24
Transming Cos + range 6	aud { to	to	to	to	to
Theorning cost tenso	1 1.97	8.56	89.89	9.84	1.04

This coal is on the dividing-line between the anthracites and semi-anthracites, and is similar to the coal of the Lykens Valley district. More recent analyses (Trans. A. I. M. E., xiv. 721) give:

Water.	Vol. H.C.	Fixed Carb.	Aah.	Sulphur.
Working seam 0 65	9,40	83.6 9	5.84	0.91
Working seam 0 65 60 ft. below seam 8.67	15.42	71.84	8.97	0.59

The first is a semi-anthracite, the second a semi-bituminous.

Space Occupied by Anthracite Coal. (J. O. I. W., vol. iii.)—The cubic contents of 2240 lbs, of hard Lehigh coal is a little over 36 feet; an average Schuylkill W. A., 37 to 38 feet; Shamokin, 38 to 39 feet; Lorberry, rearly 41.

According to measurements made with Wilkesbarre anthracite coal from the Wyoming Valley, it requires 32.2 cu. ft. of lump, 33.9 cu. ft. broken, 34.5 cu. ft. egg, 34.8 cu. ft. of stove, 35.7 cu. ft. of chestnut, and 36.7 cu. ft. of pea, to make one ton of coal of 3340 lbs.; while it requires 23.8 cu. ft. of lump, 30.3 cu. ft. of broken, 80.8 cu. ft. of egg, 31 1 cu. ft. of stove, \$1.9 cu. ft. of chestnut, and 32.8 cu. ft. of pea, to make one ton of 2000 lbs.

Composition of Anthracite and Semi-bituminous Coals, (Trans. A. I. M. E., vi. 430.)—Hard dry anthracites, 16 analyses by Rogers, show a range from 94.10 to 82.47 fixed carbon, 1.40 to 9.53 volatile matter, and 4.50 to 8.00 ash, water, and impurities. Of the fuel constituents alone, the fixed carbon ranges from 98.88 to 89.68, and the volatile matter from 1.47 to 10.37, the corresponding carbon ratios, or C + Vol. H.C. being from 67.02 to 8.64.

Semi-anthracites.—12 analyses by Rogers show a range of from 90.23 to 74.55 fixed carbon, 7.07 to 13.75 volatile matter, and 2.20 to 12.10 water, ash, and impurities. Excluding the ash, etc., the range of fixed carbon is 93.75 to 84.42, and the volatile combustible 7.27 to 15.58, the corresponding carbon ratio being from 12.75 to 5.41.

front hitemateries (Scale, -10 analyses of Penna, and Maryland coals give fixed outlier (\$2.00 ft.20), and ask, water, and importion 4 to 13.20. The percentage of the fact constituents is fixed carbon 79.74 to 98.20, volatile combinations (\$1.20 to 20.18, and the carbon ratio 11.41 to 26.18.

Amorican Semi-bituminous and Bituminous Coals.

(Selected chiefly from various papers in Trans. A. I. M. E.)

	Model- ure.	Vol. Hydro- arbon.	Pixed Carbon	Ash.	Sal- phur.
Pennet Semblituminers:		i—			
•	1 .79	13.84	28.46	6.00	.91
Brown Top, extremen of 5	28	17.26	76.14	4 81	.88
	11.27	14.32	77.77	6.63	0.66
Monnerant (%), extremes of 5	11.80	18.51	65.90	10.62	8.08
Binir Co., average of 5	1.07	26.72	60.77	9.45	2.20
(Sumboth Ch., average of 7, 1	0.74	01.01	40.04	7.51	1.98
lower had, B.	0.74	21.21	68.94	7.51	1.90
Chambrin Co., 1, L	1.14	17.18	73.42	6.58	1.41
upper hed, O. S	1	1			1.31
— Cambria Co., Houth Fork, 1	2725	15.51	78.60	5.84	
Centre (le, 1	0.60	22 60	68.71	5.40	2.69
Clearfield Co., average of 9, 1	0.70	23.94	69.28	4.62	1.42
upper hed, O	****	42.02	0.7.20	27.0.0	
(finarileld (for, average of 8,)	0.81	21.10	74.08	3.36	0.42
lower bad, D. S	(0.41	20.09	66.69	2.65	0.43
Clearfield Co., range of 17 anal		to	to	2.00 to	to
() leating ()or tanks of it sust.	1.94	25.19	74.02	7.65	1.79
Hituminous i	1		.4.00	1.00	1
Jufferson Co., average of 26	1.21	82.58	60.99	8.76	1.00
(farion ('o., average of 7	1.97	88.60	54.15	4.10	1.19
Armstrong Co., 1	1.18	42.55	49.69	4.58	2.00
Compeliaville Coal	1.26	80.10	59.61	8.28	.78
(loke from Conn'ville (Standard)		0.01	87.46	11.82	.69
Youghlogheny Coal	1 08	86.49	59.05	2.61	.81
Pittiburgh, Oosan Mins	.28	89.09	57.88	8.80	
	٠		•	•	•

The percentage of volatile matter in the Kittaning lower bed B and the Freepoint lower had D increases with great uniformity from east to west; thus:

		Volatile Matter.	Fixed Carbon.
Clearfield Co	, bed D	20 09 to 25.19	68.73 to 74,76
11 11	" "В	92.56 to 26.18	64 87 to 69.68
Clarion Co.,	" В	85,70 to 49,55	47.51 to 55.44
11	" 15		A1 80 to 56 86

Connellaville Coal and Coke. (Trans. A. I. M. E., xiii. 332.)— The Connellaville coal field, in the southwestern part of Pennsylvania, is attin shout 3 miles wide and 60 miles in length. The mine workings are confined to the Pittsburgh seam, which here has its best development as to size, and its quality best adapted to coke-making. It generally affords from 7 to 8 feel of coal.

The following analyses by T. T. Morrell show about its range of composi-

	Mointure	Vol. Mat.	Fixed C.	Ash.	Sulphur.	Phosph's.
Herold Mine	ny, 1 , , .	BH . NY	60.79	8.44	.67	.013
Herold Mine Kinta Mine,	(1.79	14.18	86.46	9.52	1.32	.02

In comparing the composition of coals across the Appalachian field, in the neutrin section of Prints Irania, it will be noted that the Connelisville earlier, accupies a peculiar position between the rather dry semi-binumious coals maintain it is not the west.

theneath the (Vamella tille or l'ittsburgh coal bed occurs an interval of from 400 to 600 from the lower measures," separating it from the lower burden't e coal measures of Western Pomertrania. The following tables

show the great similarity in composition in the coals of these upper and lower coal-measures in the same geographical belt or basin.

Analyses from the Upper Coal-measures (Penna.) in a Westward Order.

Localities.	Moisture.	Vol. Mat.	Fixed Carb.	Ash.	Sulphur.
Anthracite	1.85	8.45	89.06	5.81	0.80
Cumberland, Md	0.89	15.52	74.28	9.29	0.71
Salisbury, Pa	1.66	22.3 5	68.77	5.96	1.24
Connellsville, Pa	•••	81.38	60. 30	7.24	1.09
Greensburg, Pa	1.02	88.50	61.84	8.28	0.86
Irwin's, Pa		87.66	54.44	5.86	0.64

Analyses from the Lower Coal-measures in a Westward Order.

Localities.	Moisture.	Vol. Mat.	Fixed Carb.	Ash.	Sulphur.
Anthracite	1.35	8.45	89.06	5.81	Ø 80
Broad Top	0.77	18.18	78.84	6.69	1.02
Bennington	1.40	27.23	61.84	6.93	2.60
Johnstown		16.54	74.46	5.96	1.86
Blairsville	0.92	24.36	62.22	7.69	4.92
Armstrong Co	0.96	88.20	52.03	5.14	8.66

Pennsylvania and Ohio Bituminous Coals. Variation in Character of Coals of the same Beds in different Districts.—From 50 analyses in the reports of the Pennsylvania Geological Survey, the following are selected. They are divided into different groups, and the extreme analysis in each group is given, ash and other impurities being neglected, and the percentage in 100 of combustible matter being alone considered.

	No. of Analyses		Vol. H. C.	Carbon Ratio.
Waynesburg coal-bed, upper bench Jefferson township, Greene Co Hopewell township, Washington Co Waynesburg coal-bed, lower bench Morgan township, Greene Co Pleasant Valley, Washington Co		59.72 53.22 60.69 54.81	40.28 46.78 89.81 45.69	1.48 1.13 1.54 1.19
Sewickley coal-bed. Whitely Creek, Greene Co. Gray's Bank Creek, Greene Co. Pittsburgh coal-bed: Upper bench, Washington Co.		64.89 60.85	85.61 89.65 89.13	1.80 1.52 1.65
Lower bench, "" Main bench, Greene Cc	5 8	59.11 63.54 50.97 61.80 54.33	40.89 86.46 49.08 88.20 45.67	1.20 1.74 1.04 1.61 1.19
Frick & Co., Washington Co., average Lower bench, Greene Co Somerset Co., semi-bituminous (showing decrease of vol. mat. to the eastward). Beaver Co., Pa Diehl's Bank, Georgetown	} 8 7	66.44 57.83 {79.73 {75.47 40.68	83.56 42.17 20.27 24.58 59.82	1.98 1.37 3.93 3.07
Onto. Pittsburgh coal-bed in Ohio:		62.57	87.48	1.66
Jefferson Co., Ohio		61.45 63.46 66.14 63.46 64.93	38.55 36.54 33.86 36.54 35.07	1.59 1.78 1.95 1.78 1.85
Pomeroy Co., Ohio		60.92	89.08 87.67	1.55 1.65

Analyses of Southern and Western Coals.

Zamary web or Sou	rnorn wh	u west	PLII COMI	150	
	Moisture.	Vol. Mat.	Fixed C.	Ash.	Sul- phur.
OHIO. Hocking Valley	§ 5.00		53.15	9.05	0.44
MARYLAND.	7.40	29.20	60.45	2.95	0.93
Cumberland.,	95 1.23	19.18 15.47	72.70 78.51	6.40	0.78
Virginia.				9.09	0.70
South of James River, 23 anal- yses, range	from 0.67	27.28 38.60	46.70 67.83	2.00 15.76	2.89
Average of 23	1.48	82.24	58.89	7.72	1.45
North of James River, eastern outcrop.	0.40 1.79	19.60 23.96	71.00 59.98	10.00 14.28	1
Carbonite or Natural Coke	1.57	9.64	79.98	8.86	0.00
Western outcrop, 11 analyses,		14.26 21.38	81.61 54.97	2,24 3,35	0.23
range Average of 11	} to	30.50 26.06	70.80	22.60	
	5 0.52	23.90	63.75 74.20	10.06	0.52
Pocahontas Flat-top* (Castner & Curran's Circular) WEST VIRGINIA (New River.)	4		75.22	5.68	0,28
Quinnimont, † 8 analyses	from 0.76	17.57	75.89	1.11	0.98
	to 0.94		79.40 69.00	1.07	0.80
Nuttalburgh † Virginia and Kentucky.	1.85		70,67	2.10	0.08
Big Stone Gap Field, 19 anal-	from 0.80	81.44	54.80	1.78	0.56
yses, range	} to 2.01	36.27	63.50	8.25	1.72
Kentucky. Pulaski Co., 3 analyses, range	from 1.26		60.85	1.28	0.40
Muhlenberg Co., 4 analyses,	(10 1.32		52.48 58.80	5.52 8.40	1.00
range	to 7.06	88.70	58.70	6.50	8.16
Pike Co., Eastern Ky., 87 an- alyses, range	l) to 1.60	26.80 41.00	67.60 50.37	8.80 7.80	0.97
Kentucky Cannel Coals, 5 an	from,	40.201	59.80 coke	8.81	0.96
alyses, range	} to,	66.301	33.70 coke	4.80	1.39
Tennessee, Scott Co., Range of several. T.	from 70		46.61	16.94	8.87
Roane Co., Rockwood,	1 to 1,88		61.66 60.11	1.11	0.77
Hamilton Co., Melville	2,74	26.50	67.08	8.68	91
Marion Co., Etna Sewance Co., Tracy City	94 1.60		68.94 61.00	11.40 7.80	1.19
Kelly Co., Whiteside	1.80		74.20	2.70	
GEORGIA.	1.20	28.05	60.50	15.16	0.84
ALABAMA.		10.00	00.50		0.02
Warren Field:	8.01	42.76	48.80	8.21	2.72
Jefferson Co., Birmingham "Black Creek	.12	26.11	71.64	2.03	.10
Tuscaloosa Co	1.59		54,64 53.08	5.45 11.84	1.88
Bibb Co Coke Vein	1.78	80.60	66.58	1.09	.04
* Analyses of Pocahontas Con	al by John P	attinson, I	F.C.S., 1889):	

[◆] Analyses or Vol. Ο. N. C. H. Ash. Water. Coke. Mat. Lumps... 86.51 4.44 4.95 0.66 0.61 1.54 1.29 78.8 21.3 Small ... 88,13 4.29 5.33 0.66 0.56 4.63 1,40 79.8 30.2 † These coals are coked in beehive ovens, and yield from 63% to 64% of coke. † This field covers about 120 square miles in Virginia, and about 30 square 4.95

This next covers about to equate mines in virginia, and about to equate miles in Kentucky.

The principal use of the cannel coals is for enriching illuminating-gas.

Volatile matter including moisture.

Single analyses from Morgan, Rhea, Anderson, and Roane counties fall—ithin this range.

	Moisture.	Vol Mat.	Fixed C.	Ash.	Sul- phur.
TEXAS. Eagle Mine	8.54 1.91 1.87 0.84 0.45	80.84 20.04 16.42 29.85 21.6	50.69 62.71 68.18 50.18 45.75	15.85 18.09	3.15
Indiana.					
Caking Coals. Parke Co	4.50 2.35 7.00 3.50 8.50 2.50 5.50	45.50 45.25 89.70 45.00 31.00 44.75 86.00	45.50 51.60 47.30 46.00 57.50 51.25 53.50	●1.50	
ILLINOIS.† Bureau Co.: Ladd Seatonville Christian Co.: Pana Clinton Co.: Trenton Fulton Co.: Cuba Grundy Co.: Morris Jackson Co.: Big Muddy La Salle Co.: Streator Logan Co.: Lincoln Macon Co.: Niantic Macoupin Co.: Gillissple Staunton Madison Co.: Cullinsville Marion Co.: Centralia McLeah Co.: Pottstown Perry Co.: Du Quoth Sangamon Co.: Sarclay St. Clair Co.: St. Bernard Vermilion Co.: Danville Will Co.: Wilmington	12.0 10.0 7.2 13.3 4.2 7.1 6.4 12.0 8.4 7.9 10.4 6.8 9.3 8.8	32.3 33.8 36.4 30.4 36.4 32.1 30.6 35.8 35.0 36.3 30.6 36.7 57.1 29.9 34.0 35.5 30.3 27.3 30.9 32.8	42.5 40.9 46.9 52.0 48.6 49.7 54.6 44.5 47.4 45.3 46.1 26.8 45.5 45.5 49.9 44.4 58.9	18.2 15.8 9.5 4.3 10.8 11.1 8.3 8.9 12.1 8.5 11.5 6.8 10.3 16.1 8.5 17.1 6.4 8.5	0.9 1.5 2.4 1.5 8.5 8.9 0.9

^{*}Indiana Block Coal (J. S. Alexander, Trans. A. I. M. E., iv. 100),—The typical block coal of the Brazil (Indiana) district differs in chemical composition but little from the coking coals of Western Pennsylvania. The physical difference, however, is quite marked; the latter has a cuboid structure made up of bituminous particles lying against each other, so that under the action of heat fusion throughout the mass readily takes place, while block coal is formed of alternate layers of rich bituminous matter and a charcoal-like substance, which is not only very slow of combustion, but so

charcoal-like substance, which is not only very slow of combustion, but so retards the transmission of heat that agglutination is prevented, and the coal burns away layer by layer, retaining its form until consumed.

An ultimate analysis of block coal from Sand Creek by E. T. Cox gave: C, 72.94; H, 4.50; O, 11.77; N, 1.79; ash, 4.50; moisture, 4.50.

† The Illinois coals are generally high in moisture, volatile matter, suphur and ash, and are consequently low in heating value. The range of quality is a wide one. The Big Muddy coal of Jackson Co., which has a high reputation as a steam coal, has, according to the analysis given above, about 38% of volatile matter in the total combustible, corresponding to the coals of Western Pennsylvania and Ohio, while the Staunton coal has 68% reanking it among the nonzer varieties of lignite. A boiler-test with this coal ranking it among the poorer varieties of lignite. A boiler-test with this coal (see p. 636, also Trans. A. S. M. E., v. 266) gave only 6.19 lbs. water evaporated from and at 212° per lb. combustible. The Staunton coal is remarkable for the high percentage of volatile matter, but it is excelled in this respect by

	Moisture.	Vol. Mat.	Fixed C.	Ash.	Sul- phur.
Iowa.*					
Hiteman	4.99	85.27	25.87	94 97	
Keb	9.81	37.49	44.75		
Flaglers		40.16	37.69		
Chisholm	9.18	40.42	39.58	10 82	
Missouri.*	•		00.00	20.00	
Brookfield	4.34	40.27	50,60	4 70	ح.
Mendota	9.03	37.48	46.24		
Hamilton	5.06	34.24	47.69		
Lingo	7.83	38.29	47.24		
	1.00	90.20	41.64	1.14	
Nebraska.*	0.04				
Hastings	0.21	27.82	60.88	11.09	
Wyoming.*	l 、 !				
Cambria	4.2	40.6	41.5	13.7	
	2.5	87.4	87.9	22.2	
Goose Creek	9.7	40.2	46.3	8.8	
	13.92	36.78	42.03	7.27	
Deek Creek	12.8	85.0	47.7	3.6	
Sheridan	6.04	42.37	35.57	16.02	
Colorado.1					
Sunshine, Colo, average Newcastle, " "	2.8	36.3	37.1	23.8	
Newcastle, " "	1.7	37.95	48.6	11.6	
El Moro. " "	1.32	38.23	55.86	3.59	
Crested Buttes. "	1.10	23.20	72.60		
UTAH (Southern).					
Castledale	8.48	42.81	47.81+	0 73	
Cedar City	8.50	48.66	48.11+		
OREGON.	0.00			0.00	
Coor Por	15.45	41.55	84.95	احد ہ	2.58
Coos Bay	17.27	44.15	82.40	6.18	1.37
Yaquina Bay	18.03	46.20	82.60	7.10	1.07
John Day River	4.55	40.00	48.19	7.26	.60
John Day River	6.54	84.45	52.41	5.95	.65
VANCOUVER ISLAND.	0.04	07.70	OW. 21	0.50	.00
Comox Coal	1.7	27.17	68.27	2.86	
	4	~ /	· · · · · · · · · · · · · · · · · · ·	~.001	

the Boghead coal of Linlithgowshire, Scotland, an analysis of which by Dr. Penny is as follows: Proximate—moisture 0.84; vol. 67.95; fixed C, 9.54, ash, 21.4; Ultimate-C,68.94; H, 8.86; O, 4.70; N, 0.96; which is remarkable for the high percentage of H

*The analyses of Iowa, Missouri, Nebraska, and Wyoming coals are selected from a paper on The Heating Value of Western Coals, by Wm. Forsyth, Mech. Engr. of the C., B. & Q. R. R., Engr. Jan. 17, 1895.

†Includes sulphur, which is very high. Coke from Cedar City analyzed:

Water and volatile matter, 1.42; fixed carbon, 76.70; ash, 16.61; sulphur, 5.27.

Colorado Coals.-The Colorado coals are of extremely variable composition, ranging all the way from lighte to anthracite. G. C. Hewitt (Trans. A. I. M. E., xvii. 377) says: The coal seams, where unchanged by heat and flexure, carry a lightee containing from 5% to 20% of water. In the south-eastern corner of the field the same have been metamorphosed so that in four miles the same seams are an anthracite, coking, and dry coal. In the basin of Coal Creek the coals are extremely fat, and produce a hard, bright, sonorous coke. North of coal basin half a mile of development shows a gradual change from a good coking coal with patches of dry coal to a dry coal that will barely agglutinate in a beenive oven. In another half mile the same seam is dry. In this transition area, a small cross-fault makes the coal fat for twenty or more feet on either side. The dry seams also present wide chemical and physical changes in short distances. A soft and loosely bedded coal has in a hundred feet become compact and hard without the intervention of a fault. A couple of hundred feet has reduced the water of combination from 12% to 5%.

Western Arkansas and Indian Territory. (H. M. Chance, Trans. A. I. M. E. 1890.)—The Choctaw coal-field is a direct westward extension of the Arkansas coal-field, but its coals are not like Arkansas coals, ex-

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sion of the Arkansas coal-field, but its coals are not like Arkansas coals, except in the country immediately adjoining the Arkansas line.

The western Arkansas coals are dry semi-bituminous or semi-anthracitic coals, mostly non-coking, or with quite feeble coking properties, ranging from 145 to 165 in volatile matter, the highest percentage yet found, according to Mr. Winslow's Arkansas report, being 17 655.

In the Mitchell basin, about 10 miles west from the Arkansas line, coal recently opened shows 198 volatile matter; the Mayberry coal, about 8 miles farther west, contains 23% volatile matter; and the Bryan Mine coal, about the same distance wast shows 36% volatile matter. the same distance west, shows 26% volatile matter. About 80 miles farther west, the coal shows from 38% to 4116% volatile matter, which is also about the percentage in coals of the McAlester and Lehigh districts.

Western Lignites. (R. W. Raymond, Trans. A. I. M. E., vol. ii. 1873.)

	C.	Н,	N.	0.	s.	Mois- ture.	Ash.	Calorific Power, calories.
Monte Diabolo	59.72 64.84			15.69				
Weber Cañon, Utah Echo Cañon, Utah	69.84			10.99				
Carbon Station, Wyo	69.14			15.20	1.07	11.56 8.06		
Coos Bay, Oregon,	56.24	3,38	0.42	21.82	0.81	13.28		4565
Alaska	55.79 67.67			19.01 12.80				4610 6428
Canon City, Colo	67.58	7.42	4225	13.42	0.63	5.18	5.77	7330
Baker Co., Ore	60.72	4.30		14.42	2.08	14.68	3.80	5602

The calorific power is calculated by Dulong's formula.

$$8080C + 34462 \left(H - \frac{O}{8}\right)$$
,

deducting the heat required to vaporize the moisture and combined water, that is, 587 calories for each unit of water. 1 calorie = 1.8 British thermal

Analyses of Foreign Coals. (Selected from D. L. Barnes's paper on American Locomotive Practice, A. S. C. E., 1893.)

	Volatile Matter.	Fixed Carbon.	Λsh.	
Great Britain: South Wales. "" Lancashire, Eng. Derbyshire, "" Durham, "" Scotland. Staffordshire, Eng. South America: Chili, Conception Bay "Chiroqui. Brazil. Canada: Nova Scotla. Cape Breton. Australia Anstralian lignite. Sydney, South Wales. Borneo. Van Diemen's Land.	8.5 6.2 17.2 17.7 15.05 17.1 17.5 20.4 21.98 24.11 24.35 40.5 26.9 15.8 14.98 26.5 6.16	88.3 92.8 80.1 79.5 63.1 78.6 70.55 82.25 67.9 60.7 67.6 64.3 82.39 70.3 63.4	3.2 1.5 2.4 1.1 19.8 2.4 1.0 7.52 36.91 13.4 1.6 12.5 5.5	

An analysis of Pictou, N. S., coal, in Trans. A. I. M. E., xiv. 560, is: Vol., 29.63; carbon, 56.98; ash, 13.89; and one of Syduey, Cape Breton, coal is: vol., 84.07; carbon, 61.43; ash, 4.50.

Nixon's Navigation Welsh Coal is remarkably pure, and contains not more than 8 to 4 per cent of ashes, giving 88 per cent of hard and lustrous coke. The quantity of fixed carbon it contains would classify it among the dry coals, but on account of its coke and its intensity of combustion it belongs to the class of fat, or long-flaming coals.

Chemical analysis gave the following results: Carbon, 90.27; hydrogen,

Chemical analysis gave the following results: Carbon, 9.24; hydrogen, 4.39; sulphur, 69; nitrogen, 49; oxygen (difference), 4.16.

The analysis showed the following composition of the volatile parts: Carbon, 22.53; hydrogen, 34.96; O + N + S, 42.51.

The heat of combustion was found to be, as a result of several experiments, 8864 calories for the unit of weight. Calculated according to its composition, the heat of combustion would be 8805 calories = 15,849 British

thermal units per pound.

This coal is generally used in trial-trips of steam-vessels in Great Britain. Sampling Coal for Analysis.—J. P. Kimball, Trans. A. I. M. E., xii. 317, says: The unsuitable sampling of a coal-seam, or the improper preparation of the sample in the laboratory, often gives rise to errors in determinations of the ash so wide in range as to vitiate the analysis for all practical purposes; every other single determination, excepting moisture, showing its relative part of the error. The determination of sulphur and seame all will likely to expect they are interested in termination. ash are especially liable to error, as they are intimately associated in the

Wm. Forsyth, in his paper on The Heating Value of Western Coals (Eng'g News, Jan. 17, 1895), says: This trouble in getting a fairly average sample of anthracite coal has compelled the Reading R. R. Co., in getting their samples, to take as much as 300 lbs. for one sample, drawn direct from the chutes, as

it stands ready for shipment.

The directions for collecting samples of coal for analysis at the C., B. & Q.

laboratory are as follows:

Two samples should be taken, one marked "average," the other "select." Each sample should contain about 10 lbs., made up of lumps about the size of an orange taken from different parts of the dump or car, and so selected that they shall represent as nearly as possible, first, the average lot; second, the best coal

An example of the difference between an "average" and a "select" An example of the difference of the sample, taken from Mr. Forsyth's paper, is the following of an Illinois coal:

Moisture. Vol. Mat. Fixed Carbon. Ash.

1.36 27.69 85.41 85.54 1.90 84.70 48.23 15.17

The theoretical evaporative power of the former was 9.13 lbs. of water from and at 212° per lb. of coal, and that of the latter 11.44 lbs.

Relative Value of Fine Sizes of Anthracite.—For burning

on a grate coal-dust is commercially valueless, the finest commercial anthracites being sold at the following rates per tou at the mines, according to an address by Mr. Eckley B. Coxe (1893):

Size.	Range of Size.	Price at Mines.
Chestnut	. 11/4 to 3/4 inch	\$2.75
Pea	. 36 to 9/16	1.25
Buckwheat	. 9/16 to 3∕s	0.75
Rice	. '34 to 3716	0.25
Barley	. 8/18 to 2/82	0.10

But when coal is reduced to an impalpable dust, a method of burning it becomes possible to which even the finest of these sizes is wholly unadapted; the coal may be blown in as dust, mixed with its proper proportion

of air, and no grate at all is then required.

Pressed Fuel. (E. F. Loiseau, Trans. A. I. M. E., vili. 314.)—Pressed fuel has been made from anthracite dust by mixing the dust with ten per cent of its bulk of dry pitch, which is prepared by separating from tar at a temperature of 572° F. the volatile matter it contains. The mixture is kept heated by steam to 212°, at which temperature the pitch acquires its comenting properties, and is passed between two rollers, on the periphery of which are milled out a series of semi-oval cavities. The lumps of the mixture, about the size of an egg, drop out under the rollers on an endless belt which carries them to a screen in eight minutes, which time is sufficient to cool the lumps, and they are then ready for delivery.

The enterprise of making the pressed fuel above described was not commercially successful, on account of the low price of other coal. In France, however, "briquettes" are regularly made of coal-dust (bituminous and

semi-bituminous).

BELATIVE VALUE OF STEAM COALS.

The heating value of a coal may be determined, with more or less approximation to accuracy, by three different methods.

1st. by chemical analysis; 2d. by combustion in a coal calorimeter; 3d, by actual trial in a steam-boiler. The first two methods give what may be

The securacy of the first two methods depends on the precision of the method of analysis or calorimetry adopted, and upon the care and skill of the operator. The results of the third method are subject to numerous sources of variation and error, and may be taken as approximately true only for the particular conditions under which the test is made. Analysis and calorimetry give with considerable accuracy the heating value which may be obtained under the conditions of perfect combustion and complete absorption of the heat produced. A boiler test gives the actual result under conditions of more or less imperfect combustion, and of numerous and variable wastes. It may give the highest practical heating value, if the conditions of grate-bars, draft, extent of heating surface, method of firing, etc., are the best possible for the particular coal tested, and it may give results far beneath the highest if these conditions are adverse or unsuitable to the

The results of boiler tests being so extremely variable, their use for the purpose of determining the relative steaming values of different coals has requently led to false conclusions. A notable instance is found in the record of Prof. Johnson's tests, made in 1844, the only extensive series of tests of American coals ever made. He reported the steaming value of the Lehigh Coal & Navigation Co.'s coal to be far the lowest of all the anthracites, a result which is easily explained by an examination of the conditions under which he made the test, which were entirely unsulted to that coal. He also reported a result for Pittsburgh coal which is far beneath that now obtainable in every-day practice, his low result being chiefly due to the use

of an improper furnace.

or an improper furnace.

In a paper entitled Proposed Apparatus for Determining the Heating Power of Different Coals (Trans. A. I. M. E., xiv. 727) the author described and illustrated an apparatus designed to test fuel on a large scale, avoiding the errors of a steam-boiler test. It consists of a fire-brick furnace enclosed in a water-casing, and two cylindrical shells containing a great number of tubes, which are surrounded by cooling water and through which the gases of combination pass while being cooled. No steam is generated in the agreements but materia pages of the combined the combined of t paratus, but water is passed through it and allowed to escape at a tempera-ture below 200° F. The product of the weight of the water passed through the apparatus by its increase in temperature is the measure of the heating value of the fuel.

There has been much difference of opinion concerning the value of chemical analysis as a means of approximating the heating power of coal. was found by Scheurer-Kestner and Meunier-Dollfus, in their extensive series of tests, made in Europe in 1868, that the heating power as determined by calorimetric tests was greater than that given to chemical analysis accord-

ing to Dulong's law.

Recent tests made in Paris by M. Mahler, however, show a much closer agreement of analysis and calorimetric tests. A brief description of these tests, translated from the French, may be found in an article by the author in The Mineral Industry, vol. i. page 97.

Dulong's law may be expressed by the formula,

Heating Power in British Thermal Units = 14,500C + 62,500 $\left(H - \frac{O}{g}\right)$,*

in which C, H, and O are respectively the percentage of carbon, hydrogen, and oxygen, each divided by 100. A study of M. Maher's calorimetric tests shows that the maximum difference between the results of these tests and the calculated heating power by Dulong's law in any single case is only a little over 3%, and the results of 31 tests show that Dulong's formula gives an average of only 47 thermal units less than the calorimetric tests, the average total heating value being over 14,000 thermal units, a difference of less than 4/10 of 1%.

Heating Power = $14,650C + 62,025 \left(H - \frac{(O+N)-1}{8}\right)$.

^{*} Mahler gives Dulong's formula with Berthelot's figure for the heating value of carbon, in British thermal units,

634 PURL

Mahler's calorimetric apparatus consists of a strong steel vessel or "bomb" immersed in water, proper precaution being taken to prevent radiation. One gram of the coal to be tested is placed in a platinum boat within this bomb, oxygen gas is introduced under a pressure of 20 to 25 atmospheres, and the coal ignited explosively by an electric spark. Combustion is complete and instantaneous, the heat is radiated into the surrounding water, weighing 2200 grams, and its quantity is determined by the rise in temperature of this water, due corrections being made for the heat capacity of the apparatus itself. The accuracy of the apparatus is remarkable, duplicate tests giving results varying only about 2 parts in 1000.

tests giving results varying only about 2 parts in 1000.

The close agreement of the results of calorimetric tests when properly conducted, and of the heating power calculated from chemical analysis, indicates that either the chemical or the calorimetric method may be accepted as correct enough for all practical purposes for determining the total heating power of coal. The results obtained by either method may be taken as a standard by which the results of a boiler test are to be compared, and the difference between the total heating power, and the result of the boiler test is a measure of the inefficiency of the boiler under the con-

ditions of any particular test.

In practice with good anthracite coal, in a steam-boller properly proportioned, and with all conditions ravorable, it is possible to obtain in the steam 8% of the total heat of combustion of the coal. This result was nearly obtained in the tests at the Centennial Exhibition in 1876, in five different bollers. An efficiency of 70% to 75% may exhibition in 1876, in five different tollers. An efficiency of 70% to 75% may exhibition in 1876, in five different tollers. With bituminous coals it is difficult to obtain as close an approach to the theoretical maximum of economy, for the reason that some of the volatile combustible portion of the coal escapes unburned, the difficulty increasing rapidly as the content of volatile matter increases beyond 20%. With most coals of the Western States it is with difficulty that as much as 60% or 65% of the theoretical efficiency can be obtained without the use of gas-producers.

The chemical analysis beretofore referred to is the ultimate analysis, or the perceutage of carbon, hydrogen, and oxygen of the dry coal. It is found, however, from a study of Mahler's tests that the proximate analysis, which gives fixed carbon, volatile matter, moisture, and ash, may be relied on as giving a measure of the heating value with a limit of error of only about 3%. After deducting the moisture and ash, and calculating the fixed carbon as a percentage of the coal dry and free from ash, the author has constructed the following table:

APPROXIMATE HEATING VALUE OF COALS.

Percentage F. C. in Coal Dry and Free from Ash.	Heating Value B.T.U. per lb. Comb'le.	Equiv. Water Evap. from and at 212° per lb. Combustible.	F. C. in Coal Dry and Free	Heating Value B.T.U. per lb. Comb'le.	Equiv. Water Evap. from and at 212° per lb. Combustible.
100	14500	15.00	68	15480	16.08
97	14760	15.28	68	15120	15.65
94	15120	15.65	60	14580	15.09
90	15480	16.08	57	14040	14.58
87	15660	16.21	54	13320	18.79
80	15840	16.40	51	12600	13.04
72	15 660	16.21	50	12240	12.67

Below 50% the law of decrease of heating-power shown in the table apparently does not hold, as some cannel coals and lignites show much higher heating-power than would be predicted from their chemical constitution.

The use of this table may be shown as follows:

Given a coal containing moisture 2%, ash 8%, fixed carbon 61%, and volatile matter 29%, what is its probable heating value? Deducting moisture and ash we find the fixed carbon is 61/90 or 68% of the total of fixed carbon and volatile matter. One pound of the coal dry and free from ash would, by the table, have a heating value of 15.480 thermal units, but as the ash and moisture, having no heating value, are 10% of the total weight of the coal, the coal would have 90% of the table value, or 18,932 thermal units. This divided by 966, the latent heat of steam at 212° gives an equivalent evaporation per 18,000 of 14.42 lbs.

The heating value that can be obtained in practice from this coal would epend upon the efficiency of the boiler, and this largely upon the difficulty thoroughly burning its volatile combustible matter in the boiler furnace. a boiler efficiency of 65% could be obtained, then the evaporation per lb. of oal from and at 212° would be $14.42 \times .65 = 9.87$ lbs.

With the best anthracite coal, in which the combustible portion is, say, 97% sed carbon and 3% volatile matter, the highest result that can be expected a boiler-test with all conditions favorable is 12.2 lbs. of water evaporated om and at 212° per lb. of combustible, which is 80% of 15.28 lbs. the theotical heating-power. With the best semi-bituminous coals, such as Cumrland and Pocahontas, in which the fixed carbon is 80% of the total comistible, 125 lbs., or 76% of the theoretical 16.4 lbs., may be obtained. For ttsburgh coal, with a fixed carbon ratio of 68%, 11 lbs., or 69% of the theoretical 16.03 lbs., is about the best practically obtainable with the best boilers ith some good Ohio coals, with a fixed carbon ratio of 60%, 10 lbs., or 66% the theoretical 15.09 lbs., has been obtained, under favorable conditions, th a fire-brick arch over the furnace. With coals mined west of Ohio, th lower carbon ratios, the boiler efficiency is not apt to be as high as 60%. From these figures a table of probable maximum boiler-test results from als of different fixed carbon ratios may be constructed as follows:

xed carbon ratio . . . 97 60 ap. from and at 212° per lb. combustible, maximum in boiler-tests: 12.2 12.5 11 10 8.3 80 76 69 66 60 55 iler efficiency, per cent..... ss, chimney, radiation, imperfect combustion, etc: 24 84 20

The difference between the loss of 20% with anthracite and the greater ses with the other coals is chiefly due to imperfect combustion of the uminous coals, the more highly volatile coals sending up the chimney the ater quantity of smoke and unburned hydrocarbon gases. It is a measure the inefficiency of the boiler furnace and of the inefficiency of heating-

face caused by the deposition of soot, the latter being primarily caused the imperfection of the ordinary furnace and its unsuitability to the oper burning of bituminous coal. If in a boiler-test with an ordinary furnace se lower results are obtained than those in the above table, it is an indican of unfavorable conditions, such as bad firing, wrong proportions of ler, defective draft, and the like, which are remediable. Higher results be expected only with gas-producers, or other styles of furnace espe-

lly designed for smokeless combustion.

Kind of Furnace Adapted for Different Coals. (From the hor's paper on "The Evaporative Power of Bituminous Coals," Trans. S. M. E. iv, 257.)—Almost any kind of a furnace will be found well peted to burning anthracite coals and semi-bituminous coals containing than 20% of volatile matter. Probably the best furnace for burning se coals which contain between 20% and 40% volatile matter, including the tch, English, Welsh, Nova Scotia, and the Pittsburgh and Monongahela er coals, is a plain grate-bar furnace with a fire-brick arch thrown over or the purpose of keeping the combustion-chamber thoroughly hot. The t furnace for coals containing over 40% volatile matter will be a furnace counded by fire-brick with a large combustion-chamber, and some speappliance for introducing very hot air to the gases distilled from the l. or, preferably, a separate gas-producer and combustion-chamber, with lities for heating both air and gas before they unite in the combustion-The character of furnace to be especially avoid d in burning all minous coals containing over 20% of volatile matter is the ordinary fure, in which the boiler is set directly above the grate bars, and in which the ting-surfaces of the boiler are directly exposed to radiation from the on the grate. The question of admitting air above the grate is still unled. The London Engineer recently said: "All our experience, extending many years, goes to show that when the production of smoke is pre-ed by special devices for admitting air, either there is an increase in the sumption of fu'l or a diminution in the production of steam. * * * The smoke-preventer yet devised is a good fireman."

ownward-draught Furnaces. - Recent experiments show that bituminous coal considerable saving may be made by causing the ght to go downwards from the freshly fired coal through the hot coal ie grate. Similar good results are also obtained by the upward draught eding the fresh coal under the bed of hot coal instead of on top. (See

rs.)

Calerimetric Tests of American Coals,—From a number of tests of American and foreign coals, made with an oxygen calorimeter, by Geo. H. Barrus (Trans. A. S. M. E., vol. xiv. 816), the following are selected, showing the range of variation:

	Percentage of Ash.		Total Heat reduced to Fuel free from Ash.
Semi-bituminous.	§ 6.1	14,217	15,141
George's Cr'k, Cumberl'd, Md.,10 tests	8.6	12,874	14,085
Pocahontas, Va., 5 tests	8.2	14,608	15,086
	6.2	18,608	14,507
New River, Va., 6 testa	3.5	13,922	14,427
	5.7	13,858	14.696
Elk Garden, Va., 1 test	7.8	13,180	14,295
	7.7	13,581	14,714
Youghiogheny, Pa., lump	5.9	12,941	18,752
Frontenac, Kansas	10.2	11,664	12,988
	17.7	10,506	12,765
	8.7	12,420	18, 6 02
Lancashire, Eng	6.8	12,123 12,123 11,521	13,006 12,873
Anthracite, 11 tests	9.1	13,189	14,509

Evaporative Power of Bituminous Coals.

(Tests with Babcock & Wilcox Boilers, Trans. A. S. M. E., iv. 207.)

Name of Coal.	Dura- tion of Test.	Grate Surface, sq. ft.	Heating Surface, sq. ft.	Percentage of Refuse.	Coal burned per sq. ft, of Grate, pounds.	Water evaporated per sq. ft. of Heating Surface per hour, pounds.	Water per pound Coal from and at 212°, lbs.	Water per pound Combus- tible from and at 212°.	Rated Horse-power.	Horse-power developed.
1. Welsh	1314 hrs	40	1679	7.5	6.3	2.07	11.53	12.46	146	96
2. Anthracite scr's 1/5 Powelton, Pa., Semi-bit. 4/5,	1034 h	60	3126	8.8	17.6	4.32	11.32	12.42	272	448
 Pittsbg'h fine slack 3d Pool lump 	4 hrs				21.9		8.12 10.47	9.29	146 240	250 419
4. Castle Shannon, nr Pittsb'gh, 36 nut,	}4234 h	69.1	4784	10.5	27.9	4.13	10.00	11.17	416	570
6. Ill. "run of mine"	6 days.		1196			1.41	9,49		104	54
" Ind. block, "very good"	3 d'ys		1196			2.95	9.47		104	111
6. Jackson, O., nut Stainton, Ill., nut., 7. Renton screenings Wellington scr'gs Black Diam. scr'gs Seattle screenings	6 h 80 m 5 h 58 m 6 h 94 m	60 21,2 21,2 21,2 21,2	1564 1564 1564 1564	17.7 13.8 18.3 19.3 13.4	27 36.4 31.3	2.95 2.93 3.11 2.91	8.93 5.09 6.88 7.89 6.29 6.86	9.88 6.19 7.98 9.66 7.80 7.92	292 292 186 186 186 136	460 246 151 150 160 150
" Cardiff lump. " South Paine lump. " Seattle lump.	6 h 47 m 7 h 23 m 6 h 35 m	21.2 21.2 21.2	1564 1564 1564	11.7 19.1 13.9	26.7 25.6 28.9	3.69 3.35 3.53	9.02 10.07 9.62 8.96 7.68	10.46 11.40 11.89 10.41 8,49	136 136 136 136 136	171 189 174 182 184

637 COKE.

Place of Test: 1. London, England; 2. Peacedale, R. I.; 3. Cincinnati, O.; 4. Pittsburgh. Pa.; 5. Chicago, Ill.; 6. Springfield, O.; 7. San Francisco,

In all the above tests the furnace was supplied with a fire-brick arch for preventing the radiation of heat from the coal directly to the boiler.

Weathering of Coal. (I. P. Kimball, Trans. A. I. M. E., viii. 204.)—
The practical effect of the weathering of coal, while sometimes increasing its absolute weight, is to diminish the quantity of carbon and disposable pydrogen and to increase the quantity of oxygen and of indisposable hydrogen. Hence a reduction in the calorific value.

An excess of pyrites in coal tends to produce rapid oxidation and mechan-cal disintegration of the mass, with development of heat, loss of coking

lower, and spontaneous ignition.

ower, and spontaneous ignition. The only appreciable results of the weathering of anthracite within the ridinary limits of exposure of stocked coal are condined to the oxidation of is accessory pyrites. In coking coals, however, weathering reduces and inally destroys the coking power, while the pyrites are converted from the tate of bisulphide into comparatively innocuous sulphates. Richters found that at a temperature of 188 to 180° Fahr., three coals lost 1 fourteen days an average of 3.5% of calorific power. (See also paper by P. Bothwell, Trans. A. I. M. E., iv. 55.)

COKE.

Coke is the solid material left after evaporating the volatile ingredients of al, either by means of partial combustion in furnaces called coke ovens,

by distillation in the retorts of gas-works.

Coke made in ovens is preferred to gas coke as fuel. It is of a dark-gray lor, with slightly metallic lustre, porous, brittle, and hard. The proportion of coke yielded by a given weight of coal is very different r different kinds of coal, ranging from 0.9 to 0.35.

Being of a porous texture, it readily attracts and retains water from the mosphere, and sometimes, if it is kept without proper shelter, from 0.15 to 0 of its gross weight consists of moisture.

Analyses of Coke. (From report of John R. Procter, Kentucky Geological Survey.)

V	Fixed Carbon	Ash.	Sul- phur.				
inellsville, Pa. ittanooga, Tenn. ningham, Ala. ahontas, Va. v River, W. Va. Stone Gap, Ky.	(Average	of 3	44 44	8)	88.96 80.51 87.29 92.53 92.88 93.23	9.74 16.34 10.54 5.74 7.21 5.69	0.810 1.595 1.195 0.597 0.562 0.749

Experiments in Coking. Connellsville Region. (John Fulton, Amer. Mfr., Feb. 10, 1893.)

.e -:	1 2	je j	oke 6	gg.	oke.	Pe	범			
Time ir Oven.	Charged	Ash made.	Fine Co made	Market Coke ma	Total C made.	Ash.	Fine Coke.	Market Coke	Total Coke.	Per Cent Lost.
h. m. 67 00 68 00 45 00 45 00	12,420 11,090 9,120	90 77	1b. 885 859 272 849	lb. 7,518 6,580 5,418 5,334	1b. 7,908 6,989 5,690 5,683	00.80 00.81 00.84 00.82	3.24	60.53 59.33 59.41 59.13	62.57 62.89	36.62 a
1	41,650	840	1865	24,850	26,215	00.82	8.28	59.66	62.94	86.24

se results show, in a general average, that Connellsville coal carefully in a modern beehive oven will yield 66.17% of marketable coke, 2.30 all coke or braize, and 0.82% of ash.

The total average loss in volatile matter expelled from the coal in coking amounts to 30.71%.

The modern beehive coke oven is 12 feet in diameter and 7 feet high at crown of dome. It is used in making 48 and 72 hour coke.

In making these tests the coal was weighed as it was charged into the

oven; the resultant marketable coke, small coke or braize and ashes weighed dry as they were drawn from the oven.

Coal Washing.—In making coke from coals that are high in ash and sulphur, it is advisable to crush and wash the coal before coking it. A coalwashing plant at Brookwood. Ala., has a capacity of 50 tons per hour. The washing plant at Brookwood, Ala., has a capacity of 50 tons per hour. The average percentage of ash in the coal during ten days' run varied from 14% to 21%, in the washed coal from 4.8% to 8.1%, and in the coke from 6.1% to 10.5%. During three months the average reduction of ash was 60.9%. (Eng. and Mining Jour., March 25, 1893.)

Recovery of By-products in Coke Manufacture.-In Germany considerable progress has been made in the recovery of by products. The Hoffman-Otto oven has been most largely used, its principal feature being that it is connected with regenerators. In 1884 40 ovens on this system were running, and in 1892 the number had increased to 1209.

A Hoffman-Otto oven in Westphalia takes a charge of 6¼ tons of dry coal and converts it into coke in 48 hours. The product of an oven annually is 1025 tons in the Ruhr district, 1170 tons in Silesia, and 960 tons in the Saar district. The yield from dry coal is 75% to 77% of coke, 2.5% to 3% of tar, and 1.1% to 1.2% of sulphate of ammonia in the Ruhr district; 65% to 70% of coke, 4% to 4.5% of tar, and 1% to 1.25% of sulphate of ammonia in the Upper Silesia region and 68% to 72% of coke, 4% to 4.3% of tar and 1.8% to 1.9% of sulphate of ammonia in the Saar district. A group of 60 Hoffman ovens, therefore, yields annually the following:

District.	Coke, tons.	Tar, tons.	Sulphate Ammonia, tons.
Ruhr	51,200	1860	780
Upper Silesia	48,000	8000	840
Saar	40.500	2400	492

An oven which has been introduced lately into Germany in connection An oven which has been introduced nately into Germany in connection with the recovery of by-products is the Semet-Solvay, which works hotter than the Hoffman-Otto, and for this reason 73% to 77% of gas coal can be mixed with 23% to 27% of coal low in volatile matter, and yet yield a good coke. Mixtures of this kind yield a larger percentage of coke, but, on the other hand, the amount of gas is lessened, and therefore the yield of tar and ammonia is not so great.

The yield of coke by the beehive and the retort ovens respectively is given as follows in a pamphlet of the Solvay Process Co.: Connelisville coal: beehive, 60%, retort, 73%; Pocahontas: beehive, 60%, retort, 74%. (See article in Mineral Industry, vol. viii., 1900.)

References: F. W. Luerman, Verein Deutscher Eisenhuettenleute 1891, Iron Age, March 31, 1892; Amer. Mfr., April 28, 1898. An excellent series of articles on the manufacture of coke, by John Fulton, of Johnstown, Pa.,

of atteres on the manufacture of coac, by John runon, of Johnstown, Fu., is published in the Colliery Engineer, beginning in January, 1893.

Making Hard Coke.—J. J. Fronheiser and C. S Price, of the Cambria Iron Co., Johnstown, Pa., have made an improvement in coke manufacture by which coke of any degree of hardness may be turned out. It is accomplished by first grinding the coal to a coarse powder and mixing it is with a hydrate of live (six or water alcabed causit lives) before it is accomplished by first grinding the coal to a coarse powder and mixing it with a hydrate of lime (air or water slacked caustic lime) before it is charged into the coke-ovens. The caustic lime or other fluxing material used is mechanically combined with the coke, filling up its cell-walls. It has been found that about 5% by weight of caustic lime mixed with the fine coal gives the best results. However, a larger quantity of lime can be added to coals containing more than 5% to 7% of ash. (Amer. Mfr.)

Generation of Steam from the Waste Heat and Gases of Coke-ovens. (Erskine Rumsey, Amer. Mfr., Feb. 16, 1894)—I he gases from a number of adjoining ovens of the beehive type are led into a long horizontal flue, and thence to a combustion-chamber under a battery of bollers. Two plants are in satisfactory operation at Tracy City, Tenn., and two at Pratt Mines. Als.

A Bushel of Coal.—The weight of a bushel of coal in Indiana is 70 lbs.

A Bushel of Coal.—The weight of a bushel of coal in Indiana is 70 lbs in Penna. 76 lbs.; in Ala., Colo., Ga., Ill., Ohio, Tenn., and W. Va. it is 80 lbs. A Bushel of Coke is almost uniformly 40 lbs., but in exceptional cases, when the coke is very light, 38, 36, and 33 lbs. are regarded as a bushel. In others, from 42 to 50 lbs are given as the weight of a bushel; in this case

the coke would be quite heavy

Products of the Distillation of Coal.—S. P. Sadler's Handbook of Industrial Organic Chemistry gives a diagram showing over 50 chemical products that are derived from distillation of coal. The first derivatives are coal-gas, gas liquor, coal-tar, and coke. From the gas-liquor are derived ammonis and sulphate, chloride and carbonate of ammonis. The coal-tar is split up into oils lighter than water or crude naphtha, oils heavier than water—otherwise dead oil or tar, commonly called creosote,—and pitch. From the two former are derived a variety of chemical products.

From the coal-tar there comes an almost endless chair of known combinations. The greatest industry based upon their use is the manufacture of dyes, and the enormous extent to which this has grown can be judged from the fact that there are over 600 different coal-tar colors in use, and many more which as yet are too expensive for this purpose. Many medicinal preparations come from the series, pitch for paving purposes, and chemicals for the photographer, the rubber manufacturers and tanners, as well as for

preserving timber and cloths.

The composition of the hydrocarbons in a soft coal is uncertain and quite complex; but the ultimate analysis of the average coal shows that it approaches quite nearly to the composition of CH_4 (marsh-gas). (W. H. Blauvelt, Trans. A. I. M. E., xx. 625.)

WOOD AS FUEL.

Wood, when newly felled, contains a proportion of moisture which varies very much in different kinds and in different specimens, ranging between 10% and 50%, and being on an average about 40%. After 8 or 12 months' ordinary drying in the air the proportion of moisture is from 20 to 25%. This legree of dryness, or almost perfect dryness if required, can be produced by a few days' drying in an oven supplied with air at about 240° F. When soal or coke is used as the fuel for that oven, 1 lb. of fuel suffices to expel tout 3 lbs. of moisture from the wood. This is the result of experiments on a large scale by Mr. J. R. Napier. If air dried wood were used as uel for the oven, from 2 to 2½ lbs. of wood would probably be required to produce the same effect.

The specific gravity of different kinds of wood ranges from 0.3 to 1.2.

Perfectly dry wood contains about 50% of carbon, the remainder consisting lmost entirely of oxygen and hydrogen in the proportions which form rater. The coniferous family contain a small quantity of turpentine, which is a hydrocarbon. The proportion of ash in wood is from 1% to 5%. The stal heat of combustion of all kinds of wood, when dry, is almost excetly the same, and is that due to the 50% of carbon.

ctly the same, and is that due to the 50% of carbon.

The above is from Rankine; but according to the table by S. P. Sharpless I Jour. C. I. W., iv. 36, the ash varies from 0.03% to 120% in American woods, nd the fuel value, instead of being the same for all woods, ranges from 367 (for white oak) to 5546 calories (for long-leaf pine) = 6600 to 9888 British ermal units for dry wood, the fuel value of 0.50 lbs. carbon being 7272

. T. U

Heating Value of Wood.—The following table is given in several paks of reference, authority and quality of coal referred to not stated. The weight of one cord of different woods (thoroughly air-dried) is about if follows:

ickory or hard maple.... 4500 lbs. equal to 1800 lbs. coal. (Others give 2000.) 8850 hite oak.... 1540 1715. ech, red and black oak .. 8250 " 46 1800 " 46 .. 1450. 44 44 46 " plar, chestnut, and elm.. 2350 940 1050. 800 1e average pine...... 2000

Referring to the figures in the last column, it is said:

From the above it is safe to assume that 2½ lbs. of dry wood are equal to b. average quality of soft coal and that the full value of the same weight different woods is very nearly the same—that is, a pound of hickory is orth no more for fuel than a pound of pine, assuming both to be dry. It important that the wood be dry, as each 10% of water or moisture in wood ll detract about 12% from its value as fuel.

Faking an average wood of the analysis C 51%, H 6.5%, O 42.0%, ash 0.5%.

Taking an average wood of the analysis C 51%, H 5.5%, O 42.0%, ash 0.5%, rfectly dry, its fuel value per pound, according to Dulong's formula. V

 $\left[14,500 \text{ C} + 62,000 \text{ (H} - \frac{\text{O}}{8})\right]$, is 8170 British thermal units. If the wood, as ordinarily dried in air, contains 25% of moisture, then the heating value of a pound of such wood is three quarters of 8170 = 6127 heat-units, less the heat required to heat and evaporate the ½ lb. of water from the atmospheric temperature, and to heat the steam made from this water to the temperature of the chimney gases, say 150 heat-units per pound to heat the water. to raise the temperature and 100 heat the units to raise the temperature of the steam to 420° F., or 1216 in all = 304 for ½ lb., which subtracted from the 8127 leaves 5894 heat-units as the net fuel value. which subtracted from the 6127, leaves 5824 heat-units as the net fuel value of the wood per pound, or about 0.4 that of a pound of carbon.

Composition of Wood. (Analysis of Woods, by M. Eugene Chevandier.)

Woods.	Composition.						
Woods.	Carbon.	Hydrogen.	Oxygen.	Nitrogen.	Ash.		
Beech	49.36% 49.64 50.20 49.87 49.96	6.01% 5.92 6.20 6.21 5.96	42.69% 41.16 41.62 41.60 89.56	0.91\$ 1.29 1.15 0.96 0.96	1.06% 1.97 0.81 1.86 8.37		
Average	49.70%	6.06%	41.30%	1.05%	1.80%		

The following table, prepared by M. Violette, shows the proportion of water expelled from wood at gradually increasing temperatures:

Temperature,	Water Expelled from 100 Parts of Wood.						
Temperature,	Oak.	Ash.	Elm.	Walnut.			
257° Fahr	15.26 17.93 82.13 85.80 44.81	14.78 16.19 21.29 27.51 83.38	15.82 17.02 86.941 88.38 40.56	15.55 17.43 21.00 41.77?			

The wood operated upon had been kept in store during two years. When wood which has been strongly dried by means of artificial heat is left exposed to the atmosphere, it reabsorbs about as much water as it contains in its air-dried state.

A cord of vocad = $4 \times 4 \times 8 = 128$ cu. ft. About 56% solid wood and 44% interstitial spaces. (Marcus Bull, Phila., 1829. J. C. I. W., vol. i. p. 293.) B. E. Fernow gives the per cent of solid wood in a cord as determined officially in Prussia (J. C. I. W., vol. iii. p. 20):

Timber cords, 74.07% = 80 cu. ft. per cord; Firewood cords (over 6" diam.), 69.44% = 75 cu. ft. per cord; "Billet" cords (over 8" diam.), 55.55% = 60 cu. ft. per cord; "Brush" woods less than 8" diam., 18.52%; Roots, 37.00%.

CHARCOAL.

Charcoal is made by evaporating the volatile constituents of wood and peat, either by a partial combustion of a conical heap of the material to be charred, covered with a layer of earth, or by the combustion of a separate portion of fuel in a furnace, in which are placed retorts containing the material to be charged.

According to Peclet, 100 parts by weight of wood when charred in a heap yield from 17 to 22 parts by weight of charcoal, and when charred in a retort from 28 to 80 parts.

This has reference to the ordinary condition of the wood used in charcoalmaking, in which 25 parts in 100 consist of moisture. Of the remaining 75 parts the carbon amounts to one half, or 87145 of the gross weight of the wood. Hence it appears that on an average nearly half of the carbon in the

Vield | priso

59.5

| |42.9'17.1| 85 0 | 17.5

13.3

18.3 17 5

ood is lost during the partial combustion in a heap, and about one quarter iring the distillation in a retort.

To char 100 parts by weight of wood in a retort, 1214 parts of wood must burned in the furnace. Hence in this process the whole expenditure of ood to produce from 28 to 30 parts of charcoal is 11214 parts; so that if the sight of charcoal obtained is compared with the whole weight of wood pended, its amount is from 25% to 27%; and the proportion lost is on an

erage 1114 + 8714 = 0.8, nearly. According to Peclet, good wood charcoal contains about 0.07 of its weight ash. The proportion of ash in peat charcoal is very variable, and is esnated on an average at about 0.18. (Rankine.)

Much information concerning charcoal may be found in the Journal of the arcoal-iron Workers' Assn., vols. i. to vi. From this source the following tes have been taken:

Field of Charcoal from a Cord of Wood.—From 45 to 50 shels to the cord in the kiln, and from 80 to 35 in the meiler. Prof. Eglesin Trans. A. I. M. E., viii. 895, says the yield from kilns in the Lake amplain region is often from 50 to 60 bushels for hard wood and 50 for t wood; the average is about 50 bushels.

'he apparent yield per cord depends largely upon whether the cord is a

l cord of 128 cu. ft. or not.

meilers excep-

ish meilers, av. results

n a four months' test of a kiln at Goodrich, Tenn., Dr. H. M. Pierce found ults as follows: Dimensions of kiln-inside diameter of base, 28 ft. 8 in.; m. at spring of arch, 26 ft. 8 in.; height of walls, 8 ft.; rise of arch, 5 ft.; acity, 30 cords. Highest yield of charcoal per cord of wood (measured) 7 bushels, lowest 50.14 bushels, average 53.65 bushels.

o. of charges 12, length of each turn or period from one charging to ther 11 days. (J. C. I. W., vol. vi. p. 26.) lesults from Different Methods of Charcoal-making,

	ł	1 -1	Ju.	20	<u>ವ</u> ಹ .
Coaling Methods.	Character of Wood used.	In Volume per cent.	In Weight per cent.	Bushels of Charcoal Cord of W	Weight in per Bush Charcoal.
	Birch dried at 230 F		85.9		
ded	I AIF GEV. BV. 2000 VEI-	77.0	28.8	63.4	15.7
ieu's retorts, fuel in- ded	low pine weighing abt. 28 lbs. per cu. ft.	65.8	24.2	54.2	15.7
ish ovens, av. results	Good dry fir and pine, and pine,	81.0	27.7	66.7	13.8
ish ovens, av. results	(Doon mond mined Au)	70.0	25 8	62.0	18.3

and pine

ish meilers, av. results | Wood, miss. ft. | 52.5118 of the can kilns, av. results | Av. good yellow pine | 54.7 22.0 45.0 weighing abt. 25 lbs. | 42.9 17.1 35 0 nsumption of Charcoal in Blast-furnaces per Ton of Iron; average consumption according to census of 1880, 1.14 tons oal per ton of pig. The consumption at the best furnaces is much this average. As low as 0 853 ton, is recorded of the Morgan furnace; rrnace, 0.888; Elk Rapids, 0.884. (1892.)

Fir and white-pine wood, mixed. Av. 25 lbs. per cu. ft. 52.518 8

sorption of Water and of Gases by Charcoal. -Svedlius, sorption of Water and of Gases by Charcoal.—Svedius, hand-book for charcoal-burners, prepared for the Swedish Governsays: Fresh charcoal, also reheated charcoal, contains scarcely ater but when cooled it absorbs it very rapidly, so that after four hours, it may contain 45 to 8% of water. After the lapse of a seks the moisture of charcoal may not increase perceptibly, and may mated at 10% to 15%, or an average of 12%. A thoroughly charted of charcoal ought, then, to contain about 84 parts carbon 12 parts 3 parts ash, and 1 part hydrogen. M. Saussure, operating with blocks of fine boxwood charcoal, freshly burnt, found that by simply placing such blocks in contact with certain gases they absorbed them in the following proportion:

	Volumes.	V olu	
Ammonia	90.00	Carbonic oxide	9.42
Hydrochloric-acid gas	85.00	Oxygen	9.25
Sulphurous acid		Nitrogen	
Sulphuretted hydrogen		Carburetted hydrogen	5.00
Nitrous oxide (laughing-gas		Hydrogen	
Carbonic acid			

It is this enormous absorptive power that renders of so much value a comparatively slight sprinkling of charcoal over dead animal matter, as a preventive of the escape of odors arising from decomposition.

In a box or case containing one cubic foot of charcoal may be stored without mechanical compression a little over nine cubic feet of oxygen, representing a mechanical pressure of one hundred and twenty-six pounds to the square inch. From the store thus preserved the oxygen can be drawn by a small hand-pump.

Composition of Charcoal Produced at Various Temperatures. (By M. Violette.)

П			C	ompositio	omposition of the Solid Product.							
	Temperature of Car- bonization.		Temperature of Ca bonization.		honization		Carbon.	Hydro- gen.	Oxygen.	Nitrogen and Loss.	n Ash.	
1284 567	150° 200 250 250 800 8 850 6 482	ahr. 802° 892 482 592 662 810	Per cent. 47.51 51.82 65.59 73.24 76.64 81.64 81.97	Per cent. 6.12 8.99 4.81 4.25 4.14 4.63 2.30	Per cent. 46.29 43.98 28.97 21.96 18.44 15.24 14.15	Per cent. 0.08 0.23 0.63 0.57 0.61 1.61 1.60	Per cent. 47.51 89.88 82.98 24.61 22.42 15.40 15.30					

The wood experimented on was that of black alder, or alder buckthorn, which furnishes a charcoal suitable for gunpowder. It was previously dried at 150 deg. C. = 302 deg. F.

MISCELLANEOUS SOLID FUELS.

Bust Fuel-Dust Explosions.—Dust when mixed in air burns with such extreme rapidity as in some cases to cause explosions. Explosions of flour-mills have been attributed to ignition of the dust in confined passages. Experiments in England in 1876 on the effect of coal-dust in carrying flame in mines showed that in a dusty passage the flame from a blown-out shot may travel 50 yards. Prof. F. A. Abel (Trans. A. I. M. E., xiii. 260) says that coaldust in mines much promotes and extends explosions, and that it may readily be brought into operation as a fiercely burning agent which will carry flame rapidly as far as its mixture with air extends, and will operate as an explosive agent though the medium of a very small proportion of freedamp in the air of the mine. The explosive violence of the combustion of dust is largely due to the instantaneous heating and consequent expansion of the air. (See also paper on "Coal Dust as an Explosive Agent," by Dr. R. W. Raymond, Trans. A. I. M. E. 1894.) Experiments made in Germany in 1893, show that pulverized fuel may be burned without smoke, and with high economy. The fuel, instead of being introduced into the fire-box in the ordinary manner, is first reduced to a powder by pulverizers of any construction. In the place of the ordinary boiler fire-box there is a combustion chamber in the form of a closed furnace lined with fire-brick and provided with an air injet... The nozzemnows a constant stream of fuel into the chamber, scattering it throughout the whole space of the fire-box. When

lining to a high temperature by an open fire, the combustion continues in

an intense and regular manner under the action of the current of air which carries it in. (Mf. is. Record, April, 1883.)

Records of tests with the Wegener powdered-coal apparatus, which is now (1800) in use in Germany, are given in Eng. News, Sept. 16, 1897. Coaldust fuel is now extensively used in the United States in rotary kilns for burning Portland cement.

Foudered fuel was used in the Crompton rotary puddling-furnace at Woolwich Arsenal, England, in 1873. (Jour. I. & S. I., i. 1873, p. 91.)

Peat or Turf, as usually dried in the air, contains from 25, to 30, of water, which must be allowed for in estimating its heat of combustion. This water having been evaporated, the analysis of M. Regnault gives, in 100 parts of perfectly dry peat of the best quality: C 58%, H 6%, O 31%, Ash 5%. In some examples of peat the quantity of ash is greater, amounting to 7%

and sometimes to 11%.

The specific gravity of peat in its ordinary state is about 0.4 or 0.5. It can be compressed by machinery to a much greater density. (Rankine.) Clark (Steam-engine. 1. 61) gives as the average composition of dried Irish peat: C 59%, H 6%, O 30%, N 1.25%, Ash 4%.

Applying Dulong's formula to this analysis, we obtain for the heating value of perfectly dry peat 10,280 heat-units per pound, and for air-dried peat containing 25% of moisture, after making allowance for evaporating the water, 7391 heat-units per pound.

Sawdust as Fuel.—The heating power of sawdust is naturally the same per pound as that of the wood from which it is derived but if allowed to get wet it is more like spent tan (which see below). The conditions necessary for burning sawdust are that plenty of room should be given it in the furnace, and sufficient air supplied on the surface of the mass. The same applies to shavings, refuse lumber, etc. Sawdust is frequently burned in saw-mills, etc., by being blown into the furnace by a fan-blast.

saw-mills, etc., by being blown into the furnace by a fan-blast.

Wet Tan Bark as Fuel.—Tan, or oak bark, after having been used in the processes of tanning, is turned as fuel. The spent tan consists of the fibrous portion of the bark. According to M Peelet, five parts of oak bark produce four parts of dry tan; and the heating power of perfectly dry tan, containing 15% of ash, is 6100 English units; whilst that of tan in an ordinary state of dryness, containing 80% of water, is only 4284 English units. The weight of water evaporated from and at 2129 by one pound of tan, equivalent to these heating powers, is, for perfectly dry tan, 5 46 lbs., for tan with 80% moisture, 8.54 lbs. Experiments by Prof. R. H. Thurston (Jour. Frank, Inst., 1874) gave with the Crockett furnace, the wet tan containing 55% of water, an evaporation from and at 212° F. of 4.24 lbs. of water per pound of the wet tan, and with the Thompson furnace an evaporation of 3.19 lbs. per pound of wet tan containing 55% of water. The Thompson furnace conservations of the second of the containing 55% of water. The Thompson furnace conper pound of wet tan containing 55% of water. The Thompson furnace consisted of six fire-brick ovens, each 9 feet × 4 feet 4 inches, containing 234 square feet of grate in all, for three boilers with a total heating surface of 3000 square feet, a ratio of heating to grate surface of 9 to 1. The tan was ed through holes in the top. The Crockett furnace was an ordinary fireprick furnace, 6 × 4 feet, built in front of the boiler, instead of under it. the atio of heating surface to grate being 14.6 to 1. According to Prof. Thurson the conditions of success in burning wet fuel are the surrounding of the nass so completely with heated surfaces and with burning fuel that it may e rapidly dried, and then so arranging the apparatus that thorough com-ustion may be secured, and that the rapidity of combustion be precisely

usition may be secured, and that the rapidity of combustion be precisely qual to and never exceed the rapidity of desiccation. Where this rapidity of combustion is exceeded the dry portion is consumed completely, leaving nuncovered mass of fuel which refuses to take fire.

Straw as Fuel. (Eng'g Mechanics, Feb., 1893, p. 55.)—Experiments in ussla showed that winter-wheat straw, dried at 230° F., had the following mposition: C, 46.1; H, 5.6; N, 0.42; O, 43.7; Ash. 4.1. Heating value in ritish thermal units: dry straw, 6290; with 6% water, 5770; with 10% water, 48. With straws of other grains the heating value of dry straw ranged om 5590 for buckwheat to 6750 for flax.

Clark (S. E. vol. 1, n.89; gives the mean composition of wheat and harley

Clark (S. E. vol. 1, p. 62) gives the mean composition of wheat and barley raw as C, 36; H. 5; 0. 38; O, 0.60; Ash, 4.75; water, 15.75, the two straws trying less than 1s. The heating value of straw of this composition, accordg to Dulong's formula, and deducting the heat lost in evaporating the ater, is 5155 heat units. Clark erroneously gives it as 8144 heat units.

Bagasse as Fuel in Sugar Manufacture,-Bagasse is the name ven to refuse sugar-cane, after the juice has been extracted. Prof. L. A.

Becuel, in a paper read before the Louisiana Sugar Chemists' Association, in 1892, says: "With tropical case containing 12.5% woody fibre, a juice containing 16.18% solids, and 83.67% water, bagasse of, say, 66% and 72% mill extraction would have the following percentage composition:

	Woody Fibre.	Combustible Salta	Water.
66% bagasse	87	10	58
72% bagasse	45	y	46

"Assuming that the woody fibre contains 51% carbon, the sugar and other combustible matters an average of 42.1%, and that 12,906 units of heat are generated for every pound of carbon consumed, the 66% bagasse is capable of generating 297,834 heat units per 100 lbs. as against 345,200, or a difference of 47,366 units in favor of the 72% bagasse.

"Assuming the temperature of the waste gases to be 450° F., that of the surrounding atmosphere and water in the bagasse at 86° F., and the quantity of air necessary for the combustion of one pound of carbon at 24 lbs., the lost heat will be as follows: In the waste gases, heating air from 86° to 450° F., and in vaporizing the moisture, etc., the 68% bagasse will require 112,546 heat units, and 116,150 for the 72% bagasse.

"Subtracting these quantities from the above, we find that the 66% bagasse will produce 185,288 available heat units per 100 lbs., or nearly 2½ less than the 72% bagasse, which gives 229,050 units. Accordingly, one ton of came of 2000 lbs. at 66% mill extraction will produce 680 lbs. bagasse, equal to 1,259,958 available heat units, while the same cane at 72% extraction will produce 560 lbs. bagasse, equal to 1,282,680 units.

"A similar calculation for the case of Louisiana cane containing 10% woody

fibre, and 16% total solids in the juice, assuming 75% mill extraction, shows that bagasse from one ton of cane contains 1,573,856 heat units, from which

561,465 have to be deducted.

"This would make such bagasse worth on an average nearly 92 lbs. coal per ton of cane ground. Under fairly good conditions, 1 lb. coal will evaporate 7% lbs. water, while the best boiler plants evaporate 10 lbs. Therefore orate 716 lbs. water, while the best boiler plants evaporate 10 lbs. Therefore, the begasse from 1 ton of cane at 75% mill extraction should evaporate from 689 lbs. to 919 lbs. of water. The juice extracted from such cane would under these conditions contain 1200 lbs. of water. If we assume that the water added during the process of manufacture is 10% (by weight of the juice made, the total water handled is 1410 lbs. From the juice represented in this case. the commercial massecuite would be about 15% of the weight of the original mill juice, or say 225 lbs. Said mill juice 1500 lbs., plus 10%, equals 1650 lbs. liquor handled; and 1650 lbs. minus 225 lbs., equals 1425 lbs., the countility of water to be appropriated during the process of manufacture. the quantity of water to be evaporated during the process of manufacture. To effect a 714-lb. evaporation requires 190 lbs. of coal, and 14214 lbs. for a 10lb. evaporation.

"To reduce 1650 lbs. of juice to syrup of, say, 27° Baumé, requires the evaporation of 1170 lbs. of water, leaving 480 lbs. of syrup. If this work be according to the state of the state o complished in the open air, it will require about 156 lbs, of coal at 714 lbs.

boiler evaporation, and 117 at 10 lbs. evaporation.

With a double effect the fuel required would be from 59 to 78 lbs., and with a triple effect, from 36 to 52 lbs.

"To reduce the above 480 lbs. of syrup to the consistency of commercial massecuite means the further evaporation of 255 lbs. of water, requiring the expenditure of 84 lbs. coal at 7½ lbs. boiler evaporation, and 25½ lbs. with a 10-lb. evaporation. Hence, to manufacture one ton of cane into sugar and molasses, it will take from 145 to 190 lbs. additional coal to do the worth by the open evaporator process; from 85 to 112 lbs. with a double effect, and only 7½ lbs. evaporation in the boilers, while with 10 lbs. boiler evaporation the bagasse alone is capable of furnishing 8% more heat than is actually required to do the work. With triple-effect evaporation depending on the excellence of the boiler plant, the 1425 lbs. of water to be evaporated from the julice will require between 62 and 86 lbs. of coal. These values show that from 6 to 30 lbs. of coal can be spared from the value of the bagasse to run engines, grind cane, etc.

It accordingly appears," says Prof. Becuel, "that with the best boiler plants, those taking up all the available heat generated, by using this heat economically the bagasse can be made to supply all the fuel required by ow

sugar-houses."

PETROLEUM.

Products of the Distillation of Crude Petroleum.

Crude American petroleum of sp. gr. 0.800 may be split up by fractional fistillation as follows (Robinson's Gas and Petroleum Engines):

Temp. of Distillation Fahr.	Distillate.	Percent- ages.	Specific Gravity.	Flashing Point. Deg. F.
113° 113 to 140° 140 to 158° 158 to 248° 248° to 847° 388° and } 1pwards. } 482°	Rhigolene. { Chymogene. } Gasolene (petroleum spirit) Benzine, naphtha C, benzolene. } Benzine, naphtha B Polishing oils. Kerosene (lamp-oil) Lubricating oil Paraffine wax. Residue and Loss.	10. 2.5 2. 50.	.590 to .625 .686 to .657 .680 to .700 .714 to .718 .725 to .787 .802 to .820 .850 to .915	14 82 100 to 122 230

Lima Petroleum, produced at Lima, Ohio, is of a dark green color, ery fluid, and marks 48° Baumé at 15° C. (sp. gr., 0.792).

The distillation in fifty parts, each part representing 2% by volume, gave ne following results:

'er	Sp.	Per	Sp.	Per	Sp.	Per	Sp.	Per	Sp.	Per	Sp.
ent	. Gr.	cent.	Gr.	cent.	Gr.	cent.	Gr.	cent.	Gr.	cent.	Gr.
;	0.680	18	0.720	84	0.764	50	0.802	68	0.820	88	0.815
Ł	.683	20	.7:28	36	.768	52)		70	.825	90	.815
i	.685	22	.780	88	.772	to >	.806	72	.830		
;	.690	24	.785	40	.778	58		78	.830	92 1	8.
1	.694	26	.740		.782	60 '	.800	76	.810	to	ã
!	.698	28	.742	44	788	62	.804	78	.820	100	Ę
	.700	30	.746	46	.792	64	.808	82	.818	,	80
	.706	82	.760		.800	66	.812	86	.816		Residuum

RETURNS.

16 per cent naphtha, 70° Baumé. 6 per cent paraffine oil. residuum. burning oil. 10

The distillation started at 28° C., this being due to the large amount of phtha present, and when 60% was reached, at a temperature of 310° C., e hydrocarbons remaining in the retort were dissociated, then gases e hydrocarbons remaining in the retort were dissociated, then gases caped, lighter distillates were obtained, and, as usual in such cases, the mperature decreased from 310° C. down gradually to 200° C., until 75% of was obtained, and from this point the temperature remained constant it the end of the distillation. Therefore these hydrocarbons in statu wiendi absorbed much heat. (Jour. Am. Chem. Soc.)

Value of Petroleum as Fuel.—Thos. Urquhart, of Russia (Proc. 5t. M. E., Jan. 1899), gives the following table of the theoretical evaporae power of petroleum in comparison with that of coal, as determined by

ssrs. Favre & Silbermann:

	Specific Gravity Chem. Comp.			power,	Theoret. Evap., lbs. Water per	
Fuel.	32° F., Water = 1.000.	C.	н.	о.	British Thermal Units.	lb. Fuel, from and at 212° F.
nna. heavy crude oil ucasian light crude oil heavy "" troleum refuse od English Coal, Mean	0.938 0.928	p. c. 84.9 86.3 86.6 87.1	p. c. 13.7 13.6 12.3 11.7	p. c. 1.4 0.1 1.1 1.2	Units. 20,736 22,027 20,138 19,832	lbs. 21.48 22.79 20.85 20.53
f 98 Samples	1.880	80.0	5.0	8.0	14,112	14.61.

646 PUEL.

In experiments on Russian railways with petroleum as fuel Mr. Urquhart obtained an actual efficiency equal to 82% of the theoretical heating-value. The petroleum is fed to the furnace by means of a spray-injector driven by An induced current of air is carried in around the injector-nozzle,

and additional air is supplied at the bottom of the furnace.

Oil vs. Coal as Fuel. (Iron Age, Nov. 2, 1893.)—Test by the Twin City Rapid Transit Company of Minneapolis and St. Paul. This test showed that with the ordinary Lima oil weighing 6 6/10 pounds per gallon, and costing 2½ cents per gallon, and coal that gave an evaporation of 7½ lbs. of water per pound of coal, the two fuels were equally economical when the price of coal was \$8.85 per ton of 2000 lbs. With the same coal at \$2.00 per ton, the coal was 37% more economical, and with the coal at \$4.85 per ton, the coal was 20% more expensive than the oil. These results include the

difference in the cost of handling the coal, ashes, and oil.

In 1892 there were reported to the Engineers Club of Philadelphia some comparative figures, from tests undertaken to ascertain the relative value

of coal, petroleum, and gas.

•	Lbs. Water, from
	and at 212° F.
1 lb. anthracite coal evaporated	9.70
1 lb. bituminous coal	10.14
1 lb. fuel oil, 86° gravity	16 48
1 lb. fuel oil, 86° gravity	1.28

The gas used was that obtained in the destillation of petroleum, having about the same fuel-value as natural or coal-gas of equal candie-power.

Taking the efficiency of bituminous coal as a basis, the calorific energy of petroleum is more than to greater than that of coal; whereas, theoretically, petroleum exceeds coal only about 46%—the one containing 14,500 heat-units.

and the other 21,000.

Orude Petroleum vs. Indiana Block Coal for Steam-raising at the South Chicago Steel Works. (E. C. Potter, Trans. A. I. M. E., xvii, toc.)—With coal, 14 tubular boilers 16 ft. × 5 ft. required 25 men to operate them; with fuel oil, 6 men were required, a saving of 19 men at \$2 per day, or \$35 per day.

For one week's work 2731 barrels of oil were used, against 848 tons of coal

required for the same work, showing 3.22 barrels of oil to be equivalent to 1 ton of coal. With oil at 60 cents per barrel and coal at \$2.15 per ton, the relative cost of oil to coal is as \$1.93 to \$2.15. No evaporation tests were

made.

Petroleum as a Metallurgical Fuel.—C. E. Felton (Trans. A. I. M. E., Xvii, 509) reports a series of trials with oil as fuel in steel-heating and open-hearth steel-furnaces, and in raising steam, with results as follows: 1. In a run of six weeks the consumption of oil, partly refined (the paraffine and some of the nearby the best services) in hearing 14 in the insertion. and some of the naphtha being removed), in heating 14-inch ing tis in Siemens furnaces was about 614 gallons per ton of blooms. 2. In melting in a 30-ton open-hearth furnace 48 gallons of oil were used per ton of ingots. 3. In a six weeks' trial with Lima oil from 47 to 54 gallons of oil were required per ton of ingots. 4. In a six months' trial with Siemens heating-furnaces the consumption of Lima oil was 6 gallons per ton of ingots. Under the most favorable circumstances, charging hot ingots and running full capacity, 416 to 5 gallons per ton were required. 5. In raising steam in two 100-H, tubular boilers, the feed-water being supplied at 160° F., the average evaporation was about 12 pounds of water per pound of oil, the best 12 hours' work being 16 pounds.

In all of the trials the oil was vaporized in the Archer producer, an apparatns for mixing the oil and superheated steam, and heating the mixture to a high temperature. From 0.5 lb. to 0.75 lb. of pea-coal was used per gallon of oil in the producer itself.

FUEL GAS.

The following notes are extracted from a paper by W. J. Taylor on "The Energy of Fuel" (Trans. A. I. M. E., xviii. 205):

Carbon Gase.—In the old Siemens producer, practically, all the heat of primary combustion—that is, the burning of solid carbon to carbon monoxide, or about 80% of the total carbon energy—was lost, as little or no steam was used in the producer, and nearly all the sensible heat of the gas was dissipated in its passage from the producer to the furnace, which was usually placed at a considerable distance.

**Godern practice has improved on this plan, by introducing steam with the

ir blown into the producer, and by utilizing the sensible heat of the gas in he combustion-furnace. It ought to be possible to oxidize one out of every our lbs. of carbon with oxygen derived from water-vapor. The thermic eactions in this operation are as follows:

The steam which is blown into a producer with the air is almost all conensed into finely-divided water before entering the fuel, and consequently

s considered as water in these calculations.

The 1.5 lbs, of water liberates .167 lb, of hydrogen, which is delivered to be gas, and yields in combustion the same heat that it absorbs in the proucer by dissociation. According to this calculation, therefore, 60% of the eat of primary combustion is theoretically recovered by the dissociation of team, and, even if all the sensible heat of the gas be counted, with radiation and other minor items, as loss, yet the gas must carry 4 × 14.500 – 1748 + 3519 = 50,733 heat-units, or 87% of the calorific energy of the carbon, his estimate shows a loss in conversion of 13%, without crediting the gas ith its sensible heat, or charging it with the heat required for generating enecessary steam, or taking into account the loss due to oxidizing some f the carbon to CO₂. In good producer-practice the proportion of CO₂ in 12 me gas represents from 4% to 7% of the C burned to CO₂, but the extra heat this combustion should be largely recovered in the dissociation of more ater-vapor, and therefore does not represent as much loss as it would indicate. As a conveyer of energy, this gas has the advantage of carrying 4.46 s. less nitrogen than would be present if the fourth pound of coal had en gasified with air; and in practical working the use of steam reduces earount of clinkering in the producer.

Anthracite Gas.—In anthracite coal there is a volatile combustible trying in quantity from 1.5% to over 7%. The amount of energy derived on the coal is shown in the following theoretical gasification made with all of assumed composition: Carbon, 85%; vol. HC, 5%; ash, 10%; 80 lbs. carna assumed to be burned to CO; 5 lbs. carbon burned to CO; there fourths the necessary oxygen derived from air, and one fourth from water.

	Products,—			
Process.	Pounds.	Cubic Feet.	Anal. by Vol.	
9 lbs. C burned to CO	186.66	2529.24	33.4	
5 lbs. C burned to	18.33	157.64	2.0	
i lbs. vol. HC (distilled)	5.00	116. 6 0	1.6	
) lbs. oxygen are required, of which				
30 lbs. from H ₂ O liberate	8.75	712.50	9.4	
) lbs. from air are associatied with N	301.05	4064.17	53.6	
	514.79	7580.15	100.0	

he sum of CO and H exceeds the results obtained in practice. The senle heat of the gas will probably account for this discrepancy, and, theree, it is safe to assume the possibility of delivering at least 82% of the ergy of the anthracite.

Bituminous Gas.—A theoretical gasification of 100 lbs. of coal, conning 55% of carbon and 33% of volatile combustible (which is above the rage of Pittsburgh coal), is made in the following table. It is assumed it 50 lbs. of C are burned to CO and 5 lbs. to CO₂; one fourth of the O is

derived from steam and three fourths from air; the heat value of the volatile combustible is taken at 20,000 heat-units to the pound. In computing volumetric proportions all the volatile hydrocarbons, fixed as well as condensing, are classed as marsh-gas, since it is only by some such tentative assumption that even an approximate idea of the volumetric composition can be formed. The energy, however, is calculated from weight:

Process.	Pounds.	Cubic Feet.	Anal. by Vol.
50 lbs. C burned to	116.66	1580.7	27.8
5 lbs. C burned to	18.33	157. 6	2.7
32 lbs. vol. HC (distilled)	82.00	746.2	18.2
80 lbs. O are required, of which 20 lbs.,			
derived from H ₂ O, liberate H	2.5	475.0	8.8
60 lbs. O, derived from air, are asso-			
ciated withN	200.70	2709.4	47.8
	870.19	5668.9	99.8
Energy in 116.66 lbs. CO	504,	554 heat-units	
" " 82.00 lbs. vol. HC	640,0		
" 2.50 lbs. H	155,0	000 44	
	1,299,		
Energy in coal	1,487,0	i00 4	
Per cent of energy delivered	ingas	90.0)
Heat-units in 1 lb. of gas			

Water-gas.-Water-gas is made in an intermittent process, by blowing up the fuel-bed of the producer to a high state of incandescence (and in

up the fuelbed of the producer to a high state of incandecence (and in some cases utilizing the resulting gas, which is a lean producer gas), then shutting off the air and forcing steam through the fuel, which dissociates the water into its elements of oxygen and hydrogen, the former combining with the carbon of the coal, and the latter being liberated.

This gas can never play a very important part in the industrial field, owing to the large loss of energy entailed in its production, yet there are places and special purposes where it is desirable, even at a great excess in cost per unit of heat over producer gas; for instance, in small high-temperature furnaces, where much regeneration is impracticable, or where the "blow-up" gas can be used for other purposes instead of being wasted.

The reactions and energy required in the production of 1000 feet of watergas, composed, theoretically, of equal volumes of CO and H, are as follows:

2.635 lbs.

Total weight of 1000 cubic feet....... 39.525 lbs.

Now, as CO is composed of 12 parts C to 16 of O, the weight of C in 86.89 lbs. is 15.81 lbs. and of O 21.08 lbs. When this oxygen is derived from water it liberates, as above, 2.635 lbs. of hydrogen. The heat developed and absorbed in these reactions (roughly, as we will not take into account the energy required to elevate the coal from the temperature of the atmosphere to say 1800°) is as follows:

Heat-units. 2.635 lbs. H absorb in dissociation from water $2.625 \times 62,000... = 163,370$ 15.81 lbs. C burned to CO develops 15.81 × 4400..... = 69,564 Excess of heat-absorption over heat-development = 93,806

If this excess could be made up from C burnt to CO, without loss by radiation, we would only have to burn an additional 4.83 lbs. C to supply this heat, and we could then make 1000 feet of water-gas from 20.61 lbs. of carbon (equal 24 lbs. of 85% coal). This would be the perfection of gas-making, as the gas would contain really the same energy as the coal; but instead, we require in practice more than double this amount of coal, and do not deliver require in practice more than double this amount of coal, and to not derive more than 50% of the energy of the fuel in the gas, because the supporting heat is obtained in an indirect way and with imperfect combustion. Besides this, it is not often that the sum of the CO and H exceed 90%, the balance being CO₂ and N. But water-gas should be made with much less loss of energy by burning the "blow-up" (producer) gas in brick regenerators, the stored-up heat of which can be returned to the producer by the air used in blowing. blowing-up. The following table shows what may be considered average volumetric

dyses, and the weight and energy of 1000 cubic feet, of the four types of as used for heating and illuminating purposes:

	Natural Gas.	Coal- gas.	Water- gas.	Producer-gas.	
<u></u>	0.50 2.18 92.6 0.81 0.26 3.61 0.84	6.0 46.0 40.0 4.0 0.5 1.5 0.5	45.0 45.0 2.0 2.0 2.0 0.5	Anthra. 27.0 12.0 1.2 2.5 57.0 0.3	Bitu. 27.0 12.0 2.5 0.4 2.5 56.2 0.3
	%45.6 1,100,000	1.5 82.0 785,000	1.5 45.6 322,000	65.6 187,455	65.9 156,917

Natural Gas in Ohio and Indiana.

(Eng. and M. J., April 21, 1894.)

Ohio.				Indiana.				
escription.	Fos- toria.	Findlay	St Mary's.	Muncie.	Ander- son.	Koko- mo.	Mar- ion.	
rogen	1.89 92.84 .20 .55 .20 .35 3.82	1.64 98.35 .35 .41 .25 .89 8.41	1.94 98.85 .20 .44 .23 .85 2.98	2.35 92.67 .25 .45 .25 .25 .35	1.86 98.07 .47 .73 .26 .42 8.02	1.42 94.16 .80 .55 .29 .30 2.80	1.20 93.57 .15 .60 .30 .55 3.42	

proximately 30,000 cubic feet of gas have the heating power of one f coal.

Producer-gas from One Ton of Coal.

(W. H. Blauvelt, Trans. A. I. M. E., xviii. 614.)

rsis by Vol	Per Cent.	Cubic Feet.	Lbs.	Equal to—
difference.	25.3 9.2 3.1 0.8 3.4 58.2	12,077.76 4,069.68 1,050.24 4,463.52	174.66 77.78	77.78 " C ₂ H ₄ .
	100.0	131,280.00	8945.85	

ulated upon this basis, the 131,280 ft. of gas from the ton of coal con-120,311,162 B.T.U., or 155 B.T.U. per cubic ft., or 2270 B.T.U. per lb. composition of the coal from which this gas was made was as follows: 1.20%; volatile matter, 36.22%; fixed carbon, 57.98%; sulphur, 0.70%; 78%. One ton contains 1159.6 lbs. carbon and 724.4 lbs. volatile comle, the energy of which is 31,302,300 B.T.U. Hence, in the processes of ation and purification there was a loss of 35.2% of the energy of the

composition of the hydrocarbons in a soft coal is uncertain and quite ex; but the ultimate analysis of the average coal shows that it apies quite nearly to the composition of CH₄ (marsh-gas). Blauvelt emphasizes the following points as highly important in soft-

oducer-practice:

650 FUEL

First. That a large percentage of the energy of the coal is lost when the gas is made in the ordinary low producer and cooled to the temperature of the air before being used. To prevent these sources of loss, the producer should be placed so as to lose as little as possible of the sensible heat of the gas, and prevent condensation of the hydrocarbon vapors. A high fuel-bed should be carried, keeping the producer cool on top, thereby preventing the breaking-down of the hydrocarbons and the deposit of soot, as well as keeping the carbonic acid low.

Second. That a producer should be blown with as much steam mixed with the air as will maintain incandescence. This reduces the percentage of nitrogen and increases the hydrogen, thereby greatly enriching the gas. The temperature of the producer is kept down, diminishing the loss of heat by radiation through the walls, and in a large measure preventing clinkers.

by radiation through the walls, and in a large measure preventing clinkers.

The Combustion of Producer-gas. (H. H. Campbell, Trans. A. 1 M. E., xix. 128.)—The combustion of the components of ordinary pro-

ducer-gas may be represented by the following formulæ:

$$C_2H_4 + 6O = 2CO_2 + 2H_2O;$$
 $2H + O = H_2O;$ $CH_4 + 4O = CO_2 + 2H_2O;$ $CO + O = CO_2.$

AVERAGE COMPOSITION BY VOLUME OF PRODUCER-GAS: A, MADE WITH OPEN GRATES, NO STEAM IN BLAST; B, OPEN GRATES, STEAM-JET IN BLAST. 10 SAMPLES OF EACH.

	CO ₂ .	0.	C ₂ H ₄ .	co.	H.	CH ₄ .	N.
A min	3.6	0.4	б.2 `	20.0	5.3	3.0	58.7
A max	5.6	0.4	0.4	24.8	8.5	5.2	64.4
A average	4.84	0.4	0.34	22.1	6.8	3.74	61.78
B min		0.4	0.2	20.8	6.9	2.2	57.2
B max	6.0	0.8	0.4	24.0	9.8	8.4	62.0
B average		0.54	0.36	22.74	8.37	2.56	60.13

The coal used contained carbon 82%, hydrogen 4.7%.

The following are analyses of products of combustion:

	CO ₂ .	О.	co.	CH₄.	н.	N.
Minimum	15.2	0.2	trace.	trace.	trace.	80.1
Maximum	17.2	1.6	2.0	0.6	2.0	83.6
A verage	16.3	0.8	0.4	0.1	0.2	82.2

Use of Steam in Producers and in Boiler-furnaces. (R. W. Raymond, Trans. A. I. M. E., xx. 635.)—No possible use of steam can cause a gain of heat. If steam be introduced into a bed of incandescent carbon it is decomposed into hydrogen and oxygen.

The heat absorbed by the reduction of one pound of steam to hydrogen is much greater in amount than the heat generated by the union of the oxygen thus set free with carbon, forming either carbonic oxide or carbonic acid. Consequently, the effect of steam alone upon a bed of incandescent fuel is to chill it. In every water-gas apparatus, designed to produce by means of the decomposition of steam a fuel-gas relatively free from nitrogen, the loss of heat in the producer must be compensated by some reheating device.

This loss may be recovered if the hydrogen of the steam is subsequently burned, to form steam again. Such a combustion of the hydrogen is contemplated, in the case of fuel-gas as secured in the subsequent use of that gas. Assuming the oxidation of H to be complete, the use of steam will cause neither gain nor loss of heat, but a simple transference, the heat absorbed by steam decomposition being restored by hydrogen combustion. In practice, it may be doubted whether this restoration is ever complete. But it is certain that an excess of steam would defeat the reaction altogether, and that there must be a certain proportion of steam, which permits the realization of important advantages, without too great a net loss in

The advantage to be secured (in boiler furnaces using small sizes of anthractic) consists principally in the transfer of heat from the lower side of the fire, where it is not wanted, to the upper side, where it is wanted. The decomposition of the steam below cools the fuel and the grate-bars, whereas a blast of air alone would produce, at that point, intense combustion (forming at first CO_2), to the injury of the grate, the fusion of part of the fuel, etc.

The proportion of steam most economical is not easily determined. The temperature of the steam itself, the nature of the fuel mixture, and the use or non-use of auxiliary air-supply, introduced into the gases above or

reyond the fire-bed, are factors affecting the problem. (See Trans. 1. M. E., xx. 625)

Gas Analyses by Volume and by Weight.—To convert an analysis of a mixed gas by volume into analysis by weight: Multiply the perentage of each constituent gas by the density of that gas (see p. 166). Divide sach product by the sum of the products to obtain the percentages by weight.

Gas-fuel for Small Furnaces.—E. P. Reichhelm (Am. Mach., Ian. 10, 1895) discusses the use of gaseous fuel for forge fires, for droporging, in annealing-ovens and furnaces for melting brass and copper, for ase-hardening, muffle-furnaces, and kilns. Under ordinary conditions in uch furnaces he estimates that the loss by draught, radiation, and the neating of space not occupied by work is, with coal, 80%, with petroleum 70%, and with gas above the grade of producer-gas 25%. He gives the following able of comparative cost of fuels, as used in these furnaces:

Kind of Gas.	No. of Heat- units in 1,000 cu. ft. used.	No. of Heatunits in Furnaces after Deducting 25 Loss.	Average Cost per 1,000 Ft.	Cost of 1,000,- 000 Heat- units Ob- tained in Fur- naces.
latural gas. bal-gas, 20 candle-power larburetted water-gas. lasolene gas, 20 candle-power. Vater-gas from coke. Vater-gas from bituminous coal. Vater-gas and producer-gas mixed. roducer-gas laphtha-gas, fuel 2½ gals. per 1000 ft.	646,000 690,000 313,000 877,000 185,000 150,000 306,365	506,250 484,500 517,500 284,750 282,750 198,750 112,500 229,774	\$1.25 1.00 .90 .40 .45 .90	2.06 1.78 1.70 1.59 1.44 1.83
oal, \$4 per ton, per 1,000,000 heat-units rude petroleum, 3 cts. per gal., per 1,0	utilized	at-units.	•••••	.78 .73

Mr. Reichhelm gives the following figures from practice in melting brass ith coal and with naphtha converted into gas: 1800 lbs. of metal require 180 lbs. of coal, at \$4.65 per ton, equal to \$2.51, or, say, 15 cents per 101 lbs. fr T.'s report: 2500 lbs. of metal require 47 gals. of naphtha, at 6 cents per al., equal to \$2.82, or, say, 11½ cents per 100 lbs.

ILLUMINATING-GAS.

Coal-gas is made by distilling bituminous coal in retorts. The retort usually a long horizontal semi-cylindrical or a shaped chamber, holding om 180 to 300 lbs. of coal. The retorts are set in benches of from to 9, heated by one fire, which is generally of coke The vapora distilled om the coal are converted into a fixed gas by passing through the retort, hich is heated almost to whiteness.

The gas passes out of the retort through an "ascension-pipe" into a long orizontal pipe called the hydraulic main, where it deposits a portion of ne tar it contains; thence it goes into a condenser, a series of iron tubes arrounded by cold water, where it is freed from condensable vapors, as mmonia-water, then into a washer, where it is exposed to jets of water, nd into a scrubber, a large chamber partially filled with trays made of ood or iron, containing coke, fragments of brick or paving-stones, which re wet with a spray of water. By the washer and scrubber the gas is freed om the last portion of tar and ammonia and from some of the sulphur mpounds. The gas is then finally purified from sulphur compounds by assing it through lime or oxide of iron. The gas is drawn from the hyperbolic productions of the sulphur compounds by the production of the pro raulic main and forced through the washer, scrubber, etc., by an exhauster rgas pump.

The kind of coal used is generally caking bituminous, but as usually this cal is deficient in gases of high illuminating power, there is added to it a ortion of cannel coal or other enricher.

The following table, abridged from one in Johnson's Cyclopedia, showie analysis, candle power, etc., of some gas-coals and enrichers:

· Gas-coals, etc.	Vol. Matter.	d Carb.		per ton 2240 lbs. cu. ft.	pow'r las.	ton o	e per of 2240 bs.	purified bush. of incu.ft.
	Vol. 1	Fixed	Ash.	Gas 1 of 2 in c	Cand.	lbs.	bush.	Gas by 1 line
Pittsburgh, Pa	36.76 36.00 37.50 40.00 43.00 46.00 58.50	56.90 53.30 40.00 41.00	6.00 5.60 6.70 17.00 13.00	10,642 10,528 10,765	18.81 20.41 34.98	1480 1540 1320 1380	40 86 86 82 82 44	6420 8998 2494 2806 4510

The products of the distillation of 100 lbs. of average gas-coal are about as follows. They vary according to the quality of coal and the temperature of distillation.

Coke, 64 to 65 lbs.; tar, 6.5 to 7.5 lbs.; ammonia liquor, 10 to 12 lbs.; puri-

fied gas, 15 to 12 lbs.; impurities and loss, 4.5% to 3.5%.

The composition of the gas by volume ranges about as follows: Hydrogen, 38% to 48%; carbonic oxide, 2% to 14%; marsh-gas (Methane, CH₄), 48% to 31%; heavy hydrocarbons (C₂H₂n, ethylene, propylene, benzole vapor, etc.),

7.5% to 4.5%; nitrogen, 1% to 8%.

In the burning of the gas the nitrogen is inert; the hydrogen and carbonic oxide give heat but no light. The luminosity of the flame is due to the decomposition by heat of the heavy hydrocarbons into lighter hydrocarbons and carbon, the latter being separated in a state of extreme subdivision. By the heat of the flame this separated carbon is heated to intense whiteness, and the illuminating effect of the flame is due to the light of incandescence of the particles of carbon.

The attainment of the highest degree of luminosity of the flame depends upon the proper adjustment of the proportion of the heavy hydrocarbons (with due regard to their individual character) to the nature of the diluent

mixed therewith.

Investigations of Percy F. Frankland show that mixtures of ethylene and hydrogen cease to have any luminous effect when the proportion of ethylene does not exceed 10% of the whole. Mixtures of ethylene and carbonic oxide cease to have any luminous effect when the proportion of the former does not exceed 20%, while all mixtures of ethylene and marsh-gas have more or less luminous effect. The luminosity of a mixture of 10% ethylene and 90% ethylene and 80% marsh-gas about 25 candles, and that of one of 20% ethylene and 80% marsh-gas about 25 candles. The illuminating effect of marsh-gas

and on the burned in an argand burner, is by no means inconsiderable.

For further description, see the Treatises on Gas by King. Richards, and Hughes; also Appleton's Cyc. Mech., vol. i. p. 900.

Water-gas.—Water-gas is obtained by passing steam through a bed of coal, coke, or charcoal heated to redness or beyond. The steam is deconnected the burners and the standard of the steam is deconnected. cost, coke, or charcoal neated to redness or beyond. The steam is decomposed, its hydrogen being liberated and its oxygen burning the carbon of the fuel, producing carbonic-oxide gas. The chemical reaction is, $C + H_2O = CO + 2H$, or $2C + 2H_2O = C + CO_2 + 4H$, followed by a splitting upon the CO₂, making 2CO + 4H. By weight the normal gas CO + 2H is composed of C + O + H = 28 parts CO and 2 parts H, or 93.33% CO and 6.67% H; by volume it is composed of equal parts of carbonic oxide and hydrogen are produced as above described here were the states now but no

Water-gas produced as above described has great heating-power, but no illuminating-power. It may, however, be used for lighting by causing it to heat to whiteness some solid substance, as is done in the Welsbach incan-

descent light.

An illuminating-gas is made from water-gas by adding to it hydrocarbon gases or vapors, which are usually obtained from petroleum or some of its products. A history of the development of modern illuminating water-gas processes, together with a description of the most recent forms of apparatus, is given by Alex. C. Humphreys, in a paper on "Water-gas in the United States," read before the Mechanical Section of the British Association for Advancement of Science, in 1889. After describing many earlier patents, he states that success in the manufacture of water-gas may be said to date com 1874, when the process of T. S. C. Lowe was introduced. All the later lost successful processes are the modifications of Lowe's, the essential stures of which were "an apparatus consisting of a generator and superester internally fired; the superheater being heated by the secondary mbustion from the generator, the heat so stored up in the loose brick of superheater being used, in the second part of the process, in the fixing rendering permanent of the hydrocarbon gases; the second part of the rocess consisting in the passing of steam through the generator fire, and is admission of oil or hydrocarbon at some point between the fire of the enerator and the loose filling of the superheater."

The water-gas process thus has two periods: first the "blow," during hich air is blown through the bed coal in the generator, and the partially urned gaseous products are completely burned in the superheater, giving p a great portion of their heat to the fire-brick work contained in it, and ien pass out to a chimney; second, the "run" during which the air blast stopped, the opening to the chimney closed, and steam is blown through is incandescent bed of fuel. The resulting water-gas passing into the carrecting chamber in the base of the superheater is there charged with hyrocarbon vapors, or spray (such as naphtha and other distillates or crude i) and passes through the superheater, where the hydrocarbon vapors be me converted into fixed illuminating gases. From the superheater the mbined gases are passed, as in the coal-gas process, through washers, rubbers, etc., to the gas-holder. In this case, however, there is no amonta to be removed.

The specific gravity of water-gas increases with the increase of the heavy drocarbons which give it illuminating power. The following figures, taken om different authorities, are given by F. H. Shelton in a paper on Waters, read before the Ohio Gas Light Association, in 1894:

Analyses of Water-gas and Coal-gas Compared,

The following analyses are taken from a report of Dr. Gideon E. Moore the Granger Water-gas, 1885:

	Compos	ition by V	olume.	Composition by Weight.			
	Water-gas.		Coal-gas. Heidel-	Water-	Coal-		
	Wor- cester.	Lake.	berg.	Wor- cester.	Lake.	gas.	
rogenrbonic acidygenyleneyptleneyptleneyptlenezole vaporrbonic oxide.rsh-gasdrogen	2.64 0.14 0.06 11.29 0.00 1.58 28.26 18.88 87.20	8.85 0.30 0.01 12.80 0.00 2.63 23.58 20.95 85.88	2.15 8.01 0.65 2.55 1.21 1.33 8.88 34.02 46.20	0.04402 0.00365 0.00114 0.18759 0.07077 0.46984 0.17928 0.04421	0.06175 0.00753 0.00018 0.20454 0.11700 0.87664 0.19138 0.04108	0.18758	
nsity : Theory.	0.5825	0.6057	0.4580	1.00000	1.00000	1.00000	
Practice. . U. from 1 cu: Water liquid vapor.	650.1	0.6018 688.7 646.6	642.0 577.0				
me-temp	5311.2°F.	5281.1°F.	5202.9°F.				
candle-power.	22.06	26.31	1	<u> </u>	J	<u> </u>	

ne heating values (B. T. U.) of the gases are calculated from the analysis veight, by using the multipliers given below (computed from results of

J. Thomsen), and multiplying the result by the weight of 1 cu. ft. of the gas at 62° F., and atmospheric pressure.

The flame temperatures (theoretical) are calculated on the assumption of complete combustion of the gases in air, without excess of air.

The candle-power was determined by photometric tests, using a pressure of 16-in, water-column, a candle consumption of 120 grains of spermaceti per hour, and a meter rate of 5 cu. ft. per hour, the result being corrected for a temperature of 62° F. and a barometric pressure of 30 in. It appears that the candle-power may be regulated at the pleasure of the person in charge of the appearatus, the range of candle-power being from 20 to 29 candles, according to the manipulation employed.

Calorific Equivalents of Constituents of Illuminatingcor.

	Heat-units	from 1 lb.	F	Ieat-units	from 1 lb
	Water	Water		Water	Water
	Liquid.	Vapor.			· Vapor.
Ethylene	21,524.4	20,134.8	Carbonic oxide	4,395.6	4,395.6
Propylene	21,222.0		Marsh-gas		21,592.8
Benzole vapor		17,847.0	Hydrogen	61,524.0	51,804.0
			_ ^ . ~		

Efficiency of a Water-gas Plant.—The practical efficiency of an illuminating water-gas setting is discussed in a paper by A. G. Glasgow (Proc. Am. Gaslight Assn., 1890), from which the following is abridged:

The results refer to 1000 cu. ft. of unpurified carburetted gas, reduced to

60° F. The total anthracite charged per 1000 cu. ft. of gas was 33.4 lbs., ash and unconsumed coal removed 9.9 lbs., leaving total combustible consumed 23.5 lbs., which is taken to have a fuel-value of 14500 B. T. U. per pound, or a total of 340,750 heat-units.

	Composi- tion by Volume.	Weight per 100 cu. ft.	Composition by Weight.	Specific Heat.
I. Carburetteŭ Water-gas, $\begin{bmatrix} CO_2 + H_2S \\ C_2H_{2n} \\ CO & \\ CH_4 \\ N \end{bmatrix}$	3.8 14.6 28.0 17.0 35.6 1.0	.465842 1.139968 2.1868 .75854 .1991464 .078596	.09647 .23607 .45285 .15710 .04124 .01627	.02088 .08720 .11226 .09314 .14041 .00397
	100.0	4.8288924	1.00000	.45786
II. Uncarburetted gas. $\begin{cases} \frac{\text{CO}_2}{\text{co}} & \dots & \dots \\ \text{H} & \dots & \dots \\ \frac{\text{N}}{\text{N}} & \dots & \dots \end{cases}$	8.5 48.4 51.8 1.3	.429065 3.389540 .289821 .102175 4.210601	.1019 .8051 .0688 .0242	.02205 .19958 .23424 .00591
III. Blast products escaping from superheater.	17.4 3.2 79.4 100.0	2.133066 .2856096 6.2405224 8.6591980	.7207	.05342 .00718 .17585
IV. Generator blast-gases. $\begin{bmatrix} CO_2 & \dots & \\ CO & \dots & \\ N & \dots & \end{bmatrix}$	17.8 72.5	1.189123 1.390180 5.698210	.1436 .1680 .6884	.031075 .041647 .167970
	100.0	8.277518	1.0000	.240692

The heat energy absorbed by the apparatus is $23.5 \times 14,500 = 340,750$ heat units = A. Its disposition is as follows:

P, the energy of the CO produced;C, the energy absorbed in the decomposition of the steam;

D, the difference between the sensible heat of the escaping illuminating gases and that of the entering oil;

E, the heat carried off by the escaping blast products; F, the heat lost by radiation from the shells:

G. the heat carried away from the shells by convection (air-currents);

H, the heat rendered latent in the gasification of the oil;

I, the sensible heat in the ash and unconsumed coal recovered from the generator.

The heat equation is A = B + C + D + E + F + G + H + I; A being known. A comparison of the CO in Tables I and II show that $\frac{280}{484}$, or 64.5%

of the volume of carburetted gas is pure water-gas, distributed thus: CO₃, 2.8%; CO, 28.0%; H, 33.4%; N, 0.8%; = 64.5%. 1 lb. of CO at 60° F. = 13 531 eu. ft. CO per 1000 cu. ft. of gas = 280 + 13.531 e 20.694 lbs. Energy of the CO = 20.694 \times 4.20 \t

(The specific heat of the entering oil is approximately that of the issuing

The heat carried off in 1000 cu. ft. of the escaping blast products is 86.592 (weight) \times .23645 (sp. heat) \times 1474° (rise of temp.) = 30,180 heat-units: the temperature of the escaping blast gases being 1550° F., and that of the entering air 76° F. But the amount of the blast gases, by registration of an anemometer, checked by a calculation from the analyses of the blast gases, was 2457 cubic feet for every 1000 cubic feet of carburetted gas made. Hence the heat carried off per M. of carburetted gas is 30,180 \times 2.457 = 74.152 heat-units = E.

Experiments made by a radiometer covering four square feet of the shell of the apparatus gave figures for the amount of heat lost by radiation = 12,454 heat-units = F, and by convection = 15,696 heat-units = G.

The heat rendered latent by the gasefication of the oil was found by taking the difference between all the heat fed into the carburetter and superheater and the total heat dissipated therefrom to be 12.841 heat-units = H. The sensible heat in the ash and unconsumed coal is 9.9 lbs. \times 1500° \times .25 (sp. ht.) = 3712 heat-units = I.

(sp. ht.) = 3712 heat-units = I. The sum of all the items B+C+D+E+F+G+H+I=827,395 heat-units, which substracted from the heat energy of the combustible consumed, 340,750 heat-units, leaves 13,455 heat-units, or 4 per cent, unaccounted for

Of the total heat energy of the coal consumed, or 340,750 heat-units, the energy wasted is the sum of items D, E, F, G, and I, amounting to 132,878 heat-units, or 89 per cent; the remainder, or 207,872 heat-units, or 61 per cent, being utilized. The efficiency of the apparatus as a heat machine is therefore 61 per cent.

Five gallons, or 35 lbs. of crude petroleum were fed into the carburetter per 1000 cu. ft. of gas made; deducting 5 lbs. of tar recovered, leaves 30 lbs. 20,000 = 600,000 heat-units as the net heating value of the petroleum used. Adding this to the heating value of the coal, 340,750 B. T. U., gives 940,750 heat-units, of which there is found as heat energy in the carburetted gas, as in the table below, 764,050 heat units, or 81 per cent, which is the commercial efficiency of the apparatus, i.e., the ratio of the energy contained in the finished product to the total energy of the coal and oil consumed.

The heating power per M. cu. ft. of] The heating power per M. of the uncarburetted gas is the carburetted gas is CO3 85.0 $434.0 \times .078100 \times 4395.6 = 148991$ $280.0 \times .078100 \times 4895.6 = 96120 \text{ H}$ $170.0 \times .044620 \times 24021.0 = 182210 \text{ N}$ $856.0 \times .005594 \times 61524.0 = 122520 \text{ N}$ $518.0 \times .005594 \times 61524.0 = 178277$ ĊH₄ 18,0 1000.0 327268 10.0 1000.0 764050

^{*}The heating value of the illuminants CaH_{2n} is assumed to equal that of C₂H₄.

The candle-power of the gas is 31, or 6.2 candle-power per gallon of oil used. The calculated specific gravity is .6355, air being 1.

For description of the operation of a modern carburetted water-gas plant, see paper by J. Stelfox, Eng'g, July 20, 1894, p. 89.

Space required for a Water-gas Plant.—Mr. Shelton, taking 15 modern plants of the form requiring the most floor-space, figures the average floor-space required per 1000 cubic feet of daily capacity as follows:

Water-gas Plants of Capacity Require an Area of Floor-space for each 1000 cu. ft. of about in 24 hours of 100,000 cubic feet...... 4 square feet. 200,000 " 2.75 " 400,000 " 600,000 "

These figures include scrubbing and condensing rooms, but not boiler and engine rooms. In coal-gas plants of the most modern and compact forms one with 16 benches of 9 retorts each, with a capacity of 1,500,000 cubic feet per 24 hours, will require 4.8 sq. ft. of space per 1000 cu. ft. of gas, and one of 6 benches of 6 retorts each, with 300,000 cu. ft. capacity per 24 hours will require 6 sq. ft. of space per 1000 cu. ft. capacity per 24 hours will require 6 sq. ft. of space per 1000 cu. ft. The storage-room required for the gas-making materials is: for coal-gas, 1 cubic foot of room for every 232 cubic feet of gas made; for water-gas made from coke, 1 cubic foot of room for some 232 cu. ft. of gas made; for water-gas made from coke, 1 cubic foot of room for every 878 cu. ft. of gas made; and for water-gas made from anthracite, 1 cu. ft. of room for every 645 cu. ft. of gas made. The comparison is still more in favor of water-gas if the case is considered

The comparison is still more in favor of water-gas if the case is considered of a water-gas plant added as an auxiliary to an existing coal-gas plant for, instead of requiring further space for storage of coke, part of that already required for storage of coke produced and not at once sold can be cut off, by reason of the water-gas plant creating a constant demand for more or less of the coke so produced.

Mr. Shelton gives a calculation showing that a water-gas of .625 sp. gr. would require gas-mains eight per cent greater in diameter than the same quantity coal-gas of .425 sp. gr. if the same pressure is maintained at the holder. The same quantity may be carried in pipes of the same diameter than the same pressure is increased in proportion to the specific gravity. With the same pressure the increase of candle-power about balances the decrease of fow. With five feet of coal-gas, giving, say, eighteen candle-power, 1 cubic foot equals 3.6 candle-power, and 4 cubic feet gives 18.4 candle-power, more than is given by 5 cubic feet of coal-gas. Water-gas may be made from oven-coke or gas-house coke as well as from anthracite coal. A water-gas plant may be conveniently run in connection with a coal-gas plant, the surplus retort coke of the latter being used as the fuel of the former. surplus retort coke of the latter being used as the fuel of the former. In coal-gas making it is impracticable to enrich the gas to over twenty

candle-power without causing too great a tendency to smoke, but water-gas of as high as thirty candle-power is quite common. A mixture of coal-gas and water-gas of a higher C.P. then 20 can be advantageously distributed.

Fuel-value of, Illuminating-gas.—E. G. Love (School of Mines Qtly, January, 1892) describes F. W. Hartley's calorimeter for determining Otly, January, 1892) describes F. W. Hartley's calorimeter for determining the calorific power of gases, and gives results obtained in tests of the carburetted water-gas made by the municipal branch of the Consolidated Copf New York. The tests were made from time to time during the past two fears, and the figures give the heat-units per cubic foot at 60° F. and 80 inches pressure: 715, 692, 725, 732, 691, 788, 785, 708, 784, 780, 781, 727. Average, 721 heat units. Similar tests of mixtures of coal- and water-gases made by other branches of the same company give 694, 715, 684, 692, 727, 665, 695, and 686 heat-units per foot, or an average of 694.7. The average of all these tests was 710.5 heat-units, and this we may fairly take as representing the calorific power of the illuminating gas of New York. One thousand feet of this gas, costing \$1.25, would therefore yield 710,500 heat-units, which would be equivalent to 568,400 heat-units for \$1.00.

The common coal-gas of London, with an illuminating power of 16 to 17 candles, has a calorific power of about 668 units per foot, and costs from 60 to 70 cents per thousand.

to 70 cents per thousand.

The product obtained by decomposing steam by incandescent carbon, as effected in the Motay process, consists of about 40% of CO, and a little over 50% of H.

This mixture would have a heating-power of about 300 units per cubic foot, and if sold at 50 cents per 1000 cubic feet would furnish 600,000 units for \$1.00, as compared with 568,400 units for \$1.00 from illuminating gas at \$1.25 per 1000 cubic feet. This illuminating-gas if sold at \$1.15 per thousand would therefore be a more economical heating agent than the fuel-gas mentioned, at 50 centers are thousand and be made and the second and the second and the second and the second are second as a second as a second and the second and the second are second as a second cents per thousand, and be much more advantageous than the latter, in that one main, service, and meter could be used to furnish gas for both lighting and heating.

A large number of fuel-gases tested by Mr. Love gave from 184 to 470 heat-

units per foot, with an average of 309 units.

Taking the cost of heat from illuminating gas at the lowest figure given by Mr. Love, viz., \$1.00 for 600,000 heat-units, it is a very expensive fuel, equal to coal at \$40 per ton of 2000 lbs., the coal having a calorific power of only 12,000 heat-units per pound, or about 83% of that of pure carbon:

 $600,000: (12,000 \times 2000):: $1:$40.$

FLOW OF GAS IN PIPES.

The rate of flow of gases of different densities, the diameter of pipes required, etc., are given in King's Treatise on Coal Gas, vol. ii. 874, as follows:

If
$$d=$$
 diameter of pipe in inches, $Q=$ quantity of gas in cu. ft. per $l=$ length of pipe in yards, $l=$ length of pipe in yards, $l=$ specific gravity of gas, air being 1,
$$d=\frac{c}{\sqrt{(1850)^3h^5}},$$

$$d=\frac{c^3}{\sqrt{(1850)^3h^5}},$$

$$d=\frac{c^3}{\sqrt{(1850)^3h^5}},$$

$$Q=1850d^3\sqrt{\frac{dh}{sl}}=1850\sqrt{\frac{d^5h}{sl}}.$$
 Molesworth gives $Q=1000\sqrt{\frac{d^5h}{sl}}$.

Molesworth gives
$$Q = 1000 \sqrt{\frac{sl}{sl}}$$
.

J. P. Gill, Am. Gas-light Jour. 1894, gives
$$Q = 1291 \sqrt{\frac{d^4h}{s(l+d)}}$$
.

This formula is said to be based on experimental data, and to make allowance for obstructions by tar, water, and other bodies tending to check the

flow of gas through the pipe.

A set of tables in Appleton's Cyc. Mech. for flow of gas in 2, 6, and 12 in. pipes is calculated on the supposition that the quantity delivered varies

as the square of the diameter instead of as $d^2 \times \sqrt[4]{d}$, or $\sqrt[4]{d^5}$. These tables give a flow in large pipes much less than that calculated by the formulæ above given, as is shown by the following example. Length of pipe 100 yds., specific gravity of gas 0.42, pressure 1-in. water-column

		6-in. Pipe.	12-in. Pipe,
$Q = 1350 \sqrt{\frac{d^5h}{st}} \dots$	1178	18,368	108,912
$Q = 1000 \sqrt{\frac{d^5h}{sl}} \cdots$	873	18,606	76,972
$Q = 1291 \sqrt{\frac{d^5h}{s(l+d)}} \cdots$	1116	16,827	98,845
Table in App. Cyc	1290	11,657	46,628

An experiment made by Mr. Clegg, in London, with a 4-in. pipe, 6 miles long, pressure 3 in. of water, specific gravity of gas .898, gave a discharge into the atmosphere of 852 cu. ft. per hour, after a correction of 33 cu. ft. was made for leakage.

Substituting this value, 852 cu. ft., for Q in the formula $Q = C \sqrt{d^5h + sl}$, we find C, the coefficient, = 997, which corresponds nearly with the formula given by Molesworth.

Services for Lamps. (Molesworth.)

_ Ft. from	Require		Ft. from	Require
Lamps. Main.	Pipe-bore.	Lamps.	Main.	Pipe-bore.
2 40	3% in.	15	130	l in.
4 40	⅓ in.	20	150	1¼ in.
6 50	5% in.	25	180	116 in.
10 100	¾ in.	80	200	1 % in.

(In cold climates no service less than ¾ in. should be used.)

Maximum Supply of Gas through Pipes in cu. ft. per Hour, Specific Gravity being taken at .45, calculated from the Formula $Q=1000 \sqrt{d^5h+st}$. (Molesworth.)

LENGTH OF PIPE = 10 YARDS.

Diameter of Pipe in	Pressure by the Water-gauge in Inches.											
Inches.	.1	.જ	.8	.4	.5	.6	.7	.8	.9	1.0		
96 14 24 14	13 26 78 149 260	18 37 103 211 368	22 46 126 258 451	26 53 145 298 521	29 59 162 338 582	81 64 187 865 638	84 70 192 394 689	86 74 205 422 787	88 79 218 447 781	41 83 230 471 823		
11/4 11/2 2	411 843	591 1192	711 1460	821 1686	918 1886	1006 2066	1082 2281	1162 2385	1232 2530	1299 2667		

LENGTH OF PIPE = 100 YARDS.

		Pressure by the Water-gauge in Inches.											
	.1	.2	.3	.4	.5	.75	1.0	1.25	1.5	2	2.5		
34	8	12		17	19	23	26	29	82	36 103	42		
.34	23	32	42	46	51	68	73	81	89	108	115		
1	47	67	88	94	105	129	149	167	183	211	236		
11/4	82	116	143	165	184	225	260	291	819	3 68	412		
112	180	184	225	260	290	356	411	459	503	581	649		
2′~	267	377	462	533	596	730	843	948	1083	1198	1338		
216	466	659		982	1042	1276	1473	1647	1804	2083	2329		
8/*		1039		1470	1648	2012	2323	2598	2846	8286	3674		
814		1528		2161	2416	2958	3416	3820	4184	4831	5402		
114 114 214 214 3	1508				3373	4131	4770	5333	5842	6746	7542		

LENGTH OF PIPE = 1000 YARDS.

		Pressure by the Water-gauge in Inches.											
	.5	.75	1.0	1.5	2.0	2.5	8.0						
1 11/6 28/6 3	33 92 189 829 520	41 118 281 403 636	47 180 267 466 785	58 159 827 571 900	67 184 877 659 1039	75 205 422 787 1162	89 226 462 807 1278						
5 6	1067 1863 2989	1806 2282 8600	1508 2685 4157	1847 8227 5091	2188 8727 5879	2885 4167 6678	2613 4564 7 200						

LENGTH OF	Pipe =	5000	YARDS.
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Diameter of Pipe		Pressure by the Water-gauge in Inches.									
in Inches.	1.0	1.5	2.0	2.5	8.0						
2 3 4 5 6	119 329 675 1179 1859 2783	146 402 826 1443 2277 8847	169 465 955 1667 2629 3865	189 520 1067 1868 2939 4321	207 569 1168 2041 3220 4734						
8 9 10 12	8816 5128 6667 10516	4674 6274 8165 12880	5897 7245 9428 14872	6034 8100 10541 16628	6610 8873 11547 18215						

Mr. A. C. Humphreys says his experience goes to show that these tables give too small a flow, but it is difficult to accurately check the tables, on account of the extra friction introduced by rough pipes, bends, etc. For bends, one rule is to allow 1/42 of an inch pressure for each right-angle bend.

Where there is apt to be trouble from frost it is well to use no service of less diameter than ¾ in., no matter how short it may be. In extremely cold climates this is now often increased to 1 in., even for a single lamp. The best practice in the U.S. now condemns any service less than ¾ in.

STEAM.

The Temperature of Steam in contact with water depends upon the pressure under which it is generated. At the ordinary atmospheric pressure (14.7 lbs. per sq. in.) its temperature is 212° F. As the pressure is increased, as by the steam being generated in a closed vessel, its temperature, and that of the water in its presence, increases.

Saturated Steam is steam of the temperature due to its pressure not superheat-d

Superheated Steam is steam heated to a temperature above that due to its pressure.

Dry Steam is steam which contains no moisture. It may be either

saturated or superheated.

Wet Steam is steam containing intermingled moisture, mist, or spray.

It has the same temperature as dry saturated steam of the same pressure. Water introduced into the presence of superheated steam will fash into vapor until the temperature of the steam is reduced to that due its pressure. Water in the presence of saturated steam has the same temperature as the steam. Should cold water be introduced, lowering the temperature of the whole mass, some of the steam will be condensed, reducing the pressure and temperature of the remainder, until an equilibrium is established.

Temperature of the remainder, until an equilibrium is established.

Temperature and Pressure of Saturated Steam.—The relation between the temperature and the pressure of steam, according to Regnault's experiments, is expressed by the formula (Buchanan's, as given 2938.16

by Clark) $t = \frac{2300 \cdot 10}{6.1993544 - \log p} - 371.85$, in which p is the pressure in pounds per square inch and t the temperature of the steam in Fahrenheit degrees.

per square inch and t the temperature of the steam in Fahrenheit degrees. It applies with accuracy between 120° F. and 446° F., corresponding to pressures of from 1.68 lbs. to 445 lbs per square inch. (For other formulæ see Wood's and Peabody's Thermodynamics.)

Total Heat of Saturated Steam (above 32° F.).—According to Regnault's experiments, the formula for total heat of steam is H=1091.7+305(t-32°), in which t is temperature Fahr., and H the heat-units. (Rankine and many others; Clark gives 1091.16 instead of 1091.7.)

Latent Heat of Steam.—The formula for latent heat of steam, as given by Rankine and others, is $L = 1091.7 - .695(t - 32^\circ)$. Clausius's formula, in Fahrenheit units, as given by Clark, is $L = 1092.6 - .708(t - 32^\circ)$.

The total heat in steam (above 32°) includes three elements:

1st. The heat required to raise the temperature of the water to the temperature of the steam.

2d. The heat required to evaporate the water at that temperature, called

internal latent heat.

3d. The latent heat of volume, or the external work done by the steam in making room for itself against the pressure of the superincumbent atmosphere (or surrounding steam if inclosed in a vessel).

The sum of the last two elements is called the latent heat of steam. In Buel's tables (Weisbach, vol. ii., Dubois's translation) the two elements are

given separately.

Latent Heat of Volume of Saturated Steam. (External Work)—The following formulas are sufficiently accurate for occasional use within the given ranges of pressure (Clark, S. E.):

From 14.7 lbs. to 50 lbs. total pressure per square inch... 55.900 + .0772t. From 50 lbs. to 200 lbs. total pressure per square inch... 59.191 + .0655t.

Heat required to Generate 1 lb. of Steam from water at 32° F.

Heat-units. Sensible heat, to raise the water from 82° to 212° = Latent heat, 1, of the formation of steam at 212° = 894.0 180.9 2, of expansion against the atmospheric pressure, 2116.41bs, per sq. ft. ×26.86 cu. ft. = 55,786 foot-pounds + 778 = 965.7 71.7 Total heat above 82° F...... 1146.6

The Heat Unit, or British Thermal Unit.—The definition of the heat-unit used in this work is that of Rankine, accepted by most modern writers, viz., the quantity of heat required to raise the temperature of 1 lb. of water 1° F. at or near its temperature of maximum density (39.1° F.). Peabody's definition, the heat required to raise a pound of water from 62° to 63° F. is not generally accepted. (See Thurston, Trans. A. S. M. E.,

Specific Heat of Saturated Steam.—The specific heat of saturated steam is .805, that of water being 1; or it is 1.281, if that of air be 1. The expression .305 for specific heat is taken in a compound sense, relating to changes both of volume and of pressure which takes place in the eleva-tion of temperature of saturated steam. (Clark, S. E.)

This statement by Clark is not strictly accurate. When the temperature

of saturated steam is elevated, water being present and the steam remaining saturated, water is evaporated. To raise the temperature of 1 lb. of water 1° F. requires 1 thermal unit, and to evaporate it at 1° F. higher word require 0.695 less thermal unit, the latent heat of saturated steam decreasing 0.695 B.T.U. for each increase of temperature of 1° F. Hence 0.305 is the specific heat of water and its saturated vapor combined.

When a unit weight of saturated steam is increased in temperature and in

pressure, the volume decreasing so as to just keep it saturated, the specific heat is negative, and decreases as temperature increases. (See Wood, Therm., p. 147; Peahody, Therm., p. 93.)

Density and Volume of Saturated Steam.—The density of

steam is expressed by the weight of a given volume, say one cubic foot; and the volume is expressed by the number of cubic feet in one pound of steam.

Mr. Brownlee's expression for the density of saturated steam in terms of

the pressure is $D = \frac{p^{.941}}{330.36}$, or log $D = .941 \log p - 2.519$, in which D is the density, and p the pressure in pounds per square inch. In this expression, p^{-941} is the equivalent of p raised to the 16/17 power, as employed by Rankine. The volume v being the reciprocal of the density,

$$v = \frac{830.36}{p^{.941}}$$
, or $\log v = 2.519 - .941 \log p$.

Relative Volume of Steam.—The relative volume of saturated steam is expressed by the number of volumes of steam produced from one

volume of water, the volume of water being measured at the temperature 39° F. The relative volume is found by multiplying the volume in cu. ft. of one lb, of steam by the weight of a cu. ft. of water at 39° F., or 62.425 lbs. Gaseous Steam.—When saturated steam is superheated, or surcharged with heat, it advances from the condition of saturation into that of gaseity. The gaseous state is only arrived at by considerably elevating the

temperature, supposing the pressure remains the same. Steam thus suffi-ciently superheated is known as gaseous steam or steam gas. Total Heat of Gaseous Steam.—Regnault found that the total heat of gaseous steam increased, like that of saturated steam, uniformly with the temperature, and at the rate of .475 thermal units per pound for

each degree of temperature, under a constant pressure.

each degree of temperature, under a constant pressure. The general formula for the total heat of gaseous steam produced from 1 pound of water at 32° F. is H=1074.6+.475t. [This formula is for vapor generated at 32° . It is not true if generated at 312° , or at any other temperature than 32° . (Prof. Wood.)]

The Specific Heat of Gaseous Steam is .475, under constant pressure, as found by Regnault. It is identical with the coefficient of increase of total heat for each degree of temperature. [This is at atmospheric pressure and 212° F. He found it not true for any other pressure. Theory indicates that it would be greater at higher temperatures. (Prof. Wood.)]

The Specific Density of Gaseous Steam is 623, that of air being 1. That is to say, the weight of a cubic foot of gaseous steam is about five eighths of that of a cubic foot of air, of the same pressure and temperature. The density or weight of a cubic foot of gaseous steam is expressible by the same formula as that of air, except that the multiplier or coefficient is

less in proportion to the less specific density. Thus,

$$D' = \frac{2.7074p \times .622}{t + 461} = \frac{1.684p}{t + 461},$$

in which D' is the weight of a cubic foot of gaseous steam, p the total pressure per square inch, and t the temperature Fahrenheit.

Superheated Steam. -The above remarks concerning gaseous steam are taken from Clark's Steam-engine. Wood gives for the total heat (above 32°) of superheated steam $H=1091.7+0.48(t-32^{\circ})$. The following is abridged from Peabody (Therm., p. 115, etc.).

When far removed from the temperature of saturation, superheated steam follows the laws of perfect gases very nearly, but near the temperature of saturation the departure from those laws is too great to allow of calculations by them for engineering purposes.

The specific heat at constant pressure, Cp, from the mean of three experi-

ments by Regnault, is 0.4805.

Values of the ratio of Cp to specific heat at constant volume:

Pressure p, pounds per square inch.. 1.885 1.882 1.880 1.824 1.816 Ratio Cp + Cv = k =

Zeuner takes k as a constant = 1.833.

SPECIFIC HEAT AT CONSTANT VOLUME, SUPERHEATED STEAM.

Pressure, pounds per square inch.... 100 200 .346 .344 .841

It is quite as reasonable to assume that C_v is a constant as to suppose that C_p is constant, as has been assumed. If we take C_v to be constant, then C_p will appear as a variable.

If p = pressure in lbs. per sq. ft., v = volume in cubic feet, and T =temperature in degrees Fahrenheit + 460.7, then $pv = 93.5T - 971p^{\frac{1}{4}}$.

Total heat of superheated steam, $H = 0.4805(T - 10.38p^{\frac{1}{4}}) + 857.2$.

The Bationalization of Regnault's Experiments on Steam. (J. McFarlane Gray, Proc. Inst. M. E., July, 1889.)—The formule constructed by Begnault are strictly empirical, and were based entirely on his experiments. They are therefore not valid beyond the range of temperatures and pressures observed.

Mr. Gray has made a most elaborate calculation, based not on experiments but on fundamental principles of thermodynamics, from which he deduces formulæ for the pressure and total heat of steam, and presents tables cell662

lated therefrom which show substantial agreement with Regnault's figures. He gives the following examples of steam-pressures calculated for tempertures beyond the range of Regnault's experiments.

Tempe	rature.	Pounds per	Temp	erature.	Pounds per	
C.	Fahr.	sq. in.	C.	Fahr	sq. in.	
230 240 250 260 280 300 320	446 464 482 500 536 572 608	406.9 488.9 579.9 691.6 940.0 1261.8 1661.9	340 360 380 400 415 427	644 680 716 752 779 800.6	2156.2 2742.5 3448.1 4300.2 5017.1 5659.9	

These pressures are higher than those obtained by Regnault's formula.

which gives for 415° C, only 4067.1 lbs. per square inch.

Table of the Properties of Saturated Steam.—In the table of properties of saturated steam on the following pages the figures for temof properties of saturated steam on the following pages the figures for temperature, total heat, and latent heat are taken, up to 210 lbs, absolute pressure, from the tables in Porter's Steam-engine Indicator, which tables have been widely accepted as standard by American engineers. The figures for total heat, given in the original as from 0°F., have been changed to heat above 32°F. The figures for weight per cubic foot and for cubic feet per pound have been taken from Dwelshauvers-Dery's table, Trans. A.S. M. E., vol. xi, as being probably more accurate than those of Porter. The figures for relative volume are from Buel's table, in Dubois's translation of Weisbach, vol. ii. They agree quite closely with the relative volumes calculated from weights as given by Dwelshauvers. From 211 to 219 lbs. the figures for temperature, total heat, and latent heat are from Dwelshauvers table; and from 220 to 1000 lbs. all the figures are from Buel's table. The figures have not been carried out to as many decimal places as they are in most of the have not been carried out to as many decimal places as they are in most of the tables given by the different authorities; but any figure beyond the fourth significant figure is unnecessary in practice, and beyond the limit of error of the observations and of the formulæ from which the figures were derived.

Weight of 1 Cubic Foot of Steam in Decimals of a Pound. Comparison of Different Authorities.

olute Bure, or eq. in	W	eight acco	of 1 cording		ot	Absolute Pressure, s. per sq. in.	w	eight o	of 1 cu		ot
Absolut Pressur lbs. per R	Porter. Clark Buel. Dery. Per bod					Absol Press lbs. per	Por- ter.	Clark	Buel.	Dery.	Pea- body
1 14.7 20 40 60 80 100	.0030 .08797 .0511 .0994 .1457 .19015		.00303 .08793 .0507 .0972 .1424 .1866 .2803		.00299 .0376 .0502 .0964 .1409 .1843	120 140 160 180 200 220 240	.27428 .31386 .35209 .38895 .42496	.2738 .3162 .3590 .4009 .4431 .4842 .5248	.2735 .8168 .8589 .4012 .4433 .4852	.8147 .8567 .3988 .4400	.3113 .3530 .3945

There are considerable differences between the figures of weight and volume of steam as given by different authorities. Porter's figures are based on the experiments of Fairbairn and Tate. The figures given by the other authorities are derived from theoretical formulæ which are believed to give more reliable results than the experiments. The figures for temperature, total heat, and latent heat as given by different authorities show a practical agreement, all being derived from Regnault's experiments. See Peabody's Tables of Saturated Steam; also Jacobus, Trans, A. S. M. E., vol. xii., 593.

STRAM.

Properties of Saturated Steam.

, 100 M	h de la la la la la la la la la la la la la	يبو		Heat 32° F.	t. L.	lume ater	Cu. ft. Steam.	5 .6
Vacuum Gauge, Inches of Mee	Absolute Pressure, lbs. per square inch.	Temperature Fahrenheit.	In the Water h Heat- units.	In the Steam H Heat-units.	Latent Heat $I = H - h$. Heat-units.	Relative Volume Vol. of Water at 39° F. = 1.	Volume. Cr	Weight of 1 ft. Steam,
29. 29. 29. 29.	67 .125 56 .170	2 40 5 50	0 8. 18. 28.01	1091.7 1094.1 1097.2 1100.2	1091.7 1086.1 1079.2 1072.2	208080 154330 107630 76870	8333.8 2472.2 1724.1 1223.4	.00030 .00040 .00058 .00082
29. 28. 28. 28.	90 l .50:	2 80 2 90	38.02 48.04 58.06 68.08	1103.3 1106.3 1109.4 1112.4	1065.8 1058.8 1051.8 1044.4	54660 89690 29290 21830	875.61 635.80 469.20 849.70	.00115 .00158 .00218 .00286
27.8 25.8 23.8 21.7	5 2 3 8	102.1 126.8 141.6 153.1	70.09 94.44 109.9 121.4	1118.1 1120.5 1125.1 1128.6	1043.0 1026.0 1015.8 1007.2	20628 10730 7325 5588	834.23 173.23 117.98 89.80	.00299 .00577 .00848 .01112
19.74	5 1 8	162.8	130.7	1131.4	1000.7	4580	72.50	.01878
17.70		170.1	138.6	1133.8	995.3	3816	61.10	.01631
15.63		176.9	145.4	1135.9	990.5	3302	53.00	.01887
13.68		182.9	151.5	1137.7	986.2	2912	46.60	.02140
11.60		188.8	156.9	1139.4	982.4	2607	41.82	.02891
9.56	11 12	198.2	161.9	1140.9	979.0	2861	87.80	.02641
7.52		197.8	166.5	1142.8	975.8	2159	84.61	.02889
5.49		202.0	170.7	1143.5	972.8	1990	81.90	.03136
8.45		205.9	174.7	1144.7	970.0	1846	29.58	.03381
1.41		209.6	178.4	1145.9	967.4	1721	27.59	.03625
Gauge Pressur lbs. per sq. in.	e 14.7	213	180.9	1146.6	965.7	1646	26.36	.03794
0.804	15	218.0	181.9	1146.9	965.0	1614	25.87	.03868
1.3	16	216.8	185.8	1147.9	962.7	1519	24.33	.04110
2.3	17	219.4	188.4	1148.9	960.5	1484	22.98	.04352
8.3	18	229.4	191.4	1149.8	958.3	1359	21.78	.04592
4.3	19	225.2	194.8	1150.6	956.8	1292	20.70	.04831
5.3	20	227.9	197.0	1151.5	954.4	1281	19.72	.05070
6.3	21	280.5	199.7	1152.2	952.6	1176	18.84	.05308
7.3	22	238.0	202.2	1153.0	950.8	1126	18.08	.05545
8.3	23	285.4	204.7	.7	949.1	1080	17.30	.05782
9.3	24	287.8	207.0	1154.5	947.4	1088	16.62	.06018
10.3	25	240.0	209.3	1155.1	945.8	998.4	15.99	.06253
11.3	26	242.2	211.5	.8	944.3	962.8	15.42	.06487
12.3	27	244.3	213.7	1156.4	942.6	928.8	14.88	.06721
13.3	28	246.3	215.7	1157.1	941.3	897.6	14.38	.06955
14.3	29	248.3	217.8	.7	939.9	868.5	18.91	.07188
15.3	80	250.2	219.7	1158.3	938.9	841.8	13,48	.07420
6.3	81	252.1	221.6	.8	937.2	815.8	13,07	.07652
7.3	82	254.0	223.5	1159.4	935.9	791.8	12,68	.07884
8.3	83	255.7	225.3	.9	984.6	769.2	12,32	.08115
9.8	84	257.5	227.1	1160.5	988.4	748.0	11,98	.08346
).8	85	259.2	228.8	1161.0	932,2	727.9	11.66	.08576
.8	86	260.8	230.5	1161.5	931.0	708.8	11.86	.0880*
.8	87	262.5	232.1	1162.0	929.8	6 90.8	11.07	.08*

Properties of Saturated Steam,

Gauge Pressure, Ibs. per sq. in.	Absolute Pressure, lbs. per square inch.	Temperature Fahrenhett.	In the Water h Heat-units.	In the Steam H Heat-units.	Latent Heat L. $= H - h$. Heat-units.	Relative Volume. Vol. of Water at 89° F. = 1.	Volume. Cu. ft. in 1 lb. of Steam	Weight of 1 cu. ft. Steam, lb.					
98.8	38	264.0	288.8	1162.5	928.7	673.7	10.79	.09264					
94.8	80	265.6	285.4	.9	927.6	657.5	10.53	.09498					
25.3	40	267.1	236.9	1163.4	926.5	642.0	10.28	.09721					
26.3	41	268.6	238.5	.9	925.4	627.8	10.05	.09949					
27.3	42	270.1	240.0	1164.8	924.4	618.8	9.88	.1018					
28.3	48	271.5	241.4	.7	923.8	599.9	9.61	.1040					
29.3	44	272.9	242.9	1165.2	922.8	587.0	9.41	.1068					
80.8	45	274.8	244.8	.6	921.8	574.7	9.21	.1086					
81.8	46	275.7	245.7	1166.0	920.4	568 0	9.02	.1108					
82.8	47	277.0	247.0	.4	919.4	551.7	8.84	.1131					
88.3	48	278.8	248.4	.8	918.5	540.9	8.67	.1153					
84.3	49	279.6	249.7	1167.2	917.5	530.5	8.50	.1176					
\$5.3 86.3 87.8 88.3 89.3	50 51 52 58 54	280.9 282.1 283.8 284.5 285.7	251.0 252.2 253.5 254.7 256.0	1168.0 .4 .7 1169.1	916.6 915.7 914.9 914.0 918.1	520.5 510.9 501.7 492.8 484.2	8.34 8.19 8.04 7.90 7.76	.1198 .1221 .1243 .1256 .1288					
40.8	55	286.9	257.2	.4	912.8	475.9	7.63	.1811					
41.3	56	288.1	258.3	.8	911.5	467.9	7.50	.1833					
49.8	57	289.1	259.5	1170.1	910.6	460.2	7.88	.1855					
48.8	58	290.8	260.7	.5	909.8	452.7	7.26	.1877					
44.8	59	291.4	261.8	.8	909.0	445.5	7.14	.1400					
45.3	60	292.5	262.9	1171.9	908.2	438.5	7.08	.1422					
46.8	61	298.6	264.0	.5	907.5	431.7	6.92	.1444					
47.3	62	294.7	265.1	.8	906.7	425.2	6.82	.1465					
48.3	68	295.7	266.2	1172.1	905.9	418.8	6.72	.1488					
49.8	64	296.8	267.2	.4	905.2	412.6	6.62	.1511					
50,8	65	297.8	268.8	.8	904.5	406.6	6.58	.1533					
51,8	66	298.8	269.3	1178.1	903.7	400.8	6.43	.1555					
52,8	67	299.8	270.4	.4	903.0	895.2	6.84	.1577					
58,8	68	300.8	271.4	.7	902.3	889.8	6.25	.1599					
54,8	69	801.8	272.4	1174.0	901.6	884.5	6.17	.1621					
55.8 56.3 57.3 58.3 59.8	70 71 72 78 74	802.7 803.7 804.6 805.6 806.5	278.4 274.4 275.3 276.8 277.2	.8 .8 1175.1 .4	900.9 900.2 899.5 898.9 898.2	879.8 874.8 869.4 864.6 860.0	6.09 6.01 5.93 5.85 5.78	.1648 .1665 .1687 .1709 .1781					
60.3 61.3 62.3 63.8 64.3	75 76 77 78 79	807.4 808.8 809.2 810.1 810.9	278.2 279.1 280.0 280.9 281.8	1176.0 .2 .5 .8	897.5 896.9 896.2 895.6 895.0	855.5 951.1 846.8 342.6 888.5	5.71 5.68 5.57 5.50 5.43	.1753 .1775 .1797 .1819 .1840					
65.3	80	811.8	282.7	1177.0	894.8	\$34.5	5.87	.1869					
66.8	81	812.7	283.6	.3	893.7	\$80.6	5.81	.1884					
67.8	89	813.5	284.5	.6	893.1	\$26.8	5.95	.1906					
68.8	88	814.4	285.3	.8	892.5	\$23.1	5.18	.1928					
69.8	84	815.2	286.2	1178.1	891.9	\$19.5	5.18	.1950					
70.8	85	816.0	287.0	.8	891.3	815.9	5.07	.1971					

STEAM.

Properties of Saturated Steam.

	Properties of Saturated Steam.											
	Gauge Pressure, lbs. per sq. in.	Absolute Press- ure, lbs per square inch.	Temperature Fahrenheit.	In the Water h Heat-units.	Heat 32° F. In the Steam H Heat- units.	Latent Heat L = $H - h$. Heat units.	Belative Volume. Vol. of Water at 39° F. = 1.	Volume. Cu. ft. in 1 lb. of Steam	Weight of 1 cu. ft. Steam, lb.			
,	71.8	86	816.8	287.9	1178.6	890.7	812.5	5.08	.1998			
	72.8	87	817.7	288.7	.8	890.1	309.1	4.96	.2015			
	78.8	88	818.5	289.5	1179.1	889.5	805.8	4.91	.2036			
	74.8	89	819.8	290.4	.8	888.9	802,5	4.86	.2058			
	75.8	90	320.0	291.2	.6	888.4	299.4	4.81	.2080			
	76.3	91	320.8	292.0	.8	887.8	296.8	4.76	.2102			
	77.8	92	321.6	292.8	1180.0	887.2	293.2	4.71	.2123			
	78.3	98	322.4	293.6	.3	886.7	290.2	4.66	.2145			
	79.8	94	323.1	294.4	.5	896.1	287.3	4.68	.2166			
-	80.3	95	823.9	295.1	.7	885.6	284.5	4.57	.2188			
	81.3	96	824.6	295.9	1181.0	885.0	281.7	4.58	.2210			
	82.3	97	825.4	296.7	.2	884.5	279.0	4.48	.2281			
	83.3	98	826.1	297.4	.4	884.0	276.3	4.44	.2258			
	84.8	99	826.8	298.2	.6	883.4	278.7	4.40	.2874			
	85.3	100	827.6	298.9	.8	882.9	271.1	4.86	.2296			
	86.3	101	828.8	299 7	1182.1	882.4	268.5	4.82	.2317			
	87.8	102	829.0	300.4	.8	881.9	266.0	4.28	.2389			
	88.3	108	829.7	801.1	.5	881.4	268.6	4.24	.2360			
	89.3	104	830.4	801.9	.7	880.8	261.2	4.20	.2382			
	90.8	105	831.1	302.6	.9	880.3	258.9	4.16	.2408			
	91.3	106	831.8	308.3	1188.1	879.8	256.6	4.12	.2425			
	92.3	107	832.5	304.0	.4	879.3	254.8	4.09	.2446			
	93.3	108	833.2	304.7	.6	878.8	252.1	4.05	.2467			
	94.8	109	883.9	805.4	.8	878.3	249.9	4.02	.2489			
	95.8	110	884.5	306.1	1184.0	877.9	247.8	8.98	.9510			
	96.8	111	835.2	306.8	.2	877.4	245.7	8.95	.2581			
	97.8	112	385.9	307.5	.4	876.9	243.6	3.92	.2583			
	98.8	118	836.5	308.2	.6	876.4	241.6	8.88	.2574			
	99.3	114	887.2	308.8	.8	875.9	289.6	8.85	.2596			
	100.8	115	837.8	809.5	1185.0	875.5	287.6	8.82	.2617			
	101.8	116	838.5	810.2	.2	875.0	285.7	8.79	.2638			
	102.8	117	339.1	810.8	.4	874.5	283.8	8.76	.2660			
	103.8	118	839.7	811.5	.6	874.1	231.9	8.78	.2681			
	104.8	119	840.4	812.1	.8	873.6	230.1	8.70	.2708			
	105.8	120	841.0	812.8	.9	873.2	228.8	8.67	.2724			
	106.8	121	841.6	813.4	1186.1	872.7	226.5	8.64	.2745			
	107.8	123	842.2	814.1	.8	872.3	224.7	8.68	.2766			
	108.8	123	842.9	814.7	.5	871.8	223.0	8.59	.2788			
	109.8	124	843.5	815.8	.7	871.4	221.8	8.56	.2809			
	110.8 111.8 112.8 118.8 118.8	125 126 127 128 129	844.1 844.7 845.3 845.9 846.5	816.0 816.6 817.2 817.8 818.4	1187.1 .8 .4 .6	870.9 870.5 870.0 869.6 869.2	219.6 218.0 216.4 214.8 213.2	8.58 8.51 8.49 8.46 8.43	.2880 .2851 .2872 .2894 .2915			
_	115.8 116.8 117.8 118.8 119.8	180 181 182 188 184	847.1 847.6 848.2 848.8 849.4	819.1. 819.7 820.8 820.8 821.5	1188.0 .2 .3 .5	868.7 868.3 867.9 867.5 867.0	211.6 210.1 208.6 207.1 205.7	8.41 8.38 8.36 8.83 8.81	.2936 .2957 .2978 .8000 .8091			

Properties of Saturated Steam.

Froperates of Saturated Steams											
Gauge Pressure, lbs. per sq. in.	Absolute Pressure, lbs. per square inch.	5 tj	Total above	Heat 82° F.	atent Heat L. = H - h. Heat units.	Relative Volume. Vol. of water at 89° F. = 1.	Cu. ft. Steam.	Weight of 1 cu. ft. Steam, lb.			
fauge Press lbs. per sq.	bsolute P ure, lbs. square in	검축	In the	In the	2 4 E	> 8 -		~ £			
A b	걸으로	25	Water	Steam		25.11	90	# 5			
80,7	25 5	हुन्द्व	,h	H	8 T 8	T. B.	52	7.00			
.	A b c	Temperature Fahrenheit,	Heat- units.	Heat- units.	Latent Heat $= H - h$. Heat-units	26,08	Volume. In 1 lb. of	₽₽			
120.8 121.3	135 136 187 188 189	850.0 850.5	322.1 822.6	1188.7	866.6 866.2	204.2 202.8	8.29 8.27	.3042 .8063			
122.8	187	851.1	822.6 823.2	11189.0	866.2 865.8 865.4	2014	8.24	.8084 .8105			
121.3 122.8 123.8 124.8	189 189	351.8 852.2	823.8 824.4	.2	865.4 865.0	200.0 198.7	8.24 8.22 8.20	.8105 .8126			
125.8 126.8	140 141	852.8 853.8	825.0	.5 .7	864.6 864.2	197.8 196.0	8.18 3.16	.8147 .8169			
127.8	148	853.9	825.5 826.1	.9	868.8	194.7	8.14	.8190			
127.8 128.8 129.8	148 144	854.4 855.0	326.7 327.2	1190.0	863.4 863.0	193.4 192.2	8.14 8.11 8.09	.3211 .3232			
130.8 131.8 182.3 183.8	145	855.5 856.0	327.8 328.4	.4 .5 .7	862.6 862.2	190.9 189.7	8.07 8.05	.8258 .8274			
182.8	146 147	856.6	828.9	.7	861.8	188.5	8.04	.8295			
183.8	148 149	857.1	329.5	9	861.4	187.3	8.04 8.09	.8316			
184.8	(857.6	830.0	1191.0	861.0	186.1	8.00	.8387			
185.8 186.8 187.8	150 151	358.2 358.7	830.6 831.1	9.35.5.7.8.	860.6 860 2	184.9 183.7	2.98 2.96	.3358 .3379			
187 8	152	859.2	3 31.6	.5	859.9	182.6 181.5	2.94	.3400			
188.8 189.8	158 154	859.7 860.2	332.2 332.7	.7	859.5 859.1	181.5 180.4	2.92 2.91	.8421 .8449			
								1			
140.8 141.8	155 158	360.7 361.8	383.2 883.8	1192.0	858.7 858.4 858.0 857.6	179.2 178.1	2.89 2.87	.8468 .3483			
142.8	157	861.8	884.8	.81	858.0	177.0	2.85	.8504			
142.8 148.8 144.8	155 156 157 158 159	362.8	834.8	.4 .6	857.6	177.0 176.0	9 84	.8525			
		362.8	885.8		857.2	174.9	2.82	.3546			
145.8	160 161	363.3 363.8	335.9 886.4	.7 .9	856.9 856.5	178.9 172.9 171.9 171.0 170.0	9.80 9.79	.3567 .3588			
147.8	162 163	364.8	336.9	I 119 3.0 I	856.1 855.8	171.9	9.77	.3609			
146.8 147.8 148.8 149.8	163	3 64.8	837.4	.2 .8	855.8	171.0	2.76 2.74	.8630			
	164	865.8	837.9		855.4			.3650			
150.8 151.8 152.8 158.8	165 166 167 168 169	865.7 866.2	838.4 838.0	.5 .6	855.1 854.7 854.4	169.0 168.1 167.1	2.72 2.71	.3671 .3692			
152.8	167	866.7	838.9 839.4	.8	854.4	167.1	2.69	.3718			
153.8	168	867.2	889.9	.9	854.0	1 166.2	2.68 2.66	.8784			
104.8		867.7	840.4	1194.1	858.6	165.8		.8754			
155.8 156.3 157.8	170 171 172 178	868.2 868.6	840.9 841.4	.2	853.8 852.9	164.8 163.4	8.65 8.68	.8775 .8796			
157.8	172	369.1	841.9	.5	RED. R	162.5	2.62	.8817			
158 8 159.8	178	869.6	842.4	.4 .5 .7 .8	852.3 851.9	161.6	2.61	.2828			
	174	870.0	842.9			160.7	2.59	.8858			
160 8 161 .8	175 176 177 178 179	870.5 871.0	843.4 843.9	.9 1195.1	851.6 851.2 850.9	159.8 158.9	2.58 2.56	.8879 .8900 .8921			
162.8	177	871.4	844.3	2180.1	850.9	158.1	2.55	.8921			
162.8 163.8	178	871.9	844.8	.4	850.5	158.1 157.2	2.54 2.52	.8942			
164.8		872.4	845.8	.5	850.9	156.4		.8962			
165.8 166.8	180 181	872.8 873.3	345.8 846.3	.7 .8	849.9 849.5	155.6 154.8	2.51 2.50	.8983 .4004			
166.8 167.8 168.8	182 188	878.7	346.7	.9	849.2	154.0 158.9	2.48	.4025			
168.8	188	874.2	817.2	1196.1	848.9	158.9	2.47	.4048			

STEAM.

Properties of Saturated Steam.

ure,	ess-	ر و	Total above	Heat 82° F.	7 T.	Water at = 1.	of Steam	cu.
Gauge Pressure, ibs. per sq. in.	Absolute Pressure, ibs. per square inch.	Temperature Fahrenheit,	In the Water	In the	Latent Heat $I = H - h$. Heat-units.	'e Vol f wat = 1.	e. Cr	Weight of 1 cu. ft. Steam, lb.
suge	solu re, quar	ahre	h Heat-	Steam H Heat-	tent = H Heat	Relative Vol. of v 39° F.=	Volume. in 1 lb. o	eight E. Ste
			units.	units.	1			
169.8	184	874.6	847.7	1196.2	848.5	152.4	2.46	.4066
170.3 171.8	185 186 187 188 189	875.1 375.5	348.1 348.6	.8 .5	848.2 847.9	151.6 150.8	2.45 2.43	.4087 .4108 .4129 .4150
171.8 172.8 173.8 174.8	187 188	375.9 876.4	349.1 849.5	.6 .7 .9	847.6 847.2	150.0 149.2	2.42 2.41	.4129 .4150
174.8	189	876.9	850.0		846.9	148.5	2.40	.4170
175.8	190	877.8	350.4 350.9	1197.0	846.6 846.3	147.8 147.0	2.39 2.37	.4191 .4212
177.8	192	377.7 378.2	351.3	.1	845.9	146.3	2.36	.4233
176.8 177.8 178.8 179.8	191 192 193 194	378.6 379.0	851.8 852.2	.4 .5	845.6 845.3	145.6 144.9	2.85 2.34	.4254 .4275
180.8 181.8	195	879.5 880.0	352.7 353.1	.7 .8	845.0 844.7	144.2 148.5	2.88 2.82	.4296 .4317
182.8	196 197	880.3	353.6	.9	844.4	142.8	2.81	4337
183.8 184.8	198 199	380.7 381.2	354.0 354.4	1198.1 .2	844.1 843.7	142.1 141.4	2.29 2.28	.4358 .4379
185.3	200 201	381.6	854.9	.3 .4	843.4	140.8	2.27 2.26	.4400
186.3 187.3	201 202 203	382.0 382.4	855.8 855.8	.6	843.1 842.8	140.1 139.5	2.25	.4420 .4441
88.3 89.3	203 204	382.8 3 83.2	356.2 356.6	.6 .7 .8	842.5 842.2	138.8 138.1	2.25 2.24 2.23	.4462 .4482
90.8	205	383.7	857.1	1199.0	841.9 841.6	187.5 186.9	2.22 2.21 2.20 2.19	.4508
91.3 92.8 93.8	200	384.1 384.5	357.5 357.9 358.3	.2	841.3	136.3	2.20	.4523 .4544
93.8 94.3	205 206 207 208 209	384.9 385.3	358.3 358.8	.1 .2 .3 .5	841 0 840.7	185.7 185.1	2.19 2.18	.4564 .4585
95.8 96.3 97.8	210 211	385.7 386.1	359.2 359.6	.6 .7	840.4 840.1	184 5 133.9	2.17 2.16 2.15	.4605
97.8	212	886.5	360.0	.8	839 8	133.3	2.15	.4626 .4646
98.3 99.8	213 214	886.9 887.3	360.4 360.9	.9 1200.1	839.5 839.2	132.7 132.1	2.14 2.13	.4667 .4687
00.8	215 216	887.7 388 1	361.3 361.7	.2 .3	838.9 838.6	181.5 130.9	2.12 2.12	.4707 .4728
01.3 02.3	217	388.5	362.1	.4	838.3	180.3	2.11	.4748
03.3 04.3	218 219	388.9 889.3	362.5 362.9	.6 .7	838.1 837.8	129.7 129.2	2.10 2.09	.4768 .4788
05.8 15.8	220 230	389.7 393.6	862.2* 866.2	1200.8 1202.0	838.6* 835.8	128.7 123.3 118.5	2.06 1.98	.4852 .5061
25.3	240	397.8	370 0	1203.1	833.1	118.5	1.90	.5270
35.8	250	400.9	878.8	1204.2	830.5	114.0	1.83	.5478
45.8 55.8	260 270	404.4 407.8	377.4 380.9	1205.3 1206.8	827.9 825.4	109.8 105.9	1.76 1.70	.5686 .5894
45.3 55.8 65.8 75.3	280 290	411.0 414.2	384.3 387.7	1206.8 1207.3 1208.3	825.4 823.0 820.6	102.3 99.0	1.64 1.585	.6101 .6308
35.8 35.3	300 350	417.4 432.0	390.9 406.3	1209.2 1213.7	818.3 807.5	95.8 82.7	1.535 1.325	.6515 .7545

The discrepancies at 205.3 lbs, gauge are due to the change freelshauvers-Dery's to Buel's figures.

Properties of Saturated Steam.

Pressure, r sq. fn.	Press. per nch.	ن. ع	Total above	82° F. Å		Volume.	1. ft.	
Gauge Pres. lbs per sq.	Absolute Press- ure, lbs. per square inch.	Temperature Fahrenheit.	In the Water h Heat- units.	In the Steam H Heat-units.	Latent Heat $= H - h$. Heat-unita.	Relative Vo Vol. of wate 89° F. = 1.	Volume. Cu. of Steam in 1	Weight of 1 ft. Steam, 1
385.3	400	444.9	419.8	1217.7	797.9	72.8	1.167	.8572
485.3	450	456.6	482.2	1221.8	789.1	65.1	1.042	.9595
485.3	500	467.4	443.5	1224.5	781.0	58.8	.942	1.062
585.8	550	477.5	454.1	1227.6	773.5	58.6	.859	1.164
5 85.8	600	486.9	464.2	1230.5	766.8	49.8	.790	1.266
635.3	650	495.7	478.6	1233.2	759.6	45.6	.781	1.368
685.8	700	504.1	482.4	1285.7	753.3	42.4	.680	1.470
785.3	750	512.1	490.9	1238.0	747.2	89.6	.636	1.572
785.8	800	519.6	498.9	1240.8	741.4	87.1	.597	1.674
885.3	850	526.8	506.7	1242.5	785.8	84.9	.568	1.776
885.8	900	533.7	514.0	1244.7	780.6	88.0	.588	1.878
985.8	950	540.3	521.3	1246.7	725.4	81.4	.505	1.980
985.8	1000	546.8	528.3	1248.7	720.3	80.0	.480	2.062

FLOW OF STEAM.

Flow of Steam through a Nozzle. (From Clark on the Steamengine.)—The flow of steam of a greater pressure into an atmosphere of a
less pressure increases as the difference of pressure is increased, until the
external pressure becomes only 58% of the absolute pressure, until the
oblier. The flow of steam is neither increased nor diminished by the fall of the external pressure below 58%, or about 4/7ths of the inside pressure, even to the
extent of a perfect vacuum. In flowing through a nozzle of the best form,
the steam expands to the external pressure, and to the volume due to this
pressure, so long as it is not less than 58% of the internal pressure. For an
external pressure of 58%, and for lower percentages, the ratio of expansion
is 1 to 1.624. The following table is selected from Mr. Brownlee's data exempilifying the rates of discharge under a constant internal pressure. into plifying the rates of discharge under a constant internal pressure, into various external pressures:

Outflow of Steam; from a Given Initial Pressure into Various Lower Pressures.

Absolute initial pressure in boiler, 75 lbs. per sq. in.

Absolute Pressure in Boiler per square inch.	External Pressure per square inch.	Ratio of Expansion in Nozzle.	Velocity of Outflow at Constant Density.	Actual Velocity of Outflow Expanded.	Discharge per square inch of Orifice per minute.
lbs. 75 75 75 75 75 75 76 76	lbs, 74 72 70 65 61.62 60 50	ratio, 1.012 1.037 1.063 1.136 1.198 1.219 1.434 1.575	feet per sec. 227.5 886.7 490 660 786 765 878 890	feet p. sec. 280 401 581 749 876 983 1252 1401	10s. 16.68 28.85 85.98 48.38 58.97 56.12 64 65.24
75 75 75	43.46 58 p. cent }	1.624 1.624 1.624	890.6 890.6 890.6	1446.5 1446.5 1446.5	65.8 65.8 65.8

When steam of varying initial pressures is discharged into the atmosphere—the atmospheric pressure being not more than 58% of the initial ressure—the velocity of outflow at constant density, that is, supposing the litial density to be maintained, is given by the formula $V=3.5953\,\sqrt{h}$.

- = the velocity of outflow in feet per second, as for steam of the initial density;
- = the height in feet of a column of steam of the given absolute initial pressure of uniform density, the weight of which is equal to the pressure on the unit of base.

The lowest initial pressure to which the formula applies, when the steam discharged into the atmosphere at 14.7 lbs. per square inch, is $(14.7 \times 0.58 =) 28.87$ lbs. per square inch. Examples of the application of the rmula are given in the table below.

From the contents of this table it appears that the velocity of outflow into e atmosphere, of steam above 25 lbs. per square inch absolute pressure, 10 lbs. effective, increases very slowly with the pressure, obviously be use the density, and the weight to be moved, increase with the pressure. In average of 900 feet per second may, for approximate calculations, be ken for the velocity of outflow as for constant density, that is, taking the slume of the steam at the initial volume.

Outflow of Steam into the Atmosphere.—External pressure r square inch 14.7 ibs. absolute. Ratio of expansion in nozzle, 1.624.

Pressure per square fach.	Velocity of Out- flow as at Con- stant Density.	Actual Velocity of Outflow Expanded.	Discharge per square inch of Orffice per min	Horse-power per sq. in. of Orifice if H. P. = 30 lbs. per hour.	Absolute Initial Pressure per square inch.	Velocity of Outflow as at Constant Density.	Actual Velocity of Outflow Expanded.	Discharge per square inch of Orifice per minute.	Horse-power per sq.in.of Orifice if H. P. = 30 lbs. per hour.
bs.	feet p.sec.	feet per sec.	lbs.	H.P.	lbs.	feet p.sec.	feet per sec.	lbs.	H.P.
5.87	868	1401	22.81	45.6	90	895	1454	77.94	155.9
10	867	1408	26.84	58.7	100	898	1459	86.34	172.7
Ó	874	1419	35.18	70.4	115	902	1466	98.76	197.5
0	880	1429	44.06		185	906	1472	115.61	231.2
Q :	885	1487	52.59	105.2	155	910	1478	182.21	264.4
0 0 5	889	1444	61.07	122.1	165	912	1481	140.46	290.9
5	891	1447	65.80	130.6	215	919	1493	181.58	253.2

Vapier's Approximate Rule.—Flow in pounds per second = abute pressure X area in square inches + 70. This rule gives results which sely correspond with those in the above table, as shown below.

rof. Peabody, in Trans. A. S. M. E., xi, 187, reports a series of experints on flow of steam through tubes 1/2 inch in diameter, and 1/4, 1/4, and 1/4 h long, with rounded entrances, in which the results agreed closely with sier's formula, the greatest difference being an excess of the experimental r the calculated result of 3.2%. An equation derived from the theory of rmodynamics is given by Prof. Peabody, but it does not agree with the erimental results as well as Napier's rule, the excess of the actual flow 19 6.6%.

low of Steam in Pipes.—A formula commonly used for velocity low of steam in pipes is the same as Downing's for the flow of water in

oth cast-iron pipes, viz., $V = 50 \sqrt{\frac{H}{L}}D$, in which V = velocity in feet

second, L = length and D = diameter of pipe in feet, H = height in of a column of steam, of the pressure of the steam at the entre

which would produce a pressure equal to the difference of pressures at the two ends of the pipe. (For derivation of the coefficient 50, see Briggs on "Warming Buildings by Steam," Proc. Inst. C. E. 1882.) If Q = quantity in cubic feet per minute, d = diameter in inches, L and H being in feet, the formula reduces to

$$Q = 4.7233 \sqrt{\frac{H}{L}} d^{5}, \quad H = .0448 \frac{Q^{9}L}{d^{5}}, \quad d = .5874 \sqrt[6]{\frac{Q^{9}L}{H}}.$$

(These formulæ are applicable to air and other gases as well as steam.) If $p_1 = \text{pressure}$ in pounds per square inch of the steam (or gas) at the entrance to the pipe, $p_2 = \text{the pressure}$ at the exit, then $144(p_1 - p_2) = \text{difference}$ in pressure per square foot. Let w = density or weight per cubic foot of steam at the pressure p_1 , then the height of column equivalent to the difference in pressures difference in pressures

$$= H = \frac{144(p_1 - p_2)}{w}, \text{ and } Q = 60 \times .7854 \times 50 D^2 \sqrt{\frac{144(p_1 - p_2)\overline{D}}{wL}}.$$

If W = weight of steam flowing in pounds per minute = Qw, and d is taken in inches, L being in feet,

$$\begin{split} W &= 56.68 \sqrt{\frac{w(p_1 - p_2)d^5}{L}}; \quad Q = 56.68 \sqrt{\frac{(p_1 - p_2)d^5}{Lw}}; \\ d &= 0.199 \sqrt[5]{\frac{W^2L}{w(p_1 - p_2)}} = 0.199 \sqrt[5]{\frac{Q^2wL}{p_1 - p_2}}. \end{split}$$

Velocity in feet per minute = $V = Q + .7854 \frac{d^2}{144} = 10392 \sqrt{\frac{(p_1 - p_2)d}{anL}}$.

For a velocity of 6000 feet per minute, $d = \frac{wL}{3(v_1 - v_2)}$; $p_1 - p_2 = \frac{wL}{3d}$.

For a velocity of 6000 feet per minute, a steam-pressure of 100 lbs. gauge, or w = .264, and a length of 100 feet, $d = \frac{8.8}{p_1 - p_2}$; $p_1 - p_2 = \frac{8.8}{d}$. That is, a pipe 1 inch diameter, 100 feet long, carrying steam of 100 lbs. gauge-pressure at 6000 feet velocity per minute, would have a loss of pressure of 8.8 lbs. per square inch, while steam travelling at the same velocity in a pipe 8.8 inches diameter would lose only 1 lb. pressure.
G. H. Babcock, in "Steam," gives the formula

$$W = 87 \sqrt{\frac{\overline{w(p_1 - p_2)d^3}}{L\left(1 + \frac{3.6}{3}\right)}}.$$

In earlier editions of "Steam" the coefficient is given as 300,—evidently an error,—and this value has been reprinted in Clark's Pocket-Book (1892 edition). It is apparently derived from one of the numerous formulæ for flow of water in pipes, the multiplier of L in the denominator being used for an expression of the increased resistance of small pipes. Putting this formula

in the form $W = c_4 \sqrt{\frac{w(p_1 - p_2)d^6}{L}}$, in which c will vary with the diameter

of the pipe, we have,

For diameter, inches.... 18 Value of c..... 79.8

instead of the constant value 56.68, given with the simpler formula.

One of the most widely accepted formulæ for flow of water is D'Arcy's, $V = c_4 \sqrt{\frac{HD}{T.4}}$, in which c has values ranging from 65 for a 1/4-inch pipe up to 111.5 for 24-inch. Using D'Arcy's coefficients, and modifying his formula to make it apply to steam, to the form

$$Q=c\sqrt{\frac{(p_1-p_2)d^6}{wL}}, \text{ or } W=c\sqrt{\frac{w(p_1-p_2)d^6}{L}},$$

we obtain.

In the absence of direct experiments these coefficients are probably as accurate as any that may be derived from formulæ for flow of water.

Loss of pressure in lbs. per sq. in. = $p_1 - p_3 = \frac{Q^2wL}{c^2d^4}$.

Loss of Pressure due to Radiation as well as Friction.— E. A. Rudiger (*Mechanics*, June 30, 1883) gives the following formulæ and tables for flow of steam in pipes. He takes into consideration the losses in pressure due both to radiation and to friction.

Loss of power, expressed in heat-units due to friction, $Hf = \frac{W^2 fl}{10p^2 d^4}$.

Loss due to radiation, Hr = 0.262rld.

In which W is the weight in lbs. of steam delivered per hour, f the coefficient of friction of the pipe, l the length of the pipe in feet, p the absolute terminal pressure, d the diameter of the pipe in inches, and r the coefficient of radiation. f is taken as from .0165 to .0175, and r varies as follows:

TABLE OF VALUES FOR 1.

Di G	Absolute Pressure.						
Pipe Covering.	40 lbs.	65 lbs.	90 lbs.	115 lbs.			
Uncovered pipe	437	555	620	684			
2-inch cement composition 2 " asbestos	146 157	178 192	193 202	209 209			
2 " asbestos	150 100	185 122	197 145	210 151			
2 " mineral wool	61	76	85	93			
2 " hair felt	48	58	66	73			

The appended table shows the loss due to friction and radiation in a steampipe where the quantity of steam to be delivered is 1000 lbs. per hour, l=1000 feet, the pipe being so protected that loss by radiation r=64, and the absolute terminal pressure being 90 lbs.:

Diameter of Pipe, inches.	Loss by Friction, <i>Hf</i> .	Loss by Radia- tion, <i>Hr</i> .	Total Loss, L.	Diam. of Pipe, inches.	Loss by Friction, <i>Hf</i> .	Loss by Radia- tion, <i>Hr</i> .	Total Loss, L.
1	197,531	16.768	214,300	31/6	876	58,688	59,064
ร ีน	64,727	20,960	85,687	4′*	193	67,072	67,265
i12	26,012	25,152	51,164	5	63	83,840	83,903
114 114 194	12,025	29,844	41,379	6	25	100,608	1:0,623
2 3	6,173	83,536	39,709	7	.12	117.876	117,388
21/4	2.023	41,920	43,943	8	l -6	184,144	134,150
8′*	813	50,804	51,117		*	,	202,100

If the pipes are carrying steam with minimum loss, then for same τ , ι , and p, the loss of pressure L for pipes of different diameters varies inversely as the diameters.

The general equation for the loss of pressure for the minimal loss from

friction and radiation is

$$L = \frac{0.0007028 \ drlp}{W}.$$

The loss of pressure for pipes of 1 inch diameter for different absolute terminal pressures when steam is flowing with minimal loss is expressed by the formula $L = Cl_A/r^2$, in which the coefficient C has the following values:

For	65	lbs.	abs.	term.	pressure		0.00089887
**	75	66	46	4	***		0.00098684
66	90	66	66	46	44		0.00099578
66	100	44	66	64	46	••••	0.00103132
66	115	44	64	46	66		0.00108051

In order to find the loss of pressure for any other diameter, divide the loss of pressure in a 1-inch pipe for the given terminal pressure by the given diameter, and the quotient will be the loss of pressure for that diameter.

The following is a general summary of the results of Mr. Rudiger's inves-

tigation:

The flow of steam in a pipe is determined in the same manner as the flow of water, the formula for the flow of steam being modified only by substituting the equivalent loss of pressure, divided by the density of the steam,

for the loss of head.

The losses in the flow of steam are two in number—the loss due to the friction of flow and that due to radiation from the sides of the pipe. The sum of these is a minimum when the equivalent of the loss due to friction of flow is equal to one fifth of the loss of heat by radiation. For w greater or less loss of pressure—i.e., for a less or greater diameter of pipe—the total loss increases very rapidly.

For delivering a given quantity of steam at a given terminal pressure, with minimal total loss, the better the non-conducting material employed,

the larger the diameter of the steam-pipe to be used.

The most economical loss of pressure for a pipe of given diameter is equal to the most economical loss of pressure in a pipe of 1 inch diameter for same conditions, divided by the diameter of the given pipe in inches.

The following table gives the capacity of pipes of different diameters, to deliver steam at different terminal pressures through a pipe one half mile long for loss of pressure of 10 bs., and a mean value of f = 0.0175. Let W

denote the number of pounds of steam delivered per hour:

Diameter of Pipe.	Abs. T	erm. Pr	essure.	Diameter of Pipe,	Abs. Term. Pressure,			
inches.	65 lbs. 80 lbs.		100 lbs.	inches.	65 lbs.	80 lbs.	100 lbs.	
1	102 179 282 415 579 1,011 1,595 2,346	118 198 312 459 641 1,121 1,768 2,599	125 219 846 508 710 1,240 1,956 2,875	434	W 4,897 5,721 9,024 13,266 18,526 24,870 32,364 41,081	W 4,879 6,389 10,000 14,701 20,528 27,556 35,860 45,507	5,890 7,018 11,063 16,265 22,711 50,498 39,675 50,349	

Hesistance to Flow by Bends, Valves, etc. (From Briggs on Warming Buildings by Steam.)—The resistance at the entrance to a tube when no special bell-mouth is given consists of two parts. The head $v^2 + 2g$ is expended in giving the velocity of flow; and the head 0 505 $\stackrel{v^0}{=}$

oming the resistance of the mouth of the tube. Hence the whole loss of ead at the entrance is 1.505 $\frac{v^3}{2g}$. This resistance is equal to the resistance

a straight tube of a length equal to about 60 times its diameter.
The loss at each sharp right-angled elbow is the same as in flowing rough a length of straight tube equal to about 40 times its diameter. For globe steam stop-valve the resistance is taken to be 11/4 times that of the ght-angled elbow.

Sizes of Steam-pipes for Stationary Engines.—Authorities the steam-engine generally agree that steam-pipes supplying engines ould be of such size that the mean velocity of steam in them does not ceed 6000 feet per minute, in order that the loss of pressure due to friction ay not be excessive. The velocity is calculated on the assumption that the linder is filled at each stroke. In very long pipes, 100 feet and upward, it well to make them larger than this rule would give, and to place a large am receiver on the pipe near the engine, especially when the engine cuts

'early in the stroke. An article in Power, May, 1898, on proper area of supply-pipes for engines es a table showing the practice of leading builders. To facilitate comrison, all the engines have been rated in horse-power at 40 pounds mean ective pressure. The table contains all the varieties of simple engines, om the side-valve to the Corliss, and it appears that there is no general ference in the sizes of pipe used in the different types. The averages selected from this table are as follows:

he factor .1875 in formula (1) is thus derived: Assume that the linear scity of steam in the pipe should not exceed 6000 feet per minute, then e area = cyl. area × piston-speed + 6000 (a). Assume that the av. mean ctive pressure is 40 lbs. per sq. in., then cyl. area × piston-speed × 40 + 00 = horse-power (b). Dividing (a) by (b) and cancelling, we have pipe + +H.P. = .1875 sq. in. If we use 8000 ft. per min. as the allowable city, then the factor .1875 becomes .1031; that is, pipe area + H.P. = 1, or pipe area × 9.7 = horse-power. This, however, gives areas of pipe liler than are used in the most recent practice. A formula which gives ilts closely agreeing with practice, as shown in the above table is

Horse-power =
$$6d^2$$
, or pipe diameter = $\sqrt{\frac{\text{H.P.}}{6}}$ = .408 $\sqrt{\text{H.P.}}$.

METERS OF CYLINDERS CORRESPONDING TO VARIOUS SIZES OF STEAM-PIPES BASED ON PISTON-SPEED OF ENGINE OF 600 FT. PER MINUTE, AND ALLOWABLE MEAN VELOCITY OF STEAM IN PIPE OF 4000, 6000, AND 8000 FT. PER MIN. (STEAM ASSUMED TO BE ADMITTED DURING FULL STROKE,)

a. of pipe, mches	2	234	3	316	4	416	5	6
4000	5.2	6.5	7.7	9.0	10.3	11.6	12.9	15.5
6000	6.3	7.9	9.5	11.1	12.6	14.2	15.8	19.
B000	7.8	9.1	10.9	12.8	14.6	16.4	18.8	21.9
e-power, approx	20	81	45	62	80	100	125	180
i, of pipe, inches	7	8	9	10	11	12	18	14
1000.	18.1	20.7	23,2	25.8	28.4	81.0	33.6	86.1
3000	22.1	25.8	28.5	31.6	34.8	87.9	41.1	44.8
3000		29.2	32.9	36.5	40.2	43.8	47.5	51.1
9-power, approx		820	406	500	606	718	845	981

mula. Area of pipe = $\frac{\text{Area of cylinder} \times \text{piston-speed}}{\text{monopoly}}$

piston-speed of 600 ft. per min. and velocity in pipe of 4000, 6000, and t. per min. area of pipe = respectively .15, .10, and .075 × area of cyl-Diam. of pipe a respectively .8878, 3162, and .2789 × diam. of cylin-Reciprocals of these figures are 2.583, 8.162, and 8 651. first line in the above table may be used for proportioning exhaust

pipes, in which a velocity not exceeding 4000 ft, per minute is advisable. The last line, approx. H.P. of engine, is based on the velocity of 6000 ft. per min. in the pipe, using the corresponding diameter of piston, and taking $H.P. = \frac{1}{2}(\overline{\text{diam. of piston in inches}})^2$

Sizes of Steam-pipes for Marine Engines. —In marine-engine practice the steam pipes are generally not as large as in stationary practice for the same sizes of cylinder. Seaton gives the following rules:

Main Steam-pipes should be of such size that the mean velocity of flow does not exceed 8000 ft. per min.

In large engines, 1000 to 2000 H.P., cutting off at less than half stroke, the steam-pipe may be designed for a mean velocity of 9000 ft., and 10,000 ft. for still larger engines.

In small engines and engines cutting later than half stroke, a velocity of less than 8000 ft. per minute is desirable.

Taking 8100 ft. per min. as the mean velocity, 8 speed of piston in feet per min., and D the diameter of the cyl.,

Diam. of main steam-pipe =
$$\sqrt{\frac{D^3S}{8100}} = \frac{D}{90} \sqrt{S_{\bullet}}$$

Stop and Throttle Valves should have a greater area of passages than the area of the main steam-pipe, on account of the friction through the circuitous passages. The shape of the passages should be designed so as to avoid abrupt changes of direction and of velocity of flow as far as possible.

Area of Steum Ports and Passages =

$$\frac{\text{Area of piston} \times \text{speed of piston in ft. per min.}}{6000} = \frac{\text{(Diam.)}^2 \times \text{speed}}{7639}$$

Opening of Port to Steam .- To avoid wire-drawing during admission the opening of Port to Steam.—To avoid wire-drawing during admission the area of opening to steam should be such that the mean velocity of flow does not exceed 10,000 ft. per min. To avoid excessive clearance the width of port should be as short as possible, the necessary area being obtained by length (measured at right angles to the line of travel of the valve). In practice this length is usually 0.6 to 0.8 of the diameter of the cylinder, but

practice this length is insularly to to to de the thickness of a mean velocity of the steam should not exceed 6000 ft. per min., and the area should be greater if the length of the exhaust-pipe is comparatively long. The area of passages from cylinders to receivers should be such that the velocity will not exceed 5000 ft. per min.

The following table is computed on the basis of a mean velocity of flow.

The following table is computed on the basis of a mean velocity of flow of 8000 ft. per min. for the main steam-pipe, 10,000 for opening to steam, and 6000 for exhaust. A =area of piston, D its diameter.

STEAM AND EXHAUST OPENINGS.

Piston- speed, ft. per min.	Diam. of Steam-pipe + D.	Area of Steam-pipe + A.	Diam. of Exhaust + D.	Area of Exhaust + A.	Opening to Steam + A.
800	0.194	0.0875	0.228	0.0500	0.08
400	0.224	0.0500	0.258	0.0667	0.04
500	0.250	0.0625	0.288	0.0888	0.05
600	0.274	0.0750	0.816	0.1000	0.06
700	0.296	0.0875	0.841	0.1167	0.07
800	0.816	0.1000	0.865	0.1333	0.08
900	0.835	0.1125	0.387	0.1500	0.09
1000	0.858	0.1250	0.400	0.1667	0.10

STEAM PIPES.

Bursting-tests of Copper Steam-pipes. (From Report of Chief Engineer Melvile, U.S. N., for 1892.)—Some tests were made at the New York Navy Yard which show the unreliability of brazed seams in coper pipes. Each pipe was 8 in, diameter inside and 8 ft. 1% in long. Both ends were closed by ribbed heads and the pipe was subjected to a hotwater pressure, the temperature being maintained constant at \$71° F. Three of the pipes were made of No. 4 sheet copper ("Stubbs" gauge) and the fourth was made of No. 8 sheet.

The following were the results, in lbs. per sq. in., of bursting-pressure:

Pipe number	1	2	8	4	4'
Actual bursting-strength	835	785	950	1225	1275
Calculated "	1336	1836	1569	1568	1568
Difference	501	551	619	848	293

The theoretical bursting-pressure of the pipes was calculated by using the figures obtained in the tests for the strength of copper sheet with a brazed oint at 850° F. Pipes 1 and 2 are considered as having been annealed.

The tests of specimens cut from the ruptured pipes show the injurious action of heat upon copper sheets; and that, while a white heat does not hange the character of the metal, a heat of only slightly greater degree auses it to lose the fibrous nature that it has acquired in rolling, and a

erious reduction in its tensile strength and ductility results.

All the brazing was done by expert workmen, and their failure to make a sipe-joint without burning the metal at some point makes it probable that, with copper of this or greater thickness, it is seldom accomplished.

viin copper of this or greater thickness, it is seldom accomplished. That it is possible to make a joint without thus injuring the metal was roven in the cases of many of the specimens, both of those cut from the ijes and those made separately, which broke with a fibrous fracture. **Bule for Thickness of Copper Steam-pipes**, (U. S. Superising Inspectors of Steam Vessels.—Multiply the working steam-pressure albs, per sq. in. allowed the boiler by the diameter of the pipe in inches, hen divide the product by the constant whole number 8000, and add .0625 to be motivate: the sum will give the thickness of material required. he quotient; the sum will give the thickness of material required.

EXAMPLE.—Let 175 lbs. = working steam pressure per sq. in, allowed the

oiler, 5 in. = diameter of the pipe; then $\frac{175 \times 5}{8000} + .0625 = .1718 + inch,$ nickness required.

Reinforcing Steam-pipes. (Eng., Aug. 11, 1893.)—In the Italian any copper pipes above 8 in. diam. are reinforced by wrapping them with close spiral of copper or Delta-metal wire. Two or three independent birals are used for safety in case one wire breaks. They are wound at a

insion of about 11/4 tons per sq. in.

Wire-wound Steam-pipes.—The system instituted by the British dmiralty of winding all steam-pipes over 8 in. in diameter with 3/16-in. ppper wire, thereby about doubling the bursting-pressure, has within reont years been adopted on many merchant steamers using high-pressure eam, says the London Engineer. The results of some of the Admiralty

eam, says the London Engineer. The results of some of the Admiralty sts showed that a wire pipe stood just about the pressure it ought to have not when unwired, had the copper not been injured in the brazing.

Eliveted Steel Steam-pipes have recently been used for high essures. See paper on A Method of Manufacture of Large Steam-pipes, 'Chas. H. Manning, Trans. A. S. M. E., vol. xv.

Valves in Steam-pipes. — Should a globe-valve on a steam-pipe have e steam-pressure on top or underneath the valve is a disputed question, ith the steam-pressure on top, the stuffing-box around the valve-stem can to be repacked without shutting off steam from the whole line of pipe; on e other hand, if the steam-pressure is on the bottom of the valve it all has be sustained by the screw-thread on the valve-stem, and there is dauger stripping the thread. stripping the thread.

A correspondent of the American Machinist, 1892, says that it is a very common thing in the ordinary globe-valve to have the thread give out, t by water-hammer and merciless screwing the seat will be crushed down ite frequently. Therefore with plants where only one boiler is used he vises placing the valve with the boiler-pressure underneath it. On plants ere several boilers are connected to one main steam-pipe he would rese the position of the valve, then when one of the valves needs repacking y valve can be closed and the pressure in the boiler whose pine it controls a be reduced to atmospheric by lifting the safety-valve. The repacking then be done without interfering with the operation of the other boilers the plant.

Ie proposes also the following other rules for locating valves: Place ves with the stems horizontal to avoid the formation of a water-pocket, ver put the junction-valve close to the boiler if the main pipe is above boiler, but put it on the highest point of the junction-pipe. If the other

plan is followed, the pipe fills with water whenever this boiler is stopped and the others are running, and breakage of the pipe may cause serious results. Never let a junction-pipe run into the bottom of the main pipe, but into the side or top. Always use an angle-valve where convenient, as there is more room in them. Never use a gate valve under high pressure unless a by-pass is used with it. Never open a blow-off valve on a boiler a little and then shut it; it is sure to catch the sediment and ruin the valve; throw it well open before closing. Never use a globe-valve on an indicator-pipe. For water, always use gate or angle valves or stop-cocks to obtain a clear passage. Buy if possible valves with renewable disks. Lastly, never let a man go inside a boiler to work, especially if he is to hammer on it, unless you break the joint between the boiler and the valve and put a plate of steel between the flanges.

A Failure of a Brazed Copper Steam-pipe on the British steamer *Prodano* was investigated by Prof. J. O. Arnold. He found that the brazing was originally sound, but that it had deteriorated by oxidation

the brazing was originally sound, but that it had deteriorated by exidation of the zinc in the brazing alloy by electrolysis, which was due to the presence of fatty acids produced by decomposition of the cil used in the engines. A full account of the investigation is given in The Engineer, April 15, 1898.

The **Steam Leop** is a system of piping by which water of condensation in steam-pipes is automatically returned to the boiler. In its simplest form it consists of three pipes, which are called the riser, the horizonial, and the drop-leg. When the steam-loop is used for returning to the boiler the water of condensation and entrainment from the steam-pipe through which the steam flows to the cylinder of an engine, the riser is generally attached to a separator; this riser empties at a suitable height into the horizonial, and from thence the water of condensation is led into the drop-leg, which is connected to the boiler, into which the water of condensation is led into the drop-leg, which is connected to the boiler, into which the water of condensation is led into the drop-leg in connection with tion is fed as soon as the hydrostatic pressure in drop-leg in connection with the steam-pressure in the pipes is sufficient to overcome the boiler-pressure. The action of the device depends on the following principles: Difference of pressure may be balanced by a water-column; vapors or liquids tend to flow to the point of lowest pressure; rate of flow depends on difference of pressure and mass; decrease of static pressure in a steam-pipe or chamber in proportional to rate of condensation; in a steam-current water will be carried or swept along rapidly by friction. (Illustrated in Modern Mechanism,

Loss from an Uncovered Steam-pipe. (Bjorling on Pumping-engines.)—The amount of loss by condensation in a steam-pipe carried down engines.)—The amount of loss by condensation in a steam-pipe carried down a deep mine-shaft has been ascertained by actual practice at the Clay Cross Colliery, near Chesterfield, where there is a pipe 7½ in. internal diam., 1100 ft. long. The loss of steam by condensation was ascertained by direct measurement of the water deposited in a receiver, and was found to be equivalent to about 1 lb. of coal per I.H.P. per hour for every 100 ft. of steam-pipe; but there is no doubt that if the pipes had been in the upcast shaft, and well covered with a good non-conducting material, the loss would have been less. (For Steam-pipe Coverings, see p. 469, ante.)

THE STEAM-BOILER.

The Horse-power of a Steam-boiler.—The term horse power tas two meanings in engineering: First, an absolute unit or measure of the ate of work, that is, of the work done in a certain definite period of time, by a source of energy, as a steam-boiler, a waterfall, a current of air or sater, or by a prime mover, as a steam-engine, a water-wheel, or a wind-nill. The value of this unit, whenever it can be expressed in foot-pounds nini. The value of this unit, whenever it can be expressed in foot-pounds of energy, as in the case of steam-engines, water-wheels, and waterfalls, is 5,000 foot-pounds per minute. In the case of boilers, where the work done, he conversion of water into steam, cannot be expressed in foot-pounds of twallable energy, the usual value given to the term horse-power is the evep-ration of 30 hs. of water of a temperature of 100° F. into steam at 70 hs. pressure above the atmosphere. Both of these units are arbitrary; the first, 3,000 foot-pounds per minute, first adopted by James Watt, being considered equivalent to the power exerted by a good London draught-horse, and the 10 hs. of water evaporated per hour being considered to be the steam re-nirement per indicated horse-power of an average engine. quirement per indicated horse-power of an average engine.

pulrement per indicated horse-power of an average engine.

The second definition of the term horse-power is an approximate measure of the size, capacity, value, or "rating" of a boiler, engine, water-wheel, or ther source or conveyer of energy, by which measure it may be described, ought and sold, advertised, etc. No definite value can be given to this neasure, which varies largely with local custom or individual opinion of nakers and users of machinery. The nearest approach to uniformity which can be arrived at in the term "horse-power," used in this sense, is to say that a boiler, engine, water-wheel, or other machine, "rated" at a certain orse-power, should be capable of steadily developing that horse-power for a long period of time under ordinary conditions of use and practice, leaving o local custom, to the judgment of the buyer and seller, to written contracts of purchase and sale, or to legal decisions upon such contracts, the interpretation of what is meant by the term "ordinary conditions of use and practice." (Trans. A. S. M. E., vol. vii. p. 226.)

The committee of the A. S. M. E. on Trials of Steam-boilers in 1884 (Trans., vol. vi. p. 235) discussed the question of the horse-power of boilers as follows:

vol. vi. p. 265) discussed the question of the horse-power of boilers as follows: The Committee of Judges of the Centennial Exhibition, to whom the trials of competing boilers at that exhibition were intrusted, met with this same problem, and finally agreed to solve it, at least so far as the work of that committee was concerned, by the adoption of the unit, 30 lbs. of water evaporated into dry steam per hour from feed-water at 100° F., and under a reessure of 70 lbs. per square inch above the atmosphere, these conditions using considered by them to represent fairly average practice. The quantity of best depended to expresse and of ferrors made these conditions is the considered by their to represent tainly average practice. The quartity of heat demanded to evaporate a pound of water under these conditions a 1110.2 British thermal units, or 1.1496 units of evaporation. The unit of lower proposed is thus equivalent to the development of 23,305 heat units or hour, or 34.488 units of evaporation. . .

Your committee, after due consideration, has determined to accept the

entennial Standard, the first above mentioned, and to recommend that in II standard trials the commercial horse-power be taken as an evaporation f 30 lbs. of water per hour from a feed-water temperature of 100° F. into team at 70 lbs. gauge pressure, which shall be considered to be equal to 34½ nits of evaporation, that is, to 34½ lbs. of water evaporated from a feed-water temperature of 212° F. into steam at the same temperature. This tendard is equal to 33,305 thermal units per hour.

It is the opinion of this committee that a boiler rated at any stated number f horse-powers should be capable of developing that power with easy firing, oderate draught, and ordinary fuel, while exhibiting good economy; and arther, that the boiler should be capable of developing at least one third tore than its rated power to meet emergencies at times when maximum

onomy is not the most important object to be attained.

Unit of Evaporation.—It is the custom to reduce results of bolistic to the common standard of weight of water evaporated by the unit sight of the combustible portion of the fuel, the evaporation being considered to have taken place at mean atmospheric pressure, and at the temperature of the combustible portion of the fuel, the evaporation being considered to have taken place at mean atmospheric pressure, and at the temperature to be a superstant of the combustible portion of the fuel of the combustible pressure, and at the temperature to be a superstant of the combustible pressure. ture due that pressure, the feed-water being also assumed to have been upriled at that temperature. This is, in technical language, said to be the nuivalent evaporation from and at the boiling point at atmospheric preserve, or "from and at 22° F." This unit of evaporation, or one pound of water evaporated from and at 212°, is equivalent to 965.7 British thermal units.

Measures for Comparing the Puty of Bollers.—The measure of the efficiency of a boiler is the number of pounds of water evaporation per pound of combustible, the evaporation being reduced to the standard of "from and at 212°;" that is, the equivalent evaporation from feed-water at a temperature of 212° F. into steam at the same temperature.

The measure of the capacity of a boiler is the amount of "boiler horse-

The measure of the capacity of a boiler is the amount of "holler horsepower" developed, a horse-power being defined as the evaporation of 30 lbs. of water per hour from 100° F, into steam at 70 lbs, pressure, or 34½ lbs. per

hour from and at 212°.

The measure of relative rapidity of steaming of boilers is the number of pounds of water evaporated per hour per square foot of water-heating surface.

The measure of relative rapidity of combustion of fuel in boiler-furnaces is the number of pounds of coal burned per hour per square foot of grate-surface.

STEAM-BOILER PROPORTIONS.

Proportions of Grate and Heating Surface required for a given Horse-power.—The term horse-power here means capacity to evaporate 30 lbs. of water from 100°F., temperature of feed-water, to steam of 70 lbs., gauge-pressure = 34.5 lbs. from and at 212°F.

Average proportions for maximum economy for land boilers fired with good anthracite coal:

Heating surface per horse-power	11.5	8Q. Í
Grate " " "		34
Ratio of heating to grate surface	84.5	66
Water evap'd from and at 212° per sq. ft. H.S. per hour		lbs.
Combustible burned per H.P. per hour	8	44
Coal with 1/6 refuse, lbs. per H.P. per hour		66
Combustible burned per sq. ft. grate per hour	9	44
Coal with 1/6 refuse, lbs. per sq. ft. grate per hour	10.8	44
Water evap'd from and at 212° per lb. combustible	11.5	66
" " " " coal (1/6 refuse)	9.6	*

The rate of evaporation is most conveniently expressed in pounds evaporated from and at 212° per sq. ft. of water-heating surface per hour, and the rate of combustion in pounds of coal per sq. ft. of grate-surface per hour.

Heating-surface.—For maximum economy with any kind of fuel a boiler should be proportioned so that at least one square foot of heating-surface should be given for every 8 lbs. of water to be evaporated from and at 212° F. per hour. Still more liberal proportions are required if a portion of the heating-surface has its efficiency reduced by: 1. Tendency of the heated gases to short-circuit, that is, to select passages of least resistance and flow through them with high velocity, to the neglect of other passages. 2. Deposition of soot from smoky fuel. 3. Incrustation. If the heating-surface are clean, and the heated gases pass over it uniformly, little if any increase in economy can be obtained by increasing the heating-surface beyond the proportion of 1 sq. ft. to every 3 lbs. of water to be evaporated, and with all conditions favorable but little decrease of economy will take place if the proportion is 1 sq. ft. to every 4 lbs. evaporated; but in order to provide for driving of the boiler beyond its rated capacity, and for possible decrease of efficiency due to the causes above named, it is better to adopt 1 sq. ft. to 3 lbs. evaporation per hour as the minimum standard proportion. Where economy may be sacrificed to capacity, as where fuel is very cheap,

Where economy may be sacrificed to capacity, as where fuel is very cheap, it is customary to proportion the heating-surface much less ilberally. The following table shows approximately the relative results that may be expected with different rates of evaporation, with anthractic coal.

Lbs. water evapor'd from and at 212° per sq. ft. heating-surface per hour: 2.5 8 10 8.5 Sq. ft. heating-surface required per horse-power: 7.3 13.8 11.5 9.8 8.6 6.8 5.8 4.8 3.8 8.5 Ratio of heating to grate surface if 1/3 sq. ft, of G. S. is required per H.P.:
41.4 84.5 29.4 25.8 20.4 17.4 13.7 12.9 11.4 10.5 Probable relative economy 100 100 95 75 70 65 60 Probable temperature of chimney gases, degrees F.: 50 450 450 518 585 652 720 787 855 990 518

The relative economy will vary not only with the amount of heating-surface per horse-power, but with the efficiency of that heating-surface as regards its capacity for transfer of heat from the heated gases to the water, which will depend on its freedom from soot and incrustation, and upon the circulation of the water and the heated gases.

With bituminous coal the efficiency will largely depend upon the thoroughness with which the combustion is effected in the furnace.

The efficiency with any kind of fuel will greatly depend upon the amount of air supplied to the furnace in excess of that required to support combustion. With strong draught and thin fires this excess may be very great,

causing a serious loss of economy.

Measurement of Heating-surface.—Authorities are not agreed as to the methods of measuring the heating-surface of steam-boilers. The usual rule is to consider as heating-surface all the surfaces that are surrounded by water on one side and by flame or heated gases on the other, but there is a difference of opinion as to whether tuoular heating-surface should be figured from the inside or from the outside diameter. Some writers say, measure the heating-surface always on the smaller side—the fire side of the tube in a horizontal return tubular boiler and the water side in a water-tube boiler. Others would deduct from the heating surface thus measured an allowance for portions supposed to be ineffective on account of being cov-

ered by dust, or being out of the direct current of the gases.

It has hitherto been the common practice of boiler-makers to consider all surfaces as heating-surfaces which transmit heat from the flame or gases to the water, making no allowance for different degrees of effectiveness; also, to use the external instead of the internal diameter of tubes, for greater convenience in calculation, the external diameter of boiler-tubes usually being made in even inches or half inches. This method, however, is inaccurate, for the true heating-surface of a tube is the side exposed to the hot gases, the inner surface in a fire-tube boiler and the outer surface in a water-tube boiler. The resistance to the passage of heat from the hot gases on one side of a tube or plate to the water on the other consists almost

gases on one side of a tube or plate to the water on the other consists almost entirely of the resistance to the passage of the heat from the gases into the metal, the resistance of the metal itself and that of the wetted surface being practically nothing. See paper by C. W. Baker, Trans. A. S. M. E., vol. xix. Rulle for finding the heating-surface of vertical tubular boilers: Multiply the circumference of the fire-box (in inches) by its height above the grate; multiply the combined circumference of all the tubes by their length, and to these two products add the area of the lower tube-sheet; from this sum subtract the area of all the tubes and divide by 144 the quotient is the subtract the area of all the tubes, and divide by 144: the quotient is the

number of square feet of heating-surface.

RULE for finding the heating-surface of horizontal tubular boilers: Take the dimensions in inches. Multiply two thirds of the circumference of the shell by its length; multiply the sum of the circumferences of all the tubes by their common length; to the sum of these products add two thirds of the area of both tube-sheets; from this sum subtract twice the combined area of

all the tubes; divide the remainder by 144 to obtain the result in square feet. RULE for finding the square feet of heating-surface in tubes: Multiply the number of tubes by the diameter of a tube in inches, by its length in feet,

and by .2618.

Horse-power, Builder's Rating. Heating-surface per Horse-power.—It is a general practice among builders to furnish about 12 square feet of heating-surface per horse-power, but as the practice is not uniform, bids and contracts should always specify the amount of heating-surface to be furnished. Not less than one third square foot of grate-surface

should be furnished per horse-power.

Engineering News, July 5, 1894, gives the following rough-and-ready rule for finding approximately the commercial horse-power of tubular or water tube boilers: Number of tubes \times their length in feet \times their nominal diameter in inches + 50 = nLd + 50. The number of square feet of surface

in the tubes is $\frac{n\pi dL}{12} = \frac{nLd}{3.82}$, and the horse-power at 12 square feet of surface

of tubes per horse-power, not counting the shell, = nLd + 45.8. If 15 square feet of surface of tubes be taken, it is nLd + 57.3. Making allowance for the heating-surface in the shell will reduce the divisor to about 50.

Horse-power of Marine and Locomotive Boilers.—The term horse-power is not generally used in connection with boilers in marine practice, or with locomotives. The boilers are designed to suit the engines, and are rated by extent of grate and heating-surface only.

Grate-surface.—The amount of grate-surface required per horse power, and the proper ratio of heating-surface to grate-surface are extermely variable, depending chiefly upon the character of the coal and upon the rate of draught. With good coal, low in ash, approximately equal results may be obtained with large grate-surface and light draught and with small grate-surface and strong draught, the total amount of coal burned per hour being the same in both cases. With good bituminous coal, like Pittsburgh, low in ash, the best results apparently are obtained with strong draught and high rates of combustion, provided the grate-surfaces are cut down so that the total coal burned per hour is not too great for the capacity of the heating-surface to absorb the heat produced.

With coals high in ash, especially if the ash is easily fusible, tending to choke the grates, large grate-surface and a slow rate of combustion are required, unless means, such as shaking grates, are provided to get rid of Grate-surface. -The amount of grate-surface required per horse

required, unless means, such as shaking grates, are provided to get rid of

the ash as fast as it is made.

The amount of grate-surface required per horse-power under various conditions may be estimated from the following table:

	Water m and 212° 115° al.	Conf. H.P. hour.	Pounds of Coal burned per square foot of Grate per hour.
		Lbs.	8 10 12 15 20 25 80 35 40
			Sq. Ft. Grate per H. P.
Good coal and boiler,	10 9	8.45 8.83	.43 .30 .28 .23 .17 .14 .11 .10 .00 .48 .38 .32 .25 .19 .15 .13 .11 .10
Fair coal or boiler,	7	4. 4.81 4.98	.50 .40 .33 .25 .20 .16 .18 .12 .10 .54 .43 .36 .29 .22 .17 .14 .18 .11 .62 .49 .41 .38 .24 .20 .17 .14 .12
Poor coal or boiler,	6.9	5. 5.75 6.9	.63 .50 .42 .84 .25 .90 .17 .15 .18 .72 .56 .46 .88 .29 .23 .19 .17 .14
Lignite and poor boiler,	l o as	10.	.86 .69 .58 .46 .85 .28 .23 .22 .17 1.25 1.00 .88 .67 .50 .40 .88 .29 .25

In designing a boiler for a given set of conditions, the grate-surface should be made as liberal as possible, say sufficient for a rate of combustion of 10 lbs. per square foot of grate for anthracite, and 15 lbs. per square foot for bituminous coal, and in practice a portion of the grate-surface may be bricked over if it is found that the draught, fuel, or other conditions render it advisable.

Proportions of Areas of Flues and other Gas-passages.

Rules are usually given making the area of gas-passages bear a certain ratio to the area of the grate-surface; thus a common rule for horizontal tubular boilers is to make the area over the bridge wall 1/7 of the grate-surface, the flue area 1/8, and the chimney area 1/8.

Exercises the flue area 1/8 and the chimney area 1/8.

For average conditions with anthracite coal and moderate draught, say a rate of combustion of 12 bs. coal per square foot of grate per hour, and a ratio of heating to grate surface of 30 to 1, this rule is as good as any, but it is evident that if the draught were increased so as to cause a rate of combustion of 24 bs., requiring the grate-surface to be cut down to a ratio of 60 to 1, the areas of gas passages should not be reduced in proportion. The amount of coal burned per hour being the same under the changed conditions, and there being no reason why the gases should travel at a higher velocity, the actual areas of the passages should remain as before, but the ratio of the area to the grate-surface would in that case be doubled.

Mr. Barrus states that the highest efficiency with anthracite coal is obtained when the tube area is 1/9 to 1/10 of the grate-surface, and with bituminous coal when it is 1/8 to 1/7, for the conditions of medium rates of combustion, such as 10 to 12 lbs. per square foot of grate per hour, and 12 square feet of heating surface allowed to the horse-power.

The tube area should be made large enough not to choke the draught, and so lesses the capacity of the boiler; if made too large the gases are apt to select the passages of least resistance and escape from them at a high velocity and high temperature.

This condition is very commonly found in horizontal tubular boilers where

the gases go chiefly through the upper rows of tubes; sometimes also in vertical tubular boilers, where the gases are apt to pass most rapidly through the tubes nearest to the centre.

Air-passages through Grate-bars.—The usual practice is, air-opening = 30% to 50% of area of the grate; the larger the better, to avoid stoppage of the air-supply by clinker; but with coal free from clinker much smaller air-space may be used without detriment. See paper by F. A. Scheffler, Trans. A. S. M. E., vol. xv. p. 503.

PERFORMANCE OF BOILERS.

The performance of a steam-boiler comprises both its capacity for generating steam and its economy of fuel. Capacity depends upon size, both of grate-surface and of heating-surface, upon the kind of coal burned, upon the draft, and also upon the economy. Economy of fuel depends upon the completeness with which the coal is burned in the furnace, on the proper regulation of the air-supply to the amount of coal burned, and upon the thoroughness with which the boiler abscris the heat generated in the furnace. The abscrption of heat depends on the extent of heating-surface in relation to the amount of coal burned or of water evaporated, upon the arrangement of the gas passages, and upon the cleanness of the surfaces. The capacity of a boiler may increase with increase of economy when this is due to more thorough combustion of the coal or to better regulation of the air-supply, or it may increase at the expense of economy when the increased capacity is due to overdriving, causing an increased loss of heat in the chimney gases. The relation of capacity to economy is therefore a complex one, depending on many variable conditions.

Many attempts have been made to construct a formula expressing the rela-

tion between capacity, rate of driving, or evaporation per square foot of heating surface, to the economy, or evaporation per pound of combustible, but none of them can be considered satisfactory, since they make the economy depend only on the rate of driving (a few so-called "constanta," however, being introduced in some of them for different classes of boilers, however, being introduced in some of them for different classes of bones, kinds of fuel, or kind of draft), and fall to take into consideration the numerous other conditions upon which economy depends. Such formulæ are Rankine's, Clark's, Emery's, Isherwood's, Carpenter's, and Hale's. A discussion of them all may be found in Mr. R. S. Hale's paper on "Efficiency of Boiler Heating Surface," in Trans. A. S. M. E., vol. xviii, p. 828. Mr. Hale's formula takes into account the effect of radiation, which reduces the economy considerably when the rate of driving is less than 8 lbs. per square

foot of heating-surface per hour. Selecting the highest results obtained at different rates of driving obtained with anthracite coal in the Centennial tests (see p. 686), and the highest results with anthracite reported by Mr. Barrus in his book on Boller Tests, the author has plotted two curves showing the maximum results which may be expected with anthracite coal, the first under exceptional conditions such as obtained in the Centennial tests, and the second under the best conditions of ordinary practice. (Trans. A. S. M. E., xviii. 354). From these curves the following figures are obtained.

Lies water exproprised from and at \$192 per so. ft. heating-surface per hour.

Lbs. water evaporated from and at 212° per sq. ft. heating-surface per hour: 1.7 2.6 8.5

Lbs. water evaporated from and at 212° per lb. combustible: Centennial. 11.8 11.9 12.0 12.1 12.05 12 11.85 11.7 11.5 10.85 Barrus... 11.4 11.5 11.55 11.6 11.6 11.5 11.5 10.9 10.6 9.9 4.vg. Cent'l 12.0 11.6 11.3 10.8 10.4 10.0 9.6 8.8 9.2 8.0

The figures in the last line are taken from a straight line drawn as nearly as possible through the average of the pletting of all the Centennial tests.

The poorest results are far below these figures. It is evident that no formula can be constructed that will express the relation of economy to rate of driving as well as do the three lines of figures given above.

For semi-bituminous and bituminous coals the relation of economy to the

rate of driving no doubt follows the same general law that it does with anthracite, i.e., that beyond a rate of evaporation of 8 or 4 lbs. per sq. ft. of heating surface per hour there is a decrease of economy, but the figures obtained in different tests will show a wider range between maximum and average results on account of the fact that it is more difficult with bituminous than with anthracite coal to secure complete combustion in the furnace.

The amount of the decrease in economy due to driving at rates exceeding 4 lbs. of water evaporated per square foot of heating-surface per hour differe greatly with different boilers, and with the same boiler it may differ with different settings and with different coal. The arrangement and size of the gas-passages seem to have an important effect upon the relation of economy to rate of driving. There is a large field for future research to determine the causes which influence this relation.

General Conditions which secure Economy of Steamboilers. - In general, the highest results are produced where the temperature of the escaping gases is the least. An examination of this question is made by Mr. G. H. Barrus in his book on "Boiler Tests," by selecting those made by Mr. 4. H. Barrus in mis book on "Boller lests," by selecting those tests made by him, six in number, in which the temperature exceeds the average, that is, 875° F., and comparing with five tests in which the temperature is less than 375° The boilers are all of the common horizontal type, and all use anthracite coal of either egg or broken size. The average flue temperatures in the two series was 444° and 348° respectively, and the difference was 101°. The average evaporations are 10.40 lbs, and 11.02 lbs. The average evaporations are 10.40 lbs, and 11.02 lbs. The average evaporation are 10.40 lbs, and 11.02 lbs. The average evaporation are 10.40 lbs. spectively, and the lowest result corresponds to the case of the highest flue temperature. In these tests it appears, therefore, that a reduction of 101° in the temperature of the waste gases secured an increase in the evaporation of 6%. This result corresponds quite closely to the effect of lowering the temperature of the gases by means of a five-heater where a reduction of 107° was attended by an increase of 7% in the evaporation per pound of coal.

A similar comparison was made on horizontal tubular boilers using Cumberland coal. The average flue temperature in four tests is 450° and the average evaporation is 11.34 lbs. Six boilers have temperatures below 415°, the average of which is 88°, and these give an average evaporation of 11.75 lbs. With 67° less temperature of the escaping gases the evaporation is

higher by about 4%.

The wasteful effect of a high flue temperature is exhibited by other boilers than those of the horizontal tubular class. This source of waste was shown to be the main cause of the low economy produced in those vertical boilers

which are deficient in heating-surface.

Relation between the Henting-surface and Grate-surface to obtain the Highest Efficiency.—A comparison of three tests of horizontal tubular boilers with anthracite coal, the ratio of heating-surface to grate-surface being 86.4 to 1, with three other tests of similar boilers, in which the ratio was 48 to 1, showed practically no difference in the results. The evidence shows that a ratio of 36 to 1 provides a sufficient quantity of heating-surface to secure the full efficiency of anthracite coal where the rate of combustion

is not more than 12 lbs. per sq. ft. of grate per hour. In tests with bituminous coal an increase in the ratio from 36.8 to 42.8 se-In tests with niuminous coal an increase in the ratio from 36.8 to 42.8 secured a small improvement in the evaporation per pound of coal, and a high temperature of the escaping gases indicated that a still further increase would be beneficial. Among the high results produced on common horizontal tubular boilers using bituminous coal, the highest occurs where the ratio is 53.1 to 1. This belier gave an evaporation of 12.47 lbs. A double-deck boiler furnishes another example of high performance, an evaporation of 12.48 lbs. laving been obtained with bituminous coal, and in this case the ratio is 65 to 1. These examples indicate that a much larger amount of heating surface is required for obtaining the full efficiency of hitunious heating surface is required for obtaining the full efficiency of bituninous coal than for boilers using anthracite coal. The temperature of the scaping gases in the same toller is invariably higher when bituminous coal is used than when anthracite coal is used. The deposit of soot on the surfaces when bituminous coal is used interferes with the full efficiency of the surface, and an increased area is demanded as an offset to the loss which this deposit occasions. It would seem, then, that if a ratio of 36 to 1 is sufficient for anthracite coal, from 45 to 50 should be provided when bituminous coal s burned, especially in cases where the rate of combustion is above 10 or 12 lbs. per sq. ft. of grate per hour.

The number of tubes controls the ratio between the area or grate-surface and area of tube opening. A certain minimum amount of tube-opening is required for efficient work.

The best results obtained with anthracite coal in the common horizontal

boiler are in cases where the ratio of area of grate-surface to area of tubeopening is larger than 9 to 1. The conclusion is drawn that the highest effi-ciency with anthracite coal is obtained when the tube-opening is from 1/9 to 1/10 of the grate surface.

75,00

8.80 21.20

When bituminous coal is burned the requirements appear to be different. The effect of a large tube opening does not seem to make the extra tubes nefficient when bituminous coal is used. The highest result on any boiler of he horizontal tubular class, fired with bituminous coal, was obtained where he tube-opening was the largest. This gave an evaporation of 12.47 lbs., the atio of grate-surface to tube-opening being 5.4 to 1. The next highest re-ult was 12.42 lbs., the ratio being 5.2 to 1. Three high results, averaging 2.01 lbs., were obtained when the average ratio was 7.1 to 1. Without going o extremes, the ratio to be desired when bituminous coal is used is that thich gives a tube-opening having an area of from 1/6 to 1/7 of the grate-urface. This applies to medium rates of combustion of, say, 10 to 12 lbs. per q. ft. of grate per hour, 12 sq. ft. of water-heating surface being allowed per orse-power.

A comparison of results obtained from different types of boilers leads to ne general conclusion that the economy with which different types of ollers operate depends much more upon their proportions and the condions under which they work, than upon their type; and, moreover, that hen these proportions are suitably carried out, and when the conditions re favorable, the various types of boilers give substantially the same eco-

omic result.

Reficiency of a Steam-boiler.—The efficiency of a boiler is the scentage of the total heat generated by the combustion of the fuel hich is utilized in heating the water and in raising steam. With anthracite al the heating-value of the combustible portion is very nearly 14,500 T. U. per lb., equal to an evaporation from and at 212 of 14,500 — 966 15 lbs. of water. A boiler which when tested with anthracite coal shows 15 lbs. of water. A boiler which when tested with anthracite coal shows i evaporation of 12 lbs. of water per lb. of combustible, has an efficiency of +15 = 80%, a figure which is approximated, but scarcely ever quite ached, in the best practice. With bituminous coal it is necessary to have letermination of its heating-power made by a coal calorimeter before the

letermination of its neating-power made by a coal calorimeter before the letency of the boiler using it can be determined, but a close estimate may made from the chemical analysis of the coal. (See Coal.) The difference between the efficiency obtained by test and 100% is the sum the numerous wastes of heat, the chief of which is the necessary loss due the temperature of the chimney-gases. If we have an analysis and a orimetric determination of the heating-power of the coal (properly samd), and an average analysis of the chimney-gases, the amounts of the eral losses may be determined with approximate accuracy by the method werliad below. cribed below.

)ata given :

1. Analysis of the Coal. himberland Semi-bituminous.	2. A					DRY CH	IMNEY-
bon 80.55				-, -	Ċ.	Ö.	N.
drogen 4.50	CO.	=	13.6	=	8,71	9.89	••••
ygen 2.70	ČÕ.	=			.09	.11	
rogen 1.08	0					11.20	
sture 2.92	N	=	75.0	=	•••		75.0 0
1							

eating-value of the coal by Dulong's formula, 14,248 heat-units. ne gases being collected over water, the moisture in them is not deter-ied.

Ash and refuse as determined by boiler-test, 10.25, or 2% more than that id by analysis, the difference representing carbon in the ashes obtained 1e boiler-test.

100.0

Temperature of external atmosphere, 60° F.

Relative humidity of air, 60%, corresponding (see air tables) to .007 lb. of or in each lb. of air.

Temperature of chimney-gases, 560° F.

lculated results:

e carbon in the chimney-gases being 3.8% of their weight, the total ht of dry gases per lb. of carbon burned is 100 + 8.8 = 26.82 lbs. Since arbon burned is 80.55 - 2 = 78.55% of the weight of the coal, the weight e dry gases per lb. of coal is $26.32 \times 78.55 + 100 = 20.67$ lbs. ch pound of coal furnishes to the dry chimney-gases .7855 lb. C, .0108N,

+ 100 = .0214 lb. O; a total of .8177, say .82 lb. This sub-

tracted from 20.67 lbs. leaves 19.85 lbs. as the quantity of dry air (not including moisture) which enters the furnace per pound of coal, not counting the ing moisture) which enters the furnace per pound of coal, not counting the air required to burn the available hydrogen, that is, the hydrogen minus one eighth of the oxygen chemically combined in the coal. Each lb. of coal burned contained .045 lb. H, which requires .045 × 8 = .36 lb. O for its combustion. Of this, .037 lb. is furnished by the coal itself, leaving .333 lb. to come from the air. The quantity of air needed to supply this oxygen (air containing 235 by weight of oxygen) is .333 + .23 = 1.45 lb., which added to the 19.85 lbs, aiready found gives 21.30 lbs, as the quantity of dry air supplied to the furnace per lb. of coal burned.

The air carried in as vapor is .0071 lb. for each lb. of dry air, or 21.3 × .0071 = 0.15 lb. for each lb. of coal. Each lb. of coal contained .029 lb. of moisture, which was evaporated and carried into the chimney-gases. The .045 lb. of H per lb. of coal when burned formed .045 v 9 = .405 lb. of H pc. D. of From the analysis of the chimney-gas it appears that .09 + 3.50 = 2.37\$ of the carbon in the coal was burned to CO instead of to CO₂.

We now have the data for calculating the various losses of heat, as follows,

We now have the data for calculating the various losses of heat, as follows, for each pound of coal burned:

		Heat- units.	Heat-value of the Coal
20.67 lbs. dry gas \times (560° - 60°) \times sp. heat 0.24	=	2480.4	17.41
	=	86.0	0.25
	=	4.4	0.08
	=	28.0	0.20
	=	4.8	0 08
.405 lb. H ₂ O from H in coal \times (152 + 966 + 848 \times .48) =	=	520.4	8.65
.0237 lb. C burned to CO; loss by incomplete com-			
bustion, $.0237 \times (14544 - 4451)$	=	239.2	1.68
	=	290.9	2.04
Radiation and unaccounted for, by difference	=	624.0	4.81
Utilized in making steam, equivalent evaporation		4228.1	29.68
	=	10,014.9	70.82
		14,248.0	100.00

The heat lost by radiation from the boiler and furnace is not easily determined directly, especially if the boiler is enclosed in brickwork, or is protected by non-conducting covering. It is customary to estimate the heat lost by radiation by difference, that is, to charge radiation with all the heat lost which is not otherwise accounted for.

One method of determining the loss by radiation is to block off a portion of the grate-surface and build a small fire on the remainder, and drive this fire with just enough draught to keep up the steam-pressure and supply the heat lost by radiation without allowing any steam to be discharged, weighing the coal consumed for this purpose during a test of several hours' duration.

Estimates of radiation by difference are apt to be greatly in error, as in this difference are accumulated all the errors of the analyses of the coal

this difference are accumulated all the errors of the analyses of the coal and of the gases. An average value of the heat lost by radiation from a boiler set in brickwork is about 4 per cent. When several boilers are in a battery and enclosed in a boiler-house the loss by radiation may be very much less, since much of the heat radiated from the boiler is returned to it in the air supplied to the furnace, which is taken from the boiler-room. An important source of error in making a "heat balance" such as the one above given, especially when highly bituminous coal is used, may be due to the non-combustion of part of the hydrocarbon gases distilled from the coal immediately after firing, when the temperature of the furnace may be reduced below the point of ignition of the gases. Each pound of hydrogen which escapes burning is equivalent to a loss of heat in the furnace of \$2,500 heat-units.

in analysing the chimney gases by the usual method the percentages of the constituent gases are obtained by volume instead of by weight. To reduce percentages by volume to percentages by weight, multiply the per-centage by volume of each gas by its specific gravity as compared with air, and divide each product by the sum of the products.

if 0, 00, 002, and N represent the per cents by volume of oxygen, caronic oxide, carbonic acid, and nitrogen, respectively, in the gases of combustion:

Lbs. of air required to burn one pound of carbon
$$= \frac{3.089 \text{ N}}{\text{CO}_3 + \text{CO}}$$

Ratio of total air to the theoretical requirement = $\frac{1}{N-8.782}$ O $11CO_2 + 8O + 7(CO + N)$

Lbs. dry gas produced per pound of carbon = 8(CO. + CO)

TESTS OF STEAM-BOILERS.

Boiler-tests at the Centennial Exhibition, Philadelphia, 1876.—(See Reports and Awards Group XX, International Exhibition, Phila., 1876; also, Clark on the Steam-engine, vol. i, page 253.)

Competitive tests were made of fourteen boilers, using good anthracite coal, one boiler, the Galloway, being tested with both anthracite and semi-bituminous coal. Two tests were made with each boiler: one called the capacity trial, to determine the economy and capacity at a rapid rate of driving; and the other called the economy trial, to determine the economy when driven at a rate supposed to be near that of maximum economy and rated capacity. The following table gives the principal results obtained in the economy trial, together with the capacity and economy figures of the capacity trial for comparison.

	Economy Tests.								Capa	Capacity Tests.	
Name of Boiler.	Ratio Water-heating Sur- face to Grate-surface.	Coal burned per sq. ft. Grate per hour.	Per cent Ash and Refuse.	Water evap, from 100° to 70 lbs. p. s.ft. H.S.per hr.	ap.	Temperature in Uptake.	Moisture in Steam.	Superheating of Steam.	Horse power.	Horse-power.	Water evap, from and at 212° per lb. Com- bustible.
Root. Firmenich. Lowe. Smith. Babeock & Wilcox Galloway. Do. semi-bit, coal Andrews. Harrison. Wiegand. Anderson. Kelly. Exeter. Fierce. Rogers & Black.	30.6 45.8 37.7 23.7 23.7 15.6 27.3 30.7 17.5 20.9 33.5 14.0	9.1 12.0 6.8 12.1 10.0 9.6 7.9 8.0 12.4 12.3 9.7 10.8 9.3 8.0	10.4 11.3 11.1 11.0 11.1 8.8 10.3 8.5 9.5 9.3 9.0 11.4	2.25 1.68 1.87 2.42 2.43 3.63 3.20 2.32 2.75 5.30 2.64 3.82 1.38	11.906 11.822 11.583 12.125 11.089 10.930 10.834 10.618 10.312 10.041 10.021	333 411 296 303 325 420 517 524 417	1.3 2.7 0.3 0.9 5.6 4.2 5.2	deg 41.4 32.6 9.4 1.4 71.7 20.5 15.7	H.P. 119.8 57.8 47.0 99.8 135.6 103.3 90.9 42.6 82.4 147.5 98.0 81.0 72.1 51.7 45.7	68.4 69.3 125.0 186.6 133.8	1bs. 10.441 11.064 11.103 11.925 10.330 11.216 11.602 9.745 9.889 9.145 9.568 9.9568 9.974 9.865 9.429
Averages				2.77	11.123	44			85.0	110.8	10.251

The comparison of the economy and capacity trials shows that an average crease in capacity of 30 per cent was attended by a decrease in economy I S per cent, but the relation of economy to rate of driving varied greatly the different boilers. In the Kelly boiler an increase in capacity of 22 per mit was attended by a decrease in economy of over 18 per cent, while the mith boiler with an increase of 25 per cent in capacity showed a slight crease in economy.

One of the most important lessons gained from the above tests is that there is no necessary relation between the type of a boiler and economy. Of the five boilers that gave the best results, the total range of variation between the highest and lowest of the five being only 2.3%, three were watertube boilers, one was a horizontal tubular boiler, and the fifth was a combination of the two types. The next boiler on the list, the Galloway, was internally fired boiler, all of the others being externally fired. The following is a brief description of the principal constructive features of the fourteen boilers.

Root	4-in. water-tubes, inclined 20° to horizontal; reversed draught.
Firmenich	8-in. water-tubes, nearly vertical; reversed draught.
Lowe	Cylindrical shell, multitubular flue.
Smith	Cylindrical shell, multitubular fluewater-tubes in side flues.
Babcock & Wilcox	3½-in. water-tubes, inclined 15° to horizontal; reversed draught.
Galloway	Cylindrical shell, furnace-tubes and water-tubes.
Andrews	Square fire-box and double return multitubular flues.
Harrison	8 slabs of cast-iron spheres, 8 in. in diameter; reversed draught.
Wiegand	4-in. water-tubes, vertical, with internal circulating tubes.
Anderson	
Anderson	8-in. flue-tubes, nearly horizontal; return circulation.
Kelly	8-in. water-tubes, slightly inclined; each divided by
	internal diaphragm to promote circulation.
Exeter	27 hollow rectangular cast-iron slabs.
Pierce	Rotating horizontal cylinder, with flue-tubes.
Rogers & Black	Vertical cylindrical boiler, with external water-tubes.

Tests of Tubulous Boilers.—The following tables are given by 8. H. Leonard, Asst. Engr. U. S. N., in Jour. Am. Soc. Naval Engrs. 1890. The tests were made at different times by boards of U. S. Naval Engineers, except the test of the locomotive-torpedo boiler, which was made in England.

Type. Part P		Evaporation from and at 212° F.				We	in. of	e, lbs.	B, Bit.				
2 Herreshoff { 9.8 10.28 8.1 9.1 E 2,945 96 14.8 4.8 Jet 3 Towne { 4.3 13.4 2.7 10 E 1,380 173 21.8 8.1 Nat 4.5 6.77 8.2 30.4 8.1,640 56 4.5 15.5 10.01 3.2 11 1.8 154 1.8 2.6 1.5 5 10.01 3.2 11 1.90 28 18.2 4.07 Jet 5 Scotch { 24.8 9.93 8.6 11 E 18,900 120 41.2 3.1 4.7 2.8 5 Scotch { 38 9.06 12.8 16.8 5 90,000 80 41.2 3.1 4.7 2.8 5 Locom'tive torpedo. 120.8 17.1 30.5 8.2 34,990 33.3 31.3 1.8 3.1 6 Locom'tive torpedo. 120.8 120.05 36.2 28.990 33.3 3.3 31.3 1.2 4.8 6 Locom'tive torpedo. 120.8 120.05 36.2 28.990 33.3 31.3 1.2 4.8 6 Locom'tive torpedo. 120.8 120.05 36.2 28.990 33.3 31.3 1.2 4.8 6 Locom'tive torpedo. 120.8 120.05 36.2 28.990 33.3 31.3 1.2 1.2 4.8 6 Locom'tive torpedo. 120.8 120.05 36.2 28.990 33.3 31.3 1.2 1.8 3.8 6 Locom'tive torpedo. 120.8 120.05 36.2 30.4 30.4 30.5	No.	Туре.		Per lb. Com'ble.	Per sq. ft. H. Surface.	Per cu. ft. Space.	E, Empty. S, Steaming Level.	Per L.H.P.	Per sq. ft. H. Surface.	Per lb. Water evaporated.	Air-pressure, i Water.	Steam-pressure,	Coal. A, Anth.;
2 Herreshoff { 9.8 10.28 8.1 9.1 E 2,945 96 14.8 4.8 Jet Jet State S	-	Polle-file	10.0	10.49	E 0	8.4	E 40,670	904	K9 0	10.1	Many	111	_
2 Herresholt { 25.8 8.68 8 28.8 8.3050 86 14.5 1.8 Jet	1	penevine					8 42,770	204	م.س				•
4 Ward 7.9 10.77 1.7 5.8 E 1.682 15.4 13.2 7.7 Nat 5 Scotch 24.8 9.93 8.6 11 E 18,900 120 41.2 4.7 1.8 1.8 1.8 6 Locom'tive torpedo, 120.8 98.3	2	Herreshoff	25.8	8.68	8	28.8	E 2,945 S 8,050	88	14.8	1.8	Jet. Jet.	120 195	A.
4 Ward { 7.9 10.77 1.7 5.8 E 1.682 154 89 18.2 4.07 Jef 1.5 10.01 3.2 11 1.5 1.00 34.2 15 1.930 26 1.8 1.00	8	Towne		6 77	8.2	80.4	E 1,380 S 1,640	56	21.8	8.1 2.6	Nat'l. 1.14	148 152	A.
6 Loom'tive 98.8 17.1 80.5 8 40,990 47.7 81.1 1.8 8. torpedo, 120.8 120.05 86.2 8 49,990 83.8 81.8 1.2 4.	1	Ward	7.9	10.01 7.01	8.2 10	11 84.2	E 1,682 S 1,930	154 82 26	18.2	7.7 4.07 1.8	Nat'l. Jet. Jet.	0 17 161	A.
torpedo, 120.8 20.05 86.2 37,500 83.8 1.2 4.	5	Scotch) 24.8) 88		8.6 12.8	11 16.8			41.2	8.1	2.08 4.01	78	A. A.
	6	Locom'tive torpedo,	98.8		17.1	80.5	8 84,990	47.7 83.8	81.8	1.8	8.18 4.95	125 123	В.
7 Ward 55.04 8.44 9.47 82.1 E 26,538 26 12.8 1.8 8		Ward	55.04	8.44	9.47	82.1	10 90 474	zo	12.8	1.8	8	160	B.
8 Thorny- croft (U. 8.8.Cush- ing.) 45	8	croft. (U. 8.S.Cush-	45		.	. 	E 20.160	*81	10.3	· · · · · ·	8	845	B,

*Approximate.

Per cent moisture in steam: Belleville, 5.3; Herreshoff (first test), 3.5

Scotch, 1st, 3.44; 3d, 4.29; Ward, 11.6; others not given.

DIMENSIONS OF THE BOILERS.

No.	1	2	8	4	5	6	7	8
Length, ft. and in. Width, " " " Height, " " Space, cu. ft. Grate-area, sq. ft. Heating-surface, sq. ft. Ratio H.S. + G	8' 6" 7 0 11 0 645.5 84.17 804 23.5		2' 6" 2 6 8 3 20 8 4.25 75 17.6	8' 2'' 1 7 7 3 42.7 8.68 146 89.5	9' 0'' 9 0 572.5 31.16 727 23.3	16' 8 6 4 7 6 630.3 28 1116 39.8	10' 8''* 4 6 † 11 8 729.8 66.5 2490 87.4	10' 0''\$ 7 0\$ 8 0\$ 560\$ 38.3 2875 62

Diameter. † Diam. of drum. ‡ Approximate.

The weight per I.H.P. is estimated on a basis of 20 lbs. of water per hour The weight per I.H.F. is estimated on a basis of 2008. Of water per nour for all cases excepting the Scotch boiler, where 25 lbs. have been used, as this boiler was limited to 80 lbs. pressure of steam.

The following approximation is made from the large table, on the assumption that the evaporation varies directly as the combustion, and 25 lbs. of coal per square foot of grate per hour used as the unit.

Type of Boiler.	Com bustion.	Evapora- tion per cu. ft. of Space.	Weight per I.H.P.	Weight per sq. ft. Heating- surface.	Weight per lb. Water Evapo- rated.
Belleville	0.50	0.50	2.02	2.10	2.50
	1.00	0.95	- 0.72	0.60	0.90
	1.00	1.20	1.12	0.87	1.30
	1.00	0.44	2.40	1.64	2.30
	8.90	0.31	8.70	1.25	8.50
	2.20	0.58	1.27	0.50	1.58

The Belleville boiler has no practical advantage over the Scotch either in space occupied or weight. All the other tubulous boilers given greatly exceed the Scotch in these advantages of weight and space.

Some High Rates of Evaporation.—Eng'y, May 9, 1884, p. 415. Torpedo-boat. Locomotive. Water evap. per sq. ft. H.S. per hour. ... lb. fuel from and at 212°. 12.57 18.78 12.54 20.74 8.22 8.94 8.87 7 04 12,113 20,034 Thermal units transf'd per sq. ft. of H.S. 12,142 13,268 Efficiency542 .468

Economy Effected by Heating the Air Supplied to Boller-furnaces. (Clark, S. E.)—Meunier and Scheurer-Kestner obtained about 7% greater evaporative efficiency in summer than in winter, from the same boilers under like conditions,—an excess which had been explained by the difference of loss by radiation and conduction. But Mr. Poupardin, surmising that the gain might be due in some degree also to the greater temperature of the air in summer, made comparative trials with two groups of three boilers, each working one week with the heated air, and the next week with cold air. The following were the several efficiencies:

FIRST TRIALS: THREE BOILERS; RONCHAMP COAL.
Water per lb. of Water per lb. of
Coal.
Combustible. With heated air (128° F.) 7.77 lbs. 8.95 lbs. 8.63 ** 0.32 " Difference in favor of heated air ... 0.44 "

SECOND TRIALS: SAME COAL; THE	EE OTHER	Boilers.
With heated air (120°.4 F.)	8.70 lbs.	10.08 lbs.
With cold air (75°.2)	0.61 44	9.84 " 0. 74 "

These results show economies in favor of heating the air of 6% and 736%. Mr. Poupardin believes that the gain in efficiency is due chiefly to the better combustion of the gases with heated air. It was observed that with heated air the flames were much shorter and whiter, and that there was

notably less smoke from the chimney.

notably less smoke from the chimney.
An extensive series of experiments was made by J. C. Hoadley (Trans. A. S. M. E., vol. vi., 676) on a "Warm-blast Apparatus," for utilizing the heat of the waste gases in heating the air supplied to the furnace. The apparatus, as applied to an ordinary horizontal tn ular bolier 60 in, diameter, 21 feet long, with 65 3½-inch tubes, consisted of 240 2-inch tubes, 18 feet long, through which the hot gases passed while the air circulated around them. The net saving of fuel effected by the warm blast was from 10.7% to 15.5% of the fuel used with cold blast. The comparative temperatures averaged as follows: in decrease F. follows, in degrees F.:

•	Cold-blast Boiler.	Warm-blast Boiler.	Difference.
In heat of fire	2408	2798	300
At bridge wall		1600	260
In smoke box	878	875	2
Air admitted to furnace	82	882	800
Steam and water in boiler		800	0
Gases escaping to chimney	878	162	211
External air	32	82	0

With anthracite coal the evaporation from and at 212° per lb. combustible was, for the cold-blast boiler, days 10.85 lbs., days and nights 10.51; and for the warm-blast boiler, days 11.83, days and nights 11.08.

Results of Tests of Heine Water-tube Boilers with Different Coals.

(Communicated by E. D. Meier, C.E., 1894.)

Number	1	2	8	4	5	6	7	8
Kind of Coal.	Cumberland, Semi-bitum.	2d I Youg en	hiogh-	Turkey Hill, Ill.	Carbon Hill, Wash.	Hocking Val., Ohio.	Gillespie, Lump, Ill.	Collingville, Ill.
Per cent ash	5.1 2900 54 53.7 24.7	4.89 2040 44.8 45.5 28.5	2040 44.8 45.5 22.7	11.6 2300 50 46 85	16.1 1260 21 60 88.7	11.5 8780 73.8 50.9 26.2	91.8 1168 27.9 41.9 27.7	12.8 2770 50 55.4 36
hr. from and at 2120 Water evap, from and at	5.08	5.14	5.24	5.56	4.26	4.28	4.86	5.08
212° per lb. coal Per lb. combustible Temp. of chimney gases	10.91 11.50	9.94 10.48	10.51	7.81 8.27 567	7.59 9.05 571	8.38 9.41	7.86 9.41 609	7.81 8.96 707
Calorific value of fuel Efficiency of boiler per c.	18,800	12, 986 74.8				11,610 69.8		10,859 72.6

Tests Nos. 7 and 8 were made with the Hawley Down-draught Furnace. the others with ordinary furnaces.

These tests confirm the statement already made as to the difficulty of obtaining, with ordinary grate furnaces, as high a percentage of the calorific value of the fuel with the Western as with the Eastern coals.

Test No 3, 78.5% efficiency, is remarkably good for Pittsburgh (Youghiogheny) coal. If the Washington coal had given equal efficiency, the saving of fuel would be $\frac{78.5 - 62.5}{2} = 20.25$. The results of tests Nos. 7 and 8 indicate 78.5 that the downward-draught furnace is well adapted for burning Illinois

Maximum Boiler Efficiency with Cumberland Coal.—
About 12.5 lbs. of water per lb. combustible from and at 212° is about the nighest evaporation that can be obtained from the best steam fuels in the Jaired States, such as Cumberland, Pocahontas, and Clearfield. In excep-ional cases 13 lbs. has been reached, and one test is on record (F. W. Dean, Ing'y News, Feb. 1, 1894) giving 18,23 lbs. The boiler was internally fired, of the Belpaire type, 82 inches diameter, 31 feet long, with 160 3-inch tubes 21/4 feet long. Heating-surface, 1998 square feet; grate-surface, 45 square feet, educed during the test to 3014 square feet. Double furnace, with fire-brick rches and a long combustion-chamber. Feed-water heater in smoke-box. 'he following are the principal results:

•	lst Test.	2d Test.
ry coal burned per sq. ft. of grate per hour, lbs	8.85	16.06
Vater evap, per sq. ft. of heating-surface per hour, lbs		8.00
7ater evap, from and at 212° per lb, combustible, in-		
cluding feed-water heater	13.17	18.23
7ater evaporated, excluding feed-water heater		12,90
emperature of gases after leaving heater, F	860°	4690

BOILERS USING WASTE GASES.

Proportioning Boilers for Blast-Furnaces.—(F. W. Gordon, Trans. A. I. M. E., vol. xii., 1883.)

Mr. Gordon's recommendation for proportioning boilers when properly set r burning blast-furnace gas is, for coke practice, 30 sq. ft. of heating-surce per ton of iron per 24 hours, which the furnace is expected to make, lenlating the heating-surface thus: For double-flued boilers, all shellrface exposed to the gases, and half the flue-surface; for the French type, I the exposed surface of the upper boiler and half the lower boiler-rface; for cylindrical boilers, not more than 60 ft. long, all the heating-

To the above must be added a battery for relay in case of cleaning, repairs, and more than one battery extra in large plants, when the water carries

uch lime.

For anthracite practice add 50% to above calculations. For charcoal prac-

e deduct 20%.

in a letter to the author in May, 1894, Mr. Gordon says that the blast-nace practice at the time when his article (from which the above extract aken) was written was very different from that existing at the present is testion was written was very different from that existing at the present ie; besides, more economical engines are being introduced, so that less in 30 sq. ft. of boiler-surface per ton of iron made in 24 hours may now be opted. He says further: Blast-furnace gases are seldom used for other in furnace requirements, which of course is throwing away good fuel. In s case a furnace in an ordinary good condition, and a condition where it itake its maximum of blast, which is in the neighborhood of 200 to 225 ic fL, atmospheric measurement, per sq. ft. of sectional area of hearth, I generate the necessary H.P. with very small heating-surface, owing to high heat of the escaping gases from the boilers, which frequently is) degrees.

furnace making 200 tons of iron a day will consume about 900 H.P. in wing the engine. About a pound of fuel is required in the furnace per

nd of pig metal.

practice it requires 70 cu ft. of air-piston displacement per lb. of fuel sumed, or 22,400 cu. ft. per minute for 200 tons of metal in 1400 working utes per day, at, say, 10 lbs. discharge-pressure. This is equal to 94 lbs. .P. on the steam-piston of equal area to the blast-piston, or 900 I.H.P. To add 20% for hoisting, pumping and other purposes for which steam is emed around blast-furnaces, and we have 1100 H.P., or say 5½ H.P. per of iron per day. Dividing this into 80 gives approximately 5½ sq. ft. of ing-surface of boiler per H.P.

7ater-tube Boilers using Blast-furnace Gases.-D. S. bus (Trans. A. I. M. E., xvii. 50) reports a test of a water tube boiler using t-furnace gas as fuel. The heating-surface was 2535 sq. ft. It developed H.P. (Centennial standard), or 5.01 lbs of water from and at 212° per t. of heating-surface per hour. Some of the principal data obtained, as follows: Calorific value of 1 lb. of the gas, 1418 B T.U., including affect of its initial temperature, which was 650° F. Amount of air used 1rn 1 lb. of the gas = 0.9 lb. Chimney draught, 1½ in. of water. Area content 300° sq. in content 300° sq. in content 300° sq. in content 300° sq. in content 300° sq. in the sq. in inlet, 300 sq. in.; of air inlet, 100 sq. in. Temperature of the chim

gases, 775° F. Efficiency of the boiler calculated from the temperatures and analyses of the gases at exit and entrance, 61%. The average analyses were as follows, hydrocarbons being included in the nitrogen:

•	By We	ight.	By Volume.		
	At Entrance.	At Exit.	At Entrance.	At Exit.	
CO ₂ O CO Nitrogen C in CO ₂ C in CO Total C	26.71	26.37 8.05 1.78 68.80 7.19 .76 7.95	7.08 .10 27.80 65.02	18.64 2.96 1.98 76.43	

Steam-boilers Fired with Waste Gases from Puddling and Heating Furnaces.—The Iron Age, April 6, 1898, contains a report of a number of tests of steam-boilers utilizing the waste heat from puddling and heating furnaces in rolling-mills. The following principal data are selected: In Nos. 1, 2, and 4 the boiler is a Babcock & Wilcox water-tube boiler, and in No. 3 it is a plain cylinder boiler, 42 in. diam. and 26 t. long. No. 4 boiler was connected with a heating-furnace, the others with puddling furnaces.

	No. 1.	No. 2.	No. 8.	No. 4.
Heating-surface, sq. ft	1026	1196	143	1380
Grate-surface, sq. ft	19.9	18 6	13.6	16.7
Ratio H.S. to G.S.	52	87.2	10.5	8 2.8
Water evap. per hour, lbs	3358	2159	1812	8055
" " per sq. ft. H.S. per hr., lbs	8.3	1.8	12.7	2.2
" per lb. coal from and at 212°.	5.9	6.24	8.76	6.84
" " comb. " " "	• • • •	7.20	4.81	8.34

In No. 2, 1.88 lbs. of iron were puddled per lb. of coal. In No. 8, 1.14 lbs. of iron were puddled per lb. of coal.

No. 3 shows that an insufficient amount of heating-surface was provided for the amount of waste heat available.

BULES FOR CONDUCTING BOILER-TESTS.

Code of 1899.

(Reported by the Committee on Boiler Trials, Am. Soc. M. E.*)

I. Determine at the outset the specific object of the proposed trial, Letermine at the outset the specific object of the proposed trial, whether it be to ascertain the capacity of the boiler, its efficiency as a steam-generator, its efficiency and its defects under usual working conditions, the economy of some particular kind of fuel, or the effect of changes of design, proportion, or operation; and prepare for the trial accordingly.

II. Examine the boiler, both outside and inside; ascertain the dimensions of grates, heating surfaces and all important restatements.

of grates, heating surfaces, and all important parts; and make a full rec-ord, describing the same, and illustrating special features by sketches. III. Notice the general condition of the boiler and its equipment, and record such facts in relation thereto as hear upon the objects in view.

record such facts in relation thereto as bear upon the objects in view.

If the object of the trial is to ascertain the maximum economy or capacity of the boiler as a steam-generator, the boiler and all its appurtenances should be put in first-class condition. Clean the heating surface inside and outside, remove clinkers from the grates and from the sides of the inside and outside, remove all dust, soot, and ashes from the chambers, smoke-connections, and flues. Close air-leaks in the masonry and poorly fitted cleaning-doors. See that the damper will open wide and close tight. Test for air-leaks by firing a few shovels of smoky fuel and immediately closing the damper, observing the second of smoky through the creatives or by passing the flame serving the escape of smoke through the crevices, or by passing the flame of a candle over cracks in the brickwork.

^{*}The code is here slightly abridged. The complete report of the Committee may be obtained in pamphlet form from the Secretary of the American Society of Mechanical Engineers, 12 West 31st St., New York.

IV. Determine the character of the coal to be used. For tests of the efficiency or capacity of the boiler for comparison with other boilers the coal should, if possible, be of some kind which is commercially regarded as a standard. For New Eugland and that portion of the country east of the standard. For New England and that portion of the country east of the Allegheny Mountains, good anthracite egg coal, containing not over 10 per cent. of ash, and semi-bituminous Clearfield (Pa.), Cumberland (Md.), and Pocahontas (Va.) coals are thus regarded. West of the Allegheny Mountains, Pocahontas (Va.) and New River (W. Va.) semi-bituminous, and Youghiogheny or Pittsburg bituminous coals are recognized as standards.*

For tests made to determine the performance of a boiler with a particular kind of coal, such as may be specified in a contract for the sale of a boiler, the coal used should not be higher in ash and in moisture than that received since increase in each and moisture than that

specified, since increase in ash and moisture above a stated amount is apt to cause a falling off of both capacity and economy in greater proportion than

the proportion of such increase.

V. Establish the correctness of all apparatus used in the test for weighing and measuring. These are:

1. Scales for weighing coal, ashes, and water.

2. Tanks or water-meters for measuring water. Water-meters, as a rule, should only be used as a check on other measurements. For accurate work the water should be weighed or measured in a tank.

3. Thermometers and pyrometers for taking temperatures of air, steam,

feed-water, waste gases, etc.

4. Pressure-gauges, draught-gauges, etc.
VI. See that the boiler is thoroughly heated before the trial to its usual working temperature. If the boiler is new and of a form provided with a brick setting, it should be in regular use at least a week before the trial, so as to dry and heat the walls. If it has been laid off and become cold, it

should be worked before the trial until the walls are well heated.

VII. The boiler and connections should be proved to be free from leaks briore beginning a test, and all water connections, including blow and extra feed-pipes, should be disconnected, stopped with blank flanges, or bied through special openings beyond the valves, except the particular pipe through which water is to be fed to the boiler during the trial. During the test the blow-off and feed pipes should remain exposed to view.

If an injector is used, it should receive steam directly through a felted

pipe from the boiler being tested.†

If the water is metered after it passes the injector, its temperature should be taken at the point where it leaves the injector. If the quantity is determined before it goes to the injector, the temperature should be determined on the suction side of the injector, and if no change of temperature occurs other than that due to the injector, the temperature thus determined is properly that of the feed water. When the temperature changes between the injector and the boiler, as by the use of a heater or by radiation, the temperature at which the water enters and leaves the injector and that at which it enters the boiler should all be taken. In that case the weight to be used is that of the water leaving the injector, computed from the heat units if not directly measured; and the temperature, that of the water entering the boiler.

```
w =  weight of water entering the injector; x =  " steam " " ;
Let
            h_1 = \text{heat-units per pound of water entering injector};
            h_2 =
                                             " steam
                                             " water leaving
            h_2 =
```

*These coals are selected because they are about the only coals which

^{*}These coals are selected because they are about the only coals which possess the essentials of excellence of quality, adaptability to various kinds of furnaces, grates, bollers, and methods of firing, and wide distribution and general accessibility in the markets.

†In feeding a boiler undergoing test with an injector taking steam from another boiler, or from the main steam-pipe from several boilers, the evaporative results may be modified by a difference in the quality of the steam from such source compared with that supplied by the boiler being tested, and in some cases the connection to the injector may act as a drip for the main steam-pipe. If it is known that the steam from the main pipe is of the same pressure and quality as that furnished by the boiler undergoing the test, the steam may be taken from such main pipe. the test, the steam may be taken from such main pipe.

Then

$$w + x =$$
 weight of water leaving injector,
 $x = w \frac{h_3 - h_2}{h_2 - h_2}$.

See that the steam-main is so arranged that water of condensation cannot run back into the boiler.

run back into the boner.

VIII. Duration of the Test.—For tests made to ascertain either the maximum economy or the maximum capacity of a boiler, irrespective of the particular class of service for which it is regularly used, the duration should be at least ten hours of continuous running. If the rate of combustion exceeds 25 pounds of coal per square foot of grate-surface per hour, it may be stopped when a total of 250 pounds of coal has been burned per square foot of grate.

of grate.

IX Starting and Stopping a Test.—The conditions of the boiler and furnace in all respects should be, as nearly as possible, the same at the end as at the beginning of the test. The steam-pressure should be the same; the fire upon the grates should be the same in quantity and condition; and the walls, flues, etc., should be of the same temperature. Two methods of obtaining the desired equality of conditions of the fire may be used, viz., those which were called in the Code of 1885 "the standard method" and "the alternate method," the latter being employed where it is inconvenient to make use of the standard method.*

X. Standard Method of Sturting and Stopping a Test.—Steam being raised to the working pressure, remove rapidly all the fire from the grate, close the damper, clean the ash-pit, and as quickly as possible start a new fire with weighed wood and coal, noting the time and the water-level † while the water is in a quiescent state, just before lighting the fire.

At the end of the test remove the whole fire, which has been burned low, clean the orders and see hit and note the water level when the protest is in

At the end of the test remove the whole fire, which has been burned low, clean the grates and ash-pit, and note the water-level when the water is in a quiescent state, and record the time of hauling the fire. The water-level should be as nearly as possible the same as at the beginning of the test. If it is not the same, a correction should be made by computation, and not by operating the pump after the test is completed.

XI. Alternate Method of Starting and Stopping a Test.—The boiler being thoroughly heated by a preliminary run, the fires are to be burned low and well cleaned. Note the amount of coal left on the grate as nearly as it can be estimated; note the pressure of steam and the water-level. Note the time, and record it as the starting-time. Fresh coal which has been weighed should now be fired. The ash-pits should be thoroughly cleaned at once after starting. Before the end of the test the fires should be burned low, just as before the start, and the fires cleaned in such a manner as to leave a bed of coal on the grates of the same depth, and in the same condition, as at the start. When this stage is reached, note the time and record it as the stopping-time. The water-level and steam-pressures should previously be brought as nearly as possible to the same point as at the start. If the water-level is not the same as at the start, a correction should be made by computation, and not by operating the pump after the test is completed.

putation, and not by operating the pump after the test is completed.

XII. Uniformity of Conditions.—In all trials made to ascertain maximum economy or capacity the conditions should be maintained uniformly constant. Arrangements should be made to dispose of the steam so that the rate of evaporation may be kept the same from beginning to end.

XIII. Keeping the Records.—Take note of every event connected with the progress of the trial, however unimportant it may appear. Record the time of every occurrence and the time of taking every weight and every observation.

The coal should be weighed and delivered to the fireman in equal proportions, each sufficient for not more than one hour's run, and a fresh portion

^{*}The Committee concludes that it is best to retain the designations "standard" and "alternate," since they have become widely known and established in the minds of engineers and in the reprints in the Code of 1885. Many engineers prefer the "alternate" to the "standard" method on account of its being less liable to error due to cooling of the boiler at the beginning and end of a test.

beginning and end of a test.

†The gauge-glass should not be blown out within an hour before the water-level is taken at the beginning and end of a test, otherwise an error in the reading of the water-level may be caused by a change in the temperature and density to the water in the pipe leading from the bottom of the glass into the boller.

nould not be delivered until the previous one has all been fired. The time squired to consume each portion should be noted, the time being recorded the instant of firing the last of each portion. It is desirable that at the me time the amount of water fed into the boiler should be accurately sted and recorded, including the height of the water in the boiler, and the erage pressure of steam and temperature of feed during the time. By ms recording the amount of water evaporated by successive portions of al, the test may be divided into several periods if desired, and the degree uniformity of combustion, evaporation, and economy analyzed for each uniformity of combustion, evaporation, and economy analyzed for each riod. In addition to these records of the coal and the feed-water, half-mily observations should be made of the temperature of the feed-water, the flue-gases, of the external air in the boiler-room, of the temperature the furnace when a furnace-pyrometer is used, also of the pressure of sam, and of the readings of the instruments for determining the moisture the steam. A log should be kept on properly prepared blanks containing lumns for record of the various observations.

IIV. Quality of Steam.—The percentage of moisture in the steam should determined by the use of either a throttling or a separating steam-calorater. The sampling-nozzle should be placed in the vertical steam-pipe

neter. The sampling-nozzle should be placed in the vertical steam-pipe ing from the boiler. It should be made of 4-inch pipe, and should extend ross the diameter of the steam-pipe to within half an inch of the opposite e, being closed at the end and perforated with not less than twenty i-inch less equally distributed along and around its cylindrical surface, but none these holes should be nearer than \(\frac{1}{2}\) inch to the inner side of the steamer. The calorimeter and the pipe leading to it should be well covered h feiting. Whenever the indications of the throtting or separating orimeter show that the percentage of moisture is arregular, or occasionate with a should be absoluted by in excess of three per cent., the results should be checked by a steamarator placed in the steam-pipe as close to the boiler as convenient, with alorimeter in the steam-pipe just beyond the outlet from the separator, drip from the separator should be caught and weighed, and the pertage of moisture computed therefrom added to that shown by the caloeter.

uperheating should be determined by means of a thermometer placed in nercury-well inserted in the steam-pipe. The degree of superheating uld be taken as the difference between the reading of the thermometer superheated steam and the readings of the same thermometer for satuad steam at the same pressure as determined by a special experiment,

not by reference to steam tables.

V. Sampling the Coal and Determining its Moisture.—As each barrowor fresh portion of coal is taken from the coal pile, a represenre shovelful is selected from it and placed in a barrel or box in a cool e and kept until the end of the trial. The samples are then mixed and ten into pieces not exceeding one inch in diameter, and reduced by the sess of repeated quartering and crushing until a final sample weighing it five pounds is obtained, and the size of the larger pieces is such that will pass through a sieve with 1-inch meshes. From this sample two quart, air-tight glass preserving jars, or other air-tight vessels which prevent the escape of moisture from the sample, are to be promptly t, and these samples are to be kept for subsequent determinations of sure and of heating value and for chemical analyses. During the proof quartering, when the sample has been reduced to about 100 pounds, arter to a half of it may be taken for an approximate determination of ture. This may be made by placing it in a shallow fron pan, not over inches deep, carefully weighing it, and setting the pan in the hottest that can be found on the brickwork of the boiler-setting or flues, ing it there for at least 12 hours, and then weighing it. The determination of modeline the proportion of the sample is a believed to be appropriately accurate for of moisture thus made is believed to be approximately accurate for cacite and semi-bituminous coals, and also for Pittsburg or Youghloveal; but it cannot be relied upon for coals mined west of Pittsburg, rother coals containing inherent moisture. For these latter coals it is rtant that a more accurate method be adopted. The method recomed by the Committee for all accurate tests, whatever the character of sal, is described as follows:

te one of the samples contained in the glass jars, and subject it to a ugh air-drying, by spreading it in a thin layer and exposing it for all hours to the atmosphere of a warm room, weighing it before and thereby determining the quantity of surface moisture it contains, Then crush the whole of it by running it through an ordinary coffee-mill adjusted so as to produce somewhat coarse grains (less than $\frac{1}{4}$ inch), thoroughly mix the crushed sample, select from it a portion of from 10 to 50 grams, weigh it in a balance which will easily show a variation as small as I part in 1000, and dry it in an air- or sand-bath at a temperature between 240 and 230 degrees Fahr, for one hour. Weight it and record the loss, then heat and weigh it again repeatedly, at intervals of an hour or less, until the minimum weight has been reached and the weight begins to increase by oxidation of a portion of the coal. The difference between the original and the minimum weight is taken as the moisture in the air-dried coal. This moisture test should preferably be made on duplicate samples, and the results should agree within 0.3 to 0.4 of one per cent., the mean of the two determinations being taken as the correct result. The sum of the percentage of moisture thus found and the percentage of surface moisture previ-

ously determined is the total moisture.

XVI. Treatment of Ashes and Refuse.—The ashes and refuse are to be weighed in a dry state. If it is found desirable to show the principal characteristics of the ash, a sample should be subjected to a proximate analysis and the actual amount of incombustible material determined. For elabo-

rate trials a complete analysis of the ash and refuse should be made.

XVII. Calorific Tests and Analysis of Coal.—The quality of the should be determined either by heat test or by analysis, or by both.

The rational method of determining the total heat of combustion is to burn the sample of coal in an atmosphere of oxygen gas, the coal to be

sampled as directed in Article XV of this code.

The chemical analysis of the coal should be made only by an expert chemist. The total heat of combustion computed from the results of the ultimate analysis may be obtained by the use of Dulong's formula (with constants modified by recent determinations), viz.,

14,600 C + 62,000 (H
$$-\frac{O}{8}$$
) + 4000 S,

in which C, H, O, and S refer to the proportions of carbon, hydrogen, oxygen, and sulphur respectively, as determined by the ultimate analysis.*

It is desirable that a proximate analysis should be made, thereby determining the relative proportions of volatile matter and fixed carbon. proportions furnish an indication of the leading characteristics of the fuel,

and serve to fix the class to which it belongs.

XVIII. Analysis of Flue-yases.—The analysis of the flue-gases is an especially valuable method of determining the relative value of different methods of firing or of different kinds of furnaces. In making these analyses great care should be taken to procure average samples, since the composition is apt to vary at different points of the flue. The composition is also apt to vary from minute to minute, and for this reason the drawings of gas should last a considerable period of time. Where complete determinations are desired, the analyses should be intrusted to an expert chemist. For approximate determinations the Orsat or the Hempel appa-

ratus may be used by the engineer.

For the continuous indication of the amount of carbonic acid present in

the flue gases an instrument may be employed which shows the weight of CO, in the sample of gas passing through it.

XIX. Smoke Observations.—It is desirable to have a uniform system of determining and recording the quantity of smoke produced where bituminous coal is used. The system commonly employed is to express the degree of smokiness by means of percentages dependent upon the judgment of the observer. The actual measurement of a sample of soot and smoke by some form of meter is to be preferred.

XX. Miscellaneous.—In tests for purposes of scientific research, in which the determination of all the variables entering into the test is desired, certain observations should be made which are in general unnecessary for ordinary tests. As these determinations are rarely undertaken, it is not

deemed advisable to give directions for making them.

XXI. Calculations of Efficiency.-Two methods of defining and calculating the efficiency of a boiler are recommended. They are:

^{*} Favre and Silbermann give 14,544 B.T.U. per pound carbon; Berthelot, 14,647 B.T.U. Favre and Silbermann give 62,032 B.T.U. per pound hydrogen; Thomsen, 61,816 B.T.U.

- Heat absorbed per lb. combustible 1. Efficiency of the boiler = Calorific value of 1 lb, combustible
- Heat absorbed per lb. coal 2. Efficiency of the boiler and grate = Calorific value of 1 lb. coal

The first of these is sometimes called the efficiency based on combustible, and the second the efficiency based on coal. The first is recommended as a standard of comparison for all tests, and this is the one which is understood to be referred to when the word "efficiency" alone is used without qualification. The second, however, should be included in a report of a test, together with the first, whenever the object of the test is to determine the efficiency of the boller and furnace together with the grate (or mechan-ical stoker), or to compare different furnaces, grates, fuels, or methods of

The heat absorbed per pound of combustible (or per pound coal) is to be calculated by multiplying the equivalent evaporation from and at 212 degrees

per pound combustible (or coal) by 965.7.

XXII. The Heat Balance.—An approximate "heat balance," may be included in the report of a test when analyses of the fuel and of the chimneygases have been made. It should be reported in the following form:

HEAT BALANCE, OR DISTRIBUTION OF THE HEATING VALUE OF THE COM-BUSTIBLE.

Total Heat Value of 1 lb. of Combustible..... B. T. U.

	B. T. U.	Per Cent.
1. Heat absorbed by the boiler = evaporation from and at	1 1	
212 degrees per pound of combustible × 965.7	1 1	
ferred to combustible $+ 100 \times [(212 - t) + 966 +$		
0.48(T-212)](t= temperature of air in the boiler-room, $T=$ that of the flue-gases)	1	
3. Loss due to moisture formed by the burning of hydro-	1 1	
gen = per cent of hydrogen to combustible $+ 100 \times 9$		•
\times [(212-t)+966 + 0.48(T-212)]4.* Loss due to heat carried away in the dry chimney-gases		
= weight of gas per pound of combustible × 0.24 ×	1 1	
(T-t)		
$= \frac{\text{CO}}{\text{CO}_2 + \text{CO}} \times \frac{\text{per cent. C in combustible}}{100} \times 10{,}150$	1 1	
	1 1	
6. Loss due to unconsumed hydrogen and hydrocarbons,		
to heating the moisture in the air, to radiation, and unaccounted for. (Some of these losses may be sep-	1 1	
arately itemized if data are obtained from which	1	
they may be calculated)		
Totals		100.00

^{*} The weight of gas per pound of carbon burned may be calculated from the gas analyses as follows:

Dry gas per pound carbon = $\frac{11CO_2 + 8O + 7(CO + N)}{2CO_2 + 8O + 7(CO + N)}$, in which CO₂, CO₃

O, and N are the percentages by volume of the several gases. As the sampling and analyses of the gases in the present state of the art are liable to considerable errors, the result of this calculation is usually only an approximate one. The heat balance itself is also only approximate for this reason, as well as for the fact that it is not possible to determine accurately the percentage of unburned hydrogen or hydrocarbons in the flue-gases.

The weight of dry gas per pound of combustible is found by multiplying the dry gas per pound of carbon by the percentage of carbon in the combustible, and dividing by 100.

† CO₂ and CO are respectively the percentage by volume of carbonic acid and carbonic oxide in the flue-gases. The quantity 10,150 = number of heatunits generated by burning to carbonic acid one pound of carbon contained in carbonic oxide.

Mada hr

XXIII. Report of the Trial.-The data and results should be reported in Alli. Report of the Trial.—The data and results should be reported in the manner given in either one of the two following tables [only the "Shore Form" of table is given here], omitting lines where the tests have not been made as elaborately as provided for in such tables. Additional lines may be added for data relating to the specific object of the test. The Short Form of Report, Table No. 2, is recommended for commercial tests and as a convenient form of abridging the longer form for publication when saving of space is desirable. For elaborate trials it is recommended that the full log of the trial he shown graphically. We means of a chert trial be shown graphically, by means of a chart.

TABLE NO. 2.

DATA AND RESULTS OF EVAPORATIVE TEST.

Arranged in accordance with the Short Form advised by the Boiler Test Committee of the American Society of Mechanical Engineers. Code of 1899.

Made byonboiler, determine	at to
determine Kind of fuel Kind of furnace	
Method of starting and stopping the test ("standard" or "alternate," Arts. X and XI, Code)	sq. ft.
TOTAL QUANTITIES.	
1. Date of trial 2. Duration of trial 3. Weight of coal as fired * 4. Percentage of moisture in coal † 5. Total weight of dry coal consumed 6. Total ash and refuse 7. Percentage of ash and refuse in dry coal 8. Total weight of water fed to the boiler; 9. Water actually evaporated, corrected for moisture or superheat in steam 9a. Factor of evaporation; 10. Equivalent water evaporated into dry steam from and at 212 degrees. (Item 9 x Item 9a.)	hours lbs. per cent. lbs. per cent. lbs.
HOURLY QUANTITIES.	
11. Dry coal consumed per hour	. "
12. Dry coal per square foot of grate surface per	"
13. Water evaporated per hour corrected for quality of steam	
14. Equivalent evaporation per hour from and at	"
15. Equivalent evaporation per hour from and at 212 degrees per square foot of water-heating surface	"

this is the total moisture in the coal as found by drying it artificially, as described in Art. XV of Code.

† Corrected for inequality of water-level and of steam-pressure at beginning and end of test.

§ Factor of evaporation $=\frac{H-h}{965.7}$, in which H and h are respectively the total heat in steam of the average observed pressure, and in water of the average observed temperature of the feed.

The symbol 'U. E.," meaning "units of evaporation," may be con-

^{*} Including equivalent of wood used in lighting the fire, not including unhurnt coal withdrawn from furnace at times of cleaning and at end of test. One pound of wood is taken to be equal to 0.4 pound of coal, or, in case greater accuracy is desired, as having a heat value equivalent to the evaporation of 6 pounds of water from and at 212 degrees per pound. (6 × 965.7 = 5794 B.T.U.) The term "as fired" means in its actual condition, including moisture.

AVERAGE PRESSURES, TEMPERATURES, ETC.	
16. Steam pressure by gauge	. deg.
 Force of draft between damper and boiler Percentage of moisture in steam, or number of 	ins. of water
degrees of superheating	per cent.or deg.
HORSE-POWER.	
11. Horse-power developed. (Item 14 + 34½.)¶ 22. Builders' rated horse-power	
23. Percentage of builders' rated horse-power de	• · · · · · · · · · · · · · · · · · · ·
veloped	per cent.
economic results.	i
M. Water apparently evaporated under actual con- ditions per pound of coal as fired. (Item	1
8 + Item 8.)	lbs.
$8 \rightarrow \text{Item } 8.$). 5. Equivalent evaporation from and at 213 degrees	
per pound of coal as fired. (Item 10+Item 3.) 6. Equivalent evaporation from and at 212 degrees	il i
per pound of dry coal ! (Item 10 + Item 5.)	, " ;
 Equivalent evaporation from and at 212 degrees per pound of combustible. [Item 10 (Item 	
5 - Item 6) 1	{ "
(If Items 25, 26, and 27 are not corrected for quality of steam, the fact should be stated.)	'i
• •	1
EFFICIENCY. 8. Calorific value of the dry coal per pound	B.T.U.
9 Calorific value of the combustible per pound	
0. Efficiency of boiler (based on combustible)**	per cent.
1. Efficiency of boiler, including grate (based on dry coal)	1 . "
COST OF EVAPORATION.	
2. Cost of coal per ton of —— lbs. delivered in	1 1
boiler-room	1 S 1
Cost of coal required for evaporating 1000 pounds of water from and at \$12 degrees	1 _ 1

veniently substituted for the expression "Equivalent water evaporated into dry steam from and at 212 degrees," its definition being given in a foot-note.

Held to be the equivalent of 30 lbs. of water evaporated from 100 degrees

Fahr. into dry steam at 70 lbs. gauge-pressure.

** In all cases where the word "combustible" is used, it means the coal without moisture and ash, but including all other constituents. It is the

same as what is called in Europe "coal-dry and free from ash."

Factors of Evaporation,—The table on the following pages was originally published by the author in Trans. A. S. M. E., vol. vi., 1884, under the title, Tables for Facilitating Calculations of Boiler-tests. The table gives the factors for every 3° of temperature of feed-water from 2° to 21°. F., and for every two pounds pressure of steam within the limits of ordinary working steam.pressures.

working steam-pressures.

The difference in the factor corresponding to a difference of 3° temperature of feed is always either .0031 or .0032. For interpolation to find a factor for a feed-water temperature between 82° and 212°, not given in the table, take the factor for the nearest temperature and add or subtract, as the case may be, .0010 if the difference is .0031, and .0011 if the difference is .0032. As in nearly all cases a factor of evaporation to three decimal places is accurate enough, any error which may be made in the fourth decimal place by interpolation is of no practical importance.

The tables used in calculating these factors of evaporation are those given in Charles T. Porter's Treatise on the Richards' Steam-engine Indicator.

The formula is Factor $= \frac{H-h}{h}$ in which H is the state of the state

The formula is Factor $=\frac{H-h}{965.7}$, in which H is the total heat of steam at the observed pressure, and h the total heat of feed-water of the observed temperature.

	Lbs.					·				
Gauge-pressur Absolute pre	res0 +	10 + 25	20 + 35	30 + 45	40 + 55	45 + 60	50 + 65	52 + 67	54 + 69	56 + 71
Feed-water Temperature. FACTORS OF EVAPORATION.										
212° F.	1.0003			1.0197	1.0237					1.0290
206	66	51	1.0212	60	99	1.0817	84	40	46	52
908	1.0129		48 75	91 1.0323	1.0331	80		72 1.0403		84 1.0415
197	60			54	94	1			41	47
194	92	77	88	85	1.0425	48	60	66	72	78
191 188	1.0228		69 1.0400	1.0417	57 88			97 1.0528	1.0503	1.0510
185	86	71	82	80	1	37	54	60		72
182 179	1.0317		68 95	1.0511	51 82				98 1.0629	1.0604
176	80	65	1.0526	74		81	48	54	60	66
178	1.0411		57 89	1.0605 86	45				92 1.0723	1.0729
167	74			68	1.0707			1	54	60
164	1.0505		51	99	88	56	73		86	92
161 158	87 68			1.0730 62					1.0817	1.0823
155	99	84	45	93	83	50	67	78	80	86
152	1.0631		76 1.0808	1.0824 55	64 95				1.0911 42	1.0917
149 146	93		39	87	1.0926			67	78	48 79
148	1.0724		70 1.0901	1.0918 49	58 89					1.1011
197	87	41 72	1.0901	80		1		1.1030	36 67	42 73
184	1.0818	1.0903	64	1.1012	51	69	86	92	98	1.1104
181 128	49 81		95 1.1026	43 74	83 1.1114	1.1100		1.1123	1.1130	36 67
125	1.0912		57	1.1105	45			86	92	98
122	48		. 89	86	76			1.1217	1.1223	1.1229
119 116	1.1005		1.1120	68 99	1.1207			48 79	54 86	60 92
118	. 86		82	1.1230	70	88		1.1810	1.1817	1.1328
107	68 99	53 84	1.1218 45	61 92	1.1301 82	1.1819 50		42 78	48 79	54 85
104	1 1180	1.1215	76	1.1328	63	81	98	1.1404	1.1410	1.1416
101 98	61 92	46 77	1.1307 38	55 86	94 1,1426	1.1412		85 66	41 73	47 79
95	1.1223		. 69	1.1417	57	75	91	97	1.1504	1.1510
92	55	40	1.1400	48	88	1.1506		1.1529	85	41
89 86	86 1.1317	71 1.1402	81 63	79 1.1510	1.1519 50	37 68	53 84	60 91	66 97	72 1.1603
88	48	33	94	41	81	99	1.1616	1.1622	1.1628	84
80 77	79 1.1410	64 95	1.1525 56	73 1.1604	1.1612 44	1.1630	47 78	53 84	59 90	65 96
74	41	1.1526	87	85	75	92	1.1709	1.1715	1.1722	1.1728
71 68	72 1.1504	58 89	1.1618 49	66 97	1.1706 87	1.1723 55	40 71	46 78	53 84	59 90
65	35	1.1620	80	1.1728	68	86		1.1809	1.1815	1.1821
62	66	51	1.1711	59	99	1.1817	83	40	46	52
59 56	97 1.1628	82 1.1718	43 74	90 1.1821	1.1880 61	48 79	64 96	$\frac{71}{1.1902}$	$\frac{77}{1.1908}$	83 1 1914
58	59	44	1.1805	52	92	1.1910	1.1927	83	89	45
50 47	90 1.1721	75 1.1806	36 67	84 1.1915	1.1928 54	41	58 89	64 95	70 1.2001	76 1.2007
44	52	87	98	46	86	72 1.2003	1.2020	1.2026	32	39
41 88	88 1.1814	68 1.1900	1.1929 60	77 1.2008	1.2017 48	84 65	51 82	57 88	64 95	70 1.2101
86	45	81	91	39	79	96	1.2118	1.2119	1.2126	83
88	76	62	1.2022	70	1 2110	1.2128	44	51	57	68

nge-press.,	lbs. 58 +	60 +	69 + 77	64 + 79	66 + 81	68 + 83	70 + 85	73 + 87	74 + 89	76 + 91
ed-water Temp.				FACTO	RS OF	EVAPOR	ATION.			
912° F. 909 906	1.0295 1.0827 58	1.0801 38 64	1. 03 07 88 70	1.0812 44 75	1.0818 49 81	1.0823 55 86	1.0329 60 91	1.0834 65 97	1.0339 70 1.0402	1.0844 75 1.0407
908 200 197 194	90 1.0421 58 84	96 1.0427 58 90	1.0401 83 64 96	1.0407 88 70 1.0501	1.0412 44 75 1.0507	1.0418 49 80 1.0512	1.0428 54 86 1.0517	1.0428 59 91 1.0522	88 65 96 1.0527	38 69 1.0501 82
191 188 185 182	1.0515 47 78 1.0610	1.0521 58 84 1.0615	1.0527 58 90 1.0621	83 64 95 1.0627	88 69 1.0601	43 75 1.0606 87	49 80	54 85 1.0616 48	59 90	64 95
179 176 173 170	1.0010 41 72 1.0704 85	47 78 1.0709 41	52 84 1.0715 46	58 89 1.0721 52	63 95 1.0726 57	69	74	79 1.0711 42 78	1.0716 47 78	89
167 164 161 158	66 98 1.0829 60	72 1.0803 85 66	78 1.0809 40 72	1.08:5 46	1.0820 51 88	94	1.0831 62 93	1.0805 86 67		1.0815 46 77 1.0908
155 153 149 146	92 1.0928 54 85		1.0903 84	1.0909 40 71	1.0914 45 77 1.1008	1.0919 51 82	1.0925 56 87 1.1018	1.0930 61 92	35 66 97	1.0500 40 71 1.1002 34
143 140 187	1.1017 48 79 1.1110	1.1022 54 85 1.1116	1.1028 59 91	84 65 96	89 70	44 76	1.1018 50 81 1.1112 43	55 86 1.1117	1.1029 60 91 1.1122	65 96 1.1127
84 81 28 25	42 78 1.1204	47 79 1.1210	53 84 1.1215	1.1127 59 90 1.1221	64 95 1.1226	1.1201 32	75 1.1206 87	49 80 1.1211 42	54 85 1.1216 47	59 90 1.1221 52
222 19 16 13 10	85 66 98 1.1829 60	41 72 1,1303 84 66	47 78 1.1809 40 71	52 83 1.1815 46 77	58 89 1.1820 51 82	68 94 1.1825 57 88	68 99 1.1331 62 93	73 1.1805 86 67	41 72	46 77
07 04 01 98	91 1.1422 58 85	97 1.1428 59	1.1403 84 65 96	1.1408 89 70 1.1502	1.1414 45 76	1.1419 50 81	1.1424 55 86 1.1518	98 1.1429 60 92	1.1403 84 65 97	1.1408 39 70 1.1502 33
95 92 39	1.1516 47 78 1.1609	1.1521 58 84 1.1615	1.1527 58 89	83 64 95	88 69 1.1600		49 80 1.1611	1.1523 54 85 1.1616	1.1528 59 90 1.1621	64 95 1.1626
36 33 30 7 '4	40 71 1.1702	46 77 1 1708		1.1626 57 88 1.1719			42 78 1.1704 85	47 78 1.1710 41	52 83 1.1715 46	57 88 1.1720 51
'1 8 5	84 65 96 1.1827 58	89 70 1 1802 83	3 8	51 82 1.1813 44	49	55	67 98 1.1829 60	72 1.1803 84 65	77 1.1808 89 70	1.1818 44 75
2 9 6 3 0	58 89 1.1920 51 82	64 95 1.1926 57 88	1.1901 32 63 94	75 1,1906 87 68 99	80 1.1912 43 74 1.2005	86 1.1917 48 79 1.2010	91 1.1922 58 84 1.2015	96 1.1927 58 89 1.2021	1.1901 82 63 94 1.2026	1.1906 37 68 99 1.2031
7 4 1	1.2018 44 76 1.2107	1.2019 50 81 1.2112	1.2025 56 87 1.2118	1.2080 61 93 1.2124	36 67 98 1.2129	41 72	46 78 1.2109 40	52 88 1.2114 45	57 88 1.2119 50	62 98 1.2124 55
8 5 2	1.2107 88 69	1.2112 43 75	49 80	1.2124 55 86	1.2129 60 91	65	71	76	81	86

Gange	ressures 4., 78 +	80 +	82 +	84 +	86 +	88 +	90 +	92 +	84+	86+	* +
Absolute	ures, 93	95	97	99	101	108	105	107	109	111	112
Feed-wa Temp	teri		··				APORATI			-	-
212		1.0858	11.0858				1.0876		1.0006	1,0880	1.0093
209	80	85	90	94	99	1.0403	1.0408	1.0412	1.0416	1.0421	1.0425
206 203	1.0411	1.0416	1.0421	1.0426	1.0430	35 66	39 71	48 75	48 79	52 88	56 88
200	74	79	84	89	93		1.0502			1,0515	1.0619
197	1.0506		1.0515				88	38	42	46	50
194 191	87 69	42 73	47 78		56 87		65 96	69	73 1. 060 5	78 1.0609	82
188		1.0605		1.0614				82	36	40	1.0618 45
185	81	36	41	46			59	63	68	72	76
182	68	68	72		81	86	90	95	99	1.0708	1.0707
179 176	94 1.0725					1.0717	1.0722	1.0726	1.0730 62	85 66	89 70
178	57	62	66	71	75	80	84	89	98	97	1.0801
170	88	93		1.0802			1.0816			1,0829	83
167 164	1.0819 51	1.0884	1.0829	84 65	88		47 78	51 88	56 87	60 91	64 95
161	82	87	92		1.0901			1.0914	1.0018	1,0923	1.0927
158	1.0918		1.0923	1.0927	32	37	41	45	50	54	58
155	45	49	54	59	68	68	78	77	81	85	89
152 149	76 1.1007	81 1.1012	85 1.1017	90 1.1021	95 1.1026	99 1.1030	1.1004 85	1.1008 89	1.1012 48	1,1016 48	1,1021
146	88	48	48	58	57	62	66	70	76	79	83
143	70		79	84	88		97	1.1100			
140	1.1101 82	1.1106	1.1110					88	87	41	46
187 184	68	68	42 73	46 78	51 82	55 87	60 91	64 96	1 1900	73 1,1204	1,1208
181	95	99	1.1204		1.1218	1.1218	1.1222	1.1227	81	85	39
198	1.1226		85 67	40	45 76		53 85	58 89	62	66	71
125 122	57 88	62		71 1.1302				1.1320	98 1.1325	98 1,1329	1.1302
119		1.1824	1.1329	84	88		47	51	56	60	64
116	51	55	60	65	69		78	88	87	91	95
118 110	82 1. 1418	87 1.1418	91 1.1422		1.1401	1.1405	1.1409	1.1414 45	1.1418 49	1,1422	1.1426
107	44	49	54	58	68	67	72	76	80	85	89
104	75	80	85	89	94	99	1.1503	1.1507	1.1519	1,1516	
101 98	1.1506 88	1.1511	1.1516 47		1.1525		84 65	38 70	48 74	47 78	51 82
95	69	74	78	52 83	56 87	61 92			1.1605		1.1618
92	1.1600				1.1619		1.1628	32	86	40	45
89	81	86	41	45	50	54	59	63	67	72	76
86 83	62 98	67 98	72 1.1708	76 1.1707	81 1.1712	85 1,1717	90 1.1721	94 1.1725	1.1730	1,1703	1,1707
80	1.1724		34	89	48	48	52	56	61	65	69
77	56	60	65	70	74	79	88	. 88	85	96	
74 71	87 1 1818	91 1.1828	96 1,1827	1.1801 32	1.1805		1.1814 45	1,1819 50	1,1828 54	1.1827	81 62
68	49	54	58	68	68		77	81	85	89	94
65	80	85	89		99	1.1903	1.1908	1.1912	1.1916		1.1925
62	1.1911			1.1925		84	39	48	47	52	56
59 56	42 73	47 78	83	56 87	61 92	65 96	70 1.2001	74 1 9005	78 1 .20 10	83 1,2014	87 1.2018
58	1.2004	1 2009	1.2014	1.2018	1.2023	1,2028	32	86	41	45	49
50	85		45			59	63	67	. 72	76	80
47 44	66	71 1.2102	1 9107	81 1.2112	85 1.2116	90 1,2121	94 1,2125	98 1,2180	1.2108 84	1,2107 38	1.2111
41	1.8129	88	88		47	52	56	61	65	69	78
88 85	60		69		78	88	87	99	96		1.2204
80 80	91 1, 999 9	96 1.8997	1.2200 81					1,2228 54	1,2227 58	81 62	85 67
-	77.77		. 41	<u> </u>	. **	<u>. =u</u>	. 70		<u></u>	, ,	

lbs	. 100 + Press.	105 +	110 +	115 +	120 +	125 +	130 +	135 +	140 +	145 +	150 -
_	bs. 115.	120	125	130	135	140	145	150	155	160	165
emp.					FACTO	RS OF I	EVAPOR	ATION.			
120	1.039	7 1.0407	1.0417	1.0427	1.0436	1.0445	1.0453	1.0462	1.0470	1.0478	1.048
09	1.042	9 39	49	58	67	76	85		1.0501	1.0509	1.051
06	60			89	99	1.0508	1.0516	1.0525	33	41	4
03	1.052		1.0511	1.0521	1.0530	39 70	48 79	56 87	64 96	1.0604	1.061
77	50	100	1	84	93	1.0602	1.0610	1.0619	1.0627	35	1.001
4	86			1.0615	1.0624	33	42	50	58	66	7
i l	1.0617	1.0627	37	47	56	65	73	82	90	98	1.070
8	49		69	78	87	96	1.0705	1.0718	1.0721	1.0729	1 8
5	80			1.0709	1.0719	1.0727	36	44	53 84	61	4 000
9	1.0715		81 63	41 72	50 81	59 90	67 99	1.0807	1.0815	1.0823	1.080
6	74		94	1.0803	1.0813	1.0821	1.0830	39	47	55	1
	1.0806		1.0825	35	44	53	61	70	78	86	1
0	87		57	66	75	84	98	1.0901	1.0909	1.0917	1.09
7	68		88	97	1.0907	1.0915	1.0924	82	41	49	
1 1	81		1.0919	1.0929	88 69	47 78	55 87	64 95	1.1008	80	1.101
8	65		82	91	1.1000	1.1009	1.1018	1.1026	35	1.1011	1.10
5	0.5		1.1013	1.1023	82	41	49	58	66	74	8
2 1	.1025	35	44	54	63	72	81	89	97	1.1105	1.111
9	56		76	. 85	94	1.1103	1.1112	1,1120	1.1128	36	9
1	87		1.1107	1.1116	1.1126	34 66	43	51	60 91	68	1 10
1	.1118		38 70	48 79	57 88	97	74 1.1206	1.1214	1.1222	1,1230	1.120
	81		1.1201	1.1210	1.1219	1.1228	37	45	53	61	
1	.1212		32	41	51	59	68	76	85	93	1.130
	43	53	63	73	82	91	99	1.1308	1.1316	1.1324	8
1	75		94	1.1304	1.1313	1.1322	1.1331	39	47	55	1
- 1	.1306		1.1326	35	44	53	62	70	78	86	2
	37 68	47 78	57 88	66 97	1.1407	1.1415	93	1.1401	1.1409	1.1417	1.149
	99		1.1419	1.1429	38	47	55	64	72	49 80	8
	.1431	41	50	60	69	78	86	95	1.1503	1.1511	1.15
	62	72	82	91	1.1500	1.1509	1.1518	1.1526	34	42	5
1.	93		1.1518	1.1522	81	40	49	57	65	78	8
1	.1524	84 65	44 75	53 84	62 94	71	80	88	1.1628	1.1605	1.161
1	86		1.1606	1.1616	1.1625	1.1602	1.1611	1.1620	59	36 67	4
1	1618		87	47	56	65	73	82	90	98	1.170
	49	59	68	78	87	96	1.1705	1.1713	1.1721	1.1729	3
1.	80	90	1.1700	1.1709	1.1718	1.1727	86	44	52	60	6
11.	1711	1.1721	31 62	40	49	58	67	1 1904	83	91	4 400
	73	83	93	71 1.1802	1.1812	1.1820	98 1.1829	1.1806	1.1815	1.1823	1.188
1	1804	1.1814	1.1824	34	43	52	60	69	77	85	9
1.	35	45	55	65	74	83	91	1,1900	1.1908	1.1916	1.192
1	67	77	86	96	1.1905	1.1914	1.1922	81	39	47	5
1	98	1.1908	1.1917	1.1927	36	45	54	62	70	78	. 004
1.	1929	39	49	58	67	76	85	93	1.2001	1.2009	1.201
1	91	1.2001	1.2011	1.2020	1.2029	1.2007	1.2016	1.2024	32 63	40 71	47
1	2022	82	42	51	60	69	78	86	94	1.2102	1.211
1	53	63	73	82	91	1.2100	1.2109	1.2117	1.2126	34	4
	84	94	1.2104	1.2113	1.2123	31	40	48	57	65	7
1.	2115	1.2125	85	44	54	63	71	80	88	96	1,220
16	46	56 87	66 97	1 9907	1 9016	1 999	1.2202	1.2211	1.2219	1.2227	3
1	77 2208	1.2219	1.2228	1.2207	1.2216	1.2225	88 64	42 73	50 81	58 89	6 9
	40	50	59	69	78	87	95	1.2304	1.2312	1.2320	1.232
	71	81	90	1.2300		1.2318	1.2326	35	43	51	

STRENGTH OF STEAM-BOILERS. VARIOUS RULES FOR CONSTRUCTION.

There is a great lack of uniformity in the rules prescribed by different writers and by legislation governing the construction of steam-boilers In the United States, boilers for merchant vessels must be constructed ac-cording to the rules and regulations prescribed by the Board of Supervising Inspectors of Steam Vessels; in the U. S. Navy, according to rules of the Navy Department, and in some cases according to special acts of Congress. On land, in some places, as in Philadelphia, the construction of boilers is governed by local laws; but generally there are no laws upon the subject, and boilers are constructed according to the idea of individual engineers and boiler-makers. In Europe the construction is generally regulated by string element inspection laws. The rules of the U.S. Supervising Inspectors of Steam-vessels, the British Lloyd's and Board of Trade, the Freuch Bureau Veritas, and the German Lloyd's are ably reviewed in a paper by Nelson Foley, M. Inst. Naval Architects, etc., read at the Chicago Engineering Congress, Division of Marine and Naval Engineering. From this paper the following notes are taken, chiefly with reference to the U.S. and British rules: (Abbreviations.—T. S., for tensile strength; El., elongation; Contr., con-

traction of area.)

Hydraulic Tests.—Board of Trade, Lloyd's, and Bureau Veritas.—

Twice the working pressure.

United States Statutes.—One and a half times the working pressure.

Mr. Foley proposes that the proof pressure should be 1½ times the work-

ing pressure + one atmosphere

Established Nominal Factors of Safety. -Board of Trade, 4.5 for a boiler of moderate length and of the best construction and work-

manship.

Lloyd's.—Not very apparent, but appears to lie between 4 and 5.

Lloyd's.—Indefinite, because the strength of the joint is not considered, except by the broad distinction between single and double. riveting.

Bureau Veritas: 4.4.
German Lloyd's: 5 to 4.65, according to the thickness of the plates.
Material tor Eliveting.—Board of Trade.—Tensile strength of rivet bars between 26 and 30 tons, el. in 10" not less than 25%, and contr. of

area not less than 50%.

Lloyd's.—T. S., 26 to 80 tons; el. not less than 20% in 8". The material must stand bending to a curve, the inner radius of which is not greater than 1% times the thickness of the plate, after having been uniformly heated ta a low cherry-red, and quenched in water at 82° F.

United States Statutes.—No special provision.

Bules Connected with Riveting.—Board of Trade.—The shearing resistance of the rivet steel to be taken at 23 tons per square inch, 5 to

ing resistance of the river steer to be taken at 25 tons per square inco, to be used for the factor of safety indepen jently of any addition to this factor for the plating. Rivets in double shear to have only 1.75 times the single section taken in the calculation instead of 2. The diameter must not be less than the thickness of the plate and the pitch never greater than 8½". The thickness of double butt-straps (each) not to be less than 5% the thickness of the plate; single butt-straps not less than 9/8.

Distance from centre of rivet to edge of hole = diameter of rivet × 11/4.

Distance between rows of rivets

 $= 2 \times \text{diam.}$ of rivet or $= [(\text{diam.} \times 4) + 1] + 2$, if chain, and

$$= \frac{\sqrt{[(\text{pitch} \times 11) + (\text{diam}, \times 4)]} \times (\text{pitch} + \text{diam}, \times 4)}{10} \text{ if zigzag.}$$

Diagonal pitch = (pitch \times 6 + diam. \times 4) + 10. Lloyd's.—Rivets in double shear to have only 1.75 times the single section taken in the calculation instead of 2. The shearing strength of rivet steel to be taken at 85% of the T. S. of the material of shell plates. In any case where the strength of the longitudinal joint is satisfactorily shown by experiment to be greater than given by the formula, the actual strength may be taken in the calculation.

United States Statutes .- No rules.

Material for Cylindrical Shells Subject to Internal Pressure.—Board of Trade.—T. S. vetween 27 and 32 tons. In the normal con-'nn, el. not less than 18% in 10", but should be about 25%; if annealed, not 188 than 20%. Strips 2" wide should stand bending until the sides are arallel at a distance from each other of not more than three times the

late's thickness.

Lloyd's.—T. S. between the limits of 26 and 30 tons per square inch. El. ot less than 20% in 8". Test strips heated to a low cherry-red and plunged to water at 82° F. must stand bending to a curve, the inner radius of hich is not greater than 1½ times the plate's thickness.

U. S. Statutes.—Plates of ½" thick and under shall show a contr. of not so than 50%; when over ½" and up to ¾", not less than 45%; when over

, not less than 40%.

Mr. Foley's comments: The Board of Trade rules seem to indicate a steel too high T. S. when a lower and more ductile one can be got: the lower asile limit should be reduced, and the bending test might with advantage made after tempering, and made to a smaller radius. Lloyd's rule for ality seems more satisfactory, but the temper test is not severe. The nited States Statutes are not sufficiently stringent to insure an entirely tisfactory material.

Wir. Foley suggests a material which would meet the following: 25 tons ver limit in tension; 25% in 8" minimum elongation; radius for bending after tempering = the plate's thickness.

shell-plate Formulæ. – Board of Trade:
$$P = \frac{T \times B \times t \times 2}{D \times F}$$
.

) = diameter of boiler in inches;

= working-pressure in lbs, per square inch;

! = thickness in inches ;

? = percentage of strength of joint compared to solid plate;

'= tensile strength allowed for the material in lbs. per square inch; '= a factor of safety, being 4.5, with certain additions depending on method of construction.

$$loyd's: P = \frac{C \times (t-2) \times B}{D}.$$

= thickness of plate in sixteenths; B and D as before; C = a constant ending on the kind of joint.

'hen longitudinal seams have double butt-straps, C=20. When longinal seams have double butt-straps of unequal width, only covering on side the reduced section of plate at the outer line of rivets, C = 19.5. hen the longitudinal seams are lap-jointed, C = 18.5. S. Statutes.—Using same notation as for Board of Trade,

$$P=rac{t imes 2 imes T}{D imes 6}$$
 for single-riveting; add 20% for double-riveting;

re T is the lowest T. S. stamped on any plate. \cdot Foley criticises the rule of the United States Statutes as follows: The ignores the riveting, except that it distinguishes between single and sle, giving the latter 20% advantage; the circumferential riveting or of seam is altogether ignored. The rule takes no account of workmanor method adopted of constructing the joints. The factor, one sixth, ly covers the actual nominal factor of safety as well as the loss of ight at the joint, no matter what its percentage; we may therefore iss it as unsatisfactory.

ules for Flat Plates.—Board of Trade; $P = \frac{C(t+1)^2}{S-6}$.

P =working pressure in lbs. per square inch;

S = surface supported in square inches;t =thickness in sixteenths of an inch;

C = a constant as per following table:

125 for plates not exposed to heat or flame, the stays fitted with nuts and washers, the latter at least three times the diameter of the stay and % the thickness of the plate; 87.5 for the same condition, but the washers % the pitch of stays in

diameter, and thickness not less than plate;

of for the same condition, but doubling plates in place of washers, the
width of which is % the pitch and thickness the same as the plate;

12.5 for the same condition, but the stays with nuts only;

5 when exposed to impact of heat or flame and steam in contact with the plates, and the stays fitted with nuts and washers three times th diameter of the stay and % the plate's thickness:

C=67.5 for the same condition, but stays fitted with nuts only: C=100 when exposed to heat or flame, and water in contact with the plates. and stays screwed into the plates and fitted with nuts;

C = 66 for the same condition, but stays with riveted heads.

U. S. Statutes.—Using same notation as for Board of Trade, $P = \frac{C \times P}{C}$ where p =greatest pitch in inches, P and t as above;

U = 112 for plates 7/16" thick and under, fitted with screw stay-bolts riveted over, screw stay-bolts and nuts, or plain bolt fitted with single nut and socket, or riveted head and socket;

= 120 for plates above 7/16", under the same conditions;

C = 140 for flat surfaces where the stays are fitted with nuts inside

and outside: C = 200 for flat surfaces under the same condition, but with the addition of a washer riveted to the plate at least 1/2 plate's thick-ness, and of a diameter equal 10% of the pitch of the stay-bolts.

N.B.—Plates fitted with double angle-irons and riveted to plate, with leaf at least 1/4 the thickness of plate and depth at least 1/4 of pitch, would be allowed the same pressure as determined by formula for plate with washer riveted on.

N.B.—No brace or stay-bolt used in marine boilers to have a greater pitch

than 104" on fire-boxes and back connections.

Certain experiments were carried out by the Board of Trade which showed that the resistance to bulging does not vary as the square of the plate's thickness. There seems also good reason to believe that it is not inversely as the square of the greatest pitch. Bearing in mind, says Mr. Foley, that mathematicians have signally failed to give us true theoretical foundations for calculating the resistance of bodies subject to the simplest forms of stresses, we therefore cannot expect much from their assistance in the matter of flat plates.

The Board of Trade rules for flat surfaces, being based on actual experiment, are especially worthy of respect; sound judgment appears also to

have been used in framing them.

Furnace Formule, -Board of Trade, -Long Furnaces. -

 $C \times t^{3}$ $P = \frac{\sqrt{1 + 1}}{(L+1) \times D}$, but not where L is shorter than (11.5t – 1), at which length

the rule for short furnaces comes into play. P = working-pressure in pounds per square inch; t = thickness in inches; D = outside diameter in inches; L = length of furnace in fact up to 10 ft.;

C = a constant, as per following table, for drilled holes: C = 99,000 for welded or butt-jointed with single straps, double-

rivated; C = 88,000 for butts with single straps, single-riveted; C = 99,000 for butts with double straps, single-riveted.

Provided always that the pressure so found does not exceed that given by the following formulæ, which apply also to short furnaces ;

$$P = \frac{C \times t}{D}$$
 for all the patent furnaces named;

$$P = \frac{C \times t}{3 \times D} \left(5 - \frac{L \times 12}{67.5 \times t} \right)$$
 when with Adamson rings.

$$C = 8,800 \text{ for plain furnaces;}$$

$$C = 14,000 \text{ for Fox; minimum thickness 5/16", greatest 5%"; plain part 1000 to exceed 6" in langth;$$

not to exceed 6'' in length; C = 13,500 for Morison; minimum thickness 5/16'', greatest 56''; plain

part not to exceed 6" in length;
C = 14,000 for Purves-Brown; limits of thickness 7/16" and %"; plain
part 9" in length;

C = 8.800 for Adamson rings; radius of flange next fire 114".

U. S. STATUTES .- Long Furnaces. - Same notation.

$$P = \frac{89,600 \times t^2}{L \times D}, \text{ but } L \text{ not to exceed 8 ft.}$$

M.B.-If rings of wrought iron are fitted and riveted on properly around and to the flue in such a manner that the tensile stress on the rivets shall ot exceed 6000 lbs. per sq. in., the distance between the rings shall be taken the length of the flue in the formula.

Furnaces, Plain and Patent.-P, as before, when not 8 ft. Short $89.600 \times t^2$

$$P = \frac{\frac{89,000 \times t^2}{L \times D}}{D};$$

C=14,000 for Fox corrugations where D= mean diameter; C=14,000 for Purves-Brown where D= diameter of flue; C=5677 for plain flues over 16" diameter and less than 40", when not over 8 ft. lengths.

Mr. Foley comments on the rules for long furnaces as follows: The Board of Trade general formula, where the length is a factor, has a very limited range indeed, vis., 10 ft. as the extreme length, and 125 thicknesses — 12", Ox t2

The original formula, $P = \frac{U \wedge V^2}{L \times D}$, is that of Sir W. as the short limit.

Fairbairn, and was, I believe, never intended by him to apply to short furnaces. On the very face of it, it is apparent, on the other hand, that if it is true for moderately long furnaces, it cannot be so for very long ones. We are therefore driven to the conclusion that any formula which includes

simple L as a factor must be founded on a wrong basis.

With Mr. Traill's form of the formula, namely, substituting (L+1) for L, the results appear sufficiently satisfactory for practical purposes, and in-deed, as far as can be judged, tally with the results obtained from experi-ment as nearly as could be expected. The experiments to which I refer were six in number, and of great variety of length to diameter; the actual

were six in number, and of great variety of length to diameter; the actual factors of safety rauged from 4.4 to 6.2, the mean being 4.78, or practically 5. It seems to me, therefore, that, within the limits prescribed, the Board of Trade formula may be accepted as suitable for our requirements. The United States Statutes give Faribairn's rule pure and simple, except that the extreme limit of length to which it applies is fixed at 8 feet. As far as can be seen, no limit for the shortest length is prescribed, but the rules to me are by no means clear, flues and furnaces being mixed or not well distinguished.

That real for **That multitude** **That

Material for Stays.—The qualities of material prescribed are as

follows:

Board of Trade.—The tensile strength to lie between the limits of 27 and 32 tons per square inch, and to have an elongation of not less than 20% in 10". Steel stays which have been welded or worked in the fire should not be used.

Lloyd's.—36 to 30 ton steel, with elongation not less than 30% in 8".

U. S. Statutes.—The only condition is that the reduction of area must not be less than 40% if the test bar is over 3/" diameter.

Loads allowed on Stays.—Board of Trade.—9000 lbs. per square inch is allowed on the net section, provided the tensile strength ranges from

27 to 32 tons. Steel stays are not to be welded or worked in the fire.

Lloyd's.—For screwed and other stays, not exceeding 1½", diameter effective, 8000 lbs. per square inch is allowed; for stays above 1½", 9000 lbs. No stays are to be welded.

U. S. Statutes.—Braces and stays shall not be subjected to a greater stress

O. 3. States.—Fraces and such years and to be subjected to a greater stress than 600 lbs. per square inch.

[Rankine, S. E., p. 459, says: "The iron of the stays ought not to be exposed to a greater working tension than 3000 lbs. on the square inch, in order to provide against their being weakened by corrosion. This amounts to making the factor of safety for the working pressure about 20." It is evident, however, that an allowance in the factor of safety for corrosion may reasonably be decreased with increase of diameter. W. K.]

Girders.—Board of Trade. $P = \frac{C \times d^2 \times t}{(W - p)D \times L}$. P = working pressure in ibs. per sq. in.; W = width of flame-box in inches; L = length of girder in inches; p = pitch of bolts in inches; D = distance between girders from centre to centre in inches; d = depth of girder in inches; t = thickness of sum of same in inches; D = a constant = 6600 for 1 bolt, 9900 for 2 or 3 bolts, and 11,220 for 4 bolts.

Lloyd's.—The same formula and constants, except that C=11,000 for 4 or 5 bolts, 11,550 for 6 or 7, and 11,880 for 8 or more.

U. S. Statutes.—The matter appears to be left to the designers.

 $P = \frac{t(D-d) \times 20,000}{W \times D}. \quad D = \text{least}$ Tube-Flates. - Board of Trade.

horizontal distance between centres of tubes in inches; d= inside diameter of ordinary tubes; t= thickness of tube-plate in inches; W= extreme width of combustion-box in inches from front tube-plate to back of firebox, or distance between combustion-box tube plates when the boiler is double-ended and the box common to both ends.

double-ended and the box common to both ends.

The crushing stress on tube-plates caused by the pressure on the flame-box top is to be limited to 10,000 lbs. per square inch.

Material for Tubes.—Mr. Foley proposes the following: If iron, the quality to be such as to give at least 22 tons per square inch as the minimum tensile strength, with an elongation of not less than 15% in 8". If steel, the elongation to be not less than 26% in 8" for the material before being rolled into strips; and after tempering, the test bar to stand completely closing together. Provided the steel welds well, there does not seem to be any object in providing tensile limits ject in providing tensile limits.

The ends should be annealed after manufacture, and stay-tube ends should

be annealed before screwing.

Holding-power of Boiler-tubes.—Experiments made in Washington Navy Yard show that with 21/4 in. brass tubes in no case was the holdingpower less, roughly speaking, than 6000 lbs., while the average was upwards of 20,000 lbs. It was further shown that with these tubes nuts were superfluous, quite as good results being obtained with tubes simply expanded into the tube-plate and fitted with a ferrule. When nuts were fitted it was shown that they drew off without injuring the threads.

In Messrs, Yarrow's experiments on iron and steel tubes of 2" to 2½4" diameter the first 5 tubes gave way on an average of 23,740 lbs., which would appear to be about 3½ the ultimate strength of the tubes themselves. In all these cases the hole through the tube plate was parallel with a sharp edge to it, and a ferrule was driven into the tube.

Tests of the next 5 tubes were made under the same conditions as the first 5, with the exception that in this case the ferrule was omitted, the tubes being simply expanded into the plates. The mean pull required was 15,270 lbs., or considerably less than half the ultimate strength of the tubes.

or considerably less than half the utilinate strength of the tubes. Effect of beading the tubes, the holes through the plate being parallel and ferrules omitted. The mean of the first 8, which are tubes of the same kind, gives 26,876 lbs. as their holding-power, under these conditions, as compared with 23,740 lbs. for the tubes fitted with ferrules only. This high figure is, however, mainly due to an exceptional case where the holding-power is greater than the average strength of the tubes themselves.

power is greater than the average strength of the tubes themselves.

It is disadvantageous to cone the hole through the tube-plate unless its sharp edge is removed, as the results are much worse than those obtained with parallel holes, the mean pull being but 16.081 lbs., the experiments being made with tubes expanded and ferruled but not beaded over.

In experiments on tubes expanded into tapered holes, beaded over and fitted with ferrules, the net result is that the holding-power is, for the size experimented on, about ¾ of the tensile strength of the tube, the mean pull being 28,797 lbs.

With tubes expanded into tapered holes and simply beaded over, better results were obtained than with ferrules; in these cases, however, the sharp edge of the hole was rounded off, which appears in general to have a good

effect.

In one particular the experiments are incomplete, as it is impossible to reproduce on a machine the racking the tubes get by the expansion of a boiler as it is heated up and cooled down again, and it is quite possible, therefore, that the fastening giving the best results on the testing-machine may not prove so efficient in practice.

N.B.—It should be noted that the experiments were all made under the cold condition so that reference should be made with causing the circums.

cold condition, so that reference should be made with caution the circumstances in practice being very different, especially when there is scale on the tube-plates, or when the tube-plates are thick and subject to intense

Iron versus Steel Boller-tubes. (Foley.) — Mr. Blechynden prefers iron tubes to those of steel, but how far he would go in attributing the leaky-tube defect to the use of steel tubes we are not aware. It appears, however, that the results of his experiments would warrant him in going a considerable distance in this direction. The test consisted of heating and cooling two tubes, one of wrought iron and the other of steel. Both tubes were 2% in. in diameter and .16 in. thickness of metal. The tubes were put in the same furnace, made red-hot, and then dipped in water. The length was gauged at a temperature of 46° F.

This operation was twice repeated, with results as follows:

Steel.	Iron.
55,495 in.	55.495 in.
.052 ''	.048 **
.0000067	.0000063
.007 in.	.003 in.
.081 in.	.004 in.
.017 in.	.006 in.
.055 in.	.018 in.
	55.495 in. .052 .0000067 .007 in. .081 in. .017 in.

Mr. A. C. Kirk writes: That overheating of tube ends is the cause of the leakage of the tubes in boilers is proved by the fact that the ferrules at present used by the Admiralty prevent it. These act by shielding the tube ends from the action of the flame, and consequently reducing evaporation, and so allowing free access of the water to keep them cool.

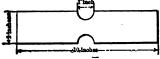
Although many causes contribute, there seems no doubt that thick tube-

plates must bear a share of causing the mischief.

Rules for Construction of Bollers in Merchant Vessels in the United States. Extracts from General Rules and Regulations of the Board of Supervising

Inspectors of Steam-vessels (as amended 1898).)

Tensile Strength of Plate. (Section 3.)—To ascertain the tensile strength and other qualities of iron plate there shall be taken from each sheet to be used in shell or other

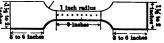


parts of boiler which are subject to tensile strain a test piece prepared in form according to the following diagram, viz.: 10 inches in length, inches in width, cut out in the centre in the manner indicated.

To ascertain the tensile strength

and other qualities of steel plate, there shall be taken from each sheet to be used in shell or other parts of boiler which are subject to tensile strain a testsiece prepared in form according to the following diagram:

The straight part in centre shall o 9 inches in length and 1 inch in vidth, marked with light prickounch marks at distances 1 inch part, as shown, spaced so as to ive 8 inches in length.



The sample must show when ested an elongation of at least 25% in a length of 2 in. for thickness up to 4 in., inclusive; in a length of 4 in. for over ½ to 7/16, inclusive; in a angth of 6 in., for all plates over 7/16 in. and under 1½ in. thickness.

The reduction of area shall be the same as called for by the rules of the

loard. No plate shall contain more than .06% of phosphorus and .04% of

ulphur.

The samples shall also be capable of being bent to a curve, of which the ner radius is not greater than 1½ times the thickness of the plates after awing been heated uniformly to a low cherry-red and quenched in water 682° F.

I SZ F.

[Prior to 1894 the shape of test-piece for steel was the same as that for tron, iz., the grooved shape. This shape has been condemned by authorities on trength of materials for over twenty years. It always gives results which re too high, the error sometimes amounting to 25 per cent. See pages 242, 18, ante; also, Strength of Materials, W. Kent, Van N. Science Series No. 41, and Powerstee on Wayner's row and Chein Cebbea. nd Beardslee on Wrought-iron and Chain Cables.]

Ductility. (Section 6.)—To ascertain the ductility and other lawful ualities, iron of 45,000 lbs. tensile strength shall show a contraction of area f 15 per cent, and each additional 1000 lbs. tensile strength shall show 1 er cent additional contraction of area, up to and including 55,000 tensile rength. Iron of 55,000 tensile strength and upwards, showing 25 per cent eduction of area, shall be deemed to have the lawful ductility. All steel late of 1/4 inch thickness and under shall show a contraction of area of not as than 50 per cent. Steel plate over 1/4 inch in thickness, up to 3/4 inch in

thickness, shall show a reduction of not less than 45 per cent. All steel place over 34 inch thickness shall show a reduction of not less than 40 per cent. Bumped Heads of Boilers, (Section 17 as amended 1894.)—Pressure Allored on Bumped Heads.—Multiply the thickness of the plate by one sixth of the tensile strength, and divide by six tenths of the radius to which head is bumped, which will give the pressure per square inch of steam allowed.

Presure Allowable for Concaved Heads of Boilers.—Multiply the pressure per square inch allowable for bumped heads attached to boilers or drums convexly, by the constant 6, and the product will give the pressure per square inch allowable in concaved heads.

The pressure on unstayed flat-heads on steam-drums or shells of boilers, when flanged and made of wrought iron or steel or of cast steel,

or boilers, when hanged and made or wrought from or steel or of cast steel, shall be determined by the following rule:

The thickness of plate in inches multiplied by one sixth of its tensile strength in pounds, which product divided by the area of the head in square inches multiplied by 0.9 will give pressure per square inch allowed. The material used in the construction of flat-heads when tensile strength has not been officially determined shall be deemed to have a tensile strength of 45,000 lbs.

Table of Pressures allowable on Steam-boilers made of Hiveted Iron or Steel Plates.

(Abstract from a table published in Rules and Regulations of the U.S. Board of Supervising Inspectors of Steam-vessels.)

Plates 1/2 inch thick. For other thicknesses, multiply by the ratio of the thickness to 1/4 inch.

, o	Stre	Tensile	55,000 Tensile Strength.			Tensile ngth.		Tensile	70,000 Tensile Strength.	
Diameter Boiler, ins	Pressure.	20% Additional.	Pressure. 20% Additional.		Preseure.	20% Additional.	Pressure.	20% Additional.	Pressure.	20% Additional.
40 42 44 46 48 54 66 72	115.74 109.64 104.16 99.2 94.69 90.57 86.8 77.16 69.44 68.18 57.87	131.56 124.99 119.04 118.62 108.68 104.16 92.59 88.32 75.75 69.44	127.31 120.61 114.58 109.12 104.16 99.63 95.48 84.87 76.38 69.44 68.65	144.73 187.49 130.94 124.99 119.55 114.57 101.84 91.65 83.32 76.88	188.88 181.57 125 119.04 113.68 108.69 104.16 92.59 83.83 75.75 69.44	124.99 111.10 99.99 90.90 83.32	150.46 142.54 135.41 128.96 123.1 117.75 112.84 100.3 90.27 82.07 75.22	180.55 171.04 162.49 154.75 147.72 141.8 135.4 120.36 108.32 98.48 90.26	162.03 153.5 145.83 138.88 132.56 126.8 121.52 108.02 97.22 88.37 81.01	194 43 184 20 174 99 166 85 159 07 152 16 145 82 129 62 116 66 106 04 97 21
78 84 90 96	58.41 49.6 46.29 48.4	64.09 59.52 55.44 58.08	58.76 54.56 50.92 47.74	70.5 65.47 61.1 57.28	64.4 59.52 55.55 52.08	76.92 71.42 66.66 62.49	69.44 64.48 60.18 56.42	88.82 77.37 72.21 67.67	74.78 69.44 64.81 60.76	89.73 88.32 77.77 72.91

The figures under the columns headed "pressure" are for single-riveted bilers. Those under the columns headed "20% Additional" are for doubleboilers. riveted.

U. S. RULE FOR ALLOWABLE PRESSURES.

The pressure of any dimension of boilers not found in the table annexed

The pressure or any dimension of boners not found in the control of the to these rules must be ascertained by the following rule:

Multiply one sixth of the lowest tensile strength found stamped on any plate in the cylindrical shell by the thickness (expressed in inches or parts of an inch) of the thinnest plate in the same cylindrical shell, and divide by the radius or half diameter (also expressed in inches), the quotient will be the pressure allowable per square inch of surface for single-riveting, the which add twenty per centum for double-riveting when all the rivet-holes in the shell of such boller have been "fairly drilled" and no part of such hole has been punched.

The author desires to express his condemnation of the above rule, and of

the tables derived from it, as giving too low a factor of safety. (See also miticism by Mr. Foley, page 701, ante.)

If P_b = bursting-pressure, t = thickness, T = tensile strength, c = coefacient of strength of riveted joint, that is, ratio of strength of the joint to that of the solid plate, d = diameter, $P_0 = \frac{2tTc}{d}$, or if c be taken for doubleriveting at 0.7, then $P_b = \frac{1.4tT}{2}$

By the U. S. rule the allowable pressure $P_{\alpha} = \frac{1/6tT}{1/6d} \times 1.90 = \frac{0.4tT}{d}$; whence Pb = 8.8Pa; that is, the factor of safety is only 3.5, provided the "tensile trength found stamped in the plate" is the real tensile strength of the naterial. But in the case of iron plates, since the stamped T.8. is obtained rom a grooved specimen, it may be greatly in excess of the real T.8., which vould make the factor of safety still lower. According to the table, a boiler oin diam, ½ in. thick, made of iron stamped 60,000 T.8., would be licensed o carry 150 lbs. pressure if double-riveted. If the real T.8. is only \$0,000 lbs. he calculated hursting-strength would be he calculated bursting-strength would be

$$P = \frac{2tTc}{d} = \frac{2 \times 50,000 \times .25 \times .70}{40} = 487.5 \text{ lbs.}$$

nd the factor of safety only 487.5 + 150 = 2.91!

The author's formula for safe working-pressure of externally-fired boilers rith longitudinal seams double-riveted, is $P = \frac{14000t}{d}$; $t = \frac{Pd}{14000}$; P = gauge

ressure in lbs. per sq. in.; t = thickness and d = diam. in inches.This is derived from the formula $P = \frac{2tTc}{fd}$, taking c at 0.7 and f = 5 for teel of 50,000 lbs. T.S., or 6 for 60,000 lbs. T.S.; the factor of safety being icreased in the ratio of the T.S., since with the higher T.S. there is greater anger of cracking at the rivet-holes from the effect of punching and rivetig and of expansion and contraction caused by variations of temperature, or external shells of internally-fired boilers, these shells not being exposed to the fire, with river-holes drilled or reamed after punching, a lower factor I safety and steel of a higher T.S. may be allowable.

If the T.S. is 60,000, a working pressure $P = \frac{16000t}{t}$ would give a factor of **ifety of 5.25**.

The following table gives safe working pressures for different diameters shell and thicknesses of plate calculated from the author's formula.

afe Working Pressures in Cylindrical Shells of Hollers, Tanks, Pipes, etc., in Pounds per Square Inch.

Longitudinal seams double-riveted. (Calculated from formula $P = 14,000 \times \text{thickness} + \text{diameter.}$)

Inch.	Diameter in Inches.										
an Ibths of	94	80	86	38	40	42	44	46	48	50	52
1 2 3	36.5	29.2	24.8	23.0	21.9	20.8	19.9	19.0	18.2	17.5	16.8
2	72.9	58.3	48.6	46.1	43.8	41.7	39.8	38.0	36.5	25.0	33.7
3	109.4	87.5	72.9	69.1	65.6	62.5	59.7	57.1	54.7	52.5	50.5
4	145.8	116.7	97.2	93.1	87.5	88.8	79.5	76.1	72.9	70.0	67,3
5	182.3	145.8	121.5	115.1	109.4	104.2	99.4	95.1	91.1	87.5	84.1
6	218.7	175.0	145.8	138.2	131.3	125.0	119.3	114.1	109.4	105.0	101.0
7	255.2	204.1	170.1	161.2	158.1	145.9	139.2	133.2	127.6	122.5	117.8
8	291.7	283.3	194.4	184.2	175.0	166.7	159.1	152.2	145.8	140.0	134.6
4 5 6 7 8 9	328.1	262.5	218.8	207.2	196.9	187.5	179.0	171.2	164.1	157.5	151.4
ŏ	364.6	291.7	243.1	230.3	218.8	208.3	198.9	190.2	182.3	175.0	168.3
1	401.0	320.8	267.4	253.3	240.6	229.2	218.7	209.2	200.5	192.5	185.1
9	437.5	350.0	291.7	276.3	262.5	250.0	238.6	228.3	218,7	210.0	201.9
2 3 4	473.9	379.2	316.0	299.3	284.4	270.9	258.5	247.3	337.0	227.5	218.8
2	410.4	408.3	340.3	322.4	806.3	291.7	278.4	266.3	255.2	245.0	235.6
5	546.9	437.5	364.6	345.4	328.1	312.5	298 8	285.3	273.4	266.5	252.4
6	588.3	466.7	388.9	368.4	350.0	833.3	318.2	304.4	291.7	280.0	269.2

Thickness in 16thsof an Inch.	Diameter in Inches.											
This is	54	60	66	72	78	84	90	96	102	108	114	120
1 2 3 4 5 6 7 8	16.2 32.4 48.6 64.8 81.0 97.2 113.4 129.6 145.8	29.2 43.7 58.8 72.9 87.5 102.1	89.8 53.0 66.8 79.5 92.8 106.1	12.2 24.3 86.5 48.6 60.8 72.9 85.1 97.2 109.4	11.2 22.4 33.7 44.9 56.1 67.3 78.5 89.7	20.8 31.3 41.7 52.1 62.5 72.9 83.3	9.7 19.4 29.2 38.9 48.6 58.3 68.1 77.8 87.5	68.8 72.9	25.7 84.3 42.9 51.5 60.0 68.6	40.5 48.6 56.7 64.8	7.7 15.4 23.0 36.7 38.4 46.1 53.7 61.4 69.1	7.3 14.6 21.9 29.2 36.5 43.8 51.0 58.3 65.6
10 11 12 13 14 15 16	162.0 178.2 194.4 210.7 226.9 248.1 259.3	145.8 160.4 175.0 189.6 204.2 218.7 233.8	132.6 145.8 159.1 172.4	121.5 188.7 145.8 58.0 170.1 182.3 194.4	112.5 123.4 134.6 145.8 157.1 168.3	104.2 114.6 125.0 135.4 145.8 156.8	97.2 106.9 116.7 126.4 136.1 145.8	91.1 100.8 109.4 118.5 127.6 136.7	85.8	81.0 89.1 97.2 105.8 118 4 121.5	76.8 84.4 92.1 99.8 107.5 115.1	72.9 80.2 87.5 94.8 102.1 109.4

Rules governing Inspection of Boilers in Philadelphia.

In estimating the strength of the longitudinal seams in the cylindrical shells of boilers the inspector shall apply two formulæ, A and B:

Area of hole filled by rivet \times No. of rows of rivets in seam \times shear-

ing strength of rivet pitch of rivets x thickness of sheet x tensile strength of sheet percentage of strength of the rivets in the seam.

Take the lowest of the percentages as found by formulæ A and B and apply that percentage as the "strength of the seam" in the following formula C, which determines the strength of the longitudinal seams:

Thickness of sheet in parts of inch × strength of seam as obtained by formula A or B × ultimate strength of iron stamped on plates internal radius of boiler in inches × 5 as a factor of safety

safe working pressure.

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TABLE OF PROPORTIONS AND SAFE WORKING PRESSURES WITH FORMULÆ A AND C, @ 50,000 LBS., T.S.

Diameter of rivet. Diameter of rivet-hole. Pitch of rivets. Strength of seam, \$\mathbf{x}\$. Thickness of plate.	56" 11/16" 2" .656 14"	11/16 34 2 1/16 .686 5/16	18/16 21/4 .62 3/6	13/16 78 2 3/16 .60 7/16	% 15/16 21/4 .58
Diameter of boiler, in	Safe Wor	king Press Si	ure with ngle-rivet	Longitudin ed.	al Seams
24	187	165	198	220	242
30 82	109	132	154	176	194
89	102	124	144	165	182
84 i	96	117	186	155	171
86 88	91	110	129	147	161
88	86	104	122	189	153
40	82	99	116	183	145
- ii	74	91	105	120	182
48	74 68	83	96	110	121
44 48 54	ÃÕ :	78	86	98	107
ŏŏ l	60 55	73 66	86 77	98 88	97

Diameter of rivet Diameter of rivet-hole Pitch of rivets Strength of seam, \$\frac{1}{2}\$ Thickness of plate	5%" 11/16" 3" .77 14"	11/16 34 31/6 .78 5/16	34 13/16 314 .75 36	13/16 7/8 85/6 .74 7/16	76 15/16 816 .78 15
Diameter of boiler, in	Safe Wor		ure with I ouble-rivet		al Seams,
24	160	198	235	269	305
80	127	158	188	215	248
32	119	148	176	202	228
84	112	140	166	190	215
36	106	132	156	179	203
38	101	125	148	170	192
40	96	119	141	161	183
44	87	108	128	147	166
48	79	99	118	135	152
54	70	88	104	120	135
60	64	79	94	108	122

Flues and Tubes for Steam-boilers.—(From Rules of U. S. Supervising Inspectors. Steam-pressures per square inch allowable on riveted and lap-welded flues made in sections. Extract from table in Rules of U. S. Supervising Inspectors.)

T= least thickness of material allowable, D= greatest diameter in inches, P= allowable pressure. For thickness greater than T with same diameter P is increased in the ratio of the thickness.

For diameters not over 10 inches the greatest length of section allowable is 5 feet; for diameters 10 to 23 inches, 3 feet; for diameters 23 to 40 inches, 30 inches. If lengths of sections are greater than these lengths, the allowable pressure is reduced proportionately.

The U. S. rule for corrugated flues, as amended in 1894, is as follows: Rule II, Section 14. The strength of all corrugated flues, when used for furnaces or steam chimneys (corrugation not less than 1½ inches deep and not exceeding 8 inches from centres of corrugation), and provided that the plain parts at the ends do not exceed 6 inches in length, and the plates are not less than 5/16 inch thick, when new corrugated, and practically true circles, to be calculated from the following formula:

$$\frac{14,000}{D} \times T = \text{pressure.}$$

T = thickness, in inches: D = mean diameter in inches.

Ribbed Flues.—The same formula is given for ribbed flues, with rib projections not less than 1% inches deep and not more than 9 inches apart.

Flat Stayed Surfaces in Steam-boilers.—Rule II., Section 6, of the rules of the U. S. Supervising Inspectors provides as follows:

No braces or stays hereafter employed in the construction of boilers shall be allowed a greater strain than 6000 lbs. per square inch of section.

Clark, in his treatise on the Steam-engine, also in his Pocket-book, gives the following formula: p=407ts+d, in which p is the internal pressure in pounds per square inch that will strain the plates to their elastic limit, t is the thickness of the plate in inches, d is the distance between two rows of stay-bolts in the clear, and s is the tensile stress in the plate in tons of 2240 lbs. per square inch, at the elastic limit. Substituting values of s for iron, steel, and copper, 12, 14, and 8 tons respectively, we have the following:

FORMULE FOR ULTIMATE ELASTIC STRENGTH OF FLAT STAYED SURFACES

	Iron.	Steel.	Copper.
Pressure	$p = 5000 \frac{t}{d}$	$p = 5700 \frac{t}{d}$	$p = 3300 \frac{t}{d}$
Thickness of plate	$t = \frac{p \times d}{5000}$	$t = \frac{p \times d}{5700}$	$t = \frac{p \times d}{3300}$
Pitch of bolts	$d = \frac{5000t}{p}$	$d = \frac{5700t}{p}$	$d = \frac{3300t}{p}$

For Diameter of the Stay-bolts, Clark gives
$$d' = .0024 \sqrt{\frac{PP'p}{s}}$$
,

in which d'= diameter of screwed bolt at bottom of thread, P= longitudinal and P' transverse pitch of stay-bolts between centres, p= internal pressure in lbs, per sq. in. that will strain the plate to its elastic limit, s= elastic strength of the stay-bolts in lbs, per sq. in. Taking s= 12, 14, and 8 tons, respectively for iron, steel, and copper, we have

For iron,
$$d' = .00069 \sqrt{PPp}$$
 or if $P = P'$, $d' = .00069 P \sqrt{p}$;
For steel, $d' = .00064 \sqrt{PPp}$, " $d' = .00064 P \sqrt{p}$;
For copper, $d' = .00084 \sqrt{PP'p}$, " $d' = .00084 P \sqrt{p}$.

In using these formulæ a large factor of safety should be taken to allow for reduction of size by corrosion. Thurston's Manual of Steam-boilers, p. 144, recommends that the factor be as large as 15 or 20. The Hartford Steam Boiler Insp. & Ins. Co. recommends not less than 10.

Strength of Stays. -A. F. Yarrow (Engr., March 20, 1891) gives the following results of experiments to ascertain the strength of water-space stays:

Description.	Length between Plates.	Diameter of Stay over Threads.	Ulti- mate Stress.
Hollow stays screwed into plates and hole expanded Solid stays screwed into plates and riveted over.		1 in.(hole 7/16 in. and 5/16 in. 1 in.(hole 9/16 in. and 7/16 in. 76 in. 78 in.	

The above are taken as a fair average of numerous tests.

Stay-bolts in Curved Surfaces, as in Water-legs of Vertical Bollers.—The rules of the U. S. Supervising Inspectors provide as follows: All vertical boiler-furnaces constructed of wrought iron or steel plates, and having a diameter of over 42 in. or a height of over 40 in. shall be stayed with bolts as provided by § 6 of Rule II, for flat surfaces; and the thickness of material required for the shells of such furnaces shall be determined by the distance between the centres of the stay-bolts in the furnace and not in the shell of the boiler; and the steam-pressure allowable shall be determined by the distance from centre of stay-bolts in the furnace and the diameter of such stay-bolts at the bottom of the thread.

and the diameter of such stay-bolts at the bottom of the thread.

The Hartford Steam-boiler Insp. & Ins. Co. approves the above rule (The Locomotive, March, 1892) as far as it states that curved surfaces are to be computed the same as flat ones, but prefers Clark's formulæ for flat stayed surfaces to the rules of the U. S. Supervising Inspectors.

Fusible-plugs.—Fusible-plugs should be put in that portion of the heating-surface which first becomes exposed from lack of water. The rules of the U. S. Supervising Inspectors specify Banca tin for the purpose. Its melting-point is about 445° F. The rule says: All steamers shall have inserted in their boilers plugs of Banca tin, at least ½ in. in diameter at the smallest end of the Internal opening, in the following manner, to wit: Cylinder-boilers with flues shall have one plug inserted in one flue of each boiler; and also one plug inserted in the shell of each boiler from the inside, immediately before the fire line and not less than 4 ft. from the forward immediately before the fire line and not less than 4 ft. from the forward end of the boiler. All fire-box boilers shall have one plug inserted in the crown of the back connection, or in the highest fire-surface of the boiler.

All upright tubular boilers used for marine purposes shall have a fusible plug inserted in one of the tubes at a point at least 2 in, below the lower gauge-cock, and said plug may be placed in the upper head sheet when deemed advisable by the local inspectors.

Steam-domes. -Steam domes or drums were formerly almost universally used on horizontal boilers, but their use is now generally discontinued,

as they are considered a useless appendage to a steam-boiler, and unless

properly designed and constructed are an element of weakness.

Height of Furnace.—Recent practice in the United States makes the height of furnace much greater than it was formerly. With large sizes of anthracite there is no serious objection to having the furnace as low as 12 to 18 in., measured from the surface of the grate to the nearest portion of the heating surface of the boiler, but with coal containing much volatile matter and moisture a much greater distance is desirable. With very volatile coals the distance may be as great as 4 or 5 ft. Rankine (S. E., p. 457) says: The clear height of the "crown" or roof of the furnace above the gratebars is seldom less than about 18 in., and often considerably more. In the fire-baxes of locomotives it is on an average about 4 ft. The height of 18 in. is suitable where the crown of the furnace is a brick arch. Where the crown of the furnace, on the other hand, forms part of the heating-surface of the boller, a greater height is desirable in every case in which it can be obtained; for the temperature of the boiler-plates, being much lower than that of the flame, tends to check the combustion of the inflammable gases which rise from the fuel. As a general principle a high furnace is favorable to complete combustion.

IMPROVED METHODS OF FEEDING COAL.

Michanical Stokers. (William R. Roney, Trans. A. S. M. E., vol. xii.)—Mechanical stokers have been used in England to a limited extent since 1785. In that year one was patented by James Watt. It was a simple device to push the coal, after it was coked at the front end of the grate, back towards the bridge. It was worked intermittently by levers, and was designed primarily to prevent smoke from bituminous coal. (See D. K. Clark's Treatise on the Steam-engine.)

After the year 1840 many styles of mechanical stokers were patented in England, but nearly all were variations and modifications of the two forms of stokers patented by John Jukes in 1841, and by E. Henderson in 1848.

The Jukes stoker consisted of longitudinal fire-bars, confected by links,

so as to form an endless chain, similar to the familiar treadmill horse-power. The small coal was delivered from a hopper on the front of the boiler, on to the grate, which slowly moving from front to rear, gradually advanced the fuel into the furnace and discharged the ash and clinker at the back.

The Henderson stoker consists primarily of two horizontal fans revolving on vertical spindles, which scatter the coal over the fire.

Numerous faults in mechanical construction and in operation have limited the use of these and other mechanical stokers. The first American stoker was the Murphy stoker, brought out in 1878. It consists of two coal magazines placed in the side walls of the boiler furnace, and extending back from the boiler front 6 or 7 feet. In the bottom of these magazines are rectangular iron boxes, which are moved from side to side by means of a rack and pinion, and serve to push the coal upon the grates, which incline at an angle of about 85° from the inner edge of the coal magazines, forming a V-shaped receptacle for the burning coal. The grates are composed of narrow parallel bars, so arranged that each alternate bar lifts about an inch at the lower

bars, so arranged that each alternate bar lifts about an inch at the lower end, while at the bottom of the V, and filling the space between the ends of the grate-bars, is placed a cast-iron toothed bar, arranged to be turned by a crank. The purpose of this bar is to grind the clinker coming in contact with it. Over this V-shaped recepiacle is sprung a fire-brick arch.

In the Roney mechanical stoker the fuel to be burned is dumped into a hopper on the boiler front. Set in the lower part of the hopper is a "pusher" to which is attached the "feed-plate" forming the bottom of the hopper. The "pusher," by a vibratory motion, carrying with it the "feed-plate," gradually forces the fuel over the "dead-plate" and on the grate. The grate-bars, in their normal condition form a series of steps, to the top step of which coal is fed from the "dead-plate." Each bar rests in a concave seat in the bearer, and is capable of a rocking motion through an adjustable angle. All the grate-bars are coupled together by a "rocker-bar," A variable back-and-forth motion being given to the "rocker-bar," through a conable back-and-forth motion being given to the "rocker-bar," through a connecting-rod, the grate-bars rock in unison, now forming a series of steps. and now approximating to an inclined plane, with the grates partly over-lapping, like shingles on a roof. When the grate-bars rock forward the fire will tend to work down in a body. But before the coal can move too far the bars rock back to the stepped position, checking the downward motion, breaking up the cake over the whole surface, and admitting a free volume of air through the fire. The rocking motion is slow, being from 7 to 10 strokes per minute, according to the kind of coal. This alternate starting and checking motion is continuous, and finally lands the cinder and ash on the dumping-grate below.

Mr. Roney gives the following record of six tests to determine the comparative economy of the Roney mechanical stoker and hand-firing on return tubular boilers, 60 inches × 20 feet, burning Cumberland coal with natural

draught. Rating of boiler at 12.5 square feet, 105 H. P.

Three tests, hand-firing. Three tests, Stoker. Evaporation per pound, dry) 10.86 10.44 11.00 11.89 12.25 12.54 coal from and at 212° lbs H.P. developed above rating, \$ 5.8 13.5 66.7 84.3

Results of comparative tests like the above should be used with caution in drawing generalizations. It by no means follows from these results that a stoker will always show such comparative excellence, for in this case the results of hand-firing are much below what may be obtained under favor-

able circumstances from hand-firing with good Cumberland coal.

The Hawley Down-draught Furnace.—A foot or more above the ordinary grate there is carried a second grate composed of a series of water tubes, opening at both ends into steel drums or headers, through which water is circulated. The coal is fed on this upper grate, and as it is parwater is circulated. The coal is fed on this upper grate, and as it is partially consumed falls through it upon the lower grate, where the combustion is completed in the ordinary manner. The draught through the coal on the upper grate is downward through the coal and the grate. The volatile gases are therefore carried down through the bed of coal, where they are thoroughly heated, and are burned in the space beneath, where they neet the excess of hot air drawn through the fire on the lower grate. In tests in Chicago, from 80 to 45 lbs. of coal were burned per square foot of grate upon this system, with good economical results. (See catalogue of the Hawley

Down Draught Furnace Co., Chicago.)

Under-feed Stokers.—Results similar to those that may be obtained with downward draught are obtained by feeding the coal at the bottom of the bed, pushing upward the coal already on the bed which has had its volatile matter distilled from it. The volatile matter of the freshly fired coal then has to pass through a body of ignified coke, where it meets a supply of hot air. (See circular of The American Stoker Co., New York, 1898.)

SMOKE PREVENTION.

A committee of experts was appointed in St. Louis in 1891 to report on the smoke problem. A summary of its report is given in the *Iron Age* of April 7, 1892. It describes the different means that have been tried to prevent smoke, such as gas-fuel, steam-jets, fire-brick arches and checker-work, hollow walls for preheating air, coking arches or chambers, double combustion furnaces, and automatic stokers. All of these means have been more or less effective in diminishing smoke, their effectiveness depending largely upon the skill with which they are operated; but none is entirely satisfactory. Fuel-gas is objectionable chiefly on account of its expense. The average quality of fuel-gas made from a trial run of several car-loads of Illinois coal, in a well-designed fuel-gas plant, showed a calorific value of 248,391 heat-units per 1000 cubic feet. This is equivalent to 5052.8 heat-units per lb. of coal, whereas by direct calorimeter test an average sample of the coal gave 11,172 heat-units. One lb, of the coal showed a theoretical evaporation of 5.23 lbs. water, while the gas from 1 lb, showed a theoretical evaporation of 5.23 lbs. 48.17 lbs. of coal were required to furnish 1000 cubic feet of the gas. In 89 tests the smoke-preventing furnaces showed only 74\$ of the capacity of the common furnaces, reduced the work of the boilers 28%, and required about 2% more fuel to do the same work. In one case with

steam-jets the fuel consumption was increased 12% for the same work.

Prof. O. H. Landreth, in a report to the State Board of Health of Tennessee (Engineering News, June 8, 1893), writes as follows on the subject of smoke prevention:

As pertains to steam-boilers, the object must be attained by one or more of the following agencies:

1. Proper design and setting of the boiler-plant. This implies proper grate area, sufficient draught, the necessary air-space between grate-bars and

through furnace, and ample combustion-room under boilers.

2. That system of firing that is best adapted to each particular furnace to secure the perfect combustion of bituminous coal. This may be either: (a) "coke-firing," or charging all coal into the front of the furnace until partially coked, then pushing back and spreading; or (b) "alternate side-firing"; or (c) "spreading," by which the coal is spread over the whole grate area in thin, uniform layers at each charging.

3. The admission of air through the furnace-door, bridge-wall, or side walls.

4. Steam-jets and other artificial means for thoroughly mixingithe air and combartible graces.

combustible gases.

5. Preventing the cooling of the furnace and boilers by the inrush of cold air when the furnace-doors are opened for charging coal and handling the

fire.

Establishing a gradation of the several steps of combustion so that the coal may be charged, dried, and warmed at the coolest part of the furnace, and then moved by successive steps to the hottest place, where the final combustion of the coked coal is completed, and compelling the distilled combustible gases to pass through this hottest part of the fire.
7. Preventing the cooling by radiation of the unburned combustible gases

until perfect mixing and combustion have been accomplished.

8. Varying the supply of air to suit the periodic variation in demand.

9. The substitution of a continuous uniform feeding of coal instead of

intermittent charging.

10. Down-draught burning or causing the air to enter above the grate and pass down through the coal, carrying the distilled products down to the high temperature plane at the bottom of the fire.

The number of smoke-prevention devices which have been invented is

A brief classification is:

(a) Mechanical stokers. They effect a material saving in the labor of firing, and are efficient smoke-preventers when not pushed above their capacity, and when the coal does not cake badly. They are rarely susceptible to the sudden changes in the rate of firing frequently demanded in service.

(b) Air flues in side walls, bridge-wall, and grate-bars, through which air when passing is heated. The results are always beneficial, but the flues are difficult to keep clean and in order.

(c) Coking arches, or spaces in front of the furnace arched over, in which the fresh coal is coked, both to prevent cooling of the distilled gases, and to force them to pass through the hottest part of the furnace just beyond the arch. The results are good for normal conditions, but ineffective when the fires are forced. The arches also are easily burned out and injured by working the fire.

(d) Dead-plates, or a portion of the grate next the furnace doors, reserved for warming and coking the coal before it is spread over the grate. These give good results when the furnace is not forced above its normal capacity. This embodies the method of "coke-firing" mentioned before.

(e) Down-draught furnaces, or furnaces in which the air is supplied to the

coal above the grate, and the products of combustion are taken away from beneath the grate, thus causing a downward draught through the coal, carrying the distilled gases down to the highly heated incandescent coal at the bottom of the layer of coal on the grate. This is the most perfect manuer of producing combustion, and is absolutely smokeless.

(f) Steam jets to draw air in or inject air into the furnace above the grate, and also to mix the air and the combustible gases together. A very efficient smoke-preventer, but one liable to be wasteful of fuel by inducing too rapid

(g) Baffle-plates placed in the furnace above the fire to aid in mixing the

combustible gases with the air.

(h) Double furnaces, of which there are two different styles; the first of which places the second grate below the first grate; the coal is coked on the first grate, during which process the distilled gases are made to pass over the second grate, where they are ignited and burned; the coke from the first grate is dropped onto the second grate: a very efficient and economical smoke-preventer, but rather complicated to construct and maintain. In the second form the products of combustion from the first furnace pass throuthe grate and fire of the second, each furnace being charged with fresh fuel when needed, the latter generally with a smokeless coal or coke: an irrational and unpromising method.

Mr. C. F. White, Consulting Engineer to the Chicago Society for the Pre-

vention of Smoke, writes under date of May 4, 1893; The experience had in Chicago has shown plainly that it is perfectly easy to equip steam-boilers with furnaces which shall burn ordinary soft coal in such a manner that the making of smoke dense enough to obstruct the vision shall be confined to one or two intervals of perhaps a couple of minutes'

duration in the ordinary day of 10 hours.

Gas-fired Steam-boilers.—Converting coal into gas in a separate producer, before burning it under the steam-boiler, is an ideal method of smoke-prevention, but its expense has hitherto prevented its general introduction. A series of articles on the subject, illustrating a great number of devices, by F. J. Rowan, is published in the Colliery Engineer, 1889-90. See

also Clark on the Steam-engine.

FORCED COMBUSTION IN STEAM-BOILERS.

For the purpose of increasing the amount of steam that can be generated by a boiler of a given size, forced draught is of great importance. It is universally used in the locomotive, the draught being obtained by a steam-jet in the smoke-stack. It is now largely used in ocean steamers, especially in ships of war, and to a small extent in stationary boilers. Economy of fuel is generally not attained by its use, its advantages being conflued to the securing of increased capacity from a boiler of a given bulk, weight, or cost. The subject of forced draught is well treated in a paper by James Howden, entitled, "Forced Combustion in Steam-boilers" (Section G, Engineering

Congress at Chicago, in 18893, from which we abstract the following:
Edwin A. Stevens at Bordentown, N. J., in 1897, in the steamer "North America," fitted the boilers with closed ash-pits, into which the air of combustion was forced by a fan. In 1898 Ericsson fitted in a similar manner the steamer "Victory," commanded by Sir John Ross.

Mooree E Acad R L. Steame activities of forced departs for

Messrs. E. A. and R. L. Stevens continued the use of forced draught for a considerable period, during which they tried three different modes of using the fan for promoting combustion: 1, blowing direct into a closed asb-pit; 2, exhausting the base of the funnel by the suction of the fan: 8, forcing air into an air-tight boiler-room or stoke-hold. Each of these three methods was attended with serious difficulties.

In the use of the closed ash-pit the blast-pressure would frequently force the gases of combustion, in the shape of a serrated flame, from the joint around the furnace doors in so great a quantity as to affect both the effi-

ciency and health of the firemen.

The chief defect of the second plan was the great size of the fan required to produce the necessary exhaustion. The size of fan required grows in arapidly increasing ratio as the combustion increases, both on account of the greater air-supply and the higher exit temperature enlarging the volume of

the waste gases.

The third method, that of forcing cold air by the fan into an air-tight boiler-room—the present closed stoke-hold system—though it overcame the difficulties in working belonging to the two forms first tried, has serious defects of its own, as it cannot be worked, even with modern high-class boiler-construction, much, if at all, above the power of a good chimney described in most boilers, without damaging them.

draught, in most boilers, without damaging them.

In 1875 John I. Thornycroft & Co., of London, began the construction of torpedo-boats with boilers of the locomotive type, in which a high rate of combustion was attained by means of the air-tight boiler-room, into which

air was forced by means of a fan.
In 1882 H.B.M. ships "Satellite" and "Conqueror" were fitted with this system, the former being a small ship of 1500 I.H.P., and the latter an ironclad of 4500 I.H.P. On the trials with forced draught, which lasted from two to three hours each, the highest rates of combustion gave 16.9 I.H.P. per square foot of fire-grate in the "Satellite," and 13.41 I.H.P. in the "Conqueror."

None of the short trials at these rates of combustion were made without injury to the seams and tubes of the boilers, but the system was adopted,

and it has been continued in the British Navy to this day (1898).

In Mr. Howden's opinion no advantage arising from increased combustion over natural draught rates is derived from using forced draught in a closed ash-pit sufficient to compensate the disadvantages arising from difficulties

in working, there being either excessive smoke from bituminous coat or reduced evaporative economy.

In 1880 Mr. Howden designed an arrangement intended to overcome the

An air-tight reservoir or chamber is placed on the front end of the boiler and surrounding the furnaces. This reservoir, which projects from 8 to 10 inches from the end of the boiler, receives the air under pressure, which is passed by the valves into the ash-pits and over the fires in proportions suited to the kind of fuel used and the rate of combustion required. The suited to the kind of rule used and the rate of combustion required. The air nsed above the fires is admitted to a space between the outer and inner furnace-doors, the inner having perforations and an air-distributing box through which the air passes under pressure.

By means of the balance of air-pressure above and below the fires all tendency for the fire to blow out at the furnace-door is removed.

By regulating the admission of the air by the valves above and below the fires, the highest rate of combustion possible by the air-pressure used can be effected, and in same manner the rate of combustion can be reduced to far below that of natural draught, while complete and economical combustion at all rates is secured.

tion at all rates is secured.

A feature of the system is the combination of the heating of the air of combustion by the waste gases with the controlled and regulated admission of air to the furnaces. This arrangement is effected most conveniently by passing the hot fire-gases after they leave the boiler through stacks of vertical tubes enclosed in the uptake, their lower ends being immediately

above the smoke-box doors.

Installations on Howden's system have hitherto been arranged for a rate of combustion to give at full sea-power an average of from 18 to 22 I.H.P. per square foot of fire-grate with fire-bars from 5'0" to 5'6" in length.

It is believed that with suitable arrangement of proportions even 80

I.H.P. per square foot can be obtained.

For an account of recent uses of exhaust-fans for increasing draught, see paper by W. R. Roney, Trans. A. S. M. E., vol. xv.

FUEL ECONOMIZERS.

Green's Fuel Economiser.—Clark gives the following average results of comparative trials of three boilers at Wigan used with and without economizers:

	Without	With
	Economizers.	Economizers.
Coal per square foot of grate per hour	. 21.6	21.4
Water at 100° evaporated per hour		79.32
Water at 212° per pound of coal	9.60	10.56
60		

Showing that in burning equal quantities of coal per hour the rapidity of evaporation is increased 2.3% and the efficiency of evaporation 10% by the addition of the economizer.

The average temperatures of the gases and of the feed-water before and after passing the economizer were as follows:

With 6-ft, grate, With 4-ft. grate. Before. After. Before, After. 649 812 840 501 187 157 41

Taking averages of the two grates, to raise the temperature of the feed-water 100° the gases were cooled down 250°.

water 100° the gases were cooled down 250°.

Performance of a Green Economiser with a Smoky Coal.

—The action of Green's Economizer was tested by M. W. Grosseteste for a period of three weeks. The apparatus consists of four ranges of vertical pipes, 4½ feet high, 3½ inches in diameter outside, nine pipes in each range, connected at top and bottom by horizontal pipes. The water enters all the tubes from below, and leaves them from above. The system of pipes is enveloped in a brick casing, into which the gaseous products of combustion are introduced from above, and which they leave from below. The pipes are cleared of soot externally by automatic scrapers. The capacity for water is 24 qubic feet, and the total external heating-surface is 250 square feet. The apparatus is placed in connection with a boiler having 355 square feet of surface. feet of surface.

This apparatus had been at work for seven weeks continuously without having been cleaned, and had accumulated a 16-inch coating of soot and ash, when its performance, in the same condition, was observed for one week. During the second week it was cleaned twice every day; but during week. During the second week it was cleaned on Monday morning, it was worked continuously without further cleaning. A smoke-making coal was used. The consumption was maintained sensibly constant from day to day.

GREEN'S ECONOMIZER.—RESULTS OF EXPERIMENTS ON ITS EFFICIENCY AS APPROTED BY THE STATE OF THE SURFACE. (W. Grosseteste.)

	Temper	rature of water.	Feed-	Temperature of Gas- eous Products.			
Time (February and March).	Enter- ing Feed- heater.	Leav- ing Feed- heater.	Differ- ence.	Enter- ing Feed- heater.	Leav- ing Feed- heater.	Differ- ence.	
1st Week	Fahr. 73.5°	Fahr. 161.5°	Fahr. 88.0°	Fahr.	Fahr.	Fahr. 588°	
2d Week	77.0	230 0	158.0	682	297	585	
8d Week-Monday	73.4	196.0	122.6	881	284	547	
Tuesday	73.4	181.4	108.0	871	809	562	
Wednesday	79.0	178.0	99.0	l —			
Thursday	80.6	170.6	90.0	952	329	623	
Friday	80.6	169 0	88.4	889	888	551	
Saturday	79.0	172.4	93.4	901	351	550	

1st Week, 2d Week, 3d Week, Coal consumed per hour 214
Water evaporated from 82° F. per hour. 1424 214 lbs. 216 lbs. 213 lbs. 1428 6.70 Water per pound of coal.... 6.65

It is apparent that there is a great advantage in cleaning the pipes daily—the elevation of temperature having been increased by it from 88° to 153°. In the third week, without cleaning, the elevation of temperature relapsed in three days to the level of the first week; even on the first day it was quickly reduced by as much as half the extent of relapse. By cleaning the pipes daily an increased elevation of temperature of 65° F., was obtained, whilst a gain of 6% was effected in the evaporative efficiency.

INCRUSTATION AND CORROSION.

Incrustation and Scale.—Incrustation (as distinguished from mere sediments due to dirty water, which are easily blown out, or gathered up, by means of sediment collectors) is due to the presence of salts in the feed-water (carbonates and sulphates of lime and magnesia for the most part), which are precipitated when the water is heated, and form hard deposits upon the boiler-plates. (See Impurities in Water, p. 551, ante.) Where the quantity of these salts is not very large (12 grains per gallon, say) scale preventives may be found effective. The chemical preventives either form with the salts other salts soluble in hot water; or precipitate them in the form of soft mud, which does not adhere to the plates and can

them in the form of soft mud, which does not adhere to the plates, and can be washed out from time to time. The selection of the chemical must depend upon the composition of the water, and it should be introduced regularly with the feed.

EXAMPLES.—Sulphate-of-lime scale prevented by carbonate of soda: The sulphate of soda produced is soluble in water; and the carbonate of lime falls down in grains, does not adhere to the plates, and may therefore belown out or gathered into sediment collectors. The chemical reaction is:

Sulphate of lime + Carbonate of soda = Sulphate of soda + Carbonate of lime CaSO₄ Na₂CO₃ Na₂SO₄ CaCO₂

Sodium phosphate will decompose the sulphates of lime and magnesia: Sulphate of lime + Eodium phosphate = Calcium phos. + Sulphate of soda. Na HPO CaHPO. CaSO. Na.804

Sul. of magnesia+Sodium phosphate = Phosphate of magnesia+Sul. of soda. MgSO. Na₂HPO₄ MgHPO4 Na₂SO₄

Where the quantity of salts is large, scale preventives are not of much use. Some other source of supply must be sought, or the bad water purified before it is allowed to enter the boilers. The damage done to boilers by un-

suitable water is enormous.

Pure water may be obtained by collecting rain, or condensing steam by means of surface condensers. The water thus obtained should be mixed with a little bad water, or treated with a little alkali, as undiluted, pure water corrodes iron; or, after each periodic cleaning, the bad may be used or a day or two to put a skin upon the plates.

Carbonate of lime and magnesia may be precipitated either by heating the water or by mixing milk of lime (Porter Clark process) with it, the water

seing then filtered.

Corrosion may be produced by the use of pure water, or by the presence facids in the water, caused perhaps in the engine-cylinder by the action of ich pressure steam upon the grease, resulting in the production of fatty cids. Acid water may be neutralized by the addition of lime.

Amount of Sediment which may collect in a 100-H.P. steam-boiler, vaporating 8000 lbs. of water per hour, the water containing different mounts of impurity in solution, provided that no water is blown off:

rains of solid impurities per U.S. gallon:

40 50 100 quivalent parts per 100,000: 8.57 17.14 84.28 51.42 68.56 85.71 102.85 120 187.1 154.8 171.4 ediment deposited in 1 hour, pounds: .257 .514 1.028 1.542 2.056 2.571 3.085 5.14 one day of 10 hours, pounds: 2.57 5.14 10.28 15.42 20.56 25.71 80.85 36.0 51.4 onc week of 6 days, pounds: 5.48 80.85 61.7 92.55 123.4 154.8 5.48 80.85 61.7 185.1 216.0 246.8 277.6 308.5

If a 100-H.P. boiler has 1200 sq. ft. heating-surface, one week's running thout blowing off, with water containing 100 grains of solid matter per llon in solution, would make a scale nearly .02 in. thick, if evenly deposited all over the heating-surface, assuming the scale to have a sp. gr. of = 156 lbs. per cu. ft.; .02 × 1200 × 156 × 1/12 = 312 lbs.

Boiler-scale Compounds.—The Bavarian Steam-boiler Inspection on in 1828 papers of a follow:

sn. in 1885 reported as follows:

denerally the unusual substances in water can be retained in soluble form precipitated as mud by adding caustic soda or lime. This is especially sirable when the boilers have small interior spaces.

t is necessary to have a chemical analysis of the water in order to fully termine the kind and quantity of the preparation to be used for the

ove purpose.

all secret compounds for removing boiler-scale should be avoided. (A list 27 such compounds manufactured and sold by German firms is then given

ich have been analyzed by the association.)

uch secret preparations are either nonsensical or fraudulent, or contain ner one of the two substances recommended by the association for reving scale, generally soda, which is colored to conceal its presence, and retimes adulterated with useless or even injurious matter. hese additions as well as giving the compound some strange, fanciful ne, are meant simply to deceive the boiler owner and conceal from him

fact that he is buying colored sods or similar substances, for which he is

ing an exorbitant price.

hing an exo, of the prevention of scale in motive-boilers an alkaline compound consisting of 3750 gals, of water, lbs. of 70% caustic soda, and 1600 lbs. of 58% soda-ash (Eng. News, Dec. 5.

r. H. E. Smith, chemist of the Ry. Co., writes May, 1902, that this com-nd was abandoned several years ago and commercial soda-ash, known 58° soda," containing about 97% pure carbonate of soda, substituted in water in the locomotive tender tanks, where it dissolves and passes to Its action is to precipitate a portion of the scale forming solids flocculent form so that they are kept loose and free from the metal un-ney can be blown or washed out.

e amounts used vary according to the character of the water and are d on the following rules: For calcium and magnesium sulphates and

chlorides, use soda-ash equal to the chemical equivalent of those compounds present. For calcium and magnesium carbonates, the amount of soda-ash to be used varies from nothing when sulphates or chlorides are high, up to about one fifth the equivalent of the carbonates, when sulphates and chlorides are low or absent. A few waters contain carbonate of soda originally, and for these less soda-ash or none at all is necessary. It may also be necessary to make some reduction in the dose of soda-ash when large amounts of other alkali salts are present. In any case it is not desirable to use more than 2 lbs. of soda-ash per 1000 gallons of water, or more than 10 lbs. per 100 miles of locomotive run, on account of the foaming produced. The above rule assumes that the boilers are fairly dean and are kept fairly free from sludge by blowing and washing out. On the C., M. &

St. P. Ry. boilers are usually washed once in 500 to 3000 miles run, according to the character of the waters used.

In the upper Mississippi valley the majority of the waters are below 30 or 25 grains of incrusting solids per gallon, and the greater portion of this is carbonates. For these the above treatment is very successful. From 35 to 50 grains, increasing difficulty is encountered on account of foaming produced by the large a mountage of children and alkall, and there 30 grains and alkall. duced by the large amounts of sludge and alkali, and above 50 grains, sods-

ash alone fails to keep the boilers clean in practical service.

Kerosene and other Petroleum Oils; Foaming.—Kerosene L. F. Lyne (Trans. A. S. M. E., ix. 247). The Am. Mach., May 22, 1890, says: Kerosene used in moderate quantities will not make the boiler foam; it is recommended and used for loosening the scale and for preventing the formation of scale. The presence of oil in combination with other impurities increases the tendency of many boilers to foam, as the oil with the impurities impedes the tendency of many boilers to foam, as the oil with the impurities impedes the free escape of steam from the water surface. The use of common oil not only tends to cause foaming, but is dangerous otherwise. The grease appears to combine with the impurities of the water, and when the boiler is at rest this compound sinks to the plates and clings to them in a loose, spongy mass, precombound sinks to the places and chings to their first a toole, spondy mass, pre-venting the water from coming in contact with the plates, and thereby pro-ducing overheating, which may lead to an explosion. Foaming may also be caused by forcing the fire, or by taking the steam from a point over the furnace or where the ebullition is violent; the greasy and dirty state of new bollers is another good cause for foaming. Kerosene should be used at first in small quantities, the effect carefully noted, and the quantity increased if necessary for obtaining the desired results.

R. C. Carpenter (Trans. A. S. M. E., vol. xi.) says: The boilers of the State Agricultural College at Lausing, Mich., were badly incrusted with a hard scale. It was fully three eighths of an inch thick in many places. The first application of the oil was made while the boilers were being but little used, application of the oil was made while the boilers were being out little used, by inserting a gallon of oil, filling with water, heating to the boiling-point and allowing the water to stand in the boiler two or three weeks before removal. By this method fully one half the scale was removed during the warm s-ason and before the boilers were needed for heavy firing. The oil was then added in small quantities when the boiler was in actual use. For boilers 4 ft. in diam, and 12 ft. long the best results were obtained by the use of 2 qts. for each boiler per week, and for each boiler 5 ft. in diam, 3 qts. The water used in the boilers had the following analysis. Caro per week. The water used in the bollers has the following analysis: CaCO₃, 206 parts in a million; MgCO₃, 78 parts; Fe₂CO₃, 82 parts; traces of sulphates and chlorides of potash and soda. Total solids, 325 parts in 1,000,000.

Taminate of Soda Compound.—T. T. Parker writes to Am. Mach.: Should you fluid kerosene not doing any good, try this recipe: 80 lbs. sal-soda, 85 lbs. japonica; put the ingredients in a 80-gal. barrel, fill half full of water, and run a steam hose into it until it dissolves and boils. Remove the hose, fill up with water, and allow to settle. Use one quart per day of ten hours for a 40-H.P. boiler, and, if possible, introduce it as you do cylinder oil to your engine. Barr recommends tannate of soda as a remedy for scale composed of sulphate and carbonate of lime. As the japonica yields the tannate of soda as a carbona yields the tannate of soda as a carbona yields the tannate of soda as a carbona yields the tannate of soda so a carbona yields the tannate of soda so a carbona yields the tannate of soda so a carbona yields the tannate of soda so a carbona yields the tannate of soda so a carbona yields the tannate of soda so a carbona yields the tannate of soda so a carbona yields the tannate of soda so a carbona yields the tannate of yellows. posed of sulphate and carbonate of lime. As the japonica yields the tannic acid, I think the resultant equivalent to the tannate of soda.

Petroleum Olls heavier than kerosene have been used with good results. Crude oil should never be used. The more volatile oils it contains make explosive gases, and its tarry constituents are apt to form a spongy

Removal of Hard Scale.—When boilers are coated with a hard scale difficult to remove the addition of 1/4 lb. caustic soda per horse-power, and steaming for some hours, according to the thickness of the scale, just before cleaning, will greatly facilitate that operation, rendering the scale soft and loose. This should be done, if possible, when the boilers are not otherwise in use. (Steam.)

Corrosion in Marine Boilers. (Proc. Inst. M. E., Aug. 1884).—The investigations of the Committee on Boilers served to show that the internal corrosion of boilers is greatly due to the combined action of air and seawater when under steam, and when not under steam to the combined action of air and moisture upon the unprotected surfaces of the metal. There are other deleterious influences at work, such as the corrosive action of fatty acids, the galvanic action of copper and brass, and the inequalities of temperature; these latter, however, are considered to be of minor importance.

acids, the galvanic action of copper and brass, and the inequalities of temperature; these latter, however, are considered to be of minor importance. Of the several methods recommended for protecting the internal surfaces of boilers, the three found most effectual are; First, the formation of a thin layer of hard scale, deposited by working the boiler with sea-water; second, the coating of the surfaces with a thin wash of Portland cement, particularly wherever there are signs of decay; third, the use of sine slabs suspended in the water and steam spaces.

As to general treatment for the preservation of boilers in store or when laid up in the reserve, either of the two following methods is adopted, as may be found most suitable in particular cases. First, the boilers are dried as much as possible by airlug-stoves, after which 2 to 3 cwt, of quicklime, according to the size of the boiler, is placed on suitable trays at the bottom of the boiler and on the tubes. The boiler is then closed and made as air-tight as possible. Periodical inspection is made every six months, when if the lime be found slacked it is renewed. Second, the other method is to fill the boilers up with sea or fresh water, laving added soda to it in the proportion of 1 lb. of soda to every 100 or 120 lbs, of water. The sufficiency of the saturation can be tested by introducing a piece of clean new iron and leaving it in the boiler for ten or twelve hours; if it shows signs of rusting, more soda should be added. It is essential that the boilers be entirely filled, to the complete exclusion of air.

Great care is taken to prevent sudden changes of temperature in boilers. Directions are given that steam shall not be raised rapidly, and that care shall be taken to prevent a rush of cold air through the tubes by too suddenly opening the smoke-box doors. The practice of emptying boilers by blowing out is also prohibited, except in cases of extreme urgency. As a rule the water is allowed to remain until it becomes cool before the boilers are emptied.

rule the water is allowed to remain until it becomes cool before the boilers

are emptied.

Mineral oil has for many years been exclusively used for internal lubrication of engines, with the view of avoiding the effects of fatty acid, as this oil

does not readily decompose and possesses no acid properties.

Of all the preservative methods adopted in the British service, the use of zinc properly distributed and fixed has been found the most effectual in saving the iron and steel surfaces from corrosion, and also in neutralizing by its own deterioration the hurtful influences met with in water as ordinarily supplied to boilers. The zinc slabs now used in the navy boilers are 12 in long, 8 in, wide, and ½ inch thick; this size being found convenient for general application. The amount of zinc used in new boilers at present is one slab of the above size for every 20 I.H.P., or about one square foot of ginc used face to two square feet of grate surface. Rolled winc is found the zinc surface to two square feet of grate surface. Rolled zinc is found the most suitable for the purpose. To make the zinc properly efficient as a protector especial care must be taken to insure perfect metallic contact between the slabs and the stays or plates to which they are attached. The slabs should be placed in such positions that all the surfaces in the boiler shall be protected. Each slab should be periodically examined to see that its connection remains perfect, and to renew any that may have decayed; this examination is usually made at intervals not exceeding three months. Under ordinary circumstances of working these gine slabs may be expected causer organizery circumstances of working these zinc slabs may be expected to last in fit gondition from sixty to ninety days, immersed in hot sea water; but in new boilers they at first decay more rapidly. The slabs are generally secured by means of iron straps 2 in, wide and 36 inch thick, and long enough to reach the nearest stay, to which the strap is firmly attached by screw-bolts.

To promote the proper care of boilers when not in use the following order has been issued to the French Navy by the Government: On board all ships in the reserve, as well as those which are laid up, the boilers will be completely filled with fresh water. In the case of latge boilers with large tubes there will be added to the water a certain amounts of milk of lime, or a solution of soda may be used instead. In the case of tubulous boilers with small tubes milk of lime or soda may be added, but the solution will not be so strong as in the case of the larger tube, so as to avoid any danger of contracting the effective area by deposit from the solution; but the strength

of the solution will be just sufficient to neutralize any acidity of the water. (Iron Age, Nov. 2, 1893.)

Use of Zine.—Zinc is often used in boilers to prevent the corrosive action of water on the metal. The action appears to be an electrical one, the iron being one pole of the battery and the zinc being the other. The hydrogen goes to the iron shell and escapes as a gas into the steam. The

oxygen goes to the zinc.

On account of this action it is generally believed that zinc will always prevent corrosion, and that it cannot be harmful to the boiler or tank. Some experiences go to disprove this belief, and in numerous cases zinc has not only been of no use, but has even been harmful. In one case a tubular boiler had been troubled with a deposit of scale consisting chiefly of organic matter and lime, and zinc was tried as a preventive. The beneficial ganic matter and lime, and zinc was tried as a preventive. The beneficial action of the zinc was so obvious that its continued use was advised, with frequent opening of the boiler and cleaning out of detached scale until all the old scale should be removed and the boiler become clean. Eight or ten months later the water supply was changed, it being now obtained from another stream supposed to be free from lime and to contain only organic matter. Two or three months after its introduction the tubes and shell were found to be coated with an obstinate adhesive scale, and composed of were round to be costed with an obstinate annesive scare, and composed or zinc oxide and the organic matter or sediment of the water used. The deposit had become so heavy in places as to cause overheating and bulging of the platez over the fire. (The Locomotive.) Effect of Deposit on Flues. (Rankine.)—An external crust of a carbonaceous kind is often deposited from the flame and smoke of the fur-

carronaceous kind is oven deposited from the lame and smoke of the fur-naces in the flues and tubes, and if allowed to accumulate seriously impairs the economy of fuel. It is removed from time to time by means of scrapers and wire brushes. The accumulation of this crust is the probable cause of the fact that in some steamships the consumption of coal per indicated horse-power per hour goes on gradually increasing until it reaches one and

a half times its original amount, and sometimes more.

a nair times its original amount, and sometimes more.

Dangerous Steam-boilers discovered by Inspection.—

The Hartford Steam-boiler Inspection and Insurance Co. reports that its inspectors during 1893 examined 163,328 boilers, inspected 66,698 boilers, both internally and externally, subjected 7861 to hydrostatic pressure, and found 597 unsafe for further use. The whole number of defects reported was 122,898, of which 12,390 were considered dangerous. A summary is given below. (The Locomotive, Feb. 1894.)

SUMMARY, BY DEFECTS, FOR THE YEAR 1893.

		o,	
Nature of Defects. Whole No. ge			Dan- erous.
Deposit of sediment 9,774	548	Leakage around tubes21,211	2,909
Incrustation and scale18,369	865	Leakage at seams 5,424	482
Internal grooving 1,249		Water-gauges defective. 8,670	660
Internal corrosion 6,252	397	Blow outs defective 1,620	425
External corrosion 8,600	536	Deficiency of water 204	107
Def'tive braces and stays 1,966	485	Safety-valves overloaded 728	208
Settings defective 3,094	852	Safety-valves defective 942	800
Furnaces out of shape 4,575		Pressure-gauges def'tive 5,958	552
Fractured plates 3.532	640	Boilers without pressure-	
Burned plates 2,762	825		115
Blistered plates 3,331		Unclassified defects 755	4
Defective rivets 17,415	1,569		
Defective heads 1,357	850	Total122,893	12,390

The above-named company publishes annually a classified list of boiler-explosions, compiled chiefly from newspaper reports, showing that from 200 to 300 explosions take place in the United States every year, killing from 200 to 300 persons, and injuring from 300 to 450. The lists are not pretended to be complete, and may include only a fraction of the actual number of explosions.

Steam-boilers as Magazines of Explosive Energy.—Prof. H. Thurston (Trans. A. S. M. E., vol. vi.), in a paper with the above title, presents calculations showing the stored energy in the hot water and steam of various boilers. Concerning the plain tubular boiler of the steam of various boilers. Concerning the plain tubular boiler of the form and dimensions adopted as a standard by the Hartford Steam-boiler Insurance Co., he says: It is 60 inches in diameter, containing 66 3-inch tubes, and is 15 feet long. It has 850 feet of heating and 30 feet of grate surface; is rated at 60 horse-power, but is oftener driven up to 75; weighs 9500 pounds, and contains nearly its own weight of water, but only 21 pounds of steam when under a pressure of 75 pounds per square inch, which is below its safe allowance. It stores 52,000,000 foot-pounds of energy, of which but 4 per cent is in the steam, and this is enough to drive the boiler just about one mile into the air, with an initial velocity of nearly 600 feet per second.

SAFETY-VALVES.

Calculation of Weight, etc., for Lever Safety-valves.

Let W = weight of ball at end of lever, in pounds;

w = weight of lever itself, in pounds;

V = weight of valve and spindle, in pounds;

L = distance between fulcrum and centre of ball, in inches;

l = " " " " valve, in inches;

g = " " " " gravity of lever, in in.;

A = area of valve, in square inches;

P = pressure of steam, in lbs. per sq. in., at which valve will open.

Then
$$PA \times l = W \times L + w \times g + V \times l$$
;
whence $P = \frac{WL + wg + Vl}{Al}$;
 $W = \frac{PAl - wg - Vl}{L}$;
 $L = \frac{PAl - wg - Vl}{W}$.

EXAMPLE.—Diameter of valve, 4"; distance from fulcrum to centre of bali, 86"; to centre of valve, 4"; to centre of gravity of lever, 15\\(\frac{1}{2}\)"; weight of valve and spindle, 3 lbs.; weight of lever, 7 lbs.; required the weight of ball to make the blowing-off pressure 80 lbs. per sq. in.; area of 4" valve = 12.566 sq. in. Then

$$W = \frac{PAl - wg - Vl}{L} = \frac{80 \times 12.566 \times 4 - 7 \times 1514 - 8 \times 4}{36} = 108.4 \text{ lbs.}$$

The following rules governing the proportions of lever-valves are given by the U.S. Supervisors. The distance from the fulcrum to the valve-stem must in no case be less than the diameter of the valve-opening; the length of the lever must not be more than ten times the distance from the fulcrum to the valve-stem; the width of the bearings of the fulcrum must not be less than three quarters of an inch; the length of the fulcrum-link must not be less than four inches; the lever and fulcrum-link must be made of wrought iron or steel, and the knife-edged fulcrum points and the bearings for these points must be made of steel and hardened; the valve must be guided by its spindle, both above and below the ground seat and above the lever, through supports either made of composition (gun-metal) or bushed with it; and the spindle must fit lossely in the bearings or supports.

Rules for Area of Safety-valves.

(Rule of U. S. Supervising Inspectors of Steam-vessels (as amended 1894).)

Lever safety-valves to be attached to marine boilers shall have an area of not less than 1 sq. in. to 2 sq. ft. of the grate surface in the boiler, and the seats of all such safety-valves shall have an angle of inclination of 45° to the centre line of their axes.

Spring-loaded safety-valves shall be required to have an area of not less than 1 sq. in, to 3 sq. ft. of grate surface of the boiler, except as hereinafter otherwise provided for water-tube or coil and sectional boilers, and each spring-loaded valve shall be supplied with a lever that will raise the valve from its seat a distance of not less than that equal to one eighth the diameter of the valve-opening, and the seats of all such safety-valves shall have an angle of inclination to the centre line of their axes of 45°. All spring-loaded safety-valves for water-tube or coil and sectional boilers required to

carry a steam-pressure exceeding 175 lbs. per square inch shall be required to have an area of not less than 1 sq. in. to 6 sq. ft. of the grate surface of the boiler. Nothing herein shall be construed so as to prohibit the use of two safety-valves on one water-tube or coil and sectional boiler, provided the combined area of such valves is equal to that required by rule for one such valve.

Bule in Philadelphia Ordinances: Bureau of Steam-engine and Boiler Inspection.—Every boiler when fired sepa-rately, and every set or series of boilers when placed over one fire, shall have attached thereto, without the interposition of any other valve, two or more safety-valves, the aggregate area of which shall have such relations to the area of the grate and the pressure within the boiler as is expressed in schedule A.

SCHEDULE A.—Least aggregate area of safety-valve (being the least sectional area for the discharge of steam) to be placed upon all stationary boilers with natural or chimney draught [see note a].

$$A = \frac{22.5G}{P + 8.62},$$

in which A is area of combined safety-valves in inches; G is area of grate in square feet; P is pressure of steam in pounds per square inch to be carried in the boiler above the atmosphere.

The following table gives the results of the formula for one square foot of grate, as applied to boilers used at different pressures:

Pressures per square inch:

20 80 60 70 80 90 100 110 120 Area corresponding to one square foot of grate: 1.21 0.79 0.58 0.46 0.38 0.33 0.29 0.25 0.23 0.210.19 0.17

[Note a.] Where boilers have a forced or artificial draught, the inspector must estimate the area of grate at the rate of one square foot of grate-surface for each 16 lbs. of fuel burned on the average per hour.

Comparison of Various Bules for Area of Lever Safety-Valves. (From an article by the author in American Machinist, May 24, 1834, with some alterations and additions.)—Assume the case of a boiler rated at 100 horse-power; 40 sq. ft. grate; 1200 sq. ft. heating-surface; using 400 lbs. of coal per hour, or 10 lbs. per sq. ft. of grate per hour, and evaporating 3600 lbs. of water, or 3 lbs. per sq. ft. of heating-surface per hour steam-pressure by gauge, 100 lbs. What size of safety-valve, of the lever type, should be required?

A compilation of various rules for finding the area of the safety-valve disk, from The Locomotive of July, 1892, is given in abridged form below, together with the area calculated by each rule for the above example.

U. S. Supervisors, heating-surface in sq. ft. + 25 *	rea in sq. in.
English Board of Trade, grate-surface in sq. ft. + 2.	20
Molesworth, four fifths of grate-surface in sq. ft	14 K
Thurston, $\frac{1}{2}$ (5 × heating-surface) $\frac{1}{2}$ gauge pressure + 10	07.0
2 gauge pressure + 10	41.0
Rankine, .006 × water evaporated per hour	21.6

Suppose that, other data remaining the same, the draught were increased so as to burn 13½ lbs. coal per square foot of grate per hour, and the grate-surface cut down to 30 sq. ft. to correspond, making the coal burned per hour 400 lbs., and the water evaporated 3600 lbs., the same as before; then the English Board of Trade rule and Molesworth's rule would give an area of disk of only 15 and 24 sq. in., respectively, showing the absurdity of making the area of grate the basis of the calculation of disk area.

Another rule by Prof. Thurston is given in American Machinist, Dec. 1877,

Disk area =
$$\frac{\frac{1}{2} \text{ max. wt. of water evap. per hour}}{\text{gauge pressure} + 10}$$

This gives for the example considered 16.4 sq. in.

^{*} The edition of 1898 of the Rules of the Supervisors does not contain this rule, but gives the rule grate-surface + 2.

One rule by Rankine is 1/150 to 1/180 of the number of pounds of water aporated per hour, equals for the above case 27 to 20 sq. in. A communim in Power, July, 1890, gives two other rules:

ist. 1 sq. in. disk area for 3 sq. ft. grate, which would give 13.3 sq. in. &l. ¾ sq. in. disk area for 1 sq. ft. grate, which would give 30 sq. in.; but the grate-surface were reduced to 30 sq. ft. on account of increased aught, these rules would make the disk area only 10 and 22.5 sq. in., spectively.

spectively. The Philadelphia rule for 100 lbs. gauge pressure gives a disk area of 0.21 in for each sq. ft. of grate area, which would give an area of 8.4 sq. in r 40 sq. ft. grate, and only 6.3 sq. in. if the grate is reduced to 30 sq. ft. According to the rule this aggregate area would have to be divided between o valves. But if the boiler was driven by forced draught, then the in-

sctor "must estimate the area of grate at 1 sq. ft. for each 16 lbs. of fuel rned per hour."

Inder this condition the actual grate-surface might be cut down to 400 +

There this control the actual grate-surface highs be cut down to 400 \pm 85 sq. ft., and by the rule the combined area of the two safety-valves uild be only 25 \times 0.21 \pm 5.25 sq. in. Tystrom's Pocket-book, edition of 1891, gives 34 sq. in. for 1 sq. ft. grate; o quoting from Weisbach, vol. ii, 1/3000 of the heating-surface. This in case considered is 1200/3000 \pm 4 sq. ft. or 57.6 sq. in.

We thus have rules which give for the area of safety-valve of the same 100-rse-power boiler results ranging all the way from 5.25 to 57.5 sq. in. till of the rules above quoted give the area of the disk of the valve as the ng to be accertained, and it is this area which is supposed to bear some ect ratio to the grate-surface, to the heating-surface, to the water evaputed, etc. It is difficult to see why this area has been considered even proximately proportional to these quantities, for with small lifts the area actual opening bears a direct ratio, not to the area of disk, but to the cumference.

hus for various diameters of valve:

meter	1	2	3	₫)	- 75	6	7
за		3.14	7.07	12.57	19.64	28.27	88.48
cumference	8.14	6,28	9.42	12.57	15.71	18,85	21.99
cum. × lift of 0.1 in	.81	.63	،94	1.26	1.57	1.89	2,20
io to area	.4	.2	.18	.1	.08	-067	.057

he apertures, therefore, are therefore directly proportional to the diam-or to the circumference, but their relation to the area is a varying one. the lift = ½ diameter, then the opening would be equal to the area of disk, for circumference × ¼ diameter = area, but such a lift is far ond the actual lift of an ordinary safety-valve.

correct rule for size of safety-valves should make the product of the meter and the lift proportional to the weight of steam to be disobarged. "logical" method for calculating the size of safety-valve is given in Locomotive, July, 1893, based on the assumption that the actual opening uld be sufficient to discharge all the steam generated by the boiler. sier's rule for flow of steam is taken, viz., flow through aperture of one in. in lbs. per second = absolute pressure + 70, or in lbs. per hour = 51.43

bsolute pressure, the angle of the seat is 45°, as specified in the rules of the U.S. Superrs, the area of opening in sq. in. = circumference of the disk × the lift 1, 71 being the cosine of 45°; or diameter of disk × lift × 2.23.
G. Brown in his book on The Indicator and its Practical Working

idon, 1894) gives the following as the lift of the ordinary lever safety. e for 100 lbs. gauge-pressure;

Diam. of valve... 2 24 8 812 4 414 5 6 inche Rise of valve... .0583 .0523 .0507 .0492 .0478 .0462 .0446 .0430 inch. 6 inches.

ie lift decreases with increase of steam-pressure; thus for a 4-inch valve: 85 70 pressure, lbs. ge-press., lbs.. 45 65 135 155 175 105 115 195 215 80 50 120 100 140 160 180 e effective area of opening Mr. Brown takes at 70% of the rise multiplied ne circumference.

approximate formula corresponding to Mr. Brown's figures for diambetween 214 and 6 in. and gauge-pressures between 70 and 200 lbs. is

 $\frac{110}{a}$ = (.0603 = 0061d) $\times \frac{110}{a}$ abs. pressure, in which d = diam. of valve in in.

If we combine this formula with the formulæ

Flow in lbs. per hour = area of opening in sq. in. \times 51:43 \times abs. pressure, and Area = diameter of valve \times lift \times 2.23, we obtain the following, which the author suggests as probably a more correct formula for the discharging capacity of the ordinary lever safety-valve than either of those above given. Flow in lbs. per hour = $d(.0608 - .0031d) \times 115 \times 2.28 \times 51.48 = d(.795 - 41d)$.

From which we obtain:

Diameter, inches.... 1 114 2 214 Flow, lbs. per hour.. 754 1100 1426 1733 3 31/4 2016 2282 2524 2950 3556 Horse-power..... 25 58 67 76 98 37 47 84 110 119

the horse-power being taken as an evaporation of 30 lbs. of water per hour.

If we solve the example, above given, of the boiler evaporating 3500 lbs. of water per hour by this table, we find it requires one 7-inch valve, or a 2½ and a 3-inch valve combined. The 7-inch valve has an area of 3.5 sq. in., and the two smaller valves taken together have an area of only 12 sq. in.; another evidence of the absurdity of considering the area of disk as the factor which determined the capacity of the valve.

It is customary in practice not to use safety-valves of greater diameter than 4 in. If a greater diameter is called for by the rule that is adopted,

then two or more valves are used instead of one.

spring-loaded Safety-valves.—Instead of weights, springs are som-times employed to hold down safety-valves. The calculations are similar to those for lever safety-valves, the tension of the spring corresponding to a given rise being first found by experiment (see Springs, page 347). The rules of the U. S. Supervisors allow an area of 1 sq. in. of the valve

to 8 sq. ft. of grate, in the case of spring-loaded valves, except in water-tube, coil, or sectional boilers, in which 1 sq. in. to 6 sq. ft. of grate is allowed.

Spring-loaded safety-valves are usually of the reactionary or "pop" type,

in which the escape of the steam is opposed by a lip above the valve-seat, against which the escaping steam reacts, causing the valve to lift higher than the ordinary valve.

A. G. Brown gives the following for the rise, effective area, and quantity of steam discharged per hour by valves of the "pop" or Richardson type. The effective is taken at only 50% of the actual area due to the rise, on account of the obstruction which the lip of the valve offers to the escape of steam.

Dia.valve, in. Lift, inches. Area, sq. in.	.125 .196	11/6 .150 .854	2 .175 .550			31/6 .250 1.875	.275 1.728		5 .825 2. 5 53	.375 3.535	
Gauge-pres.,		Steam discharged per hour, lbs.									
30 lbs.	474	856	1830	1897	2568	3325	4178	5128	6178	8578	
50	669	1209	1878	2680	3620	4695	5901	7242	8718	12070	
70	861	1556	2417	8450	4660	6144	7596	9324	11220	15535	
90	1050	1897	2947	4207	5680	7370	9260	11365	18685	18945	
100	1144	2065	3208	4580	6185	8322	10080	12375	14895	20625	
120	1832	2405	3736	5332	7202	9342	11735	14410	17840	24015	
140	1516	2738	4254	6070	8200	10635	13365	16405		27310	
160	1696	8064	4760	6794	9175	11900	14955	18355	22095		
180	1883	8400	5288	7540	10180	13250	16595	20370		83950	
200	2062	8724	5786	8258	111150	114 165	18175	22310	26855	37185	

If we take 30 lbs. of steam per hour, at 100 lbs. gauge-pressure = 1 H.P., we have from the above table:

Diameter, inches... 1 11/2 2 21/4 3 31/4 4 41/4 5 6 Horse-power...... 38 69 107 158 206 277 886 412 496 687

A safety-valve should be capable of discharging a much greater quantity of steam than that corresponding to the rated horse-power of a boiler, since a boiler having ample grate surface and strong draught may generate more

than double the quantity of steam its rating calls for.

The Consolidated Safety-valve Co.'s circular gives the following rated capacity of its nickel-seat "pop" safety-valves:

2

11/6 316 100 11/4 10 216 60 Size, in 75 Boiler J from 8 35 125 175 30 50 150 to 10 15 75 100 125 175 200

The figures in the lower line from 2 inch to 5 inch. inclusive, correspond to he formula H.P. = 50(diameter - 1 inch).

THE INJECTOR. Equation of the Injector.

Let S be the number of pounds of steam used;

 \overline{W} the number of pounds of water lifted and forced into the boiler; h the height in feet of a column of water, equivalent to the absolute pressure in the boiler;

he the height in feet the water is lifted to the injector;

 t_1 the temperature of the water before it enters the injector; t_2 the temperature of the water after leaving the injector; H the total heat above 32° F. in one pound of steam in the boiler, in

heat-units; L the lost work in friction and the equivalent lost work due to radiation and lost heat;
778 the mechanical equivalent of heat.

Then

$$S[H - (t_2 - 32^\circ)] = W(t_2 - t_1) + \frac{(W + S)h + Wh_0 + L}{778}$$

An equivalent formula, neglecting $Wh_0 + L$ as small, is

$$S = \left[W(t_2 - t_1) + \frac{W + S}{d} \cdot p \cdot \frac{144}{778} \right] \frac{1}{H - (t_2 - 32^\circ)}$$
or
$$S = \frac{W[(t_2 - t_1)d + .1851p]}{[H - (t_2 - 32^\circ)]d - .1851p}$$

in which $d = \text{weight of 1 cu. ft. of water at temperature } t_2$; p = absolute

pressure of steam, lbs. per sq. in.

The rule for finding the proper sectional area for the narrowest part of the nozzles is given as follows by Rankine, S. E. p. 477:

Area in square inches = cubic feet per hour gross feed-water.

800 1 pressure in atmospheres

An important condition which must be fulfilled in order that the injector will work is that the supply of water must be sufficient to condense the steam. As the temperature of the supply or feed-water is higher, the

amount of water required for condensing purposes will be greater.

The table below gives the calculated value of the maximum ratio of water to the steam, and the values obtained on actual trial, also the highest admissible temperature of the feed-water as shown by theory and the highest actually found by trial with several injectors.

	MAXIMUM RATIO WATER TO STEAM.				MAXIMUM TEMPERATURE OF FEED-WATER.						
Gauge- pres-	pres-		Actual Expe-		Gauge- pres-	Theoretical.		Experi'tal Result			sults.
sure, pounds per sq. in.	Calculated from Theory.	 	rime	nt.	sure, pounds per sq. in.	Temp. discharge 180°.	Temp. discharge 212°.	н.	P.	м.	S.
•		H.	P.	М.		dis	T sg				
10	86.5	80.9			10						182°
20	25.6		19.9	21.5	20	1420	178°	1350	120°	1800	134
30	20.9	19.0	17.2	19.0	80	132	162	l			134
40	17.87	15.8	15.0	15.86	40	126	156	140	113	125	132
50	16.2	18.3	14.0	13.3	50	120	150	l			181
6 0	14.7		11.2		60	114	143		115	128	130
70	18.7		11.7		70	109	139	141*		123	130
80	12.9	11.4	11.2		80	105	134	141*	118	122	181
90	12.1				90	99	129			• • • • •	182*
100	11.5				100	95	125				132*
	1	1		1	120	87	117		•••	· · ·	134*
		J		l	150	77	107	ا ا		l • • • • l	121*

* Temperature of delivery above 212°. Waste-valve closed.

H, Hancock inspirator; P, Park injector; M, Metropolitan injector; S, Sellers 1876 injector.

Efficiency of the Injector.—Experiments at Cornell University, described by Prof. R. C. Carpenter, in Cassier's Magazine, Feb. 1892, show that the injector, when considered merely as a pump, has an exceedingly low efficiency, the duty ranging from 161,000 to 2,752,000 under different circumstances of steam and delivery pressure. Small direct-acting pumps, such as are used for feeding bollers, show a duty of from 4 to 8 million lbs., and the best pumping-engines from 100 to 140 million. When used for feeding water into a boller, however, the injector has a thermal efficiency of 100%, less the trifling loss due to radiation, since all the heat rejected passes into the water which is carried into the boiler.

The loss of work in the injector due to friction reappears as heat which is

The loss of work in the injector due to friction reappears as heat which is carried into the boiler, and the heat which is converted into useful work in the injector appears in the boiler as stored-up energy.

Although the injector thus has a perfect efficiency as a boiler-feeder, it is nevertheless not the most economical means for feeding a boiler, since it can draw only cold or moderately warm water, while a pump can feed water which has been heated by exhaust steam which would otherwise be wasted.

Performance of Injectors.—In Am. Mach., April 13, 1893, are a number of letters from different manufacturers of injectors in reply to the question: "What is the best performance of the injector in raising or lifting water to any height?" Some of the replies are tabulated below.

W. Sellers & Co.-25.51 lbs. water delivered to boiler per lb. of steam; tem-

perature of water, 64°; steam pressure, 65 lbs.
Schaeffer & Budenberg—1 gal. water delivered to boile for 0.4 to 0.8 lb.

Injector will lift by suction water of

186° to 183° 140° F. 122° to 118° 118° to 107° If boiler pressure is. 80 to 60 lbs. 60 to 90 lbs. 90 to 120 lbs. 120 to 150 lbs.

If the water is not over 80° F., the injector will force against a pressure 75 lbs. higher than that of the steam.

Lift in feet	22	22	22	11
Boiler pressure, absolute, lbs	75.8	54.1	95.5	75.4
Temperature of suction	34 .9°	85.4°	47.30	58.2°
Temperature of delivery	184°	117.40	178.70	131 . 1
Water fed per lb. of steam, lbs	11.02	18.67	8.18	18.8

The theory of the injector is discussed in Wood's, Peabody's, and Ront-

The theory of the injector is discussed in Wood's, Peabody's, and Rontgen's treatises on Thermodynamics. See also "Theory and Practice of the Injector," by Strickland L. Kneass, New York, 1895.

Boller-feeding Pumps.—Since the direct-acting pump, commonly used for feeding boilers, has a very low efficiency, or less than one tenth that of a good engine, it is generally better to use a pump driven by belt from the main engine or driving shaft. The mechanical work needed to feed a boiler may be estimated as follows: If the combination of boiler and engine is such that half a cubic foot saw 22 lbs of water is needed to present the procedure of the combination of boiler and engine is such that half a cubic foot saw 22 lbs of water is needed to present the combination of boiler and engine is such that half a cubic foot saw 22 lbs of water is needed to present the combination of boiler and engine is such that half a cubic foot saw 22 lbs of water is needed to present the combination of boiler and engine is such that half a cubic foot saw 22 lbs of water is needed to present the combination of boiler and engine is such that half a cubic foot saw 22 lbs of water is needed to present the combination of boiler and engine is such that half a cubic foot saw 22 lbs of water is needed to present the combination of boiler and engine is such that the combination of boiler and engine is such that the combination of boiler and engine is such that the combination of boiler and engine is such that the combination of boiler and engine is such that the combination of boiler and engine is such that the combination of boiler and engine is such that the combination of boiler and engine is such that the combination of boiler and engine is such that the combination of boiler and engine is such that the combination of boiler and engine is such that the combination of boiler and engine is such that the combination of boiler and engine is such that the combination of boiler and engine is such that the combination of boiler and engine is such a boiler may be estimated as follows: If the combination of boiler and engine is such that half a cubic foot, say 32 lbs. of water, is needed per horsepower, and the boiler-pressure is 100 lbs. per eq. in., then the work of feeding the quantity of water is 100 lbs. \times 144 sq. in. \times ½ ft.-lbs. per hour = 120 ft.-lbs. per min. = 120/83,000 = .0036 H.P., or less than 4/10 of 1% of the power exerted by the engine. If a direct-acting pump, which discharges its exhaust steam into the atmosphere, is used for feeding, and it has only 1/10 the efficiency of the main engine, then the steam used by the pump will be equal to nearly 4% of that senerated by the boiler. equal to nearly 4% of that generated by the boiler.

The following table by Prof. D. S. Jacobus gives the relative efficiency of

steam and power pumps and injector, with and without heater, as used upon a boiler with 80 lbs. gauge-pressure, the pump having a duty of 10,000,000 ft.-lbs. per 100 lbs. of coal when no heater is used; the injector heating the water from 60° to 150° F.

Direct-acting pump feeding water at 60°, without a heater	1.000 .985
Injector feeding water through a heater in which it is heated from 150° to 200°	.988
Direct-acting pump feeding water through a heater, in which it is heated from 60° to 200°	.879
Geared pump, run from the engine, feeding water through a heater, in which it is heated from 60° to 200°	.868

PERD-WATER HEATERS. Percentage of Saving for Each Degree of Increase in Temperature of Feed-water Heated by Waste Steam.

Initial Temp.	Atmosphere.										Initial Temp.	
Feed.	0	20	40	60	80	100	120	140	160	180	200	iomp.
82°	.0872	.0861	0855	.0851	0847	0844	.0841	.0839	.0887	.0885	.0888	32
40	.0878			.0856						.0841		
50		0875	0868	.0864	0860	0857	0854	0849	.0850			
60		.0883		.0872					.0856			
70		.0890						.0867				
80		.0898					.0877					80
90	.0919	.0907						.0888			.0875	
100	.0927	.0915		.0903				.0890				
110	.0936	.0928						.0898	.0895	.0898	.0891	110
120	.0945	.0982						.0906				
130	.0954							.0914				180
140	.0963	.0950	.0943	.0937	.0932	i.0929	.0925	. 0923	.0920	.0918	.0916	140
150	.0978	.0959	.0951	.0946	.0941	.0937	.0934	.0931	.0929	.0926	.0924	150
160	.0982							.0940	.0937	.0985	.0933	160
170	.0992							.0949				170
180	.1002					.0965				.0953		180
190		.0998			.0978	.0974	.0971	.0968	.0964	.0962	.0960	
200	.1022	.1008	.0999	.0993	.0988	.0984	.0980	.0977	.0974	.0972	.0969	200
210	.1033	.1018	.1009	.1003	.0998	.0994	.0990	.0987	.0984	.0981	.0979	210
220	l	.1029	.1019	. 1018	1.1008	.1004	.1000	.0997	.0994	.0991	.0989	220
230			.1031			. 1012		.1007		.1001		
240	1							.1017				
250		1.1062	1.1052	1.1045	.1040	. 1035	.1031	.1027	.1025	.1022	.1019	250

An approximate rule for the conditions of ordinary practice is a saving

An approximate further conditions of ordinary practice is a saving of 1% is made by each increase of 11° in the temperature of the feed-water. This corresponds to .0909% per degree.

The calculation of saving is made as follows: Boiler-pressure, 100 lbs, gauge; total heat in steam above 22° = 1185 B.T.U. Feed-water, original temperature 60°, final temperature 209° F. Increase in heat-units, 150. Heat-units above 32° in feed-water of original temperature = 28. Heat-units in steam above that in cold feed-water 1185 — 28 — 1187 Saving by the units in steam above that in cold feed-water, 1185 - 28 = 1157. Saving by the feed-water heater = 150/1157 = 12.90%. The same result is obtained by the use of the table. Increase in temperature 150° × tabular figure .0664 = 12.96%. Let total heat of 1 lb. of steam at the boiler-pressure = H; total heat of 1 lb. of feed-water before entering the heater $= h_1$, and after passheat of 1 lb. of feed-water perore entering the heater $= h_1$; then the saving made by the heater is $\frac{h_2 - h_1}{H - h_1}$

Strains Caused by Cold Feed-water.—A calculation is made in The Locomotive of March, 1893, of the possible strains caused in the section of the shell of a boiler by cooling it by the injection of cold feed-water. Assuming the plate to be cooled 200° F., and the coefficient of expansion of steel to be .0000067 per degree, a strip 10 in, long would contract .018 in., if it were free to contract. To resist this contraction, assuming that the strip is firmly held at the ends and that the modulus of elasticity is 29,000,000, would require a force of 87,700 lbs. per sq. in. Of course this amount of strain can-not actually take place, since the strip is not firmly held at the ends, but is allowed to contract to some extent by the elasticity of the surrounding metal. But, says The Locomotive, we may feel pretty confident that in the case considered a longitudinal strain of somewhere in the neighborhood of 8000 or 10,000 lbs. per sq. in. may be produced by the feed-water striking directly upon the plates; and this, in addition to the normal strain produced by the steam-pressure, is quite enough to tax the girth-seams beyond their elastic limit, if the feed-pipe discharges anywhere near them. Hence it is not surprising that the girth-seams develop leaks and cracks in 99 cases out of every 100 in which the feed discharges directly upon the firesheets.

STRAM SEPARATORS.

If moist steam flowing at a high velocity in a pipe has its direction sudthe mosts seam howing at a high velocity in a pipe has its direction such dealy changed, the particles of water are by their momentum projected in their original direction against the bend in the pipe or wall of the chamber in which the change of direction takes place. By making proper provision for drawing off the water thus separated the steam may be dried to a greater or less extent.

For long steam-pipes a large drum should be provided near the engine for trapping the water condensed in the pipe. A drum 3 feet diameter, 15 feet high, has given good results in separating the water of condensation of a steam-pipe 10 inches diameter and 800 feet long.

Efficiency of Steam Separators.—Prof. R. C. Carpenter, in 1891, made a series of tests of six steam separators, furnishing them with steam contains a different percentages of registure and testing the quality of

containing different percentages of moisture, and testing the quality of steam before entering and after passing the separator. A condensed table of the principal results is given below.

tor.	Test with	Steam of ab Moisture.	out 10% of	Tests with	Varying Mo	oisture.
Make of Separator.	Quality of Steam before.	Quality of Steam after.	Efficiency per cent.	Quality of Steam before.	Quality of Steam after.	Av'ge Effi- ciency.
. В	87.0%	98.8%	90.8	66,1 to 97.54	97.8 to 99%	87.6
	90.1	98.0	80.0	51.9 * 98	97.9 " 99.1	76.4
D	89.6	95.8	59.6	72.2 " 96.1	95.5 " 98.2	71.7
C	90.6	93.7	83.0	67.1 " 96.8	93.7 " 98.4	63.4
D C E F	88.4	90.2	15.5	68.6 " 98.1	79.3 " 98.5	36.9
F	88.9	92.1	28.8	70.4 " 97.7	84.1 " 97.9	28.4

Conclusions from the tests were: 1. That no relation existed between the volume of the several separators and their efficiency.

2. No marked decrease in pressure was shown by any of the separators, the most being 1.7 lbs. in E.

8. Although changed direction, reduced velocity, and perhaps centrifugal force are necessary for good separation, still some means must be provided to lead the water out of the current of the steam.

The high efficiency obtained from B and A was largely due to this feature. In B the interior surfaces are corrugated and thus catch the water thrown out of the steam and readily lead it to the bottom.

In A, as soon as the water falls or is precipitated from the steam, it comes in contact with the perforated diaphragm through which it runs into the space below, where it is not subjected to the action of the steam.

Experiments made by Prof. Carpenter on a "Stratton" separator in 1894 showed that the moisture in the steam leaving the separator was less than 15 when that in the steam supplied ranged from 6% to 21%.

DETERMINATION OF THE MOISTURE IN STRAM-STEAM CALORIMETERS.

In all boiler-tests it is important to ascertain the quality of the steam, i.e., 1st, whether the steam is "saturated" or contains the quantity of heat due to the pressure according to standard experiments; 2d, whether the quantity of heat is deficient, so that the steam is wet; and 8d. whether the quantity of heat is delicitied, so that the seam is very and it whether the heat is in excess and the steam superheated. The best method of ascer-taining the quality of the steam is undoubtedly that employed by a com-mittee which tested the boilers at the American Institute Exhibition of 1871-2, of which Prof. Thurston was chairman, i.e., condensing all the water

1871-2, of which Prof. Thurston was chairman, i.e., condensing all the water evaporated by the boiler by means of a surface condenser, weighing the condensing water, and taking its temperature as it enters and as it leaves the condenser; but this plan cannot always be adopted.

A substitute for this method is the barrel calorineter, which with careful operation and fairly accurate instruments may generally be relied on to give results within two per cent of accuracy (that is, a sample of stem which gives the apparent result of 2% of moisture may contain anywhere be tween 0 and 4%). This calorimeter is described as follows: A sample of the steam is taken by inserting a perforated ½-inch pipe into and through the main pipe near the boiler, and led by a hose, thoroughly felted, to a barrel, holding preferably 400 lbs. of water, which is set upon a platform scale and

provided with a cock or valve for allowing the water to flow to waste, and

with a small propeller for stirring the water

with a small propeller for surring the water.

To operate the calorimeter the barrel is filled with water, the weight and temperature ascertained, steam blown through the hose outside the barrel until the pipe is thoroughly warmed, when the hose is suddenly thrust into the water, and the propeller operated until the temperature of the water is increased to the desired point, say about 110° usually. The hose is then withdrawn quickly, the temperature noted, and the weight again taken.

An error of 1/10 of a pound in weighing the condensed steam, or an error of 1/20 of a pound in weighing the condensed steam, or an error of 1/2 degree in the temperature, will cause an error of over 1/2 in the calculated percentage of moisture. See Trans. A. S. M. E., vi. 298.

The calculation of the percentage of moisture is made as below:

$$Q = \frac{1}{H-T} \left[\frac{\widetilde{W}}{w} (h_1 - h) - (T - h_1) \right].$$

Q = quality of the steam, dry saturated steam being unity.
H = total heat of 1 lb. of steam at the observed pressure.
T = """ the temperature of the

water at the temperature of steam of the ob-

served pressure. condensing water, original. h = ..

apparatus. w = weight of the steam condensed.

Percentage of moisture = 1 - Q.

If Q is greater than unity, the steam is superheated, and the degrees of superheating = 2.0833 (H-T)(Q-1).

Difficulty of Obtaining a Correct Sample.—Recent experiments by Prof. D. S. Jacobus, Trans. A. S. M. E., xvi. 1017, show that it is practically impossible to obtain a true average sample of the steam flowing in a pipe. For accurate determinations all the steam made by the boiler should be passed through a separator, the water separated should be weighed, and a calorimeter test made of the steam just after it has passed the separator.

Coil Calorimeters.—Instead of the open barrel in which the steam

is condensed, a coil acting as a surface-condenser may be used, which is placed in the barrel, the water in coil and barrel being weighed separately. For description of an apparatus of this kind designed by the author, which he has found to give results with a probable error not exceeding ½ per cent of moleture, see Trans. A. S. M. E., vi. 294. This calorimeter may be used continuously, if desired, instead of intermittently. In this case a continuously, if desired, instead of intermittently. ous flow of condensing water into and out of the barrel must be established, and the temperature of inflow and outflow and of the condensed steam read at short intervals of time.

Throttling Calorimeter. - For percentages of moisture not exceeding 3 per cent the throttling calorimeter is most useful and convenient and remarkably accurate. In this instrument the steam which reaches it in a ½-inch pipe is throttled by an orifice 1/16 inch diameter, opening into a chamber which has an outlet to the atmosphere. The steam in this chamber has its pressure reduced nearly or quite to the pressure of the atmosphere, but the total heat in the steam before throttling causes the steam in the chamber to be superheated more or less according to whether the steam before throttling was dry or contained moisture. The only observations required are those of the temperature and pressure of the steam on

each side of the orifice.

The author's formula for reducing the observations of the throttling calorimeter is as follows (Experiments on Throttling Calorimeters, Am. Mach., Aug. 4, 1892): $w = 100 \times \frac{H - h - K(T - t)}{I}$, in which w = percent

age of moisture in the steam; H = total heat, and L = latent heat of steamin the main pipe; h = total heat due the pressure in the discharge side of the calorimeter, = 1146.6 at atmospheric pressure: K = specific heat of superheated steam; T = temperature of the throttled and superheated steam in the calorimeter; t =temperature due the pressure in the calorimeter, = 212° at atmospheric pressure.

Taking K at 0.48 and the pressure in the discharge side of the calorimeter

as atmospheric pressure, the formula becomes
$$w = 100 \times \frac{H - 1146.6 - 0.48(T - 212^{\circ})}{T}.$$

From this formula the following table is calculated:

MOISTURE IN STEAM-DETERMINATIONS BY THROTTLING CALORIMETER.

Super.					Ga	nge-t	ressu	res.				
Degree of Suheating, T-212°.	5	10	20	30	40	50	60	70	75	80	85	90
Degre				Per	Cent	of Mo	isture	in St	eam.			
0° 10° 20° 80° 40° 50° 60° 70°	0.51 0.01	0.90	1.54 1.02 .51 .00	2.06 1.54 1.02 .50	2.50 1.97 1.45 .92 .39	2.90 2.36 1.83 1.80 .77 .24	8.24 2.71 2.17 1.64 1.10 .57	8.56 8.02 2.48 1.94 1.40 .87 .33	8.71 8.17 2.68 2.09 1.55 1.01	3.86 3.32 2.77 2.23 1.69 1.15 .60	8.99 8.45 2.90 2.85 1.80 1.26 .72 .17	4.18 8.58 8.03 2.49 1.94 1.40 .85
Dif.p.deg	.0503	.0507	.0515	.0521	.0526	.0531	.0535	.0539	.0541	.0542	.0544	.0546
uper-					Gε	uge-p	ressu	res.				
Degree of Superheating $T = 212^{\circ}$.	100	110	120	130	140	150	160	170	180	190	200	250
Degra				Per	Cent	of Mo	isture	in S	team.			
0° 10° 20° 80° 40° 50° 60° 70° 80° 100° 110°	4.89 8.84 8.29 2.74 2.19 1.64 1.09 .55 .00	4.68 4.08 8.52 2.97 2.42 1.87 1.82 .77	4.85 4.29 8.74 8.18 2.68 2.08 1.52 .97 .42	2.85 2.29	5 29 4.73 4.17 8.61 8.05 2.49 1.93 1.88 .82 .26	5.49 4.98 4.87 8.80 8.24 2.68 2.12 1.56 1.00	5.68 5.12 4.56 3.99 3.43 2.87 2.30 1.74 1.18 .05	5.87 5.80 4.74 4.17 8.61 8.04 2.48 1.91 1.84 .21	6.05 5.48 4.91 4.34 8.78 8.21 2.64 2.07 1.50 .94	6.22 5.65 5.08 4.51 8.94 8.87 2.80 2.28 1.66 1.09	6.89 5.82 5.25 4.67 4.10 3.58 2.96 2.38 1.81 1.24 .67	7.16 6.58 6.00 5.41 4.83 4.25 8.67 8.09 2.51 1.98 1.34
Dif.p.deg	.0549	.0551	.0554	.0556	.0559	.0561	.0564	.0566	.0568	.0570	.0572	.0581

Separating Calorimeters.—For percentages of moisture beyond the range of the throttling calorimeter the separating calorimeter is used, which is simply a steam separator on a small scale. An improved form of this calorimeter is described by Prof. Carpenter in Power, Feb. 1893.

For fuller information on various kinds of calorimeters, see papers by Prof. Peabody, Prof. Carpenter, and Mr. Barrus in Trans. A. S. M. E., vols. xi. xii. 1889 to 1891; Appendix to Report of Com. on Boiler Tests, A. S. M. E., vol. vi, 1884; Circular of Schaener & Budenberg, N. Y., "Calorimeters, Throttling and Separating," 1894.

Identification of Dry Steam by Appearance of a Jet.—Prof. Denton (Trans. A. S. M. E., vol. x.) found that jets of steam show unnistakable change of appearance to the eye when steam varies less than 14

mistakable change of appearance to the eye when steam varies less than 1% from the condition of saturation either in the direction of wetness or superheating.

If a jet of steam flow from a boiler into the atmosphere under circumstances such that very little loss of heat occurs through radiation, etc., and the jet be transparent close to the orifice, or be even a grayish-white color, the steam may be assumed to be so nearly dry that no portable condensing calorimeter will be capable of measuring the amount of water in the steam. If the jet be strongly white, the amount of water may be roughly judged up to about 2%, but beyond this a calorimeter only can determine the exact amount of moisture.

A common brass pet-cock may be used as an orifice, but it should, if possible, be set into the steam-drum of the boiler and never be placed further away from the latter than 4 feet, and then only when the intermediate reservoir or pipe is well covered.

Usual Amount of Moisture in Steam Escaping from a Boiler.—In the common forms of horizontal tubular land boilers and water-tube boilers with ample horizontal drums, and supplied with water free from substances likely to cause foaming, the moisture in the steam does not generally exceed 25 unless the boiler is overdriven or the waterlevel is carried too high.

CHIMNEYS.

Chimney Draught Theory.-The commonly accepted theory of chimney draught, based on Peclet's and Rankine's hypotheses (see Rankine, S. E.), is discussed by Prof. De Volson Wood in Trans. A. S. M. E., vol. xi. Peclet represented the law of draught by the formula

$$h=\frac{u^2}{2g}\Big(1+G+\frac{fl}{m}\Big),$$

in which h is the "head," defined as such a height of hot gases as, if added to the column of gases in the chimney, would produce the same pressure at the furnace as a column of outside air, of the same area of base, and a height equal to that of the chimney;

u is the required velocity of gases in the chimney; G a constant to represent the resistance to the passage of air through the coal;
the length of the flues and chimney;

m the mean hydraulic depth or the area of a cross-section divided by the perimeter:

f a constant depending upon the nature of the surfaces over which the gases pass, whether smooth, or sooty and rough.

Rankine's formula (Steam Engine, p. 288), derived by giving certain values to the constants (so-called) in Peclet's formula, is

$$h = \frac{\frac{\tau_0}{\tau_2} \left(0.0807\right)}{\frac{\tau_0}{\tau_1} \left(0.084\right)} H - H = \left(0.98 \frac{\tau_1}{\tau_3} - 1\right) H;$$

in which H= the height of the chimney in feet; $\tau_0=493^\circ$ F., absolute (temperature of melting ice); $\tau_1=$ absolute temperature of the gases in the chimney;

 τ_2 = absolute temperature of the external air.

Prof. Wood derives from this a still more complex formula which gives the height of chimney required for burning a given quantity of coal per second, and from it he calculates the following table, showing the height of chimney required to burn respectively 24, 20, and 16 lbs. of coal per square foot of grate per hour, for the several temperatures of the chimney gases given.

	Chimne	y Gas.	Coal per sq. f	t. of grate p	er hour, lbs.
Outside Air.	7,	Temp.	24	20	16
	Absolute.	Fahr.	Не	ight <i>H</i> , feet.	
520° absolute or 59° F.	700 800 1000 1100 1200 1400 1600 2000	289 889 589 689 789 989 1189	250.9 172.4 149.1 148.8 152.0 159.9 168.8 206.5	157.6 115.8 100.0 98.9 100.9 105.7 111.0 182.2	67.8 55.7 48.7 48.2 49.1 51.3 58.5 63.0

Rankine's formula gives a maximum draught when $\tau=2$ 1/12 r_2 , or 622° F., when the outside temperature is 60°. Prof. Wood says: "This result is not a fixed value, but departures from theory in practice do not affect the result largely. There is, then, in a properly constructed chimney, properly working, a temperature giving a maximum draught," and that temperature is not far from the value given by Rankine, although in special cases it may be 50° or 75° more or less."

All attempts to base a practical formula for chimneys upon the theoretical formula of Peclet and Rankine have failed on account of the impossibility of assigning correct values to the so-called "constants" G and f. (See Trans. A. S. M. E., xi. 984.)

Worce or Intensity of Braught.—The force of the draught is equal to the difference between the weight of the column of hot gases inside of the chimney and the weight of a column of the external air of the same height. It is measured by a draught-gauge, usually a U-tube partly filled with water, one leg connected by a pipe to the interior of the flue, and the other open to the external air.

If D is the density of the air outside, d the density of the hot gas inside, in list per cubic foot, h the height of the chimney in feet, and .192 the factor for converting pressure in lbs. per sq. ft. into inches of water column, then the formula for the force of draught expressed in inches of water is,

$$F = .192h(D-d).$$

The density varies with the absolute temperature (see Rankine).

$$d = \frac{\tau_0}{\tau_1} 0.084; \quad D = 0.0807 \frac{\tau_0}{\tau_2},$$

where τ_0 is the absolute temperature at 32° F.. = 493., τ_1 the absolute temperature of the chimney gases and τ_2 that of the external air. Substituting these values the formula for force of draught becomes

$$F = .192h \left(\frac{39.79}{\tau_2} - \frac{41.41}{\tau_1} \right) = h \left(\frac{7.64}{\tau_3} - \frac{7.95}{\tau_1} \right).$$

To find the maximum intensity of draught for any given chimney, the heated column being 600° F., and the external air 60°, multiply the height above grate in feet by .0073, and the product is the draught in linches of water. Height of Water Column Due to Unbalanced Pressure in Chimney 100 Feet High. (The Locomotive, 1884.)

			, 10	U A C	OU ARA	<u> </u>	(1/100 1	2000	******	~,	
Temp. in the Chimuey.	Ten	_	<u> </u>			∆ir—				-	
2 5	00	10°	20°	30°	40°	50°	60°	700	80°	90°	1000
200	.458	.419	.384	.858	.821	.292	.268	.284	.209	.182	.157
2:20	.488	.453	.419	.388	.855	.826	.298	269	.244	.217	.192
240	.520	.488	.451	.421	.888	.859	.880	.301	.276	.250	.225
260	.555	.528	.484	.453	.420	.392	.868	.834	.809	.289	.257
280	.584	.549	.515	.482	.451	.422	.894	.865	.840	.813	.288
800	.611	.576	.541	.511	.478	.449	.420	.392	.367	.840	.815
320	.687	.603	.568	.588	.505	.476	.447	.419	.894	.367	.842
340	.662	.688	.593	.563	.580	.501	.472	.443	.419	.392	.367
860	.687	.658	.618	.588	.555	.526	.497	.468	.444	.417	.892
880	.710	.676	.641	.611	.578	.549	.520	.492	.467	.440	.415
400	.782	.697	.662	.632	.599	.570	.541	.518	.488	.461	.436
420	.758	.718	.684	.658	.620	.591	.568	.584	.509	.482	.457
440	.774	.789	.705	.674	.641	.612	.584	.555	.580	.508	.478
460	.798	.758	.724	.694	.660	.632	.608	.574	.549	.522	.497
480	.810	.776	.741	.710	.678	.649	.620	.591	.566	.540	.515
500	. 829	.791	.760	.780	.697	.669	.639	.610	.586	.559	.534

^{*}Much confusion to students of the theory of chimneys has resulted from their understanding the words maximum draught to mean maximum intensity or pressure of draught, as measured by a draught-gauge. It here means maximum quantity or weight of gases passed up the chimney. The maximum intensity is found only with maximum temperature, but after the temperature reaches about 622° F. the density of the gas decreases more rapidly than its velocity increases, so that the weight is a maximum about 622° F., as shown by Rankine.—W. K.

For any other height of chimney than 100 ft, the height of water column s found by simple proportion, the height of water column being directly proportioned to the height of chimney.

The calculations have been made for a chimney 100 ft, high, with various emperatures outside and inside of the flue, and on the supposition that the emperature of the chimney is uniform from top to bottom. This is the asis on which all calculations respecting the draught-power of chimneys have been made by Rankine and other writers, but it is very far from the ruth in most cases. The difference will be shown by comparing the readng of the draught-gauge with the table given. In one case a chimney 122 ft. 11gh showed a temperature at the base of 320°, and at the top of 230°.

Box, in his "Treatise on Heat," gives the following table:

DRAUGHT POWERS OF CHIMNEYS, ETC., WITH THE INTERNAL AIR AT 552°, AND THE EXTERNAL AIR AT 62°, AND WITH THE DAMPER NEARLY CLOSED.

it of ey in t.	ght n ins. ter.	Theoretica in feet pe		it of ey in t.	ght n ins. ter.	Theoretica in feet per	
Heigh Chimn fee	Drau Power i	Cold Air Entering.	Hot Air at Exit.	Heigh Chimn fee	Draug Power i	Cold Air Entering.	Hot Air at Exit.
10	.073	17.8	35.6	80	.585	50.6	101.2
20	.146	25.3	50.6	90	.657	53.7	107.4
30	.219	81.0	62.0	100	.730	56.5	118.0
40 50	.292	85.7	71.4	120	.876	62.0	124.0
50	.365	40.0	80.0	150	1.095	69.3	138.6
60	.438	48.8	87.6	175	1.277	74.8	149.6
70	.511	47.3	94.6	200	1.460	80.0	160.0

Hate of Combustion Due to Height of Chimney.—
Irowbridge's "Heat and Heat Engines" gives the following table showing
he heights of chimney for producing certain rates of combustion per sq.
t. of section of the chimney. It may be approximately true for anthractic
n moderate and large sizes, but greater heights than are given in the table
re needed to secure the given rates of combustion with small sizes of
inthractic, and for bituminous coal smaller heights will suffice if the coal
a researchyly free from set.—See researchy. 3 reasonably free from ash-5% or less.

Heights in feet.	Lbs. of Coal Burned per Hour per Sq. Ft. of Section of Chimney.	Lbs. of Coal Burned per Sq. Ft. of Grate, the Ratio of Grate to Sec- tion of Chimney be- ing 8 to 1.	Heights in feet.	of Chimney.	Lbs. of Coal Burned per Sq. Ft. of Grate, the Ratio of Grate to Sec- tion of Chimney be- ing 8 to 1.
20 25 80 85 40 45 50 58 60	60 68 76 84 98 99 105 111 116	7.5 8.5 9.5 10.5 11.6 12.4 18.1 13.8 14.5	70 75 80 85 90 95 100 105 110	. 126 181 185 189 144 148 152 156	15.8 16.4 16.9 17.4 18.0 18.5 19.0 19.5 20 0

Thurston's rule for rate of combustion effected by a given height of chimey (Trans. A. S. M. E., xi. 991) is: Subtract 1 from twice the square root of the height, and the result is the rate of combustion in pounds per square foot ' grate per hour, for anthracite. Or rate = $2\sqrt{h} - 1$, in which h is the eight in feet. This rule gives the following:

h = 50ഭവ 70 80 90 100 110 125 150 175 900 $\sqrt{h} - 1 = 13.14$ 14.49 15.78 16.89 17.97 19 19.97 21.36 23.49 25.45 27.28 The results agree closely with Trowbridge's table given above. In "

tice the high rates of combustion for high chimneys given by the formula are not generally obtained, for the reason that with high chimneys there are usually long horizontal flues, serving many boilers, and the friction and the interference of currents from the several boilers are apt to cause the inteninterference of currents from the several boilers are apt to cause the intensity of draught in the branch flues leading to each boiler to be much less than that at the base of the chimney. The draught of each boiler is also usually restricted by a damper and by bends in the gas-passages. In a bettery of several boilers connected to a chimney 150 ft. high, the author found a draught of %-inch water-column at the boiler nearest the chimney and only %-inch at the boiler farthest away. The first boiler was wasting fuel from too high temperature of the chimney-gases, 900°, having too large a grate-surface for the draught, and the last boiler was warking below its rated capacity and with poor economy, on account of insufficient draught. The effect of changing the length of the flue leading into a chimney 60 ft. high and 2 ft. 9 in square is given in the following table, from Box on

high and 2 ft. 9 in. square is given in the following table, from Box on "Heat":

Length of Flue in feet.	Horse-power.	Length of Flue in feet.	Horse-power.
50	107.6	800	56.1
100	100.0	1.000	51.4
200	85.3	1.500	48.8
400	70.8	2,000	88.2
600	62.5	8,000	81.7

The temperature of the gases in this chimney was assumed to be 552° F... and that of the atmosphere 62°.

High Chimneys not Necessary.—Chimneys above 150 ft. in height are very costly, and their increased cost is rarely justified by increased efficiency. In recent practice it has become somewhat common to build two or ncelency. In recent practice it has become somewhat common to uniat two or more smaller chimneys instead of one large one. A notable example is the Spreckels Sugar Refinery in Philadelphia, where three separate chimneys are used for one boiler-plant of 7500 H.P. The three chimneys are said to have cost several thousand dollars less than a single chimney of their combined capacity would have cost. Very tall chimneys have been characterised by one writer as a 'monument to the folly of their builders'. one writer as "monuments to the folly of their builders."

Heights of Chimney required for Different Fuels.—The minimum height necessary varies with the fuel, wood requiring the least, then good bituminous coal, and fine sizes of onthractic the greatest. It also varies with the character of the boiler—the smaller and more circuitous the gas-passages the higher the stack required; also with the number of boilers, a single boiler requiring less height than several that discharge into a horizontal flue. No general rule can be given.

SIZE OF CHIMNEYS.

The formula given below, and the table calculated therefrom for chimneys The formula given below, and the table calculated therefrom for cnimneys up to 96 in. diameter and 200 ft. high, were first published by the author in 1884 (Trans. A. S. M. E. vi., 81). They have met with much approval since that date by engineers who have used them, and have been frequently published in boiler-makers' catalogues and elsewhere. The table is now extended to cover chimneys up to 12 ft. diameter and 300 ft. high. The sizes corresponding to the given commercial horse-powers are believed to be ample for all cases in which the draught areas through the boiler-flues and connections are sufficient; say not less than 20° greater than the area of the

ample for all cases in which the draught areas through the boiler-flues and connections are sufficient, say not less than 20% greater than the area of the chimney, and in which the draught between the boilers and chimney is not checked by long horizontal passages and right-angled bends.

Note that the figures in the table correspond to a coal consumption of 5 lbs. of coal per horse-power per hour. This liberal allowance is made to cover the contingencies of poor coal being used, and of the boilers being driven beyond their rated capacity. In large plants, with economical boilers and engines, good fuel and other favorable conditions, which will reduce the maximum rate of coal consumption at any one time to less than 5 lbs. premaximum rate of coal consumption at any one time to less than 5 lbs. per H. P. per bour, the figures in the table may be multiplied by the ratio of 5 to the maximum expected coal consumption per H.P. per hour. Thus, with conditions which make the maximum coal consumption only 2.5 lbs, per hour, the chimney 800 ft. high \times 12 ft. diameter should be sufficient for 6155 \times 2 = 12,310 horse-power. The formula is based on the following data:

Formula, H.P. = $3.38(A-0.6 \sqrt{A}) \sqrt{H}$. (Assuming 1 H.P. ≈ 5 lbs. of cosl burned per hour.) Size of Chimneys for Steam-bollers.

									Heig	Height of Chimney.	imney.						
Diam. Inches.	Area 4. sq. ft.	Effective Area. $E=A-0.6 \sqrt{A}$.	30 ft.	80 ft.	£ £	8 ‡	13 13	100 ft.	110 ft.	125 ft.	150 ft.	175 ft.	200 ft.	226 ft.	250 ft.	300 ft.	Equivalent Square Chimney. Side of Square
		.d. 10.						Comi	mercial	Commercial Horse-power of Boiler.	ower of	Boiler.					$\sqrt{E} + 4$ inches.
2222	1.000	1.47 1.47 2.08 2.78	22843	2283	2288	8488	288										\$10 \$20 \$30 \$40 \$40 \$40 \$40 \$40 \$40 \$40 \$40 \$40 \$4
8888	4.05.8 19.92 19.05 19.05	6.54.0 6.54.0 6.4.18	2	25.23	5828	5888	113 173 208	119 149 182 193	25 23	22	898						2888
4448	12.57 15.90 19.62	7.76 10.44 13.51 16.98			916	55 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	3828	2225	25.55 25.55	8858 8858	816 551 693	25.52	86.88 80.88 80.88	848 848	25		8332
2552	23.76 28.27 38.18	8.55.38 8.52.38 8.52.55						288	728 876 1038 1214	5.20 100 100 100 100 100 100 100 100 100 1	849 1023 1418	918 1105 1310 1531	1181 1400 1637	1046 1786 1786	1097 1586 1586	1901 1447 1715 2005	3322
8822	44.18 50.27 56.75 63.62	6233 61233 61233 8								1496 1719 1944 2090	1639 1876 2399	1770 1500 1500 1500 1500 1710	1893 2167 2469 2771	9999 9999 9999 9999 9999 9999 9999 9999 9999	\$116 \$750 \$098	2318 2654 3012 3393	2253
 1887	70.88 78.54 95.03	25.83 26.22 26.72									2086 2086 2087 2087	2000 3226 3929 4701	\$100 \$448 \$300 \$300	88.8 15.6 15.6 15.6 15.6 15.6 15.6 15.6 15.6	9866 9866 4696 5618	3797 4223 5144 6156	101 117 117 88

1. The draught power of the chimney varies as the square root of the

height.

neight.

2. The retarding of the ascending gases by friction may be considered as equivalent to a diminution of the area of the chimney, or to a lining of the chimney by a layer of gas which has no velocity. The thickness of this lining is assumed to be 2 inches for all chimneys, or the diminution of area equal to the perimeter \times 2 inches (neglecting the overlapping of the corners of the lining). Let D = diameter in feet, A = area, and E = effective areain square feet.

For square chimneys,
$$E = D^2 - \frac{8D}{12} = A - \frac{2}{8} \sqrt{A}$$
.

For round chimeys,
$$E = \frac{\pi}{4} \left(D^2 - \frac{8D}{12} \right) = A - 0.591 \sqrt{A}$$
.

For simplifying calculations, the coefficient of \sqrt{A} may be taken as 0.6 for both square and round chimneys, and the formula becomes

$$E = A' - 0.6 \sqrt{A}.$$

3. The power varies directly as this effective area E.

4. A chimney should be proportioned so as to be capable of giving sufficient draught to cause the boiler to develop much more than its rated power, in case of emergencies, or to cause the combustion of 5 lbs. of fuel per rated

horse-power of boiler per hour.

5. The power of the chimney varying directly as the effective area, E, and as the square root of the height, H, the formula for horse-power of boiler for a given size of chimney will take the form H.P. = $CE\sqrt{H}$, in which C is a constant, the average value of which, obtained by plotting the results obtained from numerous examples in practice, the author finds to be 3.83.

The formula for horse-power then is

H.P. =
$$8.83E\sqrt{H}$$
, or H.P. = $8.83(A - .6\sqrt{A})\sqrt{H}$.

If the horse-power of boiler is given, to find the size of chimney, the height being assumed,

$$E = 0.3 \text{ H.P.} + \sqrt[4]{H.}; = A - 0.6 \sqrt[4]{A}$$

For round chimneys, diameter of chimney = diam. of E + 4''.

For square chimneys, side of chimney = $\sqrt{E} + 4$ ". If effective area E is taken in square feet, the diameter in inches is d =13.54 \sqrt{E} + 4", and the side of a square chimney in inches is $s = 12 \sqrt{E}$ + 4".

If horse-power is given and area assumed, the height
$$H = \left(\frac{0.3 \text{ H.P.}}{E}\right)^3$$
. In proportioning chimneys the height is generally first assumed, with due production to the heights of surrounding buildings as kills was to the

In proportioning chimneys the height is generally first assumed, with due consideration to the heights of surrounding buildings or hills near to the proposed chimney, the length of horizontal flues, the character of coal to be used, etc., and then the diameter required for the assumed height and horse-power is calculated by the formula or taken from the table.

216 $D^2\sqrt{H}$. This gives the H.P. somewhat greater than the figures in the table. An approximate formula for chimneys above 1000 H.P. is H.P. =

The Protection of Tail Chimney-shafts from Lightning.

C. Molyneux and J. M. Wood (Industries, March 28, 1890) recommend for tail chimneys the use of a coronal or heavy band at the top of the chimney, with copper points 1 ft. in height at intervals of 2 ft. throughout the circumference. The points should be gilded to prevent oxidation. The most approved form of conductor is a copper tape about ½ in. by ½ in. thick, weighing 6 ozs. per ft. If iron is used it should weigh not less than 2½ lbs. per ft. There must be no insulation, and the copper tape should be fastened to the chimney with holdfasts of the same material, to prevent voltade action. An allowance for expansion and contraction should be made, say in. in 40 ft. Slight bends in the tape, not too abrupt, answer the purpose. For an earth terminal a plate of metal at least 8 ft. sq. and 1/16 in. thick should be buried as deep as possible in a damp spot. The plate should be of the same metal as the conductor, to which it should be soldered. The best earth terminal is water, and when a deep well or other large body of water earth terminal is water, and when a deep well or other large body of water is at hand, the conductor should be carried down into it. Right-angled heads in the conductor should be avoided. No bend in it should be over 30°.

Some Tall Brick Chimneys.

		Diam.	Outs Diam		Aut	y by the hor's mula.
	Height.	Internal	Base.	Top.	н. Р.	Pounds Coal per hour,
1. Hallsbrückner Hütte, Sax.	460	15.7′	83′	16'	13,221	66,105
2. Townsend's, Glasgow	454		82			
8. Tennant's, Glasgow	485	18' 6''	40		9,795	48,975
4. Dobson & Barlow, Bolton,	86716	13' 2''	33′10′′		8,245	41,225
Eng 5. Fall River Iron Co., Boston	850	11	80	21	5,558	27,790
6. Clark Thread Co., Newark,			00	21	0,566	21,100
N. J.	335	11	28' 6"	14	5,485	27,175
7. Merrimac Mills, Low'l, Mass		12	"		5,980	29,900
8. Washington Mills, Law-	l				1	1
rence, Mass	250	10	1		8,839	19,195
Amoskeag Mills, Manches-			1	l		
ter, N. H	250	10			8,839	19,195
10. Narragansett E. L. Co.,	000	مه ا		1		00 505
Providence, R. I	288	14			7,515	87,575
11. Lower Pacific Mills, Law- rence, Mass	214	8	1		2,248	11,240
12. Passaic Print Works, Pas-			1	ł	~,~=0	11,220
saic, N. J	200	۱۹	1	Ī	2,771	13,855
18. Edison Sta, B'klyn, Two e'ch		50" × 120"	1	each		7,705

Notes on the right bank of the Mulde, at an elevation of 219 feet above that of the foundry works, so that its total height above the sea will be 711% feet. The works are situated on the bank of the river, and the furnace-gases are conveyed across the river to the chimney on a bridge, through a pipe 8227 feet in length. It is built throughout of brick, and will cost about \$40,000.—Mfr. and Bldr.

2. Owing to the fact that it was struck by lightning, and somewhat damaged, as a precautionary measure a copper extension subsequently was added to it, making its entire height 488 feet.

1, 2, 3, and 4 were built of these great heights to remove deleterious gases from the neighborhood, as well as for draught for boilers.

sases from the neignborhood, as well as for draught for oblers.

5. The structure rests on a solid granite foundation, 55 × 30 feet, and 16 feet deep. In its construction there were used 1,700,000 bricks, 2000 to stote, 2000 barrels of mortar, 1000 loads of sand, 1000 barrels of Portland cement, and the estimated cost is \$40,000. It is arranged for two flues, 9 feet 6 inches by 6 feet, connecting with 40 bollers, which are to be run in connection with four triple-expansion engines of 1850 horse-power each.

connection with four triple-expansion engines of 1350 horse-power each.

6. It has a uniform batter of 2.85 inches to every 10 feet. Designed for 21 boilers of 200 H. P. each. It is surmounted by a cast-iron coping which weighs six tons, and is composed of thirty-two sections, which are boiled together by inside flanges, so as to present a smooth exterior. The foundation is in concrete, composed of crushed limestone 6 parts, sand 3 parts, and Portland cement 1 part. It is 40 feet square and 5 feet deep. Two qualities of brick were used; the outer portions were of the first quality North River, and the backing up was of good quality New Jersey brick. Every twenty feet in vertical measurement an iron ring, 4 inches wide and 34 to 14 inch thick, placed edgewise, was built into the walls about 8 inches from the outer circle. As the chimney starts from the base it is double. The outer wall is 5 feet 2 inches in thickness, and inside of this is a second wall 20 inches thick and spaced off about 20 inches from main wall. From the interior surface of the main wall eight butresses are carried, nearly touching this inner or main flue wall in order to keep it in line should it tend to sag. The interior wall, starting with the thickness described, is gradually reduced until a height of about 20 feet is reached, when it is diminished to 8 luches. At 165 feet it ceases,

and the rest of the chimney is without lining. The total weight of the chimney and foundation is 5000 tons. It was completed in September, 1888.
7. Connected to 12 boilers, with 1200 square feet of grate-surface. Draught-

gauge 1 9/16 inches. 8. Connected to 8 boilers, 6'8" diameter × 18 feet. Grate-surface 448

zguare feet. 9. Connected to 64 Manning vertical boilers, total grate surface 1810 sq. ft.

Designed to burn 18,000 lbs. anthracite per hour.

Designed to burn 18,000 hep. of engines; (compound condensing),
10. Designed for 12,000 h.P. of engines; (compound condensing),
11. Grate-surface 434 square feet; H.P. of boilers (Galloway) about 2500.
13. Eight boilers (water-tube) each 450 H.P.; 12 engines, each 300 H.P. Plant designed for 36,000 incandescent lights. For the first 60 feet the exterior wall is 23 inches thick, then 24 inches for 20 feet, 20 inches for 30 feet, 16 inches for 20 feet, and 12 inches for 20 feet. The interior wall is 9 inches thick of fire-brick for 50 feet, and then 8 inches thick of red brick for the next 30 feet. Illustrated in Iron Age, January 2, 1890.

A number of the above chimneys are illustrated in Power, Dec., 1890.
Chimney at Knoxyille. Tenn., illustrated in Emo'o News. Nov. 2, 1893.

Chimney at Knoxville, Tenn., illustrated in Eng'g News, Nov. 2, 1893. 6 feet diameter, 120 feet high, double wall:

Exterior wall, height 20 feet, 30 feet, 30 feet, 40 feet, 41 feet thickness 21½ in., 17 in., 13 in., 8½ in., 11 in., 8½ in., 11 in., 8½ in., 12 in., 29 ft., 29 ft., 25 ft., 2 20 feet, 80 feet, 80 feet, 40 feet;

Exterior diameter, 15' 6" at bottom; batter, 7/16 inch in 12 inches from bottom to 8 feet from top. Interior diameter of inside wall, 6 feet uniform to top of interior wall. Space between walls, 16 inches at bottom, diminishing to 0 at top of interior wall. The interior wall is of red brick except a lining of 4 inches of fire-brick for 20 feet from bottom.

Stability of Chimneys.—Chimneys must be designed to resist the maximum force of the wind in the locality in which they are built, (see Weak Chimneys, below). A general rule for diameter of base, of brick chimneys, approved by many years of practice in England and the Inited

Weak Chimneys, below). A general rule for diameter of base, of brick chimneys, approved by many years of practice in England and the United States, is to make the diameter of the base one tenth of the height. If the chimney is square or rectangular, make the diameter of the inscribed circle of the base one tenth of the height. The "batter "or taper of a chimney should be from 1/16 to 14 inch to the foot on each side. The brickwork should be one brick (8 or 9 inches) thick for the first 25 feet from the top, increasing 14 brick (4 or 414 inches) for each 25 feet from the top downwards. If the inside diameter exceed 5 feet, the top length should be 114 bricks; and if under 3 feet, it may be 14 brick for ten feet.

(From The Locomotive, 1834 and 1836.) For chimneys of four feet in diameter and one hundred feet high, and upwards, the best form is circular, with a straight batter on the outside. A circular chimney of this size, in addition to being cheaper than any other form, is lighter, stronger, and looks much better and more shapely.

better and more shapely.

Chimneys of any considerable height are not built up of uniform thickness. from top to bottom, nor with a uniformly varying thickness of wall, but the

wall, heaviest of course at the base, is reduced by a series of steps.

Where practicable the load on a chimney foundation should not exceed two tons per square foot in compact sand, gravel, or loam. Where a solid rock-bottom is available for foundation, the load may be greatly increased. If the rock is sloping, all unsound portions should be removed, and the face dressed to a series of horizontal steps, so that there shall be no tendency to

slide after the structure is finished.

slide after the structure is finished.

All boller-chimneys of any considerable size should consist of an outer stack of sufficient strength to give stability to the structure, and an inner stack or core independent of the outer one. This core is by many engineers extended up to a height of but 50 or 60 feet from the base of the chimney, but the better practice is to run it up the whole height of the chimney; it may be stopped off, say, a couple feet below the top, and the outer shell contracted to the area of the core, but the better way is to run it up to about 6 or 12 inches of the top and not contract the outer shell. But under no circumstances should the core at its upper end be bullt into or connected with the outer stack. This has been done in several instances by bricklayers, and the outer stack. This has been done in several instances by bricklayers, and the result has been the expansion of the inner core which lifted the top of the outer stack squarely up and crecked the brickwork. For a height of 100 feet we would make the outer shell in three steps, the

first 30 feet high, 16 inches thick, the second 80 feet high, 12 inches thick, the

third 50 feet high and 8 inches thick. These are the minimum thicknesses admissible for chimneys of this height, and the batter should be not less than 1 in 36 to give stability. The core should also be built in three steps, isan 1 in 36 to give stability. The core should also be built in three steps, such of which may be about one-third the height of the chimney, the lowest 12 inches, the middle 8 inches, and the upper step 4 inches thick. This will insure a good sound core. The top of a chiuney may be protected by a sast-fron cap; or perhaps a cheaper and equally good plan is to lay the mamental part in some good cement, and plaster the top with the same material.

Weak Chimneys.—James B. Francis, in a report to the Lawrence Mfg. Co. in 1873 (Eng g News, Aug. 28, 1880), gives some calculations concerning the probable effects of wind on that company's chimney as then constructed. Its outer shell is octagonal. The inner shell is cylindrical, with an air-space between it and the outer shell; the two shells not being bonded together, except at the openings at the base, but with projections in the brickwork, at intervals of about 20 ft. in height, to afford lateral superty by contact of the two shells. The principal dimensions of the chimney port by contact of the two shells. The principal dimensions of the chimney are as follows :

Height above the surface of the ground	211 ft.
Diameter of the inscribed circle of the octagon near the ground	. 15 **
Diameter of the inscribed circle of the octagon near the top	10 ft. 134 in.
Thickness of the outer shell near the base, 6 bricks, or	2814 in.
Thickness of the outer shell near the top, 3 bricks, or	. 1112 "
Thickness of the inner shell near the base, 4 bricks, or	. 15 4
Thickness of the inner shell near the top, 1 brick, or	. 8% "

One tenth of the height for the diameter of the base is the rule commonly adopted. The diameter of the inscribed circle of the base of the Lawrence Manufacturing Company's chimney being 15 ft., it is evidently much less than is usual in a chimney of that height.

Soon after the chimney was built, and before the mortar had hardened, it was found that the top had swayed over about 29 in. toward the east. This was evidently due to a strong westerly wind which occurred at that time. it was soon brought back to the perpendicular by sawing into some of the

joints, and other means.

The stability of the chimney to resist the force of the wind depends mainly on the weight of its outer shell, and the width of its base. The cohesion of the mortar may add considerably to its strength; but it is too uncertain to be relied upon. The inner shell will add a little to the stability, but it may be cracked by the heat, and its beneficial effect, if any, is too uncertain to

e taken into account.

The effect of the joint action of the vertical pressure due to the weight of he chimney, and the horizontal pressure due to the force of the wind is to hift the centre of pressure at the base of the chimney, from the axis toward one side, the extent of the shifting depending on the relative magnitude of the two forces. If the centre of pressure is brought too near the ide of the chimney, it will crush the brickwork on that side, and the chimlee of the chimney, it will crush the brickwork on that side, and the chim-ley will fall. A line drawn through the centre of pressure, perpendicular to he direction of the wind, must leave an area of brickwork between it and he side of the chimney, sufficient to support half the weight of the chim-ley; the other half of the weight being supported by the brickwork on the rindward side of the line.

rindward side of the line.

Different experimenters on the strength of brickwork give very different esuits. Kirkaldy found the weights which caused several kinds of bricks, sid in hydraulic lime mortar and in Roman and Portland cements, to fail lightly, to vary from 19 to 60 tons (of 2000 lbs.) per sq. ft. If we take in this see 22 tons per sq. ft., as the weight that would cause it to begin to fail, we hall not err greatly. To support half the weight of the outer shell of the himney, or 5:22 tons, at this rate, requires an area of 12.88 sq. ft. of brickwork. From these data and the drawings of the chimney, Mr. Francis calulates that the area of 12.88 sq. ft. is contained in a portion of the chimney xtending 2.428 ft. from one of its octagonal sides, and that the limit to high the centre of pressure may be shifted is therefore 5.072 ft. from the xis. If shifted beyond this, he says, on the assumption of the strength f the brickwork, it will crush and the chimney will fall.

Calculating that the wind-pressure can affect only the upper 141 ft. of the himney, the lower 70 ft. being protected by buildings, he calculates that a ind-pressure of 44 02 lbs. per sq. ft. would blow the chimney down.

Rankine, in a paper printed in the transactions of the Institution of Engi-

neers, in Scotland, for 1867-68, says: "It had previously been ascertained by observation of the success and failure of actual chimneys, and especially of those which respectively stood and fell during the violent storms of 1856 that, in order that a rund chimney may be sufficiently stable, its weight should be such that a pressure of wind, of about 55 lbs. per sq. ft. of a plane surface, directly facing the wind, or 27½ lbs. per sq. ft. of the plane projection of a cylindrical surface, . . . shall not cause the resultant pressure at any bed-joint to deviate from the axis of the chimney by more than one quarter of the outside diameter at that joint,"

According to Rankine's rule, the Lawrence Mfg. Co.'s chimney is adapted to a maximum pressure of wind on a plane acting on the whole height of 18.80 lbs. per sq. ft., or of a pressure of 21.70 lbs. per sq. ft. acting on the uppermost 141 ft. of the chimney.

Steel Chimneys are largely coming into use, especially for tall chimneys of iron-works, from 150 to 300 feet in height. The advantages claimed are: greater strength and safety; smaller space required; smaller cost, by 30 to 50 per cent, as compared with brick chimneys; avoidance of infiltration of air and consequent checking of the draught, common in brick chimneys. They are usually made cylindrical in shape, with a wide curved flare for 10 to 25 feet at the bottom. A heavy cast-iron base-plate is provided, to which the chimney is riveted, and the plate is secured to a massive foundation by holding-down bolts. No guys are used. F. W. Gordon, of the Phila. Engineering Works, gives the following method of calculating their resistance to wind pressure (Power, Oct. 1893):

In tests by Sir William Fairbairn we find four experiments to determine the strength of thin hollow tubes. In the table will be found their elements, with the beautiful strein.

with their breaking strain. These tubes were placed upon hollow blocks, and the weights suspended at the centre from a block fitted to the inside of

the tube.

	Clear Span, ft. in.	Thick- ness Iron, in.	Outside Diame- ter, in.	Sectional Area, in.	Breaking Weight, lbs.	Breaking W't, lbs., by Clarke's Formula, Constant 1.2,
I. II. IV.	17 15 714 23 5 28 5	.087 .118 .0631 .119	12 12.4 17.68 18.18	1.8901 4,8669 8.487 6.74	2,704 11,440 6,400 14,240	2,627 9,184 7,302 18,910

Edwin Clarke has formulated a rule from experiments conducted by him during his investigations into the use of iron and steel for hollow tube bridges, which is as follows:

Center breaking load, in tons.

When the constant used is 1.2, the calculation for the tubes experimented When the constant used is 1.2, the calculation for the tubes experimented upon by Mr. Fairbairn are given in the last column of the table. D. K. Clark's "Rules, Tables, and Data," page 513, gives a rule for hollow tubes as follows: $W=3.14D^2TS+L$. W= breaking weight in pounds in centre, D= extreme diameter in inches; T= thickness in inches; L= length between supports in inches; S= ultimate tensile strength in pounds per sq. in. Taking S, the strength of a square inch of a riveted joint, at 85,000 lbs. per. sq. in., this rule figures as follows for the different examples experimented upon by Mr. Fairbairn: I, 2870; II. 10,190; III, 7700; IV, 15,320. This shows a close approximation to the breaking weight obtained by experiments and that derived from Edwin Clarke's and D. K. Clark's rules. We therefore assume that this system of calculation is practically correct.

experiments and that derived from Edwin Clarke's and D. K. Clark's rules. We therefore assume that this system of calculation is practically correct, and that it is eminently safe when a large factor of safety is provided, and from the fact that a chimney may be standing for many years without receiving anything like the strain taken as the basis of the calculation, viz., fifty pounds per square foot. Wind pressure at fifty pounds yer square foot may be assumed to be travelling in a horizontal direction, and be of the same velocity from the top to the bottom of the stack. This is the extreme assumption. If, however, the chimney is round, its effective area would be only half of its diameter plane. We assume that the entire force may be concentrated in the centre of the height of the section of the chimney under consideration. under consideration.

Taking as an example a 125-foot iron chimney at Poughkeepsie, N. Y., the average diameter of which is 90 inches, the effective surface in square feet upon which the force of the wind may play will therefore be 7½ times 125 divided by 2, which multiplied by 50 gives a total wind force of 23,437 pounds. The resistance of the chimney to breaking across the top of the foundation would be 8 14 × 163° (that is, diameter of base) × .25 × 25,000 + (750 × 4) = 228,486, or 10.6 times the entire force of the wind. We multiply the half height above the joint in inches, 750, by 4, because the chimney is considered a fixed beam with a load suspended on one end. In calculating the strength half was united by the half of the serve observed. considered a fixed beam with a load suspended on one end. In calculating its strength half way up, we have a beam of the same character. It is a fixed beam at a line half way up the chimney, where it is 90 inches. In diameter and .137 inch thick. Taking the diametrical section above this line, and the force as concentrated in the centre of it, or half way up from the point under consideration, its breaking strength is: $8.14 \times 90^3 \times .187 \times 35,000 \div (381 \times 4) = 109.320$; and the force of the wind to tear it apart through its eross-section, $7.4 \times 6.24 \times 50 + 3 = 11,352$, or a little more than one tenth of the strength of the stack.

The Babcock & Wilcox Co.'s book "Steam" illustrates a steel chimney at the works of the Maryland Steel Co., Sparrow's Point, Md. It is 225 ft. in height above the base, with internal brick lining 13' 9'' uniform inside diameter. The shell is 25 ft. diam. at the base, tapering in a curve to 17 ft. 25 ft. above the base, thence tapering almost imperceptibly to 14' 8'' at the

25 ft. above the base, thence tapering almost imperceptibly to 14'8" at the top. The upper 40 feet is of 14-inch plates, the next four sections of 40 ft. each are respectively 9/82, 5/16, 11/82, and 34 inch.

Sizes of Foundations for Steel Chimneys.

(Selected from circular of Phila. Engineering Works.)

Ħ.	t.m.T	TWPT.	CHIMNEY	

Diameter, clear, feet	8	4	5	6	7	9	11
Height, feet	100	100	150	150	150	150	150
Least diameter foundation	15′9′′	16'4''	20'4"	21'10"	22'7''	28'8"	24'8'
Least depth foundation	6′	6′	8′	8′.	.9/	10′	10'
Height, feet	••••	125	200	200	250	275	300
Least diameter foundation		18'5"	28'8"	25'	29'8"	83'6"	86′
Least depth foundation	••••	7"	10'	10'	12′	12′	14'

Weight of Sheet-iron Smoke-stacks per Foot.

(Porter Mfg. Co.)

Diam., inches.	Thick- ness W. G.		Diam., inches.	Thick- ness W. G.	I W GIBUU	Diam. inches.	Thick- ness W. G.	Weight per ft.
10 12 14 16 20 22	No. 16	7.20 8.66 9.58 11.68 18.75 15.00 16.25	25 26 80 10 12 14	No. 16 No. 14	17.50 18.75 20.00 9.40 11.11 18.69 15.00	20 22 24 25 28 20	No. 14	18.38 20.00 21.66 23.33 25.00 26.66

Sheet-iron Chimneys. (Columbus Machine Co.)

Diameter Chimney, inches.	Length Chimney, feet.	Thick- ness Iron, B. W. G.	lbs.	Diameter Chimney, inches		Thick- ness Iron, B. W. G	Weight lbs.
10 15 20 22 24 26 28	20 20 20 20 80 40 40	No. 16 44 16 44 16 44 16 44 16 44 16 44 16 44 16 44 16 44 16	160 940 820 850 760 826 900	80 82 84 86 88 40	40 40 40 40 40 40	No. 15 15 16 17 18 19 19 19 19 19 19 19 10 10 10 10 10 10 10 10 10 10 10 10 10	960 1,020 1,170 1,240 1,800 1,890

THE STEAM-ENGINE.

Expansion of Steam. Isothermal and Adiabatic.—According to Mariotte's law, the volume of a perfect gas, the temperature being kept constant, varies inversely as its pressure, or $p \propto \frac{1}{v}$; pv = a constant. The curve constructed from this formula is called the isothermal curve, or

curve of equal temperatures, and is a common or rectangular hyperbola. The relation of the pressure and volume of saturated steam, as deduced from Regnault's experiments, and as given in Steam tables, is approximately, according to Rankine (S. E., p. 463), for pressures not exceeding 120 lbs., $p \propto \frac{1}{v^{15}}$, or $p \propto v^{-\frac{1}{15}}$, or $pv^{\frac{1}{15}} = pv^{\frac{1.025}{15}} = a$ constant. Zeuner has

found that the exponent 1,0646 gives a closer approximation.

When steam expands in a closed cylinder, as in an engine, according to Rankine (S. E., p. 885), the approximate law of the expansion is p

 $p \propto v^{-\frac{19}{4}}$, or $pv^{1.111} = a$ constant. The curve constructed from this formula is called the adiabatic curve, or curve of no transmission of heat. Peabody [Therm., p. 112] says: "It is probable that this equation was obtained by comparing the expansion lines on a large number of indicator-diagrams. . . There does not appear to be any good reason for using an exponential equation in this connection, . . and the action of a lagged steamengine cylinder is far from being adiabatic. . . For general purposes the hyperbola is the best curve for comparison with the expansion curve of an indicator-card. . ." Wolff and Denton, Trans. A. S. M. E., ii. 175, say: "From a number of cards examined from a variety of steam-engines in curvent use we find that the actual expansion line varies between the 10/9 rent use, we find that the actual expansion line varies between the 10/9 adiabatic curve and the Mariotte curve."

Prof. Thurston (A. S. M. E., ii. 203), says he doubts if the exponent ever becomes the same in any two engines, or even in the same engines at dif-

ferent times of the day and under varying conditions of the day.

Expansion of Steam according to Mariotte's Law and to the Adiabatic Law. (Trans. A. S. M. E., ii. 186).—Mariotte's law

 $pv = p_1v_1$; values calculated from formula $\frac{Pm}{p_1} = \frac{1}{R}(1 + \text{hyp log } R)$, in which $R = v_2 + v_1$, $p_1 = \text{absolute initial pressure}$, Pm = absolute mean pressure, $v_1 = \text{initial volume of steam in cylinder at pressure}$ p_1 , $v_2 = \text{flual volume of steam at final pressure}$. Adiabatic law: $pv^{\frac{1}{2}} = p_1v_1^{\frac{1}{2}}$; values calculated from formula $\frac{Pm}{p_1} = 10R^{-1} - 9R^{-\frac{1}{2}}$.

Ratio of Expan- sion R.	Ratio of Mean to Initial Pressure.		Ratio of Mean to Initial Pressure.		Ratio of Expan-	Ratio of Mean to Initial Pressure.		
	Mar.	Adiab.	sion R.	Mar.	Adiab.	sion R.	Mar.	Adiab.
1.00 1.25 1.50 1.75 2.2 2.4 2.5 2.6 2.8 3.1 3.2 8.5 8.6	1.000 .978 .937 .891 .847 .813 .781 .762 .735 .700 .688 .676 .665 .654	1.000 .976 .981 .881 .798 .765 .748 .783 .704 .678 .606 .630 .630	8.7 8.9 4.1 4.2 4.4 4.5 4.6 4.9 5.25 5.75	.624 .614 .605 .597 .589 .572 .564 .556 .549 .542 .528 .528 .528 .528 .478	.600 .590 .590 .590 .571 .569 .554 .530 .530 .523 .516 .509 .502 .479 .479 .484 .450	6. 25 6. 5 6. 75 7. 25 7. 75 8. 25 8. 75 9. 25 9. 75	.465 .453 .442 .481 .411 .402 .393 .855 .877 .369 .362 .355 .349 .342 .336	.458 .425 .413 .405 .393 .833 .874 .365 .857 .349 .312 .335 .828 .321 .315 .308

Ican Pressure of Expanded Steam.—For calculations of inest is generally assumed that steam expands according to Mariotte's, the curve of the expansion line being a hyperbola. The mean pressure, saured above vacuum, is then obtained from the formula

$$P_m = p_1 \frac{1 + \text{hyp log } R}{R}$$
, or $P_m = P_1(1 + \text{hyp log } R)$,

which P_m is the absolute mean pressure, p, the absolute initial pressure en as uniform up to the point of cut-off, Pt the terminal pressure, and R ratio of expansion. If l = length of stroke to the cut-off, L = total stroke.

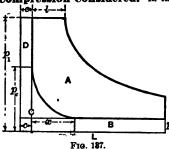
$$P_{m} = \frac{p_{1}l + p_{1}l \operatorname{hyp} \log \frac{L}{l}}{L}; \quad \text{and if } R = \frac{L}{l}, \quad P_{m} = p_{1}\frac{1 + \operatorname{hyp} \log R}{L}.$$

Hean and Terminal Absolute Pressures.—Mariotte's ive.—The values in the following table are based on Mariotte's law, ept those in the last column, which give the mean pressure of superheated am, which, according to Rankine, expands in a cylinder according to law $p \propto v^{-\frac{1}{14}}$. These latter values are calculated from the formula $\frac{17-16R-\frac{1}{14}}{R}$. $R^{-\frac{1}{14}}$ may be found by extracting the square root of $\frac{1}{R}$.

r times. From the mean absolute pressures given deduct the mean back sture (absolute) to obtain the mean effective pressure.

ate of pan- on.	Cut- off.	Ratio of Mean to Initial Pressure.	Ratio of Mean to Terminal Pressure.	Ratio of Terminal to Mean Pressure.	Patio of Initial to Mean Pressure.	Ratio of Mean to Initial Dry Steam.
88	0.083 0.086 0.088 0.042 0.045 0.055 0.063 0.066 0.077 0.077 0.083 0.100 0.110 0.110	0.1467 0.1547 0.1639 0.1741 0.1860 0.1998 0.2161 0.2858 0.2479 0.2630 0.2742 0.2904 0.3069 0.3568 0.3568 0.3849	4.40 4.33 4.28 4.18 4.09 4.09 4.09 8.87 8.77 8.74 8.56 8.48 8.49 8.30 8.30	0.227 0.231 0.225 0.225 0.244 0.250 0.255 0.265 0.275 0.275 0.279 0.280 0.287 0.284 0.308 0.312	6.82 6.46 6.11 5.75 5.88 5.00 4.63 4.24 4.05 3.72 3.65 3.44 3.24 3.00 2.81	0.186 0.186 0.254
66 00 71 044 00 88 90 96 90 98 90 98 90 98 90 98 90 98 90 98 90 94 90 90 90 90 90 90 90 90 90 90 90 90 90	0.148 0.150 0.166 0.175 0.200 0.250 0.275 0.303 0.375 0.305 0.375 0.450 0.500 0.550 0.650 0.625 0.625	0.4310 0.4847 0.4658 0.4807 0.5218 0.5608 0.5608 0.6615 0.69095 0.7171 0.7440 0.8085 0.8784 0.8786 0.9066 0.9187 0.9989	2.95 2.79 2.74 2.61 2.50 2.39 2.39 2.30 2.05 1.91 1.60 1.60 1.47 1.48	0.389 0.345 0.380 0.364 0.883 0.400 0.419 0.487 0.484 0.476 0.488 0.505 0.502 0.502 0.680 0.690 0.718	2.37 2.30 2.15 2.08 1.78 1.68 1.51 1.43 1.84 1.31 1.24 1.18 1.14 1.10 1.09	0.417 0.506 0.582 0.648 0.707 0.756 0.800 0.840 8.874 0.900 0.826

Calculation of Mean Effective Pressure, Clearance and Compression Considered.—In the above tables no account is taken



of clearance, which in actual steam-engines modifies the ratio of expansion and the mean pressure; nor of compression and back-pressure, which diminish the mean effective pressure. In the following calculation these elements are considered.

L = length of stroke, l = lengthbefore cut-off, x = length of com-pression part of stroke, c = clear-ance, $p_1 = \text{initial pressure}, p_0 =$ back pressure, $p_0 =$ pressure of clearance steam at end of comp pression. All pressures are abso-lute, that is, measured from a

perfect vacuum.

Area of ABCD =
$$p_1(l+c) \Big(1 + \text{hyp log } \frac{L+c}{l+c} \Big) i$$

B = $p_b(L-x)$;
C = $p_{cc} \Big(1 + \text{hyp log } \frac{x+c}{c} \Big) = p_b(x+c) \Big(1 + \text{hyp log } \frac{x+c}{c} \Big) i$
D = $(p_1 - p_c)c = p_1c - p_b(x+c)$.
Area of A = ABCD - $(B+C+D)$
= $p_1(l+c) \Big(1 + \text{hyp log } \frac{L+c}{l+c} \Big)$
 $- \Big[p_b(L-x) + p_b(x+c) \Big(1 + \text{hyp log } \frac{x+c}{c} \Big) + p_1c - p_b(x+c) \Big]$
= $p_1(l+c) \Big(1 + \text{hyp log } \frac{L+c}{l+c} \Big)$
- $p_b \Big[(L-x) + (x+c) \text{ hyp log } \frac{x+c}{c} \Big] - p_1c$.

Mean effective pressure = area of A

Example.—Let L = 1, l = 0.25, x = 0.25, c = 0.1, $p_1 = 50$ lbs., $p_h = 2$ lbs. Area A = $60(.25 + .1)(1 + \text{hyp log } \frac{1.1}{9\pi})$ $-2\left[(1-.25)+.85 \text{ hyp log } \frac{.85}{.}\right]-60 \times .1$

> $= 21(1 + 1.145) - 2[.75 + 85 \times 1.258] - 6$ = 45.045 - 2.377 - 6 = 36.668 = mean effective pressure.

The actual indicator-diagram generally shows a mean pressure considerably less than that due to the initial pressure and the rate of expansion. The causes of loss of pressure are: 1. Friction in the stop-valves and steampipes. 2. Friction or wire-drawing of the steam during admission and cutoff, due chiefly to defective valve-gear and contracted steam-passages.

8. Liquefaction during expansion. 4. Exhausting before the engine has completed its stroke. 5. Compression due to early closure of exhaust. 6. Friction in the exhaust-ports, passages, and pipes,

Be-evaporation during expansion of the steam condensed during admissions of the steam condensed during admission.

sion, and valve-leakage after cut-off, tend to elevate the expansion line of the diagram and increase the mean pressure. If the theoretical mean pressure be calculated from the initial pressure and the rate of expansion on the supposition that the expansion curve fol-

lows Mariotte's law, pv = a constant, and the necessary corrections are made for clearance and compression, the expected mean pressure in practice may be found by multiplying the calculated results by the factor in the following table, according to Seaton.

Particulars of Engine.	Factor.
Expansive engine, special valve-gear, or with a separate cut-off valve, cylinder jacketed	0.94
Expansive engine having large ports, etc., and good or- dinary valves, cylinders jacketed	0.9 to 0.98
Expansive engines with the ordinary valves and gear as in general practice, and unjacketed	0.8 to 0.85
Compound engines, with expansion valve to h.p. cylinder; cylinders jacketed, and with large ports, etc	0.9 to 0.98
Compound engines, with ordinary slide-valves, cylinders jacketed, and good ports, etc	0.8 to 0.85
jackets and expansion-valves	0.7 to 0.8
in war-ships	0.6 to 0.8

If no correction be made for clearance and compression, and the engine is in accordance with general modern practice, the theoretical mean pressure may be multiplied by 0.96, and the product by the proper factor in the table, to obtain the expected mean pressure.

Given the Initial Pressure and the Average Pressure, to Find the Ratio of Expansion and the Period of Admission.

P = initial absolute pressure in ibs. per sq. in.;
p = average total pressure during stroke in ibs. per sq. in.;
L = length of stroke in inches;
l = period of admission measured from beginning of stroke;

= clearance in inches;

$$B = \text{actual ratio of expansion} = \frac{L+e}{l+e}.$$

$$p \approx \frac{P(1+\text{hyp}\log E)}{R}.$$

To find average pressure p, taking account of clearance.

$$\mathbf{p} = \frac{P(l+c) + P(l+c) \text{ hyp log } R - P\mathbf{e}}{L}, \quad \dots \quad \mathbf{e}$$

$$\mathbf{pL} + P\mathbf{e} = P(l+c)(1 + \text{hyp log } R) \mathbf{e}$$

whence

hyp
$$\log R = \frac{pL + Pc}{Pl + Pc} - 1 = \frac{\frac{p}{P}L + e}{l + c} - 1$$
. (8)

Given p and P, to find R and l (by trial and error).—There being two unknown quantities R and l, assume one of them, viz., the period of admission l, substitute it in equation (3) and solve for R. Substitute this value of R in the formula (1), or $l = \frac{L+c}{R} - c$, obtained from formula (1), and find l. If

the result is greated than the assumed value of l, then the assumed value of the period of admission is too long; if less, the assumed value is too short. Assume a new value of l, substitute it in formula (3) as before, and continue by this method of trial and error till the required values of R and l are obtained.

EXAMPLE.—P = 70, p = 42.78, $L = 60^{\circ}$, $c = 8^{\circ}$, to find l. Assume l = 21 in.

hyp log
$$R = \frac{\frac{p}{P}L + c}{l + c} - 1 = \frac{\frac{42.78}{70} \times 60 + 8}{21 + 8} - 1 = 1.658 - 1 = .653;$$

hyp $\log R = .658$, whence R = 1.93.

$$l = \frac{L+c}{R} - c = \frac{63}{192} - 3 = 29.8$$

which is greater than the assumed value, 21 inches.

Now assume l = 15 inches:

hyp
$$\log R = \frac{49.78}{70} \times 60 + 8$$

 $15 + 8 - 1 = 1.204$, whence $R = 8.5$;
 $l = \frac{L+c}{R} - c = \frac{63}{3.5} - 3 = 18 - 3 = 15$ inches, the value assumed.

Therefore R = 3.5, and l = 15 inches.

Period of Admission Required for a Given Actual Ratio of Expansion:

$$l = \frac{L+c}{R} - c$$
, in inches (4)

In percentage of stroke,
$$l = \frac{100 + \text{p.ct. clearance}}{R} - \text{p. ct. clearance}$$
. (5)

Terminal pressure =
$$\frac{P(l+c)}{L+c} = \frac{P}{B}$$
. (6)

Pressure at any other Point of the Expansion.—Let $L_1 = \text{length of stroke}$ up to the given point.

WORK OF STEAM IN A SINGLE CYLINDER.

To facilitate calculations of steam expanded in cylinders the table on the mext page is abridged from Clark on the Steam-engine. The actual ratios of expansion, column 1, range from 1.0 to 8.0, for which the hyperbolic logarithms are given in column 2. The 3d column contains the periods of admission relative to the actual ratios of expansion, as percentages of the stroke, calculated by formula (5) above. The 4th column gives the values of the mean pressures relative to the initial pressures, the latter being taken as 1, calculated by formula (2). In the calculation of columns 3 and 4, clearance is taken into account, and its amount is assumed at 7% of the stroke, the final pressures, in the 5th column, are such as would be arrived at by the continued expansion of the whole of the steam to the end of the stroke, the initial pressure being equal to 1. They are the reciprocals of the ratios of expansion; the total performance, when steam is admitted for the whole of the stroke, without expansion, being equal to 1. They are obtained by dividing the figures in column 4 by those in column 5.

The pressures have been calculated on the supposition that the pressure of To facilitate calculations of steam expanded in cylinders the table on the

The pressures have been calculated on the supposition that the pressure of steam, during its admission into the cylinder, is uniform up to the point of cutting off, and that the expansion is continued regularly to the end of the stroke. The relative performances have been calculated without any allow-

ance for the effect of compressive action.

ance for the effect of compressive action. The calculations have been made for periods of admission ranging from 100%, or the whole of the stroke, to 6.4%, or 1/16 of the stroke. And though, nominally, the expansion is 16 times in the last instance, it is actually only 8 times, as given in the first column. The great difference between the nominal and the actual ratios of expansion is caused by the clearance, which is equal to 7% of the stroke, and causes the nominal volume of steam admitted, namely, 6.4%, to be augmented to 6.4 + 7 \approx 13.4% of the stroke, or, say, double, for expansion. When the steam is cut off at 1/9, the actual expansion is only 6 times; when cut off at 1/5, the expansion is 2% times; and to effect an actual expansion to twice the initial volume, the steam is cut off at 4616% of the stroke, ot at half-stroke. ot at half-stroke.

pansive Working of Steam-Actual Ratios of Expansion, with the Helative Periods of Admission, Pressures, and Performance.

team-pressure 100 lbs, absolute. Clearance at each end of the cylinder 7% he stroke.

(SINGLE CYLINDER.)

	(GIRGLE CILINDER.)									
1	2	8	4	5	6	8	8 .	9		
Volumes to which the Initial Volume is Expanded.	Hyperbolic Logarithm of Actual Ratio of Expansion.	Period of Admission or Cut-off, 7% Clearance.	Average Total Press- ure. Initial Pressure = 1.	Total Final Press- ure. Initial Pressure = 1.	Ratio of Total Per- formance of Equal Weights of Steam, (Col. 4 + Col 5.)	Actual Work done by 1 lb, of 100 lbs, Steam, Ftlbs.	Quantity of Steam Consumed per H.P. of Actual Workdoneper hour	Net Capacity of Cyl- inder per lb. of 100 lbs. Steam ad- mitted in 1 stroke. Cubic feet.		
1 1.1 1.18 1.23 1.8 1.39 1.45 1.54	.0000 .0953 .1698 .2070 .2624 .3298 .3716	100 90.3 88.3 80 75.8 70 66.8	1.000 .986 .986 .969 .953 .942 .925 .918 .880 .886 .787 .766 .726 .692 .637 .608 .569 .569	1.000 .909 .847 .818 .769 .719	1.000 1.096 1.164 1.206 1.261 1.325 1.365	58,273 68,850 67,836 70,246 73,513 77,242 79,555 83,055	34.0 31.0 29.2 28.2 26.9 25.6 24.9	4.05 4.45 4.78 4.98 5.26 5.68 5.87 6.28		
1.6 1.75	.4817 .4700 .5595 .6314 .6981 .8241 .8755	62.5 59.9 54.1 50 46.5 40 87.6 83.3	.925 .918 .888 .860 .886	.719 .690 .649 .625 .571 .582 .5	1.425 1.461 1.546 1.616 1.672 1.793 1.887	90,115 94,200 97,489	22.0 21.0	6.28 6.47 7.08 7.61 8.09 9.28 9.71		
1.88 2.28 2.4 2.65 2.9 3.2 3.35 3.6	.9745 1.065 1.163 1.209 1.281 1.385 1.386	29.9 26.4 25	726 .692 .652 .637 .608	.417 .377 .845 .813 .298 .278 .263	1.925 2.006 2.083 2.129 3.187 2.240	104,466 107,050 112,220 116,885 121,386 124,066 197,450 180,538 182,770	16.0 15.5	11.74 12.95 18.56 14.57 15.38		
4.2 4.5 4.8 5.5 5.8 5.9	1.886 1.435 1.504 1.569 1.609 1.649 1.705 1.758	21.2 19.7 18.5 16.8 15.8 14.4 13.6 12.5	.503 .488	.845 .813 .298 .298 .263 .250 .238 .229 .206 .200 .198 .182 .173 .169	2.278 2.315 2.370 2.418 2.440 2.466 2.511	134,900 188,180 140,920 142,180	14.34 14.05 18.92 18.78	16.19 17.00 18.21 19.48 90.28 21.04 22.25 28.47		
6.8 6.6	1.758 1.775 1.825 1.841 1.887 1.946 1.988 2.028	11.4 11.1 10.8 10 9.2 8.8 7.7 7.1	.457 .438 .482 .419 .418 .898 .881 .369 .857	.161 .159 .152	2.547 2.556 2.585 2.585 2.597 2.619 2.664 2.693	146,825 148,390 148,940 150,680 151,870 152,595 155,200 156,960	18.14 18.08 12.98 12.75 12.61	28.87 25.09 25.49 26.71 28.33 29.54		
7.8 7.6 7.8 8	2.028 2.054 2.079	7.1 6.7 6.4	.857 .848 .842	.137 .132 .128 .125	2.711 2.719 2.786	157,975 158,414 159,488	12.50	80.76 81.57 82.88		

SSUMPTIONS OF THE TABLE.—That the initial pressure is uniform; that expansion is complete to the end of the stroke; that the pressure in exsion varies inversely as the volume; that there is no back-pressure of aust or of compression, and that clearance is 7% of the stroke at each of the cylinder. No allowance has been made for loss of steam by cylor-condensation or leakage.

Though a uniform clearance of ?% at each end of the stroke has been assumed as an average proportion for the purpose of compiling the table, the clearance of cylinders with ordinary alides varies considerably—say from 5% to 10%. (With Corliss engines it is sometimes as low as 2%) With the clearance, 7%, that has been assumed, the table gives approximate resuits sufficient for most practical purposes, and more trustworthy than results deduced by calculations based on simple tables of hyperbolic logarithms, where clearance is neglected.

Weight of steam of 100 lbs. total initial pressure admitted for one stroke,

per cubic foot of net capacity of the cylinder, in decimals of a pound = reciprocal of figures in column 9.

Total actual work done by steam of 100 lbs. total initial pressure in one stroke per cubic foot of net capacity of cylinder, in foot-pounds = figures

in column 7 + figures in column 9.

Rule 1: To find the net capacity of cylinder for a given weight of steam admitted for one stroke, and a given actual ratio of expansion. (Column 9 of table,)—Multiply the volume of 1 b. of steam of the given pressure by the given weight in pounds, and by the actual ratio of expansion. Multiply the product by 100, and divide by 100 plus the percentage of clearance. The quotient is the net capacity of the cylinder.

RULE 2: To find the net capacity of cylinder for the performance of a given amount of total actual work in one stocks with a size initial power.

given amount of total actual work in one stroke, with a given initial pressure and actual ratio of expansion.—Divide the given work by the total actual work done by 1 lb. of steam of the same pressure, and with the same actual ratio of expansion; the quotient is the weight of steam necessary to do the given work, for which the net capacity is found by Rule 1 preceding. Norm.—1. Conversely, the weight of steam admitted per cubic foot of net capacity for one stroke is the reciprocal of the cylinder-capacity per pound

of steam, as obtained by Rule 1.

2. The total actual work done per cubic foot of net capacity for one stroke is the reciprocal of the cylinder-capacity per foot-pound of work done, as obtained by Rule 2.

3. The total actual work done per square inch of piston per foot of the

stroke is 1/144th part of the work done per cubic foot.

4. The resistance of back pressure of exhaust and of compression are to be added to the net work required to be done, to find the total actual work.

APPENDIX TO ABOVE TABLE-MULTIPLIERS FOR NET CYLINDER-CAPACITY, AND TOTAL ACTUAL WORK DONE.

(For steam of other pressures than 100 lbs. per square inch.)

	Multi	pliers.		Multipliers.			
Total Pressures per square inch.	For Col. 7. Total Work by 1 lb. of Steam.	For Col. 9. Capacity of Cylinder.	Total Pressures per square inch.	For Col. 7. Total Work by 1 lb. of Steam.	For Col. 9. Capacity of Cylinder.		
1bs, 65 70 75 80 85 90	.975 .981 .986 .988 .991 .995	1.50 1.40 1.81 1.94 1.17 1.11	lbs. 100 110 120 180 140 150	1,000 1,009 1,011 1,015 1,022 1,025 1,081	1.00 .917 .848 .781 .780 .683		

The figures in the second column of this table are derived by multiplying the total pressure per square foot of any given steam by the volume in cubic feet of 1 lb. of such steam, and dividing the product by 62.852, which is the product in foot-pounds for steam of 100 lbs. pressure. The quotient

is the multiplier for the given pressure.

The figures in the third column are the quotients of the figures in the second column divided by the ratio of the pressure of the given steam to 100 lbs.

Measures for Comparing the Duty of Engines.—Capacity is measured in horse-powers, expressed by the initials, H.P.: # 38,000 ft.-lbs. per minute, = 550 ft.-lbs. per second, = 1,980,000 ft.-lbs. per hour

ift.-lb. = a pressure of 1 lb. exerted through a space of 1 ft. Economy is measured, 1, in pounds of coal per horse-power per hour, 2s, in pounds of steam per horse-power per hour. The second of these measures is the more accurate and scientific, since the engine uses steam and not coal, and it is

independent of the economy of the boiler.

In gas-engine tests the common measure is the number of cubic feet of gas (measured at atmospheric pressure) per horse-power, but as all gas is not of the same quality, it is necessary for comparison of tests to give the analysis of the gas. When the gas for one engine is made in one gas-producer, then the number of pounds of coal used in the producer per hour per horse received of the progress

horse-power of the engine is the proper measure of economy.

Economy, or duty of an engine, is also measured in the number of footpounds of work done per pound of fuel. As I horse-power is equal to 1,980,000 ft.-lbs. of work in an hour, a duty of 1 lb. of coal per H.P. per hour would be equal to 1,980,000 ft.-lbs. per lb. of fuel; 2 lbs. per H.P. per hour equals 990,000 ft.-lbs. per lb. of fuel, etc.

The duty of pumping-engines is commonly expressed by the number of foot-pounds of work done per 100 lbs. of coal.

When the duty of pumping-engines is to the coal.

When the duty of a pumping engine is thus given, the equivalent number of pounds of fuel consumed per horse-power per hour is found by dividing 198 by the number of millions of foot-pounds of duty. Thus a pumping engine giving a duty of 99 millions is equivalent to 198/99 = 2 lbs. of fuel pet horse-power per hour.

Rificiency Measured in Thermal Units per Minute.— Some writers express the efficiency of an engine in terms of the number of thermal units used by the engine per minute for each indicated horse-power,

instead of by the number of pounds of steam used per hour.

The heat chargeable to an engine per pound of steam is the difference between the total heat in a pound of steam at the boiler-pressure and that in a pound of the feed-water entering the boiler. In the case of condensing engines, suppose we have a temperature in the hot-well of 101° F., corresponding to a vacuum of 28 in. of mercury, or an absolute pressure of 1 because the pressure of 1 by the polya a parfect vacuum we may feed the water into the boiler. per sq. in. above a perfect vacuum: we may feed the water into the boiler at that temperature. In the case of a non-condensing-engine, by using a portion of the exhaust steam in a good feed-water heater, at a pressure a triffe above the atmosphere (due to the resistance of the exhaust passages through the heater), we may obtain feed-water at 212°. One pound of steam used by the engine then would be equivalent to thermal units as follows:

Pressure of steam by gauge: 100 125 150 175 200

Total heat in steam above 32°:

1179.6 1172.8 1185.0 1189.5 1193.5 1197.0 1200.2 Subtracting 69.1 and 180.9 heat-units, respectively, the heat above 32° in feed-water of 101° and 212° F., we have—

Heat given by boiler:

Feed at 101°..... 1103.7 Feed at 212°.... 991.9 1110.5 1115.9 1120.4 998.7 1008.6 1012.6 1004.1 1016.1 1019.8

Thermal units per minute used by an engine for each pound of steam used per indicated horse-power per hour: Feed at 101°..... 18.40 18.51 18.60 18.67 18.74 18.80 18.85

Feed at 212°..... 16.53 16.65 16.81 16.88 16.94 16.99

EXAMPLES.—A triple-expansion engine, condensing, with steam at 175 lbs., gauge and vacuum 28 in., uses 13 lbs. of water per I.H.P. per hour, and a high-speed non-condensing engine, with steam at 100 lbs. gauge, uses 30

high-speed non-condensing engine, with steam at 100 lbs. gauge, uses 30 lbs. How many thermal units per minute does each consume?

Ans.—13×18.80 = 244.4, and 30×16.74 = 502.2 thermal units per minute.

A perfect engine converting all the heat-energy of the steam into work would require 33,000 ft.-lbs. + 778 = 42.4164 thermal units per minute per indicated horse-power. This figure, 42.4164, therefore, divided by the number of thermal units per minute per I.H.P. consumed by an engine, gives its efficiency as compared with an ideally perfect engine. In the examples above, 42.4164 divided by 244.4 and by 502.2 gives 17.35% and 8.45% efficiency, respectively

Total Work Done by One Pound of Steam Expanded in a Single Cylinder. (Column 7 of table.)—If I pound of water be converted into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., it occupies a volume equal to 26.36 cu, ft. The work done is equal to 2116.8 lbs.

 \times 26.86 ft. = 55,786 ft.-lbs. The heat equivalent of this work is (55,788 + 778 =) 71.7 units. This is the work of 1 lb. of steam of one atmosphere acting on a piston without expansion.

The gross work thus done on a piston by 1 lb. of steam generated at total pressures varying from 15 lbs. to 100 lbs. per sq. in. varies in round numbers from 56,000 to 62,000 ft. lbs., equivalent to from 72 to 80 units of heat.

This work of 1 lb. of steam without expansion is reduced by clearance according to the proportion it bears to the net capacity of the cylinder. If the clearance be % of the stroke, the work of a given weight of steam with-out expansion, admitted for the whole of the stroke, is reduced in the ratio of 107 to 100.

Having determined by this ratio the quantity of work of 1 lb. of steam with-

Having determined by this ratio the quantity of work of 1 lb. of steam without expansion, as reduced by clearance, the work of the same weight of steam for various ratios of expansion may be found by multiplying it by the relative performance of equal weights of steam, given in the 6th column of the table, Quantity of Steam Consumed per Horse-power of Total Work per Henr. (Column 8 of table.)—The measure of a horse-power is the performance of 33,000 ft.-lbs. per minute, or 1,980,000 ft.-lbs. per hour. This work, divided by the work of 1 lb. of steam, gives the weight of steam required per horse-power per hour. For example, the total actual work done in the cylinder by 1 lb. of 100 lbs. steam, without expansion and with 7% of clearance, is 58,273 ft.-lbs.; and $\frac{1,900,900}{56,273} = 34$ lbs. of steam, is the weight of steam consumed for the total work done in the cylinder per horse-power of steam consumed for the total work done in the cylinder per horse-power per hour. For any shorter period of admission with expansion the weight of steam per horse-power is less, as the total work of 1 lb. of steam is more, and may be found by dividing 1,980,000 ft.-lbs. by the respective total work done; or by dividing 34 lbs. by the ratio of performance, column 6 in the

ACTUAL EXPANSIONS. With Different Clearances and Cut-offs.

Computed by A. F. Nagle.

Cut- off.	Per Cent of Clearance.													
	0	1	2	8	4	5	6	7	8	9	10			
.01	100.00	50.5	34.0	25.75	20.8	17.5		13.88	12.00	10.9	10			
.02	50.00		25.50	20.60	17.58	15.00		11.89	10.80	9.91	9.17			
.03	83.88		20.40		14.86		11.78	10.70	9.82	9.08	8.46			
.04	25.00		17.00	14.71	13.00	11.66	10.60	9.78	9.00	8.89	7.86			
.05	20.00		14.57	12.87	11.55	10.50	9.64	8.92	8.31	7.79	7.33			
.06	16.67		12.75	11.44	10.40	9.55	8.83	8.23	7.71	7.27	6.88			
.07	14.28		11.83	10.80	9.46	8.75	8.15	7.64	7.20	6.81	6.47			
.06	12.50	11.22		9.36	8.67	8.08	7.57	7.18	6.75	6.41	6.11			
.09	11.11	10.10		8.58	8.00	7.50	7.07	6.69	6.35	6.06	5.79			
.10	10.00	9.18		7.92	7.48	7.00	6.62	6.30	6.60	5.74	5.50			
.11	9.09	8.42	7.84	7.36	6.93	6.56	6.24	5.94	5.68	5.45	5.24			
. 12	8.83	7.78		6.86	6.50	6.18	5.89	5.63	5.40	5.19	5.00			
.14	7.14	6.78		6.06	5.78	5.58	5.80	5.10	4.91	4.74	4.5			
.16	6.25	5.94		5.42	5.20	5.00	4.82	4.65	4.50	4.86	4.2			
.20	5.00	4.81	4.64	4.48	4.88	4.20	4.08	8.96	8.86	8.76	8.6			
.25	4.00	8.88		3.68	8.58	8.50	8.42	8.84	8.27	8.21	8.14			
.80	8.88	8.26		8.12	8.06	8.00	2.94	2.90	2.84	2.80	2.7			
.40	2.50	2.46		2.40	2.86	2.88	2.80	2.28	2.25	2.23	2.2			
.50	2.00	1.98		1.94	1.92	1.90	1.89	1.88	1.86	1.85	1.8			
.60	1.67	1.66	1.65	1.64	1.63	1.615								
.70	1.48	1.42		1.41	1.41	1.400								
.80	1.25	1.25												
.90 1.00	1.111	1.11												

Relative Efficiency of 1 lb. of Steam with and without Clearance: back pressure and compression not considered,

Mean total pressure =
$$p = \frac{P(l+c) + P(l+c) \text{ hyp. log. } R - Pc}{L}$$

Let P = 1; L = 100; l = 25; c = 7.

$$p = \frac{82 + 82 \text{ hyp. log.} \frac{107}{32} - 7}{100} = \frac{32 + 32 \times 1,209 - 7}{100} = .637.$$

If the clearance be added to the stroke, so that clearance becomes zero, the same quantity of steam being used, admission l being then = l + c =82, and stroke L + c = 107.

$$p_1 = \frac{33 + 38 \text{ hyp. log.} \frac{107}{83} - 0}{107} = \frac{32 + 33 \times 1.209}{107} = .707.$$

That is, if the clearance be reduced to 0, the amount of the clearance 7 being added to both the admission and the stroke, the same quantity of steam will do more work than when the clearance is 7 in the ratio 707: 637, or 11% more.

or 11% more.

Back Pressure Considered.—If back pressure = .10 of P, this amount has to be subtracted from p and p_1 giving p = .537, $p_1 = .607$, the work of a given quantity of steam used without clearance being greater than when clearance is 7 per cent in the ratio of 607:587, or 18% more.

Effect of Compression.—By early closure of the exhaust, so that a portion of the exhaust-steam is compressed into the clearance-space, much of the loss due to clearance may be avoided. If expansion is continued down to the back pressure, if the back pressure is uniform throughout the exhaust-stroke, and if compression begins at such point that the exhaust team remaining in the cylinder is compressed to the initial pressure at the steam remaining in the cylinder is compressed to the initial pressure at the end of the back stroke, then the work of compression of the exhaust-steam equals the work done during expansion by the clearance-steam. The clearance-space being filled by the exhaust-steam thus compressed, no new steam is required to fill the clearance-space for the next forward stroke, and the work and efficiency of the steam used in the cylinder are just the same as if there were no clearance and no compression. When, however, there is a drop in pressure from the final pressure of the expansion, or the terminal pressure, to the exhaust or back pressure (the usual case), the work of compression the terminal case of the contract of the con pression to the initial pressure is greater than the work done by the expansion of the clearance-steam, so that a loss of efficiency results. In this case a greater efficiency can be attained by inclosing for compression a less quantity of steam than that needed to fill the clearance space with steam of the initial pressure. (See Clark, S. E., p. 399, et seq.; also F. H. Ball, Traus. A. S. M. E., xiv. 1067.) It is shown by Clark that a somewhat greater effi-ciency is thus attained whether or not the pressure of the steam be carried down by expansion to the back exhaust-pressure. As a result of calcula-tions to determine the most efficient periods of compression for various percentages of back pressure, and for various periods of admission, he gives

percentages of back pressure, and for various periods of admission, he gives the table on the next page:

Olearance in Low- and High-speed Engines. (Harris Tabor, Am. Mach., Sept. 17, 1891.)—The construction of the high-speed engine is such, with its relatively short stroke, that the clearance must be much larger than in the releasing-valve type. The short-stroke engine is, of necessity, an engine with large clearance, which is aggravated when a variable compression is a feature. Conversely, the releasing-valve gear is, from necessity, an engine of slow rotative speed, where great power is obtainable from long stroke, and small clearance is a feature in its construction. In one case the clearance will vary from 8% to 12% of the piston-displacement, and in the other from 2% to 3%. In the case of an engine with a clearance equalling 10% of the piston-displacement the waste room becomes clearance equalling 10% of the piston-displacement the waste room becomes enormous when considered in connection with an early cut-off. The system of compounding reduces the waste due to clearance in proportion as the steam is expanded to a lower pressure. The farther expansion is carried through a train of cylinders the greater will be the reduction of waste due to clearance. This is shown from the fact that the high-speed engine, expanding steam much less than the Corliss, will show a greater gain when changed from simple to compound than its rival under similar conditions.

COMPRESSION OF STEAM IN THE CYLINDER.

Best Periods of Compression: Clearance 7 per cent.

Cut-off in	Total Back Pressure, in percentages of the total initial pressure												
Percent- ages of the	21/6	5	10	15	20	25	80	35					
Stroke.		Periods	of Com	pressio	n, in par	ts of the	stroke.						
10≰	65≰ (57%	44%	32%	T	T	1	1					
10% 15 20 25 30 85 40	65 × 65 × 65 × 65 × 65 × 65 × 65 × 65 ×	52	40	29	28%								
20	52	47	40 87 84 83 29 27 25	29 27 26 25 23 21 20	22	1							
25	47	42	84	26	22 21	17%							
80	42	42 89 85 82 80 27 24 22	82	25	20	16	14%	12%					
85	89	85	29	23	19	15	18	11					
40	86	32	27	21	18	14	18	11					
45	88	30	25	20	17	14	12	10					
50	80	27	28 21	18	16	18	12	10					
45 50 55	27	24	21	17	15	18	11	9					
60	24	22	19	15	14	12	11	9					
65	22	20	17	15	14	12	10	8					
70	19	17	16	14	14	12	10	9 8 8 8					
75	17	16	14	13	12	11	9	8					

Notes to Table.—1. For periods of admission, or percentages of back pressure, other than those given, the periods of compression may be readily found by interpolation.

2. For any other clearance, the values of the tabulated periods of compression are to be altered in the ratio of 7 to the given percentage of

clearance.

Cylinder-condensation may have considerable effect upon the best point of compression, but it has not yet (1893) been determined by experiment. (Trans. A. S. M. E., xiv. 1078.)

Cylinder-condensation.—Rankine, S. E., p. 421, says: Conduction of heat to and from the metal of the cylinder, or to and from liquid water contained in the cylinder, has the effect of lowering the pressure at the be-giuning and raising it at the end of the stroke, the lowering effect being on the whole greater than the raising effect. In some experiments the quantity of steam wasted through alternate liquefaction and evaporation in the cylinder has been found to be greater than the quantity which performed the work.

Percentage of Loss by Cylinder-condensation, taken at Cut-off. (From circular of the Ashcroft Mfg. Co. on the Tabor Indicator, 1889.)

ge of appleted off.	Percent. of for by t	of Feed-wate he Indicator	r accounted diagram.	Percent. of Feed water Consumption due to Cylinder-condensat'n.				
Percenta Stroke con at Cut	Simple Engines.	Compound Engines, h.p. cyl.	Triple-ex- pansion Engines, h.p. cyl.	Simple Engines.	Compound Engines, h.p. cyl.	Triple-ex- pansion Engines, h.p. cyl.		
5 10	58 66	74		42 84	26			
15 20 80	71	76	78	84 29 26	24	22		
20 90	74 78 82	78	80	26	55	20		
40	1 69	82 85	84 87	18	18 15	16 13		
40 50	86	88	90	14	12	10		

Theoretical Compared with Actual Water-consumption, Single-cylinder Automatic Out-off Engines. (From the catalogue of the Buckeye Engine Co.)—The following table has been prepared on the basis of the pressures that result in practice with a constant boiler-pressure of 80 lbs. and different points of cut-off, with Buckeye engines and others with similar clearance. Fractions are omitted, except in the percentage column, as the degree of accuracy their use would seem to imply is not attained or aimed at.

Cut-off Part	Mean	Total	Indicated Rate, lbs. Water.	Assumed.			
of Stroke.	Effective Pressure.	Terminal Pressure.	per I.H.P. per hour.	Act'l Rate.	Per ct. Loss.		
.10 .15 .20 .25 .30 .35 .40 .45	18 97 85 43 48 58 57 61 64	11 15 20 25 80 85 88 43 48	20 19 19 20 20 21 22 28 24	82 27 25 25 24 25 26 27 27	58 41 81.5 25 81.8 19 16.7 15		

It will be seen that while the best indicated economy is when the cut-off is about at .15 or .20 of the stroke, giving about 30 lbs. M.E.P., and a terminal 3 or 4 lbs. above atmosphere, when we come to add the percentages due nat a or a los, solve atmosphere, when we come to an the percentages up to a constant amount of unindicated loss, as per sixth column, the most economical point of cut-off is found to be about .30 of the stroke, giving 48 lbs.

M.E.P. and 30 lbs. terminal pressure. This showing agrees substantially with modern experience under automatic cut-off regulation.

Experiments on Cylinder-condensation.—Experiments by Motor Those Evaluation [1987, p. 1987, p

Major Thos. English (Eng'g, Oct. 7, 1887, p. 386) with an engine 10×14 in., jacketed in the sides but not on the ends, indicate that the net initial condensation (or excess of condensation over re-evaporation) by the clearance surface varies directly as the initial density of the steam, and inversely as the square root of the number of revolutions per unit of time. The mean results gave for the net initial condensation by clearance-space per sq. ft. of surface at one rev. per second 6.06 thermal units in the engine when run non-condensing and 5.75 units when condensing.

G. R. Bodmer (Eng's, March 4, 1892, p. 299) says: Within the ordinary limits of expansion desirable in one cylinder the expansion ratio has practically no influence on the amount of condensation per stroke, which for simple engines can be expressed by the following formula for the weight of water condensed [per minute, probably; the original does not state]:

S(T-t) $L^{2}\sqrt{N^{2}}$, where T denotes the mean admission temperature, t the

mean exhaust temperature, S clearance-surface (square feet), N the number of revolutions per second, L latent heat of steam at the mean admission temperature, and C a constant for any given type of engine.

Mr. Bodmer found from experimental data that for high-pressure non-

jacketed engines $\mathcal{O}=$ about 0.11, for condensing non-jacketed engines 0.085 to 0.11, for condensing jacketed engines 0.085 to 0.053. The figures for jacketed engines apply to those jacketed in the usual way, and not at the outs. \mathcal{O} varies for different engines of the same class, but is practically con-

stant for any given engine. For simple high-pressure non-jacketed engines it was found to range from 0.1 to 0.112.

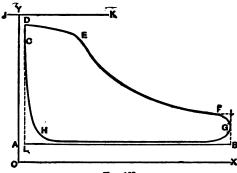
Applying Mr. Bodmer's formula to the case of a Corliss non-jacketed non-condensing engine, 4-ft. stroke, 24 in. dlam, 60 revs. per min., initial pressure 90 lbs. gauge, exhaust pressure 2 lbs., we have $T - t = 112^\circ$, N = 1, L = 890, S = 7 sq. ft.; and, taking C = .112 and W = lbs, water condensed

per minute, $W = \frac{.112 \times 112 \times 7}{1.1 \times .000} = .09$ lb. per minute, or 5.4 lbs. per hour. If

per minute, $W=\frac{1\times880}{1\times880}=.09$ ib. per minute, or 5.4 ios. per nour. In the steam used per I.H.P. per hour according to the diagram is 20 lbs., the actual water consumption is 25.4 lbs., corresponding to a cylinder condensation of 27%.

INDICATOR-DIAGRAM OF A SINGLE-CYLINDER RNGINE.

Definitions.—The Atmospheric Line, AB, is a line drawn by the pencil of the indicator when the connections with the engine are closed and both sides of the piston are open to the atmosphere,



Fra. 138.

The Vacuum Line, OX, is a reference line usually drawn about 14 7/10 pounds by scale below the atmospheric line.

The Clearance Line, OY, is a reference line drawn at a distance from the end of the diagram equal to the same per cent of its length as the clearance

and waste room is of the piston-displacement.

The Line of Botler pressure, JK, is drawn parallel to the atmospheric line, and at a distance from it by scale equal to the boiler-pressure shown

by the gauge.

The Admission Line, CD, shows the rise of pressure due to the admission of steam to the cylinder by opening the steam-valve.

The Steam Line, DE, is drawn when the steam-valve is open and steam is

being admitted to the cylinder. The Point of Cut-off, E, is the point where the admission of steam is stopped by the closing of the valve. It is often difficult to determine the exact point at which the cut-off takes place. It is usually located where the

outline of the diagram changes its curvature from convex to concave.

The Expansion Curve, EF, shows the fall in pressure as the steam in the cylinder expands doing work.

The Point of Release, F, shows when the exhaust-valve opens.

The Exhaust Line, FG, represents the change in pressure that takes place when the exhaust-valve opens.

The Back-pressure Line, GH, shows the pressure against which the piston acts during its return stroke.

The Point of Exhaust Closure, H, is the point where the exhaust-valve oses. It cannot be located definitely, as the change in pressure is at first due to the gradual closing of the valve.

The Compression Curve, HC, shows the rise in pressure due to the compression of the steam remaining in the cylinder after the exhaust-valve has

The Mean Height of the Diagram equals its area divided by its length.

The Mean Effective Pressure is the mean net pressure urging the piston

forward = the mean height \times the scale of the indicator-spring.

To find the Mean Rejective Pressure from the Diagram.—Divide the length, LB, into a number, say 10, equal parts, setting off half a part at L, half a part at B, and nine other parts between; erect ordinates perpendicular to the atmospheric line at the points of division of LB, cutting the diagram; add together the lengths of these ordinates intercepted between the upper and lowes thought the discrept and divide by the disc upper and lower lines of the diagram and divide by their number. This

es the mean height, which multiplied by the scale of the indicator-spring es the M.E.P. Or find the area by a planimeter, or other means (see neutration, p. 55), and divide by the length LB to obtain the mean height. The Initial Pressure is the pressure acting on the piston at the beginning the stroke.

The Terminal Pressure is the pressure above the line of perfect vacuum it would exist at the end of the stroke if the steam had not been released lier. It is found by continuing the expansion-curve to the end of the gram.

VDICATED HORSE-POWER OF ENGINES, SINGLE-CYLINDER.

Indicated Horse-power I.H.P.=
$$\frac{PLan}{83.000}$$
,

which P = mean effective pressure in lbs. per sq. in.; L = length of stroke leet; a = area of piston in square inches. For accuracy, one half of the tional area of the piston-rod must be subtracted from the area of the ton if the rod passes through one head, or the whole area of the rod if it ses through both heads; n = No. of single strokes per min. = $2 \times \text{No.}$ of

L.H.P.
$$=\frac{PaS}{33,000}$$
, in which $S=$ piston speed in feet per minute.

LH.P. =
$$\frac{PLd^3n}{42.017} = \frac{Pd^3S}{42.017} = .0000238PLd^3n = .0000238Pd^3S$$
,

which $d=\dim$ of cyl. in inches. (The figures 238 are exact, since l+33=23.8 exactly.) If product of piston-speed x mean effective scure = 42.017, then the horse-power would equal the square of the

SETTE = 42,017, then the norse-power would equal the square of the meter in inches. [andy Bulle for Estimating the Horse-power of a gle-cylinder Engine.—Square the diameter and divide by 2. This is not whenever the product of the mean effective pressure and the piston-sd = $\frac{1}{2}$ of 42,017, or, say, 21,000, viz., when M.E.P. = 30 and S = 700; m M.E.P. = 35 and S = 500; when M.E.P. = 32 and when i.P. = 42 and S = 500. These conditions correspond to those of ordinary states with both Carlier sending and shaft-governor high-speed engines. ctics with both Coriss engines and shaft-governor high-speed engines.

iven Horse-power, Mean Effective Pressure, and ston-speed, to find Size of Cylinder.—

Area =
$$\frac{88,000 \times I.H.P.}{PLn}$$
. Diameter = 205 $\sqrt{\frac{I.H.P.}{PS}}$. (Exact.)

rake Horse-power is the actual horse-power of the engine as sured at the fly-wheel by a friction-brake or dynamometer. It is the cated horse-power minus the friction of the engine.

able for Roughly Approximating the Horse-power of Compound Engine from the Diameter of its Low-ssure Cylinder.—The indicated horse-power of an engine being

 $\frac{1}{2}$, in which P = mean effective pressure per sq. in., s = piston-speed in

rer min., and de diam. of cylinder in inches; if s = 600 ft. per min., th is approximately the speed of modern stationary engines, and P = 35 which is an approximately average figure for the M.E.P. of single-der engines, and of compound engines referred to the low-pressure ider, then I.H.P. = $\frac{1}{2}67$; hence the rough-and-ready rule for horse-power n above: Square the diameter in inches and divide by 2. This applies to and quadruple expansion engines as well as to single cylinder and pound. For most economical loading, the M.E.P. referred to the low-sure cylinder of compound engines is usually not greater than that of he engines; for the greater economy is obtained by a greater number of insions of steam of higher pressures, and the greater the number of unsions for a given initial pressure the lower the mean effective pressure, following table gives approximately the figures of mean total and effecfollowing table gives approximately the figures of mean total and effective pressures for the different types of engines, together with the factor by which the square of the diameter is to be multiplied to obtain the horsepower at most economical loading, for a piston-speed of 600 ft. per minute.

Initial Absolute Pressure, Initial Back Real to Pressure, Initial Absolute Stone, I be a slone, I be
--

Non-condensing.

Single Cylinder.		20	.522			600	.524
Compound	7.5 10.	16 16	.402	48.2 52.8	15.5 15.5	**	.467 .533
Quadruple	12.5			56.4		66	.584

Condensing Engines.

Single Cylinder.			1	10	ī	.830	33.0	2	81.0	600	.443
Compound	120 160	15. 20.	1	8	1	.247 .200	29.6 32.0	2	27.6 30.0	"	.890
Triple	200	25.	1	8		.169	83.8	2	81.8		.454

For any other piston-speed than 600 ft. per min., multiply the figures in the last column by the ratio of the piston-speed to 600 ft.

Nominal Horse-power.—The term "nominal horse-power" origi-nated in the time of Watt, and was used to express approximately the power of an engine as calculated from its diameter, estimating the mean pressure in the cylinder at 7 lbs. above the atmosphere. It has long been obsolete in America, and is nearly obsolete in England.

Horse-power Constant of a given Engine for a Fixed Speed = product of its area of piston in square inches, length of stroke in feet, and number of single strokes per minute divided by 83,000, or

= C. The product of the mean effective pressure as found by the diagram and this constant is the indicated horse-power.

Horse-power Constant of a given Engine for Varying Speeds = product of its area of piston and length of stroke divided by \$3,000. This multiplied by the mean effective pressure and by the number of single strokes per minute is the indicated horse-power.

Horse-power Constant of any Engine of a given Diameter of Cylinder, whatever the length of stroke = area of piston + 33,000 = square of the diameter of piston in inches × .0000238. A table of constants

derived from this formula is given below.

The constant multiplied by the piston-speed in feet per minute and by the M.E.P. gives the I.H.P.

Errors of Indicators.—The most common error is that of the spring, which may vary from its normal rating; the error may be determined by proper testing apparatus and allowed for. But after making this correction, even with the best work, the results are liable to variable errors which may amount to 2 or 3 per cent. See Barrus, Trans. A. S. M. E., v. 810; Denton, A. S. M. E., xi. 839; David Smith, U. S. N., Proc. Eng'g Congress, 1838, Marine Division.

marine Division.

Indicator "Rigs," or Reducing-motions; Interpretation of Diagrams for Errors of Steam-distribution, etc. For these see circulars of manufacturers of Indicators; also works on the Indicator.

Table of Engine Constants for Use in Figuring Horse-power.—"Horse-power constant" for cylinders from 1 inch to 60 inches in diameter, advancing by 8ths, for one foot of piston-speed per minute and one pound of M.E.P. Find the diameter of the cylinder in the column at the state. If the diameter court is not found is the side. If the diameter contains no fraction the constant will be found in the column headed Even Inches. If the diameter is not in even inches, follow the line horizontally to the column corresponding to the required fraction.

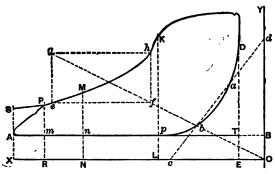
constants multiplied by the piston-speed and by the M.E.P. give the e-power.

	1			1	1			
1eter	Even	+ 1/8	+ 1/4 or	+ 3%	+ 1/2 or	+5%	+ 34	+ 3% or
f ider.	Inches.	or .125.	.25.	or .375.	.5.	or .625.	or .75.	.875.
1	.0000238	.0000301	.0000372	.0000450	.0000535	.0000628	.0000729	.000063
2	.0000952	.0001074	.0001205	.0001342	.0001487	.0001640	.0001800	000196
2 3	.0002142	.0002324	.0002514	.0002711	.0002915	.0003127	0003347	.000357
4	.0003808	.0004050	.0004299	.0004554	.0004819	.0005091	.0005870	.000565
4 5 6 7 8 9	.0005950 .0008568	.0006251	.0006560	.0006876	.0007199	.0007530 .0010445	.0007869	.000821
7	.0011662	.0012082	.0012510	.0012944	.0013387	.0013837	.0014295	.001475
8	.0015232	.0015711	.0016198	.0016698	.0017195	.0017705	.0018222	.001874
9	.0019278	.0019817	.0020363	.0020916	.0021479	.0022018	.0022625	.002820
0	.0023800	.0024398	.0025004	.0025618	.0026239	.0026867	.0027502	.002814
1	.0028798 .0084272	.0029456	.0030121	.0030794	.0031475 .0037187	.0082163	.0032859	.008856
2 2	.0040222	.0010999	.0033714	.0030347	.0043375	.0044182	.0044997	.003543
4	.0046648	.0017484	.0018328	.0049181	.0050039	.0050906	.0051780	.005266
5	.0053550	.0054446	.0055349	.0056261	.0057179	.0058105	.0059039	.005997
8	.0060928	.0061884	.0062847	.0063817	.0064795	.0065780	.0066774	.006777
7	.0068782	.0069797	.0070819	.0071850	.0072887	.0078932	.0074985	.007604
2 8 4 5 8 7 8	.0077112	.0078187	.0079268	.0080860	.0081452	.0082560	.0083672	.008479
ő	.0095200	.0096393	.0097594	.0098803	.0100019	.0101243	.0102474	.010371
ĭ l	.0104958	.0106211	.0107472	.0108739	.0110015	.0111299	.0112589	.011388
8	.0115192	.0116505	.0117825	.0119152		.0121830	.0123179	.012453
B	.0125902	.0127274	.0128654	.0130040	.0131485	.0132837	.0134247	.013566
<u> </u>	.0137088	.0138519 .0150241	.0139959	.0141405 .0153246	.0142859 .0154759	.0144321 .0156280	.0145789	.014726 .015984
4 5 8 7	.0148750 .0160888	.0162439	.0151789 .0163997	.0165568	.0167185	.0168716	.0170804	.017189
ž l	.0173502	.0175112	0176729	.0178355	.0179988	.0181627	.0188275	.018492
3 I	.0186592	.0188262	.0189939	.0191624	.0193316	.0195015	.0196722	.019848
9	.0200158	.0201887	.0208674	.0205368	.0207119	.0208879	.0210645	.021241
?	.0214200	.0215988 .0230566	.0217785	.0219588	.0221399 .0236155	.0223218	.0225044	.022657
1	.0243712	.0245619	.0247535	.0249457	.0251387	.0253825	.0255269	.025722
š	.0259182	.0261149	.0263124	0265106	.0267095	.0269092	.0271097	.027810
.	.0275128	.0277155	.0279189	.0281281	.0283279	.0285856	.0287899	.028947
8 4 5	.0291550	.0293636	.0295729	.0297831	.0299939	.0802056	.0304179	.030630
3	.0308448	.0810594	.0312747	.0314908	.0317075	.0819251	.0821484	.082362
7	.0325822	.0328027	.0330239	.0332460	.0334687	0355070	.0839165 .0857372	.084141
6	.0361998	0364322	.0366654	.0368993	.0371389	0373694	.0376055	.087842
5	.0380800	.0383184	.0385575	.0387973	.0390379	.0392798	.0395214	.089764
!	.0400078	.0402521	.0404972	.0407430	.0409895	.0412868	.0414849	.041738
}	.0419832	.0422885	.0424845	.0427862	.0429687	.0482420	.0434959	.043750
	.0440062 .0460768	.0442624	.0445194	.0447771	.0450355	.0452947	.0455547	.045815
5	.0481950	.0484681	.0487320	.0490016	.0492719	.0495430	.0498149	.050087
i	.0503608	.0506349	.0509097	.0511853	.0514615	.0517886	.0520164	.052294
r	.0525742	.0528542	.0531849	.0534165	.0586988	.0589818	.0542655	.054549
3	.0548352	.0551212	.0554079	.0556953	.0559885	.0562725	.0565622	.056852
?	.0571488	.0574357	.0577284	.0580218	.0588159	.0586109	.0589065 .0612984	.059202
1	.0595000 .0619088	.0697979	.0600965 .0625122	.0603959 .0628175	.0606959 .0682285	.0609969 .0634804	.0637879	.061600 .064046
	.0643552	.0646649	.0619753	.0652867	.0655987	.0659115	.0662250	.066539
i	.0668542	.0671699	.0674864	.0678036	.0681215	.0684402	.0687597	.069079
	.0694008	.0697225	.0700449	.0703681	.0705293	.0710166	.0713419	071668
<u> </u>	.0719950	.0724226	.0726510	.0729801	.0783099	.0736406	.0739719	.074808
	.0746368	.0749704	.075 3047 .0780060	.0756398 .0783476	.075 97 55	.0763120 .0790812	.0766494	.076987 .079718
	.0800682	.0804087	.0807549	.0811019	.0814495	.0817980	.0821472	.082497
	.0828478	.0881992	.0835514	.0889048	.0842579	.0846123	.0849675	.065828
	.0856800		.0868955		.0871189		.0878854	.088197

Horse-power per Pound Mean Effective Pressure. Area in sq. in. X piston-speed.

Diam. of Speed of Piston in feet per minute. Cylinder, 100 200 300 | 400 | 500 | 700 800 600 900 inches. .1142 .1523 0381 1904 .2285 .2666 0762 .3046 3427 .1928 2410 2892 .3374 .3856 436 .0482 0964.1446 .4338 .2380 .5355 .1190 .1785 .2975 .8570 .4165 .4760 .0595 ,2880 .1440 .2160 514 .0720 .3600 .4820 .5040 .5760 .6480 .3427 .1714 .2570 4284 .5141 .5998 .6854 .0857 .7711 .2011 ,3017 .5028 .7089 614 .1006 .4022 .6033 .8044 .9050 .4665 .5831 .6997 .8163 .2332 .3499 .9330 1.0496 .1166 .5355 .1839 .4016 .6694 .8033 .9871 1.0710 1.2049 .2678 .6098 .3046 .4570 .1616 .1523 1.0662 1.2186 .9139 1.3709 .6878 .8598 .1720 .3439 1.0317 1.2037 1.8756 1.5476 .5159 .3856 .1928 .5783 .7711 .0639 1.1567 1.8495 1.5422 1.5056 1.7184 1.7350 1.2888 .8592 1.0740 914 .2148 .4296 .6444 1.9532 10 .7140 .9520 1.1900 1.4280 1.0600 1.9040 2.1420 .2380 .4760 1.1519 1.4399 1.7279 2.0159 .2880 .5760 2.8038 11 .8639 2.8990 2.7418 2.8155 8.2178 2.5818 1.8709 1.7136 2.0563 1.6089 2.0111 2.4133 1.8659 2.3824 2.7989 2.1420 2.6775 3.2130 .8427 .6854 1.0282 3.0845 12 18 .4022 .8044 1.2067 .9330 1.3994 8.2178 8.7318 8 6200 8.2654 4.1983 .4665 14 5.2053 4 2840 4.2650 4.8742 4.6147 5.4026 5.3978 6.1690 6.0148 6.8734 6.6640 7.6160 15 .5855 1.0710 1.6065 4.8195 2,4371 3,0464 8.6557 16 .6093 1,2186 1.8278 5.4835 1.2756 1.9635 1.5422 2.3134 1.7184 2.5775 2.6518 3.3891 4.0269 6.1904 17 .6878 1,2:00 1.15492 2.8134 8.084b 6 2009 5.1551 6.0149 0.610 1.7184 2.5775 8.4467 4.2959 5.1551 6.0149 0.610 1.7184 2.5775 8.4467 4.2959 5.7120 6.6840 7.6160 8.5690 9.4662 2.0992 3.1488 4.1983 5.2479 6.2975 7.3471 8.3966 9.4462 2.3038 3.4558 4.6077 5.7596 6.9115 8.0634 9.2154 10.367 2.5180 3.7771 5.0616 6.2951 7.5541 8.8131 [10.072 11.381 2.7418 4.1126 5.4835 6.8544 8.2253 9.5963 [10.967 12.388 2.9750 4.4625 5.9900 7.4875 8.9250 [10.418 11.900 12.388 3.2178 4.8256 6.4955 8.0444 9.6234 [11.282 12.871 14.480 3.4700 5.2051 6.9101 8.6751 [10.410 12.145 18.880 15.615 8.7318 5.5978 7.4637 9.2296 [11.196 13.061 14.927 16.793 18.014 19.278 18.0047 8.0063 10.006 12.009 14.011 16.013 18.014 19.278 19.278 18 8.0845 8 8556 4.6267 .7711 19 .8592 20 .9520 21 1.0496 22 1.1519 23 1.2590 24 1.3709 25 26 1.4875 1.6089 27 1.7850 8,7318 5.5978 7.4637 9.329611.196 13.061 4.0032 6.0047 8.0063 10.008 12.009 14.011 4.9840 6.4260 8.5680 10.710 12.862 14.994 4.5744 6.8615 9.1487 11.436 13.723 16.010 4.8742 7.3114 9.7485 12.86 14.623 17.060 51.836 7.7755 10.367 12.369 15.561 18.148 5.5026 8.2538 11.005 13.756 16.508 19.259 5.8310 8.7465 11.662 14.578 17.493 20.409 6.4000 13.4000 1 28 1.8659 29 30 2.0016 2.1420 81 2.2872 18.297 20.585 14.497 20.785 21.934 82 2.4371 23.326 88 84 85 86 87 2.5918 22.010 24.762 2.7518 2.9155 20.409 21.591 22.808 24.067 25.340 28.824 26.240 18.507 19.549 20.620 21.720 3.0845 6,1690 9,2534 12,338 15,422 24.676 27.760 16.291 17.184 18.100 6.5164 9.7747 13.033 6.8784 10.310 13.747 7.2400 10.860 14.480 26.066 29.824 3.2582 27.494 30.930 3.4367 88 28.960 82,580 89 3.6200 22.848 26.656 80 464 3.8080 7.6160 11.424 15 232 19.040 34.272 40 4 0008 8 0016 12 002 16 003 20 004 4 1938 8 3966 12 585 16 783 20 982 82.006 36.007 41 88.577 85.205 37.775 39.606 41.469 42 4.4006 8.8012 13.202 17.602 22.003 4.6077 9.2154 13.823 18.431 23.088 4.8195 9.6390 14.459 19.278 24.098 48 86.861 44 88.556 48.876 45 5.0861 10.072 15.108 20.144 25.180 40.289 45.825 46 | 15.0661 | 10 072 | 15.108 | 20.144 | 25.180 | 15.274 | 10.515 | 15.772 | 21.039 | 29.87 | 5.4885 | 10.967 | 16.451 | 21.994 | 27.418 | 15.7144 | 11.429 | 17.143 | 22.858 | 28.672 | 25.672 | 23.800 | 29.750 | 6.1904 | 12.381 | 18.571 | 24.762 | 39.185 | 25.4855 | 24.855 | 24.855 | 24.875 | 23.278 | 23.278 | 25.485 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 25.278 | 42.059 47.817 47 43.868 49.852 48 51.429 45.715 49 47.600 49.523 51.484 50 53.550 55.718 57.920 51 25.742 82.178 26.742 83.427 27.760 84.700 59 58.483 55.521 60.169 53 54 55 56 57 6.9401 13.880 | 20.820 7.1995 14.899 | 21.599 62,461 57.596 28.798 35.998 64.796 44.789 52.246 46.396 54.128 48.088 56.044 49.709 57.998 87.818 59.709 67.178 7.4637 14.927 29.855 22.391 69.594 78.057 74.568 77.112

To draw the Clearance-line on the Indicator-diagram, the actual clearance not being known.—The clearance-line may be obtained approximately by drawing a straight line, cbad, across the compression curve, first having drawn OX parallel to the atmospheric line and 14.7 lbs. below. Measure from a the distance ad, equal to cb, and draw YO perpendicular to OX through d; then will TB divided by AT be the percentage of



F1g. 139.

clearance. The clearance may also be found from the expansion-line by constructing a rectangle efhg, and drawing a diagonal gf to intersect the line XO. This will give the point O, and by erecting a perpendicular to XO we obtain a clearance-line OY.

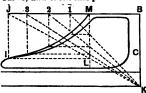
Both these methods for finding the clearance require that the expansion and compression curves be hyperbolas. Prof. Carpenter (Power, Sept., 1893) says that with good diagrams the methods are usually very accurate, and give results which check substantially.

and give results which check substantially.

The Buckeye Engine Co., however, say that, as the results obtained are seldom correct, being sometimes too little, but more frequently too much, and as the indications from the two curves seldom agree, the operation has little practical value, though when a clearly defined and apparently undistorted compression curve exists of sufficient extent to admit of the application of the process, it may be relied on to give much more correct results that the expension curve. than the expansion curve.

To draw the Hyperbolic Curve on the Indicator-diagram.—Select any point I in the actual curve, and from this point draw a

line perpendicular to the line JB, meeting the latter in the point J. The line JB may be the line of boiler-pressure, but this is not material; it may be drawn at any convenient height near the top of diagram and parallel to the atmospheric line. From J draw a diagonal to K, the latter point being the intersection of the vacuum and clearance lines; from I draw *IL* parallel with the atmospheric line. From *L*, the point of intersection of the diagonal *JK* and the horizontal line IL, draw the vertical line LM. The

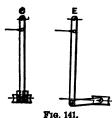


Frg. 140.

point M is the theoretical point of cut-off, and LM the cut-off line. Fix upon any number of points 1, 2, 3, etc., on the line JB, and from these points draw diagonals to K. From the intersection of these diagonals with LM draw horizontal lines, and from 1, 2, 3, etc., vertical lines. Where these lines meet will be points in the hyperbolic curve.

Pendulum Indicator Hig.—Power (Feb. 1893) gives a graphical representation of the errors in indicator-diagrams, caused by the use of

correct form of the pendulum rigging. It is shown that the "brumbo" pulley on the pendulum, to which the cord is attached, does not generate the condition of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum of the pendulum rigging.



o which the cord is attached, does not generally give as good a reduction as a simple pin attachment. When the end of the pendulum is slotted, working in a pin on the crosshead, the error is apt to be considerable at both ends of the card. With a vertical slot in a plate fixed to the crosshead, and a pin on the pendulum working in this slot, the reduction is perfect, when the cord is attached to a pin on the pendulum a slight arror being introduced if the dulum, a slight error being introduced if the brumbo pulley is used. With the connection between the pendulum and the crosshead made by means of a horizontal link, the reduction is nearly perfect, if the construction is such that the connecting link vibrates equally above and below the horizontal, and the cord is attached by a pin. If the link is horizontal at mid-stroke

a serious error is introduced, which is magnified if a brumbo pulley also is used. The adjoining figures show the two forms recommended.

used. The adjoining figures show the two forms recommended. Theoretical Water-consumption calculated from the Indicator-card.—The following method is given by Prof. Carpenter [Power, Sept. 1848): p = mean effective pressure, l = length of stroke in feet, a = area of piston in square inches, a + 144 = area in square feet, c = percentage of clearance to the stroke, b = percentage of stroke at point where water rate is to be computed. n = number of strokes per minute, 60n = number per hour, w = weight of a cubic foot of steam having a pressure as shown by the diagram corresponding to that at the point where sure as shown by the diagram corresponding to that at the point where water rate is required, w' = that corresponding to pressure at end of compression.

Number of cubic feet per stroke = $l(\frac{b+c}{100})\frac{a}{144}$

Corresponding weight of steam per stroke in lbs. = $l(\frac{b+c}{100})\frac{a}{144}w$.

Volume of clearance = $\frac{lca}{14,400}$

Weight of steam in clearance = $\frac{lcaw'}{14.400}$.

Total weight of steam per stroke $= l\left(\frac{b+c}{100}\right)\frac{wa}{144} - \frac{lcaw'}{14400} = \frac{la}{14400}\left[(b+c)w - cw'\right].$

Total weight of steam $= \frac{60nla}{14.400} [(b+c)w - cw'].$

The indicated horse power is $p \mid a \mid n + 33,000$. Hence the steam-consump tion per hour per indicated horse power is

$$= \frac{\frac{60nla}{14,400} \left[(b+c)w - cw' \right]}{\frac{p \ l \ a \ n}{83,000}} = \frac{187.50}{p} \left[(b+c)w - cw' \right].$$

Changing the formula to a rule, we have: To find the water rate from the indicator diagram at any point in the stroke.

RULE.—To the percentage of the entire stroke which has been completed by the piston at the point under consideration add the percentage of clearance. Multiply this result by the weight of a cubic foot of steam, having a pressure of that at the required point. Subtract from this the product of percentage of clearance multiplied by weight of a cubic foot of steam having a pressure equal to that at the end of the compression. Multiply this result by 187.50 divided by the mean effective pressure.*

Notz.—This method only applies to points in the expansion curve or be-

Norz.—This method only applies to points in the expansion curve or be-

tween cut-off and release.

[•] For compound or triple-expansion engines read: divided by the equivalent mean effective pressure, on the supposition that all work is done in one vlinder.

e beneficial effect of compression in reducing the water-consumption of agine is clearly shown by the formula. If the compression is carried to a point that it produces a pressure equal to that at the point under ideration, the weight of steam per cubic foot is equal, and w=w'. In case the effect of clearance entirely disappears, and the formula mes $\frac{187.5}{(bw)}$.

case of no compression, w' becomes zero, and the water-rate =

$$\frac{187}{p}$$
⁵[(b + c)w].

of. Denton (Trans. A. S. M. E., xiv. 1863) gives the following table of retical water-consumption for a perfect Mariotte expansion with steam i0 lbs. above atmosphere, and 2 lbs. absolute back pressure:

tio of Expansion, r.	M.E.P., lbs. per sq. in.	Lbs. of Water per hour per horse-power, W.		
10	52.4	9.68		
15	88.7	8.74		
20	80.9	8.20		
25	25.9	7.84		
80	22.2	7.63		
35	19.5	7.45		

ne difference between the theoretical water-consumption found by the nula and the actual consumption as found by test represents "water not unted for by the indicator," due to cylinder condensation, leakage ugh ports, radiation, etc.

eakage of Steam.-Leakage of steam, except in rare instances, has ttle effect upon the lines of the diagram that it can scarcely be detected, only satisfactory way to determine the tightness of an engine is to take hen not in motion, apply a full boiler-pressure to the valve, placed in a ed position, and to the piston as well, which is blocked for the purpose at ee point away from the end of the stroke, and see by the eye whether age occurs. The indicator-cocks provide means for bringing into view m which leaks through the steam-valves, and in most cases that which is by the piston, and an opening made in the exhaust-pipe or observas at the atmospheric escape-pipe, are generally sufficient to determine fact with regard to the exhaust-valves.

he steam accounted for by the indicator should be computed for both cut-off and the release points of the diagram. If the expansion-line dets much from the hyperbolic curve a very different result is shown at point from that shown at the other. In such cases the extent of the occasioned by cylinder condensation and leakage is indicated in a much e truthful manner at the cut-off than at the release. (Tabor Indicator

:ular.)

COMPOUND ENGINES.

ompound, Triple- and Quadruple-expansion Engines. compound engine is one having two or more cylinders, and in which steam after doing work in the first or high-pressure cylinder completes

expansion in the other cylinder or cylinders.

he term "compound" is commonly restricted, however, to engines in the expansion takes place in two stages only—high and low pressure, terms triple-expansion and quadruple-expansion engines being used when expansion takes place respectively in three and four stages. The number ylinders may be greater than the number of stages of expansion, for structive reasons; thus in the compound or two-stage expansion engine structive reasons; thus in the compound or two-stage expansion engine low-pressure stage may be effected in two cylinders oa sto obtain the antages of nearly equal sizes of cylinders and of three cranks at angles of . In triple-expansion engines there are frequently two low-pressure nders, one of them being placed tandem with the high-pressure, and the er with the intermediate cylinder, as in mill engines with two cranks at In the triple-expansion engines of the steamers Campania and Lucania,

with three cranks at 120°, there are five cylinders, two high, one intermediate, and two low, the high-pressure cylinders being tandem with the low.

Advantages of Compounding.—The advantages secured by dividing the expansion into two or more stages are twofold: 1. Reduction of wastes of steam by cylinder-condensation, clearance, and leakage; 2. Dividing the pressures on the cranks, shafts, etc., in large engines so as to avoid excessive pressures and consequent friction. The diminished loss by cylinder-condensation is effected by decreasing the range of temperature of the metal surfaces of the cylinders, or the difference of temperature of the steam at admission and exhaust. When high-pressure steam is admitted into a single-cylinder engine a large portion is condensed by the comparatively cold metal surfaces; at the end of the stroke and during the exhaust the water is re-evaporated, but the steam so formed escapes into the atmosphere or into the condenser, doing no work; while if it is taken into a second cylinder, as in a compound engine, it does work. The steam lost in the first cylinder by leakage and clearance also does work in the second cylinder. Also, if there is a second cylinder, the temperature of the steam exhausted from the first cylinder is higher than if there is only one cylinder, and the metal surfaces therefore are not cooled to the same degree. The difference in temperatures and in pressures corresponding to the work of steam of of steam by cylinder-condensation, clearance, and leakage; 2. Dividing the In temperatures and in pressures corresponding to the work of steam of 150 lbs. gauge-pressure expanded 20 times, in one, two, and three cylinders, is shown in the following table, by W. H. Weightman, Am. Mach., July 28,

	Single Cyl- inder.	Comp Cylin		Trip	le-expan ylinders	sion
Diameter of cylinders, in	60	88	61	28	46	61
Area ratios		1	8.416	1	2.70	4.741
Expansions	20	1 5	4	8.714	2.714	2.714
Initial steam - pressures-	ŀ					
absolute-pounds		165	88	165	60.8	22.4
Mean pressures, pounds	82.96	86.11	19.68	121.44	44.75	16.49
Mean effective pressures.		57722				
pounds	28.96	58.11	15.68	60.64	22,85	12.49
Steam temperatures into		55.52		55152		
cylinders	8660	8660	259 .9	3669	293°.5	234°.1
Steam temperatures out of		000		300		
the cylinders	1840.2	2590.9	1840.2	298°.5	2840.1	184°.2
Difference in temperatures		106.1	75.7	72.5	59.4	49.9
Horse-power developed	800	899	408	269	268	264
Speed of piston	822	290	290	238	288	288
Total initial pressures on		~~~				
pistons, pounds	455.218	112,900	84,752	64.169	68.817	58,778

66 Woolf? and Receiver Types of Compound Engines.— The compound steam-engine, consisting of two cylinders, is reducible to two forms, 1, in which the steam from the 1.p. cylinder is exhausted direct into the 1.p. cylinder, as in the Woolf engine; and 2, in which the steam from the h.p. cylinder is exhausted into an intermediate reservoir, whence the steam is supplied to, and expanded in, the 1.p. cylinder, as in the "receiverengine.

If the steam be cut off in the first cylinder before the end of the stroke, the total ratio of expansion is the product of the ratio of expansion in the first cylinder, into the ratio of the volume of the second to that of the first cylinder; that is, the product of the two ratios of expansion.

Thus, let the areas of the first and second cylinders be as 1 to 314, the strokes being equal, and let the steam be cut off in the first at 1/4 stroke; then

..... 1 to 8½

Total or combined expansion, the product of the two ratios... 1 to 7

Woolf Engine, without Clearance-Ideal Diagrams. The diagrams of pressure of an ideal Woolf engine are shown in Fig. 149, as they would be described by the indicator, according to the arrows. In these diagrams pg is the atmospheric line, mn the vacuum line, ed the admission

dg the hyperbolic curve of expansion in the first cylinder, and gA the con-

tive expansion-line of back pressure he return-stroke of the first piston, of positive pressure for the steam-ke of the second piston. At the point the end of the stroke of the second on, the steam is exhausted into the lenser, and the pressure falls to the of perfect vacuum, mu.

e diagram of the second cylinder, wgh, is characterized by the absence ny specific period of admission; the ie of the steam-line gh being expanal, generated by the expansion of initial body of steam contained in irst cylinder into the second. When return-stroke is completed, the first is shut into the second cylin-

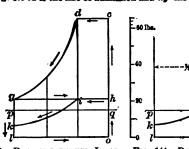
The final pressure and volume of Fig. 142.—Woolf Engine—IDEAL steam in the second cylinder are the

60 lbs.

s as if the whole of the initial steam had been admitted at once into the nd cylinder, and then expanded to the end of the stroke in the manner single-cylinder engine.

e net work of the steam is also the same, according to both distributions. scolver-engine, without Clearance—Ideal Biagrams.—
ne ideal receiver-engine the pistons of the two cylinders are coned to oranks at right angles to each other on the same shaft. The iver takes the steam exhausted from the first cylinder and supplies it to second, in which the steam is cut off and then expanded to the end of troke. On the assumption that the initial pressure in the second cylins equal to the final pressure in the first, and of course equal to the present in the receiver, the volume out off in the second cylinder must be I to the volume of the first cylinder, for the second cylinder must admit uch steam at each stroke as is discharged from the first cylinder.

Fig. 148 cd is the line of admission and Ag the exhaust-line for the first



48.—Receiver-engine, Ideal INDICATOR-DIAGRAMS.

Fig. 144.—RECEIVER ENGINE, IDEAL DIAGRAMS REDUCED AND COMBINED.

ler; and dg is the expansion-curve and pq the atmospheric line. gion below the exhaust-line of the first cylinder, between it and the perfect vacuum, ol, the diagram of the second cylinder is formed; hi, cond line of admission, coincides with the exhaust-line hg of the first er, showing in the ideal diagram no intermediate fall of pressure, and se expansion-curve. The arrows indicate the order in which the diaare formed.

ne action of the receiver-engine, the expansive working of the steam. n clearly divided into two consecutive stages, is, as in the Woolf, essentially continuous from the point of cut-off in the first cylinder and of the stroke of the second cylinder, where it is delivered to the iser; and the first and second diagrams may be placed together and

combined to form a continuous diagram. For this purpose take the second diagram as the basis of the combined diagram, namely, hiklo, Fig. 144. The period of admission, hi, is one third of the stroke, and as the ratios of the cylinders are as 1 to 3, hi is also the proportional length of the first diagram cylinders are as 1 to 3, ht is also the proportional length of the first diagram as applied to the second. Produce oh upwards, and set off oc equal to the total height of the first diagram above the vacuum-line; and, upon the shortened base hi, and the height hc, complete the first diagram with the steam-line cd, and the expansion-line di.

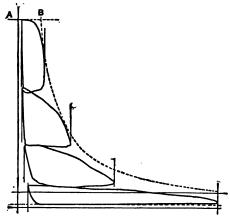
It is shown by Clark (S. E., p. 432, et seq.) in a series of arithmetical calculations, that the receiver-engine is an elastic system of compound engine, which considers his latitude is afforded for adopting the pressure in the

in which considerable latitude is afforded for adapting the pressure in the receiver to the demands of the second cylinder, without considerably diminishing the effective work of the engine. In the Woolf engine, on the contrary, it is of much importance that the intermediate volume of space between the first and second cylinders, which is the cause of an intermediate fall of pressure, should be reduced to the lowest practicable amount.

Supposing that there is no loss of steam in passing through the engine, by cooling and condensation, it is obvious that whatever steam passes through the first cylinder must also find its way through the second cylindrical statement of the second der. By varying, therefore, in the receiver-engine, the period of admission in the second cylinder, and thus also the volume of steam admitted for each stroke, the steam will be measured into it at a higher pressure and of a less bulk, or at a lower pressure and of a greater bulk; the pressure and density naturally adjusting themselves to the volume that the steam from the receiver is permitted to occupy in the second cylinder. With a sufficiently restricted admission, the pressure in the receiver may be maintained at the pressure of the steam as exhausted from the first cylinder. On the contrary, with a wider admission, the pressure in the receiver may fall or "drop" to three fourths or even one half of the pressure of the exhauststeam from the first cylinder.

(For a more complete discussion of the action of steam in the Woolf and

receiver engines, see Clark on the Steam-engine,)
Combined Diagrams of Compound Engines.—The only way of making a correct combined diagram from the indicator-diagrams of the several cylinders in a compound engine is to set off all the diagrams on the same horizontal scale of volumes, adding the clearances to the cylinder ca-



pacities proper. When this is attended to, the successive diagrams fall exactly into their right places relatively to one another, and would compare properly with any theoretical expansion-curve. (Prof. A. B. W. Kennedy. Proc. Inst. M. E., Oct. 1886.)

his method of combining diagrams is commonly adopted, but there are ctions to its accuracy, since the whole quantity of steam consumed in first cylinder at the end of the stroke is not carried forward to the add, but a part of it is retained in the first cylinder for compression. For ethod of combining diagrams in which compression is taken account of, discussions by Thomas Mudd and others, in Proc. Inst. M. E., Feb., p. 48. The usual method of combining diagrams is also criticised by k H. Ball as inaccurate and misleading (Am. Mach., April 12, 1894; 18, A. S. M. E., xiv. 1405, and xv. 408).

is, A. S. M. E., XIV. 1406, and XV. 400.

gure 145 shows a combined diagram of a quadruple-expansion engine, vn according to the usual method, that is, the diagrams are first reduced night to relative scales that correspond with the relative psicon-displacet of the three cylinders. Then the diagrams are placed at such distances 1 the clearance-line of the proposed combined diagram as to correctly esent the clearance in each cylinder.

culated Expansions and Pressures in Two-cylinder pround Engines. (James Tribe, Am. Mach., Sept. & Oct. 1891.)

TWO-CYLINDER COMPOUND NON-CONDENSING.

al gauge-	100	110	120	130	140	150	160	170	175
al absolute						l			
388ure	115	125	135	145	155	165	175	185	190
l expansion.	7.89	7.84	8.41	9	9.61	10.24	10.89	11.56	11.9
ansionsin						1			1
ch cylinder	2.7	2.8	2.9	3	3.10	8.2	8.8	3.4	3.45
log, plus 1.				2.098		2.168			
ard High.			90		106.5			120.9	123.2
sures Low.			83.1						85.7
High.		44.6	46.5		50	51.5		54.4	55
sures Low.			15.5		15.5				15.5
wine J migu.	42.3		49.5		56.5				68.2
MAY L GAME	15.8	16.8	17.6	18.2	18.8	19.3	19.7	20.1	20.2
sures (Down						l	,		
-cylinder					١.	٠	یہ ما		
88	2.67	2.73	2.81	2.91	8	8.11	8.21	8.31	8.87

TWO-CYLINDER COMPOUND CONDENSING.

warma & & Iha ahora raguum

ck pressure 1/4 lb. above atmosphere.

ar biosente, oro rost anove	vacuu				-		
I gauge-pressures	90	100	110	120	180	140	150
l absolute pressures	105	115	125	135	145	155	165
able per cent of loss	2.6	2.9	3.8	8.6	8.8	4.0	4.8
expansions	15.7	17	18.5	90	21.5	22.7	24.2
in each cylinder	3.96	4.13	4.3	4.47	4.64	4.77	4.92
log. plus 1				2.497	2.534	2.562	2.593
forward (High			71.4	75.4	79.8	83.2	87
ssures Low					16.5	16.75	17.05
back High		27.8				32.4	33.5
ures Low	4.8	4.8	4.8	4.3	4.8	4.3	4.3
in High	36.4	39.5	42.4	45.2	47.9	50.8	58.5
ive Low	10.95	11.25					12.75
ires (
	26.5	27.8					33.5
ires Low	6.4	6.45	6.45	6.5	6.55	6.55	6.6
pressure in l. p. cyl	25.3						32.4
of cylinder areas	3.32	8.51	3.66	8.8	3.92	4.08	4.19

probable percentage of loss, line 3, is thus explained: There is always of heat due to condensation, and which increases with the pressure of . The exact percentage cannot be predetermined, as it depends rupon the quality of the non-conducting covering used on the cylinceiver, and pipes, etc., but will probably be about as shown.

Portions of Cylinders in Compound Engines.—Authorities as to the proportions by volume of the high and low pressure

ers v and V. Thus Grashof gives $V + v = 0.85 \sqrt{r}$; Hrahak. 0.90 \sqrt{r} ;

Werner, \sqrt{r} ; and Rankine, $\sqrt{r^2}$, r being the ratio of expansion. Busier makes the ratio dependent on the boiler-pressure thus:

(See Seaton's Manual, p. 25, etc., for analytical method; Sennett, p. 492, etc.; Clark's Steam-engine, p. 445, etc.; Clark, Bules, Tables, Data, p. 849, etc.)
Mr. J. McFarlane Gray states that he finds the mean effective pressure in the compound engine reduced to the low-pressure cylinder to be approxi-

mately the square root of 6 times the boiler-pressure.

Approximate Horse-power of a Modern Compound Marine-engine. (Seaton.)—The following rale will give approximately the horse-power developed by a compound engine made in accordance with

modern marine practice. Estimated H.P. =
$$\frac{D^{n} \times \sqrt{p} \times R \times S}{8500}$$

D = diameter of l.p. cylinder; p = boller-pressure by gauge;

R = revs. per units.: S = stroke of piston in feet.

Hatio of Cylinder Capacity in Compound Marine En-gines. (Seaton.)—The low-pressure cylinder is the measure of the power games. (ceach).—In low-pressure cylinder is the measure of the power of a compound engine, for so long as the initial steam-pressure and rate of expansion are the same, it signifies very little, so far as total power only is converned, whether the ratio between the low and high-pressure cylinders is 3 or 4; but as the power developed abould be nearly equally divided between the two cylinders, in order to get a good and steady working engine, there is a necessity for exercising a considerable amount of discretion in fixing on the ratio.

In choosing a particular ratio the objects are to divide the power evenly and to avoid as much as possible "drop" and high initial strain.

If increased economy is to be obtained by increased boiler pressures, the rate of expansion should vary with the initial pressure, so that the pressure at which the steam enters the condenser should remain constant. In this case, with the ratio of cylinders constant, the cut-off in the high-pressure cylinder will vary inversely as the initial pressure. Let R be the ratio of the cylinders; r, the rate of expansion; p, the initial pressure: then cut-off in high-pressure cylinder = R + r; r varies with p_1 ,

pressure: then cut-off in high-pressure cylinder = E + r; r varies with p_1 , so that the terminal pressure p_n is constant and consequently $r = p_1 + p_n$; therefore, cut-off in high-pressure cylinder = $R \times p_n + p_1$. **Ratios of Cylinders as Found in Marine Practice.**—The rate of expansion may be taken at one tenth of the boller-pressure (or about one twelfth the absolute pressure), to work economically at full speed. Therefore, when the diameter of the low-pressure cylinder does not exceed 100 inches, and the boller-pressure 70 lbs., the ratio of the low-pressure to the high-pressure cylinder should be 3.5; for a boller-pressure of 50 lbs., 8.75 for 90 lbs. 4.0. for 190 lbs. 4.5. If these proportions are adhered to there for 90 bs., 40; for 190 bs., 48. If these proportions are adhered to, there will be no need of an expansion-valve to either cylinder. If, however, to avoid "drop," the ratio be reduced, an expansion-valve should be fitted to the high-pressure cylinder.

Where economy of steam is not of first importance, but rather a large power, the ratio of cylinder capacities may with advantage be decreased, so that with a boiler-pressure of 100 lbs. it may be 3.75 to 4.

In tandem engines there is no necessity to divide the work equally. The ratio is generally 4, but when the steam-pressure exceeds 99 Ha. absolute 4.5 is better, and for 100 lbs. 5.0.

When the power requires that the l. p. cylinder shall be more than 760 in. diameter, it should be divided in two cylinders. In this case the ratio of the

diameter, it should be divided in two cylinders. In time case the rath of the combined capacity of the two i. p. cylinders to that of the h. p. may be 3.0 for 35 lbs. absolute, 3.4 for 95 lbs., 3.7 for 105 lbs., and 4.9 for 115 lbs.

**Becedwer Space in Compound Engines should be from 1 to 1.5 times the capacity of the high-pressure cylinder, when the cranks are at an angle of from 90° to 120°. When the cranks are at 180° or nearly this, the apace may be very much reduced. In the case of triple-compound engines, with cranks at 190°, and the intermediate cylinder leading the high-pressure, a very small receiver will do. The pressure in the receiver should never exceed half the boiler-pressure. (Seaton.)

ormula for Calculating the Expansion and the Work of Steam in Compound Engines.

(Condensed from Clark on the "Steam-engine.")

s = area of the first cylinder in square inches;
' = area of the second cylinder in square inches;

= area of the second cylinder in square inches;
= ratio of the capacity of the second cylinder to that of the first;
= length of stroke in feet, supposed to be the same for both cylinders;
i= period of admission to the first cylinder in feet, excluding clearance;
= clearance at each end of the cylinders, in parts of the stroke, in feet;
= length of the stroke plus the clearance, in feet;
= period of admission plus the clearance, in feet;
= length of a given part of the stroke of the second cylinder, in feet;
= total initial pressure in the first cylinder, in lbs. per square inch, supposed to be uniform during admission;
= total pressure at the end of the given part of the stroke s;
= average total pressure for the whole stroke;
= nominal ratio of expansion in the first cylinder, or L+2;
= actual ratio of expansion in the first cylinder, or L+2;

'' = actual ratio of expansion in the first cylinder, or L' + l'; '' = actual combined ratio of expansion, in the first and second cylinders together;

together;
t = ratio of the final pressure in the first cylinder to any intermediate fall of pressure between the first and second cylinders;
f = ratio of the volume of the intermediate space in the Woolf engine, reckoned up to, and including the clearance of, the second piston, to the capacity of the first cylinder plus its clearance. The value of N is correctly expressed by the actual ratio of the volumes as stated, on the assumption that the intermediate space is a vacuum when it receives the exhaust-steam from the first cylinder. In point of fact, there is a residuum of unexhausted steam in the intermediate mace at low pressure and the value of N is thereby pracdiate space, at low pressure, and the value of N is thereby prac-

tically reduced below the ratio here stated. $N = \frac{n}{n-1} - 1$.

whole net work in one stroke, in foot-pounds.

latio of expansion in the second cylinder:

In the Woolf engine,
$$\frac{\left(r\frac{L}{L'}\right) + \pi}{1 + \lambda'}$$

In the receiver-engine,
$$\frac{(n-1)r}{r}$$
.

Total actual ratio of expansion = product of the ratios of the three con-native expansions, in the first cylinder, in the intermediate space, and the second cylinder.

In the Woolf engine,
$$R'\left(r\frac{L}{L'} + N\right)_{\xi}$$

In the receiver-engine,
$$r_{\overline{k'}}^{\underline{L'}}$$
, or rR' .

combined ratio of expansion behind the pistons = $\frac{m-1}{rR'} = R''$.

Nork done in the two cylinders for one stroke, with a given cut-off and a en combined actual ratio of expansion;

Woolf engine,
$$w = aP[l'(1 + \text{hyp log } R'') - c];$$

Receiver engine,
$$w = aP \left[l'(1 + \text{hyp log } R'') - c \left(1 + \frac{r-1}{R'} \right) \right]$$
.

ion there is no intermediate fall of pressure. When there is an intermediate fall, when the pressure falls to 34, 36, 36 of a final pressure in the 1st cylinder, the reduction of work is 0.2%, 1.0%, 4.6% that when there is no fall.

Total work in the two cylinders of a receiver-engine, for one stroke for any intermediate fall of pressure,

$$w = aP\left[l'\left(\frac{n+1}{n} + \text{hyp log } R''\right) - c\left(1 + \frac{(n-1)(r-1)}{nR'}\right)\right].$$

Example.—Let a=1 sq. in., P=63 lbs., l'=2.42 ft., n=4, R''=5.969, c=.42 ft., r=3, R'=2.653;

$$w = 1 \times 63 \left[2.42(5/4 \text{ hyp log } 5.969) - .42 \left(1 + \frac{3 \times 2}{4 \times 2.658} \right) \right] = 421.55 \text{ ft.-lbs.}$$

Calculation of Diameters of Cylinders of a compound condensing engine of 2000 H.P. at a speed of 700 feet per minute, with 100 lbs.

boiler-pressure.

100 lbs. gauge-pressure = 115 absolute, less drop of 5 lbs. between boiler and cylinder = 110 lbs. initial absolute pressure. Assuming terminal pressure in l. p. cylinder = 6 lbs., the total expansion of steam in both cylinders = 110+6 = 18.33. Hyp log 18.33 = 2.909. Back pressure in l. p. cylinder, 3 lbs. absolute.

The following formulæ are used in the calculation of each cylinder:

 $H.P. \times 33,000$ (1) Area of cylinder = $\frac{1}{\text{M.E.P.} \times \text{piston-speed}}$

(2) Mean effective pressure = mean total pressure - back pressure.
 (3) Mean total pressure = terminal pressure × (1 + hyp log R).

(4) Absolute initial pressure = absolute terminal pressure × ratio of expansion.

First calculate the area of the low-pressure cylinder as if all the work were done in that cylinder.

From (3), mean total pressure = $6 \times (1 + \text{hyp log } 18.38) = 23.454 \text{ lbs.}$ From (2), mean effective pressure = 23.454 - 3 = 20.454 lbs.

 $2000 \times 83,000$ From (1), area of cylinder = $\frac{2000 \times 5000}{20.454 \times 700}$ = 4610 sq. ins. = 76.6 ins. diam.

If half the work, or 1000 H.P., is done in the l. p. cylinder the M.E.P. will be half that found above, or 10.227 lbs., and the mean total pressure 10.227 + 3 = 13.227 lbs.

3 = 13.227 lbs.
From (3), 1 + hyp log R = 13.227 + 6 = 2.2045.
Hyp log R = 1.2045, whence R in l. p. cyl. = 3.835.
From (4), 8.335 × 6 = 20.01 lbs. initial pressure in l. p. cyl. and terminal pressure in h. p. cyl., assuming no drop between cylinders. 110 + 20.01 = 18.33 + 8.335 = 5.497, R in h. p. cyl.
From (3), mean total pres. in h. p. cyl. = 20.01 × (1 + hyp log 5.497) = 54.11.
From (2), 54.11 - 20.01 = 34.10, M.E.P. in h. p. cyl.
From (1), area of h. p. cyl. = $\frac{1000 \times 83,000}{700 \times 84.1}$ = 1382 sq. ins. = 42 ins. diam.

Cylinder ratio = 4610 + 1382 = 8.336.

The area of the h. p. cylinder may be found more directly by dividing the area of the l. p. cyl. by the ratio of expansion in that cylinder. 4610 +

3.335 = 1382 sq. ins.

In the above calculation no account is taken of clearance, of compression, of drop between cylinders, nor of area of piston-rods. It also assumes that the diagram in each cylinder is the full theoretical diagram, with a horizontal steam-line and a hyperbolic expansion line, with no allowance for counding of the corners. To make allowance for these, the mean effective pressure in each cylinder must be multiplied by a diagram factor, or the ratio of the area of an actual diagram of the class of engine considered, with the

given initial and terminal pressures, to the area of the theoretical diagram. Such diagram factors will range from 0.6 to 0.94, as in the table on p. 745.

Best Ratios of Cylinders.—The question what is the best ratio of areas of the two cylinders of a compound engine is still (1901), a disputed one, but there appears to be an increasing tendency in favor of large ratios, even as great as 7 or 8 to 1, with considerable terminal drop in the high-pressure cylinder. A discussion of the subject together with a description pressure cylinder. A discussion of the subject, together with a description of a new method of drawing theoretical diagrams of multiple-expansion engines, taking into consideration drop, clearance, and compression, will be found in a paper by Bert C, Ball, in Trans. A. S, M. E., xxi. 1002.

TRIPLE-EXPANSION ENGINES.

Proportions of Cylinders.—H. H. Suplee, Mechanics, Nov. 1887, es the following method of proportioning cylinders of triple-expansion

gines:
As in the case of compound engines the diameter of the low-pressure
linder is first determined, being made large enough to furnish the entire wer required at the mean pressure due to the initial pressure and expan-nratio given; and then this cylinder is only given pressure enough to per-m one third of the work, and the other cylinders are proportioned so as to ide the other two thirds between them.

et us suppose that an initial pressure of 150 lbs. is used and that 900 H.P. to be developed at a piston-speed of 800 ft. per min., and that an expann ratio of 16 is to be reached with an absolute back pressure of 2 lbs. The theoretical M.E.P. with an absolute initial pressure of 150 + 14.7 =

.7 lbs. initial at 16 expansions is

$$\frac{P(1 + \text{hyp log 16})}{16} = 164.7 \times \frac{8.7726}{16} = 38.83,$$

s 2 lbs. back pressure, = 88.83 - 2 = 36.83. n practice only about 0.7 of this pressure is actually attained, so that $33 \times 0.7 = 25.781$ lbs. is the M.E.P. upon which the engine is to be protioned.

to obtain 900 H.P. we must have $83,000 \times 900 = 29,700,000$ foot-pounds, and s divided by the mean pressure (25.78) and by the speed in feet (800) will e 1440 sq. in. for the area of the l. p. cylinder, about equivalent to 43 in.

low as one third of the work is to be done in the l.p. cylinder, the M.R.P.

to will be 25.78 + 8 = 8.59 lbs., the cut-off in the high-pressure cylinder is generally arranged to cut off 1.6 of the stroke, and so the ratio of the h. p. to the 1. p. cylinder is equal $16 \times 0.6 = 9.6$, and the h. p. cylinder will be 1440 + 9.6 = 150 sq. in. area, or at 14 in diameter, and the M.E.P. in the h. p. cylinder is equal to $\times 8.59 = 82.46$ lbs.

I the intermediate cylinder is made a mean size between the other two size would be determined by dividing the area of the l. p. cylinder by the are root of the ratio between the low and the high; but in practice this is and to give a result too large to equalize the stresses, so that instead the a of the int. cylinder is found by dividing the area of the l. p. piston by times the square root of the ratio of l. p. to h. p. cylinder, which in this

e is $1440 + (1.1 \sqrt{9.6}) = 422.5$ sq. in., or a little more than 23 in. diam. he choice of expansion ratio is governed by the initial pressure, and is erally chosen so that the terminal pressure in the l. p. cylinder shall be

ut 10 lbs. absolute.

Formulæ for Proportioning Cylinder Areas of Triple-pansion Engines.—The following formulæ are based on the method irst finding the cylinder areas that would be required if an ideal hyperc diagram were obtainable from each cylinder, with no clearance, comsion, wire-drawing, drop by free expansion in receivers, or loss by order condensation, assuming equal work to be done in each cylinder, then dividing the areas thus found by a suitable diagram factor, such as e given on page 715, expressing the ratio which the area of an actual ram, obtained in practice from an engine of the type under considerables are to the ideal or theoretical diagram. It will vary in different classes ngine and in different cylinders of the same engine, usual values ranging 10.6 to 0.9. When any one of the three stages of expansion takes place to cylinders, the combined area of these cylinders equals the area found te formulæ.

NOTATION.

 $p_b = back$

 p_2 = term. press. in h. p. cyl. and initial press. in intermediate cyl. p_3 = " int. " " l. p. cyl.

 R_1 , R_2 , R_3 , ratio of exp. in h. p. int. and l. p. cyls. $R = \text{total ratio of exp.} = R_1 \times R_2 \times R_3$. $P = \text{mean effec. press. of the combined ideal diagram, referred to the second of the combined ideal diagram.$ cyl.

P.
$$P_2$$
 = m. c. p in the h. p. int., and . p. cyle.

H. v. have proper of the engine = $F_1 A_2 V + R_1 R_2$.

L. a benefit of structs in facts, $V = \text{manner} f$ starts strukes per min.

A. A. A. stream on ma. of h. p. int. and l. p. cyle. liked,

W. work dense n. one cylinder per $V \cap K A$ struct.

y. a Pair, of $A_1 V \cap A_1 = 1 - \text{min} A_1 V \cap A_2$.

y. P_2 diagram factors of a. p. int. and l. p. cyl.

G. P_3 = P_4 diagram factors of a. p. int. and l. p. cyl.

(i.) $E = p_1 + p_1$.

(i.) $E = p_1 + p_2$.

(1) $H_1 = 0.000 HF +$

THEOGRATICAL MEAN ESPECTIVE PRESCREE, CYLINDER RATIOS, ETC., OF TRIPLE EXPANSION ENGINEE.

Back pressure, 3 lbs. Terminal pressure, 8 lbs. (absolute).

p 1.	B.	P.	Pg.	R ₂ .	R ₁ , R ₂ .	P2.	p ₂ .	P2.	P_1 .	rs.
120 140 160 160 190 220 220	15 11 5 20 24,5 25 27.5	28 66 27,90 29,97 29,91 80,75 31,51 32,81	8,89 9,30 9,66 9,97 10,25 10,50 10,74	1.626 1.712 1.790 1.861 1.928 1.990 2.049	8.037 8.197 3.343 3.477 3.601 3.715 3.826	13.70 14.32 14.59 15.42 15.91	48.79 47.86 51.77 55.54 59.16	14.45 15.92 17.29 18.55 19.76 20.90 22.00	50.89 57.76 64.52 71.16 77.69	5.472 5.980 6.471 6.948 7.397

Back pressure, 8 lbs. Terminal pressure, 10 lbs. (absolute).

ν1.	R.	P.	P ₃ ,	R ₃ .	R ₁ , R ₂ , or r ₂ .	p ₂ .	p ₂ .	P3.	Pi.	rs.
190 140 160 160 900 990 940	19 14 16 18 90 93 94	81.85 88.89 84.78 85.90 86.96 87.91 88.78	11.18 11.58	1.486 1.511 1.580 1.648 1.702 1.757 1.809	2.890 8.044 8.182 8.810 8 428 8.538 8.642	14.86 15.11 15.80 16.43 17.02 17.57 18.09	45.99 50.28 54.88 58.84 62.15	16.82 18.29	58.20 65.09 71.88	4.600 5.027 5.439 5.834 6.215

(liven the required H.P. of an engine, its speed and length of stroke, and the assumed diagram factors F_1 , F_2 , F_3 for the three cylinders, the areas of the cylinders may be found by using formulæ (11), (12), and (14), and the values of P_1 , P_2 , and P_3 in the above table.

I Common Rule for Proportioning the Cylinders of mulle-expansion engines is: for two-cylinder compound engines, the cylinder io is the square root of the number of expansions, and for triple-expansion times the ratios of the high to the intermediate and of the intermediate the low are each equal to the cube root of the number of expansions, the io of the high to the low being the product of the two ratios, that is, the are of the cube root of the number of expansions. Applying this rule to pressure above given, assuming a terminal pressure (absolute) of 10 lbs. 18 lbs. respectively, we have, for triple-expansion engines:

Boiler-	Terminal	Pressure, 10 lbs.	Termina	l Pressure, 8 lbs.
essure	No. of Ex-	Cylinder Ratios,	No. of Ex-	Cylinder Ratios,
solute).	pansions.	areas.	pansions.	areas.
130	18	1 to 2.35 to 5.53	1634	1 to 2.58 to 6.42
140	14	1 to 2.41 to 5.81	1734	1 to 2.60 to 6.74
150	15	1 to 2.47 to 6.08	1894	1 to 2.66 to 7.06
160	16	1 to 2.52 to 6.35	20	1 to 2.71 to 7.87

he ratio of the diameters is the square root of the ratios of the areas, and ratio of the diameters of the first and third cylinders is the same as the io of the areas of first and second.

eaton, in his Marine Engineering, says: When the pressure of steam emyed exceeds 115 lbs. absolute, it is advisable to employ three cylinders, ough each of which the steam expands in turn. The ratio of the low-ssure to high-pressure cylinder in this system should be 5, when the am-pressure is 125 lbs. absolute; when 135 lbs. absolute, 5.4; when 145 absolute, 5.8; when 155 lbs. absolute, 6.2; when 165 lbs. absolute, 6.4. ratio of low-pressure to intermediate cylinder should be about one half t between low-pressure and high-pressure, as given above. That is, if ratio of l. p. to h. p. is 6, that of l. p. to int. should be about 3, and consently that of int. to h. p. about 2. In practice the ratio of int. to h. p. is rly 2.25, so that the diameter of the int. cylinder is 1.5 that of the h. p. introduction of the triple-compound engine has admitted of ships being pelled at higher rates of speed than formerly obtained without exceeding consumption of fuel of similar ships fitted with ordinary compound ines: in such cases the higher power to obtain the speed has been develd by decreasing the rate of expansion, the low-pressure cylinder being y 6 times the capacity of the high-pressure, with a working pressure of lbs. absolute. It is now a very general practice to make the diameter of low pressure cylinder equal to the sum of the diameters of the h. p. and cylinders: hence.

Diameter of int, cylinder = 1.5 diameter of h. p. cylinder; Diameter of l. p. cylinder = 2.5 diameter of h. p. cylinder.

this case the ratio of 1, p. to h. p. is 8.25; the ratio of int. to h. p. is 2.25; ratio of 1, p. to int. is 2.78. tatios of Cylinders for Different Classes of Engines. c. Inst. M. E., Feb. 1837, p. 36.)—As to the best ratios for the cylinders triple engine there seems to be great différence of opinion. Consideralatitude, however, is due to the requirements of the case, inasmuch as ould not be expected that the same ratio would be suitable for an econical land engine, where the space occupied and the weight were of or importance, as in a war-ship, where the conditions were reversed. In land engine, for example, a theoretical terminal pressure of about 7 above absolute vacuum would probably be almed at, which would give tio of capacity of high pressure to low pressure of 1 to 8½ or 1 to rhilst in a war ship a terminal pressure would be required of 12 to 18 lbs. ch would need a ratio of capacity of 1 to 5; yet in both these instances cylinders were correctly proportioned and suitable to the requirements he case. It is obviously unwise, therefore, to introduce any hard-and-and-

ypes of Three-stage Expansion Engines.—1. Three cranks 20 deg. 2. Two cranks with let and the contract of the 30 deg. 2. Two cranks with 1st and 2d cylinders tandem. 8. Two ks with 1st and 2d cylinders tandem. The most common type is the , with cylinders arranged in the sequence high, intermediate, low.

Sequence of Cranks.—Mr. Wyllie (Proc. Inst. M. E., 1887) favors the sequence high, low, intermediate, while Mr. Mudd favors high, intermediate, low. The former sequence, high, low, intermediate, gave an approximately horizontal exhaust-line, and thus minimizes the range of temperature and the initial load; the latter sequence, high, intermediate, low, increased the range and also the load.

Mr. Morrison, in discussing the question of sequence of cranks, presented a diagram showing that with the cranks arranged in the sequence high,

low, intermediate, the mean compression into the receiver was 1916 per cent of the stroke; with the sequence high, intermediate, low, it was 57 per cent. In the former case the compression was just what was required to keep the receiver-pressure practically uniform; in the latter case the compression caused a variation in the receiver-pressure to the extent sometimes of

Yelocity of Steam through Passages in Compound Engines. (Proc. Inst. M. E., Feb. 1887.)—In the SS. Para, taking the area of the cylinder multiplied by the jiston-speed in feet per second and dividing by the area of the cylinder by the piston-speed in feet per second the high-pressure cylinder port would be about 100 feet per second; the xhaust would be about 90. In the intermediate cylinder the initial steam had a velocity of about 180, and the exhaust of 120. In the low-pressure cylinder the initial steam entered through the port with a velocity of 250, and in the exhaust-port the velocity was about 140 feet per second.

QUADRUPLE-EXPANSION ENGINES.

H. H. Suplee (Trans. A. S. M. E., x. 583) states that a study of 14 different quadruple expansion engines, nearly all intended to be operated at a pressure of 180 lbs. per sq. in., gave average cylinder ratios of 1 to 2, to 3.78, to 7.70, or nearly in the proportions 1, 2, 4, 8.

If we take the ratio of areas of any two adjoining cylinders as the fourth root of the number of expansions, the ratio of the 1st to the 4th will be the cbe of the fourth root. On this basis the ratios of areas for different pressures and rates of expansion will be as follows:

Gauge- pressures.	Absolute Pressures.	Terminal Pressures.	Ratio of Expansion.	Ratios of Areas of Cylinders.
160	175	\ \begin{pmatrix} 12 \\ 10 \\ 8 \end{pmatrix}	14.6 17.5 21.9	1:1.95:8.81:7.48 1:2.05:4.18:8.55 1:2.16:4.68:10.12
180	195	112 10 8	16.2 19.5 24.4	1:2.01:4.02:8.07 1:2.10:4.42:9.28 1:2.22:4.94:10.98
200	215	12 10 8	17.9 21.5 26.9	1:2.06:4.28:8.70 1:2.15:4.64:9.98 1:2.28:5.19:11.81
220	235	· } 12 10 8	19.6 23.5 29.4	1:2.10:4.43: 9.31 1:2.20:4.85:10.67 1:2.83:5.42:12.69

Seaton says: When the pressure of steam employed exceeds 190 lbs. absolute, four cylinders should be employed, with the steam expanding through each successively; and the ratio of 1, p. to h, p. should be at least 7.5, and if economy of fuel is of prime consideration it should be 8; then the ratio of first intermediate to h, p. should be 1.8, that of second intermediate to first int. 2, and that of 1, p. to second int. 2.2.

In a paper read before the North East Coast Institution of Engineers and Shipbuilders, 1890, William Russell Cummins advocates the use of a fourcylinder engine with four cranks as being more suitable for high speeds than the three-cylinder three-crank engine. The cylinder ratios, he claims, should be designed so as to obtain equal initial loads in each cylinder. The ratios determined for the triple engine are 1, 2.04, 6.54, and for the quadruple, 1, 2.08, 4.46, 10.47. He advocates long stroke, high piston-speed, 100 revolutions per minute, and 250 lbs. boiler-pressure, unjacketed cylinders, and separate steam and exhaust valves.

Diameters of Cylinders of Recent Triple-expansion Engines, Chiefly Marine.

Compiled from several sources, 1890-1893.

iam, in inches: H = high pressure, I = intermediate, L = low pressure.

!	I	L	H	I	L	H	I	L	Н	I	L
34	5 7.5	8 13 12	16 16¼	25.6 23%	41 38.5	22 23	86	{ 40 40 61 60	36 38	58 61.5	94 100
.5	10.5 9 11.8	16.5 12.5 18.9	16.5 17 17	24.5 27 26.5	\ 31 \ 31 44	23.5 24 25	38 38 37 40	60 56 64	36 38 28 28 39 40 40	56 61 59	86 97 88
.5	12 11.5 14.5	19 16 22.5	17	28 27	42 45 40 48	- ୭୫	42 42.5 44	69 70	40 40 41	67 66 66	106 100 101
.8	15.7 16 16	25.6 25 24	18 18 18 18.7 1834	29 805 29.5 23.6	40 48 51 43.3 85.4 47.8	2936 29.5 30	44 48 48	72 70 70 70 70 70 83 83 84 66	4186 42 43 48	67 59 66	10684 92 92
.5	18 18 18 17.5	25 30	19.7 20 20	29.6 30	47.8 45 { 86 { 86 52	828	46 51 54	70 82 82	48% 45	68 67 71	110 10614 113 § 85.7
.5	19.2 22	30.7 33.5	20 ·	83	48	83 33.9 84	58 55.1 54	88 84.6 85	32.5 } 32.5 }	68 75	85.7
.5	22.4 24 24 24.5	36 39 39 38	21 21.7 21.9 22	32 86 33.5 34 84	51 49.2 57 51	34.5 34.5	50 51 57	85 90 85 92	87 } 87 }	79	81.5 98 98

here the figures are bracketed there are two cylinders of a kind. Two = one 39.6°, two 31" = one 43.8°, two 32.5° = one 46.0°, two 36" = one ".two 37" = one 52.8°, two 40" = one 56.6°, two 81.5° = one 115°, two = one 121°, two 98" = one 140". The average ratio of diameters of nders of all the engines in the above table is nearly 1 to 1.60 to 2.56 and ratio of areas nearly 1 to 2.56 to 6.55.

The Progress in Steam-engines between 1876 and 1893 is shown

he Progress in Steam-engines between 1876 and 1893 is shown in following comparison of the Corliss engine at the Centennial Exhibitin 1876 and the Allis-Corliss quadruple-expansion engine at the Chicago libition.

	18 98 .	1876.
jine	Quadruple-	Simple
nders, number	4	2
" diameter		40 in.
stroke	72 in.	120 in.
-wheel, diameter	° 30 ft.	30 ft.
" width of face	76 in.	24 in.
" weight	136,000 lbs.	125,440 lbs.
olutions per minute	60	36
acity, economical	2000 H.P.	1400 H.P.
" maximum	8000 H.P.	2500 H.P.
al weight	650,000 lbs.	1,860,588 lbs.

ne crank-shaft body or wheel-seat of the Allis engine has a diameter of nches, journals 19 inches, and crank bearings 18 inches, with a total th of 18 feet. The crank-disks are of cast iron end are 8 feet in diamThe grank-pins are 9 inches in diameter by 9 inches long.

The grans-pins are y menes in mainter by menes long.

Double-tandem Triple-expansion Engine, built by Watts, ipbell & Co., Newark, N. J., is described in Am. Mach., April 23, 1894. two three-cylinder tandem engines coupled to one shaft, cranks at 90°, iders 21, 32 and 48 by 60 in. stroke, 65 revolutions per minute, rated H.P.; fly-wheel 28 feet diameter, 12 ft. face, weight 174,000 lbs.; main shaft idiameter at the swell; main journals 19 × 38 in.; crank-pins 94 × 10 distance between centre lines of two engines 24 ft. 736 in.; Corlisses, with separate eccentrics for the exhaust-valves of the 1p. cylinder

Principal Engines in the Power-Plant at the World's Columbian Exposition, 1893.

Name of Engine and where Built.	Type of Engine.	Hortzontal or Vertical.	Cylinders, ins. Diameters and Stroke.	I.H.P. Maxi- mum Econ- omy.	I.H.P. Maxi- mum Load.	Driv. Pulley. Diameter in. Face, in.	Revolutions per Minute.	Size of Steam- pipe.	Size of Ex- haust-pipe.	Weight of En- gine, lbs.
E. P. Allis Co., Milwaukee. Fraser & Chalmers, Chicago. Methorsh-Serpinorr, Automr. N. Y. Bankeye Engithe Co., Salem. O. Awa. Indianapolis Ind. Westinghouse. Pittsburg Pa.	Quad. exp. condensing. eyl, trip, exp. cond. Double tand. comp. cond. ecyl, trip. exp. cond. ecyl, trip. exp. cond. Comp. condensing.	H; ; ; ; Þ,	24, 40, 60, 70 x 72 29, 34, 2-34 x 60, 38, 2-35 x 60 18, 32 x 36 double 20, 30, 2-30 x 48 11, 38 x 39	000000000000000000000000000000000000000	8,000 1,250 1,500 1,300	300 x 76 336 x 68 195 x 78 240 x 75 135 x 14	64 1-2 118 85 150 200	22.2850	29.45.84 20.45.84	650,000 950,000 250,000 120,000 114,000 195,000*
Russell Massillon, O. Allas, Indianapols, Ind. Esses, F., Wayne, Ind. Lane & Bodley Cincinnati O.	Double Funder Cross	: H: : :	18,25,25,25,25,25,25,25,25,25,25,25,25,25,	82238	887 887 850 850	2824282 2824282 282823	555 55 55 55 55 55 55 55 55 55 55 55 55	00 to 20 10	22,025	83,298 57,000 61,000
Wetertown, Wetertown, N. Y. Buckleye, Salem, Oth., J. Ball & Wood, Elinabelh, N. J. N. Y. Safety Steam-Power Co.	Tandem comp. cond. Double tand. comp. cond. Gross compound. cond. Gross compound.	:::::	60.0.4.4.5 86.88.8.5 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	838 8 3	8 8 8 8 8 8 8	2150 2150 2150 2150 2150 2150 2150 2150	88288	4 1-8 64 1-8	55 86	21,200 33,000
Schichau, Germany Stearns ang. Co., Erie, Pa. Phoenix Iron Works Co., Meadville, Pa.		>표:	23, 37, 57 x 27 19, 31 x 94 16, 24, 2-26 x 18	5.00 g	:	102 x 31	55 8	- 9	27	75,000
		:::>	13, 24 x 18 13, 23 x 16 19, 26 x 48	8888		108 x 26 72 x 16 1-2 193	888	2001-0	≎∞ಟನೆ	24,000 85,000
Guiden English Co., Bris. Providence, R. I. Ball English Co., Erie. Pa. McEwen, Ridgway, Pa.		H :::	18 x 21 18, 36 x 18 14, 23 x 30	38	23	282 H H S S		·	2222	65,000 24,000
Stour City Stour City, 18. Gold St. Min. Iron Wits., San Fran'co, Cal. Bates Machine Co., Johlet, Ill. Harrishner, Harrishner, Pa.	Simple Simple Tandem compound	:::	28 x 48 18, 22 x 30 20 x 48 17, 28 x 18	252	1235	198 x 26 198 x 25 2 x 25 2 x 25	382	0400		8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
Providence Steam-Engine Works, R. I. Erie Otty Iron Works, Erie, Pa	Simple.	:::	19, 20 x 43 18 x 22	38	88	144 x 26 84 x 24 1-2			00 t-	18,000
Willams & Robinson, England Schichau, Germany	Comp. cond., 9-throw		9-14, 20 x 8 12, 19, 20 1-8 x 14	3 3	360	05 x 82	••••	4	20	
	Bull .	ine an	* Engine and dynamo.							

ECONOMIC PERFORMANCE OF STEAM-ENGINES. |conomy of Expansive Working under Various Conditions, Single Cylinder.

(Abridged from Clark on the Steam Engine.)

l. SINGLE CYLINDERS WITH SUPERHEATED STEAM, NONCONDENSING.—Inle cylinder locomotive, cylinders and steam-pipes enveloped by the hot ses in the smoke-box. Net boiler pressure 100 lbs.; net maximum presse in cylinders 80 lbs. per sq. in.

1. SINGLE CYLINDERS WITH SUPERHEATED STEAM, CONDENSING.—The best units obtained by Hirn, with a cylinder 23% × 67 in. and steam superated 150° F., expansion ratio 3% to 41%, total maximum pressure in cyling 63 to 69 lbs. were 15.63 and 15.69 lbs. of water per I.H.P. per hour.

. SINGLE CYLINDERS, NOT STEAM-JACKETED, CONDENSING.—Best results.

Engine.	Cylinder, Diam. and Stroke.	Cut-off.	Actual Expan- sion Ratio.	Total Maxi- mum Pressure in Cylin- der per sq. in.	Water as Steam per I.H.P. per hour.
liss and Wheelock n, No. 6 ir, M he tter las latin	ins. 18 × 48 2334 × 67 82 × 66 25 × 24 26 × 36 36 × 30 30.1 × 30	per cent. 12.5 16.8 24.6 15.5 18.3 18.3 15.0	ratio. 6.95 5.84 8.84 5.32 4.46 5.07 4.94	lbs. 104.4 61.5 54.5 87.7 80.4 46.9 81.7	lbs. 19.58 19.93 26.46 26.25 23.86 26.69 21.89

SAME ENGINES, AVERAGE RESULTS.

Long Stroke.	Inches.	Cut-off, Per cent.	Lbs.	Lbs.
liss and Wheelock n Short Stroke.	18 × 48 23¾ × 67	12.5 16.8	104.4 61.5	19.58 19.93
:he	25 × 24 26 × 36	15.5 § 18.8 to 33.8 }	87.7 79.0	26.25 24.05
las, Nos. 27, 28, 29	36 × 30	} average 25 {	46.8	26.86
latin, Nos, 24, 25, 22, }	30.1 × 30	(10 0 to 10 k)	78.2	23.50

'eed-water Consumption of Different Types of Engines, he following tables are taken from the circular of the Tabor Indicator heroft Mfg. Co., 1889). In the first of the two columns under Feed-water uired, in the tables for simple engines, the figures are obtained by putation from nearly perfect indicator diagrams, with allowance for cyler condensation according to the table on page 752, but without allowe for leakage, with back-pressure in the non-condensing table taken at 16 above zero, and in the condensing table at 3 lbs. above zero. The comssion curve is supposed to be hyperbolic, and commences at 0.91 of the irn-stroke, with a clearance of 3% of the piston-displacement.

able No. 2 gives the feed-water consumption for jacketed compound-cop-

densing engines of the best class. The water condensed in the jackets is included in the quantities given. The ratio of areas of the two cylinders are as 1 to 4 for 120 lbs. pressure; the clearance of each cylinder is 35; and the cut-off in the two cylinders occurs at the same point of stroke. The initial pressure in the l. p. cylinder is 1 lb. per sq. in. below the back-pressure of the h. p. cylinder. The average back pressure of the whole stroke in the l. p. cylinder is 4.5 lbs. for 10% cut-off; 4.75 lbs. for 20% cut-off; and 5 lbs. for 30% cut-off. The steam accounted for by the indicator at cut-off in the h. p. cylinder (allowing a small amount for leakage) is .74 at 10% cut-off, .78 at 20%, and .82 at 30% cut-off. The loss by condensation between the cylinders is such that the steam accounted for at cut-off in the l. p. cylinder, expressed in proportion of that shown at release in the h. p. cylinder, is .85 at 10% cut-off, .87 at 20% cut-off, and .89 at 30% cut-off.

The data upon which table No. 3 is calculated are not given, but the feedwater consumption is somewhat lower than has yet been reached (1894), the lowest steam consumption of a triple-exp. engine yet recorded being 11.7 lbs.

TABLE No. 1.

FEED-WATER CONSUMPTION, SIMPLE ENGINES.

NON-CONDENSING ENGINES.

CONDENSING ENGINES.

NON-CONDENSING ENGINES. CONDENSING ENGINES.

	Atmos.	Pressure,	quired p	ater Re- er I.H.P. Hour.		Atmos	Pressure,	quired 1	ater Re- per I.H.P. Hour.
Per Cent Cut-off.	Initial Pressure above Atmosphere, lbs.	Mean Effective Pribs.	Corresponding to Diagrams with no Leakage, lbs.	Corresponding to Actual Results Attained in Practice, assuming Slight Leakage.	Per Cent Cut-off.	Initial Pressure above Atmosphere, lbs.	Mean Effective Prilbs.	Corresponding to Diagrams with no Leakage, Ibs.	Corresponding to Actual Results Attained in Practice, assuming Slight Leakage.
10 {	60 70 80 90 100	8.70 12.89 16.07 19.76 23.45	37.26 30.99 27.61 25.43 23.90	40.95 83.68 29.88 27.43 25.73	5	60 70 80 90 100	14.42 16.96 19.50 22.04 24.58	18.22 17.96 17.76 17.57 17.41	20.00 19.69 19.47 19.27 19.07
20 {	60 70 80 90 100	21.12 26.57 82.02 87.47 42.92	27.55 25.44 21.04 23.00 22.25	29.43 27.04 25.68 24.57 23.77	10	60 70 80 90 100	22.34 26.08 29.72 33.41 37.10	17.68 17.47 17.80 17.15 17.02	19.34 19.09 18.89 18.70 18.56
30 {	60 70 30 90 100	30.47 37.21 48.97 50.73 57.49	27.24 25.76 24.71 23.91 23.27	29.10 27.43 26.29 25.38 24.68	15	60 70 80 90 100	29.00 33.65 38.28 42.92 47.56	17.98 17.75 17.60 17.45 17.82	19.51 19.27 19.09 18.91 18.74
40	60 70 80 90 100	87.75 45.50 53.25 61.01 68.76	27.99 26.66 25.76 25.03 24.47	29.63 28.18 27.17 26.35 25.73	20 {	60 70 80 90 100	34.78 40.18 45.63 51.08 56.53	18.58 18.40 18.27 18.14 18.02	20.09 19.85 19.69 19.51 19.36
50.	60 70 80 90 100	43.42 51.94 60.44 68.96 77.48	28.94 27.79 26.99 26.33 25.78	30.66 29.31 28.38 27.62 26.99	30	60 70 80 90 100	44.06 50.81 57.57 64.32 71.08	20.19 20.04 19.91 19.78 19.67	21.64 21.41 21.25 21.06 20.93
-					40	60 70 80 90 100	51.35 59.10 66.85 74.60 82.36	21.63 21.49 21.36 21.24 21.18	22.98 22.74 22.56 23.41 22.24

TABLE No. 2. FEED-WATER CONSUMPTION FOR COMPOUND CONDENSING ENGINES.

tut-off,	Initial Pres	sure above	Mean Effect	Feed-water		
	Atmos	phere.	Atmos	Required		
or cent.	H.P. Cyl.,	L.P. Cyl	H.P. Cyl.,	L.P. Cyl.,	per I.H.P. per	
	lbs.	lbs.	lbs.	lbs.	Hour, Lbs.	
10 {	80	4.0	11.67	2.65	16.92	
	100	7.8	15.33	3.87	15.00	
	120	11.0	18.54	5.23	18.86	
20 {	80	4.8	26.73	5.48	14.60	
	100	8.1	33.13	7.56	18.67	
	120	12.1	89.29	9.74	18.09	
80 {	80	4.6	87.61	7.48	14.99	
	100	8.5	46.41	10.10	14.21	
	120	11.7	56.00	12.26	18.87	

TABLE No. 3. RED-WATER CONSUMPTION FOR TRIPLE-EXPANSION CONDENSING ENGINES.

t-off,		Pressure mosphe		Mean Ef	Feed-water Required		
ent.	H.P. Cyl., lbs.	I. Cyl., lbs.	L.P. Cyl., lbs.	H.P. Cyl., lbs.	I. Cyl., lbs.	L.P. Cyl., lbs.	per l.H.P. per Hour, lbs.
, {	120	87.8	1.3	38.5	17.1	6.5	12.05
	140	43.8	2.8	46.5	18.6	7.1	11.4
	160	49.8	3.8	55.0	20.0	8.0	10.75
, {	120	38.8	2.8	51.5	22.8	8.6	11.65
	140	45.8	3.9	59.5	23.7	9.1	11.4
	160	51.3	5.3	70.0	25.5	10.0	10.85
, {	120	89.8	3.7	60.5	26.7	10.1	12.9
	140	46.8	4.8	70.5	28.0	10.8	11.6
	160	52.8	6.3	82.5	80.0	11.8	11.15

Iost Economical Point of Cut-off in Steam-engines.

paper by Wolff and Denton, Trans. A. S. M. E., vol. ii. p. 147-281; also, to of Expansion at Maximum Efficiency, R. H. Thurston, vol. ii. p. 128.) he problem of the best ratio of expansion is not one of economy of conption of fuel and economy of cost of boiler alone. The question of rest on cost of engine, depreciation of value of engine, repairs of engine, enters as well; for as we increase the rate of expansion, and thus, in certain limits fixed by the back-pressure and condensation of steam, rease the amount of fuel required and cost of boiler per unit of work, nave to increase the dimensions of the cylinder and the size of the en, to attain the required power. We thus increase the cost of the engine, , to attain the required power. We thus increase the cost of the engine, as we increase the rate of expansion, while at the same time we dese the fuel consumption, the cost of boiler, etc. So that there is in y engine some point of cut-off, determinable by calculation and graphiconstruction, which will secure the greatest efficiency for a given expense of money, taking into consideration the cost of fuel, wages of engineer fremen, interest on cost, depreciation of value, repairs to and insurance oiler and engine, and oil, waste, etc., used for engine. In case of freight-ying vessels, the value of the room occupied by fuel should be considin estimating the cost of fuel.

zes and Calculated Performances of Vertical Highed Engines.—The following tables are taken from a circular of the d Engineering Co., New York, describing the engines made by the Lake Engineering Works, Buffalo, N. Y. The engines are fair representatives et ype now coming largely into use for driving dynamos directly withbelts. The tables were calculated by E. F. Williams, designer of the nes. They are here somewhat abridged to save space:

Simple Engines-Non-condensing.

of Cyl-	e, inches.	per Min-	H.P. when Cutting off at 1/5 stroke.			Cu	H.P. when Cutting off at ¼ stroke.			H.P. when Cutting off at 1/2 stroke.			Dimensions of Wheels.		Exhaust-pipe.
Diam. c	Stroke,	Revs. ute.	70 lbs.	80 lbs.	90 lbs.	70 lbs.	80 lbs.	90 lbs.	70 lbs.	80 lbs.	90 lbs.	Ft.	In.	Steam-pipe,	Exha
71/2 81/3 10/2 12 13/2 16 18 22 241/2 27	10 12 14 16 18 20 24 28 32 84	370 818 277 246 222 181 158 138 120 112	20 27 41 53 66 95 119 179 221 269	80 115 144 216 267	39 60 77 96 138 178 261 322	34 52 67 84 120 151 227 281	41 62 81 100 144 181 272 336	71 93 116	41 63 82	48 74 96 120 172 215 324 400	85 111 138 198 248 373 460	4 4 29 446 5 26 5'9' 636 31 6'8' 9 4 736 11 4 10 19 5 11'8' 28 6 13'4'' 34 8			4 316 4 4 416 5
Mean	eff. pr	ess.lb.	24	29	35	30.5	36,5	42	37	43.5	50	N	o en p		The
Ratio	Ratio of expans'n.			5			4			3		nomi	nal.	po	wer
Terminal pressure (about)lbs. Cyl.condensat'n, & Steam per I.H.P. per hourlbs.		17.9 26	26	26	22.4 24 31.2	25 24 29.0	27.6 24 27.9	21	33.3 21 31.4	21	nominal - pow rating of the gines is at 80 li gauge pressu steam cut-off 1/4 stroke.			lbs. ure,	

Compound Engines -- Non-condensing -- High - pressure Cylinder and Receiver Jacketed.

	Diam		inches.	s per	off	whe at 1/2 i.p. (Str	oke	off	at 1	neut Str Cylin	oke	off	H.P. when cutting off at 1/4 Stroke in h.p. Cylinder.			
	Cylinder, inches.		Stroke, inc	Revolutions Minute.	Cyl. Ratio, 31/8:1.		Ra	Cyl. Ratio, 41/2 : 1.		Cyl. Ratio, 3½: 1.		yl. tio,	Cyl. Ratio, 31/6:1.		Cyl. Ratio, 41/4: 1.		
H.P.	H.P.	L.P.	Str	Rev	80 lbs.	90 lbs.	130 lbs.	150 lbs.	80 lbs.	90 lbs.	130 lbs.		80 lbs.	90 lbs.	130 lbs.	150 lbs.	
12 1316 16 18 20	9 1014 12 1314 1514 1814 2014 2214 2814	161/6 19 221/6 25 281/6 331/6 38 43	10 12 14 16 18 20 24 28 82 84 42 48	370 318 277 246 222 185 158 120 112 93 80	7 9 14 18 26 32 43 57 74 94 188 180	15 19 28 37 53 65 88 118 152 194 285 374	19 24 36 47 68 84 112 151 194 249 365 477	32 40 60 78 112 139 186 249 821 412 603 789	23 29 43 57 81 100 135 180 282 297 436 570		67 87 125 154 206 277 357	59 87 114 164 202 271 363 468 601 880	192 258 846 446 572 888	70 104 136 195 241 323 433 558 715 1048	81 121 158 226 279 374 502 647 829 1215	79 101 159 196 281 846 464 623 803 1030 1508 1973	
Mea	n eff	ec. p	ress	lbs	8.8	6.8	8.7	14.4	10,4	14.0	16	21	50	25	29	36	
Ratio of expansion				13	16	18	34	10	14	13	34	6	34	9	14		
Cyl. condensation, % Ter. press. (about).lbs.					14 7.3	14 7.7	16 7.9	16	12 9.2	12 10.4	18 10.5	13 12	10 14	10 15.5	11 14.6	11 17.8	
be	below atmosphere, ast. per I.H.P. p. hr.lbs.					15 42	17 47	8 29	5 33.3	0 27.7	28.7	0 25.4	0 30	26.2	0 21	20	

The original table contains figures of horse-power, etc., for 110 and 120 lbs., cylinder ratio of 4 to 1; and 140 lbs., ratio 4½ to 1.

CALCULATED PERFORMANCES OF STEAM-ENGINES. 779

Compound-engines-Condensing-Steam-jacketed.

	Diam		inches.	ber .	off	whe at 1/2 .p. C	Str	oke	off	at 1	n cut i Str ylin	oke	H.P. when cutti off at 1/4 Strok in h.p. Cylinde			
Jylinder, Inches.			Stroke, inc	Revolutions Minute.	Cyl. Ratio, 3½: 1.		Cyl. Ratio, 4:1.		Cyl. Ratio, 31/6:1.		Cyl. Ratio, 4:1.		Cyl. Ratio, 3½: 1.		Re	yl. tio,
	H.P.	L.P.	Str	Rev	80 lbs.	110 lbs.	115 lbs.	125 lbs.	80 1bs.	110 lbs.		125 lbs.	80 lbs.	110 lbs.		125 lbs.
161418 16	1836 2036 2236 2836	1816 1616 19 2216 25 2816 3816 43	10 12 14 16 18 20 24 28 32 34 42 48	370 318 277 246 222 185 158 120 112 93 80	44 56 83 109 156 192 258 346 446 572 838 1096	59 76 112 147 210 260 348 467 602 772 1131 1480	100 131 187 231 310 415 585 686 1006	152 218 269 361 484 624 801 1174	195 241 843 433 558 715 1048	90 133 174 250 308 413 554 714 915 1341	87 129 169 242 298 400 536 691 887 1299	327 439 588 758 972 1425	250 308 413 554 714 915 1341	123 183 239 343 423 568 761 981 1258 1844	179 234 885 414 555 744 959 1280 1801	134 200 261 374 462 619 830 1070 1373
		200		lbs.	-	27	24	28	25	32	31	34	32	44	43	48
yl. condensation, ≰ per I.H.P. p. hr.lbs.			18	18 16.6	20	20 15.2	15	15 16.4	18	18 15.8	12	12 17.0	14	14 16.0		

The original table contains figures for 95 lbs., cylinder ratio $3\frac{1}{2}$ to 1; and 20 lbs., ratio 4 to 1.

Triple-expansion Engines, Non-condensing.—Receiver only Jacketed.

Diameter Cylinders, inches.					when (off at cent of in Firs	-power Cutting 42 per Stroke t Cylin- er.	when (off at cent of in First	power Cutting 50 per Stroke t Cylin- er.	Horse-power when Cutting off at 67 per cent of Stroke in First Cylin- der.		
. P.	L.P.	L. P.	Stroke,	Rev	180 lbs.	200 lbs.	180 lbs.	200 lbs.	180 lbs.	200 lbs.	
484 514 614 714 0	716 812 1012 12	12	10		55	64	70	84	95	108	
516	81/6	1816	12	818		81	90	106	120	137	
614	101/6	161/6	14	277	104	121	188	158	179	204	
71/2	12	19	16	246	186	158	174	207	284	267	
9	1416	221/6	18	222	195	226	250	296	835	882	
0	16	25	20	185	241	279	808	866	414	471	
11/6	18	2814	24	158	823	874	418	490	555	632	
3 5 7	22	8312	28	188	433	502	554	657	744	848	
5	241/6	88	32	120	558	647	714	847	959	1093	
	27	48	34	112	715	829	915	1089	1230	1401	
0	33	52	42	93	1048	1215	1341	1592	1801	2053	
31/6	88	60	48	80	1370	1589	1754	2082	2856	2685	
ean	effecti	ve p	38.,	lbs.	25	29	82	88	48	49	
o. of	expar	sions.	٠		1	б	1	8	10		
er ce	nt cyl.	conde	ens		1	4	1:	2	10		
eam	p. I.H	.P. n.)	ır	lhs.	20.76	19.36	19.25	17.00	17.89	17.20	
bs. c	oal at 8	lb. ev	AD.	lbs.	2.59	2.89	2.40	2.12	2.23	2.15	

Triple-expansion Engines-Condensing-Steam-Jacketed.

Cy	ame linde nche	rs,	, inches.	ntions per	wh ting Sta Firs	se-pe en C off a roke st Cy der.	ut- at 14 in	wh ting Str Firs	en C	ut- at 1/8 in	wh ting St Firs	en C	in lin-	ting St	ower out- at 34 in vlin-	
H.P.	I.P.	L.P.	Stroke,	Revolt	120 lbs.	140 lbs.		120 lbs.	140 lbs.		120 lbs.	140 lbs.	160 lbs.	120 lbs.		
434 516 616	1016	12 1316 1616	10 12 14	370 318 277	35 45 67	53 79	48 62 92	44 56 83	58 67 100	59 76 112	57 78 108	79 92 187	159	81 104 154		110 140 208
10	1416	19 2216 25	16 18 20	246 222 185	125 154	103 148 183	212	109 156 192	181 187 231	211 260	141 203 250	180 257 317	299 368	201 289 356	428	272 390 481
111/6 18 15	18 22 2416	2816 3316 38	24 28 32	158 138 120	206 277 357	245 329 424	284 381 491	258 346 446	310 415 535	348 467 602	335 450 580	426 571 736	663	477 640 825		645 865 1115
17 20 2316	27 33	48 52 60	34 42 48	112 93 80	458 670 877	543 796 1041	629 922 1206	572 838 1096	686 1006 1316	772 1131 1480	744 1089 1424	1383	1095 1605 2099	1551	1258 1844 2411	1430 2096 2740
Mea	n eff	ec. p	ress	,lbs.	16	19	22	20	24	27	26	33	38.3	37	44	50
	lo. of expansions					26.8	_	_	20.1			13.4		8.9		
St. p	.I.H	.P. p	hr.	lens. , lbs. , lbs.	14.7	19 18.9 1.73	19 13.8 1.66	16 14.3 1.78	16 13.98 1.74	16 13.2 1.65	12 14.3 1.78	12 13.6 1.70	12 13.0 1.62	8 15.7 1.96	8 14.9 1.86	14.2 1.77

Type of Engine to be used where Exhaust-steam is needed for Heating.—In many factories more or less of the steam exhausted from the engines is utilized for boiling, drying, heating, etc. Where all the exhaust-steam is so used the question of economical use of steam in the engine itself is eliminated, and the high-pressure simple engine is entirely suitable. Where only part of the exhaust-steam is used, and the quantity so used varies at different times, the question of adopting a simple, a condensing, or a compound engine becomes more complex. This problem is treated by C. T. Main in Trans. A. S. M. E., vol. x. p. 48. He shows that the ratios of the volumes of the cylinders in compound engines should vary according to the amount of exhaust-steam that can be used for heating. A case is given in which three different pressures of steam are required or could be used, as in a worsted dye-house: the high or boiler pressure for the engine, an intermediate pressure for crabbing, and low-pressure for boiling, drying, etc. If it did not make too much complication of parts in the engine, the boiler-pressure might be used in the high-pressure cylinder, exhausting into a receiver from which steam could be taken for running small engines and crabbing, the steam remaining in the receiver passing into the intermediate cylinder and expanded there to from 5 to 10 lbs. above the atmosphere and exhausted into a second receiver. From this receiver is drawn the low-pressure steam needed for drying, boiling, warming mills, etc., the steam remaining in receiver passing into the condensing cylinder.

Comparison of the Economy of Compound and Single-cylinder Corliss Condensing Engines, each expanding about Sixteen Times. (D. S. Jacobus, Trans. A. S. M. E., xii. 948.)

The engines used in obtaining comparative results are located at Stations I. and II. of the Pawtucket Water Co.

1. and 11. Of the Pawtherset Water CO.

The tests show that the compound engine is about 30½ more economical than the single-cylinder engine. The dimensions of the two engines are as follows: Single 20" × 48"; compound 15" and 80½" × 30". The steam used per horse-power per hour was: single 20.35 lbs., compound 13.78 lbs. Both of the engines are steam-jacketed, practically on the barrels only, with steam at full boiler-pressure, viz. single 106.3 lbs., compound 127.5 lbs.

The steam-pressure in the case of the compound engine is 127 lbs., or 21 s. higher than for the single engine. If the steam-pressure be raised this count in the case of the single engine, and the indicator-cards be increased cordingly, the consumption for the single-cylinder engine would be 19.97

s. per hour per horse-power.

her nour per note-power.

Ewo-cylinder vs. Three-cylinder Compound Engine.—
Wheelock triple-expansion engine, built for the Merrick Thread Co., blyoke, Mass., is constructed so that the intermediate cylinder may be cut to fit occurred the circuit and the high-pressure and low-pressure cylinders run as a o-cylin'er compound, using the same conditions of initial steam-pressure obeying of compound, using the same controls of initial season pressure of the cylinders are 12, 16, and 2441 inches, the oke of the first two being 36 in, and that of the low-pressure cylinder 48. The results of a test reported by S. M. Green and G. I. Rockwood, Trans. S. M. E., vol. xiii. 647, are as follows: In lbs. of dry steam used per I.H.P. r hour, 12 and 2413 in cylinders only used, two tests 13.06 and 12.76 lbs., erage 12.91. All three cylinders used, two tests 12.67 and 12.90 lbs., average 79. The difference is only 1%, and would indicate that more than two cylinrs are unnecessary in a compound engine, but it is pointed out by Prof. cobus, that the conditions of the test were especially favorable for the o-cylinder engine, and not relatively so favorable for the three cylinders.
e steam-pressure was 142 lbs. and the number of expansions about 25.
e also discussion on the Rockwood type of engine, Trans. A. S. M. E., vol.

Effect of Water contained in Steam on the Efficiency of e Steam-engine. (From a lecture by Walter C. Kerr, before the anklin Iustitute, 1891.)—Standard writers make little mention of the effect entrained moisture on the expansive properties of steam, but by common usent rather than any demonstration they seem to agree that moisture

oduces an ill effect simply to the percentage amount of its presence, at is, 5% moisture will increase the water rate of an engine 5%. Experiments reported in 1893 by R. C. Carpenter and L. S. Marks, Trans. S. M. E., xv., in which water in varying quantity was introduced into the sam-pipe, causing the quality of the steam to range from 99% to 58% dry, owed that throughout the range of qualities used the consumption of dry am per indicated horse-power per hour remains practically constant, and licated that the water was an inert quantity, doing neither good nor harm. **Belative Commercial Economy of Best Modern Types of smpound and Triple-expansion Engines.** (J. E. Denton, nerican Machinist, Dec. 17, 1891.)—The following table and deductions ow the relative commercial economy of the compound and triple type for a best stationary practice in steam plants of 500 indicated horse-power, a table is based on the tests of Prof. Schröter, of Munich, of engines built Augsburg, and those of Geo. H. Barrus on the best plants of America, and detailed estimates of cost obtained from several first-class builders.

ip motion, or Corliss engines of he twin-compound-receiver conlensing type, expanding 16 times. Boiler pressure 120 lbs.

p motion, or Corliss engines of he triple-expansion four-cyliner-receiver condensing type, exanding 22 times. Boiler pressure, 50 lbs.

Lbs. water per hour per H.P., by measurement.	} 13.6	14.0
Lbs. coal per hour per H.P., assuming 8.5 lbs. actual evaporation.	1.60	1.65
Lbs. water per hour per H.P., by measurement.	12.56	12.80
Lbs. coal per hour per H.P., assuming 8.5 lbs. actual evaporation.	1.48	1.50

he figures in the first column represent the best recorded performance 11), and those in the second column the probable reliable performance. he table on the next page shows the total annual cost of operation, with il at \$4.00 per ton, the plant running 800 days in the year, for 10 hours and 24 hours per day.

reased cost of triple-expansion plant per horse-power, including oilers, chimney, heaters, foundations, piping and erection. 57.50 aking the total cost of the plants at \$33.50, \$36.50 and \$41 per horsever respectively, the figures in the table imply that the total annual savis as follows for coal at \$4 per ton:

A compound 500 horse-power plant costs \$18,250, and saves about \$1630 10 hours' service, and \$4885 for 24 hours' service, per year over a single nt costing \$16,750. That is, the compound saves its extra cost in 10-br vice in about one year, or in 24-hour service in four months.

2. A triple 500 horse-power plant costs \$20,000, and saves about \$114 per year in 10-hour service, or \$325 in 34-hour service, over a compound plant, thereby saving its extra cost in 10-hour service in about 10% years, or in 34-hour service in about 2% years.

Hours running per day	10	84
Expense for coal. Compound plant Expense for coal. Triple plant	Per H.P. \$9.90 9.00 0.90	Per H.P. \$28.50 25.92 2.60
Annual interest at 5% on \$4.50. Annual depreciation at 5% on \$4.50. Annual extra cost of oil 1 cellon new 94 hours	\$0.23 0.28	\$0.28 0.23
Annual extra cost of oil, 1 gallon per 24-hour day, at \$0.50, or 15% of extra fuel cost	0.15 0.06	0.86
	\$0.67	\$0.96
Annual saving per H.P	\$0.23	\$1.64

Highest Economy of Pumping Engines, 1900. (Eng. News. Sept. 27, 1900.)

		-	
Name of Builder	E, P. A	Nordberg Mfg. Co.	
Location	ChestnutHill, Boston.	St. Louis (No. 10),	Wildwood, Pa.
Expansions	Triple.	Triple.	Quadruple.
Cyls. diam. and stroke, in Plungers, diam., in. Revs. per min Steam pressure, lbs. per sq. in. Vacuum, lbs. per sq. in Ind. horse-power Capacity, million gals Total head, ft Duty per million B.T.U Dry steam per I.H.P. hour, lbs. B.T.U. per i.H.P. per min Thermal efficiency, per cent Friction, per cent Ratio of expansion, about.	17.5 187.4 13.8 801.6 80 140.35 157,052,500 * 10.335 196.08 * 31.63 * 6.71	34, 62, 92 × 72 994 16.43 180.9 14:04 801.6 15 292.11 158,077,384 10.676 901.96 21.003 3.16 23.4	194,994,494,574 × 42 144 86.5 199.9 18.11 712 6 504.06 162,943,624 12.26 185.96 22.51 6.12

^{*} These figures do not include the heat saved by the economiser; including this they are 163,912,800; 187.8; 22.58. The Nordberg engine had a series of feed-water heaters taking steam respectively from the exhaust, from the low-pressure cylinder, and from the third, second, and first receivers. The feed-water was thereby treated successively to 105°, 136°, 133°, 200°, and 311° F. The coal consumption of the Chestnut Hill engine was 1.062 lbs. per I.H.P. per hour, including the coal used by the fan, stoker, and economiser engines. This is the lowest figure yet recorded.

Steam Consumption of Sulzer Compound and Tripleexpansion Engines with Superheated Steam.

The figures on the next page were furnished to the author (Aug., 1902) by Sulser Bros., Winterthur, Switserland. They are the results of official tests by Prof. Schröter of Munich, Prof. Weber of Zurich, and other eminent engineers.

Notes.—A, B, C, D, tandem engines at electrical stations: A, Frankrt a/M.; B, Zurich; C. Mannheim; D, Mayence. E, F. tandem engine ith intermediate superheater: E, Metallwarenfabrik, Geislingen, Würtemerg; F, Neue Baumwoll-Spinnerei, Hof, Bavaria. G, H, engines at electrial stations, Berlin: G, Moabit station, horizontal 4-cyl.; H, Louisenstrasse, cyl. vertical.

COMPOUND ENGINE	28.

		nute.	re,	'n,	jo sər			n Consu in Poun		Effici	iency
Normal Power I.H.P.	Dimensions of Cylinders, Inches.	Revs. per Minute.	Initial Pressure, Pounds.	Temp. of Steam Deg. F.	Vacuum, Inches Mercury.	I.H.P.	Per I.H.P. Hour.	Per B.H.P. Hour.	Per K.W. Hour.	of Engine.	of Engine and Dynamo.
1 1500 to 1800	30.5 and 49.2×59.1	85	130 132 122	428	26.4 26.4 26.6	842	12.05	14.90 2 13.52 1 13.24 1	9.48	0.891	0.842
1050 to 1250	43.3×51.2	100	108	455	26.8	1167	13.10	13.77 1	9.72	0. 9 51	0.004
800 to 1000	40.4×51.2	83	134 135	357 356 356 547 533 545	28 27.6 28	750 1078 515 788	13.10 14.10 11.32 11.52	14.68 2 14.14 2 14.95 2 12.70 1 12.38 1 12.50 1	$0.35 \\ 1.30 \\ 8.69 \\ 7.90$	0.926 0.932 0.894 0.931	0.877 0.892 0.824 0.875
950 to 1150	42.3×51.2	1	$\frac{129}{132}$	358	28	1316 1071	14.50	14.82 2 15.10 2 12.33 1 16.30 2	$\frac{1.55}{7.70}$	$0.960 \\ 0.951$	$0.915 \\ 0.903$
400 to 500	17.7 and 30.5×35.4	110	135 135		26.4 26.4		10.80 10.35	Interme superh temp. at enti l.p. cy	eatir of ste rance	ıg, ∫3 am, ∫	349° F. 31° F.
1000 to 1200	26.9 and 47.2×66.9	65	127	664	27.2 27.2 27.1	788 797 788	9.91 9.68 10.70		• • • •	J s	07° F.

TRIPLE-EXPANSION ENGINES.

	Normal Power, I.H.P.	Dimensions of Cylinders, Inches.	Revolutions per Minute.	Initial Pressure, Pounds.	Temp. of Steam, Deg. F.	Vacuum, Inches.	I.H.P.	Steam Cons. per I.H.P. Hour, Pounds.
7	3000	321,471,58×59	85	188 190	606 397	28 27‡	2860 2880	8.97 11.28
7	3000	34, 49, 61×51	831	189 196	613 381	27 261	2908 3040	9.41 11.57

Relative Reconomy of Compound Non-condensing Engines under Variable Loads.—F. M. Rites, in a paper on the Steam Distribution in a Form of Single-acting Engine (Trans. A. S. M. E., xili, 587), discusses an engine designed to meet the following problem: Given an discusses an engine designed to meet the following problem: Given an extreme range of conditions as to load or steam-pressure, either or both, to fluctuate together or apart, violently or with easy gradations, to construct an engine whose economical performance should be as good as though the engine were specially designed for a momentary condition—the adjustment to be complete and automatic. In the ordinary non-condensing compound engine with light loads the high-pressure cylinder is frequently forced to supply all the power and in addition drag along with it the low-pressure piston, whose cylinder indicates negative work. Mr. Rites shows the peculiar value of a receiver of predetermined volume which acts as a clear-ance chamber for compression in the high-pressure cylinder. The Westinghouse compound single-acting engine is designed upon this principle. The following results of tests of one of these engines rated at 175 H.P. for most economical load are given: economical load are given:

WATER RATES UNDER VARYING LOADS, LBS. PER H.P. PER HOUR.

Horse-power	210	170	140	115	100	80	50
Non-condensing	22.6	21.9	22.2	22.2	22.4	24.6	28.8
Condensing		18.1	18.2	18.2	18.8	18.3	20.4

Efficiency of Non-condensing Compound Engines. (W. Lee Church, Am. Mach., Nov. 19, 1891.)—The compound engine, non-condensing, at its best performance will exhaust from the low-pressure cylinder at a pressure 2 to 6 pounds above atmosphere. Such an engine will be limited in its economy to a very short range of power, for the reason that its valve-motion will not permit of any great increase beyond its rated power, and any material decrease below its rated power at once brings the expansion curve in the low pressure cylinder below atmosphere. In other expansion curve in the low-pressure cylinder below atmosphere. In other words, decrease of load tells upon the compound engine somewhat sooner, and much more severely, than upon the non-compound engine. The loss commences the moment the expansion line crosses a line parallel to the atmospheric line, and at a distance above it representing the mean effective atmospheric line, and at a distance above it representing the mean effective pressure necessary to carry the frictional load of the engine. When expanion falls to this point the low-pressure cylinder becomes an air-pump over more or less of its stroke, the power to drive which must come from the high-pressure cylinder alone. Under the light loads common in many industries the low-pressure cylinder is thus a positive resistance for the greater portion of its stroke. A careful study of this problem revealed the functions of a fixed intermediate clearance, always in communication with the high-pressure cylinder, and having a volume bearing the same ratio to that of the high-pressure cylinder that the high-pressure cylinder bears to the low-pressure. Engines laid down on these lines have fully confirmed the judgment of the designers.

The effect of this constant clearance is to supply sufficient steam to the low-pressure cylinder under light loads to hold its expansion curve up to atmosphere, and at the same time leave a sufficient clearance volume in the high-pressure cylinder to permit of governing the engine on its compression

high-pressure cylinder to permit of governing the engine on its compression

under light loads.

Economy of Engines under Varying Loads. (From Prof. W. C. Unwin's lecture before the Society of Arts, London, 1892.)—The general result of numerous trials with large engines was that with a consumption of light pounds of coal per indicated horse-power for a condensing engine, and light pounds for a non-condensing engine, figures which correspond to about 154 pounds to 254 pounds of coal per effective horse-power. It was much more difficult to ascertain the consumption of coal in ordinary every-day work, but such facts as were known showed it was more than on trial. but such facts as were known showed it was more than on trial.

In electric-lighting stations the engines work under a very fluctuating load, and the results are far more unfavorable. An excellent Willans non-condensing engine, which on full-load trials worked with under 2 pounds concerning engine, which on full-toat disas worked with under 2 pounds per effective horse-power hour, in the ordinary daily working of the station used 7½ pounds per effective H.P. hour in 1886, which was reduced to 4.3 pounds in 1890 and 3.8 pounds in 1891. Probably in very few cases were the engines at electric-light stations working under a consumption of 4½ pounds per effective H.P. hour. In the case of small isolated motors working with a fluctuating load, still more extravagant results were obtained.

Engines in Electric Central Stations.

Year	1886.	1890.	1892.
Coal used per hour per effective H.P		5.6	4.9
" " " if " indicated "	RK		

t electric lighting stations the load factor, viz., the ratio of the average 1 to the maximum, is extremely small, and the engines worked under y unfavorable conditions, which largely accounted for the excessive fuel

sumption at these stations.

1 steam-engines the fuel consumption has generally been reckoned on indicated horse-power. At full-power trials this was satisfactory ugh, as the internal friction is then usually a small fraction of the total. experiment has, however, shown that the internal friction is nearly connt, and hence, when the engine is lightly loaded, its mechanical efficiency reatly reduced. At full load small engines have a mechanical efficiency 9.8 to 0.85, and large engines might reach at least 0.9, but if the internal tion remained constant this efficiency would be much reduced at low vers. Thus, if an engine working at 100 indicated horse power had an effiacy of 0.85, then when the indicated horse-power fell to 50 the effective se-power would be 35 horse-power and the efficiency only 0.7. Similarly, 25 horse-power the effective horse-power would be 10 and the efficiency

experiments on a Corliss engine at Creusot gave the following results: 0.125 ective power at full load 1.0 0.750.50 0.25 0.68 0.82 0.79 0.74 idensing, mechanical efficiency..... 0.480.86 0.83 0.78 0.52 n condensing, 0.67

t light loads the economy of gas and liquid fuel engines fell off even re rapidly than in steam engines. The engine friction was large and rly constant, and in some cases the combustion was also less perfect at at loads. At the Dresden Central Station the gas-engines were kept rking at nearly their full power by the use of storage-batteries. The

ults of some experiments are given below:
ke load,per Gas-engine, cu. ft. Petrole
ent of full of Gas per Brake Lbs.of Petroleum Eng., Petroleum Eng., Lbs.of Oil per Lbs. of Oil per B.H.P. per hr. 0.96 1.11 B.H.P. per hr. 0.88 Power. H.P. per hour. 100 28.8 75 0.99 59 1.44 1.20 20 1.82 40.8 2.88 4.25 8.07

iteam Consumption of Engines of Various Sizes.—W. C. win (Cassier's *Magazine*, 1894) gives a table showing results of 49 tests of win (classier's malgiant, 1984) gives a table showing results of a teste or rines of different types. In non-condensing simple engines, the steam sumption ranged from 65 lbs. per hour in a 5-horse-power engine to 22 in a 184-H.P. Harris-Corliss engine. In non-condensing compound enes, the only type tested was the Willans, which ranged from 27 lbs. in a H.P. slow-speed engine, 122 ft. per minute, with steam-pressure of 64 lbs. 19,2 lbs. in a 40-H.P. engine, 401 ft. per minute, with steam-pressure 165.

A Willans triple-expansion non-condensing engine, 39 H.P., 172 lbs. super and 400 ft. pixton speed per minute, axe a consumption of 185 lbs. A Willans triple-expansion non-condensing engine, 39 H.P., 172 lbs. ssure, and 400 ft. piston speed per minute, gave a consumption of 18.5 lbs. condensing engines, nine tests of simple engines gave results ranging only m 18.4 to 22 lbs., and, leaving out a beam pumping-engine running at slow ed (240 ft. per minute) and low steam-pressure (45 lbs.), the range is only m 18.4 to 19.8 lbs. In compound-condensing engines over 100 H.P., in 13 ts the range is from 18.9 to 20 lbs. In three triple-expansion engines the res are 11.7, 12.2, and 12.45 lbs., the lowest being a Sulzer engine of 360 P. In marine compound engines, the Fusiyama and Colchester, tested Prof. Kennedy, gave steam consumption of 21.2 and 21.7 lbs.; and the teor and Tartar triple-expansion engines gave 15.0 and 19.8 lbs. aking the most favorable results which can be regarded as not excepnal, it appears that in test trials, with constant and full load, the expensive of steam and coal is about as follows:

Per Indicated Horse-Per Effective Horsepower Hour. power Hour. Kind of Engine. Coal, Steam, Coal, Steam, lbs. lbs. lbs. lbs. a-condensing..... 1.80 16.5 2.00 18.0

1.50

13.5

15.8

ure of steam and coal is about as follows:

idensing.....

These may be regarded as minimum values, rarely surpassed by the most efficient machinery, and only reached with very good machinery in the favorable conditions of a test trial.

Small Engines and Engines with Fluctuating Loads are usually very wasteful of fuel. The following figures, illustrating their low economy, are given by Prof. Unwin, Cassier's Magazine, 1894.

COAL CONSUMPTION PER INDICATED HORSE-POWER IN SMALL ENGINES.

In Workshops	in	Birmingham,	Eng.
--------------	----	-------------	------

Probable I.H.P. at full load... Average I.H.P. during obser-12 60 60 2.96 vation. 7.37 8.2 8.6 23.64 19.08 20.08

Coal per L.H.P. per hour during observation, lbs...... 86.0 21.25 22.61 18.13 11.68 9.58

It is largely to replace such engines as the above that power will be distributed from central stations.

Steam Consumption in Small Engines.

Tests at Royal Agricultural Society's show at Plymouth, Eng. Engineering, June 27, 1890.

Rated H.P.			of ders.	Stroke,		Per Bi	3≒4		
	Simple.	h.p.	l.p.	108.	pressure.	Coal.	Water.	8 §S	
5 3 2	simple compound simple	7 8 41⁄2	6	10 6 714	75 110 75	12.12 4.82 11.77	42.03 "	6.1 lb. 8.72 '' 7.64 ''	

Steam-consumption of Engines at Various Speeds. (Profs. Denton and Jacobus, Trans. A. S. M. E., x. 722)—17 × 30 in. engine, non-condensing, fixed cut-off, Meyer valve.

STEAM-CONSUMPTION, LBS. PER I.H.P. PER HOUR.

Figures taken from plotted diagram of results.

Revs. per min	8	12	16	20	24	32	40	48	56	72	88
cut off, lbs		35	32	30	29.3	29	28.7	28.5	28.8	28	27.7
14 " "	39	34	31	29.5	29	28.4	28	27.5	27.1	26.3	25.6
1/4 " "	39	36	34	33	32	30.8	29.8	29.2	28.8	28.7	• • • •

STEAM-CONSUMPTION OF SAME ENGINE; FIXED SPEED, 60 REVS. PER MIN.

Varying cut-off compared with throttling-engine for same horse-power and boiler-pressures:

Cut-off, fraction of stroke 0.1 0.15 0.2 0.25 0.8 0.4 0.5 0.6 0.7 0.8 Boiler-pressure, 90 lbs... 29 27.5 27 27 27 27.2 28.5 60 lbs... 39 84.2 32.2 81.5 81.4 81.6 82.2 84.1 36.5 89

Throttling-engine, 1/2 Cut-off, for Corresponding Horse-powers. Boiler-pressure, 90 lbs... 42 87 33.8 81.5 29.8 60 lbs... 49 46.8 44.6 41 50.1

Some of the principal conclusions from this series of tests are as follows: 1. There is a distinct gain in economy of steam as the speed increases for 14, 14, and 14 cut-off at 90 lbs, pressure. The loss in economy for about 14 cut-off is at the rate of 1/12 lb. of water per H.P. for each decrease of a revolution per minute from 86 to 26 revolutions, and at the rate of 1/18 lb. of water below 26 revolutions. Also, at all speeds the 14 cut-off is more economical than either the 16 or 16 cut-off.

2. At 90 lbs. boiler-pressure and above 1/2 cut-off, to produce a given H.P. requires about 20% less steam than to cut off at % stroke and regulate by the

throttle.

3. For the same conditions with 60 lbs. boiler-pressure, to obtain, by throttling, the same mean effective pressure at % cut-off that is obtained by tting off about 1/2, requires about 30% more steam than for the latter ndition.

High Piston-speed in Engines. (Proc. Inst. M. E., July, 1883, p. 1).—The torpedo boat is an excellent example of the advance towards the speeds, and shows what can be accomplished by studying lightness detrength in combination. In running at 22% knots an hour, an engine the cylinders of 16 in. stroke will make 480 revolutions per minute, which res 1200 ft, per minute for piston-speed; and it is remarked that engines nning at that high rate work much more smoothly than at lower speeds, d that the difficulty of lubrication diminishes as the speed increases.

A High-speed Corliss Engine.—A Corliss engine, 20 × 42 in., has en running a wire-rod mill at the Trenton Iron Co.'s works since 1877, at 1 revolutions or 1120 ft. piston-speed per minute (Trans. A. S. M. E., ii. . A piston-speed of 1200 ft. per min. has been realized in locomotive actice.

Free Limitation of Engine-speed. (Chas. T. Porter, in a paper the Limitation of Engine-speed, Trans. A. S. M. E., xiv. 806.)—The actical limitation to high rotative speed in stationary reciprocating steam. gines is not found in the danger of heating or of excessive wear, nor, as gines is not found in the danger of heating or of excessive wear, nor, as generally believed, in the centrifugal force of the fly-wheel, nor in the idency to knock in the centres, nor in vibration. He gives two objections very high speeds: First, that "engines ought not to be run as fast as y can be;" second, the large amount of waste room in the port, which required for proper steam distribution. In the important respect of momy of steam, the high-speed engine has thus far proved a failure, rge gain was looked for from high speed, because the loss by condensan on a given surface would be divided into a greater weight of steam, but sexpectation has not been realized. For this unsatisfactory result we to lay the blame chiefly on the excessive amount of waste room. The re to lay the blame chiefly on the excessive amount of waste room. The linary method of expressing the amount of waste room in the percentage led by it to the total piston displacement, is a misleading one. It should expressed as the percentage which it adds to the length of steam admisexpressed as the percentage which it must to the length of section admission. For example, if the steam is cut off at 1/5 of the stroke, 8% added by waste room to the total piston displacement means 40% added to the ume of steam admitted. Engines of four, five and six feet stroke may perly be run at from 700 to 800 ft. of piston travel per minute, but for inary sizes, says Mr. Porter, 600 ft. per minute should be the limit.

nfluence of the Steam-jacket.—Tests of numerous engines with I without steam-jackets show an exceeding diversity of results, ranging the way from 30% saving down to zero, or even in some cases showing an ual loss. The opinions of engineers at this date (1894) is also as diverse as results, but there is a tendency towards a general belief that the jacket is as valuable an appendage to an engine as was formerly supposed. An exsive resume of facts and opinions on the steam-jacket is given by Prof. 17ston, in Trans. A. S. M. E., xiv. 462. See also Trans. A. S. M. E., xiv. and 1840; xiii. 176; xii. 426 and 1840; and Jour. F. I., April, 1891, p. 276.

following are a few statements selected from these papers.

he results of tests reported by the research committee on steam-jackets ointed by the British Institution of Mechanical Engineers in 1886, indian increased efficiency due to the use of the steam-jacket of from 15 to

r 30%, according to varying circumstances.

nnett asserts that "it has been abundantly proved that steamtets are not only advisable but absolutely necessary, in order that high s of expansion may be efficiently carried out and the greatest possible nomy of heat attained."

herwood finds the gain by its use, under the conditions of ordinary tice, as a general average, to be about 20% on small and 8% or 9% on engines, varying through intermediate values with intermediate sizes, eing understood that the jacket has an effective circulation, and that i heads and sides are jacketed.
ofessor Unwin considers that "in all cases and on all cylinders the

et is useful; provided, of course, ordinary, not superheated, steam is ; but the advantages may diminish to an amount not worth the interest xtra cost."

ofessor Cotterill says: Experience shows that a steam-jacket is advanous, but the amount to be gained will vary according to circumstances.

nany cases it may be that the advantage is small. Great caution is ssary in drawing conclusions from any special set of experiments on influence of jacketing.

Mr. E. D. Leavitt has expressed the opinion that, in his practice, steam-jackets produce an increase of efficiency of from 15% to 20%.

In the Pawtucket pumping-engine, 15 and 30½ × 30 in., 50 revs. per min., steam-pressure 125 lbs. gauge, cut-off ½ in hp. and ½ in lp. cylinder, the barrels only jacketed, the saving by the jackets was from 1% to 4%.

The superintendent of the Holly Mfg. Co. (compound pumping-engines) says: "In regard to the benefits derived from steam-jackets on our steam-cylinders, I am somewhat of a skeptic. From data taken on our own enjures and tests made. I am wat to be convinced that there is any reactical gines and tests made I am yet to be convinced that there is any practical value in the steam-jacket." . . . "You might practically say that there

is no difference."

Professor Schröter from his work on the triple-expansion engines at Augs-Professor Schröter from his work on the triple-expansion engines at Augsburg, and from the results of his tests of the jacket efficiency on a small engine of the Sulzer type in his own laboratory, concludes: (1) The value of the jacket may vary within very wide limits, or even become negative. (2) The shorter the cut-off the greater the gain by the use of a jacket. (3) The use of higher pressure in the jacket than in the cylinder produces an advantage. The greater this difference the better. (4) The high-pressure cylinder may be left unjacketed without great loss, but the others should always be jacketed.

The test of the Laketon triple-expansion pumping-engine showed a gain of 8.3% by the use of the jackets, but Prof. Denton points out (Trans. A. S. M. E., xiv. 1412) that all but 1.9% of the gain was ascribable to the greater range of expansion used with the jackets.

range of expansion used with the jackets.

Test of a Compound Condensing Engine with and with-out Jackets at different Loads. (R. C. Carpenter, Trans. A. S. M. E., xiv. 428.)—Cylinders 9 and 16 in.×14 in. stroke; 112 lbs. boiler-pressure; rated capacity 100 H.P.; 265 revs. per min. Vacuum, 23 in. From the results of several tests curves are plotted, from which the following principal figures are taken.

This table gives a clue to the great variation in the apparent saving due to the steam-jacket as reported by different experimenters. With this particular engine it appears that when running at its most economical rate of 100 H.P., without jackets, very little saving is made by use of the jackets. When running light the jacket makes a considerable saving, but when overloaded it is a detriment.

At the load which corresponds to the most economical rate, with no steam in jackets, or 100 H.P., the use of the jacket makes a saving of only 1s; but at a load of 60 H.P. the saving by use of the jacket is about 11s, and the shape of the curve indicates that the relative advantage of the jacket would be still greater at lighter loads than 60 H.P.

Counterbalancing Engines.—Prof. Unwin gives the formula for counterbalancing vertical engines:

in which W_1 denotes the weight of the balance weight and p the radius to its centre of gravity, W_2 the weight of the crank-pin and half the weight of the connecting-rod, and r the length of the crank. For horizontal engines:

$$W_1 = \frac{9}{6}(W_2 + W_3)\frac{r}{p}$$
 to $\frac{3}{6}(W_2 + W_3)\frac{r}{p}$, (3)

in which W_2 denotes the weight of the piston, piston-rod, cross-head, and the other half of the weight of the connecting-rod.

The American Machinist, commenting on these formulæ, says: For horizontal engines formula (2) is often used; formula (1) will give a counterbalance too light for vertical engines. We should use formula (2) for computing the counterbalance for both horizontal and vertical engines, excepting locomotives, in which the counterbalance should be heavier.

eventing Vibrations of Engines.—Many suggestions have made for remedying the vibration and noise attendant on the working big engines which are employed to run dynamos. A plan which has great satisfaction is to build hair-felt into the foundations of the e. An electric company has had a 90-horse-power engine removed its foundations, which were then taken up to the depth of 4 feet. A of felt5 inches thick was then placed on the foundations and run up 2 feet sides, and on the top of this the brickwork was built up.—Safety Valve, **am*-engine Foundations Embedded in Air.—In the sugarry of Claus Spreckels, at Philadelphia, Pa., the engines are distributed ically all over the buildings, a large proportion of them being on upper i. Some are bolted to iron beams or girders, and are consequently ent of all foundation. Some of these engines ran noiselessly and satisfily, while others produced more or less vibration and rattle. To corhe latter the engineers suspended foundations from the bottoms of the spot of the corner of the corn

st of Coal for Steam-power.—The following table shows the int and the cost of coal per day and per year for various horse-powers, 1 to 1000, based on the assumption of 4 lbs. of coal being used per hour orse-power. It is useful, among other things, in estimating the saving may be made in fuel by substituting more economical boilers and es for those already in use. Thus with coal at \$3.00 per ton, a saving 000 per year in fuel may be made by replacing a steam plant of 1000 requiring 4 lbs. of coal per hour per horse-power, with one requiring 2 lbs.

per E	LP, per	mption hour; lays in a	10 hou	irs a	\$1.	50,	\$5	2.00.	\$3	.00.	\$4.	00.
Lbs.	Long	Tons.	She		Short			er t Ton.		er t Ton.	Per Short Ton.	
Per Day.	Per	Per Year.	Per Day.	Per	Cost in Dollars,		Cost in Dollars.		Cost in Dollars.		Cost in Dollars.	
	Day.				Per Day.	Per Year	Per Day.	Per Year.	Per Day.	Per Year.	Per Day.	Per Year
400 400 1,000	.0179	5,357 53,57 133,92	.02	60 150	.03 .30 .75	90 90 925	,04 ,40 1.00	12 120 300	.06 .60	18 180 450	.08 .80 2.00	24 240 600
2,000	,4464 ,8928	267.85	1.00	300	1.50	450	2.00	600	3.00	900	4.00	1,200
3,000	1.3393	401.78	1.50	450	2.25	675	3,00		4.50	1,350	6,00	1,800
4,000	1.7857	535.71	8.00	600	3,00	900	4,00	1,200	6.00	1,800	8,00	2,400
6,000	2,6785	800.56	3.00	900		1,350	6,00		9,00	2,700	12.00	3,600
8,000	3.5714	1,071.49	4.00	1,200	6.00	1,800	8.00	2,400	12.00	3,600	16.00	4,800
10,000	4.4643		5.00	1,500	7.50	2,250	10.00	3,000	15.00	4,500 5,400	20.00	6,000
12,000	5 3571	1,607.13	6.00	1,800		2,700	14.00	4,200	21,00	6,200	28.00	8,400
14,000	6,2500 7,1428	1,874.98 2,112,84	7.00	2,100		3,600	16,00	4,800	24.00	7.200	32.00	9,600
18,000		2,410,69	9.00	2,700	13.50	4,050	18 00	5,400	27.00	8,100		10,800
20,000	8,9285	2,678.55	10.00	3,000	15.00	4,500	20.00	6,000	30.00	9,000		12,000
24,000		3,214,26	12.00	3,600		5.400	24.00	7,200	36,00	10,800		14,400
38,000		3,749,97	14.00	4.900	21.00	6,300	28,00	8,400	42,00	11,600		16,800
12,000		4,285.68	16,00	4,800		7,200	32,00	9,600	48,00	12,400		19,200
15,000		4,821,39	18,00	5,400		8,100	36.00		54.00	14,200		21,600
		5,357.10	20,00	6,000		9,000	40.00	12,000	60.00	18,000	80.00	24,000

ring Steam Heat.—There is no satisfactory method for equalizing ut on the engines and boilers in electric-light stations. Storage-batteries seen used, but they are expensive in first cost, repairs, and attention. alpin, of London, proposes to store heat during the day in specially ucted reservoirs. As the water in the boilers is raised to 250 lbs. prest is conducted to cylindrical reservoirs resembling English horizontal, and stored there for use when wanted. In this way a comparatively boiler-plant can be used for heating the water to 250 lbs. pressure all the the twenty-four hours of the day, and the stored water may be on at any time, according to the magnitude of the demand. The

steam-engines are to be worked by the steam generated by the release of pressure from this water, and the valves are to be arranged in such a way that the steam shall work at 130 lbs. pressure. A reservoir 8 ft. in diameter and 80 ft. long, containing 84,000 lbs. of heated water at 250 lbs. pressure, would supply 5250 lbs. of steam at 130 lbs. pressure. As the steam consumption of a condensing electric-light engine is about 18 lbs. per horse-power hour, such a reservoir would supply 256 effective horse-power hours. In 1878, in France, this method of storing steam was used on a tramway. M. France, the engineer, designed a smokeless locomotive to work by steam power supplied by a reservoir containing 400 gallons of water at 220 lbs. pressure. The reservoir was charged with steam from a stationary boiler at one end of the tramway.

Cost of Steam-power. (Chas. T. Main, A. S. M. E., x. 48.)—Estimated costs in New England in 1888, per horse-power, based on engines of 1000 H.P.

	C	ompound Engine.	Condensing Engine.	Non-con- densing Engine.
2,	Cost engine and piping, complete Engine-house	8.00	\$20.00 7.50 5.50	\$17.50 7.50 4.50
, 4.	Total engine plant		88.00	29.50
6. 7. 8.	Depreciation, 4% on total cost	0.80 2.00 0.45 0.165	1.82 0.66 1.65 0.871 0.138	1.18 0.59 1.475 0.889 0.125
10.	Total of lines 5, 6, 7, 8, 9		4.189	8.709
12.	Cost boilers, feed-pumps, etc	. 2.92	18.88 4.17 7.80	16.00 5.00 8.00
14.	Total boiler-plant	18.86	24.80	29.00
16. 17. 18.	Depreciation, 5% on total cost	0.918 867 918 207	1.240 .496 1.240 .279 .124	1.450 .580 1.450 .826 .145
20.	Total of lines 15 to 19		8.879	8.951
21.	Coal used per L.H.P. per hour, lbs	1.75	2.50	8.00
23.	Cost of coal per I H.P. per day of 10 hours at \$5.00 per ton of 2240 lbs	4.00 0.60	cts. 5.78 0.40	cts. 6.86 0.85
24. 25.	Oil, waste, and supplies, per day	0.25	0.75 0.22	0.90 0.90
26.	Total daily expense	5.88	7.09	8.81
25.	Yearly running expense, 808 days, p. I.H.P. Total yearly expense, lines 10, 80, and 87 Total yearly expense per I.H.P. for pow	916.570 24.087	\$81,687 89,855	\$95.595 88.948
80.	if 50% of exhaust-steam is used for hea ing	19.597	14,907 7.916	16.668 7.709

When exhaust-steam or a part of the receiver-steam is used for heating, or if part of the steam in a condensing engine is diverted from the condenser, and used for other purposes than power, the value of such steam should e deducted from the cost of the total amount of steam generated in order arrive at the cost properly chargeable to power. The figures in lines 29

nd 30 are based on an assumption made by Mr. Main of losses of heat mounting to 25% between the boiler and the exhaust-pipe, an allowance

hich is probably too large.

See also two papers by Chas. E. Emery on "Cost of Steam Power," Trans.

S. C. E., vol. xii, Nov. 1883, and Trans. A. I. E. E., vol. x, Mar. 1893.

ROTABY STEAM-ENGINES.

Steam Turbines.—The steam turbine is a small turbine wheel which uns with steam as the ordinary turbine does with water. (For description f the Parsons and the Dow steam turbines see Modern Mechanism, p. 298, tc.) The Parsons turbine is a series of parellel-flow turbines mounted side y side on a shaft; the Dow turbine is a series of radial outward-flow tury side on a shart; the Dow turbine is a series of concentration of the short production in series of concentration ings in a single plane, a stationary uide-ring being between each pair of movable rings. The speeds of the team turbines enormously exceed those of any form of engine with recipcating piston, or even of the so-called rotary engines. The three- and four-ylinder angines of the Brotherhood type, in which the several cylinders re usually grouped radially about a common crank and shaft, often exceed 300 revolutions per minute, and have been driven, experimentally, above 300; but the steam turbine of Parsons makes 10,000 and even 20,000 revoluons, and the Dow turbine is reputed to have attained \$5,000. (See Trans. S. M. E., vol. x. p. 680, and xil. p. 868; Trans. Assoc. of Eng'g Societies, bl. viii. p. 583; Eng'g, Jan. 13, 1886, and Jan. 8, 1892; Eng'g News, Feb. 27, 982.) A Dow turbine, exhibited in 1889, weighed 68 lbs. and developed 10. P., with a consumption of 47 lbs. of steam per H. P., per hour, the steam passure being 70 lbs. The Dow turbine is used to spin the diy-wheel of the correll torage. owell torpedo. The dimensions of the wheel are 13.8 in, diam, 6.5 in, idth, radius of gyration 5.57 in. The energy stored in it at 10,000 revs. or min. is 500,000 ft.-lbs.

The De Laval Steam Turbins, shown at the Chicago exhibition, 93, is a reaction wheel somewhat similar to the Pelton water-wheel. The eam jet is directed by a nozzle against the plane of the turbine at quite a nall angle and tangentially against the circumference of the medium riphery of the blades. The angle of the blade is the same at the side of mission and discharge. The width of the blade is constant along the

tire thickness of the turbine.

The steam is expanded to the pressure of the surroundings before arrive at the blades. This expansion takes place in the nozzler and is caused uply by making its sides diverging. As the steam passes through this annel its specific volume is increased in a greater proportion than the ess section of the channel, and for this reason its velocity is increased, dalso its momentum, till the end of the expansion at the last sectional action would be reasonable to the expansion at the last sectional contents. as of the nozzle. The greater the expansion in the nozzle the greater its locity at this point. A pressure of 75 lbs. and expansion to an absolute assure of one atmosphere give a final velocity of about 2625 ft. per second. Expansion is carried further in this steam turbine than in ordinary steam-gines. This is on account of the steam expanding completely during its rk to the pressure of the surroundings. For obtaining the greatest possible effect the admission to the blades must

free from blows and the velocity of discharge as low as possible. These rice from blows and the velocity of discharge as low as possible. These riditions would require in the steam turbine an enormous velocity of iphery—as high as 1300 to 1650 ft. per second. The centrifugal force, rertheless, puts a limit to the use of very high velocities. In the 5 horsewer turbine the velocity of periphery is 574 ft. per second, and the numof revolutions 30,000 per minute.

Iowever carefully the turbine may be manufactured it is impossible, on ount of unevenness of the material, to get its centre of gravity to correand exactly to its geometrical axle of revolution; and however small this erence may be, it becomes very noticeable at such high velocities. val has succeeded in solving the problem by providing the turbine with a dible shaft. This yielding shaft allows the turbine at the high rate of ed to adjust itself and revolve around its true centre of gravity, the tre line of the shaft meanwhile describing a surface of revolution.

1 the gearing-box the speed is reduced from 30,000 revolutions to 3000 means of a driver on the turbine shafts, which sets in motion a cog-sel of 10 times its own diameter. These gearings are provided with spiral s placed at an angle of about 45°.

or descriptions of the most recent forms of steam turbines, see circulars he Westinghouse Machine Co., Pittsburg, Pa., and the De Laval Steam

Turbine Co., Trenton, N. J.; also paper by Dr. R. H. Thurston in Trans. A. S. M. E., vol. xxii., p. 170.

Rotary Stcam-engines, other than steam turbines, have been invented by the thousands, but not one has attained a commercial success, as regards economy of steam. The possible advantages, such as saving of space, to be gained by a rotary engine are overbalanced by its waste of steam. Rotary engines are in use, however, for special purposes, such as steam fire-engines and steam feeds for sawmills, in which steam economy is not a matter of importance. not a matter of importance.

DIMENSIONS OF PARTS OF ENGINES.

The treatment of this subject by the leading authorities on the steam-engine is very unsatisfactory, being a confused mass of rules and formulæ based partly upon theory and partly upon practice. The practice of builders shows an exceeding diversity of opinion as to correct dimensions. The treatment given below is chiefly the result of a study of the works of Rankine. Seaton, Unwin, Thurston, Marks, and Whitham, and is largely a condensa-tion of a series of articles by the author published in the American Ma-chinist, in 1894, with many alterations and much additional matter. In order to make a comparison of many of the formulæ they have been applied

to make a comparison or many of the formulæ they have been applied to the assumed cases of six engines of different sizes, and in some cases this comparison has led to the construction of new formulæ.

Cylinder. (Whitham.)—Length of bore = stroke + breadth of piston-ring - ½ to ½ in; length between heads = stroke + thickness of piston + sum of clearances at both ends; thickness of piston = breadth of ring + thickness of piston = proceedings of the comparison thickness of flange on one side to carry the ring + thickness of followerplate.

Thickness of flange or follower.... % to 14 in. For cylinder of diameter...... 8 to 10 in. 1 in. 60 to 100 tp.

Clearance of Piston. (Seaton.)—The clearance allowed varies with the size of the engine from ½ to ¾ in. for roughness of castings and 1/16 to ½ in. for each working joint. Naval and other very fast-running engines have a larger allowance. In a vertical direct-acting engine the parts which wear so as to bring the piston nearer the bottom are three, viz., the shaft journals, the crank-pin brasses, and Diston-rod gudgeon-brasses.

Thickness of Cylinder. (Thurston.)—For engines of the older types and under moderate steam-pressures, some builders have for many years restricted the stress to about 2550 lbs. per sq. in.

is a common proportion; t, D, and b being thickness, diam., and a constant added quantity varying from 0 to $\frac{1}{2}6$ in., all in inches; p, is the initial unbalanced steam-pressure per sq. in. In this expression b is made larger for horizontal than for vertical cylinders, as, for example, in large engines 0.5 in the one case and 0.2 in the other, the one requiring re-boring more than the other. The constant a is from 0.004 to 0.0005; the first value for vertical cylinders, or short strokes; the second for horizontal engines, or for long strokes. long strokes.

Thickness of Cylinder and its Connections for Marine Engines. (Seaton).—D =the diam, of the cylinder in inches; p =load on the safety-valves in lbs. per sq. in.; f, a constant multiplier = thickness of barrel + .25 in.

Thickness of metal of cylinder barrel or liner, not to be less than $p \times D$ +

" liner = $1.1 \times f$

Thickness of liner when of steel $p \times D + 6000 + 0.5$

metal of steam-ports = $0.6 \times f$.

"valve-box sides = $0.65 \times f$.

When made of exceedingly good material, at least twice melted, the rickness may be 0.8 of that given by the above rules.

itham gives the following from different authorities:

Van Buren:	$\begin{cases} t = 0.0001Dp + 0.15 \sqrt{D}; \\ t = 0.03 \sqrt{Dp}. \end{cases}$:	:	•	•	(5) (6)
	$t = \frac{(D+2.5)p}{1900}.$					
Weisbach:	t = 0.8 + 0.00033pD					(8)
Seaton:	t = 0.5 + 0.0004pD.	•	•	•	•	(9)
Haswell:	$\begin{cases} t = 0.0004pD + \frac{1}{16} \text{ (vertical); } \\ t = 0.0005pD + \frac{1}{16} \text{ (horizontal).} \end{cases}$:	:	:	:	(10) (11)

tham recommends (6) where provision is made for the reboring, and ample strength and rigidity are secured, for horizontal or vertical lers of large or small diameter; (9) for large cylinders using steam 100 lbs. gauge-pressure, and

: is a smaller value than is given by the other formulæ quoted; but : says that it is not advisable to make a steam-cylinder less than 0.75 ick under any circumstances.

following table gives the calculated thickness of cylinders of engines 30, and 50 in. diam., assuming p the maximum unbalanced pressure on ston = 100 lbs, per sq. in. As the same engines will be used for calcuof other dimensions, other particulars concerning them are here for reference.

DIMENSIONS, ETC., OF ENGINES.

9 No	1 and 2.	8 and 4.	5 and 6.
ted horse-powerI.H.P. of cyl., in	250 125 500 78.54 42 7854	450 30 21.6 5 130 65 650 706.86 32.3 70,686	1250 50 4 8 90 45 700 1963.5 30 196,350 100

THICKNESS OF CYLINDER BY FORMULA.	1 and 2.	8 and 4.	5 and 6.
(1) $.0004pD + 0.5$, short stroke	.90	1.70	2.50
(1) $.0005pD + 0.5$, long stroke	1.00	2.00	8,00
(2) $.00033pD$.83	.99	1 67
(8) $.0002pD + 0.6$,80	1.40	1,66
(5) $.0001pD + .15 \sqrt{D}$.57	1.19	1.56
(6) .08 \sqrt{Dp}	.95	1.64	2,12
(7) $\frac{(D+2.5)}{1900} p$.66	1.71	9.76
(8) $.00088pD + 0.8$	1.18	1.79	2,45
9) $.0004pD + 0.5$.90	1.70	2.50
0) $.0004pD + \frac{1}{6}$ (vertical)	.68	1.88	2.18
1) $.0005pD + \frac{1}{18}$ (horizontal)	.63	1.63	2.63
2) $.009D \sqrt{p}$ (small engines)	.80(?)		••••
(8) .00028pD	.28(?)	.84(?)	1.40(?)
Average of first eleven.	.76	1.48	2.26

The average corresponds nearly to the formula t=.00037Dp+0.4 in. A convenient approximation is t=.0004Dp+0.3 in., which gives for Diameters..... 10 20 80 40 50

1.10 1.50 1.90 2.30 2.70 in.

The last formula corresponds to a tensile strength of cast iron of 12,500 lbs., with a factor of safety of 10 and an allowance of 0.3 in. for reboring. Cylinder-heads.—Thurston says: Cylinder-heads may be given a thickness, at the edges and in the flanges, exceeding somewhat that of the cylinder. An excess of not less than 25% is usual. It may be thinner in the middle. Where made, as is usual in large engines, of two disks with intermediate radiating connecting ribs or webs, that section which is safe mediate radiating, connecting ribs or webs, that section which is safe against shearing is probably ample. An examination of the designs of experienced builders, by Professor Thurston, gave

$$t = \frac{Dp}{8000} + \frac{1}{24} \text{ inch.} \qquad (1)$$
D being the diameter of that circle in which the thickness is taken.

Thurston also gives $t = .005D \sqrt{p} + 0.25$ $t = 0.008D \sqrt{p}. \dots$ Marks gives

He also says a good practical rule for pressures under 100 lbs, per sq. in, is to make the thickness of the cylinder-heads 1½ times that of the walls; and applying this factor to his formula for thickness of walls, or .00028pD, we

$$t = .00035pD.$$
 (4)

Whitham quotes from Seaton,

$$t = \frac{pD + 500}{2000}$$
, which is equal to .0005pD + .25 inch. . . . (5)

Seaton's formula for cylinder bottoms, quoted above, is

$$t = 1.1f$$
, in which $f = .0002pD + .85$ inch, or $t = .00022pD + .98$. (6)

Applying the above formulæ to the engines of 10, 30, and 50 inches diameter, with maximum unbalanced steam-pressure of 100 lbs. per sq. in., we have

Cylinder diameter, inches	; =	10	80	90
(1) $t = .00038Dp + .95$	=	.53	1.25	1.89
(2) $t = .005D \sqrt{p} + .25$	=	.75	1.75	2.75
(8) $t = .003D \sqrt{p}$	=	.30	.90	1.50
(4) $t = .00085 D\bar{p}$	=	.85	1.05	1.75
(5) $t = .0005Dp + .25$	=	.75	1.75	2.75
(5) $t = .0005Dp + .25$ (6) $t = .00022Dp + .93$	=	1.15	1.59	2.08
Average of 6		65	1.88	2.10

The average is expressed by the formula t = .00086Dp + .31 mcm. never's "Modern Locomotive Construction," p. 24, gives for locomotive linder-heads for pressures up to 120 lbs.:

16 to 18 14 to 15 r diameters, in...... 19 to 22 9 to 10 11 to 18 34 ickness, in.......

aking the pressure at 120 lbs. per sq. in., the thicknesses 134 in. and 34 in. cylinders 22 and 10 in. diam., respectively, correspond to the formula

= .00035Dp + .33 inch.

Web-stiffened Cylinder-covers.—Seaton objects to webs for flening cast-iron cylinder-covers as a source of danger. The strain on tweb is one of tension, and if there should be a nick or defect in the er edge of the web the sudden application of strain is apt to start a sck. He recommends that high-pressure cylinders over 24 in. and low-ssure cylinders over 40 in. diam. should have their covers cast hollow. In two thicknesses of metal. The depth of the cover at the middle should about $\frac{1}{4}$ the diam of the piston for pressures of 80 lbs. and upwards, it hat of the low-pressure cylinder-cover of a compound engine equal to to fit the high-pressure cylinder-cover of a compound engine equal to to fit the high-pressure cylinder-cover of a compound engine equal to to fit the high-pressure cylinder-cover of the piston-rod. In the tish Navy the cylinder-covers are made of steel castings, $\frac{3}{4}$ to $\frac{1}{4}$ in. As, generally cast without webs, stiffness being obtained by their form, ich is often a series of corrugations.

Thinder-head Bolts.—Diameter of bolt-circle for cylinder-head meter of cylinder $+2 \times$ thickness of cylinder $+2 \times$ diameter of bolts. bolts should not be more than 6 inches apart (Whitham).

Arks gives for number of bolts $b = \frac{784D^2p}{5000c} = .0001871 \frac{D^2}{2}$, in which $c = \frac{1}{2} = \frac{1}{2$ h two thicknesses of metal. The depth of the cover at the middle should

s of a single bolt, p = boiler-pressure in lbs. per sq. in.; 5000 lbs. is taken he safe strain per sq. in on the nominal area of the bolt.

aton says: Cylinder-cover studs and bolts, when made of steel, should if such a size that the strain in them does not exceed 5000 lbs, per sq. in. en of less than % inch diameter it should not exceed 4500 lbs. per sq. in. en of iron the strain should be 20% less.

jurston says: Cylinder flanges are made a little thicker than the cylinand usually of equal thickness with the flanges of the heads. Cylinders should be so closely spaced as not to allow springing of the flanges leakage, say, 4 to 5 times the thickness of the flanges. Their diameter lid be proportioned for a maximum stress of not over 4000 to 5000 lbs.

square inch. $D = \text{diameter of cylinder}, p = \text{maximum steam-pressure}, b = \text{number site}, e = \text{size or diameter of each boit, and 5000 lbs. be allowed per sq. f nominal area of the bolt, .7854<math>D^2p = 3927bs^2$; whence $bs^2 = .0002D^2p$;

 $.0002 \frac{D^2 p}{a^2}$; $s = .01414 D \sqrt{\frac{p}{b}}$. For the three engines we have:

Diameter of cylinder, inches...... Diameter of bolt-circle, approx.... Gircumference of circle, approx.... Minimum No. of bolts, circ. + f.... 18 67.5 Diam. of bolts, $s = .01414D_4 / \frac{p}{5} \dots$ % in.

diameter of bolt for the 10-inch cylinder is v.84 in. by the formula, inch is as small as should be taken, on account of possible overstrain

wrench in screwing up the nut.
Piston. Details of Construction of Ordinary Pist.
(Seaton.)—Let D be the diameter of the piston in inches, p the effective of the piston of the piston in inches. ressure per square inch on it, a a constant multiplier, found as follows:

```
The thickness of front of piston near the boss = 0.2 \times s rim = 0.17 \times s.
                                                                            = 0.18 \times 3
                           back
                                                                            = 0.8 \times x.
= 0.28 \times x.
                           boss around the rod
                           flange inside packing-ring
                                                                            = 0.25 \times x.
= 0.15 \times r,
                                     at edge
                           packing-ring
junk-ring at edge
                                          inside packing-ring = 0.21 \times x, at bolt-holes
                           metal around piston edge
                                                                            = 0.25 \times x
The breadth of packing-ring
                                                                            = 0.63 \times x
     of preading of packing ring depth of piston at centre 0.45 \times x, lap of junk-ring on the piston 0.45 \times x, space between piston body and packing-ring 0.3 \times x, diameter of junk-ring bolts 0.1 \times x + 0.55 in.
      diameter of junk-ring bolts
                                                                             = 10 diameters.
       number of webs in the piston
                                                                            = (D + 20) + 12,
= 0.18 \times x.
      thickness
```

Marks gives the approximate rule: Thickness of piston-head= \(\lambda \text{id} \), in which l = length of stroke, and d = diameter of cylinder in inches. which t = length or stroke, and a = chameter or cylinder in incines. what ham says in a horizontal engine the rings support the piston, or at least a part of it, under ordinary conditions. The pressure due to the weight of the piston upon an area equal to 0.7 the diameter of the cylinder x breadth of ring-face should never exceed 200 bs. per sq. in. He also execute the control of the cylinder x formula much used in this country: Breadth of ring-face $\approx 0.15 \times \text{diameter}$ eter of cylinder.

For our engines we have diameter = 20 50

Thickness of piston-head.

Marks, \sqrt{lD} ; long stroke	8.81	5.48	7.00
	8.94	6.51	8.32
Seaton, depth at centre = 1.4x	4.30	9.80	15.40
	1.89	4.41	6.98
	1.50	4.50	7.50

Diameter of Piston Packing-rings. — These are generally turned, before they are cut, about ¼ inch diameter larger than the cylinder,

turned, before they are cut, about ¼ inch diameter larger than the cylinder, for cylinders up to 20 inches diameter, and then enough is cut out of the ring to spring them to the diameter of the cylinder. For larger cylinders the rings are turned proportionately larger. Seaton recommends an excess of 1% of the diameter of the cylinder.

Cross-section of the Hings.—The thickness is commonly made 1/30th of the diam. of cyl. + ½ inch, and the width = thickness + ½ inch. For an eccentric ring the mean thickness may be the same as for a ring of uniform thickness, and the minimum thickness = ¾ the maximum. A circular issued by J. H. Dunbar, manufacturer of packing-rings. Youngstown, O., says: Unless otherwise ordered, the thickness of rings will be made equal to 08 x their diameter. This thickness has been found to be satisfactory in practice. It admits of the ring being made about 3/16" to the foot larger than the cylinder, and has, when new, a tension of about two pounds per inch of circumference, which is ample to prevent leakage. two pounds per inch of circumference, which is ample to prevent leakage. if the surface of the ring and cylinder are smooth.

if the surface of the ring and cylinder are smooth. As regards the width of rings, authorities "scatter" from very narrow to very wide, the latter being fully ten times the former. For instance, Unwin gives W=d. 0.14 + .08. Whitham's formula is W = d. 15. In both for nula W is the width of the ring in inches, and d the diameter of the cylinder in inches. Unwin's formula makes the width of a 20° ring $W = 20 \times$.014 + .08 = .89°, while Whitham's is $20 \times$.15 = 3° for the same diameter of ring. There is much less difference in the practice of engine-builders in thirespect, but there is still room for a standard width of ring. It is believed that for cylinders over 18° diameter 3° is a popular and practical width, and 4%" for cylinders of that size and under.

Fit of Piston-rod into Piston. (Seaton)—The most convenient and reliable practice is to turn the piston-rod end with a shoulder of 1/16 "ach for small engines, and $\frac{1}{2}$ 6 inch for large ones, make the taper 8 in. to

oot until the section of the rod is three fourths of that of the body, then the remaining part parallel; the rod should then fit into the piston so leave 14 inch between it and the shoulder for large pistons, and 1/16 in. mall. The shoulder prevents the rod from splitting the piston, and sof the rod being turned true after long wear without encroaching on

sper.

piston is secured to the rod by a nut, and the size of the rod should ch that the strain on the section at the bottom of the thread does not a 5500 lbs, per sq. in. for iron, 7000 lbs, for steel. The depth of this nut not exceed the diameter which would be found by allowing these is. The nut should be locked to prevent its working loose.

ameter of Piston-rods.—Unwin gives

$$d'' = bD \sqrt{p}, \qquad (1)$$

ich D is the cylinder diameter in inches, p is the maximum unbalanced ure in lbs. per sq. in., and the constant b=0.0167 for iron, and b= for steel. Thurston, from an examination of a considerable number is in use, gives

$$d'' = \sqrt[4]{\frac{D^2 p L^2}{a} + \frac{D}{80}}$$
, nearly, (2)

feet, D and d in inches), in which a = 10,000 and upward in the various of engines, the marine screw engines or ordinary fast engines on given the lowest values, while "low-speed engines" being less to accident from shock give a = 15,000, often.

nections of the piston-rod to the piston and to the crosshead should

a factor of safety of at least 8 or 10. Marks gives

factor of safety of at least 8 or 10. Marks gives
$$d'' = 0.0179D \sqrt{p}, \text{ for iron; for steel } d'' = 0.0105D \sqrt{p}; . . (3)$$

$$d d'' = 0.08901 \sqrt[4]{D^2 l^2 p}, \text{ for iron; for steel } d'' = 0.08525 \sqrt[4]{D^2 l^2 p}, \quad (4)$$

ich l is the length of stroke, all dimensions in inches. Deduce the ter of piston-rod by (3), and if this diameter is less than 1/12l, then use

eaton gives: Diameter of piston-rod =
$$\frac{\text{Diameter of cylinder}}{F} \sqrt{p}$$
.

following are the values of F:

Naval engi	nes, direct-acting	$\dots F = 60$
Mercantile	return connecting-rod, 2 rods ordinary stroke, direct-acting	$F = 50$
4	very long "	F = 48 $ F = 45$
4		T - 45

...Long and very long, as compared with the stroke usual for the of engine or size of cylinder.

or engine or size or cylinder.

naidering an expansive engine p, the effective pressure should be as the absolute working pressure, or 15 lbs, above that to which the safety-valve is loaded; for a compound engine the value of p for the ressure piston should be taken as the absolute pressure, less 15 lbs. same as the load on the safety-valve; for the medium-pressure, its, same as the load on the safety-valve; for the medium-pressure; and for pressure cylinder the pressure to which the escape-valve is loaded so, or the maximum absolute pressure, which can be got in the reor about 25 lbs. It is an advantage to make all the rods of a comengine alike, and this is now the rule.

ying the above formulæ to the engines of 10, 30, and 50 in. diameter, ort and long stroke, we have:

Diameter of Piston-rods.

Diameter of Cylinder, inches	10	0	80		50	
Stroke, inches	12	24	30	60	48	96
Unwin, iron, .0167D 4p	1.67	1.67	5.01	5.01	8.85	8.35
Unwin, steel, .0144 D Vp	1.44	1.44	4.32	4.82	7.20	7.20
Thurston $\sqrt[4]{\frac{\overline{D^2pL^2}}{10,000}} + \frac{D}{80}$ (L in feet).	1.18		8.12	· · · · · · ·	5.10	
Thurston, same with $a = 15,000$	 	1.40		3.88		6.35
Marks, iron, .0179D \(\sqrt{p} \)	1.79		5.37	5.37	8.95	8.95
Marks, iron, .03901 \$\square\$\overline{D^2l^2p}	1.85	1.91	8.70	5.18	6.04	8.54
Marks, steel, .0105 $D\sqrt{p}$	(1.05)		(3.15)		(5.25)	
Marks, steel, .03525 $\sqrt[4]{D^2 l^2 p}$	1,22	1.78	3.34	4.72	5.46	7.72
Seaton, naval engines, $\frac{D}{60}\sqrt{p}$	1.67		5.01	.	8.35	····•
Seaton, land engine, $\frac{D}{45} \sqrt{p} \dots$]	2.22		6.67	. .	11.11
Average of four for iron	1.49	1.82	4,80	5.26	7.11	8.74

The figures in brackets opposite Marks' third formula would be rejected since they are less than 16 of the stroke, and the figures derived by his fourth formula would be taken instead. The figure 1.79 opposite his first formula would be rejected for the engine of 24-inch stroks.

An empirical formula which gives results approximating the above aver-

ages is $d'' = .013 \sqrt{Dip}$.

The calculated results from this formula, for the six engines, are, respectively, 1.42, 1.88, 8.90, 5.61, 6.37, 9.01.

Piston=rod Guides.—The thrust on the guide, when the connecting-rod is at its maximum angle with the line of the piston-rod, is found from the formula: Thrust = total load on piston × tangent of maximum angle of connecting-rod = $p \tan \theta$. This angle, θ , is the angle whose sine = half stroke of piston + length of connecting-rod. stroke of piston + length of connecting-rod.

Ratio of length of connecting-rod to stroke Maximum angle of connecting-rod with line of	2	21/6	8
piston-rod	140 29	11° 98′	9° 36'
Tangent of the angle	.258 1.08 27	.204 1.0 206	.169 1.014

Seaton says: The area of the guide-block or slipper surface on which the thrust is taken should in no case be less than will admit of a pressure of 400 this, on the square inch; and for good working those surfaces which take the thrust when going ahead should be sufficiently large to prevent the maximum pressure exceeding 100 lbs. per sq. in. When the surfaces are kept well lubricated this allowance may be exceeded.

Thurston says: The rubbing surfaces of guides are so proportioned that

if V be their relative velocity in feet per minute, and p be the intensity of pressure on the guide in lbs. per sq. in., pV < 60,000 and pV > 40,000. The lower is the safer limit; but for marine and stationary engines it is allowable to take p = 60,000 + V. According to Rankine, for locomotives,

 $p = \frac{1}{V + 20}$ where p is the pressure in lbs. per sq. in. and V the velocity of rubbing in feet per minute. This includes the sum of all pressures forcing the two rubbing surfaces together.

Some British builders of portable engines restrict the pressure between For a mean velocity of 600 feet per minute, Prof. Thurston's formulas give, p < 100, p > 66.7; Rankine's gives p = 73.2 lbs. per square inch. itham gives.

$$A = \text{area of slides in square inches} = \frac{P}{p_0 \sqrt{n^2 - 1}} = \frac{.7864d^3p_1}{p_0 \sqrt{n^2 - 1}}$$

ich P = total unbalanced pressure, p_1 = pressure per square inch ston, d = diameter of cylinder, p_0 = pressure allowable per square inch

ston, d=0 diameter of cylinder, $p_0=$ pressure allowable per square inch ides, and n= length of connecting-rod + length of crank. This is alent to the formula, A=P tan $\theta+p_0$. For n=5, $p_1=100$ and p_0 $A=2004d^p$. For the three engines 10, 20 and 50 in. diam., this would for area of slides, A=20, 180 and 500 sq. in., respectively. Whitham The normal pressure on the slide may be as high as 500 lbs. per sq. in., his is when there is good lubrication and freedom from dust. Station-in marine engines are usually designed to carry 100 lbs. per sq. in., he area in this case is reduced from 50% to 60% by grooves. In locomognies the pressure ranges from 40 to 50 lbs. per sq. in. of slide, on act of the inaccessibility of the slide, dirt, cinder, etc.

The inaccessibility of the slide, dirt, cinder, etc.

The is perfect agreement among the authorities as to the formula for of the slides, A=P tan $\theta+p_0$; but the value given to p_0 , the allowers sure per square inch, ranges all the way from 38 lbs. to 500 lbs. to Connecting-rod. Ratio of length of connecting-rod to length observations of long the slides of the connecting-rod. Whitham gives the ratio of from 2 to 4½, farks from 2 to 4.

The slower per square form the connecting-rod.—The calculation of the diameter of

narks from 2 to 4.

nensions of the Connecting-rod.—The calculation of the diameter of necting-rod on a theoretical basis, considering it as a strut subject to compressive and bending stresses, and also to stress due to its inertia, gh-speed engines, is quite complicated. See Whitham, Steam-engine n, p. 217; Thurston, Manual of S. E., p. 100. Empirical formulas are as ver. For circular rods, largest at the middle, D = diam. of cylinder, the hof connecting-rod in inches, p = maximum steam-pressure per sq. in.

Whitham, diam. at middle, $d'' = 0.0272 \sqrt{Di \sqrt{p}}$. Whitham, diam. at necks, d'' = 1.0 to $1.1 \times diam$. of piston-rod.

Sennett, diam. at-middle, $d'' = \frac{D}{55} \sqrt{p}$. Sennett, diam. at necks, $d'' = \frac{D}{80} \sqrt{p_e}$

Marks, diam., $d'' = 0.0179D \sqrt{p}$, if diam. is greater than 1/24 length.

Marks, diam., $d'' = 0.02758 \sqrt{Dl} \sqrt{p}$ if diam. found by (5) is less than ength.

Thurston, diam. at middle, $d'' = a \sqrt{DL} \sqrt{p} + C$, D in inches, L in a = 0.15 and $C = \frac{1}{2}$ inch for fast engines, a = 0.08 and $C = \frac{3}{2}$ inch for rate speed.

Seaton says: The rod may be considered as a strut free at both ends, calculating its diameter accordingly,

diameter at middle =
$$\frac{\sqrt{R(1+4ar^2)}}{48.5}$$

e R = the total load on piston P multiplied by the secant of the maxi-1 angle of obliquity of the connecting-rod, r wrought iron and mild steel a is taken at 1/8000. The following are alues of r in practice:

val engines-Direct-acting r = 9 to 11; Return connecting-rod r = 10 to 18, old;66 r = 8 to 9, modern; Trunk r = 11.5 to 18.rcantile " Direct-acting, ordinary r = 12.

"long stroke r = 13 to 16.

The following empirical formula is given by Seaton as agreeing closely good modern practice:

imeter of connecting-rod at middle = $\sqrt{lK} + 4$, l = length of rod ins. and K = 0.08 Veffective load on piston in pounds.

The diam, at the ends may be 0.875 of the diam, at the middle. Seaton's empirical formula when translated into terms of D and p is the same as the second one by Marks, viz., $d'' = 0.02758 \sqrt{Dl} \sqrt{p}$. Whitham's

(1) is also practically the same.

(10) Taking Seaton's more complex formula, with length of connecting-rod = $2.5 \times$ length of stroke, and r = 12 and 16, respectively, it reduces to: Diam. at middle = .02294 \sqrt{P} and .02411 \sqrt{P} for short and long stroke engines, respectively.

Applying the above formulas to the engines of our list, we have

Diameter of Connecting-rods.

Diameter of Cylinder, inches	1	0	8	0	5	i0
Stroke, inches	12 80	24 60	80 75	60 150	48 120	96 240
(3) $d'' = \frac{D}{55} \sqrt{p} = .0182D \sqrt{p}$	1.82	1.82	5.46	5.46	9.09	9.09
(5) $d'' = .0179D \sqrt{p}$	1.79	 	5.87		8.95	.
(6) $\mathbf{d''} = .02758 \sqrt[4]{Dl \sqrt{p}}$:	2.14	 	5.85		9.51
(7) $d'' = 0.15 \sqrt{DL \sqrt{p}} + \frac{1}{2} \dots$	2.87	 .	7.00	 .	11.11	
(7) $d'' = 0.08 \sqrt{DL \sqrt{p}} + \frac{3}{4} \dots$		2.54	 	5.65		8.75
$(9) \ d^{\prime\prime} = .08 \ \sqrt{P}$	2.67	2.67	7.97	7.97	18.29	13.29
(10) $d'' = .02294 \sqrt{P}$; .02411 \sqrt{P}	2.03	2.14	6.09	6.41	10.16	10.68
Average	2,24	2.26	6.88	6.27	10.52	10.26

Formulæ 5 and 6 (Marks), and also formula 10 (Seaton), give the larger diameters for the long-stroke engine; formulæ 7 give the larger diameters for the short-stroke engines. The average figures show but little difference in diameter between long- and short-stroke engines; this is what might be expected, for while the connecting-rod, considered simply as a column, would require an increase of diameter for an increase of length, the load would require an increase of diameter for an increase of length, the load remaining the same, yet in an engine generally the shorter the connecting-rod the greater the number of revolutions, and consequently the greater the strains due to inertia. The influences tending to increase the diameter therefore tend to balance each other, and to render the diameter to some extent independent of the length. The average figures correspond nearly to the simple formula $d'' = .021D \ Vp$. The diameters of rod for the three diameters of engine by this formula are, respectively, 2.10, 6.30, and 10.50 in. Since the total pressure on the piston $P = .7854D^2p$, the formula is equivalent to $d' = .0237 \sqrt{P}$.

Connecting-rod Ends.—For a connecting-rod end of the marine type, where the end is secured with two bolts, each bolt should be proportioned for a safe tensile strength equal to two thirds the maximum pull or

thrust in the connecting rod.

The cap is to be proportioned as a beam loaded with the maximum pull of the connecting-rod, and supported at both ends. The calculation should or the connecting-rod, and supported at four ends. The calculation should be made for rigidity as well as strength, allowing a maximum deflection of 1/100 inch. For a strap-and-key connecting rod end the strap is designed for tensile strength, considering that two thirds of the pull on the connecting rod may come on one arm. At the point where the metal is slotted for the key and gib, the straps must be thickened to make the cross-section equal to that of the romainday of the strap. Between the and of the strap and the connection of the strap index of the strap and the strap index of the strap i Rey and gib, the straps must be thickened to make the cross-section equal to that of the remainder of the strap. Between the end of the strap and the slot the strap is liable to fail in double shear, and sufficient metal must be provided at the end to prevent such failure.

The breadth of the key is generally one fourth of the width of the strap, and the length, parallel to the strap, should be such that the cross-section will have a shearing strength equal to the tensile strength of the section of the strap. The taper of the key is generally about % inch to the foot.

*spered Connecting-rods.—In modern high-speed engines it is comary to make the connecting-rods of rectangular instead of circular ion, the sides being parallel, and the depth increasing regularly from crosshead end to the crank-pin end. According to Grashof, the bending on on the rod due to its inertia is greatest at 6/10 the length from the shead end, and, according to this theory, that is the point at which the ion should be greatest, although in practice the section is made greatest he crank-pin end.

refessor Thurston furnishes the author with the following rule for tapered necting-rod of rectangular section: Take the section as computed by the

nula $d''=0.1\sqrt[4]{DL}\sqrt[4]{p}+3/4$ for a circular section, and for a rod 4/8 the ial length, placing the computed section at 2/8 the length from the small and carrying the taper straight through this fixed section to the large. This brings the computed section at the surge point and makes it vier than the rod for which a tapered form is not required, sking the above formula, multiplying L by 4/8, and changing it to l in

ies, it becomes $d=1/30 \sqrt[4]{Dl} \sqrt{p}+3/4"$. Taking a rectangular section he same area as the round section whose diameter is d, and making the th of the section h= twice the thickness t, we have .7854 $d^3=ht=2t^3$,

nce t=.627d=.0209 $\sqrt{D}l\sqrt{p}+.47''$, which is the formula for the thick-i or distance between the parallel sides of the rod. Making the depth at crosshead end = 1.5t, and at 2/3 the length = 2t, the equivalent depth at crank end is 2.25t. Applying the formula to the short-stroke engines of examples, we have

neter of cylinder, inches	19 80	80 80 75	50 48 120
kness, $t = .0209 \sqrt{Dl \sqrt{p} + .47} =$ th at crosshead end, $1.5t =$	1.61	8.60 5.41	5.59 8.89
th at crank end, $2\frac{1}{4}t$	8.69	8.11	12.58

te thicknesses t, found by the formula $t=.0209 \sqrt{Dl \sqrt{p}}+.47$, agree sly with the more simple formula $t=.010 \sqrt{p}+.60'$, the thicknesses alated by this formula being respectively 1.6, 3.6, and 5.6 inches. He Orank-pin.—A crank-pin should be designed (1) to avoid heating, or strength, (8) for rigidity. The beating of a crank-pin depends on the sure on its rubbing-surface, and on the coefficient of friction, which r varies greatly according to the effectiveness of the lubrication. It also nds upon the facility with which the heat produced may be carried τ : thus it appears that locomotive crank-pins may be prevented to some ee from overheating by the cooling action of the air through which they at a high speed.

Marks gives
$$l = .0000247 \, fp ND^3 = 1.088 f \frac{(I.H.P.)}{L}$$
 (1)

hich l= length of crank-pin journal in inches, f= coefficient of friction, h may be taken at .08 to .05 for perfect lubrication, and .08 to .10 for imset; p= mean pressure in the cylinder in pounds per square inch; D ameter of cylinder in inches; N= number of single strokes per minute; 2. = indicated horse-power; L= length of stroke in feet. These ules are independent of the diameter of the pin, and Marks states as a ral law, within reasonable limits as to pressure and speed of rubbing, noger a bearing is made, for a given pressure and number of revolutions, socier it will work; and its diameter has no effect upon its heating, of the above formules are deduced empirically from dimensions of k-pins of existing marine engines. Marks says that about one-fourth ength required for crank-pins of propeller engines will serve for the pina le-wheel engines, and one tenth for locomotive engines, making

formula for knownotive crank-pins $l=.00000247/pND^6$, or if p=100, f=06, and N=600, $l=018D^3$.

Whitham recommends for pressure per square inch of projected area, for naval engines 500 pounds, for merchant engines 400 pounds, for paddle-wheel engines 800 to 900 pounds.

Thurston person the pressure should in the same sure of the pressure of the same sure of the same sure should be same sure of the same

bearings are used.

Thurston also says: The size of crank-pins required to prevent heating of the journals may be determined with a fair degree of precision by either of the formulæ given below:

$$l = \frac{P(V + 90)}{44,800d}$$
 (Rankine, 1865); (4)

$$l = \frac{PN}{850,000}$$
 (Van Buren, 1866). (6)

The first two formulæ give what are considered by their authors fair work-

The first two formule give what are considered by their authors fair working proportions, and the last gives minimum length for iron pins. (V = velocity of rubbing-surface in feet per minute.)

Formula (1) was obtained by observing locomotive practice in which great liability exists of annoyance by dust, and great risk occurs from inaccessibility while running, and (2) by observation of crank-pins of naval screwengines. The first formula is therefore not well suited for marine practice.

Steel can usually be worked at nearly double the pressure admissible with iron running at similar speed.

Since the length of the crank-pin will be directly as the power expended

upon it and inversely as the pressure, we may take it as

$$l = a \frac{\text{I.H.P.}}{L}, \dots, (7)$$

in which a is a constant, and L the stroke of piston, in feet. The values of the constant, as obtained by Mr. Skeel, are about as follows: a=0.04 where water can be constantly used; a=0.04 where water is not generally used; a=0.05 where water is seldom used; a=0.06 where water is never needed. Unwin gives

$$l = a \frac{\text{I.H.P.}}{r}, \dots$$
 (8)

in which r= crank radius in inches, a=0.8 to a=0.4 for fron and for marine engines, and a=0.066 to a=0.1 for the case of the best steel and for locomotive work, where it is often necessary to shorten up outside pins as much as possible.

J. B. Stanwood (Eng'g, June 12, 1891), in a table of dimensions of parts of American Corliss engines from 10 to 80 inches diameter of cylinder, gives sizes of crank-pins which approximate closely to the formula

$$l = .275D'' + .5 \text{ in.}; d = .25D''.......................(9)$$

By calculating lengths of iron crank-pins for the engines 10, 30, and 50 inches diameter, long and short stroke, by the several formulæ above given, it is found that there is a great difference in the results, so that one formulæ in certain cases gives a length three times as great as another. Nos. (4), $\langle l^* \rangle$ and (6) give lengths much greater than the others. Marks (1), Whitham (2), Thurston (7), l = 0.01 H.P. + L, and Unwin (8), l = 0.4 I.H.P. + r, give rewise which agree more closely.

The calculated lengths of iron grank-pins for the several cases by formulæ), (2), (7), and (8) are as follows:

Length of Crank-pins.

ameter of cylinder	10	10	80	80	50	50
roke		2	614	. 5	4	8
volutions per minute R		125	130	65	90	45
rse-powerI.H.P.	50	50	450	450		
iximum pressurelbs.			70,686			
an pressure per cent of max	42	42	82.5	32.8	80	30
an pressureP.	3,299	8,299	22,832	22,832	58,905	58,900
ngth of crank-pin	1					
Whitham, $l = .9075 \times .05 \text{ I.H.P.} + L.$		1.00	8.17		14.18	
Marks, $l = 1.038 \times .05 \text{ I.H.P.} + L.$	2.59	1.30	0.34		16.22	
Thurston, $l = .06$ I.H.P. $+L$	3.00	1.50	10,80	5.40	18.75	
Unwin, $l = .4$ I.H.P. $+ \gamma$		1.67	12.0	60	20.83	
" $l = .8 \text{ LH.P.} + r$	2.50	1.25	9.0	4.5	15.62	7.81
erage	2.72	1.36	9.86	4.03	17.12	8.56
Unwin, best steel, $l = .1 \frac{I.H.P.}{r} \dots$.83	.42	8.0	1.5	5.21	2.61
Thurston, steel, $l = \frac{PR}{600,000}$	1.87	.69	4.95	2.47	8.84	4.42

he calculated lengths for the long-stroke engines are too low to prevent essive pressures. See "Pressures on the Crank-pins," below.

The Strength of the Crank-pin is determined substantially as is t of the crank. In overhung cranks the load is usually assumed as ried at its extremity, and, equating its moment with that of the resister of the pin.

$$\frac{1}{2}Pl = 1/32t\pi d^3$$
, and $d = \sqrt[3]{\frac{5.1Pl}{t}}$,

which d = diameter of pm in inches, P = maximum load on the piston, the maximum allowable stress on a square inch of the metal. For iron asy be taken at 9000 lbs. For steel the diameters found by this formula r be reduced 10%. (Thurston.) pwin gives the same formula in another form, viz.;

$$d = \sqrt[4]{\frac{5.1}{t}} \sqrt[4]{P_t} = \sqrt{\frac{5.1}{t}} \sqrt{P_{d}^{t}}$$

last form to be used when the ratio of length to diameter is assumed. x wrought iron, t=6000 to 9000 los. per sq. in.,

$$\sqrt[4]{\frac{5.1}{t}} = .0947 \text{ to } .0827;$$
 $\sqrt{\frac{5.1}{t}} = .0291 \text{ to } .0238.$

or steel, t = 9000 to 18,000 lbs. per sq. in.,

$$\sqrt[3]{\frac{5.1}{t}} = .0827 \text{ to .0728}; \sqrt{\frac{5.1}{t}} = .0238 \text{ to .0194.}$$

bitham gives $d = 0.0827 \sqrt[3]{Pl} = 2.1058 \sqrt[3]{\frac{l \times LH.P.}{LR}}$ for strength, and

1.0406 $\sqrt[4]{Pis}$ for rigidity, and recommends that the diameter be calculated oth formulæ, and the largest result taken. The first is the same as in's formulæ, with t taken at 9000 lbs, per sq. in. The second is based an arbitrary assumption of a deflection of 1-300 in, at the centre of mass (one third of the length from the free end).

Marks, calculating the diameter for rigidity, gives

$$d = 0.066 \sqrt[4]{pl^3D^3} = 0.945 \sqrt[4]{\frac{(\text{H.P.})l^3}{LN}};$$

 $p=\max \max$ steam-pressure in pounds per square inch, D= diameter of cylinder in inches, L= length of stroke in feet, N= number of single strokes per minute. He says there is no need of an investigation of the strength of a crank-pin, as the condition of rigidity gives a great excess of strength. Marks's formula is based upon the assumption that the whole load may be concentrated at the outer end, and cause a deflection of .01 inch at that point.

It is serviceable, he says, for steel and for wrought iron alike. Using the average lengths of the crank-pins already found, we have the following for our six engines:

Diameter of Crank-pins.

Diameter of cylinder Stroke, ft Length of crank-pin	10 1 2.72	10 2 1.36	30 21.6 9.86	30 5 4.93	50 4 17.12	50 8 8.56
Unwin, $d = \sqrt[3]{\frac{5.1Pl}{t}}$	2.29	1.92	7.84	5.82	12.40	9.84
Marks, $d = .066 \sqrt[3]{pl^5 D^2}$	1.89	.85	6.44	8.78	18.41	7.89

Pressures on the Crank-pins.—If we take the mean pressure upon the crank-pin = mean pressure on piston, neglecting the effect of the varying angle of the connecting-rod, we have the following, using the average lengths already found, and the diameters according to Unwin and Marks:

Engine No	1.	2	8	4	5	6
Diameter of cylinder, inches	1 8,299 6.28 8.78 530	10 2 8,299 236 1.16 1,398 2,845	72.4 63.5 815	30 5 22,882 28.7 18.6 796 1,228	50 4 58,905 212.8 219.5 277 277	

The results show that the application of the formulæ for length and diam-The results show that the application of the formulae for length and utami-eter of crank-pins give quite low pressures per square inch of projected area for the short-stroke high-speed engines of the larger sizes, but too high pressures for all the other engines. It is therefore evident that after calcu-lating the dimensions of a crank-pin according to the formulae given that the results should be modified, if necessary, to bring the pressure per square inch down to a reasonable figure.

In order to bring the pressures down to 500 pounds per square inch, we divide the mean pressures by 500 to obtain the projected area, or product of length by diameter. Making l=1.5d for engines Nos. 1, 2, 4 and 6, the revised table for the six engines is as follows:

Crosshead-pin or Wrist-pin.—Whitham says the bearing surface for the wrist-pin is found by the formula for crank-pin design. Seaton says the diameter at the middle must, of course, be sufficient to withstand the bending action, and generally from this cause ample surface is provided for good working; but in any case the area, calculated by multiplying the diameter of the journal by its length, should be such that the pressure does not exceed 1200 lbs. per sq. in., taking the maximum load on the piston as the total pressure on it.

For small engines with the gudgeon shrunk into the laws of the connect-

g-rod, and working in brasses fitted into a recess in the piston-rod end and scured by a wrought-iron cap and two bolts, Seaton gives:

Diameter of gudgeon = $1.25 \times \text{diam.}$ of piston-rod. Length of gudgeon = $1.4 \times \text{diam.}$ of piston-rod.

If the pressure on the section, as calculated by multiplying length by ameter, exceeds 1200 lbs. per sq. in., this length should be increased.

J. B. Stanwood, in his "Ready Reference" book, gives for length of oshead-pin 0.25 to 0.3 diam. of piston, and diam. = 0.18 to 0.2 diam. of ston. Since he gives for diam. of piston-rod 0.14 to 0.17 diam. of piston, of diamensions for diameter and length of crosshead-pin are about 1.25 and 3 diam. of piston-rod respectively. Taking the maximum allowable presse at 1200 lbs. per sq. in. and making the length of the crosshead-pin = I of its diameter, we have $d=\sqrt{P+40}$, $l=\sqrt{P+80}$, in which $P=\max$ um total load on piston in lbs., $d=\dim$ and l=length of pin in inches. r the engines of our example we haves

ameter of piston, inches	10	80	50
ximum load on piston, lbs	7854	70,686	196,350
ameter of crosshead-pin, inches	2.22	6.65	11.08
ngth of crosshead-pin, inches	2.96	8.86	14.77
nwood's rule gives diameter, inches	1.8 to 2	5.4 to 6	9.0 to 10
nwood's rule gives length, inches	2.5 to 8	7.5 to 9	12.5 to 15
inwood's largest dimensions give pressure			
per sq. in., lbs	1809	1829	1309

ich pressures are greater than the maximum allowed by Seaton. The Crank-arm.—The crank-arm is to be treated as a lever, so that is the thickness in direction parallel to the shaft-axis and b its breadth section x inches from the crank-pin centre, then, bending moment M that section = Px, P being the thrust of the connecting-rod, and f the strain per square inch,

$$Px = \frac{fab^3}{6}$$
 and $\frac{a \times b^3}{6} = \frac{T}{f}$, or $a = \frac{6T}{b^3 \times f}$; $b = \sqrt{\frac{6T}{fa}}$.

a crank-arm were constructed so that b varied as \sqrt{x} (as given by the ve rule) it would be of such a curved form as to be inconvenient to manture, and consequently it is customary in practice to find the maxin value of b and draw tangent lines to the curve at the points; these s are generally, for the same reason, tangential to the boss of the crankat the shaft.

ie shearing strain is the same throughout the crank-arm; and, conserily, is large compared with the bending strain close to the crank-pin; so it is not sufficient to provide there only for bending strains. The ion at this point should be such that, in addition to what is given by the ulation from the bending moment, there is an extra square inch for y 8000 lbs. of thrust on the connecting rod (Seaton).

e length of the boss h into which the shaft is fitted is from 0.75 to 1.0 e diameter of the shaft D, and its thickness e must be calculated from wisting strain PL. (L = length of crank.) r different values of length of boss h, the following values of thickness

ss e are given by Seaton:

nen h = D, then e = 0.35 D; if steel, 0.3. h = 0.9 D, then e = 0.38 D, if steel, 0.32. h = 0.8 D, then e = 0.40 D, if steel, 0.38. h = 0.7 D, then e = 0.41 D, if steel, 0.34.

erank-eye or boss into which the pin is fitted should bear the same lon to the pin that the boss does to the shaft.

diameter of the shaft-end onto which the crank is fitted should be diameter of shaft.

arston says: The empirical proportions adopted by builders will comybe found to fall well within the calculated safe margin. These prons are, from the practice of successful designers, about as follows:

the wrought-iron crank, the hub is 1.75 to 1.8 times the least diameter at part of the shaft carrying full load; the eye is 2.0 to 2.25 the diametric inserted portion of the pin, and their depths are, for the hub, 1.0 the diameter of shaft, and for the eye, 1.25 to 1.5 the diameter of p The web is made 0.7 to 0.75 the width of adjacent hub or eye, and is given a depth of 0.5 to 0.6 that of adjacent hub or eye.

depth of 0.5 to 0.8 that of adjacent hub or sye.

For the east-iron crank the hub and eye are a little larger, ranging in diameter respectively from 1.8 to 2 and from 2 to 2.2 times the diameters of shaft and pin. The flanges are made at either end of nearly the full depth of hub or eye. Cast-iron has, however, fallen very generally into dispute. The crank-shaft is usually enlarged at the seat of the crank to about 1.1 its diameter at the journal. The size should be nicely adjusted to allow for the shrinkage or forcing on of the crank. A difference of diameter of one fifth of 1% will usually suffice; and a common rule of practice gives an allowance of but one half of this, or .001.

The formulæ given by different writers for crank-arms practically agree, since they all consider the crank as a beam loaded at one end and fixed the taste of the designer. Calculated dimensions for our six engines are as fol lows: lows:

Dimensions of Crank-arms.

10 24 7854 2.10	80 80 70,696 7.84	80 60 70,686 5.56	50 48 196,850	50 96 196, 8 50
7854	70,686	70,686	196,850	
				196,850
2.10	7.84	6.58		
			12.40	8.67
				1
8.46	7.70	9.70	12,55	15,82
- 1				
2.77	6.16	7.76	10.04	12.65
1.89	8.08	3.88	5.02	6.82
6.23	13.86	17.46	22.59	28.47
1.76	5.87	4.46	9.92	7.10
.88	2.94	2.23	4.46	8.55
l				
0 881	790 1/A	1 8/8 /30	9 470 999	7,871,671
0,001	100,149	1,040,408	0,910,042	1,011,011
2.60	5.78	7.28	9.41	11.87
	71.7			,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
			1	
4.55	9.54	18.0	15.7	21.0
6,493	528,635	894,428	2,484,740	1,741,625
z.06	7.81	ช.01	13.18	9.69
	1.39 3.23 1.76 .88 0,661 2.60	1.39 3.08 5.23 13.86 1.76 5.87 .88 2.94 0,661 788,149 2.00 5.78 4.55 9.54 6,493 528,635	1.39 3.08 3.88 17.46 1.76 5.87 4.46 .	1.39

The Shaft,-Twisting Resistance,-From the general formula for torsion, we have: $T = \frac{\pi}{16} d^3S = .19635 d^3S$, whence $d = \sqrt[3]{\frac{6.17}{S}}$, in which

T= torsional moment in inch-pounds, d= diameter in inches, and S= the shearing resistance of the material in pounds per square inch. If a constant force P were applied to the crank-pin tangentially to its path, the work done per minute would be

$$P \times L \times \frac{2\pi}{12} \times R = 83,000 \times LH.P.$$

in which L = length of crank in inches, and R = revs. per min, and the mean twisting moment $T = \frac{I.H.P.}{B} \times 63,025$. Therefore

$$d = \sqrt[4]{\frac{5.1T}{S}} = \sqrt[4]{\frac{321,427 \text{ I.H.P.}}{RS}}$$

is may take the form

$$d = \sqrt[4]{\frac{\text{I.H.P.}}{R} \times F}$$
, or $d = a \sqrt[4]{\frac{\text{I.H.P.}}{R}}$.

hich F and a are factors that depend on the strength of the material on the factor of safety. Taking S at 45,000 pounds per square inch for ught iron, and at 60,000 for steel, we have, for simple twisting by a unia tangential force,

tor of safety = 5 6 8 10 5 6 8 10 1ron.....
$$F = 35.7$$
 42.8 57.1 71.4 $a = 3.8$ 8.5 3.85 4.15 Steel.... $F = 36.8$ 83.1 49.8 58.5 $a = 3.0$ 3.18 3.5 3.77

awin, taking for safe working strength of wrought iron 9000 lbs., steel 0 lbs., and cast iron 4500 lbs., gives a=3.294 for wrought iron, 2.877 for 1, and 4.15 for cast iron. Thurston, for crank-axles of wrought iron, s=41.15 or more.

aton says: For wrought iron, f, the safe strain per square inch, should exceed 9000 lbs., and when the shafts are more than 10 inches diameter, lbs. Steel, when made from the ingot and of good materials, will adof a stress of 12,000 lbs. for small shafts, and 10,000 lbs. for those above iches diameter.

ne difference in the allowance between large and small shafts is to comsate for the defective material observable in the heart of large shafting, ag to the hammering failing to affect it.

ne formula
$$d = a \sqrt{\frac{\overline{1.H.P.}}{R}}$$
 assumes the tangential force to be uniform

that it is the only acting force. For engines, in which the tangential v varies with the angle between the crank and the connecting-rod, and the variation in steam-pressure in the cylinder, and also is influenced he inertia of the reciprocating parts, and in which also the shaft may be jected to bending as well as torsion, the factor a must be increased, to vide for the maximum tangential force and for bending.

eaton gives the following table showing the relation between the maxin and mean twisting moments of engines working under various condist, the momentum of the moving parts being neglected, which is allowed:

Description of Engine.	Steam Cut-off at	Max. Twist Divided by Mean Twist. Mome't	of the Ratio.
rie-crank expansive	0.2 0.4 0.6 0.8 0.2 0.8 0.4 0.5 0.6 0.7 0.8 h.p. 0.66	8.625 9.125 1.835 1.698 1.616 1.415 1.298 1.256 1.270 1.829 1.857 1.40	1.38 1.29 1.20 1.17 1.12 1.09 1.08 1.08 1.10 1.11 1.12

aton also gives the following rules for ordinary practice for ordinary-cylinder marine engines:

Diameter of the tunnel-shafts =
$$\sqrt[n]{\frac{\text{I.H.P.}}{R} \times F_1}$$
 or $a \sqrt[n]{\frac{\text{I.H.P.}}{R}}$.

Compound engines, cranks at right angles:

Boiler pressure 70 lbs., rate of expansion 6 to 7, F=70, a=4.12. Boiler pressure 80 lbs., rate of expansion 7 to 8, F=72, a=4.16. Boiler pressure 90 lbs., rate of expansion 8 to 9, F=75, a=4.22.

Triple compound, three cranks at 120 degrees:

Boiler pressure 150 lbs., rate of expansion 10 to 12, F=62, a=3 96. Boiler pressure 160 lbs., rate of expansion 11 to 13, F=64, a=4. Boiler pressure 170 lbs., rate of expansion 12 to 15, F=67, a=4.06.

Expansive engines, cranks at right angles, and the rate of expansion 5, boiler-pressure 60 lbs., F = 90, a = 4.48.

Single-crank compound engines, pressure 80 lbs., F = 96, $\alpha = 4.58$. For the engines we are considering it will be a very liberal allowance for ratio of maximum to mean twisting moment if we take it as equal to the ratio of the maximum to the mean pressure on the piston. The factor α , then, in the formula for diameter of the shaft will be multiplied by the cube

root of this ratio, or
$$\sqrt[3]{\frac{100}{42}} = 1.34$$
, $\sqrt[3]{\frac{100}{32.3}} = 1.45$, and $\sqrt[3]{\frac{100}{30}} = 1.49$ for the

10, 30, and 50-in. engines, respectively. Taking $\alpha=3.5$, which corresponds to a shearing strength of 60,000 and a factor of safety of 8 for steel, or to 65,000 and a factor of 6 for iron, we have for the new coefficient a_1 in the

formula $d_1 = a_1 \sqrt[4]{\frac{\overline{1.H.P.}}{R}}$, the values 4.69, 5.08, and 5.22, from which we

obtain the diameters of shafts of the six engines as follows:

These diameters are calculated for twisting only. When the shaft is also

subjected to bending strain the calculation must be modified as below: **Resistance to Bending.**—The strength of a circular-section shaft to resist bending is one half of that to resist twisting. If B is the bending moment in inch-lbs., and d the diameter of the shaft in inches,

$$B = \frac{\pi d^3}{32} \times f$$
; and $d = \sqrt[3]{\frac{B}{f} \times 10.2}$;

f is the safe strain per square inch of the material of which the shaft is

composed, and its value may be taken as given above for twisting (Seaton). **Equivalent Twisting Moment.**—When a shaft is subject to both twisting and bending simultaneously, the combined strain on any section of it may be measured by calculating what is called the *equivalent* twisting moment; that is, the two strains are so combined as to be treated as a twisting strain only of the same magnitude and the size of shaft calculated accordingly. Rankine gave the following solution of the combined action of the two strains.

If T = the twisting moment, and B = the bending moment on a section of

a shaft, then the equivalent twisting moment $T_1=B+\sqrt{B^2+T^2}$. Seaton says: Crank-shafts are subject always to twisting, be ording, and shearing strains; the latter are so small compared with the former that they are usually neglected directly, but allowed for indirectly by means of the factor f.

The two principal strains vary throughout the revolution, and the maximum equivalent twisting moment can only be obtained accurately by a series of calculations of bending and twisting moments taken at fixed intervals, and from them constructing a curve of strains.

Considering the engines of our examples to have overhung cranks, the maximum bending moment resulting from the thrust of the connecting rod on the crank-pin will take place when the engine is passing its centres (neglecting the effect of the inertia of the reciprocating parts), and it will be the product of the total pressure on the piston by the distance between parallel lines passing through the centres of the crank-pin and of the ift bearing, at right angles to their axes; which distance is equal to ength of crank-pin bearing + length of hub + ½ length of shaft-bearing + y clearance that may be allowed between the crank and the two bearings, rour six engines we may take this distance as equal to ½ length of ink-pin + thickness of crank-arm + 1.5 × the diameter of the shaft as eady found by the calculation for twisting. The calculation of diameter then as below:

Engine No.	1	2	8	4	5	6
am. of cyl., in orse-power vs. per min	10 50 250	10 50 125	30 450 180	30 450 65	50 1250 90	50 1250 45
verage,* Lin	7,854 6.32	7,854 7,94 62,361 94,248	70,686 22,20 1,569,222 1,060,290	70,686 26.00 1,887,886 2,120,580	196,350 36.80 7,225,680 4,712,400	196,350 42.25 8,295,788
uiv.Twist. mom. $I_1 = B + \sqrt{B^2 + T^2}$ approx.)	,	,			15,840,000	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,

^{&#}x27;Leverage = distance between centres of crank-pin and shaft bearing = 1+2.25d.

Having already found the diameters, on the assumption that the shafts are subjected to a twisting moment T only, we may find the diameter for sisting combined bending and twisting by multiplying the diameters ready found by the cube roots of the ratio $T_1 + T$, or

ving corrected diameters $d_1 = \dots 3.84$ 1.27 1.46 1.34 1.64 1.36 ving corrected diameters $d_2 = \dots 3.84$ 4.39 11.35 12.99 20.58 21.52

By plotting these results, using the diameters of the cylinders for abscissas d diameters of the shafts for ordinates, we find that for the long-stroke gines the results lie almost in a straight line expressed by the formula, ameter of shaft = .43 × diameter of cylinder; for the short-stroke engines e line is slightly curved, but does not diverge far from a straight line nose equation is, diameter of shaft = .4 diameter of cylinder. Using these of formulas, the diameters of the shafts will be 4.0, 4.3, 12.0, 12.9, 20.0, 21.5, J.B. Stanwood, in Engineering, June 12, 1891, gives dimensions of shafts Corliss engines in American practice for cylinders 10 to 30 in. diameter, le diameters range from 4 15/16 to 14 15/16, following precisely the equation, ameter of shaft = $\frac{1}{2}$ diameter of cylinder - $\frac{1}{2}$ (16 inch.

ameter of shaft= ¼ diameter of cylinder - 1/16 inch.

Fly-wheel Shafts.—Thus far we have considered the shaft as resist ghe force of torsion and the bending moment produced by the pressure i the crank-pin. In the case of fly-wheel engines the shaft on the opposite of the bearing from the crank-pin has to be designed with reference to bending moment caused by the weight of the fly-wheel, the weight of e shaft itself, and the strain of the belt. For engines in which there is an itboard bearing, the weight of fly-wheel and shaft being supported by to bearings, the point of the shaft at which the bending moment is a aximum may be taken as the point midway between the two bearings or the middle of the fly-wheel hub, and the amount of the moment is the oduct of the weight supported by one of the bearings into the distance om the centre of that bearing to the middle point of the shaft. The shaft thus to be treated as a beam supported at the ends and loaded in the iddle. In the case of an overhung fly-wheel, the shaft having only one aring, the point of maximum moment should be taken as the middle of the bearing, and its amount is very nearly the product of half the weight the fly-wheel and the shaft into the distance from the middle of its hub om the middle of the bearing. The bending moment should be calculated ad combined with the twisting moment as above shown, to obtain the juivalent twisting moment, and the diameter necessary at the point of aximum moment calculated therefrom.

In the case of our six engines we assume that the weights of the fly-heels, together with the shaft, are double the weight of fly-wheel rim $\frac{d^3s}{dt^2}$

btained from the formula, $W = 785,400 \frac{a \cdot s}{D2.772}$ (given under Fly-wheels):

that the shaft is supported by an outboard bearing, the distance between the two bearings being 2½, 5, and 10 feet for the 10-in., 30-in., and 50-in. engines, respectively. The diameters of the fly-wheels are taken such that their rim velocity will be a little less than 6000 feet per minute.

Engine No	1	2	3	4	5	6
Diam. of cyl., inches	10	10	30	30	50	50
Diam. of fly-wheel, ft	7.5	15	14.5	29	21	42
Revs. per min		125	130	65	90	45
Half wt fly-wh'l and shaft, lb.	268	536	5,968	11,986	26,384	52,709
Lever arm for max.mom.,in.	15	15	30	90	60	60
Max. bending moment, in. lb.	4020	8040	179,040	358,080	1.583,070	8,168,140

As these are very much less than the bending moments calculated from the pressures on the crank-pin, the diameters already found are sufficient for the diameter of the shaft at the fly wheel hub.

In the case of engines with heavy band fly-wheels and with long fly-wheel shafts it is of the utmost importance to calculate the diameter of the shaft with reference to the bending moment due to the weight of the fly-wheel and the shaft.

B. H. Coffey (Power. October, 1892) gives the formula for combined bending and twisting resistance, $T_1=196d^3S$, in which $T_1=B+\sqrt{B^2+T^2}$, the maximum not the mean twisting moment; and finds empirical working values for .196S as below. He says: Four points should be considered in determining this value: First, the nature of the material; second, the manner of applying the loads, with shock or otherwise; third, the ratio of the bending moment to the torsional moment—the bending moment in a revolving shaft produces reversed strains in the material, which tend to rupture it; fourth, the size of the section. Inch for Inch. large sections are weaker than small ones. He puts the dividing line between large and small sections at 10 in. diameter, and gives the following safe values of $S \times .196$ for steel, wrought iron, and cast iron, for these conditions.

Value of $S \times .196$.

Ratio.				Shock. Heavy			ht Shefts Shock.		
B to T.	Steel.	Wro't Iron.	Cast Iron.	Steel.	Wro't Iron.		Steel.	Wro't Iron.	
8 to 10 or less 8 to 5 or less 1 to 1 or less B greater than T	1045 941 855 784	880 785 715 655	440 398 858 838	1566 1410 1281 1176	1820 1179 1074 984	660 589 537 498	2090 1882 1710 1568	1760 1570 1480 1810	880 785 715 655

Mr. Coffey gives as an example of improper dimensions the fly-wheel shaft of a 1500 H.P. engine at Williamntic, Conn., which broke while the engine was running at 425 H.P. The shaft was 17 ft. 5 in. long between centres of bearings, 18 in. diam, for 8 ft. in the middle, and 15 in. diam, for the remainder, including the bearings. It broke at the base of the fillet connecting the two large diameters, or 564 in from the centre of the bearing. He calculates the mean torsional moment to be 446,654 inch-pounds, and the maximum at twice the mean; and the total weight on one bearing at 87,530 lbs., which, multiplied by 56½ in., gives 4,945,445 in.-lbs. bending moment at the fillet. Applying the formula $T_1 = B + \sqrt{B^2 + T^2}$, gives for equivalent twisting moment 9,971,045 in.-lbs. Substituting this value in the formula $T_1 = 196$, S63 gives for S the shearing strain 15,070 lbs. per sq. in., or if the metal had a shearing strength of 45,000 lbs., a factor of safety of only 3 Mr. Coffey considers that 600 lbs. is all that should be allowed for S under these circumstances. This would give d = 20.85 in. If we take from Mr. Coffey's table a value of .196S = 1100, we obtain $d^2 = 9000$ nearly, or d = 20.8 in. in the actual diameter.

Longth of Shaft-bearings.—There is as great a difference of opinion among writers, and as great a variation in practice concerning length of a journal-bearings, as there is concerning crank-pins. The length of a

urnal being determined from considerations of its heating, the observaons concerning heating of crank-pins apply also to shaft-bearings, and the rmulæ for length of crank-pins to avoid heating may also be used, using the total load upon the bearing the resultant of all the pressures brought r the total load upon the bearing the resultant of all the pressures brought on it, by the pressure on the crank, by the weight of the fly-wheel, and by it pull of the belt. After determining this pressure, however, we must sort to empirical values for the so-called constants of the formulæ, really raiables, which depend on the power of the bearing to carry away heat, ind upon the quantity of heat generated, which latter depends on the preserve, on the number of square feet of rubbing surface passed over in a inuite, and upon the coefficient of friction. This coefficient is an exceedigly variable quantity, ranging from .01 or less with perfectly polished urmals, having end-play, and lubricated by a pad or off-bath, to .100 more ith ordinary off-cup lubrication.

For shafts resisting torsion only. Marks gives for length of bearing length of bearing length of the control of the co

For shafts resisting torsion only, Marks gives for length of bearing $l=000247fpND^2$, in which f is the coefficient of friction, p the mean pressure i pounds per square inch on the piston. N the number of single strokes per tinute, and D the diameter of the piston. For shafts under the combined ress due to pressure on the crank-pin, weight of fly-wheel, etc., he gives to following: Let Q = reaction at bearing due to weight, B = stress due eam pressure on piston, and B_1 = the resultant force; for horizontal engines, $R_1 = \sqrt{Q^2 + S^2}$, for vertical engines $R_1 = Q + S$, when the pressure on the rank is in the same direction as the pressure of the shaft on its bearings at $R_1 = Q - S$ when the steam pressure tends to lift the shaft from its earings. Using empirical values for the work of friction per square inch the triple of the projected area, taken from dimensions of crank-pins in marine vessels, e finds the formula for length of shaft-journals $l = .0000325/R_1N$, and secommends that to cover the defects of workmanship, neglect of oiling, and the introduction of dust, f be taken at .16 or even greater. He says hat 500 lbs. per sq. in, of projected area may be allowed for steel or wroughtnown that in brass bearings with good results if a less pressure is not attainble without inconvenience. Marks says that the use of empirical rules that not take account of the number of turns per minute hear resulted in hearo not take account of the number of turns per minute has resulted in bearags much too long for slow-speed engines and too short for high-speed ngines.

Whitham gives the same formula, with the coefficient .00002575.

Thurston says that the maximum allowable mean intensity of pressure may be, for all cases, computed by his formula for journals, l =60,000d, or

by Rankine's, $l = \frac{P(V+20)}{44,800d}$, in which P is the mean total pressure in pounds, 7 the velocity of rubbing surface in feet per minute, and d the diameter of he shaft in inches. It must be borne in mind, he says, that the friction work on the main bearing next the crank is the sum of that due the action of the iston on the pin, and that due that portion of the weight of wheel and haft and of pull of the belt which is carried there. The outboard bearing sarries practically only the latter two parts of the total. The crank-shaft curnals will be made longer on one side, and perhaps shorter on the other, han that of the crank-pin, in proportion to the work falling upon each, i.e., o their respective products of mean total pressure, speed of rubbing surless and coefficients of fairly the contract of the crank-pin. aces, and coefficients of friction.

Unwin says: Journals running at 150 revolutions per minute are often partially one diameter long. Fan shafts running 150 revolutions per minute have plurnals six or eight diameters long. The ordinary empirical mode of proportioning the length of journals is to make the length proportional to the liameter, and to make the ratio of length to diameter increase with the

speed. For wrought-iron journals:

Revs. per min. = 50 100 150 200 250 500 1000
$$\frac{l}{d}$$
 = .004R + 1.
Length + diam. = 1.2 1.4 1.6 1.8 2.0 3.0 5.0.

Cast-iron journals may have l + d = 9/10, and steel journals l + d = 11/4. of the above values.

Unwin gives the following, calculated from the formula $l = \frac{0.4 \text{ H.P.}}{r}$, in which r is the crank radius in inches, and H.P. the horse-power transmitted to the grank-pin.

THEORETICAL JOURNAL LENGTH IN INCHES.

Load on Journal	Revolutions of Journal per minute.								
in pounds.	50	100	200	300	500	1000			
1,000 2,000	.2 .4 .8	.4 .8	.8 1.6	1.2	2. 4. 8.	4. 8.			
4,000 5,000	1.0	1.6 2.	8.2 4. 8.	4.8 6.	10.	16. 20.			
10,000 15,000 20,000	2. 8.	4. 6. 8.	8. 12. 16.	12. 18. 24.	20. 30. 40.	40.			
80,000 40,000	4. 6. 8.	12. 16.	24. 82.	36.	••••				
50,000	10.	20.	40.	••••					

Applying these different formluæ to our six engines, we have:

Engine No	1	2	8	4	5	6
Diam, cyl	10	10	80	80	50	50
Revs. per min	50 250	50 125	450 130	450 65	1,250 90	1,250 45
Mean pressure on crank-pin = S		8,299	23,185			
Half wt. of fly-wheel and shaft $= Q$ Resultant press. on bearing	268	536	5,968	11,986	26,470	
$\sqrt{Q^2 + S^2} = R_1.$	3,810	3,835	23,924	26,194	64,580	79,200
Diam. of shaft journal	8.84	4.89	11.85	12.99	20.58	21.52
Marks, $l = .0000325 fR_1 N (f=.10)$	5.38	2.71	20.87	11.07	87.78	28.17
Whitham, $l = .0000515fR_1R(f=10)$.	4.27	2.15	16.53	8.77	29.95	18.85
Thurston, $l = \frac{PV}{60,000d}$	8.61	1.82	14.00	7.48	25.86	15.55
Rankine, $l = \frac{P(V+20)}{44,800d}$	5.22	2.78	21.70	10.85	85.16	22.47
Unwin, $l = (.004R + 1)d$	7.68	6.59	17.25	16.36	27.99	25.39
Unwin, $l = \frac{0.4 \text{ H.P.}}{r}$	8.33	1.60	12.00	ı)	1
Average	4.92	2.99	17.05	10.00	29.54	19.22

If we divide the mean resultant pressure on the bearing by the projected area, that is, by the product of the diameter and length of the journal, using the greatest and smallest length out of the seven lengths for each journal given above, we obtain the pressure per square inch upon the bearing, as follows:

Engine No	1	2	8	4	5	6
Pressure per sq. in., shortest journal. Longest journal. Average journal Journal of length = diam	112 175	455 115 254	176 97 124	886 128 202 155	151 83 106	858 145 191 175

Many of the formulæ give for the long-stroke engines a length of journal less than the diameter, but such short journals are rarely used in practice, The last line in the above table has been calculated on the supposition that

e journals of the long-stroke engines are made of a length equal to the

In the dimensions of Corliss engines given by J. B. Stanwood (Eng., June 1891), the lengths of the journals for engines of diam. of cyl. 10 to 20 in. e the same as the diam. of the cylinder, and a little more than twice the am. of the journal. For engines above 20 in diam. of cyl. the ratio of gylt to diam. is decreased so that an engine of 30 in. diam. has a journal in long, its diameter being 144\forall in. These lengths of journal are greater an those given by any of the formulæ above quoted.

There thus appears to be a hopeless confusion in the various formulæ for

There thus appears to be a hopeless confusion in the various formulæ for 19th of shaft journals, but this is no more than is to be expected from the riation in the coefficient of friction, and in the heat-conducting power of 19th in actual use, the coefficient varying from .10 (or even .16 as given Marks) down to .01, according to the condition of the bearing surfaces

d the efficiency of lubrication. Thurston's formula, $l = \frac{PV}{60,000d}$, reduces to

e form l=.00004363PR, in which P= mean total load on journal, and = revolutions per ninute. This is of the same form as Marks' and hitham's formulae, in which, if f the coefficient of friction be taken at .10, a coefficients of PR are, respectively, .000065 and .0000615. Taking the san of these three formulae, we have l=.0000053PR, if f=.10 or l=.0053PR for any other value of f. The author believes this to be as safe ormula as any for length of journal, with the limitation that if it brings esuit of length of journal less than the diameter, then the length should made equal to the diameter. Whenever with f=.10 it gives a length ich is inconvenient or impossible of construction on account of limited ace, then provision should be made to reduce the value of the coefficient friction below .10 by means of forced lubrication, end play, etc., and to rry away the heat, as by water-cooled journal-boxes. The value of P build be taken as the resultant of the mean pressure on the crank, and the A brought on the bearing by the weight of the shaft, fly-wheel, etc., as culated by the formula already given, viz., $R_1 = \sqrt{Q^2 + S^2}$ for horizontal sines, and $R_1 = Q + S$ for vertical engines.

for our six engines the formula l = .0000083PR gives, with the limitation the long-stroke engines that the length shall not be less than the diamr, the following:

rank - shafts with Centro-crank and Double-crank ms_* —In centre-crank engines, one of the crank-arms, and its adjoining rnal, called the after journal, usually transmit the power of the engine he work to be done, and the journal resists both twisting and bending ments, while the other journal is subjected to bending moment only: the after crank-journal the diameter should be calculated the same as an overhung crank, using the formula for combined bending and twistmoment, $T_1 = B + \sqrt{B^2 + T^2}$, in which T_1 is the equivalent twisting ment, B the bending moment, and T the twisting moment. This value

 T_1 is to be used in the formula diameter = $\sqrt[3]{\frac{5.1T}{8}}$. The bending mo-

nt is taken as the maximum load on piston multiplied by one fourth of length of the crank-shaft between middle points of the two journal length of the crank-shaft between middle points of the two journal length of the centre crank is midway between the bearings, or by one of the distance measured parallel to the shaft from the middle of the nk-pin to the middle of the after bearing. This supposes the crankfit to be a beam loaded at its middle and supported at the ends, but itham would make the bending moment only one half of this, considerable and to be a beam secured or fixed at the ends, with a point of conflexure one fourth of the length from the end. The first supposition is safer, but since the bending moment will in any case be much less than twisting moment, the resulting diameter will be but little greater than whitham's supposition is used. For the forward journal, which is sub-

ted to bending moment only, diameter of shaft = $\sqrt[3]{\frac{10.2B}{B}}$, in which B

is the maximum bending moment and $\mathcal B$ the safe shearing strength of the metal per square inch.

For our six engines, assuming them to be centre-crank engines, and considering the crank-shaft to be a beam supported at the ends and loaded in the middle, and assuming lengths between centres of shaft bearings as given below, we have:

Engine No	1	9	8	4	6	0
Length of shaft, assumed, inches, L	20 7,854	24 7,854	48 70,696	60 70,686	76 196,850	96 196,350
$B = \frac{1}{4}PL$, inch-lbs Twisting moment, T Equiv. twisting moment,	39,270 47,124	49,637 94,248	848,232 1,060,290	1,060,290 2,120,580	3,729,750 4,712,400	4,712,400 9,4 24,800
$B + \sqrt{B^2 + T^2}$	101, 0 00	156,000	2,208,000	8,430,000	9,740,000	15,240,000
$d = \sqrt[8]{\frac{5.1T_1}{8000}}$	8.98	4.60	11.15	18.00	18.25	21.90
Diam. of forward journal, $d_1 = \sqrt[3]{\frac{10.2B}{8000}} \dots$	8.68	8.99	10.28	11.16	16.82	18.18

The lengths of the journals would be calculated in the same manner as in the case of overhung cranks, by the formula $l \approx .000089/PR$, in which P is the resultant of the mean pressure due to pressure of steam on the pistors, and the load of the fly-wheel, shaft, etc., on each of the two bearings. Unless the pressures are equally divided between the two bearings. Unless the pressures are equally divided between the two bearings, the calculated lengths of the two will be different; but it is usually enstomary to make them both of the same length, and in no case to make the length less than the diameter. The diameters also are usually made alike for the two journals, using the largest diameter found by calculation.

calculated lengths of the two will be different; but it is usually customary to make them both of the same length, and in no case to make the length less than the diameter. The diameters also are usually made alike for the two journals, using the largest diameter found by calculation. The crank-pin for a centre crank should be of the same length as for an overhung crank, since the length is determined from considerations of heating, and not of strength. The diameter also will usually be the same, since it is made great enough to make the pressure per square inch on the projected area (product of length by diameter) small enough to allow of free lubrication, and the diameter so calculated will be greater than is re-

quired for strength.

Orank-shaft with Two Cranks coupled at 90°.—If the whole power of the engine is transmitted through the after journal of the after crank-shaft, the greatest twisting moment is equal to 1.414 times the maximum twisting moment due to the pressure on one of the crank-pins. If T = the maximum twisting moment produced by the steam-pressure on one of the pistons, then T_1 the maximum twisting moment on the after part of the crank-shaft, and on the line-shaft, produced when each crank makes an angle of 45° with the centre line of the engine, is 1.4147. Substituting this value in the formula for diameter to resist simple torsion, via. d =

$$\sqrt[3]{\frac{5.1T}{S}}$$
, we have $d = \sqrt[3]{\frac{5.1 \times 1.414T}{S}}$, or $d = 1.932 \sqrt[3]{\frac{T}{S}}$, in which T is

the maximum twisting moment produced by one of the pistons, d = diam eter in inches, and S = safe working shearing strength of the material. For the forward journal of the after crank, and the after journal of the forward crank, the torsional moment is that due to the pressure of steam on the forward piston only, and for the forward journal of the forward crank, if none of the power of the engine is transmitted through it, the torsional moment is zero, and its diameter is to be calculated for bending moment only.

moment only. For Combined Torsion and Flexure.—Let $B_1 =$ bending moment on either journal of the forward crank due to maximum pressure on

rward piston, $B_2 =$ bending moment on either journal of the after crank is to maximum pressure on after piston, $T_1 = \max_i \min m$ twisting moments after journal of forward orank, and $T_1 = \max_i \min m$ twisting moment on ter journal of after crank due to pressure on the after piston.

Then equivalent twisting moment on after journal of forward crank = B_1

 $\sqrt{B_1^3 + T_1^3}$

On forward journal of after crank = $B_2 + \sqrt{B_2^2 + T_1^2}$. On after journal of after crank = $B_0 + \sqrt{B_0^2 + (T_1 + T_2)^2}$.

These values of equivalent twisting moment are to be used in the formula

r diameter of journals $d = \sqrt[3]{\frac{5.1T}{8}}$. For the forward journal of the

rward orank-shaft $d = \sqrt[8]{\frac{10.2B_1}{S}}$.

It is customary to make the two journals of the forward crank of one ameter, viz., that calculated for the after journal.

For a Three-cylinder Engine with cranks at 120°, the greatest risting moment on the after part of the shaft, if the maximum pressures the three pistons are equal, is equal to twice the maximum pressure on yo one piston, and it takes place when two of the cranks make angles of with the centre line, the third crank being at right angles to it. (For densitration, see Whitham's "Steam-engine Design," p. 522.) For combined rision and flexure the same method as above given for two crank engines adopted for the first two cranks; and for the third, or after crank, if all e power of the three cylinders is transmitted through it, we have the e power of the three cylinders is transmitted through it, we have the uivalent twisting moment on the forward journal = $B_2 + \sqrt{B_3^2 + (T_1 + T_2)^2}$, and on the after journal = $B_2 + \sqrt{B_3^2 + (T_1 + T_2 + T_2)^2}$, B_3 and T_3 being spectively the bending and twisting moments due to the pressure on the ird piston.

ird piston.

Crank - shafts for Triple-expansion Marine Engines, cording to an article in The Engineer, April 25, 1890, should be made rger than the formulæ would call for, in order to provide for the stresses ie to the racing of the propeller in a sea-way, which can scarcely be callated. A kind of unwritten law has sprung up for fixing the size of a ank-shaft, according to which the diameter of the shaft is made about 45D, where D is the diameter of the high-pressure cylinder. This is for lid shafts. When the speeds are high, as in war-ships, and the stroke ort, the formula becomes 0.4D, even for hollow shafts.

The Valve-sterm or Valve-rod...The valve-rod should be designed move the valve under the most unfavorable conditions, which are when

The Valve-stem of Valve-rod...-The valve-rod should be designed move the valve under the most unfavorable conditions, which are when e stem acts by thrusting, as a long column, when the valve is unbalanced balanced valve may become unbalanced by the joint leaking) and when it imperfectly lubricated. The load on the valve is the product of the area to the greatest unbalanced pressure upon it per square inch, and the colicient of friction may be as high as 20%. The product of this coefficient d the load is the force necessary to move the valve, which equals the aximum thrust on the valve-rod. From this force the diameter of the live-rod may be calculated by Hodgkinson's formula for columns. An

ipirical formula given by Seaton is: Diam. of rod = $d = \sqrt{\frac{lbp}{E}}$, in which

: length and b = breadth of valve, in inches; p = maximum absolute essure on the valve in lbs. per sq. in., and F a coefficient whose values are, iron: long rod 10,000, short 12,000; for steel: long rod 12,000, short 14,500. Whitham gives the short empirical rule: Diam. of valve-rod = 1/30 diam. cyl. = $\frac{1}{2}$ diam. of piston-rod.

$$D = \sqrt{\frac{lbp}{12,000}};$$

en Diameter of block-pin when overhung = D,

secured at both ends = 0.75 × D,

secured at both ends = 0.75 × D,

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secured ends = 0.75 × D,

secured ends = 0.75 × eccentric-rod pins
suspension-rod pins
pin when overhung = 0.55 ×

. 2

= 0.8 to $0.9 \times D$. = 1.8 to $1.6 \times D$. = $0.7 \times D$. Breadth of link Length of block Thickness of bars of link at middle

If a single suspension rod of round section, its diameter = $0.7 \times D$. If two suspension rods of round section, their diameter = $0.55 \times D$.

Size of Double-bar Links.—When the distance between centres of eccentric pins = 6 to 8 times throw of eccentrics (throw = eccentricity = half-travel of valve.at full gear) D as before:

Depth of bars $\begin{array}{ll} = 1.25 \times D + \% \text{ in.} \\ = 0.5 \times D + 14 \text{ in.} \\ = 0.5 \times D + 14 \text{ in.} \\ \text{Length of sliding-block} \\ = 2.5 \text{ to } 3 \times D. \\ \text{Diameter of eccentric-rod pins} \\ = 0.8 \times D + 14 \text{ in.} \\ \text{centre of sliding-block} \\ = 1.3 \times D. \end{array}$

When the distance between eccentric-rod pins = 5 to 51/4 times throw of eccentrics:

Depth of bars Thickness of bars Length of sliding-block = $1.25 \times D + \frac{1}{16}$ in. = $0.5 \times D + \frac{1}{16}$ in. = 2.5 to $3 \times D$. Diameter of eccentric-rod pins = $0.75 \times D$.

Diameter of eccentric bolts (top end) at bottom of thread = $0.42 \times D$ when

If Iron, and 0.38 × D when of steel.

The Eccentric.—Diam. of eccentric-sheave = 2.4 × throw of eccentric + 1.2 × diam. of shaft. D as before

Breadth of the sheave at the shaft $= 1.15 \times D + 0.65 \text{ inch}$ Breadth of the sheave at the strap = D + 0.6 linch. Thickness of metal around the shaft $= 0.7 \times D + 0.5 \text{ inch}.$ Thickness of metal at circumference $= 0.6 \times D + 0.4 \text{ inch}.$ Breadth of key $= 0.7 \times D + 0.5 \text{ inch}.$ Thickness of key $= 0.25 \times D + 0.5 \text{ inch}.$ Diameter of bolts connecting parts of strap $= 0.6 \times D + 0.1 \text{ inch}.$

THICKNESS OF ECCENTRIC-STRAP.

When of bronze or malleable cast iron:

Thickness of eccentric-strap at the middle..... = $0.4 \times D + 0.6$ inch. """ sides..... = $0.3 \times D + 0.5$ inch.

When of wrought iron or cast steel:

Thickness of eccentric strap at the middle = $0.4 \times D + 0.5$ inch.

""" sides = $0.27 \times D + 0.4$ inch

The Eccentric-rod.—The diameter of the eccentric-rod in the body and at the eccentric end may be calculated in the same way as that of the connecting-rod, the length being taken from centre of strap to centre of pin. Diameter at the link end = 0.8D + 0.2 inch.

This is for wrought-iron; no reduction in size should be made for steel.

Eccentric-rods are often made of rectangular section.

Beversing-gear should be so designed as to have more than sufficient strength to withstand the strain of both the valves and their gear at the same time under the most unfavorable circumstances; it will then have the

stiffness requisite for good working.

Assuming the work done in reversing the link-motion, W, to be only that due to overcoming the friction of the valves themselves through their whole travel, then, if T be the travel of valves in inches; for a compound engine

$$W = \frac{T}{12} \left(\frac{l \times b \times p}{5} \right) + \frac{T}{12} \left(\frac{l^1 \times b^1 \times p^1}{5} \right);$$

 l^1 , b^1 and p^1 being length, breadth and maximum steam-pressur; on valve of the second cylinder; and for an expansive engine

$$W = 2 \times \frac{T}{12} \left(\frac{l \times b \times p}{5} \right)$$
; or $\frac{T}{30} (l \times b \times p)$.

To provide for the friction of link-motion, eccentrics and other gear, and for abnormal conditions of the same, take the work at one and a half times the above amount.

o find the strain at any part of the gear having motion when reversing, ide the work so found by the space moved through by that part in feet; quotient is the strain in pounds; and the size may be found from the inary rules of construction for any of the parts of the gear. (Seaton.) ingine-frames or Bed-plates.—No definite rules for the design signe-frames have been given by authors of works on the steam-engine. Proportions are left to the designer who uses "rule of thumb," or ies from existing engines. F. A. Halsey (Am. Mach., Feb. 14, 1895) has de a comparison of proportions of the frames of horizontal Corliss ines of several builders. The method of comparison is to compute from measurements the number of square inches in the smallest cross-sector of the frame, that is, immediately behind the pillow-block, also to pute the total maximum pressure upon the piston, and to divide the er quantity by the former. The result gives the number of pounds sure upon the piston allowed for each square inch of metal in the ne. He finds that the number of pounds per square inch of smallest on of frame ranges from 217 for a 10 × 30-in. engine up to 575 for a $\langle 48\text{-inch}. A 80 \times 60\text{-inch}$ engine shows 350 lbs., and a 32-inch engine thas been running for many years shows 657 lbs. Generally the ins increase with the size of the engine, and more cross-section of metal lowed with relatively long strokes than with short ones.

com the above Mr. Halsey formulates the general rule that in engines noderate speed, and having strokes up to one and one-half times the neter of the cylinder, the load per square inch of smallest section ild be for a 10-inch engine 300 pounds, which figure should be increased larger bores up to 500 pounds for a 30-inch cylinder of same relative ke. For high speeds or for longer strokes the load per square inch all he reduced per square inch.

ild be reduced.

FLY-WHEELS.

ie function of a fly-wheel is to store up and to restore the periodical flucions of energy given to or taken from an engine or machine, and thus see approximately constant the velocity of rotation. Rankine calls the ΔR

tity $\frac{\Delta E}{2E_0}$ the coefficient of fluctuation of speed or of unsteadiness, in in E_0 is the mean actual energy, and ΔE the excess of energy received or ork performed, above the mean, during a given interval. The ratio of erriodical excess or deficiency of energy ΔE to the whole energy exerted e period or revolution General Morin found to be from 1/6 to ½ for e-cylinder engines using expansion; the shorter the cut-off the higher alue. For a pair of engines with cranks coupled at 90° the value of the is about ½, and for three engines with cranks at 120°, 1/12 of its value ingle-cylinder engines. For tools working at intervals, such as punch-lotting and plate-cutting machines, coning-presses, etc., ΔE is nearly 1 to the whole work performed at each operation.

ly-wheel reduces the coefficient $\frac{\Delta E}{2E_0}$ to a certain fixed amount, being t 1/82 for ordinary machinery, and 1/50 or 1/60 for machinery for fine 38es.

n be the reciprocal of the intended value of the coefficient of fluctuaif speed, ΔE the fluctuation or energy, I the moment of inertia of the heel alone, and a_0 its mean angular velocity, $I = \frac{mg\Delta E}{2}$. As the rim of

wheel is usually heavy in comparison with the arms, I may be taken all Wr^2 , in which W= weight of rim in pounds, and r the radius of the ; then $W=\frac{mg\Delta E}{a_0^2r^2}=\frac{mg\Delta E}{v^2}$, if v be the velocity of the rim in feet per

1. The usual mean radius of the fly-wheel in steam-engines is from to five times the length of the crank. The ordinary values of the prod g, the unit of time being the second, lie between 1000 and 2000 feet. igod from Rankine, S E. p. 62.)

riston gives for engines with automatic valve-gear W = 250,000in which A =area of piston in square inches, S =stroke in feet, p =

steam-pressure in lbs. per sq. in., R = revolutions per minute, D = out ameter of wheel in feet. Thurston also gives for ordinary forms of

non-condensing engine with a ratio of expansion between 8 and 5, W= $\frac{a}{R^2D^3}$, in which a ranges from 10,000,000 to 15,000,000, averaging 12,000,000. For gas-engines, in which the charge is fired with every revolution, the Amerioan Machinist gives this latter formula, with a doubled, or 24,000,000. Presumably, if the charge is fired every other revolution, a should be again doubled.

Rankine ("Useful Rules and Tables," p. 247) gives $W = 475,000 \frac{4 \text{Sp}}{VD^2 E^2}$, in

which V is the variation of speed per cent. of the mean speed. There is first rule above given corresponds with this if we take V at 1.9 per cent. Hartnell (Proc. Inst., M. E. 1882, 427) says; The value of V, or the variation permissible in portable engines, should not exceed 8 per cent. with an ordinary load, and 4 per cent when heavily loaded. In fixed engines, or crimary purposes, V = 294, to 8 per cent. For good governing or special purposes, such as cotton-spinning, the variation should not exceed 1% to 8 per cent.

F. M. Rites (Trans. A. S. M. E., xiv. 100) develops a new formula for weight of rim, viz., $W = \frac{C \times I.H.P.}{R^3D^3}$, and weight of rim per borse-power = $\frac{C}{R^3D^3}$, in which C varies from 10,000,000,000 to 20,000,000,000; also using the latter value of C, he obtains for the energy of the fly-wheel $\frac{Mv^2}{2} = \frac{W}{64.4} \frac{8.14^2 D^2 R^2}{8600} =$

850,000 H.P. Fly-wheel energy per H.P. = 850,000 $C \times H.P.(8.14)^{q} D^{q} R^{q}$ $R^3D^2 \times 64.4 \times 8600$ R. Fig. wheel energy per H.F. = R. The limit of variation of speed with such a weight of wheel from excess of

power per fraction of revolution is less than .0028.

The value of the constant C given by Mr. Rites was derived from practice of the Westinghouse single-acting engines used for electric-lighting. For double-acting engines in ordinary service a value of C = 5,000,000,000 would

probably be ample.

From these formulæ it appears that the weight of the fly-wheel for a given horse-power should vary inversely with the cube of the revolutions and the

square of the diameter, 'August 12, 1891) says: Whenever 480 feet is the lowest piston-speed probable for an engine of a certain size, the fly-wheel weight for that speed approximates closely to the formula

$$W = 700,000 \frac{d^9s}{D^2R^2}$$

W =weight in pounds, d =diameter of cylinder in inches, a =stroke in inches, D = diameter of wheel in feet, R = revolutions per minute, corre

sponding to 480 feet piston-spead.

In a Ready Reference Book published by Mr. Stanwood, Cincinnati, 1892, he gives the same formula. with coefficients as follows: For slide-valve engines, ordinary duty, 550,000; same, electric-lighting, 700,000; for automatic high-speed engines, 1,000,000; for Corliss engines, ordinary duty 700,000, electric-lighting 1,000,000.

Thurston's formula above given, $W = \frac{aAS}{R^2D^2}$, with a = 19,000,000, when reduced to terms of d and s in inches, becomes $W = 785,400 \frac{d^2s}{D^2/M}$

in which P = mean effective pressure. Taking this at 40 lbs., we obtain $W = 5,000,000,000 \frac{\text{I.H.P.}}{R^2 D^2}$. If mean effective pressure = 30 lbs., then $W = 5,000,000 \frac{\text{I.H.P.}}{R^2 D^2}$. 6,666,000,000 <u>I.H.P.</u>

Emil Theiss (Am. Mach., Sept. 7 and 14, 1898) gives the following values of d, the coefficient of steadiness, which is the reciprocal of what Rankine calls the coefficient of fluctuation:

or engines operating— Hammering and crushing machinery Pumping and shearing machinery	d:	20	to 30
Weaving and paper-making machinery	d = d = d =	= 40 = 50	
Ordinary driving engines (mounted on bed-plate), belt transmission Gear-wheel transmission	d:	s 50	,
. Theirs's formula for weight of fly wheel in mounts is	W	_	$d\times 1.H.P.$

re d is the coefficient of steadiness, V the mean velocity of the flyel rim in feet per second, n the number of revolutions per minute, i = sefficient obtained by graphical solution, the values of which for dittint on the divenience of the following table. In the lines under "cut" p means "compression to initial pressure," and O "no compression":

VALUES OF 4. SINGLE-CYLINDER NON-CONDENSING ENGINES.

ti d	Out-off, 1/6.		Cut-o	A, 14.	· Cut-o	n, 36.	Cut-off, 14.		
speco, ft. per min.	Comp.	0	Comp.	0	Comp.	0	Comp.	0	
900 100 500 900	972,090 240,810 194,670 168,900	187,430 145,400	206,200 168,590	179,460 136,460	188,510 165,210	170,040	174,630		

SINGLE-CYLINDER CONDENSING ENGINES.

nın.	Cut-off, 16. Cut-off, 1/6.		Cut-c	n, 14.	Out-o	ff, 1/6.	Cut-off, 16.			
_	Comp.	-	Comp.		Comp.	'	Comp.	"	Comp.	
5	965,560 194,560	176,5 6 0 117,870	234,160 174,880	178,660 118,850	204,210 164,720	167,140 188,080	189,600 174,680	161,830 151,680	172,690	156,990
	148,780	140,090	1	1	1	l	l <u></u>	L		l

TWO-CYLINDER ENGINES, CRANES AT 90°.

min.	Cut-o	T, 1/6.	Cut-c	at, 14.	Cut-o	ff, 1/6.	Cut-off, 1/4.	
peri	$ \begin{array}{c} \text{Comp.} \\ p \end{array} $	0	Comp.	o	Comp.	0	Comp.	0
00 00 00 00	71,980 70,160 70,040 70,040	Mean 60,140		Mean 54,840		Mean 50,000	87,920 85,500	} Mean } 36,950

THREE-CYLINDER ENGINES, CRANKS AT 120°.

Min.	Cut-off, 1/6.		Cut-o	nt, 14.	Cut-o	A, 16.	Cut-off, 1/2.	
.ed	Comp.	0	Comp.	0	Comp.	0	Comp.	o
)O	8 3,810 8 0,190	82,240 81,570	83,810 85,140	8 5,500 8 3,810	84,540 86,470	88,450 82,850	85,960 83,810	82,370 32,370

As a mean value of i for these engines we may use 83.810.

Centrifugal Force in Fly-wheels.—Let W =weight of rim in pounds; R = mean radius of rim in feet; r = revolutions per minute, g = mean radius of rim in feet; r = revolutions per minute, q = mean radius of rim in feet; r = revolutions per minute, q = mean radius of rim in feet; r = revolutions per minute, q = mean radius of rim in feet; r = revolutions per minute, q = mean radius of rim in feet; q = mean radius; q =82.16; $v = \text{velocity of rim in feet per second} = 2\pi Rr + 60$.

Centrifugal force of whole rim = $F = \frac{Wv^2}{gR} = \frac{4W\pi^2Rv^2}{3600g}$ $= .000841WRr^{2}$.

The resultant, acting at right angles to a diameter of half of this force, tends to disrupt one half of the wheel from the other half, and is resisted by the section of the rim at each end of the diameter. The resultant of half the radial forces taken at right angles to the diameter is $1 + \frac{1}{2\pi} = \frac{3}{\pi}$ of the sum

of these forces; hence the total force F is to be divided by $2^{\infty} \times 2 \times 1.5708 = 6.2832$ to obtain the tensile strain on the cross-section of the rim, or, total strain on the cross-section of the rim or, total strain on the cross-section $S = .C000842^{\circ}WR^{\circ}$. The weight W_1 of a rim of cast iron 1 inch square in section is $2\pi R \times 3.125 = 19.635R$ pounds, whence strain per square inch of sectional area of rim = $S_1 = .0010656R^{\circ}$, outled 40.000270° , in which D = diameter of wheel in feet, and V is velocity of rim in feet per minute. $S_1 = .0972v^2$, if v is taken in feet per second second.

The specific gravity of the wood being taken at 0.6 = 37.5 lbs. per cu. ft., or 1/12 the weight of cast iron.

Example.—Required the strain per square inch in the rim of a cast-iron wheel 30 ft. diameter, 60 revolutions per minute.

Answer. $15^2 \times 60^2 \times .0010656 = 868.1$ lbs. Required the strain per square inch in a cast-iron wheel-rim running a mile a minute. Answer. $.000027 \times 5280^2 = 752.7$ lbs.

In cast-iron fly-wheel rims, on account of their thickness, there is difficulty in securing soundness, and a tensile strength of 10,000 lbs. per sq. in. is as much as can be assumed with safety. Using a factor of safety of 10 gives a maximum allowable strain in the rim of 1000 lbs. per sq. in., which corresponds to a rim velocity of 6085 ft. per minute.

For any given material, as cast iron, the strength to resist centrifugal force

For any given material, as east iron, the strength to resist centrirugal force depends only on the velocity of the rim, and not upon its bulk or weight. Chas. E. Emery (Cass. Mag., 1892) says: By calculation half the strength of the arms is available to strengthen the rim, or a trifle more if the flywheel centres are relatively large. The arms, however, are subject to transverse strains, from belts and from changes of speed, and there is, moreover, no certainty that the arms and rim will be adjusted so as to pull exactly together in resisting disruption, so the plan of considering the rim by itself and making it strong enough to resist disruption by centrifugal force within safe limits, as is assumed in the calculations above, is the safer way.

sate limits, as is assumed in the calculations above, is the safer way.

It does not appear that fly-wheels of customary construction should be
unsafe at the comparatively low speeds now in common use if proper
materials are used in construction. The cause of rupture of fly-wheels that
have failed is usually either the "running away" of the engine, such as may
be caused by the breaking or slackness of a governor-belt, or incorrect
design or defective materials of the fly-wheel.

Chas. T. Porter (Trans. A. S. M. E., xiv. 808) states that no case of the
bursting of a fly-wheel with a solid rim in a high-speed engine is known. He
bursting of a fly-wheel which a solid rim in a high-speed engine is known.

attributes the bursting of wheels built in segments to insufficient strength other of the flanges and bolts by which the segments to insufficient strength of the flanges and bolts by which the segments are held together. (See also Thurston, "Manual of the Steam-engine," Part II, page 413, etc.)

Arms of Fly-wheels and Pulleys, — Professor Torrey (Am. Mach., July 30, 1891) gives the following formula for arms of elliptical cross-section of cast-iron wheels:

W =load in pounds acting on one arm; S =strain on belt in pounds per inch of width, taken at 56 for single and 112 for double belts; v =width of belt in inches; n = number of arms; L = length of arm in feet; b = breadth

of arm at hub; d = depth of arm at hub, both in inches:

The breadth of the arm is its least dimension = minor axis of the ellipse, and the depth the major axis. This formula is based on a factor of safety of 10.

using the formula, first assume some depth for the arm, and calculate equired breadth to go with it. If it gives too round an arm, assume depth a little greater, and repeat the calculation. A second trial will

st always give a good section.
e size of the arms at the hub having been calculated, they may be ewhat reduced at the rim end. The actual amount cannot be calculated, here are too many unknown quantities. However, the depth and dth can be reduced about one third at the rim without danger, and this give a well-shaped arm.

illeys are often cast in halves, and bolted together. When this is done reatest care should be taken to provide sufficient metal in the bolts. is apt to be the very weakest point in such pulleys. The combined area ne bolts at each joint should be about 28/100 the cross-section of the pulit that point. (Torrey.)

win gives

$$d = 0.6887 \sqrt{\frac{^3}{n}} \text{ for single belts };$$

$$d = 0.798 \sqrt[3]{\frac{BD}{n}}$$
 for double belts;

sing the diameter of the pulley, and B the breadth of the rim, both in eq. These formulæ are based on an elliptical section of arm in which 0.4d or d=2.5b on a width of belt =4/5 the width of the pulley rim, ximum driving force transmitted by the belt of 56 lbs. per inch of width single belt and 112 lbs. for a double belt, and a safe working stress of these of 900 lbs. iron of 2250 lbs. per square inch. in Torrey's formula we make b=0.4d, it reduces to

$$b=\sqrt[3]{\frac{\overline{WL}}{187.5}}; \quad d=\sqrt[3]{\frac{\overline{WL}}{12}}.$$

ample.—Given a pulley 10 feet diameter; 8 arms, each 4 feet long; face, ches wide; belt, 30 inches: required the breath and depth of the arm at ub. According to Unwin,

$$d = 0.6387 \sqrt[3]{\frac{BD}{n}} = 0.633 \sqrt[3]{\frac{36 \times 120}{8}} = 5.16$$
 for single belt, $b = 2.06$;

$$\vec{z} = 0.798 \sqrt[3]{\frac{BD}{n}} = 0.798 \sqrt[3]{\frac{36 \times 120}{8}} = 6.50$$
 for double belt, $b = 2.60$.

cording to Torrey, if we take the formula $b = \frac{WL}{90d^2}$ and assume d = 5

i.5 inches, respectively, for single and double belts, we obtain b=1.08. 33, respectively, or practically only one half of the breadth according win, and, since transverse strength is proportional to breadth, an arm

one half as strong.
rey's formula is said to be based on a factor of safety of 10, but this rean be only apparent and not real, since the assumption that the non-each arm is equal to the strain on the belt divided by the number ons, is, to say the least, inaccurate. It would be more nearly correct to hat the strain of the belt is divided among half the number of arms. in makes the same assumption in developing his formula, but says it is in a rough sense true, and that a large factor of safety must be allowed, erefore takes the low figure of 2250 lbs. per square inch for the safe ing strength of cast iron. Unwin says that his equations agree well practice.

amoters of Fly-wheels for Various Speeds.—If 6000 feet inute be the maximum velocity of rim allowable, then $6000 = \pi RD$, in 1 R = revolutions per minute, and D = diameter of wheel in feet, so $D = \frac{6000}{\pi R} = \frac{1910}{R}$.

MAXIMUM DIAMETER OF FLY-WHEEL ALLOWABLE FOR DIFFERENT NUMBERS OF REVOLUTIONS.

Revolutions		mum Speed of er minute.	Assuming Maximum Speed of 6000 feet per minute.			
per minute.	Circum. ft.	Diam. ft.	Circum, ft.	Diam. ft.		
40 50	125 100	39. 8 81.8	150. 120.	47.7 88.9		
60	83.3	26.5	100.	81.8		
70	71.4	22.7	85.79	27.3		
80	62.5	19.9	75.00	23.9		
90	55.5	17.7	66.66	21.2		
100	50.	15.9	60.00	19.1		
120	41.67	18.3	50.00	15.9		
140	85.71	11.4	42.86	13.6		
160	81.25	9.9	87.5	11.9		
180	27.77	8.8	88.88	10.6		
200	25.00	8.0	80.00	9.6		
220 240	22.73	7.2	27.27	8.7		
240 260	20.88 19.28	6.6	25.00	8.0 7.3		
280	17.86	6.1 5.7	23.08 21.48	6.8		
800	16.66	5.8	20.00	6.4		
850	14.29	4.5	17.14	5.5		
400	12.5	4.0	15.00	4.8		
450	11.11	8.5	18.88	4.2		
500	10.00	3.2	12.00	1 8.8		

Strains in the Rims of Fly-band Wheels Produced by Centrifugal Force. (James B. Stanwood, Trans. A. S. M. E., xiv. 251.)

—Mr. Stanwood mentions one case of a fly-band wheel where the periphery velocity on a 17 % wheel is over 7500 ft. per minute.

In band saw-mills the blade of the saw is operated successfully over

In band saw-mills the blade of the saw is operated successfully over wheels 8 and 9 ft. in diameter, at a periphery velocity of 9000 to 10,000 ft. per minute. These wheels are of cast fron throughout, of heavy thickness, with a large number of arms.

In shingle-machines and chipping-machines where cast-iron disks from 2 to 5 ft. in diameter are employed, with knives inserted radially, the speed is frequently 10,000 to 11,000 ft. per infinite at the periphery.

If the rim of a fly-wheel alone be considered, the tensile strain in pounds

If the rim of a fly-wheel alone be considered, the tensile strain in pounds per square inch of the rim section is $T = \frac{V^2}{10}$ nearly, in which V = velocity

in feet per second; but this strain is modified by the resistance of the arms, which prevent the uniform circumferential expansion of the rim, and induce a bending as well as a tensile strain. Mr. Stanwood discusses the strains in band-wheels due to transverse bending of a section of the rim between a pair of arms.

When the arms are few in number, and of large cross-section, the ring will be strained transversely to a greater degree than with a greater number of lighter arms. To illustrate the necessary rim thicknesses for various rim velocities, pulley diameters, number of arms, etc., the following table is given, based upon the formula

$$\xi = \frac{.475d}{N^2 \left(\frac{F}{V^2} - \frac{1}{10}\right)},$$

in which t= thickness of rim in inches, d= diameter of pulley in inches, N= number of arms, V= velocity of rim in feet per second, and F= the greatest strain in pounds per square inch to which any fibre is subjected. The value of F is taken at 6000 lbs. per sq. in.

Thickness	af	#frene	1m	SAHA	Wheele.
T TITES HOSE	•			SOME	AS TROOTING

ameter of Pulley in inches.	Velocity of Rim in feet per second.	Velocity of Rim in feet per minute.	No. of Arms.	Thickness in inches.
24 24 48 106 106	50 88 88 184 184	8,000 5,290 5,290 11,040 11,040	6 6 6 16 86	2/10 15/32 15/16 21/4

the limit of rim velocity for all wheels be assumed to be 88 ft. per sec-, equal to 1 mile per minute, F = 6000 lbs., the formula becomes

$$t = \frac{.475d}{.67N^2} = 0.7 \frac{d}{N^2}$$

hen wheels are made in halves or in sections, the bending strain may such as to make t greater than that given above. Thus, when the joint set half way between the arms, the bending action is similar to a beam ported simply at the ends, uniformly loaded, and t is 50% greater. Then formula becomes

$$t = \frac{.719d}{N^9 \left(\frac{F'}{V^3} - \frac{1}{10} \right)}$$

or a fixed maximum rim velocity of 88 ft. per second and F = 8000 lbs., $\frac{1}{N^2}$. In segmental wheels it is preferable to have the joints opposite

arms. Wheels in halves, if very thin rims are to be employed, should a double arms along the line of separation, arme.

students along the nine of separation, iteration should be given to the proportions of large receiving and tighting pulleys. The thickness of rim for a 48-in, wheel (shown in table) with m velocity of 85 ft. per second, is 15/16 in. Many wrecks have been ed by the failure of receiving or tightening pulleys whose rims have been thin. Fly-wheels calculated for a given coefficient of steadiness are frently lighter than the minimum safe weight. This is true especially of wheels a received studie to the minimum weight of wheels can be do e wheels. A rough guide to the minimum weight of wheels can be dee wheels. A rough guide to the minimum weight of wheels can be dedeform our formulæ. The arms, hub, lugs, etc., usually form from one rier to one third the entire weight of the wheel. If b represents the face wheel in inches, the weight of the rim (considered as a simple annular) will be w=82dt bls. If the limit of speed is 88 ft. per second, then solid wheels $t=0.7d+N^2$. For sectional wheels (joint between arms) $1.06d+N^3$. Weight of rim for solid wheels, $w=57d^3b+N^3$ in pounds, then in sectional wheels with joints between arms, $w=86d^3b+N^3$ to $b+N^3$, in pounds. Total weight of wheel: for solid wheel, $W=.76d^3b+N^3$ to $b+N^3$ to $b+N^3$ in pounds, is subject is further discussed by Mr. Stanwood, in vol. xv., and by Gaetano Lanza, in vol. xvi.. Trans. A. S. M. E.)

Wooden Him Fly-wheel, built in 1891 for a pair of Corliss ens at the Amoskeag Mfg. Co.'s mill, Manchester, N. H., is described by Manning in Trans. A. S. M. E., xiii. 618. It is 30 ft. diam, and 108 in. face, rim is 12 inches thick, and is built up of 44 courses of ash plank, 2, 3, 4 inches thick, reduced about ½ inch in dressing, set edgewise, so as to k joints, and glued and bolted together. There are two hubs and two of arms, 12 in each, all of cast iron. The weights are as follows:

Weight (calculated) of ash rim	81,855 lbs.
of 24 arms (foundry 45,020)	40,849 **
44 * 2 hubs (* 85,030)	81.394 - 4
Counter-weights in 6 arms	664 4
Total excluding holts and screws	104 262 4

e wheel was tested at 76 revs. per min., being a surface speed of nearly feet per minute.

Mr. Manning discusses the relative safety of cast fron and of wooden wheels as follows: As for safety, the speeds being the same in both cases, the hoop tension in the rim per unit of cross-section would be directly as the weight per cubic unit; and its capacity to stand the strain directly as the tensile strength per square unit; therefore the tensile strengths divided by the weights will give relative values of different materials. Cast iron weighing 450 lbs. per cubic foot and with a tensile strength of 1,440,000 lbs. weighing 450 los. per cube foot and with a tensite strength of 1,775,000 per square foot would give a value of 1,440,000 + 450= 3200, whilst ash, of which the rim was made, weghing 34 lbs. per cubic foot, and with 1,152,000 lbs. tensile strength per square foot, gives a result 1,152,000 + 34 = 33,882 and 33,882 + 3200 = 10.58, or the wood-rimmed pulley is ten times safer than the cast-iron when the castings are good. This would allow the wood-

rimmed pulley to increase its speed to $\sqrt{10.58} = 3.25$ times that of a sound cast-iron one with equal safety.

Wooden Fly-wheel of the Willimantic Linen Co. (Illustrated in Power, March, 1898.)—Rim 28 ft, diam., 110 in. face. The rim is carried upon three sets of arms, one under the centre of each belt, with 12

arms in each set.

The material of the rim is ordinary whitewood, % in. in thickness, cut into segments not exceeding 4 feet in length, and either 5 or 8 inches in width. These were assembled by building a complete circle 13 inches in width, first with the 8 inch inside and the 5-inch outside, and then beside it another circle with the widths reversed, so as to break joints. Each piece as it was added was brushed over with glue and nailed with three-inch wire nails to the pieces already in position. The nails pass through three and into the fourth thickness. At the end of each arm four 14-inch bolts secure the rim, the ends being covered by wooden plugs glued and driven into the face

of the wheel.

Wire-wound Fly-wheels for Extreme Speeds. (Eng'g News, August 2, 1890.)—The power required to produce the Mannesmann tubes is very large, varying from 2000 to 10,000 H.P., according to the dimensions of the tube. Since this power is only needed for a short time (it takes only 30 to 45 seconds to convert a bar 10 to 12 ft. long and 4 in. in diameter into a tube), and then some time clapses before the next bar is ready, an engine of 1200 H.P. provided with a large fig-wheel for storing the energy will supply power enough for one set of rolls. These fly-wheels are so large and run at such great speeds that the ordinary method of constructing them cannot be followed. A wheel at the Manuesmann Works, made in Komotau, Hungary, in the usual manner, broke at a tangential velocity of 125 ft. per second. The fly-wheels designed to hold at more than double this speed consist of a cast-iron hub to which two steel disks, 20 ft. in diameter, are bolted; around the circumference of the wheel thus formed 70 tons of No. 5 wire are wound under a tension of 50 lbs. In the Mannesmann Works at Landore, Wales such a wheel makes 240 revolutions a minute, corresponding to a tangential velocity of 15,080 ft. or 2.85 miles per minute.

THE SLIDE-VALVE.

Definitions. - Travel = total distance moved by the valve.

Throw of the Eccentric = eccentricity of the eccentric = distance from the pentre of the shaft to the centre of the eccentric disk = 1/6 the travel of the valve. (Some writers use the term "throw" to mean the whole travel of the valve.)

Lap of the valve, also called outside lap or steam-lap = distance the outer

Inside lap, or exhaust-lap — distance the inner or exhaust edge of the valve extends beyond or laps over the steam edge of the port when the valve is in its central position.

Inside lap, or exhaust-lap — distance the inner or exhaust edge of the valve extends beyond or laps over the exhaust edge of the port when the valve is in its central position. The inside lap is sometimes made zero, or even negative, in which latter case the distance between the edge of the valve and the edge of the port is sometimes called exhaust clearance, or inside clearance.

Lead of the valve = the distance the steam-port is opened when the engine is on its centre and the piston is at the beginning of the stroke.

Lead-angle = the angle between the position of the crank when the valve begins to be opened and its position when the piston is at the beginning of the stroke.

The valve is said to have lead when the steam-port opens before the picton

ns its stroke. If the piston begins its stroke before the admission of m begins the valve is said to have negative lead, and its amount is the of the edge of the valve over the edge of the port at the instant when piston stroke begins.

ip-angle = the angle through which the eccentric must be rotated to the steam edge to travel from its central position the distance of the

igular advance of the eccentric = lap-angle + lead angle. near advance = lap + lead.

frect of Lap, Lead, etc., upon the Steam Distribution.—

n valve-travel 2M in., lap 3k in., lead 1/16 in., exhaust-lap 1/6 in., redect and position for admission, cut-off, release and compression, and test port-opening. (Halsey on Slide-valve Gears.) Draw a circle of neter fh = travel of valve. From 0 the centre set off 0a = lap and ab ad, erect perpendiculars 0e, ac, bd; then ec is the lap-angle and ec the angle, measured as arcs. Set off fg = cd, the lead-angle, then 0g is osition of the crank for steam admission. Set off 2ec + cd from h to i; of is the crank-angle for cut-off, and fk + fh is the fraction of stroke pleted at cut-off. Set off fp = ec + cd - em, and 0n is the position of crank compression, fo + fh is the fraction of stroke completed at release, and -hf is the fraction of the return stroke completed when compression ns; 0h, the throw of the eccentric, minus 0a the lap, equals ah the immum port-opening.

a valve has neither lap nor lead, the line joining the centre of the eccen-

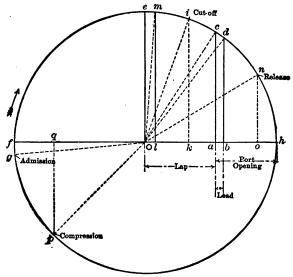


Fig. 146.

disk and the centre of the shaft being at right angles to the line of the k, the engine would follow full stroke, admission of steam beginning at beginning of the stroke and ending at the end of the stroke. Iding lap to the valve enables us to cut off steam before the end of the right the eccentric being advanced on the shaft an amount equal to the angle enables steam to be admitted at the beginning of the stroke, as

before lap was added, and advancing it a further amount equal to the lead angle causes steam to be admitted before the beginning of the stroke.

Having given lap to the valve, and having advanced the eccentric on the shaft from its central position at right angles to the crank, through the angular advance = lap-angle and lead-angle, the four events, admission, angular advance = lap-angle and lead-angle, the four events, admission, cut-off, release or exhaust-opening, and compression or exhaust-closure, take place as follows: Admission, when the crank lacks the lead-angle of having reached the centre; cut-off, when the crank lacks two lap-angles and one lead-angle of having reached the centre. During the admission of steam the crank turns through a semicircle less twice the lap-angle. The greatest port-opening is equal to half the travel of the valve less the lap. Therefore for a given port-opening the travel of the valve must be increased if the lap is increased. When exhaust-lap is added to the valve incleays the opening of the exhaust and hastens its closing by an angle of rotation equal to the exhaust-lap angle, which is the angle through which the excentric rotates from its middle position while the exhaust edge of the valve uncovers its lap. Release then takes place when the crank lacks one the eccentric rotates from its middle position while the exhaust edge of the valve uncovers its lap. Release then takes place when the crank lacks one lap-angle and one lead-angle minus one exhaust-lap angle of having reached the centre, and compression when the crank lacks lap-angle + lead-angle + exhaust-lap angle of having reached the centre.

The above discussion of the relative position of the crank, piston, and valve for the different points of the stroke is accurate only with a connecting-rod of infinite length.

For actual connecting-rods the angular position of the rod causes a distortion of the relative causes the experts to take place to

distortion of the position of the valve, causing the events to take place too late in the forward stroke and too early in the return. The correction of this distortion may be accomplished to some extent by setting the valve so as to give equal lead on both forward and return stroke, and by altering the exhaust lap on one end so as to equalize the release and compression. F. A. Halsey, in his Slide valve Gears, describes a method of equalizing the cut-off without at the same time affecting the equality of the lead. In designing slide-valves the effect of angularity of the connecting-rod should be studied on the drawing-board, and preferably by the use of a model.

Sweet's Valve-diagram. To find outside and inside lap of valve for different cut-offs and compressions (see Fig. 147): Draw a circle whose

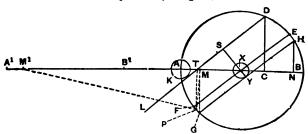


Fig. 147.—Sweet's Valve-diagram.

diameter equals travel of valve. Draw diameter BA and continue to A1, so that the length AA1 bears the same ratio to XA as the length of con-

so that the length AA^* bears the same ratio to AA as the length of connecting-rod does to length of engine-crank. Draw small circle K with a radius equal to lead. Lay off AC so that ratio of AC to AB = cut-off in parts of the stroke. Erect perpendicular CD. Draw DL tangent to K; draw XS perpendicular to DL; XS is then outside lap of valve.

To find release and compression: If there is no inside lap, draw FE through X parallel to DL. F and E will be position of crank for release and compression. If there is an inside lap, draw a circle about X, in which radius XY equals inside lap. Draw HG tangent to this circle and parallel to DL; then H and G are crank position for release and compression. radius XY equals inside lap. Draw BG targeth while circle and parallel to DL; then H and G are crank position for release and compression. Draw HN and MG, then AN is piston position at release and AM piston position at compression, AB being considered stroke of engine.

To make compression alike on each stroke it is necessary to increase the

haide lap on crank end of valve, and to decrease by the same amount the

) dap on back end of valve. To determine this amount, through M with us $MM = AA^1$, draw are M P, from P draw PT perpendicular to AB, PM is the amount to be added to inside lap on crank end, and to be sted from inside lap on back end of valve, inside lap being XY.

the Bilgram Valve Diagram, see Halsey on Slide-valve Gears.

10 Zeuner Valve-diagrams is given in most of the works on the lengine, and in treatises on valve-gears, as Zeuner's, Peabody's, and

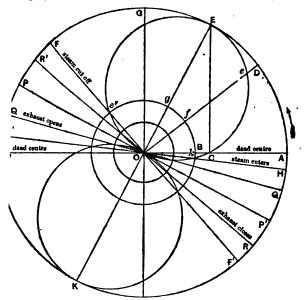


Fig. 148.—Zeuner's Valve-diagram.

ler's. The following is condensed from Holmes on the Steam-engine: be a circle, with radius OA equal to the half travel of the valve. O measure off OB equal to the outside lap, and BC equal to the lead, the crank-pin occupies the dead centre A, the valve has already to the right of its central position by the space OB + BC. From C the perpendicular CE and join OE. Then will OE be the position led by the line joining the centre of the eccentric with the centre of ank-ahaft at the commencement of the stroke. On the line OE as ter describe the circle OCE; then any chords, as Oe, OE, Oe, will ent the spaces travelled by the valve must have moved from its central position when ank-pin occupies respectively the positions opposite to D, E, and F, the port is opened at all the valve must have moved from its central not by an amount equal to the lap OB. Hence, to obtain the space by the port is opened, subtract from each of the arcs Oe, OE, etc., a equal to OB. This is represented graphically by describing from O a circle with radius equal to the lap OB; then the spaces fe, gE, tercepted between the circumferences of the lap-circle Efe and the fircle OCE, will give the extent to which the steam-port is opened. Le point E, at which the chor E of is common to both valve and lap it is evident that the valve E as moved to the right by the amount of E, and is consequently just on the point of opening the steam-port, the steam is admitted before the commencement of the stroke, when

lution still remains to be accomplished. When the crank-pin reaches the position A, that is to say, at the commencement of the stroke, the port is already opened by the space OC - OB = BC, called the lead. From this point forward till the crank occupies the position OE the port continues to open, but when the crank is at OE the valve has reached the furthest limit of its travel to the right, and then commences to return, till when in the position OF the edge of the valve just covers the steam-port, as is shown by the chord Oe', being again common to both lap and valve circles. Hence when the crank occupies the position OF the cut-off takes place and the steam commences to expand, and continues to do so till the exhaust opens.

steam commences to expand, and continues to do so till the exhaust opens. For the return stroke the steam-port opens again at H' and closes at F'. There remains the exhaust to be considered. When the line joining the centres of the eccentric and crank-shaft occupies the position opposite to OG at right angles to the line of dead centres, the crank is in the line OP at right angles to OE; and as OP does not intersect either valve-circle the valve occupies its central position, and consequently closes the port by the amount of the inside lap. The crank must therefore move through such an angular distance that its line of direction OQ must intercept a chord on the valve-circle OK equal in length to the inside lap before the port can be opened to the exhaust. This point is ascertained precisely in the same manner as for the outside lap, namely, by drawing a circle from centre O, with a radius equal to the inside lap; this is the small inner circle in the figure. Where this circle intersects the two valve-circles we get four points which show the positions of the crank when the exhaust opens and closes during each revolution. Thus at O the valve opens the exhaust on the side of the piston which we have been considering, while at O the exhaust closes and compression commences and continues till the fresh steam is read-mitted at O. mitted at H.

Thus the diagram enables us to ascertain the exact position of the crank when each critical operation of the valve takes place. Making a résumé of these operations of one side of the piston, we have: Steam admitted before the commencement of the stroke at H. At the dead centre A the valve is already opened by the amount BC. At E the port is fully opened, and valve has reached one end of its travel. At F steam is cut off, consequently admission lasted from H to F. At P valve occupies central position, and ports are closed both to steam and exhaust. At Q exhaust opened, consequently expansion lasted from F to Q. At K exhaust opened to maximum extent, and valve reached the end of its travel to the left. At R exhaust closed, and compression begins and continues till the fresh steam is admitted

at H.

PROBLEM.—The simplest problem which occurs is the following: Given the length of throw, the angle of advance of the eccentric, and the laps of the valve, find the angles of the crank at which the steam is admitted and cut off and the exhaust opened and closed. Draw the line OE, representing the half-travel of the valve or the throw of the eccentric at the given angle of advance with the perpendicular OE. Produce OE to E. On OE and OE and OE are dependently the travellar of the states. With centra and radii could be as diameters describe the two valve-circles. With centre and radii equal to the given laps describe the outside and inside lap-circles. Then the intersection of these circles with the two valve-circles give points through which the lines OH, OF, OQ, and OR can be drawn. These lines give the required positions of the crank.

Numerous other problems will be found in Holmes on the Steam-engine, including problems in valve-setting and the application of the Zeuner diagram to link motion and to the Meyer valve-gear.

Port Opening.—The area of port opening should be such that the velocity of the steam in passing through it should not exceed 6000 ft. per min. The ratio of port area to piston area will then vary with the piston-speed as follows: For speed of piston, \

100 200 300 400 500 600 700 800 900 1000 1200 ft. per min. Port area = piston (.017 .038 .05 .067 .088 .1 .107 .188 .15 .167 area X

For a velocity of 6000 ft. per min.,

Port area = sq. of diam. of cyl. × piston speed

The length of the port opening may be equal to or something less than the diameter of the cylinder, and the width = area of port opening + its length.

The bridge between steam and exhaust ports should be wide enough to prevent a leak of steam into the exhaust due to overtravel of the valve.

hincloss gives: Width of exhaust port = width of steam port + rel of valve - width of bridge.

ad. (From Peabody's Valve-gears.)—The lead, or the amount that lve is open when the engine is on a dead point, varies, with the type ze of the engine. From a very small amount, or even nothing, up to \(\frac{3}{2} \) inch or more. Stationary-engines running at slow speed may have 1/64 to 1/16 inch lead. The effect of compression is to fill the waste at the end of the cylinder with steam; consequently, engines having compression need less lead. Locomotive-engines having the valves illed by the ordinary form of Stephenson link-motion may have illead when running slowly and with a long cut-off, but when at speed short cut-off the lead is at least \(\frac{1}{2} \) inch; and locomotives that have gear which gives constant lead commonly have \(\frac{1}{2} \) inch lead. The ngle is the angle the crank makes with the line of dead points at ston. It may vary from 0° to 8°.

sion. It may vary from 0° to 8°.

1de Lead. — Weisbach (vol. ii. p. 296) says: Experiment shows that riler opening of the exhaust ports is especially of advantage, and in st engines the lead of the valve upon the side of the exhaust, or the lead; is 1/25 to 1/15; i.e., the slide-valve at the lowest or highest posithe piston has made an opening whose height is 1/25 to 1/15 of the throw of the slide-valve. The outside lead of the slide-valve or the n the steam side, on the other hand, is much smaller, and is orten 100 of the whole throw of the valve.

fect of Changing Outside Lap, Inside Lap, Travel and Angular Advance. (Thurston.)

Admission	Expansion	Exhaust	Compression		
is later,	occurs earlier,	is unchanged	begins at		
ceases sooner	continues longer		same point		
unchanged	begins as before,	occurs later,	begins sooner,		
	continues longer	ceases earlier	continues longer		
begins sooner,	begins later,	begins later,	begins later,		
ontinues longer	ceases sooner	ceases later	ends sooner		
begins earlier,	begins sooner,	begins earlier,	begins earlier,		
period unaltered	per. the same	per. unchanged	per. the same		

er gives the following relations (Weisbach-Dubois, vol. ii. p. 807):

= travel of valve, p = maximum port opening;

= steam-lap, l = exhaust-lap;

= ratio of steam-lap to half travel =
$$\frac{L}{.5S}$$
, $L = \frac{R}{2} \times S$;

= ratio of exhaust lap to half travel =
$$\frac{l}{1.58}$$
, $l = \frac{r}{2} \times S_i$

$$= 2p + 2L = 2p + R \times S; S = \frac{2p}{1-R}$$

= angle HOF between positions of crank at admission and at cut-off, and $\beta = \text{angle }QOR$ between positions of crank at release and at compression, then $R = \frac{1}{3}\frac{\sin{(180^{\circ} - \alpha)}}{\sin{\frac{1}{3}\alpha}}; \quad r = \frac{1}{3}\frac{\sin{(180^{\circ} - \beta)}}{\sin{\frac{1}{3}\beta}}.$

of Lap and of Port-opening to Valve-travel.—The page 831, giving the ratio of lap to travel of valve and ratio of travel opening, is abridged from one given by Buel in Weisbach-Dubois, It is calculated from the above formulæ. Intermediate values may by the formulæ, or with sufficient accuracy by interpolation from res in the table. By the table on page 830 the crank-angle may be hat is, the angle between its position when the engine is on the and its position at cut-off, release, or compression, when these are n fractions of the stroke. To illustrate the use of the tables the g example is given by Buel: width of port = 22 in; width of port = width of port + 0.3 in; overtravel = 2.5 in; length of connect. = 2½ times stroke; cut-off = 0.75 of stroke; release = 0.95 of lead-sangle, 10°. From the first table we flud crank-angle = 114.°

add lead-angle, making 134.6.° From the second table, for angle between admission and cut-off, 125°, we have ratio of travel to port-opening = 3.73, or for 134.6° = 8.74, which, multiplied by port-opening 2.5, gives 9.45 in travel. The ratio of lap to travel, by the table, is .2324, or 9.45 \times .2324 = 2.2 in lap. For exhaust-lap we have, for release at .95, crank-angle = 151.3; add lead-angle 10° = 161.8°. From the second table, by interpolation, ratio of lap to travel = .0811, and .0811 \times 9.45 = 0.77 in., the exhaust-lap.

```
Lap-angle = \frac{1}{2} (180° - lead-angle - crank-angle at cut-off);

= \frac{1}{2} (180° - 10 - 114.6) = 27.7°.

Angular advance = lap-angle + lead-angle = 27.7 + 10 = 37.7°.

Exhaust lap-angle = crank-angle at release + lap-angle + lead-angle - 180°;

= 151.3 + 27.7 + 10 - 180° = 9°.

Crank-angle at components of the pression measured on return stroke | = 180° - lap-angle - lead-angle - exhaust lap-angle;

= 180 - 27.7 - 10 - 9 = 133.8°; corresponding, by
```

table, to a piston position of .8i of the return stroke; or Crank-angle at compression = 180° - (angle at release - angle at cut-off) + lead-angle;

 $= 180 - (151.3 - 114.6) + 10 = 133.8^{\circ}$.

The positions determined above for cut-off and release are for the forward stroke of the piston. On the return stroke the cut-off will take place at the same angle, 114.6°, corresponding by table to 66.6% of the return stroke, instead of 75%. By a slight adjustment of the angular advance and the length of the eccentric rod the cut-off can be equalized. The width of the bridge should be at least 2.5 + 0.25 - 2.2 = 0.55 in.

Orank Angles for Connecting-rods of Different Length.

Forward and Return Strokes.

of om	1	Ra	tio of	Leng	th of	Conne	ecting	rod t	o Ler	gth o	f Stro	ke.	
Fraction of Stroke from Commencement,	1	2 234		3 33		33/4		1	1	5	Infi		
	For.	Ret	For.	Ret.	For.	Ret.	For.	Ret.	For.	Ret.	For.	Ret.	For or Ret
.01	10.3	13.2	10.5			12.6	10.7	12.4	10.8	12.3	10.9	12.1	11.
.02	14.6	18.7	14.9	18.1	15.1	17.8	15.2	17.5		17.4		17.1	16.
.03	17.9	99.9		22.2	18.5	21.8	18.7	21.5	18.8	21.3	19.0	21.0	19.
.04	20.7	26.5			21.4	25.2	21.6	24.9				24.8	
.05	23,2	29.6		28.7	24.0		24.2	27.8	24,4	27.5	24.7	27.2	
.10	33.1	41.9			34.3	40.1	34 6 42.9	39.6 48.7	34.9 43.2	48.3		38.7	36
.15	41 48	51.5		50.2	42.4	49.8 57.3	50.1	56.6		56.2	43.6	47.7	45.
,20	54.3	59.6		58.2 65.4	56.1	64.4	56.6		57.0				
.25	60.3	73.5				71.0	62.8		63.8		63.9	69.1	66.
.35	66.1					77.3		76.6		76.1			
,40	71.7										75.7	81 3	78
.45	77.2				79.6					87.9		87.1	84.
.50	82.8		84.3	95.7	85.2							92.9	90
.55		102.8		101.4		100.4				99.3	92.9	98.6	
,60		108.3		107.0	96.7	106.1		105.5		105.0		104.3	
,65			101.7		102.7	111.9			103.9			110.1	107
.70			108.0		109.0	117.8	109.7	117.2	110.2	116.7	110.9	116.1	113.
,75	113.1								116.7			120 4	120
,80	120.4										124.5	1:29.1	126
,85	128.5	139	129.8	138.1	130.7	137.6	131.3	137.1	131.7	136.8	132.3	130.4	134
.90	138, 1	146.9	139.2	146.2	139.9	145.7	140.4	145.4	140.8	145.7	141.3	144.8	148
,95	150.4	156.8	151.8	156.4	151.8	156.0	152.2	155.8	152.5	155.6	152.8	155.3	154.
.96	153.5	159.3	154.3	158.9	154.8	158.6	155.1	158.4	155.4	158.2	155.7	158.0	158
,97	157.1	162.1	157.8	161.8	158.2	161.5	158.5	161.3	158.7	161.2	159.0	161.0	160.
,98	161.3	165.4	161.9	165.1	162.2	164.9	162.5	164.8	162.6	164.7	102.9	161.5	163
.99	166.8	169.7									167.9		
1.00	180	180	180	180	180	180	180	180	180	180	180	180	180

elative Motions of Cross-head and Crank,—If L = length nuecting-rod, R = length of crank, $\theta = \text{angle}$ of crank with centre line gine, D = displacement of cross-head from the beginning of its stroke,

 $3 = R(1 - \cos \theta) + L - \sqrt{L^2 - R^2 \sin^2 \theta}.$

Lap and Travel of Valve.

or Release and Compression.	Ratio of Lap to Travel of Valve.	Ratio of Travel of Valve to Width of Port-open- ing.	Angle between Positions of Crank at Points of Admission and Cut-off, or Release and Compression.	Ratio of Lap to Travel of Valve.	Ratio of Travel of Valve to Width of Port-open- fog.	Angle between Positions of Crank at Points of Admission and Cut-off, or Release and Compression.	Ratio of Lap to Travel of Valve.	Ratio of Travel of Valve to Width of Port-open- ing.
)a 5 7 5 7 5	.4830 .4769 .4699 .4619 .4532 .4435 .4330 .4217 .4096 .3967 .3880	58.70 43.22 83.17 26.27 21.34 17.70 14.93 12.77 11.06 9.68 8.55	85° 90 95 100 105 110 115 130 125	.8586 .8536 .8378 .8214 .3044 .2868 .2687 .2500 .2309 .2113	7.61 6.88 6.17 5.60 5.11 4.69 4.83 4.00 3.73 8.46	185° 140 145 150 155 160 165 170 175 180	.1918 .1710 .1504 .1894 .1082 .0668 .0653 .0436 .0218 .0000	8,34 8,04 2,86 2,70 2,55 2,48 2,30 2,19 2,00

LIODS OF ADMISSION, OB CUT-OFF, FOR VARIOUS LAPS AND TRAVELS OF SLIDE-VALVES.

itwo following tables are from Clark on the Stram-engine. In the first are given the periods of admission corresponding to travels of valve m 12 in. to 2 in., and laps of from 2 in. to 26 in., with 14 in. and 15 in. of With greater leads than those tabulated, the steam would be ant off than as shown in the table.

influence of a lead of 5/16 in. for travels of from 154 in. to 6 in., and if from 14 in. to 114 in., as calculated for in the second table, is exhibited mparison of the periods of admission in the table, for the same lap and l. The greater lead shortens the period of admission, and increases the for expansive working.

ods of Admission, or Points of Cut-off, for Given Travels and Laps of Slide-valves.

Lead.	Perio	xls of	Admis	sion, o Laps o	r Poin f Val	ts of C res in i	ut off, nches	for th	e tollo	wing
	8	134	11/6	114	1	%	34	96	14	36
in. 444 444 646 646 646 646 646 646 646 64	\$88 882 722 500 443 832 14	\$0 87 78 62 56 47 85 17	\$39 89 84 71 68 61 51	\$ 95 92 88 79 77 72 66 57 44 23	95 95 92 86 85 82 78 72 63 50 27	97 96 94 89 88 88 78 71 61	98 98 97 95 91 91 89 87 83 79 71	98 98 96 94 94 92 90 88 84 79 70	*38888888888888888888888888888888888888	99 99 98 97 97 97 96 95 94 91 88

Periods of Admission, or Points of Cut-off, for given Travels and Laps of Slide-valves.

Constant lead, 5/16,

Travel.	_					1			
Inches.	1/6	56	3/4	3/6	1	13/6	134	1%	13%
15/8 15/4 17/8 2	19								
194	39								
134	47	17							
2	55	34							
21/6 21/4	61	42	14		.	1	<i>.</i>	l	
21/4	65	50	30						
29%	68	55	30 38	13				l	.
212	71	59	45	27					
25%	74	63 67 70 73	49	86	12			[.]	
22/4 27/6 31/4 37/6 37/6 37/6 37/6 37/4	76 78 80	67	56 59 62	43	26	}			
274	78	70	59	47	82	11		·	l
8	80	73	62	50	88	23	 .	 .	l
31/4	81	74	65	55	44	30	10	. <i>.</i>	l
314	83	76	68	59	48	84	22		l
89%	84	78	71	62	51	40	22 29 34 38 42	9	.
816	85	80	73	64	53	45	34	20 26 32	l
852	86	81	75	66	57	49	38	26	9
394	87	82	76	68	60	52	42	82	19
874	87	83	78	70	63	55	46	136	25
4"	88	84	79	72	66	58	49	40	29 27
41/4	89	86	81	76	70	68	56 61	47	27
412	90	87	83	79	78	67	61	54	45
41/4 41/4 48/4 5 51/6	81 83 84 85 86 87 87 88 89 90 92	74 76 78 80 81 82 83 84 86 87 89	65 68 71 73 75 76 78 79 81 83 85	27 36 43 47 50 55 62 64 66 68 70 72 76 79 81	76	70	65	58	45 51 56
5	98	90	87	83	78	78	67	62	56
516	94	92	89	86	82	78	78	68	63
6 6	95	98	89 91	86 88	26 328 344 48 553 57 60 66 70 78 82 85	30 34 40 45 49 52 55 58 68 67 70 73 88	78 78	68 74	68 69

Diagram for Port-opening, Cut-off, and Lap.—The diagram on the opposite page was published in *Power*, Aug., 1898. It shows at a glance the relations existing between the outside lap, steam port-opening, and cut-off in slide valve engines.

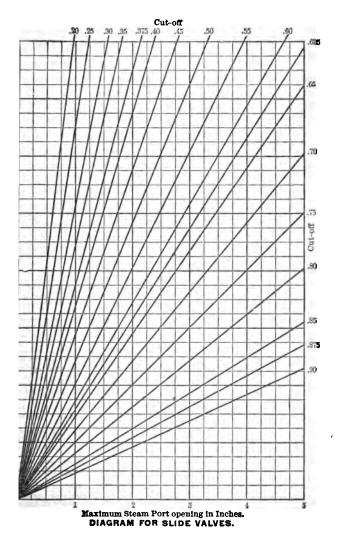
In order to use the diagram to find the lap, having given the cut-off and maximum port-opening, follow the ordinate representing the latter, taken on the horizontal scale until it meets the oblique line representing the given cut-off. Then read off this height on the vertical lap scale. Thus, with a

port-opening of 1% inch and a cut-off of .50, the intersection of the two lines occurs on the horizontal 3. The required lap is therefore 3 in.

If the cut-off and lap are given follow the horizontal representing the latter until it meets the oblique line representing the cut-off. Then vertically

ister until it meets the collique line representing the cut-off. Then vertically below this read the corresponding port-opening on the horizontal scale. If the lap and port-opening are given, the resulting cut-off may be ascertained by finding the point of intersection of the ordinate representing the port-opening with the horizontal representing the lap. The oblique line passing through the point of intersection will give the cut-off. If it is desired to take lead into account, multiply the lead in inches by the numbers in the following table corresponding to the cut-off, and deduct the result from the lap as obtained from the diagram:

Cut-off.	Multiplier.	Cut-off.	Multiplier.
.20	4.717	.60	1.858
.25	8.731	.625	1.288
.30	8.048	.625 .65	1.222
.30 .33 .875	2.717	.70	1,108
.875	2.881	.75	1,000
.40	2.171	.80	0.904
	1.930	.85	0.815
.45 .50 .55	1.706	.875	0.772
.55	1.515	.90	0.781



F1G. 149.

Piston-valve.—The piston-valve is a modified form of the slide-valve. The lap, lead, etc., are calculated in the same manner as for the common slide-valve. The diameter of valve and amount of port-opening are calculated on the basis that the most contracted portion of the steam-passage between the valve and the cylinder should have an area such that the velocity of steam through it will not exceed 6000 ft. per minute. The area of the opening around the circumference of the valve should be about double the area of the steam-passage, since that portion of the opening that is

the area of the steam-passage, since that pornon of the opening that is opposite from the steam-passage is of little effect.

Setting the Valves of an Engine.—The principles discussed above are applicable not only to the designing of valves, but also to adjustment of valves that have been improperly set; but the final adjustment of the eccentric and of the length of the rod depend upon the amount of lost motion, temperature, etc., and can be effected only after trial. After the valve has been set as accurately as possible when cold, the lead and lap for the forward and return strokes being equalized, indicator diagrams should be taken and the length of the eccentric-rod adjusted, if necessary, to cor-

rect slight irregularities.

To Put an Engine on its Centre.—Place the engine in a posi-tion where the piston will have nearly completed its outward stroke, and opposite some point on the cross head, such as a corner, make a mark upon the guide. Against the rim of the pulley or crank-disk place a pointer and mark a line with it on the pulley. Then turn the engine over the centre until the cross-head is again in the same position on its inward stroke. This will bring the crank as much below the centre as it was above it before. With the pring thecrank as much below the centre as it was above it serors. With the pointer in the same position as before make a second mark on the pulleyrim. Divide the distance between the marks in two and mark the middle point. Turn the engine until the pointer is opposite this middle point, and it will then be on its centre. To avoid the error that may arise from the looseness of crank-pin and wrist-pin bearings, the engine should be turned a little above the centre and then be brought up to it, so that the crank pin will press against the same brass that it does when the first two marks are

Link-motion.—Link-motions, of which the Stephenson link is the most commonly used, are designed for two purposes: first, for reversing the motion of the engine, and second, for varying the point of cut-off by varying the travel of the valve. The Stephenson link-motion is a combination of two eccentrics, selled forward and back eccentrics, with a link connecting the extremities of the eccentric-rods; so that by varying the position of the link the valve-rod may be put in direct connection with either eccentric, or may be given a movement controlled in part by one and in part by the other eccentric. When the link is moved by the reversing lever into a position such that the block to which the valve-rod is attached is at either end of the link, the valve receives its maximum travel, and when the link is in mid-gear the travel is the least and cut-off takes place early in the stroke.

mid-gear the travel is the least and cut-out taxes place early at the surface. In the ordinary shifting-link with open rods, that is, not crossed, the lead of the valve increases as the link is moved from full to mid-gear, that is, as the period of steam admission is shortened. The variation of lead is equalized for the front and back strokes by curving the link to the radius of the eccentric-rods concavely to the axles. With crossed eccentric-rods the lead eccentric-rods concavely to the axles. With crossed eccentric-rods the lead decreases as the link is moved from full to mid-gear. In a valve-motion with stationary link the lead is constant. (For illustration see Clark's Steamengine, vol. fi. p. 22.)

The linear advance of each eccentric is equal to that of the valve in full gear, that is, to lap + lead of the valve, when the eccentric-rods are attached to the link in such position as to cause the half-travel of the valve to equal the eccentricity of the eccentric.

The angle between the two eccentric radii, that is, between lines drawn from the centre of the eccentric disks to the centre of the shaft equals 180°

less twice the angular advance.

Buel, in Appleton's Cyclopedia of Mechanics, vol. ii. p. 316, discusses the Stephenson link as follows: "The Stephenson link does not give a perfectly correct distribution of steam; the lead varies for different points of cut-off The period of admission and the beginning of exhaust are not alike for both ends of the cylinder, and the forward motion varies from the backward. "The correctness of the distribution of steam by Stephenson's link-motion

depends upon conditions which, as much as the circumstances will permit, ought to be fulfilled, namely: 1. The lish should be curved in the arc of a circle whose radius is equal to the length of the eccentric-rod. 2 The

itric-rods ought to be long; the longer they are in proportion to the itricity the more symmetrical will the travel of the valve be on both of the centre of motion. 3. The link ought to be short. Each of its a describes a curve in a vertical plane, whose ordinates grow larger the or the considered point is from the centre of the link; and as the horid motion only is transmitted to the valve, vertical oscillation will cause ularities. 4. The link-hanger ought to be long. The longer it is the will be the are in which the link is suspended in its centre, the sthat are described by points equidistant on both sides from the centre of allike, and hence results the variation between the forward and backgear. If the link is suspended at its lower end, its lower half will have vertical oscillation and the upper half more. 5. The centre from which ink-hanger swings changes its position as the link is lowered or raised, the occases irrecularities. To reduce them to the smallest amount the of the lifting-shaft should be placed at the height corresponding to enteral position of the centre on which the link-hanger swings."

these conditions can never be fulfilled in practice, and the variations is lead and the period of admission can be somewhat regulated in an itself way, but for one grear only. This is accomplished by giving differend to the two eccentrics, which difference will be smaller the longer the ntric-rods are and the shorter the link, and by suspending the link not try on its centre line but at a certain distance from it, giving what is

d" the offset."

r application of the Zeuner diagram to link-motion, see Holmes on the m-engine, p. 290. See also Clark's Railway Machinery (1865), Clark's m-engine, Zeuner's and Auchincloss's Treatises on Slide-valve Gears, Halsey's Locomotive Link Motion. (See page 859a.)

e following rules are given by the American Machinist for laying out a for an upright slide-valve engine. By the term radius of link is meant adius of the link-are ab, Fig. 150, drawn through the centre of the slot;

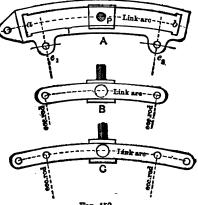


Fig. 150.

radius is generally made equal to the distance from the centre of shaft antre of the link-block pin P when the latter stands midway of its travel, distance between the centres of the eccentric-rod pins e, e, should not set than 2½ times, and, when space will permit, three times the throw of eccentric. By the throw we mean twice the eccentricity of the eccentricate is generally suspended from the end next to the forward eccent a point in the link-are prolonged. This will give comparatively a II amount of alip to the link-block when the link is in forward gear; but alip will be increased when the link is in backward gear. This increase

of slip is, however, considered of little importance, because marine engines, as a rule, work but very little in the backward gear. When it is necessary that the motion shall be as efficient in backward gear as in forward gear, then the link should be suspended from a point midway between the two eccentric-rod pins; in marine engine practice this point is generally located on the link-arc; for equal cut-offs it is better to move the point of suspension a small amount towards the eccentrics.

For obtaining the dimensions of the link in inches: Let L denote the length of the valve, B the breadth, p the absolute steam-pressure per sq. in., and R a factor of computation used as below; then $R = .01 \sqrt{L \times B \times p}$.

Breadth of the link	=	$R \times 1.6$
Thickness T of the bar		
Length of sliding-block	=	$R \times 2.5$
Diameter of eccentric-rod pins	=	$(R \times .7) + 14$
Diameter of suspension-rod pin	=	$(R \times .6) + 12$
Diameter of suspension-rod pin when overhung	=	$(R \times .8) + 14$
Diameter of block-pin when overhung	=	R+14
Diameter of block-pin when overhung Diameter of block-pin when secured at both ends	=	$(R \times 8) + 14$

The length of the link, that is, the distance from a to b, measured on a straight line joining the ends of the link-arc in the slot, should be such as to allow the centre of the link-block pin P to be placed in a line with the eccentric-rod pins, leaving sufficient room for the slip of the block. Another type of link frequently used in marine engines is the double-bar link, and this type is again divided into two classes: one class embraces those links which have the eccentric-rod ends as well as the valve-spindle end between the bars, as shown at B (with these links the travel of the valve is less than the throw of the eccentric); the other class embraces those links, shown at C, for which the eccentric-rods are made with fork-ends, so as to connect to stude on the outside of the bars, allowing the block to slide to the end of the link, so that the centres of the eccentric-rod ends and the block-pin are in line when in full gear, making the travel of the valve equal to the throw of the eccentric. The dimensions of these links when the distance between the eccentric-rod pins is 2½ to 2¾ times the throw of eccentrics can be found as follows:

Depth of bars	=	$(R \times 1.25) + \frac{1}{4}$ "
Thickness of bars	=	$(R \times .5) + \frac{1}{2}$ "
Diameter of centre of sliding-block	=	$R \times 1.8$

When the distance between the eccentric-rod pins is equal to 8 or 4 times the throw of the eccentrics, then

Depth of bars
$$= (R \times 1.25) + \frac{1}{2}$$
 Thickness of bars $= (R \times 1.25) + \frac{1}{2}$

All the other dimensions may be found by the first table. These are em-An into the remains may see found by the irise table. In see are empirical rules, and the results may have to be slightly changed to suit given conditions. In marine engines the eccentric-rod ends for all classes of links have adjustable brasses. In locomotives the slot-link is usually employed, and in these the pin-holes have case-hardened bushes driven into the pin-holes, and have no adjustable brasses in the ends of the eccentric-rods. The link in B is generally suspended by one of the eccentric-rod pins; and the link in C is suspended by one of the pins in the end of the link, or by one of the eccentric-rod pins. (See note on Locomotive Link Motion in Appendix. p. 1077.)

Other Rorms of Valve-Gear, as the Joy, Marshall, Hackworth, Bremme, Walschaert, Corliss, etc., are described in Clark's Steam-engine, vol. ii. The design of the Reynolds-Corliss valve-gear is discussed by A. H. Eldridge in Power, Sep. 1898. See also Henthorn on the Corliss engine. Bules for laying down the centre lines of the Joy valve-gear are given in American Machinist, Nov. 18, 1890. For Joy's "Fluid-pressure Reversingvalve," see *Eng'g*, May 25, 1894.

GOVERNORS.

Pendulum or Fly-ball Governor.—The inclination of the arms of a revolving pendulum to a vertical axis is such that the height of the point of suspension h above the horizontal plane in which the centre of ravity of the balls revolve (assuming the weight of the rods to be small

ipared with the weight of the balls) bears to the radius r of the circle cribed by the centres of the balls the ratio

$$\frac{h}{r} = \frac{\text{weight}}{\text{centrifugal force}} = \frac{w}{\frac{wv^2}{gr}} = \frac{gr}{v^2},$$

ich ratio is independent of the weight of the balls, v being the velocity the centres of the balls in feet per second. ? T = number of revolutions of the balls in 1 second, $v = 2\pi rT = ar$, in ich a = the angular velocity, or $2\pi T$, and

$$h = \frac{gr^2}{v^3} = \frac{g}{4\pi^2 T^2}$$
, or $h = \frac{0.8146}{T^2}$ feet $= \frac{9.775}{T^2}$ inches,

eing taken at 32.16. If N = number of revs. per minute, $h = \frac{35196}{N^2}$ 108.

For revolutions per minute..... The height in inches will be..... 45 21.99 17.38 14.08 9.775 6.256

umber of turns per minute required to cause the arms to take a given le with the vertical axis: Let l = length of the arm in inches from the tre of suspension to the centre of gyration, and a the required angle;

$$N = \sqrt{\frac{35190}{l \cos a}} = 187.6 \sqrt{\frac{1}{l \cos a}} = 187.6 \sqrt{\frac{1}{h}}$$

ad; then
$$a = \sqrt{\frac{32.16}{h} \left(1 + \frac{2l_1}{l} \frac{Q}{G}\right)}$$
; $h = \frac{32.16}{a^2} \left(1 + \frac{2l_1}{l} \frac{Q}{G}\right)$ in feet, or

 $\frac{85190}{N^2}\left(1+\frac{2l_1}{l}\frac{Q}{G}\right)$ in inches, N being the number of revolutions per

r various forms of governor see App. Cycl. Mech., vol. ii. 61, and Clark's

or various forms of governor see App. Cycl. Mech., vol. ii. 61, and Clark's m-engine, vol. ii. p. 65.

o Change the Speed of an Engine Having a Fly-ball vernor.—A slight difference in the speed of a governor changes the tion of its weights from that required for full load to that required for ad. It is evident therefore that, whatever the speed of the engine, the nal speed of the governor must be that for which the governor was ded; i.e., the speed of the governor must be kept the same. To change the dof the engine the problem is to so adjust the pulleys which drive the ernor that the engine at its new speed shall drive it just as fast as it was en at its original speed. In order to increase the engine-speed we must ease the pulley upon the shaft of the engine, i.e., the driver, or increase on the governor, i.e., the driven, in the proportion that the speed of the on the governor, i.e., the driven, in the proportion that the speed of the ne is to be increased.

Fly-wheel or Shaft Governors,-At the Centennial Exhibition in 1876 there were shown a few steam-engines in which the governors were contained in the fly-wheel or band-wheel, the fly-balls or weights revolving around the shaft in a vertical plane with the wheel and shifting the eccentric so as autometically to vary the travel of the valve and the point of cut. tric so as automatically to vary the travel of the valve and the point of curoff. This form of governor has since come into extensive use, especially for
high-speed engines. In its usual form two weights are carried on arms the
ends of which are proveded to two points on the pulley near its circum
ference, 180° apart. Links connect these arms to the eccentric. The
eccentric is not rigidly keyed to the shaft but is free to move transversely across it for a certain distance, having an oblong hole which allows
of this movement. Centrifugal force causes the weights to fly towards the
elicumference of the wheel and to mult the excentric into a rosition of minof this movement. Centrifugal force causes the weights to fly towards the circumference of the wheel and to pull the eccentric into a position of minimum eccentricity. This force is resisted by a spring attached to each arm which tends to pull the weights towards the shaft and shift the eccentric to the position of maximum eccentricity. The travel of the valve is thus varied, so that it tends to cut off earlier in the stroke as the engine increases its speed. Many modifications of this general form are in use. For discussions of this form of governor see Hartnell, Proc. Inst. M. E., 1882, p. 408: Trans. A. S. M. E., ix. 300; xi. 1061; xiv. 92; xv. 929; Modern Mechanism, p. 399; Whitham's Constructive Steam Engineering; J. Begtrup, Am. Mach., Oct. 19 and bec. 14, 1893, Jan. 18 and March 1, 1894.

Calculation of Springs for Shaft-governors. (Wilson Hart-

Calculation of Springs for Shaft-governors. (Wilson Hart-neil, Proc. Inst. M. E., Aug. 1882.)—The springs for shaft-governors may be conveniently calculated as follows, dimensions being in inches:

Let W =weight of the balls or weights, in pounds:

 r_1 and r_2 = the maximum and minimum radial distances of the centre of the balls or of the centre of gravity of the weights;

l₁ and l₂ = the leverages, i.e., the perpendicular distances from the centre of the weight-pin to a line in the direction of the centrifugal force drawn through the centre of gravity of the weights or balls at radii

 m_1 and m_2 = the corresponding leverages of the springs; C_1 and C_2 = the centrifugal forces, for 100 revolutions per minute, at

radii r_1 and r_2 ; P_1 and P_2 = the corresponding pressures on the spring; (It is convenient to calculate these and note them down for reference.) C_3 and C_4 = maximum and minimum centrifugal forces;

8 = mean speed (revolutions per minute);

 S_1 and S_2 = the maximum and minimum number of revolutions per minute;

minute; P_0 and P_0 = the pressures on the spring at the limiting number of revolutions $(S_1$ and $S_2)$; $P_0 - P_1 = D$ = the difference of the maximum and minimum pressures on the springs; V = the percentage of variation from the mean speed, or the sensitive

t = the travel of the spring;
 u = the initial extension of the spring;

v = the stiffness in pounds per inch;

w =the maximum extension = u + t.

The mean speed and sensitiveness desired are supposed to be given. Then

$$\begin{split} S_1 &= S - \frac{SV}{100}; & S_2 &= S + \frac{SV}{100}; \\ C_1 &= 0.28 \times r_1 \times W; & C_2 &= 0.28 \times r_2 \times W; \\ P_1 &= C_1 \times \frac{l_1}{n_1}; & P_3 &= C_2 \times \frac{l_3}{n_2}; \\ P_3 &= P_1 \times \left(\frac{S_1}{100}\right)^2; & P_4 &= P_2 \times \left(\frac{S_2}{100}\right)^3; \\ v &= \frac{D}{t}, \ u &= \frac{P_3}{n}, \ w &= \frac{P_4}{n}. \end{split}$$

It is usual to give the spring-maker the values of P_4 and of v or w. To ensure proper space being provided, the dimensions of the spring should be

sulated by the formulæ for strength and extension of springs, and the st length of the spring as compressed be determined.

The governor-power =
$$\frac{P_3 + P_4}{2} \times \frac{t}{12}$$
.

Vith a straight centripetal line, the governor-power

$$=\frac{C_3+C_4}{9}\times \left(\frac{r_3-r_1}{19}\right).$$

or a preliminary determination of the governor-power it may be taken squal to this in all cases, although it is evident that with a curved ceneral line it will be slightly less. The difference D must be constant for same spring, however great or little its initial compression. Let the ing be screwed up until its minimum pressure is P_b . Then to find the cd $P_b = P_b + D$,

$$S_{\delta} = 100 \sqrt{\frac{\overline{P}_{\delta}}{\overline{P}_{i}}}; \qquad S_{\epsilon} = 100 \sqrt{\frac{\overline{P}_{\delta}}{\overline{P}_{\delta}}}.$$

he speed at which the governor would be isochronous would be

$$100\sqrt{\frac{D}{P_1-P_1}}$$

uppose the pressure on the spring with a speed of 100 revolutions, at the ximum and minimum radii, was 200 lbs. and 100 lbs., respectively, then pressure of the spring to suit a variation from 95 to 105 revolutions will $100 \times \left(\frac{95}{100}\right)^2 = 90.2$ and $200 \times \left(\frac{105}{100}\right)^2 = 220.5$. That is, the increase esistance from the minimum to the maximum radius must be 220-90 = 10s. be extreme speeds due to such a spring, screwed up to different pressar are shown in the following table:

he speed at which the governor would become isochronous is 114. ny spring will give the right variation at some speed; hence in experiting with a governor the correct spring may be found from any wrong by a very simple calculation. Thus, if a governor with a spring whose loses is 50 libs. per inch acts best when the engine runs at 25, 30 being its per speed, then $50 \times \left(\frac{90}{95}\right)^3 = 45$ lbs. is the stiffness of spring required. In determine the speed at which the governor acts best, the springs may crowed up until it begins to "hunt" and then slackened until the governor acts as a scompatible with steadiness.

CONDENSERS, AIR-PUMPS CIRCULATING-PUMPS, ETC.

he Jet Condenser. (Chiefly abridged from Seaton's Marine Enginal.)—The jet condenser is now uncommon in marine practice, being really supplanted by the surface condenser. It is commonly used where I water is available for boiler feed. With the jet condenser a vacuum of 24 ras considered fairly good, and 25 in, as much as was possible with most lensers; the temperature corresponding to 24 in. vacuum, or 8 lbs. pressure dute, is 140°. In practice the temperature in the hot-well varies from 110° 10°, and occasionally as much as 180° is maintained. To find the quantity rjection-water per pound of steam to be condensed: Let T, when the cooling of t

water; T_2 = temperature of the water after condensation, or of the hot-well; Q =pounds of the cooling-water per lb. of steam condensed; then

$$Q=\frac{1114^{\circ}+0.3T_{1}-T_{2}}{T_{2}-T_{0}}.$$

Another formula is: $Q = \frac{WH}{R}$, in which W is the weight of steam con-

densed, H the units of heat given up by 1 lb. of steam in condensing, and R the rise in temperature of the cooling-water.

This is applicable both to jet and to surface condensers. The allowance made for the injection-water of engines working in the temperate zone is usually 27 to 30 times the weight of steam, and for the tropics 30 to 35 times; 30 times is sufficient for ships which are occasionally in the tropics, and this is what we usual to ellow for convert traders. what was usual to allow for general traders.

Area of injection orifice = weight of injection-water in lbs. per min. + 650

A rough rule sometimes used is: Allow one fifteenth of a square inch for every cubic foot of water condensed per hour.

Another rule: Area of injection orifice = area of piston + 250. The volume of the jet condenser is from one fourth to one half of that of the cylinder. It need not be more than one third, except for very quickrupning engines.

Ejector Condensers.—For ejector or injector condensers (Bulkley's, Schutte's, etc.) the calculations for quantity of condensing-water is the same as for jet condensers.

as for jet condensers.

The Surface Condenser—Cooling Surface.—Pecket found that with cooling water of an initial temperature of the to 77°, one sq. ft. of copper plate condensed 21.5 lbs. of steam per hour, while Joule states that 100 lbs. per hour can be condensed. In practice, with the compound engine, brass condenser-tubes, 13 B.W.G thick, 18 lbs. of steam per sq. ft. per hour, with the cooling-water at an initial temperature of 60°, is considered very fair work when the temperature of the feed-water is to be maintained at 120°. It has been found that the surface in the condenser may be half the heating surface of the helicar and under some circumstances considerably less than surface of the boiler, and under some circumstances considerably less than this. In general practice the following holds good when the temperature of sea-water is about 60°:

Terminal pres., lbs., abs.... മ Sq. ft. per I.H.P.... 2.50 1.80 1.60 1.50

For ships whose station is in the tropics the allowance should be increased by 20%, and for ships which occasionally visit the tropics 10% increase will give satisfactory results. If a ship is constantly employed in cold climates 10% lers suffices

Whitham (Steam-engine Design, p. 288, also Trans. A. S. M. E., ix. 481) gives the following: $S = \frac{WL}{ck(T_1 - t)}$, in which S = condensing surface in sq.

ft.; T_1 = temperature Fahr. of steam of the pressure indicated by the vacuum gauge; t = mean temperature of the circulating water, or the arithmetical mean of the initial and final temperatures; L = latent heat of saturated steam at temperature T_1 ; k = perfect conductivity of 1 sq. ft. of the metal used for the condensing surface for a range of 1° F. (or 557 B.T.U. per hour for brass, according to lisherwood's experiments); c = fraction denoting the efficiency of the condensing surface; W = pounds of steam condensed per hour. From experiments by Loring and Emery, on U.S.S. Dallas.

c is found to be 0.323, and ck=180; making the equation $S=\frac{1}{180(T_1-t)}$

Whitham recommends this formula for designing engines having indepen dent circulating pumps. When the pump is worked by the main engine the value of S abould be increased about 10%.

Taking T_1 at 135° F., and L=1020, corresponding to 25 in, vacuum, and 35°

1020 W for summer temperatures at 75°, we have: S =180(135 - 75)

For a mathematical discussion of the efficiency of surface condensers see a paper by T. E. Stanton in Proc. Inst. C. E., cxxxvi, June 1899, p. 321. Condenser Tubes are generally made of solid-drawn brass tubes, and

tested both by hydraulic pressure and steam. They are usually made of a composition of 68% of flest selected copper and 82% of best Silesian spelter.

Admiralty, however, always specify the tubes to be made of 70% of best cted copper and to have 1% of tin in the composition, and test the tubes

pressure of 300 lbs. per sq. in. (Seaton.) he diameter of the condenser tubes varies from 1/4 inch in small condenser. s, when they are very short, to I inch in very large condensers and longes. In the mercantile marine the tubes are, as a rule, % inch diameter ernally, and 18 B.W.G. thick (0.049 inch); and 16 B.W.G. (0.055), under exceptional circumstances. In the British Navy the tubes are also, a rule, % inch diameter, and 18 to 19 B.W.G. thick, tinned on both sides; in the condenser is made of brass the Admiralty do not require the tubes be tinned. Some of the smaller engines have tubes % inch diameter, and l.W.G. thick. The smaller the tubes, the larger is the surface which be got in a certain space.

the merchant service the almost universal practice is to circulate the

er through the tubes.

hitham says the velocity of flow through the tubes should not be less

n 400 nor more than 700 ft. per min.

'ube-plates are usually made of brass. Rolled-brass tube-plates uld be from 1.1 to 1.5 times the diameter of tubes in thickness, depending he method of packing. When the packings go completely through the est he latter, but when only partly through the former, is sufficient, ice, for 34-inch tubes the plates are usually % to 1 inch thick with glands tape-packings, and 1 to 134 inch thick with wooden ferrules.

The tube-plates should be secured to their seatings by brass stude and the brase corner below in the control of the contr

ne tube-plates should be secured to their seatings by brass studs and 3, or brass scrow-bolts; in fact there must be no wrought iron of any 1 inside a condenser. When the tube-plates are of large area it is advisto stay them by brass-rods, to prevent them from collapsing, pacing of Tubes, etc.—The holes for ferrules, glands, or indiacer are usually ½ inch larger in diameter than the tubes; but when abtely necessary the wood ferrules may be only 3/32 inch thick. In the plate of tubes when packed with wood ferrules is usually ½ inch e than the diameter of the ferrule-hole. For example, the tubes are arelly arranged signar and the number which may be fitted into a

erally arranged zigzag, and the number which may be fitted into a are foot of plate is as follows:

ch of ubes.	No. in a sq. ft.	Pitch of Tubes.	No. in a sq. ft.	Pitch of Tubes.	No. in a sq. ft.
1/16"	172	1 5/82"	128	134"	110
	150	1 3/16"	121	1 9/82"	106
	137	1 7/32"	116	1 5/16"	99

mantity of Cooling Water.—The quantity depends chiefly upon itial temperature, which in Atlantic practice may vary from 40° in the or of temperate zone to 80° in subtropical seas. To raise the temperate 100° in the condenser will require three times as many thermal units e former case as in the latter, and therefore only one third as much ng-water will be required in the former case as in the latter.

$$Q=$$
 quantity of circulating water in lbs. = $\frac{1114+0.3(T_1-T_2)}{T_2-T_0}$.

s usual to provide pumping power sufficient to supply 40 times the it of steam for general traders, and as much as 50 times for ships stain subtropical seas, when the engines are compound. If the circular ump is double-acting, its capacity may be 1/58 in the former and 1/42 latter case of the capacity of the low-pressure cylinder.

r-pump.—The air-pump in all condensers abstracts the water condand the air originally contained in the water when it entered the

. In the case of jet-condensers it also pumps out the water of contion and the air which it contained. The size of the pump is calculate these conditions, making allowance for efficiency of the pump.

Ordinary sea-water contains, mechanically mixed with it, 1/20 of its volume of air when under the atmospheric pressure. Suppose the pressure in the condenser to be 2 lbs. and the atmospheric pressure 15 lbs., neglecting the effect of temperature, the air on entering the condenser will be expanded to 15/2 times its original volume; so that a cubic foot of see-water, when it has entered the condenser, is represented by 19/20 of a cubic foot of water and 15/40 of a cubic foot of air.

Let q be the volume of water condensed per minute, and Q the volume of sea-water required to condense it; and let T, be the temperature of the

condenser, and T_1 that of the sea-water. Then 19/20 (q+Q) will be the volume of water to be pumped from the condenser per minute,

and
$$\frac{15}{40}(q+Q) \times \frac{T_1 + 461^{\circ}}{T_1 + 461^{\circ}}$$
 the quantity of air.

If the temperature of the condenser be taken at 120°, and that of seawater at 60°, the quantity of air will then be .418(q+Q), so that the total volume to be abstracted will be

$$.95(q+Q) + .418(q+Q) = 1.768(q+Q).$$

If the average quantity of injection-water be taken at 25 times that condensed, q+Q will equal 27q. Therefore, volume to be pumped from the condenser per minute = 37q, nearly. In surface condensation allowance must be made for the water occasion—

ally admitted to the boilers to make up for waste, and the air contained in it, also for slight leak in the joints and glands, so that the air-pump is made

It, also for slight least in the joints and glands, so that the air-pump is made about half as large as for jet-condensation.

The efficiency of a single-acting air-pump is generally taken at 0.5, and that of a double-acting pump at 0.35. When the temperatur of the sea is 60°, and that of the jet) condenser is 120°. Q being the volume of the cooling water and q the volume of the condensed water in cubic feet, and a the number of strokes per minute,

The volume of the single-acting pump = $2.74 \left(\frac{Q+q}{r} \right)$.

The volume of the double-acting pump = $4(\frac{Q+q}{q})$.

The following table gives the ratio of capacity of cylinder or cylinders to that of the air-pump; in the case of the compound engine, the low-pressure cylinder capacity only is taken.

Description of Pump.	Description of Engine.	Ratio.	
Single-acting vertical """" """" Double-acting horizontal """" """" """" """" """" """" """"	Jet-condensing, expansion 114 to 2 Surface " " 114 to 2 Jet " 3 to 5 Surface " compound Jet " expansion 114 to 2 Surface " compound Jet " a sto 5 Jet " 3 to 5 Surface " 3 to 5 Surface " 5 to 5 Surface " compound	6 to 8 8 to 10 10 to 13 12 to 15 15 to 18 10 to 13 15 to 16 16 to 19 19 to 24 94 to 28	

The Area through Valve-seats and past the valves should not be less than will admit the full quantity of water for condensation at a velocity not exceeding 400 ft. per minute. In practice the area is generally in excess of this.

Area through foot-valves $= D^2 \times S + 1000$ square inches. Area through head-valves $= D^2 \times S + 800$ square inches.

Diameter of discharge-pipe = $D \times \sqrt{8} + 35$ inches. $D = \text{diam. of air-pump in inches, } \theta = \text{its speed in ft. per min.}$

mes Tribe (Am. Mach., Oct. 8, 1891) gives the following rule for all-

mps used with jet-condensers: Volume of single-acting air-pump driven main engine = volume of low-pressure cylinder in cubic feet, multiplied 8.5 and divided by the number of cubic feet contained in one pound of saust-steam of the given density. For a double-acting air-pump the ne rule will apply, but the volume of steam for each stroke of the pump 1 be but one half. Should the pump be driven independently of the fine, then the relative speed must be considered. Volume of jet-conser = volume of air-pump × 4. Area of injection valve = vol. of air-pump in cubic inches + 520.

Freulating-pump.—Let Q be the quantity of cooling water in cubic t, n the number of strokes per minute, and S the length of stroke in feet.

Capacity of circulating-pump = Q + n cubic feet.

Diameter " = 18.55
$$\sqrt{\frac{Q}{n \times S}}$$
 inches.

The following table gives the ratio of capacity of steam-cylinder or cyliners to that of the circulating pump:

Description	on of Pump.	Description of Engine.	Ratio.
Single-a	cting.	Expansive 114 to 2 times.	18 to 16
**		Compound.	90 to 25 25 to 30
Double	66 68	Expansive 11% to 2 times.	25 to 30
	4	Compound.	36 to 46 46 to 56

The cear area through the valve-seats and past the valves should be such at the mean velocity of flow does not exceed 450 feet per minute. The w through the pipes should not exceed 500 ft. per min. in small pipes and 0 in large pipes.

For Centrifugal Circulating-pumps, the velocity of flow in the inlet and the pipes should not exceed 400 ft. per min. The diameter of the fan-wheel from 2% to 8 times the diam. of the pipe, and the speed at its periphery 0 to 500 ft. per min. If W = quantity of water per minute, in American Illons, d = diameter of pipes in inches, R = revolutions of wheel per min.

= $\sqrt{\frac{W}{16.44}}$; diam. of fan-wheel = not less than $\frac{1700}{R}$. Breadth of blade at

 $0 = \frac{W}{36d}.$ Diam. of cylinder for driving the fan = about 2.8 $\sqrt{\text{diam. of pipe}}$,

d its stroke = 0.28 \times diam. of fan. Feed-pumps for Marine Engines.—With surface-condensing gines the amount of water to be fed by the pump is the amount condensed om the main engine plus what may be needed to supply auxiliary engines d to supply leakage and waste. Since an accident may happen to the rface-condenser, requiring the use of jet-condensation, the pumps of gines fitted with surface-condensers must be sufficiently large to do duty der such circumstances. With jet-condensers and bollers using salt water e dense salt water in the boller must be blown off at intervals to keep the nsity so low that deposits of salt will not be formed. Sea-water contains out 1/32 of its weight of solid matter in solution. The boiler of a surfacendensing engine may be worked with safety when the quantity of salt is ur times that in sea-water. If Q = net quantity of feed-water required in tyen time to make up for what is used as steam, n = number of times the itness of the water in the boiler is to that of sea-water, then the gross feed-

ster $=\frac{n}{n-1}Q$. In order to be capable of filling the boiler rapidly each ad-pump is made of a capacity equal to twice the gross feed-water. Two ad-pumps should be supplied, so that one may be kept in reserve to be ed while the other is out of repair. If Q be the quantity of net feed-water cubic feet, l the length of stroke of feed-pump in feet, and n the numr of strokes per minute,

Diameter of each feed-pump plunger in inches = $\sqrt{\frac{550 \times Q}{n \times k}}$

If W be the not feed-water in pounds,

Diameter of each feed-pump plunger in inches =
$$\sqrt{\frac{8.9 \times W}{n \times l}}$$

An Evaporative Surface Condenser built at the Virginia Agricultural College is described by James H. Fitts (Trans. A. S. M. E., xiv. 690). It consists of two rectangular end chambers connected by a series of horizontal rows of tubes, each row of tubes immersed in a pan of water. Through the spaces between the surface of the water in each pan and the bottom of the pan above air is drawn by means of an exhaust-fan. At the cop of one of the end-chambers is an inlet for steam, and a horizontal diaphragm about midway causes the steam to traverse the upper half of the tubes and back through the lower. An outlet at the bottom leagts to the airpump. The condenser, exclusive of connection to the exhaust-fan, occupies a floor space of 5'41/4" × 1'93/", and 4'11/4" high. There are 27 rows of tubes, 8 in some and 7 in others; 210 tubes in all. The tubes are of brass, No 20 B.W.G., 3/" external diameter and 4'93/" in length. The cooling surface (internal) is 176.5 sq. ft. There are 27 cooling pans, each 4'93/" × 1'93/", and 17/16" deep. These pans have galvanized iron bottoms which slide into horizontal grooves 1/4" wide and 1/4" deep, planed into the tube-sheets. The total evaporating surface is 234.8 sq. ft. Water is fed to every third pan through small cocks, and overflow-pipes feed the rest. A wood casing connects one side with a 30" Buffalo Forge Co.'s disk-wheel. This wheel is belied to a 8" × 4" vertical engine. The air-pump is 53/" diameter as 6" stroke, is vertical and single-acting.

6" stroke, is vertical and single-acting.

The action of this condenser is as follows: The passage of air over the water surfaces removes the vapor as it rises and thus bastens evaporation. The heat necessary to produce evaporation is obtained from the steam in the tubes, causing the steam to condense. It was designed to condense 800 lbs. steam per hour and give a vacuum of 22 in., with a terminal pressure in the

cylinder of 20 lbs. absolute.

Results of tests show that the cooling-water required is practically equal in amount to the steam used by the engine. And since consumption of steam is reduced by the application of a condenser, its use will actually reduce the total quantity of water required. From a curve showing the rate of evaporation per square foot of surface in still air, and also one show ng the rate when a current of air of about 2300 ft. per min. velocity is passed over its surface, the following approximate figures are taken:

Temp,		on, lbs. per er hour.	Temp. F.	Evaporation, lbs. per sq. ft. per hour.		
F	Still Air.	Current.		Still Air.	Current.	
100° 110 120 130	0.8 0.25 0.4 0 6	1.1 1.6 2.5 8.5	140° 150 160 170	0.8 1.1 1.5 2.0	5.0 6.7 9.5	

The Continuous Use of Condensing-water is described in a series of articles in Power, Aug.-Dec., 1892. It finds its application in situations where water for ondensing purposes is expensive or difficult to obtain. In San Francisco J. H. Stut cools the water after it has left the hotwell by means of a system of pans upon the roof. These pans are shallow troughs of galvantzed iron arranged in tiers, on a slight incline, so that the water flows back and forth for 1800 or 2000 ft., cooling by evaporation and radiation as it flows. The pans are about 5 ft. in width, and the water as if itows has a depth of about half an inch, the temperature being reduced from about 140° to 90°. The water from the hot-well is pumped up to the highest roint of the cooling system and allowed to flow as above described, discharge. point of the cooling system and allowed to flow as above described, discharging finally into the main tank or reservoir, whence it again flows to the condenser as required. As the water in the reservoir lowers from evaporation, an auxiliary feed from the city mains to the condenser is operated, thereby keeping the amount of water in circulation practically constant. An accumulation of oil from the engines, with dust from the surrounding streets, makes a cleaning necessary about once in six weeks or two months. It is found by comparative trials, running condensing and non-condensing, that

out 50% less water is taken from the city mains when the whole apparatus n use than when the engine is run non-condensing. 22 to 23 in. of vacuum maintained. A better vacuum is obtained on a warm day with a brisk eze blowing than on a cold day with but a slight movement of the air. n another plant the water from the hot-well is sprayed from a number of ntains, and also from a pipe extending around its border, into a large

id, the exposure cooling it sufficiently for the obtaining of a good vacuum

its continuous use.

n the system patented by Messrs. See, of Lille, France, the water is dis-irged from a pipe laid in the form of a rectangle and elevated above a id through a series of special nozzles, by which it is projected into a fine av. On coming into contact with the air in this state of extreme divinthe water is cooled 40° to 50°, with a loss by evaporation of only one thof its mass, and produces an excellent vacuum. A 3000-H.P. cooler in this system has been erected at Lannoy, one of 2500 H.P. at Madrid, and of 1200 H.P. at Liege, as well as others at Roubaix and Tourcoing. of 1200 H.P. at Liege, as well as others at Roubaix and Tourcoing.

the tem could be used upon a roof if ground space were limited.

1 the "self-cooling" system of H. R. Worthington the injection-water is en from a tank, and after having passed through the condenser is disriged in a heated condition to the top of a cooling tower, where it is scated by means of distributing-pipes and trickles down through a cellular state of the towns of the terms of the towns icture made of 6-in. terra-cotta pipes, 2 ft. long, stood on end. The er is cooled by a blast of air furnished by a disk fan at the bottom of the er and the absorption of heat caused by a portion of the water being orized, and is led to the tank to be again started on its circuit. (Eny'g

vs, March 5, 1896.)

vs. March 5, 1896.)

1 the evaporative condenser of T. Ledward & Co. of Brockley, London, water trickles over the pipes of the large condenser or radiator, and by poration carries away the heat necessary to be abstracted to condense steam inside. The condensing pipes are fitted with corrugations unted with circular ribs, whereby the radiating or cooling surface is rely increased. The pipes, which are cast in sections about 76 in. long by in. bore, have a cooling surface of 26 sq. ft., which is found sufficient ler favorable conditions to permit of the condensation of 20 to 30 lbs. team per hour when producing a vacuum of 18 lbs. per sq. in. In a denser of this type at Rixdorf, near Berlin, a vacuum ranging from M 6 in. of mercury was constantly maintained during the hottest weather ugust. The initial temperature of the cooling-water used in the apparaunder notice ranged from 80° to 85° F., and the temperature in the sun, which the condenser was exposed, varied each day from 100° to 115° F, ing the experiments it was found that it was possible to run one engine er a load of 100 horse-power and maintain the full vacuum without the of any cooling water at all on the pipes, radiation afforded by the pipes

e sufficing to condense the steam for this power.

Klein's condensing water-cooler, the hot water coming from the con-er enters at the top of a wooden structure about twenty feet in height, is conveyed into a series of parallel narrow metal tanks. The water flowing from these tanks is spread as a thin film over a series of wooden itions suspended vertically about 3½ inches apart within the tower, upper set of partitions, corresponding to the number of metal tanks, hes half-way down the tower. From there down to the well is sused a second set of partitions placed at right angles to the first set. This des the rapidity of the downflow of the water, and also thoroughly is the water, thus affording a better cooling. A fan blower at the base of ower drives a strong current of air with a velocity of about twenty feet econd against the thin film of water running down over the partitions, estimated that for an effectual cooling two thousand times more air water must be forced through the apparatus. With such a velocity ir absorbs about two per cent of aqueous vapor. The action of the gair-current is twofold: first, it absorbs heat from the hot water by itself warmed by radiation; and, secondly, it increases the evapora-which process absorbs a great amount of heat. These two cooling are different during the different seasons of the year. During the r months the direct cooling effect of the cold air is greater, while g summer the heat absorption by evaporation is the more important. r. Taking all the year round, the effect remains very much the same, reaporation is never so great that the deficiency of water would not popiled by the additional amount of water resulting from the condense, while in very cold winter months it may be necessary to occasional. e cistern of surplus water. It was found that the vacuum obtained

this continual use of the same condensing water varied during the year between 27.5 and 28.7 inches. The great saving of space is evident from the fact that only the five-hundredth part of the floor-space is required as if cooling tanks or ponds were used. For a 100-horse-power engine the floor-space required is about four square yards by a height of twenty feet. For one horse-power 3.6 square yards cooling-surface is necessary. The vertical suspension of the partitions is very essential. With a ventilator 50 inches in diameter and a tower 6 by 7 feet and 20 feet high, 10,500 galions of water per hour were cooled from 104° F. to 66° F. The following record was made at Mannheim, Germany: Vacuum in condenser, 28.1 inches; temperature of the cooled for the cooled form 104° F. perature of condensing-water entering at top of tower, 104° to 106° F.; temperature of water leaving the cooler, 65.2° to 71.6° F. The engine was of the Sulzer compound type, of 120 horse-power. The amount of power necessary for the arrangement amounts to about three per cent of the total

necessary for the arrangement amounts to about three per cent of the total horse-power of the engine for the ventilator, and from one and one half to three per cent for the lifting of the water to the top of the cooler, the total being four and one half to six per cent.

A novel form of condenser has been used with considerable success in Germany and other parts of the Continent. The exhaust-steam from the engine passes through a series of brass pipes immersed in water, to which it gives up its heat. Between each section of tubes a number of galvanized disks are caused to rotate. These disks are cooled by a current of air supplied by a fan and pass down into the water, cooling it by abstracting the heat given out by the exhaust-steam and carrying it up where it is driven off by the air-current. The disks serve also to agitate the water and thus aid it in abstracting the heat from the steam. With 85 per cent vacuum the temperature of the cooling water was about 180° F., and a consumption of water for condensing is guaranteed to be less than a pound for each pound of steam condensed. For an engine 40 in. × 50 in., 70 revolutions per minute, 90 lbs. pressure, there is about 1150 sq. ft. of condensing-surface. Another condenser, 1000 sq. ft. of condensing-surface, is used for surface. Another condenser, 1600 sq. ft. of condensing surface, is used for three engines, $32 \text{ in.} \times 48 \text{ in.}, 27 \text{ in.} \times 40 \text{ in.}, \text{ and } 80 \text{ in.} \times 40 \text{ in.}, \text{ respectively.}$

—The Steamship. The Increase of Power that may be obtained by adding a condense: giving a vacuum of 26 inches of mercury to a non-condensing engine may be approximated by considering it to be equivalent to a net gain of 12 pounds mean effective pressure per square inch of piston area. If A = area of piston in square inches, S = piston-speed in ft. per minute, then $\frac{12AS}{38,000} = \frac{AS}{2750} = \text{H.P.}$

made available by the vacuum. If the vacuum = 18.2 lbs. per sq. in. = 27.9 in. of mercury, then H.P. = AS + 2500.

The saving of steam for a given horse-power will be represented approximately by the shortening of the cut-off when the engine is run with the condenser. Clearance should be included in the calculation. To the mean effective pressure non-condensing, with a given actual cut-off, clearance considered, add 3 lbs. to obtain the approximate mean total pressure, condensing. From tables of expansion of steam find what actual cut-off will give this mean total pressure. The difference between this and the original actual cut-off, divided by the latter and by 100, will give the percentage of saving.

The following diagram (from catalogue of H. R. Worthington) shows the percentage of power that may be gained by attaching a condenser to a non-condensing engine, assuming that the vacuum is 12 lbs. per sq. in. The diagram also shows the mean pressure in the cylinder for a given initial pres

sure and cut-off, clearance and compression not considered

sure and cut-on, clearance and compression not considered.

The pressures given in the diagram are absolute pressures above a vacuum. To find the mean effective pressure produced in an engine-cylinder with 90 lbs. gauge (= 105 lbs. absolute) pressure, cut-off at ½ stroke: find 105 in the left-hand or initial-pressure column, follow the horizontal line to the right until it intersects the oblique line that corresponds to the ½ cut-off, and read the mean total pressure from the row of figures directly above the point of intersection, which in this case is 63 lbs. From this subtract the mean about the back pressure (say 3 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. for a condensing engine and 18 lbs. intersection, which in this case is 63 lbs. From this subtract the mean absolute back pressure (say 3 lbs. for a condensing engine and 15 lbs. for a non-condensing engine exhausting into the atmosphere) to obtain the mean effective pressure, which in this case, for a non-condensing engine, gives 48 lbs. To find the gain of power by the use of a condenser with this engine, read on the lower scale the figures that correspond in position to 48 lbs. in the upper row, in this case 25. As the diagram does not take into consideration clearance or compression, the results are only approximate.

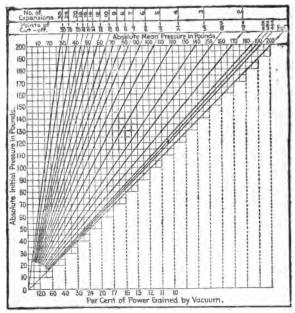


Fig. 151.

vaporators and Distillers are used with marine engines for the ose of providing fresh water for the boilers or for drinking purposes. sie of proving resi water for the bollers of to draming purposes.

easily taken to pieces and cleaned. The water in it is evaporated by steam from the main boilers passing through a set of tubes placed in its om. The steam generated in this boiler is admitted to the low-sure valve-box, so that there is no loss of energy, and the water coned in it is returned to the main boilers.

Weir's Feed-heater the feed-water before entering the boiler is heated ery nearly to boiling-point by means of the waste water and steam the low-pressure valve-box of a compound engine.

AS, PETROLEUM, AND HOT-AIR ENGINES.

LS-ongines.—For theory of the gas-engine, see paper by Dugald r. Proc. Inst. C. E. 1882, vol. lxix.; and Van Nostrand's Science Series, 12. See also Wood's Thermodynamics. Three standard works on gas-ness are "A Practical Treatise on the 'Otto' Cycle Gas-engine," by Win, is: "A Text-book on Gas, Air, and Oil Engines," by Bryan Donkin; and e Gas and Oil Engine," by Dugald Clerk (6th edition, 1896).

the ordinary type of single-cylinder gas-engine (for example the Otto) m as a four-cycle engine one ignition of gas takes place in one end of ylinder every two revolutions of the fly-wheel, or every two double es. The following sequence of operations takes place during four conive strokes: (a) inspiration during an entire stroke; (b) compression in the second (return) stroke; (c) ignition at the dead-point, and expandiuring the third stroke; (d) expulsion of the burnt gas during the fourth. rn) stroke. Beau de Rochas in 1863 laid down the law that there

four conditions necessary to realize the best results from the elastic force of gas: (1) The cylinders should have the greatest capacity with the smallest circumferential surface; (2) the speed should be as high as possible; (3) the circumferential surface; (2) the speed should be as high as possible; (3) the cut-off should be as early as possible; (4) the initial pressure should be as high as possible. In modern engines it is customary for ignition to take place, not at the dead point, as proposed by Beau de Rochas, but somewhat later, when the piston has already made part of its forward stroke. At first sight it might be supposed that this would entail a loss of power, but experience shows that though the area of the diagram is diminished, the power registered by the friction-brake is greater. Starting is also made easier by this method of working. (The Simplex Engine, Proc. Inst. M. E. 1889)

In the Otto engine the mixture of gas and air is compressed to about 3 atmospheres. When explosion takes place the temperature suddenly rises to somewhere about 2900° F. (Robinson.)

to somewhere about 2900° F. (Robinson.)

The two great sources of waste in gas-engines are: 1. The high temperature of the rejected products of combustion; 2. Loss of heat through the cylinder walls to the water-jacket. As the temperature of the water-jacket is increased the efficiency of the engine becomes higher.

is increased the emciency of the engine becomes higher.
With ordinary coal-gas the consumption may be taken at 20 cu. ft. per hour per I.H.P., or 24 cu. ft. per brake H.P. The consumption will vary with the quality of the gas. When burning Dowson producer-gas the consumption of anthracite (Welsh) coal is about 1.3 los. per I.H.P. per hour for ordinary working. With large twin engines, 100 H.P., the consumption is reduced to about 1.1 lb. The mechanical efficiency or B.H.P. + I.H.P. in ordinary engines is about 8%; the friction loss is less in larger engines.

Effectency of the Gas-engine. (Thurston on Heat as a Form of

Energy.)

Heat	transferred into useful work		17%
44	" to the jacket-water	52	
66	lost in the exhaust-gas	16	
44	" by conduction and radiation	15	
	•	_	88%

This represents fairly the distribution of heat in the best forms of gasengine. The consumption of gas in the best engines ranges from a minimum of 18 to 20 cu. ft. per L.H.P. per hour to a maximum exceeding in the smaller engines 25 cu. ft. or 30 cu. ft. In small engines the consumption per

brake horse-power is one third greater than these figures.

The report of a test of a 170-H.P. Crossley (Otto) gas-engine in England, 1892, using producer-gas, shows a consumption of but 85 lb. of coal per H.P. hour, or an absolute combined efficiency of 21.3% for the engine and pro-

ducer. The efficiency of the engine alone is in the beginned at the Otto gas-engine at the Otto Gas-engine Works in Philadelphia. The only loss is due to radiation through the walls of the producer and a small amount of heat carried off in the water from the scrubber. Experiments on a 100-H.P. engine show a consumption of 97/100 lb. of carbon per l.H.P. per hour. This

result is superior to any ever obtained on a steam-engine. (From Age, 1892.)

Tests of the Simplex Gas-engine. (Proc. Inst. M. E. 1892.)

Cylinder 76x × 1534 in, speed 160 revs. per min. Trials were made with town gas of a heating value of 607 heat-units per cubic foot, and with Dowson

gas, rich in CO, of about 150 heat-units per cubic foot.

	Town Gas.			Dowson Gas.		
Effective H.P. Gas per H.P. per hour, cu. ft Water per H.P. per hour, ibs. Temp. water entering, F effluent	54.7 51°	2. 8.67 20.12 44.4 51° 144°	3. 9.28 20.78 43.8 51° 172°	1. 7.12 88.08 58.3 48° 144°	2, 3.61 114.85	8, 5.26 97.86

The gas volume is reduced to 32° F. and 30 in barometer. A 50-H.P. engine working 35 to 40 effective H.P. with Dowson generator consumed 51 lbs. English antiracite per hour, equal to 1.48 to 1.3 lbs. per effective H.P. A 16-H.P. engine working 12 H.P. used 19.4 cu. ft. of gas per effective H.P. A 320-H.P. Gas-engine.—The flour-mills of M. Leblanc, at Pantin, France, have been provided with a 320-horse-power fuel-gas engine of the Simplex type. With coal-gas the machine gives 450 horse-power. There is one cylinder, 34.8 in. diam.; the piston-stroke is 40 in.; and the speed 100 revs.

nin. Special arrangements have been devised in order to keep the rent parts of the machine at appropriate temperatures. The coal used 312 lb. per indicated or 1.03 lb. per brake horse power. The water used gallons per brake horse-power per hour.

of an Otto Gas-engine. (Jour. F. I., Feb. 1890, p. 115.)—En-7 H.P. nominal; working capacity of cylinder 2594 cu. ft.; clearance e .1796 cu. ft.

• F. 1	Heat-units. Per cent.
perature of gas supplied 62.2 "exhaust 774.8	Transferred into work 22.94
	Taken by jacket-water 49.94
" enteringwater 50.4	Taken by jacket-water
" exit water 89.2	
sure of gas, in. of water 8.06	Composition of the gas:
plution per min., av'ge 161.6	By Volume. By Weight.
losions missed per min.,	CO ₂ 0.50% 1.923%
erage 6.8	C ₂ H ₄ 4.82 10.520
n effective pressure, lbs.	0 1.00 2.797
r sq. in 59.	CO 5.33 15.419
se power, indicated 4.94	CH ₄
k per explosion, foot-	H 51.57 9.021
ounds	N 9.06 22,278
per I.H.P. per hour, cu. ft. 23.4	99.96 99.995

est of the Clerk Gas-engine. (Proc. Inst. C. E. 1882, vol. lxlx.)—nter 6 × 12 in., 150 roys. per min.; mean available pressure, 70.1 lbs., 9P.; maximum pressure, 220 lbs. per sq. in. above atmosphere; pressure re ignition, 41 lbs. above atm.; temperature before compression, 60° F.,

reignition, 41 abs. above atm.; temperature after ignition calculated from pres, 2800° F.; gas required per I.H.P. per hour, 22 cu. ft. ore Recent Tests of gas-engines, 1898, have given higher economical resthan those above quoted. The gas-consumption (city gas) has been as as 15 cu. ft. per I.H.P. per hour, and the efficiency as high as 27% of the ing value of the gas. The principal improvement in practice has been seen from the procession of the working charge.

ise of much higher compression of the working charge.

In bustion of the Gas in the Otto Engine.—John Imray, in ussion of Mr. Clerk's paper on Theory of the Gas-engine, says: The ige which Mr. Otto introduced, and which rendered the engine a success, that, instead of burning in the cylinder an explosive mixture of gas and he burned it in company with, and arranged in a certain way in respect large volume of incombustible gas which was heated by it, and which nished the speed of combustion. W. R. Bousfield, in the same discussays: In the Otto engine the charge varied from a charge which was rplosive mixture at the point of ignition to a charge which was merely ert fluid near the piston. When ignition took place there was n exploclose to the point of ignition that was gradually communicated throughthe mass of the cylinder. As the ignition got farther away from the ary point of ignition the rate of transmission became slower, and if the ne were not worked too fast the ignition should gradually catch up to piston during its travel, all the combustible gas being thus consumed, theory of slow combustion is, however, disputed by Mr. Clerk, who is that the whole quantity of combustible gas is ignited in an instant.

Imperatures and Pressures developed in a Gas-engine.

k on the Gas-engine.)—Mixtures of air and Oldham coal-gas. Temper-before explosion, 17° C.

Mixture.		Max. Press above Atmos.,	Temp. of Explo- sion calculated from observed	Theoretical Temp. of Explo- sion if all Heat		
las.	Air.	lbs, per sq. in.	Pressure.	were evolved.		
vol.	14 vols.	4 0.	806° C.	1786° C.		
66	18 "	51.5	1033	1912		
44	12 "	60.	1202	2058		
-4	11 "	61.	1220	2228		
46	9 "	78. 87.	1557	2670		
46	7 4	87.	1788	8334		
46	6 4	90.	1792	8808		
66	5 "	91.	1812	• • • •		
**	4 "	80.	1595	••••		

e of Carburetted Air in Gas-engines .- Air passed

gasoline or volatile petroleum spirit of low sp. gr., 0.65 to 0.70, liberates some of the gasoline, and the air thus saturated with vapor is equal in heatlog or lighting power to ordinary coal-gas. It may therefore be used as a fuel for gas-engines. Since the vapor is given off at ordinary temperatures gasoline is very explosive and dangerous, and should be kept in an underground tank out of doors. A defect in the use of carburetted air for gasengines is that the more volatile products are given off first, leaving an oily residue which is often useless. Some of the substances in the oil that are taken up by the air are apt to form troublesome deposits and incrustations when burned in the engine cylinder.

The Otto Gasoline-engine. (Eng'g News, May 4, 1893.)—It is claimed that where but a small gasoline-engine is used and the gasoline bought at retail the liquid fuel will be on a par with a steam-engine using 6 bls. of coal per horse-power per hour, and coal at \$3.50 per ton, and will besides save all the handling of the solid fuel and sehes, as well as the attendance for the bollers. As very few small steam-engines consume less than 6 lbs. of coal per hour, this is an exceptional showing for economy. At 8 cts. per gallon for gasoline and 1/10 gal. required per H.P. per hour, the

cost per H.P. per hour will be 0.8 cent.

Gasoline-engines are coming into extensive use (1898). In these engines the gasoline is pumped from an underground tank, located at some distance outside the engine-room, and led through carefully soldered pipes to the working cylinder. In the combustion chamber the gasoline is sprayed into a current of air, by which it is vaporized. The mixture is then compressed and ignited by an electric spark. At no time does the gasoline come in contact with the air outside of the engine, nor is there any flame or burning

gases outside of the cylinder.

Naphtha-engines are in use to some extent in small yachts and sunches. The naphtha is vaporized in a boiler, and the vapor is used exlaunches. The naphtha is vaporized in a coller, and the vapor is used and returned to the boiler. A portion of the naphtha vapor is used for fuel under the boiler. According to the circular of the builders, the Gas Engine and Power Co. of New York, a 2-H.P. engine requires from 3 to 4 quarts of naphtha per hour, and a 4-H.P. engine from 4 to 6 quarts. The chief advantages of the naphtha engine and boiler for launches are the saving of weight and the quickness of operation. A 2-H.P. engine weighs 200 lbs., a 4-H.P. 200 lbs. It takes only about two minutes to get under headway. (Modern Mechanism, p. 270.)

Hot-air (or Calorie) Engines.—Hot-air engines are used to some

Hot-air (or Caloric) Engines.—Hot-air engines are used to some extent, but their bulk is enormous compared with their effective power. For an account of the largest hot-air engine ever built (a total failure) see Church's Life of Ericsson. For theoretical investigaton, see Rankine's Steam-engine and Rontgen's Thermodynamics. For description of constructions, see Appleton's Cyc. of Mechanics and Modern Mechanism, and Babcock on Substitutes for Steam, Trans. A. S. M. E., vii., p. 693.

Test of a Hot-air Engine (Robinson).—A vertical double-cylinder (Caloric Engine Co.'s) 13 nominal H.P. engine gave 20.19 I.H.P. in the working cylinder and 11.28 I.H.P. in the pump, leaving 8.81 net I.H.P.; while the effective brake H.P. was 5.9, giving a mechanical efficiency of 67%. Coasumption of coke, 3.7 lbs. per brake H.P. per hour. Mean pressure on pistons 15.37 lbs. per square inch, and in pumps 15.9 lbs., the area of working cylinders being twice that of the pumps. The hot air supplied was about 1160° F. and that rejected at end of stroke about 890° F.

The Priestman Petroleum-engine. (Jour. Frank. Inst., Feb.

The Priestman Petroloum-engine. (Jour Frank Inst., Feb. 1893)—The following is a description of the operation of the engine: Any ordinary high-test (usually 150° test) oil is forced under air-pressure to an ordinary high test (usually 150° test) oil is forced under air-pressure to an atomizer, where the oil is met by a current of air and broken up into atoms and sprayed into a mixer, where it is mixed with the proper proportion of supplementary air and sufficiently heated by the exhaust from the cylinder passing around this chamber. The mixture is then drawn by suction into the cylinder, where it is compressed by the piston and ignited by an electric spark, a governor controlling the supply of oil and air proportionately to the work performed. The burnt products are discharged through an exhaust-valve which is actuated by a cam. Part of the air supports the compustion of the oil and the heat generated by the combustion of the oil. baust-vaive which is actuated by a cam. Fare of the air supports the combustion of the oil, and the heat generated by the combustion of the oil expands the air that remains and the products resulting from the explosion, and thus develops its power from air that it takes in while running. In other words, the engine exerts its power by inhaling air, heating that air, and expelling the products of combustion when done with. In the largest rugines only the 1/250 part of a pint of oil is used at any one time, and in smallest sizes the fuel is prepared in correct quantities varying from 00 of a pint upward, according to whether the engine is running on light ull duty. The cycle of operations is the same as that of the Otto gasine.

rials of a 5-H.P. Priestman Petroleum-engine. (Prof. J. Unwin, Proc. Inst. C. E. 1892.)—Cylinder, 84 × 12 in., making normally revs. per min. Two oils were used, Russian and American. The more ortant results were given in the following table:

	Trial V. Full Power.	Trial I. Full Power.	Trial IV. Full Power.	Trial II. Half Power.	Trial III. Light.
used	Day- light.	Russo- lene. 6.765	Russo- lene. 6.882	Russo- lene.	Russo- lene.
re H.Phanical efficiency used per brake H.P.	9.369 0.824	7.408 0.91	8.832 0.876	8.62 4.70 0.769	0.889
ur, lbused per indicated	0.848	0.946	0.988	1.881	
P. hour, lb of air per lb. of oil n explosion pressure,	0.694 38.4	0.864 81.7	0.81G 43.2	1.068 21.7	5.784 10.1
s. per sq. in n compression pres- re, lbs. per sq. in	151.4	134.3 27.6	128.5 26.0	48.5 14.8	9.6
n terminal pressure, s. per sq. in		23.7	25.5	15.6	

compare the fuel consumption with that of a steam-engine, 1 lb. of night be taken as equivalent to 1½ lbs. of coal. Then the consumption is oil-engine was equivalent, in Trials I., IV., and V., to 1.42 lbs., 1.48 lbs., 1.26 lbs. of coal per brake horse-power per hour. From Trial IV. the wing values of the expenditure of heat were obtained:

	Per cent
Useful work at brake	2.81
Heat shown on indicator-diagram Rejected in jacket-water " in exhaust-gases Radiation and unaccounted for	16.12 47.54 26.72 9.61
Total	99.99

LOCOMOTIVES.

esistance of Trains.—Resistance due to Speed.—Various formulæ tables for the resistance of trains at different speeds on a straight level t have been given by different writers. Among these are the following: George R. Henderson (Proc. Engrs. Club of Phila., 1886):

$$R = 0.0015(1 + v^2 + 650),$$

hich $R={
m resistance}$ in lbs. per ton of 2240 lbs. and $v={
m speed}$ in miles per

eed i	in mile	s per	hour:								
5	10	15	20	25	30	35	40	45	50	55	60
sista	nce in	poun	ds per	ton e	of 2000	lbs.:					
8.1	8.4	¯ 4 .	4.8	5.8	7.1	8.6	10.2	12.1	14.8	16.8	19.2
D. 1	L Barr	nes (E	Ing. M	ag.),	June,	1894:					
Spec	ed, mile	es mei	hour			50	60	70	80	90	100
Resi	stance	, pou	nds pe	r gro	ss ton	. 12	12.4	18.	5 15	17	20

By Engineering News, March 8, 1894:

Resistance in lbs. per ton of 2000 lbs. = $\frac{1}{4}v + 4$.

Speed 5 10 15 20 25 30 38 40 45 50 60 70 80 90 Resistance.. 3¼ 4.5 5¾ 7 8¼ 9.5 10¾ 12 13¼ 14.5 17 19.5 22 24.5

By Baldwin Locomotive Works:

Resistance in lbs. per ton of 2000 lbs. = 3 + v + 6.

Speed...... 5 10 15 20 25 30 35 40 45 50 55 60 70 80 90 100 Re-istance.. 3.8 4.7 5.5 6.3 7.2 8 8.8 9.7 10.5 11.3 12.2 13 14.7 16.3 18 19.7

The resistance due to speed varies with the condition of the track, the number of cars in a train, and other conditions.

For tables showing that the resistance varies with the area exposed to the resistance and friction of the air per ton of loads, see Dashiell, Trans. A. S.

resistance and friction of the air per ton of 1080s, see Dasmen, 1780s. A. S. M. E., vol. xiii. p. 371.

P. H. Dudley (Bulletin International Ry. Congress, 1900, p. 1734) shows that the condition of the track is an important factor of train resistance which has not hitherto been taken account of. The resistance of heavy trains on the N. Y. Central R. R. at 20 miles an hour is only about 3½ lbs. per ton on smooth 80-lb. 5½-in. rails. The resistance of an 80-car freight train, 60.000 lbs. per car, as given by indicator cards, at speeds between 15 and 25 miles per hour is represented by the formula $R = 1 + \frac{1}{2}V$, in which R = 10 sistance in lbs. per ton and V = 11 miles per hour.

Resistance due to Grade.—The resistance due to a grade of 1 ft. per mile

Resistance due to Grade. - The resistance due to a grade of 1 ft. per mile is, per ton of 2000 lbs., $2000 \times \frac{1}{5280} = 0.3788$ lb. per ton, or if R_g = resistance

in lbs. per ton due to grade and G = ft. per mile, Rg = 0.3788G.

If the grade is expressed as a percentage of the length, the resistance is 20 lbs per ton for each per cent of grade.

Resistance due to Curves.—Mr. Henderson gives the resistance due to curvature as 0.5 lb. per ton of 2000 lbs. per degree of the curve. (For defini-

tion of degrees of a railroad curve see p. 58.) If c is the number of degrees, Re the resistance in lbs. per ton, = 0.5c. The Baldwin Locomotive Works take the approximate resistance due to each degree of curvature as that due to a straight grade of 11/2 ft. per mile. This

corresponds to $R_c = 0.5682c$. Resistance due to Acceleration.—This may be calculated by means of the

ordinary formulæ for acceleration, as follows:

Let V_1 = velocity in ft. per second at the beginning of a mile run, V_2 = velocity at the end of the mile. $Y_2 = V_1 = V_2 = V_2 = V_3 =$

 $f = \text{resistance in lbs. due to acceleration} = \frac{w}{c} \frac{(V_2 - V_1)}{w}$

$$= \frac{w}{32.2} \times \frac{(V_3 - V_1)^2}{10,560} = .005882 W(V_3 - V_1)^3.$$

S= increase of speed in miles per hour ; $(V_2-V_1)^2=S^2\times(22/15)^2.$ Ra= resistance in lbs. per ton = .01265 $S^2.$

Total Resistance.—The total resistance in lbs. per ton of 2000 lbs. due to speed, to grade, to curves, and to acceleration is the sum of the resistances calculated above. Taking the Baldwin Locomotive Works' rules for speed and curvature, we have

$$Rt = \left(3 + \frac{v}{6}\right) + 0.8788G + 0.5682c + .01265S^2,$$

in which Rt is the resistance in lbs. per ton of 2000 lbs., v = speed in miles per

in which R_i is the resistance in lbs. per ton of 2000 lbs., v = speed in miles per hour, G = grade in ft. per mile. c = degrees of curvature, S = rate of increase of speed in miles per hour in a run of one mile.

Resistance due to Friction.—In the above formula no account has been taken of the resistance to the friction of the working parts of the engine, nor to the friction of the engine and tender on curves due to the rigid wheel bases. No satisfactory formula can be given for these resistances. Mr. Henderson takes them as being proportional to the tractive power, so that, if the total tractive power be P, the effective tractive is uP,

the resistance (1-u)P, the value of the coefficient u being probably

he Baldwin Locomotive Works in their "Locomotive Data" take the I resistance on a straight level track at slow speeds at from 6 to 10 lbs. ton and in a communication printed in the fourth edition (1888) of this ket-book, p. 1076, say: "We know that in some cases, for instance in e construction, the frictional resistance has been shown to be as much as bs, per ton at slow speed. The resistance should be approximated to the conditions of each individual case, and the increased resistance due peed added thereto."

olimes on the Steam-engine, p. 142, says: "The frictional resistance miform motion of the whole train including the engine and tender, is ally expressed by giving the direct pull in pounds necessary in order to sel each ton's weight of the train along a level line at slow speed. The varies with the condition of the line, the state of the surface of the rails, state of the rolling stock, and the speed. If M be the speed in miles per r, and T the weight of the train in tons [2240 lbs.] exclusive of engine tender, the resistance to uniform motion may be expressed by the าเปล

$$R = [6 + 0.3(M - 10)T].$$

, be the weight of the engine and tender, the corresponding resistance is

$$R_1 = [12 + 0.8(M - 10)T_1],$$

the expression includes the friction of the mechanism of the engine. limes also says that a strong side wind by pressing the tires of the els against the rails may increase the frictional resistance of the train by

nuch as 20 per cent.

auling Capacity due to Adhesion.—The limit of the hauling city of a locomotive is the adhesion due to the weight on the driving els. Holmes gives the adhesion, in English practice, as equal to 0.15 of load on the driving wheels in ordinary dry weather, but only 0.07 in p weather or when the rails are greasy. In American practice it is gener-taken as from 1/4 to 1/5 of the load on the drivers. The hauling capacity ow speed on a track of different grades may be calculated by the folng formula:

t = t tons of 2000 lbs., locomotive and train, per 1000 lbs, load on ers, a = the reciprocal of the coefficient of adhesion, g = the per cent ade, R = the frictional resistance in lbs. per ton. Then $T = \frac{1000 + a}{R + ac}$

om this formula the following table has been calculated:

ade Per Cent, 0 0.5 1 1.5 2 2.5 6

Tons Hauling Capacity per 1000 lbs. Weight on Drivers.

x = 4, R = 6.. 42 15.6 9.2 6.9 5.4 4.5 3.8 3.3 2.9 2.4 2.0 1.7 $\ddot{x} = 5, R = 8.$ 25 11.1 7.2 5.3 4.2 3.4 $\ddot{x} = 5, R = 10.$ 20 10. 6.7 5. 4. 8.3 2.9 2.6 2.8 1.9 2.9 2.5 2.2

active Power of a Locomotive.—Single Expansion.

P =tractive power in lbs.

p = average effective pressure in cylinder in lbs. per sq. in. S = stroke of piston in inches. d = diameter of cylinders in inches. D = diameter of driving wheels in inches. Then

$$P = \frac{4\pi d^2 pS}{4\pi D} = \frac{d^2 pS}{D}.$$

average effective pressure can be obtained from an indicator-dia-or by calculation, when the initial pressure and ratio of expansion are n, together with the other properties of the valve-motion. The sub i table from "Auchincloss" gives the proportion of mean effective ure to boiler-pressure above atmosphere for various proportions of

Stroke, Cut off at—	M.E.P. (Boiler- pres. = 1).	Stroke, Cut of at	(M.E.P. Boiler- pres. = 1).	Stroke, Cut off at—	M.E.P. (Boiler- pres. = 1).
.1 .125 = 1/6 .15 .175 .2 .25 = 1/4	.15 .2 .24 .28 .32 .4 .46	$.333 = \frac{1}{2}$ $.375 = \frac{3}{2}$ $.4$ $.45$ $.5 = \frac{1}{2}$.5 = ½ .55 .57 .63 .67	.625 = 56 .666 = 38 .7 .75 = 34 .875 = 36	.79 .82 .35 .89 .93

These values were deduced from experiments with an English locomotive by Mr. Gooch. As diagrams vary so much from different causes, this table will only fairly represent practical cases. It is evident that the cut-off must be such that the boiler will be capable of supplying sufficient steam at the given speed.

Compound Locomotives.—The Baldwin Locomotive Works give the following formulæ for compound engines of the Vauclain four-cylinder type:

$$T = \frac{C^2S \times {}^2\%P}{D} + \frac{c^2S \times {}^14P}{D}.$$

$$T = t \text{ nection power in the } t$$

T = tractive power in lbs. C = diam. of high-pressure cylinder in ins. c = "low"

P =boiler pressure in lbs.

S =stroke of piston in ins. D =diam. of driving-wheels in ins.

For a two-cylinder or cross-compound engine it is only necessary to consider the high pressure cylinder, allowing a sufficient decrease in boiler pressure to compensate for the necessary back-pressure. The formula is

$$T = \frac{C^2S \times \frac{2}{2} P}{D}.$$

Efficiency of the Mechanism of a Locomotive.—Frank C. Wagner (Proc. A. A. A. S., 1900, p. 140) gives an account of some dynamometer tests which indicate that in ordinary freight service the power used to drive the locomotive and tender and to overcome the friction of the mechanism is from 10% to 35% of the total power developed in the steam-cylinder. In one test the weight of the locomotive and tender was 16% of the total weight of the train; while the power consumed in the locomotive and tender was from 30% to 33% of the indicated horse-power.

The Size of Locomotive Cylinders is usually taken to be such

that the engine will just overcome the adhesion of its wheels to the rails

under favorable circumstances.

The adhesion is taken by a committee of the Am. Ry. Master Mechanics' Assn. as 0.25 of the weight on the drivers for passenger engines, 0.24 for freight, and 0.22 for switching engines; and the mean effective pressure in the cylinder, when exerting the maximum tractive force, is taken at 0.85 of the boiler-pressure.

Let W = weight on drivers in lbs.; P = tractive force in lbs., = say 0.25 W: p_1 = boiler-pressure in lbs per sq. in.; p = mean effective pressure, = 0 85 p_1 ; d = diam. of cylinder, S = length of stroke, and D = diam. of driving-wheels, all in inches. Then

$$W = 4P = \frac{4d^2pS}{D} = \frac{4d^2 \times 0.85p_1S}{D}.$$

Whence

$$d = 0.5 \sqrt{\frac{\overline{DW}}{pS}} = 0.542 \sqrt{\frac{\overline{DW}}{p_1 S}}.$$

Von Borries's rule for the diameter of the low-pressure cylinder of a compound locomotive is $d^2 = \frac{2ZD}{ph}$

here d = diameter of l.p. cylinder in inches;

D =diameter of driving-wheel in inches;

p = mean effective pressure per sq. in., after deductin machine friction

h = stroke of piston in inches:

Z = tractive force required, usually 0.14 to 0.16 of the adhesion.

The value of p depends on the relative volume of the two cylinders, and om indicator experiments may be taken as follows:

lass of Engine. Ratio of Cylinder o in percentage p for Boiler-press Volumes. 1:2 or 1:2.05 of Boiler-pressure. ure of 176 lbs. irge-tender eng's 1:2 or 1:2.2 ink-engines.....

Horse-power of a Locomotive.—For each cylinder the horse-wer is H.P. = pLaN + 33,000, in which p = mean effective pressure, L stroke in feet, a = area of cylinder $= \frac{1}{4}\pi d^3$, N = number of single strokes r minute, LN = piston speed, ft. per min. Let M = speed of train in miles r hour, S = length of stroke in inches, and D = diameter of driving-wheel inches. Then $LN = M \times 88 \times 2S + \pi D$. Whence for the two cylinders e horse-power is

$$\frac{2 \times p \times \frac{1}{4}\pi d^2 \times 176S \times M}{\pi D \times 33,000} = \frac{pd^2SM}{375D}.$$

The Size of Locomotive Bollers. (Forney's Catechism of the comotive.)—They should be proportioned to the amount of adhesive ight and to the speed at which the locomotive is intended to work. Thus ocomotive with a great deal of weight on the driving wheels could pull a vier load, would have a greater cylinder capacity than one with little nesive weight, would consume more steam, and therefore should have a ger boiler.

he weight and dimensions of locomotive boilers are in nearly all cases ermined by the limits of weight and space to which they are necessarily ifined. It may be stated generally that within these limits a locomotive ler cannot be made too large. In other words, boilers for locomotives uld always be made as large as is possible under the conditions that denine the weight and dimensions of the locomotives. (See also Holmes on Steam-engine, pp. 371 to 377 and 383 to 389, and the Report of the Am. Ry. M. Assn. for 1897, pp. 218 to 232.) [olmes gives the following from English practice:

Evaporation, 9 to 12 lbs. of water from and at 212°.

Ordinary rate of combustion, 65 lbs. per sq. ft. of grate per hour.

Ratio of grate to heating surface, 1:60 to 90.

Heating surface per lb. of coal burnt per hour, 0.9 to 1.5 sq. ft.

"unlities Essential for a Free-steaming Locomotive."

In a paper by A. E. Mitchell, read before the N. Y. Rairoad Club; "ig News, Jan. 24, 1891.)—Square feet of boiler-heating surface for bituous coal should not be less than 4 times the square of the diameter in less of a cylinder 1 inch larger than the cylinder to be used. One tenth his should be in the fire-box. On arthrogital locomotives more beginner. his should be in the fire-box. On authracite locomotives more beating-ace is required in the fire-box, on account of the larger grate-area gired, but the heating-surface of the flues should not be materially

eased. **Tootten's Locomotive.** (Clark's Steam-engine; see also Jour. ik. Inst. 1891, and Modern Mechanism, p. 485.)—J. E. Wootten designed constructed a locomotive boiler for the combustion of anthracite and te, though specially for the utilization as fuel of the waste produced in nining and preparation of authracite. The special feature of the engine e fire-box, which is made of great length and breadth, extending clear the wheels, giving a grate-area of from 64 to 85 sq. ft. The draught sed over these large areas is so gentle as not to lift the fine per-ticles of

uel. A number of express-engines having this type of boiler are engaged to fast trains between Philadelphia and Jersey City. The fire-box shell t. 8 in. wide and 10 ft. 5 in. long; the fire-box is 8×9½ ft., making 76 sq. grate-area. The grate is composed of bars and water-tubes alternately. regular types of cast-iron shaking grates are also used. The height of ire-box is only 2 ft. 5 in, above the grate. The grate is terminated by dge of fire-brick, beyond which a combustion-chamber, 27 in. long to the flue-tubes, about 184 in number, 134 in. diam. The cylinders

21 in. diam., with a stroke of 22 inches. The driving-wheels, four-coupled, 21 in. diam., with a stroke of 22 inches. The driving-wheels, four-coupled, are 5 it. 8 in. diam. The engine weighs 44 tons, of which 29 tons are on driving wheels. The heating-surface of the fire-box is 135 sq. ft., that of the flue-tubes is 982 sq. ft.; together, 1117 sq. ft., or 14.7 times the grate-area, Hauling 15 passenger-cars, weighing with passengers 360 tons, at an average speed of 42 miles per hour, over ruling gradients of 1 in 89, the engine consumes 62 bls. of fuel per mile, or 344 ibs. per sq. ft of grate-per hour Grate-surface, Smoke-stacks, and Exhaust-nozzles for Locomotives. (Am. Mach., Jan. 8, 1891.)—For grate-suriace for anthractic coal: Multiply the displacement in cubic feet of one piston during a stroke by 8.5 the product will be the area of the crate in surers factors.

stroke by 8.5; the product will be the area of the grate in square feet.

For bituminous coal: Multiply the displacement in feet of one piston during a stroke by 61%; the product will be the grate-area in square feet for engines with cylinders 12 in. in diameter and upwards. For engines with smaller cylinders the ratio of grate-area to piston-displacement should be 73/4 to 1, or even more, if the design of the engine will admit this proportion.

The grate-areas in the following table have been found by the foregoing rules, and agree very closely with the average practice:

Smoke-stacks.—The internal area of the smallest cross-section of the stack

should be 1/17 of the area of the grate in soft-coal-burning engines.

A. E. Mitchell, Supt. of Motive Power of the N. Y. L. E. & W. R. R., says that recent practice varies from this rule. Some roads use the same size of stack, 1314 in. diam. at throat, for all engines up to 20 in. diam. of cylinder. The area of the orifices in the exhaust-nozzles depends on the quantity and

quality of the coal burnt, size of cylinder, construction of stack, and the condition of the outer atmosphere. It is therefore impossible to give rules for computing the exact diameter of the orifices. All that can be done is to give a rule by which an approximate diameter can be found. The exact diameter can only be found by trial. Our experience leads us to believe that the area of each orifice in a double exhaust-nozzle should be equal to 1/400 part of the grate-surface, and for single nozzles 1/200 of the grate-surface. These ratios have been used in finding the diameters of the nozzles given in the following table. The same sizes are often used for either hard or soft coal-burners.

Size of	Grate-area for Anthra-	Grate-area for Bitumin-	Diameter	Double Nozzles.	Single Nozzles.
Cylinders, in inches.	cite Coal, in sq. in.	ous Coal, in sq. in.	of Stacks, in inches.	Diam. of Orifices, in inches.	Diam. of Orifices, in inches.
12 × 20 13 × 20 14 × 20 15 × 22 16 × 24 17 × 24 18 × 24 19 × 24 20 × 24	1591 1873 2179 2742 3415 3856 4321 4810 5337	1217 1432 1666 2097 2611 2948 3804 3678 4081	916 1014 1114 1214 14 15 1584 1614 1712	2 25/16 25/16 29/16 23/6 31/16 31/4 37/16	2 13/16 3 31/4 8 11/16 4 1/16 4 5/16 4 18/16 5 1/16

Exhaust-nozzles in Locomotive Bollers.—A committee of the Am. Ry. Master Mechanics' Assn. in 1890 reported that they had, after two years of experiment and research, come to the conclusion that, owing to the great diversity in the relative proportions of cylinders and boilers, together with the difference in the quality of fuel, any rule which does not

recognize each and all of these factors would be worthless.

The committee was unable to devise any plan to determine the size of the exhaust-nozzle in proportion to any other part of the engine or boiler, and believes that the best practice is for each user of locomotives to adopt a nozzle that will make steam freely and fill the other desired conditions, best determined by an intelligent use of the indicator and a check on the fuel account. The conditions desirable are: That it must create draught enough on the fire to make steam, and at the same time impose the least possible amount of work on the pistons in the shape of back pressure. It should be large enough to produce a nearly uniform blast without lifting or tearing e fire, and be economical in its use of fuel. The Annual Report of the Asciation for 1896 contains interesting data on this subject.

Fire-brick Arches in Locomotive Fire-boxes.—A comtree of the Am. Ry. Master Mechanics' Assn. in 1890 reported strongly in or of the use of brick arches in locomotive fire-boxes. They say: It is a unanimous opinion of all who use bituminous coal and brick arch, that a most efficient in consuming the various gases composing black smoke, d by impeding and delaying their passage through the tubes, and mingg and subjecting them to the heat of the furnace, greatly lessens the time ejected, and intensifies combustion, and does not in the least check trather augments draught, with the consequent saving of fuel and inased steaming capacity that might be expected from such results. This particular when used in connection with extension front.

itize, Weight, Tractive Power, etc., of Different Sizes of comotives. (J. G. A. Meyer. Modern Locomotive Construction. An. Ch., Aug. 8, 1885.—The tractive power should not be more or less than adhesion. In column 3 of each table the adhesion is given, and since the estimate tractive power are expressed by the same unuber of pounds, se figures are obtained by finding the tractive power of each engine, for 1 purpose always using the small diameter of driving-wheels given in mnn 2. The weight on drivers is shown in column 4, which is obtained by ltiplying the adhesion by 5 for all classes of engines. Column 5 gives the ights on the trucks, and these are based upon observations. Thus, the ght on the truck for an eight-wheeled engine is about one half of that

ced on the drivers.

or Mogul engines we multiply the total weight on drivers by the decimal and the product will be the weight on the truck.

or ten wheeled engines the total weight on the drivers, multiplied by the

imal 32, will be equal to the weight on the truck.

Ind lastly, for consolidation engines, the total weight on drivers multid by the decimal 16, will determine the weight on the truck.

1 column 6 the total weight of each engine is given, which is obtained by ing the weight on the drivers to the weight on the truck. Dividing the

1	LIGHT.	WHEE	LED I	LOCOM	OTIV	ES.		TEN-	WHE	CLED	ENGI	NES.	
	Diameter of Driving- wheels.	Adheston.	Weight on Drivers.	Weight on Truck.	Total Weight.	Hauling Capacity on Level Track in tons of 2000 lbs., includ- ing Tender.	Cylinders—Diameter, Stroke,	Diameter of Driving- wheels.	Adhesion.	Weight on Drivers.	Weight on Truck.	Total Weight, with Water and Fuel.	Hauling Capacity on Level Track in tons of 2000 lbs., includ- ing Tender.
•	2	8	4	5	6	7	1	28	8	4	5	6	7
The second second	in. 45-51 45-51 48-54 49-57 55-61 55-66 58-66 60-66 61-66	lbs. 4000 5324 5940 6828 7697 8836 9533 10404 11472	1bs. 20000 26620 29700 34140 38485 44180 47665 52020 57360	lbs. 10000 13310 14850 17070 19242 22000 23832 26010 28680	1bs, 30000 39930 44550 51210 57727 66270 71497 78030 86040	533 709 792 910 1026 1178 1271 1387 1529	in, 12×18 13×18 14×20 15×22 16×24 17×24 18×24 19×24		8905 9900 11520 12240 13722	57600 61200 68611	168. 9570 10683 13127 15840 18433 19584 21955 23104	1bs; 39477 44070 54150 65340 76032 80784 90566 95304	797 890 1093 1320 1536 1632 1829 1925
-		Mogt	JL EN	GINE	5.		(Conso	LIDA	TION	Engi	nes.	
	in. 35-40 36-41 37-42 39-43 42-47 45-51 45-54 51-56 54-60	lbs. 4978 6480 7399 9046 10607 12288 12739 13722 14440	1bs. 24891 32400 36997 45230 53035 61440 63697 68611 72200	lbs. 4978 6480 7399 9046 10607 12288 12739 13722 14440	1bs, 29869 38880 44396 54276 63642 73738 76436 82333 86640	663 864 986 1206 1414 1638 1698 1829 1925	in. 14×16 15×18 20×24 22×24	in. 36-38 36-38 48-50 50-52	lbs. 7840 10125 18000 20909	lbs, 39200 50625 90000 104544	14400	lbs. 45472 58725 104400 121271	1045 1350 2400 2787

adhesion given in column 3 by 714 gives the tons of 2000 lbs. that the engine is capable of hauling on a straight and level track, column 7, at slow speed.

The weight of engines given in these tables will be found to agree generally with the actual weights of locomotives recently built, although it must not be expected that these weights will agree in every case with the actual weights, because the different builders do not build the engines alike.

The actual weight on trucks for eight-wheeled or ten-wheeled engines will not differ much from those given in the tables, because these weights depend greatly on the difference between the total and rigid wheel-base, and these are not often changed by the different builders. The proportion between the rigid and total wheel-base is generally the same.

The rule for finding the tractive power is:

 $\left\{ \begin{array}{l} \text{Square of dia. of } \\ \text{piston in inches} \end{array} \right\} \times \left\{ \begin{array}{l} \text{Mean effect. steam} \\ \text{press. per sq. in.} \end{array} \right\} \times \left\{ \begin{array}{l} \text{stroke} \\ \text{in feet} \end{array} \right\}$ = tractive power. Diameter of wheel in feet.

Leading American Types of Locomotive for Freight and Passenger Service.

The eight-wheel or "American" passenger type, having four coupled driving wheels and a four-wheeled truck in front.
 The "ten-wheel" type, for mixed traffic, having six coupled drivers and

a leading four-wheel truck.

8. The "Mogul" freight type, having six coupled driving-wheels and a pony or two-wheel truck in front.

4. The "Consolidation" type, for heavy freight service, having eight coupled driving-wheels and a pony truck in front.

coupled driving-wheels and a pony truck in front.

Besides these there is a great variety of types for special conditions of service, as four-wheel and six-wheel switching-engines, without trucks; the Forney type used on elevated railroads, with four coupled wheels under the engine and a four-wheeled rear truck carrying the water-tank and fuel; locomotives for local and suburban service with four coupled driving-wheels, with a two-wheel truck front and rear, or a two-wheel truck front and a four-wheel truck rear, etc. "Decapod" engines for heavy freight service have ten coupled driving-wheels and a two-wheel truck in front.

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\bigcirc \bigcirc \bigcirc \bigcirc \bigcirc	00000

Classification of Locomotives (Penna. R. R. Co., 1900).—Class A. two pairs of drivers and no truck. Class B, three pairs of drivers and no truck. Class C, four pairs of drivers and no truck. Class D, two pairs of drivers and four-wheel truck. Class E, two pairs of drivers four-wheel truck, and trailing wheels. Class F, three pairs of driving-wheels and two-wheel truck. Class G, three pairs of drivers and four-wheel truck. Class H, four pairs of drivers and two-wheel truck. Class A is commonly called a "four-wheeler"; B, a "six-wheeler"; D, an "eight-wheeler," or "American" type; E, "Atlantic" type; F, "Mogul"; G, "ten-wheeler"; H, "Consolidation."

Steam-distribution for High-speed Locomotives.

(C. H. Quereau, Eng'g News, March 8, 1894.)

Balanced Valves.—Mr. Philip Wallis, in 1886, when Engineer of Tests for the C., B. & Q. R. R., reported that while 6 H.P. was required to work unbalanced valves at 40 miles per hour, for the balanced valves 2.2 H.P. only WAS DECESSARY.

Effect of Speed on Average Cylinder-pressure.—Assume that a locomotive s a train in motion, the reverse ever is placed in the running notch, and track is level; by what is the maximum speed limited? The resistance the train and the load increase, and the power of the locomotive deases with increasing speed till the resistance and power are equal, when speed becomes uniform. The power of the engine depends on the range pressure in the cylinders. Even though the cut-off and boiler-ssure remain the same, this pressure decreases as the speed increases; cause of the higher piston-speed and more rapid valve-travel the steam s a shorter time in which to enter the cylinders at the higher speed. The lowing table, from indicator-cards taken from a locomotive at varying seds, shows the decrease of average pressure with increasing speed:

les per houreed, revolutions		51 248	51 248	53 258	54 263	57 277	60 292	66 321
erage pressure per eq. in.: Actual	51.5	44.0 46.5	47.8 46.5	43.0 44.7	41.3 48.8	42.5 41.8	87.8 89.5	36.3 35.9

he "average pressure calculated" was figured on the assumption that mean effective pressure would decrease in the same ratio that the speed reased. The main difference lies in the higher steam-line at the lower reased. The main uncrence here in the ingler steam-line at an over eds, and consequent higher expansion-line, showing that more steam ered the cylinder. The back pressure and compression-lines agree quite sely for all the cards, though they are slightly better for the slower eds. That the difference is not greater may safely be attributed to the ge exhaust-ports, passages, and exhaust tip, which is 5 in. diameter. see are matters of great importance for high speeds.

loiler-pressure.—Assuming that the train resistance increases as the speed er about 20 miles an hour is reached, that an average of 50 lbs. per sq. is the greatest that can be realized in the cylinders of a given engine at 40 es an hour, and that this pressure furnishes just sufficient power to keep train at this speed, it follows that, to increase the speed to 50 miles, the an effective pressure must be increased in the same proportion. To inase the capacity for speed of any locomotive its power must be increased, l at least by as much as the speed is to be increased. One way to accom-h this is to increase the boiler-pressure. That this is generally realized, hown by the increase in boiler pressure in the last ten years. For twentyes single-expansion locomotives described in the railway journals this
r the steam-pressures are as follows: 3, 160 lbs.; 4, 165 lbs.; 2, 170 lbs.;
180 lbs.; 1, 190 lbs.

"alve-travel.—An increased average cylinder-pressure may also be ained by increasing the valve-travel without raising the boiler-pressure, better results will be obtained by increasing both. The longer travel as a higher steam-pressure in the cylinders, a later exhaust-opening, rexhaust-closure, and a larger exhaust-opening—all necessary for high eds and economy. I believe that a 20-in. port and 614-in. (or even 7-in.) rel could be successfully used for high-speed engines, and that frequently to doing the cylinders could be economically reduced and the counter-nice lightened. Or, better still, the diameter of the drivers increased, iring lighter counterbalance and better steam-distribution.

ze of Drivers.—Economy will increase with increasing diameter of ers, provided the work at average speed does not necessitate a cut-off er than one fourth the stroke. The piston-speed of a locomotive with a drivers at 55 miles per hour is the same as that of one with 68-in.

ers at 61 miles per hour.

eam-ports.—The length of steam-ports ranges from 15 in, to 23 in., and considerable influence on the power, speed, and economy of the locoive. In cards from similar engines the steam-line of the card from the ne with 23-in, ports is considerably nearer boiler-pressure than that of and from the engine with 1714-in. ports. That the higher steam-line is to the greater length of steam-port there is little room for doubt. The port produced 531 H.P. in an 18½ in. cylinder at a cost of 23.5 lbs. of sated water per I.H.P. per hour. The 17½ in. port, 424 H.P., at the rate 9 lbs. of water, in a 19 in. cylinder.

len Valves —There is considerable difference of opinion as to the advan-

of the Allen ported valve (See Eng. News., July 6, 1893.)

ced of Hailway Trains.—In 1834 the average speed of trains on iverpool and Manchester Railway was twenty miles an hour; in 1884

was twenty-five miles an hour. But by 1840 there were engines on the Great

Western Railway capable of running fift? miles an hour with a train, and eighty miles an hour without. (Trans. A. S. M. E., vol. xiii., 363.)

The limitation to the increase of speed of heavy locomotives seems at present to be the difficulty of counterbalancing the reciprocating parts. The present to be the difficulty of counterbalancing the reciprocating parts. The sune of the driver on the rail to vary with every revolution. Whenever the speed is high, it is of considerable magnitude, and its change in direction is so rapid that the resulting effect upon the rail is not inappropriately called a "hammer blow." Heavy rails have been kinked, and bridges have been shaken to their fall under the action of heavily balanced drivers revolving at high speeds. The means by which the evil is to be overcome has not yet been made clear. See paper by W. F. M. Goss, Trans. A. S. M. E., vol. xvi. Engine No. 999 of the New York Central Railroad ran a mile in 32 seconds equal to 112 miles per hour. May 11. 1893.

equal to 112 miles per hour, May 11, 1893.

Speed in miles $= \frac{\text{circum. of driving-wheels in in. } \times \text{no. of rev. per min. } \times 60}{\text{circum. of driving-wheels in in. } \times \text{no. of rev. per min. } \times 60}$ per hour 63,360

= diam, of driving-wheels in in. × no of rev. per min. × .003 (approximate, giving result 8/10 of 1 per cent too great).

Formulæ for Curves. (Baldwin Locomotive Works.)

Approximate Formula for Radius. Approximate Formula for Swing. $R = \frac{.7646W}{}$ w_T

R = radius of min. curve in feet.

P = play of driving-wheels in decimals of 1 ft. W = rigid wheel-base in feet.

= 8.

W = rigid wheel base.T = total

R = radius of curve. S = swing on each side of centre."

Performance of a High-speed Locomotive.—The Baldwin compound locomotive No. 1027, on the Phila. & Atlantic City Ry., in July and

eompound locomotive No. 1927, on the Phila. & Atlautic City Ry., in July and August, 1897, made a record of which the following is a summary:
On July 2d a train was placed in service scheduled to make the run between the terminal cities in 1 hour. Allowing 8 minutes for ferry from Philadelphia to Camden, the time for the 55½ miles from the latter point to Atlantic City was 52 minutes, or at the rate of 64 miles per hour. Owing to the inability of the ferry-boats to reach Camden on time, the train always left late, the average detention being upwards of 2 minutes. This loss was invariably made up, the train arriving at Atlantic City ahead of time, 2 minutes on an average, every day. For the 52 days the train ran, from July 2d to August 31st, the average time consumed on the run was 48 minutes, equivalent to a uniform rute of speed from start to stop of 69 miles per hour. On July 14th the run from Camden to Atlantic City was made in 445 min., an average of 71.6 miles per hour f r the total distance. On 22 days the train consisted of 5 cars and on 30 days it was made up of 6, the weight of cars being as follows: combination car, 57,200 lbs.; coaches, each, 59,200 lbs. cars being as follows: combination car, 57,200 lbs.; coaches, each, 59,200 lbs.;

cars being as follows: combination car, 57,200 lbs.; coaches, each, 59,200 lbs.; Pullman car, 85,500 lbs.

The general dimensions of the locomotive are as follows: cylinders, 13 and 22 × 26 in.; height of drivers, 84¼ in.; total wheel-base, 26 ft. 7 in.; driving-wheel base, 7 ft. 3 in.; length of tubes, 13 ft.; diameter of boiler, 68¼ in.; diameter of tubes, 1¼ in.; number of tubes, 278; length of fire-box, 137% in.; width of fire-box, 96 in.; heating-surface of fire-box, 186.4 sq. ft.; teals curface of tubes, 161.4, 9a, ft.; total heating-surface, 1835.1 sq. ft.; tank capacity, 4000 gallons; boiler-pressure, 200 lbs. per sq. in.; total weight of engine and tender, 27.000 lbs.; weight on drivers (about), 78,600 lbs.

Locomotive Link Motion," 1688, shows that the location of the eccentric-rods introduce two errors in the motion which are corrected by the engular

rods introduce two errors in the motion which are corrected by the angular

ribration of the connecting-rod and by locating the saddle-stud back of the ink-arc. He holds that it is probable that the opinions of the critics of the comotive link motion are mistaken ones, and that it comes little short of ill that can be desired for a locomotive valve motion. The increase of lead rom full to mid gear and the heavy compression at mid gear are both alvantages and not defects. The cylinder problem of a locomotive is endvantages and not defects. The cylinder problem of a locomotive is en-irely different from that of a stationary engine. With the latter the problem is to determine the size of the cylinder and the distribution of team to drive economically a given load at a given speed. With locomotives he cylinder is made of a size which will start the heaviest train which the udhesion of the locomotive will permit, and the problem then is to utilize hat cylinder to the bess advantage at a greatly increased speed, but under

greatly reduced mean effective pressure.

Negative lead at full gear has been used in the recent practice of some ailroads. The advantages claimed are an increase in the power of the ugine at full gear, since positive lead offers resistance to the motion of the siston; easier riding; reduced frequency of hot bearings; and a slight gain a fuel economy. Mr. Halsey gives the practice as to lead on several roads

s follows, showing great diversity:

	Full Gear	Full Gear	Reversing
	Forward, in.	Back, in.	Gear, in.
lew York, New Haven & Hartford	1/16 pos. 0 1/32 pos. 1/16 neg. 0 3/16 neg.	14 neg. 14 neg. 9/64 neg. 0	14 pos. abt 3/16 5/16 pos. 3/16 to 9/16 14 pos.

The link-chart of a locomotive built in 1897 by the Schenectady Locomotive Vorks for the Northern Pacific Ry. is as follows:

Le	ad.	Valve	Open.	Cut	-off.
Forward Stroke, in.	Rearward Stroke, in.	Forward Stroke, in.	Rearward Stroke, in.	Forward Stroke, in.	Rearward Stroke, in.
- ½ - 1/3? + 1/3? + 1/32 3/82 1/6 9/64 5/82 s. 5/32 5/32 f.	- 1/82 - 1/32 + 1/32 3/32 1/6 9/64 5/32 s. 5/32 5/32 f.	1 76 1 7/16 1 1/16 23/82 14 98 5/16 14 7/82	1 76 1 7/16 1 1/16 23/32 3/6 5/16 1/4 7/32	22 9/16 21 19 16 13 10 8 6 4	225/8 21 19 16 133/8 10 8 6 4 1/16

Cylinders 20×26 in., driving-wheels 69 in., six coupled wheels, main rods 3614 in., radius of link 40 in., lap 11/4 in., travel 6 in., Allen valve.

DIMENSIONS OF SOME LARGE AMERICAN LOCOMOTIVES, 1893.

The four locomotives described below were exhibited at the Chicago Exposition in 1893. The dimensions are from Engineering News, June, 1893. The first, or Decapod engine, has ten-coupled driving wheels. It is one of he heaviest and most powerful engines ever built for freight service. The ne neaviest and most powerful engines ever outlit for rieignt service. The 'hiladelphia & Reading engine is a new type for passenger service, with four-oupled drivers. The Rhode Island engine has six drivers, with a 4-wheel sading truck and a 2-wheel trailing truck. These three engines have all ompound cylinders. The fourth is a simple engine, of the standard Amerian 8-wheel type, 4 driving-wheels, and a 4-wheel truck in front. This ngine holds the world's record for speed (1893) for short distances, having un a mile in 32 seconds.

	T =	1 - 11 1		
	Baldwin.	Baldwin.	Rhode Isl.	N. Y. C. & H. R. R.
	N. Y., L. E.	Phila.	Locomoti'e	H. K. K.
	&&		Works.	Tambite
	W. R. R.	Read. R. R.	Heavy	_State
	Decaped	Express	Express.	Express,
	Freight.	Passenger.	Express.	No. 999.
Running-gear:		i	1	1
Driving-wheels, diam	4 ft. 2 in.	6 ft. 6 in. 4 " 0 "	6 ft. 6 in.	7 ft. 2 in.
Truck " "	2 " 6 "	4 " 0 "	2 " 9 "	8 " 4 "
Journals, driving-axles	9 × 10 in.	816 × 12 in.	8 × 834 in.	9 × 1236in.
" truck- "	5 × 10 "	616×10 "	516 × 10 "	614 × 10 "
" tender- "	416× 9 "	41/6×8 "	41/4×8 "	416×8 "
Wheel-base:				l
Driving	18 ft. 10 in.	6 ft. 10 in.	13 ft. 6 in.	8 ft. 6 in. 23 " 11 " 15 ft. 216 "
Total engine	27 " 8 "	28 " 4 " 16 " 0 "	29 11 974 11	23 " 11 "
" tender	16 " 8 " 53 " 4 "	16 " 0 "	10 0	15 π. 216 "
engine and tender	53 " 4 "	47 3	50 " 694 "	47 " 8/8 "
Wt. in working-order:	100 000 15-	93 COO 11-	00 500 15-	04 000 11-
On drivers	170,000 lbs.	82,700 lbs. 47,000 " 129,700 "	88,500 lbs. 54,500 "	84,000 lbs.
On truck-wheels	20,000	190 200 (143,000 "	40,000 **
Engine, total	192,500 " 117,500 "	80,578 "	75,000 "	124,000 " 80,000 "
Engine and tender, loaded	1 11,000	210,273 "	218,000 "	204,000 **
Cylindars .	310,000	210,610	210,000	204,000
Cylinders: h.p. (2)	16 × 28 in.	13 × 24 in.	one 21 × 26	19×24 in.
l.p. (2)	27×28	22 × 24 "	one 31 × 26	10 ~ ~ 1111.
Distance centre to centre.	7 ft. 5 "	7 ft. 414 in.	7 ft. 1 in.	6 ft. 5 in.
Piston-rod, diam	4 in.	31/2 in.	346 in.	8% in.
Connecting rod, length	9' 8 7/16"	8 ft. 016 in.	10 ft. 316 in. 116 × 20 and 116 × 25	8 ft. 116 in.
	1		11/6 × 20 and	l
Steam-ports	281/2×2 in.	24 × 11/2 in.	11/2×25	13/6 × 18 in.
Exhaust-ports	281/4×8 "	24 × 41/6 "	8×20 in.	2% × 18 "
Slide-valves, out. lap, h.p.	% in.	% in.	1¼ in.	1 in.
" out lap, l.p	76 "	% in.	1 in.	
ш. шр, п.р		(neg.) ¼ in. None		1/10 in.
m, m, inp, i.p		None		
" max. travel." lead, h.p	6 in.	5 in.	6¼ in. 8/82 "	51∕≨ in.
" " lead in	1/16 in.	16 " 18 "	8/82 "	····
	5/16 "	Straight	Wagon ton	Wagon ton
Boiler-Type Diam. of barrel inside	Straight	4 ft. 81/4 in.	Wagon top 5 ft. 2 in.	Wagon top 4 ft. 9 in.
Thickness of barrel-plates	6 ft. 21% in.	% in.	% in.	9/16 in.
Height from rail to centre	74	78 ****	78	•/10 111.
line	8 ft. 0 in.		8 ft. 11 in.	7 ft. 1136 in.
Length of smoke-box	8 ft. 0 in. 5 " 7% "		8 ft. 11 in.	7 ft. 1134 in.
Working steam pressure	180 ĺbs.	180 lbs.	200 lbs.	190 lbs.
Firebox—type	Wootten	Wootten	Radial stav	Buchanan
Length inside	10′ 11 9/16′′	9 ft. 6 in.	10 ft. 0 in.	9 ft. 6% in.
Width "	8 ft. 21/8 in.	9 ft. 6 in. 8 " 016 " 3 " 294 "	10 ft. 0 in.	9 ft. 6% in. 3 " 4% " 6 " 114 "
Depth at front	4 " 6 "	3 " 294 "	6 " 1034 "	6 " 11/4 "
Thickness of side plates	5/16 in.	1 D/101n.	i a/inan	I OZIDIN.
oack plate	5/16 "	5/16 "	26	5/16 "
Thickness of crown-sheet.	36 "	5/16 " 5/16 "	36 " 37 "	5/16
" "tube " .	90 28 24	70 0 0 0 0		90 75
Grate-areaStay-bolts, diam., 11/6 in.	89.6 sq. ft.	76.8 sq. ft.	28 sq. ft. 4 in.	30.7 sq. ft. 4 in.
Tubes—iron	354	324	272	268
Pitch	23/4 in.	2 1/16 in.	23% in.	~~~
Diam., outside	274	134 in.	274	g in.
Length betw'n tube-plates		10 ft. 0 in.	12 ft. 856 in.	12 ft. 0 in.
Heating-surface:	ŀ			
Tubes, exterior	2,208.8 ft.	1,262 sq. ft.		1,697 sq. ft.
Fire-box	284.3 "	178 " "		1,697 sq. ft. 288 '' ''
Miscellaneous:	1			
Exhaust-nozzle, diam	5 in.	516 in.		81/g in.
Smokestack, smal'st diam.	1 ft. 6 "	1 ft. 6 in.	1 ft. 8 in.	1 ft. 814 in.
" height from	18 11 01/ 11			14 11 10 11
rail to top	15 61/6 ,,	14 ft. 0% in.	15 " % "	14 " 10 "

Name of Railroad.	Passenger or	No. of Drivers.	No. of Front Truck-wheels	Diam. of Driv- ing-wheels, in	Size of Cylinders, Inches.	Total Weight of Engine, lbs.	Total Weight on Driving. wheels, los.	Area of Grate, sq. ft.	Firebox Heat- ing-surface, sq. ft.	Tube Heating- surface, sq. ft.	Steam-press- ure per sq. in. Atmospheric, lbs.	Length of Tubes, ft. and in.	Piam.of Tubes,	Fatio of Cyl- inder-power to Weight, Avail- able for Ad- hesion.
C. M. & St. P.	<u> 4</u>	4	4	88	16×94		64,000	15.5	115	<u>8</u>	160	!		0.461
<u>~</u>	::	4 4	4.4	8 2	19×24 01 0 06		75.90 0.80 0.80 0.80 0.80	5 84 84	88	1846.8	35			0.421
C, C, & St. L.	:	9	4	88	18½×34		102,800	18.2		1888.4	160			9.80
Penn. R. R.	::	44	4 4	82	19×94 10×94	193,000	88. 80. 80. 80. 80.	8 % 8 %	144.3	1672.2	3,2	200	35 35	0.358
	:	4	4	28	18×24		99	24.5	===	1301	89	:	•	0.426
N. Y. C. & H. R.	: :	4 1	4.	တ္ ရွင္ ရွ	19×24	126,150	26.8 6.5 6.5	20 00 20 00 20 00	147.7	1670.7	36	21.2	S 0	200
βE	:	• 9	* 4	888	20×24 =	127,600	100,00	88.5	8		38		9	0.855
1 :	:	9	4	74	and 29	135,000	000,66	28.5	141.2	1839.5	8		<u>:</u>	0.889
ĸ,	::	9	4.	7.5	and 30		102,000	88.8	141.7		<u>8</u> 9		0 2 C	9.404
C. R. R. of N. J	: :	4 æ	4 4	<u>ي</u>	13 and 22 x 24	123,800	50	88			38	-	s 01	0.542
Philadelphia & Reading	;	4	.03	200	and 22	129,000	83,000	92	128.9	1261.7	170		7.	0.423
3	:	9	જ	83	and 29		000	22.7	138	88	88		•	
C., M. & St. P.	= [9	4:	ည် ကို	and 31	143,000	86	:	:	:	3			
8	<u>.</u> :	0 5	× C	82			150.800		9	2171	38			
C C & St L	:	9	4	328			99,66		147	1883.4	99			
٠:	:	00	C)	23		125,000	113,400			158	25			
	: :	9	4.	8:	30×36	127,500	101 86,500	88.2 70.7	146.2	1608	35			
2 I. E	:	00	4 C	42	EXXEL	190,000	18,000			ecte.	35			
Parific	:	~	1 4	4.5	and 28 x	126,000	90,20			1788.3	26			
V L E	;	2	. 63	28	and 27 ×	200,550	173,700		182.5	808	35			
rnwall &	:	00	Q	28	and 24 ×	150,000	135,000		:	:	25			
M. & St.	: :	4:	4.0	3	and 20 x	122,400	97,970		:	:	6.5			
N. Y., L. E. & W. Cornwall & Lebanon C. M. & St. P. Ilnois Central	::::	<u>5</u>	St St 4 St	8888	16 and 27 × 28 14 and 24 × 28 12 and 20 × 26 20 and 29 × 26	200,550 150,000 122,400 128,500	173,700 135,000 107,970	8 8 8 8 8 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6		9022		8858	2885	

Dimensions of Some American Locomotives.—The table on page 861 is condensed from one given by D. L. Barnes, in his paper on "Distinctive Features and Advantages of American Locomotive Practice," Trans. A.S.C. E., 1893. The formula from which column marked "Ratio of cylinder-power to weight available for adhesion" is calculated as follows:

 $2 \times \text{cylinder area} \times \text{boiler-pressure} \times \text{stroke}$

Weight on drivers x diameter of driving-wheel

(Ratio of cylinder-power of compound engines cannot be compared with

that of the single-expansion engines.)

Where the boiler-pressure could not be determined from the description of the locomotives, as given by the builders and operators of the locomotives,

of the locomotives, as given by the officiers and operators of the locomotives, it has been assumed to be 160 lbs, per sq. in. above the atmosphere. For compound locomotives the figures in the last column of ratios are based on the capacity of the low-pressure cylinders only, the volume of the high-pressure being omitted. This has been done for the purpose of comparison, and because there is no accurate simple way of comparing the cylinder-power of single-expansion and compound locomotives.

Dimensions of Standard Locomotives on the N. Y. C. & H. R. and Penna. R. R., 1882 and 1893.

C. H. Quereau. Eng'a News. March 8, 1894.

	N.	Y. C. 8	t H. R	. R.	Per	nsylva	nia R	R.
		ough enger.		ough ght.		ough enger.		ough ight.
	1882.	1893.	1882.	1893.	1882.	1893.	1882.	1893.
Grate surface, sq. ft Heating surface, sq. ft Boiler, diam., in Driver, diam., in Steam-pressure, lbs	17.87 1853 50 70 150	58 78, 86	17.87 1353 50 64 150	29.8 1763 58 67 160	17.6 1057 50 62 125	83.2 1583 57 78 175	28. 1260 54 50 125	81.5 1498 60 50 140
Cylin., diam. and stroke. Valve-travel, ins Lead at full gear, ins	17×24	19×24 516	17×24	19×26	17×24 5 1/16		20×24	20×24 5 1/16
Outside lap	3⁄8 0 15⅓	1 0 18	1/16l 151/4	3/321 18	34 0 16	1 16cl 1714	1/8:21 1/8:21 16	3/4 1/321 16
" width Type of engine	1½ Am.	1½ Am.	13/4 Am.	Mog.	11/4 Am.	11/4 Am.	Cons.	158 Cons.

Indicated Water Consumption of Single and Compound Locomotive Engines at Varying Speeds.

C. H. Quereau, Eng'a News, March 8, 1894.

Two-c	ylinder Cor	npound.	Single-expansion.		
Revolu- tions.	Speed, miles per hour.	Water per I.H.P. per hour.	Revolu- tions.	Miles per Hour,	Water.
100 to 150 150 " 200 200 " 250 250 " 275	21 to 31 81 " 41 41 " 51 51 " 56	18.33 lbs. 18.9 " 19.7 " 21.4 "	151 219 258 807 821	81 45 52 63 66	21.70 20.91 20.52 20.28 20.01

It appears that the compound engine is the more economical at low speeds, the economy decreasing as the speed increases, and that the single engine increases in economy with increase of speed within ordinary limits, becoming more economical than the compound at speeds of more than 50 miles

per hour.

The C., B. & Q. two-cylinder compound, which was about 80% less economical than simple engines of the same class when tested in passenger nomical than simple engines of the the more economical in freight service

nan the best single-expansion engine, and 29% more economical than the verage record of 40 simple engines of the same class on the same division. Indicator-tests of a Locomotive at High Speed. (Locomo-ive Eng'y, June, 1893.)—Cards were taken by Mr. Angus Sinclair on the comotive drawing the Empire State Express.

RESULTS OF INDICATOR-DIAGRAMS.

ard No.	Revs.	Miles per hour.	I.H.P.	Card No.	Revs.	Miles. per hour.	I.H.P.
1	160	37.1	648.3	. 7	804	70.5	977
2	260	60.8	728	1 8	296	68.6	972
8	190	44	551	9	800	69.6	1,045
4	250	58	891	10	804	70.5	1,059
5	260	60	960	11	340	78.9	1,120
6	298	69	988	12	810	71.9	1,026

The locomotive was of the eight-wheel type, built by the Schenectady ocomotive Works, with 19 × 24 in. cylinders, 78-in. drivers, and a large oiler and fire-box. Details of important dimensions are as follows: leating-surface of fire-box, 180.8 sq. ft.; of tubes, 1870.7 sq. ft.; of boiler, 21.5 sq ft. Grate area, 27.3 sq. ft. Fire-box: length, 8 ft.; width, 8 ft. 47& 1. Tubes, 268; outside diameter, 2 in. Ports: steam, 18×1½ in.; exhaust, 3 × 2½ in. Valve-travel, 5½ in. Outside lap, 1 in.; inside lap, 1/64 in. ournals: driving-axle, 8½ × 10½ in.; truck-axle, 6 × 10 in.

The train consisted of four coaches, weighing, with estimated load, 340,000 s. The locomotive and tender weighed in working order 200,000 lbs, aking the total weight of the train about 270 tons. During the time that ie engine was first lifting the train into speed diagram No. 1 was taken. It lows a mean cylinder-pressure of 59 lbs. According to this, the power certed on the rails to move the train is 6558 lbs., or 24 lbs. per ton. The edd is 37 miles an hour. When a speed of nearly 60 miles an hour was sached the average cylinder-pressure is 40.7 lbs., representing a total action force of 4520 lbs., without making deductions for internal friction. we deduct 10% for friction, it leaves 15 lbs. per ton to keep the train going the speed mamed. Cards 6, 7, and 8 represent the work of keeping the ain running 70 miles an hour. They were taken three miles apart, when e speed was almost uniform. The average cylinder-pressure for the three rds is 47.6 lbs. Deducting 10% again for friction, this leaves 17.6 lbs. per nas the power exerted in keeping the train up to a velocity of 70 miles. roughout the trip 7 lbs. of water were evaporated per lb. of coal. The roughout the trip 7 lbs. of water were evaporated per lb. of coal. The ork of pulling the train from New York to Albany was done on a coal comption of about 3½ lbs. per H.P. per hour. The highest power recorded as at the rate of 1120 H.P.

Locomotive-testing Apparatus at the Laboratory of urdue University. (W. F. M. Goss, Trans. A. S. M. E., vol. xiv. 826.)—
te locomotive is mounted with its drivers upon supporting wheels which e carried by shafts turning in fixed bearings, thus allowing the engine to run without changing its position as a whole Load is supplied by four ction-brakes fitted to the supporting shafts and offering resistance to the raing of the supporting wheels. Traction is measured by a dynamometer ached to the draw-bar. The boiler is fired in the usual way, and an haust-blower above the engine, but not in pipe connection with it, carries

all that may be given out at the stack.

4 Standard Method of Conducting Locomotive-tests is given in a report a Committee of the A. S. M. E. in vol. xiv. of the Transactions, page 1312. Waste of Fuel in Locomotives,—In American practice economy fuel is necessarily sacrificed to obtain greater economy due to heavy sin-loads. D. L. Barnes, in Eng. Mag., June, 1894, gives a diagram showing reduction of efficiency of boilers due to high rates of combustion, from ich the following figures are taken:

120 160 75 67 59 51

A rate of 12 lbs. is given as representing stationary-boiler practice, 40 lbs. English locomotive practice, 120 lbs. average American, and 200 lbs. maxum American, locomotive practice.

Advantages of Compounding.—Report of a Committee of the perican Railway Master Mechanics' Association on Compound Locomotives n. Mach., July 8, 1890) gives the following summary of the advantages ned by compounding: (a) It has achieved a saving in the fuel burnt rraging 18st at reasonable boiler-pressures, with encouraging possibilities

of further improvement in pressure and in fuel and water economy. has lessened the amount of water (dead weight) to be hauled, so that (c) the tender and its load are materially reduced in weight. (d) It has increased the possibilities of speed far beyond 60 miles per hour, without unduly straining the motion, frames, axies, or axie-boxes of the engine. (e) It has increased the haulage-power at full speed, or, in other words, has increased the continuous H.P. developed, per given weight of engine and boiler. (f) In some classes has increased the starting-power. (g) It has materially lessened the slide-valve friction per H.P. developed. (h) It has equalized or distributed the turning force on the crank-pin, over a longer portion of its path, which, of course, tends to lengthen the repair life of the engine. (i) In the two-cylinder type it has decreased the oil consumption, and has even done so in the Woolf four-cylinder engine. (j) Its smoother and steadier draught on the fire is favorable to the combustion of all kinds of soft coal; and the on the fire is tayorable to the combustion of all kinds of soft coar; and the sparks thrown being smaller and less in number, it lessens the risk to property from destruction by fire. (k) These advantages and economies are gained without having to improve the man handling the engine, less being left to his discretion (or careless indifference) than in the simple engine. (l) Valve-motion, of every locomotive type, can be used in its best working and most effective position. (m) A wider elasticity in locomotive design is permitted; as if design side-roles and compared with or articulated engines. mitted; as, if desired, side-rods can be dispensed with, or articulated engines of 100 tons weight, with independent trucks, used for sharp curves on mountain service, as suggested by Mallet and Brunner.

Of 27 compound locomotives in use on the Phila. and Reading Railroad (in

1892), 12 are in use on heavy mountain grades, and are designed to be the equivalent of 22 × 24 in. simple consolidations; 10 are in somewhat lighter service and correspond to 20 × 24 in. consolidations; 5 are in fast passenger

service. The monthly coal record shows:

Class of Engine.	No.	Gain in Fuel Economy.
Mountain locomotives	12	25% to 30%
Heavy freight service	10	12% to 17%
Fast passenger		9% to 11%

(Report of Com. A. R. M. M. Assn. 1892.) For a description of the various types of compound locomotive, with discussion of their relative merits, see paper by A. Von Borries, of Germany, The Development of the Compound Locomotive, Trans. A. S. M. E. 1898, vol. xiv., p. 1172.

Counterbalancing Locomotives.—The following rules, adopted by different locomotive-builders, are quoted in a paper by Prof. Lanza (Trans. A. S. M. E., x. 302):

A. "For the main drivers, place opposite the crank-pin a weight equal to one half the weight of the back end of the connecting-rod plus one half the

one half the weight of the dock end of the connecting-rod, piston, piston-rod, and cross-head. For balancing the coupled wheels, place a weight opposite the crank-pin equal to one half the parallel rod plus one half of the weights of the front end of the main-rod, piston, piston-rod, and cross-head. The centres of gravity of the above weights must be at the same distance from the crafts are the craft, pin."

axles as the crank-pin.

B. The rule given by D. K. Clark: "Find the separate revolving weights of crank-pin boss, coupling-rods, and connecting-rods for each wheel, also of crank-pin boss, coupling-rods, and connecting-rods for each wheel, also the reciprocating weight of the piston and appendages, and one half the connecting-rod, divide the reciprocating weight equally between each wheel and add the part so allotted to the revolving weight on each wheel the sums thus obtained are the weights to be placed opposite the crank-pin, and at the same distance from the axis. To find the counterweight to be used when the distance of its centre of gravity is known, multiply the above weight by the length of the crank in inches and divide by the given distance." This rule differs from the preceding in that the same weight is placed in each wheel. placed in each wheel.

C. " $W = \frac{S \times \left(w - \frac{w}{f}\right)}{G}$, in which S = one half the stroke, G = distance

from centre of wheel to centre of gravity in counterbalance, w = weight at crank-pin to be balanced, W = weight in counterbalance, f = coefficient of friction so called, = 5 in ordinary practice. The reciprocating weight is found by adding together the weights of the piston, piston-rod, cross-head, and one half of the main rod. The revolving weight for the main wheel is found by adding together the weights of the crank-pin half early with the counterbalance. found by adding together the weights of the crank-pin hub, crank-pin, one

If of the main rod, and one half of each parallel-rod connecting to this eel; to this add the reciprocating weight divided by the number of eels. The revolving weight for the remainder of the wheels is found in same manner as for the main wheel, except one half of the main rod is t added. The weight of the crank-pin hub and the counterbalance does t include the weight of the spokes, but of the metal inclosing them. This culation is based for one cylinder and its corresponding wheels."

). "Ascertain as nearly as possible the weights of crank-pin, additional ight of wheel boss for the same, add side rod, and main connections, ton-rod and head, with cross head on one side: the sum of these multi-ed by the distance in inches of the centre of the crank-pin from the centre the wheel, and divided by the distance from the centre of the wheel to common centre of gravity of the counterweights, is taken for the total interweight for that side of the locomotive which is to be divided among wheels on that side."

Balance the wheels of the locomotive with a weight equal to the ights of crank-pin, crank-pin hub, main and parallel rods, brasses, etc. is two thirds of the weight of the reciprocating parts (cross-head, piston

d rod and packing)."

rough packing."

"Balance the weights of the revolving parts which are attached to the wheel with exactness, and divide equally two thirds of the weights of reciprocating parts between all the wheels. One half of the main rod is

nputed as reciprocating, and the other as revolving weight." lee also articles on Counterbalancing Locomotives, in R. R. & Eng. Jour., rch and April, 1890; Trans. A. S. M. E., vol. xvi, 305; and Trans. A. M. E., ster Mechanics' Assn., 1897. W. E. Dalby's book fon the "Balancing of gines" (Longmans, Green & Co., 1902) contains a very full discussion of š subject.

Saximum Safe Load for Steel Tires on Steel Bails.
S. M. E., vii., p. 786.)—Mr. Chanute's experiments led to the deduction to 12,000 lbs. should be the limit of load for any one driving wheel. Mr. gus Sinclair objects to Mr. Chanute's figure of 12,000 lbs., and says that occurred which has a light load on it is more injurious to the rail in one which has a heavy load. In English practice 8 and 10 tons are clay used. Mr. Oberlin Smith has used steel estings for committee of the same ely used. Mr. Oberlin Smith has used steel castings for cam-rollers 4 in. m. and 8 in. face, which stood well under loads of from 10,000 to 20,000 Mr. C. Shaler Smith proposed a formula for the rolls of a pivot-bridge ich may be reduced to the form: Load = $1760 \times \text{face} \times \sqrt{\text{diam.}}$, all in . and inches.

ee dimensions of some large American locomotives on pages 860 and 861, the "Decapod" the load on each driving-wheel is 17,000 lbs., and on lo. 999, "21.000 lbs.

larrow-gauge Railways in Manufacturing Works,-bramway of 18 inches gauge, several miles in length, is in the works of Lancashire and Yorkshire Railway. Curves of 13 feet radius are used. Lancashire and Yorkshire Railway. Curves of 18 feet radius are used. slocomotives used have the following dimensions (Proc. Inst. M. E., July, 3): The cylinders were 5 in. diameter with 6 in. stroke, and 2 ft. 314 in. tree to centre. The wheels were 1614 in. diameter, the wheel-base 9 in.; the frame 7 ft. 414 in. long, and the extreme width of the engine et. The boiler, of steel, 2 ft. 3 in. outside diameter and 2 ft. long between e-plates, containing 55 tubes of 184 in. outside diameter; the fire-box, of and cylindrical, 2 ft. 3 in. long and 17 in. inside diameter. The heating-face 10.42 sq. ft. in the fire-box and 36.12 in the tubes, total 46.54 sq. ft.; grate-area, 1.78 sq. ft.; capacity of tank, 2616 gallons; working-pressure, les, per sq. in.; tractive power, say, 1412 lbs., or 9.22 lbs. per lb. of effector pressure per sq. in. on the piston. Weight, when empty, 2.80 tons; and full and in working order, 3.19 tons.

on full and in working order, 3.19 tons.

or description of a system of narrow-gauge railways for manufactories, circular of the C. W. Hunt Co., New York.

Aght Locomotives.—For dimensions of light ocomotives used for, ing, etc., and for much valuable information concerning them, see catale of H. K. Porter & Co., Pittsburgh.

'etroleura-burning Locomotives. (From Clark's Steam-ens.)—The combustion of petroleum refuse in locomotives has been success y practised by Mr. Thos. Urquhart, on the Grazi and Tsaritsin Railway, theast Russia. Since November, 1884, the whole stock of 143 locomotives en his superintendence has been fired with petroleum refuse. The oil is er his superintendence has been fired with petroleum refuse. The oil is cted from a nozzle through a tubular opening in the back of the fire-box, neans of a jet of steam, with an induced current of air.

A brickwork cavity or "regenerative or accumulative combustion-chamber" is formed in the fire-box, into which the combined current breaks as spray against the rugged brickwork slope. In this arrangement the brickwork is maintained at a white heat, and combustion is complete and smokeless. The form, mass, and dimensions of the brickwork are the most important elements in such a combination.

Compressed air was tried instead of steam for injection, but no appreciable

The heating-power of petroleum refuse is given as 19,832 heat-units, equivalent to the evaporation of 30,63 lbs. of water from and at 212° F., or to 17.1 lbs. at 8½ atmospheres, or 125 lbs. per sq. in., effective pressure. The highest evaporative duty was 14 lbs, of water under 8½ atmospheres per lb. of the fuel, or nearly 82 efficiency.

There is no probability of any extensive use of petroleum as fuel for local and the 17. Local content of the fuel for local and the 17. Local content of the fuel for local and the 17. Local content of the fuel for local and the 17. Local content of the fuel for local and the 17. Local content of the fuel for local and the 17. Local content of the pull for local and the 17. Local content of the pull for local and the 17. Local content of the pull for local and the 17. Local content of the pull for local and the 17. Local content of the pull for local and the 17. Local content of the pull for local and the 17. Local content of the pull for local and the 17. Local content of the 18. Local content of

motives in the United States, on account of the unlimited supply of coal and the comparatively limited supply of petroleum. Texas oil is now (1902) used in locomotives of the Southern Pacific Railway.

Fireless Locomotive. - The principle of the France locomotive is that it depends for the supply of steam on its spontaneous generation from a body of heated water in a reservoir. As steam is generated and drawn

a body of heated water in a reservoir. As steam is generated and drawn off the pressure falls; but by providing a sufficiently large volume of water heated to a high temperature, at a pressure correspondingly high, a margin of surplus pressure may be secured, and means may thus be provided for supplying the required quantity of steam for the trip.

The fireless locomotive designed for the service of the Metropolitan Railway of Paris has a cylindrical reservoir having segmental ends, about 5 ft. 7 in. in diameter, 26% ft. in length, with a capacity of about 620 cubic feet. Four fifths of the capacity is occupied by water, which is heated by the aid of a nowerful jet of steam supplied from stationary boilers. The water is of a powerful jet of steam supplied from stationary boilers. The water is heated until equilibrium is established between the boilers and the reservoir. The temperature is raised to about 390° F., corresponding to 225 ibs. per sq. in. The steam from the reservoir is passed through a reducing valve, by which the steam is reduced to the required pressure. It is then passed through a tubular superheater situated within the receiver at the passed through a tubular superheater situated within the receiver at the upper part, and thence through the ordinary regulator to the cylinders. The exhaust-steam is expanded to a low pressure, in order to obviate noise of escape. In certain cases the exhaust-steam is condensed in closed vessels, which are only in part filled with water. In the upper free space a pipe is placed, into which the steam is exhausted. Within this pipe another pipe is fixed, perforated, from which cold water is projected into the sur-rounding steam, so as to effect the condensation as completely as may be.

rounding steam, so as to effect the condensation as completely as may be. The heated water falls on an inclined plane, and flows off without mixing with the cold water. The condensing water is circulated by means of a centrifugal pump driven by a small three-cylinder engine.

In working off the steam from a pressure of 225 lbs. to 67 lbs., 530 cubic feet of water at 390° F, is sufficient for the traction of the trains, for working the circulating-pump for the condensers, for the brakes, and for electric-lighting of the train. At the stations the locomotive takes from 2200 to 3300 lbs. of steam—nearly the same as the weight of steam consumed during the number tween two consecutive charging stations. run between two consecutive charging stations. There is 210 cubic feet of condensing water. Taking the initial temperature at 60° F., the tempera-

ture rises to about 180° F. after the longest runs underground.

The locomotive has ten wheels, on a base 24 ft. long, of which six are coupled, 4½ ft. in diameter. The extreme wheels are on radial axles. The

cylinders are 23½ in. in diameter, with a stroke of 23½ in.

The engine weighs, in working order, 53 tons, of which 36 tons are on the coupled wheels. The speed varies from 15 miles to 25 miles per hour. The trains weigh about 140 tons.

Compressed-air Locomotives.—For an account of the Mekarski system of compressed-air locomotives see page 510 ante.

SHAFTING.

(See also Torsional Strength; also Shafts of Steam-engines.)

r diameters of shafts to resist torsional strains only, Molesworth gives $\sqrt[3]{\frac{Pl}{K}}$, in which d= diameter in inches, P= twisting force in pounds ied at the end of a lever-arm whose length is l in inches, K= a coefficience 460, bronze 425, copper 380, tin 220, lead 170. The value given for steel probably applies only to high-carbon steel, urston gives:

= horse-power transmitted, d = diameter of shaft in inches, R = revins per minute.

3. Francis gives for turned-iron shafting $d = \sqrt[3]{\frac{100 \text{ H.P.}}{R}}$.

es and Laughlins give the same formulæ as Prof. Thurston, with the ving exceptions: For line shafting, hangers 8 ft. apart:

cold-rolled iron, H.P. =
$$\frac{d^3R}{50}$$
, $d = \sqrt[3]{\frac{50}{R}}$.

simply transmitting power and short counters

turned iron, H.P. =
$$\frac{d^3R}{50}$$
, $d = \sqrt[3]{\frac{50 \text{ H.P.}}{R}}$; cold-rolled iron, H.P. = $\frac{d^3R}{30}$, $d = \sqrt[3]{\frac{30 \text{ H.P.}}{R}}$.

y also give the following notes: Receiving and transmitting pulleys d always be placed as close to 1 earings as possible; and it is good practoframe short "headers" between the main tie-beams of a mill so as poort the main receivers, carried by the head shafts, with a bearing to each side as is contemplated in the formulæ. But if it is preferred, cessary, for the shaft to span the full width of the "bay" without in

termediate bearings, or for the pulley to be placed away from the bearings towards or at the middle of the bay, the size of the shaft must be largely increased to secure the stiffness necessary to support the load without un-

increased to secure the stiffness necessary to support the load without unded deflection. Shafts may not deflect more than 1/80 of an inch to each foot of clear length with safety.

To find the diameter of shaft necessary to carry safely the main pulley at the centre of a bay: Multiply the fourth power of the diameter obtained by above formulæ by the length of the "bay." and divide this product by the distance from centre to centre of the bearings when the shaft is supported as required by the formula. The fourth root of this quotient will be the diameter required.

The following table, computed by this rule, is practically correct and safe.

it given the For- læ for d Shafts.	Diame	ter of Si a Bay, w	aft nece hich is f	ssary to rom Cen	carry th	e Load a	at the Ce Bearings	entre of
Dian Sha by min Hea	21% ft.	8 ft.	31% ft.	4 ft.	5 ft.	6 ft.	8 ft.	10 ft,
in.	in. 21/8	in. 21/4	in. 284	in. 216	in. 25%	in. 23/4	in. 276	in.
23/6 8 83/6	878	296 816 316	234 814 856	27/6 88/6 88/4	8 31/4	816 894 414	87% 4 416	896 414 484
41/6		4	416	41/4 45/6	41/6 47/8	497	512	553
51⁄2				51/g 6	5% 6%	6 65/6	614 718	633

As the strain upon a shaft from a load upon it is proportional to the product of the parts of the shaft multiplied into each other, therefore, should the load be applied near one end of the span or bay instead of at the centre, multiply the fourth power of the diameter of the shaft required to carry the load at the centre of the span or bay by the product of the two parts of the shaft when the load is near one end, and divide this product whe product of the two parts of the shaft when the load is carried at the centre. The fourth root of this quotient will be the diameter required.

The shaft in a line which carries a receiving-nulley, or which carries a

The shaft in a line which carries a receiving-pulley, or which carries a transmitting-pulley to drive another line, should always be considered a head-shaft, and should be of the size given by the rules for shafts carrying

main pulleys or gears

Deflection of Shafting. (Pencoyd Iron Works.)—As the deflection of steel and iron is practically alike under similar conditions of dimensions and loads, and as shafting is usually determined by its transverse stiffness rather than its ultimate strength, nearly the same dimensions should be

used for steel as for iron.

used for steel as for iron. For continuous line-shafting it is considered good practice to limit the deflection to a maximum of 1/100 of an inch per foot of length. The weight of bare shafting in pounds $= 2.6d^3L = W$, or when as fully loaded with pulleys as is customary in practice, and allowing 40 lbs, per inch of width for the vertical pull of the belts, experience shows the load in pounds to be about $18d^3L = W$. Taking the modulus of transverse elasticity at 26,000,000 lbs, we desire from authoristics formulas the following: lbs., we derive from authoritative formulæ the following:

$$L = \sqrt[3]{873d^3}$$
, $d = \sqrt{\frac{L^3}{873}}$, for bare shafting;
 $L = \sqrt[3]{175d^3}$, $d = \sqrt{\frac{L^3}{175}}$, for shafting carrying pulleys, etc.;

L being the maximum distance in feet between bearings for continuous shafting subjected to bending stress alone, d = diam, in inches.

The torsional stress is inversely proportional to the velocity of rotation. while the bending stress will not be reduced in the same ratio. It is there fore impossible to write a formula covering the whole problem and suffily simple for practical application, but the following rules are correct in the range of velocities usual in practice. reontinuous shafting so proportioned as to deflect not more than 1/100 inch per foot of length, allowance being made for the weakening to five-seats.

$$d = \sqrt[3]{\frac{50 \,\mathrm{H.P.}}{R}}, \ L = \sqrt[3]{720 d^3}, \text{ for bare shafts;}$$

$$d = \sqrt[3]{\frac{70 \, \mathrm{H:P.}}{R}}$$
, $L = \sqrt[3]{140 d^2}$, for shafts carrying pulleys, etc.

iam, in inches, L= length in feet, $R\Rightarrow$ revs. per min. following table (by J. B. Francis) gives the greatest admissible dissective the bearings of continuous shafts subject to no transverse except from their own weight, as would be the case were the power off from the shaft equal on all sides, and at an equal distance from inger-bearings.

	Distance bet Bearings, i			Distance bet Bearings, i	
of Shaft, inches.	Wrought-iron Shafts, 15.46 17.70 19.48 20.99	Steel Shafts. 15.89 18.19 20.02 21.57	Diam of Shaft, in inches, 6 7 8		Steel Shafts 22.92 24.13 25.23 26.24

e conditions, however, do not usually obtain in the transmission of by belts and pulleys, and the varying circumstances of each case it impracticable to give any rule which would be of value for univerilication.

example, the theoretical requirements would demand that the beare nearer together on those sections of shafting where most power vered from the shaft, while considerations as to the location and contiguity of the driven machines may render it impracticable to the driving-pulleys by the intervention of a hanger at the theory required location. (Joshua Rose.)

-power Transmitted by Turned Iron Shafting at Different Speeds.

me Mover or Head Shaft carrying Main Driving-pulley or Gear, well supported by Bearings. Formula: H.P. = d^3R + 125.

Number of Revolutions per Minute.													
60	80	100	125	150	175	200	225	250	275	300			
I.P. 2.6	H.P. 8.4	H.P. 4.8	H.P. 5.4	H.P. 6.4	H.P. 7.5	H.P. 8.6	H.P. 9.7	H.P. 10.7	H.P. 11.8	H.P.			
8.8	5.1	6.4	8.4	9.6		12.8		16.7	17.6	12.9 19.2			
5.4	7.8		10	12	14	16	18	20	22	24			
7.5	10	12.5		18	22	25	28	31	84	37			
b	18	16	20	24 30	28	82	86	40	44	48			
3	17	20	25	30	85	40	45	50	55	60			
3	22	20 27 84 42	84	40 51	47	54	61	67	74	81			
)	27	84	42	51	59	68	76	85	98	102			
5	88	42	52	63	73	84	94	105	115	126			
)	41	51	64	76	89	102	115	127	140	153			
:]	58 80	72	90	108	126	144	162	180	198	216			
١	80	100	125	150	175	200	225	250	275	800			
١ ١	106	183	166	199	288	266	299	833	866	400			

As Second Movers or Line-shafting, Bearings 8 ft. apart. Formula : H.P. = $d^3R + 90$.

1 .4			N	umber	r of Revolutions per Minute.							
Diam. of Shaft.	100	125	150	175	200	225	250	275	800	825	850	
Ins.	H.P.	H.P.	H.P. 8.9	H.P. 10.4	H.P.	H.P. 18.4	H.P. 14.9	H.P. 16.4	H.P. 17.9	H.P. 19.4	H.P. 20.9	
13/4 12/6	7.8 8.9	9.1 11.1	10.9 18.3	12.7 15.5	14.5 17.7	16.8	18.2	20	21.8 26.6	28.6 28.8	25.4 81 87	
21/4 21/4 21/4 21/4 21/4	10.6 12.6 15	18.2 15.8 18	15.9 19 22	18.5 22 26	21.2 25 29 84	20 23.8 28 88 89	26.5 31 37	29.1 85 41	81.8 38 44	84.4 41 48	87 44 52	
217	17 23	21 29	26 84	80 40	46	89 52	58	47	52 69	56 75	60 81	
8	80 88	8? 47	45 57	52 66	60 76	67 85	75 95	64 82 104	90 114	97 123	105 133	
31/4 81/4 84/4	47 58 71	59 78 89	71 88 107	88 102 125	95 117 142	107 182 160	119 146 178	181 162 196	148 176 218	155 190 281	167 205 249	

FOR SIMPLY TRANSMITTING POWER. Formula: H.P. = $d^3R + 50$.

8.4			N	umber	of Rev	olutio	ns per	Minut	θ.				
Diar of Shal	100	125	150	175	200	233	267	300	883	367	400		
Ins.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.		
136	6.7	8.4		11.8	13.5		17.9	20.8		24 8	27.0		
157	8.6	10.7	12.8	15	17.1	80	22.8	25.8	28.6	81.5	84.J		
192	10.7	13.4	16	18.7	21.5	25	28	82	86	39	48		
11/6 15/6 15/4 13/8	18.2	16.5	19.7	23	26.4	81	35	39	44	48	59		
2′°	16	20	24	28	82 88	87	42	48	58	58	64		
	19	24	29	83	88	44	51	57	63	70	76		
21/4 21/4 21/4 21/4 21/4	22	28	84	89	45	52	60	68	75	88	90		
262	27	88	40	47	58	62	70	79	88	96	105		
212	81	89	47	54	62	78	88	93	104	114	125		
287	41	52	62	78	88	97	111	125	189	158	167		
8	54	67	81	94	108	126	144	162	180	198	216		
31/4	68	86	103	120	187	160	182	205	228	250	273		
312	85	107	128	150	171	200	228	257	285	813	342		

Horse-power Transmitted by Cold-rolled Iron Shafting at Different Speeds.

As Prime Mover or Head Shaft carrying Main Driving-pulley or Gear, well supported by Bearings. Formula: H.P. = $d^2R + 75$.

e_ 4			N	umber	of Re	volutio	ns per	Minu	te.		
Dia Sha	60	80	100	125	150	175	200	225	250	275	800
Ins.	H.P. 2.7	H.P. 8.6	H.P.	H.P.	H.P.	H.P	H.P.	HP.	H.P.	H.P.	H.P.
114	4.8	5.6 8.5	4.5 7.1 10.7	8.9	6.7 10.6	12.4	14.2	16	11 18	19	18 21
214 214 214	6.4 9 12	12 17	15	19	16 28 31	19 26 86	21 80 41	24 34 47	26 38 52	42	46 83
257	16 21	22	21 27 86	26 85 45	41 54	48 68	55 72	62 81	70	57 76 98	83 108
814 812 813	27 84	86 45	45 57	57 71	68 86	80 100	91 114	108 129	114 142	126 157	186
4	42 51	56 69	70 85	87 106	105 128	128	140 170	158 192	174 212	198 944	210 256
436	78	97	121	151	182	212	248	278	802	888	864

As Second Movers or Line-shafting, Bearings 8 PT. LAPART.

Formula: H.P. = $d^3R + 50$.

	Number of Revolutions per Minute.													
100	125	150	175	200	225	250	275	800	325	850				
H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.				
8.6	8.4 10.7	10.1 12.8	11.8 15	13.5 17.1	19.3	21.5	18.5 28.6	25.7	28.9	28.6 31				
10.7	18.4 16.5 20	16 19.7	18.7 28	21.5 26.4 83	24.2 29.6 36	82.9	29.5 36.2 44	82.1 89.5 48	84.8 48.8 52	89 46 56				
16 19 22	24 28	24 29 84	28 28 33 89	88 45	48 50	40 48 56 -	52 61	57 68	62 74	67 ·				
27 81	83 89	40 47	47 54	58 62	60 69	67 78	78 86	80 98	86 101	91 109				
41 54	52 67	62 81	78 94	88 108	93 121	104 184	114 148	125 162	185 175	145 189				
68 85	86 107	103 128	120 150	187 171	154 192	172 214	188 285	205 257	222 278	240 800				

FOR SIMPLY TRANSMITTING POWER AND SHORT COUNTERS. Formula: H.P. = $d^3R + 80$.

1	Number of Revolutions per Minute.													
100	125	150	175	200	238	267	800	888	867	400				
H.P.	H.P.	H.P.	H.P.	H.P.	HP.	H.P.	H.P.	H.P.	H.P.	H.P.				
6.5	8.1	9.7	11.3	18	15.2			21.7	23.9	26				
8.5	10.7		15	17	19.8			28.4	81	34				
11.2	14	16.8	19.6			30	88	87	41	45				
14.2	17.7			28.4		38	42	47	52	57				
18	22	27	81	85	41	47	58	59	65	71				
35	27	83	88	44	51	58	65	72	79	87				
26	88	40	46	53	62	71	80	88	97	106				
82 88	40	47	55	63	78	84	95	105	116	127				
88	47	57	66	76	89	101	114	127	139	152				
44	55	66 78	77	88	103	118	133	148	163	178				
52	65	78	91	104	121	138	155	172	190	207				
69	84	99	118	188	161	184	207	281	254	277				
90	112	185	157	180	210	240	270	800	330	860				

 SPEED OF SHAFTING.—Machine shops
 120 to 180

 Wood-working
 250 to 300

 Cotton and woollen mills
 300 to 400

re are in some factories lines 1000 ft. long, the power being applied at iddle.

How Shafts.—Let d be the diameter of a solid shaft, and d_1d_2 the al and internal diameters of a hollow shaft of the same material. the shafts will be of equal torsional strength when $d^3 = \frac{d_1^4 - d_2^4}{d_2^4}$

ich hollow shaft with internal diameter of 4 inches will weigh 168 less solid 10-inch shaft, but its strength will be only 2 56% less. If the hole nereased to 5 inches diameter the weight would be 25% less than that solid shaft, and the strength 6.2% less.

Ile for Laying Out Shafting.—The table on the opposite page the Stevens Indicator, April, 1892) is used by Wm. Sellers & Co. to see the laying out of shafting.

wood-cuts at the head of this table show the position of the hangers sition of couplings, either for the case of extension in both directions central head-shaft or extension in one direction from that head-shaft

ı			1		Double Conevise Coupling.	Diameter, inches.	8,4,5,7,0 ° ° ° ° ° ° ° ° ° ° ° ° ° ° ° ° ° ° °	90 1/16 10 1/18 119%	8447 C 00 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
4	5	-	>		Doub vise C	Length, inches.	225.925±	122 2 20	25 28 28 28 28 28 28 28 28 28 28 28 28 28
1		1			Bear- ox, ins.	Length of a ro ,gai	000011	12252	8 8888
SHAFT.		WFT.			à	13.	hand p line shaft ; this re of gives	other,	, J
SECOND BHAFT.	1	SECOND SHAFT.	1	į.	13%	as 's	the to f the stb B	Make bearings at equal distances from each other, when practicable, and always put two bearings on the first, which is the col-	# 25 Z
8	П	SEC.			1,12	1, 2,	aft in din did in director tree to lenge 1, B	rom rom vyc b	3 8 8 8
					63/8″	Fig	aft shared the rest of the centre of the cen	ke be nces f prac put t	2776 2896 38 38 38 38 38 38 38 38 38 38 38 38 38
		_		4	%	Jee B	ing from the first	Ma dista when ways the fi	
100				ğ	278,,,	Distance from Centre of Bearing to End of Shaft for Coupling. See B , Figs. 1, 2, and 3.	Use of TARRE—Look for size of first shaft in leth-han, ochumu under the head of Size of first shaft, and in the top line to be coupled to it. The intersection gives the size of the shaft to be coupled to it. The intersection gives the length L or distance from centre size equal to bearing, and in cases similar to Fig. 3, to the length L of the size shaft, thus, as in Fig. 1, $B + A + B = \log k$ if Fig. 3, $C + A + B = \log k$.		2222222 2422222
1	1	-	1	BIL	ì	light	of Six Seconds of Control of the Con	8	18322288
END3.	-1	END.	oi.	Table for Laying Out Sharting.	41/8") is	tr. The A-	ଛ	2328888 2328888
Вотн	Fig. 1.	T ONE	Fig. 2.	0	1,4	laft f	ABLE. rked to i d to i e leng of the	8191	888 <u>8</u> 888
OUPLED	1	UPLED		, L	378	of Si	n, und le, ma le, ma to th fo th g, and	\$5.50 \$5.50	3 8 8 8 8 8
FIRST SHAFT COUPLED BOTH ENDS.		FIRST SHAFT COUPLED AT ONE END		La	3¼" 34 g "	End	Use thum of tab of be odded searin	2022	្តី 2 នងនឹង
FIRST		RST SH		for	à.	ag to		12,67 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	20 22 83 20 22 83 20 22 83
-		-	4	able	7,762	Searth	41	15 15 16 16 17 18 18 18 18 18 18 18 18 18 18 18 18 18	100 H
4	7	-11	7	Ħ	374" 2348" 284"	oo	8185. 200.	42585	in the standard
					, X	Mentr	61 50 E	4422	In coupling sharks of different sizes, estimate of different sizes, estimate of different sizes, estimate or small coupling, or use a coupling to suit the larger shaft, with one core loved for the smaller nominal
1	٢				- &	Į į		25 4 15 26 4 15	reduction of the control of the cont
1	U	1	L		19%"	00 E	20011100 20011100 20011100		In coupling shafts of differences and use a coupling to the large shaft in dismeter, and use a small coupling or use a coupling to suif the larger shaft, with one core bored for the smaller nominal
SECOND SHAFT.	1	-	X	Ī	13/8/1	istar			Libe lates
SEGO		-11	4	1		!	8 0 5 N		Page 20 a L
A.	1		1		Nominal Size of 2d Shaft.	Nominal Size of 1st Shaft ins.	72° 22°		
1			Fig. 3,		- S	Length of Collared End for Fast Coll., ins.	L-17 L 26	8 15/16 10 16/16	######################################

PULLEYS.

roportions of Pulleys. (See also Fly-wheels, pages 820 to 823.)—n= number of arms, D= diameter of pulley, S= thickness of belt, t= kness of rim at edge, T= thickness in middle, B= width of rim, $\beta=$ th of belt, h= breadth of arm at hub, $h_1=$ breadth of arm at rim, e= kness of arm at tub $e_1=$ thickness of arm at rim, c= amount of crown-dimensions in inches.

```
Unwin.
                                                                             Reuleaux.
                                                                          9/8$ to 5/4$ (thick, of rim.)
 width of rim.....
                                                 9/8 (\beta + 0.4)
 thickness at edge of rim ......
                                                 0.78 + .005D
                                                                             1/5h to \frac{1}{4}h
              " middle of rim....
                                          For single
                                          belts = .68371
 breadth of arm at hub.
                                          For double belts = .798
                     " rim.....
 thickness of arm at hub. ....
                            rim.....
number of arms, for a
                                                          150
 single set.
                                       f not less than 2.58, B for sin.-arm pulleys. is often %B. 2B "double-arm"
length of hub .....
thickness of metal in hub.....
                                                                                h to 34h
                                                     1/24B
crowning of pulley.....
e number of arms is really arbitrary, and may be altered if necessary.
lleys with two or three sets of arms may be considered as two or three
rate pulleys combined in one, except that the proportions of the arms ld be 0.8 or 0.7 time that of single-arm pulleys. (Reuleaux.)

AMPLE.—Dimensions of a pulley 60" diam., 16" face, for double belt 1/4"
olution by ....
Juwin.....
euleaux .....
                             5.0 4.0 2.5
following proportions are given in an article in the Amer. Machinist,
ority not stated:
0.0625D + .5 in., h_1 = 0.04D + 8125 in., e = 0.025D + .2 in., e_1 = 0.016D + .2
se give for the above example: h = 4.25 in., h_1 = 2.71 in., e = 1.7 in.
1.09 in. The section of the arms in all cases is taken as elliptical.
following solution for breadth of arm is proposed by the author:
ne a belt pull of 46 lbs. per inch of width of a single belt, that the
strain is taken in equal proportions on one half of the arms, and that
m is a beam loaded at one end and fixed at the other. We have the
ila for a beam of elliptical section fP = .0983 \frac{Rbd^2}{r}
                                                                    \frac{\sigma a^{-}}{l}, in which P = the
R = the modulus of rupture of the cast iron, b = breadth, d = depth,
= length of the beam, and f = factor of safety. Assume a modulus oture of 36,000 lbs., a factor of safety of 10, and an additional allowfor safety in taking l = \frac{1}{2} the diameter of the pulley instead of \frac{1}{2}
ie radius of the hub.
e d = h, the breadth of the arm at the hub, and b = c = 0.4h, the
         We then have fP = 10 \times \frac{45B}{n+2} = \frac{900B}{n} = \frac{3535 \times 0.4h^3}{14D},
                           \frac{BD}{m}, which is practically the same as the value
```

ed by Unwin from a different set of assumptions.

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Convexity of Pulleys.—Authorities differ. Morin gives a rise equal to 1/10 of the face; Molesworth, 1/24; others from ½ to 1/96. Scott A. Smith says the crown should not be over ½ inch for a 24-inch face. Pulleys for shifting belts should be "straight," that is, without crowning.

CONE OR STEP PULLEYS.

To find the diameters for the several steps of a pair of cone-pulleys:

1. Crossed Belts.—Let D and d be the diameters of two pulleys connected by a crossed belt, L = the distance between their centres, and β = the angle either half of the belt makes with a line joining the centres of the

pulleys: then total length of belt =
$$(D+d)^{\pi}_{2}+(D+d)^{\pi\beta}_{180}+2L\cos\beta$$
.

$$\beta$$
 = angle whose sine is $\frac{D+d}{2L}$. $\cos \beta = \sqrt{L^2 - \left(\frac{D+d}{2}\right)}$. The length of the helt is constant, when $D+d$ is constant; that is, in a rair of step-

the belt is constant when D+d is constant; that is, in a rair of step-pulleys the belt tension will be uniform when the sum of the diameters of each opposite pair of steps is constant. Crossed belts are seldom used for cone-pulleys, on account of the friction between the rubbing parts of the

belt. To design a pair of tapering speed-cones, so that the belt may fit equally tight in all positions: When the belt is crossed, use a pair of equal and similar cones tapering opposite ways. 2. **Open Helts.**—When the belt is uncrossed, use a pair of equal and similar conoids tapering opposite ways, and bulging in the middle, according to the following formula: Let L denote the distance between the axes of the conoids; R the radius of the larger end of each; r the radius of the smaller end; then the radius in the middle, r_0 , is found as follows:

$$r_0 = \frac{R+r}{2} + \frac{(R-r)^2}{6.28L}$$
. (Rankine.)

If D_0 = the diameter of equal steps of a pair of cone-pulleys, D and d = the diameters of unequal opposite steps, and L = distance between the axes, $D_0 = \frac{D+d}{2} + \frac{(D-d)^2}{12.566L}$.

If a series of differences of radii of the steps, R-r, be assumed, then for each pair of steps $\frac{R+r}{2} = r_0 - \frac{(R-r)^3}{6.28L}$, and the radii of each may be computed from their half sum and half difference, as follows:

$$R = \frac{R+r}{2} + \frac{R-r}{2}; \quad r = \frac{R+r}{2} - \frac{R-r}{2}.$$

A. J. Frith (Trans. A. S. M. E., x. 298) shows the following application of Rankine's method: If we had a set of cones to design, the extreme diameters of which, including thickness of belt, were 40" and 10", and the ratio desired 4, 3, 2, and 1, we would make a table as follows, L being 100":

Trial Sum of	Ratio.	Trial Dia	ameters.	Values of $(D-d)^2$	Amount to be	Corrected Values.			
D+d.	iestio.	D	đ	12.58L	Added.	D	đ		
50 50	4 8	40 87.5	10 12.5	.7165 .4975	.0000 .2190	40 87.7190	10 12.7190		
50 50	2	83.838 25	16.666 25	.0000	.4958 .7165	88.8286 25.7165	17.1619 25.7165		

The above formulæ are approximate, and they do not give satisfactory results when the difference of diameters of opposite steps is large and when the axes of the pulleys are near together, giving a large belt-angle. The following more accurate solution of the problem is given by C. A. Smith

following more accurate solution of the problem is given by C. A. Smith (Trans. A. S. M. E., x. 299) (Fig 152):

Lay off the centre distance C or EF, and draw the circles D_1 and d_1 equal to the first pair of pulleys, which are always previously determined by known conditions. Draw HI tangent to the circles D_1 and d_1 . From B midway between E and F, erect the perpendicular BG, making the length

.314C. With G as a centre, draw a circle tangent to HI. Generally ircle will be outside of the belt-line, as in the cut, but when C is short he first pulleys D_1 and d_1 are large, it will fall on the inside of the belt-The belt-line of any other pair of pulleys must be tangent to the cir; hence any line, as JK or LM, drawn tangent to the circle G, will give

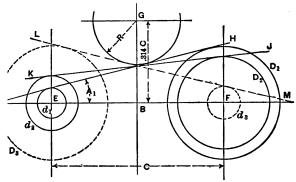


Fig. 152.

imeters D_2 , d_2 or D_3 , d_3 of the pulleys drawn tangent to these lines he centres E and F. The centres E and E. as above method is to be used when the belt-angle A does not exceed when it is between 18° and 30° a slight modification is made. In that 1 addition to the point G, locate another point m on the line BG. 28° CB. Draw a tangent line to the circle G, making an angle of 18° to the centres EF, and from the point m draw an arc tangent to this tan1e. All belt-lines with angles greater than 1)° are tangent to this arc,
lowing is the summary of Mr. Smith's mathematical method:

angle in degrees between the centre line and the belt of any pair of

and 30°

an angle depending on the velocity ratio;

the centre distance of the two pulleys; diameters of the larger and smaller of the pair of pulleys;

an angle depending on Bo;

the length of the belt when drawn tight around the pulleys; D + d, or the velocity ratio (larger divided by smaller).

(1) Sin
$$A = \frac{D-d}{2C}$$
; (2) $\tan B^{\circ} = \frac{2a(r-1)}{r+1}$;

(3) Sin
$$E^{\circ} = \sin B^{\circ} \left(\cos A - \frac{D+d}{4aC}\right);$$

 $B^{\circ} - E^{\circ}$ when $\sin E^{\circ}$ is positive; $= B^{\circ} + E^{\circ}$ when $\sin E^{\circ}$ is negative; $\frac{2C \sin A}{r-1}$; = .3183(L-2C) when A=0 and r=1;

 $2C\cos A + .01745d[180 + (r-1)(90 + A)].$

ion (1) is used only once for any pair of cones to obtain the constant y the aid of tables of sines and cosines, for use in equation (8).

BELTING.

Theory of Belts and Bands.—A pulley is driven by a belt by means of the friction between the surfaces in contact. Let T_1 be the tension on the driving side of the belt, T_2 the tension on the loose side; then $S_1 = T_1$ on the driving side of the beh. I_2 the tension of the roose side; then $S_1 = I_2$, at the total friction between the band and the pulley, which is equal to the tractive or driving force. Let f = the coefficient of friction, θ the ratio of the length of the arc of contact to the length of the ardius, a = the angle of the arc of contact in degrees, e = the base of the Naperian logarithms = 2.71823, m = the modulus of the common logarithms = 0.434235. The following formulæ are derived by calculus (Rankine's Mach'y & Millwork, p. 351; Carpenter's Exper. Eng'g, p. 173):

$$\begin{split} &\frac{T_1}{T_2} = e^{f\theta}; \ T_2 = \frac{T_1}{e^{f\theta}}; \ T_1 - T_2 = T_1 - \frac{T_1}{e^{f\theta}} = T_1(1 - e^{-f\theta}). \\ &T_1 - T_2 = T_1(1 - e^{-f\theta}) = T_1(1 - 10^{-f\theta m}) = T_1(1 - 10^{-0.00758/a}); \\ &\frac{T_1}{T_2} = 10^{.00758/a}; \ T_1 = T_2 \times 10^{.00758/a}; \ T_2 = \frac{T_1}{10^{.00758/a}}. \end{split}$$

If the arc of contact between the band and the pulley expressed in turns and fractions of a turn = n, $\theta = 2\pi n$; $e^{f\theta} = 10^{3.7388/n}$; that is, $e^{f\theta}$ is the natural number corresponding to the common logarithm 2.7288/n. The value of the coefficient of friction f depends on the state and material of the rubbing surfaces. For leather belts on iron pulleys, Morin found f = .56 when dry, .36 when wet, .23 when greasy, and .15 when oily. In calculating the proper mean tension for a belt, the smallest value, f = .15, is to be taken if there is a probability of the belt becoming wet with oil. The experiments of Henry R. Towne and Robert Briggs, however (Jour. Frank. Inst., 1868), show that such a state of lubrication is not of ordinary occurrence; and that in designing machinery we may in most cases safely take f = 0.42. Repleaux takes f = 0.25. The following table shows the values of the coefficient 2.7288/, by which n is multiplied in the last equation, corresponding to different values of f; also the corresponding values of various ratios among the forces, when the arc of contact is half a circumference: f = 0.15 0.25 0.42 0.56

$$f = 0.15 \quad 0.25 \quad 0.42 \quad 0.56$$

$$2.7286 f = 0.41 \quad 0.68 \quad 1.15 \quad 1.53$$
Let $\theta = \pi$ and $n = \frac{1}{2}$, then
$$T_1 + T_2 = 1.608 \quad 2.188 \quad 3.768 \quad 5.821$$

$$T_1 + S = 2.66 \quad 1.84 \quad 1.36 \quad 1.21$$

$$T_1 + T_2 + 2S = 2.16 \quad 1.34 \quad 0.86 \quad 0.71$$

In ordinary practice it is usual to assume $T_2 = S$; $T_1 = 2S$; $T_1 + T_2 + 2S = 1.5$. This corresponds to f = 0.22 nearly.

For a wire rope on cast iron f may be taken as 0.15 nearly; and if the groove of the pulley is bottomed with gutta-percha, 0.25. (Rankine.)

Centrifugal Tension of Belts.—When a belt or band runs at the belt of the produces a tension in addition to that a sixther than the second runs at the second

Centrifugal Tension of Heits.—When a belt or band runs at a high velocity, centrifugal force produces a tension in addition to that existing when the belt is at rest or moving at a low velocity. This centrifugal tension diminishes the effective driving force.

Rankine says: If an endless band, of any figure whatsoever, runs at a given speed, the centrifugal force produces a uniform tension at each cross-section of the band, equal to the weight of a piece of the band whose length is twice the height from which a heavy body must fall, in order to acquire the relegity of the band. (See Cooper on Belting, p. 101). the velocity of the band. (See Cooper on Belting, p. 101.)

If $T_0 = \text{centrifugal tension}$;

V = velocity in feet per second;

g = acceleration due to gravity = 82.2; W = weight of a piece of the belt 1 ft. long and 1 sq. in. sectional area,—

Leather weighing 56 lbs. per cubic foot gives W = 56 + 144 = .888.

$$T_0 = \frac{WV^2}{g} = \frac{.888V^4}{$9.9} = .018V^2,$$

elting Practice. Handy Formulæ for Belting. - Since ne practical application of the above formulæ the value of the coefficient iction must be assumed, its actual value varying within wide limits (15% 15%), and since the values of T₁ and T₂ also are fixed arbitrarily, it is cusary in practice to substitute for these theoretical formulæ more simple sirical formulæ and rules, some of which are given below.

** d = diam. of pulley in inches; **d = circumference; ** V = velocity of belt in ft. per second; **v = vel. in ft. per minute;

we vertex of each it. For section, v = v of m in Ferminia a = angle of the arc of contact; L = length of arc of contact in feet $= \pi da + (12 \times 860)$; F = t ractive force per square inch of sectional area of belt; w = w width in inches; t = t incheses; S = t ractive force per inch of width = F + t; M = t revs. per minute; rps. = t revs. per second = t rpm. = t 60.

$$V = \frac{\pi d}{12} \times \text{rps.} = \frac{\pi d}{12} \times \frac{\text{rpm.}}{60} = .004368d \times \text{rpm.} = \frac{d \times \text{rpm.}}{$239.3};$$

$$v = \frac{\pi d}{12} \times \text{rpm.}; = .2618d \times \text{rpm.}$$

se-power, H.P. =
$$\frac{Svvv}{82000} = \frac{SVvv}{550} = \frac{Svd \times rpm}{126050} = .000007988Svd \times rpm$$
.

F = working tension per square inch = 275 lbs., and t = 7/82 inch, S =s. nearly, then

H.P. =
$$\frac{vw}{550}$$
 = .109 Vw = .000476 $wd \times \text{rpm.}$ = $\frac{wd \times \text{rpm.}}{2101}$. (1)

F = 180 lbs. per square inch, and t = 1/6 inch, S = 30 lbs., then

H.P. =
$$\frac{vw}{1100}$$
 = .055 Vw = .000238 $wd \times \text{rpm.}$ = $\frac{wd \times \text{rpm.}}{4202}$. . (2)

the working strain is 60 lbs, per inch of width, a belt 1 inch wide travel-550 ft. per minute will transmit 1 horse-power. If the working strain is 0s. per inch of width, a belt 1 inch wide, travelling 1100 ft. per minute, transmit 1 horse-power. Numerous rules are given by different writers elting which vary between these extremes. A rule commonly used is: h wide travelling 1000 ft. per min. = I.H.P.

H.P. =
$$\frac{vw}{1000}$$
 = .06 Vw = .000262 $wd \times \text{rpm.}$ = $\frac{wd \times \text{rpm.}}{8820}$. . . (8)

corresponds to a working strain of 33 lbs. per inch of width, my writers give as safe practice for single belts in good condition a sing tension of 45 lbs. per inch of width. This gives

H.P. =
$$\frac{wv}{733}$$
 = .0818 Pw = .000357 wd × rpm, = $\frac{vd$ × rpm. (4)

r double belts of average thickness, some writers say that the transing efficiency is to that of single belts as 10 to 7, which would give

of double belts =
$$\frac{wv}{518}$$
 = .1169 Vw = .00051 $wd \times \text{rpm.}$ = $\frac{wd \times \text{rpm.}}{1960}$. (5)

r authorities, however, make the transmitting-power of double belts a that of single belts, on the assumption that the thickness of a doubleis twice that of a single belt.

less for horse-power of belts are sometimes based on the number of re feet of surface of the belt which pass over the pulley in a minute, it. per min. = 100 + 12. The above formulæ translated into this form

The above formulæ are all based on the supposition that the arc of contact is 180°. For other arcs, the transmitting power is approximately proportional to the ratio of the degrees of arc to 180°. Some rules base the horse-power on the length of the arc of contact in feet. Since $L = \frac{\pi da}{12 \times 360}$ and H.P. $= \frac{Srw}{83000} = \frac{Sw}{33000} \times \frac{\pi d}{12} \times \text{rpm.} \times \frac{a}{180}$. we

obtain by substitution H.P. = $\frac{500}{16500} \times L \times \text{rpm.}$, and the five formulæ then take the following form for the several values of S:

H.P =
$$\frac{wL \times \text{rpm.}}{275}$$
 (1); $\frac{wL \times \text{rpm.}}{550}$ (2); $\frac{wL \times \text{rpm.}}{500}$ (3); $\frac{wL \times \text{rpm.}}{367}$ (4).
H.F. (double belt) = $\frac{wL \times \text{rpm.}}{987}$ (5).

None of the handy formulæ take into consideration the centrifugal ten sion of belts at high velocities. When the velocity is over 3000 ft. per min ute the effect of this tension becomes appreciable, and it should be taken account of as in Mr. Nagle's formula, which is given below.

Horse-power of a Leather Belt One Inch wide. (NAGLE.)

Formula: H.P. = $CVtw(S - .012V^2) + 550$,

For
$$f = .40$$
, $a = 180^{\circ}$, $C = .715$, $w = 1$.

	L	CED	BEL	Ts, S	= 2	75.			1	RIVE	TED I	BELTS,	S =	400.	
ty in sec.		Thiel	ness	s in i	nche	S = 1	t.	r sec.		Th	ickne	ss in i	inche	s = t.	
Velocity ft. per 8		1/6 .167	3/16 .187	7/82	1/4 ,250	5/16 .312	1/3	Velocity ft. per s	7/32 219	1/4 .250	5/16	16.15.47	8/8 .375	7/16 .437	1/2
10 15 20 25 30 35 40 45 50 65 70 75 80 85 90	.51 .75 1.00 1.23 1.47 1.69 1.90 2.27 2.44 2.58 2.51 2.89 2.94 2.97	.59 .88 1.17 1.43 1.72 1.97 2.22 2.45 2.65 2.84 8.01 3.16 3.27 3.37 3.43 3.47	.63 1.00 1.82 1.61 1.93 2.22 2.49 2.75 2.75 2.98 3.38 3.55 8.68 3.79 3.86 3.90		.84 1.82 1.75 2.16 2.58 2.96 3.32 3.67 3.98 4.26 4.51 4.74 4.91 5.05 5.15 5.20	1.05 1.66 2.19 2.69 3.22 3.70 4.15 4.58 4.58 4.57 5.32 5.32 6.14 6.31 6.44 6.50	1.18 1.77 2.31 2.86 3.44 3.94 4.44 4.89 5.30 5.69 6.02 6.54 6.73 6.86	15 20 25 30 35 40 45 50 55 60 65 70 75 80 85 90	2.24 2.79 3.31 3.82 4.33 4.85 5.26 5.68 6.09 6.45 7.09 7.36 7.74	4 87 4 95 5 49 6 01 6 50 6 56 7 37 7 75 8 11 8 41 8 66 8 85	3. 98 4. 74 5. 46 6. 19 6. 86 7. 51 8. 12 8. 70 9. 22 9. 69 10. 18 10. 51 10. 82 11. 06	3.42 4.25 5.05 5.83 6.60 7.32 8.02 8.66 9.28 9.83 10.33 10.84 11.21 11.55 11.80	3.85 4.78 5.67 6.56 7.49 9.02 9.74 10.43 11.06 11.62 12.16 12.61 13.00 13.27	5.57 6.62 7.65 8.66	5.13 6.37 7.58 8.75 9.90 10.98 12.03 13.00 14.75 15.50 16.81 17.82 17.69

In the above table the angle of subtension, a, is taken at 180°.

A. F. Nagle's Formula (Trans. A. S. M. E., vol. ii., 1881, p. 91 Tables published in 1882.)

H.P. =
$$CVtw(\frac{S - .012V^2}{550})$$
;

$$C=1-10^{-.00758fa}$$
;

Taking S at 275 lbs, per sq. in. for laced belts and 400 lbs, per sq. in. for pped and riveted belts, the formula becomes

H.P. = $CVtw(.50 - .0000218V^2)$ for laced belts; H.P. = $CVtw(.727 - .0000218V^2)$ for riveted belts.

VALUES OF $(? = 1 - 10^{-.00758 fo}]$. (NAGLE.)

friction.	Degrees of contact = a.										
fre	90°	100°	1100	120°	1800	1400	1500	1600	170°	180•	200*
15	210	.230	.250	.270	.288	.307	.825	.342	.859 .448	.376	.408
25	.825 .876	.854	.881 .438	.407	.432	.457 .520	.480 .544	.508	.524 .590	.544	.582
85 40	.423	.457 .502	.489	.520	.548	.624	.600	.624 .678	.646	.667	.705
45 55 60	.507 .578 .610	.544 .617 .649	.579 .652 .684	.610 .684 .715	.640 .718 .744	.667 .789 .769	.692 .763	.715 .785 .818	.787 .805 .832	.757 .822 .848	.792 .853 .877
00	.792	.825	.853	.877	.897	.918	.927	.937	.947	.956	.969

The following table gives a comparison of the formulæ already given for case of a belt one inch wide, with arc of contact 180°.

orse-power of a Belt One Inch wide, Arc of Contact 180°. Comparison of Different Formulæ.

per sec.	ity in min.	ft. of 9. min.	Form, 1 H.P. =	Form. 2 H.P. =	Form. 8 H.P. =	Form. 4 H.P. =	Form. 5 dbl.belt H.P. =	Nagle's Form. 7/32''single belt	
rt. pe	Velocity in ft. p. min.	Sq. f Belt p	<u>wv</u> .	1100	1000	738	100 518	Laced.	Riveted
?	600 1200	50 100	1.09 2.18	.55 1.09	.60 1.20	.82 1.64	1.17 2.84	.78 1.54	1.14 2.24
j	1800	150	8.27	1.64	1.80	2.46	8.51	2.25	8.81
)	2400	200	4.36	2.18	2.40	8.27	4.68	2.90	4.88
)	8000	250	5.45	2.78	8.00	4.09	5.85	8.48	5.26
) 1	3600	300	6.55	8.27	8.60	4.91	7.02	8.95	6.09
)	4200	350	7.63	8.82	4.20	5.78	8.19	4.29	6.78
)	4800	400	8.78	4.86	4.80	6.55	9.36	4.50	7.86
)	5400	450	9.82	4.91	5.40	7.87	10.58	4.55	7.74
)	6000	500	10.91	5.45	6.00	8.18	11.70	4.41	7.96
)	6600	550				l	[4.05	7.97
)	7200	600	l	l		J <u></u>		3 49	7.75

Vidth of Belt for a Given Horse-power.—The width of belthined for any given horse-power may be obtained by transposing the for less for horse-power so as to give the value of w. Thus:

m formula (1),
$$w = \frac{550 \text{ H.P.}}{v} = \frac{9.17 \text{ H.P.}}{V} = \frac{2101 \text{ H.P.}}{d \times \text{rpm.}} = \frac{275 \text{ H.P.}}{L \times \text{rpm.}}$$
m formula (3), $w = \frac{1100 \text{ H.P.}}{v} = \frac{18.83 \text{ H.P.}}{V} = \frac{4202 \text{ H.P.}}{d \times \text{rpm.}} = \frac{530 \text{ H.P.}}{L \times \text{rpm.}}$
m formula (3), $w = \frac{1000 \text{ H.P.}}{v} = \frac{16.67 \text{ H.P.}}{V} = \frac{8820 \text{ H.P.}}{d \times \text{rpm.}} = \frac{500 \text{ H.P.}}{L \times \text{rpm.}}$
m formula (4), $w = \frac{738 \text{ H.P.}}{v} = \frac{12.22 \text{ H.P.}}{V} = \frac{2800 \text{ H.P.}}{d \times \text{rpm.}} = \frac{360 \text{ H.P.}}{L \times \text{rpm.}}$
m formula (5), $w = \frac{513 \text{ H.P.}}{v} = \frac{8.56 \text{ H.P.}}{V} = \frac{1960 \text{ H.P.}}{d \times \text{rpm.}} = \frac{257 \text{ H.P.}}{L \times \text{rpm.}}$
For double belts.

Many authorities use formula (1) for double belts and formula (2) or (3) for single belts.

To obtain the width by Nagle's formula, $w = \frac{550 \text{ H.P.}}{CVt(S - .012V^2)}$, or divide the given horse power by the figure in the table corresponding to the given

thickness of belt and velocity in feet per second.

The formula to be used in any particular case is largely a matter of judgment. A single belt proportioned according to formula (1), if tightly stretched, and if the surface is in good condition, will transmit the horse-power calculated by the formula, but one so proportioned is objectionable, first because it requires so great an initial tension that it is apt to stretch, slip, and require frequent restretching and relacing; and second, because this tension will cause an undue pressure on the pulley-shaft, and therefore an undue loss of power by friction. To avoid these difficulties, formula (2), (3), or (4,) or Mr. Nagle's table, should be used; the latter especially in cases in which the velocity exceeds 4000 ft. per min.

Taylor's Rules for Belting.—F. W. Taylor (Trans. A. S. M. E., 2014 describes a nine vear's experiment, on belting in a machine-shop.

Taylor's Rules for Belting.—F. W. Taylor (Trans. A. S. M. E., xv. 204) describes a nine years' experiment on beiting in a machine-shop, giving results of tests of 42 belts running night and day. Some of these belts were run on cone pulleys and others on shifting, or fast-and-loose, pulleys. The average net working load on the shifting belts was only 4/10 of that of the cone belts.

The shifting belts varied in dimensions from 39 ft. 7 in. long, 3.5 in. wide, .25 in. thick, to 51 ft. 5 in. long, 6.5 in. wide, .37 in. thick. The cone belts varied in dimensions from 24 ft. 7 in. long, 2 in. wide, .25 in. thick, to 31 ft. 10 in. long, 4 in. wide, .37 in. thick.

Belt-clamps were used having spring-balances between the two pairs of clamps, so that the exact tension to which the belt was subjected was accurately weighed when the belt was first put on, and each time it was tightened

tightened.

The tension under which each belt was spliced was carefully figured so as to place it under an initial strain—while the belt was at rest immediately after tightening—of 71 lbs. per inch of width of double belts. This is equivalent, in the case of

From the nine years' experiment Mr. Taylor draws a number of conclusions, some of which are given in an abridged form below.

In using belting so as to obtain the greatest economy and the most satisfactory results, the following rules should be observed:

	Oak Tanned and Fulled Leather Belts.	Other Types of Leather Belts and 6- to 7-ply Rubber Belts.
A double belt, having an arc of contact of 180°, will give an effective pull on the face of a pulley per inch of width of belt of Or, a different form of same rule: The number of sq. ft. of double Belt passing	85 lbs.	80 lbs.
around a pulley per minute required to transmit one horse power is	80 sq. ft.	90 sq. ft.
per minute required to transmit one horse- power is	950 ft.	1100 ft.
Or: A double belt 6 in. wide, running 4000 to 5000 ft. per min., will transmit	80 H.P.	25 H.P.

The terms "initial tension," "effective pull," etc., are thus explained by Mr. Taylor: When pulleys upon which belts are tightened are at rest, bots strands of the belt (the upper and lower) are under the same stress per in of width. By "tension," "initial tension," or "tension while at rest, " we

n the stress per in. of width, or sq. in. of section, to which one of the nds of the belt is tightened, when at rest. After the belts are in motion transmitting power, the stress on the slack side, or strand, of the belt mes less, while that on the tight side—or the side which does the pull-becomes greater than when the belt was at rest. By the term "tetal "we mean the total stress per in. of width, or sq. in. of section, on the

t side of belt while in motion.

ie difference between the stress on the tight side of the belt and its slack while in motion, represents the effective force or pull which is transed from one pulley to another. By the terms "working load," "net king load," or "effective pull," we mean the difference in the tension he tight and slack sides of the belt per in, of width, or sq. in. section, e in motion, or the net effective force that is transmitted from one pul-

o another per in. of width or sq. in. of section, le discovery of Messrs. Lewis and Bancroft (Trans. A. S. M. E., vil. 749) the "sum of the tension on both sides of the belt does not remain tant," upsets all previous theoretical belting formulæ.

ie belt speed for maximum economy should be from 4000 to 4500 ft. per

ie best distance from centre to centre of shafts is from 20 to 25 ft. ler pulleys work most satisfactorily when located on the slack side of beit about one quarter way from the driving-pulley. Its are more durable and work more satisfactorily made narrow and

k, rather than wide and thin.

is safe and advisable to use: a double belt on a pulley 12 in. diameter or er; a triple belt on a pulley 20 in. diameter or larger; a quadruple belt pulley 80 in. diameter or larger.

belts forease in width they should also be made thicker.

e ends of the belt should be fastened together by splicing and cementinstead of lacing, wiring, or using hooks or clamps of any kind.

V-splice should be used on triple and quadruple belts and when idlers

ised. Stepped splice, coated with rubber and vulcanized in place, is best ubber belts,

r double belting the rule works well of making the splice for all belts of 10 in. wide the splice should be ame width as the belt, 18 in. being the greatest length of splice required ouble belting.

uble leather belts will last well when repeatedly tightened under a n (when at rest) of 71 lbs. per in. of width, or 240 lbs. per sq. in. section.

will not maintain this tension for any length of time, however, it-clamps having spring-balances between the two pairs of clamps ld be used for weighing the tension of the belt accurately each time it

htened.

a stretch, durability, cost of maintenance, etc., of belts proportioned ecording to the ordinary rules of a total load of 111 lbs. per inch of a corresponding to an effective pull of 65 lbs. per inch of width, and (B) ding to a more economical rule of a total load of 54 lbs., corresponding effective pull of 26 lbs. per inch of width, are found to be as follows: end it is impracticable to accurately weigh the tension of a belt in tight; it it is safe to shorten a double belt one half inch for every 10 ft. of

h for (A) and one inch for every 10 ft. for (B), if it requires tightening, ible leather belts, when treated with great care and run night and day iderate speed, should last for 7 years (A); 18 years (B). Seest of all labor and materials used in the maintenance and repairs of

le belts, added to the cost of renewals as they give out, through a term are, will amount on an average per year to 37% of the original cost of elts (A); 14% or less (B).

figuring the total expense of belting, and the manufacturing cost

eable to this account, by far the largest item is the time lost on the

ines while belts are being relaced and repaired.

total stretch of leather belting exceeds % of the original length.

stretch during the first six months of the life of belts is 36% of their
stretch (A); 15% (B).

ouble belt will stretch 4/100 of 1% of its length before requiring to be

med (A); 81/100 of 1% (B).
most important consideration in making up tables and rules for the nd care of belting is how to secure the minimum of interruptions to facture from this source. The average double belt (A), when running night and day in a machine-shop, will cause at least 26 interruptions to manufacture during its life, or interruptions per year, but with (B) interruptions to manufacture will not average oftener for each belt than one in sixteen months.

The oak-tanned and fulled belts showed themselves to be superior in all respects except the coefficient of friction to either the oak-tanned not fulled.

the semi-raw-hide, or raw-hide with tanned face.

Belts of any width can be successfully shifted backward and forward on tight and loose pulleys. Belts running between 5000 and 6000 ft. per min, and driving 300 H.P. are now being daily shifted on tight and loose pulleys, to throw lines of shafting in and out of use.

The best form of belt-shifter for wide belts is a pair of rollers twice the width of belt, either of which can be pressed onto the flat surface of the belt on its slack side close to the driven pulley, the axis of the roller making an angle of 75° with the centre line of the belt.

Remarks on Mr. Taylor's Rules. (Trans. A. S. M. E., xv., 242.)

—The most notable feature in Mr. Taylor's paper is the great difference between his rules for proper proportioning of belts and those given by earlier writers. A very commonly used rule is, one horse-power may be transmitted by a single belt 1 in. wide running x ft. per min., substituting for x various values, according to the ideas of different engineers, ranging usually from 550 to 1100.

The practical mechanic of the old school is apt to swear by the figure 600 as being thoroughly reliable, while the modern engineer is more apt to use the figure 1000. Mr. Taylor, however, instead of using a figure from 550 to 1100 for a single belt, uses 950 to 1100 for double belts. If we assume that a double belt is twice as strong, or will carry twice as much power, as a single belt, then he uses a figure at least twice as large as that used in modern practice, and would make the cost of belting for a given shop twice as large as if the belting were proportioned according to the most liberal of

the customary rules.

This great difference is to some extent explained by the fact that the problem which Mr. Taylor undertakes to solve is quite a different one from problem which mr. I sylor undertakes to solve is quite a different one from that which is solved by the ordinary rules with their variations. The problem of the latter generally is, "How wide a belt must be used, or how narrow a belt may be used, to transmit a given horse-power?" Mr. Taylor's problem is: "How wide a belt must be used so that a given horse-power may be transmitted with the minimum cost for belt repairs, the longest life to the belt, and the smallest loss and inconvenience from stopping the machine while the belt is being tightened or repaired?"

The difference between the old practical mechanic's rule of a 1-in.-wide single belt, 600 ft. per min., transmits one horse-power, and the rule com-monly used by engineers, in which 1000 is substituted for 600, is due to the belief of the engineers, not that a horse-power could not be transmitted by the belt proportioned by the older rule, but that such a proportion involved undue strain from overtightening to prevent slipping, which strain entailed too much journal friction, necessitated frequent tightening, and decreased

the length of the life of the belt.

Mr. Taylor's rule substituting 1100 ft. per min. and doubling the belt is a further step, and a long one, in the same direction. Whether it will be taken in any case by engineers will depend upon whether they appreciate the extent of the losses due to slippage of belts slackened by use under overstrain, and the loss of time in tightening and repairing belts, to such a degree as to induce them to allow the first cost of the belts to be doubled in order to avoid these losses.

It should be noted that Mr. Taylor's experiments were made on rather narrow belts, used for transmitting power from shafting to machinery, and his conclusions may not be applicable to heavy and wide belts, such as engine fly-wheel belts.

MISCELLANEOUS NOTES ON BELTING.

Formulæ are useful for proportioning belts and pulleys, but they furnish no means of estimating how much power a particular belt may be transno means or estimating flow mucin power a particular belt may be transmitting at any given time, any more than the size of the engine is a measure of the load it is actually drawing, or the known strength of a horse is a measure of the load on the wagon. The only reliable means of determining the power actually transmitted is some form of dynamometer. (See Trans. 4. S. M. E., vol. xii. p. 707.)

we increase the thickness, the power transmitted ought to increase in we increase the thickness, the power transmitted ought to increase in portion; and for double belts we should have half the width required for ngle belt under the same conditions. With large pulleys and moderate ocities of belt it is probable that this holds good. With small pulleys rever, when a double belt is used, there is not such perfect contact ween the pulley-face and the belt, due to the rigidity of the latter, and re pliable belt is used. The centrifugal force tending to throw the belt in the pulley also increases with the thickness, and for these reasons the thore a double belt required to transmit a given horse-rower when used. th of a single belt to transmit the same power. (Flather on "Dynamomrs and Measurement of Power.")

Tw. Taylor, however, finds that great pliability is objectionable, and ors thick belts even for small pulleys: The power consumed in bending belt around the pulley he considers inappreciable. According to Ransis of the belt, and hence it does not increase with increase of threes when the width is decreased in the case of the contraction. kness when the width is decreased in the same proportion, the sectional

a remaining constant.

cott A. Smith (Trans. A. S. M. E., x. 765) says: The best belts are made m all oak-tanned leather, and curried with the use of cod oil and tallow, to be of superior quality. Such belts have continued in use thirty to ty years when used as simple driving belts, driving a proper amount of ver, and having had suitable care. The flesh side should not be run to pulley-face, for the reason that the wear from contact with the pulley uld come on the grain side, as that surface of the belt is much weaker ta tensile strength than the flesh side; also as the grain is hard it is more luring for the wear of attrition; further, if the grain is actually worn off, n the belt may not suffer in its integrity from a ready tendency of the

d grain side to crack.

he most intimate contact of a belt with a pulley comes, first, in the othness of a pulley-face, including freedom from ridges and hollows left turning-tools; second, in the smoothness of the surface and evenness in texture or body of a belt; third, in having the crown of the driving and rering pulleys exactly alike,—as nearly so as is practicable in a commercial se; fourth, in having the crown of pulleys not over 36" for a 24" face, that one say, that the pulley is not to be over 34" larger in diameter in its centre; h, in having the crown other than two planes meeting at the centre; h, the use of any material on or in a belt, in addition to those necessarily in the use of any material of or in a ben, in adultion to those necessarily d in the currying process, to keep them pliable or increase their tractive slity, should wholly depend upon the exigencies arising in the use of is; non-use is safer than over-use; seventh, with reference to the lacing belts, it seems to be a good practice to cut the ends to a convex shape by g a former, so that there may be a nearly uniform stress on the lacing

ng a former, so that there may be a nearly uniform stress on the lacing ough the centre as compared with the edges. For a belt 10" wide, the tre of each end should recede 1/10".

neting of Belts.—In punching a belt for lacing, use an oval punch longer diameter of the punch being parallel with the sides of the belt. In two rows of holes in each end, placed zigzag. In a 8-in, belt there uld be four holes in each end—two in each row. In a 8-in, belt there is —four in the row nearest the end. A 10-inch belt should have nine is . The edge of the holes should not come nearer than 34 of an inch from sides, nor 36 of an inch from the ends of the belt. The second row should it least 134 inches from the end. On wide belts these distances should even a little greater.

ven a little greater.

egin to lace in the centre of the belt and take care to keep the ends ctly in line, and to lace both sides with equal tightness. The lacing uld not be crossed on the side of the belt that runs next the pulley. In

ing up belts, observe the same rules as putting on new ones.

etting a Belt on Quarter-twist.—A belt must run squarely on to pulley. To connect with a belt two horizontal shafts at right angles a each other, say an engine-shaft near the floor with a line attached to ceiling, will require a quarter-turn. First, ascertain the central point he face of each pulley at the extremity of the horizontal diameter where belt will leave the pulley, and then set that point on the driven pulley mb over the corresponding point on the driver. This will cause the belt un squarely on to each pulley, and it will leave at an angle greater or, according to the size of the pulleys and their distance from each other In quarter-twist belts, in order that the belt may remain on the pulleys, the central plane on each pulley must pass through the point of delivery of the other pulley. This arrangement does not admit of reversed motion.

To find the Length of Belt required for two given

To find the Length of Belt required for two given Pulleys.—When the length cannot be measured directly by a tape-line, the following approximate rule may be used: Add the diameter of the two pulleys together, divide the sum by 2, and multiply the quotient by 334, and add the product to twice the distance between the centres of the sharts. (See accurate formula below.)

To find the Angle of the Are of Contact of a Belt.—Divide the difference between the radii of the two pulleys in inches by the distance between their centres, also in inches, and in a table of natural sines find the angle most nearly corresponding with the quotient. Multiply this angle by 2, and add the product to 180° for the angle of contact with the larger pulley or subtract is from 180° for the angle of contact with the larger pulley, or subtract it from 180° for the smaller pulley.

Or, let R = radius of larger pulley, r = radius of smaller; L = distance between centres of the pulleys;

a =angle whose sine is (R - r) + L

Arc of contact with smaller pulley = $180^{\circ} - 2a$; " larger pulley = $180^{\circ} + 2a$.

To find the Length of Belt in Contact with the Bulley.— For the larger pulley, multiply the angle a, found as above, by .0849, to the product add 3.1416, and multiply the sum by the radius of the pulley. Or length of belt in contact with the pulley

= radius
$$\times$$
 (τ + .0849 α) = radius \times τ (1 + $\frac{\alpha}{90}$),

For the smaller pulley, length = radius $\times (\pi - .0349a) = \text{radius} \times \pi \left(1 - \frac{a}{20}\right)$.

The above rules refer to Open Belts. The accurate formula for length of an open belt is,

Length =
$$\pi R \left(1 + \frac{q}{90}\right) + \pi r \left(1 - \frac{q}{90}\right) + 2L \cos a$$

= $R(\pi + .0349a) + r(\pi - .0349a) + 2L \cos a$,

in which E = radius of larger pulley, r = radius of smaller pulley, L = distance between centres of pulleys, and a = angle whose size is

$$(R-r)+L$$
; $\cos a = \sqrt{L^2-(R-r)^2}+L$

For Crossed Belts the formula is

Length of belt =
$$\pi R \left(1 + \frac{\beta}{90}\right) + \pi r \left(1 + \frac{\beta}{90}\right) + 2L \cos \beta$$
,
= $(R + r) \times (\pi + .03496) + 2L \cos \beta$,

in which $\beta =$ angle whose sine is (R+r) + L; $\cos \beta = \sqrt{L^2 - (R+r)^2} + L$.

To find the Length of Belt when Closely Rolled.—The sum of the diameter of the roll, and of the eye in inches, X the number of turns made by the belt and by 1308, = length of the belt in feet

To find the Approximate Weight of Belts—Multiply the length of belt, in feet, by the width in inches, and divide the product by 13 for single, and 8 for double belt.

Relations of the Size and Speeds of Briving and Priven Pulleys.—The driving pulley is called the driver, D, and the driven pulley the driver, c. If the number of teeth in gears is used instead of diameter, in these calculations, number of teeth must be substituted wherever diameter. occurs. R = revs. per min. of driver, r = revs. per min. of driven

$$D=dr+R;$$

Diam, of driver = diam. of driven \times revs. of driven + revs. of driver.

$$d = DR + r$$
:

Diam. of driven = diam. of driver \times revs. of driver + revs. of driven.

$$R = dr + D$$
:

Revs. of driver = revs. of driven × diam. of driver + diam. of driver.

r = DR + dt

Revs. of driven = revs. of driver \times diam. of driver + diam. of driven.

Evils of Tight Belts. (Jones and Laughlins.)—Clamps with powerful

Evils of Tight Belts. (Jones and Laughlins.)—Clamps with powerful screws are often used to put on belts with extreme tightness, and with most injurious strain upon the leather. They should be very judiciously used for horizontal belts, which should be allowed sufficient slackness to move with a loose undulating vibration on the returning side, as a test that they have no more strain imposed than is necessary simply to transmit the power. On this subject a New England cotton-mill engineer of large experience, says: I believe that three quarters of the trouble experienced in broken pulleys, hot boxes, etc., can be traced to the fault of tight belts. The enormous and useless pressure thus put upon pulleys must in time break them, if they are made in any reasonable proportions, besides wearing out the whole outfit, and causing heating and consequent destruction of the bearings. Below are some figures showing the power it takes in average modern mills with first-class shafting, to drive the shafting alone:

Mill, No.	Whole	Shaftin	g Alone.		Whole	Shafting	ing Alone.	
	Load, H.P.		Per cent of whole.	Mill, No.	Load, H.P.	Horse- power.	Per cent of whole.	
1 2 8 4	199 472 486 677	51 111.5 134 190	25.6 28.6 27.5 28.1	5 6 7 8	759 235 670 677	172,6 84.8 962.9 182	22.7 36.1 89.2 26.8	

These may be taken as a fair showing of the power that is required in many of our best mills to drive shafting. It is unreasonable to think that all that power is consumed by a legitimate amount of friction of bearings and belts. I know of no cause for such a loss of power but tight belts. These, when there are hundreds or thousands in a mill, easily multiply the friction on the bearings and would account for the form.

on the bearings, and would account for the figures.

Sag of Helts.—In the location of shafts that are to be connected with each other by belts, care should be taken to secure a proper distance one from the other. This distance should be such as to allow of a gentle sag to the belt when in motion.

A general rule may be stated thus: Where narrow belts are to be run over

A general rule may be stated thus: Where narrow belts are to be run over small pulleys 15 feet is a good average, the belt having a sag of 1½ to 2 inches. For larger belts, working on larger pulleys, a distance of 20 to 25 feet does well, with a sag of 2½ to 4 inches. For main belts working on very large pulleys, the distance should be 25 to 30 feet, the belts working well with a sag of 4 to 5 inches. If too great a distance is attempted, the belt will have an unsteady flapping motion, which will destroy both the belt and machinery.

Arrangement of Helts and Pulleys.—If possible to avoid it, connected shafts should never be placed one directly over the other, as in such case the helt must be kent very tight to do the work. For this purpose belts case the belt must be kept very tight to do the work. For this purpose belts should be carefully selected of well-stretched leather.

should be carefully selected of well-stretched leather.

It is desirable that the angle of the belt with the floor should not exceed

5°. It is also desirable to locate the shafting and machinery so that belts
should run off from each shaft in opposite directions, as this arrangement
will relieve the bearings from the friction that would result when the belts all
pull one way on the shaft.

In arranging the belts leading from the main line of shafting to the
counters, those pulling in an opposite direction should be placed as near
each other as practicable, while those pulling in the same direction should be
separated. This can often be accomplished by changing the relative positions of the pulleys on the counters. By this procedure much of the friction
on the fournals may be avoided. on the journals may be avoided.

If possible, machinery should be so placed that the direction of the belt motion shall be from the top of the driving to the top of the driven pulley,

when the sag will increase the arc of contact.

The pulley should be a little wider than the belt required for the work.

The motion of driving should run with and not against the laps of the belts. Tightening or guide pulleys should be applied to the slack side of belts and

Jones & Laughlins, in their Useful Information, say: The diameter of the pulleys should be as large as can be admitted, provided they will not produce a speed of more than 4750 feet of belt motion per minute.

They also say: It is better to gear a mill with small pulleys and run them at a high velocity, than with large pulleys and to run them slower. A mill thus geared costs less and has a much neater appearance than with large

M. Arthur Achard (Proc. Inst. M. E., Jan. 1881, p. 62) says: When the belt is wide a partial vacuum is formed between the belt and the pulley at a high velocity. The pressure is the greater than that computed from the tensions in the belt, and the resistance to slipping is greater. This has the advantage of permitting a greater power to be transmitted by a given belt, and of diminishing the strain on the shafting.

On the other hand, some writers claim that the belt entraps air between itself and the pulley, which tends to diminish the friction, and reduce the tractive force. On this theory some manufacturers perforate the belt with numerous holes to let the air escape.

Care of Belts.-Leather belts should be well protected against water, loose steam, and all other moisture, with which they should not come in contact. But where such conditions prevail fairly good results are obtained by using a special dressing prepared for the purpose of water-proofing leather, though a positive water-proofing material has not yet been discovered.

Belts made of coarse, loose-fibred leather will do better service in dry and

warm places, but if damp or moist conditions exist then the very finest and

firmest leather should be used. (Fayerweather & Ladew.)

Do not allow oil to drip upon the belts. It destroys the life of the leather.

Leather belting cannot safely stand above 10° of heat.

Strength of Belting.—The ultimate tensile strength of belting does

not generally enter as a factor in calculations of power transmission. The strength of the solid leather in belts is from 2000 to 5000 lbs. per square inch; at the lacings, even if well put together, only about 1000 to 1500. If riveted, the joint should have half the strength of the solid belt. The working strain on the driving side is generally taken at not over one third of the

strength of the lacing, or from one eighth to one sixteenth of the strength of the solid belt. Dr. Hartig found that the tension in practice varied from 30 to 532 lbs. per square inch, averaging 273 lbs.

Adhesion Independent of Diameter. (Schultz Belting Co.)-1. The adhesion of the belt to the pulley is the same—the arc or number of

a. The sumeshold it the cold to the puncy is the same—the art of number of degrees of contact, aggregate tension or weight being the same—without reference to width of belt or diameter of pulley.

2. A belt will slip just as readily on a pulley four feet in diameter as it will on a pulley two feet in diameter, provided the conditions of the faces of the pulleys, the arc of contact, the tension, and the number of feet the belt through read which care the serve is belt care. travels per minute are the same in both cases

8. To obtain a greater amount of power from belts the pulleys may be covered with leather; this will allow the belts to run very slack and give 25%

more durability.

Endless Belts.—If the belts are to be endless, they should be put on and drawn together by "belt clamps" made for the purpose. If the belt is made endless at the belt factory, it should never be run on to the pulleys, lest the irregular strain spring the belt. Lift out one shaft, place the belt on the

pulleys, and force the shaft back into place.

Belt Data.—A fly-wheel at the Amoskeag Mfg. Co., Manchester, N. H.,
30 feet diameter, 10 inches face, running 61 revs. per min., carried two heavy
double-leather belts 40 inches wide each, and one 24 inches wide. The engine

double-leading to the set of the minute, on to a pulley 5 feet diameter, and transmitting 5.56 H.1. This gives a velocity of 210 feet per minute for 1 H.P. per inch of width. By Mr. Nagle's table of riveted belts this belt would be designed for 832 H.P. By Mr. Taylor's rule it would be used to transmit only 123 H.P.

The above may be taken as examples of what a belt may be made to do, but they should not be used as precedents in designing. It is not stated how much power was lost by the journal friction due to over-tightening of these belts.

Belt Drossings.—We advise that no belt dressing should be used except when the belt becomes dry and husky, and in such instances we recommend the use of a dressing. Where this is not used beef tallow at bloodwarm temperature should be applied and then dried in either by artificial heat or the sun. The addition of beeswax to the tallow will be of some service if the helts are used in wet or damp places. Our experience convinces us that resin should never be used on leather belling. (Fayerweather & Ladew.)

Belts should not be soaked in water before oiling, and penetrating oils should but solden be used, except occasionally when a belt gets very dry and husky from neglect. It may then be moistened a little, and have neat's foot oil applied. Frequent applications of such oils to a new belt render the leather soft and flabby, thus causing it to stretch, and making it liable to run out of line. A composition of tallow and oil, with a little resin or beeswax, is better to use. Prepared castor-oil dressing is good, and may be applied with a brush or rag while the belt is running. (Alexander Ross)

described with a brush or rag while the belt is running. (Alexander Bros.)

Coment for Cloth or Leather. (Molesworth.)—16 parts guttapercha, 4 india-rubber, 2 pitch, 1 shellac, 2 linseed-oil, cut small, melted to-

gether and well mixed.

Bubber Belting.—The advantages claimed for rubber belting are perfect uniformity in width and thickness; it will endure a great degree of heat and cold without injury; it is also specially adapted for use in damp or wet places, or where exposed to the action of steam; it is very durable, and has great tensile strength, and when adjusted for service it has the most per-fect hold on the pulleys, hence is less liable to slip than leather.

Never use animal oil or grease on rubber belts, as it will greatly injure and

soon destroy them

Rubber belts will be improved, and their durability increased, by putting on with a painter's brush, and letting it dry, a composition made of equal parts of red lead, black lead, French yellow, and litharge, mixed with boiled linesed-oil and japan enough to make it dry quickly. The effect of this will be to produce a finely polished surface. If, from dust or other cause, the belt should slip, it should be lightly moistened on the side next the pulley with boiled linseed-oil. (From circulars of manufacturers.)

The best conditions are large pulleys and high speeds, low tension and reduced width of belt. 4000 ft. per min. is not an excessive speed on proper

sized pulleys.

H.P. of a 4-ply rubber belt = (length of arc of contact on smaller rulley in ft. \times width of belt in ins. \times rows. per min.) + 325. For a 5-ply belt multiply by 1½, for a 6-ply by 1½, for a 6-ply by 1½, for a 8-ply by 2½. When the proper weight of duck is used a 3- or 4-ply rubber belt is equal to a single leather belt and a 5- or 6-ply rubber to a double leather belt. When the arc of contact is 180°, H.P. of a 4-ply belt = width in ins. \times velocity in ft. per min. + 650. (Boston Belting Co.)

GEARING.

TOOTHED-WHEEL GEARING.

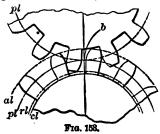
Pitch, Pitch-circle, etc.—If two cylinders with parallel axes are pressed together and one of them is rotated on its axis, it will drive the other by means of the friction between the surfaces. The cylinders may be considered as a pair of spur-wheels with an infinite number of very small teeth. If actual teeth are formed upon the cylinders, making alternate elevations and depressions in the cylindrical surfaces, the distance between the exes and depressions in the cylindrical surfaces, the distance between the sxes remaining the same, we have a pair of grar-wheels which will drive one another by pressure upon the faces of the teeth, if the teeth are properly shaped. In making the teeth the cylindrical surface may entirely disappear, but the position it occupied may still be considered as a cylindrical surface, which is called the "pitch-surface," and its trace on the end of the wheel, or on a plane cutting the wheel at right angles to its axis, is called the "pitch-circle" or "pitch-line." The diameter of this circle is called the otto-diameter and the distance from the face of one toth to the correpitch-diameter, and the distance from the face of one tooth to the corresponding face of the next tooth on the same wheel, measured on an arc of the pitch-circle, is called the "pitch of the tooth," or the circular pitch. If two wheels having teeth of the same pitch are geared together so that their pitch-circles touch, it is a property of the pitch-circles that their diam-

sters are proportional to the number of teeth in the wheels, and vice v-

thus, if one wheel is twice the diameter (measured on the pitch-circle) of the other, it has twice as many teeth. If the teeth are properly shaped the linear velocity of the two wheels are equal, and the angular velocities, or speeds of rotation, are inversely proportional to the number of teeth and to the diameter. Thus the wheel that has twice as many teeth as the other

will revolve just half as many times in a minute.

The "pitch," or distance measured on an arc of the pitch-circle from the face of one tooth to the face of the next, consists of two parts—the "thickness" of the tooth and the "space" between it and the next tooth. space is larger than the thickness by a small amount called the "back-lash," which is allowed for imperfections of workmanship. In finely cut gears the backlash may be almost nothing



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The length of a tooth in the direction of the radius of the wheel is called the "depth," and this is di-vided into two parts: First, the "addendum," the height of the tooth above the pitch line; second, the "dedendum," the depth below the pitch line, which is an amount equal to the addendum of the mating gear. The depth of the space is usually given a little "clearance" to allow for inaccuracies of workmanship, especially in cast gears.

Referring to Fig. 153, pl, pl are the

pitch-lines, al the addendum-line, rl the root-line or dedendum-line, cl

the clearance-line, and b the backlash. The addendum and dedendum are usually made equal to each other. No. of teeth 8.1416

Diametral pitch = $\frac{\text{No. of teeth}}{\text{diam. of pitch-circle in inches}}$ Circular pitch: = $\frac{\text{diam. } \times 8.1416}{\text{No. of teeth}} = \frac{3.1416}{\text{diam. et al. ni}}$ circular pitch' No. of teeth diametral pitch

Some writers use the term diametral pitch to mean No. of teeth

circular pitch, but the first definition is the more common and the more convenient. A wheel of 12 in. diam, at the pitch-circle, with 48 teeth is 48/12 = 4 diametral pitch, or simply 4 pitch. The circular pitch of the same wheel is $\frac{12\times8.1416}{12\times8.1416}$ = .7854, or $\frac{8.1416}{4} = .7854$ in.

Relation of Diametral to Circular Pitch.

	Delai	TOIL OF	Diamet	I all to C	IICUIAI	E 10CH.	
Diame- tral Pitch.	Circular Pitch.	Diame- tral Pitch.	Circular Pitch.	Circular Pitch.	Diame- tral Pitch.	Circular Pitch.	Diame- tral Pitch.
1 11/2 2 23/4 23/4 3 3 4 5 5 5	8.142 in. 2.094 1.571 1.896 1.257 1.142 1.047 .896 .785 .628	11 12 14 16 18 20 28 24 24 26 28		8 21/2 2 17/6 18/4 15/6 1 7/16 13/6 1 5/16	1.047 1.257 1.571 1.676 1.795 1.938 2.094 2.185 2.285 2.394 2.513	15/16 36 13/16 34 11/16 56 9/16 1/6 7/16	8.851 8.590 8.867 4.189 4.570 5.027 5.585 6.283 7.181 8.378 10.053
7 8 9 10	.449 .898 .849 .314	82 86 40 48	.098 .087 .079 .065	1 3/16 1 4 1 1/16 1	2.646 2.793 2.957 3.142	3/16 3/16 1/16	12.566 16.755 25.188 50.266

diam. = circ. pitch \times No. of teeth Since circular pitch = $\frac{\text{diam.} \times 3.1416}{\text{No. of teeth}}$,

which always brings out the diameter as a number with an inconvenient

action if the pitch is in even inches or simple fractions of an inch. By the ametral-pitch system this inconvenience is avoided. The diameter may a in even inches or convenient fractions, and the number of teeth is usually reven multiple of the number of inches in the diameter.

lameter of Pitch-line of Wheels from 10 to 100 Teeth of 1 in. Circular Pitch.

0 3.183 26 8.276 41 13.051 56 17.825 71 22.600 86 27 1 3.501 27 8.594 42 13.369 57 18.44 72 22.918 87 27	1	Teeth.		Diam., in.	No Teeth.	Diam., in.	No. Teeth.	Diam., in.	No. Teeth.	Diam., in.	No. Teeth.	Diam., in.
5 4.775 81 9.868 46 14.642 61 19.417 76 24.192 91 28 6 5.098 82 10.186 47 14.961 62 19.735 77 24.510 22 28 7 5.411 83 19.504 48 15.279 63 20.054 78 24.828 23 29 8 5.730 84 10.828 49 15.597 64 20.372 79 25.146 94 29 9 6.048 85 11.141 50 15.915 65 20.690 80 25.465 94 29 10 6.686 86 11.459 51 16.234 66 21.008 81 25.789 96 30 16.686 87 11.777 52 16.552 67 21.327 82 26.101 97 30 22 7.003 88 12.096 53 16.870 68 21.645 83 26.419 98 81 25.783 39 12.414 54 17.189 69 21.963 84 25.738 99 81	3.183 3.501 3.820 4.138 4.456 4.775 5.098 5.411 5.730 6.048 6.366 6.685 7.003 7.321	1 2 3 4 5 6 7 8 9 9 1 2 2 3	3.501 27 3.820 28 4.138 30 4.775 81 5.098 32 5.411 38 6.048 35 6.685 37 7.003 38 7.003 38	8.594 8.513 9.231 9.549 9.868 10.186 10.504 10.823 11.141 11.459 11.777 12.096 12.414	42 43 44 45 46 47 48 49 50 51 52 58	18.369 18.687 14.006 14.324 14.642 14.642 15.279 15.597 15.915 16.234 16.552 16.870 17.189	57 58 59 60 61 62 63 64 65 66 67 68	18 44 16 462 18 781 19 099 19 117 19 785 20 554 20 50 21 327 21 645 21 963	72 73 74 75 76 77 78 79 81 82 83 84	22.918 22.286 23.555 23.555 24.192 24.510 25.146 25.146 25.101 26.101 26.738	88899133343657889	29.285 29.603 29.921 80.239

For diameter of wheels of any other pitch than 1 in., multiply the figures the table by the pitch. Given the diameter and the pitch, to find the numer of teeth. Divide the diameter by the pitch, look in the table under iameter for the figure nearest to the quotient, and the number of teeth will 3 found opposite.

Proportions of Teeth. Circular Pitch = 1.

	1.	2.	3.	4.	5.	6.
epth of tooth above pitch-line	.35	.30	.37	.33	.30	.30 .35
'orking depth of tooth	.70	.60	.73	.66	•	
otal depth of tooth	.75	.70	.80 .07	.75	.70	.65
nickness of tooth	.45	.45	.47	.45	.475	.485
idth of space	.54	.55	.53	.55	.525 .05	.515
ickness of rim			.47	.45	.70	.65
	7.	8.		9.	1 3	0.*
epth of tooth above pitch-line " "below pitch-line	.35 to .4	l2 .35 ∔ .	08"	.318 .369		1÷ <i>P</i> 7÷ <i>P</i>
orking depth of tooth				.637		2+P
earance at root	.6 10 .7	0 .00+.		.687 4 to .05		7÷P ′÷P
nickness of tooth				8 to .5	1.57	
idth of space	.52 to .5	15 .52+.	03" .5	2 to .5	1.57	+Pto +P
cklash	1.04 tc .0	8 .04+.	06" .0	to .04	0 to	0 6+P

* In terms of diametral pitch.

AUTHORITIES.—1. Sir Wm. Fairbairn. 2, 3. Clark, R. T. D.; "used by eners in good practice." 4. Molesworth. 5, 6. Coleman Sellers: 5 for st, 6 for cut wheels. 7, 8. Unwin. 9, 10. Leading American manufacturers cut gears.

The Chordal Pitch (erroneously called "true pitch" by some thors) is the length of a straight line or chord drawn from centre to ntre of two adjacent teeth. The term is now but little used.

Chordal pitch = diam. of pitch-circle \times sine of $\frac{100^{\circ}}{\text{No. of teeth}}$ Chordal pitch of a wheel of 10 in. pitch diameter and 10 teeth, 10 × sin 18° = 3.0903 in. Circular pitch of same wheel = 3 1416. Chordal pitch is used with chain or sprocket wheels, to conform to the pitch of the chain,

Formulæ for Determining the Dimensions of Small Gears. (Brown & Sharpe Mfg. Co.)

P = diametral pitch, or the number of teeth to one inch of diameter of pitch-circle:

D' = diameter of pitch circle	Larger Wheel.	These wheels
d' = diameter of pitch-circle d = whole diameter v = number of teeth v = velocity	Smaller Wheel	together,

a =distance between the centres of the two wheels:

b =number of teeth in both wheels;

t =thickness of tooth or cutter on pitch-circle;

s = addendum;

D'' = working depth of tooth; f = amount added to depth of tooth for rounding the corners and for clearance; D''+f= whole depth of tooth; $\pi=3.1416$.

P' = circular pitch, or the distance from the centre of one tooth to the centre of the next measured on the pitch-circle.

Formulæ for a single wheel:

$$P = \frac{N+2}{D}; \quad D' = \frac{D \times N}{N+2}; \quad D'' = \frac{2}{P} = 2s; \quad s = \frac{1}{P} = \frac{P'}{\pi} = .8188P';$$

$$P = \frac{N}{D}; \quad D' = \frac{N}{P}; \quad N = PD'; \quad s = \frac{D'}{N} = \frac{D}{N+2};$$

$$P = \frac{\pi}{P}; \quad D = \frac{N+2}{P}; \quad f = \frac{t}{10}; \quad s + f = \frac{1}{P} \left(1 + \frac{\pi}{20}\right) = .8686 t^{x}$$

$$P = \frac{\pi}{P}; \quad D = D' + \frac{2}{P}; \quad t = \frac{1.67}{P} = \frac{1}{2}P'.$$

Formulæ for a pair of wheels:

$$b = 2aP; \qquad n = \frac{PD'V}{v} \qquad D = \frac{2a(N+9)}{b};$$

$$N = \frac{nv}{V}; \qquad v = \frac{PD'V}{n}; \qquad d = \frac{2a(n+9)}{b};$$

$$n = \frac{NV}{v}; \qquad v = \frac{NV}{n}; \qquad a = \frac{b}{2P};$$

$$N = \frac{bv}{v+V}; \qquad V = \frac{nv}{N}; \qquad a = \frac{D+d'}{9};$$

$$n = \frac{bV}{v+V}; \qquad D' = \frac{2av}{v+V}; \qquad d' = \frac{2aV}{v+V}.$$

The following proportions of gear wheels are recommended by vrot. Coleman Sellers. (Stevens Indicator, April, 1862.)

Proportions of Gear-wheels.

			Inside of I	Pitch-line.	Width o	f Space.
Diametral Pitch.	Circular Pitch.	Outside of Pitch-line. $P \times .3$	For Cast or Cut Bevels or for Cast Spurs. P × .4	For Cut Spurs. P × .85	For Cast Spurs or Bevels. P × .525	For Cut Bevels or Spurs. P × .51
12 10	.2618 .31416	.075 .079 .094	.100 .105 .126	.088 .092 .11	.131 .137 .165	.128 .184 .16
8 7	.8927 .4477	.113 .118 .134 .15	.150 .157 .179	. 181 . 187 . 157	.197 .206 .235	.191 .2 .228
6	5286 9/16 56	.157	.20 .209 .225 .25	.175 .183 .197 .219	.263 .275 .295 .328	.255 .267 .287 .319
5	.62832 84	.188 .188 .225	.251 .8	.22	.33	.32
4	.7854 76	.236 .268	.814 .85	.275 .307	.412 .459	.401 .446
8	1.0478	.8 .814 .338	.4 .419 .45	.35 .364 .894	.525 .55	.51 .584
23/4	136 1.1424	.848 .875	.457 .5	.40 .438	.591 .6 .656	.574 .583 .638
21/2	136	.877 .418	.508 .55	.44 .481	.66 .722	.641 .701
2	112 1.5708 184	.45 .471 .525	.6 .629	.525 .55 .618	.780 .825 .919	.765 .801 .893
134	2	.6 .628 .675	.8 .838	.7 .788 .788	1.05 1.1 1.181	1.02 1.068 1.148
	212	.75 .825	1.0	.875 .968	1.318 1.444	1.275 1.408
1	8.1416	.9	1.2 1.257	1.05	1.575 1.649	1.53 1.602
	81/4 81/2	.975 1.05	1.8 1.4	1.138 1.225	1.706 1.888	1.657 1.785

Thickness of rim below root = depth of tooth,

Width of Teeth.—The width of the faces of teeth is generally made from 2 to 3 times the circular pitch—from 6.28 to 9.42 divided by the diametral pitch. There is no standard rule for width.

The following sizes are given in a stock list of cut gears in "Grant's Gears:"

Diameter pitch.... 3 4 6 8 12 16 Face, inches...... 3 and 4 2½ 1¾ and 2 1¼ and 1⅓ ¾ and 1 ⅓ and 56 The Walker Company give:

Circular pitch, in.. 34 54 34 76 1 114 2 214 3 4 5 6 Face, in....... 114 114 114 2 214 6 714 9 12 16 21

Rules for Calculating the Speed of Gears and Pulleys.— The relations of the size and speed of driving and driven gear wheels are the same as those of belt pulleys. In calculating for gears, multiply or divide by the diameter of the pitch-circle or by the number of teeth, as may be required. In calculating for pulleys, multiply or divide by their diameter in inches.

If D = diam, of driving wheel, d = diam, of driven, R = revolutions per minute of driver, r = revs, per min. of driven.

R = rd + D; r = RD + d; D = dr + R; d = DR + r.If N = number of teeth of driver and n = number of teeth of driven, N = nr + R; n = NR + r; R = rn + N; r = RN + n.

To find the number of revolutions of the last wheel at the end of a train of spur-wheels, all of which are in a line and mesh into one another, when the revolutions of the first wheel and the number of teeth or the diameter of the first and last are given: Multiply the revolutions of the first wheel by its number of teeth or its diameter, and divide the product by the number

of teeth or the diameter of the last wheel.

To find the number of teeth in each wheel for a train of spur-wheels, each to have a given velocity. Multiply the number of revolutions of the driving wheel by its number of teeth, and divide the product by the number

of revolutions each wheel is to make.

To find the number of revolutions of the last wheel in a train of wheels and pinions, when the revolutions of the first or driver, and the diameter, the teeth, or the circumference of all the drivers and pinions are given: Multiply the diameter, the circumference, or the number of teeth of all the mutiply the diameter, he circumference, of the number of reen of all the driving-wheels together, and this continued product by the continued product of the diameter, the circumference, or the number of teeth of all the driven wheels, and the quotient will be the number of revolutions of the last wheel. Example.—1. A train of wheels consists of four wheels each 12 in diameter of pitch-circle, and three pinions 4, 4, and 3 in diameter. The targe wheels are the drivers, and the first makes 36 revs. per min: Required the speed of the leat wheel

of the last wheel.

$$\frac{36 \times 12 \times 12 \times 12}{4 \times 4 \times 8} = 1296 \text{ rpm.}$$

2. What is the speed of the first large wheel if the pinions are the drivers. the 8-in. pinion being the first driver and making 86 fevs. per min.?

$$\frac{86 \times 3 \times 4 \times 4}{12 \times 12 \times 12} = 1 \text{ rpm. } Ans.$$

Milling Cutters for Interchangeable Gears.—The Pratt & Whitney Co. make a series of cutters for cutting epicycloidal teeth. The number of cutters to cut from a pinion of 12 teeth to a rack is 24 for each pitch coarser than 10. The Brown & Sharpe Mfg. Co. make a similar series, and also a series for involute teeth, in which eight cutters are made for each pitch, as follows:

No	. 1.	2.	8.	4.	5.	6.	۲:	8.
Will cut from	135	55	85	26	21	17	14	12
to	Rack	134	54	84	25	20	16	18

FORMS OF THE TEETH.

In order that the teeth of wheels and pinions may run together smoothly and with a constailt relative velocity; it is necessary that their working faces shall be formed of certain curves called odontoids. The essential property of these curves is that when two teeth are in contact the common normal to the tooth curves at their point of contact must pass through the pitch-point, or point of contact of the two pitch circles. Two such curves are in common use—the cyloid and the involute.

The Cycloidal Tooth.—In Fig. 154 let PL and pl be the pitch-circles of two gear-wheels; GC and gc are two equal generating-circles, whose raddishould be taken as not greater than one half of the radius of the smaller should be taken as not greater than one half of the radius of the smaller pitch-circle. If the circle go be rolled to the left on the larger pitch-circle PL, the point O will describe an epicycloid, or gh. If the other generating circle GU be rolled to the right on PL, the point O will describe a hypocycloid oabed. These two curves, which are tangent at O, form the two parts of a tooth curve for a gear whose pitch-circle is PL. The upper part. A is called the face and the lower part of is called the flank, If the same circles be rolled on the other pitch-circle pl, they will describe the curve for a tooth of the central which will work principly with the tooth or PM

of the gear pl, which will work properly with the tooth on PL. The cycloidal curves may be drawn without actually rolling the generating-circle, as follows: On the line PL, from O, step off and mark equal dising-circle, as rollows: On the line FL, from 0, seep on and main equal interaces, at 1,2,8,4 etc. From 1, 2, 3, etc., draw radial lines toward the centre of PL, and from 6, 7, 8, etc., draw radial lines from the same centre, but beyond PL. With the radius of the generating-circle, and with centres successively placed on these radial lines, draw arcs of tircles tangent to PL at 1,2,3,6,7,8, etc. With the dividers set to one of the equal divisions, as O_1 , step off 1a and 6e; step off two such divisions on the circle from 2 to b, and from 7 to f; three such divisions from 3 to c, and from 6 to g; and so on, thus locating the several points abcdH and efgk, and through these points draw the tooth curves.

The curves for the mating tooth on the other wheel may be found in like manner by drawing arcs of the generating-circle tangent at equidistant

points on the pitch-circle pl.

The tooth curve of the face oh is limited by the addendum-line r or r_{10}

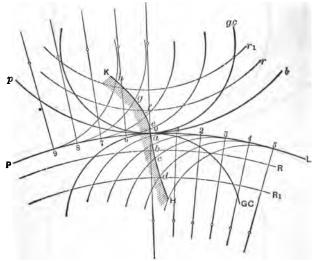


Fig. 154.

and that of the flank oH by the root curve R or R_1 . R and r represent the root and addendum curves for a large number of small teeth, and R_1r the like curves for a small number of large teeth. The form or appearance of the tooth therefore varies according to the number of teeth, while the pitch-

circle and the generating-circle may remain the same.

In the cycloidal system, in order that a set of wheels of different diameters but equal pitches shall all correctly work together, it is necessary that the generating-circle used for the teeth of all the wheels shall be the same, and it should have a diameter not greater than half the diameter of the pitchline of the smallest wheel of the set. The customary standard size of the generating-circle of the cycloidal system is one having a diameter equal to the radius of the pitch-circle of a wheel having 12 teeth. (Some gearmakers adopt 15 teeth.) This circle gives a radial flank to the teeth of a wheel having 12 teeth. A pinion of 10 or even a smaller number of teeth can be made, but in that case the flanks will be undercut, and the tooth will not be as strong as a tooth with radial flanks. If in any case the describing circle be half the size of the pitch-circle, the flanks will be radial; if it be less, they will spread out toward the root of the tooth, giving a stronger form; but if greater, the flanks will curve in toward each other, whereby the teeth become weaker and difficult to make.

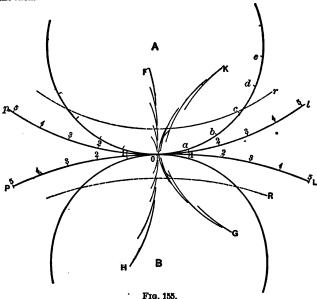
teeth become weaker and difficult to make.

In some cases cycloidal teeth for a pair of gears are made with the generating-circle of each gear, having a radius equal to half the radius of its pitch-circle. In this case each of the gears will have radial flanks. This method makes a smooth working gear, but a disadvantage is that the wheels are not interchangeable with other wheels of the same pitch but different numbers.

bers of teeth.

894 GEARING.

The rack in the cycloidal system is equivalent to a wheel with an infinite number of teeth. The pitch is equal to the circular pitch of the mating gear. Both faces and fianks are cycloids formed by rolling the generating-circle of the mating gear-wheel on each side of the straight pitch-line of the rack.



Another method of drawing the cycloidal curves is shown in Fig. 155. It is known as the method of tangent arcs. The generating-circles, as before, are drawn with equal radii, the length of the radius being less than half the radius of pl, the smaller pitch-circle. Equal divisions 1, 2, 3, 4, etc., are marked off on the pitch circles and divisions of the same length stepped of on the generating-circles, as oabc, etc. From the points 1, 2, 3, 4, 5 on the line po, with radii successively equal to the chord distances oa, ob, oc, od, oe, draw the five small arcs F. A line drawn through the outer edges of these small arcs tangent to them all, will be the hypocycloidal curve for the flank of a tooth below the pitch-line pl. From the points 1, 2, 3, etc., on the line ol, with radii as before, draw the small arcs G. A line tangent to these arcs will be the epicycloid for the face of the same tooth for which the flank curve has already been drawn. In the same way, from centres on the line P_0 , and oL, with the same radii, the tangent arc: H and K may be drawn, which will give the tooth for the gear whose pitch-circle is PL.

If the generating-circle had a radius just one half of the radius of pl, the hypocycloid F id be a straight line, and the flank of the tooth would have been radial.

The Involute Tooth,—In drawing the involute tooth curve, the angle of obliquity or the angle which a common tangent to the teeth, when they are in contact at the pitch-point, mak... with a line joining the centres of the wheels, is first arbitrarily determined. It is customary to take it at 15°. The pitch-lines pl and PL being drawn in contact at 0, the line of obliquity AB is drawn through Onormal to a common tan-ent to the tooth curves, or at the given angle of obliquity to a common tangent to the pitch-pircles. In

the cut the angle is 20° . From the centres of the pitch-circles draw circles and d tangent to the line AB. These circles are called base-lines or base-circles, from which the involutes F and K are drawn. By laying off convenient distances, 0, 1, 2, 8, which should each be less than 1/10 of the diameter of the base-circle, small arcs can be drawn with successively increasing radii, which will form the involute. The involute extends from the points F

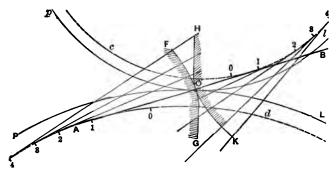


Fig. 156.

and K down to their respective base-circles, where a tangent to the involute becomes a radius of the circle, and the remainders of the tooth curves,

as G and H, are radial straight lines.

In the involute system the customary standard form of tooth is one having an angle of obliquity of 15° (Brown and Sharpe use 14½°), an addendum of about one third the circular pitch, and a clearance of about one eighth of the addendum. In this system the smallest gear of a set has 12 teeth, this being the smallest number of teeth that will gear together when made with this angle of obliquity. In gears with less than 30 teeth the points of the teeth must be slightly rounded over to avoid interference (see Grant's Teeth of Gears). All involute teeth of the same pitch and with the same angle of obliquity work smoothly together. The rack to gear with an involute-toothed wheel has straight faces on its teeth, which make an angle with the middle line of the tooth equal to the angle of obliquity, or in the standard form the faces are inclined at an angle of 30° with each other.

standard form the faces are inclined at an angle of 30° with each other. To draw the teelh of a rack which is to gear with an involute wheel (Fig. 157).—Let AB be the pitch-line of the rack and AI = II' = the pitch. Through

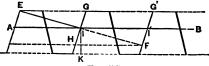


Fig. 157.

the pitch-point I draw EF at the given angle of obliquity. Draw AE and I'F perpendicular to EF. Through E and F draw lines EGG' and FH parallel to the pitch-line. EGG' will be the addendum-line and HF the flank line. From I draw IK perpendicular to AB equal to the greatest addendum in the set of wheels of the given pitch and obliquity plus an allowance for clearance equal to 1/2 of the addendum. Through K, parallel to AB, draw the clearance-line. The fronts of the teeth are planes perpendicular to EF, and the backs are planes inclined at the same angle to AB in the contrary direction. The outer half of the working face AE may be slightly curved. AF. Grant makes it a circular arc drawn from a centre on the pitch-line

with a radius = 1.. inches divided by the diametral pitch, or .67 in. × circular pitch.

To Draw an Angle of 15° without using a Protractor.—From C, on the

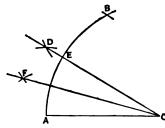


Fig. 158.

line AC, with radius AC, draw an arc AB, and from A, with the same radius, cut the arc at B. Bisect the arc BA by draw-ing small arcs at D from A and B as centres, with the same radius. which must be greater than one half of AB. Join DC, cutting BA at E. The angle ECA is 80°. Bisect the arc AE in like manner, and the angle FCA will be 15°

A property of involute-toothed wheels is that the distance between the axes of a pair of gears may be altered to a considerable extent without interfering with their ac-tion. The backlash is therefore variable at will, and may be ad-

justed by moving the wheels farther from or nearer to each other, and may thus be adjusted so as to be no greater than is necessary to prevent jamming of the teeth.

The relative merits of cycloidal and involute-shaped teeth are still a subject of dispute, but there is an increasing tendency to adopt the involute

tooth for all purposes.

Clark (R. T. D., p. 784) says: Involute teeth have the disadvantage of being too much inclined to the radial line, by which an undue pressure is

exerted on the bearings.
Unwin (Elements of Machine Design, 8th ed., p. 265) says: The obliquity of action is ordinarily alleged as a serious objection to involute wheels. Its

importance has perhaps been overrated.
George B. Grant (Am. Mach., Dec. 26, 1885) says:

1. The work done by the friction of an involute tooth is always less than the same work for any possible epicycloidal tooth.

2. With respect to work done by friction, a change of the base from a gear of 12 teeth to one of 15 teeth makes an improvement for the epicycloid of less than one half of one per cent.

3. For the 12-tooth system the involute has an advantage of 1 1/5 per

cent, and for the 15-tooth system an advantage of \$4 per cent.

4. That a maximum improvement of about one per cent can be accomplished by the adoption of any possible non-interchangeable radial flank tooth in preference to the 12-tooth interchangeable system.

5. That for gears of very few teeth the involute has a decided advantage.

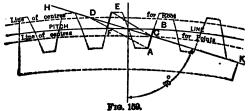
6. That the common opinion among millwrights and the mechanical public in general in favor of the epicycloid is a prejudice that is founded on long-continued custom, and not on an intimate knowledge of the properties

of that curve.

Wilfred Lewis (Proc. Engrs. Club of Phila., vol. x., 1893) says a strong
Wilfred Lewis (Proc. Engrs. Club of Phila., vol. x., 1893) says a strong

an involute tooth of 2216° obliquity will finally supplant all other forms.

Approximation by Circular Ares.—Having found the form of the actual tooth-curve on the drawing-board, circular arcs may be found by trial which will give approximations to the true curves. and these may be



sed in completing the drawing and the pattern of the gear-wheels. The of of the curve is connected to the clearance by a filet, which should be a large aspossible to give increased strength to the tooth, provided it is not

rge enough to cause interference. Molesworth gives the following method of construction by circular arcs: From the radial line at the edge of the tooth on the pitch-line, lay off the ie HK at an angle of 75° with the radial line; on this line will be the cen-The RA at an angle of r_0 with the radial mie; on this line will be the centres of the root AB and the point EF. The lines struck from these centres e shown in thick lines. Circles drawn through centres thus found will be the lines in which the remaining centres will be. The radius DA for riking the root AB is = pitch + the thickness of the tooth. The radius E for striking the point of the tooth EF = the pitch.

George B. Grant says: It is sometimes attempted to construct the curve some handy method or empirical rule, but such methods are generally

orthless.

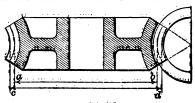
Stepped Gears. -- Two gears of the same pitch and diameter mounted le by side on the same shaft will act as a single gear. If one gear is keyed the shaft so that the teeth of the two wheels are not in line, but the eth of one wheel slightly in advance of the other, the two gears form a pped gear. If mated with a similar stepped gear on a parallel shaft the imber of teeth in contact will be twice as great as in an ordinary gear, ich will increase the strength of the gear and its smoothness of action.

Twisted Teeth.—If a great number of very thin gears were placed gether, one slightly in advance of the other, they would still act as a epped gear. Continuing the subdivision until the ickness of each separate gear is infinitesimal, the ses of the teeth instead of being in steps take the rin of a spiral or twisted surface, and we have a isted gear. The twist may take any shape, and if it is one direction for half the width of the gear and in the posite direction for the other half, we have what is own as the herring-bone or double helical tooth. The liguity of the twisted tooth if twisted in one direction uses an end thrust on the shaft, but if the herring-ne twist is used, the opposite obliquities neutralize the twist is used, the opposite conductes neutralize the other. This form of tooth is much used in heavy ling-mill practice, where great strength and resistance shocks are necessary. They are frequently made of shocks are necessary. They are frequently made of el castings (Fig. 160). The angle of the tooth with a e parallel to the axis of the gear is usually 30°.



ipiral Gears. - If a twisted gear has a uniform twist it becomes a ral gear. The line in which the pitch-surface intersects the face of the this part of a helix drawn on the pitch-surface. A spiral wheel may be de with only one helical tooth wrapped around the cylinder several tes, in which it becomes a screw or worm. If it has two or three teeth wrapped, it is a double- or triple-threaded screw or worm. A spiral-gear shing into a rack is used to drive the table of some forms of planing-

when the axes of two spiral gears are at right tes, and a wheel of one, two, or three threads works with a larger wheel many threads, it becomes a worm-gear, or endless screw, the smaller



Frg. 161.

ed or driver being called the worm, and the larger, or driven wheel, the m-wheel. With this arrangement a high velocity ratio may be obtained a single pair of wheels. For a one-threaded wheel the velocity ratio

the number of teeth in the worm-wheel. The worm and wheel are commonly so constructed that the worm will drive the wheel, but the wheel will not drive the worm.

To find the diameter of a worm-wheel at the throat, number of teeth and putch of the worm being given: Add 2 to the number of teeth, multiply the

sum by 0 3188, and by the pitch of the worm in inches

To find the number of teeth, diameter at throat and pitch of worm being riven: Divide 3.1416 times the diameter by the pitch, and subtract 2 from the quotient.

In Fig. 161 ab is the diam. of the pitch-circle, cd is the diam. at the throat, Example.—Pitch of worm $\frac{1}{2}$ in., number of teeth 70, required the diamatthe throat. (70 + 2) × .3183 × .25 = 5.73 in.

Teeth of Bevel-wheels. (Rankine's Machinery and Millwork.)—

The teeth of a bevel-wheel have acting surfaces of the conical kind, generated by the motion of a line traversing the apex of the conical pitchsurface, while a point in it is carried round the traces of the teeth upon a spherical surface described about that apex.

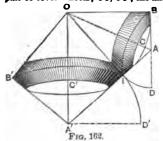
The operations of drawing the traces of the teeth of bevel-wheels exactly, whether by involutes or by rolling curves, are in every respect analogous to those for drawing the traces of the teeth of spur-wheels; except that in the case of bevel-wheels all those operations are to be performed on the surface of a sphere described about the apex. instead of on a plane, substituting

poles for centres and great circles for straight lines.

In consideration of the practical difficulty, especially in the case of large wheels, of obtaining an accurate spherical surface, and of drawing upon it when obtained, the following approximate method, proposed originally by Tredgold, is generally used:

Let O, Fig. 162, be the common apex of the pitch-cones. OBI, OB'I, of a

pair of bevel-wheels; OC, OC, the axes of those cones; OI their line of con-tact. Perpendicular to OI draw



AIA', cutting the axes in A, A'; make the outer rims of the patterns and of the wheels portions of the cones ABI. A'B'I, of which the narrow zones occupied by the teeth will be sufficiently near for practical pur-poses to a spherical surface described about O. As the cones ABI, A'B'I cut the pitch-cones at right angles in the outer pitch-circles IB, IB, they may be called the normal cones. To find the traces of the teeth upon the normal cones, draw on a flat surface faces ABI, A'B'I are spread out flat.

Describe the traces of teeth for the developments of arcs of the pitch.

Describe the traces of teeth for the

developed arcs as for a pair of spur-wheels, then wrap the developed arcs on the normal cones, so as to make them coincide with the pitch circles, and

trace the teeth on the conical surfaces.

For formulæ and instructions for designing bevel-gears, and for much other valuable information on the subject of gearing, see "Practical Treatise on Gearing," and "Formulas in Gearing," published by Brown & Sharpe Mf'g Co.; and "Teeth of Gears," by George B. Grant, Lexington, Mass. The student may also consult Rankine's Machinery and Millwork, Reuleaux's Constructor, and Unwin's Elements of Machine Design. See also article on Gearling by C. W. MacCond.

Constructor, and Unwin's Elements of Machine Design. See also article on Gearing, by C. W. MacCord in App. Cyc. Mech., vol. ii.

Annular and Differential Gearing. (S. W. Balch., Am. Mach., Aug. 24, 1893.)—In internal gears the sum of the diameters of the described circles for faces and flanks should not exceed the difference in the pltch diameters of the pinion and its internal gear. The sum may be equal to this difference or it may be less; if it is equal, the faces of the teeth of each wheel will drive the faces as well as the flanks of the teeth of the other wheel. The teeth will therefore make courter with each other at two orders. wheel. The teeth will therefore make contact with each other at two points

at the same time.

Cycloidal tooth-curves for interchangeable gears are formed with describing circles of about 56 the pitch diameter of the smallest gear of the series. To admit two such circles between the pitch-circles of the pinion and internal gear the number of teeth in the internal gear should exceed the number in the pinion by 12 or more, if the teeth are of the customary proportions and curvature used in interchangeable gearing.

Very often a less difference is desirable, and the teeth may be modified in

several ways to make this possible. First. The tooth curves resulting from smaller describing circles may be

employed. These will give teeth which are more rounding and narrower at their tops, and therefore not as desirable as the regular forms.

Second. The tips of the teeth may be rounded until they clear. This is a cut-and-try method which aims at modifying the teeth to such outlines as smaller describing circles would give.

Third. One of the describing circles may be omitted and one only used, which may be equal to the difference between the pitch-circles. This will permit the meshing of gears differing by six teeth. It will usually prove inexpedient to put wheels in inside gears that differ by much less than 12 teeth.

If a regular diametral pitch and standard tooth forms are determined on, the diameter to which the internal gear-blank is to be bored is calculated by subtracting 2 from the number of teeth, and dividing the remainder by the

diametral pitch.

The tooth outlines are the match of a spur-gear of the same number of teeth and diametral pitch, so that the spur gear will fit the internal gear as a punch fits its die, except that the teeth of each should fail to bottom in the tooth spaces of the other by the customary clearance of one tenth the thickness of the tooth.

Internal gearing is particularly valuable when employed in differential action. This is a mechanical movement in which one of the wheels is mounted on a crank so that its centre can move in a circle about the centre of the other wheel. Means are added to the device which restrain the wheel on the crank from turning over and confine it to the revolution of the crank.

The ratio of the number of teeth in the revolving wheel compared with the difference between the two will represent the ratio between the revolving wheel and the crank-shaft by which the other is carried. The advantage in accomplishing the change of speed with such an arrangement, as compared with ordinary spur-gearing, lies in the almost entire absence of

friction and consequent wear of the teeth.

But for the limitation that the difference between the wheels must not be too small, the possible ratio of speed might be increased almost indefinitely, and one pair of differential gears made to do the service of a whole train of wheels. If the problem is properly worked out with bevel-gears this limitation may be completely set aside, and external and internal bevel-gears, differing by but a single tooth if need be, made to mesh perfectly with each

Differential bevel-gears have been used with advantage in mowing-machines. A description of their construction and operation is given by Mr.

Balch in the article from which the above extracts are taken.

EFFICIENCY OF GEARING.

An extensive series of experiments on the efficiency of gearing, chiefly worm and spiral gearing, is described by Wilfred Lewis in Trans. A. S. M. E., vii. 273. The average results are shown in a diagram, from which the following approximate average figures are taken :

EFFICIENCY OF SPUR. SPIRAL, AND WORM GRARING.

Gearing.	Pitch.	Velocity at Pitch line in feet per min.						
dom mg.		8	10	40	100	200		
Spur pinion	45° 80 20 15 10 7	.90 .81 .75 .67 .61 .51 .48	.935 .87 .815 .75 .70 .615 .58	.97 .93 .89 .845 .805 .74 .72	.98 .955 .93 .90 .87 .82 .765	.985 .965 .945 .93 .90 .86 .815		

The experiments showed the advantage of spur-gearing over all other kinds in both durability and efficiency. The variation from the mean results rarely exceeded 5% in either direction, so long as no cutting occurred, but the variation became much greater and very irregular as soon as cutting began. The loss of power varies with the speed, the pressure, the temperature, and the condition of the surfaces. The excessive friction of worm and spiral gearing is largely due to thee nd thrust on the collars of the shaft. This may be considerably reduced by roller-bearings for the collars.

When two worms with opposite spirals run in two spiral worm-gears that also work with each other, and the pressure on one gear is opposite that on the other, there is no thrust on the shaft. Even with light loads a worm will begin to heat and cut if run at too high a speed, the limit for safe working being a velocity of the rubbing surfaces of 200 to 300 ft, per minute, the former being preferable where the gearing has to work continuously. The wheel teeth will keep cool, as they form part of a casting having a large radiating surface; but the worm itself is so small that its heat is dissipated slowly. Whenever the heat generated increases faster than it can be conducted and radiated away, the cutting of the worm may be expected to begin. A low efficiency for a worm-gear means more than the loss of power, since the power which is lost reappears as heat and may cause the rapid destruction of the worm.

Unwin (Elements of Machine Deshin, p. 294) says: The efficiency is greater the less the radius of the worm. Generally the radius of the worm = 1.5 to 8 times the pitch of the thread of the worm or the circular pitch of the worm-wheel. For a one-threaded worm the efficiency is only 2.5 to 4; for a two-threaded worm, 4/7 to 2.5; for a three-threaded worm, 36 to 3.6 Since so much work is wasted in friction it is not surprising that the wear is excessive. The following table gives the calculated efficiencies of worm-wheels of 1, 2, 3, and 4 threads and ratios of radius of worm to pitch of teeth of from 1 to 6, assuming a coefficient of friction of 6.15:

No. of	Radius of Worm + Pibch.											
Threads.	1	11/4	11/6	13/4	Ž	21/4	8	4	6			
1 2 3 4	.50 67 75 .80	.44 .62 .70 .76	.40 .57 .67 .73	.36 .53 .63 .70	.33 .50 .60 .67	.28 .44 .55 .62	.25 .40 .50	.20 .33 .43 .50	14,033.4			

STRENGTH OF GEAR-TRETH.

The strength of gear-teeth and the horse-power that may be transmitted by them depend upon so many variable and uncertain factors that it is not surprising that the formulas and rules given by different writers show a wide variation. In 1879 John H. Cooper (Jour. Frank. Inst., July, 1879) found that there were then in existence about 48 well-established rules for horse-power and working strength, differing from each other in extreme cases about 500%. In 1886 Prof. Wm. Harkness (Proc. A. A. A. S. 1886), from an examination of the bibliography of the subject, beginning in 1796, found that according to the constants and formulæ used by various authors there were differences of 15 to 1 in the power which could be transmitted by a given pair of geared wheels. The various elements which enter into the constitution of a formula to represent the working strength of a toothed wheel are the following: 1. The strength of the metal, usually cast fron, which is an extremely variable quantity. 2. The shape of the tooth, and especially the relation of its thickness at the root or point of least strength to the pitch and to the length. 3. The point at which the load is taken to be applied, assumed by some authors to be at the pitch-line, by others at the extreme end, along the whole face, and by still others at a single outer corner. 4. The consideration of whether the total load is at any time received by a single tooth or whether it is divided between two teeth. 5. The influence of velocity in causing a tendency to break the teeth by shock. 6. The factor of asfety assumed to bover all the uncertainties of the other elements of the problem.

Prof. Harkness, as a result of his investigation, found that all the formulæ on the subject might be expressed in one of three forms, viz.:

Horse-power =
$$CVpf$$
, or CVp^2 , or CVp^2f ;

in which C is a coefficient, V= velocity of pitch-line in feet per second, p= pitch in inches, and f= face of tooth in inches.

From an examination of precedents he proposed the following formula

for cast-iron wheels:

$$H.P. = \frac{0.910Vpf}{\sqrt{1+0.65}V}.$$

He found that the teeth of chronometer and watch movements were subject to stresses four times as great as those which any engineer would dare

to use in like proportion upon cast-fron wheels of large size.

It appears that all of the earlier rules for the strength of teeth neglected the consideration of the variations in their form; the breaking strength, as said by Mr. Cooper, being based upon the thickness of the teeth at the pitch-line or circle, as if the thickness at the root of the tooth were the same in all cases as it is at the pitch-line.

Willied Lovis (1992 First Club, Phile Lov 1992 Av. Mach. Lune 29)

Wilfred Lewis (Proc. Eng'rs Club, Phila., Jan. 1893; Am. Mach., June 22, 1898) seems to have been the first to use the form of the tooth in the construction of a working formula and table. He assumes that in well-con-structed machinery the load can be more properly taken as well distributed across the tooth than as concentrated in one corner, but that it cannot be safely taken as concentrated at a maximum distance from the root less than the extreme end of the tooth. He assumes that the whole load is taken upon one tooth, and considers the tooth as a beam loaded at one end, and from a series of drawings of teeth of the involute, cycloidal, and radial flank systems, determines the point of weakest cross-section of each, and the ratio of the thickness at that section to the pitch. He thereby obtains the general formula,

$$W = spfy;$$

in which W is the load transmitted by the teeth, in pounds; s is the safe working stress of the material, taken at 8000 lbs. for east iron, when the working speed is 100 ft. or less per minute; $p=\operatorname{pltch}; f=\operatorname{face}$, in inches; y=a factor depending on the form of the tooth, whose value for different cases is given in the following table:

NT - 4	Factor	for Streng	th, y.	37	Factor	Factor for Strength, y.				
No. of Teeth.	Involute 20° Obliquity.	Involute 15° and Cycloidal	Radial Flanks.	No. of Teeth.	Involute 20° Obliquity.	Involute 15° and Cycloidal	Radial Flanks.			
12	.078	.067	.052	27	.111	.100	.064			
13	.083	.070	.053	30	.114	102	.065			
14	.088	.072	.054	84	.118	.104	.066			
15	.092	.075	.055	8 8	.122	.107	.067			
16	.094	.077	.056	- 48	126	.110	.068			
17	.096	.080	.057	50	780	.112	.069			
18	.098	.083	.058	60	184	.114	.070			
19	.100	.087	.059	75	.138	.116	.071			
20	.102	.090	.060	100	.142	.118	.072			
21	.104	.092	.061	150	146	.120	.078			
28	.106	.094	.062	300	.150	122	.074			
25	.108	.097	.068	Rack.	.154	.194	.075			

SAFE WORKING STRESS, s, FOR DIFFERENT SPEEDS.

Speed of Teeth in ft. per minute.	100 or less.	200	800	600	900	1200	1800	2400
Cast iron	8000 20000	6000 15000		4000 10000	8000 7500	2400 6000	2000 5000	1700 4500

The values of s in the above table are given by Mr. Lewis tentatively, in the absence of sufficient data upon which to base more definite values, but



the absence of sufficient data upon which to base more definite values, but they have been found to give satisfactory results in practice.

Mr. Lewis gives the following example to illustrate the use of the tables: Let it be required to find the working strength of a 12-toothed pinion of 1 inch pitch, 2% inch face, driving a wheel of 60 teeth at 100 feet or less perminute, and let the teeth be of the 20-degree involute form. In the formula W = spfy we have for a cast-iron pinion s = 8000, pf = 2.5, and y = .078; and multiplying these values together, we have W = 1560 pounds. For the wheel we have y = .134 and y = .2680 pounds. The cast-iron pinion is, therefore, the measure of strength; but if a steel pinion be substituted we have s = .20,000 and s = .20,000 and it therefore becomes the measure of strength; but if a steel pinion be substituted we have s = .20,000 and s = .20,000 and it therefore becomes the measure of strength.

the wheel is the weaker, and it therefore becomes the measure of strength.

For bevel-wheels Mr. Lewis gives the following, referring to Fig. 168: $D = \text{large diameter of bevel; } a = \text{small diameter of bevel; } p = \text{pitch at large diameter; } n = \text{actual number of teeth; } f = \text{face of beve.; } N = \text{formative number of teeth} = n \times \text{secant } a, \text{ if the number or orresponding to radius } R; y = \text{factor depending upon shape of teeth and formative number } N; W = \text{working load on teeth.}$

$$W = spfy \frac{D^2 - d^2}{3D^2(D - d)};$$
 or, more simply, $W = spfy \frac{d}{D}$,

which gives almost identical results when d is not less than $\frac{3}{4}D$, as is the case in good practice.

In Am. Mach., June 22, 1893, Mr. Lewis gives the following formulæ for the working strength of the three systems of gearing, which agree very closely with those obtained by use of the table:

For involute, 20° obliquity,
$$W = spf\left(.154 - \frac{.912}{n}\right);$$

For involute 15°, and cyc'oidal, $W = spf\left(.124 - \frac{.684}{n}\right);$
For radial flank system, $W = spf\left(.075 - \frac{.276}{7}\right);$

in which the factor within the parenthesis corresponds to y in the general formula. For the horse-power transmitted, Mr. Lewis's general formula $W = spfy_v = \frac{83,000 \text{ H.P.}}{v}$, may take the form H.P. $= \frac{spfy_v}{33,000}$, in which v =velocity in feet per minute; or since $v = d\pi \times \text{rpm.} + 12 = .2618d \times \text{rpm.}$, in which d = diameter in inches and rpm. = revolutions per minute

H.P. =
$$\frac{Wv}{88.000} = \frac{spfy \times d \times rpm}{126.050} = .000007933dspfy \times rpm$$
.

It must be borne in mind, however, that in the case of machines which consume power intermittently, such as punching and shearing machines, the gearing should be designed with reference to the maximum load W, which can be brought upon the teeth at any time, and not upon the average horse-power transmitted

Take an average case in which the safe working strength of the material, s=6000, v=200 ft. per min., and y=.100, the value in Mr. Lewis's table for an involute tooth of 15° obliquity, or a cycloidal tooth, the number of teeth in the wheel being 27.

H.P. =
$$\frac{spf/v}{88,000} = \frac{6000pfv \times .100}{38,000} = \frac{pfv}{55} = 1.091pfV_{\bullet}$$

if
$$V$$
 is taken in feet per second.
Prof. Harkness gives H.P. = $\frac{0.910Vpf}{\sqrt{1+0.65V}}$. If the V in the denominaton

be taken at 200 $\omega = 3\%$ feet per second, $\sqrt{1 + 0.05V} = \sqrt{3.167} = 1.78$, and H.P. $=\frac{.910}{1.78}Vpf=.571pfV$, or about 52% of the result given by Mr. Lewis's formula. This is probably as close an agreement as can be expected, since Prof. Harkness derived his formula from an investigation of ancient precedents and rule-of-thumb practice, largely with common cast gears, while Mr. Lewis's formula was derived from considerations of modern practice

with machine-moulded and cut gears.

Mr. Lewis takes into consideration the reduction in working strength of a tooth due to increase in velocity by the figures in his table of the values of the safe working stress s for different speeds. Prof. Harkness gives expression to the same reduction by means of the denominator of his formula,

 $\sqrt{1+0.65}V$. The decrease in strength as computed by this formula is somewhat less than that given in Mr. Lewis's table, and as the figures given in the table are not based on accurate data, a mean between the values given by the formula and the table is probably as near to the true values given by the formula and the table is probably as near to the true value as may be obtained from our present knowledge. The following table gives the values for different speeds according to Mr. Lewis's table and Prof. Harkness's formula, taking for a basis a working stress s, for cast-iron 8000, and for steel 20,000 lbs. at speeds of 100 ft. per minute and less:

v = speed of teeth, ft. per min. $V = $ "ft. per sec		200 81/8	800 5	600 10	900 15	1200 20	1800 80	2400 40
bafe stress s , cast-iron, Lewis Relative do., $s \rightarrow 8000$	8000	6000 .75	4800 .6		8000 .875		2000 .25	1700 .2125
Relative val. $c + .698$	1	.811	.700	.526	.439	.885	.818	.277
$s_1 = 8000 \times (c + .698)$ Mean of s and s_1 , cast-iron = s_2 . for steel = s_3 .	8000		5200	4100	8300	2700	2800	2000
Safe stress for steel, Lewis	20000	15000	12000	10000	7500			

Comparing the two formulæ for the case of s = 8000, corresponding to a speed of 100 ft. per min., we have

Harkness: H.P. = $1 + \sqrt{1 + 0.65V} \times .910Vpf = .695 \times .91 \times 1\%pf = 1.051pf$

Lewis: H.P. =
$$\frac{spfyv}{83,000} = \frac{spfyv}{550} = \frac{8000 \times 196 pfy}{550} = 24.24 pfy$$
,

in which y varies according to the shape and number of the teeth.

For radial-flank gear with 12 teeth y = .052; 24.24pfy = 1.260pf; For 20° involute, 300 teeth or 15° inv., 27 teeth y = .100; 24.24p/y = 2.424p/y. For 20° involute, 300 teeth y = .150; 24.24p/y = 3.686pf.

Thus the weakest-shaped tooth, according to Mr. Lewis, will transmit 20 per cent more horse-power than is given by Prof. Harkness's formula, in which the shape of the tooth is not considered, and the average-shaped tooth, according to Mr. Lewis, will transmit more than double the horse power given by Prof. Harkness's formula.

Comparison of Other Formulæ.—Mr. Cooper, in summing up his examination, selected an old English rule, which Mr. Lewis considers as

his examination, selected an old English rule, which Mr. Lewis considers as a passably correct expression of good general averages, viz.: X = 2000pt. X = breaking load of tooth in pounds, <math>p = pitch, f = face. If a factor of safety of 10 be taken, this would give for safe working load W = 200pf. George B. Grant, in his Teeth of Gears, page 33. takes the breaking load at 3500pf, and, with a factor of safety of 10, gives W = 350pf. Nystrom's Pocket-Book, 20th ed., 1891, says: "The strength and durability of cast-iron teeth require that they shall transmit a force of 80 lbs. per inch of pitch and per inch breadth of face." This is equivalent to W = 80pf, or only 40% of that given by the English rule.

F. A. Halsey (Clark's Pocket Book) gives a table calculated from the formula

H. P. = pfd × rpm. + 850.

These formula transformed give W = 128pf and W = 218pf respectively.

These formulæ transformed give W = 128pf and W = 218pf, respectively.

Unwin, on the assumption that the load acts on the corners of the teeth, derives a formula $p=K\sqrt{W}$, in which K is a coefficient derived from existing wheels, its values being: for slowly moving gearing not subject to much vibration or shock K=.04; in ordinary mill-gearing, running at greater speed and subject to considerable vibration, K=.06; and in wheels Breads spoon and studies to considerable violation, $\Lambda=00$; and in whether subjected to excessive vibration and shock, and in mortise gearing, K=00. Reduced to the form W=Cpf, assuming that f=2p, these values of K give W=202pf, 200pf, 200pf, and 13pf, respectively.

Unwin also gives the following formula, based on the assumption that the

pressure is distributed along the edge of the tooth: $p = K_{1A} / \frac{p}{2} \sqrt{W}$,

where K_1 = about .0707 for iron wheels and .0848 for mortise wheels when the breadth of face is not less than twice the pitch. For the case of f=2p and the given values of K_1 this reduces to W=200pf and W=130pf, respectively.

Box, in his Treatise on Mill Gearing, gives H.P. = $\frac{12p^2f\sqrt{dn}}{1000}$, in which n = number of revolutions per minute. This formula differs from the more modern formulæ in making the H.P. vary as p^2f , instead of as pf, and in this respect it is no doubt incorrect.

Making the H.P. vary as $\sqrt[4]{dn}$ or as $\sqrt[4]{v}$, instead of directly as v, makes the velocity a factor of the working strength as in the Harkness and Lewis formulæ, the relative strength varying as $\frac{1}{v}$, or as $\frac{1}{\sqrt{v}}$, which for different

velocities is as follows: Speed of teeth in ft. per min., v = 100 200 800 600 900 1200 Relative strength = 1 .707 .574 .408 .333 .289 .236 .204

Showing a somewhat more rapid reduction than is given by Mr. Lewis. For the purpose of comparing different formulæ they may in general be reduced to either of the following forms:

$$H.P. = Cpfv$$
, $H.P. = C_1pfd \times rpm$., $W = cpf$,

in which p = pitch, f = face, d = diameter, all in inches; v = velocity in feet per minute, rpm, revolutions per minute, and C_0 , C_1 and c coefficients. The formulæ for transformation are as follows:

$$H.P. = \frac{Wv}{33000} = \frac{W \times d \times rpm.}{126,050};$$

$$W = \frac{33,000 \text{ H.P.}}{v} = \frac{126,050 \text{ H.P.}}{d \times rpm.} = 33,000 Cpf; pf = \frac{\text{H.P.}}{Cv} = \frac{\text{H.P.}}{C_1 d \times rpm.} = \frac{W}{e}.$$

$$C_1 = .2618C; \quad c = 33,000C; \quad C = 3.82C_1, = \frac{c}{23,000}; \quad c = 126,050C_1.$$

In the Lewis formula C varies with the form of the tooth and with the speed, and is equal to sy + 38,000, in which y and s are the values taken from the table, and c = sy.

In the Harkness formula C varies with the speed and is equal to $\frac{1}{4(1+0.65)^7}$

(V being in feet per second), =
$$\frac{.01517}{\sqrt{1+.011v}}$$

In the Box formula C varies with the pitch and also with the velocity. and equals $\frac{12p \sqrt{d \times rpm.}}{1000v} = .02845 \frac{p}{\sqrt{v}}$. $c = 38,0000 = .774 \frac{p}{\sqrt{v}}$

For v=100 ft. per min. C=77.4p; for v=600 ft. per minute c=31.6p. In the other formulæ considered C, C_1 , and c are constants. Reducing the several formulæ to the form W=cpf, we have the following:

COMPARISON OF DIFFERENT FORK LE FOR STRENGTH OF GEAR-TEETH.

Safe working pressure per inch pitch and per inch of face, or value of c in rmula W = cpf:

	v = 100 ft.	v = 600 ft.
والمقاومة والأوالين المراسطين	per min.	per min.
wis: Weak form of tooth, radial flank, 12 teeth.	c = 436	208 400
Medium tooth, inv, 15°, or cycloid, 27 teeth	c = 800	400
Strong form of tooth, inv. 20°, 300 teeth		600 184
arkness: Average tooth		
x: Tooth of 1 inch pitch		\$1.6
" " 8 inches pitch	$\dots c = 282$	95

Various, in which c is independent of form and speed: Old English the, c=200; Grant, c=350; Nystrom, c=80; Halsey, c=128; Jones & aughlins, c=218; Unwin, c=262, 200, or 139, according to speed, shock, id vibration.

The value given by Nystrom and those given by Box for teeth of small that are so much smaller than those given by the other authorities that they ay be rejected as having an entirely unnecessary surplus of strength. The dues given by Mr. Lewis seem to rest on the most logical basis, the form of tues given by in. Lewis seem to test on the most operations, the form of the test has well as the velocity being considered; and since they are said to ave proven satisfactory in an extended machine practice, they may be condered reliable for gears that are so well made that the pressure bears ong the face of the teeth instead of upon the corners. For rough ordinary work the old English rule W = 200pt is probably as good as any, expet that the figure 200 may be too high for weak forms of tooth and for igh speeds.

The formula W = 200pf is equivalent to H.P. $= \frac{pfd \times rpm}{630} = \frac{pfv}{165}$, or

I.P. = $.0015873pfd \times \text{rpm.} = .006063pfv.$ Maximum Specii of Gearing.—A. Towler, $Eng^{\dagger}g$, April 19, 1889, 388, gives the maximum speeds at which it was possible under favorable onditions to run toothed gearing safely as follows:

									Ft.	per min.
Ordinary	cast	-iron	wheel	s			 			. 1800
Helical	**	**	**				 			. 2400
Mortise	**	66	**				 			2400
Mortise Ordinary	cast	steel	wheel	S			 			2600
Helical	••	**	**				 			3000
Special c	est_i	on m	achin	e-cut	wheels	4		44,000		3000

Prof. Coleman Sellers (Stevens Indicator, April, 1892) recommends that earing be not run over 1200 ft. per minute, to avoid great noise. The 7alker Company, Cleveland, O., say that 2200 ft. per min. for iron gears and 300 ft. for wood and iron (mortise gears) are excessive, and should be roided if possible. The Corliss engine at the Philadelphia Exhibition (1876) and a fly-wheel 30 ft. in diameter running 33 rpm. geared into a pinion 12 ft. igm. The speed of the pitch-line was 3300 ft. per min.

A Heavy Machine-cut Spur-gear was made in 1891 by the 7aiker Company, Cleveland, O., for a diamond mine in South Africa, with mensions as follows: Number of feeth, 192; pitch and the property of the pitch of the segments of the hill by the faiker Company, Cleveland, O., for a diamond mine in South Africa, with mensions as follows: Number of feeth, 192; pitch, 67; bore, 27"; diameter of hub, 97.2"; weight of nub, 15 tons; and teal weight of gear, 663 tons. The rim was made in 12 segments, being fastened with two bolts each. The spokes were bolted the middle of the segments and to the hub with four bolts in each end. The segments being fastened with two bolts each. The spokes were botted the middle of the segments and to the hub with four bolts in each end. The middle of the segments and to the hub with four bolts in each end the segments which are pressed together. They may be used where the power be transmitted is not very great; when the speed is so high that toothed heels would be noisy; when the shafts require to be frequiently put into do out of gear or to have their relative direction of motion reversed; or hen it is desired to change the velocity-ratio while the machinery is in moon, as in the case of disk friction-wheels for changing the feed in machine ols. ols.

ois. Let $P \doteq$ the normal pressure in pounds at the line of contact by which to wheels are pressed together. T = tangential resistance of the driven heel at the line of contact, f = the coefficient of friction, $V \doteq$ the velocity the pitch-surface in feet per second, and H.P. \rightleftharpoons horse-power; then may be equal to or less than fP; H.P. \rightleftharpoons $TV \rightarrow$ 500. The value of f for

metal on metal may be taken at .15 to .20; for wood on metal, .25 to .30; and for wood on compressed paper, 20. The tangential driving force T may be as high as 80 lbs. per inch width of face of the driving surface, but this is ac-

as high as on the per incident with of face of the driving surface, and this is accompanied by great pressure and friction on the journal-hearings. In frictional grooved gearing circumferential wedge-shaped grooves are cut in the faces of two wheels in contact. If P = the force pressing the wheels together, and N = the normal pressure on all the grooves, P = N (sin $a + f \cos a$), in which 2a = the inclination of the sides of the grooves, and the maximum tangential available force T = fN. The inclination of the sides of the grooves to a plane at right angles to the axis is usually 30°.

Frictional Grooved Gearing.—A set of friction-gears for transmitting 150 H.P. is on a steam-dreige described in Proc. Inst. M. E., July, 1888. Two grooved pinions of 54 in. diam., with 9 grooves of 1% in. pitch and angle of 40° cut on their face, are geared into two wheels of 1274 in diam. smilarly grooved. The wheels can be thrown in and out of gear by levers operating eccentric bushes on the large wheel shaft. The circumferential speed of the wheels is about 500 ft. per min. Allowing for engine-friction, if half the power is transmitted through each set of gears the tangential force at the rims is about 3960 lbs. requiring, if the angle is 40° and the coefficient of friction 0.18, a pressure of 7524 lbs. between the wheels and pinion to prevent slipping.

The wear of the wheels proving excessive, the gears were replaced by spurgear wheels and brake-wheels with steel brake-bands, which arrangement has proven more durable than the grooved wheels. Mr. Daniel Adamson states that if the frictional wheels had been run at a higher speed the results would have been better, and says they should run at least 30 ft. per second.

HOISTING AND CONVEYING.

Approximate Weight and Strength of Cordage. (Boston and Lockport Block Co.)—See also pages 339 to 345.

Size in Circum- ference.	Size in Diam- eter.	Weight of 100 ft. Manila, in lbs.	Strength of Manila Rope, in lbs.		Size in Diam- eter.	Weight of 100 ft. Manila, in lbs.	Strength of Manila Rope, in lbs.
inch. 2 2 4 2 4 2 4 3 4 3 4 4 4 4 4	inch. 56 58 13/16 78 1 1/16 11/6 11/6 11/6 11/6 11/6 11/6 11	13 16 20 24 28 33 38 45 51	4,000 5,000 6,250 7,500 9,000 10,500 12,250 14,000 16,000 18,062 20,250	inch. 43/4 5 5 6 6 6 7 7 6 8 6 9 9	inch. 1 9/16 156 154 2 214 214 214 215 258 278 378	72 80 97 113 133 158 164 211 236 262	22,500 25,000 30,250 86,000 42,250 49,000 56,250 64,000 72,250 81,000

Working Strength of Blocks. (B. & L. Block Co.)

Regular Mortise-blocks Single and Wide Mortise and Extra Heavy Double, or Two Double Iron-Single and Double, or Two Double. strapped Blocks, will hoist about-Iron-strapped Blocks, will hoist about_

inch.	lbs.	inch.	lbs.
۴	250	8	2,000
6	350	10	6,000
7	600	12	12,000
8	1,200	14	24,000
9	2,000	16	86,000
10	4,000	18	50,000
12	10,000	20	90,000
14	16,000		,

Where a double and triple block are used together, a certain extra proportioned amount of weight can be safely hoisted, as larger hooks are used.

Comparative Efficiency in Chain-blocks both in Hoisting and Lowering.

(Tests by Prof. R. H. Thurston, Hoisting, March, 1892.)

~		Work of Hoisting. Load of 2000 lbs.				Work of Lowering. Load of 2000 lbs., lowered 7 ft. in each case.						
-¥.	ű	cy,	.		Exclusi	ive of Fa	ctor of '	Time.	Inclusive of Time.			
Number of Block.	Waste by Friction per cent.	Actual Efficiency per cent.	Relative Effi- ciency.	Velocity-ratio	Pull on Hand Chain, lbs.	Length of Hand Chain, feet.	Work performed, ftlbs.	Relative Force expended by Operator.	Time in Min.	Relative Efficiency.		
1 2 8 4 5 6 7 8	20.50 68.00 69.00 71.20 73.96 75.66 77.00 81.03	81.00 28.80 26.04 24.84 23.00	.40 .39 .36 .33 .31	32.50 62.44 30 00 28 00 48.00 53.00 44.30 61.00	92.30 92.60 73.30 56.60 55.00	227. 436. 196. 168. 17.5 370. 810. 426.	1,816 6,104 18,090 15,556 1,282 20,942 17,050 20,000	1.00 3.33 10.00 8 60 0.71 11.60 9 40 11 60	1 20 1.50 2.50 2 80 1.80 2.75	1.000 .186 .050 .035 .380 .036 .029 .018		

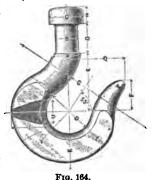
No. 1 was Weston's triplex block; No. 3, Weston's differential; No. 4, Weston's imported. The others were from different makers, whose names

are not given. All the blocks were of one-ton capacity. **Proportions of Hooks.**—The following formulæ are given by Henry R. Towne, in his Treatise on Cranes, as a result of an extensive experimental and mathematical investi-

gation. They apply to hooks of capacities from 250 lbs. to 20,000 lbs. Each size of hook is made from some commercial size of round irou. The basis in each case is, therefore, the size of iron of which the hook is to be made, indicated the size of the diagram. The dimension D by A in the diagram. The dimension D is arbitrarily assumed. The other dimensions, as given by the formulæ, are those which, while preserving a proper bearing-face on the interior of the hook for the ropes or chains which may be passed through it, give the greatest resistance to spreading and to ultimate rupture, which the amount of material in the original bar admits of. The symbol Δ is used to indicate the nominal capacity of the hook in tons of 2000 lbs. The formulæ which determine the lines of the other parts of the hooks of the several sizes are as follows, the measure-ments being all expressed in inches:

several sizes are as follows, the measurments being all expressed in inches:

$$D=.5$$
 $\Delta+1.25$ $G=.75D$.
 $E=.64$ $\Delta+1.60$ $O=.863$ $\Delta+.66$
 $F=.83$ $\Delta+.85$ $Q=.64$ $\Delta+1.60$



H = 1.08AL = 1.05AI = 1.83A $\widetilde{M} =$.50A

.85B - .16

N =

U =.866A

The dimensions A are necessarily based upon the ordinary merchant sizes of round iron. The sizes which it has been found best to select are the following:

 $\bar{J} = 1.20A$

K = 1.13A

Capacity of hook: 136 10 tons. Dimension A: 1 1/16 11/4 11/16 8¼ in.

Experiment has shown that hooks made according to the above formula will give way first by opening of the jaw, which, however, will not occur except with a load much in excess of the nominal capacity of the hook. This yielding of the hook when overloaded becomes a source of safety, as it constitutes a signal of danger which cannot easily be overlooked, and which must proceed to a considerable length before rupture will occur and the load be dropped.

POWER OF HOISTING-ENGINES.

Horse-power required to raise a Load at a Given Speed. – H.P. = Gross weight in its × speed in ft. per min. To this add 33,000

25% to 50% for friction, contingencies, etc. The gross weight includes the weight of cage, rope, etc. In a shaft with two cages balancing each other use the net load + weight of one rope, instead of the gross weight To find the load which a given pair of engines will start.—Let A= area of cylinder in square inches, or total area of both cylinders, if there are two: P= mean effective pressure in cylinder in lbs. per sq. in.; S= stroke of cylinder in inches; C= circumference of hoisting-drum in inches; L= load lifted by hoisting-rope in lbs.; F= friction, expressed as a diminution of $\frac{APS}{APS}$ the load. Then $L = \frac{AP2S}{C} - F$

An example in Colly Engr., July, 1891, is a pair of hoisting-engines $24'' \times 40''$, drum 12 ft. diam., average steam-pre-sure in cylinder = 59.5 lbs.; A = 904.8; P = 59.5; S = 40; C = 452.4. Theoretical load not allowing for friction, AP2S + C = 9589 lbs. The actual load that could just be lifted on trial was 7988 lbs., making friction loss F = 1601 lbs., or 20 + per cent of the actual loadlifted, or 163% of the theoretical load.

The above rule takes no account of the resistance due to inertia of the load, but for all ordinary cases in which the acceleration of speed of the load, but for all ordinary cases in the allowance for friction, etc. The resistance due to inertia is equal to the force required to give the load the velocity acquired in a given time, or, as shown in Mechanics, equal to the

product of the mass by the acceleration, or $R = \frac{WV}{\phi T}$, in which R = resistance in lbs. due to inertia; W = weight of load in lbs.; V = maximum yeloc. ity in feet per second; T = time in seconds taken to acquire the velocity V;

Effect of Slack Rope upon Strain in Hoisting.—A series of tests with a dynamometer are published by the Trenton Iron Co., which show that a dangerous extra strain may be caused by a few inches of slack rope In one case the cage and full tubs weighed 11,300 lbs.; the strain when the load was lifted gently was 11,525 lbs.; with 3 in. of slack chain it was 19,025 lbs., with 6 in. slack 25,750 lbs., and with 9 in. slack 27,950 lbs.

19,025 lbs., with 6 in. slack 25,750 lbs., and with 6 in. slack 27,000 lbs.

Limit of Depth for Hoisting. Taking the weight of a cast-steel hoisting-rope of 1½ inches diameter at 2 lbs. per running foot, and its breaking strength at 84,000 lbs., it should, theoretically, sustain itself until 42,000 feet long before breaking from its own weight. But taking the usual factor of safety of 7, then the safe working length of such a rope would be only 8000 feet. If a weight of 8 tong is row, but a rope would be only 6000 feet. If a weight of 3 tons is now hung to the rope, which is equivalent to that of a cage of moderate capacity with its loaded cars, the maximum length at which such a rope could be used, with the factor of safety of 7, is 3000 feet, or

$$2x + 6000 = \frac{84,000}{2}$$
: $x = 8000$ feet.

This limit may be greatly increased by using special steel rope of higher

This limit may be greatly increased by using special steel rope of higher strength, by using a smaller factor of safety, and by using taper ropes. (See paper by H. A. Wheeler, Trans. A. I. M. E., xix. 107.)

Large Holsting Records.—At a colliery in North Derbyshire during the first week in June, 1890, 6309 tons were raised from a depth of 509 yards, the time of winding being from 7 a.m. to 3.30 p.m.

At two other Derbyshire pits, 170 and 140 yards in depth, the speed of winding and changing has been brought to such perfection that tubs are drawn and changed three times in one minute. (Proc. Inst. M. E., 1890.)

At the Nottingham Colliery near Wilkesbarre, Pa., in Oct. 1891, 70,152 tons were shipped in 24.15 days, the average hoist per day being 1818 mine cars. The depth of hoist was 470 feet, and all coal came from one opening. The engines were fast motion, 22 × 48 inches, conical drums 4 feet 1 inch long. The feet diameter at small end and 9 feet at large end. (Eng's News, Nov. 1891.)

Pneumatic Hoisting. (H. A. Wheeler, Trans. A. I. M. E., xix. 107.)—
A pneumatic hoist was installed in 1876 at Epinac, France, consisting of two continuous air-tight iron cylinders extending from the bottom to the top of the shaft. Within the cylinder moved a piston from which was hung the cage. It was operated by exhausting the air from above the piston, the lower side being open to the atmosphere. Its use vas discontinued on account of the failure of the mine. Mr. Wheeler gives a description of the system, but criticises it as not being equal on the whole to hoisting by steel ropes. Pneumatic hoisting-cylinders using compressed air have been used at blast-furnaces, the weighted piston counterbalancing the weight of the cage, and the two being connected by a wire rope passing over a pulley-sheave above the top of the cylinder. In the more modern furnaces steam-engine hoists are generally used.

Counterbalancing of Winding-engines. (H. W. Hughes, Co-

Counterbalancing of Winding-engines. (H. W. Hughes, Columbia Coll. Qly.)—Engines running unbalanced are subject to enormous variations in the load; for let W = weight of cage and empty tubs, say 6870 lbs.; c = weight of coal, say 4480 lbs.; r = weight of hoisting rope, say 6000 lbs.; $r' = \text{weight of counterbalance rope hanging down pit, say 6000 lbs. The$ weight to be lifted will be:

If weight of rope is unbalanced.

If weight of rope is balanced.

At beginning of lift:
$$W+c+r-W$$
 or 10,480 lbs. $W+c+r-(W+r')$, At middle of lift: $W+c+\frac{r}{2}-\left(W+\frac{r}{2}\right)$ or 4480 lbs. $W+c+\frac{r}{2}+\frac{r'}{2}-\left(W+\frac{r}{2}+\frac{r'}{2}\right)$. At end of lift: $W+c-(W+r)$ or minus 1520 lbs. $W+c+r'-(W+r)$,

That counterbalancing materially affects the size of winding-engines is shown by a formula given by Mr. Robert Wilson, which is based on the fact that the greatest work a winding-engine has to do is to get a given mass into a certain velocity uniformly accelerated from rest, and to raise a load the distance passed over during the time this velocity is being obtained.

Let W = the weight to be set in motion: one cage, coal, number of empty tubs on cage, one winding rope from pit head-gear to bottom, and one rope from banking level to bottom.

v = greatest velocity attained, uniformly accelerated from rest;

g = gravity = 82.2;

t = time in seconds during which v is obtained;

 \dot{L} = unbalanced load on engine;

R = ratio of diameter of drum and crank circles;
P = average pressure of steam in cylinders;
N = number of cylinders;

S =space passed over by crank-pin during time t;

 $C = \frac{3}{6}$, constant to reduce angular space passed through by crank, to

the distance passed through by the piston during the time t; $\Delta =$ area of one cylinder, without margin for friction. To this an addition for friction, etc., of engine is to be made, varying from 10 to 30% of A.

1st. Where load is balanced.

$$A = \frac{\left\{ \left(\frac{Wv^2}{2g} \right) + \left(L \frac{vt}{2} \right) \right\} R}{PNSC_*}$$

2d. Where load is unbalanced:

The formula is the same, with the addition of another term to allow for the variation in the lengths of the ascending and descending ropes. In this CASO

 h_1 = reduced length of rope in t attached to ascending cage; h_2 = increased length of rope in t attached to descending cage; w = weight of rope per foot in pounds. Then

$$A = \frac{\left[\left(\frac{Wv^2}{2g}\right) + \left\{\left(\frac{vt}{L^2}\right) - \frac{h_1w + h_2w}{2}\right\}\right]R}{PNSC.}$$

Applying the above formula when designing new engines, Mr. Wilson found that 30 inches diameter of cylinders would produce equal results, when balanced, to those of the 36-inch cylinder in use, the latter being unbalanced.

Counterbalancing may be employed in the following methods:

(a) Tapering Rope.—At the initial stage the tapering rope enables us to wind from greater depths than is possible with ropes of uniform section. The thickness of such a rope at any point should only be such as to safely bear the load on it at that point.

With tapering ropes we obtain a smaller difference between the initial and final load, but the difference is still considerable, and for perfect equalization of the load we must rely on some other resource. The theory of taper ropes is to obtain a rope of uniform strength, thinner at the cage end where the weight is least, and thicker at the drum end where it is greatest.

(b) The Counterpoise System consists of a heavy chain working up and down a staple pit, the motion being obtained by means of a special small drum placed on the same axis as the winding drum. It is so arranged that the chain hangs in full length down the staple pit at the commencement of the winding; in the centre of the run the whole of the chain rests on the bottom of the pit, and, finally, at the end of the winding the counterpoise has been rewound upon the small drum, and is in the same condition as it was at the commencement.

(c) Loaded-wagon System.—A plan, formerly much employed, was to have a loaded wagon running on a short incline in place of this heavy chain; the rope actuating this wagon being connected in the same manner as the above to a subsidiary drum. The incline was constructed steep at the commencement, the inclination gradually decreasing to nothing. At the beginning of a wind the wagon was at the top of the incline, and during a portion of the run gradually passed down it till, at the meet of cages, no pull was exerted on the engine—the wagon by this time being at the bottom. In the latter part of the wind the resistance was all against the engine, owing to its having to pull the wagon up the incline, and this resistance increased from nothing at the meet of cages to its greatest quantity at the conclusion of the lift.

(d) The Endless-rope System is preferable to all others, if there is sufficient sump room and the shaft is free from tubes, cross timbers, and other impediments. It consists in placing beneath the cages a tail rope, similar in diameter to the winding rope, and, after conveying this down the pit, it is

attached beneath the other cage.

(e) Flat Ropes Coiling on Reels—This means of winding allows of a certain equalization, for the radius of the coil of tascending rope continues to increase, while that of the descending one continues to diminish. Consequently, as the resistance decreases in the ascending load the leverage increases, and as the power increases in the other, the leverage diminishes. The variation in the leverage is a constant quantity, and is equal to the thickness of the rope where it is wound on the drum.

By the above means a remarkable uniformity in the load may be obtained, the only objection being the use of flat ropes, which weigh heavier

and only last about two thirds the time of round ones.

(f) Conical Drums.—Results analogous to the preceding may be obtained by using round ropes coiling on conical drums, which may either be smooth, with the successive coils lying side by side, or they may be provided with a spiral groove. The objection to these forms is, that perfect equalization is not obtained with the conical drums unless the sides are very steep, and consequently there is great risk of the rope slipping; to obviate this, scroll drums were proposed. They are, however, very expensive, and the lateral displacement of the winding rope from the centre line of pulley becomes

very great, owing to their necessary large width.

(g) The Koepe System of Winding.—An iron pulley with a single circular groove takes the place of the ordinary drum. The winding rope passes from one cage, over its head-gear pulley, round the drum, and, after pass

ing over the other head-gear pulley, is connected with the second cage. The winding rope thus encircles about half the periphery of the drum in the same manner as a driving-belt on an ordinary pull y. There is a balance rope beneath the cages, passing round a pulley in the sump; the arrangement may be likened to an endless rope, the two cages being simply points of attachment.

CRANES.

Classification of Cranes. (Henry R. Towne, Trans. A. S. M. E., iv. 88. Revised in *Hoisting*, published by The Yale & Towne Mfg. Co.)
A Hoist is a machine for raising and lowering weights. A Crane is a

hoist with the added capacity of moving the load in a horizontal or lateral direction.

Cranes are divided into two classes, as to their motions, viz., Rotary and Rectilinear, and into four groups, as to their source of motive power, viz.:

Hand—When operated by manual power.

Power.—When driven by power derived from line shafting.
Steam, Electric. Hydraulic, or Pneumatic.—When driven by an engine or motor attached to the crane, and operated by steam, electricity, water, or air transmitted to the crane from a fixed source of supply.

Locomotive.-When the crane is provided with its own boiler or other generator of power, and is self-propelling; usually being capable of both

rotary and rectilinear motions.

Rotary and Rectilinear Cranes are thus subdivided:

ROTARY CRANES.

(1) Swing-cranes.—Having rotation, but no trolley motion.

(2) Jib-cranes.—Having rotation, and a trolley travelling on the jib.

(8) Column-cranes.—Identical with the jib-cranes, but rotating around a fixed column (which usually supports a floor above).

(4) Pillar-cranes.—Having rotation only; the pillar or column being supported entirely from the foundation.

(5) Pillar Jib-cranes.—Identical with the last, except in having a jib and

(6) Derrick-cranes.-Identical with jib-cranes, except that the head of the mast is held in position by guy-rods, instead of by attachment to a roof or

ceiling.

(7) Walking-cranes.—Consisting of a pillar or jib-crane mounted on wheels and arranged to travel longitudinally upon one or more rails.

(8) Locomotive-cranes.—Consisting of a pillar crane mounted on a truck, and provided with a steam-engine capable of propelling and rotating the crane, and of hoisting and lowering the load.

RECTILINEAR CRANES.

(9) Bridge-cranes.-Having a fixed bridge spanning an opening, and a trolley moving across the bridge.

(10) Tram-cranes.—Consisting of a truck, or short bridge, travelling longitudinally on overhead rails, and without trolley motion.

(11) Travelling-cranes.—Consisting of a bridge moving longitudinally on

overhead tracks, and a trolley moving transversely on the bridge. (12) Gantries.—Consisting of an overhead bridge, carried at each end by a

trestle travelling on longitudinal tracks on the ground, and having a trolley moving transversely on the bridge.

(13) Rotary Bridge-cranes.—Combining rotary and rectilinear movements and consisting of a bridge pivoted at one end to a central pier or post, and supported at the other end on a circular track; provided with a trolley moving transversely on the bridge.

For descriptions of these several forms of cranes see Towne's "Treatise on Cranes."

Stresses in Cranes.—See Stresses in Framed Structures, p. 440, ante. Position of the Inclined Brace in a Jib-crane.—The most economical arrangement is that in which the inclined brace intersects the jib at a distance from the mast equal to four fifths the effective radius of the crane. (Hoisting.)

A Large Travelling-crane, designed and built by the Morgan Engineering Co., Alliance, O., for the 12-inch-gun shop at the Washington Navy Yard, is described in American Machinist, June 12, 1890. Capacity. 150 net tons; distance between centres of inside rails, 59 ft. 6 in.; maxim cross travel, 44 ft. 2 in.; effective lift, 40 ft.; four speeds for main hoist

4, and 8ft. per min.; loads for these speeds, 150, 75, 871/4, and 1884 tons respectively; traversing speeds of trolley on bridge, 25 and 50 ft. per minute; speeds of bridge on main track, 30 and 60 ft. per minute. Square shafts are

employed for driving.

A 150-ton Pillar-crane was erected in 1893 on Finnieston Quay, Glasgow. The jib is formed of two steel tubes, each 39 in. diam. and 90 ft. long. The radius of sweep for heavy lifts is 65 ft. The jib and its load are counterbalanced by a balance-box weighted with 100 tons of iron and steel punchings. In a test a 180-ton load was lifted at the rate of 4 ft. per minute, and a complete revolution made with this load in 5 minutes. Eng'g News,

July 20, 1893.

Compressed-air Travelling-cranes.—Compressed-air overhead travelling-cranes have been built by the Lane & Bodley Co., of Cincinnati. travening-cranes have been built by the Lane & Bodley Co., of Cincinnatt. They are of \$0 tons nominal capacity, each about \$0 ft. span and \$00 ft. length of travel, and are of the triple-motor type, a pair of simple reversing-engines being used for each of the necessary operations, the pair of engines for the bridge and the pair for the trolley travel being each 5-inch bore by 7-inch stroke, while the pair for hoisting is 7-inch bore by 9-inch stroke. Air is furnished by a compressor having steam and air cylinders each 10-in. diam. and 12-in. stroke, which with a boiler-pressure of about \$0 pounds gives an air-pressure when required of somewhat over 100 pounds. The air-compressor is allowed to run continuously without a covernor the speed before recrulated is allowed to run continuously without a governor, the speed being regulated by the resistance of the air in a receiver. From a pipe extending from the receiver along one of the supporting trusses communication is continuously maintained with an auxiliary receiver on each traveller by means of a one inch hose, the object of the auxiliary receiver being to provide a supply of air near the engines for immediate demands and independent of the hose connection, which may thus be of small dimension. Some of the advantages said to be possessed by this type of crane are: simplicity; absence of all moving parts, excepting those required for a particular motion when that motion is in use; no danger from fire, leakage, electric shocks, or freezing; ease of repair; variable speeds and reversal without gearing; almost entire absence of noise; and moderate cost.

Quay-cranes.—An illustrated description of several varieties of stationary and travelling cranes, with results of experiments, is given in a paper on Quay-cranes in the Port of Hamburg by Chas. Nehls, Trans. A. S. C. E., Chicago Meeting, 1893.

Hydraulic Cranes, Accumulators, etc.—See Hydraulic Pressure Transmission, page 616, ante.

Electric Oranes.—Travelling-cranes driven by electric motors have largely supplanted cranes driven by square shafts or flying-ropes. Each of the three motions, viz., longitudinal, traversing and hoisting, is usually accomplished by a separate motor carried upon the crane.

COAL-HANDLING MACHINERY.

The following notes and tables are supplied by the Link-Belt Engineering Co. of Philadelphia, Pa.:
In large boiler-houses coal is usually delivered from hopper-cars into a track-hopper, about 10 feet wide, and 12 to 16 feet long. A feeder set under the track-hopper feeds the coal at a regular rate to a crusher, which reduces it to a size suitable for stokers.

After crushing, the coal is elevated or conveyed to overhead storage-bins.

Overhead storage is preferred for several reasons:

1. To avoid expensive wheeling of coal in case of a breakdown of the

coal-handling machinery.

 To avoid running the coal-handling machinery continuously.
 Coal kept under cover indoors will not freeze in winter and clog the supply-spouts to the boilers.

4. It is often cheaper to store overhead than to use valuable ground-

space adjacent to the boiler-house.

5. As distinguished from vault or outside hopper storage, it is cheaper to build steel bins and supports than masonry pits.

Weight of Overhead Rins.—Steel hins of approximately ractangular cross-section, say 10×10 feet, will weigh, axclusive of supports, about one-sixth as much as the contained coal. Larger bins, with signing bottoms, may weigh one-eighth as much as the contained coal. Bag hottom bins of the Berquist type will weigh about one-twelfth as much as the contained

the Herquist type will weigh about one-twellth as much as the contained coal, not including posts, and about one-ninth as much, including posts.

The supply-pipes from Mins.—The supply-pipes from overhead bing to the boiler-room floor, or to the stoker-hoppers, should not be less than 12 inches in diameter. They should be fitted at the ton with a flanged easting and a cut-off gate, to permit removal of the pipe when the hollers are to be cleaned or repaired.

Types of Coal Elevators.—Coal elevators consist of buckets of various shapes attached to one or more strands of link-belting or chain, or to rubber belting. The buckets may either be attached continuously or at intervals.**

various shapes attached to one or more strands of link-belting or chain, or to rubber belting. The buckets may either be attached continuously or at intervals. The various types are as fallows:

Continuous bucket elevators consist usually of one strand of chain and two sprocket-wheels with buckets attached continuously to the chain. Each bucket after passing the head wheel acts as a chute to direct the flow from the next bucket. This type of elevator will handle the larger sizes of coal. It runs at slow speeds, usually from 90 to 175 feet per minute, and has a maximum capacity of about 120 tons per hour.

Centrifued discharge elevators consist usually of a single strand of chain

Centrifugal discharge elevators consist usually of a single strand of chain, with the buckets attached thereto at intervals. They are used to handle the smaller sizes of coal in small quantities. They run at high speeds, usually 34 to 40 revolutions of the head wheel per minute, and have a

canscity up to 40 tons per hour.

respectly up to 40 tons per hour.

Perfect discharge elevators consist of two strands of chain, with buckets at intervals between them. A pair of idlers set under the head wheels cause the buckets to be completely inverted, and to make a plean delivery into the chutes at the elevator head. This type of elevator is useful in handling material which tends to cling to the buckets. It runs at slow speeds, usually less than 150 feet per minute. The capacity depends on the size of the buckets.

Companying the elevators and Companying are of the following types:

Combined Elevators and Conveyors are of the following types: Combined Elevators and Conveyors are of the following types:
Gravity discharge elevators, consisting of two strands of chain, with spaced
V-shaped buckets fastened between them. After passing the head wheels
the buckets act as conveyor-flights and convey the coal in a trough to
any desired point. This is the cheapest type of combined elevator and
conveyor, and is economical of power. A machine carrying 100 tons of
coal per hour, in buckets 20 inches wide, 10 inches deep, and 24 inches long,
spaced 3 feet apart, requires 5 H.P. when loaded and 1½ H.P. when empty
for each 100 feet of horizontal run, and ½ H.P. for each foot of vertical lift.

Rigid bucket-carriers consist of two strands of chain with a special bucket
rigidly fastened between them. The buckets overlap and are so shaped
that they will carry coal around three sides of a rectangle. The coal is
carried to any desired point and is discharged by completely inverting
the bucket over a turn-wheel.

the bucket over a turn-wheel.

Pivoted bucket-carriers consist of two strands of long pitch steel chain to which are attached, in a pivotal manner, large malleable iron or steel buckets so arranged that their adjacent lips are close together or overlap. Overlapping buckets require special devices for changing the lap at the corner turns. Carriers in which the buckets do not overlap should be fitted with auxiliary pans or buckets, arranged in such a manner as to catch the spill which falls between the lips at the loading point, and so shaped as to return the spill to the buckets at the corner turns. Pivoted bucket carriers will carry coal around four sides of a rectangle, the buckets being dumped on the horizontal run by striking a cam suitably placed. Carriers of this type are economical of power, but are costly and of relatively low capacity.

Coal Conveyors.—Coal conveyor are of four general types, viz., scraper or flight, bucket, screw, and belt conveyors.

The flight conveyor consists of a trough of any desired cross-section and checked and other conveyors.

a single or double strand of chain carrying scrapers or flights of approximately the same shape as the trough. The flights push the coal ahead of them in the trough to any desired point, where it is discharged through openings in the bottom of the trough.

For short, low-capacity conveyors, malleable link hook-joint chains are used. For heavier service, malleable pin-joint chains, steel link chain-

or monobar, are required. For the heaviest service, two strands of steel link chain, usually with rollers, are used.

Flight conveyors are of three types: plain scraper, suspended flight,

and roller flight

and roller flight

In the plain scraper conveyor, the flight is suspended from the chain
and drags along the bottom of the trough. It is of low first cost and is
useful where noise of operation is not objectionable. It has a maximum
capacity of about 30 tons per hour, and requires more power than either
of the other two types of flight conveyors.

Suspended Right conveyors use one or two strands of chain. The flights
are attached to cross-bars having wearing-shoes at each end. These wearing-shoes slide on angle-iron tracks on each side of the conveyor trough. The
flights do not touch the trough at any point. This type of conveyor is
used where quietness of operation is a consideration. It is of higher first
cost than the plain scraper conveyor, but requires one-fourth less power

used where quietness of operation is a consideration. It is of higher first cost than the plain scraper conveyor, but requires one-fourth less power for operation. It is economical up to a capacity of about 80 tons per hour. The roller flight conveyor is similar to the suspended flight, except that the wearing-shoes are replaced by rollers. It is highest in first cost of all the flight conveyors, but has the advantages of low power consumption (one-half that of the scraper), low stress in chain, long life of chain trough, and flights, and noiseless operation. It has an economical maximum capacity of about 120 tons per hour.

The following formula gives approximately the horse-power at the head

The following formula gives approximately the horse-power at the head

wheel required to operate flight conveyors: H.P. = (ATL + BWS) + 1000. T = tons of coal per hour; L = length of conveyor in feet, centre to centre; W = weight of chain, flights, and shoes (both runs) in pounds; S = speed in feet per minute; A and B constants depending on angle of incline from horizontal. See example below.

Values of A and B.

Angle, Deg.	A	В	Angle, Deg.	A	В	Angle, Deg.	A	В
0 2 4 6 8	.343 .378 .40 .44 .47	.01 .01 .01 .01 .01	10 14 18 22 26	.50 .57 .63 .69	.01 .01 .009 .009	30 34 38 42 46	.79 .84 .88 .92 .95	.009 .008 .008 .007 .007

For suspended flight conveyors take B as 0.8, and for roller flights as 0.6, of the values given in the table.

Weight of Chain in Pounds per Foot.

:	Link-	BELT	ING.					Mor	NOBAR.				
Chain	Pit	ch of Incl	Fligh	ıts,	Chain No.*							3.	
No.	12	18	24	36	No.*	12	18	24	36	48	54	72	
78 88 85 103 108 110 114 122 124	2.4 2.8 3.1 4.6 4.9 5.6 6.3 8.1 8.9	2.7 2.8 4.4 4.7 5.2 6.0 7.7	$\frac{2.7}{4.3}$	2.2 2.5 2.6 4.2 4.1 4.7 5.7 7.2 7.9	818 824 1018 1024 1224 1236		3.0 5.7 11.5	3.6 4.9 9.6 14.7	2.8 5.5 10.7	4.7 9.07 14.04		4.6 8.8 13.8 11.34 19.4	

^{*} In monobar the first one or two figures in the number of the chain denote the diameter of the chain in eighths of an inch. The last two figures denote the pitch in inches,

	Pin	Сна	INS.	!			F	COLLER	Снаг	NS.	
No.	Pit	ch of Inc	Flig hes.	hts,	No.	No. Pitch of Flig				s, In	ches.
No.	12	18	24	36		12	18	24	36		
720 730 825	5.9 6.9 9.6		5.4 6.4 9.1	5.3 6.3 8.9	1112 1113 1130	7.7 9.5 10.5	6.9 8.8 9.5	6.2 8.0 9.0	5.7 7.5 7.8		

Weight of Flights with Wearing-shoes and Bolts.

Size, Inches.	Steel.	Malleable Iron.	Suspende	ed Flights.
		Tron.	Size.	Weight, Lbs.
· 4×10 4×12 5×10 5×12 5×15 6×18 8×18 8×20 8×24 10×24	3.5 3.9 4.1 4.6 5.8 8.1 10.1 11.0 12.6 15.2	4.3 4.7 5.2 5.7 5.9 9.2 12.7 13.4 14.4	$\begin{array}{c} 6\times14\\ 8\times19\\ 10\times24\\ 10\times30\\ 10\times36\\ 10\times42\\ \end{array}$	12.37 15.55 25.57 29.37 33.17 34.97

EXAMPLE.—Required the H.P. for a monobar conveyor 200 ft. centre to centre, carrying 100 tons of coal per hour, up a 10° incline at a speed of 100 feet per minute. Conveyor has No. 818 chain and 8×19 suspended flights, spaced 18 inches apart.

H.P. =
$$\frac{.5 \times 100 \times 200 + .008(400 \times 5.7 + 267 \times 15.55) \times 100}{1000} = 15.15.$$

The following table shows the conveying capacities of various sizes of flights at 100 feet per minute in tons of 2000 lbs. per hour. The values are true for continuous feed only.

	F	Iorizontal	Conveyor	rs.	Inclined Conveyors.			
Size of Flight.	Flight Every 16".	Flight Every 18".	Flight Every 24".	Pounds Coal per Flight.	10° Flights Every 24".	20° Flights Every 24".	30° Flights Every 24".	
6×14 8×19 10×24 10×30 10×36 10×42		Tons. 62 130	Tons. 46.5 97.5 172.5 220 268 315	31 65 115 147 179 210	Tons. 40.5 78 150 184 225 264	Tons. 31.5 62 120 146 177 210	Tons. 22.5 52 90 116 142 167	

Bucket Conveyors.—Rigid bucket-carriers are used to convey large quantities of coal over a considerable distance when there is no intermediate point of discharge. These conveyors are made with two strands of steel roller chain. They are built to carry as much as 10 tons of coal per minute.

Screw Conveyors.—Screw conveyors consist of a helical steel flight, either in one piece or in sections, mounted on a pipe or shaft, and running in a steel or wooden trough. These conveyors are made from 4 to 18 inches in diameter, and in sections 8 to 12 feet long. The speed ranges from 20 to 60 revolutions per minute and the capacity from 10 to 30 tons of coal per hour. It is not advisable to use this type of conveyor for coal, as it will only handle the smaller sizes and the flights are very easily dam-

aged by any foreign substance of unusual size or shape.

Belt Conveyors.—Rubber or cotton belt conveyors are used for handling coal, grain, sand, or other finely divided material. They combine a high carrying capacity with low power consumption, but are rela-

tively high in first cost.

In some cases the belt is flat, the material being fed to the belt at it: centre in a narrow stream. In the majority of cases, however, the belt is troughed by means of idler pulleys set at an angle from the horizontal and placed at intervals along the length of the belt. Rubber belts are very often made more flexible for deep troughing by removing some of the layers of cotton from the belt and substituting therefor an extra thickness of rubber.

Belt conveyors may be used for elevating materials up to about 23° incline. On greater inclines the material slides back on the belt and spills. With many substances it is important to feed the belt steadily if the convevor stands at or near the limiting angle. If the flow is interrupted

the material may slide back on the belt.

Belt conveyors are run at any speed from 200 to 800 feet per minute, and are made in widths varying from 12 inches to 60 inches.

Capacity of Belt Conveyors in Tons of Coal per Hour.

Width of		Ve	locity of	Belt, Feet	per Minu	te.	
Belt, Ins.	300	350	400	450	500	550	600
12 14 16 18 20 24 30 36	27 36.7 48 60.7 75 108 168.7 243	31.5 42.8 56 70.8 87.5 126 197 283	36 49 64 81 100 144 225 324	40.5 55.2 72 91.2 112.5 162 253 365	45 61.3 80 101 125 180 281 405	49.5 67.4 88 111 137.5 198 307 446	54 73.6 96 135 150 216 338 486

For materials other than coal, the figures in the above table should be multiplied by the coefficients given in the table below:

Material.	Coefficient.	Material.	Coefficient.
Ashes (damp). Cement. Clay. Coke.	1.76 1.26	Earth	1.8

Carrying-bands or Belts, used for the purpose of sorting coal and removing impurities, are sometimes made of an endless length of woven wire, or of two or three endless chains, carrying steel plates varying in width from 6 inches to 14 inches. (Proc. Inst. M. E., July, 1890.)

Grain-elevators.—American Grain-elevators are described in a paper by E Lee Heidenreich, read at the International Engineering Congress at Chicago (Trans. A. S. C. E., 1893). See also Trans. A. S. M. E., vii, 6500

WIRE-ROPE HAULAGE.

Methods for transporting coal and other products by means of wire rope. though varying from each other in detail, may be grouped in five classes;

J. The Self-acting or Gravity Inclined Plane.

II. The Simple Engine-plane.

III. The Tail-rope System.

IV. The Endless-rope System V. The Cable Tramway.

The following brief description of these systems is abridged from a camphiet on Wire-rope Haulage, by Wm. Hildenbrand, C.E., published by John A. Boebling's Sons Co., Trenton, N. J.

I. The Self-acting Inclined Plane.—The motive power for the self-acting inclined plane is gravity; consequently this mode of transporting coal finds application only in places where the coal is conveyed from a higher to a lower point and where the plane has sufficient grade for the

nigner to a lower point and where the plane has sufficient grade for the loaded descending cars to raise the empty cars to an upper level.

At the head of the plane there is a drum, which is generally constructed of wood, having a diameter of seven to ten feet. It is placed high enough to allow men and cars to pass under it. Loaded cars coming from the pit are either singly or in sets of two or three switched on the track of the plane, and their speed in descending is regulated by a brake on the drum. Supporting rollers, to prevent the rope dragging on the ground, are generally of wood, 5 to 6 inches in diameter and 18 to 24 inches long, with ½- to ½-inch iron axies. The distance between the rollers varies from 15 to 30 feet, steeper planer requiring less rollers than these with easy grades

33 feet, steeper planes requiring less rollers than those with easy grades. Considering only the reduction of friction and what is best for the preservation of rope, a general rule may be given to use rollers of the greatest possible diameter, and to place them as close as economy will permit.

The smallest angle of inclination at which a plane can be made self-acting

will be when the motive and resisting forces balance each other. The motive forces are the weights of the losded car and of the descending rope. The resisting forces consist of the weight of the empty car and ascending rope, of the rolling and axle friction of the cars, and of the axle friction of the supporting rollers. The friction of the drum, stiffness of rope, and resistance of air may be neglected. A general rule cannot be given, because a change in the length of the plann or in the weight of the cars changes the proportion of the forces; also, because the coefficient of friction, depending on the condition of the road, construction of the cars, etc., is a very uncertain factor.

For working a plane with a \$6 inch steel rope and lowering from one to four pit cars weighing empty 1400 lbs. and loaded 4000 lbs., the rise in 100 feet necessary to make the plane self-acting will be from about 5 to 10 feet, decreasing as the number of cars increase, and increasing as the length of plane increases.

A gravity inclined plane should be slightly concave, steeper at the top than at the bottom. The maximum deflection of the curve should be at an inclination of 45 degrees, and diminish for smaller as well as for steeper

The Simple Engine-plane. The name "Engine-plane" is given to a plane on which a load is raised or lowered by means of a single wire rope and stationary steam-engine. It is a cheap and simple method of conveying coal underground, and therefore is applied wherever circumstances permit it.

Under ordinary conditions such as prevail in the Pennsylvania mine region, a train of twenty-five to thirty loaded cars will descend, with reasonable velocity, a straight plane 5000 feet long on a grade of 114 feet in 100 while it would appear that 214 feet in 100 is necessary for the same number of empty cars. For roads longer than 5000 feet, or when containing sharp

of empty cars. For roads longer than 5000 feet, or when containing sharp curves, the grade should be correspondingly larger.

III. The Tail-rope Systems.—Of all methods for conveying coal underground by wire rope, the tail-rope system has found the most application. It can be applied under almost any condition. The road may be straight or curved, level or undulating, in one continuous line or with side branches. In general principle a tail-rope plane is the same as an engine plane worked in both directions with two ropes. One rope, called the "main rope," serves for drawing the set of full cars outward; the other, called the "tail-rope," is necessary to take beck the empty set, which on a level or undulating road cannot return by gravity. The two drums may be located at the opposite ends of the road, and driven by separate engines, but more frequently they are on the same shaft at one end of the plane. but more frequently they are on the same shaft at one end of the plane. In the first case each rope would require the length of the plane, but in the second case the tail rope must be twice as long, being led from the drunaround a sheave at the other end of the plane and back again to its startir

point. When the main rope draws a set of full cars out, the tail-rope drum runs loose on the shaft, and the rope, being attached to the rear car, unwinds itself steadily. Going in, the reverse takes place. Each drum is provided with a brake to check the speed of the train on a down grade and prevent its overrunning the forward rope. As a rule, the tail rope is strained less than the main rope, but in cases of heavy grades dipping outward it is possible that the strain in the former may become as large, or even larger, than in the latter, and in the selection of the sizes reference should be had to this circumstance. should be had to this circumstance.

IV. The Endless-rope System.—The principal features of this

system are as follows:

The rope, as the name indicates, is endless.
 Motion is given to the rope by a single wheel or drum, and friction is obtained either by a grip-wheel or by passing the rope several times around

the wheel.

3. The rope must be kept constantly tight, the tension to be produced by artificial means. It is done in placing either the return-wheel or an extra tension wheel on a carriage and connecting it with a weight hanging over a pulley, or attaching it to a fixed post by a screw which occasionally can be shortened.

4. The cars are attached to the rope by a grip or clutch, which can take hold at any place and let go again, starting and stopping the train at will,

without stopping the engine or the motion of the rope.

5. On a single-track road the rope works forward and backward, but on a double track it is possible to run it always in the same direction, the full

cars going on one track and the empty cars on the other.

This method of conveying coal, as a rule, has not found as general an introduction as the tail-rope system, probably because its efficacy is not so apparent and the opposing difficulties require greater mechanical skill and more complicated appliances. Its advantages are, first, that it requires one third less rope than the tail-rope system. This advantage, however, is partially counterbalanced by the circumstance that the extra tension in the rope requires a heavier size to move the same load than when a main and tail rope are used. The second and principal advantage is that it is possible to start and stop trains at will without signalling to the engineer. On the other hand, it is more difficult to work curves with the endless system, and still more so to work different branches, and the constant stretch of the rope under tension or its elongation under changes of temperature frequently causes the rope to slip on the wheel, in spite of every attention,

causing delay in the transportation and injury to the rope.

V. Wire-rope Tramways.—The methods of conveying products on a suspended rope tramway find especial application in places where a mine is located on one side of a river or deep ravine and the loading station on the other. A wire rope suspended between the two stations forms the track on which material in properly constructed "carriages" or "buggles" is transported. It saves the construction of a bridge or treatlework, and is practical for a distance of 2000 feet without an intermediate support.

There are two distinct classes of rope tramways:

1. The rope is stationary, forming the track on which a bucket holding the material moves forward and backward, pulled by a smaller endless wire rope.

2. The rope is movable, forming itself an endless line, which serves at

the same time as supporting track and as pulling rope.

Of these two the first method has found more general application, and is especially adapted for long spans, steep inclinations, and heavy loads. The second method is used for long distances, divided into short spans, and is only applicable for light loads which are to be delivered at regular intervals.

For detailed descriptions of the several systems of wire-rope transportation, see circulars of John A. Roebling's Sons Co., The Trenton Iron Co., and other wire-rope manufacturers. See also paper on Two-rope Haulage Systems, by R. Van A. Norris, Trans. A. S. M. E., xii. 636.

In the Bleichert System of wire-rope tramways, in which the track rope is

stationary, loads of 1000 pounds each and upward are carried. While the average spans on a level are from 150 to 200 feet, in crossing rivers, ravines, average spans on a level are from 130 to 200 feet, in crossing rivers, ravines, contact, spans up to 1500 feet are frequently adopted. In a tramway on this system at Granite, Montana, the total length of the line is 9750 feet, with a fall of 1225 feet. The descending loads, amounting to a constant weight of about 11 tons, develop over 14 horse-power, which is sufficient to haul the ampty buckets as well as about 50 tons of supplies per day up the line, and also to run the ore crusher and elevator. It is capable of delivering 250 tons of material in 10 hours.

Suspension Cableways or Cable Hoist-conveyors.

(Trenton Iron Co.)

In quarrying, rock-cutting, stripping, piling, dam-building, and many other operations where it is necessary to hoist and convey large individual loads economically, it frequently happens that the application of a system of derricks is impracticable, by reason of the limited area of their efficiency

and the room which they occupy.

To meet such conditions cable hoist-conveyors are adapted, as they can be operated in clear spans up to 1500 feet, and in lifting individual loads up to 15 tons. Two types are made—one in which the hoisting and conveying are done by separate running ropes, and the other applicable only to inclines, in which the carriage descends by gravity, and but one running rope is required. The moving of the carriage in the former is effected by means of an endless rope, and these are commonly known as "endless-rope" hoistconveyors to distinguish them from the latter, which are termed "inclined" hoist-conveyors.

The general arrangement of the endless-rope hoist-conveyors consists of a main cable passing over towers, A frames or masts, as may be most convenient, and anchored firmly to the ground at each end, the requisite $t \in nsion$ in the cable being maintained by a turnbuckle at one anchorage.

in the cable being maintained by a turnbuckle at one anchorage. Upon this cable travels the carriage, which is moved back and forth over the line by means of the endless rope. The hoisting is done by a separate rope, both ropes being operated by an engine specially designed for the purpose, which may be located at either end of the line, and is constructed in such a way that the hoisting-rope is colled up or paid out automatically as the carriage is moved in aid out. Loads may be picked up or disharged at any point along the line. Where sufficient inclination can be obtained in the main cable for the carriage to descend by gravity, and the loading and unloading is done at fixed points, the endless rope can be dispensed with. The carriage, which is similar in construction to the carriage used in the endless rope cableways is arrested in its descent by a stor-block, which endless-rope cableways, is arrested in its descent by a stop-block, which may be clamped to the main cable at any desired point, the speed of the descending carriage being under control of a brake on the engine-drum.

Stress in Hoisting-ropes on Inclined Planes.

			(110	HOIL TLOI	1 (0.)			
Rise per 100 ft. horizontal.	Angle of inclination.	Stress in lbs. per ton of 2000 lbs.	Rise per 100 ft. horizontal.	Angle of inclination.	Stress in lbs. per ton of 2000 lbs.	Rise per 100 ft. horizontal.	Angle of inclination.	Stress in lbs. per ton of 2000 lbs.
ft. 5 10 15 20 25 30 35 40 45 50	2° 52′ 5° 48′ 8° 32′ 11° 10′ 14° 08′ 16° 42′ 19° 18′ 21° 49′ 24° 14′ 26° 34′	140 240 336 432 527 618 700 782 860 933	ft. 555 60 65 70 75 80 85 90 95	28° 49′ 30° 58′ 33° 02′ 35° 00′ 36° 53′ 38° 40′ 40° 22′ 42° 00′ 43° 32′ 45° 00′	1008 1067 1128 1185 1238 1287 1332 1875 1415	ft. 110 120 130 140 150 160 170 180 190 200	47° 44′ 50° 12′ 52° 26′ 54° 28′ 56° 19′ 58° 00′ 59° 33′ 60° 57′ 62° 15′ 63° 27′	1516 1573 1620 1663 1699 1730 1758 1782 1804 1822

The above table is based on an allowance of 40 lbs, per ton for rolling friction, but an additional allowance must be made for stress due to the weight of the rope proportional to the length of the plane. A factor of safety of 5 to 7 should be taken.

In hoisting the slack-rope should be taken up gently before beginning the

If noising the state-rope stoud to taken the gently delive beginning the fift, otherwise a severe extra strain will be brought on the rope.

A Double-suspension Cableway, carrying loads of 15 tons, erected near Williamsport, Fa., by the Trenton Iron Co., is described by E. G. Spilsbury in Trans. A. I. M. E. xx. 766. The span is 733 feet, crossing the Susquehanna River. Two steel cables, each 2 in. diam., are used. On these cables runs are longer to the state of the sta carriage supported on four wheels and moved by an endless cable 1 inch indiam. The load consists of a cage carrying a railroad-car loaded with in

ber, the latter weighing about 12 tons. The power is furnished by a 50-H.P. engine, and the trip across the river is made in about three minutes.

A hoisting cableway on the endless-rope system, erected by the Lidgerwood Mfg. Co., at the Austin Dam, Texas, had a single span 1350 ft. in length, with main cable 2½ in. diam., and hoisting-rope 1½ in. diam. Loads of 7 to 8 tons were handled at a speed of 600 to 800 ft. per minute.

Another, of still longer span, 1650 ft., was erected by the same company at Holyoke, Mass, for use in the construction of a dam. The main cable is the Elliott or locked wire cable, having a smooth exterior. In the construction of the Chicago Drainage Canal twenty cableways, of 700 ft. span and 8 tons canacity, were used, the towers travelling on rail:

Tension required to Prevent Silpping of Hope on Drume. (Trenton Iron Co.)—The amount of artificial tension to be applied in an onlies rome to prevent slipping of the divinged winders of the characteristics.

endless rope to prevent slipping on the driving-drum depends on the character of the drum, the condition of the rope and number of laps which it makes. If T and S represer, respectively the tensions in the taut and slack lines of the rope; W, the necessary weight to be applied to the tail-sheave; R, the resistance of the cars and rope, allowing for friction; n, the number of half-laps of the rope on the driving-drum; and f, the coefficient of friction, the following relations must exist to prevent slipping:

$$T = Se^{f\pi \pi}$$
, $W = T + S$, and $R = T - S$;
from which we obtain $W = \frac{e^{f\pi \pi} + 1}{e^{f\pi \pi} - 1}R$,

in which e = 2.71828, the base of the Naperian system of logarithms.

The following are some of the values of f:

The importance of keeping the rope dry is evident from these figures.

The importance of keeping where $\frac{e^{fn\pi}+1}{e^{fn\pi}-1}$, corresponding to the above values

of f, for one up to six half-laps of the rope on the driving-drum or sheaves, are as follows:

f	n = Number of Half-laps on Driving-wheel.									
	1	2	3	4	5	6				
.070	9,180	4.623	E.111	2 418	1.999	1.729				
.085	7.586	8.833	2.629	2.047	1.714	1.505				
.120	5.845	2.777	1.953	1.570	1.858	1.282				
.140	4.623	2.418	1.729	1.416	1.249	1.154				
.170	8.833	2.047	1.505	1.268	1.149	1.085				
,205	8.212	1.762	1.838	1.165	1.088	1.048				
.235	2.831	1.592	1.245	1.110	1.051	1.094				
.400	1.795	1.176	1.047	1.018	1.004	1.001				
.495	1,538	1.093	1.619	1.004	1.001	l				

When the rope is at rest the tension is distributed equally on the two lines

When the rope is at rest the tension is distributed equally on the two lines of the rope, but when running there will be a difference in the tensions of the tant and slack lines equal to the resistance, and the values of T and S may be readily computed from the foregoing formulas.

Taper Hopes of Uniform Tensile Strength.—The true form of rope is not a regular taper but follows a logarithmic curve, the girth rapidly increasing toward the upper end. Mr. Chas. D. West gives the following formula, based on a breaking strain of 80.000 lbs. per sq. in. of the rope, core included, and a factor of safety of 10: $\log G = F/860 + \log g$, in which $F = \operatorname{length}$ in fathoms, and G and g the girth in inches at any two sections F fathoms apart. The girth g is first calculated for a safe strain of 8000 lbs. per sq. in., and then G is obtained by the formula. For a mathematical investigation see The Engineer, April, 1880, p. 267.

TRANSMISSION OF POWER BY WIRE ROPE.

The following notes have been furnished to the author by Mr. Wm. Hewitt, Vice-President of the Trenton Iron Co. (See also circulars of the Trenton Iron Co. and of the John A. Roebling's Sons Co., Trenton, N. J.: "Transmission of Power by Wire Ropes," by A. W. Stahl, Van Nostrand's Science Series, No. 28; and Reuleaux's Constructor.)

The force transmitted should not exceed the difference between the elastic limit of the wires and the bending stress as determined by the following tables, taking the elastic limit of tempered steel, such as is used in the best rope, at 57,000 lbs. per sq. in., and that of Swedish iron at half this. or 28,500 lbs. (The el. lim. of fine steel wires may be higher than 57,000 lbs.)

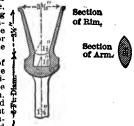
Elastic Limit of Wire Ropes.

7-Wire Rope.	Diam. of Wires.	Aggregate Area of Wires.	Elastic Limit. Steel.	Elastic Limit. Iron.		
diam., in,	ins. sq. in.		lbs.	lbs.		
1/4	.028	.025862	1,474	787		
5/16	.085	.040409	2,803	1,152		
86	.042	.058189	8.817	1,659		
7/16	.049	.079201	4,514	2,257		
⅓	.055	.099785	5,688	2,844		
9/16	.0625	.128855	7,845	3,672		
5∕6	.070	.161635	9,218	4,607		
11/16	.076	.190582	10,860	5,480		
%	.083	.227246	12.953	6,477		
%	.097	.310373	17,691	8,846		
1	.111	.406430	28,167	11,583		
19-Wire Rope.						
34	.017	.025876				
5/16	.021	.039485				
₹6	.024	.051573	The elastic	limit of 19-wire		
3/6 7/16	.029	.075299	rope may be	taken the same		
9/16	.033	.097504	as for 7-wire	rope since the		
9/16	.0375	.125909		ength of the		
5% 11/16	.042	.157941	wires is 7	to 10 per cent		
11/16	.046	.189458	greater.	-		
¾	.050	.223839	i			
₹	.058	.301198	l			
1	.067	.401925	İ			

The working tension may be greater, therefore, as the bending stress is less; but since the tension in the slack portion of the rope cannot be less than a certain proportion of the tension in the taut portion, to avoid slipping, a ratio exists between the diameter

of sheave and the wires composing the rope, corresponding to a maximum safe working tension. This ratio depends upon the number of laps that the rope makes about the sheaves, and the kind of filling in the rims or the character of the material upon which the rope tracks.

The sheaves (Fig. 165) are usually of cast iron, and are made as light as possible ous materials have been used for filling the bottom of the groove, such as tarred oakum. jute yarn, hard wood, India-rubber, and leather. The filling which gives the best satisfaction, however, in ordinary transmissatisfaction, in visuality visuality states and stone consists of segments of leather and blocks of India-rubber soaked in tar and racked alternately in the groove. Where the working tension is very



great, however, the wood filling is to be preferred, as in the case of long-distance transmissions where the rope makes several laps about the sheaves, and is run at a comparatively slow speed.

The Bending Stress is determined by the formula

$$k = \frac{Ea}{2.06(R+a)+C}.$$

k= bending stress in lbs.; E= modelus of elasticity = 28,500,000; a= aggregate area of wires, sq. ins.; R= radius of bend; d= diam. of wires, ins.

For 7-wire rope d = 1/9 diam. of rope; C = 27.54.

" 19-wire " d=1/15 " " ; C=45.9. From this formula the tables below have been calculated.

Bending Stresses, 7-wire Rope.

Diam. Bend.	84	36	48	60	72	84	96	108	120	132
Diam. Rope			1	1					1	
54	810	545	411	330	275			184	166	
0/32	1,095	738	556	447	878	321	281	250		205
5/16	1,569	1,060	8:10	048	587	461	404	359	524	294
36	2.691	1.822	1.377	1,106	9:25	794	696	620	558	508
7/16	4,243	2.878	2.178	1,751	1,465	1.259	1.104	982	885	806
36	5.962	4.053	3.070		2,067	1,777	1,558		1,250	1.138
9/16	8.701	5,915	4,486	3,613	3,025		2,282		1.831	1,667
96		8,267	6,278	5,060	4,289	3,646				
11/16		10,535		6,459	5,412	4.657	4,087		3,283	
			10,392		7,032	6,053				
34 38		21,585		13,309	11,168	9,620				
1 0					16,651				10,151	9,249
11/6								16,01I		18.172
114								21,942		
136								29,164		
136 116								37,799		

Bending Stresses, 19-Wire Rope.

Diam. Bend	12	24	36	48	60	72	84	96	108	120
Diam. Rope.										
1/4	965	495	339	250	200					
5/16	1,774	920	621	468	376					189
86	2,620	1,366		698	561	469	403			283
7/16	4,546	2,389	1,620	1,226			706		558	498
16	6,609	8,495	2,376		1,448	1,212	1,042	913		738
9/16	1	5,089	8,4(8			1,778	1,525	1,338	1,191	1,074
58	1 .		4,847	3,680	2,967	2,485	2,137	1,876	1,671	1,506
11716				4,818	3,886	8,257	2,802	2.459	2,191	1.976
		11,807	8,101	6,165	4,977	4,173	3,591	8,153		2.534
34 38		18,183			7.724			4,886	4.871	8,948
1′°				14,614	11,830	9,937	8,566			
ī1⁄6		,	26,566	20,357	16,500					
ií3			35.683	27,400	22,239	18.713	16, 153	14,209	12.682	11,458
186			48,109	37.028	30,096	25,350	21.897	19.272	17.209	15.545
. 112			61.238	47,229	38,436	32,408	28,008	24.662	22,030	19,906
156										25,005
132				74 565	60.844	49,919	14 476	39.208	35.048	31,689
13/4 17/8	l		••••	00 325	73 795	62 379	54 022	47 6:0	12 608	38,584
2'8			· · · · · ·	30,000	88,400	74 795	61 814	57 183	31 160	46,285
21/4										66,002
212							22,200			90.540

Horse-Power Transmitted.—The general formula for the amount of power capable of being transmitted is as follows:

H.P. =
$$[cd^2 - .000006 (w + g_1 + g_2)]v;$$

in which d = diameter of the rope in inches, v = velocity of the rope in feet per second, w = weight of the rope, $g_1 =$ weight of the terminal sheaves and shafts, $g_2 =$ weight of the intermediate sheaves and shafts (all in lbs.), and c = a constant depending on the material of the rope, the filling in the grooves of the sheaves, and the number of laps about the sheaves or drums, a single lap meaning a half-lap at each end. The values of c for one up to six laps for steel rope are given in the following table:

	Number of Laps about Sheaves or Drums.							
c = for steel rope on	1	2	8	4	5	6		
Iron	5.61 6.70 9.29	8.81 9.93 11.95	10.62 11.51 12.70	11.65 12.26 12.91	12.16 12.66 12.97	12.56 12.83 13.00		

The values of c for iron rope are one half the above.

When more than three laps are made, the character of the surface in

contact is immaterial as far as slippage is concerned.

From the above formula we have the general rule, that the actual horsepower capable of being transmitted by any wire rope approximately equals c times the square of the diameter of the rope in inches, less six millionthe the entire weight of all the moving parts, multiplied by the espeed of the rope, in feet per second.

Instead of grooved drums or a number of sheaves, about which the rope makes two or more laps, it is sometimes found more desirable, especially where space is limited, to use grip-pulleys. The rim is fitted with a continuous series of steel jaws, which bite the rope in contact by reason of the pressure of the same against them, but as soon as relieved of this pressure

In the ordinary or "flying" transmission of power, where the rope makes a single lap about sheaves lined with rubber and leather or wood, the ratio between the diameter of the sheaves and the wires of the rope, corresponding to a maximum safe working tension, is: For 7-wire rope, steel, 76.9; iron, 157.8. For 12-wire rope, steel, 59.3; iron, 122.6. For 19-wire rope, steel, 44.5; iron, 93.1.

Diameters of Minimum Sheaves in Inches, Corresponding to a Maximum Safe Working Tension.

Diameter		Steel.			Iron.			
of Rope, In.	7-Wire.	12-Wire.	19-Wire.	7-Wire.	12-Wire.	19 Wire		
5/16 5/16 7/16 9/16 9/16 11/16 3/4	19 24 29 34 38 43 48 53 58 67	15 19 22 26 30 33 37 41 44 52	11 14 17 19 22 25 25 28 31 84 •	39 49 59 69 79 89 99 109 119 138 158	31 38 46 54 61 69 77 84 92 107	28 29 35 41 47 52 58 64 70 81 98		

Assuming the sheaves to be of equal diameter, and of the sizes in the above table, the horse-power that may be transmitted by a steel rope making a single lap on wood-filled sheaves is given in the table on the next page.

The transmission of greater horse-powers than 250 is impracticable with filled sheaves, as the tension would be so great that the filling would quickly cut out, and the adhesion on a metallic surface would be insufficient where the rope makes but a single lap. In this case it becomes necessary to use the Re-uleaux method, in which the rope is given more than one lap, as referred to below, under the caption "Long-distance Transmissions."

Horse-power Transmitted by a Steel Hope on Wood-filled Sheaves.

Diameter		Velocity of Rope in Feet per Second.										
of Rope. In.	10	20	80	40	50	60	70	80	90	100		
5/16 5/16 3/6 7/16 1/16 9/16 5/6	4 7 10 18 17 22 27 32 38	8 13 19 26 84 43 53 63	13 20 28 88 51 65 79 95	17 26 38 51 67 86 104 126 150	21 38 47 63 83 106 130 157 186	25 40 55 75 99 128 155 186 223	28 44 64 88 115 147 179 217	32 51 73 99 130 167 203 245	37 57 80 109 144 184 225	40 62 89 121 159 203 247		
, %	52 68	104 185	156 202	206	100	~~						

The horse-power that may be transmitted by iron ropes is one half of the above.

This table gives the amount of horse-power transmitted by wire ropes under maximum safe working tensions. In using wood-lined sheaves, therefore, it is well to make some allowance for the stretching of the rope, and to advocate somewhat heavier equipments than the above table would give; that is, if it is desired to transmit 25 horse-power, for instance, to put in a plant that would transmit 25 to 30 horse-power, thus avoiding the necessity of having to take up a comparatively small amount of stretch. On rubber and leather filling, however, the amount of power capable of being transmitted is 40 per cent greater than for wood, so that this filling is generally used, and in this case no allowance need be made for stretch, as such sheaves will likely transmit the power given by the table, under all possible deflections of the rope.

Under ordinary conditions, ropes of seven wires to the strand, laid about a hemp core, are best adapted to the transmission of power, but conditions often occur where 12- or 19-wire rope is to be preferred, as stated below.

Deflections of the Rope.—The tension of the rope is measured by the amount of sag or deflection at the centre of the span, and the deflection corresponding to the maximum safe working tension is determined by the following formulæ, in which S represents the span in feet:

Limits of Span.—On spans of less than sixty feet, it is impossible to splice the rope to such a degree of nicety as to give exactly the required deflection, and as the rope is further subject to a certain amount of stretch, it becomes necessary in such cases to apply mechanical means for producing the proper tension, in order to avoid frequent splicing, which is very objectionable; but care should always be exercised in using such tightening devices that they do not become the means, in unskilled hands, of overstraining the rope. The rope also is more sensitive to every irregularity in the sheaves and the fluctuations, in the amount of power transmitted, and is apt to sway to such an extent beyond the narrow limits of the required deflections as to cause a jerking motion, which is very injurious. For this reason on very short spans it is found desirable to use a considerably heavier rope than that actually required to transmit the power; or in other words, instead of a 7-wire rope corresponding to the conditions of maximum tension, it is better to use a 19-wire rope of the same size wires, and to run this under a tension considerably below the maximum. In this way is obtained the advantages of increased weight and less#iretch, without

having to use larger sheaves, while the wear will be greater in proportion to the increased surface.

In determining the maximum limit of span, the contour of the ground and the available height of the terminal sheaves must be taken into consideration. It is customary to transmit the power through the lower portion of the rope, as in this case the greatest deflection in this portion occurs when the rope is at rest. When running, the lower portion rises and the upper portion siaks, thus enabling obstructions to be avoided which otherwise would have to be removed, or make it necessary to erect very high towers. The maximum limit of span in this case is determined by the maximum deflection that may be given to the upper portion of the rope when running, which for sheaves of 10 ft. diameter is about 600 feet.

Much greater spans than this, however, are practicable where the contour of the ground is such that the upper portion of the rope may be the driver, and there is nothing to interfere with the proper deflection of the under portion. Some very long transmissions of power have been effected in this way without an intervening support, one at Lockport, N. Y., having a clear

span of 1700 feet.

Long-distance Transmissions.—When the distance exceeds the limit for a clear span, intermediate supporting sheaves are used, with plain grooves (not filled), the spacing and size of which will be governed by the contour of the ground and the special conditions involved. The size of these aheaves will depend on the angle of the bend, gauged by the tangents to the curves of the rope at the points of inflection. If the curvature due to this angle and the working tension, regardless of the size of the sheaves, as determined by the table on the next page, is less than that of the minimum sheave (see table p. 919) the intermediate sheaves should not be smaller than such minimum sheave, but if the curvature is greater, smaller intermediate sheaves may be used.

In very long transmissions of power, requiring numerous intermediate supports, it is found impracticable to run the rope at the high speeds maintained in "flying transmissions." The rope therefore is run under a higher working tension, made practicable by wrapping it several times about grooved terminal drums, with a lap about a sheave on a take-up or countert varieties of activities, which preserves a constant tension in the slack portion.

weighted carriage, which preserves a constant tension in the slack portion. Inclined Transmissions.—When the terminal sheaves are not on the same elevation, the tension at the upper sheave will be greater than that at the lower, but this difference is so slight, in most cases, that it may be ignored. The span to be considered is the horizontal distance between the sheaves, and the principles governing the limits of span will hold good in this case, so that for very steep inclinations it becomes necessary to resort to tightening devices for maintaining the requisite tension in the rope. The limiting case of inclined transmissions occurs when one wheel is directly above the other. The rope in this case produces no tension whatever on the lower wheel, while the upper is subject only to the weight of the rope, which is usually so insignificant that it may be neglected altogether, and on vertical transmissions, therefore, mechanical tension is an absolute necessity.

Bending Curvature of Wire Ropes.—The curvature due to any bend in a wire rope is dependent on the tension, and is not always the same as the abase in contact, but may be greater, which explains how it is that large ropes are frequently run around comparatively small sheaves without detriment, since it is possible to place these so close that the bending angle on each will be such that the resulting curvature will not overstrain the wires. This curvature may be ascertained from the formula and table on the next page, which give the theoretical radii of curvature in inches for various sizes of ropes and different angles for one pound tension in the rope. Dividing these figures by the actual tension in pounds, gives the radius of curvature assumed by the rope in cases where this exceeds the curvature of the sheave. The rigidity of the rope or internal friction of the wires and core has not been taken into account in these figures, but the effect of this is insignificant, and it is on the safe side to ignore it. By the "angle of bend" is meant the angle between the tangents to the curves of the rope at the points of inflection. When the rope is straight the angle is 180°. For angles less than 160° the radius of curvature in most cases will be ess than that corresponding to the safe working tension, and the proper size of sheave to use in such cases will be governed by the table headed. "Dismeters of Minimum Sheaves Corresponding to a Maximum F Working Tension" or page 919,

Radius of Curvature of Wire Ropes in Inches for 1-lb. Tension.

Formula: $R = E\delta^4 n + 5.25t$ cos $\frac{1}{2}\theta$; in which R = radius of curvature; E = modulus of elasticity = 28,500,000; $\delta = \text{diameter of wires}$; n = nc. of wires; $\theta =$ angle of bend; t = working stress (lbs. and ins.).

Divide by stress in pounds to obtain radius in inches.

Diam. of wire.	1 60° .	165°	170°	172°	1740	176°	178•
19-Wire Rope	4,226	5,628	8,421	10,949	14,593	21,884	43,762
	11,090	14,753	22,095	26,731	35,628	58,429	106,847
	22,274	29,633	45,412	54,417	72,580	108,767	217,50
	43,184	57,451	86,040	102,688	136,869	205,251	410,44
	71,816	95,541	148,085	175,182	233,492	350,150	700,193
	112,763	150,016	224,667	260,607	374,010	560,872	1,121,574
7-Wire Rope 19	169,135	225,012	836,983	427,680	570,050	854,658	1,709,456
	12,914	17,179	25,727	81,125	41,485	62,212	124,405
	29,762	39,594	59,297	75,988	101,282	151.884	308,728
	62,313	82,899	124,151	157,570	210,018	314,948	629,800
	116,239	154,641	281,593	291,917	389,065	583,479	1,164,099
	199,323	265,173	397,129	497,998	663,767	995,300	1,990,478
	820,556	426,459	688,674	797,697	1,063,217	1,594,422	8,188,859
	504,402	671,041	1,004,965	1,215,817	1,620,518	2,480,151	4,859,561

ROPE-DRIVING.

The transmission of power by cotton or manila ropes is a competitor wit! gearing and leather belting when the amount of power is large, or the distance between the power and the work is comparatively great. The followtance between the power and the work is comparatively great. The following is condensed from a paper by C. W. Hunt, Trans. A. S. M. E., xii. 230:

But few accurate data are available, on account of the long period re-

quired in each experiment, a rope lasting from three to six years. Installs tions which have been successful, as well as those in which the wear of ne rope was destructive, indicate that 200 lbs. on a rope one inch in diametral is a safe and economical working strain. When the strain is mu! A. ally increased, the wear is rapid.

In the following equations

C = circumference of rope in inches;

g = gravity; H = horse-power;D =sag of the rope in inches;

F =centrifugal force in pounds; w = working strain in po. Lis;

P =pounds per foot of rope; v =working R =force in pounds doing useful work;

S =strain in pounds on the rope at the pulley;

T = tension in pounds of driving side of the rope;

tension in pounds on slack side of the rope;
v = velocit of the rope in feet per second;

W = ultim ... breaking strain in pounds.

$$W = 720C^2$$
; $P = .032C^2$; $w = 20C^2$.

This makes the normal working strain equal to 1/86 of the breaking strength, and about 1/25 of the strength at the splice. The ict ia! strains are ordinarily much greater, owing to the vibrations in rucking, & well as from imperfectly adjusted tension mechanism.

For this investigation we assume that the strain on the driving side of a rope is equal to 200 lbs. on a rope one inch in diameter, and an equivalent strain for other sizes, and that the rope is in motion at various velocities of from 10 to 140-ft. per second.

The centrifugal force of the rope in running over the calley will reduce

the amount of force available for the transmission of power. The centrifu-

gal force $F = Pv^2 + g$.

At a speed of about 80 ft. per second, the centrifugal force increases faster than the power from increased velocity of the rope, and at about 140 ft. per second equals the assumed allowable tension of the rope. Computing this force at various speeds and then subtracting it from the assumed maximum whole of this force cannot be used, because a certain amount of tension, we have the force available for the transmission of power. The whole of this force cannot be used, because a certain amount of tension on the slack side of the rope is needed to give adhesion to the pulley. What tension should be given to the rope for this purpose is uncertain, as there are no experiments which give accurate data. It is known from considerable experience that when the rope runs in a groove whose sides are inclined toward each other at an angle of 45° there is sufficient adhesion when the

ratio of the tensions T+t=2.

For the present purpose, T can be divided into three parts: 1. Tension doing useful work; 2. Tension from centrifugal force; 3. Tension to balance

the strain for adhesion.

The tension t can be divided into two parts: 1. Tension for adhesion:
2. Tension from centrifugal force.
It is evident, however, that the tension required to do a given work should

It is evident, however, that the tension required to do a given work should not be materially exceeded during the life of the rope.

There are two methods of putting ropes on the pulleys; one in which the ropes are single and spliced on, being made very taut at first, and less so as the rope lengthens, stretching until it slips, when it is respliced. The other method is to wind a single rope over the pulley as many turns as needed to obtain the necessary horse-power and put a tension pulley to give the necessary adhesion and also take up the wear. The tension if required to transmit the normal horse-power for the ordinary speeds and sizes of rope is computed by formula (1), below. The total tension I on the driving side of the rope is assumed to be the same at all speeds. The centrifugal force, as well as an amount equal to the tension for adhesion on the slack side of the rope must be taken from the total tension I to ascertain the amount of force must be taken from the total tension T to ascertain the amount of force

available for the transmission of power. It is assumed that the tension on the slack side necessary for giving adhesion is equal to one half the force doing useful work on the driving side of the rope; hence the force for useful work is $R = \frac{2(T-F)}{3}$; and the tension on the slack side to give the required adhesion is $\frac{1}{2}(T-F)$. Hence

The sum of the tensions T and t is not the same at different speeds, as the equation (1) indicates.

As F varies as the square of the velocity, there is, with an increasing speed of the rope, a decreasing useful force, and an increasing total tension, f, on the slack side. With these assumptions of allowable strains the horse-power will be

$$H = \frac{2v(T-F)}{3\times550}.................(2)$$

Transmission ropes are usually from 1 to 134 inches in diameter. A computation of the horse-power for four sizes at various speeds and under

putation of the horse-power for four sizes at various speeds and under ordinary conditions, based on a maximum strain equivalent to 200 lbs. for a rope one inch in diameter, is given in Fig. 166. The horse-power of other sizes is readily obtained from these. The maximum power is transmitted, under the assumed conditions, at a speed of about 80 feet per second. The wear of the rope is both internal and external; the internal is caused by the movement of the fibres on each other, under pressure in bending over the sheaves, and the external is caused by the slipping and the wedging in the grooves of the pulley. Both of these causes of wear are, within the limits of ordinary practice, assumed to be directly proportional to the speed. Hence, if we assume the coefficient of the wear to be k, the wear will be kv, in which the wear increases directly as the velocity, but the horse-power that can be transmitted, as equation (2) shows, will not vary at the same rate. the same rate.

The rope is supposed to have the strain T constant at all speeds on the driving side, and in direct proportion to the area of the cross-section; here-

the catenary of the driving side is not affected by the speed or by the diameter of the rope.

The deflection of the rope between the pulleys on the slack side varies with each change of the load or change of the speed, as the tension equation (1) Indicates

The deflection of the rope is computed for the assumed value of T are !

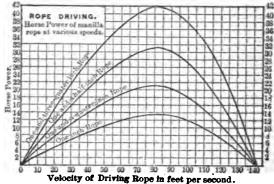


Fig. 166.

by the parabolic formula $S = \frac{PL^2}{8D} + PD$, S being the assumed strain T on the driving side, and t, calculated by equation (1), on the slack side. The tension t varies with the speed.

Horse-power of Transmission Rope at Various Speeds. Computed from formula (2), given above.

			О				- (-71					
n. of pes.	Speed of the Rope in feet per minute.										n. of	
Diam Rop	1500	2000	2500	8000	3500	4000	4500	5000	6000	7000	8000	Sme Diam Tuli
1/6	1.45	1.9 8.2	2.8 8.6	2.7 4.2	8 4.6	8.2 5.0	8.4 5.8	8.4 5.3	4.9	2.2 3.4	0	20 24
16	8.8 4.5 5.8	4.8 5.9 7.7	5.2 7.0 9.2	5.8 8.2 10.7	6.7 9.1	7.2 9.8 12.8	7.7 10.8 13.6	7.7 10.8 13.7	7.1 9.8 12.5	4.9 6.9 8.8	0	24 80 86 42
134 134 134 134	9.2 13.1	12.1 17.4	14.8 20.7	16.8 23.1	18.6 26.8	20.0	21.2 80.6	21.4 80.8	19.5	13.8 19.8	0	54 60
134	18 23.2	23.7 30.8	28.2 36.8	82.8 42.8	88.4 47.6	39.2 51.2	41.5 54.4	41.8 54 8	87.4 50	27.6 85.2	0	54 60 72 84

The following notes are from the circular of the C. W. Hunt Co., New York:

For a temporary installation, when the rope is not to be long in use, it might be advisable to increase the work to double that given in the table.

For convenience in estimating the necessary clearance on the driving and on the slack sides, we insert a table showing the sag of the rope at different on the stack states, we insert a table showing the sag of the rope at different speeds when transmitting the horse-power given in the preceding table. When at rest the sag is not the same as when running, being greater or the driving and less on the slack sides of the rope. The sag of the driving side when transmitting the normal horse-power is the same no matter what size of rope is used or what the speed driven at, because the assumption is that the strain on the rope shall be the same at all speeds when transmitting the

assumed horse-power, but on the slack side the strains, and consequently the sag, vary with the speed of the rope and also with the horse-power. The table gives the sag for three speeds. If the actual sag is less than given in the table, the rope is strained more than the work requires.

This table is only approximate, and is exact only when the rope is running at its normal speed, transmitting its full load and strained to the assumed amount. All of these conditions are varying in actual work, and the table must be used as a guide only.

Sag of the Rope between Pulleys.

Distance between	Driving Side.	Slack Side of Rope.							
Pulleys in feet.	All Speeds.	80 ft. per sec.	60 ft. per sec.	40 ft. per sec.					
40	0 feet 4 inches	Ofeet 7 inches	Ofeet 9 inches						
40 60 80	1 " 5 "	2 " 4 "	2 " 10 "	8 " 8 "					
100 120	2 " 0 " · · · · · · · · · · · · · · · · ·	3 " 8 " 5 " 8 "	6 " 8 "	5 " 8 " 7 " 4 "					
140 160	8 " 10" "	7 " 2 "	8 " 9 "	9 " 9 "					

The size of the pulleys has an important effect on the wear of the ropethe larger the sheaves, the less the fibres of the rope slide on each other, and consequently there is less internal wear of the rope. The pulleys should not

be less than forty times the diameter of the rope. The pulleys should not as much larger as it is possible to make them. This rule applies also to the idle and tension pulleys as well as to the main driving-pulley.

The angle of the sides of the grooves in which the rope runs varies, with different engineers, from 45° to 60°. It is very important that the sides of these grooves should be carefully polished, as the fibres of the rope rubbing on the metal as it comes from the lathe tools will gradually break fibre by thre and so give the rope a short life. It is also necessary to carefully avoid

on the metal as it comes from the lathe tools will gradually break fibre by fibre, and so give the rope a short life. It is also necessary to carefully avoid all sand or blow holes, as they will cut the rope out with surprising rapidity. Much depends also upon the arrangement of the rope on the pulleys, especially where a tension weight is used. Experience shows that the increased wear on the rope from bending the rope first in one direction and then in the other is similar to that of wire rope. At mines where two cages are used, one being hoisted and one lowered by the same engine doing the same work, the wire ropes, cut from the same coil, are usually arranged so that one rope is bent continuously in one direction and the other rope is bent first in one direction and the other in which is midding on the draw of the first in one direction and then in the other, in winding on the drum of the engine. The rope having the opposite bends wears much more rapidly than the other, lasting about three quarters as long as its mate. This difference in wear shows in manila rope, both in transmission of power and in coal-hoisting. The pulleys should be arranged, as far as possible, to bend the rope in one direction.

TENSION ON THE SLACK PART OF THE ROPE.

Speed of ope, in feet		eter of	the R	ope an	d Pour	ıds Ten	sion on	the Slac	k Rop
er second.	36	5%	34	3 /8	1	11/4	11/6	134	2
20	10	27	40	54	71	110	162	216	285
80	14	29	42	56	74	115	170	226	296
40	15	81	45	60	79	123	181	240	818
50	16	88	49	65	85	132	195	259	389
60	18	86	53	71	98	145	214	285	87
70	19	89	59	78	101	158	236	810	400
80	21	43	64	85	111	178	255	840	44
90	24	48	70	93	122	190	279	878	48

For large amounts of power it is common to use a number of ropes lying side by side in grooves, each spliced separately. For lighter drives some engineers use one rope wrapped as many times around the pulleys as is necessary to get the horse-power required, with a tension pulley to take up the slack as the rope wears when first put in use. The weight put upon this tension pulley should be carefully adjusted, as the overstraining of the rope from this cause is one of the most common errors in rope driving. We therefore give a table showing the proper strain on the rope for the various sizes, from which the tension weight to transmit the horse-power in the tables is easily deduced. This strain can be still further reduced if the horse-power transmitted is usually less than the nominal work which the rope was proportioned to do, or if the angle of groove in the pulleys is acute.

DIAMETER OF PULLEYS AND WEIGHT OF ROPE.

Diameter of Rope, in inches.	Smallest Diameter of Pulleys, in inches.	Length of Rope to allow for Splicing, in feet.	Approximate Weight, in lbs. per foot of rope.
1/6	20 24	6 .	.12 .18 .24
1/8	80 86 42	7 8 9	.32 .49
114 116 182	54 60 72	10 12 13	.60 .83 1.10
274	1 84	14	1.40

With a given velocity of the driving-rope, the weight of rope required for transmitting a given horse-power is the same, no matter what size rope is adopted. The smaller rope will require more parts, but the weight will be the same.

Miscellaneous Notes on Rope-driving.—W. H. Booth communicates to the Amer. Ma. kinist the following data from English practice with cotton ropes. The calculated figures are based on a total allowable tension on a 134-inch rope of 600 lbs., and an initial tension of 1/10 the total allowed stress, which corresponds fairly with practice.

Diameter of rope	11/4"	186′′	116"	156"	134"	136"	2"
Weight per foot, lbs	.5	.6	.72	156" .844	184'' .98	1.125	1.3
Centrifugal tension = V^2 divided by	64	53	44	38	88	28	25
" for $V = 80$ ft, per sec., lbs.	100	121	145	170	193	228	256
Total tension allowable	300	360	430	500	600	675	780
Initial tension	80	36	48	50	60	67	78
Net working tension at 80 ft. velocity	170	203	242	280	347	880	446
Horse-power per rope " "	24	28	84	41	49	54	63

The most usual practice in Lancashire is summed up roughly in the following figures: 134-inch cotton ropes at 5000 ft. per minute velocity = 50 H.P. per rope. The most common sizes of rope now used are 134 and 154 in. The maximum horse-power for a given rope is obtained at about 80 to 83 feet per second. Above that speed the power is reduced by centrifugal tension. At a speed of 2500 ft. per minute four ropes will do about the same work as three at 5000 ft. per min.

Cotton ropes do not require much lubrication in the sense that it is required by ropes made of the rough fibre of manila hemp. Merely a slight surface dressing is all that is required. For small ropes, common in spinning machinery, from ½ to ¾ inch diameter, it is the custom to prevent the fluffing of the ropes on the surface by a light application of a mixture of black-lead and molasses,—but only enough should be used to lay the fibres,—but upon one of the pulleys in a series of light data.

black-lead and molasses,—but only enough should be used to lay the fibres,—put upon one of the pulleys in a series of light dabs.

Reuleaux's Constructor gives as the "specific capacity" of hemp rope in actual practice, that is, the horse-power transmitted per square inch of cross-section for each foot of linear velocity per minute, .004 to .002, the cross-section being taken as that due to the full outside diameter of the rope. For a 134-in. rope, with a cross-section of 2.405-q. ln., at a velocity of 5000 ft. per min., this gives a horse-power of from 24 to 48, as against 41.8 by Mr. Hunt's table and 49 by Mr. Booth's.

Reuleaux gives formulæ for calculating sources of loss in hemp-rope transmission due to (1) journal friction, (2) stiffness of ropes, and (3) creep of ropes. The constants in these formulæ are, however, uncertain from lack of experimental data. He calculates an average case giving loss of power due to journal friction = 4%, to stiffness 7.8%, and to creep 5%, or 16.8% in all, and says this is not to be considered higher than the actual loss

in all, and says this is not to be considered higher than the actual loss. Spencer Miller, in a paper entitled "A Problem in Continuous Rope-driving, with a continuous rope from a large to a small pulley. He adopts the angle of 45° as a minimum angle to use on the smaller pulley, and recommends that the larger pulley be grooved with a wider angle to a degree such that the resistance to slipping is equal in both wheels. By doing this the effect of the tension weight is felt equally throughout all the slack strands of the rope-drive, hence the tight ropes pull equally. It is shown that when the wheels are grooved alike the strains in the various ropes may differ greatly, and to such a degree that danger is introduced, for while one-half the tension weight should represent the maximum strain on the slack rope, it is demonstrated in the paper that the actual maximum strain ray

be even four or six times as great.

In a drive such as is recommended, with a wide angle in the large sheave with the larger arc of contact, the conditions governing the ropes are the same as if the wheels were of the same diameter; and where the wheels are of the same dianeter, with a proper tension weight, the ropes pull alike. It is claimed that by widening the angle of the large sheave not only is there no power lost, but there is actually a great gain in power transmitted. An example is given in which it is shown that in that instance the power transmitted. An example is nearly doubled. Mr. Miller refers to a 250-horse-power drive which has been running ten years, the large pulley being grooved 60° and the smaller 45°. This drive was designed to use a 1¼-in. manila rope, but the grooves were made deep enough so that a ½-in. rope would not bottom. In order to determine the value of the drive a common ½-in, rope was put in at first, and lasted six years, working under a factor of safety of only 14. He recommends, however, the employment in continuous rope-driving of a factor of safety of not less than 20.

The Walker Company adopts a curved form of groove instead of one with

The Walker Company adopts a curved form of groove instead of one with straight sides inclined to each other at 45°. The curves are concave to the rope. The rope rests on the sides of the groove in driving and driven pulleys. In idler pulleys the rope rests on the bottom of the groove, which is semicircular. The Walker Company also uses a "differential" drum for heavy rope-drives, in which the grooves are contained each in a separate ring which is free to slide on the turned surface of the drum in case one rope

pulls more than another.

A heavy rope-drive on the separate, or English, rope system is described and illustrated in *Power*, April, 1892. It is in use at the India Mill at Darwen, England. This mill was originally driven by gears, but did not prove successful, and rope-driving was resorted to. The 85,000 spindles and preparation are driven by a 2000-horse-power tandem compound engine, with cylinders 23 and 44 inches in diameter and 72-inch stroke, running at 54 revolutions per minute. The fly-wheel is 30 feet in diameter, weighs 65 tons, and is arranged with 30 grooves for 134-inch ropes. These ropes lead off to receiving pulleys upon the several floors, so that each floor receives its power direct from the fly-wheel. The speed of the ropes is 5089 feet per minute, and five-floot receivers are used, the number of ropes upon each being proportioned to the amount of power required upon the several floors. Lambeth cotton ropes are used. (For much other information on this subject see "Rope-Driving," by J. J. Flather, John Wiley & Sons, 1895.)

FRICTION AND LUBRICATION.

Friction is defined by Rankine as that force which acts between two bodies at their surface of contact so as to resist their sliding on each other, and which depends on the force with which the bodies are pressed together.

and which depends on the force with which the bodies are pressed logether. Coefficient of Friction.—The ratio of the force required to slide a body along a norizontal plane surface to the weight of the body is called the coefficient of friction. It is equivalent to the tangent of the angle of repose, which is the angle of inclination to the horizontal of an inclined plane on which the body will just overcome its tendency to slide. The angle is usually denoted by θ , and the coefficient by f, $f = \tan \theta$.

Friction of Best and of Motion.—The force required to start a body sliding is called the friction of rest, and the force required to continue its sliding after having started is called the friction of motion.

Boiling Frietians is the force required to report.

Rolling Friction is the force required to roll a cylindrical or spherical body on a plane or on a curved surface. It depends on the nature of the surfaces and on the force with which they are pressed together, but is essentially different from ordinary, or aliding, friction.

Friction of Solids.—Rennie's experiments (1829) on friction of solids,

usually unlubricated and dry, led to the following conclusions:

1. The laws of sliding friction differ with the character of the bodies

- rubbing together.

 2. The friction of fibrous material is increased by increased extent of the friction of fibrous material is increased by increased extent of the friction of fibrous material is increased by increased extent of the fibrous material is increased by the fibrous material is increased by the fibrous material is increased surface and by time of contact, and is diminished by pressure and speed.

 8. With wood, metal, and stones, within the limit of abrasion, friction varies only with the pressure, and is independent of the extent of surface, time of contact and velocity.
 - 4. The limit of abrasion is determined by the hardness of the softer of the

two rubbing parts.

5. Friction is greatest with soft and least with hard materials.

6. The friction of lubricated surfaces is determined by the nature of the lubricant rather than by that of the solids themselves.

Friction of Rest. (Rennie.)

Pressure,	Values of f.							
lbs. per square inch.	Wrought iron on Wrought Iron.	Wrought on Cast Iron.	Steel on Cast Iron.	Brass on Cast Iron.				
187 224 336 448	.25 .27 .31 .38	.28 .29 .33 .37 .37	.80 .83 .85 .85	.23 .23 .21 .21 .23 .23				
560 672 784	Abraded	.37 .38 Abraded	.86 .40 Abraded	.23 .23 .23				

Law of Unlubricated Friction.—A. M. Wellington, Eng'g News April 7, 1888, states that the most important and the best determined of all

the laws of unlubricated friction may be thus expressed:

The coefficient of unlubricated friction decreases materially with velocity, is very much greater at minute velocities of 0 +, falls very rapidly with minute increases of such velocities, and continues to fall much less rapidly with higher velocities up to a certain varying point, following closely the laws which obtain with lubricated friction.

Friction of Steel Tires Sliding on Steel Rails. (Westing house & Galton.)

Speed, miles per hour..... 10 Coefficient of friction..... 0.110 Adhesion, lbs. per ton (2240 lbs.) 246

Rolling Friction is a consequence of the irregularities of form and the roughness of surface of bodies rolling one over the other. Its laws are not yet definitely established in consequence of the uncertainty which exists in experiment as to how much of the resistance is due to roughness of surface, how much to original and permanent irregularity of form, and how

surface, now much to original and permanent irregularity of form, and now much to distortion under the load. (Thurston.)

Coefficients of Bolling Friction.—If R = resistance applied at the circumference of the wheel, W = total weight, r = radius of the wheel, and f = a coefficient, R = fW + r. f is very variable. Coulomb gives ,06 for wood, .005 for metal, where W is in pounds and r in feet. Tredgold made the value of f for into the fmade the value of f for iron on iron .002.

For wagons on soft soil Morin found f = .065, and on hard smooth roads

A Committee of the Society of Arts (Clark, R. T. D.) reported a loaded omnibus to exhibit a resistance on various loads as below:

Pavement	Speed per hour.	Coefficient,	Resistance.
Granite	2.87 miles.	.007	17.41 per ton.
Asphalt	8.56 44	.0191	27.14 "
Wood	8.34 "	.0135	41.60 "
Macadam, gravelled	8.45 4	.0199	44.48 "
" granite, new		.0451	101.09 "

Thurston gives the value of f for ordinary railroads, .003, well-laid railroad track, .002; best possible railroad track, .001.

The few experiments that have been made upon the coefficients of rolling

The few experiments that have been made upon the coefficients of rolling friction, apart from axle friction, are too incomplete to serve as a basis for practical rules. (Trautwine).

Laws of Finid Friction.—For all finids, whether liquid or gaseous, the resistance is (1) independent of the pressure between the masses in contact; (2) directly proportional to the area of rubbing-surface; (3) proportional to the square of the relative velocity at moderate and high speeds, and to the velocity nearly at low speeds; (4) independent of the nature of the surfaces of the solid against which the stream may flow, but dependent to some extent upon their degrees of roughness; (5) proportional to the degree of roughness; (6) proportional to the degree of roughness; (6) proportional to the degree of roughness; (6) proportional to the degree of roughness; (6) proportional to the degree of roughness; (6) proportional to the degree of roughness; (6) proportional to the degree of roughness; (6) proportional to the degree of roughness; (6) proportional to the degree of roughness; (6) proportional to the degree of roughness. to some extent upon their degree of roughness; (5) proportional to the density of the fluid, and related in some way to its viscosity. (Thurston.) The Friction of Labricated Surfaces approximates to that of solid friction as the journal is run dry, and to that of fluid friction as it is flooded

with oil.

Angles of Repose and Coefficients of Friction of Building Materials. (From Rankine's Applied Mechanics.)

		••			
	0.	$f = \tan \theta$	tan d		
Dry masonry and brickwork Masonry and brickwork with	81° to 85°	.6 to .7	1.67 to 1.4		
damp mortar	86 149	.74	1.85		
Timber on stone	စွဲ့၌စီ	about 4	2.5		
Iron on stone	85° to 10%6°	.7 to .8	1.48 to 3.8		
Timber on timber	2816° to 1114°	.5 to .2	2 to 5		
" " metals	81° to 1134°	.6 to .2	1.67 to 5		
Metals on metals	14° to 816°	.25 to .15	4 to 6.67		
Masonry on dry clay moist clay	27° 1814°	.51 .83	1.96		
Earth on earth dry sand, clay,	14° to 45°	.25 to 1.0	4 to 1		
and mixed earth	21° to 37°	.38 to .75	2.63 to 1.88		
Earth on earth, damp clay	450	1.0	7.00 10 1.00		
" to " wet clay " shingle and	170	.81	3.23		
gravel	89° to 48°	.81	1.28 to 0.9		

Friction of Motion. The following is a table of the angle of repose θ , the coefficient of friction $f=\tan\theta$, and its reciprocal, 1+f, for the materials of mechanism—condensed from the tables of General Morin (1831). and other sources, as given by Rankine:

No.	Surfaces.	0.	f.	1+f.
1	Wood on wood, dry	14° to 2614°	.25 to .5	4 to 2
2	" " soaped	1116° to 20	.2 to .04	5 to 25
3	Metals on oak, dry	2514° to 31°	.5 to .6	2 to 1.67
4	" " " wet	1314° to 14°	.24 to .26	4.17 to 8.85
5	" " " воару	11140	.2	5
6	" " elm, dry	1114° to 142	.2 to .25	5 to 4
7	Hemp on oak, dry	280	.53	1.89
8	" " wet	18140	.33	3
ğ	Leather on oak	15° to 1914°	.27 to .38	3.7 to 2.86
20	" " metals, dry	2914	.56	1.79
îĭ	" " wet	2914° - 20°	.36	2.78
12	" " greasy	130	.23	4.35
13	" " " oily	814.	.15	6.67
14	Metals on metals, dry	814° to 11°	.15 to .2	6.67 to 5
15	wet	1614°	.13 10 .2	3.33
16	Smooth surfaces, occa-	1072		0.00
10	sionally greased	4° to 414°	.07 to .08	14.3 to 12.5
17	Smooth surfaces, con-	7.0		
	tinuously greased	30	.05	20
18	Smooth surfaces, best	•	""	
-0	results	134° to 2°	.03 to .036	I
19	Bronze ou lignum vitæ,	-/4 00 0	1	!
10	constantly wet	3º ?	.05 ?	1

Coefficients of Friction of Journals, (Morin.)

•• • • •		Lubrication.			
Material.	Unguent.	Continuous.			
Cast iron on cast iron	Oil, lard tallow.	.07 to .08	.03 to .654		
Cast iron on bronze	Oil, lard, tallow. Unctuous and wet.	.07 to .08	.03 to .054		
Cast iron on lignum vitæ			.09		
Wrought iron on castiron (Oil, lard, tallow.	.07 to .08	.03 to .054		
Iron on lignum vitæ	Oil, lard. Unctuous.	.11 .19			
Bronze on bronze	Olive-oil. Lard.	.10 .09			

Prof. Thurston says concerning the above figures that much better results are probably obtained in good practice with ordinary machinery. Those here given are so greatly modified by variations of speed, pressure, and temperature, that they cannot be taken as correct for general purposes.

Average Coefficients of Friction. Journal of cast iron in bronze bearing; velocity 720 feet per minute; temperature 70° F.; intermittent feed through an oil-hole. (Thurston on Friction and Lost Work.)

0.00	P	ressu	ıres,	po	unds	per	8q	uare	inel	h.	_
Ofls.	8		16		822			48			
Sperm, lard, neat's-foot, etc. Olive, cotton-seed, rape, etc. Cod and menhaden Mineral lubricating-oils	.160 " .248 "	.283 .278	.107 .124	44	.245 .167	.101	**	.168 .102	.077 .079 .081 .094	44	.144 .181 .122 .222

With fine steel journals running in bronze bearings and continuous lubrication, coefficients far below those above given are obtained. Thus with sperm-oil the coefficient with 50 lbs. per square inch pressure was .0034; with 200 lbs., .0051; with 300 lbs., .0057.

For very low pressures, as in spindles, the coefficients are much higher. Thus Mr, Woodbury found, at a temperature of 100° and a velocity of 600 feet per minute,

These hig... coefficients, however, and the great decrease in the coefficient at increased pressures are limited as a practical matter only to the smaller pressures which exist especially in spinning machinery, where the pressure is so light and the film of oil so thick that the viscosity of the oil is an import-

ant part of the total frictional resistance.

Experiments on Friction of a Journal Lubricated by an Oll-bath (reported by the Committee on Friction, Proc. Inst. M. E. Nov. 1883) show that the absolute friction, that is, the absolute tangential force per square inch of bearing, required to resist the tendency of the brass to go round with the journal, is nearly a constant under all loads, within ordinary working limits. Most certainly it does not increase in direct proportion to the load, as it should do according to the ordinary theory of solid friction. The results of these experiments seem to show that the friction of a perfectly lubricated journal follows the laws of liquid friction much more closely than those of solid friction. They show that under these circumstances the friction is nearly independent of the pressure per square inch, and that it increases with the velocity, though at a rate not nearly so rapid as the square of the velocity.

The experiments on friction at different temperatures indicate a great diminution in the friction as the temperature rises. Thus in the case of land-oil, taking 6 speed of 450 revolutions per minute, the coefficient of friction at a temperature of 120° is only one third of what it was at a tempera-

ture of 60.

The journal was of steel, 4 inches diameter and 6 inches long, and a gunmetal brasa, embracing somewhat less than half the circumference of the journal, rested on its upper side, on which the load was applied. When the bottom of the journal was immersed in oil, and the oil therefore carried under the brass by rotation of the journal, the greatest load carried with range oil was 573 lbs. per source juch and with mineral oil 625 lbs.

rape-oil was 573 bs. per square inch, and with mineral oil 625 ibs.

In experiments with ordinary lubrication, the oil being fed in at the centre of the top of the brass, and a distributing groove being cut in the brass parallel to the axis of the journal, the bearing would not run cool with only 100 lbs. per square inch, the oil being pressed out from the bearing surface and through the oil-hole, instead of being carried in by it. On introducing the oil at the sides through two parallel grooves, the lubrication appeared to be satisfactory, but the bearing seized with 380 lbs. per square inch.

When the oil was introduced through two oil-holes, one near each end of the brass, and each connected with a curved groove, the brass refused to take its oil or run cool, and seized with a load of only 200 lbs. per square

inch.

With an oil-pad under the journal feeding rape-oil, the bearing fairly carried 551 lbs. Mr. Tower's conclusion from these experiments is that the friction depends on the quantity and uniformity of distribution of the oil, and may be anything between the oil-bath results and seizing, according to the perfection or imperfection of the lubrication. The lubrication may be very small, giving a coefficient of 1/100; but it appeared as though it could not be diminished and the friction increased much beyond this point without imminent risk of heating and seizing. The oil-bath probably represents the most perfect lubrication possible, and the limit beyond which friction cannot be reduced by lubrication; and the experiments show that with speeds of from 100 to 200 feet per minute, by properly proportioning the bearing surface to the load, it is possible to reduce the coefficient of friction to as low as 1/1000. A coefficient of 1/1500 is easily attainable, and probably is frequently attained, in ordinary engine-bearings in which the direction of the force is rapidly alternating and the oil given an opportunity to get between the surfaces, while the duration of the force in one direction is not sufficient to allow time for the oil film to be squeezed out.

Observations on the behavior of the apparatus gave reason to believe that with perfect lubrication the speed of minimum friction was from 100 to 150 feet per minute, and that this speed of minimum friction tends to be higher with an increase of load, and also with less perfect lubrication. By the speed of minimum friction is meant that speed in approaching which from

rest the friction diminishes, and above which the friction increases.

Coefficients of Friction of Journal with Oil-beth.—Abstract of results of Tower's experiments on friction (Froc. Inst. M. E., Nov. 188). Journal, 4 in. diam., 6 in. long, temperature, 90° F.

Lubricant in Bath.	Nominal Load, in pounds per square inc							
Zidonomio in Zoom	625	520	415	810	205	153	100	
		Coeff	lcient	s of F	rictio	n.		
Lard-oil: 157 ft. per min	••••		.0012					
157 ft. per min	.001 .002		.0016 .0027					
157 ft. per min	(578 lb.)	seiz'd		.0011 .0019				
157 ft. per min	.001	.001	.0009 .0016				.004 .007	
Mineral-oil: 157 ft. per min	.0013		.0012 .002				.004 .007	
					.0098		.0125 .0152	
Rape-oil, pad under journal: 157 ft. per min					.0105 .0078		.0099	

Comparative friction of different lubricants under same circumstances, temperature 90°, oil-bath;

Sperm-oil	100 per cent.	LardOlive-oil	135 per cent.
Mineral oil		Mineral grease	

Coefficients of Friction of Motion and of Rest of a Journal.—A cast-iron journal in steel boxes, tested by Prof. Thurston at a speed of rubbing of 150 feet per minute, with lard and with sperm oil, gave the following:

Pressures per sq. in., lbs 50 Coeff., with sperm	100 .008 .0187	250 .005 .0085	500 .004 .0053	750 .0048 .0066	1000 .009 .0125
The coefficients at starting were:					
With sperm	.185 .11	.14 .11	.15 .10	.185 .19	.18 .12

The coefficient at a speed of 150 feet per minute decreases with increase of pressure until 500 lbs. per sq. in, is reached; above this it increases. The coefficient at rest or at starting increases with the pressure throughout the range of the tests.

Value of Anti-friction Metals. (Denton.)—The various white netals available for hims brasses do not afford coefficient of friction lower than can be obtained with bare brass, but they are less liable to "overheating," because of the superiority of such material over bronse in ability to permit of abrasion or crushing, without excessive increase of friction.

Thurston (Friction and Lost Work) says that gun-bronse, Babbitt, and other soft white alloys have substantially the same friction; in other words, the friction is determined by the nature of the unguent and not by that of the rubbing-surfaces, when the latter are in good order. The soft metals run at higher temperatures than the bronze. This, however, does not necessarily indicate a serious defect, but simply deficient conductivity. The value of the white alloys for bearings lies mainly in their ready reduction to a smooth surface after any local or general injury by alteration of either surface or form.

Cast-iron for Bearings. (Joshua Rose.)—Cast iron appears to be an exception to the general rule, that the harder the metal the greater the resistance to wear, because cast iron is softer in its texture and easier to cut with steel tools than steel or wrought fron, but in some situations it is far more durable than hardened steel; thus when surrounded by steam it will wear better than will any other metal. Thus, for instance, experience has demonstrated that piston-rings of cast iron will wear smoother, better, and equally as long as those of steel, and longer than those of either wrought iron or brass, whether the cylinder in which it works be composed of brass, steel, wrought iron, or cast iron; the latter being the more noteworthy, since two surfaces of the same metal do not, as a rule, wear or work well together. So also slide-valves of brass are not found to wear so long or so smoothly as those of cast iron, let the metal of which the seating is composed be whatever it may; while, on the other hand, a cast iron slide-valve will wear longer of itself and cause less wear to its seat, if the latter is of cast iron, than if of steel, wrought iron, or brass.

Friction of Metals under Steam-pressure.—The friction of brass upon iron under steam-pressure is double that of iron upon iron. (G. H. Babcock, Trans. A. S. M. E., i. 151.)

Moria's 'Laws of Friction."—1. The friction between two bodies

is directly proportioned to the pressure; i.e., the coefficient is constant for all pressures.

2. The coefficient and amount of friction, pressure being the same, is in-

dependent of the areas in contact.

8 The coefficient of friction is independent of velocity, although static

friction (friction of rest) is greater than the friction of motion.

Eng'g News, April 7, 1888, comments on these "laws" as follows: From 1831 till about 1876 there was no attempt worth speaking of to enlarge our knowledge of the laws of friction, which during all that period was assumed to be complete, although it was really worse than nothing, since it was for the most part wholly false. In the year first mentioned Morin began a series of experiments which extended over two or three years, and which resulted in the enunciation of these three "fundamental laws of friction,"

no one of which is even approximately true.

For fifty years these laws were accepted as axiomatic, and were quoted as such without question in every scientific work published during that whole period. Now that they are so thoroughly discredited it has been attempted to explain away their defects on the ground that they cover only a very limited range of pressures, areas, velocities, etc., and that Morin himself only announced them as true within the range of his conditions. It is now clearly established that there are no limits or conditions within which any one of them even approximates to exactitude, and that there are many conditions under which they lead to the wildest kind of error, while many of the constants were as inaccurate as the laws. For example, in Morin's "Table of Coefficients of Moving Friction of Smooth Plane Surfaces, perfectly lubricated, "which may be found in bundreds of text-books now in use the coeffi-cient of wrought iron on brass is given as 075 to .108, which would make the rolling friction of railway trains 15 to 20 lbs. per ton instead of the 8 to 6 lbs. which it actually is.

General Morie, in a letter to the Secretary of the Institution of Mechanical Engineers, dated March 15, 1879, writes as follows concerning his experiments on friction made more than forty years before: "The results furnished by my experiments as to the relations between pressure, surface, and speed on the one hand, and sliding friction on the other, have always been regarded by myself, not as mathematical laws, but as close approximations to the truth, within the limits of the data of the experiments themselves. The same holds.

in my opinion, for many other laws of practical mechanics, such as those of rolling resistance, fluid resistance, etc."

Prof. J. E. Denton (Stevens Indicator, July, 1890) says: It has been generally assumed that friction between lubricated surfaces follows the simple law that the amount of the friction is some fixed fraction of the pressure be-tween the surfaces, such fraction being independent of the intensity of the pressure per square inch and the velocity of rubbing, between certain limits of practice, and that the fixed fraction referred to is represented by the coefficients of friction given by the experiments of Moria or obtained from experimental data which represent conditions of practical lubrication, such as those given in Webber's Manual of Power.

By the experiments of Thurston, Woodbury, Tower, etc., however,

appears that the friction between lubricated metallic surfaces, such as r

chine bearings, is not directly proportional to the pressure, is not independent of the speed, and that the coefficients of Morin and Webber are about tenfold too great for modern journals.

Prof. Denton offers an explanation of this apparent contradiction of au-

thorities by showing, with laboratory testing machine data, that Morin's laws hold for bearings lubricated by a restricted feed of lubricant, such as is afforded by the oil-cups common to machinery; whereas the modern ex-periments have been made with a surplus feed or superabundance of lubricant, such as is provided only in railroad car journals, and a few special

cases of practice.

That the low coefficients of friction obtained under the latter conditions That the low coemicians of triction obtained under the latter conditions are realized in the case of car-journals, is proved by the fact that the temperature of car-boxes remains at 100° at high velocities; and experiment shows that this temperature is consistent only with a coefficient of friction of a fraction of one per cent. Deductions from experiments on train resistance also indicate the same low degree of friction. But these low co-efficients do not account for the internal friction of steam-engines as well as do the coefficients of Morin and Webber.

In American Machinist, Oct. 23, 1890, Prof. Denton says: Morin's measurement of friction of lubricated journals did not extend to light pressures.

They apply only to the conditions of general shafting and engine work.

He clearly understood that there was a frictional resistance, due solely to the viscosity of the oil, and that therefore, for very light pressures, the laws which he enunciated did not prevail.

He applied his dynamometers to ordinary shaft-journals without special preparation of the rubbing-surfaces, and without resorting to artificial

methods of supplying the oil.

Later experimenters have with few exceptions devoted themselves exclusively to the measurement of resistance practically due to viscosity alone. They have eliminated the resistance to which Morin confined his measurements, namely, the friction due to such contact of the rubbing-surfaces as prevail with a very thin film of lubricant between comparatively rough surfaces.

Prof. Denton also says (Trans. A. S. M. E., x. 518): "I do not believe there is a particle of proof in any investigation of friction ever made, that Morin's

laws do not hold for ordinary practical oil-cups or restricted rates of feed."

Laws of Friction of well-lubricated Journals.—John Goodman (Trans. Inst. C. E. 1886, Engly News, Apr. 7 and 14, 1885), review ing the results obtained from the testing-machines of Thurston, Tower, and Stroudley, arrives at the following laws:

LAWS OF FRICTION: WELL-LUBRICATED SURFACES. (Oil-bath.)

1. The coefficient of friction with the surfaces efficiently lubricated is from 1/6 to 1/10 that for dry or scantily lubricated surfaces.
2. The coefficient of friction for moderate pressures and speeds varies ap-

proximately inversely as the normal pressure: the frictional resistance varies as the area in contact, the normal pressure remaining constant.

3 At very low journal speeds the coefficient of friction is abnormally high; but as the speed of sliding increases from about 10 to 100 ft per min, the friction diminishes, and again rises when that speed is exceeded, varying

approximately as the square root of the speed.

4. The coefficient of friction varies approximately inversely as the temperature, within certain limits, namely, just before abrasion takes place.

The evidence upon which these laws are based is taken from various modern experiments. That relating to Law 1 is derived from the "First Report on Friction Experiments," by Mr. Beauchamp Tower.

Method of Lubrication.	Coefficient of Friction.	Comparative Friction.
Oil-bath	.0098	1.00 7.06 6.48

With a load of 293 lbs. per sq. in, and a journal speed of 314 ft. per mir. Mr. Tower found the coefficient of friction to be .0016 with an oil-bath, and .0097, or six times as much, with a pad. The very low coefficients obtained by Mr. Tower will be accounted for by Law 2, as he found that the frictional resistance per square inch under varying loads is nearly constant, as below:

Load in lbs. per sq. in.... 529 Frictional resist. per sq. in. .416 468 415 363 810 258 205 153 100 .498 .472 .464 .488 .43 .458 .45 .514

The frictional resistance per square inch is the product of the coefficient of friction into the load per square inch on horizontal sections of the brass. Hence, if this product be a constant, the one factor must vary inversely as the other, or a high load will give a low coefficient, and vice versa.

For ordinary lubrication, the coefficient is more constant under varying loads; the frictional resistance then varies directly as the load, as shown by

Mr. Tower in Table VIII of his report (Proc. Inst. M. E. 1883).

With respect to Law 3, A. M. Wellington (Trans. A. S. C. E. 1884), in experiments on journals revolving at very low velocities, found that the friction was then very great, and nearly constant under varying conditions of the lubrication, load, and temperature. But as the speed increased the friction fell slowly and regularly, and again returned to the original amount when the velocity was reduced to the same rate. This is shown in the following table:

Speed, feet per minute: 0+2.16 3.83 4.868.82 21.42 35.37 53.01 89.28 106.02Coefficient of friction: .118 .055 .047 .040 .035 .030 .094 .069

It was also found by Prof. Kimball that when the journal velocity was increased from 6 to 110 ft. per minute, the friction was reduced 70%; in another case the friction was reduced 67% when the velocity was increased from 1 to 100 ft. per minute; but after that point was reached the coefficient varied approximately with the square root of the velocity.

The following results were obtained by Mr. Tower:

Feet per minute	209	262	814	366	419	471	Nominal Load per sq. in.
Coeff. of friction	.0010 .0013 .0014	.0014	.0015	.0017	.0018	.0017 .002 .0024	468 ''

The variation of friction with temperature is approximately in the inverse ratio, Law 4. Take, for example, Mr. Tower's results, at 262 ft. per minute:

Temp. F.	110°	100°	960	80°	70°	60°
Observed Calculated	.0044	.0051 .00518	.006 .00608	.0073	.0092 .00964	.0119 .01252

This law does not hold good for pad or siphon lubrication, as then the coefficient of friction diminishes more rapidly for given increments of temperature, but on a gradually decreasing scale, until the normal temperature has been reached; this normal temperature increases directly as the load This is shown in the following table taken from Mr. Stroudlev's per sq. in. experiments with a pad of rape oil:

Temp. F	105°	110°	115°	120°	125°	130°	1 3 5°	140°	1450
Coefficient Decrease of coeff	.022	.0180 .0040	.0160	.0140 0020	.0125 .0015	.0115 .0010	.0110 .0005	.0106 .0004	.0102

In the Galton-Westinghouse experiments it was found that with velocities below 100 ft. per min., and with low pressures, the frictional resistance varied directly as the normal pressure; but when a velocity of 100 ft. per min. was exceeded, the coefficient of friction greatly diminished; from the same experiments Prof. Kennedy found that the coefficient of friction for high pressures was sensibly less than for low.

Allowable Pressures on Bearing-surfaces. (Proc. Inst. M. E., May, 1888.)—The Committee on Friction experimented with a steel ring

rectangular section, pressed between two cast-iron disks, the annular bearing-surfaces of which were covered with gun-metal, and were 12 in inside diameter and 14 in. outside. The two disks were rotated together, and the steel ring was prevented from rotating by means of a lever, the bolding force of which was measured. When oiled through grooves cut in eac. face of the ring and tested at from 50 to 130 revs. per min., it was found that a pressure of 75 lbs. per sq. in. of bearing-surface was as much as it would bear safely at the highest speed without seizing, although it carried 90 lbs. bear sarely at the highest speed without seizing, although it carried without seizing, although it carried without seizing, and the friction is also much higher than for a cylindrical bearing, and the friction follows the law of the friction of solids much more nearly than that of liquids. This is doubtless due to the much less perfect lubrication applicable to this form of bearing compared with a cylindrical one. The coefficient of friction appears to be about the same with the same load at all speeds, or, in other words, to be independent of the speed; but it seems to diminish somewhat as the load is increased, and may be stated approximately as 1/20 at 15 lbs. per sq. in., diminishing to 1/30 at 75 lbs. per sq. in.

The high coefficients of friction are explained by the difficulty of lubricating a collar-bearing. It is similar to the slide-block of an engine, which can carry only about one tenth the load per sq. in. that can be carried by the

crank-pins.

In experiments on cylindrical journals it has been shown that when a cylindrical journal was lubricated from the side on which the pressure bore, cymingrical journal was indirected from the side on which the pressure bore 100 lbs, per sq. in, was the limit of pressure that it would carry; but when it came to be lubricated on the lower side and was allowed to drag the oil in with it, 600 lbs, per sq. in, was reached with impunity; and if the 600 lbs, per sq. in, which was reckoned upon the full diameter of the bearing, came to be reckoned on the sixth part of the circle that was taking the greater proportion of the load, it followed that the pressure upon that part of the circle amounted to about 1200 lbs. per sq. in.

In connection with these experiments Mr. Wicksteed states that in drilling-machines the pressure on the collars is frequently as high as 330 lbs, per sq. in., but the speed of rubbing in this case is lower than it was in any of the experiments of the Research Committee. In machines working very slowly and intermittently, as in testing-machines, very much higher pres-

sures are admissible.

Mr. Adamson mentions the case of a heavy upright shaft carried upon a small footstep-bearing, where a weight of at least 20 tons was carried on a shaft of 5 in. diameter, or, say, 20 sq. in. area, giving a pressure of 1 ton per sq. in. The speed was 190 to 200 revs. per min. It was necessary to force the oil under the bearing by means of a pump. For heavy horizontal shafts, such as a fly-wheel shaft, carrying 100 tons on two journals, his practice for getting oil into the bearings was to flatten the journal along one side throughout its whole length to the extent of about an eighth of an inch in width for each inch in diameter up to 8 in. diameter; above that size rather less flat in proportion to the diameter. At first sight it appeared alarming to get a continuous flat place coming round in every revolution of a heavily loaded shaft; yet it carried the oil effectually into the bearing, which ran much better in consequence than a truly cylindrical journal without a flat side.

In thrust-bearings on torpedo-boats Mr. Thornycroft allows a pressure of never more than 50 lbs. per sq. in.

Prof. Thurston (Friction and Lost Work, p. 240) says 7000 to 9000 lbs.

pressure per square inch is reached on the slow-working and rarely moved

pivots of swing bridges.

Mr. Tower says (Proc. Inst M E., Jan. 1884): In eccentric-pins of punching and shearing machines very high pressures are sometimes used without seizing. In addition to the alternation in the direction, the pressure is applied for only a very short space of time in these machines, so that the oil

has no time to be squeezed out.

In the discussion on Mr. Tower's paper (Proc. Inst. M. E. 1885) it was stated that it is well known from practical experience that with a constant load on an ordinary journal it is difficult and almost impossible to have more than 200 lbs. per square inch, otherwise the bearing would get hot and the oil go out of it; but when the motion was reciprocating, so that the load was alternately relieved from the journal, as with crank-pins and similar journals, much higher loads might be applied than even 700 or 800 lbs. per aquare inch.

Mr. Goodman (Proc. Inst. C. E. 1886) found that the total frictional resistance is materially reduced by diminishing the width of the brass.

The lubrication is most efficient in reducing the friction when the brass subtends an angle of from 1:0° to 60°. The film is probably at its best be-

tween the angles 80° and 110°

In the case of a brass of a railway axle-bearing where an oil-groove is cut along its crown and an oil-hole is drilled through the top of the brass into it, the wear is invariably on the off side, which is probably due to the oil escaping as soon as it reaches the crown of the brass, and so leaving the off side almost dry, where the wear consequently ensues.

In railway axies the brass wears always on the forward side. The same observation has been made in marine engine journals, which always wear in exactly the reverse way to what they might be expected. Mr. Stroudley thinks this peculiarity is due to a film of lubricant being drawn in from the under side of the journal to the aft part of the brass, which effectually lubricates and prevents wear on that side; and that when the lubricant reaches the forward side of the brass it is so attenuated down to a wedge shape that

there is insufficient lubrication, and greater wear consequently follows. Prof. J. E. Denton (Am. Mach., Oct. 30, 180) says: Regarding the pressure to which oil is subjected in railroad car-service, it is probably more severe than in any other class of practice. Car brasses, when used bare, are so imperfectly fitted to the journal, that during the early stages of their use the area of bearing may be but about one square inch. In this case the pressure per square inch is upwards of 6000 lbs. But at the slowest speeds of freight service the wear of a brass is so rapid that, within about thirty minutes the area is either increased to about three inches, and is thereby able to relieve the oil so that the latter can successfully prevent overheating of the journal, or else overheating takes place with any oil, and measures of relief must be taken which eliminate the question of differences of lubricating power among the different lubricants available. A brass which has been run about fifty miles under 5000 lbs. load may have extended the area of bearing surface to about three square inches. The pressure is then about 1700 lbs. per square inch. It may be assumed that this is an average minimum area for car-service where no violent and unmanageable overheating has occurred during the use of a brass for a short time. This area will very slowly increase with any lubricant.

C. J. Field (Power, Feb. 1893) says: One of the most vital points of an engine for electrical service is that of main bearings. They should have a surface velocity of not exceeding 850 feet per minute, with a mean bearingpressure per square inch of projected area of journal of not more than 80 lbs. This is considerably within the safe limit of cool performance and easy operation. If the bearings are designed in this way, it would admit the use of grease on all the main wearing-surface, which in a large type of engines for this class of work we think advisable.

Oil-pressure in a Bearing.—Mr. Beauchamp Tower (Proc. Inst. M. E. Jan. 1885) made experiments with a brass bearing 4 inches diameter M. E. Jan. 1885) made experiments with a brass bearing 4 inches diameter by 6 inches long, to determine the pressure of the oil between the brass and the journal. The bearing was half immersed in oil, and had a total load of 8008 bs. upon it. The journal rotated 150 revolutions per minute. The pressure of the oil was determined by drilling small holes in the bearing at different points and connecting them by tubes to a Bourdon gauge. It was found that the pressure varied from 310 to 625 bs. per square inch, the greatest pressure being a little to the "off" side of the centre line of the top of the bearing, in the direction of motion of the journal. The sum of the upward force exerted by these pressures for the whole lubileated area was ward force exerted by these pressures for the whole lubricated area was nearly equal to the total pressure on the bearing. The speed was reduced from 150 to 20 revolutions, but the oil-pressure remained the same, showing that the brass was as completely oil-borne at the lower speed as at the higher. The following was the observed friction at the lower speeds:

Nominal load, lbs. per square inch... Coefficient of friction 333 443 .00132 .00168 .00247 .0044

The nominal load per square inch is the total load divided by the product of the diameter and length of the journal. At the same low speed of 20 revolutions per minute it was increased to 676 lbs. per square inch without any signs of heating or seizing.

Friction of Car-journal Brasses. (J. E. Denton, Trans. A. S. M. E., xii. 405.)—A new brass dressed with an emery-wheel, loaded with 5000 lbs.. may have an actual bearing-surface on the journal, as shown by the polof a portion of the surface, of only 1 square inch. With this pressure of 5000 lbs. per square inch, the coefficient of friction may be \$\mathscr{6}\pi\$, and the brass may be overheated, scarred and cut but, on the contrary, it may wear down evenly to a smooth bearing, giving a highly polished area of contact of 3 square inches. or more, inside of two hours of running, gradually decreasing the pressure per square inch of contact, and a coefficient of friction of less than 0.5%. A reciprocating motion in the direction of the axis is of importance in reducing the friction. With such polished surfaces any oil will lubricate, and the coefficient of friction then depends on the viscosity of the oil. With a pressure of 1000 lbs per square inch, revolutions from 170 to \$20 per minute, and temperatures of 75° to 113° F. with both sperm and parraffine oils, a coefficient of as low as 0.11% has been obtained, the oil being fed continuously by a pad

Experiments on Overheating of Bearings.—Hot Boxes. (Denton.)—Tests with car brasses loaded from 1100 to 4500 lbs. per square inch gave 7 cases of overheating out of 32 trials. The tests show how purely a matter of chance is the overheating, as a brass which ran hot at 5000 lbs. load on one day would run cool on a later date at the same or higher presure. The explanation of this apparently arbitrary difference of behaviof is that the accidental variations of the smoothness of the surfaces, almost infinitesimal in their magnitude, cause variations of friction which are always tending to produce overheating, and it is solely a matter of chance when these tendencies preponderate over the lubricating influence of the oil. There is no appreciable advantage shown by sperm-oil, when there is no tendency to overheat—that is, parafine can lubricate under the highest pressures which occur, as well as sperm, when the surfaces are within the conditions affording the minimum coefficients of friction.

Sperm and other oils of high heat-resisting qualities, like vegetable oil and petroleum cylinder stocks, only differ from the more volatile lubricants, like paraffine, in their ability to reduce the chances of the continual accidental influtesimal abrasion producing overheating.

dental infinitesimal abrasion producing overheating.

The effect of emery or other gritty substance in reducing overheating of a bearing is thus explained:

The effect of the emery upon the surfaces of the bearings is to cover the latter with a series of parallel grooves, and apparently after such grooves are made the presence of the emery does not practically increase the friction over the amount of the latter when pure oil only is between the surfaces. The infinite number of grooves constitute a very perfect means of insuring a uniform oil supply at every point of the bearings. As long as grooves in the journal match with those in the brasses the friction appears to amount to only about 10% to 15% of the pressure. But if a smooth journal is placed between a set of brasses which are grooved, and pressure be applied, the journal crushes the grooves and becomes brazed or coated with brass, and then the coefficient of friction becomes upward of 40%. If then emery is applied, the friction is made very much less by its presence, because the grooves are made to match each other, and a uniform oil supply prevails at every point of the bearings, whereas before the application of the emery many spots of the latter receive no oil between them.

Moment of Friction and Work of Friction of Slidingsurfaces, etc.

	Moment of Fric- tion, inch-lbs.	Energy lost by Friction in ftlbs. per min.
Flat surfaces	14fWd 14fWr	fWS .2618fWdn .349fWrn
Collar-bearing	$\frac{2}{6}fW\frac{r_2^3-r_1^3}{r_2^2-r_1^3}$	$349 f W n \frac{r_2^3 - r_1^3}{r_2^2 - r_1^2}$
Conical pivot	%fWr cosec a %fWr sec a	·349fWrn cosec a ·349fWrn sec a
Truncated-cone pivot	$\frac{3}{6}fW\frac{r_2^3-r_1^3}{r_2\sin a}$	$.849 fW \frac{r_2^2 - r_1^2}{r_2 \sin \alpha}$
Hemispherical pivot	· fWr	.5296f Wrn
Tractrix, or Schiele's "anti- friction" pivot	fWr	.5286 f Wrn

In the above f = coefficient of friction; W = weight on journal or pivot in pounds; r = radius, d = diameter, in inches; S = space in feet through which sliding takes place; $r_1 = \text{outer radius}, r_1 = \text{inner radius};$ n = number of revolutions per minute;

a = the half-angle of the cone, i.e., the angle of the slope with the axis.

To obtain the horse-power, divide the quantities in the last column by 33,000. Horse-power absorbed by friction of a shaft = $\frac{fWdn}{126050}$

The formula for energy lost by shafts and journals is approximately true for loosely fitted bearings. Prof. Thurston shows that the correct formula varies according to the character of fit of the bearing; thus for loosely fitted journals, if U = the energy lost,

$$U = \frac{2f\pi r}{\sqrt{1+f^2}} Wn \text{ inch-pounds} = \frac{.2618fWdn}{\sqrt{1+f^2}} \text{ foot-lbs.}$$

For perfectly fitted journals U=2.54fwrWn inch-lbs. = .3325fWdn, ft.-lbs. For a bearing in which the journal is so grasped as to give a uniform pressure throughout, $U=fv^3+Wn$ inch-lbs. = .4112fWdn, ft.-lbs. Resistance of railway trains and wagons due to friction of trains:

Pull on draw-bar =
$$\frac{f \times 2240}{R}$$
 pounds per gross ton,

in which R is the ratio of the radius of the wheel to the radius of journal. A cylindrical journal, perfectly fitted into a bearing, and carrying a total load, distributes the pressure due to this load unequally on the bearing, the maximum pressure being at the extremity of the vertical radius, while at the extremities of the horizontal diameter the pressure is zero. At any point of the bearing-surface at the extremity of a radius which makes an angle θ with the vertical radius the normal pressure is proportional to $\cos \theta$. If p = normal pressure on a unit of surface, w = total load on a unit of length of the journal, and r = radius of journal. length of the journal, and r = radius of journal,

$$w\cos\theta = 1.57rp, \quad p = \frac{w\cos\theta}{1.57r}.$$

PIVOT-BEARINGS.

The Schiele Curve.-W. H. Harrison, in a letter to the Am. Machinist, 1891, says the Schiele curve is not as good a form for a bearing as the ist, 1891, says the Schiele curve is not as good a form for a bearing as the segment of a sphere. He says: A mill-stone weighing a ton frequently bears its whole weight upon the flat end of a hard-steel pivot 1½" diameter, or one square inch area of bearing; but to carry a weight of 3000 lbs. he advises an end bearing about 4 inches diameter, made in the form of a segment of a sphere about ½ inch in height. The die or fixed bearing should be dished to fit the pivot. This form gives a chance for the bearing to adjust itself, which it does not have when made flat, or when made with the Schiele curve. If a side bearing is necessary it can be arranged farther up the shaft. The pivot and die should be of steel, hardened; cross-gutters should be in the die to allow oil to flow, and a central oil-hole should be should be in the die to allow oil to flow, and a central oil-hole should be made in the shaft.

The advantage claimed for the Schiele bearing is that the pressure is uniformly distributed over its surface, and that it therefore wears uniformly Wilfred Lewis (An. Mach., April 19, 1894) says that its merits as a thrust-bearing have been vastly overestimated; that the term "anti-friction" applied to it is a misnomer, since its friction is greater than that of a flat step or collar of the same diameter. He advises that flat thrust-bearings should always be annular in form, having an inside diameter one half of the external diameter

Friction of a Flat Pivot-bearing.—The Research Committee on Friction (Proc. Inst. M. E. 1891) experimented on a step-bearing, flatended, 8 in. diam., the oil being forced into the bearing through a hole in its centre and distributed through two radial grooves, insuring thorough lubrication. The step was of steel and the bearing of manganese-bronze.

At revolutions per min	. 50.	126	194	200	353
The coefficient of friction varied	.0131	.0058	.0851	.0044	.9053
bet ween	and .0221	.0118	.0 102	.0178	.0167

With a white-metal bearing at 128 revolutions the coefficient of friction was a little larger than with the manganese-bronze. At the higher speeds was a miss super than with the mangames-oronze. At the ingres speech the coefficient of friction was less, owing to the more perfect lubrication, as shown by the more rapid circulation of the oil. At 128 revolutions the bronze bearing heated and seized on one occasion with a load of 260 pounds and on another occasion with 300 pounds per square iach. The white metal bearing under similar conditions heated and seized with a load of 260 pounds are squared inch. The white metal of 260 pounds are squared inch. pounds per square inch. The steel footstep on manganese-bronze was afterwards tried, lubricating with three and with four radial grooves; but the friction was from one and a half times to twice as great as with only the two groovs. (See also Allowable Pressures, page 956.)

Mercury-bath Pivet.—A nearly frictionless step-bearing may be obtained by floating the bearing with its superincumbent weight upon mer-

cury. Such an apparatus is used in the lighthouses of La Heve, Havre. It is thus described in Eng'g, July 4, 1898, p. 41:

The optical apparatus, weighing about 1 ton, rests on a circular cast-iron

table, which is supported by a vertical shaft of wrought iron 2.36 in.

diameter.

This is kept in position at the top by a bronze ring and outer iron support, and at the bottom in the same way, while it rotates on a removable steel pivot resting in a steel socket, which is fitted to the base of the support. To the vertical shaft there is rigidly fixed a floating cast-iron ring 17.1 in. diameter and 11.8 in. in depth, which is plunged into and rotates in a mercury bath contained in a fixed outer drum or tank, the clearance between twentical surfaces of the drum and ring being only 0.2 in., so as to reduce as much as possible the volume of mercury (about 220 lbs.), while the horizontal clearance at the bottom is 0.4 in.

BALL-BEARINGS, FRICTION ROLLERS, ETc.

A. H. Tyler ($Eng^{\circ}g$, Oct. 20, 1898, p. 483), after experiments and comparison with experiments of others arrives at the following conclusions:

That each ball must have two points of contact only.

The balls and race must be of glass hardness, and of absolute truth.

The balls should be of the largest possible diameter which the space at disposal will admit of.

Any one ball should be capable of carrying the total load upon the bearing. Two rows of balls are always sufficient.

A ball-bearing requires no oil, and has no tendency to heat unless overloaded.

Until the crushing strength of the balls is being neared, the frictional resistance is proportional to the load.

The frictional resistance is inversely proportional to the diameter of the balls, but in what exact proportion Mr. Tyler is unable to say. Probably it varies with the square.

The resistance is independent of the number of balls and of the speed.

No rubbing action will take place between the balls, and devices to guard

against it are unnecessary, and usually injurious.

The above will show that the ball-bearing is most suitable for high speeds The above will know that the oshi-bearing is most satisfied in fight specials and light loads. On the spindles of wood-carving machines some make as much as 30,000 revolutions per minute. They run perfectly cool, and never have any oil upon them. For heavy loads the balls should not be less than two thirds the diameter of the shaft, and are better if made equal to it.

Ball-bearings have not been found satisfactory for thrust-blocks, for the shaft of the s

the reason apparently that the tables crowd together. Better results have been obtained from coned rollers. A combined system of rollers and balls is described in Eng. 0. Oct. 6, 1898, p. 429.

Friction-rollers.—If a journal instead of revolving on ordinary

bearings be supported on friction-rollers the force required to make the journal revolve will be reduced in nearly the same proportion that the diameter of the axles of the rollers is less than the diameter of the rollers themselves. In experiments by A. M. Wellington with a journal 8½ in. diam. supported on rollers 8 in. diam., whose axies were 1½ in. diam., the friction in starting from rest was ½ the friction of an ordinary 3½-in. bearing, but at a car speed of 10 miles per hour it was ½ that of the ordinary bearing. The ratio of the diam. of the axie to diam. of roller was 1½:8, or as 1 to 4.6. Bearings for Very High Botative Speeds. (Proc. Inst. M. E., Oct. 1888, p. 482.)—In the Parsons steam-turbine, which has a speed of as high as 18,000 rev. per min., as it is impossible to secure absolute accuracy of balance, the bearings are of special construction so as to allow of a certain very small amount of lateral freedom. For this purpose the bearing is surrounded by two sets of steel washers 1/16 inch thick and of different diameters, the larger fitting close in the casing and about 1/32 inch clear of the bearing, and the smaller fitting close on the bearing and about 1/32 inch clear of the casing. These are arranged alternately, and are pressed together by a spiral spring. Consequently any lateral movement of the bearing causes them to slide mutually against one another, and by their friction to check or damp any vibrations that may be set up in the spindle. The tendency of the spindle is then to rotate about its axis of mass, or principle lateral the called and the bearing are the propriety of the spindle is then to rotate about its axis of mass, or principle lateral the called and the bearing are the propriety of the spindle. cipal axis as it is called; and the bearings are thereby relieved from excessive pressure, and the machine from undue vibration. The finding of the centre of gyration, or rather allowing the turbine itself to find its cwn centre of gyration, is a well-known device in other branches of mechanics: as in the instance of the centrifugal hydro-extractor, where a mass very much out of balance is allowed to find its own centre of gyration; the faster it ran the more steadily did it revolve and the less was the vibration. Another illustration is to be found in the spindles of spinning machinery, which run at about 10,000 or 11,000 revolutions per minute: they are made of hardened and tempered steel, and although of very small dimensions, the outside diameter of the largest portion or driving whorl being perhaps not more than 1½ in., it is found impracticable to run them at that speed in what might be called a hard-and-fast bearing. They are therefore run with some elastic substance surrounding the bearing, such as steel springs, hemp. or cork. Any elastic substance is sufficient to absorb the vibration, and permit of absolutely steady running.

FRICTION OF STEAM-ENGINES.

Distribution of the Friction of Engines.-Prof. Thurston in his "Friction and Lost Work," gives the following:

	1.	2.	8.
Main bearings	47.0	85.4	85.0
Piston and rod	82.9	25,0	21.0
Crank-pin	6.8	5.1)	18.0
Cross-head and wrist-pinValve and rod	5.4	4.1 (10.0
Valve and rod	2.5	26.4	22.0
Eccentric strap	5.8	4.0 ₹	22.0
Link and eccentric	••••		9.01
Total	100.0	100.0	100.0

No. 1, Straight-line, 6" × 19", balanced valve; No. 2, Straight-line, 6" × 12", unbalanced valve; No. 3, 7" × 10", Lansing traction locomotive valve-gear. Prof. Thurston's tests on a number of different styles of engines indicate that the friction of any engine is practically constant under all loads. (Trans. A. S. M. E., viii. 38; ix. 74.)

In a Straight-line engine, 8" × 14", I.H.P. from 7.41 to 57.54, the friction H. P. varied irregularly between 1.97 and 4.03, the variation being independent of the load. With 50 H.P. on the brake the I.H.P. was only 52.6, the friction being only 2.6 H.P. or about 54

being only 2.6 H.P., or about 5%.

In a compound condensing-engine, tested from 0 to 102.6 brake H.P., gave I.H.P. from 14.92 to 117.8 H.P., the friction H.P. varying only from 14.92 to 17.42. At the maximum load the friction was 15.2 H.P., or 12.95. The friction increases with increase of the boller-pressure from 30 to 70 lbs., and then becomes constant. The friction generally increases with in

crease of speed, but there are exceptions to this rule.

Prof. Denton (Stevens Indicator, July, 1890), comparing the calculated friction of a number of engines with the friction as determined by measurement, finds that in one case, a 75-ton ammonia ice-machine, the friction of the compressor, 17.4 H.P., is accounted for by a coefficient of friction of 75.6 on all the external bearings, allowing 65 of the entire friction of the machine for the friction of pistons, stuffing-boxes, and valves. In the case of the Pawtucket pumping-engine, estimating the friction of the external bearings with a coefficient of friction of 65 and that of the pistons, valves, and stuffing-boxes as in the case of the ice-machine, we have the total friction of the first distributed as follows:

	Horse- power.	Per cent of Whole.
Crank-pins and effect of piston-thrust on main shaft	0.71	11.4
		32.4
Steam-valves	0.23	8.7
Eccentric	0.07	1.2
Pistons	0.48	7.2
Stuffing-boxes, six altogether	0.72	11.3
Air-pump		82.8
Total friction of engine with load	6.21	100.0

The friction of this engine, though very low in proportion to the indicated power, is satisfactorily accounted for by Morin's law used with a coefficient of friction of 5%. In both cases the main items of friction are those due to the weight of the fly-wheel and main shaft and to the piston-thrust on crank-pins and main-shaft bearings. In the ice-machine the latter items are the larger owing to the extra crank-pin to work the pumps, while in the Pawtucket engine the former preponderates, as the crank-thrusts are partly absorbed by the pump-pistons, and only the surplus effect acts on the crank-shaft.

Prof. Denton describes in Trans. A. S. M. E., x. 392, an apparatus by which he measured the friction of a piston packing-ring. When the parts of the piston were thoroughly devoid of lubricant, the coefficient of friction was found to be about 74%; with an oil-feed of one drop in two minutes the coefficient was about 5%; with an oil-feed of one drop in two minutes the rates of feed gave unsatisfactory lubrication, the piston groaning at the ends of the stroke when run slowly, and the flow of oil left upon the surfaces was found by analysis to contain about 5% of iron. A feed of two drops per minute reduced the coefficient of friction to about 1%, and gave practically perfect lubrication, the oil retaining its natural color and purity.

LUBRICATION.

Measurement of the Durability of Lubricants. (J. E. Den. ton, Trans. A. S. M. E., xi. 1018.)-Practical differences of durability of lubricants depend not on any differences of inherent ability to resist being "worn out" by rubbing, but upon the rate at which they flow through and away from the bearing surfaces. The conditions which control this flow are so delicate in their influence that all attempts thus far made to measure durability of lubricants may be said to have failed to make distinctions of lubricating value having any practical significance. In some kinds of service the limit to the consumption of oil depends upon the extent to which dust or other refuse becomes mixed with it, as in railroad car lubrication and in the case of agricultural machinery. The economy of one oil over another, so far as the quality used is concerned—that is, so far as durability is concerned—is simply proportional to the rate at which it can insinuate itself into and flow out of minute orifices or cracks. Oils will differ in their ability to do this, first, in proportion to their viscosity, and, second, in proportion to the capillary properties which they may possess by virtue of the particular ingredients used in their composition. Where the thickness of film between rubbiling yeoletics which may may present a dients used in their composition. Where the thickness of film between rubbing-surfaces must be so great that large amounts of oil pass through bearings in a given time, and the surroundings are such as to permit oil to be fed at high temperatures or applied by a method not requiring a perfect fluidity, it is probable that the least amount of oil will be used when the viscosity is as great as in the petroleum cylinder stocks. When, however, the oil must flow freely at ordinary temperatures and the feed of oil is restricted, as in the case of crank-pin bearings, it is not practicable to feed such heavy oils in a satisfactory manner. Oils of fluidity approximating to lard-oil must then be used. Oils of less viscosity or of a

Belative Value of Lubricants. (J. E. Denton, Am. Mach., Oct. 30, 1890.)—The three elements which determine the value of a lubricant are the cost due to consumption of lubricants, the cost spent for coal to overcome the frictional resistance caused by use of the lubricant, and the cost due to

the metallic wear on the journal and the brasses.

The Qualifications of a Good Lubricant, as laid down by W. H. Bailey, in Proc. Inst. C. E., vol. xlv., p. 372, are: 1. Sufficient body to keep the surfaces free from contact under maximum pressure. 2. The

greatest possible fluidity consistent with the foregoing condition. 3. The lowest possible coefficient of friction, which in bath lubrication would be for fluid friction approximately. 4. The greatest capacity for storing and carrying away heat. 5. A high temperature of decomposition. 6. Power to resist oxidation or the action of the atmosphere. 7. Freedom from corrosive ac ion on the metals upon which used.

Amount of 0il needed to Bun an Engine.—The Vacuum Oil Co. in 1892, in response to an inquiry as to cost of oil to run a 1000-H.P. Co. in 1803, in response to an inquiry as to cost of oil to run a 1000-H. Corliss engine, wrote: The cost of running two engines of equal size of the same make is not always the same. Therefore while we could furnish figures showing what it is costing some of our customers having Corliss engines of 1000 H.P. we could only give a general idea, which in itself might be considerably out of the way as to the probable cost of cylinderand engine-oils per year for a particular engine. Such an engine ought to run readily on less than 8 drops of 600 W oil per minute. If 3000 drops are figured to the quart, and 8 drops used per minute, it would take about two and one half barrels (52.5 gallons) of 600 W cylinder-oil, at 65 cents per sallon or about \$85 for cylinder-oil per year, running 6 days a week and 10 gallon, or about \$85 for cylinder-oil per year, running 6 days a week and 10 hours a day. Engine-oil would be even more difficult to guess at what the cost would be, because it would depend upon the number of cups required on the engine, which varies somewhat according to the style of the engine. It would doubtless be safe, however, to calculate at the outside that not

more than twice as much engine-oil would be required as of cylinder-oil.

The Vacuum Oil Co. in 1892 published the following results of practice

with "600 W" cylinder-oil:

Ball

minutes.

Results of tests on ocean-steamers communicated to the author by Prof. Denton in 1892 gave: for 1200-H.P. marine engine, 5 to 6 English gallons (6 to 7.2 U.S. gals.) of engine-oil per 24 hours for external lubrication; and for a 1500-H.P. marine engine, triple expansion, running 75 revs. per min., 6 to 7 English gals. per 24 hours. The cylinder-cil consumption is exceedingly variable.—from 1 to 4 gals. per day on different engines, including cylinderoil used to swab the piston-rods.

Quantity of Oil used on a Locomotive Crank-pin.—Prof. Denton, Trans. A. S. M. E., xi. 1020, says: A very economical case of practical oil-consumption is when a locomotive main crank-pin consumes about six cubic inches of oil in a thousand miles of service. This is equivalent to a consumption of one milligram to seventy square inches of surface rubbed

The Examination of Lubricating-oils. (Prof. Thos. B. Stillman, Stevens Indicator, July, 1890.)—The generally accepted conditions of a good lubricant are as follows:

1. "Body" enough to prevent the surfaces, to which it is applied, from coming in contact with each other. (Viscosity.)

2. Freedom from corrosive acid, either of mineral or animal origin.

3. As fluid as possible consistent with "body."

4. A minimum coefficient of friction.
5. High "flash" and burning points.
6. Freedom from all materials liable to produce oxidation or "gumming." The examinations to be made to verify the above are both chemical and mechanical, and are usually arranged in the following order:

1. Identification of the oil, whether a simple mineral oil, or animal oil, or a mixture.

2. Density. 3. Viscosity. 4. Flash-point.

5. Burning-point.

6. Acidity. 7. Coefficient of friction.

8. Cold test.

Detailed directions for making all of the above tests are given in Prof.

Stillman's Article. See also Stillman's Engineering Chemistry, p. 366.

Notes on Specifications for Petroleum Lubricants. (C. M. Everest, Vice-Pres. Vacuum Oil Co. Proc. Engineering Congress, Chicago World's Fair, 1898.)—The specific gravity was the first standard established for determining quality of lubricating oils, but it has long since been discarded as a conclusive test of lubricating quality. However, as the specific gravity of a particular netroleum oil increases the viscosity also increases. gravity of a particular petroleum oil increases the viscosity also increase

The object of the fire test of a lubricant, as well as its flash test, is the pre vention of danger from fire through the use of an oil that will evolve in-flammable vapors. The lowest fire test permissible is 800°, which gives a liberal factor of safety under ordinary conditions.

The cold test of an oil, i.e , the temperature at which the oil will congeal. should be well below the temperature at which it is used; otherwise the co-

efficient of friction would be correspondingly increased.

Viscosity, or fluidity, of an oil is usually expressed in seconds of time in which a given quantity of oil will flow through a certain orafice at the temperature stated, comparison sometimes being made with water, sometimes with sperm-oil, and again with rape seed oil. It seems evident that within limits the lower the viscosity of an oil (without a too near approach to metallic contact of the rubbing surfaces) the lower will be the coefficient of friction. But we consider that each bearing in a mill or factory would probably require an oil of different viscosity from any other bearing in the mill, in order to give its lowest coefficient of friction, and that slight variations in the condition of a particular bearing would change the requirements of that bearing; and further, that when nearing the "danger point" the question of viscosity alone probably does not govern.

The requirement of the New England Manufacturers' Association, that

an oil shall not lose over 5% of its volume when heated to 140° Fahr, for 12

hours, is to prevent losses by evaporation, with the resultant effects.

The precipitation test gives no indication of the quality of the oil itself, as the free carbon in improperly manufactured oils can be easily removed.

It is doubtful whether oil buyers who require certain given standards of laboratory tests are better served than those who do not. Some of the standards are so faulty that to pass them an oil manufacturer must supply oil he knows to be faulty; and the requirements of the best standards can generally be met by products that will give inferior results in actual service.

Penna, R. B. Specifications for Petroleum Products,

1900.—Five different grades of petroleum products will be used.

The materials desired under this specification are the products of the distillation and refining of petroleum unmixed with any other substances.

150° Fire-test Oil.—This grade of oil will not be accepted if sample (1) is not "water white" in color: (2) flashes below 130° Fahrenheit; (3) burns below 151° Fahrenheit; (4) is cloudy or shipment has cloudy barrels when received, from the presence of glue or suspended matter; (5) becomes opaque or shows cloud when the sample has been 10 minutes at a tempera-

ture of 0° Fahrenheit.

300° Fire-test Oil.—This grade of oil will not be accepted if sample (i) is not "water-white" in color; (2) flashes below 249° Fahrenheit; (4) burse below 249° Fahrenheit; (4) to cloudy or shipment has cloudy barrels when received, from the presence of glue or suspended matter; (5) becomes opaque or shows cloud when the sample has been 10 minutes at a tempera-ture of 32° Fahrenheit; (6) shows precipitation when some of the sample is heated to 450° F. The precipitation test is made by having about two fluid ounces of the oil in a six-ounce beaker, with a thermometer suspended in the oil, and then heating slowly until the thermometer shows the required

temperature. The oil changes color, but must show no precipitation.

Paraffine and Neutral Oils.—These grades of oil will not be accepted if
the sample from shipment (1) is so dark in color that printing with longprimer type cannot be read with ordinary daylight through a layer of the oil ½ inch thick; (2) flashes below 298° F.; (3) has a gravity at 60° F., below 21° or above 35° Baumé; (4) from October lat to May ist has a cold test above 10° F., and from May 1st has a cold test above 32° F.

The color test is made by having a layer of the oil of the prescribed thickness in a proper glass vessel, and then putting the printing on one side of the vessel and reading it through the layer of oil with the back of the observer

toward the source of light.

Well Oil.—This grade of oil will not be accepted if the sample from shipment (1) flashes, from May 1st to October 1st, below 29° F., or from October 1st to May 1st to 02° F., below 28° or above 31° Baumé; (3) from October 1st to May 1st has a cold test above 10° F., and from May 1st to October 1st has a cold test above 10° F., and from May 1st to October 1st has a cold test above 32° F.; (4) shows any precipitation when 5 cubic centimetres are mixed with 95 c. c. of gasoline. The precipitation test to exclude tarry and suspended matter. It is made by putting 26 c.c. of 98° B gasoline, which must not be above 80° F. in temperature, into a 100 c. c.

graduate, then adding the prescribed amount of oil and shaking thoroughly. Allow to stand ten minutes. With satisfactory oil no separated or precipitated material can be seen.

500° Fire-test Oil.—This grade of oil will not be accepted if sample from shipment (1) flashes below 494° F.; (2) shows precipitation with gasoline when tested as described for well oil.

Printed directions for determining flashing and burning tests and for making cold tests and taking gravity are furnished by the railroad com-

Penna. B. R. Specifications for Lubricating Oils (1894). (In force 1902.)

Constituent Oils.	Parts by volume.											
Extra lard-oil. Extra No. 1 lard-oil. 5 v° fire-test oil. Paraffine oil. Well oil.	1	i :	1 1 4	1 1 2	1 2 1	1 1 4	1 1 2	1 2 1	1			
Used for	A	B	$\overline{C_1}$	C ₂	C ₃	D_1	D_2	$\overline{D_3}$	E			

A, freight cars; engine oil on shifting-engines; miscellaneous greasing in α , treignt cars; engine oil on shifting-engines; miscellaneous greasing in foundries, etc. B, cylinder lubricant on marine equipment and on stationary engines. C, engine oil; all engine machinery; engine and tender truck boxes; shafting and machine tools; bolt cutting; general lubrication except cars. D, passenger-car lubrication. E, cylinder lubricant for locomotives. C_1 , D_1 , for use in Dec., Jan., and Feb.; C_2 , D_2 , in March, April. May. Sept., Oct., and Nov.; C_2 , D_3 , in June, July, and August. Weights per gallon. A, 7.4 lbs.; B, C, D, E, 7.5 lbs.

Soda Mixture for Machine Tools. (Penna R. R. 1894.)—Dissolve to blos of common sal-soda in 40 gallons of water and stir thoroughly. When needed for use mix a gallon of this solution with about a pint of engine oil. Used for the cutting parts of machine tools instead of oil.

SOLID LUBRICANTS.

Graphite in a condition of powder and used as a solid lubricant, so called, to distinguish it from a liquid lubricant, has been found to do well

where the latter has failed.

Rennie, in 1829, says: "Graphite lessened friction in all cases where it was used." General Morin, at a later date, concluded from experiments and Prof. that it could be used with advantage under heavy pressures; and Prof. Thurston found it well adapted for use under both light and heavy pressures when mixed with certain oils. It is especially valuable to prevent abrasion and cutting under heavy loads and at low velocities

Soapstome, also called talc and steatite, in the form of powder and mixed with oil or fat, is sometimes used as a lubricant. Graphite or soapstone, mixed with soap, is used on surfaces of wood working against either

iron or wood.

iron or wood.

Fibre-graphite.—A new self-lubricating bearing known as fibre-graphite is described by John H. Cooper in Trans. A. S. M. E., xili. 374, as the invention of P. H. Holmes, of Gardiner, Me. This bearing material is composed of selected natural graphite, which has been finely divided and freed from foreign and gritty matter, to which is added wood-fibre or other growth mixed in water in various proportions, according to the purpose to be served, and then solidified by pressure in specially prepared moulds; after removal from which the bearings are first thoroughly dried, then saturated with a drying oil, and finally subjected to a current of hot, dry air for the purpose of oxidizing the oil, and hardening the mass. When finished, they may be "machined" to size or shape with the same facility and means employed on metals. (Holmes Fibre-Graphite Mig. Co. Philadelphia)

employed on metals. (Holmes Fibre-Graphite Mig. Co., Philadelphia.)

Metaline is a solid compound, usually containing graphite, made in the form of small cylinders which are fitted permanently into holes drilled in the surface of the bearing. The bearing thus fitted runs without any other lubrication. (North American Metaline Co., Long Island City, N. Y.)

THE FOUNDRY.

CUPOLA PRACTICE.

The following notes, with the accompanying table, are taken from an article by Simpson Bolland in American Machinist, June 30, 1892. The table shows heights, depth of bottom, quantity of fuel on bed, proportion of fuel and iron in charges, diameter of main blast-pipes, number of tuyeres. blast-pressure, sizes of blowers and power of engines, and melting capacity per hour, of cupolas from 24 inches to 84 inches in diameter.

Capacity of Cupola.—The accompanying table will be of service in deter-

mining the capacity of cupola needed for the production of a given quantity

of iron in a specified time.

First, ascertain the amount of iron which is likely to be needed at each cast, and the length of time which can be devoted profitably to its disposal; and supposing that two hours is all that can be spared for that purpose, and that ten tons is the amount which must be melted, find in the column, Melting Capacity per hour in Pounds, the nearest figure to five tons per hour, which is found to be 10,760 pounds per hour, opposite to which in the column Diameter of Cupolas, Inside Lining, will be found 48 inches; this will be the size of cupola required to furnish ten tons of molten iron in two hours.

Or suppose that the heats were likely to average 6 tons, with an occasional increase up to ten, then it might not be thought wise to incur the extra expense consequent on working a 48-inch cupola, in which case, by following the directions given, it will be found that a 40-inch cupola would answer the purpose for 6 tons, but would require an additional hour's time for melting

whenever the 10-ton heat came along.

The quotations in the table are not supposed to be all that can be melted in the hour by some of the very best cupolas, but are simply the amounts which a common cupola under ordinary circumstances may be expected to melt in the time specified.

Height of Cupola.-By height of cupola is meant the distance from the

base to the bottom side of the charging hole.

Depth of Bottom of Cupola.—Depth of bottom is the distance from the sand-bed, after it has been formed at the bottom of the cupola, up to the under side of the tuyeres.

All the amounts for fuel are based upon a bottom of 10 inches deep, and any departure from this depth must be met by a corresponding change in the quantity of fuel used on the bed; more in proportion as the depth is increased, and less when it is made shallower.

Amount of Fuel Required on the Bed.—The column "Amount of Fuel required on Bed, in Pounds" is based on the supposition that the cupola is a straight one all through, and that the bottom is 10 inches deep. If the bottom be more, as in those of the Colliau type, then additional fuel will be

The amounts being given in pounds, answer for both coal and coke, for, should coal be used, it would reach about 15 inches above the tuyeres; the same weight of coke would bring it up to about 22 inches above the tuyeres,

which is a reliable amount to stock with.

First Charge of Iron.—The amounts given in this column of the table are safe figures to work upon in every instance, yet it will always be in order, after proving the ability of the bed to carry the load quoted, to make a slow and gradual increase of the load until it is fully demonstrated just how much

burden the bed will carry.

Succeeding Charges of Fuel and Iron.—In the columns relating to succeeding charges of fuel and iron, it will be seen that the highest proportions are not favored, for the simple reason that successful melting with any greater proportion of iron to fuel is not the rule, but, rather, the exception. proportion of iron to fuel is not the rule, out, taker, the exception. Whenever we see that from has been melted in prime condition in the proportion of 12 pounds of iron to one of fuel, we may reasonably expect that the talent, material, and cupola have all been up to the highest degree of excellence. Diameter of Main Blast-pipe.—The table gives the diameters of main blast-pipes for all cupolas from 24 to 84 inches diameter. The sizes given

opposite each cupola are of sufficient area for all lengths up to 100 feet.

Cupola Practice.

Melting Ca- pacity per	Pounds,	1,500	5,000	2,500	3,000	8,500	4,000	4,850	5,640	6,460	7,550	8,640	9,730	10,760	11,790	12.850	13,850	14,880	15,910	16,940	18,340	19,770	21,200	22,630	24.060	26.070	27.980	29.890	31,800	88,710	85,690	87,580
H.P. of Engine to drive Sturtevant Blower.	H.P.	1	1	1	cs.	CS.	o.	00	00	60	276	512	515	93%	987	93,	16	16	16	55	55	25	55	55	250	85	200	355	35	35	200	48
Sizes of Sturtevant Blower,	No.	os.	CS.	CS.	00	00	တ	4	4	4	10	10	10	9	9	9	1-	-	7	00	80	00	00	00	00	6	6	6	6	6	6	10
H.P. of Engine to drive	H.P.	3%	1,	11/4	116	13%	c	216	31%	4	9	27%	81%	10,	22	13	14	16	1716	1812	50	55	53	52	22	655	25	37	40	42	45	47
Revolutions per minute		250	335	210	550	565	3333	241	585	325	235	270	304	212	536	256	277	170	180	192	808	33	240	142	150	163	175	8	200	140	148	160
Sizes of Root Blower re- quired.	No.	1,6	72		-	-		cs	cs	O.	00	20	60	4	4	4	4	10	10	10	20	kQ.	20	9	9	9	9	9	9	2	2	
Blast-press, required,	Oz,	9	9	9	-	2-	t	00	00	œ	10	10	10	12	55	22	14	14	14	14	14	14	14	14	14	16	16	16	16	16	16	16
Number and Dimensions I flat Tuyeres equivalent the 6-inch round ones.	Dimensions.	×	1416" × 2"	×	×	×	×	×	13' × 2"	×	×	×	×	1312" × 912"	×	×	×	×	×	×	×	×	×	×	×	×	×	×	×	1816" × 816"	×	
Num of flat to the	No.	25	00	00	00	4	4	4	9	9	9	9	9	9	00	00	00	œ	00	00	00	00	00	10	10	10	15	61	15	123	14	16
Yumber of Tuyeres 6 inches dism, required for eachCup'la,	No.	1.5	65	2.6	2.6	00	00.00	2.3	5.	20	5.8	00	8.9	8.9	80	10.7	10.7	12.3	12.2	13.7	18.7	15.4	15.4	17.1	19.	19	22.9	53.9	.98	26.	88	31
Diam. Main Biast - pipe when notex- ceed'g 100ft, in length,	Inches,	10	10	10	15	25	12	14	14	14	16	16	16	18	18	18	30	50	08	553	555	222	555	55	555	24	54	94	54	57	76	96
Succeeding charges of fron,	Pounds.	500	858	1.206	1.584	1 962	2.340	2,718	3.096	3,474	3,852	4.230	4.608	4.986	5.364	5,742	6.120	6,498	6.876	7,254	7.632	8,110	8,388	8,766	9.144	0 599	0000	10,978	10,656	11.184	11 419	2002
Succeeding charges of Fuel,	inds.	50	36	134	176	818	560	305	344	386	458	470	512	554	969	638	089	722	764	806	848	890	935	974	1.016	1 058	1,100	1 149	1 184	1 996	1 968	1,000
First charge of Iron.	Pounds.	006	1.170	1.440	1.710	1 980	2.250	2,520	2,790	3,060	3,330	3,600	8.870	4,140	4.410	4.680	4.950	5,220	5,490	5,760	6.030	6.300	6.570	6,840	2,110	7 380	7,850	2,000	8 100	8 460	8 730	0000
Am't of Fuel required in bed,	Pounds.	800	390	480	570	099	750	840	930	1.020	1.110	1.200	1.290	1,380	1.470	1,560	1.650	1.740	1.830	1.920	2,010	2,100		0.980		0.98				0.850		
Depth, from sand-bed to nnder side of Tuyeres,	Inches.	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	200
Height of A'ur pola from bot'm plate to bottom of charging of charging	Feet.	10	10	10	15	5	15	15	5	13	133	13	13	133	14	14	14	14	14	15	15	15	15	15	16	16	16	16	16	16	18	9
Diam, of Cu- pola inside lining.	Inches.	54	56	88	30	68	34	36	38	40	45	44	46	48	20	52	54	56	28	09	62	64	99	89	0.2	20	7.4	7.8	200	80	80	20

Tuyeres for Cupola.—Two columns are devoted to the number and sizes of tuyeres requisite for the successful working of each cupola; one gives the number of pipes 6 inches diameter, and the other gives the number and dimensions of rectangular tuyeres which are their equivalent in area.

From these two columns any other arrangement or disposition of tuyeres may be made, which shall answer in their totality to the areas given in the

When cupolas exceed 60 inches in diameter, the increase in diameter should begin somewhere above the tuyeres. This method is necessary in all common cupolas above 60 inches, because it is not possible to force the blast to the middle of the stock, effectively, at any greater liameter.

On no consideration must the tuyere area be reduced; thus, an 84-inch cupola must have tuyere area equal to 31 pipes 6 inches diameter, or 16 flat tuyeres 16 inches by 13½ inches.

If it is found that the given number of flat tuyeres exceed in circumference that of the diminished part of the cupola, they can be shortened, allowing the decreased length to be added to the depth, or they may be built in on end; by so doing, we arrive at a modified form of the Blakeney cupola.

Another important point in this connection is to arrange the tuyeres in such a manner as will concentrate the fire at the melting-point into the smallest possible compass, so that the metal in fusion will have less space

to traverse while exposed to the oxidizing influence of the blast.

To accomplish this, recourse has been had to the placing of additional rows of tuyeres in some instan es—the "Stewart rapid cupola" having

three rows, and the "Colliau cupola furnace" having two rows, of tuyeres.

Blast-pressure.—Experiments show that about 80,000 cubic feet of air are consumed in melting a ton of iron, which would weigh about 2400 pounds, or more than both iron and fuel. When the proper quantity of air is supplied, the combustion of the fuel is perfect, and carbonic acid gas is the result. When the supply of air is insufficient, the combustion is imperfect, and carbonic-oxide gas is the result. The amount of heat evolved in these two cases is as 15 to 416, showing a loss of over two thirds of the heat by imperfect combustion.

It is not always true that we obtain the most rapid melting when we are forcing into the cupola the largest quantity of air. Some time is required to elevate the temperature of the air supplied to the point that it will enter into combustion. If more air than this is supplied, it rapidly absorbs heat, reduces the temperature, and retards combustion, and the fire in the cupola

may be extinguished with too much blast.

Slag in Cupolas.—A certain amount of slag is necessary to protect the molten iron which has fallen to the bottom from the action of the blast; if

it was not there, the iron would suffer from decarbonization.

When slag from any cause forms in too great abundance, it should be led away by inserting a hole a little below the tuyeres, through which it will find its way as the iron rises in the bottom.

In the event of clean iron and fuel, slag seldom forms to any appreciable extent in small heats; this renders any preparation for its withdrawal un-necessary, but when the cupola is to be taxed to its utmost capacity it is then incumbent on the melter to flux the charges all through the heat, carrying it away in the manner directed.

The best flux for this purpose is the chips from a white marble yard, About 6 pounds to the ton of iron will give good results when all is clean.
When fuel is bad, or iron is dirty, or both together, it becomes imperative that the slag be kept running all the time.

Fuel for Cupolas.—The best fuel for melting iron is coke, because it re-

quires less blast, makes hotter iron, and melts faster than coal. must be used, care should be exercised in its selection. which are bright, black, hard, and free from slate, will melt iron admirably. The size of the coal used affects the melting to an appreciable extent, and, for the best results, small cupolas should be charged with the size called "egg," a still larger grade for medium-sized cupolas, and what is called "lump" will answer for all large cupolas, when care is taken to pack it carefully on the charges.

Charging a Cupola.—Chas. A. Smith (Am. Mach., Feb. 12, 1891) gives the following: A 28-in. cupola should have from 300 to 400 pounds of code on bottom bed; a 38-in. cupola, 700 to 800 pounds; a 48-in. cupola, 1500 lbs.; and a 80-in. cupola should have one ton of fuel on bottom bed. To every pound of fuel on the bed, three, and sometimes four pounds of metal can be added with safety, if the cupola has proper blast; in after-charges, to every

pound of fuel add 8 to 10 pounds of metal; any well-constructed cupola will

stand ten.

F. P. Wolcott (Am. Mach., Mar. 5, 1891) gives the following as the practice of the Colwell Iron-works, Carteret, N. J.: "We melt daily from twenty to forty tons of iron, with an average of 11.2 pounds of iron to one of fuel. In a 35-in. cupola seven to nine pounds is good melting, but in a cupola that lines up 45 to 60 inches, shything less than nine pounds shows a defect in arrangement of tweres or strength of blast, or in charging up."

arrangement of tuyeres or strength of blast, or in charging up."

"The Moulder's Text-book," by Thos. D. West, gives forty-six reports in tabular form of cupola practice in thirty States, reaching from Maine to

Cupola Charges in Stove-foundries. (Iron Age, April 14, 1892.)
No two cupolas are charged exactly the same. The amount of fuel on the bed or between the charges differs, while varying amounts of iron are used in the charges. Below will be found charging-lists from some of the prominent stove-foundries in the country:

A—Bed of fuel, coke	First charge of iron 5,000 All other charges of iron 1,000 First and second charges	each Six next charges of coke, each Nineteen next charges of coke,	150 120 100
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Thus for a melt of 18 tons there would be 5120 lbs. of coke used, giving a ratio of 7 to 1. Increase the amount of iron melted to 24 tons, and a ratio of 8 pounds of iron to 1 of coal is obtained.

BB—Bed of fuel, coke	Second and third charges of fuel	180 100
All other charges of iron,		

For an 18-ton melt 5060 lbs. of coke would be necessary, giving a ratio of 7.1 lbs. of iron to 1 pound of coke.

	lbs.	lba	
C-Bed of fuel, coke	1,600	All other charges of iron 2,00	0
First charge of iron	4.000	All other charges of coke 15	0
First and second charges			
of coke			

In a melt of 18 tons 4100 lbs. of coke would be used, or a ratio of 8.5 to 1.

	lbs. i		lbs.
D —Bed of fuel, coke	1,800	All charges of coke, each	200
		All other charges of iron	

In a melt of 18 tons, 3900 lbs. of fuel would be used, giving a ratio of 9.4 pounds of iron to 1 of coke. Very high, indeed, for stove-plate.

lbs. i	lbs.
E -Bed of fuel, coal 1,900	
First charge of iron 5,000	All other charges of coal, each 175
First charge of coal 200	<u> </u>

In a melt of 18 tons 4700 lbs, of coal would be used, giving a ratio of ?.7 lbs, of iron to 1 lb. of coal.

These are sufficient to demonstrate the varying practices existing among

different stove-foundries. In all these places the iron was proper for stove-

different stove-foundries. In all these places the iron was proper for stove plate purposes, and apparently there was little or no difference in the kind of work in the sand at the different foundries.

Results of Increased Driving. (Eric City Iron-works, 1891.)—May—Dec. 1890: 60-in. cupola, 100 tons clean castings a week, melting 8 tons per hour; iron per pound of fuel, 7½ lbs.; per cent weight of good castings to ron charged, 75½. Jan.—May, 1891: Increased rate of melting to 11½ tous per hour; iron per lb. fuel, 9½; per cent weight of good castings, 75: one week, 13½ tous per hour, 10.3 lbs. iron per lb. fuel; per cent weight of good castings, 75: one week, 13½ tous per hour, 10.3 lbs. iron per lb. fuel; per cent weight of good castings, 75.3. The increase was made by putting in an additional row of tuyeres and using stronger blast, 14 ounces. Coke was used as fuel. (W. O. Webber Trans, A. S. M. E. Xii. 1045.) Trans. A. S. M. E. xii. 1045.)

Buffalo Steel Pressure-blowers. Speeds and Capacities as applied to Cupolas.

No. of Blower.	Square inches Blast.	Diam. inside of Cupola in inches.	Pressure in oz.	Speed—No. of Revs. per minute.	Melting Capacity in lbs.	Cubic Feet of Air required per minute.	Pressure in oz.	Speed—No. of Revs. per min.	Melting Capac- ity in lbs. per hour.	Cubic Feet of Air required per minute.
4	4	20	8	4732 ·	1545	666	9	5030	1647	717
4 5 6	6	25	8	4209	2821	778	10	4726	2600	867
6	6 8	25 30 35	i a	3660	3093	951	10	4108	3671	867 1067 1668
7 8 9	14	85	8 8 10	3244	4218	1486	10	3642	4777	1668
8	18	40 45	8	2948	5425	2199	10	8310	6082	2469 3523
9	26	45	10	2785	7818	3203	12	3260	8598	8523
10	14 18 26 36	55	10	2195	11295	4938	12	2418	12378	5431
11 111/6 12	45 55	65 72	12	1952	16955	7707	14	2116	18357	8358
111/6	55	72	12	1647	22607	10276	14	1797	25176	11144
12	75	84	12	1625	25836	11744	14	1775	28019	12736

In the table are given two different speeds and pressures for each size of blower, and the quantity of iron that may be melted, per hour, with each. In all cases it is recommended to use the lowest pressure of blast that will do In all cases it is recommended to use the lowest pressure of blast that will do the work. Run up to the speed given for that pressure, and regulate quantity of air by the blast-gate. The tuyere area should be at least one ninth of the area of cupola in square inches, with not less than four tuyeres at equal distances around cupola, so as to equalize the blast throughout. Variations in temperature affect the working of cupolas materially, hot weather requiring increase in volume of air.

(For tables of the Sturtevant blower see pages 519 and 520.)

Loss in Melting Iron in Cupolas.—G. O. Vair, Am. Mach., March 5, 1891, gives a record of a 45-in. Colliau cupola as follows:

Ratio of fuel to iron, 1 to 7.42.

Good castings	21,814	lbs.
New scrap	3,005	**
Millings	200	"
Loss of metal	1,481	"
Amount melted	26,000	lbs.
Loss of metal, 5.69%. Ratio of loss, 1 to	17.55.	

Use of Softeners in Foundry Practice. (W. Graham, Iron Age, June 27, 1889.)—In the foundry the problem is to have the right proportions of combined and graphitic carbon in the resulting casting; this is done by getting the proper proportion of silicon. The variations in the proportions of silicon afford a reliable and inexpensive means of producing a cast iron of any required mechanical character which is possible with the material employed. In this way, by mixing suitable irons in the right proportions, a required grade of casting can be made more cheaply than by using irons

in which the necessary proportions are already found.

If a strong machine casting were required, it would be necessary to keep the phosphorus, sulphur, and manganese within certain limits. Professor Turner found that cast iron which possessed the maximum of the desired qualities contained, graphite, 2.59%; silicon, 1.42%; phosphorus, 0.39%; sulphur, 0.00%; manganese, 0.58% and the maximum of the desired qualities contained graphite, 2.59%; silicon, 1.42%; phosphorus, 0.39%; sulphur, 0.00%; manganese, 0.58% and 1.50% and

A strong casting could not be made it there was much increase in the aniount of phosphorus, sulphur, or manganese. Irons of the above percentages of phosphorus, sulphur, and manganese would be most suitable for this purpose, but they could be of different grades, having different percentages of silicon, combined and graphitic carbon. Thus hard irons, mottled and white irons, and even steel scrap, all containing low percentages of silicon and high percentages of combined carbon, could be employed if an iron having a large amount of silicon were mixed with them in sufficient amount. This would bring the silicon to the proper proporation and would cause the This would bring the silicon to the proper proportion and would cause the combined carbon to be forced into the graphitic state, and the resulting

casting would be soft. High-silicon irons used in this way are called "soft-The following are typical analyses of softeners:

		Fern	o-silicor	١.	Softene	rs, Am	erican.	Scotch Irons, No. 1.		
	Foreign.		American.		Well- ston.	Globe	Belle- fonte.	Eg- linton	Colt- ness.	
Silicon Combined C Graphitic C Manganese Phosphorus Sulphur	1.84 0.52 3.86 0.04	9.80 0.69 1.12 1.95 0.21 0.04	12.08 0.06 1.52 0.76 0.48 Trace	10.84 0.07 1.92 0.52 0.45 Trace	6.67 2.57 0.50 Trace	5.89 0.80 2.85 1.00 1.10 0.02	3 to 6 0.25 3. 0.58 0.35 0.03	2.15 0.21 8.76 2.80 0.62 0.03	2.59 1.70 0.85 0.01	

(For other analyses, see pages 371 to 373.)

Ferro-silicons contain a low percentage of total carbon and a high percentage of combined carbon. Carbon is the most important constituent of cast iron, and there should be about 8.4% total carbon present. By adding ferro silicon which contains only 2% of carbon the amount of carbon in the resulting mixture is lessened.

Mr. Keep found that more silicon is lost during the remelting of pig of over 10% silicon than in remelting pig iron of lower percentages of silicon. He also points out the possible disadvantage of using ferro-silicons containing as high a percentage of combined carbon as 0.70% to overcome the bad effects of combined carbon in other irons.

The Scotch irons generally contain much more phosphorus than is desired in irons to be employed in making the strongest castings. It is a mistake to mix with strong low-phosphorus irons an iron that would increase the amount of phosphorus for the sake of adding softening qualities, when softness can be produced by mixing irons of the same low phosphorus.

(For further discussion of the influence of silicon see page 365.)

Shrinkage of Castings.—The allowance necessary for shrinkage varies for different kinds of metal, and the different conditions under which they are cast. For castings where the thickness runs about one inch, cast under ordinary conditions, the following allowance can be made:

For cast-iron, 1/6 " brass. 8/16 inch per foot. For zinc, 5/16 inch per foot. brass, tin, 1/12 46 .. aluminum, 3/16 44 44 44 steel, mal, iron. Britannia, 1/32

Thicker castings, under the same conditions, will shrink less, and thinner ones more, than this standard. The quality of the material and the manner of moulding and cooling will also make a difference.

Numerous experiments by W. J. Keep (see Trans. A. S. M. E., vol. xvi.) showed that the shrinkage of cast iron of a given section decreases as the percentage of silicon increases, while for a given percentage of silicon the shrinkage decreases as the section is increased. Mr. Keep gives the following the approximate relation of shrinkage to size and pering table showing the approximate relation of shrinkage to size and percentage of silicon:

	Sectional Area of Casting.									
Percentage of Silicon.	½ ″ □	1" 0	1" × 2"	2′′ 🗆	8" 🗆	4" 0				
	Shrinkage in Decimals of an inch per foot of Length.									
1.	.188	.158	.146	.130	.118	.102				
1.5 2.	.171 .159	.145 .133	.183	.117 .104	.098	.087				
2.5	.147	.121	.108	.092	.078	.060				
8. 8.5	.135 .128	.108 .095	.095	.077 .065	.059	.045 .0 3 2				

Mr. Keep also gives the following "approximate key for regulating foundry mixtures" so as to produce a shrinkage of 1/6 in. per ft. in castings of different sections:

Weight of Castings determined from Weight of Pattern. (Rose's Pattern-maker's Assistant.)

Will weigh when cast in A Pattern weighing One Pound, made of-Cast Yellow Gun-Zinc. Copper. Brass. Iron. metal. lbs. lbs. lbs. lbs. lbs.

Mahogany-Nassau.... 10.4 12.7 8.2 10.7 12.8 12.2 12.5 Honduras.... 14.6 15. 12.9 15.3 Spanish 9.7 9.9 8.5 10.1 Pine, red.... 19,5 12.1 14.9 14.2 14.6 white..... 16.7 16.1 19.8 19.0 19.5 yellow..... 16.5 18.6 16.7 16.0 14.1

Moulding Sand. (From a paper on "The Mechanical Treatment of Moulding Sand" by Walter Bagshaw, Proc. Inst. M. E. 1891,—The chemical composition of sand will affect the nature of the casting, no matter what treatment it undergoes. Stated generally, good sand is composed of 94 parts silica, 5 parts alumina, and traces of magnesia and oxide of iron. Sand containing much of the metallic oxides, and especially lime, is to be avoided, Geographical position is the chief factor governing the selection of sand; and whether weak or strong, its deficiencies are made up for by the skill of the moulder. For this reason the same sand is often used for both heavy and light castings, the proportion of coal varying according to the nature of the casting. A common mixture of facing-sand consists of six parts by weight of old sand, four of new sand, and one of coal-dust. Floor-sand requires only half the above proportions of new sand and coal-dust to renew it. German founders adopt one part by measure of new sand to two of old sand; to which is added coal-dust in the proportion of one tenth of the bulk for large castings, and one twentieth for small castings. A few founders mistreet-sweepings with the coal in order to get porosity when the metal in the mould is likely to be a long time before setting. Plumbago is effective in must not be dusted on in such quantities as to close the pores and prevent ree exit of the gases. Powdered French chalk, soapstone, and other substances are sometimes used for facing the mould; but next to plumbago, oak charcoal takes the best place, notwithstanding its liability to float occasionally and give a rough casting.

For the treatment of sand in the moulding-shop the most primitive method is that of hand-ridding and treading. Here the materials are roughly proportioned by volume, and riddled over an iron plate in a flat heap, where the mixture is trodden into a cake by stamping with the feet; it is turned over with the shovel, and the process repeated. Tough sand can be obtained in this manner, its toughness being usually tested by squeezing a handful into a ball and then breaking it; but the process is slow and tedious. Other things being equal, the chief characteristics of a good moulding-sand are toughness and porosity, qualities that depend on the manner of mixing as

well as on uniform ramming.

Toughness of Sand—In order to test the relative toughness, sand mixed in various ways was pressed under a uniform load into bars 1 in, sq. and about 12 in, long, and each bar was made to project further and further over the edge of a table until its end broke off by its own weight Old sand from the shor floor had very irregular cohesion, breaking at all lengths of projections from ½ in, to 1½ in. New sand in its natural state held together until an overhang of 2% in, was reached. A mixture of old sand, new sand, and coal-dust

Showing as a mean of the tests only slight differences between the last three methods, but in favor of machine-work. In many instances the fractures were so uneven that minute measurements were not taken,

Dimensions of Foundry Ladles.—The following table gives the dimens one, inside the lining, of ladles from 25 lbs. to 16 tons capacity. the ladles are supposed to have straight sides. (Am. Mach., Aug. 4, 1892.)

Capacity.	Diam.	Depth.	Capacity.	Diam.	Depth.
16 tons	in. 54 59 49 46 43 89 84 81 27 2414	in. 56 58 50 48 44 40 85 88 88 25	\$4 ton	in. 20 17 1814 1112 104 10 8	in. 20 17 181/2 111/2 111/2 1101/2 81/2 7/2 66

THE MACHINE-SHOP.

SPEED OF CUTTING-TOOLS IN LATHES, MILLING MACHINES, ETC.

Relation of diameter of rotating tool or piece, number of revolutions.

and cutting-speed:

Let d = diam. of rotating piece in inches, n = No. of revs. per min.; S = speed of circumference in feet per minute;

$$S = \frac{\pi dn}{12} = .2618dn \; ; \quad n = \frac{S}{.2618d} = \frac{3.82S}{d}; \quad d = \frac{3.82S}{n}$$

Approximate rule: No. of revs. per min. = 4 x speed in ft. per min. + diam, in inches.

Speed of Cut for Lathes and Planers. (Prof. Coleman Sellers. Stevens' Indicator, April, 1892.)—Bruss may be turned at high speed like

Bronze.-A speed of 18 feet per minute can be used with the soft alloyssay 8 to 1, while for hard mixtures a slow speed is required—say 6 feet per minute.

Wrought Iron can be turned at 40 feet per minute, but planing-machines that are used for both cast and forged iron are operated at 18 feet per minute.

Machinery Steel.—Ordinary, 14 feet per minute; car-axles, etc., 9 feet per minute.

Wheel Tires.—6 feet per minute; the tool stands well, but many prefer to run faster, say 8 to 10 feet, and grind the tool more frequently. Lathes.—The speeds obtainable by means of the cone-pulley and the back

gearing are in geometrical progression from the slowest to the fastest. In a well-proportioned machine the speeds hold the same relation through all the steps. Many lathes have the same speed on the slowest of the cone and the fastest of the back-gear speeds.

The Speed of Counter shaft of the lathe is determined by an assumption of a slow speed with the back gear, say 6 feet per minute, on the largest diameter that the lathe will swing.

EXAMPLE.—A 30-inch lathe will swing 30 inches =, say, 90 inches circumference = 7' 6"; the lowest triple gear should give a speed of 5 or 6 per minute.

In turning or planing, if the cutting-speed exceed 30 ft. per minute, so much heat will be produced that the temper will be drawn from the tool. The speed of cutting is also governed by the thickness of the shaving, and by the hardness and tenacity of the metal which is being out; for instance, in cutting mild steel, with a traverse of \$4 in, per revolution or stroke, and with a shaving about \$6 in. thick, the speed of cutting must be reduced to about \$6 ft. per minute. A good average cutting-speed for wrought or \$\vec{r}\$

eron is 20 ft. per minute, whether for the lathe, planing, shaping, or slotting machine. (Proc. Inst. M. E., April, 1883, p. 248.)

Table e	of Cut	tting-s	peeds.
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Diameter, inches.	Feet per minute.										
	5	10	15	20	25	30	85	40	45	50	
	-	Revolutions per minute.									
34	76.4	152.8	229.2	805.6	382.0	458.4	534.8	611.2	687.6	764.9	
MENSANS-	50.9	101.9	152.8	203.7	254.6	305.6 229.2	356.5	407.4	458.3 343.8	509.3 382.0	
29	38.2 30.6	76.4	114.6 91.7	152.8 122.2	191.0 152.8	109 4	267.4 213.9	305.6 244.5	275.0	305.6	
29	25.5	61.1 50.9	76.4	101.8	127.8	183.4 152.8	178.2	203.7	229.1	254.6	
72	21.8	43.7	65.5	87.8	109.1	130.9	152 8	174.6	196.4	218.3	
78	19.1	38.2	57.8	76.4	95.5	114.6	183.7 118.8	152.8	171.9	191.0	
116	17.0	34.0	50.9	67.9	84.9	114.6 101.8	118.8	185.8	152.8 137.5	191.0 169.7	
112	15.8	30.6	45.8	61.1	76.4 69.5	91.7	106.9	122.2 111.1	137.5	152.8 138.9	
186	189	27.8	41.7	55.6	69.5	83.3	97.2	111.1	125.0	138.9	
11/8	12.7	25.5	38.2	50.9	63.6	76.4	89.1	101.8	114.5	127.2	
134	10.9	21.8	82.7 28.7	43.7	54.6	65.5	76.4	87.8	98.2 86.0	109.2	
2	9.6	19.1	28.7	38.2	47.8	57.3 50.9 45.8 41.7	66.9	76.4	86.0	95.5	
214	8.5	17.0	25.5	84.0	42.5	50.9	59.4 53.5	67.9 61.1	76.4 68.8	84.9 76.4	
214	7.6	15.8	22 9	30.6 27.8	38.2 34.7	90.0	48.6	55.6	62.5	69.5	
294	6.9	13.9 12.7	20.8 19.1	05 K	91 0	A1.7	44.6	50.9	57 9	63.7	
21/	5.5	10.9	16.4	61.0	97 8	99.7	88.2	43.7	57.8 49.1	54.6	
478	4.8	9.6	14 8	10 1	31.8 27.3 23.9	38.2 32.7 28.7	83.4	38 2	48.0	47.8	
416	4.2	8.5	14.8 12.7	25.5 21.8 19.1 17.0 15.3 13.9	21.2	25.5	29.7	84.0	88.2	42.5	
5	8.8	7.6	11.5	15.8	19 1	22.9	26.7	80.6	84.4	88.1	
516	4.2 8.8 8.5	6.9	10.4 9.5	13.9	17.4 15.9 18.6	20.8 19.1	24.3	27.8	81.2	84.7	
6′~	8.2	6.4	9.5	12.7	15.9	19.1	22.3	25.5	28.6	81.8	
7	2.7	5.5	8.2	10.9 9.6 8.5	13.6	16.4	19.1	21.8	24.6		
8	2.4	4.8 4.2 8.8	7.2	9.6	11.9 10.6	14.8 12.7	16.7	19.1 17.0	21.5	23.9	
•	2.1	4.2	6.4	8.5	10.6	12.7	14.8	17.0	19.1	21.2	
10	1.9	8.5	5.7	7.6 6.9	9.6 8.7	11.5 10.4	13.8 12.2	15.8 18.9	17.2 15.6	19.1 17.4	
11	1.6	8.2	5.2 4.8	6.4	8.4	10.4	11.1	12.7	14.8	15.9	
12	1.5	0.2	4.4	5.0	7.8	9.5 8.8	10.8	11.8	18.9	14.7	
14	1.4	2.9 2.7	4.1	5.9 5.5	8.0 7.8 6.8	8.2	10.8 9.5	10.9	12.3	13.6	
15	1.3	2.5	8.8	5.1	6.4	7.6	8.9	10.2	11.5	12.7	
16	1.8	2.4	8.6	5.1 4.8 4.2 8.8 8.5	6.0	7.6 7.2	8.4	9.5	10.7	11.9	
18	1.1	2.1 1.9 1.7	8.2 8.9	4.2	5.8	R 4	7.4	8.5	9.5	10.6	
20	1.0	1.9	2.9	8.8	4.8 4.3	5.7 5.2 4.8	6.7	7.6	8.6	9.€	
23	9.	1.7	2.6	8.5	4.8	5.2	6.1 5.6	6.9	7.8	8.7	
24	1 .8	1.6	2.4	8.2	4.0	4.8	5.6	6.4	7.2	8.0	
20	1 .7	1.5	2.2	2.9	8.7	4.4	5.1 4.8	5.9	6.6	7.8	
1144594 445 550 7 8 8 10 113 114 115 118 22 24 6 8 6 2 4 4 5 6 6 7 8 8 10 113 114 115 118 22 24 6 8 6 2 4 8 4 8 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	.9 .8 .7 .6 .5	1.4 1.8	2.0 1.9	2.7 2.5	8.4	4.1 8.8	4.5	5.5 5.1	6.1 5.7	6.8 6.4	
90 98	۵۰ ا	1.8	1.6	2.0 2.1	8.2 2.7	8.9	8.7	4.2	4.8	5.8	
42	.5	1:6	1.4	1.6	2.8	2.7	8.2	8.6	4.1	4.8	
48	1 .4	l å	1.2	1.8 1.6	2.0	2.4	2.8	8.2	8.6	4.0	
54	1 :4	.8	11	1.4	1.8	2.1	2.5	2.8	8.9	8.5	
6Õ	.4	.6	1.0	1.8	1.6	1.9		2.5	2.9	8.2	

Speed of Cutting with Turret Lathes.—Jones & Lamson Machine Co. give the following cutting speeds for use with their flat turret lathe on diameters not exceeding two inches:

	Ft. per	minute,
(Tool steel and taper on tubing	• • • • • • • • •	10
Threading (Machinery)		15
Very soft steel		20
(Very soft steel	l diam	20
Turning Cut which reduces the stock to 32 of its origina	l diam	95
machinery Cut which reduces the stock to 3% of its origina steel	l diam	90 to 98
Steel Cut which reduces the stock to 15/16 of its origin	el diem	40 to 48
Turning very soft machinery steel, light cut and cool work	at utalii.	FO 40 40

Forms of Metal-cutting Tools.—"Hutte," the German Engineers' Pocket-book, gives the following cutting-angles for using least power: Top Rake. Angle of Cutting-edge.

Wrought iron	8•	51°
Cast iron	4•	51*
Bronze	40	66*

The American Machinist comments on these figures as follows: We are not able to give the best nor even the generally used angles for tools, because these vary so much to suit different circumstances, such as degree of hardness of the metal being cut, quality of steel of which the tool is made, depth of cut, kind of finish desired, etc. The angles that cut with the least expenditure of power are easily determined by a few experiments, but the best angles must be determined by good judgment, guided by experience. In nearly all cases, however, we think the best practical angles are greater than those given.

For illustrations and descriptions of various forms of cutting-tools, see articles on Lathe Tools in App. Cyc. App. Mech., vol. ii., and in Modern

Cold Chisels.-Angle of cutting-faces (Joshua Rose): For cast steel, about 65 degrees; for gun-metal or brass, about 50 degrees; for copper and

soft metals, about 80 to 35 degrees.

Bule for Gearing Lathes for Screw-cutting. (Garvin Machine Co.)—Read from the lathe index the number of threads per inch cut by equal gears, and multiply it by any number that will give for a product a gear on the index; put this gear upon the stud, then multiply the number of threads per inch to be cut by the same number, and put the resulting gear upon the screw.

EXAMPLE.—To cut 1114 threads per inch. We find on the index that 48 into 48 cuts 6 threads per inch, then $6\times 4=24$, gear on stud, and $11\times \times 4=46$, grar on screw. Any multiplier may be used so long as the products include gears that belong with the lathe. For instance, instead of 4 as a multiplier we may use 6. Thus, $6\times 6=86$, gear upon stud, and $111/4\times 6=69$, gear upon screw.

Rules for Calculating Simple and Compound Gearing where there is no Index. (Am Mach.)—If the lathe is simplegeared, and the stud runs at the same speed as the spindle, select some gear for the screw, and multiply its number of teeth by the number of threads per inch in the lead-screw, and divide this result by the number of threads per inch to be cut. This will give the number of teeth in the gear for the stud. If this result is a fractional number, or a number which is not among the gears on hand, then try some other gear for the screw. Or, select the gear for the stud first, then multiply its number of teeth by the number of threads per inch to be cut, and divide by the number of threads per inch on the lead-screw. This will give the number of teeth for the grar on the screw. If the lathe is compound, select at random all the driving-gears, multiply the numbers of their teeth together, and this product by the number of threads to be cut. Then select at random all the driven gears except one; unitiply the numbers of their teeth together, and this product by the number of threads per inch in the lead-screw. Now divide the first result by the second, to obtain the number of teeth in the remaining driven gear. Or, select at random all the driven gears. Multiply the numbers of their teeth together, and this product by the number of threads per inch in the lead-screw. Then select at random all the driving gears except one. Multiply the numbers of their teeth together, and this result by the number of threads per inch of the screw to be cut. Divide the first result by the last, to obtain the number of teeth in the remaining driver. When the gears on the compounding stud are fast together, and cannot be changed, then the driven one has usually twice as many teeth as the other, or driver, in which case in the calculations consider the lead-screw to have twice as many threads per inch as it actually has, and then ignore the compounding entirely. Some lathes are so constructed that the stud on which the first driver is placed revolves only half as fast as the spindle. This can be ignored in the calculations by doubling the number of threads of the lead-screw. If both the last conditions are present ignore them in the calculations by multiplying the number of threads per inch in the lead-screw by four. If the thread to be cut is a fractional one, or if the pitch of the lead-screw is fractional, or if both are fractional, then reduce the fractions to a common denominator, and use the numerators of these fractions as if they equalled the pitch of the screto be cut, and of the lead-screw, respectively. Then use that part of the rule given above which applies to the lathe in question. For instance, suppose it is desired to cut a thread of 25/28-inch pitch, and the lead-screw has 4 threads per inch. Then the pitch of the lead-screw will be ½ inch, which is equal to 8/28 inch. We now have two fraction, 25/32 and 8/22, and the two screws will be in the proportion of 25 to 8, and the gears can be figured by the above rule, assuming the number of threads to be cut to be 8 per inch. But this latter number may and those on the lead-screw to be 25 per inch. But this latter number or may be further modified by conditions named above, such as a reduced speed of the stud, or fixed compound gears. In the instance given, if the lead-screw had been 2½ threads per inch, then its pitch being 4/10 inch, we have the fractions 4/10 and 25/22, which, reduced to a common denominator, are 64/160 and 125/160, and the gears will be the same as if the lead-screw had 125 threads per inch, and the screw to be cut 64 threads per inch.

On this subject consult also "Formulas in Gearing," published by Brown

& Sharpe Mfg. Co., and Jamieson's Applied Mechanics.

Change-gears for Screw-cutting Lathes.—There is a lack of uniformity among lathe-builders as to the change-gears provided for screw-cutting. W. R. Macdonald, in Am. Mach., April 7, 1892, proposes the following series, by which 38 whole threads (not fractional) may be cut by changes of only nine gears:

Screw.					SI	indle.	1			W	ole '	Thre	ada.
83	20	80	40	50	60	70	110	120	180				
20 80 40 50 60 70 110	18 24 80 86 42 66	8 16 20 24 28 44	6 9 12 15 18 21 83	4 4/5 7 1/5 9 8/5 14 2/5 16 4/5 26 2/5	6 8 10 14 22	8 8/7 5 1/7 6 6/7 8 4/7 10 2/7	2 2/11 8 8/11 4 4/11 5 5/11 6 6/11 7 7/11	2 8 4 5 6 7	1 11/13 2 10/13 3 9/13 4 8/13 5 7/13 6 6/13 10 2/18	5 6 7 8	11 12 13 14 15 16 18	22 24 26 28 80 83 86	44 48 52 66 72 78
110 120 180	72 78	44 48 52	36 89	26 2/5 28 4/5 81 1/5	24	18 6/7 20 4/7 22 3/7	18 1/11 14 2/11	11	11 1/18	9	18 20 21	36 39 42	

Ten gears are sufficient to cut all the usual threads, with the exception of perhaps 1114, the standard pipe-thread; in ordinary practice any fractional thread between 11 and 12 will be near enough for the customary short pipethread; if not, the addition of a single gear will give it.

In this table the pitch of the lead-screw is 12, and it may be objected to as too flue for the purpose. This may be rectified by making the real pitch or any other desirable pitch, and establishing the proper ratio between the

lathe spindle and the gear-stud.

Metric Screw-threads may be cut on lathes with inch-divided leading-screws, by the use of change wheels with 50 and 127 teeth; for 127

centimetres = 50 inches (127 \times 0.3937 = 49.9999 in.).

Rule for Setting the Taper in a Lathe. (Am. Mach.)—No rule cal be given which will produce exact results, owing to the fact that the centres enter the work an indefinite distance. If it were not for this circumstance the following would be an exact rule, and it is an approximation as it is. To find the distance to set the centre over: Divide the difference in the diameters of the large and small end of the taper by 2, and multiply this quotient by the ratio which the total length of the shaft bears to the length of the tapered portion. Example: Suppose a shaft three feet long is to have a taper turned on the end one foot long, the large end of the taper being two $\frac{2-1}{2} \times \frac{8}{1} = 1$ inches. inches and the small end one inch diameter.

Ricctric Drilling-machines - Speed of Drilling Holes in Steel Plates. (Proc. Inst. M. E., Aug. 1881, p. 329 — In drilling holes in the shell of the S.S. "Albania," after a very small amount of practice the men working the machines drilled the %-inch holes in the shell with great rapidity, doing the work at the rate of one hole every 69 seconds, inclusive of the time occupied in altering the position of the machines by means of differential pulley-blocks, which were not conveniently arranged as slings for this purpose. Repeated trials of these drilling-machines have also shows that, when using electrical energy in both holding-on magnets and motor

amounting to about ¾ H.P., they have drilled holes of 1 inch diameter through 1¼ inch thickness of solid wrought iron, or through 1¼ inch of mild steel in two plates of 13/16 inch each, taking exactly 1¾ min. for each hole.

Speed of Brills. (Morse Twist-drill and Machine Company.)—The following table gives the revolutions per minute for drills from 1/16 in. to 2 in. diameter, as usually applied:

Diameter of Drills, in.	Wrought	Speed for Cast Iron.	Speed for Brass.	Diameter of Drills, in.	Speed for Wrought Iron and Steel.	Speed for Cast Iron.	Speed for Brass.
1/16 1/6 3/16	1712 855	2883 1191	8544 1779	1 1/16	72 68	108 102	180 170
5/16 5/16	571 897 818	794 565 459	1181 855 684	1 3/16 11/4 1 5/16	64 58 55	97 89 84 81	161 150 148
7/16 14	265 227 183	877 888 267	570 489 412	136 1 7/16 116	58 50 46	77 74	136 130 129
9/16 56 11/16	163 147 183	238 214 194	867 830 300	1 9/16 156 1 11/16	44 40 38	71 66 63	117 113 109
13/16	112 103 96	168 155 144	265 244 227	134 1 13/16 136	37 36 83	61 59 55	105 101 98
15/16 1	89 76	184 115	213 191	1 15/16 2	82 81	58 51	95 92

One inch to be drilled in soft cast iron will usually require: for 1/4·in. drill, 160 revolutions; for 1/4·in. drill, 140 revolutions; for 3/4·in. drill, 100 revolutions; for 1·in. drill, 95 revolutions. These speeds should seldom be exceeded. Feed per revolution for 1/4·in. drill, .005 inch; for 1/4·in. drill, .007 inch; for 1/4·in. drill .007 inch; for 1/4·in. drill .007 inch; for 1/4·in. drill .007 inch; for 1/4·in. drill .007 inch; for 1/4·in. drill .007 inch; for 1/4·in. drill .007 inch; for 1/4·in. drill .007 inch; for 1/4·in. drill .007 inch; for 1/4·in. drill .007 inch; for 1/4·in. drill .007 inch; for 1/4·in. drill .007 inch; for 1/4·in. drill .007 inch; for 1/4·in. drill .007 inch; for 1/4·in. drill .008 inch; for 1/4·in.

MILLING-CUTTERS.

George Addy, (Proc. Inst. M. E., Oct. 1890, p. 537), gives the following:

Analyses of Steel,—The following are analyses of milling cutter
blanks, made from best quality crucible cast steel and from self-hardening
"Ivanhoe" steel:

	Crucible Cast Steel, per cent.	Ivanhoe Steel, per cent.
Carbon		1.67
Silicou	0.112	0.252
Phosphorus	0.018	0.051
Manganesė	0.86	2.557
Sulphur	0.02	0.01
Tungsten	••• •••••	4.65 90.81
	100.000	100.000

The first analysis is of a cutter 14 in. diam., 1 in. wide, which gave very good service at a cutting-speed of 60 ft. per min. Large milling cutters are sometimes built up, the cutting-edges only being of tool steel. A cutter 22 in. diam. by 5½ in. wide has been made in this way, the teeth being clamped between two cast-iron flanges. Mr. Addy recommends for this form of tooth one with a cutting-angle of 70°, the face of the tooth being set 10° back of a radial line on the cutter, the clearance angle being thus 10°. At the Clarence Iron-works, Leeds, the face of the tooth is set 10° back of the radial line for cutting wrought iron and 20° for steel.

Pitch of Teeth.—For obtaining a suitable pitch of teeth for millingcutters of various diameters there exists no standard rule, the pitch being usually decided in an arbitrary manner; according to individual taste For estimating the pitch of teeth in a cutter of any diameter from 4 in. to 15 in., Mr. Addy has worked out the following rule, which he has found capable of giving good results in practice:

Pitch in inches = $\sqrt{\text{diam. in inches} \times 8} \times 0.0625 = .177 \sqrt{\text{diam.}}$

J. M. Gray gives a rule for pitch as follows: The number of teeth in a milling cutter ought to be 100 times the pitch in inches; that is, if there were 27 teeth, the pitch ought to be 0.27 in. The rules are practically the same, for if d = diam, n = No, of teeth, p = pitch, c = circumference, c = nv, $d = \frac{pn}{n} = \frac{100p^2}{n} = 31.88n^2 \cdot n = \sqrt{0314d} = 127 Md$. No of teeth n = 1000

pn; $d = \frac{pn}{\pi} = \frac{100p^2}{\pi} = 31.83p^2$; $p = \sqrt{.0314d} = .177 \sqrt{d}$; No. of teeth, n, =

3 14d + p.

Number of Teeth in Mills or Cutters. (Joshua Rose.)—The teeth of cutters must obviously be spaced wide enough apart to admit of the emery wheel grinding one tooth without touching the next one, and the front faces of the teeth are always made in the plane of a line radiating from the axis of the cutter. In cutters up to 3 in. in diam. it is good practice to provide 8 teeth per in. of diam., while in cutters above that diameter the spacing may be coarser, as follows:

Speed of Cutters.—The cutting speed for milling was originally fixed very low; but experience has shown that with the improvements now in use it may with advantage be considerably increased, especially with cutters of large diameter. The following are recommended as safe speeds for cutters of 6 in. and upwards, provided there is not any great depth of material to cut away:

Should it be desired to remove any large quantity of material, the same cutting-speeds are still recommended, but with a finer feed. A simple rule for cutting-speed is: Number of revolutions per minute which the cutter spindle should make when working on cast iron = 240, divided by the diam-

eter of the cutter in inches.

Speed of Milling-cutters. (Proc. Inst. M. E., April, 1883, p. 248.)—
The cutting-speed which can be employed in milling is much greater than
that which can be used in any of the ordinary operations of turning in the
lathe, or of planing, shaping, or slotting. A milling-cutter with a plentiful
supply of oil, or soap and water, can be run at from 80 to 100 ft. per min,
when cutting wrought iron. The same metal can only be turned in a lathe,
with a tool holder having a good cutter, at the rate of 30 ft. per min., or at
about one third the speed of milling. A milling-cutter will cut cast steel at
the rate of 25 to 30 ft. per min.

The following extracts are taken from an article on speed and feed of milling-cutters in Eng'g, Oct. 22, 1891: Milling-cutters are successfully employed on east iron at a speed of 250 ff. per min.; on wrought iron at from 80 ft. to 100 ft. per min. The latter materials need acopious supply of good lubricant, such as oil or soapy water. These rates of speed air not approached by other tools. The usual cutting-speeds on the lathe, planing, shaping, and slotting machines rarely exceed about one third of those given above, and frequently average about a fifth, the time lost in back stroke not

being reckoned.

The feed in the direction of cutting is said by one writer to vary, in ordinary work, from 40 to 70 revs. of a 4-in. cutter per in. of feed. It must always to an extent depend on the character of the work done, but the above gives shavings of extreme thinness. For example, the circumference of a 4-in. cutter being, say, 12½ in., and having, say, 60 teeth, the advance corresponding to the passage of one cutting-tooth over the surface, in the coarse of the above-named feed-motions, is $1/40 \times 1/60 = 1/2400$ in. the finer feed gives an advance for each tooth of only $1/70 \times 1/60 = 1/4900$ in. Such fine feeds as these are used only for light finishing cuts, and the same authority recommends, also for finishing, a cutter about 9 in. in circumference, or nearly 3 in. in diameter, which should be run at about 60 revs, per min. to cut tough wrought steel, 120 for ordinary east iron, about 80 for wrought

iron, and from 140 to 160 for the various qualities of gun-metal and brass. With cutters smaller or larger the rates of revolution are increased or diminished to accord with the following table, which gives these rates of cutting speeds and shows the lineal speed of the cutting-edge:

Steel. Wrought Iron. Cast Iron. Gun-metal. Brass. Feet per minute... 120

These speeds are intended for very light finishing cuts, and they must be

reduced to about one half for heavy cutting.

The following results have been found to be the highest that could be attained in ordinary workshop routine, having due consideration to economy vanished in ordinary worksnop routine, having due consideration to economy and the time taken to change and grind the cutters when they become dull: Wrought iron—36 ft. to 40 ft. per min.; depth of cut., in.; feed, in. per min. Tough gun-metal—80 ft. per min.; depth of cut., in.; feed, in. per min. Tough gun-metal—80 ft. per min.; depth of cut., in.; feed, in. per min. Cast-iron gear-wheels—28 if. per min.; depth of cut., in.; feed, in.; feed, in. per min. Hard, close-grained cast iron—30 ft. per min.; depth of cut., if. in.; feed, in.; feed, in. per min. Gun-metal joints, if. per min.; depth of cut., if. feed, in. per min. Steel-bars—21 ft. per min.; depth of cut., if. feed, in. per min. Steel-bars—21 ft. per min.; depth of cut., if. feed, in. per min.

A stepped milling-cutter, 4 in. in diam. and 12 in. wide, tested under two conditions of speed in the same machine, gave the following results: The cutter in both instances was worked up to its maximum speed before it gave way, the object being to ascertain definitely the relative amount of work done by a high speed and a light feed, as compared with a low speed and a heavy cut. The machine was used single-geared and double-geared, and in

both cases the width of cut was 101/4 in

Single-gear, 42 ft. per min.; 5/16 in. depth of cut; feed, 1.3 in. per min. = 16 cu. in. per min. Double-gear, 19 ft. per min.; 36 in. depth of cut; feed,

4.16 cu, in. per min. Double-gear, 19 ft. per min.; 36 in. depth of cut; feed, 36 in. per min. = 2.40 cu, in. per min. Extreme Results with Milling-machines. — Horace L. Arnold (Am. Mach., Dec. 28, 1883) gives the following results in flat-surface Arnold (Am. Mach., Dec. 20, 1689) gives the following results in nat-surface milling, obtained in a Pratt & Whitney milling-machine: The mills for the flat cut were 5" diam., 12 teeth, 40 to 50 revs. and 47%" feed per min. Out the mills showed plainly at the end that this rate was greater than they could endure. At 50 revs. for these mills the figures are as follows, with 47%" feed: Surface speed, 64 ft., nearly; feed per tooth, 0.00812"; cuts per inch, 128. And with 9" feed per min.: Surface speed, 64 ft. per min.; feed per tooth, 0.015"; cuts per inch, 6524.

per inch, 66%.
At a feed of 4%" per min, the mills stood up well in this job of cast-iron surfacing, while with a 9" feed they required grinding after surfacing one piece; in other words, it did not damage the mill-teeth to do this job with 123 cuts per in. of surface finished, but they would not endure 66% cuts per inch. In this cast iron milling the surface speed of the mills does not seem to be the factor of mill destruction: it is the increase of feed per tooth that prohibits increased production of finished surface. This is precisely the reverse of the action of single pointed lathe and planer tools in general: with such tools there is a surface-speed limit which cannot be economically exceeded for dry cuts, and so long as this surface-speed limit is not reached, the cut per tooth or feed can be made anything up to the limit of the driving power of the lathe or planer, or to the safe strain on the work itself.

which can in many cases be easily broken by a too great feed.

In wrought metal extreme figures were obtained in one experiment made in cutting keyways \$5/16" wide by \$4'' deep in a bank of 8 shafts 1½" diam. at once, on a Pratt & Whitney No. 8 column milling-machine. The 8 mills were successfully operated with 45 ft. surface speed and 194 in. per min. feed; the cutters were 5" diam., with 25 teeth, giving the following figures, in steel: Surface speed, 45 ft. per min.; feed per tooth, 0.2024"; cuts per inch, 50, nearly. Fed with the revolution of mill. Flooded with oil, that is, a large stream of oil running constantly over each mill. Face of tooth radial. The resulting keyway was described as having a heavy wave or cutter-mark in the bottom, and it was said to have shown no signs of being heavy work on the cutters or on the machine. As a result of the experiment it was decided for economical steady work to run at 17 revs., with a feed of 4" per min., flooded cut, work fed with mill revolution, giving the following figures: Surface speed, 2214 ft. per min.; feed per tooth, 0.0084"; cuts per inch, 119.

An experiment in milling a wrought-iron connecting-rod of a locomotive on a Pratt & Whitney double-head milling-machine is described in the Iron 4ge, Aug. 27, 1891. The amount of metal removed at one cut measured 3½ in wide by 1 3/16 in. deep in the groove, and across the top ½ in. deep by 4½ in. wide. This represented a section of nearly 4½ sq. in. This was done at the rate of 1¾ in per min. Nearly 8 cu. in. of metal were cut up into chips every minute. The surface left by the cutter was very perfect. The cutter moved in a direction contrary to that of ordinary practice; that is, it cut down from the upper surface instead of up from the bottom.

Milling "with" or "against" the Feed.—Tests made with the Brown & Sharpe No. 5 milling-machine (described by H. L. Arnold, in Am. Mack., Oct. 18, 1894) to determine the relative advantage of running the milling-cutter with or against the feed—"with the feed" meaning that the teeth of the cutter strike on the top surface or "scale" of cast-iron work in process of being milled, and "against the feed" meaning that the teeth begin to cut in the clean, newly cut surface of the work and cut upwards toward the scale—showed a decided advantage in favor of running the cutter against the feed. The result is directly opposite to that obtained in tests of a Pratt & Whitney machine, by experts of the P. & W. Co.

In the tests with the Brown & Sharpe machine the cutters used were 6 inches face by 4½ and 3 inches diameter respectively, 15 teeth in each mile. 25 revolutions per minute in each case, or nearly 56 feet per minute usurface speed for the 4½-inch and 33 feet per minute for the 3-inch mill. The revolution marks were 6 to the inch, giving a feed of 7 inches per minute, and a cut per tooth of .011". When the machine was forced to the limit of its driving the depth of cut was 11/32 inch when the cutter ran in the "old" way, or against the feed, and only ½ inch when it ran in the "new" way, or with the feed. The endurance of the milling-cutters was much greater when they were run in the "old" way.

Spiral Milling-cutters.—There is no rule for finding the angle of the spiral; from 10° to 15° is usually considered sufficient; if much greater the end thrust on the spindle will be increased to an extent not desirable for some machines.

Milling-cutters with Inserted Teeth.—When it is required to use milling-cutters of a greater diameter than about 8 in., it is preferable to insert the teeth in a disk or head, so as to avoid the expense of making solid cutters and the difficulty of hardening them, not merely because of the risk of breakage in hardening them, but also on account of the difficulty in obtaining a uniform degree of hardenses or temper.

in obtaining a uniform degree of hardness or temper.

Milling • machine versus Planer. — For comparative data of work done by each see paper by J. J. Grant, Trans. A. S. M. E., ix. 259. He says: The advantages of the milling machine over the planer are many, among which are the following: Exact duplication of work; rapldity of production — the cutting being continuous; cost of production, as several machines can be operated by one workman, and he not a skilled mechanic; and cost of tools for producing a given amount of work.

POWER REQUIRED FOR MACHINE TOOLS.

Resistance Overcome in Cutting Metal. (Trans. A. S. M. E., siii. 208.)—Some experiments made at the works of William Sellers & Co. showed that the resistance in cutting steel in a lathe would vary from 180,000 to 700,000 pounds per square inch of section removed, while for cast iron the resistance is about one third as much. The power required to remove a given amount of metal depends on the shape of the cut and on the shape and the sharpness of the tool used. If the cut is nearly square in section, the power required is a minimum; if wide and thin, a maximum. The dulness of a tool affects but little the power required for a heavy cut.

Heavy Work on a Planer.—Wm. Sellers & Co. write as follows to the American Mackinist: The 120' planer table is geared to run 18 ft. per

Heavy Work on a Planer.—Win. Sellers & Co. write as follows to the American Machinist. The 120' planer table is geared to run 18 ft. per minute under cut, and 72 feet per minute on the return, which is equivalent, without allowance for time lost in reversing, to continuous cut of 14.4 feet per minute. Assuming the work to be 28 feet long, we may take 14 feet as the continuous cutting speed per minute, the .8 of a foot being much more than sufficient to cover time loss in reversing and feeding. The machine carries four tools. At $\frac{1}{2}$ ' feed per tool, the surface planed per hour would be 35 square feet. The section of metal cut at $\frac{3}{2}$ ' depth would be .73' \times .125'' \times 4 = .375 square inch, which would require approximately 30.000 hs.

pressure to remove it. The weight of metal removed per hour would be $14 \times 12 \times .375 \times .26 \times 60 = 1082.8$ lbs. Our earlier form of 36'' planer has removed with one tool on 34'' cut on work 200 lbs. of metal per hour, and the 120'' machine has more than five times its capacity. The total pulling

power of the planer is 45,000 ibs.

Horse-power Required to Run Lathes. (J. J. Flather, Am. Mach., April 23, 1891.)—The power required to do useful work varies with the depth and breadth of chip, with the shape of tool, and with the nature and density of metal operated upon; and the power required to run a ma-

chine empty is often a variable quantity.

For instance, when the machine is new, and the working parts have not become worn or fitted to each other as they will be after running a few months, the power required will be greater than will be the case after the running parts have become better fitted.

running parts have become better fitted.

Another cause of variation of the power absorbed is the driving-belt; a tight belt will increase the friction, hence to obtain the greatest efficiency of a machine we should use wide belts, and run them just tight enough to prevent slip. The belts should also be soft and pliable, otherwise power is consumed in bending them to the curvature of the pulleys.

A third cause is the variation of journal-friction, due to slacking up or tightening the cap-screws, and also the end-thrust bearing screw.

Hartig's investigations show that it requires less total power to turn off a given wight of metal in a given time than it does to plane off the same

given weight of metal in a given time than it does to plane off the same amount; and also that the power is less for large than for small diameters. The following table gives the actual horse-power required to drive a lathe

empty at varying numbers of revolutions of main spindle.

			_
HORSE-POWER	E/OB	SWALT.	T.ATTTEQ

Without B	ack Gears.	With Ba	ck Gears.	'
Revs. of Spindle per min.	H.P. required to drive empty. Revs. of Spindle per min. H.P. required to drive empty.		Remarks.	
132.72	.145	14.6	.126	20" Fitchburg lathe.
219.08	.197	24.33	.141	
865.00	.310	38.42	.274	
47.4	.159	4.84	.132	Smallla the (131/2"), Chemnitz. Germany. New machine.
125.0	.259	12.8	.187	
188	.339	19.2	.230	
54.6	.206	6.61	.157	171/2" lathe do. New machine.
122	.339	14.8	.206	
188	.455	22.1	.249	
18.8	.086	2.31	.035	26" lathe do.
54.6	.210	6.72	.063	
82.2	.326	10.8	.087	

If H.P.₀ = horse-power necessary to drive lathe empty, and N = number of revolutions per minute, then the equation for average small lathes is $H.P._0 = 0.095 + 0.0012N$.

For the power necessary to drive the lathes empty when the back gears are in, an average equation for lathes under 20" swing is

$$H.P._{\bullet} = 0.10 + 0.006N.$$

The larger lathes vary so much in construction and detail that no general rule can be obtained which will give, even approximately, the power required to run them, and although the average formula shows that at least 0.096 horse-power is needed to start the small lathes, there are many American lathes under 20' swing working on a consumption of less than horse-power.

The amount of power required to remove metal in a machine is determinable within more accurate limits.

Referring to Dr. Hartig's researches, $H.P._1 = CW$, where C is a constant, and W the weight of chips removed per hour.

Average values of C are .030 for cast-iron, .082 for wrought-iron, .047 for steel.

The size of lathe, and, therefore, the diameter of work, has no apparent effect on the cutting power. If the lathe be heavy, the cut can be increased, and consequently the weight of chips increased, but the value of C appears to be about the same for a given metal through several varying sizes of lathes.

Horse-power required to remove Cast Iron in a 20-inch Lathe.
(J. J. Hobart.)

Descriptive No.	Number of Trials.	Tool used.	Average Cutting- speed in feet per minute.	Depth of Cut in inches.	Average Breadth of Cut in inches.	Average H.P. required to remove	Average pounds Metal turned off per hour.	Value of Constant C .
1 2 8	22 15 17	Side tool	37.90 80.50 42.61	.125 .125 .125	.015 .015 .015	.342 .218 .352	13.30 10.70 14.95	.0:5 .0:20 .0:23
4 5	4	Left - hand round nose	26.29	.125	.015	.287	9.22	.026
6	1 1	⅓″ broad	25.82 25.27 25.64	.015 .048 .125	.125 .048 .015	.255 .200 .246	9.06 10.89 8.99	.028 .018 .027

The above table shows that an average of .26 horse-power is required to turn off 10 pounds of cast-iron per hour, from which we obtain the average value of the constant C=.024.

Most of the cuts were taken so that the metal would be reduced 1/4" in diameter; with a broad surface cut and a coarse feed, as in No. 5, the power required per pound of chips removed in a given time was a maximum; the least power per unit of weight removed being required when the chip was square, as in No. 6.

Horse-power required to remove Metal in a 29-inch Lathe. (R. H. Smith.)

Number of Ex- periments.	Metal.	Cutting-speed. ft, per min.	Depth of Cut, in.	Average Breadth of Cut, in.	Avereage H.P. required to remove Metal.	Average pounds Metal removed per hour.	Value of C.
4 4 2 4 4 4 4 4 4	Cast iron Cast iron Cast iron Wrought iron Wrought iron Wrought iron Wrought iron Wrought iron Steel Steel Steel	12.7 11.1 12.85 9.6 9.1 7.9 9.35 6.00 5.8 5.1	.05 .135 .04 .03 .06 .14 .045 .02 .04	.046 .046 .088 .046 .046 .046 .038 .046 .046	.105 .217 .098 .059 .138 .186 .092 .048 .085	5.49 12.96 3.66 2.49 4.72 9.56 2.99 1.03 2.00 2.64	.019 .017 .027 .028 .029 .019 .031 .042 .042

The small values of C, .017 and .019, obtained for cast iron are probably due to two reasons: the iron was soft and of fine quality, known as pulley metal, requiring less power to cut; and, as Prof. Smith remarks, a lower cutting-speed also takes less horse-power.

Hardness of metals and forms of tools vary, otherwise the amount of chips turned out per hour per horse-power would be practically constant, the little a retailed results but slightly the widther wasted seems.

higher cutting-speeds decreasing but slightly the visible work done.

Taking into account these variations, the weight of metal removed per hour, multiplied by a certain constant, is equal to the power necessary to do the work.

This constant, according to the above tests, is as follows:

	Cast Iron.	Wrought Iron.	Steel.
Hartig		.032	.047
Smith		.028	.042
Hobart			
Average	026	.030	.044

The power necessary to run the lathe empty will vary from about .05 to .8 H.P., which should be ascertained and added to the useful horse-power, to obtain the total power expended.

Power used by Machine-tools. (R. E. Dinsmore, from the Electrical World.)

 Shop shafting 2 3/16" × 180 ft. at 160 revs., carrying ?" pulleys from 6" diam. to 36", and running 20 idle machine belt Lodge-Davis upright back-geared drill-press with ta le, 28" 	1.32 H.P.
swing, drilling \(\frac{3}{6}'' \) hole in cast iron, with a feed of 1 u. per minute. 3. Morse twist-drill grinder No. 2, carrying \(2'' \times 6'' \) wheels t \(2800 \)	0.78 H.P.
revs	0.29 H.P.
4. Pease planer 30" × 36", table 6 ft., planing cast iron, ci 4" deep, planing 6 sq. in. per minute, at 9 reversals	1.06 H.P.
5. Shaping-machine 22" stroke, cutting steel die, 6" stroke 16" deep, shaping at rate of 1.7 square inch per minute	0.37 H.P.
6. Engine-lathe 17" swing, turning steel shaft 286" diam., cut //16 deep, feeding 7.92 inch per minute	0.43 H.P.
7. Engine-lathe 21" swing, boring cast-iron hole 5" diam., cut 3/16 diam., feeding 0.3" per minute	0.28 H.P.
8. Sturtevant No. 2, monogram blower at 1800 revs. per minute,	0.8 H.P.
no piping	U.5 H.P.
22 reversals per minute.	8.2 H.P.

The table on the next page compiled from various sources, principally from Hartig's researches, by Prof. J. J. Flather (Am. Mach., April 12, 1894), may be used as a guide in estimating the power required to run a given machine; but it must be understood that these values, although determined by dynamometric measurements for the individual machines designated. are not necessarily representative, as the power required to drive a machine itself is dependent largely on its particular design and construction. The character of the work to be done may also affect the power required to operate; thus a machine to be used exclusively for brass work may be speeded from 10% to 15% higher than if it were to be used for iron work of

similar size, and the power required will be proportionately greater.

Where power is to be transmitted to the machines by means of shafting and countershafts, an additional amount, varying from 80% to 50% of the total power absorbed by the machines, will be necessary to overcome the friction

of the shafting. of the shafting.

Horse-power required to drive Shafting.—Samuel Webber, in his "Manual of Power" gives among numerous tables of power required to drive textile machinery, a table of results of tests of shafting. A line of 2½" shafting, 342 ft. long, weighing 4098 lbs., with pulleys weighing 5331 lbs., or a total of 9429 lbs., supported on 47 bearings, 216 revolutions per minute, required 1.885 H.P. to drive it. This gives a coefficient of friction of 5.52%, In seventeen tests the coefficient ranged from 8.34% to 11.4%, averaging

Horse-power Required to Drive Machinery.

	Observe	ed Horse-power.
Name of Machine.	Total Work,	Running Light.
Small screw-cutting lathe 13½" swing, B. G. Screw-cutting lathe 17½", B. G. Screw-cutting lathe 20" (Fitchburg), B. G. Screw-cutting lathe 20", B. G. Lathe, 80" face plate, will swing 108", T. G. Large facing lathe, will swing 68", T. G. Wheel lathe 60" swing. Small shaper (stroke 4", traverse 11"). Small shaper, Richards (9½" × 22").	0.41	0.18; 0.15*-0.34†
Screw-cutting lathe 1716", B. G.	0.867 0.47	0.207; 0.16-0.466 0.12; 0.12 to 0.31
Screw-cutting lathe 98" R G	0.462	0.05: 0.03 to 0.33
Lathe 80" face plate, will swing 108", T. G.	0.53	0.05; 0.03 to 0.33 0.187; 0.12to 0.66
Large facing lathe, will swing 68", T. G	0.91	0.37; 0.39 to 0.81
Wheel lathe 60" swing		0.28 to 3.40
Small shaper (stroke 4", traverse 11")	0.16	0.086 to 0.26
Small shaper, Richards (9)4" × 22"). Shaper (15" stroke Gould & Eberhardt).	0.24 0.63	0.07; 0.07 to 0.12 0.21; 0.01 to 0.47
Large shaper Richards (90" × 91")	1.14	0.26; 0.15 to 0.79
Large shaper, Richards (29" × 91"). Crank planer (capacity 23" × 27" × 28½" stroke). Planer (capacity 38" × 36" × 31" × 11 feet). Large planer (capacity 76" × 76" × 57 feet	0.24	0.12; 0.12 to 0.40
Planer (capacity 36" × 36" × 11 feet)	0 84	0.27
Large planer (capacity $76'' \times 76'' \times 57$ feet	1.47	0.60
Sinan orm press	1 0.06	0.89
Upright slet drilling mach. (will drill 21/2" diam.)	0.41	0.15; 0.15 to 0.45
Medium drill press	1.83 1.24	0.62
Large drill press	0.53	0.44; 0.1*-0.44†
Padial dvill XIZ foot curing	1 0 67	0.30; 0.12*-0.80†
Radial drill press Slotter (8'' stroke) Slotter (15'' stroke) Universal milling mach (Brown & Sharpe No. 1)	1.08	0.46
Slotter (8" stroke)	0.28	0.09; 0.05 to 0.25
Slotter (91/2" stroke)	0.44	0.22; 0.15 to 0.65
Slotter (15" stroke) & Channe No. 1)	0.95 0.28	0.57; 0.43 to 0 94 0.01; 0 008-0.13
Milling machine (13" cutter-head, 12 cutters)	0.66	0.26; 0.26 to 0.55
Small head traversing milling machine (cutter-head	0.00	0.20, 0.20 10 0.00
11" diameter, 16 cutters)	0.18	0.10
Gear cutter will cut 20" diameter	0.28	0.11
Horizontal boring machine for iron, 221/4" swing	1	0.12; 0.10-0.12*; 0.10 to 0.25†
Hydraulic shearing machine	1.52	0 37
Large plate shears—knives 28" long, 3" stroke Large punch press, over reach 28", 3" stroke, 11/2"	7.12	0.67
stock can be punched. Small punch and shear comb'd, 7½" knives, 1½" str. Circular saw for hot iron (30½" diameter of saw).	4.41	1.00
Small punch and shear comb'd, 71/6" knives, 11/6" str.	0.79	0.16
Circular saw for hot iron (301/2" diameter of saw)	4.12	0.61
Plate-bending rolls, diam. of rolls 13", length 914 ft.	2.70	.54
Wood planer 13%" (rotary knives, 2 nor 1 2 vert	8.08	3.35 (43
Wood planer 1714" (rotary knives)	4.63	1.25
Circular saw for not from (30½" diameter of saw). Plate-bending rolls, diam. of rolls 13", length 9½ ft. Wood planer 13½" (rotary knives, 2 hor'l 2 vert. Wood planer 22" (rotary knives). Wood planer 22" (rotary knives). Wood planer 23" (Daniel's pattern). Wood planer 23" (Daniel's pattern). Wood planer and matcher (capacity 14½ × 4¾"). Circular saw for wood (23" diameter of saw).	5.00	0.742-0.175
Wood planer 28" (Daniel's pattern)	8.90	1.45
Wood planer and matcher (capacity $14\frac{1}{2} \times 4\frac{9}{4}$ ")	6.91	4.18
Circular saw for wood (23" diameter of saw)	8.23	0.70
Circular saw for wood (35" diameter of saw) Band saw for wood (34" band wheel)		1.16 0.19
Wood-mortising and boring machine	0.49	0.84
Hor'l wood-boring and mortising machine, drill 4"	'	1
diam., mortise 814 deep × 1114" long	8.68	1.67; 0.65 to 2.6
Tenon and mortising machine Tenon and mortising machine Tenon and mortising machine	2.78	1.48 0.61
Tenon and mortising machine	2.25	2.17
Edge-molder and shaper. (Vertical spindle)	2.00	1.30
Edge-molder and shaper. (Vertical spindle)	2.45	2.00
Grindstone for tools, 31" diam., 6" face. Velocity	1	1
680 ft. per minute	1 1.55	0.82 0.24
Emery wheel 111/2" diameter × 1/2". Saw grinder	0.56	0.40
# With healt many 4 With and healt and healt		

^{*} With back gears. † Without back gears. ‡ For surface cutters. § With le cutters. B. G., back-geared. T. G., triple-geared.

Horse-power consumed in Machine-shops.—How much power is required to drive ordinary machine-tools? and how many men can be employed per horse-power? are questions which it is impossible to answer by any fixed rule. The power varies greatly according to the conditions in each shop. The following table given by J. J. Flather in his work for Dynamometers gives an idea of the variation in several large works. The percentage of the total power required to drive the shafting varies from 15 to 26, and the number of men employed per total H.P. varies from 0.68 to 6.04.

Horse-power; Friction; Men Employed.

		H	orse-	powe	er,		Total	Effec-
Name of Firm.	Kind of Work.	Total.	Required to drive Shafting.	Required to drive Machinery.	Per cent to drive Shafting.	Number of Men.		No. of Men per E.
Lane & Bodley	E. & W. W. W. W. E., M. M. M. E., etc. E, L,	58 100 400 25 95 2500	-95 8	85 305 17 500	15 23 32 80	300 1600 150 280	2.27 3.00 4.00 6.00 2.42 1.64	5.24 8.82
W. Sellers & Co. (one department)	H. M. M. T.	102 180 120 230	75	61 105	40 41	432 725	2.93 2.40 6.04 3.91	
Yale & Towne Co Ferracute Machine Co T. B. Wood's Sons	C. & L. P. & D. P. & S.	135 35 12	67 11	68 24	49 31	700 90 30	5.11 2.57 2.50	
Bridgeport Forge Co Singer Mfg. Co Howe Mfg. Co Worcester Mach. Screw Co Hartford ""	H. F. S. M. M. S.	150 1300 350 40 400 350	100	300	25	1500 80 250	.86 2.69 4.28 2.00 0.62 1.14	
Nicholson File Co Averages		346.4	-	-	38.6%	_		5.13

Abbreviations: E., engine; W.W., wood-working machinery; M. M., mining machinery; M. E., marine engines; L., locomotives; H. M., heavy machiner; M. T., nachine tools; C. & L., cranes and locks; P. & D., presses and dies; P. & S., pulleys and shafting; H. F., heavy forgings; S. M., sewing-machines; M. S., machine-screws: F., files.

J. T. Henthorn states (Trans. A. S. M. E., vi. 462) that in print-mills which he examined the friction of the shafting and engine was in 7 cases below an 90% and 30% in 11 cases from 30% to 38% as below in 90% and 30% in 11 cases from 30% to 38% as below in 90% and 30% in 11 cases from 30% to 38% as below in 90% and 30% in 11 cases from 30% to 38% as below in 90% and 30% in 11 cases from 30% to 38% as below in 90% and 30% in 11 cases from 30% to 38% as below in 90% and 30% in 11 cases from 30% to 38% as below in 90% and 30% in 11 cases from 30% to 38% as below in 90% and 30% in 11 cases from 30% to 38% as below in 90% and 30% in 11 cases from 30% and 30% and 30% in 11 cases from 30% and 30% and 30% in 11 cases from 30% and 30%

J. T. Henthorn states (Trans. A. S. M. E., vi. 462) that in print-mills which he examined the friction of the shafting and engine was in 7 cases below 20% and in 35 cases between 20% and 30%, in 11 cases from 30% to 33% and in 2 cases above 35%, the average being 25.9%. Mr. Barrus in eight cotton-mills found the range to be between 18% and 25.7%, the average being 22%. Mr. Flather believes that for shops using heavy machinery the percentage of power required to drive the shafting will average from 40% to 50% of the total power expended. This presupposes that under the head of shafting are included elevators, fans, and blowers.

ABRASIVE PROCESSES.

Abrasive cutting is performed by means of stones, sand, emery, glass, corundum, carborundum, crocus, rouge, chilled globules of iron, and in some cases by soft, friable iron alone. (See paper by John Richards, read before the Technical Society of the Pacific Coast, Am. Mach., Aug. 20, 1891, p. Eng. & M. Jour., July 25 and Aug. 15, 1891.)

The "Cold Saw."-For sawing any section of iron while come one cold saw is sometimes used. This consists simply of a plain soft steel or iron disk without teeth, about 42 inches diameter and 8/16 inch thick. velocity of the circumference is about 15,000 feet per minute. One of these saws will saw through an ordinary steel rail cold in about one minute. In this saw the steel or iron is ground off by the friction of the disk, and is not cut as with the teeth of an ordinary saw. It has generally been found more profitable, however, to saw iron with disks or band-saws fitted with cutting-teeth, which run at moderate speeds, and cut the metal as do the teeth of a milling-cutter.

Reese's Fusing-disk.—Reese's fusing-disk is an application of the cold saw to cutting iron or steel in the form of bars, tubes, cylinders, etc., in which the piece to be cut is made to revolve at a slower rate of speed than the saw. By this means only a small surface of the bar to be cut is presented at a time to the circumference of the saw. The saw is about the presented at a time to the circumference of the saw. The saw is about the same size as the cold saw above described, and is rotated at a velocity of about 25,000 feet per minute. The heat generated by the friction of this saw against the small surface of the bar rotated against it is so great that the particles of iron or steel in the bar are actually fused, and the "sawdust" welds as it falls into a solid mass. This disk will cut either cast iron, wrought tron, or steel. It will cut a bar of steel 1% inch diameter in one minute, including the time of setting it in the machine, the bar being rotated about 200 turns per minute.

Cutting Stone with Wire.—A plan of cutting stone by means of a wire cord has been tried in Europe. While retaining sand as the cutting agent, M. Paulin Gay, of Marsellles, has succeeded in applying it by mechanical means, and as continuously as formerly the sand-blast and band-saw, with both of which appliances his system—that of the "helicoidal wire cord"—has considerable analogy. An engine puts in motion a continuous wire cord (varying from five to seven thirty-seconds of an inch in diameter. according to the work), composed of three mild-steel wires twisted at a certain pitch, that is found to give the best results in practice, at a speed of from 15 to 17 feet per second.

The Sand-blast. - In the sand-blast, invented by B. F. Tilghman, of Philadelphia, and first exhibited at the American Institute Fair, New York, in 1871, common sand, powdered quartz, emery, or any sharp cutting material is blown by a jet of air or steam on glass, metal, or other comparatively brittle substance, by which means the latter is cut, drilled, or engraved To protect those portions of the surface which it is desired shall not be abraded it is only necessary to cover them with a soft or tough material, such as lead, rubber, leather, paper, wax, or rubber-paint. (See description in App. Cyc. Mech.; also U. S. report of Vienna Exhibition, 1878, vol. iii. 316.)

A "jet of sand" impelled by steam of moderate pressure, or even by the

A "jet of sand" impelled by steam of moderate pressure, or even by the blast of an ordinary fan, depolishes glass in a few seconds; wood is cut quite rapidly; and metals are given the so-called "frosted" surface with great rapidity. With a jet issuing from under 300 pounds pressure, a hole was cut through a piece of corundrum 1½ inches thick in & minutes.

The sand-blast has been applied to the cleaning of metal castings and sheet metal, the graining of zinc plates for lithographic purposes, the frosting of silverware, the cutting of figures on stone and glass, and the cutting of devices on monuments or tombstones, the recutting of files, etc. The time required to sharpen a worn-out 14-inch bastard file is about four minutes. About one pint of sand, passed through a No. 120 sieve, and four horse-power of 60-lb. steam are required for the operation. For cleaning house-power of 60-lb. steam are required for the operation. For cleaning castings compressed air at from 8 to 10 pounds pressure per square inch is employed. Chilled-iron globules instead of quartz or flint-sand are used with good results, both as to speed of working and cost of material, when the operation can be carried on under proper conditions. With the expensive proper conditions. the operation can be carried on under proper conditions. With the expenditure of 2 horse-power in compressing air, 2 square feet of ordinary scale on the surface of steel and iron plates can be removed per minute. The surface thus prepared is ready for tinning, galvanizing, plating, bromsing, painting, etc. By continuing the operation the hard skin on the surface of castings, which is so destructive to the cutting edges of milling and other tools, can be removed. Small castings are placed in a sort of slowly rotating barrel, open at one or both ends, through which the blast is directed downward against them as they tumble over and over. No portion of the surface escapes the action of the sand. Plain cored work, such as valve-bodies, can be cleaned perfectly both inside and out. 100 lbs. of cast-use of the sand of the surface escapes the action of the sand. ngs can be cleaned in from 10 to 15 minutes with a blast created by 2 horse.

power. The same weight of small forgings and stampings can be scaled in from 20 to 30 minutes.—Iron Age, March 8, 1894.

EMERY-WHEELS AND GRINDSTONES.

The Selection of Emery-wheels.—A pamphlet entitled "Emery wheels, their Selection and Use," published by the Brown & Sharpe Mfg. Co., after calling attention to the fact that too much should not be expected of one wheel, and commenting upon the importance of selecting the proper wheel for the work to be done, says:

wheel for the work to be done, says:
Wheels are numbered from coarse to fine; that is, a wheel made of No. 60 emery is coarser than one made of No. 100. Within certain limits, and other things being equal, a coarse wheel is less liable to change the temperature of the work and less liable to glaze than a fine wheel. As a rule, the harder the stock the coarser the wheel required to produce a given finish. For example, coarser wheels are required to produce a given surface upon hardened steel than upon soft steel, while finer wheels are re-

quired to produce this surface upon brass or copper than upon either hardened or soft steel.

Wheels are graded from soft to hard, and the grade is denoted by the letters of the alphabet. A denoting the softest grade. A wheel is soft or hard chiefly on account of the amount and character of the material combined in its manufacture with emery or corundum. But other characteristics being equal, a wheel that is composed of fine emery is more compact and harder than one made of coarser emery. For instance, a wheel of No. 100 emery, grade B, will be harder than one of No. 60 emery, same grade.

The softness of a wheel is generally its most important characteristic. soft wheel is less apt to cause a change of temperature in the work, or to become glazed, than a harder one. It is best for grinding hardened steel, cast-iron, brass, copper, and rubber, while a harder or more compact wheel is better for grinding soft steel and wrought iron. As a rule, other things being equal, the harder the stock the softer the wheel required to produce

a given finish.
Generally speaking, a wheel should be softer as the surface in contact with the work is increased. For example, a wheel 1/16-inch face should be with the work is increased. For example, a wheel 1/16-inch face should be harder than one ½-inch face. If a wheel is hard and heats or chatters, it can often be made somewhat more effective by turning off a part of its cutting surface; but it should be clearly understood that while this will sometimes prevent a hard wheel from heating or chattering the work, such a wheel will not prove as economical as one of the full width and proper grade, for it should be borne in mind that the grade should always bear the proper relation to the width. (See the pamphlet referred to for other information. See also lecture by T. Dunkin Paret, Pres't of The Tanite Co., on Emery-wheels, Jour. Frank. Inst., March, 1890.)

Speed of Emery-wheels.—The following speeds are recommended by different makers:

by different makers:

O-51 ~			po	ute.	₩ 8	Rev	olutions	per min	ute.
Diameter of W heel, inches	Waltham E. W. Co.	Tanite Co.	Grant Corundum Wheel Co.	Norton E. W. Co	Diameter o Wheel, inch	Waltham E. W. Co.	The Tanite Co.	Grant Corundum Wheel Co.	Norton E. W. Co.
1 11½ 2 21½ 3 4 5 6 7 8	19,000 12,500 9,500 7,600 6,400 4,800 3,800 3,200 2,700 2,400 2,150	14,400 10,800 8,640 7,200 5,400 4,320 8,600 8,080 2,700 2,400	7,400 5,400 4,400 3,600 8,200 2,700 2,400	12,000 10,000 8,500 7,400 5,450 4,400 8,600 8,150 2,750 2,450	10 12 14 16 18 20 22 24 26 30 36	1,950 1,600 1,400 1,200 1,050 950 875 800 750 675 550	2,160 1,800 1,570 1,350 1,222 1,080 1,000 917	2,200 1,800 1,600 1,400 1,250 1,100 1,000 925 600 500 400	2,200 1,850 1,600 1,400 1,250 1,100 1,000 925 825 735 550

[&]quot;We advise the regular speed of 5500 feet per minute." (Detroit Emerywheel Co.) "Experience has demonstrated that there is no advantage in runni

solid emery-wheels at a higher rate than 5500 feet per minute peripheral

speed." (Springfield E. W. Mfg. Co.)

"Although there is no exactly defined limit at which a wheel must be run to render it effective, experience has demonstrated that, taking into account safety, durability, and liability to heat, 5500 feet per minute at the periphery gives the best results. All first-class wheels have the number of revolutions necessary to give this rate marked on their labels, and a column of figures in the price-list gives a corresponding rate. Above this speed all wheels are unsafe. If run much below it they wear away rapidly in proportion to what they accomplish." (Northampton E. W. Co.)

Grades of Emery.—The numbers representing the grades of emery run from 8 to 120, and the degree of smoothness of surface they leave may

be compared to that left by files as follows:

8	and	10	represent	the	cut	t of a wood rasp.
	**	20	" "	**		" a coarse rough file.
24	**	30	44	**		" an ordinary rough file.
86	44	40	66	46		" a bastard file.
46		60	64	46	66	" a second-cut file.
	86	80	44	**	66	" a smooth
90		100	48	66		" a superfine "
	F at		P "	80		" a dead-smooth file.

Speed of Polishing-wheels.

Wood covered with leather, about	7000 ft. per minute
" " a hair brush, about	2500 revs, for larges
" " 11/2" to 8" diam., hair 1" to 11/4" long, ab.	4500 " " smalles
Walrus-hide wheels, about	8000 ft, per minute
Rag-wheels, 4 to 8 in. diameter, about	7000 " " "

Safe Speeds for Grindstones and Emery-wheels.—C. D. Hiscox (Iron Age, April 7, 1892), by an application of the formula for centrifugal force in fly-wheels (see Fly-wheels), obtains the figures for strains is grindstones and emery-wheels which are given in the tables below. His formulæ are:

Stress per sq. in, of section of a grindstone = $(.7071D \times N)^2 \times .0000795$ " an emery-wheel = $(.7071D \times N)^2 \times .00010220$

D = diameter in feet, N = revolutions per minute.

He takes the weight of sandstone at .078 lb, per cubic inch, and that of an emery-wheel at 0.1 lb, per cubic inch; Ohio stone weighs about .081 lb, and Huron stone about .089 lb, per cubic inch. The Ohio stone will bear a speed at the periphery of 2500 to 3000 ft, per min., which latter should never be exceeded. The Huron stone can be trusted up to 4000 ft, when properly exceeded. The Huron stone can be trusted up to 4000 ft., when properly clamped between flanges and not excessively wedged in setting. Aparl from the speed of grindstones as a cause of bursting, probably the majority of accidents have really been caused by wedging them on the shaft and over wedging to true them. The holes being square, the excessive driving of wedges to true the stones starts cracks in the corners that eventually rus out until the centrifugal strain becomes greater than the tenacity of the remaining solid stone. Hence the necessity of great caution in the use of wedges, as well as the holding of large quick-running stones between large flaures and leather weakness. flanges and leather washers.

Strains in Grindstones. LIMIT OF VELOCITY AND APPROXIMATE ACTUAL STRAIN PER SQUARE INCH OF SECTIONAL AREA FOR GRINDSTONES OF MEDIUM TENSILE STRENGTH.

Diam-		F	Revolution	s per min	ute.		
eter.	100	150	200	250	800	850	400
feet. 2 21,6 3 81,6 4 41,6	lbs. 1.58 2.47 3.57 4.86 6.35 8.04	lbs. 8.57 5.57 8.04 10.93 14.30 18.08	lbs. 6.35 9.88 14.28 19.44 27.37 32.16	1bs. 9.98 15.49 22.34 30.38	lbs. 14.30 22.39 82.16	lbs. 18.86 28.64	lbs. 25.42 89.75
5°	9.98 14.80 19.44	82.84 82.17		times th	10 strain	reaking s for size in each o	opposin

The figures at the bottom of columns designate the limit of velocity (in revolutions per minute), at the head of the columns for stones of the diameter in the first column opposite the designating figure.

A general rule of safety for any size grindstone that has a compact and

A general rule of safety for any size grandstone that has a compact and strong grain is to limit the peripheral velocity to 47 feet per second.

There is a large variation in the listed speeds of emery-wheels by different makers—4000 as a minimum and 5600 maximum feet per minute, while others claim a maximum speed of 10,000 feet per minute as the safe speed of their best emery-wheels. Rim wheels and iron centre wheels are specialties that require the maker's guarantee and assignment of speed.

Strains in Emery-wheels.

ACTUAL STRAIN PER SQUARE INCH OF SECTION IN EMERY-WHEELS AT THE
VELOCITIES AT HEAD OF COLUMNS FOR SIZES IN FIRST COLUMN.

es.				Re	volutio	ns per	minut	e.			
Diam., inches.	600	800	1000	1200	1400	1600	1800	2000	2200	2400	2600
4 6								22.67 51.18	27.43 61.86		
8			22.67 35.47	32.65	44.45 69.51				109.76	180.62	
10 12	18.40	32.72	51.12	73.62	100.21	130.88	165.65		171.71		•••••
14 16	24.80 32.57	43.90 57.65				175.60		·····	Diam	Revs	
18 20	41.41 50.98		115.03 141.22	165.65						m	in.
22	61.81	109.41	171.23						in.	2800	3000
24 26	73.62 86.36	130.88 152.85				•••••			4	44.43	51.12
30	115.04								6	100.21	115.03
36	165.64			l • • · • • •	· · · ·	1			8	177.80	i

Joshua Rose (Modern Machine-shop Practice) says: The average speed of grindstones in workshops may be given as follows:

Circumferential Speed of Stone.

For grinding machinists' tools, about 900 feet per minute. 600 " "

The speeds of stones for file-grinding, and other similar rapid grinding is thus given in the "Grinders' List." Diam. ft..... 734 144 Revs. per min. 135 154 168 180 196 240 216

The following table, from the Mechanical World, is for the diameter of stones and the number of revolutions they should run per minute (not to be exceeded), with the diameter of change of shift pulleys required, varying each shift or change 2½ inches, 2½ inches, or 2 inches in diameter for each reduction of 6 inches in the diameter of the stone.

Diameter	Revolutions	Shift o	of Pulleys, in inc	ches.
of Stone.	per minute.	21/6	21/4	2
ft. in. 8 0 7 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	185 144 154 166 180 196 216 240 270 80G 860	40 871/2 35 321/2 321/2 35 271/2 25 221/2 20 171/2 15	86 8334 3114 3914 3914 2214 2214 2014 18 184 184	32 30 38 26 24 22 20 18 16 14
1	8	8	4	5

Columns 3, 4, and 5 are given to show that if we start an 8-foot stone with, say, a countershaft pulley driving a 40-inch pulley on the grindstone spindle, and the stone makes the right number (135) of revolutions per minute, the reduction in the diameter of the pulley on the grinding-stone spindle, when the stone has been reduced 6 inches in diameter, will require to be also reduced 2½ inches in diameter, or to shift from 40 inches to 37½ inches, and so on similarly for columns 4 and 5. Any other suitable dimensions of pulley may be used for the stone when eight feet in diameter, but the number of inches in each shift named, in order to be correct, will have to be proportional to the numbers of revolutions the stone should run, as given in column 2 of the table.

Varieties of Grindstones.

(Joshua Rose.)

FOR GRINDING MACHINISTS' TOOLS.

Name of Stone.	Kind of Grit.	Texture of Stone.	Color of Stone.
	Medium to finest	Soft and sharp	Blue or yellowish gray Uniformly light blue Reddish!

FOR WOOD-WORKING TOOLS.

Wickersley Liverpool or Melling.	Medium to fine Medium to fine	Very soft Soft, with sharp grit	Grayish yellow Reddish
Bay Chaleur (New) Brunswick),	Medium to finest	Soft and sharp	Uniform light blue
Huron, Michigan	Fine	Soft and sharp	Uniform light blue

FOR GRINDING BROAD SURFACES, AS SAWS OR IRON PLATES.

Newcastle	Coarse to med'm	The hard ones	Yellow
Independence	Coarse	Hard to medium	Grayish white Yellowish white
Massillon	Coarse	Hard to medium	Yellowish white

TAP DRILLS.

Taps for Machine-screws. (The Pratt & Whitney Co.)

Approx. Diameter, fractions of an inch.	Wire Gauge.	No. of Threads to inch.	Approx. Diameter, fractions of an inch.	Wire Gauge.	No. of Threads to inch.
7/64	No. 1 2 8 4 5	60, 72 48, 56, 64 40, 48, 56 32, 36, 40 80, 32, 36, 40	14 17/64 9/82	No. 13 14 15 16 18	20, 24 16, 18, 20, 22, 34 18, 20, 24 16, 18, 20, 23 16, 18, 20
9/64	6 7	30, 32, 36, 40 24, 30, 82	5/16	19 20 22 24 26 28 80	16, 18, 20 16, 18, 20
5/32	8 9	24, 30, 32, 36, 40 24, 28, 30, 32	% 3€	22 24	16, 18 14, 16, 18
8/16	10 11	20, 22, 24, 30, 82 22, 24		26 28	16 16
7/32	12	20, 22, 24		80	16

The Morse Twist Drill and Machine Co. gives the following table showing the different sizes of drills that should be used when a suitable thread is to be tapped in a hole. The sizes given are practically correct.

E G	Tap Drills.	Morse Twist Drill and Machine Co.)
		(The Mo

10 15 20 5/32 11/64 15 15/32 1	Diam. of Tap.		No. Threads to inch.	18	Drill fo	Drill for V Thread.	read.	Drill (Drill for U. S. Thread.	zi.	Diam. of Tap.	No. Threads to inch.	spa .	Drill for V Thread.	for ead.	Drill for U. S. S. Three	for Thread.
16 18 20 5/32 11/64 15 15/32 17 18 17 18 17 18 17 18 17 18 17 18 17 18 17 18 17 18 17 18 17 18 17 18 17 18 18				t			Ì			T		Ì	$\frac{1}{1}$				
15 20 7/32 1/2	77	16	18 20	_	5/32	11/64	12	:		8/16	1%	20	_	59/64	61/64	61/64	
16 18 17 17 18 18 18 18 18	8	16	8 2	_	3/16	18/64	00			:	1 5/32	œ		61/64	63/64		
15 15 17 18 17 18 18 17 18 18	5/16	18	18	_	2	15/64				:	1 8/16	2		63/64	11/64	:	
14 16 18 17 64 0/82 M N N N N N N N N N N N N N N N N N N	11/35	9	8	_	7	17/84					7/32	2	_	1/64	18/64	-	:
14 16 18 18 18 18 18 18 18	*	14	16	a	17,/64	8/6	×		z	:	77		_	8/64		1 5/64	:
14 16 16 16 17 17 17 17 17	18/32	14	16	-	Z	5/16	4	:	:	:	1 9/32		_	1 5/84		•	:::::::::::::::::::::::::::::::::::::::
14 18 18 18 18 18 18 18	2/18	7	16		œ	1/38	:	σΩ	:	:	1 5/16	:	_	14/01	•	:	:
12 13 14 35 35 35 35 35 35 35 3	15/32	14		_	3% 8	×	:	:	:	:	11/38	:	_	2/6		:	:
12 13 14 7/16 27/64 7/16 20/64 17/8 6 18/78 6 18/78 18/78 18/78 18/76	X	2	ž	*	×	⋟	25/6 <u>4</u>	:	18/82	:	- % - %	•	_	%	•	111/64	:
12 14 7/16 29/04 20/04 17/16 0 13/16 10/11 12 14 17/16 29/04 10/11 12 13/16 13/1	3	22	ž	*	13/32	اري 24/92	2/16		:	:	1 18/32	•	_	2/35	:	:	:
12 13 13 14 14 15 15 15 15 15 15	9/16	22	14	_	7/18	29/6 2	:	88 87	:	:	1 7/16	9	_	8/16	:	:	:
10 11 12 83/64 1772 83/64 83/64 17.78 6 117/64 117/	19/32	22	7		81/64	×	:	:		:	1 15/32	:	_	88 			:
10 12 28/64 17/782 55/04 11/782 5 119/64 11/782 5 119/64 11/782 5 119/64 11/782 5 119/64 11/782 5 119/64 11/782 5 119/64 11/782 5 119/64 11/782 5 119/64 11/782 5 119/64 11/782 5 119/64 11/782 5 119/64 11/782 5 119/64 11/782 5 119/64 11/782 5 119/64 11/782 5 119/64 119/6	*	2	# #	C)	81/64	×	88/64	:	38/64	:	22	•	_	17/64	:	1 19/64	:
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TAPER BOLTS, PINS, REAMERS, ETC.

Taper Bolts for Locomotives.—Bolt-threads, U. S. standard, except stay-bolts and boiler-stude, V threads, 12 per inch; valves, cocks, and pugs, V threads, 14 per inch, and ½-inch taper per 1 inch. Standard bolt toper 1/16 inch per foot.

Taper Reamers.—The Pratt & Whitney Co. makes standard faper reamers for locomotive work taper 1/16 inch per foot from ½ inch diam.: 4 in, length of flute to 2 in. diam.; 18 in. length of flute, diameters advancing by 16ths and 32ds. P. & W. Co.'s standard taper pin reamers taper ½ in. per foot, are made in 14 sizes of diameters, 0.135 to 1.009 in.; length of flute 1 5/16 in. to 12 in.

DIMENSIONS OF THE PRATT & WHITNEY COMPANY'S REAMERS FOR MORSE STANDARD-TAPER SOCKET.

No.	Diameter Small End, inches.	Diameter Large End, inches.	Gauge Diam.,la'ge end, inches	L'ngth,	Length Flute, inches.	Total L'ngth.	Taper per foot, inches.
1	0.865	0.525	0.475	21/6 21/6	8	5)4 6)4 7)4 8)4	0.600
2	0.578	0.749	0.699	216	814	61/4	0.602
8	0.779	0.982	0 936	35/16	4	736	0.602
4	1.026	1.283	1.231	4	j 5	84/2	0.623
5	1.486	1.796	1.746	5 ·	6	10	0.630
6	2.117	2,566	2.500	714	81/6	1216	0.625

Standard Steel Taper-pins.—The following sizes are made by The Frati & Whitney Co.:

Number: 8 7 10 Diameter large end: .172 .193 .219 .250 .289 .841 .409 .492 .591 .706 Approximate fractional sizes: 5/82 11/64 8/16 7/32 19/64 11/82 13/32 1/4 19/32 23/32 Lengths from To* Diameter small end of standard taper-pin reamer: † .135 .146 .162 .183 .208 .240 .279 .33 .331 .482 .581 .146 .162 .183 .208 .398

Standard Steel Mandrels. (The Pratt & Whitney Co.)—These mandrels are made of tool-steel, hardened, and ground true on their centres. Centres are also ground to true 60 cones. The ends are of a form best adapted to resist injury likely to be caused by driving. They are slightly taper. Sizes, ½ in. diameter by 3% in. long to 3 in. diam. by 14% in. long, diameters advancing by 16ths.

PUNCHES AND DIES, PRESSES, ETC.

Clearance between Punch and Die.—For computing the amount of clearance that a die should have, or, in other words, the difference in size between die and punch, the general rule is to make the diameter of die-hole equal to the diameter of the punch, plus 2/10 the thickness of the plate. Or, D=d+.2t, in which D= diameter of die-hole, d= diameter of punch, and t= thickness of plate. For very thick plates some mechanics prefer to make the die-hole a little smaller than called for by the above rule. For ordinary boiler-work the die is made from 1/10 to 3/10 of the thickness of the plate larger than the diameter of the punch; and some boiler-makers advocate making the punch fit the die accurately. For punching nuts, the punch fits in the die. (Am. Machinist.)

of the plate larger than the diameter of the punch; and some boiler-makers advocate making the punch fit the die accurately. For punching nuts, the punch fits in the die. (Am. Machinist.)

Kennedy's Spiral Punch. (The Pratt & Whitney Co.)—B. Martell, Chief Surveyor of Lloyd's Register, reported tests of Kennedy's spiral punches in which a %-inch spiral punch penetrated a %-inch plate at a pressure of 22 to 25 tons, while a flat punch required 33 to 35 tons. Steel boilerplates punched with a flat punch gave an average tensile strongth of 58,579

^{*} Lengths vary by ¼" each size. † Taken ¼" from extreme end. Each soverlaps smaller one about ¼". Taper ¼" to the foot.

ibs. per square inch, and an elongation in two inches across the hole of 5.2%, while plates punched with a spiral punch gave 63,929 lbs., and 10.6% elonga-

tion.

The spiral shear form is not recommended for punches for use in metal of a thickness greater than the diameter of the punch. This form is of greatest benefit when the thickness of metal worked is less than two thirds the

diameter of punch.
Size of Blanks used in the Drawing-press. Oberlin Smith (Jour. Frank. Inst., Nov. 1886) gives three methods of finding the size of blanks. The first is a tentative method, and consists simply in a series of experiments with various blanks, until the proper one is found. This is for use mainly in complicated cases, and when the cutting portions of the die and punch can be finally sized after the other work is done. The second method is by weighing the sample piece, and then, knowing the weight of the sheet metal per square inch, computing the diameter of a piece having the required area to equal the sample in weight. The third method is by computation, and the formula is $x = \sqrt{d^2 + 4dh}$ for sharp-cornered cup, where x = diameter of blank, d = diameter of cup, h = height of cup. For round-cornered cup where the corner is small, say radius of corner less than $\frac{1}{4}$ height of cup, the formula is $x = (\sqrt{d^2 + 4dh}) - r$, about; r being the radius of the corner. This is based upon the assumption that the thickness

radius of the corner. This is oused upon the assumption that the thickness of the metal is not to be altered by the drawing operation.

Pressure attainable by the Use of the Drop-press. (R. H. Thurston, Trans. A. S. M. E., v. 58.)—A set of copper cylinders was prepared, of pure Lake Superior copper; they were subjected to the action of presses of different weights and of different heights of fall. Companion specimens of copper were compressed to exactly the same amount, and measures were obtained of the loads producing compression, and of the amount of work obtained of the loads producing compression, and of the loads done in producing the compression by the drop. Comparing one with the other it was found that the work done with the hammer was 90% of the work which should have been done with perfect efficiency. That is to say, the which should have been done with perfect efficiency. That is to say, the work done in the testing-machine was equal to 90% of that due the weight of the drop failing the given distance.

Formula: Mean pressure in pounds = $\frac{\text{Weight of drop} \times \text{fall} \times \text{efficiency}}{\text{Mean pressure in pounds}}$

compression.

For pressures per square inch, divide by the mean area opposed to crush-

ing action during the operation.

Flow of Metals. (David Townsend, Jour. Frank. Inst., March, 1878.)

In punching holes 7/16 inch diameter through iron blocks 13/4 inches thick; it was found that the core punched out was only 1 1/16 inch thick, and its volume was only about 32% of the volume of the hole. Therefore, 68% of the metal displaced by punching the hole flowed into the block itself, increasing volume was only about 32% of the volume of the hole. its dimensions.

FORCING AND SHRINKING FITS.

Forcing Fits of Pins and Axles by Hydraulic Pressure.

—A 4-inch axle is turned .015 inch diameter larger than the hole into which it is to be fitted. They are pressed on by a pressure of 30 to 35 tons. (Lecture by Coleman Sellers, 1872.)

For forcing the crank-pin into a locomotive driving wheel, when the pin-hole is perfectly true and smooth, the pin should be pressed in with a pres-sure of 6 tons for every inch of diameter of the wheel fit. When the hole is not perfectly true, which may be the result of shrinking the tire on the wheel centre after the hole for the crank-pin has been bored, or if the hole is not perfectly smooth, the pressure may have to be increased to 9 tons for every inch of diameter of the wheel-fit. (Am. Machinist.)

Shrinkage Fits.—In 1886 the American Railway Master Mechanics' Association recommended the following shrinkage allowances for tires of standard locomotives. The tires are uniformly heated by gas-flames, slipped over the cast-iron centres, and allowed to cool. The centres are turned to the standard sizes given below, and the tires are bored smaller by the amount of the shrinkage designated for each:

Diameter of centre, in . . . Shrinkage allowance, in .. .053 .040 .047 .060 .066 .070

This shrinkage allowance is approximately 1/80 inch per foot, or 1/960. A common allowance is 1/1000. Taking the modulus of elasticity of steel at

30,000,000, the strain caused by shrinkage would be 30,000 lbs. per square inch, less an uncertain amount due to compression of the centre.

SCREWS, SCREW-THREADS, ETC.*

Efficiency of a Screw.—Let a = angle of the thread, that is, the angle whose tangent is the pitch of the screw divided by the circumference of a circle whose diameter is the mean of the diameters at the top and bottom of the thread. Then for a square thread

Efficiency =
$$\frac{1 - f \tan a}{1 + f \cot a}$$

in which f is the coefficient of friction. (For demonstration, see Cotterill and Slade, A police Mechanics, p. 146.) Since cotan $= 1 + \tan x$, we may substitute for cotan a the reciprocal of the tangent, or if p = pitch, and c = mean circular than a = mean circular tha cumference of the screw.

Efficiency =
$$\frac{1 - f\frac{p}{c}}{1 + f\frac{c}{p}}$$

EXAMPLE.—Efficiency of square-threaded screws of 1/4 in. pitch.

Diameter at bottom of thread, in 1	2	8	4
" top " " 136	21/6	81/6	416
Mean circumference " " 3.927	7.069	10.21	13.3a
Cotangent $a = c + p \dots = 7.854$	14.14	20.42	26.70
Tangent $a = p + c = .1278$.0707	.0490	.0375
Efficiency if $f = .10 \dots = 55.8$	41.2%	82.7%	2 7.2≴
" $f = .15 = 45$	81.7%	24.4%	19.9%

The efficiency thus increases with the steepness of the pitch. The above formulæ and examples are for square-threaded screws, and consider the friction of the screw-thread only, and not the friction of the collar or steep by which end thrust is resisted, and which further reduces the efficiency. The efficiency is also further reduced by giving an inclination to the side of the thread, as in the V-threaded screw. For discussion of this subject, see paper by Wilfred Lewis, Jour. Frank. Inst. 1880; also Trans. A. S. M. E., vol. xii. 784.

Efficiency of Screw-bolts.—Mr. Lewis gives the following approximate formula for ordinary screw-bolts (V threads, with collars): p = pthch of screw, d = othick diameter of screw, F = f force applied at circumference to lift a unit of weight, E = efficiency of screw. For an average case, in which the coefficient of friction may be assumed at .15,

$$F = \frac{p+d}{3d}, \qquad E = \frac{p}{p+d}.$$

For bolts of the dimensions given above, ½-in. pitch, and outside diameters 1½, 2½, 3½, and 4½ in., the efficiencies according to this formula would be, respectively, 25, 167, 125, and 10.

James McBride (Trans. A. S. M. E. x. xii. 781) describes an experiment with an ordinary 2-in screw-bolt, with a V thread, 4½ threads per inch, raising a weight of 7500 lbs, the force being applied by turning the nut. Of the power applied 89.8% was absorbed by friction of the nut on its supporting washer and of the threads of the bolt in the nut. The nut was not faced

washer and of the threads of the bott in the but. The but was not raced and had the flat side to the washer.

Prof. Ball in his "Experimental Mechanics" says: "Experiments showed in two cases respectively about % and % of the power was lost." Trautwine says: "In practice the friction of the screw (which under heavy loads becomes very great) make the theoretical calculations of but little value."

Weisbach says: "The efficiency is from 19% to 80%."

Rificiency of a Differential Screw.—A correspondent of the American Machinist describes an experiment with a differential screw-punch, consisting of an outer screw 2 in. diam., 3 threads per in., and an inner screw 1% in. diam., 3% threads per inch. The pitch of the outer screw

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being $\frac{1}{2}$ in. and that of the inner screw $\frac{2}{7}$ in., the punch would advance in one revolution $\frac{1}{2} - \frac{2}{7} = \frac{1}{21}$ in. Experiments were made to determine the force required to punch an $\frac{11}{16}$ -in. hole in iron $\frac{1}{2}$ in, thick, the force being applied at the end of a lever-arm of $\frac{47}{2}$ in. The leverage would be $\frac{47}{2} \times \frac{2\pi}{2} \times \frac{21}{2} = 6300$. The mean force applied at the end of the lever was 95 lbs. and the force at the punch, if there was no friction, would be $\frac{1}{2} \times \frac{1}{2} as 95 lbs., and the force at the punch, if there was no friction, would be 6300 \times 95 = 598,500 lbs. The force required to punch the iron, assuming a shearing resistance of 50,000 lbs. per sq. in., would be 50,000 \times 11/16 \times π \times 14 = 27,000 lbs., and the efficiency of the punch would be 27,000 \times 598,500 = ouly 4.5%. With the larger screw only used as a punch the mean force at the end of the lever was only 82 lbs. The leverage in this case was 478 \times 2 π \times 3 = 900, the total force referred to the punch, including friction, 900 \times 82 = 73,800, and the efficiency 27,000 \times 73,800 = 36.7%. The screws were of tool-steel, well fitted, and lubricated with lard-oil and plumbago. **Powell's New Screw-thread.**—A. M. Powell (Am. Mach., Jan. 24, 1895) has designed a new screw-thread to replace the square form of thread, giving the advantages of greater ease in making fits, and provision for "take up" in case of wear. The dimensions are the same as those of square form of thread, thread screws, with the exception that the sides of the thread, instead of

thread screws, with the exception that the sides of the thread, instead of being perpendicular to the axis of the screw, are inclined 14% to such perpendicular; that is, the two sides of a thread are inclined 29° to each other. The formulæ for dimensions of the thread are the following: Depth of thread = ½ + pitch; width of top of thread = width of space at bottom = .8707 + pitch; thickness at root of thread = width of space at top = .6298 + pitch. The term pitch is the number of threads to the inch.

PROPORTIONING PARTS OF MACHINES IN A SERIES OF SIZES.

(Stevens Indicator, April, 1892.)

The following method was used by Coleman Sellers while at William Sellers & Co.'s to get the proportions of the parts of machines, based upon the size obtained in building a large machine and a small one to any series of machines. This formula is used in getting up the proportion-book and arranging the set of proportions from which any machine can be constructed of intermediate size between the largest and smallest of the series.

Rule to Establish Construction Formulæ.—Take difference between the nominal sizes of the largest and the smallest machines that have been designed of the same construction. Take also the difference between the sizes of similar parts on the largest and smallest machines selected. Divide the latter by the former, and the result obtained will be a "factor," which multiplied by the nominal capacity of the intermediate machine, and increased or diminished by a constant "increment," will give the size of the part required. To find the "increment." Multiply the nominal capacity of some known size by the factor obtained, and subtract the result from the size of the part belonging to the machine of nominal capacity selected.

EXAMPLE.—Suppose the size of a part of a 72-in. machine is 3 in., and the corresponding part of a 42-in, machine is 1%, or 1.875 in.: then 72-42=80, and 3 in. -176 in. =1145 in. =1.125. 1.125+30=.0375= the "factor," and $.0875\times42=1.575$. Then 1.875-1.575=.3= the "increment" to be Let D = nominal capacity; then the formula will read: x =added.

 $D \times .0375 + .3$. Proof: $42 \times .0375 + .3 = 1.875$, or 1% the size of one of the selected parts. Some prefer the formula: aD + c = x, in which D = nominal capacity in inches or in pounds, c is a constant increment, a is the factor, and x = the part to be found.

KEYS.

Sizes of Keys for Mill-gearing. (Trans. A. S. M. E., xiii, 229.)—E. G. Parkhurst's rule: Width of key = $\frac{1}{16}$ diam. of shaft, depth = $\frac{1}{9}$ diam. of

shaft; taper 1/6 in. to the foot.

Custom in Michigan saw-mills: Keys of square section, side = 1/4 diam. of shaft, or as nearly as may be in even sixteenths of an inch.

J. T. Hawkins's rule: Width = ½ diam. of hole; depth of side abutment

in shaft = 1/8 diam. of hole. W. S. Huson's rule: 14-inch key for 1 to 114 in. shafts, 5/16 key for 114 to 114 in. shafts, 3/16 key for 114 to 114 in. shafts, and so on. Taper 1/2 in. to the foot. Total thickness at large end of splice, 4/5 width of key. Unwin (Elements of Machine Design) gives: Width = $\frac{1}{2}d$ + $\frac{1}{2}$ 6 in. Thieleness = $\frac{1}{2}d$ + $\frac{1}{2}$ 6 in., in which d = diam, of shaft in inches. When wheels or pulleys transmitting only a small amount of power are keyed on large shafts, he says, these dimensions are excessive. In that case, if H.P. = horsepewer transmitted by the wheel or pulley, N = revs. per min, P = force acting at the sircumference, in lbs., and R = radius of pulley in inches, take

$$d = \sqrt[3]{\frac{100 \text{ H.P.}}{N}} \text{ or } \sqrt[3]{\frac{PR}{680}}.$$

Pfof. Coleman Sellers (Stevens Indicator, April, 1882) gives the following: The size of keys, both for shafting and for machine tools, are the proportions adopted by William Sellers & Co., and rigidly adhered to during a period of nearly forty years. Their practice in making keys and fitting them is, that the keys shall always bind tight sidewise, but not top and bottom; that is, not necessarily touch either at the bottom of the key-seat litting them shaft or touch the top of the slot cut in the gear-wheel that is fastened to the shaft; but in practice keys used in this manner depend upon the fit of the wheel upon the shaft or equire screw-pressure to put the wheel in place upon the shaft.

Size of Keys for Shafting.

Diameter of Shaft, in.	Size of Key, in.
11/4 1 7/16 1 11/16	b/16× %
1 15/16 2 3/16	7/16× 14 9/16 x 44
2 7/16 2 11/16 2 15/16 3 3/16 8 7/16	11/16 × 82
3 15/16 4 7/16 4 15/16	13/16× %
6 7/16 5 15/16 6 7/16	15/16×1
6 15/16 7 7/16 7 15/16 8 7/16 8 15/1	16 1 1/18×134

Length of key-seat for coupling = 114 × nominal diameter of shaft.

Size of Keys for Machine Tools.

Diam. of Shaft, in. Size of Key, in. 8q. 15/16 and under	Diam: of Shaft, th. Size of Key in. sq. 4 to 5 7/16 13/16 15/16 15/16 15/16 15/16 11/16 9 to 10 15/16 1 3/16 11 to 12 15/16 1 3/16 11 to 12 15/16 1 5/16
24 to 2 3/16	11 to 12 15/18 1 5/16 13 to 14 15/18 1 7/10

John Richards, in an article in Cassier's Magazine, writes as follows: There are two kinds or system of keys, both proper and necessary, but which different in nature. 1. The common fastening key, usually made in width one fourth of the shaft's diameter, and the depth five eighths to one third the width. These keys are tapered and fit on all sides, or, as it is commonly described, "bear all over." They perform the double function in most cases of driving or transmitting and fastening the keyed-on member against the state of the sta movement endwise on the shaft. Such keys, when properly made, drive as a strut, diagonally from corner to corner.

2. The other kind or class of keys are not tapered and fit on their sides

only, a slight clearance being left on the back to insure against wedge action

only, a slight clearance being letted the beak would be seen or radial strain. These keys drive by shearing strain.

For fixed work where there is no sliding movement such keys are comnonly made of square section, the sides only being planed, so the depth is more than the width by so much as is gut away in finishing or fitting.

For sliding bearings, as in the ease of drilling machine spindles, the depth should be increased and in cases where there is heavy strain them; about

should be increased, and in cases where there is heavy strain there should be two keys or feathers instead of one.

The following tables are taken from proportions adopted in practical use. Flat keys, as in the first table, are employed for fixed work when the parts are to be held not only against torsional strain, but also against movethent endwise; and in case of heavy strain the strut principle being the "trongest and most secure against movement when there is strain each way, in the case of engine cranks and first movers generally. The objections to the system for general use are, straining the work out of truth, the care and expense required in fitting, and destroying the evidence of good or bad fitting of the keyed joint. When a wheel or other part is fastened with a tapering key of this kind there is no means of knowing whether the work is well fitted or net. For this reason such keys are not employed by machine-tool-makers, and in the case of accurate work of any kind, indeed, cannot be, because of the wedging strain, and also the difficulty of inspecting completed work.

I. DIMENSIONS OF FLAT KEYS, IN INCHES.

II. DIMENSIONS OF SQUARE KEYS, IN INCHES.

Diam. of shaft	1	11/4	11/6	184	2	21.6	3	81/6	4
Breadth of keys	5/82	7/32	9/32	11/32	18/32	15/32	17/82	9/16	11/16
Depth of keys	8/16	1/4	5/16	86	7/16	1/2	9/16	5/8	54

III. DIMENSIONS OF SLIDING FEATHER-KEYS, IN INCHES.

Diam. of shaft Breadth of keys Depth of keys	114 14 14 98	116 14 98	184 5/16 7/16	2 5/16 7/16	214 88 18	21/6 8/8 1/8	8 15 56	31.6 9716 34	4 9/16 94	41/6 5/8 7/8
i					l .					•

P. Pryibil furnishes the following table of dimensions to the Am. Machinist. He says: On special heavy work and very short hubs we put in two keys in one shaft 90° apart. With special long hubs, where we cannot use keys with noses, the keys should be thicker than the standard.

Diameter of Shafts, inches.		Thick- ness, in.	Diameter of Shafts, inches.		Thick- ness, in.
34 to 1 1/16 136 to 1 5/16 1 7/16 to 1 11/16 1 15/16 to 2 3/16 2 7/16 to 2 11/16 2 15/16 to 3 3/16	3/16 5/16 3/5 1/2 5/8	3/16 1/4 5/16 3/5 1/4 9/16	3 7/16 to 3 11/16 3 15/16 to 4 8/16 4 7/16 to 4 11/16 476 to 53/6 57/6 to 65/6 67/6 to 78/6	78 1 114 114 114	56 11/16 34 15/16 1 11/6

Keys longer than 10 inches, say 14 to 16'', 1/16'' thicker; keys longer than 10 inches, say 18 to 20'', $\frac{1}{2}6''$ thicker; and so on. Special short hubs to have two keys.

For description of the Woodruff system of keying, see circular of the Pratt & Whitney Co.; also Modern Mechanism, page 455.

HOLDING-POWER OF KEYS AND SET-SCREWS.

Tests of the Holding-power of Set-screws in Pulleys. (G. Lanza, Trans. A. S. M. E., x. 230.)—These tests were made by using a pulley fastened to the shaft by two set-screws with the shaft keyed to the holders; then the load required at the rim of the pulley to cause it to slip was determined, and this being multiplied by the number 6.037 (obtained by adding to the radius of the pulley one-half the diameter of the wire rope, and dividing the sum by twice the radius of the shaft, since there were two set-screws in action at a time) gives the holding-power of the set-screws. The set-screws used were of wrought-iron, 56 of an inch in diameter, and ten threads to the inch; the shaft used was of steel and rather hard, the screws making but little impression upon it. They were set up with a force of 73 lbs. at the end of a ten-inch monkey-wrench. The set-screws used were of four kinds, marked respectively A, B, C, and D. The results were as follows:

A, ends perfectly flat, 9/16-in. diameter, B, radius of rounded ends about 14 inch, C, " " " " " " " " " " " " " " " " " " "	1412 to 2294 lbs.; average 2064.
B, radius of rounded ends about 1/4 inch,	2747 " 3079 " " 2912.
C. " " " " " 12 "	1902 " 3079 " " 2573.
D ands our shared and case hardened	1089 4 9082 44 44 9420

REMARKS.—A. The set-screws were not entirely normal to the shaft: hence they bore less in the earlier trials, before they had become flattened by

B. The ends of these set-screws, after the first two trials, were found to be flattened, the flattened area having a diameter of about 1/4 inch.

C. The ends were found, after the first two trials, to be flattened, as in B. D. The first test held well because the edges were sharp, then the holdingpower fell off-till they had become flattened in a manner similar to B, when

the holding-power increased again.

Tests of the Holding-power of Keys, (Lanza.)—The load was applied as in the tests of set-screws, the shatt being firmly keyed to the holders. The load required at the rim of the pulley to shear the keys was determined, and this, multiplied by a suitable constant, determined in a similar way to that used in the case of set-screws, gives us the shearing strength per square inch of the keys.

The keys tested were of eight kinds, denoted, respectively, by the letters A. B, C, D, E, F, G and H, and the results were as follows: A, B, D and F, each 4 tests; E, 3 tests; C, G, and H, each 2 tests.

A, Norway iron, $2' \times \frac{1}{4}'' \times \frac{15}{32}''$,	40,184 to 47,760 lbs.	; average,	
B, refined iron, $2'' \times \frac{1}{4}'' \times \frac{15}{32}''$,	36,482 * 39,254;	44	38,059.
C, tool steel, $1'' \times \frac{1}{4}'' \times \frac{15}{32}''$,	91,344 & 100,056.		
D, machinery steel, $2'' \times 14'' \times 15/32''$,	64,630 to 70,186;	44	66.875.
E, Norway iron, $1\frac{1}{8}$ " \times $\frac{3}{8}$ " \times $\frac{7}{16}$ ",	36,850 * 37,222;		37,036.
F, cast-iron, $2'' \times \frac{1}{4}'' \times \frac{15}{32}''$,	30,278 " 36,944;	"	33,034.
G, cast-iron, $1\frac{1}{6}$ " $\times \frac{3}{6}$ " $\times \frac{7}{16}$ ",	37,222 & 38,700.		
H, cast-iron, $1'' \times \frac{1}{2} \times \frac{7}{16}$ ',	29,814 & 38,978.		

In A and B some crushing took place before shearing. In E, the keys being only 7/16 in. deep, tipped slightly in the key-way. In H, in the first test, there was a defect in the key-way of the pulley.

DYNAMOMETERS.

Dynamometers are instruments used for measuring power. They are of several classes, as: 1. Traction dynamometers, used for determining the power required to pull a car or other vehicle, or a plough or harrow.

2. Brake or absorption dynamometers, in which the power of a rotating shaft or wheel is absorbed or converted into heat by the friction of a brake; and. 3. Transmission dynamometers, in which the power in a rotating shaft is measured during its transmission through a belt or other connection to

another shaft, without being absorbed.

Traction Dynamometers generally contain two principal parts: (1) A spring or series of springs, through which the pull is exerted, the extension of the spring measuring the amount of the pulling force; and (2) a papercovered drum, rotated either at a uniform speed by clockwork, or at a speed covered drum, rotated either at a uniform speed by clockwork, or at a speed proportional to the speed of the traction, through gearing, on which the extension of the spring is registered by a pencil. From the average height of the diagram drawn by the pencil above the zero-line the average pulling force in pounds is obtained, and this multiplied by the distance traversed, in feet, gives the work done, in foot-pounds. The product divided by the time in minutes and by 33,000 gives the horse-power.

The Prony brake is the typical form of absorption dynamometer. (See Fig. 167, from Flather on Dynamometers and the Measurement of

Power.)

Primarily this consists of a lever connected to a revolving shaft or pulley in such a manner that the friction induced between the surfaces in contact will tend to rotate the arm in the direction in which the shaft revolves. This rotation is counterbalanced by weights P, hung in the scale pan at the end of the lever. In order to measure the power for a given number of revolutions of pulley, we add weights to the scale-pan and screw up on bolts by until the friction induced balances the weights and the lever is maintained in its horizontal position while the revolutions of shaft per minute remain constant.

For small powers the beam is generally omitted—the friction being measured by weighting a band or strap thrown over the pulley. Ropes or cords are often used for the same purpose.

Instead of hanging weights in a scale-pan, as in Fig. 167, the friction may be

weighed on a platform-scale; in this case, the direction of rotation being the same, the lever-arm will be on the opposite side of the shaft.

In a modification of this brake, the brake-wheel is keyed to the shaft, and its rim is provided with inner flanges which form an annular trough for the retention of water to keep the pulley from heating. A small stream of water constantly discharges into the trough and revolves with the pulley—tr; centrifugal force of the

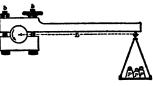


Fig. 167.

particles or water overcoming the action of gravity; a waste-pipe with its end flattened is so placed in the trough that it acts as a scoop, and removes all surplus water. The brake consists of a flexible strap to which are fitted blocks of wood forming the rubbing surface; the ends of the strap are connected by an adjustable bolt-clamp, by means of which any desired tension may be obtained.

The horse-power or work of the shaft is determined from the following:

Let W =work of shaft, equals power absorbed, per minute;

P =unbalanced pressure or weight in pounds, acting on lever-arm at distance L;

L = length of lever-arm in feet from centre of shaft;

V = velocity of a point in feet per minute at distance L, if arm were allowed to rotate at the speed of the shaft;

N = number of revolutions per minute;

H.P. = horse-power.

Then will $W = PV = 2\pi LNP$.

Since H.P. = PV + 83,000, we have H.P. = $2\pi LNP + 33,000$.

If $L = \frac{88}{2\pi}$, we obtain H.P. $= \frac{NP}{1000}$. $83 + 2\pi$ is practically 5 ft. 8 in., a value often used in practice for the length of arm.

If the rubbing-surface be too small, the resulting friction will show great irregularity—probably on account of insufficient lubrication—the jaws being allowed to seize the pulley, thus producing shocks and sudden vibra-

tions of the lever-arm. Soft woods, such as bass, plane-tree, beech, poplar, or maple are all to be preferred to the harder woods for brake-blocks. The rubbing-surface should be well lubricated with a heavy grease.

The Alden Absorption-dynamometer. (G. I. Alden, Trans. A. S. M. E., vol. xi. 958; also xii, 700 and xiii. 429.)—This dynamometer is a friction-brake, which is capable in quite moderate sizes of absorbing large powers with unusual steadiness and complete regulation. A smooth castiron disk is keyed on the rotating shaft. This is enclosed in a castiron shell, formed of two disks and a ring at their circumference, which is free to revolve on the shaft. To the interior of each of the sides of the shell is fitted a copper plate, enclosing between itself and the side a water-tight space. Water under pressure from the city pipes is admitted into each of these spaces, forcing the copper plate against the central disk. The chamber enclosing the disk is filled with oil. To the outer shell is fixed a weighted arm, which resists the tendency of the shell to rotate with the shaft, caused by the friction of the plates against the central disk. Four brakes of this type, 56 in. diam., were used in testing the experimental locomotive at Purdue University (Trans. A. S. M. E., xiii. 429). Each was designed for a maximum moment of 10,500 foot-pounds with a water-pressure of 40 lbs. per sq. in.

The area in effective contact with the copper plates on either side is represented by an annular surface having its outer radius equal to 28 inches, and its inner radius equal to 10 inches. The apparent coefficient of friction

between the plates and the disk was 31/2%.

W. W. Beaumont (Proc. Inst. C. E. 1889) has deduced a formula by means of which the relative capacity of brakes can be compared, judging from the amount of horse-power ascertained by their use.

If W = width of rubbing-surface on brake-wheel in inches; V = vel. of point on circum. of wheel in feet per minute; K = coefficient; then

K = WV + H.P.

Capacity of Friction-brakes.—Prof. Fiather obtains the values of K given in the last column of the subjoined table:

Horse-power.	R. P. M. Brake- pulley.		Diameter, fair	Length of Arm.	Design of Brake.	Value of K.
21 19 20 40 38 150 24 180 475 125 250 40	150 148.5 146 180 150 150 142 100 76.2 290 { 250 { 822 }	7 7 7 10.5 10.5 10 12 24 24 24		88" 88.88" 82.19" 82" 82" 88.81" 196.1" 191" 68"	Royal Ag. Soc., compensating	785 858 802 741 749 252 1385 209 84.7

The above calculations for eleven brakes give values of K varying from 84.7 to 1385 for actual horse-powers tested, the average being K = 655.

Instead of assuming an average coefficient, Prof. Flather proposes the

Water-cooled brake, non-compensating, K = 400; W = 400 H.P. + V.

Water-cooled brake, compensating, K = 750; W = 750 H.P. + V. Non-cooling brake, with or without compensating device, K = 900; W = 900 H.P. + V.

Transmission Dynamometers are of various forms, as the Batchelder dynamometer, in which the power is transmitted through a "train-arm" of bevel gearing, with its modifications, as the one described by the author in Trans. A. I. M. E., viii. 177, and the one described by the author in Trans. A. S. M. E., x. 514: belt dynamometers, as the Tatham; the Van Winkle dynamometer, in which the power is transmitted from a revolving shaft to another in line with it, the two almost touching, the result of the medium of colled springer featened to awms or disks beared to through the medium of coiled springs fastened to arms or disks keyed to the shafts; the Brackett and the Webb cradie dynamometers, used for measuring the power required to run dynamo-electric machines. Descriptions of the four last named are given in Flather on Dynamometers.

Much information on various forms of dynamometers will be found in Trans. A. S. M. E., vol. vii. to xv., inclusive, indexed under Dynamometers.

ice-making or refrigerating machines.

References.—An elaborate discussion of the thermodynamic theory of the action of the various fluids used in the production of cold was published by M. Ledoux in the Annales des Mines, and translated in Van Nostrand's Magu-sine in 1879. This work, revised and additions made in the light of recent ex-perience by Professors Denton, Jacobus, and Riesenberger, was reprinted in 1892. (Van Nostrand's Science Series, No. 48.) The work is largely mathe-matical, but it also contains much information of immediate practical value, from which some of the matter given below is taken. Other references are Wood's Thermodynamics, Chap. V., and numerous papers by Professors Wood, Denton, Jacobus, and Linde in Trans. A. S. M. E., vols. x. to xiv.; Johnson's Cyclopædia, article on Refrigerating-machines; also Eng'g, June 18, July 2 and 9, 1886; April 1, 1887; June 15, 1888; July 31, Aug. 23, 1889; Sept. 11 and Dec. 4, 1891; May 6 and July 8, 1892. For properties of Ammonia and Sulphur Dioxide, see papers by Professors Wood and Jacobus, Trans. A. S. M. E., vols. x. and xii.

For illustrated articles describing refrigerating-machines, see Am. Mach., May 29 and June 25, 1890, and Mfrs. Record, Oct. 7, 1892; also catalogues of builders, as Frick & Co., Waynesboro, Pa.; be La Vergne Refrigerating machine Co., New York; and others.

Operations of a Refrigerating machine.—Apparatus designed for refrigerating is based upon the following series of operations:

Compress a gas or vapor by means of some external force, then relieve it compress a gas or vapor by means of some external force, then relieve in of its heat so as to diminish its volume; next, cause this compressed gas or vapor to expand so as to produce mechanical work, and thus lower its temperature. The absorption of heat at this stage by the gas, in resuming its original condition, constitutes the refrigerating effect of the apparatus.

A refrigerating-machine is a heat-engine reversed.

From this similarity between heat-motors and freezing-machines it results that all the equations deduced from the mechanical theory of heat to determine the performance of the first, apply equally to the second.

The efficiency depends upon the difference between the extremes of tem-

The useful effect of a refrigerating-machine depends upon the ratio between the heat-units eliminated and the work expended in compressing

and expanding.
This result is independent of the nature of the body employed.
Unlike the heat-motors, the freezing-machine possesses the greatest efficiency when the range of temperature is small, and when the final temperature is elevated.

If the temperatures are the same, there is no theoretical advantage in em-ploying a gas rather than a vapor in order to produce cold. The choice of the intermediate body would be determined by practical considerations based on the physical characteristics of the body, such as the greater or less facility for manipulating it, the extreme pressures required for the best effects, etc.

Air offers the double advantage that it is everywhere obtainable, and that we can vary at will the higher pressures, independent of the temperature of the refrigerant. But to produce a given useful effect the apparatus must be of larger dimensions than that required by liquefiable vapors.

The maximum pressure is determined by the temperature of the con-

denser and the nature of the volatile liquid: this pressure is often very high. When a change of volume of a saturated vapor is made under constant pressure, the temperature remains constant. The addition or subtraction of

heat, which produces the change of volume, is represented by an increase or a diminution of the quantity of liquid mixed with the vapor.

On the other hand, when vapors, even if saturated, are no longer in contact with their liquids, and receive an addition of heat either through compression by a mechanical force, or from some external source of heat, they somport themselves nearly in the same way as permanent gases, and become superheated.

It results from this property, that refrigerating machines using a liquefi-able gas will afford results differing according to the method of working

and depending upon the state of the gas, whether it remains constantly saturated, or is superheated during a part of the cycle of working.

The temperature of the condenser is determined by local conditions. The interior will exceed by 9° to 18° the temperature of the water furnished to the exterior. This latter will vary from about 52° F., the temperature of water from considerable depth below the surface, to about 95° F., the temperature of surface-water in hot climates. The volatile liquid employed in the machine ought not at this temperature to have a tension above that

which can be readily managed by the apparatus.
On the other hand, if the tension of the gas at the minimum temperature is too low, it becomes necessary to give to the compression-cylinder large dimensions, in order that the weight of vapor compressed by a single stroke

of the piston shall be sufficient to produce a notably useful effect.

These two conditions, to which may be added others, such as those depending upon the greater or less facility of obtaining the liquid, upon the dangers incurred in its use, either from its inflammability or unhealthfulness, and finally upon its action upon the metals, limit the choice to a small number of substances.

The gases or vapors generally available are: sulphuric ether, sulphurous oxide, ammonia, methylic ether, and carbonic acid.

The following table, derived from Regnault, shows the tensions of the

vapors of these substances at different temperatures between - 22° and + 104°.

Pressures and Boiling-points of Liquids available for Use in Hefrigerating-machines.

Deg. Su phu Eth - 40 - 81 - 22 - 13 - 4 - 5 - 1, - 14 - 2, - 14 - 2, - 14	Tension of Vapor, in lbs. per sq. in., above Zero.								
81 22 13 4 5	rie Dioride	Ammonia.	Methylic Ether.	Carbonic Acid.	Pictet Fluid.				
28 2. 82 8. 41 4. 50 5. 59 6. 68 8. 77 10. 86 12. 95 14.	70	. 10.22 . 13.23 . 16.95 . 21.51 . 27.04 . 33.67 . 41.58 . 50.91 . 61.85 . 74.55 . 89.21 . 105.99 . 125.08 . 146.64 . 170.83	11, 15 13, 85 17, 06 20, 84 25, 27 83, 41 86, 34 43, 18 50, 84 59, 86 69, 35 80, 28 92, 41	251.6 292.9 340.1 393.4 453.4 520.4 676.9 786.9 971.1 1085.6 1207.9	13.5 16.2 19.3 92.9 26.9 31.2 86.2 41.7 48.1 55.6 64.1 73.2				

The table shows that the use of ether does not readily lead to the production of low temperatures, because its pressure becomes then very feeble.

Ammonia, on the contrary, is well adapted to the production of low tem-

Methylic ether yields low temperatures without attaining too great pressures at the temperature of the condenser. Sulphur dioxide readily affords temperatures of -14 to -5, while its pressure is only 3 to 4 atmospheres at the ordinary temperature of the condenser. These latter substances then lend themselves conveniently for the production of cold by means of mechanical force.

The "Pictet fluid" is a mixture of 97% sulphur dioxide and 8% carbonic acid. At atmospheric pressure it affords a temperature 14° lower than

sulphur dioxide.

Carbonic acid is as yet (1895) in use but to a limited extent, but the relaby greater compactness of compressor that it requires, and its inoffensive character, are leading to its recommendation for service on shipboard. where economy of space is important.

Certain ammonia plants are operated with a surplus of liquid present during compression, so that superheating is prevented. This practice is known

as the "cold system" of compression.

Nothing definite is known regarding the application of methylic ether or of the petroleum product chymogene in practical refrigerating service. The inflammability of the latter and the cumbrousness of the compressor

inflammability of the latter and the cumprousness of the compressor required are objections to its use.

Ice-melting Effect.?—It is agreed that the term "ice-melting effect" means the cola produced in an insulated bath of brine, on the assumption that each 142.2 B.T.U.* represents one pound of ice, this being the latent heat of fusion of ice, or the heat required to melt a pound of ice at

32° to water at the same temperature.

The performance of a machine, expressed in pounds or tons of "ice-melting capacity," does not mean that the refrigerating-machine would make the same amount of actual ice, but that the cold produced is equivalent to the effect of the melting of ice at 82° to water of the same temperature.

In making artificial ice the water frozen is generally about 70° F. when submitted to the refrigerating effect of a machine; second, the ice is chilled from 12° to 20° below its freezing point; third, there is a dissipation of cold, from the exposure of the brine tank and the manipulation of the ice-cans: therefore the weight of actual ice made, multiplied by its latent heat of fusion, 142.2 thermal units, represents only about three fourths of the cold produced in the brine by the refrigerating fluid per 1.H.P. of the engine driving the compressing pumps. Again, there is considerable fuel consumed to operate the brine-circulating pump, the condensing-water and feed-pumps, and to reboil, or purify, the condensed steam from which the ice is frezen. This fuel, together with that wasted in leakage and drip water, amounts to about one half that required to drive the main steam-engine. Hence the pounds of actual ice manufactured from distilled water is just about half the equivalent of the refrigerating effect produced in the brine per indicated horsepower of the steam-cylinders.

When ice is made directly from natural water by means of the "plate system," about half of the fuel, used with distilled water, is saved by avoiding the reboiling, and using steam expansively in a compound engine.

Ether-machines, used in India, are said to have produced about 6

lbs. of actual ice per pound of fuel consumed.

The ether machine is obsolete, because the density of the vapor of ether, at the necessary working-pressure, requires that the compressing-cylinder shall be about 6 times larger than for sulphur dioxide, and 17 times larger than for ammonia.

Air-machines require about 1.2 times greater capacity of compressing cylinder, and are, as a whole, more cumbersome than ether machines, but they remain in use on ship-board. In using air the expansion must take place in a cylinder doing work, instead of through a simple expansion-cock which is used with vapor machines. The work done in the expansion-cylinder is utilized in assisting the compressor.

Ammonia Compression-machines.—"Cold" vs. "Dry " Systems of Compression .- In the "cold" system or "humid" system some of the ammonia entering the compression-cylinder is liquid, so that the heat developed in the cylinder is absorbed by the liquid and the temperature of the ammonia thereby confined to the boiling point due to the condenser-pressure. No jacket is therefore required about the cylinder.

In the "dry" or "hot" system all ammonia entering the compressor is

gaseous, and the temperature becomes by compression several hundred degrees greater than the boiling-point due to the condenser-pressure. A water-jacket is therefore necessary to permit the cylinder to be properly lubri-

Relative Performance of Ammonia Compression- and Absorption-machines, assuming no Water to be Entrained with the Ammonia-gas in the Condenser, (Denton and Jacobus, Trans. A. S. M. E., xiii.)—It is assumed in the calculation for both machines that 1 lb. of coal imparts 10,000 B.T.U. to the boiler. The

^{*} The latent heat of fusion of ice is 144 thermal units (Phil. Mag., 1871, xli., 182); but it is customary to use 142. (Prof. Wood, Trans. A. S. M. E., xl. 834.)

condensed steam from the generator of the absorption-machine is assumed to be returned to the boiler at the temperature of the steam entering the generator. The engine of the compression-machine is assumed to exhaust through a feed-water heater that heats the feed-water to 212° F. The engine is assumed to consume 26½ lbs. of water per hour per horse-power. The figures for the compression-machine include the effect of friction, which is taken at 15% of the net work of compression.

Condenser.		Refrigerat- ing Coils.		Fe ²	Pounds of Ice-melting Effect per lb. of Coal.				or of per
	per.		per .	degrees F.	Compress. Absortant		rption- hine.*	generator s, B.T.U.	
Temp. in degrees Fahr.	Absolute pressure, 1bs. sq. in.	Temp, in degrees Eahr,	Absolute pressure, lbs.	Temp. of Absorber, deg	Using 8 lbs. of coal per hour per L.H.P.	Using 1.6 lbs. of coal per hour per I.H.P.	Absorption-machine in which the ammonia circulating-pump exhaustia into the generator.	In which the amm. circ. pemp exhausts into the atmosphere through a heater, yielding 222 temp. to the feed-water.	Heat furnished to genera absorption-machine, B.T. ib, of ammonia circulated
61.2 59.0 59.0 59.0 86.0 86.0 86.0 86.0 104.0	170.8 170.8 170.8 170.8 227.7	-22 5 -22 -22 -23 5	88.7 83.7 83.7 16.9 33.7 16.9 16.9 88.7 16.9	61.2 59.0 130.0 59.0 86.0 130.0 86.0 130.0 104.0	88.1 89.8 89.8 29.4 25.0 25.0 16.5 19.6 13.5	71.4 74.6 74.6 43.9 46.9 30.8 30.8 36.8 25.3	38.1 38.8 39.8 36.3 85.4 36.2 33.3 34.1 33.4	89.5 83.9 85.1 81.5 29.6 29.2 26.5 27.0 25.1 28.4	969 967 981 1000 988 966 1025 1002 1002 1041

The Ammonia Absorption-machine comprises a generator which contains a concentrated solution of ammonia in water; this generator is heated either directly by a fire, or indirectly by pipes leading from a steam-boiler. The condenser communicates with the upper part of the generator by a tube; it is cooled externally by a current of cold water. The cooler or brine-tank is so constructed as to utilize the cold produced; the upper part of it is in communication with the lower part of the condenser.

An absorption-chamber is filled with a weak solution of ammonia; a tube puts this chamber in communication with the cooling-tank.

The absorption chamber communicates with the boiler by two tubes; one leads from the bottom of the generator to the top of the chamber, the other leads from the bottom of the chamber to the top of the generator. Upon the latter is mounted a pump, to force the liquid from the absorption-chamber the property of the chamber the property of the liquid from the absorption chambers the property of the liquid from the absorption chambers the property of the liquid from the absorption chambers the property of the liquid from the absorption chambers the property of the liquid from the absorption chambers the property of the liquid from the absorption chambers the property of the liquid from the absorption chambers are property of the liquid from the absorption chambers are property of the liquid from the absorption chambers are property of the liquid from the liquid from the liquid from the absorption chambers are property of the liquid from the liquid ber, where the pressure is maintained at about one atmosphere, into the generator, where the pressure is from 8 to 12 atmospheres.

To work the apparatus the ammonia solution in the generator is first heated. This releases the gas from the solution, and the pressure rises. When it reaches the tension of the saturated gas at the temperature of the condenser there is a liquefaction of the gas, and also of a small amount of steam. By means of a cock the flow of the liquefled gas into the refrigerating coils contained in the cooler is regulated. It is here vaporized by absorbing the heat from the substance placed there to be cooled. As fast as it is vaporized it is absorbed by the weak solution in the absorbing-chamber.

Under the influence of the heat in the boiler the solution is unequally sat-

urated, the stronger solution being uppermost.

The weaker portion is conveyed by the pipe entering the top of the absorbing-chamber, the flow being regulated by a cock, while the pump sends an equal quantity of strong solution from the chamber back to the boiler.

^{* 5%} of water entrained in the ammonia will lower the economy of the absorption-machine about 15% to 30% below the figures given in the table.

The working of the apparatus depends upon the adjustment and regula-tion of the flow of the gas and liquid; by these means the pressure is varied, and consequently the temperature in the cooler may be controlled.

The working is similar to that of compression-machines. The absorptionchamber fills the office of aspirator, and the generator plays the part of

compressor.

The mechanical force producing exhaustion is here replaced by the affinity of water for ammonia gas; and the mechanical force required for compression is replaced by the heat which severs this affinity and sets the gas at

(For discussion of the efficiency of the absorption system, see Ledoux's work; paper by Prof. Linde, and discussion on the same by Prof. Jacobus, Trans. A. S. M. E., xiv. 1416, 1436; and papers by Denton and Jacobus, Trans. A. S. M. E. x. 792; xiii. 507.

Sulphur-Dioxide Machines.—Results of theoretical calculations

are given in a table by Ledoux showing an ice-melting capacity per hour per horse-power ranging from 134 to 63 lbs., and per pound of coal ranging from 44.7 to 21.1 lbs., as the temperature corresponding to the pressure of the vapor in the condenser rises from 59° to 104° F. The theoretical results do not represent the actual. It is necessary to take into account the loss occasioned by the pipes, the waste spaces in the cylinder, loss of time in opening of the valves, the leakage around the piston and valves, the reheating by the external air, and finally, when the ice is being made, the quantity of the ice melted in removing the blocks from their moulds. me quantity of the ice metred in removing the blocks from their motified and the motified in the state of the boiling the water, which, together with that wasted by the pumps and lost by radiation, amounts to a considerable portion of that used by the engine.

Prof. Denton says concerning Ledoux's theoretical results: The figures

given are higher than those obtained in practice, because the effect of superheating of the gas during admission to the cylinder is not considered. This superheating may cause an increase of work of about 25%. There are other losses due to superheating the gas at the brine-tank, and in the pipe leading from the brine-tank to the compressor, so that in actual practice a sulphur-dioxide machine, working under the conditions of an absolute pressure in the condenser of 56 lbs. per sq. in. and the corresponding temperature of 77° F., will give about 22 lbs. of ice-melting capacity per pound of cost, which is about 60% of the theoretical amount neglecting friction, or 70% including friction. The following tests, selected from those made by Prof. Schröter on a Pictet ice-machine having a compression-cylinder 11.3 in. bore and 24.4 in. stroke, show the relation between the theoretical and

actual ice-melting capacity.

	correspo	egrees Fahr. onding to of vapor.	Ice-melting capacity per pound of coal, assuming 3 lbs. per hour per H.P.			
No. of Test.	Condenser.	Suction.	Theoretical friction included.*	Actual.	Per cent loss due to cylinder super- heating, or differ- ence between cols. 4 and 5.	
11	77.8	28.5	41.3	88.1	19.9	
12	76.2	14.4	81.2	24.1	22.8	
18	75.2	-2.5	23.0	17.5	23.9	
14	80.6	-15.9	16.6	10.1	89.2	

The Hefrigerating Coils of a Pictet ice-machine described by Ledoux had 79 sq. ft. of surface for each 100,000 theoretic negative heat-units produced per hour. The temperature corresponding to the pressure of the dioxide in the coils is 10.4° F., and that of the bath (calcium chloride solution) in which they were immersed is 19 4°.

[•] Friction taken at figure observed in the test, which ranged from 235 to 26% of the work of the steam-cylinder.

Ammonia Compression-machines.—Ammonia gas possesses the advantage or affording about three times the useful effect of sulpling dioxide for the same volume described by the piston.

The perfection of ammonia apparatus now renders it so convenient and reliable that no practical advantage, results from the ower pressures afforded by sulphur dioxide.

PERFORMANCE OF AMMONIA COMPRESSION-MACHINES. The results of the calculations for ammonia are given in the table below:

lenser,	-tu -919 110,	Per T city, a of Te	Gals.	1290 1810 1410	
BRYGHEANDS OF ALEXAND CONFERENCE OF CONDENSE, 64.4° Fahr. Pressure in condenser, 117.44 lbs per sq. in. (Ledour.)	10	per 1bs. H.P. Th Fr	Lbs.	89.6 85.6 21.6	
	7 0 -8i4	on D	Tons.	.000244 .000221 .000115	
	ance in		Per hour per Horse- power. With Friction.		16,900 15,170 9,290
	Performance British Therm Units.		Per ftlb. of Work		.00854
	ent.	Work of Compres- sion.	With Friction, or Indicated Steam.	Ftlbs.	8130 8190 6990
	Displacen	Work of Co sion	Mithout Friction.	Ftlbs.	707 7120 6080
	Per Cubic Foot of Piston Displacemen	Per Cubic Foot of Piston	Mumber of Mega Sinu Lamai Units Veloped.	B.T.U.	88.77 88.77
			Gondenser.	B.T.U.	82.17. 88.64.
ression as			Weight of Gas C pressed.	Lbs.	. 1829 . 1206 . 0639
superheated during compression as in	pu	I 18 81	Deg. F.	158.9 170 1 241.8	
	-02	[uj (Lbs. per sq. in.	87.76 88.67 16.95	
Gas super	100	respor V Va r Coils.	Deg. F.	9.88 5.00 -22.00	

In the case of ammonia the action of the cylinder-walls in superheating the entering vapor has been determined experimentally by **For. Dento**n, and the ammonia checulated in a **For. Dento**n, and the ammonia checulated in a **For. Dento**n, and the ammonia checulated in a **For. Dento**n, and the ammonia checulated in a special meter, so that in addition to determining the effect of superheating, the latent heats can be calculated at the suction and condenser pressure. The theoretical results for ammonia are higher than the actual, for the same reasons that have been stated for sulphur dioxide.

or .12061 lb. of Ammonia Expanded through a Simple Cock to 83.67 lbs. Absolute Pressure o the Compressor at this Pressure and the Corresponding Temperature of 5º F. (LEDOUE.) Economy of Ammonia Compression-machines at Various Condenser Temperatures. Ė CO REFRIGERATING EFFCT OF 1

Per Minute per Ton of Ice-melting Ca-pacity in 24 hours. Gals. TO 16.95 LBS. ABSOLUTE PRESSURE FEMPERATURE OF - 22° F. **E884888** Condensing-water. Gals. 꽁꽝さ ing Capacity. Per Ton of Ice-melt-AND THE CORRESPONDING TEMPERATURE OF - 22° suming 30° Range of Temp. (17) 1611 1628 1628 1643 1643 28882 8882 8890 8904 8904 Gals. Per cu, ft, of Piston Displacement, as-.000218 .000215 .000201 .000206 000116 Tons. Displacement. Per cu. ft. of Piston Ice-melting Capacity. Per Pound of Coal. 28.88.48 5.4.6.4.7.9.7 With Friction. STAPLE COCK 26.9 28.7 21.1 17.1 15.5 .noit Without Frie-(13) 119.3 100.8 100.8 100.8 100.8 100.8 100.8 Per Hour ner H.P. 133 61.3 61.8 449.4 6.6 58 With Friction. 4 137.0 115.2 86.2 76.0 77.0 INTO THE COMPRESSOR AT THIS PRESSURE AND THE 281.8818 270.8818 270.88 tion. EFFECT OF 1 CU. FT. OR .06386 LBS. OF AMMONIA EXPANDED THROUGH Without Frie-B.T.U. 6.24.00 9.24.00 9.24.00 9.400 0.660 0.660 0.660 ල හැ. ද , ල ප ම දිනිසි සි ම පිනිසි සි Refrigerating Effect in Heat Units. Per Hour per H.P., including Friction. PRESSURE . 00857 .00719 .00538 .00475 .00444 .00396 .00355 .00321 Per ft.-lb. of Work Expended, includ-ing Friction. . (10) (0504 B.T.U. .00618 .00619 .00546 THIS (9) .00580 .00510 .00827 .00455 .00408 Priction. B.T.U. Expended, without Per ft. lb. of Work Y Ft.-lbs. 7,410 9,880 11,130 12,380 13,590 (8) 6,530 8,000 8,750 1,500 1,200 cated Steam-power. THE COMPRESSOR with Friction, or Indi-Compression, 10 Work Ft.-lbs 8,246 8,246 8,246 870 without Friction. of Compression, tect to Heat Expended. 264.44.8 TAKEN INTO Ratio of Refrigerating Ef-62.31 62.31 63.70 67.45 SQ. IN., AND TAKEN 88.38.39.88 80.39.39.89.98 77.49.69.98 Refrigerating Heat Units. B.T. Effect 222222 2623222 Condenser, B.T.U IN. AND Heat Carried away from 305.1 205.1 205.1 255.3 255.3 888.838.62 1.0388.838.63 1.0388.838.63 Compression, Temperature at End of REFRIGERATING PER ps.per (2) 106.0 126.1 146.6 170.8 197.8 (2) 106.0 125.1 146.6 170.8 227.8 deuser, Absolute Pressure in Con-Deg. F. Temp. Due to Press. Vapor in Condenser. 5882882 **588388**5

The following is a comparison of the theoretical ice-melting capacity of an ammonia compression machine with that obtained in some of Prof. Schröter's tests on a Linde machine having a compression-cylinder 9.9-in. bore and 16.5 in. stroke, and also in tests by Prof. Denton on a machine having two single-acting compression cylinders 12 in. × 30 in.:

No.	Temp. in Correspo	onding to	Ice-melting Capacity per lb. of Coal, assuming 3 lbs per hour per Horse-power.			
of Test.	Condenser.	Suction.	Theoretical, Friction * in- cluded.	Actual.	Per Cent of Loss Due to Cylinder Superheating.	
Schröber { 1 2 8 4 4	72.3	26.6	50.4	40.6	19.4	
	70.5	14.3	87.6	80.0	20.2	
	69.2	0.5	29.4	22.0	25.3	
	68.5	-11.8	22.8	16.1	29.4	
Denton (24) 26 (25)	84.2	15.0	27.4	24.2	11.7	
	82.7	- 8.2	21.6	17.5	19.0	
	84.6	-10.8	18.8	14.5	22.9	

Refrigerating Machines using Vapor of Water. (Ledoux.) -In these machines, sometimes called vacuum machines, water, at ordinary temperatures, is injected into, or placed in connection with, a chamber in which a strong vacuum is maintained. A portion of the water vaporizes, the heat to cause the vaporization being supplied from the water not vaporized, so that the latter is chilled or frozen to ice. If brine is used instead of pure water, its temperature may be reduced below the freezing-point of water. The water vapor is compressed from, say, a pressure of one tenth of a pound per square inch to one and one half pounds, and discharged into a condenser. It is then condensed and removed by means of an ordinary air-pump. The principle of action of such a machine is the same as that of volatile-vapor machines.

A theoretical calculation for ice-making, assuming a lower temperature of 32° F., a pressure in the condenser of 1½ lbs. per square inch, and a coal consumption of 3 lbs. per I.H.P. per hour, gives an ice-melting effect of 34.5 lbs. per pound of coal, neglecting friction. Ammonia for ice-making conditions gives 40.9 lbs. The volume of the compressing cylinder is about 150 times the theoretical volume for an ammonia machine for these conditions.

Relative Efficiency of a Refrigerating Machine.—The efficiency of a refrigerating machine is sometimes expressed as the quotient of the quantity of heat received by the ammonia from the brine, that is, the quantity of useful work done, divided by the heat equivalent of the mechanquantity of useful work done, divided by the heat equivalent of the mechanical work done in the compressor. Thus in column 1 of the table of performance of the 75-ton machine (page 998) the heat given by the brine to the ammonia per minute is 14,776 B.T.U. The horse-power of the ammonia cylinder is 65.7, and its heat equivalent = 65.7 \times 33,000 \times 778 = 2786 B.T.U. Then 14,776 \times 2786 = 5.304, efficiency. The apparent paradox that the efficiency is greater than unity, which is impossible in any machine, is thus explained The working fluid, as ammonia, receives heat from the brine and rejects heat in the condenser. If the compressor is jacketed, a partian is exacted. heat into the condenser. (If the compressor is jacketed, a portion is rejected into the jacket-water.) The heat rejected into the condenser is greater than that received from the brine; the difference (plus or minus a small difference radiated to or from the atmosphere) is heat received by the ammonia from the compressor. The work to be done by the compressor is not the mechanical equivalent of the refrigeration of the brine, but only that necessary to supply the difference between the heat rejected by the ammonia into the con-denser and that received from the brine. If cooling water colder than the brine were available, the brine might transfer its heat directly into the cooling water, and there would be no need of ammonia or of a compressor; but

^{*} Friction taken at figures observed in the tests, which range from 144 to 20% of the work of the steam-cylinder.

since such cold water is not available, the brine rejects its heat into the colder ammonia, and then the compressor is required to heat the ammonia to such a temperature that it may reject heat into the cooling water.

The efficiency of a refrigerating plant referred to the amount of fuel consumed is

The ice-melting capacity is expressed as follows:

The analogy between a heat-engine and a refrigerating-machine is as follows: A steam-engine receives heat from the boiler, converts a part of it into mechanical work in the cylinder, and throws away the difference into the condenser. The ammonia in a compression refrigerating machine receives heat from the brine-tank or cold-room, receives an additional amount of heat from the mechanical work done in the compression-cylinder, and throws away the sum into the condenser. The efficiency of the steam-engine = work done + heat received from boiler. The efficiency of the refrigerating-machine = heat received from the brine-tank or cold-room + heat required to produce the work in the compression-cylinder. In the ammonia

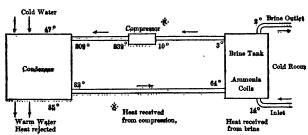


DIAGRAM OF AMMONIA COMPRESSION MACHINE.

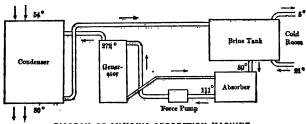


DIAGRAM OF AMMONIA ABSORPTION MACHINE.

absorption-apparatus, the ammonia receives heat from the brine-tank and additional heat from the boiler or generator, and rejects the sum into the condenser and into the cooling water supplied to the absorber. The efficiency of heat received from the brine — heat received from the boiler.

TEST-TRIALS OF REFRIGERATING-MACHINES.

(G. Linde, Trans. A. S. M. E., xiv. 1414.)

The purpose of the test is to determine the ratio of consumption and production, so that there will have to be measured both the refrigerative effect and the heat (or mechanical work) consumed, also the cooling water. The refrigerative effect is the product of the number of heat-units (Q) abstracted from the head and the method $T_0 - T$.

from the body to be cooled, and the quotient $\frac{T_0-T}{T}$; in which $T_0=$ absolute the property of T_0

lute temperature at which heat is transmitted to the cooling water, and T= absolute temperature at which heat is taken from the body to be cooled.

The determination of the quantity of cold will be possible with the proper exactness only when the machine is employed during the test to refrigerate a liquid; and if the cold be found from the quantity of liquid circulated per unit of time, from its range of refrigeration, and from its specific heat. Sufficient exactness cannot be obtained by the refrigeration of a current of circulating air, nor from the manufacture of a certain quantity of ice, nor from a calculation of the fluid circulating within the machine (for instance, the quantity of ammonia circulated by the compressor). Thus the refrigeration of brine will generally form the basis for tests making any pretension to accuracy. The degree of refrigeration should not be greater than necessary exactness; a range of temperature to be measured with the necessary exactness; a range of temperature of from 5° to 6° Fahr, will suffice.

The condenser measurements for cooling water and its temporature will

The condenser measurements for cooling water and its temperatures will be possible with sufficient accuracy only with submerged condensers. The measurement of the quantity of brine circulated, and of the cooling

The measurement of the quantity of brine circulated, and of the cooling water, is usually effected by water-meters inserted into the conduits. If encessary precautions are observed, this method is admissible. For quite precise tests, however, the use of two accurately gauged tanks must be ad

vised, which are alternately filled and emptied.

To measure the temperatures of brine and cooling water at the entrance and exit of refrigerator and condenser respectively, the employment of specially constructed and frequently standardized thermometers is indispensable; no less important is the precaution of using at each spot simultaneously two thermometers, and of changing the position of one such thermometer series from inlet to outlet (and vice versa) after the expiration of one half of the test, in order that possible errors may be compensated. It is important to determine the specific heat of the brine used in each

It is important to determine the specific heat of the brine used in each instance for its corresponding temperature range, as small differences in the composition and the concentration may cause considerable variations.

As regards the measurement of consumption, the programme will not have any special rules in cases where only the measurement of steam and cooling water is undertaken, as will be mainly the case for trials of absorption-machines. For compression-machines the steam consumption depends both on the quality of the steam-engine and on that of the refrigerating-machine, while it is evidently desirable to know the consumption of the former separately from that of the latter. As a rule steam-engine and compressor are coupled directly together, thus rendering a direct measurement of the power absorbed by the refrigerating-machine impossible, and it will have to suffice to ascertain the indicated work both of steam-engine and compressor. By further measuring the work for the engine running empty, and by comparing the differences in power between steam-engine and compressor resulting for wide variations of condenser-pressures, the effective consumption of work Le for the refrigerating-machine can be found very closely. In general, it will suffice to use the indicated work found in the steam-cylinder, especially as from this observation the expenditure of heat can be directly determined. Ordinarily the use of the indicated work in the compressor cylinder, for purposes of comparison, should be avoided; firstly because there are usually certain accessory apparatus to be driven (agitators, etc.), belonging to the refrigerating-machine proper; and secondly, because the external friction would be excluded.

Heat Balance.—We possess an important aid for checking the correctness of the results found in each trial by forming the balance in each case for the heat received and rejected. Only such tests should be regarded as correct beyond doubt which show a sufficient conformity in the heat balance. It is true that in certain instances it may not be easy to account fully for the transmission of heat between the several parts of the machine and its environment by radiation and convection, but generally

(particularly for compression-machines) it will be possible to obtain for the heat received and rejected a balance-exhibiting small discrepancies only. Report of Test.-Reports intended to be used for comparison with the figures found for other machines will therefore have to embrace at least the following observations: Refrigerator: Quantity of brine circulated per hour..... Brine temperature at inlet to refrigerator..... Brine temperature at outlet of refrigerator.....t Specific gravity of brine (at 64° Fahr.)
Specific heat of brine ABSORPTION-MACHINE. COMPRESSION-MACHINE. Still: Compressor: Steam consumed per hour..... bs. pressure of heating steam. Temperature of condensed steam at outlet ... Steam-engine: Feed-water per hour...... Absorber : Temperature of feed-water.... Quantity of cooling water per Absolute steam-pressure before hour steam-engine......
Indicated work of steam-engine Temperature at inlet Temperature at outlet..... Condensing water per hour.... Heat removed Pump for Ammonia Liquor: Indicated work of steam-engine Temperature of da..... Total sum of losses by radiation and convection... $\pm Q_2$ Steam-consumption for pump.. Thermal equivalent for work of Heat Balance: $Q_6 + AL_0 = Q_1 \pm Q_8$. pump.... ALP
Total sum of losses by radiation and convection $\dots \pm Q_3$ Heat Balance: $Qe + Q'e = Q_1 + Q_2 \pm Q_3$. For the calculation of efficiency and for comparison of various tests, the actual efficiencies must be compared with the theoretical maximum of efficiency $\left(\frac{Q}{AL}\right)$ max. = $\frac{T}{T_c - T}$ corresponding to the temperature range. Temperature Hange. — As temperatures (T and Te) at which the heat is abstracted in the refrigerator and imparted to the condenser, it is correct to select the temperature of the brine leaving the refrigerator and that of the cooling water leaving the condenser, because it is in principle impossible to keep the refrigerator pressure higher than would correspond to the lowest brine temperature, or to reduce the condenser pressure below that corresponding to the outlet temperature of the cooling water.

Prof. Linde shows that the maximum theoretical efficiency of a compression-machine may be expressed by the formula $\frac{Q}{AL} = \frac{T}{To - T},$ in which Q = quantity of heat abstracted (cold produced);AL =thermal equivalent of the mechanical work expended; L =the mechanical work, and A = 1 + 778; T = absolute temperature of heat abstraction (refrigerator); rejection (condenser).

If u = ratio between the heat equivalent of the mechanical work AL, and the quantity of heat Q' which must be imparted to the motor to produce

the work L, then

$$\frac{AL}{Q'} = u$$
, and $\frac{Q'}{Q} = \frac{To - T}{uT}$.

It follows that the expenditure of heat Q' necessary for the production of the quantity of cold Q in a compression machine will be the smaller, the smaller the difference of temperature $T_0 - T$.

Metering the Ammonia.—For a complete test of an ammonia refrigerating-machine it is advisable to measure the quantity of ammonia circulated, as was done in the test of the 75-ton machine described by Prof. Denton. (Trans. A. S. M. E., xii. 898.)

PROPERTIES OF SULPHUR DIOXIDE AND AMMONIA GAS.

Ledoux's Table for Saturated Sulphur-dioxide Gas.

Heat-units expressed in B.T.U. per pound of sulphur dioxide.

Temperature of Ebullition in deg. F.	Absolute Press- ure in lbs. per sq. in. P + 144	Total Heat reckoned from 32° F.	Heat of Liquid reckoned from & F.	Latent Heat of Evaporation	Heat Equiva- lent of Exter- nal Work.	Internal La- tent Heat.	Increase of Volume during Evaporation.	Density of Va- por or Weight of 1 cu. ft.
Deg. F.	Lbs.	B.T.U.	B.T.U.	B.T.U.	B.T.U.	B.T.U.	Cu. ft.	Lbs.
-22 -18 -4 5 14 28 82 41 50 68 77	5.56 7.28 9.27 11.76 14.74 18.31 22.53 27.48 83.25 89.98 47.61	157.43 158.64 159.84 161.03 162.20 163.36 164.51 165.65 166.78 167.90 168.99	-19.56 -16.30 -18.05 - 9.79 - 6.58 - 8.27 0.00 8.27 6.55 9.88 13.11	176.99 174.95 172.89 170.82 168.73 166.63 164.51 162.38 160.28 158.07 155.89	18.59 18.83 14.05 14.26 14.46 14.66 14.84 15.01 15.17 15.18 15.46	163.39 161.12 158.84 156.56 154.27 151.97 149.68 147.37 145.06 142.75 140,48	18.17 10.27 8.12 6.50 5.25 4.29 8.54 2.98 2.45 2.07	.076 .097 .128 .153 .190 .232 .292 .840 .40f .483
77 86	56.89 66.86	170.09 171.17	16.89 19.69	153,70 151,49	15.59 15.71	138.11 185.78	1.49 1.27	.669 ,780
95 104	77.64 90.81	172.24 173.30	22.98 26.28	149.26 147.02	15.82 15.91	188.45 181.11	i.09 91	.906 1.046

Density of Liquid Ammonia. (D'Andreff, Trans. A. S. M. E., x. 641.)

At temperature C..... - 10 F..... +14 .649250 68 .6364 .6298

These may be expressed very nearly by

 $\delta = 0.6364 - 0.0014t^{\circ}$ Centigrade; 8 = 0.6502 - 0.000777T° Fahr.

Latent Heat of Evaporation of Ammonia. (Wood, Trans. A. S. M. E., x. 641.)

 $he = 555.5 - 0.613T - 0.000219T^2$ (in B.T.U., Fahr. deg.); Ledoux found $h_0 = 583.83 - 0.5499T - 0.0001173T^2$.

For experimental values at different temperatures determined by Prof. Denton, see Trans. A. S. M. E., xii. 356. For calculated values, see vol. x. 646.

Density of Ammonia Gas.—Theoretical, 0.594; experimental, 0.596. Regnault (Trans. A. S. M. E., x. 683)

Specific Heat of Liquid Ammonia, (Wood, Trans. A. S. M. E., x. 645)—The specific heat is nearly constant at different tamperatures, and about equal to that of water, or unity. From 0° to 100° F., it is

$$c = 1.096 - .0012T$$
, nearly.

In a later paper by Prof. Wood (Trans. A. S. M. E., xij. 186) he gives a higher value, viz., c = 1.12136 + 0.000438T.

L. A. Elleau and Wm. D. Ennis (Jour. Franklin Inst., April, 1898) give the results of nine determinations, made between 0° and 20° C., which range from 0.983 to 1.086, averaging 1.0806. Von Strombeck (Jour. Franklin Inst., Dec. 1890) found the specific heat between 62° and 31° C. to be 1.2876. Ludeking and Starr (Am. Jour. Science, iii, 45, 200) obtained 0.886. Prof. Wood deduced from thermodynamic equations c=1.093 at -34° F. or -38° C., and Ledoux in like manner finds c=1.0068+.003658° C. Elleau and Ennis give Ledoux's equation with a new constant derived from their experiments, thus c=0.9854+0.003658° C.

Properties of the Saturated Vapor of Ammonia. (Wood's Thermodynamics.)

Tempe	rature.		sure, lute.	Heat of Vaporiza-	Volume of Vapor	Volume of Liquid	Weight of a cu.
Degs. F.	Abso- lute, F.	Lbs.per sq. ft.	Lbs.per sq. in.	tion, ther- mal units.	per lb., cu. ft.	per lb., cu. ft.	ft. of Vapor, lbs.
- 40	420.66	1540.7	10.69	579.67	24.872	.0234	.0410
- 85	425.66	1773.6	12.31	576.69	21.319	.0236	.0468
- 30	430.66	2035.8	14.18	573.69	18.697	.0237	.0585
- 25	435.66	2329.5	16.17	570.68	16.445	.0238	.0608
- 20	440.66	2657.5	18.45	567.67	14.507	.0240	.0689
- 15	445.66	3022.5	20.99	564.64	12.884	.0242	.0779
- 10	450.66	3428.0	28.80	561.61	11.384	.0243	.0878
– 5	455.66	8877.2	26.93	558.56	10.125	.0244	.0988
. 0	460.66	4378.5	80.87	555.50	9.027	.0246	.1108
‡ 15	465.66	4920.5	84.17	552.43	8.069	.0247	.1239
+ 10	470.66	5522.2	88.84	549.85	7.229	.0249	.1383
+ 15	475.66	6182.4	42.93	546.26	6.492	.0250	.1544
+ 20	480.66	6905.8	47.95	543.15	5.842	.0252	.1712
+ 25	485.66	7695.2	53.43	540.03	5.269	.0258 .0254	.1898
+ 80	490.66	8556.6	59.41	536.92	4.768	.0254	.2100
± 85	495.66	9498.9	65.93	583.78	4.813	.0257	.2819
1 45	500.66	10512	78.00	580.63	8.914	.0259	. 2555 . 2809
1 50	505.66 510.66	11616 12811	80.66 88.96	527.47 524.30	3.559 8.242	.0259	.2009
1 55	515.66	14102	97.93	521.12	2.958	.0263	.3381
1 60	520.66	15494	107.60	517.93	2.704	.0265	.3698
I 65	525.66	16998	118.08	514.78	2.476	.0266	.4039
I 70	580.66	18605	129.21	511.52	2.271	.0268	.4408
I 75	585.66	20336	141.25	508.29	2.087	.0270	.4793
I 80	540.66	22192	154.11	505.05	1.920	.0272	.5208
∓ 85	545.66	24178	167.86	501.81	1.770	.0273	.5650
I 🕉	550.66	26300	182.8	498.11	1.632	.0274	.6128
I 95	555.66	28565	198.37	495.29	1.510	.0277	.6623
+ 100	560.66	3098C	215.14	492.01	1.898	.0279	.7158
+ 105	565.66	38550	282.98	488.72	1.296	.0281	.7716
+ 110	570.66	36284	251.97	485.42	1.208	.0283	.8312
+ 115	575.66	39188	272.14	482.41	1.119	.0285	.8987
→ 120	580.66	42267	298.49	478.79	1.045	.0287	.9569
+ 125	585.66	45528	816.16	475.45	0.970	.0289	1.0309
- 130	590 66	48978	840.42	472.11	0.905	.0291	1.1049
- 135	595.66	52626	865.16	468.75	0.845	.0293	1.1834
+ 140	€00.66	56483	892 22	465.89	0.791	.0295	1.2642
+ 145	605.66	60550	420.49	462.01	0.741	.0297	1.3495
+ 150	610.66	64833	450.20	458.62	0.695	.0299	1.4388
+ 155	615.66	69341	481.54	455.22	0.652	.0302	1.5337
+ 160	620.66	74086	514.40	451.81	0.618	.0304	1.6843
+ 165	625.66	79071	549.04	448.89	0.577	.0306	1.7333

Specific Heat of Ammonia Vapor at the Saturation Point. (Wood, Trans. A.S. M.E., x. 644.)—For the range of temperatures ordinarily used in engineeering practice, the specific heat of saturated ammonia is negative, and the saturated vapor will condense with adiabatic expansion, and the liquid will evaporate with the compression of the vapor, and when all is vaporized will superheat.

Regnault (Rel. des. Exp., ii. 162) gives for specific heat of ammonia-groups (Wood, Trans. A. S. M. E., xii. 183.)

Properties of Brine used to absorb Hefrigerating Effect of Ammonia. (J. E. Denton, Trans, A. S. M. E., X. 199.)—A solution of Liverpool salt in well-water having a specific gravity of 1.17, or a weight per cubic foot of 73 lbs., will not sensibly thicken or congeal at 0° Fahrenheit.

The mean specific heat between 39° and 16° Fahr, was found by Denton to be 0.805. Bine of the same specific gravity has a specific heat of 0.805 at 65° Fahr, according to Naumann.

Naumann's values are as follows (Lehr- und Handbuch der Thermochemie, 1882):

Specific heat... .791 .805 * .863 .895 .931 .962 .978 Specific gravity. 1.170 1.103 1.073 1.044 1.023 1.012 *Interpolated.

Chloride-of-calcium solution has been used instead of brine. According to Naumann, a solution of 1.0255 sp. gr. has a specific heat of .957. A solution of 1.163 sp. gr. in the test reported in *Eng'g*, July 22, 1887, gave a specific heat of .827.

ACTUAL PERFORMANCES OF ICE-MAKING MACHINES.

The table given on page 996 is abridged from Denton, Jacobus, and Riesenberger's translation of Ledoux on Ice-making Machines. The following shows the class and size of the machines tested, referred to by letters in the table, with the names of the authorities:

Class of Machines.	Authority.	Dimensions of Compression-cylinder in inches.			
	,	Bore.	Stroke.		
A. Ammonia cold-compression. B. Pictet fluid dry-compression. C. Bell-Coleman air D. Closed cycle air	; Renwick &	9.9 11.3 28.0	16.5 24.4 23.8 18.0		
E. Ammonia dry-compression F. Ammonia absorption	Jacobus. Denton.	12.0	80.0		

Performance of a 75-ton Ammonia Compression-machine. (J. E. Denton, Trans. A. S. M. E., xii, 326.)—The unschine had two single-acting compression cylinders $12^{\prime\prime}\times 80^{\prime\prime}$, and one Corliss steam-cylinder, double-acting, $18^{\prime\prime}\times 86^{\prime\prime}$. It was rated by the manufacturers as a 50-ton machine, but it showed 75 tons of ice-refrigerating effect per 24 hours during the test.

The most probable figures of performance in eight trials are as follows:

of Trial.	Amm Pressu lbs. at Atmosp	ires,	Ten	rine apera- ires, rees F.	ity Tons rigerating ct per 24 rs.	per lb. of lat 3 lbs.	consump- gals. of erpermin. ton of Ca-	of Actual ights of monia cir- ted.	of Capac-
No.	Con- densing	Suc- tion.	Inlet.	Outlet.	Cape Refu Effe	Edicie Con Per gon	Water tion Wat per	Ratio We Ami	Ratio ities
1 8 7 4 6	151 161 147 159 105 135	28 27.5 13.0 8.2 7.6 15.7	86 76 86.86 14.29 6.27 6.40 4.62	28.45 2.29 2 08 -2.22	70.3 70.1 42.0 86.43 87.20 27.2	22.60 22.27 16.27 14.10 17.00 18.20	0.80 1.09 0.88 1.1 2.00 1.25	1 0 1.0 1.70 1.98 1.91 2.59	1.0 1.0 1.60 1.92 1.88 2.57

The principal results in four tests are given in the table on page 998. The fuel economy under different conditions of operation is shown in the following table;

Press.	ę́	Pounds of Ice-melting Effect with Engines—							per lb. of h Engine	
sing Press , lbs. -pressure			-con-	Non-com- pound Con- densing.		Compound Con- densing.		dents-	ısing.	ound nsing.
Condensing Jure, lbs.	Suction-p	Per lb. Coal.	Per lb. Steam.	Per lb. Coal.	Per lb. Steam.	Per lb. Coal.	Per lb. Steam.	Non-conde ing.	Condensing.	Compound Condensing
150 150 105 105	28 7 28 7	24 14 34.5 22	2.90 1.69 4.16 2.65	30 17.5 43 27.5	8.61 2.11 5.18 3.31	37.5 21.5 54 34.5	4.51 2.58 6.50 4.16	393 240 591 376	518 300 725 470	640 366 923 591

The non-condensing engine is assumed to require 25 lbs. of steam per horse-power per hour, the non-compound condensing 20 lbs., and the comdensing 16 lbs., and the boiler efficiency is assumed at 8.3 lbs. of water per lb. coal under working conditions. The following conclusions were derived

from the investigation:

1. The capacity of the machine is proportional, almost entirely, to the weight of ammonia circulated. This weight depends on the suction-pressure and the displacement of the compressor-pumps. The practical suction-pressures range from 7 lbs. above the atmosphere, with which a temperature of 0° F. can be produced, to 28 lbs. above the atmosphere, with which the temperatures of refrigeration are confined to about 28° F. At the lower pressure only about one half as much weight of ammonia can be circulated as at the upper pressure, the proportion being about in accordance with the ratios of the absolute pressures, 22 and 42 lbs, respectively. For each cubic foot of piston-displacement per minute a capacity of about on a ton of "refrigerating effect" per 24 hours can be produced at the lower pressure, and of about one third of a ton at the upper pressure. No other elements practically affect the capacity of a machine, provided the cooling-surface in the brine-tank or other space to be cooled is equal to about 86 sq. ft. per ton of capacity at 28 lbs, back pressure. For example, a difference of 100% in the rate of circulation of brine, while producing a proportional difference in the range of temperature of the latter, made no practical difference in capacity.

unerence in capacity. The brine-tank was $10\frac{1}{2} \times 13 \times 10\frac{9}{2}$ ft., and contained 8000 lineal feet of 1-in. pipe as cooling-surface. The condensing-tank was $12 \times 10 \times 10$ ft., and contained 5000 lineal feet of 1-in. pipe as cooling-surface. 2. The economy in coal-consumption depends mainly upon both the suction-pressures and condensing-pressures. Maximum economy, with a given type of engine, where water must be bought at average city prices, is obtained at 28 lbs. suction-pressure and about 150 lbs. condensing-pressure. Under these conditions, for a non-condusting steam-agrice consuming coal Under these conditions, for a non-condensing steam-engine, consuming coal at the rate of 3 lbs. per hour per I.H.P. of steam-cylinders, 24 lbs. of ice-refrigerating effect are obtained per lb. of coal consumed. For the same condensing-pressure, and with 7 lbs. suction-pressure, which affords temperatures of 0° F., the possible economy falls to about 14 lbs. of "refrigerating effect" per lb. of coal consumed. The condensing-pressure is determined by the amount of condensing water supplied to liquid the amount of condensing water supplied to liquid the amount of by the amount of condensing-water supplied to liquely the ammonia in the condenser. If the latter is about 1 gallon per minute per ton of refrigerating effect per 24 hours, a condensing-pressure of 150 lbs. results, if the initial temperature of the water is about 56° F. Twenty-five per cent less water causes the condensing-pressure to increase to 190 lbs. The work of compression is thereby increased about 20%, and the resulting "economy" is reduced to about 18 lbs. of "ice effect" per lb. of coal at 28 lbs. suction-pressure and 11.5 at 7 lbs. If, on the other hand, the supply of water is made 3 gallons per minute, the condensing pressure may be confined to about 10 lbs. per minute, the condensing pressure may be confined to about 105 lbs. The work of compression is thereby reduced about 25%, and a proportional increase of economy results. Minor alterations of economy depend on the initial temperature of the condensing-water and variations of latent heat, but these are confined within about 5% of the gross result, the main element of control being the work of compression, as affected by the back pressure and condensing-pressure, or both. If the steam-engine supplying the motion may use a condenser to secure a vacuum, an increase of economy of 25% is available over the above figures, making the lbs. of "ice effect" per lb. c

coal for 150 lbs. condensing-pressure and 28 lbs. suction-pressure 30.0, and for 7 lbs. suction-pressure, 17.5. It is, however, impracticable to use a condenser in cities where water is bought. The latter must be practically free of cost to be available for this purpose. In this case it may be assumed that water will also be available for condensing the ammonia to obtain as low a condensing-pressure as about 100 lbs., and the economy of the refrigerating-machine becomes, for 28 lbs. back pressure, 45.0 lbs. of "loe effect" per lb. of coal, or for 7 lbs. back-pressure, 27.5 lbs. of fee effect per lb. of coal. If a compound condensing-engine can be used with a steam-consumption per hour per horse-power of 16 lbs. of water, the economy of the refrigerating-machine may be 25% higher than the figures last named, making for 28 lbs. back pressure a refrigerating effect of 54.0 lbs. per lb. of coal, and for 7 lbs. back pressure a refrigerating effect of 54.0 lbs. per lb. of coal,

Actual Performance of Ice-making Machines.

Test.	Absolute Press- ure, in lbs. per aquare inch.	Temperature corresponding to Pressure, in degrees Fahr.	Temperature of Brine, in de- grees Fahr.	Revolutions per minute. Horse-power of Steam-cylinder.	Per cent of Indicated Power of Steam-cylinder lost in Friction. Ice-melting Capacity, in tons per 24 hours.	apacity in pounds f Coel. Actual.t	Difference between theoretical Ice- metting Capacity, no Cylinder Heating or Friction, and actual. Per cent.;	eat losses. Per cent of Theoretical Amount with Friction.	Mean Effective Pressure, in lbs. per square inch.
Machine. Number of	Condenser.	Condenser.	Inlet. Outlet.	Revolutions per minute. Horse-power of Steam-	Per cent of Indicated Scenn-cylinder lost Ice-melting Capacity, 24 hours.	Ice-melting Capacity in per pound of Coel.	Difference bec melting Ca Heating or Per cent.;	Heat losses. retical Amo	Mean Effective Pre per square inch.
** 2 ** 4 * 5 6 ** 6 ** 7 7 ** 8 ** 111 ** 121 ** 116 ** 117 ** 121 ** 1	135 55 131 42 128 30 126 22 200 42 136 60 131 45 126 24 137 41 130 60 7 21 56 15 55 10 60 7 91 15 61 22 59 7 54 22 89 16 62 6 62 6 62 6 62 16 167 23 167 23 167 23 167 23 162 28 176 49 176 54 177 54	72 30 71 18 68 - 9 64 18 70 31 77 28 76 14	43 37 28 23 14 9 0 5 28 28 28 28 28 28 44 37 28 28 28 0 0 6 28 44 87 28 28 28 44 87 28 28 28 0 0 6 43 37 28 28 28 28 44 87 28 28 28 28 28 28 28 28 44 87 28 28 28 6 28 28 7 28 28 28 7 28 28 28 7 28 28 28 7 28 28 28 28 7 28 28 28 28 28 28 28 28 28 28 28 28 28		10 10 10 10 10 10 10 10			19.12 29.55 19.99 28.82 20.02 58.51 19.99 28.82 20.02 58.51 19.99 28.82 20.02 58.51 19.55 56.44 19.55	54.8 58.4 58.4 77.0 56.4 46.1 52.0 24.1 20.4 16.8 25.6 25.6 25.6 25.6 25.7 26.6 26.7 27.0 26.6 27.0 27.0 28.7 29.7 29.7 29.0 29.7 29.0 29.7 29.0 29.0 29.0 29.0 29.0 29.0 29.0 29.0

^{*} Temperature of air at entrance and exit of expansion-cylinder.

⁺ On a basis of 8 lbs. of coal per hour per H.P. of steam-cylinder of compression-machine and an evaporation of 11.1 lbs. of water per pound of combustible from and at 218° F. in the absorption-machine.

[‡] Per cent of theoretical with no friction.

§ Loss due to heating during aspiration of gas in the compression-cylinder

and to radiation and superheating at brine-tank, | Actual, including resistance due to inlet and exit valves.

In class A, a German machine, the ine-melting capacity ranges from 46.29 to 16.14 lbs. of ice per pound of coal, according as the suction pressure varies from about 45 to 8 lbs. above the atmosphere, this pressure being the condition which mainly controls the economy of compression-machines. These results are equivalent to realizing from 72% to 57% of theoretically perfect performances. The higher was contact the composite to the lightern than the content of the cont fect performances. The higher per cents appear to occur with the higher suction pressures, indicating a greater loss from cylinder-heating (a pien nomenon the reverse of cylinder condensation in steam-engines), as the range of the temperature of the gas in the compression-cylinder is greater.

In B. an American compression-machine, operating on the "dry system," the percentage of theoretical effect realized ranges from 69.5% to 62.6%. The friction losses are higher for the American machine. The latter's higher efficiency may be attributed, therefore, to more perfect displacement. The largest "ice-melting capacity" in the American machine is 24.16 lbs. This corresponds to the highest suction-pressures used in American practice.

for such refrigeration as is required in beer-storage cellars using the direct-expansion system. The conditions most nearly corresponding to American brewery practice in the German tests are those in line 5, which give an "icenielting capacity " of 19.07 lbs.

For the manufacture of artificial ice, the conditions of practice are those of lines 3 and 4, and lines 25 and 26. In the former the condensing pressure used requires more expense for cooling water than is common in American practice. The ice-melting capacity is therefore greater in the German machine, being 22.08 and 16.14 lbs. against 17.55 and 14.59 for the American

apparatus.

Class B. Saiphur Dioxide or Pictet Machines.—No records are available for determination of the "ice-melting capacity" of machines using pure sulphur dioxide. This fluid is in use in American machines, but in Europe it has given way to the "Pictet fluid," a mixture of about 67% of sulphur dioxide and \$5 of carbonic acid. The presence of the carbonic acid afords a temperature about 14 Fahr. degrees lower than is obtained with pure sulphur dioxide at atmospheric pressure. The latent heat of this mixture has never been determined, but is assumed to be equal to that of pure sulphur dioxide.

For brewery refrigerating conditions, line 17, we have 26.24 lbs. "ice-melting capacity," and for ice-making conditions, line 13, the "ice-melting capacity" is 17.47 lbs. These figures are practically as economical as those for ammonia, the per cent of theoretical effect realized ranging from 65.4 to 57.8. At extremely low temperatures, —15° Fahr., lines 14 and 18, the per cent realized is as low as 42.5.

Oylinder-heating.—In compression-machines employing volatile vapors the principal cause of the difference between the theoretical and the practical result is the heating of the ammonia, by the warm cylinder walls, during its entrance into the compressor, thereby expanding it, so that to compress a pound of ammonia a greater number of revolutions must be made by the compressing-pumps than corresponds to the density of the ammonia-gas as it issues from the brine-tank.

Tosta of Ammonia Absorption-machine used in sterage-ware-houses under approaches to the New York and Brooklyn Bridge. (Eng'g, July 22, 1887.)—The circulated fluid consisted of a solution of chloride of cal-

cium of 1.163 sp. gr. Its specific heat was found to be \$27.

The efficiency of the apparatus for 24 hours was found by taking the product of the cubic feet of brine circulating through the pipes by the average difference in temperature in the ingoing and outgoing currents, as observed at frequent intervals by the specific heat of the brine (837) and its weight per cubic foot (73.48). The final product, applying all allowances for corrections from various causes, amounted to 6,218,616 heat-units as the amount abstracted in 24 hours, equal to the melting of 43,565 ibs. of ice in the same time.

The theoretical heating-power of the coal used in 24 hours was 27,000,000 heat-units; hence the efficiency of the apparatus was 23%. This is equivalent to an ice-melting effect of 16.1 lbs. per lb. of coal having a heating value of 10,000 B.T.U. per lb.

A test of a 35-ton absorption-machine in New Haven, Conn., by Prof. Denton (Trans. A. S. M. E., x. 792), gave an ice-melting effect of 20.1 lbs. per lb. of coal on a basis of boller economy equivalent to 3 lbs. of steam per L.H.P. in a good non-condensing steam-engine. The ammonia was worked between 135 and 25 lbs. pressure above the atmosphere.

Performance of a 75-ton Refrigerating-machine.

				
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	유용용	무등학생	E 5 5 8	E 8 8
	M 2 8	M S E &	FREE	7.2 g
	Maximum Capacity Economy at 28 Back Pressure.	Maximum Capacity a Economy at Zer Brine, and 8 1b Back Pressure.	Maximum Capacity a Economy for Zer Brine, 18 lbs. Ba Pressure.	Maximum Capacity Economy at 27.5 Back Pressure.
Av. high ammonia press, above atmos	151 lbs.	152 lbs.	147 lbs.	161 lbs.
Av. back ammonia press. above atmos	28 "	8.2 "	18 "	27.5 "
Av. temperature brine inlet	36.76°	6.270	14.29°	
Av. temperature brine outlet	28.86°	2.03°	2.290	28.450
Av. range of temperature	7.90	4.240	12.00°	7.91°
Lbs. of brine circulated per minute	2281	2173	943	2374
Av. temp. condensing-water at inlet	44.65°	56.65°	46.9°	54.00
Av. temp. condensing-water at outlet	83.66°	85.4°	85.46°	82.86°
Av. range of temperature	39.01°	28.75°	38.56°	28.80°
Lbs. water circulated p. min. thro' cond'ser	442	815	257	601.5
Lbs. water per min. through jackets	25	44	40	14
Range of temp-rature in jackets	24.00	16.2°	16.4°	29.1°
Lbs. ammonia circulated per min	*28.17	14.68	16.67	28.32
Probable temperature of liquid ammonia,		+40-		
entrance to brine-tank	*71.3°	*680	*63.7*	76.7°
Temp, of amm. corresp. to av. back press.	+14°	- 8°	- 5°	140
Av. temperature of gas leaving brine-tanks	34.20	14.70	3 00	29.20
Temperature of gas entering compressor.	*390	250	10.13° 239°	34° 221°
Av. temperature of gas leaving compressor	213° 200°	263° 218°	2090	1680
Av. temp. of gas entering condenser	84.5°	84.0°	82.50	88.00
Temperature due to condensing pressure	04.0	04.0	02.0	00.0
Heat given ammonia:	14776	7186	8824	14647
By brine, B T.U. per miniute By compressor, B.T.U. per minute	2786	2320	2518	3020
By atmosphere, B.T.U. per minute	140	147	167	141
Total heat rec. by amm., B.T.U. per min.	17702	9653	11409	17708
Heat taken from ammonia:	1111000	1	1	
By condenser, B.T.U. per min	17242	9056	9910	17359
By jackets, B.T.U. per min	608	712	656	406
By atmosphere, B.T.U. per min	182	338	250	252
Total heat rej. by amm., B.T U. per min	18033	10106	10816	18017
Dif. of heat rec'd and rej., B.T.U. per min.	830	458	407	309
% work of compression removed by jackets.	22%	31≴	26%	13%
Av. revolutions per min	58.09	57.7	57.88	58.89
	82.5	27.17	27.83	82.97
Mean eff. press. ammcyl., lbs. per sq. in	65.9	58.3	59.86	70.54
Av. H.P. steam-cylinder	85.00	71.7	78.6	88.63
Av. H.P. ammonia-cylinder.	65.7	54.7	59.37	71.20
Friction in per cent of steam H.P	23.0	24.0	20.0	19.67
Total cooling water, gallons per min. per				
ton per 24 hours	0.75	1.185	0.797	0.990
Tons ice-melting capacity per 24 hours Lbs. ice-refrigerating eff. per lb. coal at 3	74.8	36.43	44.64	74.56
Los ice-retrigerating eff. per 15. coal at 3		14.	100 000	
lbs. per H.P. per hour	24.1	14.1	17.27	28.37
Cost coal per ton of ice-refrigerating effect	@0 160	@ 0.000	@ 0 001	\$ 0.100
at \$4 per ton	\$0.166	\$0.283	\$0.231	\$0.170
Cost water per ton of ice-refrigerating effect	\$0.128	\$0,200	\$0.186	\$0.169
at \$1 per 1000 cu. ft	\$0.126	\$0.483	\$0.467	\$0.339
Town cope of I for or regressing en."	₩U.204	400.300	400.301	₩U.U.NB
		<u>' </u>	·	

Figures marked thus (*) are obtained by calculation; all other figures are obtained from experimental data; temperatures are in Fahrenheit degrees

Ammonia Compression-machine.

ACTUAL RESULTS OBTAINED AT THE MUNICH TESTS.
(Prof. Linde, Trans. A. S. M. E., xiv. 1419.)

No. of Test	1	8	8	4	5
Temp. of refrig- \ Inlet, deg F erated brine \ Outlet, t deg. F Specific heat of brine. Quantity of brine circ. per h., cu. ft. Cold produced, B.T.U. per hour Quant. of cooling water per h. c. ft. I.H.P. in steam-engine cylinder (Le). Cold pro- Per I.H.P. in compcyl. duced per \ Per I H.P. in steam-cyl. h. B.T.U. Per lb. of steam.	37.054 0.861 1,039.38 342,909 338.76 15.80 24,813 21.703	263,950 260.83 16.47 18,471 16,026	8.771 0.843 633.89 172,776 187.506 15.28 12,770 11,307	414.98 121,474 189.99 14.24 10,140	28.072 0.851 800.98 220,284 97.76 21.61 11,151 10,194

Means for Applying the Cold. (M. C. Bannister, Liverpool Eng g Soc'y, 1890.)—The most useful means for applying the cold to various uses is a saturated solution of brine or chloride of magnesium, which remains liquid at 5° Fahr. The brine is first cooled by being circulated in contact with the refrigerator-tubes, and then distributed through coils of pipes, arranged either in the substances requiring a reduction of temperature, or in the cold stores or rooms prepared for them; the air coming in contact with the cold tubes is immediately chilled, and the moisture in the air deposited on the pipes. It then falls, making room for warmer air, and so circulates until the whole room is at the temperature of the brine in the pipes.

pipes.

In a recent arrangement for refrigerating made by the Linde British Refrigeration Co., the cold brine is circulated through a shallow trough, in which revolve a number of shafts, each geared together, and driven by mechanical means. On the shafts are fixed a number of wrought-iron disks, partly immersed in the brine, which cool them down to the brine temperature as they revolve; over these disks a rapid circulation of air is passed by a fan, being cooled by contact with the plates; then it is led into the chambers requiring refrigeration, from which it is again drawn by the same fan; thus all moisture and impurities are removed from the chambers, and deposited in the brine, producing the most perfect antiseptic atmosphere yet invented for cold storing; while the maximum efficiency of the brine temperature was always available, the brine being periodically concentrated by suitable arrangements.

Air hus also been used as the circulating medium. The ammonia-pipes refrigerate the air in a cooling-chamber, and large wooden conduits are used to convey it to and return it from the rooms to be cooled. An advantage of this system is that by it a room may be refrigerated more quickly than by brine-coils. The returning air deposits its moisture in the form of snow on the ammonia-pipes, which is removed by mechanical brushes.

ARTIFICIAL ICE-MANUFACTURE.

Under summer conditions, with condensing water at 70°, artificial ice-machines use ammonia at about 190 lbs, above the atmosphere condenser-pressure, and 15 lbs. suction-pressure.

In a compression type of machine the useful circulation of ammonia,

In a compression type of machine the useful circulation of ammonia, allowing for the effect of cylinder-heating, is about 18 lbs. per hour per indicated horse-power of the steam cylinder. This weight of ammonia produces about 32 lbs. of ice at 15° from water at 70°. If the ice is made from distilled water, as in the "can system," the amount of the latter supplied by the boilers is about 33% greater than the weight of ice obtained. This excess represents steam exaping to the atmosphere, from the re-boiler and steam-condenser, to purify the distilled water, or free it from air; also, the loss through leaks and drips, and loss by melting of the ice in extracting it from the cans. The total steam consumed per horse-power is, therefore, about 32 \times 1.33 = 43.0 lbs. About 7.0 lbs. of this covers the steam-consum tion of the steam-engines driving the brine circulating-pumps, the sever

1000 ICE-MAKING OR REFRIGERATING MACHINES.

cold-water pumps, and leakage, drips, etc. Consequently, the main steamengine must consume 36 lbs. of steam per hour per I.H.P., or else live steam must be condensed to supply the required amount of distilled water. There is, therefore, nothing to be gained by using steam at high rates of expansion in the steam-engines, in making artificial ice from distilled water. If the cooling water for the ammonia-coils and steam-condenser is not too hard for use in the bollers, it may enter the latter at about 175° F., by restricting the quantity to 1½ gallons per minute per ton of ice. With good coal 8½ los. of feed water may then be evaporated, on the average, per lb. of coal. The ice made per pound of coal will then be 32 + (43.0 + 8.5) = 6.0 lbs.

This corresponds with the results of average practice.

If ice is manufactured by the "plate system," no distilled water is used for freezing. Hence the water evaporated by the bollers may be reduced to the amount which will drive the steam-motors, and the latter may use steam expansively to any extent consistent with the power required to compress the ammonia, operate the feed and filter pumps, and the hoisting machinery. The latter may require about 15% of the power needed for compressing the ammonia.

ammonis.

If a compound condensing steam-engine is used for driving the compressors, the steam per indicated steam horse-power, or per 32 lbs. of net ice, may be 14 lbs. per hour. The other motors at 50 lbs. of steam per horse-power will use 7.5 lbs. per hour, insking the total consumption per steam horse-power of the compressor 31.5 lbs. Taking the evaporation at 8 lbs., the feed-water temperature being limited to about 110° , the coal per horse-power is 2.7 lbs. per hour. The net ice per lb. of coal is then about $32 \rightarrow 2.7 = 11.8$ lbs. The best results with "plate-system" plants, using a compound steam-engine, have thus far afforded about 104 lbs. of ice per lb. of coal. In the "plate system" the ice gradually forms, in from 8 to 10 days, to a thickness of about 14 inches, on the hollow plates, 10×14 feet in area, in the "bate system" the water is frozen in blocks weighing about 800 lbs. each, and the freezing is completed in from 40 to 48 hours. The freezing

each, and the freezing is completed in from 40 to 48 hours. The freezing-tank area occupied by the "plate system" is, therefore, about twelve times, and the cubic contents about four times as much as required in the

"can system."
The investment for the "plate" is about one-third greater than for the "can" system. In the latter system ice is being drawn throughout the M hours, and the hoisting is done by hand tackle. Some "can" plants are equipped with pneumatic hoists and on large hoists electric tranes are used to advantage. In the "plate system" the entire daily product is drawn; cut, and stored in a few hours, the hoisting being performed by power. The distribution of cost is as follows for the two systems, taking the cost for the "can" or distilled water system as 100, which represents an actual cost of about \$1.25 per net ton;

Hoisting and storing ice		Plate System.
Engineers, firemen, and coal-passer		18.9
Coal at \$3.50 per gross ton	42.2	80.0
Water pumped directly from a natural source at 5 ets. per 1000 cubic feet	1,8	9. 6 82.7
Interest and depreciation at 10%		82.7
Repairs		3.4
	100 00	75.4

A compound condensing engine is assumed to be used by the "plate sys.

Test of the New York Hygela Ice-making Plant,— Messrs. Hupfel, Griswold, and Mackenzie; Stevens Indicator, Jan. 1894.) The final results of the tests were as follows:

Net ice made per pound of coal, in pounds. Pounds of net ice per hour per horse-power. Net ice manufactured per day (12 hours) in tons. Av. pressure of ammonia-gas at condenser, ibs. per sq. in. ab. atmos. Average back pressure of amm.gas, ibs. per sq. in. above atmos. Average temperature of brine in freezing-tanks, degrees F. Total number of cans filled per week tio of cooling-surface of coils in brine-tank to can-surface.	15.8 19.7
tio of cooling-surface of coils in brine-tank to can-surface	7 to 10

Ratio of circulating water at condensers to distilled water. 26 to Pounds of water evaporated at boilers per pound of coal. 8.1 Total horse-power developed by compressor-engines 4.1 Percentage of ice lost in removing from cans 2	0 1 085
APPROXIMATE DIVISION OF STEAM IN PER CENTS OF TOTAL AMOUNT.	
Compressor-engines	
Live steam admitted directly to condensers	.7

Compressor-engines	60.1
Live steam admitted directly to condensers	19.7
Steam for pumps, agitator, and elevator engines	7.6
Live steam for reboiling distilled water	6.5
Steam for blowers furnishing draught at boilers	5.6
Sprinklers for removing ice from cans	0.5

The precautions taken to insure the purity of the ice are thus described: The water which finally leaves the condenser is the accumulation of the exhausts from the various pumps and engines, together with an amount of live steam injected into it directly from the bollers. This last quantity used to make up any deficit in the amount of water necessary to supply the ice-cans. This water on leaving the condensers is violently repoiled, and ice-cans. This water on leaving the condensers is violently reposted, and afterwards cooled by running through a coil surface-cooler. It then passes through an oil-separator, after which it runs through three charcoal-filters and deodorizers, placed in series and containing 28 feet of charcoal. It next passes into the supply-tank in which there is an electrical attachment for detecting salt. Nitrate-of-silver tests are also made for salt daily. From this tank it is fed to the ice-cans, which are carefully covered so that the water cannot possibly receive any impurities.

MARINE ENGINEERING.

Bules for Measuring Dimensions and Obtaining Ton-nage of Vessels. (Record of American & Foreign Shipping. American Bureau of Shipping, N. Y. 1890.)—The dimensions to be measured as follows: I. Length, L.—From the fore side of stem to the after side of stern-post measured at middle line on the upper deck of all vessels, except those having a continuous hurricane-deck extending right fore and aft, in which the length is to be measured on the range of deck immediately below the hurricane-deck.

Vessels having elipper heads, raking forward, or receding stems, or raking stern-posts, the length to be the distance of the fore side of stem from aft-side of stern-post at the deep-load water-line measured at middle line. (The inner or propeller-post to be taken as stern-post in screw-steamers.

II. Breadth, R.—To be measured over the widest frame at its widest part; in other words, the moulded breadth.

III. Death D.—To be measured at the dead flat frame and at widely line.

Oakla ad bulga in tamba ta matan in assur

III. Depth, D.—To be measured at the dead-flat frame and at middle line of vessel. It shall be the distance from the top of floor-plate to the upper of vessel. It shall be the distance from the top of noor-plate to the upper deck-beam in all vessels except those having a continuous hurricane-deck, extending right fore and aft, and not intended for the American coasting trade, in which the depth is to be the distance from top of floor-plate to midway between top of hurricane deck-beam and the top of deck-beam of the deck immediately below hurricane-deck.

In vessels fitted with a continuous hurricane deck, extending right fore and aft. and intended for the American coasting trade, the depth is to be the distance from top of floor-plate to top of deck-beam of deck immediately below hurricane deck.

Bule for Obtaining Tonnage.—Multiply together the length, breadth, and depth, and their product by .75; divide the last product by 100; the quotient will be the tonnage. $\frac{L \times B \times D \times .75}{100} = \text{tonnage}.$ 100

The U. S. Custom-house Tonnage Law, May 6, 1884, provides that "the register tonnage of a vessel shall be her entire internal cubic capacity in tons of 100 cubic feet each." This measurement includes all the

capacity in tons of low cubic feet each." This measurement includes at the space between upper decks, however many there may be. Explicit directions for making the measurements are given in the law.

The Displacement of a Vessel (measured in tons of 2240 lbs.) is the weight of the volume of water which it displaces. For sea-water it is equal to the volume of the vessel beneath the water-line, in cubic feet, divided by 35, which figure is the number of cubic feet of sea-water at F

F. in a ton of 2340 lbs. For fresh water the divisor is 35.33. The U. S. register tonnage will equal the displacement when the entire internal cubic capacity bears to the displacement the ratio of 100 to 35.

The displacement or gross tonnage is sometimes approximately estimated

as follows: Let L denote the length in feet of the boat, B is extreme breadth in feet, and D the mean draught in feet; the product of these three dimensions will give the volume of a parallelopipedon in cubic feet. Putting V for this volume, we have $V = L \times B \times D$.

The volume of displacement may then be expressed as a percentage of the volume V, known as the "block coefficient." This percentage varies for different classes of ships. In racing yachts with very deep keels it varies from 22 to 33; in modern merchantmen from 55 to 75; for ordinary small boats probably 50 will give a fair estimate. The volume of displacement in cubic feet divided by 35 gives the displacement in tons.

Coefficient of Fineness.—A term used to express the relation be-tween the displacement of a ship and the volume of a rectangular prism or box whose lineal dimensions are the length, breadth, and draught of the

 $D \times 35$ Coefficient of fineness = $\frac{D \times \omega}{L \times B \times W}$; D being the displacement in tons of 35 cubic feet of sea-water to the ton, L the length between perpendiculars, B the extreme breadth of beam, and W the mean draught of water, all in feet.

Coefficient of Water-lines.—An expression of the relation of the displacement to the volume of the prism whose section equals the midship

section of the ship, and length equal to the length of the ship.

 $D \times 35$ Coefficient of water-lines = $\frac{1}{\text{area of immersed water section} \times L}$ gives the following values:

	Coefficient of Fineness.	Coefficient of Water-lines.
Finely-shaped ships	0.61	0.63 0.67
11 knots	0.65 0.70	0.72 0.76 0.83

Resistance of Ships. - The resistance of a ship passing through water may vary from a number of causes, as speed, form of body, displacement, midship dimensions, character of wetted surface, fineness of lines, etc. The resistance of the water is twofold: 1st. That due to the displacement of the water at the bow and its replacement at the stern, with the consequent formation of waves. 2d. The friction between the wetted surface of the ship and the water known as skin resistance. A common approximate formula for resistance of vessels is

Resistance = speed² × $\sqrt[3]{\text{displacement}^2}$ × a constant, or $R = S^2D^{\frac{3}{2}} \times C$.

If D = displacement in pounds, S = speed in feet per minute, R = resistance in foot-pounds per minute, $R = CS^2D^{\frac{3}{2}}$. The work done in overcoming the resistance through a distance equal to S is $R \times S = CS^*D^{\frac{1}{2}}$; and if E is the efficiency of the propeller and machinery combined, the indicated

horse-power L.H.P. = $\frac{E \times 83.000^{\circ}}{E \times 83.000^{\circ}}$

If S = speed in knots, D = displacement in tons, and C a constant which includes all the constants for form of vessel, efficiency of mechanism, etc., $I.H.P. = \frac{S^2D^{\frac{3}{2}}}{}$

The wetted surface varies as the cube root of the square of the displacement; thus, let L be the length of edge of a cube just immersed, whose displacement is D and wetted surface W. Then $D = L^p$ or $L = \sqrt[p]{D}$, and $W = 5 \times L^2 = 5 \times (\sqrt[3]{D})^2$. That is, W varies as D^2 .

Another approximate formula is

I.H.P. $=\frac{\text{area of immersed midship section} \times S^0}{K}$

The usefulness of these two formulæ depends upon the accuracy of the so-called "constants" C and K, which vary with the size and form of the ship, and probably also with the speed. Seaton gives the following, which may be taken roughly as the values of C and K under the conditions expressed:

General Description of Ship.	Speed, knots.	Value of C.	Value of K.
Ships over 400 feet long, finely shaped	15 to 17	240	620
	15 " 17	190	500
46 66 66	18 4 15	240	650
	11 4 13	260	700
Ships over 300 feet long, fairly shaped	11 " 18	240	650
	9 " 11	260	700
Ships over 250 feet long, finely shaped	18 " 15	200	580
	11 " 18	240	660
	9 " 11	260	700
Ships over 250 feet long, fairly shaped	11 " 18	220	620
	9 " 11	250	680
Ships over 200 feet long, finely shaped	11 " 12	220	600
	9 " 11	240	640
Ships over 200 feet long, fairly shaped	9 " 11	220	620
	11 " 12	200	550
" " " " " " " " " " " " " " " " " " "	10 " 11	210	580
	9 " 10	230	620
	9 " 10	200	600

Coefficient of Performance of Vessels.-The quotient

√(displacement)² × (speed in knots)³
tons of coal in 24 hours

gives a quotient of performance which represents the comparative cost of propulsion in coal expended. Sixteen vessels with three-stage expansion-engines in 1890 gave an average coefficient of 14,810, the range being from 12,180 to 16,700.

In 1881 seventeen vessels with two-stage expansion-engines gave an average coefficient of 11,710. In 1881 the length of the vessels tested ranged from 260 to 320, and in 1890 from 235 to 400. The speed in knots divided by the square root of the length in feet in 1881 averaged 0.539; and in 1890, 0.579; ranging from 0.520 to 0.641. (Proc. Inst. M E., July, 1891, p. 329.)

Defects of the Common Formula for Resistance.—Modern

Defects of the Common Formula for Resistance.—Modern experiments throw doubt upon the truth of the statement that the resistance varies as the square of the speed. (See Robt. Mansel's letters in Engineering, 1891; also his paper on The Mechanical Theory of Steamship Propulsion read before Section G of the Engineering Congress, Chicago, 1893.)

Seaton says: In small steamers the chief resistance is the skin resistance

Seaton says: In small steamers the chief resistance is the skin resistance. In very fine steamers at high speeds the amount of power required seem excessive when compared with that of ordinary steamers at ordinary speeds. In torpedo-launches at certain high speeds the resistance increases at a

lower rate than the square of the speed.

In ordinary sea-going and river steamers the reverse seems to be the case. **Hankine's Formula** for total resistance of vessels of the "waveline" type is:

$$R = ALBV^2(1 + 4\sin^2\theta + \sin^4\theta),$$

in which equation θ is the mean angle of greatest obliquity of the stream lines, A is a constant multiplier, B the mean wetted girth of the surface exposed to friction, L the length in feet, and V the speed in knots. The power demanded to impel a ship is thus the product of a constant to be determined by experiment, the area of the wetted surface, the cube of the speed, and the

quantity in the parenthesis, which is known as the "coefficient of augmentation." The last term of the coefficient may be neglected in calculating the resistance of ships as too small to be practically important. In applying the formula, the mean of the squares of the sines of the angles of maximum obliquity of the water-lines is to be taken for $\sin^2\theta$, and the rule will then read thus:

To obtain the resistance of a ship of good form, in pounds, multiply the length in feet by the mean immersed girth and by the coefficient of augmentation, and then take the product of this "augmented surface," as Rankine termed it, by the square of the speed in knots, and by the proper constant coefficient selected from the following:

For clean painted vessels, iron hulls...... A = .01For clean coppered vessels....... A = .009 to .008 For moderately rough iron vessels...... A = .011 +

The net, or effective, horse-power demanded will be quite closely obtained by multiplying the resistance calculated, as above, by the speed in knots and dividing by 326. The gross, or indicated, power is obtained by multiplying the last quantity by the reciprocal of the efficiency of the machinery and propeller, which usually should be about 0.6. Rankine uses as a divisor in his case 200 to 260.

The form of the vessel, even when designed by skilful and experienced naval architects, will often vary to such an extent as to cause the above constant coefficients to vary somewhat; and the range of variation with good forms is found to be from 0.8 to 1.5 the figures given.

For well-shaped iron vessels, an approximate formula for the horse-power required is H.P. = $\frac{SV^3}{20,000}$, in which S is the "augmented surface." The ex-

pression $\frac{SV^s}{H.P.}$ has been called by Rankine the coefficient of propulsion. In the Hudson River steamer "Mary Powell," according to Thurston, this coefficient was as high as 23,500.

The expression $\frac{D_2^8V^8}{\text{H.P.}}$ has been called the *locomotive performance*. (See Rankine's Treatise on Shipbuilding, 1864; Thurston's Manual of the Steam-

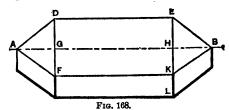
Rankine's Treatise on Shipbuilding, 1864; Thurston's Manual of the Steamengine, part ii. p. 16; also paper by F. T. Bowles, U.S.N., Proc. U.S. Naval Institute, 1883.)

Rankine's method for calculating the resistance is said by Seaton to give more accurate and reliable results than those obtained by the older rules, but it is criticised as being difficult and inconvenient of application.

Dr. Kirk's Method.—This method is generally used on the Clyde.

The general idea proposed by Dr. Kirk is to reduce all ships to so definite and simple a form that they may be easily compared; and the magnitude of certain features of this form shall determine the suitability of the ship for speed, etc.

The form consists of a middle body, which is a rectangular parallelopiped, and fore body and after body, prisms having isosceles triangles for bases, as shown in Fig. 168.



This is called a block model, and is such that its length is equal to that of the ship, the depth is equal to the mean draught, the capacity equal to the displacement volume, and its area of section equal to the area of im-

mersed midship section. The dimensions of the block model may be obtained at follows:

Let
$$AG = HB = \text{length of fore-or after-body} = F,$$
 $GH = \text{length of middle body} = M,$
 $KL = \text{mean draught} = H,$
 $KK = \frac{\text{area of immersed midship section}}{KT} = B.$

Volume of block = $(F + M) \times B \times H$; Midship section = $B \times H_1$

Displacement in tons = volume in subject. + 85.

$$AH = AG + GH = F + M = displacement \times 85 + (B \times H)_{i}$$

The wetted surface of the block is nearly equal to that of the ship of the same length, beam and draught; usually 2% to 5% greater. In exceedingly fine hollow-line ships is may be 8% greater.

> Area of bottom of block = $(F + M) \times B$; Area of sides $= 2M \times H$.

Area of sides of ends =
$$4\sqrt{F^2 + (\frac{B}{2})^2} \times H_1$$

Tangent of half angle of entrance = $\frac{1/8B}{10} = \frac{B}{0.00}$

From this, by a table of natural tangents, the angle of entrance may be obtained:

> Angle of Entrance Fore-body in of the Block Model, parts of length.

E. H. Mumford's Method of Calculating Wetted Surfaces is given in a paper by Archibald Denny, Eng'y, Sept. 21, 1894. The following is his formula, which gives closely accurate results for medium draughts, beams, and finenesses:

$$S = (L \times D \times 1.7) + (L \times B \times C),$$

in which S = wetted surface in square feet; L = length between perpendiculars in feet;

D = middle draught in feet;

B = beam in feet;

C = block coefficient.

The formula may also be expressed in the form $B \cong L(1.7D + BC)$. In the case of twin-screw ships having projecting shaft-casings, or in the case of a ship having a deep keel or blige keels, an addition must be made for such projections. The formula gives results which are in general much more accurate than those obtained by Kirk's method. It uhderestimates the surface when the beam, draught, or block coefficients are excessive; but the error is small except in the case of abnormal forms, such as stern-wheel stramers having very excessive beams (nearly one fourth the length), and also very full block coefficients. The formula gives a surface about 6% too small for such forms.

To Find the Indicated Horse-power from the Wetted Surface. (Scaton.)—In ordinary cases the horse-power per 100 feet of wetted surface may be found by assuming that the rate for a speed of 10 knots is 5, and that the quantity varies as the cube of the speed. For example: To find the number of I.H.P. necessary to drive a ship at a speed of 15 knots, having a wetted skin of block model of 16,200 square feet:

The rate per 100 feet = $(15/10)^3 \times 5 = 16,875$. Then I.H.P. required = $16.875 \times 162 = 2734$.

When the ship is exceptionally well-proportioned, the bottom quite ciean, and the efficiency of the machinery high, as low a rate as 4 I.H.P. per 100 feet of wetted skin of block model may be allowed

The gross indicated horse-power includes the power necessary to over-come the friction and other resistance of the engine itself and the shafting, and also the power lost in the propellor. In other words, I.H.P. is no measure of the resistance of the ship, and can only be relied on as a means of deciding the size of engines for speed, so long as the efficiency of the engine and propellor is known definitely, or so long as similar engines and propellers are employed in ships to be compared. The former is difficult to obtain, and it is nearly impossible in practice to know how much of the power shown in the cylinders is employed usefully in overcoming the resistance of the ship. The following example is given to show the variation in the efficiency of propellers:

	Knots.	I.	H.P.
H.M.S. "Amazon," with a 4-bladed screw, gave	12.064	with	1940
H.M.S. "Amazon," with a 2-bladed screw, increased pitch, and less revolutions per minute			
and less revolutions per minute	12.396	**	1663
H.M.S. "Iris." with a 4-bladed screw	16.577	**	7503
H.M.S. "Iris," with 2-bladed screw, increased pitch, less			

.... 18.587 revolutions per knot..... 7556 Relative Horse-power Required for Different Speeds of Vessels, (Horse-power for 10 knots = 1.)—The horse-power is taken usually to vary as the cube of the speed, but in different vessels and at different speeds it may vary from the 2.8 power to the 3.5 power, depending upor the lines of the vessel and upon the efficiency of the engines, the propeller, etc.

Speed, knots,	4	6	8	10	12	14	16	18	20	22	24	26	28	80
HP C													17.87	
82.9													19.80	
81.1													24.33	
83.2													26 97	
80.0													29.90	
	.0444													

EXAMPLE IN USE OF THE TABLE.—A certain vessel makes 14 knots speed with 587 I.H.P. and 16 knots with 900 I.H.P. What I.H.P. will be required at 18 knots, the rate of increase of horse-power with increase of speed remaining constant? The first step is to find the rate of increase, thus: 14^{α} : 16^{α} : 567: 900.

> $x \log 16 - x \log 14 = \log 900 - \log 587$; x(0.204120 - 0.146128) = 2.954243 - 2.768638

whence x (the exponent of S in formula H.P. $\propto S^2$) = 32. From the table, for $S^{3\cdot 2}$ and 16 knots, the I H.P. is 4.5 times the I.H.P. at 10 knots, \therefore H.P. at 10 knots = 900 + 4.5 = 200.

From the table, for S3.2 and 18 knots, the I.H.P. is 6.559 times the I.H.P. at 10 knots; ... H.P. at 18 knots = $200 \times 6.559 = 1812$ H P.

Resistance per Horse-power for Different Speeds. (One horse-power = 88,000 lbs. resistance overcome through 1 ft. in 1 min.)—The norse-power rorse-power for various speeds are as follows: For a speed of 1 knot, or 6080 feet per hour = $101\frac{1}{2}$ ft. per min., $33,000 + 101\frac{1}{2} = 325,658$ los. per horse-power; and for any other speed 325,658 lbs. divided by the speed in knots; or for

```
1 knot 325.66 lbs.
                       6 knots 54.28 lbs.
                                            11 knots 29.61 lbs.
                                                                   16 knots 20.85 lbs.
2 knots 162.88
                                                  ••
                                                                   17
18
                                46.52
                                            12
                                                      27.14
                                                                             19 16
                           66
                                       ..
                                                  66
                                                                        44
                                                                             18.09
         108.55
                                40.71
                                            13
                                                      25.05
                                       ..
                                                  "
                                                                        ..
                                                                                     ..
          81.41
                                86.18
                                            14
                                                      23.26
                                                                   19
                                                                             17.14
                                82.57
                                       **
         65.18
                     10
                                            15
                                                                             16.28
```

Results of Trials of Steam-vessels of Various Sizes.

(From Seaton's Marine Engineering.)

	S.S. "Torpedo."	P.S. "John Penn."	S.S. "Africa."	P.S. "Mary Powell"	S.S. "Harrar,"	R.M.P.S.
Length, perpendiculars	90' 0'' 10' 6'' 2' 6'' 29 73 24! 903	171' 9'' 18' 9'' 6' 91'6'' 280 99 3793	130' 0'' 21' 0'' 8' 10'' 370 148 3754	286' 0'' 34' 3'' 6' 0'' 800 200 8022	280' 0'' 29' 0'' 18' 6'' 1500 840 10,075	3.7' 0'' 35' 0'' 18' 0'' 1900 336 15,782
Wetted skin	45' 0"	72' 00"	42′ 6″	148′ 0′′	79' 6"	129′ 0′
Displacement × 35	12° 40′	11° 30′	23° 50′	13° 21′	17° 0′′	11° 26'
Length × Imm. mid area	0.481	0.576	0.608	0.489	0.671	0.605
Speed (knots) Indicated horse-power. (I.H P per 100 ft, wetted skin (I.H.P. per 100 ft, wetted skin, re-	22 01 460 50.9	15.8 798 21.04	10.74 871 9.88	17.20 1490 18.12	10.04 503 5.00	17.8 4751 80.00
duced to 10 knots	4.78	5.87	7.97	8.56	4.90	5.32
$\frac{D^{\frac{3}{2}} \times S^{3}}{\text{I.H.P.}}$	223	192	172.8	293.7	266	182
I.H.P.	556?	445	49 5	683	690	399
	1	į .		1		
	H.M.S.	H M.S.	H.M.S.	S.S. "Garonne."	H.M.S. "Hecla."	R.M.S.S. "Britannic."
Length, perpendiculars Breadth. extreme		図: 	300° 0° 46° 0° 18° 2° 3.90 700 18,168		392 0" 390 0" 39 0" 5767 738 26,285	Britannic."
Breadth, extreme. Mean draught water. Displacement (tons). Area Imm. mid. section. Head water water. Wetted skin. Longth, fore-body.	870' 0'' 42' 0'' 18' 10'' 8057 682 16,008	800' 0'' 46' 0'' 18' 2'' 8290 700 18,168 135' 6''	300' 0'' 46' 0'' 18' 2'' 3.90 700 18,168	870' 0" 41' 0" 18' 11" 4635 656 22,633 123' 0"	392 0" 39 0" 21' 4" 5767 738 26,235	Britannic.
Breadth, extreme. Mean draught water. Displacement (tons). Area Imm. mid. section. Wetted skin. Length, fore-body. Angle of entrance.	270' 0'' 42' 0'' 18' 10'' 8057 682 16,008	800' 0'' 46' 0'' 18' 2'' 3290 700 18,168	300' 0'' 46' 0'' 18' 2'' 3.90 700 18,168	870' 0'' 41' 0'' 18' 11'' 4685 656 22,633	392 0'' 39 0'' 21' 4'' 5767 738 26,235	32,528 900 926 926 927,73 900 928 900 900 900 900 900 900 900 900 900 90
Breadth, extreme. Mean draught water. Displacement (tons). Area Imm. mid. section. Head water water. Wetted skin. Longth, fore-body.	870' 0'' 42' 0'' 18' 10'' 8057 682 16,008	800' 0'' 46' 0'' 18' 2'' 8290 700 18,168 135' 6''	300' 0'' 46' 0'' 18' 2'' 3.90 700 18,168 185' 6'' 16° 16'	870' 0" 41' 0" 18' 11" 4635 656 22,633 123' 0"	392 0" 399 0" 5767 738 26,285 118' 0" 16° 30'	Britannic.
Breadth, extreme Mend draught water. Displacement (tons) Area Imm. mid. section Straight	270' 0" 42' 0" 18' 10' 80'57 682 16,008 101' 0' 18° 44' 0.629 14.966 4015 25.08	800' 0'' 46' 0'' 18' 2'' 8290 700 18,168 135' 6'' 16° 16' 0.548 18.573 7714 42.46	300' 0'' 46' 0'' 18' 2'' 3.90 700 18,168 135' 6'' 16° 16' 0.548 15.746 8958 21.78	870' 0'' 18' 11'' 4635 656 22,633 123' 0'' 16° 4' 0.668 13.80 2500 11.04	392 0" 39 0" 39 0" 21' 4" 5767 782 26,235 118' 0" 16° 30' 0.698 12.054 1758 6.7	50 Signary Sig
Breadth, extreme. Mean draught water. Displacement (tons) Area Imm. mid. section Wetted skin Length, fore-body Displacement × 85 Length × Imm. mid area Speed (knots) Indicated horse-power. I.H.P. per 100 ft. wetted skin, reduced to 10 knots Di × S³	270' 0'' 42' 0'' 18' 10'' 3057 65.008 101' 0' 18° 44' 0.629 14.966 4015	300' 0'' 46' 0'' 18' 2'' 3290 700 18,168 135' 6'' 16° 16' 0.548 18.573 7714	300' 0'' 18' 2'' 3.90 700 18,163 135' 6'' 16° 16' 0.548 15.746 3958	870' 0" 41' 0" 18' 11" 4685 622,633 123' 0" 16° 4' 0.668 13.80 2500	392 0" 399 0" 21' 4" 5767 738 26,285 118' 0" 0.698 12.054	50 Signary 1 Sig
Breadth, extreme. Mend draught water. Displacement (tons). Area Imm. mid. section. Wetted skin. Length, fore-body. Displacement × 85 Length × Imm. mid area. Speed (knots) Indicated horse-power. I.H.P. per 100 ft. wetted skin, reduced to 10 knots.	270' 0'' 42' 0'' 18' 10'' 8057 682 16,008 101' 0' 18° 44' 0.629 14.966 4015 25.08 7 49	300' 0'' 46' 0'' 18' 2'' 3290 700 18,168 135' 6'' 16° 16' 0.548 18.573 7714 42.46 6.634	300' 0'' 46' 0'' 18' 2'' 3.90 700 18,168 135' 6'' 16° 16' 0.548 15.746 3958 21.78	870' 0" 41' 0" 18' 11" 4685 6583 123' 0" 16° 4' 0.668 13.80 2500 11.04 4.20	392 0" 3992 0" 5767 738 26,285 118' 0" 16° 30' 0.698 12.054 1758 6.7 8.88	000 000 000 000 000 000 000 000 000 00

Results of Progressive Speed Trials in Typical Vessels. (Ena'a, April 15, 1892, p. 468.)

(Bity y	April	1 10, 1000	, p. 700	· <i>)</i>			
	Torpedo-boat.	Torpedo- gunboat, '' Sharp- shooter'' Class.	"Medusa," 8d-cl. Cruiser,	"Terpsichore," 2d-cl, Cruiser.	. "Edgar," 1st-cl. Cruiser.	"Blenhefm," 1st-cl. Cruiser.	Atlantic Passenger Steamer.
Length (in feet) Breadth " " trial. Draught (mean) on trial. Displacement (tons). L.H.P.—10 knots. " 14 " " 18 " " 20 "	135 14 5′ 1″ 108 110 960 870 1180	230 27 8' 3'' 785 450 1100 2500 8500	265 41 16' 6'' 2800 700 2100 6400 10000	3380 500 2400 6000	360 60 25' 9'' 7390 1000 2000 7500 11000	875 65 25′ 9′′ 9100 1500 4000 9000 12500	525 63 21' 8' 11560 9000 4600 10000 14500
Speed Ratio of	1 2.36 7.91 10.27	5.56	1 8 9.14 14.14	1 8 7.5 11.25	1 8 7.5	1 2.67 6. 8.42	1 2.3 5 7.25
Admiralty coeff. $\hat{C} = \frac{D^{\frac{3}{2}} \times 8^{3}}{1.\text{H.P.}}$ $\begin{cases} 10 \text{ knots.} \\ 14 & \text{or.} \\ 18 & \text{if.} \\ 90 & \text{or.} \end{cases}$	200 232 147 156	181 208 190 186	284 259 181 159	279 255 217 198	880 347 295 276	290 298 282 278	255 804 297 281

The figures for I.H.P. are "round." The "Medusa's" figures for 20 knots are from trial on Stokes Bay, and show the retarding effect of shallow water. The figures for the other ships for 20 knots are estimated for deep water.

More accurate methods than those above given for estimated to deep water. More accurate methods than those above given for estimations calculated from the results of trials of "similar" vessels driven at "corresponding" speeds; "similar" vessels being those that have the same ratio of length to breadth and to draught, and the same coefficient of fineness, and "corresponding" speeds those which are proportional to the square roots of the lengths of the respective vessels. Froude found that the resistances of such vessels varied almost exactly as wetted surface \times (speed)².

2. The method employed by the British Admiralty and by some Clyde

shipbuilders, viz., ascertaining the resistance of a model of the vessel, 12 to 20 ft. long, in a tank, and calculating the power from the results obtained.

Speed on Canals.—A great loss of speed occurs when a steam-vessel passes from open water into a more or less restricted channel. The average speed of vessels in the Suez Canal in 1882 was only 51/4 statute miles per hour.

(Eng'g. Feb. 15, 1884, p. 189.)

Estimated Displacement, Horse-power, etc.—The table on the next page, calculated by the author, will be found convenient for mak-

ing approximate estimates. The figures in 7th column are calculated by the formula H.P. $= S^3D^{\frac{3}{2}} + c$, in which c = 200 for vessels under 300 ft. long when C = .65, and 230 when C = .55; c = 200 for vessels 200 to 400 ft. long when C = .75, c = .80 when C = .75, c = .80 for vessels over 400 ft. long when C = .75, c = .80 for vessels over 400 ft. long when C = .75, 250 when C = .65, 260 when C = .55.

The figures in the 8th column are based on 5 H.P. per 100 sq. ft. of wetted surface.

The diameters of screw in the 9th column are from formula D =8.81 $\sqrt[4]{I.H.P.}$, and in the 10th column from formula D=2.71 $\sqrt[4]{I.H.P.}$

To find the diameter of screw for any other speed than 10 knots, revolutions being 100 per minute, multiply the diameter given in the table by the 5th root of the cube of the given speed + 10. For any other revolutions per minute than 100, divide by the revolutions and multiply by 100.

To find the approximate horse-power for any other speed than 10 knots, pultiply the horse-power given in the table by the cube of the matic of the matic of the speed than 10 knots, and the spe

ultiply the horse-power given in the table by the cube of the ratio of the on speed to 10, or by the relative figure from table on p. 1006.

Rstimated Displacement, Horse-power, etc., of Steamvessels of Various Sizes.

Second Color										
12	á.	Ę,m	ž0	10	ment.	Wetted Surface			Diam. of	Screw for 10 eed and 100
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16		-	<u> </u>				_			
20 4 2 .65 2.88 96 8.9 4.8 5.1 4.2 4.7 3.9 4 2 .65 2.97 120 10.3 6.0 5.8 4.3 24 3.5 1.5 .55 1.99 104 7.5 5.2 5 4.1 30 4 2 .65 3.77 168 11.5 8.4 5.5 4.5 4.5 2 .65 3.77 168 11.5 8.4 5.4 4.4 4.5 2 .65 3.77 168 11.5 8.4 5.4 4.4 4.5 2 .65 3.77 168 11.5 8.4 5.4 4.4 4.5 2 .65 5.6 6.96 224 18.2 11.2 5.9 4.8 4.6 3 .55 11.1 326 24.9 16.3 6.3 5.2 50 8 3.5 .65 11.1 326 24.9 16.3 6.3 5.2 60 10 4 .65 264 621 42.2 31.1 7.0 5.7 60 10 4 .65 44.6 861 59.4 43.1 7.5 6.1 60 12 4.5 .65 70.2 1082 88.1 54.1 8.1 6.6 60 12 4.5 .65 70.2 1082 88.1 54.1 8.1 6.6 60 13 5 .55 104.0 1408 111 70.4 8.5 70.9 60 16 6 .65 160 1854 147 79.2 77.0 7.9 6.5 60 16 6 .65 160 1854 147 79.2 77.0 7.9 6.5 60 17 6 .75 .75 .75 .75 .75 60 19 .75 .75 .75 .75 .75 .75 60 10 .75 .75 .75 .75 .75 .75 60 10 .75 .75 .75 .75 .75 .75 .75 60 .75 .75 .75 .75 .75 .75 .75 .75 .75 .75 60 .75	12	8	1.5		.85			2.4		
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	(168	26	.75	22731	58020	3489			

THE SCREW-PROPELLER.

The "pitch" of a propeller is the distance which any point in a blade, describing a helix, will travel in the direction of the axis (uring one revolution, the point being assumed to move around the axis. The pitch of a propeller with a uniform pitch is equal to the distance a propeller will advance during one revolution, provided there is no slip. In a case of this kind, the term "pitch" is analogous to the term "pitch of the thread" of an ordinary single-threaded screw.

Let $P = \text{pitch of screw in feet, } R = \text{number of revolutions per second, } V = \text{velocity of stream from the propeller} = P \times R, v = \text{velocity of the ship in feet per second, } V - v = \text{slip, } A = \text{area in square feet of section of stream from the screw, approximately the area of a circle of the same diameter, } A \times V = \text{volume of water projected astern from the ship in cubic feet per second. Taking the weight of a cubic foot of sea-water at 64 bs., and the force of gravity at 32, we have from the common formula for force of acceleration, viz.: <math>F = M \frac{v_1}{g} = \frac{W}{t} \frac{v_1}{t}$, or $F = \frac{W}{g} v_1$, when t = 1 second, v_1 being the acceleration.

the acceleration.

Thrust of screw in pounds = $\frac{64AV}{32}(V-v) = 2AV(V-v)$.

Rankine (Rules, Tables, and Data, p. 275) gives the following: To calculate the thrust of a propelling instrument (jet, paddle, or screw) in pounds, multiply together the transverse sectional area, in square feet, of the stream driven astern by the propeller; the speed of the stream relatively to the saip in knots; the real slip, or part of that speed which is impressed on that stream by the propeller, also in knots; and the constant 5.66 for sea-water, or 5.5 for fresh water. If S = speed of the screw in knots, s = speed of ship in knots, A = area of the stream in square feet (of sea-water),

Thrust in pounds =
$$A \times S(S - s) \times 5.66$$
.

The real slip is the velocity (relative to water at rest) of the water projected sternward; the apparent slip is the difference between the speed of the ship and the speed of the screw; i.e., the product of the pitch of the screw by the number of revolutions.

This apparent slip is sometimes negative, due to the working of the screw in disturbed water which has a forward velocity, following the ship. Negative apparent slip is an indication that the propeller is not suited to the

The apparent slip should generally be about 8% to 10% at full speed in wellformed vessels with moderately fine lines; in bluff cargo boats it rarely exceeds 5%.

The effective area of a screw is the sectional area of the stream of water laid hold of by the propeller, and is generally, if not always, greater than the actual area, in a ratio which in good ordinary examples is 1.2 or thereabouts, and is sometimes as high as 1.4; a fact probably due to the stiffness of the water, which communicates motion laterally amongst its particles.

(Rankine's Shipbuilding, p. 89.)

Prof. D. S. Jacobus, Trans. A. S. M. E., xi. 1028, found the ratio of the effective to the actual disk area of the screws of different vessels to be as

Size of Screw.-Seaton says: The size of a screw depends on so many things that it is very difficult to lay down any rule for guidance, and much must always be left to the experience of the designer, to allow for all the circumstances of each particular case. The following rules are given for ordinary cases. (Seaton and Rounthwaite's Pocket-book):

10183S $P = \text{pitch of propeller in feet} = \frac{101000S}{R(100 - x)}$, in which S = speed in knots, R = revolutions per minute, and x = percentage of apparent slip.For a slip of 10%, pitch = $\frac{112.68}{112.68}$

$$D$$
 = diameter of propeller = $K\sqrt{\frac{1.\text{H.P.}}{(\frac{P \times R}{100})^3}}$, K being a coefficient given

in the table below. If
$$K = 20$$
, $D = 20000 \sqrt{\frac{\text{I.H.P.}}{(P \times R)^3}}$

Total developed area of blades = $C_4 / \frac{\overline{I.H.P.}}{R}$, in which C is a coefficient

to be taken from the table.

Another formula for pitch, given in Seaton's Marine Engineering, is $\frac{C}{R}\sqrt[4]{\frac{1}{D^2}}$, in which C=737 for ordinary vessels, and 660 for slowspeed cargo vessels with full lines.

Thickness of blade at root = $\sqrt{\frac{d^3}{nb}} \times k$, in which d = diameter of tail

shaft in inches, n = number of blades, b = breadth of blade in inches where it joins the boss, measured parallel to the shaft axis; k = 4 for cast iron, 1.5

Thickness of blade at tip: Cast iron .04D + .4 in.; cast steel .08D + .4 in.; gun-metal .08D + .2 in.; high-class bronze.

Propeller Coefficients.

Description of Vessel.	Approximate Speed in knots.	Number of Screws.	Number of Blades per Screw.	Values of K.	Values of C.	Usual Material of Blades.
Bluff cargo boats	8-10	One	4	17 -17 5	19 -17.5	Cast iron
Cargo, moderate lines	10-13		4	18 -19	17 -15.5	44 44
Pass. and mail, fine lines.	13-17	**	4	19.5-20.5	15 -13	C. I. or S.
	13-17	Twin	4	20.5-21-5	14.5-12.5	" " "
" " very fine.	17-22	One	4	21 -22	12.5-11	G. M. or B
	17-22	Twin	8	22 -28	10.5- 9	
Naval vessels, " "	16-22	• •	8	21 -22.5	11.5-10.5	
	16-22	"	8	22 -23.5	8.5-7	** ** **
Torpedo-boats, " "	20-26	One	3	25	7- 6	B. or F S.

C. I., cast iron; G. M., gun-metal; B., bronze; S., steel; F. S., forged steel. From the formulæ $D=20000\sqrt{\frac{I.H.P.}{(P\times R)^3}}$ and $P=\frac{737}{R}\sqrt[4]{\frac{I.H.P.}{D^2}}$, if P=B

and R = 100, we obtain $D = \sqrt[4]{400 \times I.H.P.} = 3.31 \sqrt[4]{I.H.P.}$

If P=1.4D and R=100, then $D=\sqrt[8]{145.8\times I.H.P.}=2.71\sqrt[8]{I.H.P.}$ From these two formulæ the figures for diameter of screw in the table on page 1009 have been calculated. They may be used as rough approximations to the correct diameter of screw for any given horse-power, for a speed of

10 knots and 100 revolutions per minute.

For any other number of revolutions per minute multiply the figures in the table by 100 and divide by the given number of revolutions. For any other speed than 10 knots, since the L.H.P. varies approximately as the cube of the speed, and the diameter of the screw as the 5th root of the L.H.P., multiply the diameter given for 10 knots by the 5th root of the cube of one tenth of the given speed. Or, multiply by the following factors:

For speed of knots: 16 11 18 14 15

577 .660 .786 .807 .875 .989 1.059 1.116 1.170 1.224 1.275 1.322

Speed: 17 18 19 20 21 22 28 24 25 26 27 28
$$\sqrt[4]{(S+10)^5}$$
 = 1.875 1.423 1.470 1.515 1.561 1.605 1.648 1.691 1.783 1.774 1.815 1.855

For more accurate determinations of diameter and pitch of screw. formulæ and coefficients given by Seaton, quoted above, should be used.

Efficiency of the Propeller.—According to Rankine, if the slip of the water be s, its weight W, the resistance R, and the speed of the ship v,

$$R = \frac{Ws}{a}; \quad Rv = \frac{Wsv}{g}.$$

This impelling action must, to secure maximum efficiency of propeller, be effected by an instrument which takes hold of the fluid without shock or disturbance of the surrounding mass, and, by a steady acceleration, gives it the required final velocity of discharge. The velocity of the propeller overcoming the resistance R would then be

$$\frac{v+(v+s)}{2}=v+\frac{s}{2};$$

and the work performed would be

$$R\left(v+\frac{s}{2}\right) = \frac{Wvs}{g} + \frac{Ws^s}{2g},$$

the first of the last two terms being useful, the second the minimum lost work; the latter being the wasted energy of the water thrown backward. The efficiency is

$$E=v+\left(v+\frac{s}{2}\right);$$

and this is the limit attainable with a perfect propelling instrument, which limit is approached the more nearly as the conditions above prescribed are the more nearly fulfilled. The efficiency of the propelling instrument is probably rarely much above 0.60, and never above 0.80.

In designing the screw-propeller, as was shown by Dr. Froude, the best angle for the surface is that of 45° with the plane of the disk; but as all parts of the blade cannot be given the same angle, it should, where practicable, be so proportioned that the "pitch-angle at the centre of effort should be made 45°. The maximum rossible efficiency is then executing The maximum possible efficiency is then, according should be made 45°. to Froude, 77%.

In order that the water should be taken on without shock and discharged

with maximum backward velocity, the screw must have an axially increas-

ing pitch.

The true screw is by far the more usual form of propeller, in all steamers, both merchant and naval. (Thurston, Manual of the Steam-engine, part ii.,

p. 176.)
The combined efficiency of screw, shaft, engine, etc., is generally taken
You came the way reach 60% or 65%. Rankine takes the effective at 50%. In some cases it may reach 60% or 65%. Rankine takes the effective H.P. to equal the I.H.P. + 1.63.

Pitch-ratio and Slip for Screws of Standard Form.

Pitch-ratio.	Real Slip of Screw.	Pitch-ratio.	Real Slip of Screw
.8	15.55	1.7	21.8
1.0	16.22	1.8	21.8
	16.88	1.9	22.4
1.9	17.55 18.2	2.0 2.1	22.4 22.9 28.5
1.8	18.8	2.2	94.0
1.4	19.5	2.8	24.5
1.5	20.1	2.4	\$5.0
1.6	20.7	2.5	\$5.4

Results of Recent Researches on the efficiency of screw-propel-lers are summarized by S. W. Barnaby, in a paper read before section G of the Engineering Congress, Chicago, 1893. He states that the following gen-eral principles have been established:

(a) There is a definite amount of real slip at which, and at which only, maximum efficiency can be obtained with a screw of any given type, and this amount varies with the pitch-ratio. The slip-ratio proper to a given ratio of pitch to diameter has been discovered and tabulated for a screw of a standard type, as below (see table on page 1012):

(b) Screws of large pitch-ratio, besides being less efficient in themselves, add to the resistance of the hull by an amount bearing some proportion to their distance from it, and to the amount of rotation left in the race.

(c) The best pitch-ratio lies probably between 1.1 and 1.5.

(d) The fuller the lines of the vessel, the less the pitch-ratio should be. (e) Coarse-pitched screws should be placed further from the stern than fine-pitched ones.

(f) Apparent negative slip is a natural result of abnormal proportions of

propellers.

(g) Three blades are to be preferred for high-speed vessels, but when the diameter is unduly restricted, four or even more may be advantageously employed.

(h) An efficient form of blade is an ellipse having a minor axis equal to

four tenths the major axis.

- (i) The pitch of wide-bladed screws should increase from forward to aft, but a uniform pitch gives satisfactory results when the blades are narrow, and the amount of the pitch variation should be a function of the width of the blade.
- (j) A considerable inclination of screw shaft produces vibration, and with right-handed twin-screws turning outwards, if the shafts are inclined at all, it should be upwards and outwards from the propellers.

For results of experiments with screw-propellers, see F. C. Marshall, Proc. Inst. M. E. 1881; R. E. Froude, Trans. Institution of Naval Architects, 1886; G. A. Calvert, Trans. Institution of Naval Architects 1887; and S. W. Barnaby, Proc. Inst. Civil Eng'rs 1890, vol. cli.

One of the most important results deduced from experiments on model screws is that they appear to have practically equal efficiencies throughout a wide range both in pitch-ratio and in surface-ratio; so that great latitude is left to the designer in regard to the form of the propeller. Another important feature is that, although these experiments are not a direct guide to the selection of the most efficient propeller for a particular ship, they supply the means of analyzing the performances of screws fitted to vessels, and of thus indirectly determining what are likely to be the best dimensions of screw for a vessel of a class whose results are known. Thus a great advance has been made on the old method of trial upon the ship itself, which was the origin of almost every conceivable erroneous view respecting the screw-propeller. (Proc. Inst. M. E., July, 1891.)

THE PADDLE-WHEEL.

Paddle-wheels with Radial Floats. (Seaton's Marine En-gineering.)—The effective diameter of a radial wheel is usually taken from the centres of opposite floats; but it is difficult to say what is absolutely that diameter, as much depends on the form of float, the amount of dip, and the waves set in motion by the wheel. The slip of a radial wheel is from 15 to 30 per cent, depending on the size of float.

Area of one float =
$$\frac{\text{I.H.P.}}{D} \times C$$
.

D is the effective diameter in feet, and C is a multiplier, varying from 0.25 in tugs to 0.175 in fast-running light steamers.

The breadth of the float is usually about 14 its length, and its thickness about 16 its breadth. The number of floats varies directly with the diameter, and there should be one float for every foot of diameter.

(For a discussion of the action of the radial wheel, see Thurston, Manual

of the Steam-engine, part ii., p. 182.)

Feathering Paddle - wheels. (Seaton.)—The diameter of a feathering-wheel is found as follows: The amount of slip varies from 12 to 20 per cent, although when the floats are small or the resistance great is is as high as 25 per cent; a well-designed wheel on a well-formed ship should not exceed 15 per cent under ordinary circumstances.

If K is the speed of the ship in knots, S the percentage of slip, and R the revolutions per minute.

Diameter of wheel at centres =
$$\frac{K(100 + S)}{3.14 \times R}$$
.

The diameter, however, must be such as will suit the structure of the ship, so that a modification may be necessary on this account, and the revolutions altered to suit it.

The diameter will also depend on the amount of "dip" or immersion of

When a ship is working always in smooth water the immersion of the top edge should not exceed 1/4 the breadth of the float; and for general service at sea an immersion of 1/4 the breadth of the float is sufficient. If the ship is intended to carry cargo, the immersion when light need not be more than 2 or 3 inches, and should not be more than the breadth of float when at the deepest draught; indeed, the efficiency of the wheel falls off rapidly with the immersion of the wheel.

Area of one float =
$$\frac{\text{I.H.P.}}{D} \times C$$
.

C is a multiplier, varying from 0.3 to 0.35; D is the diameter of the wheel to the float centres, in feet.

The number of floats $= \frac{1}{2}(D+2)$. The breadth of the float $= 0.35 \times$ the length. The thickness of floats = 1/12 the breadth.

Diameter of gudgeons = 1/12 the breadth.

Diameter of gudgeons the beautiful float. Seaton and Rounthwaite's Pocket-book gives:

Number of floats =
$$\frac{60}{\sqrt{R}}$$
,

where R is number of revolutions per minute.

Area of one float (in square feet) =
$$\frac{\text{I.H.P.} \times 33000 \times K}{N \times (D \times R)^2},$$

where N = number of floats in one wheel.

For vessels plying always in smooth water K=1200. For sea-going steamers K=1400. For tugs and such craft as require to stop and start frequently in a tide-way K=1600.

It will be quite accurate enough if the last four figures of the cube

 $(D \times R)^3$ be taken as ciphers. For illustrated description of the feathering paddle-wheel see Seaton's Marine Engineering, or Seaton and Rounthwaite's Pocket-book. The diameter of a feathering wheel is about one half that of a radial wheel for equal efficiency. (Thurston)

Efficiency of Paddle-wheels.—Computations by Prof. Thurston of the efficiency of propulsion by paddle-wheels give for light river steamers with ratio of velocity of the vessel, v, to velocity of the paddle-float at centre of pressure, V, or $\frac{v}{V}$, = $\frac{3}{4}$, with a dip = 3/20 radius of the wheel, and a slip of 25 per cent, an efficiency of .714; and for ocean steamers with the same slip and ratio of $\frac{v}{V}$, and a dip = $\frac{1}{2}$ radius, an efficiency of .685.

JET-PROPULSION.

Numerous experiments have been made in driving a vessel by the reaction of a jet of water pumped through an orifice in the stern, but they have all resulted in commercial failure. Two jet-propulsion steamers, the "Waterwitch," 1100 tons, and the "Squirt," a small torpedo-boat, were built by the British Government. The former was tried in 1857, and gave an efficiency of apparatus of only 18 per cent. The latter gave a speed of 12 knots, as against 17 knots attained by a sister-ship having a screw and equal steam-power. The mathematical theory of the efficiency of the jet was discussed by Raukine in The Engineer, Jan. 11, 1867, and he showed that the greater the greater the greater of the stream of the greater of the stream of the greater of the stream of the greater of the gre the greater the quantity of water operated on by a jet-propeller, the greater

is the efficiency. In defiance both of the theory and of the results of earlier experiments, and also of the opinions of many naval engineers, more than \$200,000 were spent in 1888-90 in New York upon two experimental boats, the "Prima Vista" and the "Evolution," in which the jet was made of very small size, in the latter case only \$\frac{2}{3}\-\text{inch}\$ in the latter case only \$\frac{2}{3}\-\text{inch}\$ in diameter, and with a pressure of 2500 lbs, per square luch. As had been predicted, the vessel was a total failure (See article by the author in Mechanics, March, 1891.)

The theory of the jet-propeller is similar to that of the screw-propeller, it has the area of the jet in square feet. Vita velocity with reference to the

If A = the area of the jet in square feet, V its velocity with reference to the The arms are the per in square reet, ν its velocity with reference to the orifice, in feet per second, ν = the velocity of the ship in reference to the earth, then the thrust of the jet (see Screw-propeller, arte) is 2AV(V-v). The work done on the vessel is 2AV(V-v)v, and the work wasted on the rearward projection of the jet is $\frac{1}{2} \times \frac{2AV(V-v)^2}{2}$. The efficiency is $\frac{2AV(V-v)v}{2} = \frac{2v}{2}$. This averages of a constant to the period of th

 $\frac{2AV(V-v)v+AV(V-v)^2}{V-v} = \frac{AV}{V+v}.$ This expression equals unity when

 $2AV(V-vv)+AV(V-v)^3$ V+v V=v, that is, when the velocity of the jet with reference to the earth, or V-v, = 0; but then the thrust of the propeller is also 0. The greater the value of V as compared with v, the less the efficiency. For V=20v, as was proposed in the "Evolution," the efficiency of the jet would be less than 10 per cent, and this would be further reduced by the friction of the pumping

mechanism and of the water in pipes.

The whole theory of propulsion may be summed up in Rankine's words:

'That propeller is the best, other things being equal, which drives astern the largest body of water at the lowest velocity.'

It is practically impossible to devise any system of hydraulic or jet propulations.

sion which can compare favorably, under these conditions, with the screw

or the paddle-wheel.

Reaction of a Jet.—If a jet of water issues horizontally from a vessel, the reaction on the side of the vessel opposite the orifice is equal to the weight of a column of water the section of which is the area of the orifice, and the height is twice the head.

The propelling force in jet-propulsion is the reaction of the stream issuing from the orifice, and it is the same whether the jet is discharged under water, in the open air, or against a solid wall. For proof, see account of trials by C. J. Everett, Jr., given by Prof. J. Burkitt Webb, Trans. A. S. M. E., xii. 904.

RECENT PRACTICE IN MARINE ENGINES.

(From a paper by A. Riechynden on Marine Engineering during the past Decade, Proc. Inst. M. E., July, 1891.)

Since 1881 the three-stage-expansion engine has become the rule, and the boiler-pressure has been increased to 160 lbs. and even as high as 200 lbs.per square inch. Four-stage-expansion engines of various forms have also been adopted.

Forced Draught has become the rule in all vessels for naval service, and is comparatively common in both passenger and cargo vessels. By this means it is possible considerably to augment the power obtained from a given botler; and so long as it is kept within certain limits it need result in no injury to the boiler, but when pushed too far the increase is sometimes

purchased at considerable cost

In regard to the economy of forced draught, an examination of the appended table (page 1018) will show that while the mean consumption of coal in those steamers working under natural draught is 1.578 lbs. per indicated horse-power per hour, it is only 1.336 lbs. in those fitted with forced draught. This is equivalent to an economy of 15%. Part of this economy, however, may be due to the other heat-saving appliances with which the latter steamers are fitted.

Boilers.—As a material for boilers, iron is now a thing of the past, though it seems probable that it will continue yet awhile to be the material for tubes. Steel plates can be procured at 132 square feet superficial area and 134 inches thick. For purely boiler work a punching-machine has become obsolete in marine-engine work.

The increased pressures of steam have also caused attention to be directed

to the furnace, and have led to the adoption of various artifices in the shape of corrugated, ribbed, and spiral flues, with the object of giving increased strength against collapse without abnormally increasing the thickness of the plate. A thick furnace-plate is viewed by many engineers with great

suspicion; and the advisers of the Board of Trade have fixed the limit of thickness for furnace-plates at % inch; but whether this limitation will stand in the light of prolonged experience remains to be seen. It is a fact generally accepted that the conditions of the surfaces of a plate are far greater factors in its resistance to the transmission of heat than either the material or the thickness. With a plate free from lamination, thickness being a mere secondary element, it would appear that a furnace-plate might be increased from 14 inch to 34 inch thickness without increasing its resistance more than 142. So convinced have some engineers become of the soundness of this view that they have adopted flues 34 inch thick.

Pisten-valves.—Since higher steam pressures have become common,

piston-valves have become the rule for the high-pressure cylinder, and are not unusual for the intermediate. When well designed they have the great advantage of being almost free from friction, so far as the valve itself is concerned. In the earlier piston-valves it was customary to fit spring rings, which were a frequent source of trouble and absorbed a large amount of source is followed. of power in friction; but in recent practice it has become usual to fit spring-

less adjustable sleeves

For low-pressure cylinders piston-valves are not in favor; if fitted with spring rings their friction is about as great as and occasionally greater than that of a well-balanced slide-valve; while if fitted with springless rings there is always some leakage, which is irrecoverable. But the large port-clearances inseparable from the use of piston-valves are most objectionable; and with triple engines this is especially so, because with the customary late cut-off it becomes difficult to compress sufficiently for insuring economy and smoothness of working when in "full gear," without some special device.

Steam-pipes, .- The failures of copper steam-pipes on large vessels have drawn serious attention both to the material and the modes of con-struction of the pipes. As the brazed joint is liable to be imperfect, it is proposed to substitute solid drawn tubes, but as these are not made of large sizes two or more tubes may be needed to take the place of one brazed tube. Reinforcing the ordinary brazed tubes by serving them with steel or copper wire, or by hooping them at intervals with steel or iron bands, has been tried and found to answer perfectly.

Auxiliary Supply of Fresh Water-Evaporators.—To make up the losses of water due to escape of steam from safety-valves, leakage at glands, joints, etc., either a reserve supply of fresh water is carried in tanks, or the supplementary feed is distilled from sea-water by special apparatus provided for the purpose. In practice the distillation is effected by passing steam, say from the first receiver, through a nest of tubes inside a still or evaporator, of which the steam-space is connected either with the second receiver or with the condenser. The temperature of the steam inside the tubes being higher than that of the steam either in the second receiver or in the condenser, the result is that the water inside the still is evaporated, and passes with the rest of the steam into the condenser, where it is condensed and serves to make up the loss. This plan localizes the trouble of the deposit, and frees it from its dangerous character, because an evaporator cannot become overheated like a boiler, even though it be neglected until salts up solid; and if the same precautions are taken in working the evaporator which used to be adopted with low-pressure boilers when they were

fed with salt water, no serious trouble should result.

Weir's Feed-water Heater.—The principle of a method of heating feed-water introduced by Mr. James Weir and widely adopted in the marine service is founded on the fact that, if the feed-water as it is drawn from the hot-well be raised in temperature by the heat of a portion of steam introduced into it from one of the steam-receivers, the decrease of the coal necessary to generate steam from the water of the higher temperature bears a greater ratio to the coal required without feed-heating than the power which would be developed in the cylinder by that portion of steam would bear to the whole power developed when passing all the steam through all the cylinders. Suppose a triple-expansion engine were working under the following conditions without feed-heating: boiler-pressure 150 lbs.; I.H.P. in high-pressure cylinder 398, in intermediate and low-pressure cylinders to gether 790, total 1188. The temperature of hot-well 100° F. Then with feed-heating the same engine might work as follows: the feed might be heated to 220° F., and the percentage of steam from the first receiver required to heat it would be 10.95; the I.H.P. in the h.p. cylinder would be as before 398, and in the three cylinders it would be 1103, or 98% of the power developed without

feed-heating. Meanwhile the heat to be added to each pound of the feed-water at 220° F. for converting it into steam would be 1005 units against 1125 units with feed at 100° F., equivalent to an expenditure of only 99.4% of the heat required without feed-heating. Hence the expenditure of heat in relation to power would be 89.4 + 93.0 = 96.4%, equivalent to a heat economy of 3.6%. If the steam for heating can be taken from the low-pressure receiver, the economy is about doubled.

Passenger Steamers fitted with Twin Screws.

Vessels.	th be- in Per- liculars.		Cylinders, tw in all.	o sets	9.i.	ated e-power	
	Length tween pendic	Beam.	Diameters.	Stro.	Boiler- press per so	Indicated Horse-po	
	Feet	Feet	Inches	In.	Lbs.	I.H.P.	
City of New York Paris	525	681/4	45, 71, 113	60	150	20,000	
Majestic (565	58	48, 68, 110	60	180	18,000	
Normannia	500 4681⁄2	5714 5514	40, 67, 106 41, 66, 101	66 66	160 160	11,500 12,500	
" "Japan	440	51	82, 51, 82	54	160	10,125	
Orel	415 460	48 541⁄6	34, 54, 85 341, 571, 92	51 60	160 170	10,000 11,656	

Comparative Results of Working of Marine Engines, 1872, 1881, and 1891.

Boilers, Engines, and Coal.	1872.	1881.	1891.
Boiler-pressure, lbs. per sq. in Heating-surface per horse-power, sq. ft Revolutions per minute, revs Piston-speed, feet per min Coal per horse-power per hour, lbs	4.410 55.67 876	77.4 3.917 59.76 467 1.828	158.5 8.275 68.75 529 1 522

Weight of Three-stage - expansion Engines in Nine Steamers in Relation to Indicated Horse-power and to Cylinder-capacity.

er.		eight chine		Rela	itive We	ight of	Machin	er y.	
of Steamer.	Engine- room.	Boiler- room.	Total.		licated I power.	Iorse-	e-room 3u. ft. linder- scity.	r-room 0 sq. ft. eating- face.	Type of Machinery.
No. o	Eng	B S	Ĕ	Engine- room.	Boiler- room.	Total	Engine per of Cyl capa Boiler per 100		
1 2 8 5 6 7 8	tons. 681 638 184 38.8 719 75.2 44 78.5	695 107.8 61	1414	lbs. 226 259 207 170 167 141 77 78 62.5	Ibs. 220 251 198 208 162 202 108 116 102	lbs. 446 510 405 373 829 848 185 194	tons. 1.80 1.46 1.23 1.29 1.41 1.87 1.21 1.11 0.82	tons. 3.75 4.10 3.23 8.30 8.44 8.87 2.72 2.78 2.78	Mercantile Naval horizontal do. Naval vertice

	-	Per hou	lbs. H.67	H 968		505 812 H				510 E.	_	896	000	104	0	Q	90	365 D H	A	090	.573
	ann	Coal bu per I.H per hou	1.0	121			1.				rie	iei		-		1	.,		rir	· ·	
	190	Coal bu per sq. f grate j hour	lbs. 11.45	12.60	14.75	13.25	13.70	15.10	13.79	7.80	19.85	16.31	17.06	13.32	11.13	36.42	26.62	23.05	19.97	10.92	17.08
rials.	r sq.	I.H.P. per	1.H.P.	6.65	8 43	8.60	10 45	10.08	9.05	7.65	12.03	10.40	10.53	9 11	8.35	27.00	21.42	16.88	16.18	17.10	11.22
Results of Trials	ing- ace.	Per lb. of Coal per hour,	sq. ft.	2000	2.03	20.40	50.00	100	8 68 80 88	3.64	1.78	20.00	2.82	1.96	2.40	1.28	1 94	1.78	50.0	2.00	2.25
Res	Heating- surface.	Per LH.P.	8q. ft.	4.23	3.54	20.00	3,12	3.055	3.50	3.67	20.0	3.14	9.63	2.875	3.30	1.73	2.41	2.435	010	0.210	3.560
	pə	Indicat H.H.	I.H.P. 4295	3587	1120	1700	1065	2600	1100	3670	2360	1500	1727	1530	1250	1350	1800	1360	3400	2002	
	,nin.	Piston-sp Ft, per i	ft. 627	630	427	521	455	553	464	526	538	496	527	525	3	161	520	590	099	110	t
		Revolut per minut	revs. 52.2	57.3	61.4	61.3	20	61.5	67	58.5	53.8	62	62	75	55.5	76	65	0.69	99	13	all twenty-eight
		Stean	155 155	221	160	180	160	160	160	150	150	180	150	150	160	160	160	150	160	100	all twe
Boilers.	ate	Fire-gr Area	sq. ft. 626	240	133	193	103	240	100	710	196	144	194	168	150	200	75	154	210	188	erage of
1	.e. -Su	Heatin	sq. ft. 17,640	15,107	3.972	6,162	3.324	8,000	3,852	6.164	6.950	4,715	8,000	4,400	4,000	2,338	4.846	6.438	8,751	0,018	Ave
ller.		Pitch	ft, in.						:		24 0										
Propeller.	.19:	Diamet	ft. in.								19 0						-				
Con-	-Jng	Cooling.	3q. ft. 11,586	11,000	2,008	3,209	1,430	4,150	2,000	2,562	4,090	2,400	3,700	2,900	2,700	1.750	2,763	6,860	7,500	2,400	
	.93	Strok	fn3,	99	420	51	30	54	4 4 4 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	48	99	48	51	42	36	33	48	600	25	7	
Cylinders.		Diameter.	ins. 66	619	385	25 42 70	35	48	36	14	455	37	36%	38	39	35%	42	20%	53	40	
=			No.	_	_	_	_		_	_	-	_	_	-	-			_	_		

REMARKS.-D. forved draught; H. feed-beater.

Dimensions, Indicated Horse - power, and Cylinder - capacity of Three-stage-expansion Engines in Nine Steamers.

umber of Steamer.	Single or win Screws.	Cylinde	rs.	Revolutions per minute.	oiler- pressure per sq.‡n.	Indicated orse-power.	Cylinder- capacity.	Heatin fa	g-sur-
Number Steam	Sin	Diameters.	Stroke	Revol per n	Boiler- press per s	Indicated Horse-pow	Cyl	Total.	Per I.H.P.
1 2 3 4 5	Single " " Twin	ins. 40 66 100 89 61 97 28 38 61 17 2614 42 82 54 83	66 42 24 54	revs. 64.5 67.8 83 90 88	160 160 150 160	I.H.P. 6751 5525 1450 510 9625	cu. ft. 522 436 109 80 508	sq. ft. 17,640 15,107 8,978 1,403 20,198	sq. ft, 2.62 2.78 2.78 2.75 2.10
4 5 6 7 8 9	Single Twin	15 24 85 20 80 45 1814 29 42 3314 49 74	27 24 24	118 191 182.5 145	150 145 140 150	1194 1265 2105 9400	55 86.8 66.2 819	8,200 2,227 8,928 15,882	2.68 1.76 1.87 1.62

CONSTRUCTION OF BUILDINGS.*

(Extract from the Building Laws of the City of New York, 1893.) Walls of Warehouses, Stores, Factories, and Stables.—
25 feet or less in width between walls, not less than 12 in. to height of 40 ft.; 44

20 ft.; 20 in. to 60 ft., and 16 in. 75 to 85

to top; 85 to 100 ft. in height, not less than 28 in, to 25 ft.; 24 in. to 50 ft.; 20 in to 75 ft., and 16 in. to top; Over 100 ft. in height, each additional 25 ft. in height, or part thereof, next above the curb, shall be increased 4 inches in thickness, the upper 100 ft. in height, or part thereof a secrecified for a wall of that weight.

feet remaining the same as specified for a wall of that weight.

If walls are over 25 feet apart, the bearing-walls shall be 4 inches thicker than above specified for every 1214 feet or fraction thereof that said walls are more than 25 feet apart

Strength of Floors, Boofs, and Supports.

Floors calculated to bear

safely per sq. ft., in addition to their own weight.

Floors of dwelling, tenement, apartment-house or hotel, not	_
less than	70 lbs.
Floors of office-building, not less than	100 "
" public-assembly building, not less than	120 "
store, factory, warehouse, etc., not less than	150 4
Roofs of all buildings, not less than	50 "

Every floor shall be of sufficient strength to bear safely the weight to be imposed thereon, in addition to the weight of the materials of which the floor is composed.

Columns and Posts.—The strength of all columns and posts shall be computed according to Gordon's formulæ, and the crushing weights in pounds, to the square incl. of section, for the following-named materials, shall be taken as the coefficients in said formulæ, namely: Cas iron, 80.000;

*The limitations of space fo. bi any extended treatm nt of this subject. Much valuable information upon it will be found in Trautwine's Civil Engineer's Pocket-book, and in Kidder's Architect's an . Builder's Pocket-book. neer's Pocket-book, and in Kidder's Architect's an Builder's Pocket-book. The latter in its preface mentions the following works of reference: "Notes on Building Construction," 3 vols., Rivingtons, publishers, B. ston; "Building Superintendence," by T. M. Clark (J. R. Osgood & Co., Boston.); "The American House Carpenter," by R. G. Hatfield; "Graphical Analysis of Roof-trusses," by Prof. O. E. Greene; "The Fire Protection of Mills," by C. J. H. Woodbury; "House Drainage and Water Service," by James C. Bayles; "The Builder's Guide and Estimator's Price-book," and "Plastering Mortars and Cementa," by Fred. T. Hodgson; "Foundations and Concrete Works," and "Art of Building," by E. Dobson, Weale's Series, London.

J. H. Woodbury; "House Drainage and Water Service," by James r Bayles; "The Bullder's Guide and Estimator's Price-book," and "Plast ing Mortars and Cements," by Fred. T. Hodgson; "Foundations and C creta Works." and "Art of Building." by E. Dobson, Weale's Series, Lond

wrought or rolled iron, 40,000; rolled steel, 48,000; white pine and spruce, 3500; pitch or Georgia pine, 5000; American oak, 6000. The breaking strength of wooden beams and girders shall be computed according to the formulæ in which the constants for transverse strains for central load shall be as follows, namely: Hemlock, 400; white pine, 450; spruce, 450; pitch or Georgia pine, 550; American oak, 550; and for wooden beams and girders carrying a uniformly distributed load the constants will be doubled. The factors of safety shall be as one to four for all beams, girders, and other pieces subject to a transverse strain; as one to four for all posts, columns, and other vertical supports when of wrought iron or rolled steel; as one to five for other materials, subject to a compressive strain; as one to six for tierods, tie-beams, and other pieces subject to a tensile strain. Good, solid, natural earth shall be deemed to safely sustain a load of four tons to the superficial foot, or as otherwise determined by the superintendent of buildings, and the width of footing-courses shall be at least sufficient to meet this requirement. In computing the width of walls, a cubic foot of brickwork shall be deemed to weigh 115 lbs. Sandstone, white marble, granite, and other kinds of building-stone shall deemed to weigh 160 lbs. per cubic foot. The safe-bearing load to apply to good brickwork shall be taken at 8 tons per superficial foot when good lime mortar is used, 1114 tons per superficial foot when good lime and cement morta: mixed is used, and 15 tons per sup-

erficial foot when good cement mortar is used.

Fire-proof Buildings—Iro. and Steel Columns.—All castiron, wrought-iron, or rolled-steel columns shall be made true and smooth at both ends, and shall rest on iron or seel bed-plates, and have iron or steel cap-plates, which shall also be made true. All iron or steel trimmerbeams, headers, and tail-beams shall be suitably framed and connected together, and the iron girders, columns, beams, trusses, and all other iron work
of all floors and roofs shall be strapped, bolted, anchored, and connected together, and to the walls, in a strong and substantial manner. Where beams
are framed into headers, the angle-irons, which are bolted to the tail-beams,
shall have at least two bolts for all beams over 7 inches in depth, and three
bolts for all beams 12 inches and over in depth, and thece bolts shall not by
less them. Sinch in diameter. Each one of such angles or three when bolts of less than 34 inch in diameter. Each one of such angles or knees, when bolted to girders, shall have the same number of bolts as stated for the other leg The angle-iron in no case shall be less in thickness than the header or tim mer to which it is bolted, and the width of angle in no case shall be less than one third the depth of beam, excepting that no angle-knee shall be less than 2½ inches wide, nor required to be more than 6 inches wide. All wroughtiron or rolled-steel beams 8 inches deep and under shall have bearings equal nron or ronec-steel beams 8 inches deep and under shall have a bearings equal to their depth, if resting on a wall; 9 to 12 inch beams shall have a bearing of 10 inches, and all beams more than 12 inches in depth shall have bearings of not less than 12 inches if resting on a wall. Where beams rest on iron supports, and are properly tied to the same, no greater bearings shall be required than one third of the depth of the beams. Iron or steel floor-beams shall be so arranged as to spacing and length of beams that the load to be supported by them, together with the weights of the materials used in the construction of the said floors, shall not cause a deflection of the said beams of more than 1/80 of an inch per linear floot of same and they shall be tied of more than 1/30 of an inch per linear foot of span; and they shall be tied together at intervals of not more than eight times the depth of the beam.

Under the ends of all iron or steel beams, where they rest on the walls, a stone or cast-iron template shall be built into the walls. Said template shall be 8 inches wide in 12 inch walls, and in all walls of greater thickness said template shall be 12 inches wide; and such templates, if of stone, shall not be in any case less than 21/4 inches in thickness, and no template shall be less

than 12 inches long.

No cast-iron post or column shall be used in any building of a less average thickness of shaft than three quarters of an inch, nor shall it have an unsupported length of more than twenty times its least lateral dimensions or diameter. No wrought-iron or rolled-steel column shall have an unsupported length of more than thirty times its least lateral dimension or diameter, nor shall its metal be less than one fourth of an inch in thickness.

Lintels, Bearings and Supports.—All iron or steel lintels shall have bearings proportionate to the weight to be imposed thereon, but no lintel used to span any opening more than 10 feet in width shall have a bearing less than 12 inches at each end, if resting on a wall; but if resting on an iron post, such lintel shall have a bearing of at least 6 inches at each end, by the thickness of the wall to be supported

Strains on Cirders and Bivets.—Rolled iron or steel beam gir-

ders, or riveted from or steel plate girders used as lintels or as girders carrying a wall or floor or both, shall be so proportioned that the loads which may come upon them shall not produce strains in tension or comwhich may some upon them shall not produce strains in tension or compression upon the flanges of more than 12,000 lbs, for fron, nor more than 15,000 lbs. for steel per square inch of the gross section of each of such flanges, nor a shearing strain upon the web-plate of more than 6000 lbs, per square inch of section of such plate gives a shall be less than 44 inch in thickness. Rivets in plate girders shall not be less than 54 inch in diameter, and shall not be spaced more than 6 inches apart in any case. They shall be so spaced that their shearing strains shall not exceed 9000 lbs, per square inch, on their diameter, multiplied by the thickness of the plates through which they peas. The riveted plate girders shall be proportioned upon the supposition that the bending or chord strains are resisted entirely by the web-plate. No part of the web shall be estimated as flange area, nor more than one half of that portion of the angle-iron which lies against the web. The distance between the centres of gravity of the flange areas will be considered as the effective depth of the girder. be considered as the effective depth of the girder.

The building laws of the City of New York contain a great amount of de-

tail in addition to the extracts above, and penalties are provided for violation. See An Act creating a Department of Buildings, etc., Chapter 275, Laws of 1892. Pamphlet copy published by Baker, Voorhies & Co., New York.

MAXIMUM LOAD ON FLOORS.

(Eng'g, Nov. 18, 1892. p. 644.)—Maximum load per square foot of floor surface due to the weight of a dense crowd. Considerable variation is apparent in the figures given by many authorities, as the following table shows:

Authorities.	lbs. per sq. ft.
French practice, quoted by Trautwine and Stoney	41
Hatfield ("Transverse Strains," p. 80)	
Mr. Page, London, quoted by Trautwine	84
Maximum load on American highway bridges according	to
Waddell's general specifications	100
Mr. Nash, architect of Buckingham Palace	190
Experiments by Prof. W. N. Kernot, at Melbourne	126
Experiments by Mr. B. B. Stoney ("On Stresses," p. 617).	

The highest results were obtained by crowding a number of persons previously weighed into a small room, the men being tightly packed so as to resemble such a crowd as frequently occurs on the stairways and platforms of a theatre or other public building.

RENGTH OF FLOORS.

(From circular of the Boston Manufacturers' Mutual Insurance Co.)
The following tables were prepared by C. J. H. Woodbury, for determining safe loads on ficors. Care should be observed to select the figure giving the greatest possible amount and concentration of load as the one which may be put upon any beam or set of floor-beams; and in no case should beams be subjected to greater loads than those specified, unless a lower factor of safety is warranted under the advice of a competent engineer.

Whenever and wherever solid beams or heavy timbers are made use of in

whenever and wherever some beams or neavy timeers are made use or in the construction of a factory or warehouse, they should not be painted, varnished or cited, filled or encased in impervious concrete, air-proof plastering, or metal for at least three years, lest fermentation should destroy them by what is called "dry rot."

It is, on the whole, safer to make floor-beams in two parts, with a small

open space between, so that proper ventilation may be secured, even if the outside should be inadvertently painted or filled.

These tables apply to distributed loads, but the first can be used in respect to floors which may carry concentrated loads by using half the figure given in the table, since a beam will bear twice as much load when evenly distributed over its length as it would if the load was concentrated in the centre

The weight of the floor should be deducted from the figure given in the table, in order to ascertain the net load which may be placed upon any floor. The weight of spruce may be taken at 36 lbs. per cubic foot, and that of Southern pine at 48 lbs. per cubic foot

Table I was computed upon a working modulus of rupture of Southern pine at 2160 lbs., using a factor of safety of six. It can also be applied to ascertaining the strength of spruce beams if the figures given in the table are multiplied by 0.76; or in designing a floor to be sustained by pruce beams, multiply the required load by 1.28, and use the dimensions as given

by the table.

Theses tables are computed for beams one inch in width, because the strength of beams increases directly as the width when the beams are broad

enough not to cripple.

EXAMPLE.—Required the safe load per square foot of floor, which may be safely sustained by a floor on Southern pine 10 × 14 inch beams, 8 feet on centres, and 20 feet span. In Table I a 1 × 14 inch beam, 20 feet span, will sustain 118 lbs. per foot of span; and for a beam 10 inches wide the load would be 1180 lbs. per foot of span, or 147½ lbs. per square foot of floor for Southern-pine beams. From this should be deducted the weight of the floor, which we should be deducted the weight of the floor. which would amount to 17½ lbs. per square foot, leaving 130 lbs. per square foot as a safe load to be carried upon such a floor. If the beams are of spruce, the result of 147½ lbs. would be multiplied by 0.78, reducing the load to 115 lbs. The weight of the floor, in this instance amounting to 16 lbs., would leave the safe net load as 90 lbs. per square foot for spruce beams.

Table II applies to the design of floors whose strength must be in excess of that necessary to sustain the weight, in order to meet the conditions of delicate or rapidly moving machinery, to the end that the vibration or dis-tortion of the floor may be reduced to the least practicable limit.

In the table the limit is that of load which would cause a bending of the beams to a curve of which the average radius would be 1250 feet.

This table is based upon a modulus of elasticity obtained from observa-

tions upon the deflection of loaded storehouse floors, and is taken at 2,000,000 lbs. for Southern pine; the same table can be applied to spruce, whose modulus of elasticity is taken as 1,200,000 lbs., if six tenths of the load for Southern pine is taken as the proper load for spruce; or, in the matter of designing, the load should be increased one and two thirds times, and the dimension of timbers for this increased load as found in the table should be

used for spruce.

It can also be applied to beams and floor-timbers which are supported at each end and in the middle, remembering that the deflection of a beam supported in that manner is only four tenths that of a beam of equal span which rests at each end; that is to say, the floor-planks are two and one half times as stiff, cut two bays in length. as they would be if cut only one bay in length. When a floor-plank two bays in length is evenly loaded, three sixteenths of the load on the plank is su-tained by the beam at each end of the plank, and ten sixteenths by the beam under the middle of the plank; so that for a completed floor three eighths of the load would be sustained by the beams under the joints of the plank, and five eighths of the load by the beams under the middle of the plank; this is the reason of the importance of breaking joints in a floor-plank every three feet in order that each beam shall receive an identical load. If it were not so, three eighths of the whole load upon the floor would be sustained by every other beam, and five

whose losa upon the hoor would be sustained by every other beam, and five eighths of the load by the corresponding alternate beams.

Repeating the former example for the load on a mill floor on Southernpine beams 10 × 14 inches, and 20 feet span, laid 8 feet on centres: In Table II a 1 × 14 inch beam should receive 61 lbs. per foot of span, or 75 lbs. per sq. ft of floor, for Southern-pine beams. Deducting the weight of the floor, 17½ lbs. per sq. ft., leaves 57 lbs. per sq. ft. as the advisable load.

If the beams are of spruce, the result of 75 lbs. should be multiplied by 0.6, reducing the load to 45 lbs. The weight of the floor, in this instance amounting to 16 lbs., would leave the net load as 29 lbs, for spruce beams.

If the beams were two spans in length, they could under these conditions

If the beams were two spans in length, they could, under these conditions, support two and a half times as much load with an equal amount of deflec-tion, unless such load should exceed the limit of safe load as found by Table

In a would be the case under the conditions of this problem.

Mill Columns.—Timber posts offer more resistance to fire than iron pillars, and have generally displaced them in millwork. Experiments made on the testing-machine at the U. S. Arsenal at Watertown, Mass., show that sound timber posts of the proportions customarily used in millwork yield by direct crushing, the strength being directly as the area at the smallest part. The columns yielded at about 4500 lbs. per square inch, confirming the general practice of allowing 600 lbs. per square inch, as a safeload. Square columns are one fourth stronger than round ones of the same

I. Safe Distributed Loads upon Southern-pine Beams One Inch in Width-

(C. J. H. Woodbury.)

(If the load is concentrated at the centre of the span, the beams will sustain half the amount as given in the table.)

eet.						Dep	th o	l Bea	m ir	incl	168.				
Span, feet.	2	8	4	5	6	7	8	9	10	11	12	18	14	15	16
Sp					Loa	d in	pou	nds p	er f	oot o	f Spa	ın.			
5	38	86	154	240	346	470	614	778	960				- 1		
5	27	60	107	167	240	827	427	540	667	807			١.		
7	20	44	78	122	176	240	314		490	593	705	628	- 1		I
7 8 9	15	84	60	94	135	184	240		375	454	540	634	735		1
9		27	47	74	107	145	190	240	296	859	427	501	581	667	759
10		22	38	60	86	118	154	194	240	290	846	406	470	540	614
11			82	50	71	97	127	161	198	240	286	835	389	446	508
12			27	42	60	82	107	135	167	202	240	282	827	375	474
18	i i			36	51	70 60 52	90	115	142	172	205	240	278	820	364
18 14 15 16 17				31	44	60	78	99	1:33	148	176	207	240	276	314
15		l		27	39	52	68	86	107	129	154	180	209	240	273
16					34	46	60	76	94	118	135	158	184	211	240
17					30	41	53 47	67	88	101	120	140	168	187	217
18						36	47	60	74	90	107	125	145	167	190
19		٠					43	54	66	80 78	96	112	130	150	170
20							88	49	60	78	86	101	118	135	154
21	• • •	•••						44	54	66	78	92	107	122	139
18 19 20 21 22 23			· · ·						50	60	71	84	97	112	127
23						• • •			45	55	65	77	89	102	116
24					- 1					50	60	70	82	94	107
25			!					- 1		46	55	65	75	86	98

Distributed Loads upon Southern-pine Beams sufficient to produce Standard Limit of Deflection.

(C. J. H. Woodbury.)

et.						Dept	h of	Bear	m in	inch	es.					å,
Span, feet.	2	8	4	5	6	î	8	9	10	11	12	13	14	15	16	Deflection, inches.
Spe					Loa	d in	poun	ds pe	er fo	ot of	Spa	n.				P.=
5 6 7 8 9	3 2	10	28	44	77	122	182							1	_	.0300
6	2	7	16	81	53	85	126	180	247				l .			.0432
7	١	5	12	23	89	62	93	132	181	241						.0588
8		4	9	17	80	48 38	71	101	139	185	240	305			!	.0768
9	۱. ا		7	14	24	38	56	80	110	146	190	241	301			.0972
10	1.		6	11	19	30	46	65	89	118	154	195	244	800		.1200
11 12	i		١	9	16	25	88	54	78	98	127	161	505	248	801	.1452
12				l	13	21	8.5	45	65	83	107	136	169	208	258	.1728
18	i			1	ii	18	27	88	53	70	91	116	144	178	215	.2028
14		• • • •		1		. 16		38	45	60	78	100	124	158	186	.2352
15	١					14	20	29	40	53	78 68	87	108	133	162	.2700
16	١	•••	•••	١٠٠٠٠,			18	25	85	46	60	76	95	117	147	.8072
17				• • •			16	22	31	41	58	68	84	104	126	.8468
18		••••	••••	l	••••		10	22 20	27	37	47	60	84 75	98	112	.8888
10		•••	• • • •					18	95	33		54	68	88	101	.4332
19 20 21		•••	••••					10	25 22	30	43 88 85 82	49	61	75	91	.4800
01								•••	20	80 27	98	44	55	75 68	83	.5292
22	• •	• ••	••••	••••	••••			•••	a	24	90	40	50	63	00	
22	•••				• • •				• • •	22	29	87	46	03	75	.5808
28	٠	••••	• • • • •		••••	••••		••••	••••	ZZ	29			57	69	.6348
24	•••							[84	42	52	68	.6912
25	• •		1	· • • ·				<u> </u>	• • • • •		25	81	89	48	58	.7500

ELECTRICAL ENGINEERING.

STANDARDS OF MEASUREMENT.

C.G.S. (Centimetre, Gramme, Second) or "Absolute": System of Physical Measurements:

= 1 centimetre, cm.; Unit of space or distance Unit of mass = 1 gramme, gm.; = 1 second, s.; Unit of time Unit of velocity = space + time = 1 centimetre in 1 second: Unit of acceleration = change of 1 unit of velocity in 1 second; Acceleration due to gravity, at Paris, = 861 centimetres in 1 second; Unit of force = $1 \text{ dyne} = \frac{1}{961} \text{ gramme} = \frac{.0022046}{961} \text{ lb.} = .000002347 \text{ lb.}$

A dyne is that force which, acting on a mass of one gramme during one second, will give it a velocity of one centimetre per second. The weight of one gramme in latitude 40° to 45° is about 960 dynes, at the equator 73 dynes, and at the poles nearly 964 dynes. Taking the value of g, the acceleration due to gravity, in British measures at 32.185 feet per second at Paris, and the metre = 39.37 inches, we have

 $1 \text{ gramme} = 32.185 \times 12 + .3937 = 981.00 \text{ dynes.}$

Unit of work = 1 erg = 1 dyne-centimetre = .0000007373 foot-pound; Unit of power = 1 watt = 10 million ergs per second, = .7373 foot-pound per second, = $\frac{.7373}{5500} = \frac{1}{746}$ of 1 horse-power = .00184 H.P.

C.G.S. Unit of magnetism = the quantity which attracts or repels an equal quantity at a centimetre's distance with the force of 1 dyne.
C.G.S. Unit of electrical current = the current which, flowing through a length of 1 centimetre of wire, acts with a force of 1 dyne upon a unit of magnetism distant 1 centimetre from every point of the wire. The ampere, the commercial unit of current, is one tenth of the C.G.S. unit.
The Proceeding Units wand in Whaterian (C.G.S. unit.

The Practical Units used in Electrical Calculations are: Ampere, the unit of current strength, or rate of flow, represented by I. Volt, the unit of electro-motive force, electrical pressure, or difference of potential, represented by E.

Ohm, the unit of resistance, represented by R,

Coulomb (or ampere-second), the unit of quantity, Q. Ampere-hour = 3600 coulombs, Q. Watt (ampere-volt, or volt-ampere), the unit of power, P. Joule (volt-coulomb), the unit of energy or work, W.

Farad, the unit of capacity, represented by C.

Henry, the unit of inductance, represented by L.

Using letters to represent the units, the relations between them may be expressed by the following formulæ, in which t represents one second and T one hour:

$$I = \frac{E}{R}$$
, $Q = It$, $Q' = IT$, $C = \frac{Q}{E}$, $W = QE$, $P = IE$.

As these relations contain no coefficient other than unity, the letters may represent any quantities given in terms of those units. For example, if E represents the number of volts electro-motive force, and R the number of ohms resistance in a circuit, then their ratio E+R will give the number of amperes current strength in that circuit.

The above six formulæ can be combined by substitution or elimination, so as to give the relations between any of the quantities. The most important of these are the following:

$$\begin{split} Q &= \frac{E}{R}t, \quad C = \frac{I}{E}t, \quad W = IEt = \frac{E^2}{R}t = I^2Rt = Pt, \\ E &= IR, \quad R = \frac{E}{I}, \quad P = \frac{E^2}{R} = I^2R = \frac{W}{t} = \frac{QE}{t}. \end{split}$$

The definitions of these units as adopted at the International Electrical Congress at Chicago in 1898, and as established by Act of Congress of the

United States, July 12, 1894, are as follows:

The ohm is substantially equal to 10° (or 1,000,000,000) units of resistance of the C.G.S. system, and is represented by the resistance offered to an unvarying electric current by a column of mercury at 32° F., 14.4521 grammes in mass, of a constant cross-sectional area, and of the length of 106.3 centi-

The ampere is 1/10 of the unit of current of the C.G.S. system, and is the practical equivalent of the unvarying current which when passed through a solution of nitrate of silver in water in accordance with standard specifications deposits silver at the rate of .001118 gramme per second.

The volt is the electro-motive force that, steadily applied to a conductor whose resistance is one ohm, will produce a current of one ampere, and is practically equivalent to 1000/1484 (or .6974) of the electro-motive force between the poles or electrodes of a Clark's cell at a temperature of 15° C., and prepared in the manner described in the standard specifications.

The coulomb is the quantity of electricity transferred by a current of one

ampere in one second.

The farad is the capacity of a condenser charged to a potential of one wolt by one coulomb of electricity.

The joule is equal to 10,000,000 units of work in the C.G.S. system, and is practically equivalent to the energy expended in one second by an ampere in an ohm.

The watt is equal to 10,000,000 units of power in the C.G.S. system, and is practically equivalent to the work done at the rate of one joule per second.

The henry is the induction in a circuit when the electro-motive force induced in this circuit is one volt, while the inducing current varies at the rate of one ampere per second.

The ohm, volt, etc., as above defined, are called the "international" ohm, volt, etc., to distinguish them from the "legal" ohm, B.A. unit, etc.

The value of the ohm, determined by a committee of the British Association in 1883, called the B.A. unit, was the resistance of a certain piece of copper wire. The so-called "legal" ohm, as adopted at the International Congress of Electricians in Paris in 1884, was a correction of the B.A. unit. and was defined as the resistance of a column of mercury 1 square millimetre in section and 106 centimetres long, at a temperature of 32° F.

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1 legal ohm = 1.0119 B.A. units, 1 B.A. unit = 0.9889 legal ohm; 1 international ohm = 1.0186 " " 1 " = 0.9866 int, ohm;
                           = 1.0028 legal ohm, 1 legal ohm = 0.9977 "
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DERIVED UNITS.

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1 megohm
                 = 1 million ohms;
1 microhm
                 = 1 millionth of an ohm;
1 milliampere = 1/1000 of an ampere;
1 micro-farad = 1 millionth of a farad.
    RELATIONS OF VARIOUS UNITS.
```

```
= 1 coulomb per second;
= 1 watt = 1 volt-coulomb per second;
1 ampere.....
1 volt-ampere ..........
                              = .7373 foot-pound per second,
                              = .0009477 heat-units per second (Fahr.).
                              = 1/746 of one horse-power;
                              = .7878 foot-pound,
                              = work done by one watt in one second.
                              = .0009477 heat-unit;
                              = 1055.2 joules;
= 1000/746 or 1.3406 horse-powers;
1 British thermal unit ... ...
1 kilowatt, or 1000 watts.....
1 kilowatt-hour,
                            ( = 1.8405 horse-power hours,
1000 volt-ampere hours,
                              = 2,654,200 foot-pounds,
                             = 8412 heat-units;
= 746 watts = 746 volt-amperes,
1 British Board of Trade unit,
```

The ohm, ampere, and volt are defined in terms of one another as follows: Ohm, the resistance of a conductor through which a current of one ampere will pass when the electro-motive force is one volt. Ampere, the quantity of current which will flow through a resistance of one ohm when the electro-motive force is one volt. Volt, the electro-motive force required to cause current of one ampere to flow through a resistance of one ohm.

) 	ntt.	Unit. Equivalent Value in Other Units.	Unit,	Equivalent Value in Other Units.	Unit.	Equivalent Value in Other Units.
H,H	I. W. Hour =	1,000 w 2,654,200 ft 3,600,000 j 3,412 h 367,000 k	1. H.P. =	746 watts. 746 K. W. 38,000 ftlbs. per minute. 556 ftuls. per second. 2,56 heat-units per hour. 72, 4 heat-units per minute. 777 heat-units per minute. 175 lbs. carbon oxidized per hour.	Heat- unit ==	1.055 watt seconds. 778 ftlbs. 107.6 kilogram metres000288 H. V. hour000088 H. P. hour000088 B. carbon oxi- dized. lbs. carbon oxi- from and at 312 F
		22.75 lbs. of water raised from 62° to 212° F.		2.64 lbs. water evap per hour from and at 212° F.	1 Heat-unit per Sq. Ft.	.122 watts per square in.
Þ	1 h	1,980,000 ft. lbs. W. hours. 2,545 hear-units. 273,740 k.g. m.	Joule=	. 1 Watt Second. . 000000278 K. W. hour. . 102 k. g. m. . 0009477 heat-units. . 7373 ft -lb.	per min. = 1 Kilogram Metre =	7.233 ftlbs. 00000385 H.P hour. 00000272 K. W. hour. 0093 heat-units.
H	Hour =	with perfect efficiency. 2.64 lbs. water evaporated from and at 212° F. 17.0 lbs. water raised from 62° F. to 212° F.	Ftlb.	1.356 foules. .1383 k. g. m. .0000037 K. W. hours. .001285 heat-units. .000005 H.P. hour.	1 lb. Carbon Oxidized	14,544 heat-units. 1.11 b. Anth'cife coal ox, 2.5 bs. dry wood oxidized. 21 ct. ft. illumiating-gas. 4.26 K. W. hours
		1,000 watts. 1.34 horse-power. 2,654,200 ftlbs. per hour. 44,240 ftlbs. per minute.	Watt	1 joule per second00134 H.P. 3.412 beat-units per hour.	fect Effi- ciency =	11,315,000 ft., fbs. 15,000 ft., fbs. 15 lbs. of water evap. from and at 312° F.
K	Kilo-	3,412 heat-units per second.		.0035 lbs. water evap, per hr. 44.24 ftlbs. per minute.		.283 K. W. hour. 379 H.P. hour.
war	watt =	988 heat-unit per second. 2775 lb. carbon oxidized per hour. 8.63 lbs. water evap. per hour from and at 212° F.	1 Watt per sq. in. =	8.19 heat-units per sq. ft. per minute. 8871 ftlbs. per sq. ft. per minute. 193 H.P. per sq. ft.	Tib. water Evapor'ed from and at 212° F. =	108.900 k. ę. m. 1,019.000 joules. 751,300 ftlbs. . 0664 lb. of carbon oxi- dized.

Units of the Magnetic Circuit.—(See Electro-magnets, page 1052.) For Methods of making Electrical Measurements, Testing, etc., see Munroe & Jamieson's Pocket-Book of Electrical Rules, Tables, and Data; S. P. Thompson's Dynamo-Electric Machinery; Carhart & Patterson's Electrical Measurements; and works on Electrical Engineering.

Equivalent Electrical and Mechanical Units.-H. Ward Leonard published in *The Electrical Engineer*, Feb. 25, 1895, a table of useful equivalents of electrical and mechanical units, from which the table on page 1026 is taken, with some modifications.

ANALOGIES BETWEEN THE FLOW OF WATER AND ELECTRICITY.

WATER.

Head, difference of level, in feet. Difference of pressure, list, per sq. in. Difference of pressure, list, per sq. in. Resistance of pipes, apertures, etc., increases with length of pipe, with contractions, roughness, etc.; decreases with increase of sectional area.

Rate of flow, as cubic ft. per second, gallons per minute, etc., or volume divided by the time. In the mining regions sometimes expressed in "miners' inches."

Quantity, usually measured in cubic ft. or gallons, but is also equivalent to rate of flow x time, as cu. ft. per second for so many hours.

Work, or energy, measured in foot-pounds; product of weight of falling water into height of fall; in pumping, product of quantity in cubic feet into the pressure in lbs. per square foot against which the water is pumped.

Power, rate of work. Horse-power = ft.-lbs. of work in 1 min. + 33,000. In water flowing in pipes, rate of flow in cu. ft. per second × resistance to the flow in lbs. per sq. ft. ÷ 550.

ELECTRICITY. Volts; electro-motive force;

ence of potential; E. or E.M.F. Ohms, resistance, R. Increase Increases directly as the length of the conductor or wire and inversely as its sectional area, $R \propto l + s$. It varies with the nature of the conductor.

Amperes; current; current strength; intensity of current; rate of flow; 1 ampere = 1 coulomb per second.

Amperes = $\frac{\text{volts}}{\text{ohms}}$; $I = \frac{E}{R}$; E = IR.

Coulomb, unit of quantity, Q, = rate of flow \times time, as ampere-seconds. 1 ampere-hour = 8600 coulombs.

Joule, volt-coulomb, W, the unit of work, = product of quantity by the electro-motive force = volt-ampere-second. 1 joule = .7878 foot-pound.

If C (amperes) = rate of flow, and E (volts) = difference of pressure between two points in a circuit, energy expended = IEt, = $I^{2}Rt$.

Watt, unit of power, P, = volts × amperes, = current or rate of flow × difference of potential. watt = .7878 foot pound per second

= 1/746 of a horse-power.

ELECTRICAL RESISTANCE.

Laws of Electrical Resistance.—The resistance, R. of any conductor varies directly as its length, I, and inversely as its sectional area, s,

or $R \propto l + s$.

If r = the resistance of a conductor 1 unit in length and 1 square unit in sectional area, R = rl + s. The common unit of length for electrical calculations in English measure is the foot, and the unit of area of wires is the circular mil = the area of a circle 0.001 in, diameter. 1 mil-foot = 1 foot long 1 circ.-mil area.

Resistance of 1 mil-foot of soft copper wire at 51° F. = 10 international ohms.

EXAMPLE.—What is the resistance of a wire 1000 ft. long, 0.1 in. diam.? 0.1 in. diam. = 10,000 circ. mils.

$$R = rl + s = 10 \times 1000 + 10,000 = 1$$
 ohm.

Specific resistance, also called resistivity, is the resistance of a material of unit length and section as compared with the resistance of soft copper. Conductivity is the reciprocal of specific resistance, or the relative con-

ducting power compared with copper taken at 100.

Relative Conductivities of Different Metals at 0° and 100° C. (Matthiessen.)

	Conduc	tivities.	1	Conductivities.			
Metals.	At 0° C. " 32° F.	At 100° C. " 212° F.	Metals.	At 0° C. " 82° F.	At 100° C		
Silver, hard Copper, hard Gold, hard Zinc, pressed Cadmium Platinum, soft Iron, soft		71.56 70.27 55.90 20.67 16.77	Tin	12.86 8.32 4.76 4.62 1.60 1.245	8.67 5.86 3.33 3.26		

Electrical Conductivity of Different Metals and Alloys.

The following figures of electrical conductivity are given by Lazare Weiler

Pure silver Pure copper. Telegraphic silicious bronze Alloy of 1/2 copper, 1/2 silver Pure gold. Silicide of copper, 4/8 Si Telephonic silicious bronze	100 98 86.65 78 75 85	Pure platinum Copper with 10% of nickel Pure lead	15.45 12.6 12 10.6 10.6 8 88
Pure zinc Brass with 85% of zinc Phosphor tin	29.9 21.5 17.7	Pure lead Bronze with 20% of tin Pure nickel Phosphor-bronze, 10% tin Antimony	8 88 8.4 7 89 6.5 8.88

Conductivity of Aluminum.—J. W. Richards (Jour. Frank. Inst., Mar. 1897) gives for hard-drawn aluminum of purity 98.5, 99.0, 99.5, and 99.73% respectively a conductivity of 55, 59, 61, and 63 to 64%, copper being 100%. The Pittsburg Reduction Co. claims that its purest aluminum has a conductivity of over 64.5%. (Eng'g News, Dec. 17, 1896.)

German Silver.—The resistance of German silver depends on its committee of the committee

position. Matthiessen gives it as nearly 13 times that of copper, with a temperature coefficient of .0004433 per degree C. Weston, however (Proc. Electrical Congress 1893, p. 179), has found copper-nickel-zinc alloys (German silver) which had a resistance of nearly 28 times that of copper, and a temperature coefficient of about one half that given by Matthiessen.

Conductors and Insulators in Order of their Value.

CONDUCTORS.	INSULATO	RS (NON-CONDUCTORS).
All metals	Dry air	Ebonite
Well-burned charcoal	Shellac	Gutta-percha
Plumbago	Paraffin	India-rubber
Acid solutions	Amber	Silk
Saline solutions	Resins	Dry paper
Metallic ores	Sulphur	Parchment
Animal fluids	Wax	Dry leather
Living vegetable substances	Jet	Porcelain
Moist earth	Glass	Oils
Water	Mica	

According to Culley, the resistance of distilled water is 6754 million times

According to Cintey, the resistance of institute water is 763 minor times as great as that of copper. Impurities in water decrease its resistance.

Resistance Varies with Temperature.—For every degree Centigrade the resistance of copper wire having a resistance of 10 ohms at 82° would have a resistance of 11.11 ohms at 82° F.

The following table shows the amount of resistance of a few substances used for various electrical purposes by which 1 ohm is increased by a rise of

temperature of 1° C.

Platinoid	.00081	Gold, silver	.00080
dolling private (see above)	*****	Coppor	.00100

Annealing.—Resistance is lessened by annealing. Matthlessen gives the following relative conductivities for copper and silver, the comparison being made with pure silver at 100° C .:

Metal.	Temp. C.	Hard.	Annealed.	Ratio.
Copper	1i°	95,81	97.88	1 to 1.027
Silver	14.60	95.86	103.38	1 to 1.084

Dr. Siemens compared the conductivities of copper, silver, and brass with the following results. Ratio of hard to annealed:

Standard of Resistance of Copper Wire. (Trans. A. I. E. E., Sept. and Nov. 1890.)—Matthiessen's standard is: A hard-drawn copper wire 1 metre long, weighing 1 gramme, has a resistance of 0.1469 B.A. unit at $^{\circ}$ C. Relative conducting power (Matthiessen): silver, 100; hard or unannealed copper, 99.95; soft or annealed copper, 102.21. Conductivity of copper at other temperatures than 0° C., $C_{\xi} = C_{0}(1-.00887t+.000000009t^{2})$.

The resistance is the reciprocal of the conductivity, and is

$$R_t = R_0(1 + .00387t + .00000597t^2).$$

The shorter formula $R_t = R_0(1 + .00406t)$ is commonly used

A committee of the Am. Inst. Electrical Engineers recommend the rollowing as the most correct form of the Matthiessen standard, taking 8.89 as the sp. gr. of pure copper:

A soft copper wire 1 metre long and 1 mm, diam. has an electrical resistance of .02057 B.A. unit at 0° C. From this the resistance of a soft copper wire 1 foot long and .001 in. diam. (mil-foot) is 9.720 B.A. units at 0° C.

For tables of the resistance of copper wire, see pages 218 to 220, also pp. 1034, 1035.

Taking Matthlessen's standard of pure copper as 1006, some refined metal

has exhibited an electrical conductivity equivalent to 108%.

Matthiessen found that impurities in copper sufficient to decrease its density from 8,94 to 8.90 produced a marked increase of electrical resistance.

DIRECT ELECTRIC CURRENTS.

Ohm's Law.—This law expresses the relation between the three fundamental units of resistance, electrical pressure, and current. It is:

$$\text{Current} = \frac{\text{electrical pressure}}{\text{resistance}}; \quad I = \frac{E}{R}; \quad \text{whence} \quad E = IR, \quad \text{and} \quad R = \frac{E}{I}.$$

In terms of the units of the three quantities.

Amperes =
$$\frac{\text{volts}}{\text{ohms}}$$
; volts = amperes × ohms; ohms = $\frac{\text{volts}}{\text{amperes}}$.

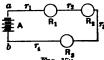
EXAMPLES: Simple Circuits.—1. If the source has an effective electrical pressure of 100 volts, and the resistance is two ohms, what is the current?

$$I = \frac{E}{R} = \frac{100}{2} = 50$$
 amperes.

2. What pressure will give a current of 50 amperes through a resistance of 2 ohms? $E=IR=50\times 2=100$ volts.

3. What resistance is required to obtain a current of 50 amperes when the pressure is 100 volts? R = E + I = 100 + 50 = 2 ohms. Ohm's law applies equally to a complete electrical circuit and to any

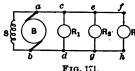
part thereof. Series Circuits.—If conductors are arranged one after the other the are said to be in series, and the total resistance of the circuit is the sum of



the resistances of its several parts. Let A, Fig. 170, be a source of current, such as a battery or generator, producing a difference of potential or E. M. F. of 120 volts, measured across ab, and let the circuit contain four conductors whose resist-

the circuit contain four conductors whose resisters B and three other resistances, R_1 , R_2 , R_3 , each 2 ohms. The total resistance is 10 ohms, and by Ohm's law. This current is constant throughout the circuit, and a series circuit is therefore one of constant throughout the circuit, and a series circuit is therefore one of constant current. The drop of potential in the whole circuit from a around to b is 120 volts, or E = RI. The drop in any portion depends on the resistance of that portion; thus from a to R_1 the resistance is 1 ohm, the constant current 12 amperes, and the drop a 1 × 12 = 12 volts. The drop in passing through each of the resistances a 1, a 2, a 2 = 24 volts is $2 \times 12 = 24$ volts.

Parallel, Divided, or Multiple Circuits.—Let B, Fig. 171, be a generator producing an E. M. F. of 220 volts across the terminals ab. The



current is divided, so that part flows through the main wires ac and part hows through the "shunt" s, having a resistance of 0.5 ohm. Also the current has three paths between c and d, viz, through the three resistances in parallel R_1, R_2, R_3 , of 2 ohms each. Consider that the resist

of 2 ohms each. Consider that the resistance R = 1 + C. The conductance of the separate conductances, and the resistance R = 1 + C. The conductance is the sum of the separate conductances, and the resistance of the combined or "parallel" paths is the reciprocal of the total conductance is the sum of the separate conductances, and the resistance of the combined or "parallel" paths is the reciprocal of the total conductance.

$$R = 1 + \left(\frac{1}{0.5} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2}\right) = 1 + 8.5 = 0.286$$
 ohm.

The current I=E+R=770 amperes.

Conductors in Series and Parallel.—Let the resistances in parallel be the same as in Fig. 171, with the additional resistance of 0.1 ohm in each of the six sections of the main wires, ac, bd, etc., in series. The voltage across ab being 220 volts, determine the drop in voltage at the several points, the total current, and the current through each path. The problem is somewhat complicated. It may be solved as follows: Consider first the points eg; here there are two paths for the current, efgh and eg. Find the resistance and the conductance of each and the total resistance (the reciprocal of the joint conductance) of the parallel paths. Next consider the points cd; here there are two paths—one through $ext{e}$ and the other through $ext{e}$. Find the total resistance as before. Finally consider the points $ext{e}d$: here there are two paths—one through $ext{e}d$. Find the conductances of each and their sum. The product of this sum and the other age at $ext{e}d$ will be the total amperes of current, and the current through any path will be proportional to the conductance of that path. The resistances, $ext{e}d$, and conductances, $ext{e}d$, of the several paths are as follows:

Total current = 220 × 3.0832 = 667.3 amperes. Current through $s = 220 \times 2 = 440$ amp.; through c = 227.3 amp.

" $cR_1d = 227.8 \times 0.5 + 1.3018 = 8.34$ amp.

" $e = 227.3 \times 0.8018 + 1.3018 = 139.96$ "

" $eR_2g = 139.96 \times 0.5 + 0.9545 = 73.81$ "

" $fR_8 = 189.96 \times 0.4545 + 0.9545 = 66.65$ "

The drop in voltage in any section of the line is found by the formula E = RI, R being the resistance of that section and I the current in it. As the R of each section is 0.1 ohm we find E for ac and bd each = 22.7 volts, the K of each section is 0.1 dum we find L for L and R each L each L each L for L and L each

Internal Resistance.—In a simple circuit we have two resistances, that of the circuit R and that of the internal parts of the source of electromotive force, called internal resistance, r. The formula of Ohm's law when the internal resistance is considered is I = E + (R + r).

Power of the Circuit.—The power, or rate of work, in watts = current in amperes \times electro-motive force in volts = $I \times E$. Since I = E + R, watts = $E^2 + R$ = electro-motive force $^2 + R$ esistance. Example.—What H.P. is required to supply 100 lamps of 40 ohms resistance.

ance each, requiring an electro-motive force of 60 volts?

The number of volt-amperes for each lamp is $\frac{E^2}{R} = \frac{60^3}{40}$, 1 volt-ampere =

.00134 H.P.; therefore $\frac{60^2}{40} \times 100 \times .00134 = 12$ H.P. (electrical) very nearly.

Electrical, Brake, and Indicated Horse-power.—The power given out by a dynamo = volts × amperes + 1000 = kilowatts, kw. Volts × amperes + 746 = electrical horse-power, E.H.P. The power put into a dynamo shaft by a direct-connected engine or other prime mover is called the shaft or brake horse-power, B.H.P. If e_1 is the efficiency of the dynamo, B.H.P. = E.H.P. + e_1 . If e_2 is the mechanical efficiency of the engine, the indicated horse-power, I.H.P. = brake H.P. + e_2 = E.H.P. +

 $(e_1 \times e_2)$. $1(e_1$ and e_2 each = 91148, I.H.P. = E.H.P. \times 1.194 = kw. \times 1.60. In direct-connected units of 250 kw. or less the rated H.P. of the engine is commonly

taken as 1.6 x the rated kw. of the generator.

Electric motors are rated at the H.P. given out at the pulley or belt. H.P.

of notor = E.H.P., supplied + efficiency of motor. **Heat Generated by a Current**,—Joule's law shows that the heat developed in a conductor is directly proportional, 1st, to its resistance; 2d, to the square of the current strength; and 3d, to the time during which the current flows, or $H = I^2Rt$. Since I = E + R,

$$I^{2}Rt = \frac{E}{R}IRt = EIt = E\frac{E}{R}t = \frac{E^{2}t}{R}.$$

Or, heat = $current^2 \times resistance \times time$

= electro-motive force \times current \times time = electro-motive force \times current \times time + resistance. Q = quantity of electricity flowing = It = (Et + R). H = EQ; or heat = electro-motive force \times quantity.

The electro-motive force here is that causing the flow, or the difference in

potential between the ends of the conductor.

The electrical unit of heat, or "joule" = 10" ergs = heat generated in one second by a current of 1 ampere flowing through a registance of one ohm = .23s gramme of water raised 1° C. $H=I^2Rt \times .239$ gramme calories = $I^2Rt \times .0009478$ Br tish thermal units.

In electric lighting the energy of the current is converted into leat in the lamps. The resistance of the lamp is made great so that the required quantity of heat may be developed, while in the wire leading to and from the lamp the resistance is made as small as is commercially practicable, so that as little energy as possible may be wasted in heating the wire.

Heating of Conductors. (From Kapp's Electrical Transmission of Energy.)—It becomes a matter of great importance to determine before.

hand what rise in temperature is to be expected in each given case, and if that rise should be found to be greater than appears safe, provision must be made to increase the rate at which heat is carried off. This can generally be done by increasing the superficial area of the conductor. Say we have one circular conductor of I square inch area, and find that with 1000 amperes flowing it would become too hot. Now by splitting up this conductor into 10 separate wires each one tenth of a square inch cross-sectional area, we have not altered the total amount of energy transformed into heat, but we have increased the surface exposed to the cooling action of the surrounding air in the ratio of $1:\sqrt{10}$, and therefore the ten thin wires can dissipate more than three times the heat, as compared with the single thick wire. Prof. Forbes states that an insulated wire carries a greater current without

overheating than a bare wire if the diameter be not too great. Assuming overheating than a bare wife it in diameter be not or great. Assuming the diameter of the cable to be twice the diam. of the conductor, a greater current can be carried in insulated wires than in bare wires up to 1.9 inch diam. of conductor. If diam. of conductor, this is the case up to 1.1 inch diam. of conductor.

Heating of Bare Wires,—The following formulæ are given by

Kennelly:

$$T = \frac{I^2}{d^2} \times 90,000 + t; d = 44.8 \sqrt[4]{\frac{I^2}{T - t}}$$

T — temperature of the wire and t that of the air, in Fahrenheit degrees; I — current in amperes, d — diameter of the wire in mils.

If we take $T - t = 90^{\circ} \text{ F.}$, $\sqrt[4]{90} = 4.48$, then

$$d = 10 \sqrt[8]{I^2}$$
 and $I = \sqrt{d^2 + 1,000}$.

This latter formula gives for the carrying capacity in amperes of bare wires almost exactly the figures given for weather-proof wires in the Fire Underwriters' table except in the case of Nos. 18 and 16, B. & S. gauge, for which the formula gives 8 and 11 ampere, respectively, instead of 5

and 3 amperes, given in the table.

Heating of Colls.—The rise of temperature in magnet coils due to the passage of current through the wire is approximately proportional to the watts lost in the coil per unit of effective radiating surface, thus:

$$t \propto \frac{I^2R}{S}$$
, or $t = \frac{I^2R}{kS}$

t being the temperature rise in degrees Fahr.; S, the effective radiating t being the temperature rise in degrees Fahr.; S, the effective radiating surface; and k a coefficient which varies widely, according to conditions. In electromagnet coils of small size and power, k may be as large as 0.015. Ordinarily it ranges from 0.012 down to 0.005; a fair average is 0.007. The more exposed the coil is to air circulation, the larger is the value of k; the larger the proportion of iron to copper, by weight, in the core and winding, the thinner the winding with relation to its dimension parallel with the magnet core, and the larger the "space factor" of the winding with relation to the sum of the value of k. The space factor is the ratio of the actual copper cross-section of the whole coil to the gross cross-section of copper, insulation and interviews. insulation, and interstices.

See also the discussion of magnet windings under Electromagnets, p. 1050. **Fusion of Wires.**—W. H. Preece gives a formula for the current required to fuse wires of different metals, viz., $I = ad^{\frac{3}{2}}$, in which d is the diameter in inches and a a coefficient whose value for different metals is as follows: Copper, 10244; aluminum, 7586; platinum, 5172; German silver, 5230; platinoid, 4750; iron, 3148; tin, 1462; lead, 1379; alloy of 2 lead and 1 tin, 1318.

Allowable Carrying Capacity of Copper Wires.

(Fire Underwriters' Rules.)

B. & S.	Circular	Am	eres.	Circular	Amperes		
Gauge.	Mils.	Rubber Covered.	Weather- proof.	Mils.	Rubber Covered	Weather- proof.	
18 16 14 12 10 8 6 5 4 3	1,624 2,583 4,107 6,530 10,380 16,510 26,250 33,100 41,740 52,630	3 6 12 17 24 33 46 54 65 76	5 8 16 23 32 46 65 77 92 110	200,000 300,000 400,000 500,000 600,000 700,000 800,000 900,000 1,000,000	200 270 330 390 450 500 600 650 690	300 400 500 590 680 760 840 920 1,000	
0 00 000 0000	52,030 66,370 83,690 105,500 133,100 167,800 211,600	90 107 127 150 177 210	131 156 185 220 262 312	1,200,000 1,300,000 1,400,000 1,600,000 1,800,000 2,000,000	730 770 810 890 970 1,050	1,150 1,220 1,290 1,430 1,550 1,670	

For insulated aluminum wire the safe-carrying capacity is 84 per cent of

that of copper wire with the same insulation.

Underwriters Insulation.**—The thickness of insulation required by the rules of the National Board of Fire Underwriters varies with the size of the wire, the character of the insulation, and the voltage. The thickness of insulation on rubber-covered wires carrying voltages up to 600 varies from of institution of rubber-covered wires carrying vottages up to obtained in the first of a No. 18 B. & S. gauge wire to a inch for a wire of 1 000 000 circular mils. Weather-proof insulation is required to be alightly thicker. For voltages of over 600 the insulation is required to be at least 1/16 inch thick for all sizes of wire under No. 8 B. & S. gauge, and to be at least 1/16 inch thick for all sizes greater than No. 0000 B. & S. gauge.

Copper-wire Table.—The table on pages 1034 and 1035 is abridged from one computed by the Committee on Units and Standards of the American Coppers of the Standards of the American Coppers of the Standards of the American Coppers of the Standards of the American Coppers of the Standards of the American Coppers of the Standards of the American Coppers of the Standards of the American Coppers of the Standards of the American Coppers of the Standards of the American Coppers of the Standards of the American Coppers of the Standards of the American Coppers of the Cop

can Institute of Electrical Engineers (Trans. Oct. 1893).

ELECTRIC TRANSMISSION, DIRECT CURRENTS.

Cross-section of Wire Required for a Given Current.-Let R = resistance of a given line of copper wire, in ohms: τ = "1 mil-foot of copper;

L = length of wire, in feet;

e = drop in voltage between the two ends;

= current, in amperes;

A = sectional area of wire, in circular mils;

then
$$I = \frac{e}{R}$$
; $R = \frac{e}{I}$; $R = r\frac{L}{A}$; whence $A = \frac{rIL}{e}$.

The value of r for soft copper wire at 75° F. is 10.505 international ohms. For ordinary drawn copper wire the value of 10.8 is commonly taken, cor-

For outliney drawn copies we the value of 10.18 commonly taken, the responding to a conductivity of 97.2 per cent.

For a circuit, going and return, the total length is 2L, and the formula becomes $A = 21.6IL + \epsilon$, Lhere being the distance from the point of supply to the point of delivery.

If E is the voltage at the generator and a the per cent of drop in the line, then e = Ea + 100, and $A = \frac{2160IL}{1000}$.

If
$$P$$
 = the power in watts, = EI , then $I = \frac{P}{E}$, and $A = \frac{2160PL}{aE^2}$. If P_k = the power in kilowatts, $A = e^{-\frac{1}{2}}$.

Gauges	ges.		Area,		Weight.	Ler	Length.	Resist	ance in Interi	Resistance in International Ohms	•
A. W. G. B. C. S. G.	B. W. G. Stubbs'.	eter, inches.	Circular mils.	Lbs. per Foot.	Lbs. per Ohm, at 20° C., 68° F.	Feet per Lb.	Ft. per Ohm,	Ohms per Lb. at 30° C., 68° F.	O. per ft., at 20° C., 68° F.	O. per ft., at 50° C., 122° F.	O. per ft., at 80° C., 176° F.
9000		99.	811,600	0.6406	13,090	1.561	20,440	0.00007639	0.00004893	0.00005467	0.00006068
	38	18	180,600	0.5468	12,420 0.538	1.899	17,450	0.0001048	0.00006732	0.00006404	0.00007097
8	:	0.4096	167,800	0.5080	886	1.969	16,210	0.0001215	0.00006170	0.00006898	0.00007640
8	8	98.0	144,400	0.4371	90.4	200	13,950	0.0001640	0.0000/170	0.00008011	0.00008878
3	•	0.340	115,600	0.3499	2,907	20.00	11,16	0.0002560	0.00008957	0.0001001	0.0001100
0		0.3840	105.500	0.3196	9,846	3.130	10,190	0.0009071	0.00009811	0.0001096	0.0001215
-	-	0.2883	90.00	0.2533	2, 9, 2, 9, 2, 9, 3, 9, 9, 3, 9, 9, 9, 9, 9, 9, 9, 9, 9, 9, 9, 9, 9,	8.671 8.947	280 280 280 280 280	0.0004883	0.0001130	0.0001382	0.0001532
•	001	0.2840	99,08	0.2441	966	4.096	7,790	0.0005258	0.0001284	0.0001434	0.0001589
e	5 0	0.5576	5,58 5,58 5,58 5,58	0.2021	1,316	4.925	6,479	0.0007661	0.0001560	0.0001743	0.0001932
•	*	0.2380	56,640	0.1715	0.886	5.832	5,471	0.001066	0.0001828	0.0002042	0.0002263
99	*	200	52,630 48,400	0.1593	0.019	6.276	5,084	0.001836	0.0001967	0.0002198	0.000%35
4	•	0.2043	41,740	0.1264	4.00	7.914	4.081 1.081	0.001963	0.0002480	0.0002771	0.0003071
,	•	0.2030	41,210	0.1247	2.96.5	8.017	8,880	0.003014	0.0002513	0.0002807	0.0003111
0		0.1819	83.8	0.1002	# 050 60 60 60 60 60 60 60 60 60 60 60 60 60	98.5	3,197	0.003128	0.0003128	0.0003496	0.0003873
	- 00	0.1650	22.23	0.08241	200.0	12.13	2,629	0.004615	0.0003808	0.0004249	0.0004709
•	•	0.1690	26.250	0.07946	201.5	12.58	8,536	0.004963	0.0003944	0.0004406	0.0004883
	•	0.1430	21,900	0.00030	96.2	15.08	8,110 9,110	0.007898	0.0004973	0.000556	0.0006158
•	2	0.1340	17,960	0.06435	94.26	18.40	1,734	0.01061	0.0005766	0.0006442	0 0007140
80	:	0 1985	16,510	0.04998	69.62	88	1,596	0.01255	0.0006271	0.0007007	0.0007765
۰	=	0.1200	13,090	0.03963	20.02	# 83 18 83	28.1	0.01895	0.0007908	0.000-835	0.0009791
• ;	2	0.1000	11,890	0.03596	16.0	27.81	1,147	0 08423	0.0008715	0.0009736	0.001079
2	2	0.1019	10,380	0.05143	8.8	25.25	7.12	0.04199	0.001147	0.001282	0.001420
=	:	0.09074	753.8	0.02493	19.88	40.18	200	0.06045	0.001257	0.001406	0.001567
2	#	0.08300	988,9	0.02085	13.67	8.8	# t-	0.07207	0.001503	0.00167	0.001861
3	91	0.07200	281.9	0.01569	7.867	. 25 25	200.1	0.1273	0.001997	0.00231	0.002473
S 1		0.07196	6,178	0.01568	7.840	3 5:3	200.1	0.1876	0.001999	0.00236	0.009476
7	2	0.06500	4,4 8,5	0.01279	5.219	28.19	200	0.1916 0.2028	0.002521	0.002817	0.003128
•	11	0.0680	8,364	0.01018	3.308	88	324.9	0.3043	0.003078	0.003439	0.008811
23		0.06707	2,257	0.009858	8.101	101 4	2.00	0.5128	0.003179	0.003508	0.003956
₹.	5 1	0000	20,00	0.007248	1.686	157.6	6.158	0.5933	0.004312	0.004818	0.005339

r Wires.—(Continued.
Coppe
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Warm, and
3001, W
es of Cool,
Resistance
s, and
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Weights,

Gan	Gauges.	Diam-	Area.	_	Weight.	IA	Length.	Resist	ance in Inter	Resistance in International Ohma	77
A. W. G. B. & S.	3. W. G. Stubbs:	-	Circular mils.	Lbs. per Foot.	Lbs. per Ohm, at 20° C., 68° F.	Feet per Lb.	Ft. per Ohm, at20°C,,68°F.	Ohms per Lb. at 20° C., 68° F.	Ohms per ft. oat 20° C.,	Ohms per ft. Ohms at 50 C., at 80 122° F.	Ohms per ft. at 80° C., 176° F.
12	91	3.04526	2,048	0.006200	1.236	161.3	197.8	0.8153	0.005055	0.005648	0.006259
•	4	0.010.0	1,624	0.004917	0.7713	203.4	156.9	1.296	0.006374	0.007122	0.00789
	8	0.03589	2,288	0.008890	0.4851	206.5	124.4	20.00	0.008038	0.008980	0.00995
	25	0.08900	188	0.003100	0.3086	329.6	98.80	3,269	0.01011	0.00	0.01050
8	1	0.03196	1,022	0.003092	0.3051	323.4	98.66	3.278	0.01014	0.01182	0.01255
=	1	0.02846	810.1	0 002452	0.1919	407.8	78.24	5.919	0.01278	0.01428	0.01583
8	23.	0.02800	784.0	0.002373	0.1797	511.4	69.05	8, 987	0.01321	0.01475	0.01630
	23	0.0250	625.0	0.001892	0.1142	528.6	60.36	8,756	0.01667	0.01861	0.02051
ន		0.00557	208.2	0.001542	0.07589	648.4	49.21	13.18	0.0%088	0.02271	0.02516
7	77	0.0220	25.0	0.001465	0.06849	817.6	20.00	90.95	0.02139	0.02290	0.02049
	25	0.0500	0.00	0.001211	0.04678	825.9	38.63	25.25	0.02588	0.02892	0.03205
	56	0.0180	324.0	0.000808	0.03069	1,020	31.29	88.	0.03196	0.03570	0.03957
3	8	0.01790	550.4	0.0009699	0.03002	1,031	30.30	35	0.08231	0.03610	0.04001
*	ā	0.01594	254.1	0.0007692	0.01888	1,300	24.54	52.97	0.04075	0.04552	0.05045
	1	0.0142	201.5	0.0006100	0.01187	1,639	19.46	35 35 35 36 36 36 36 36 36 36 36 36 36 36 36 36	0.05138	0.06740	0.06362
	88	0.0140	0.091	0.000933	0.01123	1,055	16.93	10.5	0.00283	0.00002	0.06541
25	3	0.01264	159.8	0.0004837	0.007466	2,067	15.43	133.9	0.06479	0.000	0.0808
	98	0.0130	14.0	0.0004359	0.006062	2,294	18.91	165.0	0.07190	0.08033	0.0890
25		0.01126	128.7	0.0003836	0.004696	2,607	12.24	213.0	0.08170	0.00128	0.1012
	5	0.0100	90.0	0.000007	0.002034	3,304	9.658	342.0	0.1035	0.1161	0.12/0
	33	0.0000	81.0	0.0002452	0.001918	4,078	7.823	521.3	0.1278	0.1428	0.1583
_		0.008928	29.70	0.000%13	0.001857	4,145	7.698	538.4	0.1299	0.1451	0.1608
	23	0.0080	2.5	0.0001937	0.001197	5,162	6.181	856.9	0.1618	0.1807	0.2003
123		0.007080	50.13	0.0001517	0.0007346	6,591	4.841	1.361	0.9066	2808	0.2020
_	34	0.0070	69.0	0.0001483	0.0007019	6,742	4.733	1,425	0 2113	0.2361	0.2616
*		0.006305	89.75	0.0001203	0.0004620	8,311	3 839	2,165	0.2805	9.2010	0.3225
0 4	20	0.00000	81.02 95.0	0.00008543	0.0002900	12 910	3.045	5,451	0.3294	0.3669	0.4067
35	3	0.004453	19.83	0.0000000	0.0001149	16.660	1.915	8,709	0.5152	0.1027	0.0129
	36	0.0040	16.	0.00004843	0.00007484	20,650	1.545	13,360	0.6471	0.7230	6.8011
80		0.003965	15.78	0.00004759	0.00007210	21,010	1.519	13,870	0.6585	0.7357	9.8154
-		0.003531	12.47	0.00003774	0.00004545	26,500	1 204	22,000	200	0.9277	1.028

If $L_m =$ the distance in miles, and A_c the area in circular inches. $Ac = 6405 \ PkLm + aF^2$. If As = area in square inches $As = 5030 \ PkLm + aE^2$. When the area in circular mils has been determined by either of these formulæ reference should be made to the table of Allowable Capacity of Wires, to see if the calculated size is sufficient to avoid overheating. For all interior wiring the rules of the National Board of Fire Underwriters should

all interior wiring the rules of the National Board of Fire Underwriters should be followed. See Appendix to Vol. II of Crecker's Electric Lighting. Weight of Copper for a Given Power.—Taking the weight of a mil-foot of copper at .000003027 lb., the weight of copper in a circuit of length 2L and cross-section A, in circ, mils, is 0.000006054LA lbs., = W. Substituting for A its value $2160PL + aE^2$ we have

 $W = 0.0130766PL^2 \div aE^2;$ P in watts, L in ft. $W = 13.0766 P_k L^2 + aE^2$: P_k in kilowatts, L in ft.

 $W = 364.556.000 PkL^{2}m + aE^{2}$; Pk in kilowatts, Lm in miles.

The weight of copper required varies directly as the power transmitted; inversely as the percentage of drop or loss; directly as the square of the distance; and inversely as the square of the voltage.

From the last formula the following table has been calculated.

WEIGHT OF COPPER WIRE TO CARRY 1000 KILOWATTS WITH 10% LOSS.

Distance in miles.	1	5	10	20	50	100
Volts.			Weigh	t in lbs.		
500 1,000	145,822 36,456	3,645,560 911,390	3,645,560	2 0 4 5 500		
2,000 5,000 10,000	9,114 1,458 365	227,848 36,456 9,114	911,390 145,822 36,456	3,645,560 593,290 145,822	3,645,560 911,390	3,645,56
20,000 40,000 60,000	91	2,278 570	9,114 2,278 1,013	36,456 9,114 4,051	227,848 56,962 25,316	911,39 227,84 101,26

In calculating the distance, an addition of about 5 per cent should be made for sag of the wires.

Short-circuiting.—From the law $I = \frac{E}{R}$ it is seen that with any pressure E, the current I will become very great if R is made very small. short-circuiting the resistance becomes small and the current therefore great. Hence the dangers of short-circuiting a current.

Economy of Electric Transmission.—Lord Kelvin's rule for

the most economical section of conductor is that for which the annual interest on capital outlay is equal to the annual cost of energy wasted.

Tables have been compiled by Professor Forbes and others in accordance with modifications of this rule. For a given entering horse-power the questions of the conductor

with modifications of this rule. For a given entering norse-power the ques-tion is merely one as to what current density, or how many amperes per square inch of conductor, should be employed. Kelvin's rule gives about 393 amperes per square inch, and Professor Forbes's tables give a current density of about 380 amperes per square inch as most economical. Bell (Electric Transmission of Power) shows that while Kelvin's rule cor-rectly indicates the condition of minimum cost in transmission for a given

rectry indicates the control of the first state of the great control of the great current and line, it omits many practical considerations and is inapplicable to most power transmission work. Each plant has to be considered on its merits and very various conditions are likely to determine the line loss in different cases. Several cases are cited by Bell to show that neither Kelvin's law nor any modification of it is a safe guide in determining the proper

allowance for loss of energy in the line.

Wire Tables.—The tables on the following page show the relation between load, distance, and "drop" or loss by voltage in a two-wire circuit of any standard size of wire. The tables are based on the formula

(21.6IL) + A = Drop in volts

I=current in amperes, L=distance in feet from point of supply to point of delivery. The factors I and L are combined in the table, in the compound factor "ampere feet."

WIRE TABLE—RELATION BETWEEN LOAD, DISTANCE, LOSS, AND SIZE OF CONDUCTOR.

Table I.-110-volt and 220-volt Two-Wire Circuits.

Note.—The numbers in the body of the tables are Ampere-Feet; i.e., Amperes × Distance (length of one wire) in feet. See examples on next page.

	Sizes; Gauge.						e Rated the Deli			Power
110 V.	220 V.	1	11	2	3	4	5	6	8	10
	0000 000	17,080 13,550	25,620 20,825	84,160 27,100	51,240 40,650	68,320 54,200	67,750	102,480	136,640	
000	0 1		16,125 12,780							107,500 85,200
00 0 1 2 8	2 3 4 5 6	6,750 5,360 4,250 3,370 2,670	6,375 5,055	10,720 8,500 6,740	20,280 16,080 12,750 10,110 8,010	21,440 17,000 13,480	26,800 21,250 16,850	32,160 25,500 20,220	42,880 34,000 26,960	53,600 42,500 33,700
4 5 6 7 8	7 8 9 10	2,120 1,680 1,330 1,055 838	3,180 2,520 1,995	4,240 3,360 2,660	5,040 3,990 3,165	6,720 5,320 4,220	10,600 8,400 6,650 5,275	12,720 10,800 7,980 6,330	13,440 10,640 8,440	16,800 13,300 10,550
9 10 11 12 14	12 18 14	665 527 418 332 209	790 627	1,330 1,054 836 665 418	1,580 1,254 997	2,108	2,635 2,090 1,660	3,160 2,508 1,995	4,215 3,344	5,270 4,180 3,325

Table 11.-500, 1000, and 2000 Volt Circuits.

	Wire Siz & S. G		Line L Power	oss in P Loss in	ercenta Percen	ge of th tage of	e Rated the Deli	Voltag ivered I	e; and Power.
500 V.	1000 V.	2000 V.	1	11	2	21	3	4	5
	0000	0	97,960						489,800
	900	1	77,690						388,450
	00	2	61,620						308,100
0000	0	3	48,880						244,400
000	1	4	38,750	58,125	77,500	96,875	116,250	155,000	193,750
00	2	5	30,760	46,140	61,520	76,900	92.280	123.040	153,800
ő	3	6	24,370		48,740				121,850
ĭ	2 3 4 5 6	6 7	19,820	28,980					
2	5	Ŕ	15,320	22,980					
2 3	6	8 9	12,150	18,225			36,450		
4	7	10	9.640	14,460	19,280	24,100	28,920	38,560	48,200
4 5		iĭ	7,640	11,460				30,560	
6	8	12	6,060	9,090					
ž	10	13	4,805	7,207			14,415	19,220	
7 8	iĭ	14	8,810	5,715					
9	12		8,020	4.530	6,040	7,550	9,060	12,080	15,100
10	13	• • •	2,395	3,592				9,580	
11	14		1,900	2,850					
12	12		1,510	2,265				6,040	7,55
14	• • •	٠٠.	950	1,425	1,900	2,375			4,7
14	•••	• • •	800	1,420	1,800	2,010	2,000	0,000	±,4'

Examples in the Use of the Wire Tables. — 1. Required the maximum load in amperes at 220 volts that can be carried 95 feet by No. 6

maximum load in amperes at 220 voits that can be carried so feet by 10. we wire without exceeding 11% drop.

Find No. 6 in the 220-voit column of Table I; opposite this in the 11% column is the number 4005, which is the ampere-feet. Dividing this by the required distance (95 feet), gives the load, 42.15 amperes.

Example 2. A 500-voit line is to carry 100 amperes 600 feet with a drop not exceeding 5%; what size of wire will be required?

The ampere-feet will be 100×600 = 60,000. Referring to the 5% column of the property

of Table II, the nearest number of ampere-feet is 60,750, which is opposite No. 3 wire in the 500-volt column.

These tables also show the percentage of the power delivered to a line that is lost in non-inductive alternating-current circuits. Such circuits are obtained when the load consists of incandescent lamps and the circuit wires lie only an inch or two apart, as in conduit wiring.

Efficiency of Long-distance Transmission. (F. R. Hart, Power, Feb. 1892.)—The mechanical efficiency of a system is the ratio of the power delivered to the dynamo-electric machines at one end of the line to the power delivered by the electric motors at the distant end. The commercial efficiency of a dynamo or motor varies with its load. Under the most favorable conditions we must expect a loss of say % in the dynamo and % in the motor. The loss in transmission, due to fall in electrical pressures of the live sure or "drop" in the line, is governed by the size of the wires, the other conditions remaining the same. For a long-distance transmission plant this will vary from 5% upwards. With a loss of 5% in the line the total efficiency of transmission will be slightly under 7%. With a loss of 10% in the line it will be slightly under 75%. We may call 80% the practical limit of the efficiency with the apparatus of to-day. The methods for long-distance transmission may be divided into three general classes: (1) continuous current: (2) alternating current; and (3) regenerating or "motor-dynamo" systems. systems.

There are many factors which govern the selection of a system. For each problem considered there will be found certain fixed and certain unfixed conditions. In general the fixed factors are: (1) capacity of source of power; (3) cost of power at source; (3) cost of power by other means at point of delivery; (4) danger considerations at motors; (5) operating conditions; (6) construction conditions (length of line, character of country, etc.). The partly fixed conditions are: (7) power which must be delivered, i.e., the efficiency of the system; (8) size and number of delivery units. The variable party macu conditions are: (7) power which must be delivered, i.e., the emiciency of the system; (8) size and number of delivery units. The variable conditions are: (9) initial voltage; (10) pounds of copper on line; (11) original cost of all apparatus and construction: (12) expenses, operating (fixed charges, interest, depreciation, taxes, insurance, etc.); (13) liability of trouble and stoppages; (14) danger at station and on line; (15) convenience in operating charges; ating, making changes, extensions, etc.

The relative advantages of different systems vary with each particular

transmission problem, but in a general way may be tabulated as below:

	System.	Advantages.	Disadvantages.		
_	Low voltage.	Safety, simplicity.	Expense for copper.		
	2-wire High voltage.	Economy, simplicity.	Danger; difficulty of building machines.		
Continuous	8-wire.	Low voltage on machines and saving in copper.	Not saving enough in copper for long dis-		
ర	Multiple-wire.	Low voltage at machines and saving in copper.	tonone Monagaity for		
_	Single phase.	Economy of copper.	Cannot start under load. Low efficiency.		
ternating.	Multiphase.	Economy of copper, syn- chronous speed unnec- essary; applicable to very long distances.	Requires more than two wires.		
43	Motor-dynamo.	High-voltage transmis- sion. Low-voltage de- livery.	Expensive. Low efficiency.		

TABLE OF ELECTRICAL HORSE-POWERS.

Formula: $\frac{\text{Volts} \times \text{Amperes}}{746} = \text{H.P.}$, or 1 volt-ampere = .0013405 H.P.

Read amperes at top and volts at side, or vice versa.

olts.	Volts or Amperes.													
Amperes or Volts.	1	10	20	30	40	50	60	70	80	90	100	110	120	
1 2 3	.00134 .00968 .00402	.0184 .0968 .0402	.0268 .0536 .0604	.0402 .0804 .1206	.0536 .1072 .1609	.0570 .1341 .2011	.0804 .1609 .2413	.0938 .1877 .2815	.1072 .2145 .3217	.1206 .2418 .3619	.1341 .2681 .4022	.1475 .2949 .4424	.1609 .3217 .4826	
5	.00536 .00670 .00804	.0636	.1072 .1341	.1609 .2011	.2145 .2681	.3351	.3217 .4022	.3753 .4692	.4290 .5362 .6434	.6032	.5362 .6703 .8043	.7373	.6434 .8043	
6 7 8	.00938	.0804 .0938 .1072	.1609 .1877 .2145	.2413 .2815 .3217	.3217 .3.9.3 .4290	.4022 .4692 .5362	.4826 .5630 .6434	.5630 .6568 .7507	.7507 .8579	.7239 .8445 .9652	.9384 1.072	.8847 1.032 1.180	.9652 1.126 1.287	
10	.01206	.1206	.2413 .2681	.3619 .4022	.4826 .5362	.6032 .6708	.7239 .8043	.8445 .9383	1.072	1.086	1.206	1.327 1.475	1.448	
11 12 13	.01475 .01609 .01743	.1475 .1609 .1743	.2949 .3217 .3485	.4424 .4826 .5228	.5898 .6434 .6970	.7373 .8043 .8713	.8847 .9652 1.046	1.032 1.126 1.220	1.180 1.287 1.394	1.327 1.448 1.568	1.475 1.609 1.743	1.628 1.769 1.917	1.769 1.930 2.091	
14 15	.01877	.1877 ,2011	.3753 .4022	.6032	.8043		1.126 1.206	1.314 1.408	1.501	1.689 1.810	1.877 2.011	2.064 2.213	2.258 2.413	
16 17 18 19	.02145 .02279 .02413 .02547	.2145 .2279 .2413 .2547	.4290 .4558 .4826 .5094	.6837 .7239	1.019	1.206	1.287 1.367 1.448 1.528	1.501 1.595 1.689 1.783	1.716 1.823 1.930 2.037	1.930 2.051 2.172 2.293	2.145 2.279 2.413 2.547	2.359 2.507 2.654 2.801	2.574 2.785 2.895 3.056	
20	.02681	,2681 ,2815	.5630	8445	1.126	1.340	1.609	1.877	2.145 2.252	2.413	2.681 2.815	2.949 3.097	3.217 3.378	
23 24 25	.02949 .03083 .03217 .03351	.2949 .3083 .3217 .3351	.5898 .6166 .6434 .6703	.9652	1.233	1.475 1.548 1.609 1.676	1.769 1.850 1.930 2.011	2.064 2.158 2.252 2.346	2.359 2.467 2.574 2.681	2.654 2.775 2.895 3.016	2.949 3.083 3.\$17 3.351	3.244 3.391 3.539 3.686	3.539 3.700 3.861 4.022	
20 27	.03485	.3485 3619	.6971	1.046	1 394	1.743 1.810	2.091 2.172	2.440 2.534	2.788 2.895	3.137 3.257	3.485 3.619	3.834 3.981	4.183	
28 29 30	.03753 .03887 .04022	.3753 .3887 .4023	.7507 .7775 .8043	1.126	1.448 1.501 1.555 1.609	1.877 1.944 2.011	2.252 2.332 2.413	2.627 2.721 2.815	3.003 3.110 3.217	3.378 3.499 3.619	3.753 3.887 4.022	4.129 4.276 4.424	4.504 4.665 4.826	
31 32	.04156	4156	.8311 .8579	1.947	1.662	2.078 2.145	2.493 2.574	2.909	3.394 3.432	3.740 3.861	4.156	4.571	4.987	
33 34	.04434 .04558 .04692	.4568	.8847 .9118	1.367	1.769 1.823 1.877	2.212 2.279	2.654 2.735	3.097	3,539 3,646 3,753	3.986 4.102	4.424	4.719 4.866 5.013	5.308 5.469	
35 49 45	.05362		1.079 1.206	1.408 1.609 1.810	2.145 2.413	2.681 3.016	3.217 3.619	3.284 3.753 4.223	4.290	4.828 4.825 5.439	4.692 5.363 6.032	5.161 5.898 6.635	5.630 6.434 7.239	
50 55	.06703	. 6703	1.341	2.011	2.681	3.351 3.686	4.022	4.692	5.362 5.898	6.032	6.703 7.873	7.373 8.110	8.043 8.847	
60 65 70	08043	.8043 .8713	1.609	2.413 2.614	3.917 3.485	4.029	4.826 5.228	5.630	6.434	7.239 7.842	8.043 8.713	8.047 9.584	9.657 10.46	
75 80	.10064 .10784	1.005	1.877 2.011	2.815 3.016	4.021	4.692 5.027	5.630 6.032 6.434	7.037	7.507 8.043	8.445 9.048	9.384 10.05	10.32 11.06	11.26 12.06	
85 90	.11394	1.072 1.139 1.206	2.145 2.279 2.413	3.217 3.418 3.619	4.290 4.558 4.826	5.362 5.697 6.032	6.836 7.239	7.507 7.976 8.445	8.579 9.115 9.652	9.652 10.26 10.86	10.72 11.39 12.06	11.80 12.53 13.27	12.87 13.67 14.48	
95 100	.12735 .13406	1.273 1.341	2.547 2.681	8.820 4.022	5.094 5. 36 2	6.367 6.703	7.641 8.043	8.91 <u>4</u> 9.38 <u>4</u>	10.18 10.72	11.46 12.06	12.73 13.41	14.01 14.75	15.28 16.09	
200 300 400	.95810 .40215 .58690	2.681 4.093 5.362	5.362 8.043 10.72	8.043 12.06 16.09	10.72 16.09 21.45	13.41 20.11 26.81	16.09 24.13 32.17	18.77 28.15 37.53	21.45 32.17 42.90	24.13 36.19 48.26	26.81 40.22 53.62	29.49 44.24 58.98	32.17 48.26 64.34	
500 600		6.703	13.41 16.09	20.11 24.13	26.81 32.17	33.51 40.22	40.22 48.26	46.92 56.30	53.62 64.34	60.32 72.39	67.03 80.43	73.78 88.47	80.43 96.53	
700 800	.93835 1.0724	9.384 10.72	18.77 21.45	28.15 32.17	37.53 49.90	46.92 53.62	56.30 64.34	65.68 75.07	75.07 85.79	84.45 96.52	93.84 107.2	103.2 118.0	112.6 128.7	
800 900 1,000 2,000	1.2065 1.3405 2.6810	12.06 13.41 26.81	24.18 26.81 53.68	36.19 40.22 80.43	48.96 53.62 107.2	60.82 67.03 134.1	72.39 80.43 160.9	84.45 93.84 187.7	96.53 107.2 214.5	108.6 120.6 241.3	120.6 134.1 268.1	132.7 147.5 294.9	144.8 160.9 321.7	
8,000 4,000	4.0215 5.3690	40.22 53.62	80.43 107.2	120.6 160.9	160.9 214.5	201.1 268.1	241.3 321.7	281.5 375.3	321.7 429.0	361.9 482.6	402.2 536.2	442.4 589.8	482.6 643.4	
5,000 6,000 7,000	6.7025 8.0430 9.3835	67.63 80.43 93.84	134.1 160.9 187.7	201.1 241.3 281.5	268.1 331.7 375.3	335.1 402.2 469.2	402.2 488.6 563.0	469.2 563.0 656.8	536.8 643.4 750.7	603.2 723.9 844.5	670.3 804.3 938.4	737.3 884.7 1032	804.3 965.9 1196	
8.000	10.724 18.065	107.2 120.6	214.5 241.3	391.7 361.9	429.0 482.6	536.2 603.2	643.4 793.9	750.7 844.5	857.9 965.2	965.2 1086	1072 1206	1180 1327	1987 1448	
0,000	18.405	184.1	268.1	402.2	536.2	670.3	804.3		1072	1206	1841	1475	1609	

Cost of Copper for Long-distance Transmission. (Westinghouse El. & Mfg. Co.)

COST OF COPPER REQUIRED FOR THE DELIVERY OF ONE MECHANICAL HORSE-FOWER AT MOTOR SHAPT WITH 1000, 2000, 2000, 2000, 5000, and 10,000 VOILS AT MOTOR TERMINALS, OR AT TERMINALS OF LOWERING TRANSFORMERS. Loss of energy in conductors (drop) equals 20%. Motor efficiency, 90%. Length of conductor per mile of single distance, 11,000 ft., to allow for sag. Cost of copper taken at 16 cents per pound.

Miles.	1000 v.	2000 v.	3000 v.	4000 ∀.	5000 v.	10,000 v.
1	\$2.08	\$0.52	\$0.23	\$0.13	\$0.08	\$0.02
2	8.33	2.08	0.93	0.52	0.33	0.08
2	18.70	4.68	2.08	1.17	0.75	0.19
4	33.20	8.32	3.70	2.08	1.33	0.23
5	52.05	13.00	5.78	3.25	2.08	0.52
6	74.90	18.70	8.32	4.68	3.00	0.75
7	102.00	25.50	11.30	6.37	4.08	1.02
ė	133.25	33.30	14.80	8.32	5.33	1.33
8 9	168.60	42.20	18.70	10.50	6.74	
10						1.69
	208.19	52.05	23.14	13.01	8.33	2.08
11	251.90	63.00	28.00	15.75	10.08	2.52
12	299.80	75.00	88.80	18.70	12.00	3.00
13	852.00	88.00	39.00	22.00	14.08	3.52
14	408.00	102.00	45.30	25.50	16.32	4.08
15	468.00	117.00	52.00	29.25	18.72	4.68
16	533.00	133.00	59.00	23.30	21.32	5.33
17	600.00	150.00	67.00	37.60	24.00	6.00
18	675.00	109.00	75.00	42.20	27.00	6.75
19	750.00	188.00	83.50	47.00	30.00	7.50
20	833.00	208.00	92.60	52.00	33.32	8.33

COST OF COPPER REQUIRED TO DELIVER ONE MECHANICAL HORSE-POWER AT MOTOR-SHAPT WITH VARTING PERCENTAGES OF LOSS IN CONDUCTORS, UPON THE ASSUMPTION THAT THE POTENTIAL AT MOTOR TERMINALS IS IN EACH CASE 3000 VOLTS.

Motor efficiency, 90%. Cost of copper equals 16 cents per pound. Length of conductor per mile of single distance, 11,000 ft., to allow for sag.

Miles.	10%	15%	20%	25%	30%
1	\$0.52	\$0.38	\$0.23	\$0.17	\$0.18
2	2.08	1.31	0.98	0.69	0.54
3	4.68	2.95	2.08	1.55	1.21
4	8. 32	5.25	3.70	2.77	2.15
5	13.00	8.20	5.78	4.83	3.37
6	18.70	11.75	8.32	6.23	4.88
2 3 4 5 6 7 8 9	25.50	16.00	11.30	8.45	6.60
Ř	33.30	21.00	14.80	11.00	8.60
ŏ	42.20	26.60	18.75	14.00	10.90
10	52.05	32.78	23.14	17.31	13.50
îĭ	63.00	39.75	28.00	21.00	16.30
12	75.00	47.20	33.30	24.90	19.40
18	88.00	55.30	39.00	29.20	22.80
14	102.00	64.20	45.30	33.90	26.40
15	117.00	78.75	52.00	28.90	20.90 20.30
16	133.00	88.80	89.00	44.30	
17	150.00				84.50
18		94.75	67.00	50.00	39.00
	169.00	106.00	75.00	\$ 6. 30	43.80
19	188.00	118.00	83.50	62.50	48.70
20	208.00	131.00	92.60	69.25	54.0

Systems of Electrical Distribution in Common Une.

I. DIRECT CURRENT.

A. Constant Potential.
110 to 125 and 220 to 250 Volts.—Distances less than, say, 1500

For incandescent lamps.
For arc-lamps, usually 2 in series.
For motors of moderate sizes.
200 to 250 and 440 Volts, 3-wire.—Distances less than, say, 5000 feet.

For incandescent lamps.
For arc-lamps, usually 2 in series on each branch.
For motors 110 or 220 volts, usually 220 volts.

500 Volts.—Distances less than, say, 20,000 feet. Incidentally for arc-lamps, usually 10 in series. For motors, stationary and street-car.

B. Constant Current.
Usually 5, 61, or 91 amperes, the volts increasing to several thousand, as demanded, for arc-lamps.

II. ALTERNATING CURRENT. A. Constant Potential.

For incandescent lamps, are-lamps, and motors.

Ployphase Systems.

For are and incandescent lamps, motors, and rotary converters for giving direct current.

Ployphase—2 and 3-phase—high tension (25,000 volts and over), for long-distance transmission; transformed by step-up and step-down transformers.

B. Constant Current.

Usually 5 to 6.6 amperes. For arc-lamps.

References on Power Distribution.—Abbott, Electric Transmission of Energy; Bell, Electric Power Transmission; Cushing, Standard Wiring for Incandescent Light and Power; Crocker, Electric Lighting, 2 vols.; Poole, Electric Wiring.

ELECTRIC BAILWAYS.

Space will not admit of a proper treatment of this subject in this work. Consult Crosby and Bell, The Electric Railway in Theory and Practice; Fairchild, Street Railways; Marrill, Reference Book of Tables and Formules for Street Railway Engineers; Bell. Electric Transmission of Power; Dawson, Engineering and Electric Traction Pocket-book.

ELECTRIC LIGHTING.

Are Lights.—Direct-current open are: usually require about 10 amperes at 45 volts. or 450 watts. The range of voltage is from 42 to 52 for ordinary ares. The most satisfactory light is given by 45 to 47 volts. Search-light projectors use from 50 to 100 amperes at 48 to 53 volts. The candle-power of an arc light varies according to the direction in which the light is measured; thus we have, 1, mean horizontal candle-power. Which is usually found at an angle below the horizontal; 3. mean spherical candle-power; 4, mean hemispherical candle-power.

power, below the horizontal.

The nominal candle-power of an arc lamp is an arbitrary figure. A 450-watt arc is commonly called 2000 c.-p. and a 300-watt arc is 1200 c.-p. These figures greatly exceed the true candle-power. Carhart found with an arc of 10 amperes and 45 volts a maximum c.-p. of 450, but with the same watts 8.4 amperes, and 54 volts he obtained 900 c.-p. Blondel however, found the c.-p. a maximum usually below 45 volts. Crocker explains the discrepancy as probably due to a difference in size and quality of the carbons.

Current for are lighting is furnished either on the series, constant current, or on the parallel constant potential system. In the latter the voltage of the circuit is usually 110 and two lamps are connected in series. In currents with higher voltages more lamps are used in series; for instance

10 with a 500-volt circuit.

Enclosed Arcs — Direct current enclosed ares consume about 5 amperes at 89 volts. or 400 watts. The chief advantages of the enclosed arcs, on constant potential circuits are the long life of the carbons, 100 to 150 hours, as compared with 8 to 10 hours for open ares; simplicity of construction, absence of sparks, agreeable quality and better distribution of

Alternating-current enclosed arcs usually take a current of 6 amperes at 70 or 75 voits. With 70 volts and 6 amperes, in a 104-volt circuit, the apparent watts at the lamp terminals are 625 and at the are 420, the actual watts being 445 and 390 respectively. The watts consumed in the inductive

resistance average 35 to 45.

Incandescent Lamps.—Candle-power of nominal 16 c.p. 110-volt . lamp:

Mean horizontal 15.7 to 16.6 Mean spherical 12.7 to 13.8 Mean hemispherical 14.0 to 14.6

Mean within 30° from tip 7.9 to 10.9
Ordinary lamps take from 3 to 4 watts per candle-power. A 16 candle-power lamp using 3.5 watts per candle-power or 56 watts at 110 volts takes

power lamp using 3.5 watts per candle-power or 56 watts at 110 volts takes a current of 56 + 110 = 0.51 ampere. For a given efficiency or watts per candle-power the current and the power increase directly as the candle-power. An ordinary lamp taking 56 watts, 13 lamps take 1 H.P. of electrical energy. or 18 lamps 1.008 kilowatts.

Variation in Candle-Power, Efficiency, and Life.—The following table shows the variation in candle-power, etc., of the General Electric Co.'s standard 100 to 125 volts, 3.1 and 3.5 watt lamps due to variation in voltage supplied to them. It will be seen that if a 3.1 watt lamp is run at 10 per cent below its normal voltage, it may have over 9 times as long a life, but it will give only 53 per cent of its normal lighting power, and the light will cost 50 per cent more in energy per candle-power. If it is run at 6 per cent above its normal voltage, it will give 37 per cent more light, will take nearly 20 per cent less energy for equal light power, but it will have less than one third of its normal life.

Per cent of Normal Voltage.	Per cent of Normal Can- dle-power.	Efficiency in watts per Candle, 3.1 watt Lamp.	Relative Life. 3.1 watt Lamp.	Efficiency in watts per Candle, 3.5 watts.	Relative Life. 3.5 watts.
90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 106	53 57 61 65 69.5 74 79 84 89 94.5 100 112 112 124 130	4.65 4.44 4.24 4.10 3.90 3.75 3.60 3.45 3.34 3.22 3.10 2.99 2.90 2.80 2.70 2.62 2.54	9.41 7.16 5.55 4.35 3.45 2.75 2.20 1.79 1.46 1.21 1.00 .818 .681 .682 .452 .374	5.36 5.09 4.85 4.63 4.44 4.09 3.93 3.78 3.64 3.38 3.216 3.05 2.95 2.85	3.94 3.10 2.47 1.95 1.26 1.00 .84 .68 .47 .39

The candle-power of a lamp falls off with its length of life, so that during the latter half of its life it has only 60 per cent or 70 per cent of its rated candle-power, and the watts per candle-power are increased 60 per cent or 70 per cent. After a lamp has burned for 500 or 600 hours it is more economical to break it and supply a new one if the price of electrical energy is that usually charged by central stations.

Specifications for Lamps. (Crocker.)—The initial candle-power of any lamp at the rated voltage should not be more than 9 per cent above or below the value called for. The average candle-power of a lot should be within 6 per cent of the rated value. The standard efficiencies are 3.1, 3.5, and 4 watts per candle-power. Each lamp at rated voltage should take within 6 per cent of the watts specified, and the average for the lot should be within 4 per cent. The useful life of a lamp is the time it will burn before falling to a certain candle-power, say 80 per cent of its initial candle-power. For 3.1 watt lamps the useful life is about 400 to 450 hours. for 3.5 watt lamps about 800, and 4 watt lamps about 1600 hours.

Special Lamps.—The ordinary 16 c.-p. 110-volt is the standard for interior lighting. Thousands of varieties of lamps for different voltages and candle-power are made for special purposes, from the primary lamp, supplied by primary batteries using three volts and about 1 ampere and giving 14 c.-p., and the 34 c.-p. bicycle lamp, 4 volts and 0.5 ampere, to lamps of 100 c.p. at 220 volts. Series lamps of 1 c.-p. are used in illuminating signs, 34 ampere and 12.5 to 15 volts, eight lamps being used on a 110-volt circuit. Standard sizes for different voltages, 50, 110, or 220, are 8, 16,

24, 32, 50, and 100 c-p.

Nernst Lamp.—A form of incandescent lamp originated by Dr.
Walther Nernst, of Göttingen, is being developed in this country by the
Nernst Lamp Company, Pittsburg, Pa. It depends for its operation upon
the peculiar property of certain rare earths, such as yttrium, thorium, zirconium, etc., of becoming electrical conductors when heated to a certain
temperature; when cold, these oxides are non-conductors. The lamp comprises a "glower" composed of rare earths mixed with a binding material
and pressed into a small rod; a heater for bringing the glower up to the conducting temperature; an automatic cut-out for disconnecting the heater
when the glower lights up, and a "ballast" consisting of a small resistance
coil of wire having a positive temperature-resistance coefficient. The ballast is connected in series with the glower; its presence is required to compensate the negative temperature-resistance coefficient of the glower; with-

out the ballast, the resistance of the glower would become lower and lower as its temperature rose, until the flow of current through it would destroy it. Fig. 171a shows the elementary circuits of a simple Nernst lamp. The cut-out is an electromagnet connected in series with the glower. When current begins to flow through the glower, the magnet pulls up the armature lying across the contacts of the cut-out, thereby cutting out the heater. The beater is a coil of fine wire either located very near the glower or encircling it. The glower is from 1/32 to 1/16 inch in diameter and about 1 inch long.

The material of the glower is an electrolyte, so that this type of lamp is not well adapted for operation on direct-current circuits because of the wasting away at the positive end and the deposition of material at the nega-

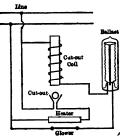


Fig. 171a.

The lamps are made with one glower, or with two, three, or six glowers connected in parallel, and for operation on 100 to 120 and 200 to 240 volt circuits.

RERCTRIC WELDING.

The apparatus most generally used consists of an alternating-current dynamo, feeding a comparatively high-potential current to the primary coil of an induction-coil or transformer, the secondary of which is made so large in section and so short in length as to supply to the work currents not exceeding two or three volts, and of very large volume or rate of flow. The welding clamps are attached to the secondary terminals. Other forms of apparatus, such as dynamos constructed to yield alternating currents direct from the armature to the welding-clamps, are used to a limited

The conductivity for heat of the metal to be welded has a decided influence on the heating, and in welding from its comparatively low heat conduction assists the work materially. (See papers by Sir F. Bramwell, Proc. Inst. C. E., part iv., vol. cii. p. 1; and Elihu Thomson, Trans. A. L. M. E., xiz.

Fred. P. Royce, fron Age, Nov. 28, 1892, gives the following figures showing the amount of power required to weld axles and tires;

AXLE-WELDING.

	econds.
1-inch round axle requires 25 H.P. for	45
1-inch square axle requires 80 H.P. for	48
114-inch round axle requires \$5 H.P. for	60
114-inch square axle requires 40 H.P. for	70
9-inch round axle requires 75 H.P. for	95
9-inch square axie requires 90 H.P. for	100

The slightly increased time and power required for welding the square axie is not only due to the extra metal in it, but in part to the care which it is best to use to secure a perfect alignment.

TIRE-WELDING.

	Second
$1 \times 8/16$ -inch tire requires 11 H.P. for	. 15
11/2 × 86-inch tire requires 28 H.P. for	. 26
112 2 \$6-inch tire requires 80 H.P. for	. 80
112 × %-inch tire requires 20 H.P. for	. 40
8 x 14-inch tire requires 29 H.P. for	. 85
2 × 3/4-inch tire requires 42 H.P. for	. 20

The time above given for welding is of course that required for the actual application of the current only, and does not include that consumed by placing the axies or tires in the machine, the removal of the upset and other finishing processes. From the data thus submitted, the cost of welding can be readily figured for any locality where the price of fuel and cost of labor are known.

In almost all cases the cost of the fuel used under the boilers for produc-

In almost all cases the cost of the fuel used under the boilers for producing power for electric welding is practically the same as the cost of fuel used in forges for the same amount of work, taking into consideration the difference in price of fuel used in either case. Prof. A. B. W. Kennedy found that 24-inch fron tubes 14 inch thick were welded in 61 seconds, the net horse-power required at this speed being 33.4 (say 33 indicated horse-power) per square inch of section. Brass tubing required 12 net horse-power, About 60 total indicated horse-power would be required for the welding of angle-irons $3\times3\times16$ inch in from two to three minutes. Copper requires about 80 horse-power per square inch of section, and an inch bar can be welded in 25 seconds. It takes about 90 seconds to weld a steel bar 2 inches in diameter.

ELECTRIC HEATERS.

Wherever a comparatively small amount of heat is desired to be automatically and uniformly maintained, and started or stopped on the instant without waste, there is the province of the electric heater.

The elementary form of heater is some form of resistance, such as coils of thin wire introduced into an electric circuit and surrounded with a substance, which will permit the conduction and radiation of heat, and at the

same time serve to electrically insulate the resistance.

This resistance should be proportional to the electro-motive force of the current used and to the equation of Joule's law:

$H = IR^2t \times 0.24$.

where I is the current in amperes; R, the resistance in ohms; t, the time in seconds; and H, the heat in gram-centigrade units. Since the resistance of metals increases as their temperature increases, a

since the resistance of metals increases as their temperature increases, a thin wire heated by current passing through it will resist more, and grow hotter and hotter until its rate of loss of heat by conduction and radiation equals the rate at which heat is supplied by the current. In a short wire before heat enough can be dispelled for commercial purposes, fusion will begin; and in electric heaters it is necessary to use either long lengths of thin wire, or carbon, which alone of all conductors resists fusion. In the metaltic of heaters colls of this wire are used accountable conducted. majority of heaters, coils of thin wire are used, separately embedded in some substance of poor electrical but good thermal conductivity.

The Consolidated Car-heating Co.'s electric heater consists of a galvanized

iron wire wound in a spiral groove upon a porcelain insulator. Each heater

is 80% in. long, 87% in. high, and 67% in. wide. Upon it is wound 892 ft. of wire. The weight of the whole is 231% ibs.

Each heater is designed to absorb 1000 watts of a 500-volt current. Six heaters are the complement for an ordinary electric car. For ordinary weather the heaters may be combined by the switch in different ways, so that five different intensities of heating-surface are possible, besides the position in which no heat is generated, the current being turned entirely off.

For heating an ordinary electric car the Consolidated Co. states that from 2 to 12 amperes on a 500-volt circuit is sufficient. With the outside temperature at 30° to 30°, about 6 amperes will suffice. With zero or lower

temperature, the full 12 amperes is required to heat a car effectively.

Compare these figures with the experience in steam-heating of railway-

cars, as follows: 1 B.T.U. = 0.29084 watt-hours.

6 amperes on a 500-volt circuit = 3000 watts.

A current consumption of 6 amperes will generate 3000 + 0.29084 = 10,315

B.T.U. per hour.

In steam-car heating, a passenger coach usually requires from 60 lbs. of steam in freezing weather to 100 lbs. in zero weather per hour. Supposing the steam to enter the pipes at 20 lbs. pressure, and to be discharged at 200 F., each pound of steam will give up 983 B.T.U. to the car. Then the equivalent of the thermal units delivered by the electrical-heating system in pounds of steam, is 10,815 + 988 = 10%, nearly.

Thus the Consolidated Co.'s estimates for electric-heating provide the

equivalent of 10% lbs. of steam per car per hour in freezing weather and 21 lbs. in zero weather.

Suppose that by the use of good coal, careful firing, well-designed boilers, and triple-expansion engines we are able in daily practice to generate 1 H.P. delivered at the fly-wheel with an expenditure of 216 lbs. of coal per

hour.

We have then to convert this energy into electricity, transmit it by wire to the heater, and convert it into heat by passing it through a resistance-coil. We may set the combined efficiency of the dynamo and line circuit at 85%, and will suppose that all the electricity is converted into heat in the resistance-coils of the radiator. Then 1 brake H.P. at the engine = 0.85 electrical H.P. at the resistance-coil = 1.688,000 ft.-lbs. energy per hour = 2190 heat-units. But since it required 21/4 lbs. of coal to develop 1 brake H.P., it follows that the heat given out at the radiator per pound of coal burned in the boiler furnace will be 2180 + 216 = 872 H.U. An ordinary steam-heating system utilizes 9652 H.U. per lb. of coal for heating; hence the efficiency of the electric system is to the efficiency of the steam-heating system as 872 to 9652, or about 1 to 11. (Eng'g News, Aug. 9, '90; Mar. 30, '92; May 15, '93.)

REFORMATION OF STORAGE-BATTERIES.

The original, or Planté, storage battery consisted of two plates of metallic lead immersed in a vessel containing sulphuric acid. An electric current being sent through the cell the surface of the positive plate was converted into peroxide of lead, PbO₂. This was called charging the cell. After being thus charged the cell could be used as a source of electric current, or discharged. Planté and other authorities consider that in charging, PbO, is formed on the positive plate and spongy metallic lead on the negative, both being converted into lead oxide, PbO, by the discharge, but others hold that sulphate of lead is made on both plates by discharging and that during the charging PbO₂ is formed on the positive plate and metallic Pb on the other, sulphuric acid being set free.

The acid being continually abstracted from the electrolyte as the discharge proceeds, the density of the solution becomes less. In the charging operation this action is reversed, the acid being reinstated in the liquid and therefore causing an increase in its density.

The difference of potential developed by lead and lead peroxide immersed

in dilute H₈O₄ is about two volts. A lead-peroxide plate gradually loses its electrical energy by local action, the rate of such loss varying according

its electrical energy by local action, the rate of such loss varying according to the circumstances of its preparation and the condition of the cell. In the Faure or pasted cells lead plates are coated with minium or litharge made into a paste with acidulated water. When dry these plates are placed in a bath of dilute H₂SO₄ and subjected to the action of the current, by which the oxide on the positive plate is converted into peroxide and that on the negative plate reduced to finely divided or porous lead. The initial electro-motive force of the Faure cell averages 2.25 volts, but after being allowed to rest some little time it is reduced to about 2.0 volts. The "chloride" accumulator, made by the Electric Storage Battery Co. of Philladelphia, consists of lead plates containing cells filled with second.

of Philadelphia, consists of lead plates containing cells filled with spongy lead or with lead peroxide. The spongy lead is formed by first casting into the lead plate pastilles of a mixture of lead and zinc chlorides, the lead in which is afterwards by an electrolytic method converted into spongy lead, while the zinc chloride is dissolved and washed away. Plates intended for positive plates have the spongy lead converted into peroxide by immersing them in sulphuric acid and passing a current through them in one

direction for about two weeks.

The following tables give the elements of several sizes of "chloride" accumulators. Type G is furnished in cells containing 11-125 plates, and type H from 21 plates to any greater number desired. The voltage of cells

of all sizes is slightly above two volts on open circuit, and during discharge varies from that point at the beginning to 1.8 at the end.

Accumulators are largely used in central lighting and power stations, in office buildings and other large isolated plants, for the purpose of absorbing the energy of the generating plant during times of light load, and for giving it out during times of heavy load or when the generating plant is idle. The advantages of their use for such purposes are thus enumerated:

1. Reduction in coal consumption and general operating expenses, due to

the generating machinery being run at the point of greatest economy while in service, and being shut down entirely during hours of light load, the bat-

tery supplying the whole of the current.

		TYPE "C." Plates, 43 8 × 4 in.				TYPE "D." Size of Plates, 6×6 in.				
Number of plates. Discharge (For 8 hours in am 5	358 358 358 5 212 4	3 114 214 214 5 2 4 7 3 5 6 12	8 3 484 7 4 514	514 712	5 21/2 8 2 61/2 9 31/4 77/8	7 10 5 14 3 61 9 41 77 8	9 616	14 20 10 26 5 61 9 73 83 1	1236 1736 25 1236 32 6 632 9	21 30 15 38 7 612 9
lbs.	1	314	4.	5	6	914	13%	1634	1434	13
Weight of acid in rubber jars in lbs.	34	1	214	25%	214	31/2	514	7	814	10
Weight of cell complete, with acid, in rubber jars in lbs Height of cell over all in inches .									4214 1219	

ELECTRICAL ACCUMULATORS OR STORAGE-BATTERIES. 1047

			TYPE "E." Size of Plates, 734 × 734 in.									
Number of plates Discharge For 8 hours in am- " 5 " peres: " 3 " Normal charge rate		7 15 21 30 15	9 20 28 40 20	11 25 35 50 25	13 30 42 60 30	15 35 49 70 35	9 40 56 80 40	11 50 10 100 50	13 60 84 120 60	15 70 98 140 70	17 80 112 160 80	19 90 126 180 90
Weight each element. 10s. Width, in., rub- Length, ber Length, jar. Width, Z z Length, Z z Width, Z z Weight of acid in glass	516 918 1114	916	43 5 816 11 8 918 1114		81/2		9 1236 1514	1216	15 1734 1056 1216	1234	15	184 2134 15 1734
jars in lbs Weight of acid in rub-	17	21	25	27	35	84	53	61	58	70		
ber javs in lbs Weight of cell com- plete, with acid, in	616	9	1116	141/6	171/6	21		lead	94	104	114	124
rubber jar in lbs Height of cell over all, iu inches	31	42 14½	54 141/6	66 1416	79 14½	91 1456	18	18	302 18	339 19	376 19	415 19
_ Size of Pla	YPE tes, 1			g in.		<u>'</u>	-		Size	of Pl	ates	,
Company of the Party of the Company	-											
Discharge For 8 hrs. in am- peres: 5 " 5 " 8 " Normal charge rate	11 100 140 200 100	13 120 168 240 120	15 140 196 280 140	17 160 224 320 160	25 240 336 480 240	125 1240 1786 2480 1240	14 20	21 400 560 800 400	28 440 616 680 440	25 480 672 960 480	125 2480 8472 4960 2480	28 40
Discharge For 8 hrs. in amperes: "5" "5" "5" "Normal charge rate Weight of each element, lbs Outside (Width.	100 140 200 100 219 1534	120 168 240 120 260 16%	140 196 280 140 300 1836	160 224 320 160 341 20	240 336 480 240 503 2756	1240 1786 2480 1240 2588	10 14 20 10 20.4	400 560 800 400 790	440 616 680 440 866	480 672 960 480	2480 8472 4960 2480	20 28 40 20 38
Discharge For 8 hrs. in amperes: 5" 5" Normal charge rate. Weight of each element, ths Ousside Width. measurement J Length	100 140 200 100 219 1534	120 168 240 120 260 16%	140 196 280 140 300 1836	160 224 320 160 341 20	240 336 480 240 503 2756	1240 1786 2480 1240 2538 1111	10 14 20 10 20.4 20.4	400 560 800 400 790 251/8	440 616 680 440 866 2634	480 672 960 480	2480 8472 4960 2480 4741 1114	20 28 40 20 38
Discharge For 8 hrs. in amperes: "5". 5". Normal charge rate. Weight of each element, lbs Outside Country of tank in Length inches. Height	100 140 200 100 219 1516 1934	120 168 240 120 260 1634 1934	140 196 280 140 300 1838 1934	160 224 320 160 341 20 1934	240 336 480 240 503 2758 2034	1240 1786 2480 1240 2538 1111	10 14 20 10 20.4 %	400 560 800 400 790 251/6	440 616 680 440 866 2634 2116	180 672 960 480 942 98% 2156	2480 8472 4960 2480 4741 1114	20 28 40 20 38
Discharge For 8 hrs. in amperes: 3 " 5 " 5 " 5 " 5 " 5 " 5 " 5 " 5 " 5 "	100 140 200 100 219 151/6 193/4 223/6	120 168 240 120 260 1634 1934	140 196 280 140 300 1836 1934 2276	160 224 320 160 341 20 1934 2276	240 836 480 240 503 2758 2034 2276	1240 1736 2480 1240 2538 1111 2116	10 14 20 10 20.4 78	400 560 800 400 790 251/6	\$40 616 680 440 866 2634 2136 4236	180 672 960 480 942 98% 215 42%	2480 8472 4960 2480 4741 1114 2136	20 28 40 20 38 78
peres: 3 % Normal charge rate. Weight of each element, lbs Outside Width. Measurement Length inches, Height Weight of acid in pounds Weight of cell, com-	100 140 200 100 219 1536 1934 2236 160	120 168 240 120 260 1634 1934 2276	140 196 280 140 300 1836 1934 2276	160 224 320 160 341 20 1934 2276	240 836 480 240 503 2758 2034 2276	1240 1786 2480 1240 2538 1111 2114 2434	10 14 20 10 20.4 38	400 550 800 400 790 251/6 211/6 427/6 515	440 616 680 440 866 2634 2114 4276 552	180 672 960 480 942 985 215 4276 590	2480 8472 4960 2486 4741 1114 2114 43%	20 28 40 20 38 78

^{*}D = addition per plate from 25 to 125 plates; approximate as to dimensions and weights.

The possibility of obtaining good regulation in pressure during fluctuations in load, especially when the day load consists largely of elevators and similar disturbing elements.

^{3.} To meet sudden demands which arise unexpectedly, as in the case of darkness caused by storm or thunder-showers; also in case of emergency due to accident or stoppage of generating-plant.

4. Smaller generating-plant required where the battery takes the peak of

^{4.} Smaller generating-plant required where the battery takes the peak of the load, which usually only lasts for a few hours, and yet where no battery is used necessitates sufficient generators, etc., being installed to provide for the maximum output, which in many cases is about double the normal output.

The Working Current, or Energy Efficiency, of a storage-cell is the ratio between the value of the current or energy expended in the charging operation, and that obtained when the cell is discharged at any specified rate.

In a lead storage-cell, if the surface and quantity of active material be accurately proportioned, and if the discharge be commenced immediately after the termination of the charge, then a current efficiency of as much as 93% may be obtained, provided the rate of discharge is low and well regulated. In practice it is found that low rates of discharge are not economical and as the current efficiency always decreases as the discharge rate increases, it is found that the normal current efficiency seldom exceeds 90%, and averages about 85%.

As the normal discharging electro-motive force of a lead secondary cell never exceeds 2 volts, and as an electro-motive force of from 2.4 to 2.5 volts is required at its poles to overcome both its opposing electro-motive

voits is required at its poles to overcome both its opposing electro-motive force and its internal resistance, there is an initial loss of 20% between the energy required to charge it and that given out during its discharge.

As the normal discharging potential is continually being reduced as the rate of discharge increases, it follows that an energy efficiency of 80% can never be realized. As a matter of fact, a maximum of 75% and a mean of 60% is the usual energy efficiency of lead-sulphuric-acid storage-cells.

Important General Bules.—Storage cells should not be allowed to stand idle when charged, and must not stand idle when uncharged or atter being discharged. If a battery is to be not out of commission

or after being discharged. If a battery is to be put out of commission for any length of time, it should be fully charged, the electrolyte all drawn off, the cells filled with pure water and then discharged slightly—say until the E.M.F. is 1.95 volts. The cells should then be emptied, and the plates dried in a warm atmosphere.

In mixing the electrolyte, the acid should always be poured into the water. The mixing must be very gradual in order to avoid excessive heating. The acid solution must be cooled before the cells are filled with

it. The acid should be tested for impurities before mixing the electrolyte.

Tests for Impurities.—To test for copper and arsenic, add a small quantity of dilute acid to an equal quantity of fresh sulphide of hydrogen (H₂S). The presence of copper will cause a black precipitate; that of arsenic, a

yellow precipitate.

To test for iron, add a few drops of nitric acid to a small quantity of dilute acid and heat the mixture; after cooling add a few drops of potassium sulphocyanide solution. The presence of iron will be indicated by a deep red color.

Charging and Discharging.—Charging should be stopped when the voltage is 26 volts per cell and gas is given off, except in the first charging, when 2.7 should be reached. Discharging should be stopped and the cells recharged when the voltage is down to 1.8 volts per cell when discharging at normal rate.

ELECTROLYSIS.

The separation of a chemical compound into its constituents by means of an electric current. Faraday gave the nomenclature relating to electrolysis. The compound to be decomposed is the Electrolyte, and the process Electrolysis. The plates or poles of the battery are Electrodes. The olate where the greatest pressure exists is the Anode, and the other pole is the Cathode. The products of decomposition are Ions.

Lord Rayleigh found that a current of one ampere will deposit 0.017253

grain, or 0.001118 gramme, of silver per second on one of the plates of a silver voltameter, the liquid employed being a solution of silver nitrate containing from 15% to 20% of the salt. The weight of hydrogen similarly set free by a current of one ampere is .00001038 gramme per second.

Knowing the amount of hydrogen thus set free, and the chemical equivalents of the constituents of other substances, we can calculate what weight ients of the constituents of other substances, we can calculate what weight of their elements will be set free or deposited in a given time by a given current. Thus, the current that liberates 1 grammes of hydrogen will liberate 8 grammes of oxygen, or 107.7 grammes of silver, the numbers 8 and 107.7 being the chemical equivalents for oxygen and silver respectively. To find the weight of metal deposited by a given current in a given time, find the weight of hydrogen liberated by the given current in the given time, and multiply by the chemical equivalent of the metal.

ELECTRO-CHEMICAL EQUIVALENTS.

Elements.	Valency.*	Atomic Weight.†	Chemical Equiv-	Electro-chemical Equivalent (mil- ligrammes per coulomb).	Coulombs per gramme,	Grammes per ampere hour.
ELECTRO-POSITIVE. Hydrogen. Potassium Sodium Aluminum Magnesium Gold Silver Copper (cuprie) (cuprous) Mercury (mercuric) (mereurous) Tin (stannic) (stannous) Iron (ferric) (ferrous) Nickel Zinc Lead	Hi Ki Nai Als Als Als Als Als Als Als Als Als Als	1,00 39.04 22.99 27.3 23.94 106.2 107.66 63.00 199.8 199.8 117.8 117.8 55.9 58.9 64.9 206.4	1.00 39.04 22.99 9.1 71.97 65.4 107.66 81.5 63.00 99.9 199.8 29.45 58.9 18.04 29.3 38.45 58.9 18.04 29.3	.010364 .40539 .25873 .09449 .12430 .67911 1.11900 .32709 .65419 .1.03740 2.07470 .30581 .61189 .19356 .29035 .30425 .39696 1.07160	96993,00 2467.50 4188.90 1058.80 1973.50 894.41 3058.60 1825.30 968.99 481.99 2270.00 1635.00 5166.4 3445.50 3466.80 2967.10	0.08788 1.45950 0.86442 0.34018 0.4477 2.44480 1.17700 2.35500 1.17700 1.1090 2.20180 0.69881 1.04480 1.90530 1.21530 8.85789
Electro-Medative. Oxygen	Os Cli Bri Na	15.96 85.37 126.59 79.75 14.01	7.98 85.37 126.58 79.75 4.67	.08296 .36728 1.31390 .82612 .04849		

^{*} Valency is the atom-fixing or atom-replacing power of an element compared with hydrogen, whose valency is unity.

† Atomic weight is the weight of one atom of each element compared with hydrogen, whose atomic weight is unity.

‡ Becquerel's extension of Faraday's law showed that the electro-chemical

equivalent of an element is proportional to its chemical equivalent. The latter is equal to its combining weight, and not to atomic weight + valency, as defined by Thompson, Hospitalier, and others who have copied their tables. For example, the ferric salt is an exception to Thompson rule, as

are sequi-saits in general.

Thus: Weight of silver deposited in 10 seconds by a current of 10 amperes = weight of hydrogen liberated per second × number seconds × current strength × 107.7 = .00001038 × 10 × 10 × 107.7 = .11178 gramme.

Weight of copper deposited in 1 hour by a current of 10 amperes =

 $.00001038 \times 3000 \times 10 \times 31.5 = 11.77$ grammes.

Since 1 ampere per second liberates .00001038 gramme of hydrogen, strength of current in amperes

> weight in grammes of H. liberated per second .00001088

weight of element liberated per second = .00001088 × chemical equivalent of element

The above table (from "Practical Electrical Engineering") is calculated apon Lord Rayleigh's determination of the electro-chemical equivalents and Roscoe's atomic weights.

ELECTRO-MAGNETS.*

Units of Electro-magnetic Measurements.

Unit magnetic pole is a pole of such strength that when placed at a distance of one centimetre from a similar pole of equal strength it repels it with a force of one dyne.

Gauss = unit of field strength, or density, symbol H, is that intensity of field which acts on a unit pole with a force of one dyne, so the of force per square centimetre. A field of H units is one which acts with H dynes on unit pole, or H lines per square centimetre. A unit magnetic pole has 4π lines of force proceeding from it.

Maxwell = unit of magnetic flux, is the amount of magnetism passing through every square centimetre of a field of unit density. Symbol, ϕ . Gilbert = unit of magneto-motive force, is the amount of M.M.F., that would be produced by a coil of $10+4\pi$ or 0.7958 ampere-turns. Symbol, F. The M.M.F. of a coil is equal to 1.2566 times the ampere-turns. If a solenoid is wound with 100 turns of insulated wire carrying a current of 5 amperes, the M.M.F. exerted will be 500 ampere-turns $\times 1.2566 = 628.3$

gilberts.

Oersted = unit of magnetic reluctance; it is the reluctance of a cubic centi-

metre of an air-pump vacuum. Symbol, R. Reluctance is that quantity in a magnetic circuit which limits the flux under a given M.M.F. It corresponds to the resistance in the electric cir-

The reluctivity of any medium is its specific reluctance, and in the C.G.S. system is the reluctance offered by a cubic centimetre of the body between opposed parallel faces. The reluctivity of nearly all substances, other than the magnetic metals, is sensibly that of vacuum, is equal to unity, and is independent of the flux density.

Permeability is the reciprocal of magnetic reluctivity. It is a number, and

the symbol is μ .

Permeance is the reciprocal of reluctance.

Lines and Loops of Force.—In discussing magnetic and electrical phenomena it is conventionally assumed that the attractions and repulsions as shown by the action of a magnet or a conductor upon iron filings are due to "lines of force" surrounding the magnet or conductor. The "number of lines" indicates the magnitude of the forces acting. As the iron filings arrange themselves in concentric circles, we may assume that the forces may be represented by closed curves or "loops of force." The following assumptions are made concerning the loops of force in a conductive circuit:

1. That the lines or loops of force in the conductor are parallel to the

axis of the conductor.

2. That the loops of force external to the conductor are proportional in number to the current in the conductor, that is, a definite current generates a definite number of loops of force. These may be stated as the strength of field in proportion to the current. 3. That the radii of the loops of force are at right angles to the axis of

the conductor.

The magnetic force proceeding from a point is equal at all points on the surface of an imaginary sphere described by a given radius about that point. A sphere of radius 1 cm. has a surface of 4π square centimetres. If $\phi = \text{total flux}$, expressed as the number of lines of force emanating from a magnetic pole having a strength, M,

$$\phi = 4\pi M \; ; \; M = \phi + 4\pi.$$

Magnetic moment of a magnet = product of strength of pole M and its length, or distance between its poles L. Magnetic moment = $\frac{\phi L}{c}$

^{*} For a very full treatment of this subject see "The Electro-Magnet," published by the Varley Duplex Magnet Co., Phillipsdale, R. I.

If B = number of lines flowing through each square centimetre of cross-section of a bar-magnet, or the "specific induction," and A = cross-section,

Magnetic Moment =
$$LAB \div 4\pi$$
.

If the bar-magnet be suspended in a magnetic field of density H, and so placed that the lines of the field are all horizontal and at right angles to the axis of the bar, the north pole will be pulled forward, that is, in the direction in which the lines flow, and the south pole will be pulled in the opposite direction, the two forces producing a torsional moment or torque,

Torque =
$$MLH = LABH + 4\pi$$
, in dyne-centimetres.

Magnetic attraction or repulsion emanating from a point varies inversely as the square of the distance from that point. The law of inverse squares, however, is not true when the magnetism proceeds from a surface of appreciable extent, and the distances are small, as in dynamo-electric machines

ciable extent, and the distances are small, as in dynamo-electric machines and ordinary electromagnets.

Permeability,—Materials differ in regard to the resistance they offer to the passage of lines of force; thus iron is more permeable than air. The permeability of a substance is expressed by a coefficient, μ , which denotes its relation to the permeability of air, which is taken as 1. If H—number of magnetic lines per square centimetre which will pass through an air-space between the poles of a magnet, and B the number of lines which will pass through a certain piece of iron in that space, then $\mu = B + H$. The permeability varies with the quality of the iron and the degree of saturation, reaching a practical limit for soft wrought iron when B = about 18,000 and for cast iron when B = about 10,000 C.G.S lines per square centimetre. The permeability of a number of materials may be determined by means of the table on the following page.

The Magnetic Circuit.—In the electric circuit

Current =
$$\frac{E.M.F.}{Resistance}$$
, or $I = \frac{E}{R}$.

Similarly, in the magnetic circuit

Magnetic Flux =
$$\frac{\text{Magnetomotive Force}}{\text{Reluctance}}$$
, or $\phi = \frac{F}{R}$.

Reluctance is the reciprocal of permeance, and permeance is equal to permeability×path area+path length (metric measure); hence

$$\phi = F \frac{\mu a}{l}$$
.

One ampere-turn produces 1.257 gilberts of magnetomotive force and one inch equals 2.54 centimetres; hence, in inch measure,

$$\phi = (1.257A_t) \frac{\mu 6.45a}{2.54l} = \frac{3.192 \,\mu a A_t}{l}.$$

The ampere-turns required to produce a given magnetic flux in a given path will be

$$^{A}_{t}\!=\!\!\frac{\phi l}{3.192\,\mu a}=\!\frac{0.3133\phi l}{\mu a}.$$

Since magnetic flux+area of path-magnetic density, the ampere-turns required to produce a density **B**, in lines of force per square inch of area of path, will be

$$A_{,} = 0.3133 Bl + \mu$$
.

This formula is used in practical work, as the magnetic density must be predetermined in order to ascertain the permeability of the material under its working conditions. When a magnetic circuit includes several

qualities of material, such as wrought iron, east iron, and air, it is most direct to work in terms of ampere-turns per unit length of path. The ampere-turns for each material are determined separately, and the winding is designed to produce the sum of all the ampere-turns. The following table gives the average results from a number of tests made by Dr. Samuel Shaldon. Sheldon:

VALUES OF B AND H.

	Ampere-turns per cent, length.	Ampere-turns per inch length.	Cast	Iron.	Cast Steel.		WroughtIron		Sheet Metal.	
H			B Kilo- gausses.	Kilomax- wells per sq. in.	В Кіlо- gansees.	Kilomax- wells per sq. in.	B Kilo- gaugees.	Kilomax- wells per sq. in.	Kilo- Kalmsee.	Kilomax- wells per eq. in.
10 20 30 40 50 60 70 80 90 150 200 250 300	7.95 15.90 23.85 31.80 39.75 47.70 55.65 63.65 71.60 79.50 119.25 159.0 198.8 238.5	26.2 40.4 60.6 80.8 101.0 121.2 141.4 161.6 181.8 202.0 303.0 404.0 505.0 606.0	4.3 5.7 6.5 7.1 7.6 8.0 8.4 8.7 9.4 10.6 11.7 12.4 13.2	27.7 36.8 41.9 45.8 49.0 51.6 59.2 56.1 58.0 60.6 68.3 75.5 80.0 85.1	11.5 13.8 14.9 15.5 16.0 16.5 16.9 17.4 17.7 18.5 19.2 19.7	74.2 89.0 96.1 100.0 103.2 108.5 109.0 111.0 111.0 112.2 123.9 127.1 129.6	13.0 14.7 15.3 15.7 16.0 16.3 16.5 16.9 17.9 18.0 18.7 19.2 19.7	83.8 94.8 98.6 101.2 03.2 105.2 106.5 107.8 109.0 116.1 120.8 123.9 127.1	14.3 15.6 16.2 16.6 16.9 17.3 17.5 17.7 18.0 18.2 19.6 20.2 20.7	99.3 100.7 104.5 107.1 109.0 111.6 112.9 114.1 116.1 117.3 122.7 126.5 130.2 133.5

H = 1.257 ampere-turns per cm. = .495 ampere-turns per inch.

Example.—A magnetic circuit consists of 12 inches of cast steel of 8 square inches cross-section; 4 inches of cast iron of 22 square inches cross-section; 3 inches of sheet iron of 8 square inches cross-section; and two air-gaps each \(\frac{1}{2} \) inches of sheet iron of 8 square inches area. Required, the ampere-turns to produce a flux of 768,000 maxwells, which is to be

uniform throughout the magnetic circuit.

The flux density in the steel is 768,000 + 8 = 96,000 maxwells; the ampereturns per inch of length, according to Sheldon's table, are 60.6, so that the 12 inches of steel will require 727.3 ampere-turns.

The density in the cast iron is 768,000+22=34,900; the ampere-turns $-4 \times 40 = 160$.

The density in the sheet iron = 768,000 + 8 = 96,000; ampere-turns per

inch=30; total ampere-turns for sheet iron=90.

The air-gap density is 768,000+12=64,000; ampere-turns per inch=0.31338; ampere-turns required for air-gap=0.3133×64,000+8=2506.4.

The entire circuit will require 727.2+160+90+2506.4-3483.6 ampere-

turns, assuming uniform flux throughout.

In practice there is considerable "leakage" of magnetic lines of force; that is, many of the lines stray away from the useful path, there being no material opaque to magnetism and therefore no means of restricting it to material opaque to magnetism and therefore no means of restricting it to a given path. The amount of leakage is proportional to the permeance of the leakage paths available between two points in a magnetic circuit which are at different magnetic potentials, such as opposite ends of a magnet coil. It is seldom practicable to predetermine with any approach to accuracy the magnetic leakage that will occur under given conditions unless one has profuse data obtained experimentally under similar conditions. In dynamo-electric machines the leakage coefficient varies from 13 to 2 1.3 to 2.

Tractive or Lifting Force of a Magnet.—The lifting power or 'pull' exerted by an electro-magnet upon an armature in actual contact with its pole-faces is given by the formula

$$\frac{B^2a}{72,134,000}$$
 = Lbs.,

a being the area of contact in square inches and B the magnetic density over this area. If the armature is very close to the pole-faces, this for nula also applies with sufficient accuracy for all practical purposes, but a considerable air-gap renders it inapplicable. The accompanying table is convenient for approximating the dimensions of cores and pole-faces for tractive magnets.

Dimensions of Lifting Magnets.

Den-	Amp inc	ere-turn h of len	s per gth.	Pull in lbs. per sq. in.			ere-turn h of len		Pull in lbs. per
sity B.	Air.	Cast Iron.	Cast Steel.		sity B.	Air.	Cast Iron.	Cast Steel.	sq. in.
10,000	3133	18	3.7	1.38	29,000	9.086	49	6.5	11.6
11,000	3447	19.2	3.81	1.65	30,000	9,400	52	6.7	12.4
12,000	3760	20.4	3.93	2	81,000	9,713	55	6.9	13.2
13,000	4073	21.6	4.05	2.3	32,000	10,026	58	7.1	14
14,000	4387	22.8	4.17	2.7	33,000	10,339	61	7.3	15
15,000	4700	24	4.3	8.1	34.000	10,652	64	7.5	16
16,000	5013	25.2	4.44	3.5	35,000	10,965	68	7.7	17
17,000	5326	26.5	4.58	4	36,000	11,278	72	7.9	18
18,000	5640	27.9	4.72	4.5	37,000	11,590	76	8.1	19
19.000	5953	29.3	4.86	5	38,000	11,904	80	8.3	20
20,000	6266	30.7	5	5.5	39,000	12,217	85	8.55	21
21,000	6580	32.2	5.16	6	40,000	12,532	90	8.8	22
21,500	6736	33.1	5.24	6.4	41,000	12,843	95	9.05	23
22,000	6893	34	5.32	67	42,000	13,159	100	9.3	24.25
22,500	7050	35	5.4	7	43,000	13,472	106	9.55	25.5
23,000	7206	36	5.48	7.3	44,000	13,785	112	9.8	26.75
23,500	7363	37	5.56	7.6	45,000	14.098	118	10.25	28
24,000	7520	38	5.64	7.9	46,000	14,412	125	10.5	29.3
25,000	7833	40	5.8	8.6	47,000	14,725	132	10.8	30.6
26,000	8146	42	5.97	9.3	48,000	15,038	140	11.15	31.9
27,000	8459	44	6.14	10	49,000	15,350	150	11.5	83.2
28,000	8773	46	6.32	10.8	50,000	15,665	160	11.9	34.6

Magnet Windings.—Knowing the ampere-turns required to produce the desired excitation of a magnetic circuit, the winding may be approximately determined as follows:

For round cores under 1 inch in diameter make the depth or thickness

For round cores under 1 inoh in diameter make the depth or thickness of winding, t, equal to the core diameter; over 1 inch, let t=cube root of core diameter. For slab-shaped cores let the coil thickness be equal to the core thickness up to 1 inch, and to the square root of the core thickness above that.

The ampere-turns produced by any coil will be

$$A_t = \frac{Vd^2}{lk}$$

in which V = volts at the coil terminals, $d^2 = \text{area}$ of the wire in circular mils,

l =mean length in inches per turn of wire,

k=a coefficient depending on the temperature of the coil.

The mean length per turn of wire is

$$g + \pi t = l_{em}$$

g being the perimeter of the core. The size of wire required for a given excitation will be

$$d^2 = \frac{kA_t}{V}(g + \pi t).$$

At 140° Fahr, k=1. The table herewith gives the values of k at various other practical temperatures.

Values of k in Magnet-coil Formula.

Temp.	k	Temp.	k	Temp.	k	Temp.	k
100	0.923	115	0.952	130	0.981	150	1.0195
105	0.933	120	0.962	135	0.99	155	1.029
110	0.942	125	0.971	145	1.01	160	1.0387

The rise above atmospheric temperature will be

$$\frac{V^2}{k_* R S} = \theta,$$

in which R = the resistance of the coil when hot, S = its radiating surface, and k_t is a variable coefficient (see p. 1032). The value of k_t will be about 0.008 for electro-magnets of ordinary size not enclosed or shielded in any

way from the surrounding air.

For fuller treatment of the subject, see American Electrician, April and

For fuller treatment of the subject, see American Electrician, April and May, 1901, and January, 1904.

Betermining the Polarity of Electro-magnets.—If a wire is wound around a magnet in a right-handed helix, the end at which the current flows into the helix is the south pole. If a wire is wound around an ordinary wood-screw, and the current flows around the helix in the direction from the head of the screw to the point, the head of the screw is the south pole. If a magnet is held so that the south pole is opposite the eye of the observer, the wire being wound as a right-handed helix around it, the current flows in a right-handed direction, with the hands of a clock.

Determining the Direction of a Current.—Place a wire carrying a current above and parallel to a pivoted magnetic needle. If the current be flowing along the wire from N. to S., it will cause the N-seeking pole to turn to the eastward; if it be flowing from S. to N., the pole will turn to the westward. If the wire be below the needle, these motions will be reversed.

motions will be reversed.

Maxwell's rule. The direction of the current and that of the resisting magnetic force are related to each other as are the rotation and the forward travel of an ordinary (right-handed) cork-screw.

DYNAMO-ELECTRIC MACHINES.

There are three classes of dynamo-electric machines, vis.:

1. Generators, for the conversion of mechanical into electrical energy. 2. Motors, for the conversion of electrical into mechanical energy.

Generators and motors are both subdivided into direct-current and alter-

nating-current machines.
3. Transformers, for the conversion of one character or voltage of current into another, as direct into alternating or alternating into direct, or from one voltage into a higher or lower voltage.

Kinds of Dynamo-electric Machines as regards Manner of Winding.

1. Separately-excited Dynamo.—The field-magnet coils have no connection with the armature-coils, but receive their current from a separate machine or source.

2. Series-wound Dynamo.—The field winding and the external circuit are connected in series with the armature winding, so that the entire armature

current must pass through the field-coils.

Since in a semes-wound dynamo the armature-coils, the field, and the external circuit are in series, any increase in the resistance of the external circuit will decrease the electro-motive force from the decrease in the magnetizing currents. A decrease in the resistance of the external circuit will, in a like manner, increase the electro-motive force from the increase in the The use of a regulator avoids these changes in the magnetizing current. electro-motive force.

3. Shunt-wound Dynamo.—The field-magnet coils are placed in a shunt to the armature circuit, so that only a portion of the current generated passes through the field-magnet coils, but all the difference of potential of

the armature acts at the terminals of the field-circuit.

In a shunt-wound dynamo an increase in the resistance of the external circuit increases the electro-motive force, and a decrease in the resistance of the external circuit decreases the electro-motive force. This is just the

reverse of the series-wound dynamo.

In a shunt-wound dynamo a continuous balancing of the current occurs, the current dividing at the brushes between the field and the external circuit in the inverse proportion to the resistance of these circuits. If the resistance of the external circuit becomes greater, a proportionately greater current passes through the field-magnets, and so causes the electro-motive force to become greater. If, on the contrary, the resistance of the external circuit decreases, less current passes through the field, and the electromotive force is proportionately decreased.

4. Compound wound Dynamo.—The field-magnets are wound with two separate sets of coils, one of which is in series with the armature and the external circuit, and the other in shunt with the armature, or the external

circuit.

Motors.—The above classification in regard to winding applies also to

Moving Force of a Dynamo-electric Machine.—A wire through which a current passes has, when placed in a magnetic field, a tendency to move perpendicular to itself and at right angles to the lines of the field. The force producing this tendency is P = lBI dynes, in which l = length of the wire, I = the current in C.G.S. units, and B = the inductive of the lines tion, or flux density, in the field in lines per square centimetre. If the current I is taken in amperes, P = lBI + 10 = lBI 10^{-1} . If Pk is taken in kilogrammes,

$Pk = lBI + 9.810,000 = 10.1937 \ lBI \ 10^{-8} \ kilogrammes.$

Example.—The mean strength of field, B, of a dynamo is 5000 C.G.S. lines; a current of 100 amperes flows through a wire; the force acts upon 10 centimetres of the wire=10.1937×10×100×5000×10⁻⁸=.5097 kilo-

grammes.

In the "English" or Kapp's system of measurement a total flow of 6000

C.G. S. lines is taken to equal one English line. Calling BE the induction in English, or Kapp's, lines per square inch, and B the induction in C. G. S. lines per square centimetre, BE = B + 930.04; and taking l'' in inches and PP in pounds, $PP = 531ll''BE10^{-6}$ pounds.

Torque of an Armature.—The torque of an armature is the moment tending to turn it. In a generator it is the moment which must be applied to the armature to turn it in order to produce current. In a motor it is the turning moment which the armature gives to the pulley.

Let I = current in the armature in amperes, E = the electro-motive force in volts, T = the torque in pound-feet, $\phi = \text{the flux through the armature}$ in maxwells, N = the number of conductors around the armature, and n = the number of revolutions per second.

Watts =
$$IE = 2\pi nT \times 1.356.*$$

In any machine if the flux be constant, E is directly proportional to the speed and $-\phi Nn + 10^{\circ}$; whence

$$\frac{\phi NI}{10^8} = 2\pi T \times 1.356;$$

$$T = \frac{\phi NI}{10^6 \times 2\pi \times 1.356} = \frac{\phi NI}{8.52 \times 10^6}$$
 pound-feet.

Let l = length of armsture in inches, d = diameter of armsture in inches. B — flux density in maxwells per square inch, and let m — the ratio of the conductors under the influence of the pole-pieces to the whole number of conductors on the armature. Then

$$\phi = \frac{\pi d}{2} \times l \times B \times m.$$

These formulæ apply to both generators and motors. They show that torque is independent of the speed and varies directly with the current and the flux. The total peripheral force is obtained by dividing the torque by the radius (in feet) of the armature, and the drag on each conductor is obtained by dividing the total peripheral force by the number of conductors

botained by dividing the total periphers force by the number of conductors under the influence of the pole-pieces at one time. Example.—Given an armsture of length l=20 inches, diameter d=12 inches, number of conductors N=120, of which 80 are under the influence of the pole-pieces at one time; let the flux density B=30,000 maxwells per sq. in. and the current I=400 amperes.

$$\phi = \frac{12\pi}{2} \times 20 \times 30,000 \times \frac{80}{120} = 7,540,000.$$

$$T = \frac{7,540,000 \times 120 \times 400}{8.52 \times 100,000,000} = 424.8 \text{ pound-feet.}$$

Total peripheral force = 424.8 + .5 = 849.6 lbs.

Drag per conductor = 849.6 + 120 = 7.08 lbs.

The work done in one revolution = torque × circumference of a circle of 1 foot radius = 424.8 × 6.28 = 2670 foot-pounds.

Let the revolutions per minute equal 500, then the horse-power

$$= \frac{2670 \times 500}{33000} = 40.5 \text{ H.P.}$$

Electro-motive Force of the Armature Circuit.—From the horse-power, calculated as above, together with the amperes. we can obtain the E.M. F., for $IE = \text{H.P.} \times 746$, whence E.M.F. or $E = \text{H.P.} \times 746 + I$.

If H.P., as above,
$$= 40.5$$
, and $I = 400$, $E = \frac{40.5 \times 746}{400} = 75.5$ volts.

The E.M.F. may also be calculated by the following formulæ:

I = Total current through armature;

- E.M.F. in armature in volts;

ea = E.M.F. in armature in voits;
 N = Number of active conductors counted all around armature;
 p = Number of pairs of poles (p = 1 in a two-pole machine);
 n = Speed in revolutions per minute;

 ϕ = Total flux in maxwells.

Electro-motive
$$\begin{cases} ea = \phi N \frac{n}{60} \ 10^{-\frac{3}{2}} \text{ for two-pole machines.} \\ ea = \frac{p\phi Nn}{10^{\alpha}} \frac{n}{60} \text{ for multipolar machines with series-wound armsture.} \end{cases}$$

Strength of the Magnetic Field.—The fundamental equation for calculations relating to the magnetic circuit is

Magneto-motive force is the magnetizing effect of an electric current.

Magneto-motive force is the magnetizing effect of an electric current. It varies directly as the number of turns in a coil, and as the current. It is numerically equal to 1.257 \times amperes \times turns. Reluctance is the resistance any material offers to the setting up in itself of magnetic lines. It varies directly as the length and inversely as the area of the cross-section of the core, taken at right angles to the direction of the magnetic lines, and inversely as the permeability of the material. Let I = current in amperes, N = number of turns in the coil, A = area of the cross-section of the core in square centimetres, I = length of core in centimetres, I

Then

$$\phi = \frac{1.257NI}{(l+A\mu)}.$$

In a dynamo-electric machine the reluctance will be made up of three separate quantities, viz.: the reluctance of the field magnet cores, the reluctance of the air spaces between the field magnet pole-pieces and the armature, and the reluctance of the armature. The total reluctance is the sum of the three. Let L_1 , L_2 , L_3 be the length of the path of magnetic lines in the field magnet cores.* in the air-gaps, and in the armature respectively; and let A_1 , A_2 , A_3 be the areas of the cross-sections perpendicular to the path of the magnetic lines in the field magnet cores, the air-gaps, and the armature respectively. Let the permeability of the field magnet cores be μ_1 , and of the armature μ_3 . The permeability of the air-gaps is taken as unity. Then the total reluctance of the machine will be In a dynamo-electric machine the reluctance will be made up of three

$$\frac{L_1}{A_1 \mu_1} + \frac{L_2}{A_2} + \frac{L_3}{A_3 \mu_3}$$

The formula for magnetic flux will now read

$$\phi = \frac{1.257NI}{(L_1 + A_1\mu_1) + (L_2 + A_2)} + (L_3 + A_3\mu_8)^{\bullet}$$

The ampere turns necessary to create a given flux in a machine may be found by the formula

$$NI = \phi \frac{\{(L_1 + A_1 \mu_1) + (L_2 + A_2) + (L_4 + A_2 \mu_2)\}}{1.257}.$$

But the total flux generated by the field coils is not available to produce current in the armature. There is a leakage between the field magnets, and this must be allowed for in calculations. The leakage coefficient varies from 1.3 to 2 in different machines. The meaning of the coefficient is that if a flux of say 100 maxwells per square cm. are desired in the field coils, it will be necessary to provide ampere turns for 1.3 × 100 = 130 maxwells, if the leakage coefficient he 1.3.

Another method of calculating the ampere turns necessary to produce a given flux is to calculate the magneto-motive force required in each portion of the machine, separately, introducing the leakage coefficient in the calculating that the leakage coefficient in the calculation that the leakage coefficient in the calculation that the leakage coefficient in the calculation that the leakage coefficient in the calculation that the leakage coefficient in the calculation that the leakage coefficient in the calculation that the leakage coefficient in the calculation that the leakage coefficient in the calculation that the leakage coefficient in the calculation that the leakage coefficient in the calculation that the leakage coefficient in the calculation that the leakage coefficient in the calculation that the leakage coefficient in the calculation that the leakage coefficient in the calculation that the le

given hax is to excluding the magneto-motive force required in each portion of the machine, separately, introducing the leakage coefficient in the calculation for the field magnets, and dividing the sum of the magnetive-moto forces by 1.257. An example of this last method is appended. Example.—Given a two-pole generator with a single magnetic circuit of the following dimensions, in centimetres and square centimetres: $L_1 = 150$, $L_2 = each.5$, $L_3 = 25$; $A_1 = 1200$, $A_2 = 1400$, $A_3 = 1000$; leakage

^{*} The length of the path in the field magnet cores L1 includes that portion of the path which lies in the piece joining the cores of the various field magnets.

coefficient $= \lambda = 1.32$; flux in armsture = 10.000,000 maxwells. Required the ampere turns on field magnets. Let B = intensity of magnetic induction, or flux density, and H = intensity of the magnetic field.

Armature:
$$B = \frac{\phi}{A_3} = \frac{10,000,000}{1000} = 10,000.$$

From the permeability table, $\mu_1 = 2000$

$$M.M.F_3 = \phi \frac{L_2}{A_2 \mu_8} = \frac{10,000,000 \times 25}{1000 \times 2000} = 125.$$

Air-gaps:

$$M.M.F_2 = \frac{10,000,000 \times 2 \times .5}{1400} = 7150.$$

Field Cores:

$$B = \frac{\phi \times \lambda}{A_1} = \frac{10,000,000 \times 1.32}{1200} = 11,000; \quad \mu = 1692.$$

$$M.M.F_1 = \frac{\phi \lambda L_1}{A_1 \mu_1} = \frac{10,000,000 \times 1.32 \times 150}{1200 \times 1692} = 975.$$

$$Total M.M.F. = 125 + 7150 + 975 = 8250.$$

$$Ampere turns = \frac{M.M.F.}{1.257} = \frac{8250}{1.257} = 6563.$$

In a machine having a double magnetic circuit, the calculation is slightly varied. The total flux is created by the two separate sets of windings, each set creating one half. The ampere turns are calculated for one set of windings. The flux, ϕ , used in the calculation is taken as one half the total flux created. The areas of the air-gaps A_2 and of the armature A_3 are also taken as one half the actual area. Except for these changes, the calculation is made in the same manner as for the single magnetic circuit: the result is the ampere turns for one set of field windings. cuit; the result is the ampere turns for one set of field windings.

In the ordinary type of multipolar machine there are as many magnetic circuits as there are poles. Each winding energizes part of two circuits. The calculation is made in the same manner as for a single magnetic circuit.

Dynamo Design.—In the design of a motor or generator the following data are usually given, being determined by local conditions Class, viz., bipolar or multipolar, series, shunt or compound wound; size, in kilowatts; voltage; and current. The following is an outline of the method pursued in the complete design. (For complete method see Wiener's Dynamo-electric Machines.)

Notation.—E = e.m.f. in external circuit in volts; E' = total e.m.f. gener-Notation.—E = e.m.t. in external circuit in voits; E = costa e.m.t. generated in armature in volts; e = e.m.t. necessary to overcome internal resistances of machine; I = current in external circuit. in amperes; I = current generated in armature in amperes; i = current in shutt field in amperes; $H_1 = assumed$ flux density of field in maxwells per sq. inch; B = actual flux density in armature, maxwells per square inch.; L = length of armature in inches; D = diameter of armature in inches; L = length of armature in L = length of armature in L = length of armature in L = length of armature in L = length of L = length of armature in L = length of active conductor (i.e., that on pole-facing surface of armature) in feet; d =diameter of armature conductor in mils; $d^2 =$ area of armature conductor, circular mils; d' =diameter of insulated armature conductor in inches; circular mils; d' = diameter of insulated armature conductor in increase. N = number of conductors on armature; p = number of pairs of poles in field; C = number of bars on commutator; ϕ = magnetic flux in armature in maxwells; ϕ' = total magnetic flux; λ = leakage coefficient of magnetic circuit; V = mean velocity of armature conductors in feet per second; h = available depth of winding space on armature, inches (in a slotted armature h is the depth of slot); n_1 = number of wires stranded in parallel to make one armature conductor; n = number of conductors in parallel to make one armature conductor; n2 - number of conductors

in parallel to make one armature conductor; n_2 — number of conductors per layer on armature; n_2 — number of layers of conductor on armature; k, m, b = variables and factors explained in the text.

A value is first assumed for H_1 . This is governed by the size of the machine, the style of armature, the number of poles, and the material of the pole-pieces, magnet cores, and frame. For a smooth core armature in a 1 kw. bipolar machine, with cast-iron pole-pieces, it may be taken as 15,000 maxwells per sq. inch for cast-iron; for wrought iron or steel pole-pieces it may be taken at 22,000 maxwells. For a 300 kw. bipolar machine

it may be assumed at 30,000 maxwells with cast-iron pole-pieces, and at 45,000 with wrought-iron pole-pieces. In multipolar machines, the figures are from 5000 to 7000 higher in each case.

A formula for the length of active armature conductor is

$$l = \frac{E' \times p}{k \times \pi \times H_1}.$$

The value of k is determined by multiplying 10^{-8} by a factor ranging from 50 to 72. depending on the percentage of polar arc, i.e., the percentage of the armature subtended by the pole-pieces. If the percentage of polar arc is 50 the factor is 50, if the percentage is 100 the factor is 72. V varies from 35 in a 1 kw. machine to 50 in a 200 or 300 kw. machine with a drum armature. With ring armatures, in high speed machines. V varies from 65 in a 1 kw. machine to 75 in a 25 kw. 85 in a 300 kw, and 100 in a 5000 kw. machine. On low speed dynamos the figures are approximately one half the above

the above. E'=(E+e). In series machines, under $1 \text{ kw.} \cdot e$ is from 40 to 20 per cent of E; in machines of from 1 to 25 kw., from 20 to 10 per cent; in 25 to 500 kw. machines, from 10 to 4 per cent; and in machines of over 500 kw. from 4 to 2.5 per cent of E. In shunt-wound machines e has approximately one half the value used in series machines; in compound-wound machines approximately three quarters the value used in series machines. The diameter of the armature core is found by means of the assumed velocity and the given revolutions per minute, $D=(12\times60V)+(r.p.m.\times\pi)$. The area of the conductors on the armature depends on the amount of current to be carried. $d^2=300I'+p$.

In a series machine I'=I; in shunt and compound machines I'=I+i. The current consumed in the shunt field varies with the size of the machine approximately as follows

approximately as follows

$$kw. = 1$$
 5 10 20 50 100 500 2000
 $i = .08I$.06I .05I .04I .03I .0275I .02I .015I

In large machines it is better, in order to diminish the eddy currents, to make the armature conductors in the form of a cable, than to use single wires. If the conductor on the armature is a single wire the thickness of insulation varies from .012 to .020 inch, depending on the voltage. If the conductor is a cable, each strand is insulated with a thickness of from .005 to .01 inch and the entire cable is covered with insulation of thickness varying from .005 to .01 inch.

varying from .005 to .01 inch. In a small machine with but a single layer of conductors on the armature L=l+N. $N=(1.885,000D\times h)+d^2$.

For drum armatures $N=2(n_2\times n_3)\div n_1;$

 $N = (n_2 \times n_3) + n_1.$ for ring armatures

A general formula given by Wiener for the length of armature is

$$L = \frac{12 \times n_1 \times l}{n_2 \times n_3}; \quad n_2 = \frac{D \times \pi}{d'}; \quad n_3 = \frac{h}{d'}.$$

The minimum number of bars on the commutator is $C_{\min} = E'p + b$. The value of b depends on the current as follows:

The number which may be used, provided it does not fall below Cmin is $C = (n_2 \times n_3) + n_1.$

For drum armatures the number of conductors attached to each commutator bar must be an even number. The quotient of C, obtained as above, by the largest even number which will give a result greater than Cmin is the proper number of commutator hars for drum armatures. For ring armatures it is the quotient of C by the largest number which will give a result greater than Cmin. In each case the divisor is the number of conductors which should be attached to each bar. The flux through the armature is:

$$\phi = \frac{6 \times p \times E' \times 10^6}{N \times \text{r.p.m.}}.$$

The flux density in the armature core is

$$B = \frac{\phi}{\pi \times D \times L \times m},$$

where m is a factor depending on the percentage of polar arc. Assuming 100 per cent and 50 per cent as the limits of polar arc, the following are the respective values of m at those limits: In bipolar, smooth armature, machines m = 1.00 and .70; in bipolar, toothed armature machines m = 1.00 and .55; in smooth armature multipolar machines m = 1.00 and .625, with from 4 to 12 poles: m = 1.00 and .60 with from 14 and 20 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 machines m = 1.00 and .60 with from 15 ma poles. With toothed armatures the figures are slightly lower.

The area of the field magnet cores depends on the flux to be generated

$$\phi' = \phi \times \lambda$$
.

A value for λ is assumed, which will vary with the size and type of machine. By means of this assumed value the principal dimeasions of the magnetic circuit are calculated. The true value of λ is next calculated when the principal dimeasions of the magnetic principal dimeasions of the magnetic principal dimeasions. of the formula

Joint permeance of useful and stray paths Permeance of useful path

The permeance of a path is its magnetic conductance.

Permeance = (Permeability X Area) + Longth.

The stray paths are those across the pole-pieces, across the magnet cores and between the pole-pieces and the yoke joining the magnet cores. With the new value of λ , ϕ' is recalculated. If the true and assumed

values of A give a large difference in flux then the dimensions of the circuit

must be changed and λ recalculated.

The areas of the various portions are found by dividing the total flux by the allowable flux density. The allowable flux densities in maxwella per square inch are as follows: Wrought iron, 90,000; cast steel, 85,000; cast iron, 40,000.

The various areas being known, the winding of the magnets is calculated as shown in the section on Strength of the Magnetic Field.

Example.—Design a 200 K.W. bipolar, smooth drum armature, shunt

EXAMPLE.—Design a 200 K.W. bipolar, smooth drum armature, shant dynamo, with wrought-iron pole-pieces, and cast iron magnet cores and yoke. Volts, 500; amperes, 400; R.P.M., 450.

Assume $H_1 = 40,000$; V = 45; e = .03E; i = .025I; percentage of polar arc 85. Then E' = 515; I' = 410 and $k = 68 \times 10^{-5}$. $l = (515 \times 1 \times 100,000,000) + (68 \times 45 \times 40,000) = 420.7$ feet. $D = (12 \times 60 \times 45) + (450 \times 3.1416) = 22.91$ inches. $d^2 = 300 \times 410 + 1 = 123,000$. In this size of machine it is desirable to use cables. Each conductor may be composed of three cables in parallel, each composed of seven wires. A No. 12 B. & S. gauge wire has an area of 6530 cir. mils, and $T \times 3 \times 6530 = 137,130$, which is near enough to d^2 .

To find d^4 : Number of strands on a diameter = 3. Insulation on each strand = .015: insulation of eable = .008: diameter No. 12 wire = .090908:

strand = .005; insulation of cable = .008; diameter No. 12 wire = .080808;

 $d' = 3 \times (.0808 + 2 \times .005) + (2 \times .006) = .2884$ inch. Assume h = .625; $n_1 = 3$; $n_2 = 22.91 \times 3.1416 + .2884 = 249$; $n_3 = .625 \div .2884 = 2 + .$ Then $L = (12 \times 3 \times 420.7) + (2 \times 249) = 30.41$ inches.

Theres, C min = 515 \times 1 + 10 = 51.5; C = (249 \times 2 + 3) + 4 = 41 (too small); (249 \times 2 + 3) + 2 = 83. $\therefore C$ = 83. N = (2 \times 249) \times 2 + 3 = 332. ϕ = 6 \times 1 \times 515 \times 1.000,000,000 + 332 \times 450 = 20,683,000. Assume m = .94; B = 20,683,000 + (3.1416 \times 22.91 \times 30.41 \times .94)

• 10777.

To calculate A would require more space than can be spared bere. As-

sume $\lambda = 1.34$. $\phi' = 1.34 \times 20,683,000 = 27,715,220$. Area of magnet cores = 27,715,220 + 40000 = 692 sq. inches.

Figure 1 in the same of the s

ALTERNATING CURRENTS.*

The advantages of alternating over direct currents are: 1. Greater sim-

The advantages of alternating over direct currents are: 1. Greater simplicity of dynamos and motors, no commutators being required; 2. The feasibility of obtaining high voltages, by means of static transformers, for cheapening the cost of transmission; 3. The facility of transforming from one voltage to another, either higher or lower, for different purposes. A direct current is uniform in strength and direction, while an alternating current rapidly rises from zero to a maximum, falls to zero, reverses its direction, attains a maximum in the new direction, and again returns to zero. This series of changes can best be represented by a curve the abscissas of which represent time and the ordinates either current or electromotive force (e.m.f.). The curve usually chosen for this purpose is the sine curve, Fig. 172; the best forms of alternators give a curve that is a very close approximation to the sine curve, and all calculations and deductions of formulæ are based on it. The equation of the sine curve is $y = \sin x$, in which y is any ordinate, and x is the angle passed over by a moving radius vector.

After the flow of a direct current has been once established, the only opposition to the flow is the resistance offered by the conductor to the passage of current through it. This resistance of the conductor, in treating of alternating currents, is sometimes spoken of as the ohmic resistance. The word resistance, used alone, always means the ohmic resistance. In alternating currents, in addition to the resistance, several other quantities, which affect the flow of current, must be taken into consideration. These quantities are inductance, capacity, and skin effect. They are discussed under separate headings.

The current and the e.m.f. may be in phase with each other, that is, attain their maximum strength at the same instant, or they may not, depending on the character of the circuit. In a circuit containing only resistance, the current and e.m.f. are in phase; in a circuit containing inductance the e.m.f. attains its maximum value before the current, or leads the current. In a circuit containing capacity the current leads the e.m.f. If both capacity and inductance are present in a circuit, they will tend to neutralize each other.

Maximum, Average, and Effective Values.—The strength and the e.m.f. of an alternating current being constantly varied, the maximum value of either is attained only for an instant in each period. The maximum values are little used in calculations, except in deducing formulæ

and for proportioning insulation, which must stand the maximum pressure.

The average value is obtained by averaging the ordinates of the sine curve representing the current, and is 2 + m or 0.637 of the maximum value.

The value of greatest importance is the effective, or "square root of the mean square," value. It is obtained by taking the square root of the mean of the squares of the ordinates of the sine curve. The effective value is the value shown on alternating-current measuring instruments. The product of the greater of the effective value of the current and the residence of uct of the square of the effective value of the current and the resistance of

circuit is the heat lost in the circuit.

The comparison of the maximum, average, and effective values is as follows:

$$E_{\text{Effec.}} = E_{\text{Max.}} \times 0.707$$
; $E_{\text{Aver.}} = E_{\text{Max.}} \times 0.637$; $E_{\text{Max.}} = 1.41 \times E_{\text{Effec.}}$

Frequency.—The time required for an alternating current to pass through one complete cycle, as from one maximum point to the next (a and b, Fig. 172) is termed the period. The number of periods in a second is termed the frequency of the current. Since the current changes its direction twice in each period, the number of reversals or alternations is double the frequency. A current of 120 alternations per second has a period of 1/60

Only a very brief treatment of the subject of alternating currents can be given in this book. The following works are recommended as valuable be given in this book. The following works are recommended as valuable for reference: Alternating Currents and Alternating Current Machinery, by D. C. and J. P. Jackson; Standard Polyphase Apparatus and Systems, by M. A. Oudin; Polyphase Electric Currents, by S. P. Thompson; Electric Lighting, by F. B. Crocker, 2 vols.; Electric Power Transmission, by Louis Bell; Alternating Currents, by Bedell and Crehore; Alternating-current Phenomens, by Chas. P. Steinmetz. The two last named are highly mathems. ical.

and a frequency of 60 The frequency of a current is equal to one half the

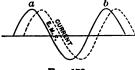
and a frequency of 60. The frequency of a current is equal to one half the number of poles on the generator, multiplied by the number of revolutions per second. Frequency is denoted by the letter f.

The frequencies most generally used in the United States are 25, 40, 60, 125, and 133 cycles per second. The Standardization Report of the A I E E recommends the adoption of three frequencies, vis. 25 60, and 120. With the higher frequencies both transformers and conductors will be less costly in a circuit of a given resistance but the capacity and inductance effects in each will be increased, and these tend to increase the cost. With high fracturation is to be become difficult to cover the attentions.

high frequencies it also becomes difficult to operate alternators in parallel.

A low frequency current cannot be used on lighting circuits, as the lights will flicker when the frequency drops below a certain figure. For arc lights the frequency should not be less than 40. For incandescent lamps it should not be less than 25. If the circuit is to supply both power and light a frequency of 60 is usually desirable. For power transmission to long distances a low frequency, say 25, is considered desirable, in order to lessen the capacity effects. If the alternating current is to be converted into direct current for lighting purpose, a low frequency may be used as the frequency will then have no effect on the lights

Inductance. —A current flowing through a conductor produces a magnetic flux around the conductor. If the current be changed in strength or direction, the flux is also changed producing in the conductor an e.m.f.



Frg. 172.

whose direction is opposed to that of the current in the conductor. This counter current in the conductor. This counter e.m.f. is the counter e.m.f. of inductance It is proportional to the rate of change of current, provided that the permeability of the medium around the conductor remains constant. The unit of inductance is the *henry* symbol L. A circuit has an inductance of one henry if a uniform variation of current at the rate of one ampere per second produces a counter e.m.f. of one volt.

The effect of inductance on the circuit is to cause the current to lag behind the e.m.f. as shown in Fig. 172, in which abscissas represent time, and

ordinates represent e.m.f. and current strengths respectively.

Capacity.—Any insulated conductor has the power of holding a quantity of static electricity. This power is termed the apacity of a circuit is measured by the quantity of electricity in it when at unit potential. It may be increased by means of a condenser. A condenser consists of two parallel conductors, insulated from each other by a non-conductor. The conductors are usually in sheet form.

The unit of capacity is a farad, symbol C. A condenser has a capacity of one farad when one coulomb of electricity contained in it produces a dif-

of one farad when one coulomb of electricity contained in it produces a dif-ference of potential of one volt. The farad is too large a unit to be conven-

iently used in practice, and the micro-farad is used instead.

The effect of capacity on a circuit is to cause the e.m.f. to lag behind the irrent. Both inductance and capacity may be measured with a Wheatstone bridge by substituting for a standard resistance a standard of induct-

ance or a standard of capacity.

Power Factor.—In direct-current work the power, measured in watts.

is the product of the volts and amperes in the circuit. In alternating curcurrent either lags or leads, the values shown on the volt and ammeters will not be true simultaneous values. Referring to Fig. 172, it will be seen that the product of the ordinates of current and e.m.f. at any particular instant will not be equal to the product of the effective values which are shown on the instruments. The power in the circuit at any instant is the product of the simultaneous values of current and e.m.f., and the volts and amperes shown on the recording instruments must be multiplied together and their product multiplied by a power factor before the true watts are obtained. This power factor, which is the ratio of the volt-amperes to the watts, is also the cosine of the angle of lag or lead of the current. Thus

 $P = I \times E \times power factor = I \times E \times cos \emptyset$

where # is the angle of lag or lead of the current.

A watt-meter, however, gives the true power in a circuit directly. The method of obtaining the angle of lag is shown below, in the section on Impedance Polygons.

Reactance, Impedance, Admittance.—In addition to the ohmic resistance of a circuit there are also resistances due to inductance, capacity, and skin effect. The virtual resistance due to inductance and capacity is termed the reactance of the circuit. If inductance only be present in the circuit, the reactance will vary directly as the inductance. If capacity only be present, the reactance will vary inversely as the capacity.

Inductive reactance =
$$2\pi fL$$
.
Condensive reactance = $\frac{1}{2\pi fC}$.

The total apparent resistance of the circuit, due to both the ohmic resistance and the reactance, is termed the impedance, and is equal to the square root of the sum of the squares of the resistance and the reactance.

Impedance = $Z = \sqrt{R^2 + (2\pi/L)^2}$ when inductance is present in the circuit.

Impedance =
$$Z = \sqrt{R^2 + \left(\frac{1}{2\pi fC}\right)^2}$$
 when capacity is present in the circuit.

Admittance is the reciprocal of impedance, $= 1 \div Z$. If both inductance and capacity are present in the circuit, the reactance of one tends to balance that of the other; the total reactance is the algebraic sum of the two reactances; thus,

$$\label{eq:Total reactance} {\rm Total \ reactance} = X = 2\pi f L - \frac{1}{2\pi f C}; \quad Z = \sqrt{R^2 + \left(2\pi f L - \frac{1}{2\pi f C}\right)^2}.$$

In all cases the tangent of the angle of lag or lead is the reactance divided by the resistance. In the last case

$$\tan \theta = \frac{2\pi f L - \frac{1}{2\pi f C}}{R}.$$

Skin Effect.—Alternating currents tend to have a greater density at the surface than at the axis of a conductor. The effect of this is to make the virtual resistance of a wire greater than its true ohmic resistance. With low frequencies and small wires the skin effect is small, but it becomes quite

important with high frequencies and large wires.

The following table, condensed from one in Foster's "Electrical Engineers' Pocket-book," shows the increase in resistance due to skin effect.

Skin-effect Factors for Conductors carrying Alternating Currents.

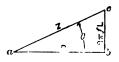
Diameter and	Frequencies.										
B. & S. Gauge.	25	40	60	100	130						
0 00 000 0000 1" 1" 11" 12"	1.001 1.002 1.007 1.020 1.053 1.098 1.265	1.001 1.002 1.005 1.006 1.016 1.052 1.118 1.223 1.531	1.001 1.002 1.005 1.006 1.008 1.040 1.111 1.239 1.420 1.826	1.005 1.006 1.010 1.015 1.022 1.100 1.263 1.506 1.765 2.290	1.008 1.010 1.017 1.027 1.039 1.156 1.397 1.694 1.983 2.560						

For virtual resistance, multiply ohmic resistance by factor from this table.

Ohm's Law applied to Alternating-current Circuits.—To apply Ohm's law to alternating-current circuits a slight change is necessary in the expression of the law. Impedance is substituted for resistance. The law should read

$$I = \frac{E}{\sqrt{R^2 + \bar{X}^2}} = \frac{E}{Z}.$$

Impedance Polygons.—1. Series Circuits.—The impedance of a circuit can be determined graphically as follows. Suppose a circuit to contain a resistance R and an inductance L, and to carry a current I of frequency f. In Fig. 173 draw the line ab proportional to R, and representing the direction of current. At b erect bc perpendicular to ab and proportional to $2\pi fL$. Join a and c. The line ac represents the impedance of the circuit. The angle b between ab and ac is the angle of lag of the current behind the e.m.f., and the power factor of the circuit is cosine b. The e.m.f. of the circuit is E = IZ.



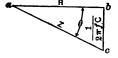


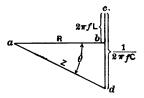
Fig. 173.

Fig. 174.

If the above circuit contained, instead of the inductance L, a capacity C, then would the polygon be drawn as in Fig. 174. The line bc would be proportional to $\frac{1}{2\pi fC}$ and would be drawn in a direction opposite to that of bc in Fig. 173. The impedance would again be Z, the e.m.f. would be $Z \times I$, but the current would lead the e.m.f. by the angle θ .

Suppose the circuit to contain resistance, inductance, and capacity. The

Suppose the circuit to contain resistance, inductance, and capacity. The lines of the impedance polygon would then be laid off as in Fig. 175. The impedance of the circuit would be represented by ad, and the angle of lag θ . If the capacity of the circuit had been such that cd was less than bc, then would the e.m.f. have led the current.



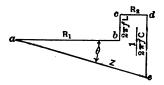


Fig. 175.

Fig. 176.

If between the inductance and capacity in the circuit in the previous examples there be interposed another resistance, the impedance polygon will take the form of Fig. 176. The lines representing either resistances, inductances, or capacities in the circuit follow each other in all cases as do the resistances, inductances, and capacities in the circuit, each line having its appropriate direction and magnitude.

Fig. 177.

Example.—A circuit (Fig. 177) contains a resistance, R_1 , of 15 ohms, a capacity, C_1 , of 100 microfarads (.000100 farad). a resistance, R_2 , of 12 ohms, an inductance L_1 , of .05 henrys, and a resistance R_3 , of 20 ohms.

Find the impedance and electromotive force when a current of 2 amperes is sent through the circuit, and the current when an e.m.f.

the circuit, and the current when an e.m.r. of 120 volts is impressed on the circuit frequency being taken as 60. Also find the angle of lag, the power factor, and the power in the circuit when 120 volts are impressed. The resistance is represented in Fig. 178 by the horizontal line ab, 15 units long. The capacity is represented by the line bc, drawn downwards from b and whose length is

length is $2x/C_1$ $2\times 3.1416\times 60\times .0001$

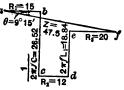


FIG. 1/8.

From the point e a horizontal line cd, 12 units long, is drawn to represent R_2 . From the point d the line de is drawn vertically upwards to represent the inductance L_1 . Its length is $2\pi L_1 = 2\times 3.1416 \times 60 \times .05 = 18.85$. From the point e a horizontal line ef, 20 units long, is drawn to represent R_3 . The line joining a and f will represent the impedance of the circuit in ohms. The angle θ , between ab and af, is the angle of lag of the e.m.f. behind the current. The impedance in this case is 47.5 ohms, and the angle of log 150. of lag is 9° 15'.

The e.m.f. when a current of 2 amperes is sent through is

 $IZ = E = 2 \times 47.5 = 95$ volts. If an e.m.f. of 120 volts be impressed on the circuit, the current flowing through will be

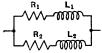
$$I = \frac{120}{Z} = \frac{120}{47.5} = 2.53$$
 amperes.

The power factor = $\cos \theta = \cos 9^{\circ} 15' = .987$.

The power in the circuit at 120 volts is

The power in the circuit at 120 volts is $I \times E \times \cos \theta = 2.53 \times 120 \times .987 = 299.6$ watts.

2. Parallel Circuits.—If two circuits be arranged in parallel, the current flowing in each circuit will be inversely proportional to the impedance of that circuit. The e.m.f. of each circuit is the e.m.f. across the terminals at either end



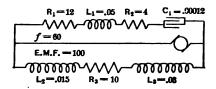
of the main circuit, where the various branches separate. Consider a circuit, Fig. 179, consisting of two branches. The first branch contains a resistance R₁ and an inductance L₁ in series with it. The second branch contains a resistance R₂ in series with an inductance L₂. The impedance of the circuit may be determined by treating each of the two branches as a separate series circuit, and drawing the impedance polygon for each branch on that assumption. Having found the impedance the current flowing in either branch will be the reciprocal of the impedance multiplied by the e.m.f. across the terminals at either end contains a resistance R₃ in series with an inductance L₂. The impedance of the current may be determined by treating each of the impedance the current is the geometrical sum of the current in the two branches.

The admittance of the equivalent simple circuit may be obtained by drawing a parallelogram, two of whose adjoining sides are made parallel to the impedance lines of each branch and equal to the two admittances respectively. of the main circuit, where the various branches

The diagonal of the parallelogram will represent the admittance of the equivalent simple circuit. The admittance multiplied by the e.m.f. gives the total current in the circuit.

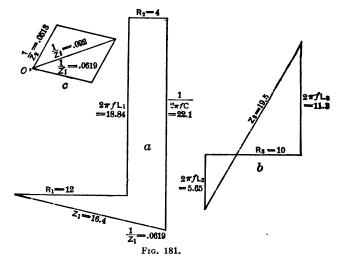
Example.—Given the circuit in Fig. 180, consisting of two branches. Branch 1 consists of a resistance $R_1=12$ ohms, an inductance $L_1=.05$ henry, a resistance $R_2=4$ ohms, and a capacity $C_1=120$ microfarads. $C_1=120$ microfarads of an inductance $C_2=.015$ henry, a resistance $C_3=10$ ohms, and an inductance $C_2=.015$ henry, a resistance $C_3=10$ ohms, and an inductance $C_2=.03$ henry. An e.m.f. of 100 volts is impressed on the circuit at a frequency of 60. Find the ad-

mittance of the entire circuit, the current, the power factor, and the power in the circuit. Construct the impedance polygons for the two branches



Frg. 180.

separately as shown in Fig. 181, a and b. The impedance in branch 1 is 16.4 ohms, and the current is $\frac{1}{16.4} \times 100 = 6.19$ amperes. The angle of



lead of the current is 12° 45'. The impedance in branch 2 is 19.5 ohms and the current is $\frac{1}{19.5} \times 100 = 5.13$ amperes. The angle of lag of the current is 61°.

The current in the entire circuit is found by taking the admittances of The current in the entire circuit is found by taking the admittances of the two branches, and drawing them from the point o, in Fig. 181 c, parallel to the impedance lines in their respective polygons. The diagonal from o is the admittance of the entire circuit, and in this case is equal to 0.092. The current in the circuit is .092×100=9.2 amperes. The power factor is 0.944 and the power in the circuit is 100×.944×9.2=868.48 watts.

Self-inductance of Lines and Circuits.—The following formula and table, taken from Crocker's "Electric Lighting," give a method of calculating the self-inductance of two parallel aerial wires forming part of the same circuit and composed of copper, or other non-magnetic material.

same circuit and composed of copper, or other non-magnetic material.

L per foot =
$$\left(15.24 + 140.3 \log \frac{2A}{d}\right) 10^{-9}$$
,
L per mile = $\left(80.5 + 740 \log \frac{2A}{d}\right) 10^{-9}$,

in which L is the inductance in henrys of each wire, A is the interaxial distance between the two wires, and d is the diameter of each, both in inches. If the circuit is of iron wire, the formule become

L per foot =
$$\left(2286 + 140.3 \log \frac{2A}{d}\right) 10^{-6}$$
,
L per mile = $\left(12070 + 740 \log \frac{2A}{d}\right) 10^{-6}$.

INDUCTANCE, IN MILLIHENRYS PER MILE, FOR EACH OF TWO PARALLEL COPPER WIRES.

-	_	1		1		1	- Turney	e Num	1			
1	0000	000	00	0	1	2	3	4	6	8	10	12
			0.982	1.019	1.056				1.243			1.46
1	260 353	1.298 1.391	1,335	$\frac{1}{1}\frac{372}{465}$	$\frac{1410}{1.502}$	1.447	$\frac{1.485}{1.577}$	1.522 1.614	1.596 1.689	1.671 1.764	$\frac{1.746}{1.838}$	1.82
1		1.614	1 651	1.596 1.688 1.760	1.725	1.764	1.800	1.838	1.912	1.986	2 061	2.13
1	707 .799	1 745 1 836	$\frac{1.784}{1.874}$	1.818	1.856	1 893 1 986	$\frac{1.931}{2.023}$	$\frac{1.968}{2.061}$	$\frac{2.043}{2.135}$	$\frac{2.117}{2.209}$	$\frac{2.192}{2.285}$	$\frac{2.26}{2.35}$
1		1 968		1.982 2.042	2.079	2 116	2.154	2.192		2.340	2,415	2.48
			2.097						2 358			2.58

Capacity of Conductors.—All conductors are included in three classes, viz. 1. Insulated conductors with metallic protection: 2. Single aerial conductor with earth return; 3. Metallic circuit consisting of two parallel aerial wires. The capacity of the lines may be calculated by means of the following formulæ taken from Crocker's "Electric Lighting".

Class 1.
$$C$$
 per foot = $\frac{7361 \times 10^{-18}}{\log (D+d)}$, C per mile = $\frac{38.83 \times 10^{-9}}{\log (D+d)}$.
Class 2. C per foot = $\frac{7361 \times 10^{-18}}{\log (4h+d)}$, C per mile = $\frac{38.83 \times 10^{-9}}{\log (4h+d)}$.
Class 3.
$$\begin{cases} C \text{ per foot of each wire} = \frac{3681 \times 10^{-18}}{\log (2A+d)} \\ C \text{ per mile of each wire} = \frac{19.42 \times 10^{-9}}{\log (2A+d)} \end{cases}$$

In which C is the capacity in farads, D the internal diameter of the metallic covering, d the diameter of the conductor, h the height of the conductor above the ground, and A the interaxial distance between two parallel wires all in inches; k is a dielectric constant which for air is equal to 1 and for pure rubber is equal to 2.5. The formulæ in cases 2 and 3 assume the wires to be bare. If they are insulated, k must be introduced in the numerator and given a value slightly greater than 1.

Single-phase and Polyphase Currents.—A single-phase current s a simple alternating current carried on a single pair of wires, and is generated on a machine having a single armature winding. It is represented by a single sine curve.

Polyphase currents are known as two-phase, three-phase, six-phase, or

any other number, and are represented by a corresponding number of sine curves. The most commonly used systems are the two-phase and three-

phase.

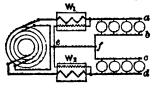
1. Two-phase Currents.—In a two-phase system there are two single-phase alternating currents bearing a definite time relation to each other and represented by two sine curves (Fig. 182). The two separate currents

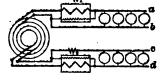


Fig. 182.

may be generated by the same or by separate machines. If by separate machines, the armatures of the two should be positively coupled together. Two-phase currents are usually generated by a machine with two armature windings, each winding terminating in two collector rings. The two windings are so related that the two currents will be 90° apart. For this reason two-phase currents are also called "quarter-phase"

Two-phase currents may be distributed on either three or four wires. The three-wire system of distribution is shown in Fig. 183. One of the return wires is dispensed with, connection being made across to the other as shown. The common return wire should be made 1.41 times the area of either of the other two wires, these two being equal in size.





Frg. 183.

Frg. 184.

The four-wire system of distribution is shown in Fig. 184. The two phases are entirely independent, and for lighting purposes may be operated

as two single-phase circuits.

2. Three-phase Currents.—Three-phase currents consist of three alternating currents, differing in phase by 120°, and represented by three sine curves, as in Fig. 185. They may be distributed by three or six wires. If distributed by the six-wire system, it is analogous to the four-wire, twophase system, and is equivalent to three single-phase circuits. In the three-wire system of distribution the circuits may be connected in two different ways, known respectively as the Y or star connection, and the \$\Delta\$ (delta) or mesh connection.

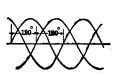


Fig. 185.

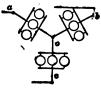


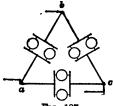
Fig. 186.

The three circuits are joined The Y connection is shown in Fig. 186. at the point o, known as the neutral point, and the three wires carrying the current are connected at the points a, b, and c, respectively. If the three circuits ao, bo, and co are composed of lights, they must be equally loaded or the lights will fluctuate. If the three circuits are perfectly balanced, the lights will remain steady. In this form of connection each wire may be

lights will remain steady. In this form of considered as the return wire for the other two. If the three circuits are unbalanced, a return wire may be run from the neutral point o to the neutral point of the armature winding on the generator. The system will then be four-wire, and will work properly with unbalanced circuits.

The Δ connection is shown in Fig. 187. Each of the three circuits ab, ac, bc, receives the current due to a separate coil in the armature winding. This form of in the armature winding. This form of connection will work properly even if the circuits are unbalanced; and if the circuit contains lamps, they will not fluctuate when the circuit changes from a balanced to an unbalanced condition, or vice versa.

Measurement of Power in Polyphase Circuits.—1. Two-lamps currents distributed by four wirest.



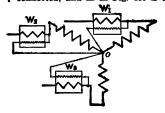
phase Circuits.—The power of two-phase currents distributed by four wires may be measured by two wattmeters introduced into the circuit as shown in Fig. 184. The sum of the readings of the two instruments is the total power. If but one wattmeter is available, it should be introduced first in one circuit,

and then in the other. If the current or e.m.f. does not vary during the operation, the result will be correct. If the circuits are perfectly balanced, twice the reading of one wattmeter will be the total power.

The power of two-phase currents distributed by three wires may be measured by two wattmeters as shown in Fig. 183. The sum of the two readings is the total power. If but one wattmeter is available, the coarsewire coil should be connected in series with the wire of and one extremity of the pressure-coil should be connected to some point on of. The other end should be connected first to the wire a and then to the wire d, a reading being taken in each position of the wire. The sum of the readings gives the

power in the circuits.

2. Three-phase Currents.—The power in a three-phase circuit may be measured by three wattmeters, connected as in Fig. 188 if the system is Y-connected, and as in Fig. 189 if the system is Δ-connected. The sum



Frg. 188.

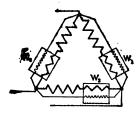
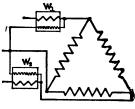


Fig. 189.

of the wattmeter readings gives the power in the system. If the circuits are perfectly balanced, three times the reading of one wattmeter is the total power.

The power in a A-connected system may be measured by two wattmeters, as shown in Fig. 190. If the power factor of the system is greater than 0.50, the arithmetical sum of the readings is the power in the circuit. If the power factor is less than 0.50, the arithmetical difference of the readings is the power. Whether the power factor is greater or less than 0.50 may be discovered by interchanging the wattmeters without disturbing the

relative connection of their coarse- and fine-wire coils. If the deflections of



Frg. 190.

the needles are reversed, the difference of the readings is the power. If the needles are deflected in the same direction as at first, the sum of the readings is the power.

Alternating-current Generators.—These differ little from directurrent generators in many respects. Any direct-current generator, if provided with collector rings instead of a commutator could be used as a single-phase alternator, The frequency would in most cases, however, be too low for any practical use. The fields of alternators are always separately excited; the machines are sometimes compounded by shunting some

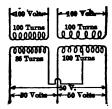
of their own current around the fields through a rectifying device which changes the current to pulsating direct current. In all large machines the armature is stationary and the field-magnets revolve.

TRANSFORMERS, CONVERTERS, ETC.

Transformers.—A transformer consists essentially of two coils of wire, one coarse and one fine, wound upon an iron core. The function of a transformer is to convert electrical energy from one potential to another. If the transformer causes a change from high to low voltage, it is known as a "step-down" transformer; if from low to high voltage, it is known as a "step-down" transformer.

The relation of the primary and secondary voltages depends on the number of turns in the two coils. Transformers may also be used to change

ber of turns in the two coils. Iransformers current of one phase to current of another phase. The windings and the arrangement of the transformers must be adapted to each particular case. In Fig. 191 an arrangement is shown whereby two-phase currents may be converted into three-phase. Two transformers are required, one having its primary and secondary coils in the relation of 100 to 100, and the other having its primary and secondary in the relation of 100 to 86. The secondary of the 100-to-100 transformer is tapped at its middle point and joined to one terminal of the other secondary. Between any pair of the three remaining terminals of the secondaries there will exist a difference of potential of 50.



Frg. 191.

There are two sources of loss in the transformer, vis., the copper loss and the iron loss. The copper loss is proportional to the square of the current, being the l^2R loss due to heat. If l_1 , R_1 , be the current and resistance respectively of the primary, and l_2 . R_2 , the current and resistance respectively of the secondary, then the total copper loss is $Wc = l_1^2R_1 + l_2^2R_2$ and the percentage of copper loss is $\frac{l_1^2R_1 + l_2^2R_2}{W}$, where W_p is the energy delivered

to the primary. The iron loss is constant at all loads, and is due to hysteresis

and eddy currents.

Transformers are sometimes cooled by means of forced air or water currents or by immersing them in oil, which tends to equalize the temperature

in all parts of the transformer.—The efficiency of a transformer is the ratio of the output in watts at the secondary terminals to the input at the primary terminals. At full load the output is equal to the input less the iron and copper losses. The full-load efficiency of transformers is usually very high, being from 92 per cent. to 98 per cent. As the copper loss varies as the square of the load, the efficiency of a transformer varies considerably at different loads. Transformers on lighting circuits usually operate at full

load but a very small part of the day, though they use some current all the

time to supply the iron losses. For transformers operated only a part of the time the "all-day" efficiency immore important than the full-load efficiency. It is computed by comparing the watt-hours output to the watt-hours input. The all-day efficiency of a 10-K.W. transformer, whose copper and iron losses at full load are each 1.5 per cent, and which operates 3 hours at full load, 2 hours at half load, and 19 hours at no load, is computed as follows:

Iron loss, all loads = $10 \times .015 = .15$ K.W. Copper loss, full load = $10 \times .015 = .15$ K.W. Copper loss, full load = $.15 \times .(4)^3 = .0375$ K.W. Iron loss K.W. hours = $.15 \times 24 = 3.6$ Copper loss, full load, K.W. hours = $.15 \times 3 = .45$. Copper loss, full load, K.W. hours = $.0375 \times 2 = .075$. Output. K.W. hours = $.(10 \times 3) + (5 \times 2) = .40$. Input, K.W. hours = $.40 \times 3 + .6 \times 45 = .075 = .44$. 125. All-day efficiency = $.40 \times 40 \times 40 = .40 \times$

The transformers heretofore discussed are constant-potential transformers and operate at a constant voltage with a variable current. For the operation of lamps in series a constant-current transformer is required. There are a number of types of this transformer. That manufactured by the General Electric ('o. operates by causing the primary and secondary coils to

approach or to separate on any change in the current.

Converters, etc.—In addition to static transformers, various machines are used for the purpose of changing the voltage of direct currents or the voltage. phase or frequency of alternating currents, and also for changing alternating currents to direct or vice versa. These machines are all rotary

and are known as rotary converters, motor-dynamos, and dynamotors.

A rotary converter consists of a field excited by the machine itself, and an armature which is provided with both collector rings and a commuta-tor. It receives direct current and changes it to alternating, working as a clirect-current motor, or it changes alternating to direct current. working as a synchronous motor.

A motor-dynamo consists of a motor and a dynamo mounted on the same

base and coupled together by a shaft.

A dynamotor has one field and two armature windings on the same core. One winding performs the functions of a motor armature, and the other those of a dynamo armature.

A booster is a machine inserted in series in a direct-current circuit to change its voltage. It may be driven either by an electric motor or other-

wise

ALTERNATING-CURRENT MOTORS.

Synchronous Motors.—Any alternator may be used as a motor. provided it be brought into synchronism with the generator supplying the current to it. The operation of the alternating-current motor and generator current to it. The operation of the alternating-current motor and generator is similar to the operation of two generators in parallel. It is necessary to supply direct current to the field. The field circuit is left open until the machine is in phase with the generator. If the motor has the same number of poles as the generator, it will run at the same speed; if a different number the speed will be that of the generator multiplied by the ratio of the number of poles of the motor to that of the generator. Single-phase, synchronous motors are not self-starting. Polyphase motors may be made self-starting but it is better to bring the machines to speed by independent means before but it is better to bring the machines to speed by independent means before supplying the current. The machines may be started by a small induction motor, the load on the synchronous motor being thrown off, or the field may be excited by a small direct-current generator belted to the motor, and may be excited by a small direct-current generator betted to the motor, and this generator may be used as a motor to start the machine, current to run it being taken from a storage battery. If the field of a synchronous motor be properly regulated to the load, the motor will exercise no inductive effect on the line, and the power factor will be 1. If the load varies the current in the motor will either lead or lag behind the e.m.f. and will vary the power factor. If the motor be overloaded so that there is a diminution of speed the motor will fall out of step with the generator and stop.

Synchronous motors are often put on the same circuit with induction motors. The synchronous motor in this case may, by increasing the field excitation, be made to cause the current to lead, while the induction motor

will cause it to lag. The two effects will thus tend to balance each other

and cause the power factor of the circuit to approach 1. Synchronous motors are best used for large units of power at high voltages, where the load is constant and the speed invariable. They are unsatisfactory where the required speed is variable and the load changes. Two great disadvantages of the synchronous motor are its inability to start

under load, and the necessity of direct-current excitation,
Induction Motors.—The distinguishing feature of an induction motor
is the rotating magnetic field. It is thus explained: In Fig. 192 let ab, cd
be two pairs of poles of a motor, a and b being wound from



Fig. 192.

one leg or pair of wires of a two-phase alternating circuit, and c and d from the other leg, the two phases being 90° apart. At the instant when a and b are receiving maximum current so as to make a a north pole and b a south pole, c and d are demagnetized, and a needle placed between the poles would stand as shown in the cut. During the progress of the cycle of the current the magnetic flux at a decreases and that at c increases causing the point of resultant maximum intensity to shift, and the needle to move clockwise toward c. A complete rotation

of the resultant point is performed during each cycle of the current. An armature placed within the ring is caused to rotate simply by the shifting of the magnetic field without the use of a collector ring. The words rotating magnetic field refer to an area of magnetic intensity and must be distinguished from the words revolving field which refer to the portion of the machine constituting the field-magnet.

The field or "primary" of an Induction motor is that portion of the machine to which current is supplied from the outside circuit.

The armature or "secondary" is that portion of the machine in which currents are induced by the rotating magnetic field. Either the primary of the secondary was vavolve. In the more modern machines the secondary

currents are induced by the rotating magnetis first. Etters the primary of the secondary may revolve. In the more modern machines the secondary revolves. The revolving part is called the "rotor." the stationary part the "stator." The rotor may be either of the ring or the drum type, the drum type being more common. A common type of armature is the "squirrel-cage." It consists of a number of copper bars placed on the armature-core eage. It consists of a number of copper uses placed in the armature-cope and insulated from it. A copper ring at each end connects the bars. The field windings are always so arranged that more than one pair of poles are produced. This is necessary in order to bring the speed down to a practical limit. If but one pair of poles were produced, with a frequency of 60, the revolutions per minute would be 3600.

of 60, the revolutions per minute would be 3600.

The revolving part of an induction motor does not rotate as fast as the field, except at no load. When loaded, a slip is necessary, in order that the lines of force may cut the conductors in the rotor and induce currents therein. The current required for starting an induction motor of the squirrel-cage type under full load is 7 or 8 times as great as the current for running at full-load. A type of induction motor known as 'Form L,' built by the General Electric Co., will start with the full load current, provided the starting torque is not greater than the torque when running at full load. Induction motors should be run as near their normal primary e.m.f. as cossible, as the output and torque are directly proportional to the square.

possible, as the output and torque are directly proportional to the square of the primary pressure. A machine which will carry an overload of the precent at normal e.m.f. will hardly carry its full load at 80 per cent of the normal e.m.f.

An induction motor exercises its greatest torque when standing still, and its least when running in synchronism with the rotating field. If it be overloaded it will slow down until the induced currents in the armature are sufficient to carry the load.

ALTERNATING-CURBENT CIRCUITS.

Calculation of Alternating-current Circuits.—The following formulæ and tables are issued by the General Electric Co. They afford a convenient method of calculating the sizes of conductors for, and determining the losses in alternating current circuits. They apply to circuits in which the conductors are spaced 18 inches apart, but a slight increase or decrease in this distance does not alter the figures appreciably. If the conductors are less than 18 inches apart, the loss of voltage is decreased and vice versa.

Let W = total power delivered in watts;
D = distance of transmission (one way) in feet;
P*= per cent loss of delivered power (W);
E = voltage between main conductors at consumer's end of circuit;
K = a constant; for continuous current = 2160;
T = a variable depending on the system and nature of the load; for

continuous current =1; M = a variable, depending on the size of wire and the frequency; for continuous current = 1;

A = a factor; for continuous current = 6.04.

Area of conductor, circular mils = $\frac{D \times W \times K}{P \times E^2}$; Current in main conductors = $\frac{W \times T}{E}$;

Volts lost in lines = $\frac{P \times E \times M}{100}$; Pounds copper = $\frac{D^2 \times W \times K \times A}{P_1 \times E^2 \times 1,000,000}$;

The following tables give values for the various constants.

Per cent of		Value	of K			·	g.		
Power Factor.	100	95	85	80	100	95	85	80	Val
System Single-phase	2160 1080 1086	2400 1200 1200	3000 1500 1500	3380 1690 1690	1.00 .50 .58			1 25 62 .72	12 08

Values	of	M	
--------	----	---	--

		2	5 Cycle	es.	60	Cycle	es.	125 Cycles.			
No. A. W. Gauge.	Area, Circular Mils.	Lights only Power Factor 95%.	Motors and Lights Power Factor 85%.	Motors only Power Factor 80≴.	Lights only Power Factor 95%.	Motors and Lights Power Factor 85%.	Motors only, Power Factor 80%.	Lights only Power Factor 95%.	Motors and Lights Power Factor 85%.	Motors only Power Factor 80%	
0000 000 00 0 0 1 2 3 4 5 6	211,600 167,805 133,079 105,592 83,694 66,373 52,633 41,742 26,250 20,816 16,509	1.23 1.18 1.14 1.107 1.05 1.03 1.02 1.00 1.00	1.33 1.24 1.16 1.10 1.05 1.02 1.00 1.00 1.00 1.00	1.34 1.24 1.16 1.09 1.00 1.00 1.00 1.00 1.00	1.62 1.49 1.34 1.31 1.24 1.18 1.14 1.11 1.08 1.05 1.03 1.02	1.99 1.77 1.60 1.46 1.34 1.25 1.18 1.11 1.06 1.02 1.00	2.09 1.95 1.66 1.49 1.36 1.17 1.10 1.04 1.00 1.00	2 35 2.08 1.86 1.71 1.56 1.45 1.35 1.27 1.21 1.16 1.12	3.24 2.77 2.40 2.13 1.88 1.70 1.53 1.40 1.30 1.21 1.14 1.09	3.49 2 94 2 57 2 25 1.97 1.57 1.43 1.31 1.21 1.13	

^{*} P should be expressed as a whole number not as a decimal; thus a per cent loss should be written 5 and not .05.

Relative Weight of Copper Required in Different Systems for Equal Effective Voltages.

Direct current, ordinary two-wire system	1.000
" three-wire system, all wires same size	. 375
" " " neutral one-half size	.313
Alternating current, single-phase two-wire, and two-phase four-wire	1.000
Two-phase three-wire, voltage between outer and middle wire same	
as in single-phase two-wire	.729
voltage between two outer wires same	1.457
Three-phase three-wire	.750
" four-wire	333

The weight of copper is inversely proportional to the squares of the voltages, other things being equal. The maximum value of an alternating e.m.f. is 1.41 times its effective rating. For derivation of the above figures, see Crocker's Electric Lighting, vol. ii.

STANDARD SIZES OF ELECTRICAL MACHINES.

(Chiefly Selected from Bulletins of the General Electric Co.)

Direct-driven Direct-current Generators for Lighting and Power.

		125	or 250 V	olts.			275 Volts.									
. 68		Speed, R.p.m.	Weight, Lbs.	Din	n en si	io ns .	Poles.		Speed, R.p.m.	Weight, Lbs.	Dim	ensi	ons			
Poles.	Kw	S. R.	¥ T	A.	B.	C.	Pol	Kw.	S. S.	ă I	A.	В.	c.			
6	25 35	305 800	3,500 4,600	40 42	48 52	21 23	10 10	300 400	150 150	40,000 55,000	116 132	129 145	40 41			
6	50 75	280	6,250 8,800	46 55	53 66	26 26	10	400 550	120	62 000 82,000	135 152	147 180	42 42			
8	100 160		11,200 15,000	58 67	71 85	28 30	18 18	1,000	100	95,000 115,000	178 178	506	44 46			
8 8	160 200	150 200	21,000 22,000	79 79	96 96	35 85	24	1,600	100	175,000	261	25	54			
8	200	150	30,000	85	112	37										

Direct-connected Direct-current Railway Generators, Form H. 575 Volts.

ės.	Poles. Kw.	₽ E.	Weight, Lbs.	Dim	ensi	ons.	Ś		ë ;	Weight, Lbs.	Dimensions.			
Pol	Kw	R.p.	¥e L	A. B. C.		Poles.	KW	Speed R.p.n	¥ L	A.	B.	C.		
<u>-</u> 6	100	275	15,000	81	95	28	10	500	100	96,000	160	178	48	
6	150		29,000	99	114	35	10	500	90	110,000	[61]	180	50	
6	500		39,000	116	183	37	10	500	80	118,000	162	180	51	
6	500		50,000	119,	136	41	12	650	90	117,000	178	188	48	
6 8	200	120	58,000	121	140	48	12	800	120	113,000	178	188	48	
8	300	150	55,000	125	141	41	14 14	800	100	118,000	186	200	46	
8	300	120	65,000	129	145	45	14	800	80	185,000	187	201	48	
8	30 0	100	75,000	130	146	48	16	1,000	80	150,000	187	500	50	
8	400	150	68,000	132	148	45	18	1,200	80	156,000	196	221	48	
8	400	120	79,000	135	150	48	22	1,600	75	180,000	240	245	45	
8	400	100	90,000	138	152	50	26	2,000	75	188,000	285	313	52	
10	500	120	81,000	145	154	45	26 28	2,400	75	225,000	320	364	52	

Dimensions in inches: A, height of frame above floor. B, diameter of ame at base. C, width of frame base.

Belted Generators. Compound- or Shunt-wound. Type CE.

		l	Amp.		np. Weight,		Dimen	sions, l	inches.	•
Poles.	Kw.	Speed.	(a)	(b)	Lbs.	A.	В.	c.	D.	E.
2 2	11/6	1,850 2,100	12 18	6 9	} 845	28	17	16	5	4
2 2 2 2 2 2	114 214 214 214 214 214 214 214 214 214	1,350 2,100	18 80	9 15	455	81	20	20	5	414
2 2	334 516	1,850 1,875	80 44	15 22	630	88	22	21	5	41/4
4	512 716	1,050 1,625	44 60	22 80	870	88	26	24	734	6
4	717	850 1,300	60 88	80 44	1,240	41	32	27	93/4	7
4	11 15	850 1,300	88 120	44 60	1,660	49	83	80	10	81/4

(a) Full load, 125 volts; no load voltage, 120. (b) Full load, 250 volts; no load voltage, 240.

Belted Generators. Slow Speed. Form H (Four Poles).

	١	Ampe	res, fu	ll load.	Weight,†	Dimensions, Inches.*						
Kw. S	Speed.	125 V.	250 V.	500 V .	Lbs.	A.	В.	c.	D.	E.		
61/6	950	52	26	18	1,030	38	86	26	11	41 61 81 81		
9	900	72	86	18	1,435	48	40	29	1114	61		
1816	850	108	54	27	1,900	50	44	83	1214 1834	8		
17	750	186	68	84	2,665	57	46	85	1884	8		
20 30	700	160	80	40	8,350	61	53	89	15	10		
30	675	240	120	60	4,935	68	59	46	2016	11		
40	605	820	160	80	5,690	72	63	49	2284	15		
40 50	600	400	200	100	7,140	79	66	52	28	18		
75	550	600	300	150	8,800	92	68	56	25	24		

Direct-current Motors. Type CE.

н.Р.	Spec	d (Shu	ın t-w o	und).	Weight,	Dimensions, Inches.*						
	110 V.	115 V.	125 V.	500 V.	Lbs.	A.	B.	c.	D.	E.		
2 8	1,000	1,025	1,075	1,200 1,800	} 885	28	17	20	5	4		
2 8 5 5	1,000 1,680	1,025 1,725	1,075 1,820	1,200 1,800	465	81	20	20	5	41/6		
5 71 <u>6</u>	975 1,490	1,000 1,525	1,050 1,600	1,250 1,650	540	83	22	21	5	41/6		
714 714 10	795 1,220	815 1,250	860 1,810	1,000 1,500	} 800	38	26	24	73/4	6		
10 15	685 975	1,000	1,050	800 1,200	1,150	41	82	27	9%	7		
15 20	665 1,000	1,040	750 1,125	750 1,125	1,400	49	33	80	10	81/		

Speeds for 220, 230, and 250 volts are the same as for 110, 115, and 125 volts.

^{*} Dimensions in inches: A, length over all in direction of shaft, including pulley; B, width or diameter at feet of frame; C, height above floor; D, diameter of pulley; E, face of pulley.
† With rails; includes pulley, but not wood base-frame.

STANDARD BELTED MOTORS AND GENERATORS.

(Crocker-Wheeler Electric Co., 1898.)

	Outpu Motor. D						Effi- ciency.			Outside Dimen- sions in inches. Net Over All.				e. C.
Size.	No. Poles.	H.P.	Speed.	Dyna *	Speed.	1/2 Load.	Full Load.	Net Weight, pounds.	Length.	Height.	Width.	Diam.	Fасе.	Rise Temp.
225 150 100 75 50 85 15 10 774 5	464444400000000000	225 150 100 75 50 35 25 10 71/2 8	400 600 625 650 700 750 800 850 900 975 1000 1200 1875	90 60 45 31.5 22.5 13 10 7.5 5 8 2	450 450 650 675 700 750 825 900 1000 1150 1175 1200 1800 2200	85 88 90 89 88 86 821 83 83 82 80 75 67 55	93 92 92 92 91 91 881 88 87 86 85 841 81 75 73 61	80000 11800 11000 6500 4500 3350 2400 1510 920 760 510 410 288 205 100 700	138 85143 7:56 6914 4676 41 3614 3614 3614 2814 1914 1734 15 978	7334 6514 55214 4614 4014 3696 8114 2134 2134 1156 1574 1106 814	6714 07 5134 4614 42 3714 33 2834 2314 1914 1614 1414 1314 10 856 614	88 32 23 20 17 15 13 11 9 8 7 6 5 4 3 11/2	29 23 16 14 12 11 9 8 7 6 5 4 ¹ / ₄ 4 3 ¹ / ₂ 3 ¹ / ₄ 1	- 45 45 45 45 45 45 45 45 45 45 45 45 45

Small Belted Dynamos and Motors (4-pole).

(Crocker-Wheeler Co.)

Size.	Out	put.		Motor Speed.		amo ed.	ight, bs.	Dimensions, Inches. (See foot-note on p. 1077.)				
	H.P.	Kw.	115- 230 V.	500 ∇.	125- 250 ∇.	550 V.	E E	A.	В.	D.	E.	
8 {	3 4	21/6 81/6	975 1,800	1,100 1,875	1,200 1,600	1,400 1,750	295	21	18	6	41/6	
5 {	5 61,6	416 594	950 1,150	1,100 1,350	1,150 1,400	1.875 1,700	} 400	22	20	7	5	
716	616 716 914	61.4 81.4	875 1,100	925 1,175	1,050 1,300	1,150 1,450	540	25	21	8	51/2	

Bi-polar Dynamos and Motors. (Crocker-Wheeler Co.)

Size.	o	Output.		otor eed.		amo eed.	Net Weight,	Pulley.		
CALC	H.P.	Kw.	115- 230 V.	500 V.	125- 250 V.	550 V.	Lbs.	Diam.	Face.	
2 {	2 216	2	975 1.500	1,025 1,500	1,800	1,450	288	5	4	
1 }	1	1	1,000	1.050	1,300	1,450	205	4	83,4	
1/6 1/6 1/12	11/4	16	1,200	1,350	1,600	1,750	100	8	1 8	
34	1/2	1 1/2	1,400	1,600	1,800	1,950	70	8	214	
1/6	1/8	110 watts	1,600	1,600	2,200		27	136	l i	
1/12	1/25		1,800				19	13/4 13/4	Grooved	

Direct-connected Alternators. (General Electric Co.)

25 CYCLES.

Poles,	Kw.	R.P.M.	Poles.						Poles.	Kw.	R.P.M.
12	78	250	24	360	125	28	810	107	3.1	1800	94
12	108	250	28	86 0	107	82	810	94	40	1800	75
14	160	214	20	540	150	24	1200	125	88	2700	94
16	240	187.5	24	540	125	28	1200	107	40	2700	75
20	240	150	28	540	107	32	1200	94	40	4080	75
20	860	150	24	810	125	28	1800	107	40	6000	75

From 860 to 810 kw. the machines are wound for 370 volts; from 72 to 810 kw. for 480 volts; from 810 to 6000 kw. for 2300 volts; and from 860 to 6000 kw. for 6600 and 13,200 volts.

60 CYCLES.

Poles.	Kw.	R.P.M.	Poles.	Kw.	R.P.M	Poles.	Kw.	R,P.M	Poles.	Kw.	R.P.M.
26	72	276	56	860	128.5	60	810	120	80	1800	~ 90
28	108	257	64	360	112.5	72	810	100	72	2700	100
32	160	225	48	540	150	60	1200	120	84	2700	86
36	240	200	56	540	128.5	72	1200	100			
48	240	150	69	54 0	1 0 6	64	1800	112.5			
48	360	150	52	810	138.5	72	1800	100	,		

From 72 to 360 kw. the machines are wound for 240 volts; from 72 to

From 72 to 360 kw. the machines are wound for 240 volts; from 72 to 2500 kw. for 480 volts; from 72 to 2700 kw. for 2800 volts; from 540 to 3700 kw. some machines are wound for 6600 volts.

The kw. ratings in the above table are based on the load that may be carried without a rise in temperature of any part exceeding 40° C. above the surrounding atmosphere when running continuously with non-inductive full load. An overload of 25%, non-inductive, may be carried for two hours without heating more than 55° C. When full non inductive load is thrown off, with fixed normal excitation, the voltage will rise approximately 8%. When full load with 80% power factor is thrown off, with fixed excitation, the rise will be approximately 2%.

A rating one-sixth less is given all machines for a rise of temperature not

A rating one-sixth less is given all machines for a rise of temperature not exceeding 35°C. above surrounding atmosphere.

Belt-driven Alternating-current Generators, 60 Cycles.

Size. Kw	50	75	100	150	200
No. of poles 6	6	8	8	12	12
Speed, r.p.m 1200	1200	900	900	600	600
Weight, with rails, lbs 3000	3800	4750	5850	8100	9650
Floor-space with rails, ins. 51×56	58×56	68×67	74×67	80×79	87×79
Size of pulley, ins 16×7	16×10	21×13	21×15	82×19	32×28

Induction Motors. 60 Cycles.

H.P	1	2	3	5	7.8	5 10	15	20	80	40	50	75	100	150	200
Poles	4	4	4	6	6	6	6	8				10	12	12	14
Speed														600	
Weight										3000	3490	5220	6800	9000	11000
Width, ins.*.										48	50	60	57	67	77
Length, "									57	57	59	64	78	78	102
Pulley, diam.	416	416	414	8	8	8	8	18	18	13	16	16	26	28	36
" width	912	912	214	. 4	- 5	6	7	7	Q	11	12	17	17	91	98

*In direction of shaft, Form K motors. Forms L and M are 4 to 10 ins. wider.

SYMBOLS USED IN RECTRICAL DIAGRAMS.

-C C- SPST -C C C- SPOT BB DPST

二吕吕吕 DPDT Galvanometer.

Voltmeter. Ammeter.

Wattmeter

Switches: S, single;
D, double; P, pole;
T, throw.

-~~~ Non-inductive Resistance.

 \sim Inductive ; Resistance.

Capacity or Condenser.

Lamps.

Motor or Generator. Shunt-wound Motor or Generator.

Series-wound Motor or Generator.











Two-phase Three-phase Generator. Generator.

Battery.

Transformer.

Compoundwound Motor excited Motor or Generator. or Generator.

Separately

APPENDIX.

STRENGTH OF TIMBER.

Safe Loads in Tons, Uniformly Distributed, for White-oak Heams.

(In accordance with the Building Laws of Boston.)

Formula: $W = \frac{4PBD^4}{3L}$

W = safe load in pounds; P, extreme fibrestress = 1000 lbs. per square inch, for white oak; B, breadth in inches; D, depth in inches; L, distance between supports in inches.

Size of Timber.		Distance between Supports in feet.													
Size	6	8	10	11	12	14	15	16	17	18	19	21	28	25	26
				8	afe l	Load	in T	ons o	f 20	00 Pc	und	 8.	١	!	
2×6 2×8 2×10 2×12 3×6 3×13 3×14 3×16 4×10 4×12 4×14 4×16 4×18	0.67 1.19 1.85 2.67 1.00 1.78 2.78 4.00 5.45 7.11 3.70 5.33 7.26 9.48 19.00	2.00 0.75 1.33 2.08 3.00 4.08 5.33 2.78 4.00 5.44 7.11	0.71 1.11 1.60 0.60 1.07 1.67 2.40 3.27 4.27 2.22 3.20 4.36 5.69	0.65 1.01 1.45 0.55 0.97 1.52 2.18 2.97 3.88 2.02 2.91 3.96 5.17	0.59 0.93 1.33 0.50 0.89 1.89 2.00 2.72 3.56 1.85 2.67 3.63 4.74	0.51 0.79 1.14 0.43 0.76 1.19 1.71 2.37 3.05 1.59 2.29 3.11 4.06	0.47 0.74 1.07 0.40 0.71 1.11 1.60 2.18 2.84 1.48 2.13 2.90 3.79	0.44 0.69 1.00 0.37 0.67 1.04 1.50 2.04 2.67 1.39 2.00 2.72 3.56	0.42 0.65 0.94 0.35 0.63 0.98 1.41 1.92 2.51 1.88 2.56 3.35	0.40 0.62 0.89 0.33 0.59 0.98 1.82 2.37 1.28 1.78 2.42 3.16	0.37 0.58 0.84 0.32 0.56 0.88 1.26 1.72 9.25 1.17 1.68 2.29 3.00	0.58 0.76 0.29 0.51 0.79 1.14 1.56 2.03 1.06 1.53 2.07	0.48 0.70 0.26 0.46 0.72 1.04 1.42 1.86 0.97 1.39 1.90 2.47	0.44 0.64 0.67 0.96 1.31 1.71 0.89 1.28	0.69 0.41 0.64 0.95 1.25 1.64 0.85 1.68 2.19

For other kinds of wood than white oak multiply the figures in the table by a figure selected from those given below (which represent the safe stress per square inch on beams of different kinds of wood according to the building laws of the cities named) and divide by 1000,

	Hemlock.	Spruce.	White pine.	Oak.	Yellow Pine.
New York Boston Chicago		900 750	900 750 900	1100 1000† 1080	1100* 1250 1440

^{*} Georgia pine.

MATHEMATICS.

Formula for Interpolation.

$$a_n = a_1 + (n-1)d_1 + \frac{(n-1)(n-2)}{1.2}d_2 + \frac{(n-1)(n-2)(n-3)}{1.2.3}d_2 + \cdots$$

 a_1 = the first term of the series; n, number of the required term; a_n , the required term; d_1 , d_2 , d_3 , first terms of successive orders of differences between a_1 , a_2 , a_3 , a_4 , successive terms.

Example.—Required the log of 40.7, logs of 40, 41, 42, 43 being given as

Terms
$$a_1$$
, a_8 , a_9 , a_4 : 1.6021 1.6128 1.6232 1.6335 1st differences: .0107 .0104 .0103 2d ...0001 -...0003 -..0001 +...0002

For log. 40 n = 1; log 41 n = 3; log 40.7 n = 1.7, n - 1 = 0.7, n - 2 = -0.8, n-8=-.1.8.

$$a_{\rm pl} = 1.8021 + 0.7(.0107) + \frac{(0.7)(-0.3)(-.0003)}{2} + \frac{(0.7)(-0.3)(-0.3)(-1.3)(.0002)}{6}$$

Maxima and Minima without the Calculus.—In the equation $y = a + bx + cx^2$, in which a, b, and c are constants, either positive y is a minimum when x = -b + 2c; if c be negative y is a maximum when x = -b + 2c. In the equation y = a + bx + c/x, y is a minimum when bx = c/x.

a minimum when ox = c/x. APPLICATION.—The cost of electrical transmission is made up (1) of fixed charges, such as superintendence, repairs, cost of poles, etc., which may be represented by a; (2) of interest on cost of the wire, which varies with the sectional ārea, and may be represented by bx; and (3) of cost of the energy wasted in transmission, which varies inversely with the area of the wire, or c/x. The total cost, y = a + bx + c/x, is a minimum when item 2 = item 8. or bx = c/x.

RIVETED JOINTS.

Pressure Required to Drive Hot Rivets.-R. D. Wood & Co., Philadelphia, give the following table (1897):

POWER TO DRIVE RIVERS HOT.

Size.	Girder- work.	Tank- work.	Boiler- work.	Size.	Girder- work.	Tank- work.	Boiler- work.
in.	tons. 9 12 15 22 30	tons. 15 18 22 80 45	tons. 20 25 33 45 60	in. 11/6 11/4 11/4 18/4	tons. 38 45 60 75	tons. 60 70 85 100	tons. 75 100 125 150

The above is based on the rivet passing through only two thicknesses of plate which together exceed the diameter of the rivet but little, if any.

As the plate thickness increases the power required increases approxi-

As the plate thickness increases the power required increases approximately in proportion to the square root of the increase of thickness. Thus, if the total thickness of plate is four times the diameter of the rivet, we should require twice the power given above in order to thoroughly fill the rivet-holes and do good work. Double the thickness of plate would increase the necessary power about 40%.

If takes about four or five times as much power to drive rivets cold as to drive them hot. Thus, a machine that will drive \(\frac{1}{2} \)-in, rivets hot will usually drive \(\frac{1}{2} \)-in, rivets cold (steel). Baldwin Locomotive Works drive \(\frac{1}{2} \)-in, soft-

on rivets cold with 15 tons.

HEATING AND VENTILATION.

Table of Capacities for Hot-blast or Plenum Heating with Fans or Blowers.

(Computed by F. R. Still, American Blower Co., Detroit, Mich.)

SESS housing.	유청용용도출한 Diam. of Fan-wheel.	24	Seese minute.	프	J	ర్	Heater: 4 20 4 5 6 25 4 5 6 25 4 5 6 7 6 7 6 7 6 7 6 7 6 7 6 7 6 7 6 7 6	000,000 000 000,000 000 000,000 00	Heat Units required	_	Velocity of Air through Coils in ft. per minute.	Free Area between 99 6 29 6 99 5 2 Pipes in sq. ft.	Heat Units given off	60	Sq. Ft. Heating Sur- 1900 120 Isoe required.
70 80 90 100 110 120 140 160 180 200	72 84 96 108 120	26 28 25 25 21 18 16 14	000005	21 3 4 5 6 8 10 12 15 18		6,90 8,50 10,50 12,50 15,80 19,80 26,20 33,00 41,60 50,00	0 1,1 0 1,5 0 1,9 0 2,4 0 8,0	18,000 72,000 30,000 96,000	2,900,0 8,870,0 4,870,0 6,130,0 7,875.0)00)00	: : : :	22. 29.1 36.7 46.3 55.5			580 714 880 1050 1825 1650 2200 2770 8490 4140
Size of Blower-housing.	Lineal Feet of One-inch	Pipe required.	Pounds of Steam condensed	per hour to 212.	Size Steam-main required.	Size Return-main required.	Boiler Capacity required, H.P.; 30 lbs. steam per hour = 1 H.P.	Sq. Ft. Heating Surface in Boiler at 15 sq. ft. per H.P.	Sq. Ft. Grate-surface at 35 sq. ft. heating surface to sq. ft grate.	Volume Air mill commend to	Capacity per minute.	Area of Conduit in sq. ft. for 900 ft. velocity per	minute.	Z	tion equal to 100 ft. of
70 80 90 100 110 120 140 160 180	1, 2, 2, 8, 8, 4, 6, 8, 10,	740 142 840 150 975 950 800 810 470 420	10 12 16 19 24 29 80 63 75	055 295 300 300 410 390 390 325 325	81 4 41 5 5 6 7 8 9 10	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	35 43 58 68 80 100 133 167 211 259	525 645 795 945 1200 1500 1995 2505 3165 8780	15 18 28 27 34 43 57 72 90 108	1	8,700 0,700 13,200 15,800 19,900 15,000 13,100 11,700 52,500 18,200	9.6 13.0 14.7 17.5 22.2 27.8 86.8 46.8 70.2	17 15 12 15 10 10 10 10 15	10 14 18 18 28 31 89 50	3.200 0.000 2.500 5,000 3.900 3,800 1,400 9,600 0,000

Temperature of fresh air, 0°; of air from colls, 120°; of steam, 227°. Pressure of steam, 5 lbs.

Peripheral velocity of fan-tips, 4000 ft.; number of pipes deep in coil, 24; depth of coil, 60 inches; area of coils approximately twice free area.

WATER-WHEELS.

Water-power Plants Operating under High Pressures.—
The following notes are contributed by the Petton Water Wheel Co.:
The Consolidated Virginia & Col. Mining Co., Virginia, Nev., has a 8-ft, steel-disk Pelton wheel operating under 2100 ft. fall, equal to 911 lbs. per sq. in. It runs at a peripheral velocity of 10,804 ft. per minute and has a capacity of over 100 H.P. The rigidity with which water under such a high pressur as this leaves the nozzle is shown in the fact that it is impossible to cut ti

stream with an axe, however heavy the blow, as it will rebound just as it

stream with an axe, however heavy the blow, as it will rebound just as it would from a steel rod travelling at a high rate of speed.

The London Hydraulic Power Co. has a large number of Pelton wheels from 12 to 18 in. diameter running under pressure of about 1000 lbs. per. sq. in. from a system of pressure-mains. The 18-in. wheels weighing 80 lbs. have a capacity of over 20 H.P. (See Blaine's "Hydraulic Machinery.")

Hydraulic Power-hoist of Milwaukee Mining Co., Idaho.—One cage travels up as the other descends; the maximum load of 5500 lbs. at a speed of 400 ft. per min. is carried by one of a pair of Pelton wheels (one for each cage) Wheels are started and stopped by opening and closing a small hydraulic valve at the engineer's stand which operates the larger valves by hydraulic valve at the engineer's takes up the shock that would otherwise occur pressure. An air-chamber takes up the shock that would otherwise occur on the pipe line under the pressure due to 850 ft. fall. The Mannesmann Cycle Tube Works, North Adams, Mass., are using four

Pelton wheels, having a fly-wheel rim, under a pump pressure of 600 lbs. per sq. in. These wheels are direct-connected to the rolls through which the

sq. in. These wheels are direct-connected to the rolls through which the ingots are passed for drawing out seamless tubing.

The Alaska Gold Mining Co., Douglass Island, Alaska, has a 22-ft. Pelton wheel on the shaft of a Riedler duplex compressor. It is used as a flywheel as well, weighing 25,000 lbs.—and develops 500 H.P. at 75 revolutions. A valve connected to the pressure-chamber starts and stops the wheel automatically, thus maintaining the pressure in the air-receiver.

At Pachuca in Mexico five Pelton wheels having a capacity of 600 H.P. each under 800 ft. head are driving an electric transmission plant. These wheels weigh less than 500 lbs. each, showing over a horse-power per pound of metal.

Formulæ for Calculating the Power of Jet Water-wheels, such as the Pelton (F. K. Blue).—HP = horse-power delivered δ = 62.86 lbs. per cu. ft; E = efficiency of turbine; q = quantity of water, cubic feet per minute; h = feet effective head; d = inches diameter of jet; p = pounds per square inch effective head; c = coefficient of discharge from nozzle, which may be ordinarily taken at 0.9.

$$\begin{split} HP &= \frac{8 \, Eqh}{83000} = .00189 \, Eqh = .00486 \, Eqp = .00496 \, Ecd^3 \, \sqrt[4]{h^3} = .0174 \, Ecd^2 \, \sqrt[4]{p^3}, \\ q &= 529.2 \, \frac{HP}{Eh} = 2299 \, \frac{HP}{Ep} = 2.62cd^2 \, \sqrt[4]{h} = 8.99cd^2 \, \sqrt[4]{p}, \\ d^3 &= 201.6 \, \frac{HP}{Ec \, \sqrt[4]{h^3}} = 57.4 \, \frac{HP}{Ec \, \sqrt[4]{p^3}} = .881 \, \frac{q}{c \, \sqrt[4]{h}} = .25 \, \frac{q}{c \, \sqrt[4]{p}}, \end{split}$$

GAS FUEL.

Average Volumetric Composition, Energy, etc., of Various Gases. (Contributed by R. D. Wood & Co., Philadelphia, 1898.)

	Natural	Coal-	Water-	Produ	cer-gas.	Air.	
	Gas.	gas.	gas.	Anthra.	Bitum.	AIF.	
co	0.50	6.0	45.0	27.0	27.0		
H	2.18	46.0	45.0	12.0	12.0		
CH4	92.6	40.0	2.0	1.2	2.5		
C.H	0.31	4.0	1	 .	0.4	l .	
CO•	0.26	0.5	4.0	2.5	2.5	trace	
N	8.61	1.5	2.0	57.0	55.8	79	
0	0.34	0.5	0.5	0.8	0.8	21	
Vapor		1.5	1.5			trace	
Lbs. in 1000 cu. ft	45.6	82.0	45.6	65.6	65.9	76.1	
H. U. in 1000 cu. ft.		735,000	822,000	137,455	156,917*	l	
Cu.ft. from each lb.		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		100,000	1 222,022	1	
of coal approx		5	25	85	75	200+	

^{*} The real energy of bituminous producer-gas when used hot is far in excess of that indicated by the above table, on account of the hydrocarbons, which do not show, as they are condensed in the act of collecting the gas for analysis. In actual practice there is found to be about 50% more effective energy in bituminous gas than in anthracite gas when used hot enough to prevent condensation in the flues.

† Cubic feet of air required to burn 1 lb, of coal with blast.

STEAM-BOILERS.

Steam-boiler Construction. (Extract from the Pules and Specifications of the Hartford Steam Boiler Inspection & Insurance Co., 1898.)

Cylindrical boiler shells of fire box steel, and tube-heads of best flange steel. Limits of tensile strength between 55,000 and 62,000 lbs. per sq. in.

Iron rivets in steel plates, 38,000 lbs, shearing strength per sq. in. in single shear, and 85% more, or 70,300 lbs., in double shear. Each shell-plate must bear a test-coupon which shall be sheared off and tested. Each coupon must fulfil the above requirements as to tensile strength, but must have a contraction of area of not less than 50% and an elongation of 25% in a length of 8 in. It must also stand bending 180° when cold, when red hot, and after being heated red hot and quenched in cold water, without fracture on outside of bent portion.

Crow-foot braces are required for boiler-heads without welds, and if of iron limit the strain to 7500 lbs. per sq. in., and stay-bolts must not be subjected to a greater strain than 6000 lbs. per sq. in.

The thickness of double butt-straps 8/10 the thickness of plates. In lap-

joints the distance between the rows of rivets is 36 the pitch. In doubleriveted lap-joints of plates up to 1/4 in. thick the efficiency is 70% and in triple-riveted lap-joints 75% of the solid plate.

In triple-riveted double-strapped butt-seams for plates from 14 in. to 1/4 in.

thick, the efficiency ranges from 88% to 86% of the solid plate.

In high-pressure boilers the holes are required to be drilled in place; that is, all holes may be punched ¼ in. less than full size, then the courses are rolled up, tube-heads and joint-covering plates bolted to courses, with all holes together perfectly fair. Then the rivet-holes are drilled to full size, and when completed the plates are taken apart and the burr removed.

The rule for the bursting-pressure of cylindrical boiler-shells is the following: Multiply the ultimate tensile strength of the weakest plate in the shell by its thickness in inches and by the efficiency of the joint, and divide result by the semi-diameter of shell; the quotient is the bursting-pressure per square inch. This pressure divided by the factor 5 gives the allowable working pressure.

BOILER FEEDING.

Gravity Boiler-feeders.—If a closed tank be placed above the level of the water in a boiler and the tank be filled or partly filled with water, then on shutting off the supply to the tank, admitting steam from the boiler to the upper part of the tank, so as to equalize the steam pressure in the boiler and in the tank, and opening a valve in a pipe leading from the tank to the boiler the water will run into the boiler. An apparatus of this kind may be made to work with practically perfect efficiency as a boilerfeeder, as an injector does, when the feed supply is at ordinary atmospheric temperature, since after the tank is emptied of water and the valves in the pipes connecting it with the boiler are closed the condensation of the steam remaining in the tank will create a vacuum which will lift a fresh supply of water into the tank. The only loss of energy in the cycle of operations is the radiation from the tank and pipes, which may be made very small by

proper covering.
When the feed-water supply is hot, such as the return water from a heating system, the gravity apparatus may be made to work by having two receivers, one at a low level, which receives the returns or other feed-supply, and the other at a point above the boilers. A partial vacuum being created in the upper tank, steam-pressure is applied above the water in the lower tank by which it is elevated into the upper. The operation of such a machine may be made automatic by suitable arrangement of valves. (See circular of the Scott Boiler Feeder, made by the Q. & C. Co., Chicago.)

FEED-WATER HEATERS.

Capacity of Feed-water Heaters.—The following extract from a letter by W. B. Billings, treasurer of the Taunton Locomotive Manufacturing Co., builders of the Wainwright feed-water heater, to Engineering Record, February, 1898, is of interest in showing the relation of the heating surface of a heater to the work done by it:

"Closed feed-water heaters are seldom provided with sufficient surface to raise the feed temperature to more than 200°. The sate of heat tre

mission may be measured by the number of British thermal units which pass through a square foot of tubular surface in one hour for each degree of difference in temperature between the water and the steam. The difficulties which attend experiments in this direction can only be appreciated by those who have attempted to make such experiments. Certain results have been reached, however, which point to what appears to be a reasonable co-clusion. One set of experiments made quite recently gave certain results which may be set forth in the table herewith.

	(5° F	67 B.T.U.	Transmitted in one
Difference between	во "	79 "	hour by each sq. ft.
final tempera-	8° " 	89 "	of surface for each
tures of water and	110 "	114 "	degree of average
steam.	15° "		difference in temper-
	18° "		atures.

"In other words, when the water was brought to within 5° of the temperature of the heating medium, heat was transmitted through the tubes at the rate of 67 B.T.U. per square foot for each degree of difference in temperature in one hour. When the amount of water flowing through the heater was selergely increased as to make it impossible to get the water any nearer than within 18° of the temperature of the steam, the heat was transmitted at the rate of 139 B.T.U. per sq. ft. of surface for each degree of difference in temperature in one hour. Note here that even with the rate of transmission as low as 67 B.T.U. the water was still 5° from the temperature of the steam. At what rate would the heat have been transmitted if the water could have been brought to within 2° of the temperature of the steam, or to 210° when the steam is at 212° ?

"For commercial purposes feed-water heaters are given a H.P. rating which allows about one-third of a square foot of surface per H.P.—a boiler H.P. allows about one-third of a square foot of surface per H.P.—a boner H.P. being 30 lbs. of water per hour. It the figures given in the table above are accepted as substantially correct, a heater which is to raise 3000 lbs. of water per hour from 60° to 207°, using exhaust steam at 212° as a heating medium, should have nearly 84 eq. ft. of heating surface—that is, a 100 H.P. feed-water heater which is to maintain a constant temperature of not less than 207°, with water flowing through it at the rate of 3000 lbs. per hour, should have nearly a square foot of surface per H.P. That feed-water heaters do not carry this amount of heating surface is well known."

THE STEAM-ENGINE.

Current Practice in Engine Proportions, 1897 (Compare pages 792 to 817.)—A paper with this title by Prof. John H. Barr, in Trans. A. S. M. E., xviii. 73r, gives the results of an examination of the proportions of parts of a great number of single-cylinder engines made by different builders. The engines classed as low speed (L. S.) are Corliss or other long-stroke engines usually making not more than 100 or 125 revs. per min. Those classed as high speed (H. S.) have a stroke generally of 1 to 1½ diameters and a speed of 200 to 300 revs. per min. The results are expressed in formulas of rational form with empirical coefficients, and are here abridged as

Thickness of Shell, L. S. only. -t = CD + B; D = diam of piston in in.; B = 0.8 in.; C varies from 0.04 to 0.06, mean = 0.05.

Flanges and Cylinder-heads.—I to 1.5 times thickness of shell, mean 1.2. Cylinder-head Studs.—No studs less than ¾ in. nor greater than 1¾ in. diam. Least number, 8, for 10 in diam. Average number = 0.7D. Average diam. = $D/40 + \frac{1}{2}$ in.

Forts and Pipes.—a = area of port (or pipe) in sq. in.; A = area of piston, sq. in.; V = mean piston-speed, ft. per min.; a = AV/C, in which C = mean velocity of steam through the port or pipe in ft. per min.

Ports, H. S. (same ports for steam as for exhaust).—C = 4500 to 6500, mean 5500. For ordinary piston-speed of 600 ft. per min. a = KA; K = .09 to .18. mean .11.

Steam-ports, L. S.—C = 5000 to 9000, mean 6800; K = .06 to .10, mean .09. Exhaust-ports, L. S.—C = 4000 to 7000, mean 5500; K = .10 to .125, mean .11 Steam-pipes, H. S.—C = 5800 to 7000, mean 6500. If d = diam. of pipe and

D = diam. of piston, d = .29D to .32D, mean .30D. Steum-pipes, L. S.—C = 5000 to 8000, mean .80D; d = .27 to .35D, mean .32D. Exhaust pipes, H. S.—C = 2500 to 5000, mean .400; d = .35 to .50D, mean .40D. Exhaust-pipes, L. S.—C = 2800 to .4700, mean .3900; d = .35 to .45D, mean .40D.

Face of Pistons.—F = face; D = diameter. F = CD. H. S.: C = .30 to .60 mean .46. L. S.: C = .25 to .45, mean .32. Piston-rods.—d = diam. of rod; D = diam. of plston; L = stroke, in.;

d=C $\sqrt[4]{DL}$. H. S.: C=.12 to .175, mean .145. L. S.: C=.10 to .18, mean .11. Connecting-rods.—H. S. (generally 6 cranks long, rectangular section); b= breadth; b= height of section; $L_1=$ length of connecting-rod; D= diam. of piston; $b = C \sqrt{DL_1}$; C = .045 to .07, mean .057; h = Kb; K = 2.2 to 4, mean 2.7. L. S. (generally 5 cranks long, circular sections only); C = .092 to .105, mean .092.

Cross-head Slides.—Maximum pressure in lbs. per sq. in. of shoe, due to the vertical component of the force on the connecting rod. H. S.: 10.5 to 38,

the vertical component of the force on the connecting-rod. H. S.: 10.5 to so, mean 27. L. S: 29 to 88, mean 40.

Cross-head Pins.—l = length; d = diam.; projected area = a = dl = CA; A = area of piston; l = Kd. H. S.: C = .00 to .11, mean .08; K = 1 to 2, mean 1.26. L. S.: C = .05 to .10, mean .07; K = 1 to 1.5, mean 1.3.

Crank-pin.—HP = horse-power of engine; L = length of stroke; l = length of pin; $l = C \times HP/L + B$; d = diam. of pin; A = area of piston; dl = KA. H. S.: C = .18 to .46, mean .39; B = 2.5 in.; K = .17 to .44, mean .24. L. S.: C = .4 to .8, mean .6; B = 2 in.; K = .065 to .115, mean .09.

Crank-shaft Main Journal.— $d = C\sqrt[3]{HP + N}$; d = diam.; l = length; N = revs. per min.; projected area = MA; A = area of piston. H.S.: C = 6.5 to 8.5, mean 7.3; K = 2 to 8, mean 2.2; M = .37 to .70, mean .6. L.S.: C = 6 to 8, mean 6.8; K = 1.7 to 2.1, mean 1.9; M = .46 to .64, mean .56. Piston-speed.—H.S.: 530 to 660, mean 600; L.S.: 500 to 850, mean 600.

Weight of Reciprocating Paris (piston, piston-rod, cross-head, and one-half of connecting-rod).— $W = CD^3 + LN^3$; D = diam. of piston; L = length of stroke, in.; N = revs per min. H. S. only; C = 1,200,000 to 2,300,000, mean 1,860,000.

Belt-surface per I.H.P.—S=CHP+B; S= product of width of belt in feet by velocity of belt in ft. per min. H. S.: C=21 to 40 mean 28; B=1800. L. S.: $S=C\times HP$; C=30 to 42, mean =35. Fly-wheel (H. S. only).—Weight of rim in lbs.: $W=C\times HP+D_1^2N^3$; $D_1=0$ diam. of wheel in in.; $C=65\times 10^{10}$ to 2×10^{12} mean $=12\times 10^{11}$, or 1,200,000,000,000.

1,200,000,000. Weight of Engine per I.H.P. in lbs., including fly-wheel.— $W=C\times H.P.$ H. S.: C=100 to 135, mean 115. L. S.: C=185 to 240, mean 175. Work of Steam-turbines. (See p. 791.)—A 300-H.P. De Laval steam-turbine at the 1-th Street station of the Edison Electric Illuminating Co. in New York City in April, 1896, showed on a test a steam-consumption of 19.275 lbs. of steam per electrical H.P. per hour, equivalent to 17.348 lbs. per brake H.P., assuming an efficiency of the dynamo of 90%. The stramperssure was 145 lbs. gauge and the vacuum 26 in. It drove two 100-K.W. dynamos. The turbine-disk was 29.5 in. diameter and its speed 9000 revs. per min. The dynamos were geared down to 750 revs. The total equipment including turbine, gearing, and dynamos, occupied a space 13 ft. 3 in.

per min. The dynamos were geared down to 750 revs. The total equipment, including turbine, gearing, and dynamos, occupied a space 13 ft. 3 in. long, 6 ft. 5 in. wide, and 4 ft. 8 in. high.

The "Turbinia," a torpedo-boat 100 ft. long, 9 ft. beam, and 44½ tons displacement, was driven at 31 knots per hour by a Parsons steam-turbine in 1897, developing a calculated I.H.P. of 1576 and a thrust H.P. of 916, the steam-pressure at the engine being 130 lbs. and at the bollers 200 lbs. The vacuum was 13½ lbs. The revolutions averaged 2100 per minute. The calculated steam-consumption was 18.86 lbs. per I.H.P. per hour. On another trial the "Turbinia" developed a speed of 323½ knots.

Relative Cost of Different Sizes of Steam-engines. (From catalogue of the Buckeye Engine Co., Part III.)

Horse-power	50	75	100	125	150	200	250	300	850	400	500	600	700	800
Cost per H.P, \$	20	1734	16	15	1416	1816	18	12 3 4	12.6	12.6	12.8	131/4	14	15
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GEARING.

Efficiency of Worm Gearing. (See also page 898.)—Worm gearing as a means of transmitting power, has until recently, generally been looked upon with suspicion, its efficiency being considered necessarily low and its life short. Recent experience, however, indicates that when properly proportioned it is both durable and reasonably efficient. Mr. F. A. Halsey discusses the subject in Am. Machinist, Jan. 13 and 20, 1898. He quotes two formulas for the efficiency of worm gearing due to Prof. John H. Barr:

$$E = \frac{\tan \alpha (1 - f \tan \alpha)}{\tan \alpha + f}, \dots (1) \qquad E = \frac{\tan \alpha (1 - f \tan \alpha)}{\tan \alpha + 2f} \text{ approx., } \dots (2)$$

in which E= efficiency; $\alpha=$ angle of thread, being angle between thread and a line perpendicular to the axis of the worm; f= coefficient of friction Eq. (1) applies to the worm thread only, while (2) applies to the worm and step combined, on the assumption that the mean friction radius of the two is equal. Eq. (1) gives a maximum for E when $\tan \alpha = \sqrt{1+f^2}-f$... (3) and eq. (2) a maximum when $\tan \alpha = \sqrt{2+4f^2}-2f$... (4) Using a value .05 for f gives a value for α in (3) of 43° 34′ and in (4) a value of 52° 49′. On plotting equations (1) and (2) the curves show the striking influence of

On plotting equations (I) and (2) the curves show the striking influence of the pitch-angle upon the efficiency, and since the lost work is expended in friction and wear, it is plain why worms of low angle should be short-lived and those of high angle long-lived. The following table is taken from Mr. Halsey's plotted curves:

RELATION BETWEEN THREAD-ANGLE SPEED AND EFFICIENCY OF WORM GEARS.

Velocity of	Angle of Thread.										
Pitch-line, feet per	5	10	20	30	40	45					
minute.		Efficiency.									
3	35	52	66 69	73	76 70	77					
10 20	40 47 52 60	56 62 67 74 82 85		73 76 79 83 87	76 79 82 85 88	80 82 86 88 91					
40 100	60 70	74 82	74 78 83 88	87 91	88 91	88 91					
200	70 76	85	91	92	91 9 2	9:2					

The experiments of Mr. Wilfred Lewis on worms show a very satisfactory correspondence with the theory. Mr. Halsey gives a collection of data comprising 16 worms doing heavy duty and having pitch-angles ranging between 4° 30′ and 45°, which show that every worm having an angle above 12° 30′ was successful in regard to durability, and every worm below 9 was unsuccessful, the overlapping region being occupied by worms some of which were successful and some unsuccessful. In several cases worms of one pitch-angle had been replaced by worms of a different angle, an increase in the angle leading in every case to better results and a decrease to poorer results. He concludes with the following table from experiments by Mr. James Christie, of the Pencoyd Iron Works, and gives data connecting the load upon the teeth with the pitch-line velocity of the worm:

LIMITING SPEEDS AND PRESSURES OF WORM GEARING.										
	Single-thread Worm 1" Pitch, 2‡ Pitch Diam.				Double- thread Worm 2" Pitch, 27 Pitch Diam.			Double- thread Worm 2‡" Pitch, 4‡ Pitch Diam.		
Revolutions per minute Velocity at pitch-line in feet		201	272	425	128	201	272	201	272	425
per minute	96			320 700			205 1100	235 1100	319 700	498 400

APPROXIMATE HYDRAULIC FORMULÆ.

(The Lombard Governor Co., Boston, Mass.)

 $\operatorname{Head}(H)$ in feet. Pressure (P) in lbs. per sq. in. Diameter (D) in feet. Area (A) in sq. ft. Quantity (Q) in cubic ft. per second. Time (T) in seconds.

Spouting velocity = $8.02 \ \sqrt{H}$.

Time (T_1) to acquire spouting velocity in a vertical pipe, or (T_2) in a pipe on an angle (θ) from horizontal:

$$T_1 = 8.02 \sqrt{H} + 82.17$$
, $T_1 = 8.02 \sqrt{H} + 82.17 \sin \theta$.

Head (H) or pressure (P) which will vent any quantity (Q) through a round orifice of any diameter (D) or area (A):

$$H = Q^2 + 14.1D^4$$
, $H = Q^2 + 28.75A^2$:
 $P = Q^2 + 34.1D^4$, $P = Q^2 + 55.3A^2$.

Quantity (Q) discharged through a round orifice of any diameter (D) or area (A) under any pressure (P) or under any head (H):

$$Q = \sqrt{P \times 55.8 \times A^2}, \qquad Q = \sqrt{P \times 84.1 \times D^4};$$

$$Q = \sqrt{H \times 28.75 \times A^2}, \qquad Q = \sqrt{H \times 14.71 \times D^4}.$$

Diameter (D) or area (A) of a round orifice to vent any quantity (Q) under any head (H) or under any pressure (P):

$$D = \sqrt{Q + 3.84 \sqrt{H}}, \quad D = \sqrt{Q + 5.8 \sqrt{P}};$$

$$A = Q + 4.89 \sqrt{H}, \qquad A = Q + 7.35 \sqrt{P}.$$

Time (T) of emptying a vessel of any area (A) through an orifice of any area (a) anywhere in its side:

$$T = .416A \sqrt{H} + a.$$

Time (T) of lowering a water level from (H) to (h) in a tank through an orifice of any area(a) in its side. Area of tank is (A).

$$T = 0.416A(\sqrt[4]{H} - \sqrt[4]{h}) + a.$$

Kinetic energy (K) or foot-pounds in water in a round pipe of any diameter (D) when moving at velocity (V):

$$K = .76 \times D^2 \times L \times V$$
.

Time-average-pressure (A.P.) in a pipe of any length (L) with water moving at any velocity (V)

$$A.P. = 0.1324LV + T.$$

Note.—This must not be confused with water-hammer pressure, which is always many times greater than A.P. and for which no simple formula may be written.

Area (a) of an orifice to empty a tank of any area (A) in any time (T) from any head (H):

$$a = T + 0.409A \sqrt{H}.$$

Area (n) of an orifice to lower water in a tank of area (A) from head (H) to (h) in time (T):

$$a = T + 0.409 \times A \times (\sqrt{H} - \sqrt{h})$$

SPECIFICATIONS FOR TIN AND TERNE PLATE.

(Penna. R. R. Co., 1903.)

Each sheet must (1) be cut as nearly exact to size ordered as possible, (2) must be rectangular and flat and free from flaws, (3) must double-seam successfully under all circumstances, (4) must show a smooth edge with no sign of fracture when bent through an angle of 180° and flattened down with a wooden mallet, (5) must be so nearly like every other sheet in the shipment, in thickness, uniformity, and amount of coating, that no difficulty will arise in the shops due to varying thickness of sheets, and (6) must correspond for the different grades to the figures in the following table:

Kind of Coating.	Tin Pläte. Pure Tin.	No. 1 Terne Plate. 14 Tin, 34 Lead.	No. 2 Terne Plate. ½ Tin, ¾ Lead.
Amt. of coating per sq. ft Grade IUweight per sq. ft "IX IXX IXXX	0.0182 lb.	0.0364 lb.	0.0182 lb.
	0.49	0.51	0.49
	0.63	0.64	0.69
	0.71	0.73	0.71
	0.81	0.83	0.81
	0.91	0.93	0.91

LIST OF AUYHORITIES QUOTED IN THIS BOOK.

When a name is quoted but once or a few times only, the page or pages are given. The names of leading writers of text-books, who are quoted frequently, have the word "various" affixed in place of the page-number. The list is somewhat incomplete both as to names and page numbers.

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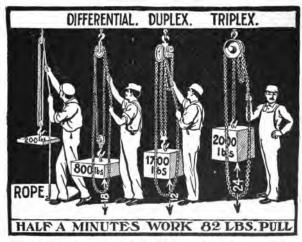
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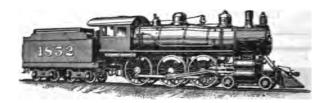
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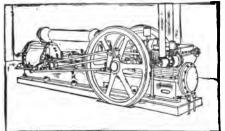


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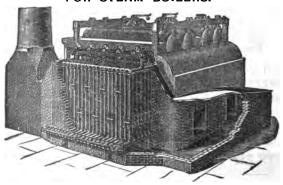
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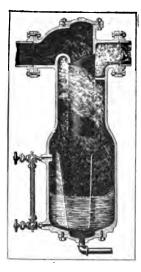


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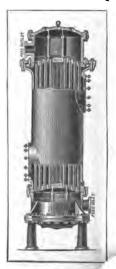
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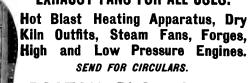
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